

# Selfconsistent studies of the dipole response in spherical heavy nuclei using realistic potentials



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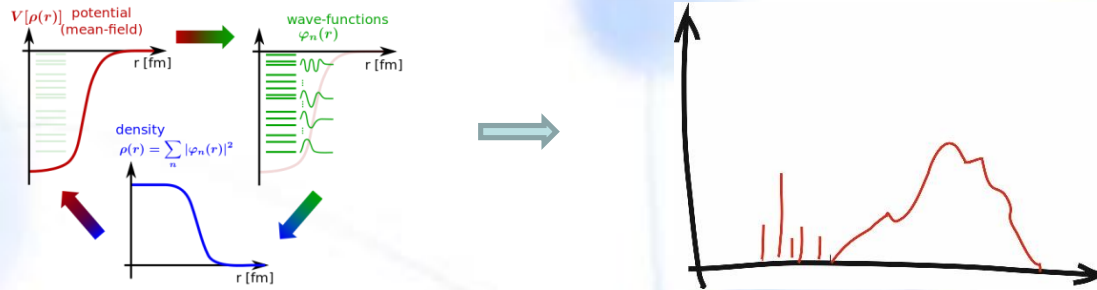
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**Eu N**  
**P C**  
**2015 European Nuclear  
Physics Conference**

# Microscopic description of dipole response



- Microscopic description of collective states (PDR, GDR): RPA suitable for gross features NOT fine structure

Methods beyond:

Second RPA, Quasiparticle Phonon Model, Extended Theory of finite Fermi systems, Relativistic Quasiparticle Time Blocking Approximation, Particle Vibration Coupling, Shell Model...

Our framework : **Equation of motion phonon method**

- Mean-field calculation: HF(B), expansion to HO basis
- Excited states and responses: matrix formulation of (Q)TDA, Q(RPA)
- Beyond 1-phonon: EMPM (Equation of Motion Phonon method) (subset of) 'complex' (2-phonon) configuration

Role of 'complex' configurations in dipole response in  $^{132}\text{Sn}$ ,  $^{208}\text{Pb}$ .

Knapp et al. Phys. Rev. C **90**, 014310 (2014)

Knapp et al. submitted to Phys. Rev. C

# Mean-field

**Ingredients:** Hamiltonian with 'realistic' 2-body NN interaction + phenomenological density dependent term

$$H = T_{int} + V. \quad T_{int} = \frac{1}{2m} \sum_i p_i^2 - T_{CM} \quad V = V_\chi + V_\rho$$

$$V_\rho = \sum_{i < j} v_\rho(ij) \quad v_\rho = \frac{C_\rho}{6} (1 + P_\sigma) \rho \left( \frac{\vec{r}_1 + \vec{r}_2}{2} \right) \delta(\vec{r}_1 - \vec{r}_2)$$

**Why DD interaction?** Simulates 3 body forces

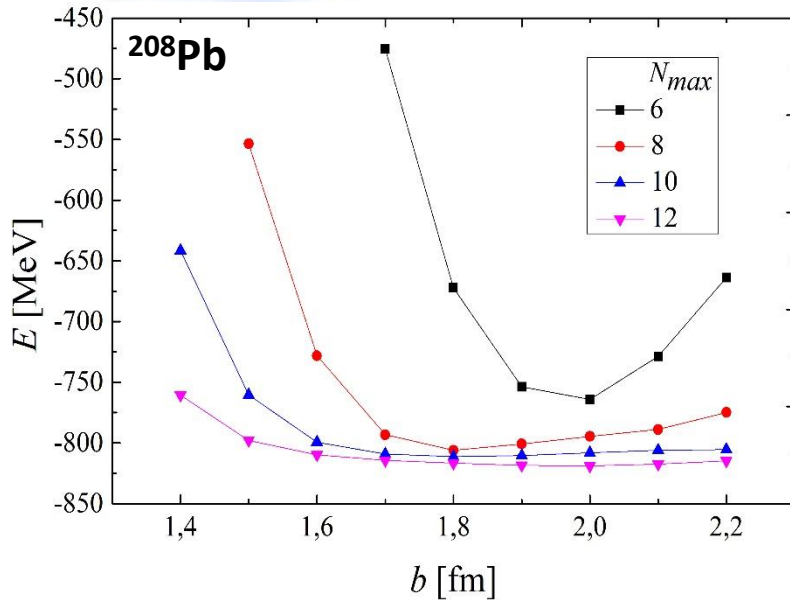
**bare chiral NNLO<sub>opt</sub>** (PRL 110, 192502 (2013)) gives large gaps between shells-> GDR peaks are too high in energy. Similar with UCOM and SRG evolved NN interactions, see H. Hergert et al., PRC 83,064317(2011).

Free parameter  $C_\rho$  can be tuned to reproduce centroids of GR at RPA(TDA) level

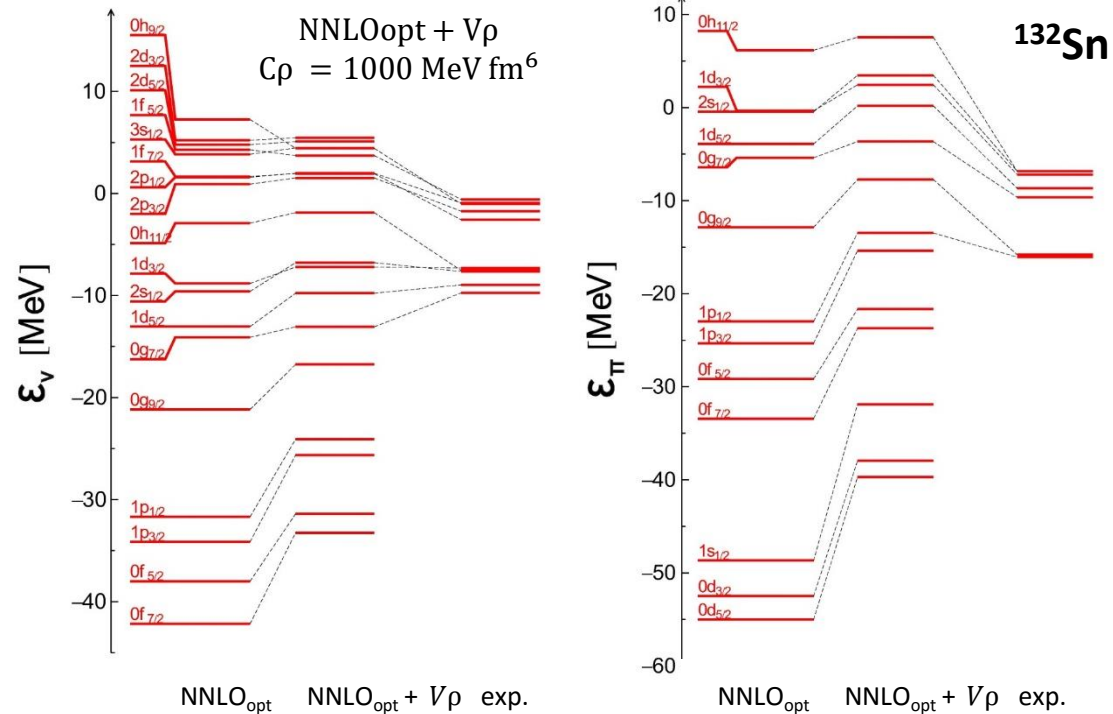
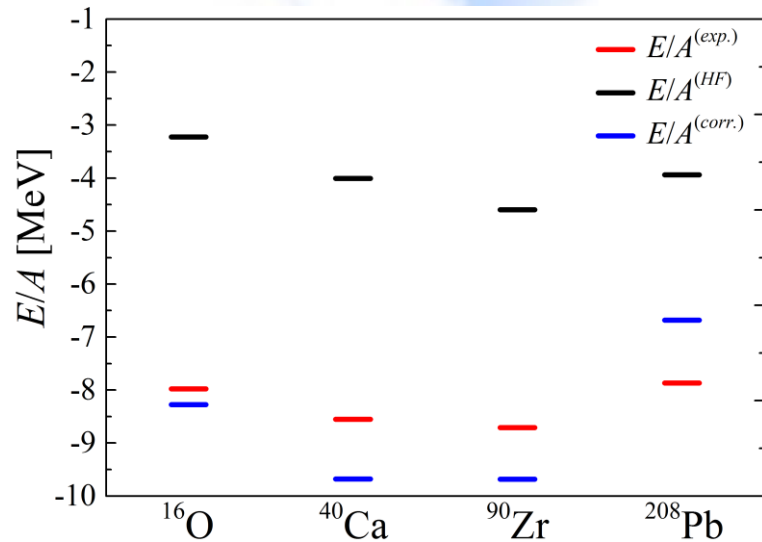
Mean-field calculation: Hartree-Fock (Bogoljubov)+residual interaction

**Future:** replace phenomenological density dependent term with consistently derived one

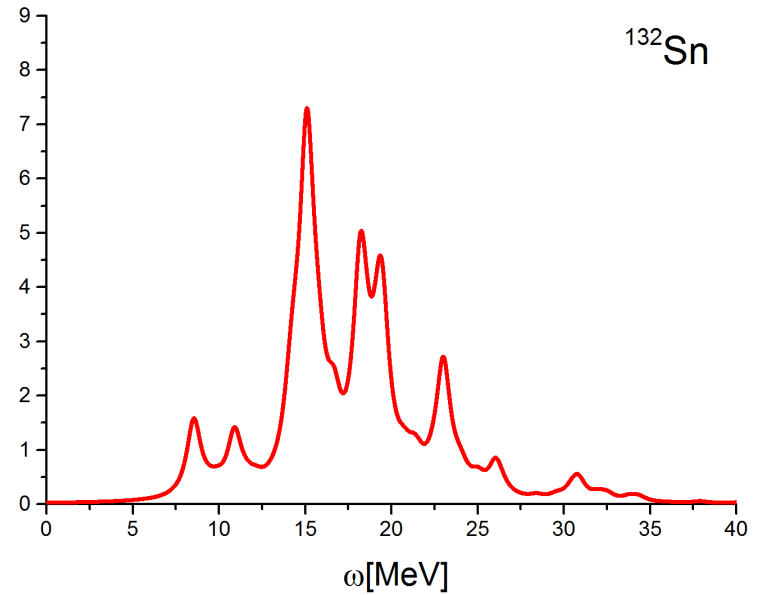
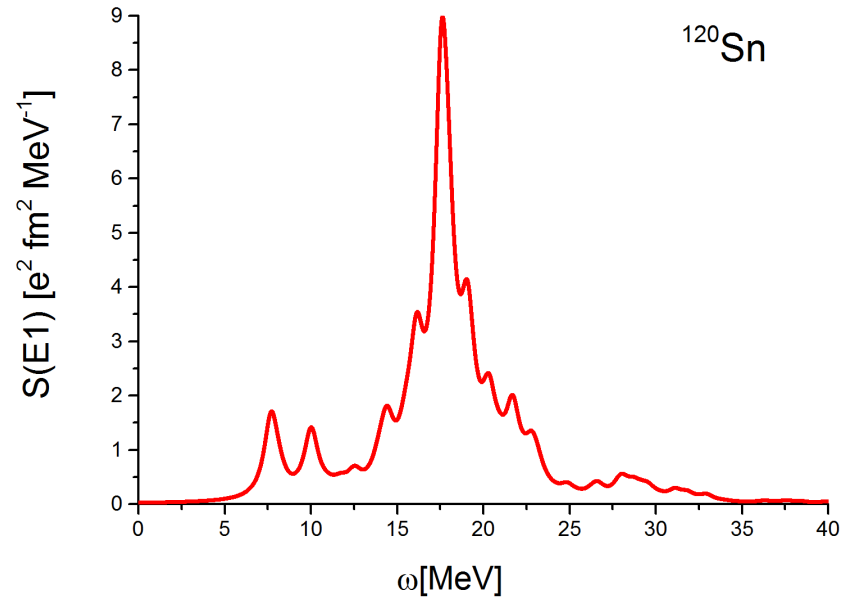
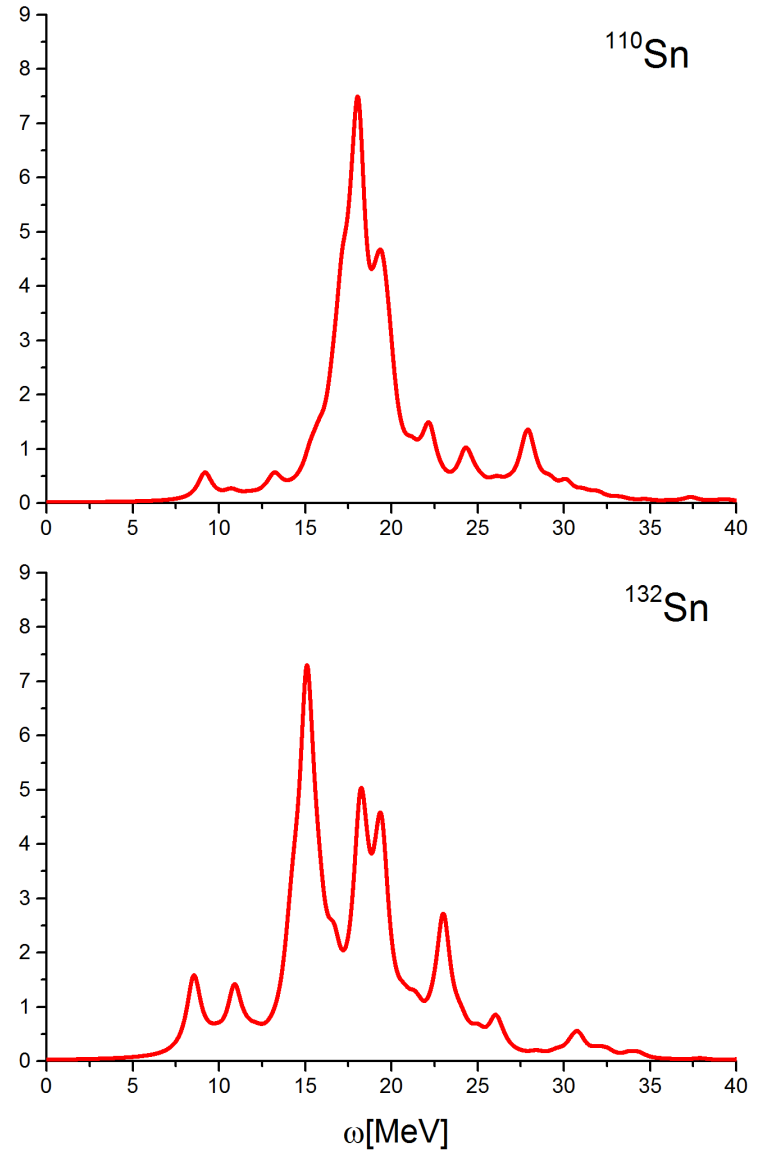
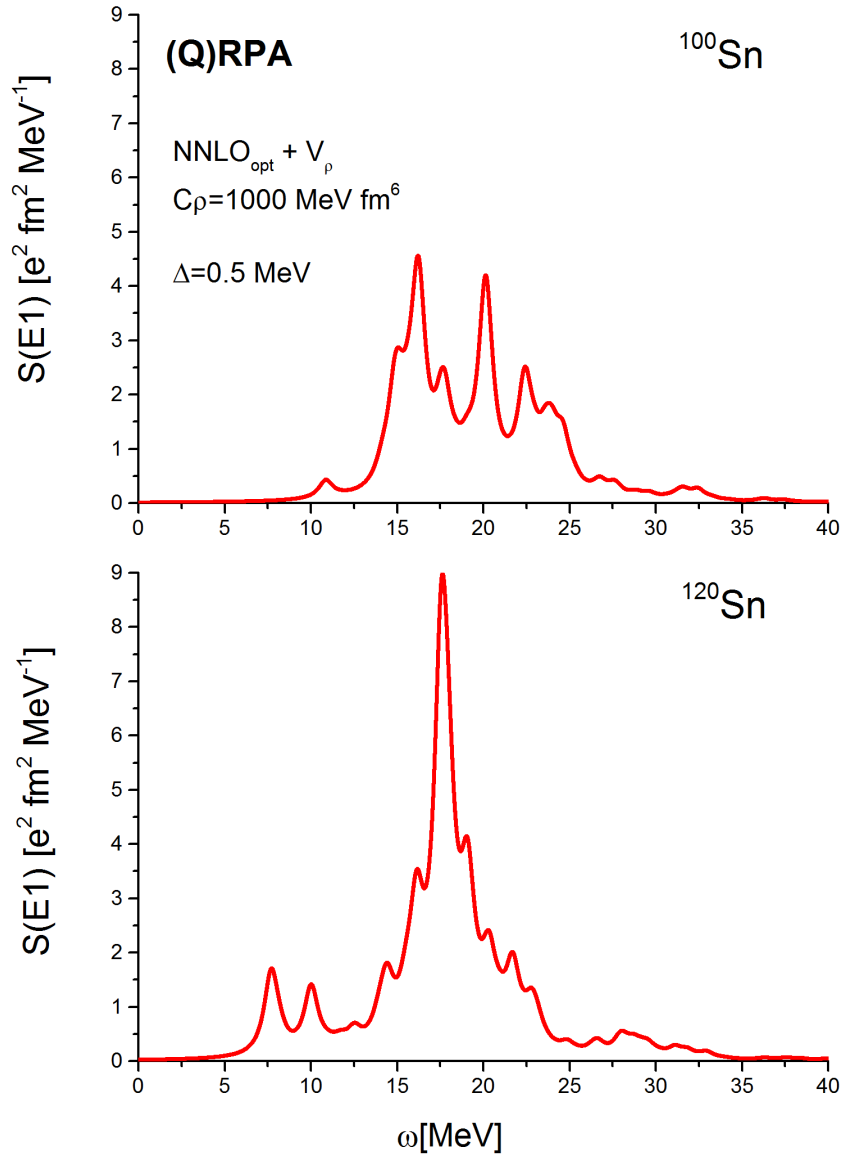
# Mean-field



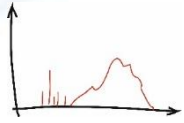
- HF calculation in HO basis
- weak dependence of HF energy on oscillator length  $b$  for 13 major shells
- 2nd order perturbation theory approaches to experimental binding energy
- effect of DD interaction: compression of s.p. spectra



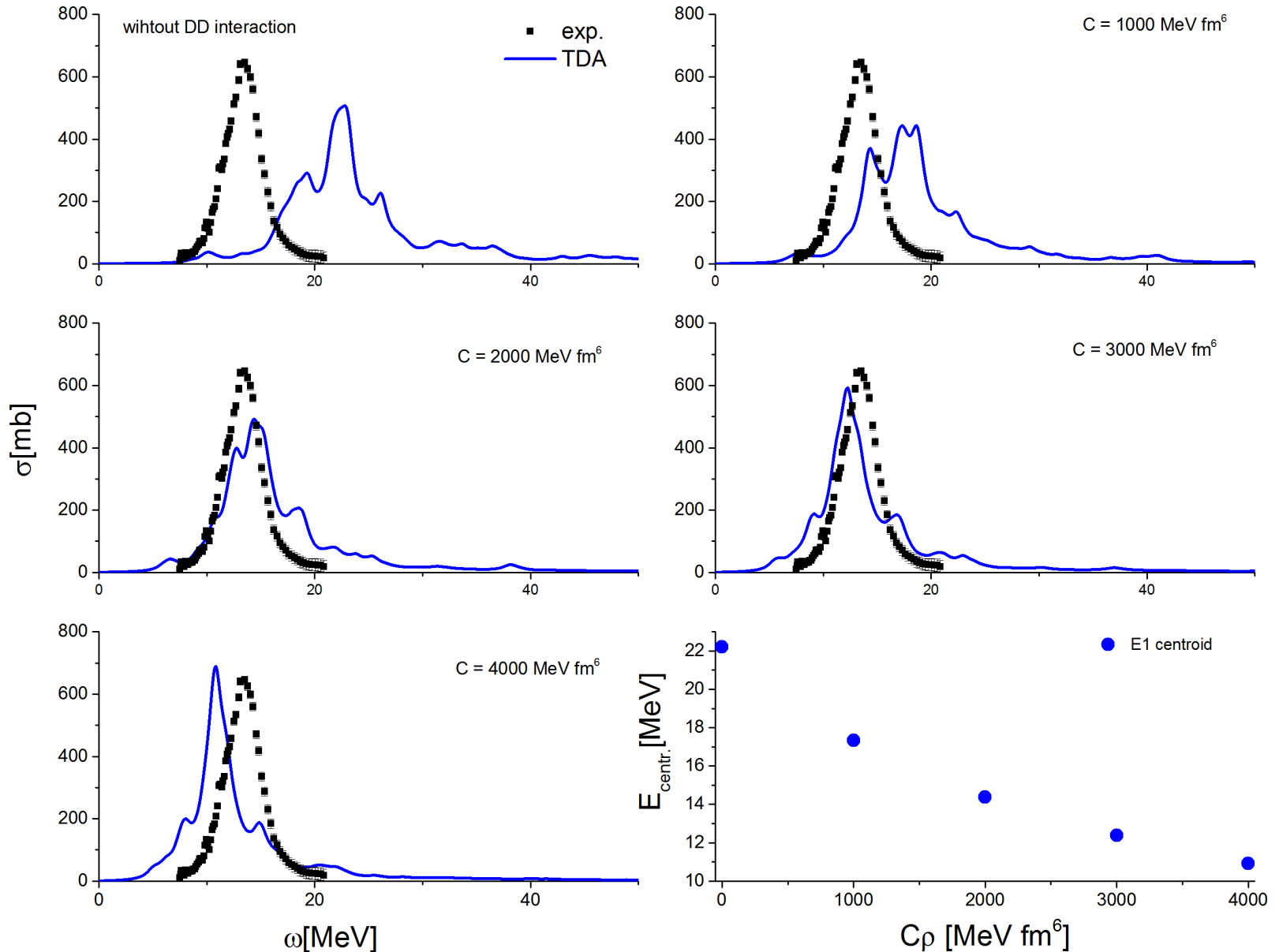
# Dipole strength in Sn



# Dipole strength in $^{208}\text{Pb}$



Dependence of GDR centroids on the strength of DD interaction



# Equation of Motion Phonon Method

**Goal:** to diagonalize **general two-body** Hamiltonian in basis of TDA 1-phonon, 2-phonon states  
**all parts of two-body interaction and Pauli principle are taken into account**

D. Bianco, F. Knapp, N. Lo Iudice, F. Andreozzi, and A. Porrino,  
 Phys. Rev. C **85**, 014313 (2012).

$$\langle n, \beta \| [H, O_\lambda^\dagger] \| n-1, \alpha \rangle = (E_\beta^{(n)} - E_\alpha^{(n-1)}) \langle n, \beta \| O_\lambda^\dagger \| n-1, \alpha \rangle$$

Basis:

$$|0\rangle$$

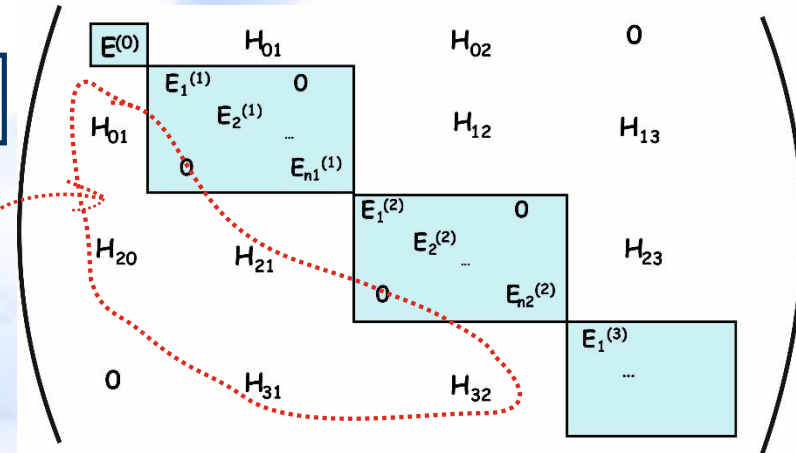
$$Q_\lambda^+ |0\rangle = |1, \lambda\rangle$$

$$Q_\lambda^+ |1, i\rangle, \quad i=1, 2, \dots, n_1$$

$$Q_\lambda^+ |2, j\rangle, \quad j=1, 2, \dots, n_2$$

**n-phonon subspace:** generalized eigenvalue problem in nonorthogonal redundant basis

*block-diagonal structure of Hamiltonian*



*couplings between phonon subspaces*

$$\mathcal{H}C = (\mathcal{A}\mathcal{D})C = EC$$

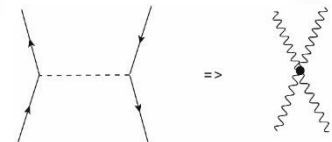
**Phonon interaction matrix**

$$\mathcal{A}^\beta(\lambda\alpha, \lambda'\gamma) = (E_\lambda + E_\alpha)\delta_{\lambda\lambda'}\delta_{\alpha\gamma} + \sum_\sigma W(\beta\lambda'\alpha\sigma; \gamma\lambda)\mathcal{V}_{\lambda\alpha, \lambda'\gamma}^\sigma$$

**Overlap matrix**

$$\mathcal{D}^\beta(\alpha\lambda; \alpha'\lambda') = \left[ \langle n-1, \alpha' | \times O_{\lambda'} \right]_\beta \left[ O_\lambda^\dagger \times | n-1, \alpha \rangle \right]$$

*redefined phonon interaction*



Final wave function

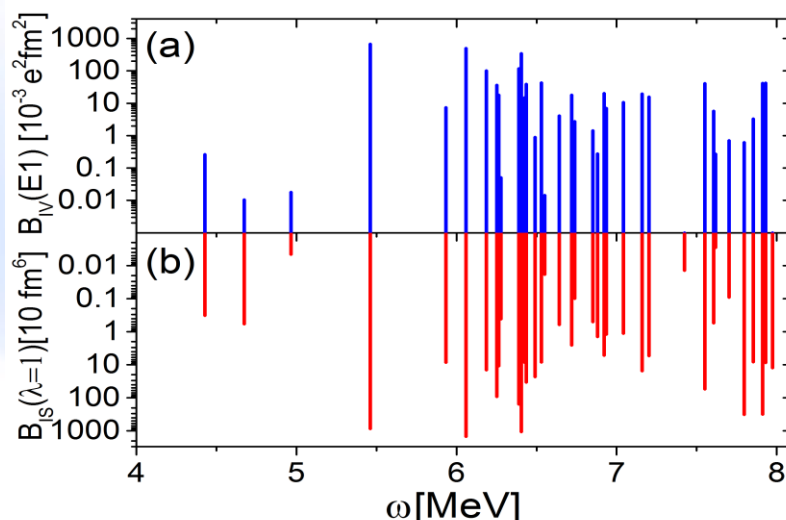
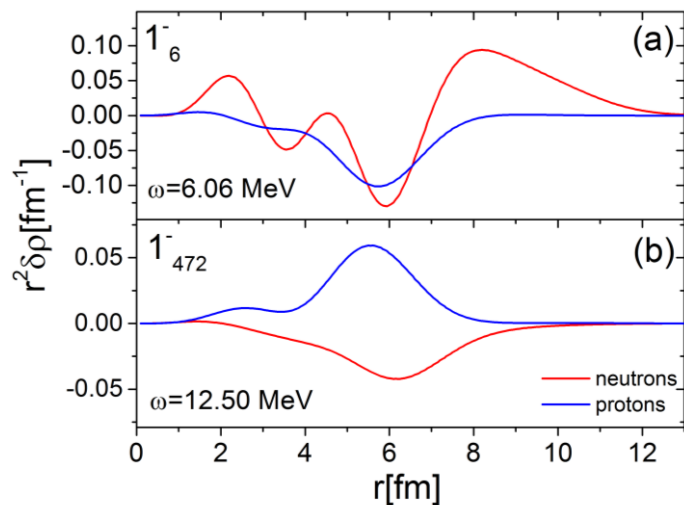
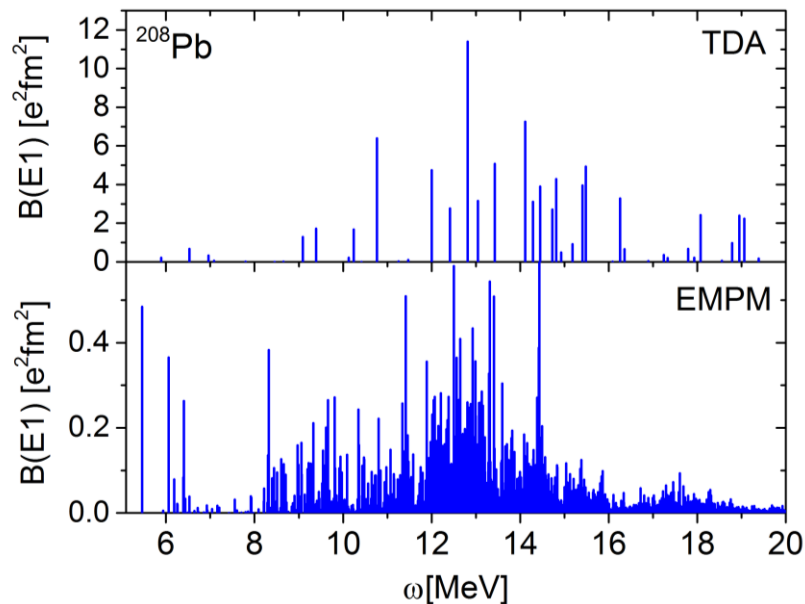
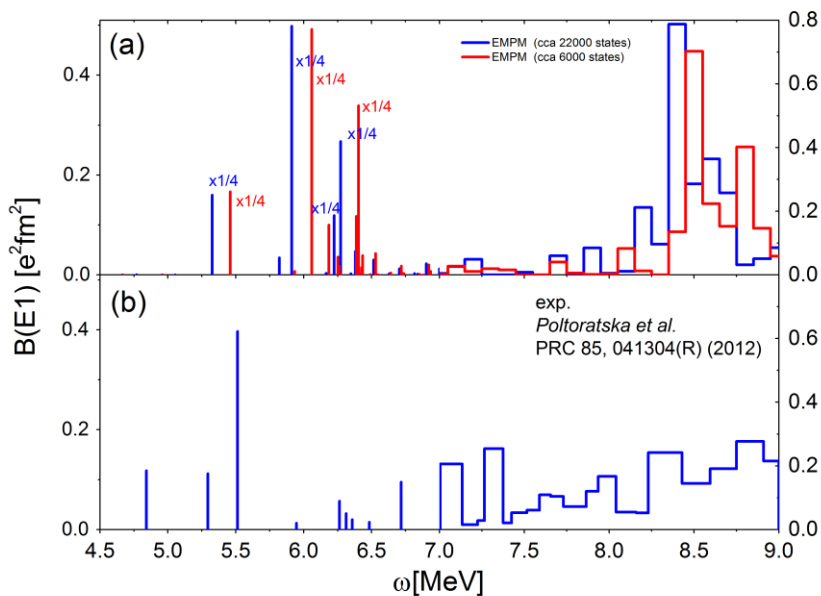
$$|\Psi_\nu\rangle = \sum_{n\alpha} C_\alpha^{(\nu)} |n; \alpha\rangle$$



# Dipole strength in $^{208}\text{Pb}$

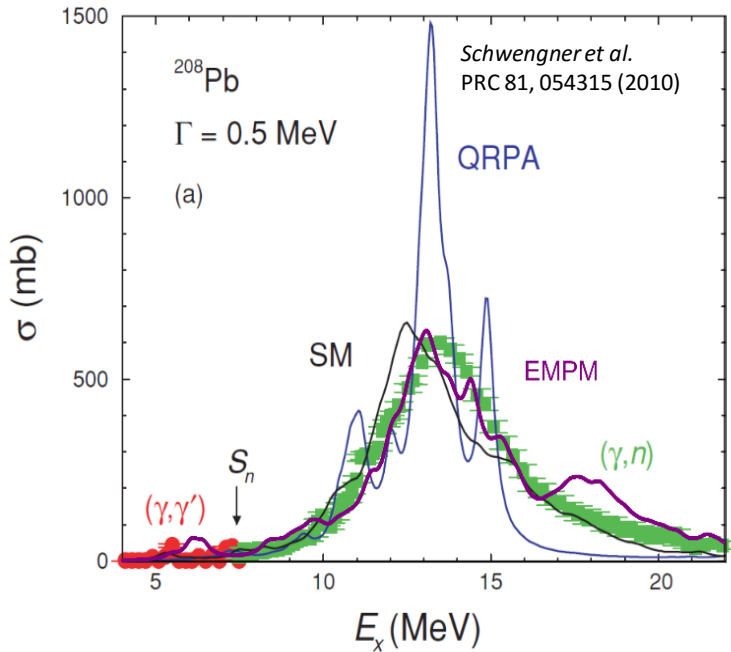
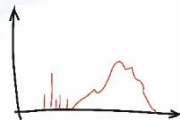


- truncation in phonon basis typically according to energy, collectivity ..
- description of spreading width due to the  $Q^+$  and  $[Q_1^+ \times Q_2^+]^{-}$  coupling
- spectrum becomes extremely rich in comparison with RPA (TDA)



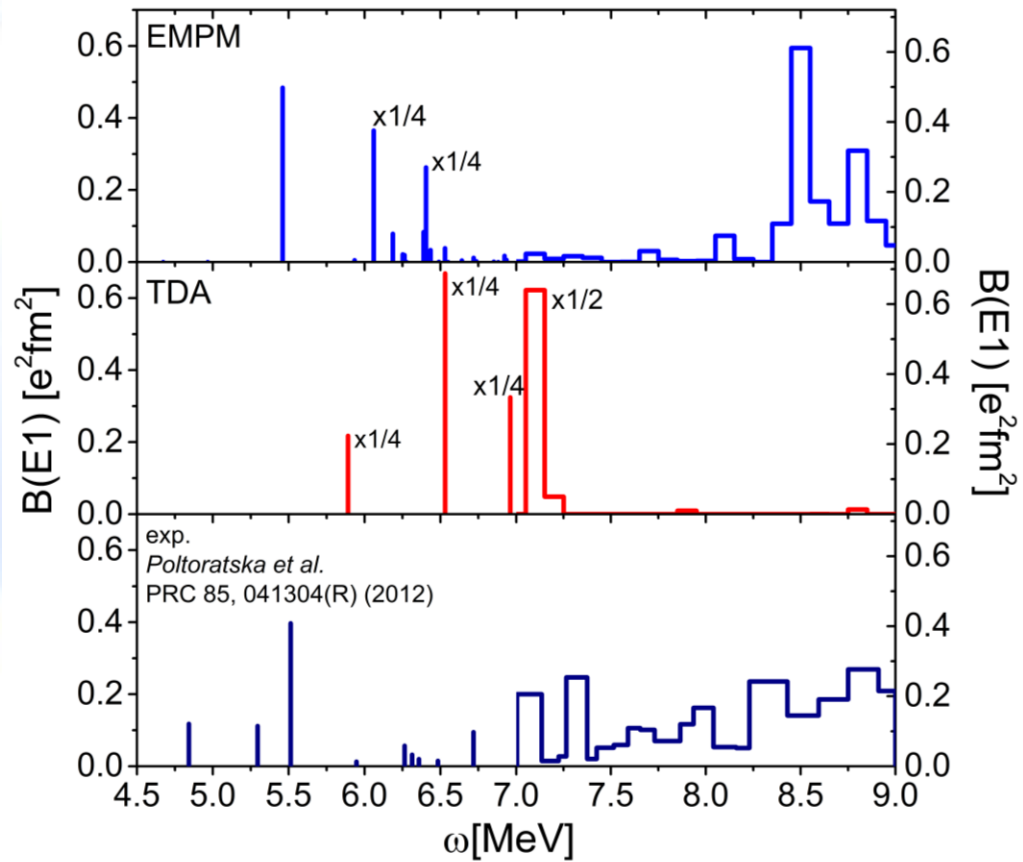
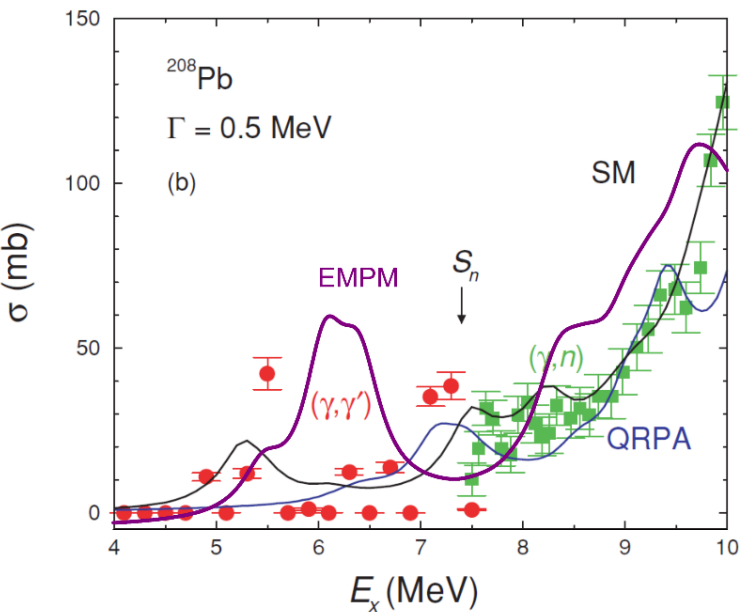


# Dipole strength in $^{208}\text{Pb}$



- EMPM predicts strength in the region 7-9 MeV whereas TDA and RPA not.
- density of states reasonable but few states are too strong

Could 3p-3h cure this? Suppression of 1p-1h component due to the 1-3 phonon coupling



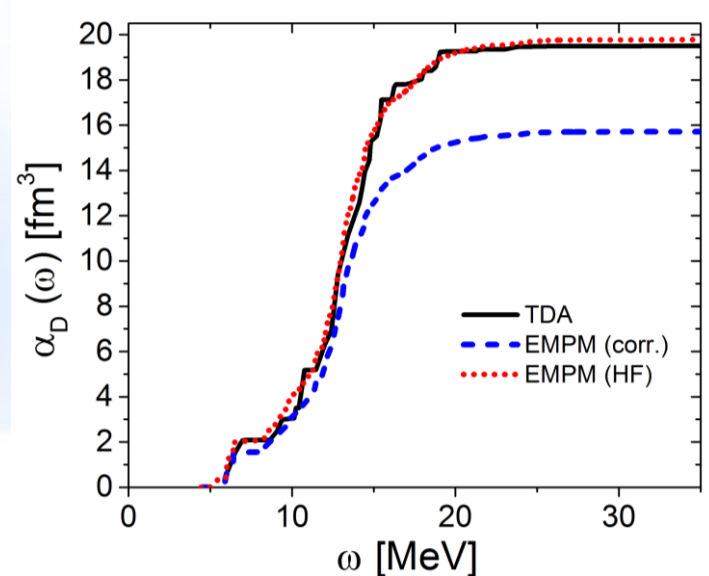
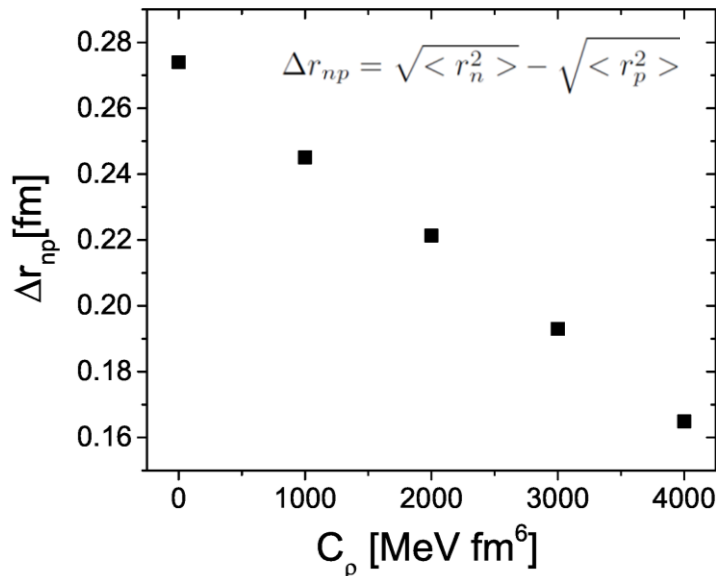
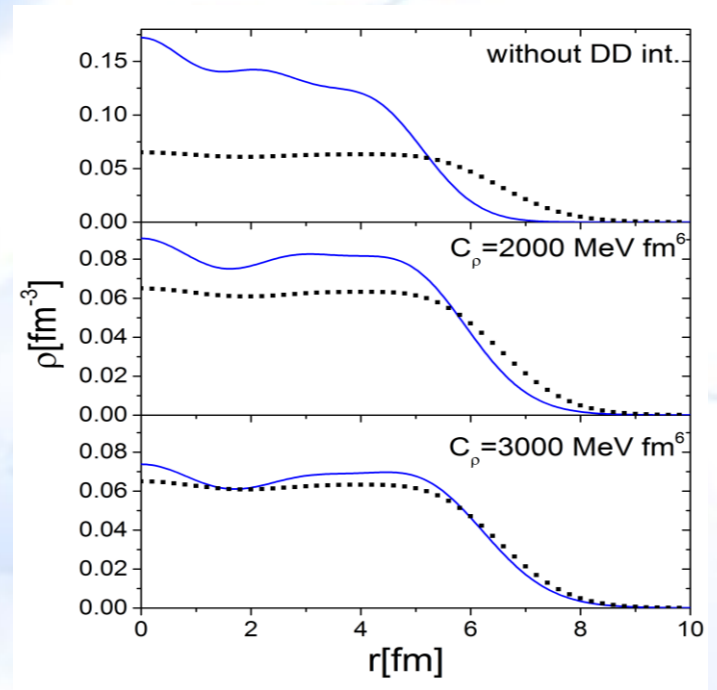
# Skin thickness and polarizability in $^{208}\text{Pb}$

- Skin thickness sensitive to strength of DD interaction.
- For  $C_p=2000 \text{ MeV fm}^6$  increase of skin thickness due to the g.s. correlations from 0.22fm at HF to 0.31 fm in EMPM

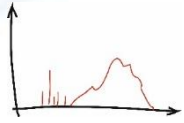
- Polarizability 
$$\alpha_D = \frac{\hbar c}{2\pi^2 e^2} \int_0^\infty \omega^{-2} \sigma(\omega) d\omega.$$

$\alpha_D(\text{HF})=19.8 \text{ fm}^3$  with HF w.f.

if correlations are taken into account we get  $\alpha_D(\text{corr.})=15.7 \text{ fm}^3$

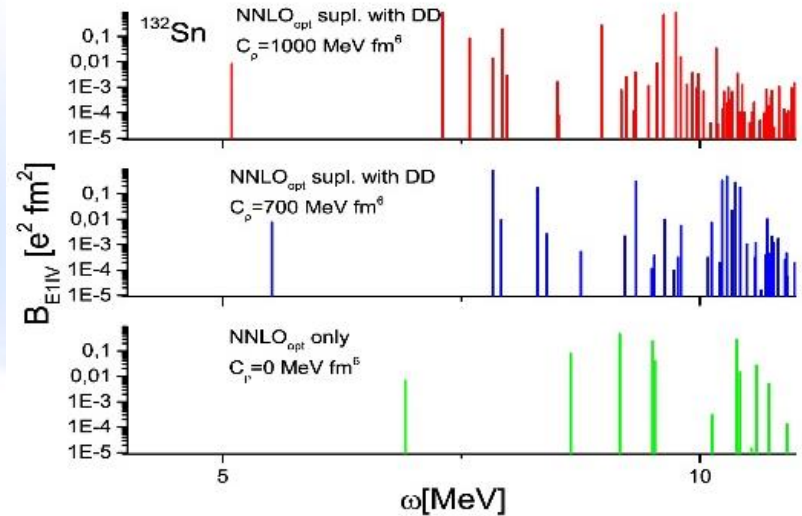
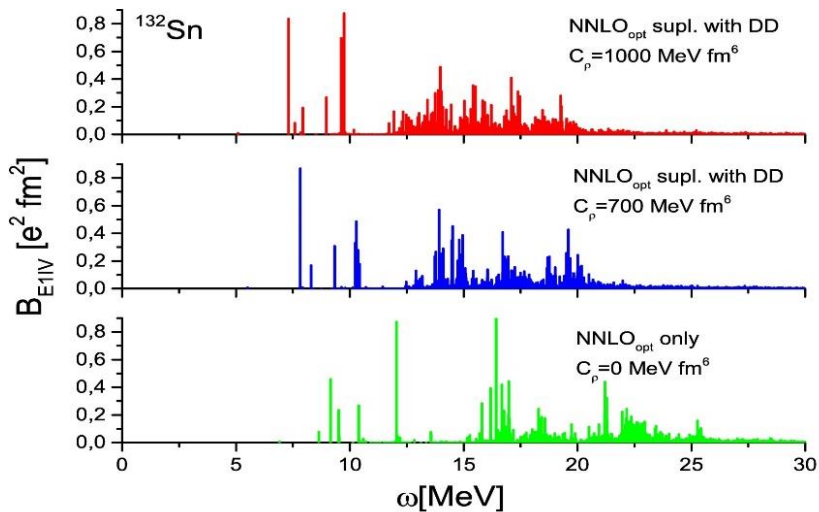
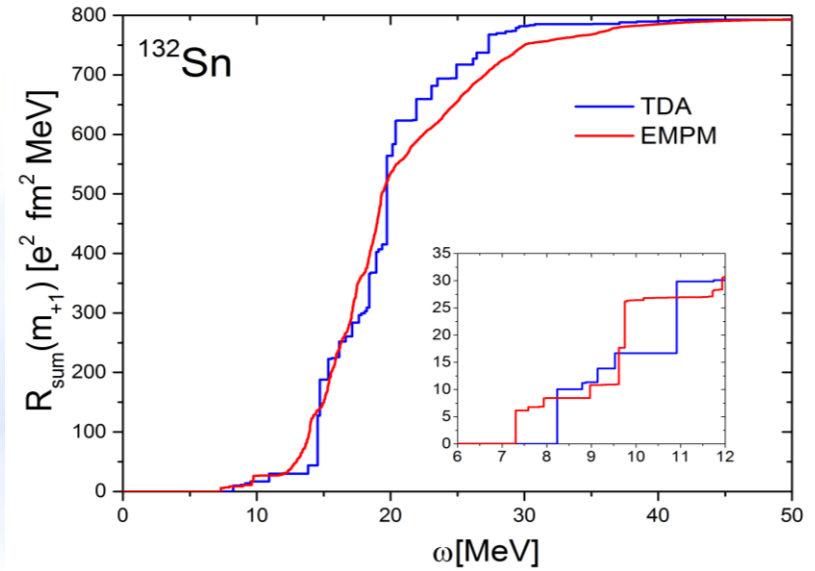
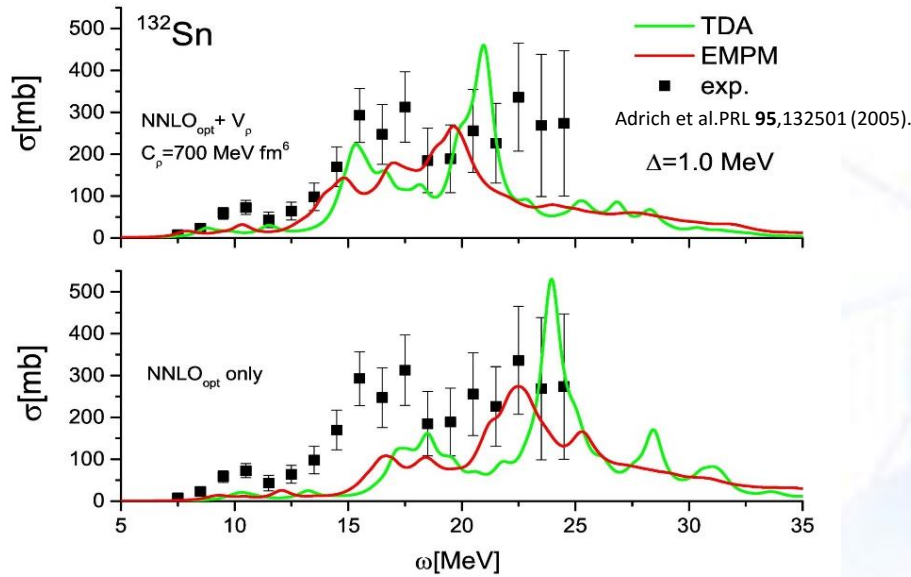


# Dipole strength in $^{132}\text{Sn}$



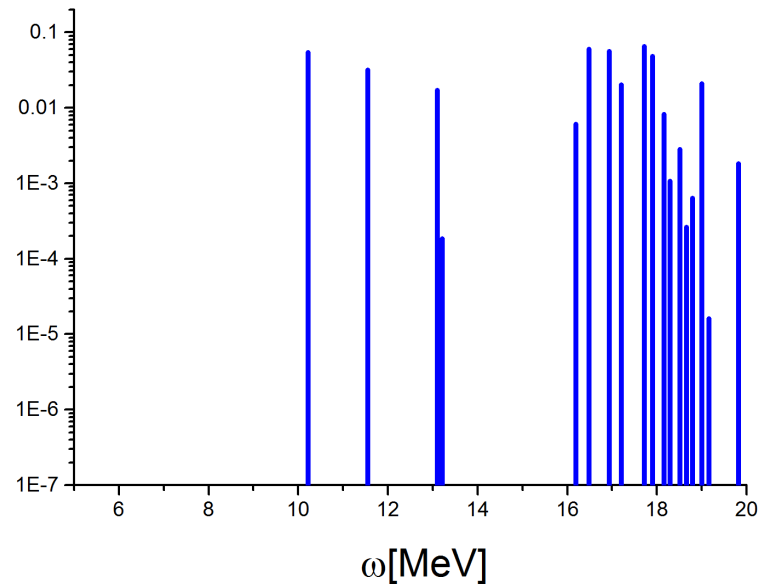
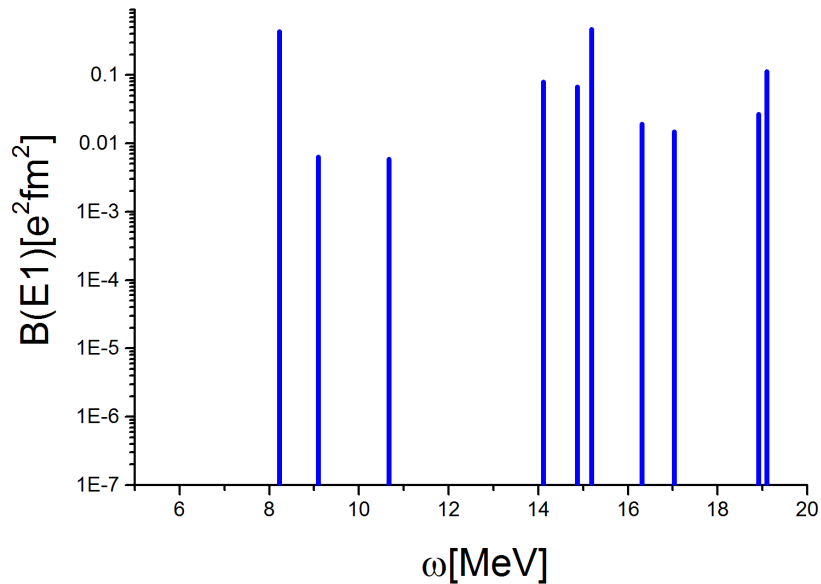
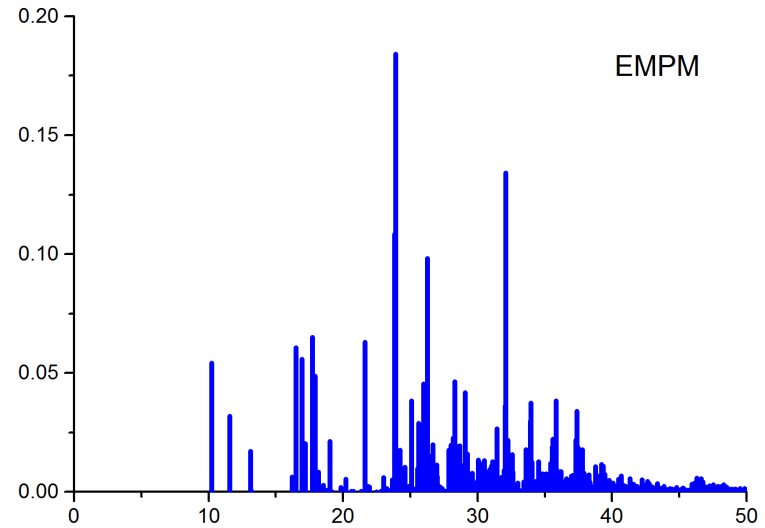
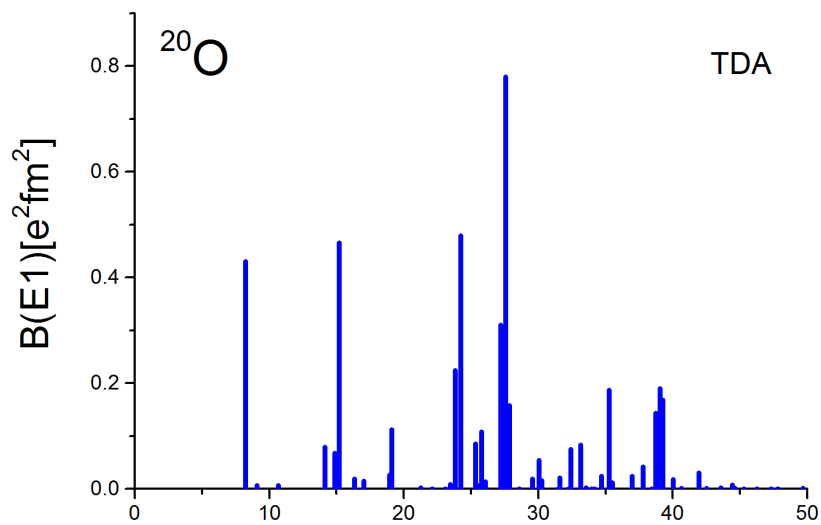
Similar picture as in lead.

details can be found in Knapp et al. Phys. Rev. C 90, 014310 (2014)



# Towards open-shell nuclei

**First results:** calculation up to 2 phonons (4qp excitations):  
strong coupling of valence neutrons with 1p-1h excitations



# Summary

- selfconsistent description of E1 strength with realistic NN potential (chiral NNLO<sub>opt</sub>)
- lowest states 1-phonon and 2-phonon character
- shape of GR: sum of many complicated states
- 2 –phonon states complicated combinations of  $[Q_1^+ \times Q_2^+] 1^-$   
 $[2^+ \times 1^-] 1^-$ ,  $[4^+ \times 3^-] 1^-$
- ground state correlations: g.s. w.f typically 80% HF and 20 % 2-phon.
- 2pon.-1-phon. coupling responsible for rich low-lying 1<sup>-</sup> spectrum  
-> detailed description of pygmy dipole mode, however, sensitive to s.p. details

## Future plans:

- first application of quasiparticle formalism for <sup>20</sup>O -> in future systematics of PDR strength for open-shell nuclei (P. Veselý)
- odd particle systems: particle phonon coupling (G. De Gregorio)
- 3-body force