## Correlations along the $\mathrm{N}=\mathrm{Z}$ line

Frédéric Nowacki ${ }^{1}$



European Gamma and Ancillary detectors Network

[^0]
## Landscape of medium mass nuclei



- New gaps: ${ }^{24} \mathrm{O},{ }^{48} \mathrm{Ni},{ }^{54} \mathrm{Ca},{ }^{78} \mathrm{Ni},{ }^{100} \mathrm{Sn}$
- Vanishing of shell closure: ${ }^{12} \mathrm{Be},{ }^{32} \mathrm{Mg},{ }^{42} \mathrm{Si},{ }^{64} \mathrm{Cr},{ }^{80} \mathrm{Zr}$...
- Island of deformation around $\mathrm{A} \sim 32, \mathrm{~A} \sim 64$
- Low-lying dipole excitations in $\mathrm{Ne}, \mathrm{Ni}$ isotopes
- Variety of phenomena dictated by shell structure
- Close connection between collective behaviour and underlying shell structure
- Interplay between
- Monopole field (spherical mean field)
- Multipole correlations (pairing, Q.Q, ...)
"Pairing plus Quadrupole propose, Monopole disposes"
A. Zuker, Coherent and Random Hamiltonians, CRN Preprint 1994



## Stable Nuclei



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In ${ }^{45} \mathrm{Sc}$, normal states and intruder states are degenerated! But the proton shell gap remains more or less constant ...


In ${ }^{45} \mathrm{Sc}$, normal states and intruder states are degenerated! But the proton shell gap remains more or less constant ...

Almost Island of Inversion at Stability !!!

## Stable Nuclei

## Intruders in Sc chain



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## Intruders in Sc chain



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## Stable Nuclei

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## Stable Nuclei

## Intruders in Sc chain



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## Stable Nuclei

## Intruders in Sc chain



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13 December 200

Physics Letters B 522 (2001) 240-244

PHYSICS LETTERS B
www.elsevier.com/locate/npe

Shell model description of isotope shifts in calcium
E. Caurier ${ }^{\text {a }}$, K. Langanke ${ }^{\text {b }}$, G. Martínez-Pinedo ${ }^{\text {b,c }}$, F. Nowacki ${ }^{\text {d }}$, P. Vogel ${ }^{\text {e }}$


## ZBM2 interaction:

- based on realistic TBME
- monopole corrections to ensure ${ }^{40} \mathrm{Ca}$ and ${ }^{48} \mathrm{Ca}$ gaps
- full space calculations
- almost free of center of mass contamination
- provides very good spectroscopy at sd-pf interface


## Isotope shifts in Calcium isotopes

Isotope shifts in Ca chain


Isotope shifts in Ca chain


## Isomer shift in ${ }^{38} \mathrm{~K}$

## Proton-neutron pairing correlations in the self-conjugate nucleus ${ }^{38} \mathrm{~K}$ probed via a direct measurement of the isomer shift



## Isomer shift in ${ }^{38} \mathrm{~K}$



## Isomer shift in



## Isomer shift in ${ }^{38} \mathrm{~K}$

Proton-neutron pairing correlations in the self-conjugate nucleus ${ }^{38} \mathrm{~K}$ probed via a direct measurement of the isomer shift
M. L. Bissell, ${ }^{1, *}$ J. Papuga, ${ }^{1}$ H. Naïdja, ${ }^{2,3,4}$ K. Kreim, ${ }^{5}$ K. Blaum, ${ }^{5}$ M. De Rydt, ${ }^{1}$ R. F. Garcia Ruiz, ${ }^{1}$ H. Heylen, ${ }^{1}$ M. Kowalska, ${ }^{6}$ R. Neugart,,${ }^{5,7}$ G. Neyens, ${ }^{1}$ W. Nörtershäuser, ${ }^{8,7}$ F. Nowacki, ${ }^{2}$ M. M. Rajabali, ${ }^{1}$ R. Sanchez, ${ }^{3,9}$ K. Sieja, ${ }^{2}$ and D. T. Yordanov ${ }^{5}$


FIG. 2. Changes in mean square charge radius referenced to
${ }^{38} \mathrm{~K}$. The systematic uncertainty related to the atomic specific mass shift is represented by the two dotted lines. Datum for ${ }^{37} \mathrm{~K}$ taken from [23].

FIG. 3. Changes in mean square charge radii between the self-conjugate nuclei ${ }^{36} \mathrm{Ar},{ }^{38} \mathrm{~K}$ and ${ }^{40} \mathrm{Ca}$ from this work and [29].

## Landscape of medium mass nuclei



# Island of inversion around ${ }^{64} \mathrm{Cr}$ 

S. M. Lenzi, ${ }^{1}$ F. Nowacki, ${ }^{2}$ A. Poves, ${ }^{3}$ and K. Sieja ${ }^{2, *}$
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${ }^{2}$ IPHC, IN2P3-CNRS et Université de Strasbourg, F-67037 Strasbourg, France
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(Received 10 September 2010; published 2 November 2010)

p1/2 $\qquad$ $\underline{\square}$
f5/2
p3/2 $\qquad$ $\longrightarrow$
$\qquad$


48
Ca

## LNPS interaction:

- based on realistic TBME
- new fit of the pf shell (KB3GR, E. Caurier)
- monopole corrections
- $g_{9 / 2}-d_{5 / 2}$ gap now constrained to 2.5 MeV in ${ }^{68} \mathrm{Ni}$


## Calculations:

- Up to $14 \hbar \omega$ excitations across $Z=28$ and $\mathrm{N}=40$ gaps
- Matrix diagonalizations up to $2.10^{10}$
- m-scheme code ANTOINE (non public parallel version)
- at first approximation, ${ }^{68} \mathrm{Ni}$ has a double closed shell structure for GS
- But low lying structure much more complex
- three coexisting $0^{+}$states appear between 0 and $\sim 2.5 \mathrm{MeV}$
- new location of $\mathrm{O}_{2}^{+}$state! Configuration mixing and relative transition rates between
low-spin states in ${ }^{68} \mathrm{Ni}$ :
F. Recchia et al.

Phys. Rev. C88, 041302(R) (2013)

- prediction of very low-lying superdeformed band ( $\beta_{2} \sim 0.4$ ) of
$6 p 6 h$ nature!
$\bullet$-S. Lenzi et al.
Phys. Rev. C82, 054301 (2010)
-A. Dijon et al.
Phys. Rev. C85, 0311301 (R) (2012)
shell model
exp.


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Triple coexistence in ${ }^{68} \mathrm{Ni}$

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```
(0p0h+2p2h)}\mp@subsup{}{}{v
```



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Evolution of Collectivity in ${ }^{72} \mathrm{Kr}$ ：Evidence for Rapid Shape Transition
H．Iwasaki，${ }^{1,2}$ A．Lemasson，${ }^{1}$ C．Morse，${ }^{1,2}$ A．Dewald，${ }^{3}$ T．Braunroth，${ }^{3}$ V．M．Bader ${ }^{1,{ }^{1,2}}$ T．Baugher，${ }^{1,2}$ D．Bazin，${ }^{1}$
J．S．Berryman，${ }^{1}$ C．M．Campbell，${ }^{4}$ A．Gade，${ }^{1,2}$ C．Langer，${ }^{1,5}$ I．Y．Lee，${ }^{4}$ C．Loelius，${ }^{1,2}$ E．Lunderberg，${ }^{1,2}$ F．Recchia，${ }^{1}$
D．Smalley，${ }^{1}$ S．R．Stroberg，,${ }^{1,2}$ R．Wadsworth，${ }^{6}$ C．Walz，${ }^{1,7}$ D．Weisshaar，${ }^{1}$ A．Westerberg，${ }^{8}$


IIIIIIIIII56 Ni

## Extension of LNPS interaction：

－based on realistic TBME
－new fit of the pf shell（KB3GR，E．Caurier）
－monopole corrections
－$g_{9 / 2}-d_{5 / 2}$ gap now constrained to 2.5 Mev in ${ }^{68} \mathrm{Ni}$
－$d_{5 / 2}$ location triggers deformation at $\mathrm{N}=\mathrm{Z}$

## Calculations：

－Up to $8 \hbar \omega$ excitations across $\mathrm{Z}=\mathrm{N}=40$ gaps
－Largest diagonalisation ever with Antoine

Evolution of Collectivity in ${ }^{72} \mathrm{Kr}$ : Evidence for Rapid Shape Transition
H. Iwasaki, ${ }^{1,2}$ A. Lemasson, ${ }^{1}$ C. Morse, ${ }^{1,2}$ A. Dewald, ${ }^{3}$ T. Braunroth, ${ }^{3}$ V. M. Bader, ${ }^{1,2}$ T. Baugher, ${ }^{1,2}$ D. Bazin, ${ }^{1}$ J. S. Berryman, ${ }^{1}$ C. M. Campbell, ${ }^{4}$ A. Gade, ${ }^{1,2}$ C. Langer, ${ }^{1,5}$ I. Y. Lee, ${ }^{4}$ C. Loelius, ${ }^{1,2}$ E. Lunderberg, ${ }^{1,2}$ F. Recchia, ${ }^{1}$ D. Smalley, ${ }^{1}$ S. R. Stroberg, ${ }^{1,2}$ R. Wadsworth, ${ }^{6}$ C. Walz, ${ }^{1,7}$ D. Weisshaar, ${ }^{1}$ A. Westerberg, ${ }^{8}$ K. Whitmore, ${ }^{1,2}$ and K. Wimmer ${ }^{1,8}$


## From Island of Inversion around $\mathrm{N}=40$ to $\mathrm{N}=\mathrm{Z}$

## Evolution of Collectivity in ${ }^{72} \mathrm{Kr}$ : Evidence for Rapid Shape Transition

H. Iwasaki, ${ }^{1,2}$ A. Lemasson, ${ }^{1}$ C. Morse, ${ }^{1,2}$ A. Dewald, ${ }^{3}$ T. Braunroth, ${ }^{3}$ V. M. Bader, ${ }^{1,2}$ T. Baugher, ${ }^{1,2}$ D. Bazin, ${ }^{1}$ J. S. Berryman, ${ }^{1}$ C. M. Campbell, ${ }^{4}$ A. Gade, ${ }^{1,2}$ C. Langer, ${ }^{1,5}$ I. Y. Lee, ${ }^{4}$ C. Loelius, ${ }^{1,2}$ E. Lunderberg, ${ }^{1,2}$ F. Recchia, ${ }^{1}$ D. Smalley, ${ }^{1}$ S. R. Stroberg, ${ }^{1,2}$ R. Wadsworth, ${ }^{6}$ C. Walz, ${ }^{1,7}$ D. Weisshaar, ${ }^{1}$ A. Westerberg, ${ }^{8}$


## ations:



- Up to $8 \hbar \omega$ excitations across $\mathrm{Z}=\mathrm{N}=40$ gaps
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## Landscape of medium mass nuclei



## New proton-neutron coupling scheme in ${ }^{92} \mathrm{Pd}$ ?



Claim for transition from Cooper pairs to aligned p-n pairs

## New proton-neutron coupling scheme in ${ }^{92} \mathrm{Pd}$ ?

shell model
$10^{+} \longrightarrow 4072$

- In A=90-100 region, spin-orbit is at play : strong $Z=50$ shell closure and the $g_{\frac{9}{2}}$ orbital deeply bound with respect to the remaining $g d s$ orbitals
- level schemes of $A \sim 90$ nuclei to be described within $g_{\frac{9}{2}}$ orbital
- regular level spacing and constant BE2's
- wave function analysis lead to

$$
\text { condensate of }(p n)^{J=9+} \text { pairs }
$$

$6^{+}-2466$
$4^{+}-1708$
$2+878$
exp.



$0^{+} \longrightarrow 0$


- 1) build $\left(j_{p} j_{n}\right)_{J=2 j}^{N}$ objects
- 2) diagonalise $(J=2 j ; T=0)$ single matrix element for given system
- take the overlap with effective wave function
- take the expectation value of pair counting operator
- first two methods give $\sim$ results , and provide relative estimate
- counting pairs should provide absolute estimate


## New proton-neutron coupling scheme in ${ }^{92} \mathrm{Pd}$

- calculations with effective $g_{\frac{9}{2}}$ (Chong et al.) and JUN45 (Otsuka et al.) interactions
- striking similarity of computed spectra
- regular level spacing and constant BE2's
- BUT quantitative differences between wave functions and underlying physics
- $29 \%$ of $\left(g_{\frac{9}{2}}\right)^{12}$ configuration left in the full space calculation
-     - vanishing Q's in $r 3 g$
- large and constant in $g_{\frac{9}{2}}$
sm g9
exp.
sm f5p3p1g9

smg9 exp. sm f5p3p1g9
Table: correlated JT=90 pairs content in the yrast band of in ${ }^{92} \mathrm{Pd}$.

| $J^{\pi}$ | cond $\mid \Psi_{92} P d$ <br> $g_{9 / 2}$ | $\langle$ cond $\| \Psi_{92} P d$ <br> r3g |
| ---: | :---: | :---: |
| $0^{+}$ | 0.83 | 0.45 |
| $2^{+}$ | 0.87 | 0.48 |
| $4^{+}$ | 0.91 | 0.58 |
| $6^{+}$ | 0.87 | 0.62 |
| $6^{+}$ | 0.73 | 0.57 |
| $8^{+}$ | 0.86 | 0.69 |
| $10^{+}$ | 0.35 | 0.34 |
| $\vdots$ | $\vdots$ | $\vdots$ |
| $24^{+}$ | 1.00 | 0.99 |

smg9 exp. sm f5p3p1g9
Table: correlated JT=90 pairs content in the yrast band of in ${ }^{92} \mathrm{Pd}$.


## Case of ${ }^{52} \mathrm{Fe}$ (mate of ${ }^{96} \mathrm{Cd}$ )

Table : correlated JT=70 pairs content in the yrast band of in ${ }^{52} \mathrm{Fe}$.

| $J^{\pi}$ | $\left\langle\right.$ cond $\left.\mid \Psi_{52} \mathrm{Fe}\right\rangle$ <br> $\mathrm{f}_{7 / 2}$ | (cond $\left\|\Psi_{52} \mathrm{Fe}\right\rangle$ <br> fp |
| :---: | :---: | :---: |
| $0^{+}$ | 0.99 | 0.66 |
| $2^{+}$ | 0.99 | 0.66 |
| $4^{+}$ | 0.99 | 0.66 |
| $6^{+}$ | 0.98 | 0.54 |
| $8^{+}$ | 0.99 | 0.75 |
| $10^{+}$ | 0.99 | 0.81 |
| $12^{+}$ | 1.00 | 0.81 |



## Case of ${ }^{52} \mathrm{Fe}$ (mate of ${ }^{96} \mathrm{Cd}$ )



## Landscape of medium mass nuclei




$\beta$ decay of ${ }^{100}$ Sn


- State-of-the art SM calculations in good agreement with experiment
- First information on the $\mathrm{Z}=50$ proton gap (neutron gap inferred from our previous studies PRL 107 (2011) 172502, PRC 84 (2011) 044311)
${ }^{100}$ Sn paradox: very stable with respect to strong force while very unstable with respect to weak force!

A. Banu et al.,

Phys. Rev. C72, 061305(R) (2005)

## Coulomb Excitation of ${ }^{104} \mathrm{Sn}$ and the Strength of the ${ }^{100} \mathrm{Sn}$ Shell Closure

G. Guastalla, ${ }^{1}$ D. D. DiJulio, ${ }^{2}$ M. Górska, ${ }^{3}$ J. Cederkäll, ${ }^{2}$ P. Boutachkov, ${ }^{1,3}$ P. Golubev, ${ }^{2}$ S. Pietri, ${ }^{3}$ H. Grawe, ${ }^{3}$ F. Nowacki, ${ }^{4}$ K. Sieja, ${ }^{4}$ A. Algora, ${ }^{5,6}$ F. Ameil, ${ }^{3}$ T. Arici, ${ }^{7,3}$ A. Atac, ${ }^{8}$ M. A. Bentley, ${ }^{9}$ A. Blazhev, ${ }^{10}$ D. Bloor, ${ }^{9}$ S. Brambilla, ${ }^{11}$
N. Braun, ${ }^{10}$ F. Camera, ${ }^{11}$ Zs. Dombrádi, ${ }^{6}$ C. Domingo Pardo, ${ }^{5}$ A. Estrade,,${ }^{3}$ F. Farinon,,${ }^{3}$ J. Gerl, ${ }^{3}$ N. Goel, ${ }^{3,1}$ J. Grȩbosz, ${ }^{12}$
T. Habermann, ${ }^{3,13}$ R. Hoischen, ${ }^{2}$ K. Jansson, ${ }^{2}$ J. Jolie, ${ }^{10}$ A. Jungclaus, ${ }^{14}$ I. Kojouharov, ${ }^{3}$ R. Knoebel, ${ }^{3}$ R. Kumar, ${ }^{15}$
J. Kurcewicz, ${ }^{16}$ N. Kurz, ${ }^{3}$ N. Lalović, ${ }^{3}$ E. Merchan, ${ }^{1,3}$ K. Moschner, ${ }^{10}$ F. Naqvi, ${ }^{3,10}$ B. S. Nara Singh, ${ }^{9}$ J. Nyberg, ${ }^{17}$
C. Nociforo, ${ }^{3}$ A. Obertelli, ${ }^{18}$ M. Pfützner, ${ }^{3,16}$ N. Pietralla, ${ }^{1}$ Z. Podolyák, ${ }^{19}$ A. Prochazka, ${ }^{3}$ D. Ralet, ${ }^{1,3}$ P. Reiter, ${ }^{10}$
D. Rudolph, ${ }^{2}$ H. Schaffner, ${ }^{3}$ F. Schirru, ${ }^{19}$ L. Scruton, ${ }^{9}$ D. Sohler, ${ }^{6}$ T. Swaleh, ${ }^{2}$ J. Taprogge, ${ }^{10,20}$ Zs. Vajta, ${ }^{6}$ R. Wadsworth, ${ }^{9}$
N. Warr, ${ }^{10}$ H. Weick, ${ }^{3}$ A. Wendt, ${ }^{10}$ O. Wieland, ${ }^{11}$ J. S. Winfield, ${ }^{3}$ and H. J. Wollersheim ${ }^{3}$


- overall agreement with recent experimental data
- strong sensitivity to (unknown) proton gap
- decrease of proton gap by 1 MeV increase $\mathrm{B}(\mathrm{E} 2)$ by $30 \%$ !!!
- Monopole drift develops in all regions but the Interplay between correlations (pairing + quadrupole) and spherical mean-field (monopole field) determines the physics. It can vary far from stability from
- island of deformation at $\mathrm{N}=20$ and $\mathrm{N}=40$
- deformation at $Z=14, N=28$ for ${ }^{42} \mathrm{Si}$ and shell weakening at $Z=28$, $\mathrm{N}=50$ for ${ }^{78} \mathrm{Ni}$
but also along $\mathrm{N}=\mathrm{Z}$ line
- enhanced $T=1$ pairing correlations
- enhanced Quadrupole correlations as in the case of extremely deformed rotors in the $\mathrm{A} \sim 80$ region
- Quadrupole energies can be huge and understood in terms of symmetries

Thanks to:

- E. Caurier, H. Naidja, K. Sieja, A. Zuker
- A. Poves, G. Martinez-Pinedo
- H. Grawe, S. Lenzi, O. Sorlin


[^0]:    ${ }^{1}$ Strasbourg-Madrid Shell-Model collaboration

