

Recent studies on the nuclear physics input for the r-process nucleosynthesis

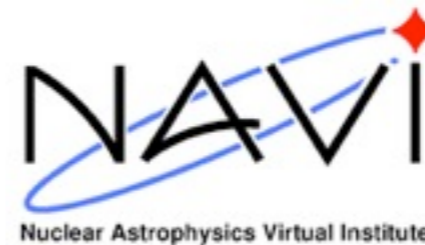
Tomás R. Rodríguez



Bundesministerium
für Bildung
und Forschung



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Nuclear Astrophysics Virtual Institute

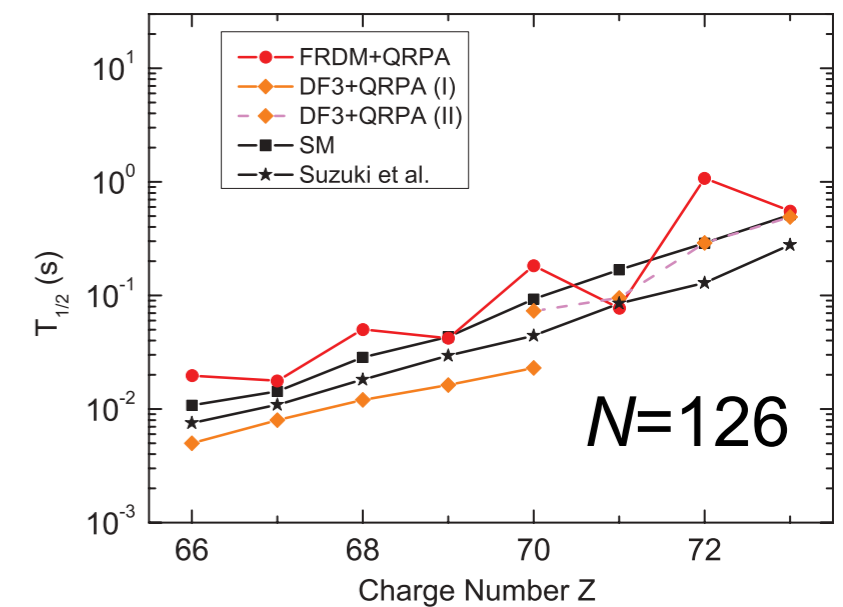
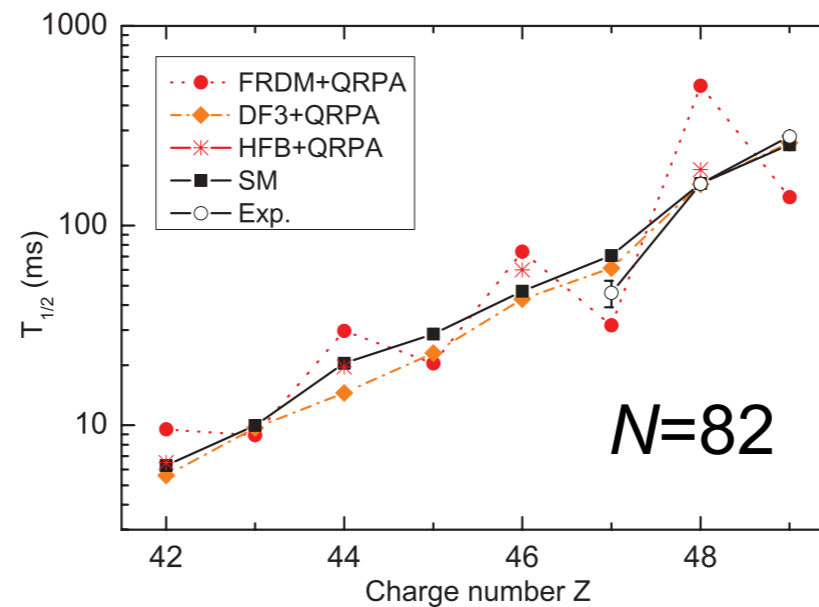
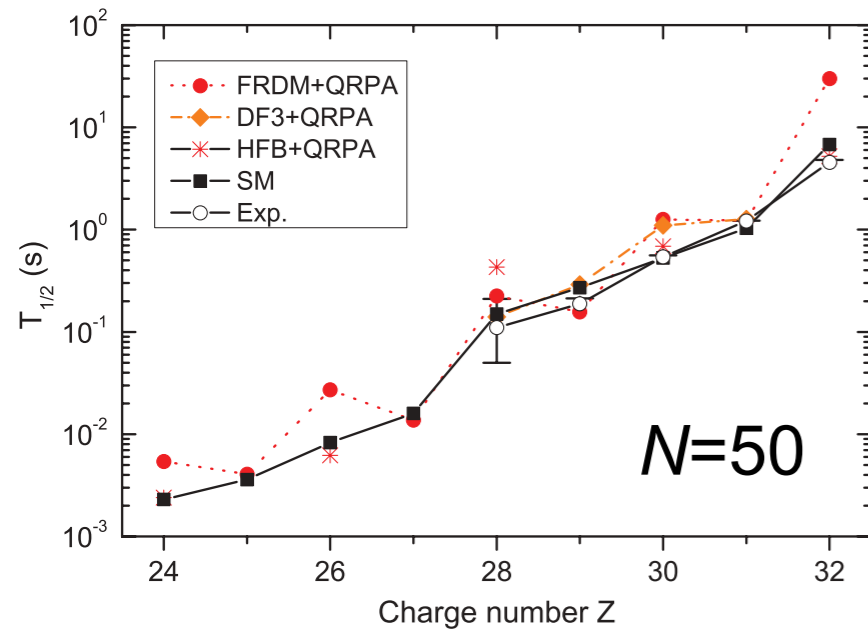


Helmholtz International Center

Outline

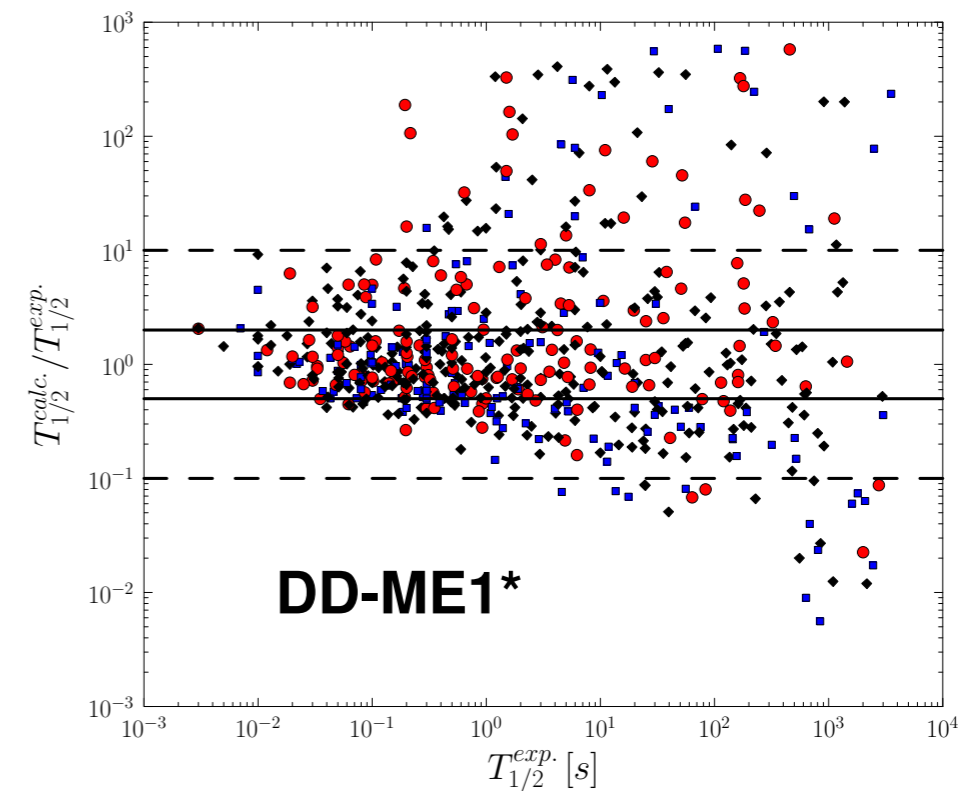
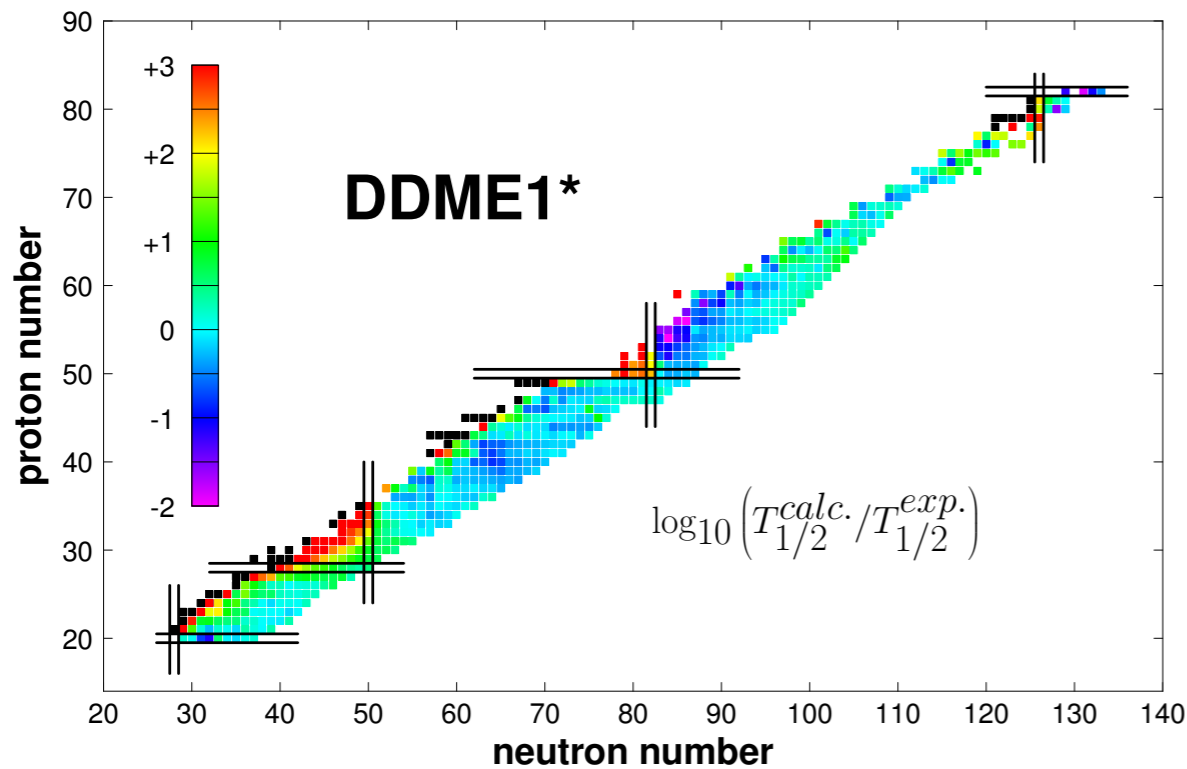
- Introduction.
- Results on beta decay half-lives.
- Developments in microscopic nuclear mass models.
- Summary and outlook

Beta-decay half-lives. Shell Model



- ▶ Shell Model calculations including first forbidden transitions for $N = 50, 82, 126$.
- ▶ Very good agreement with the available experimental data
- ▶ Less significant odd-even effects than in FRDM model

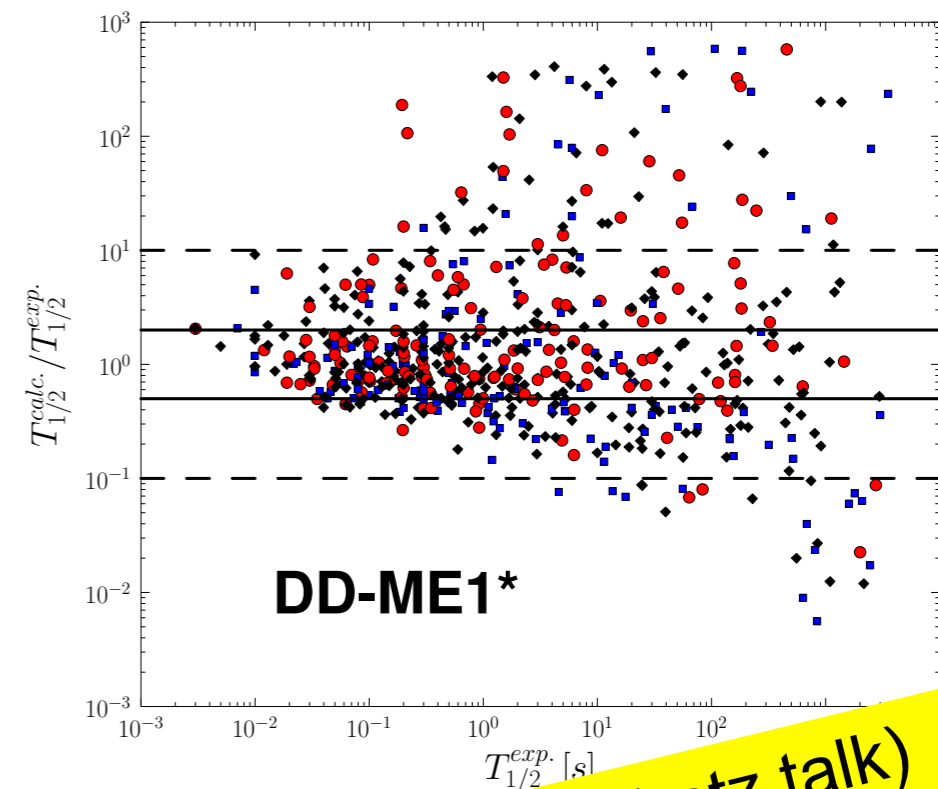
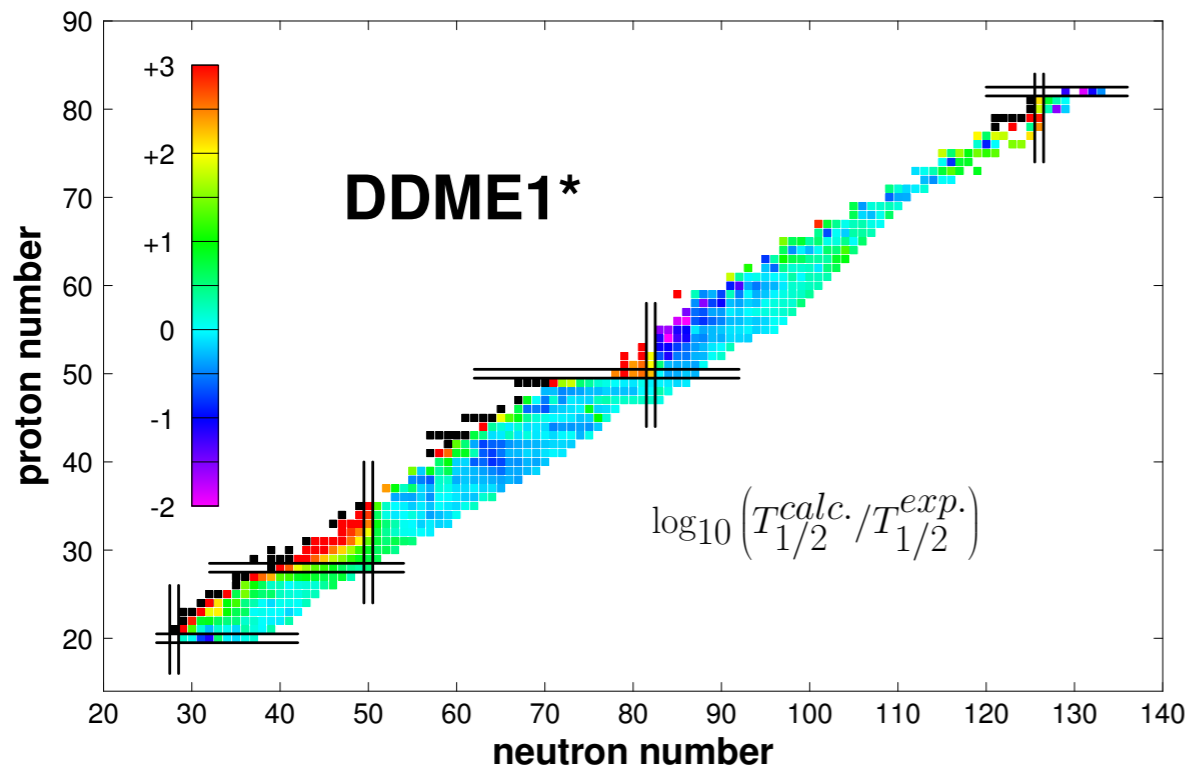
Beta-decay half-lives. CDFT method



- ▶ Global calculations using spherical covariant DFT+pnQRPA calculations.
- ▶ Good agreement with the experimental data, particularly in short-lived nuclei.

T. Marketin *et al.*, in preparation

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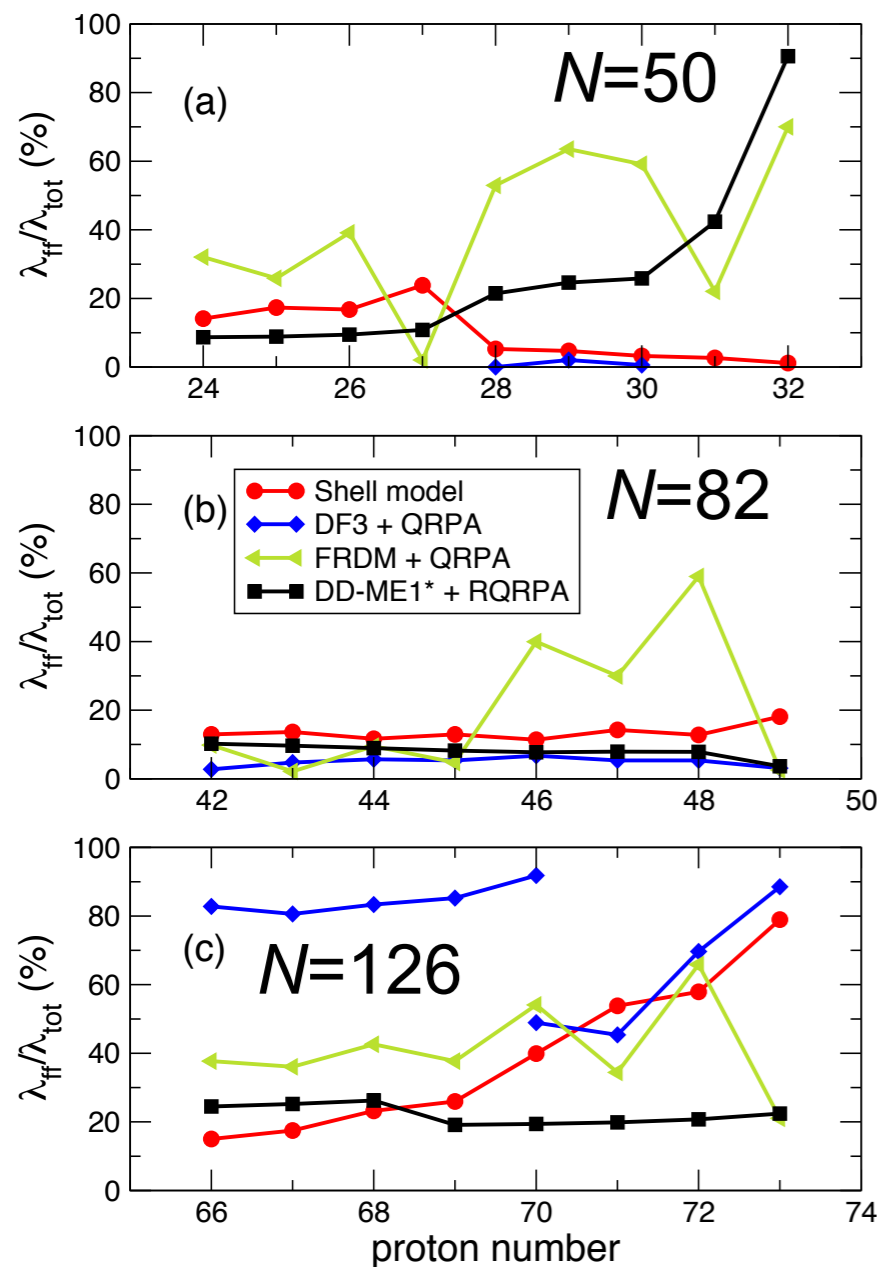


- ▶ Global calculations using spherical covariation and QRPA calculations.
- ▶ Good agreement with the experimental data, particularly in short-lived nuclei.

See also Fang and Brown QRPA calculations (see H. Schatz talk)

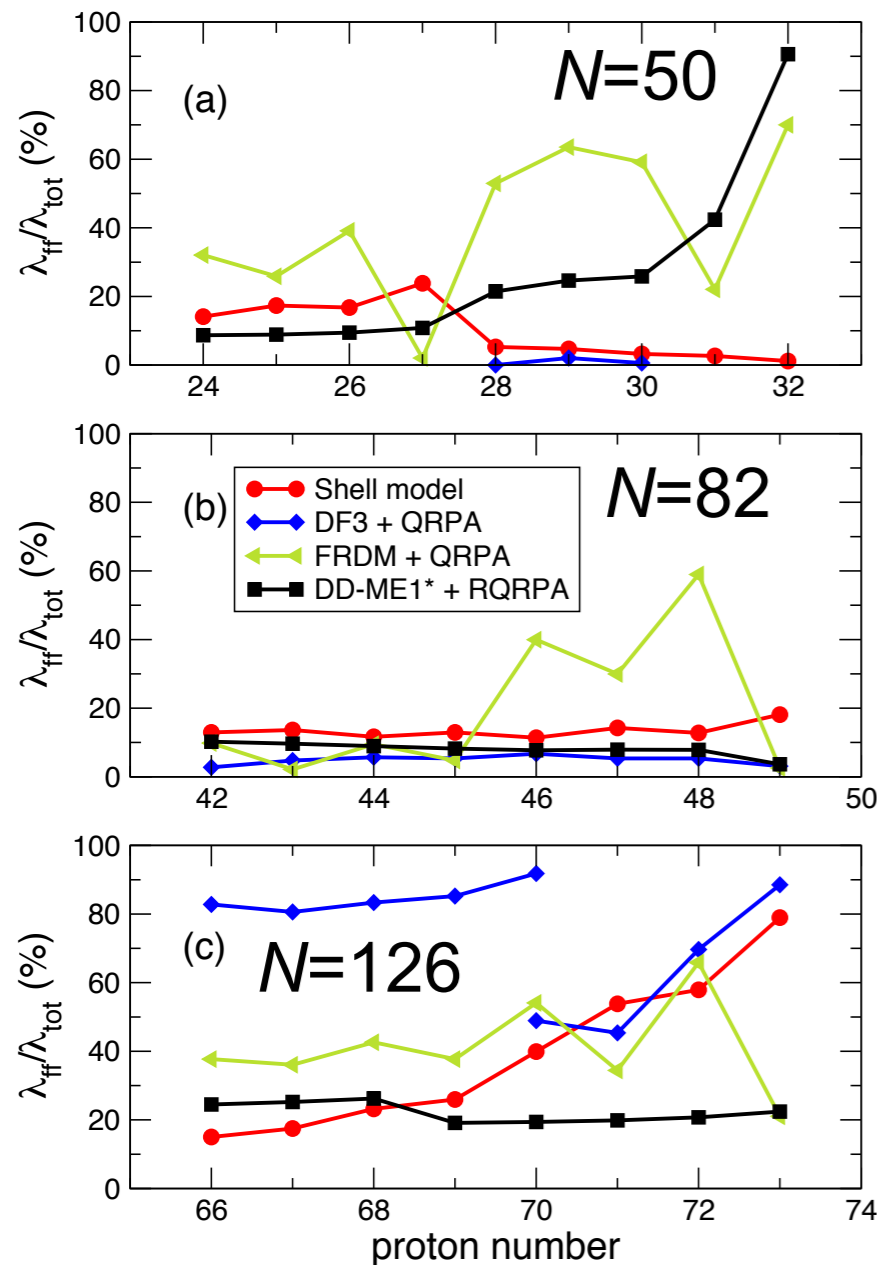
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Beta-decay half-lives. First forbidden contribution

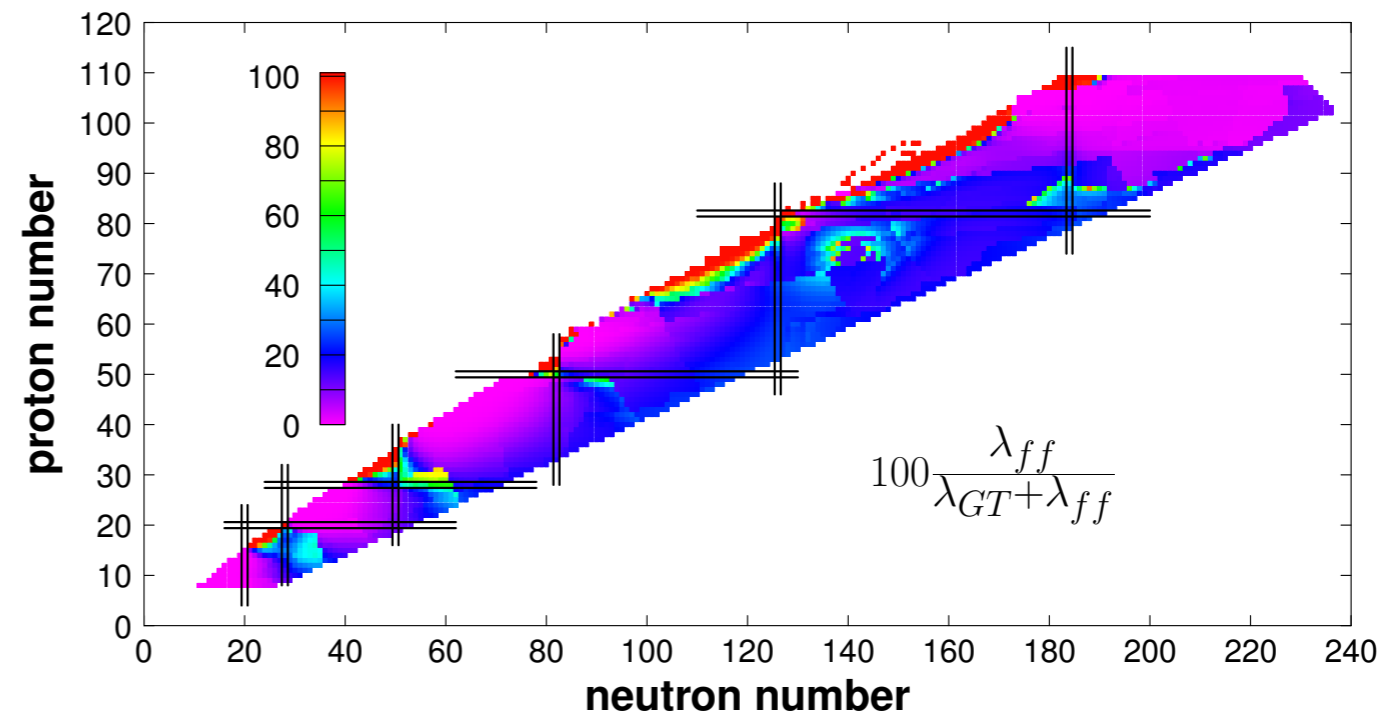


- ▶ For $N=50$, first forbidden contributions increase above $Z=28$ for CDFT calculations while they are negligible for SM.
- ▶ For $N=82$, first forbidden contributions remain small both for CDFT and SM calculations.
- ▶ For $N=126$, first forbidden contributions increase with proton number in SM while remain constant for CDFT.
- ▶ For FRDM, a less smooth result is obtained.

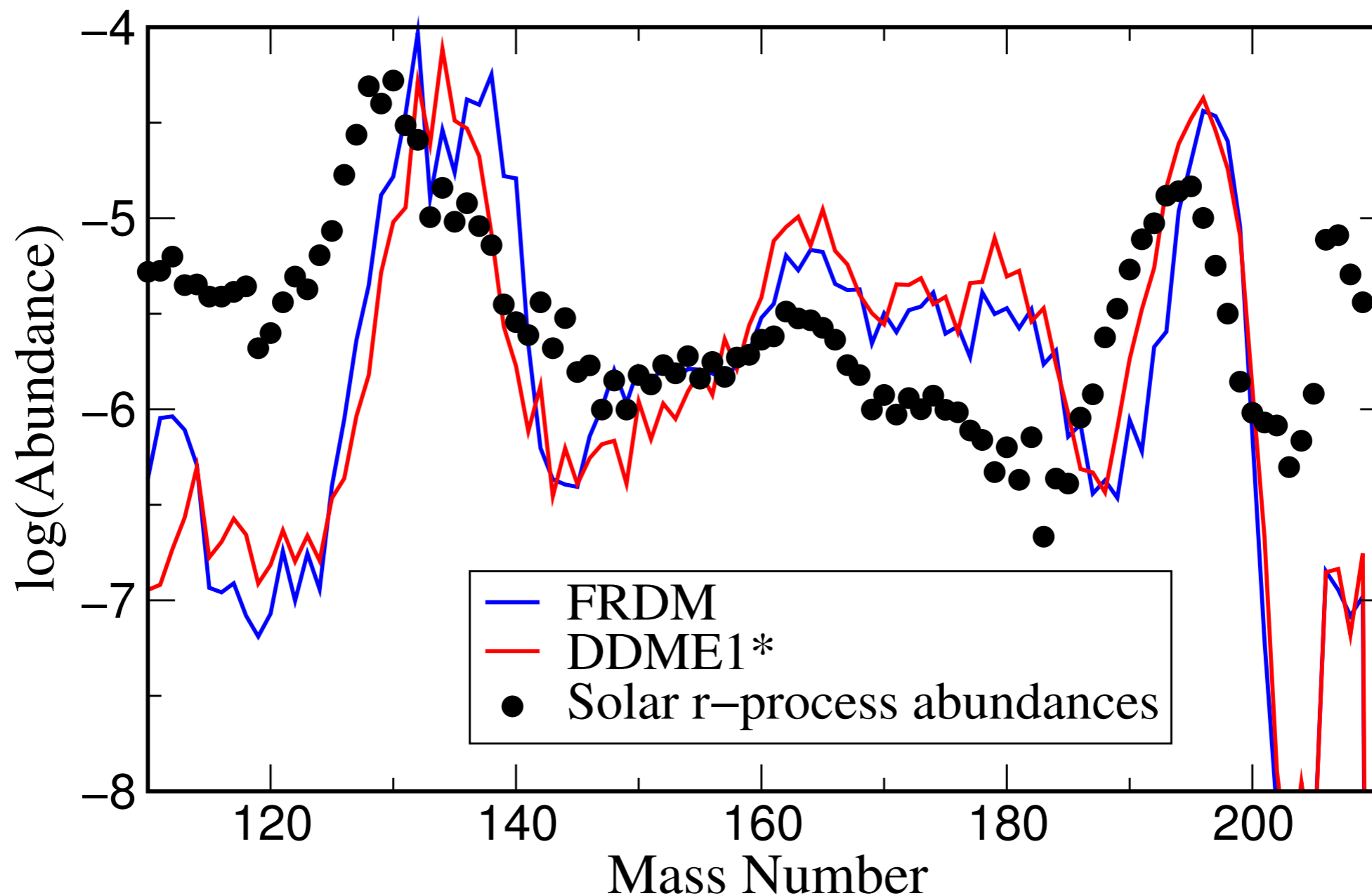
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- ▶ For $N=126$, first forbidden contributions increase with proton number in SM while remain constant for CDFT.
- ▶ For FRDM, a less smooth result is obtained.
- ▶ Systematics of the first forbidden contributions can be performed within the CDFT framework.



Beta-decay half-lives. Impact on r-process nucleosynthesis

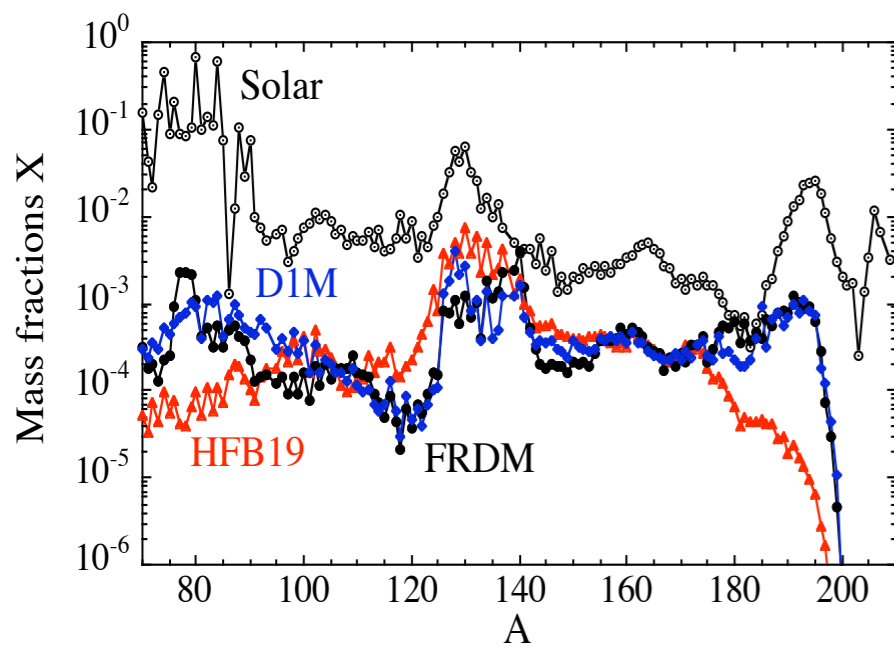


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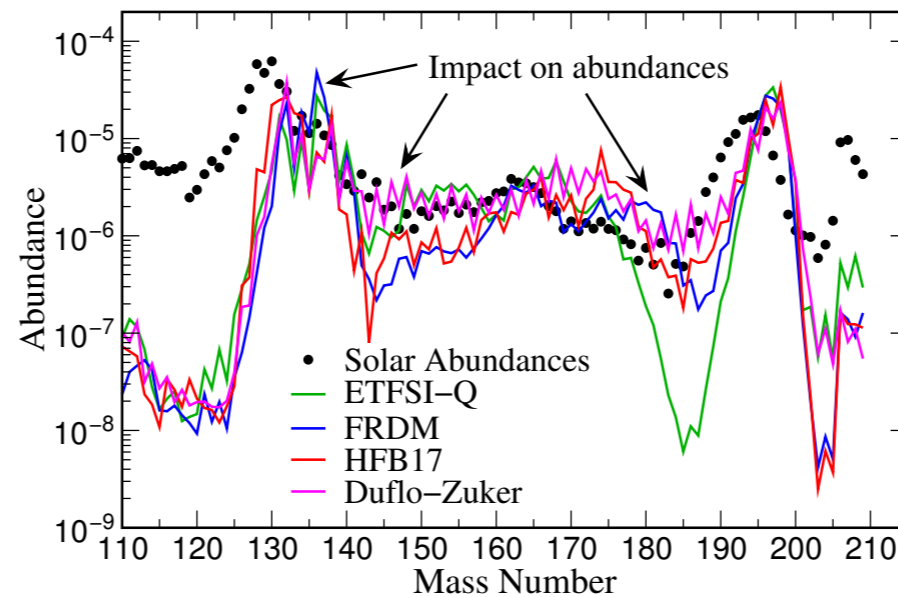
Nuclear masses

- Nuclear masses determine in r-process nucleosynthesis:
 - ▶ Neutron capture rates.
 - ▶ Beta decay Q-values.

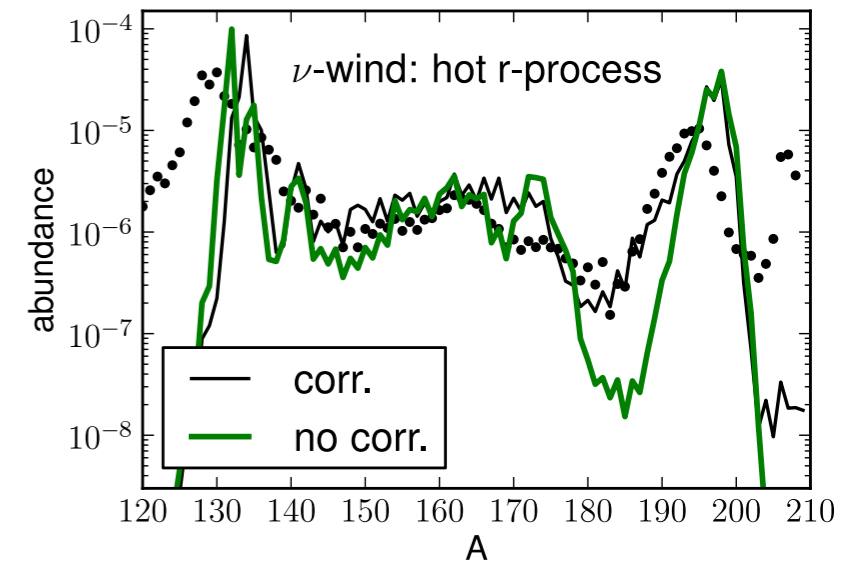
Final abundances depend on the mass model used (for the same astrophysical conditions)



Goriely et al.



Arcones and Martínez-Pinedo,
PRC 83, 045809 (2011)

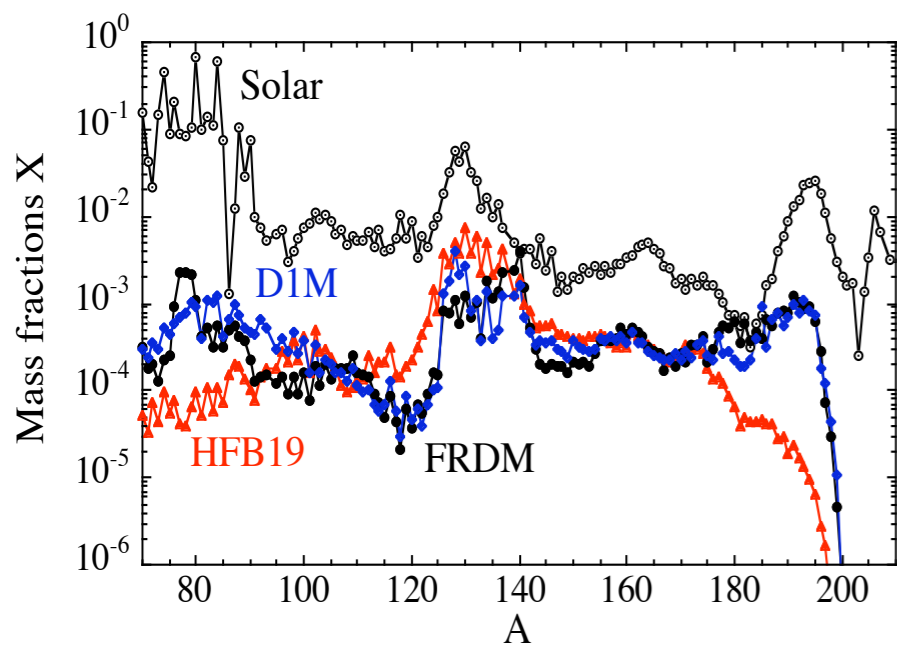


Arcones and Bertsch,
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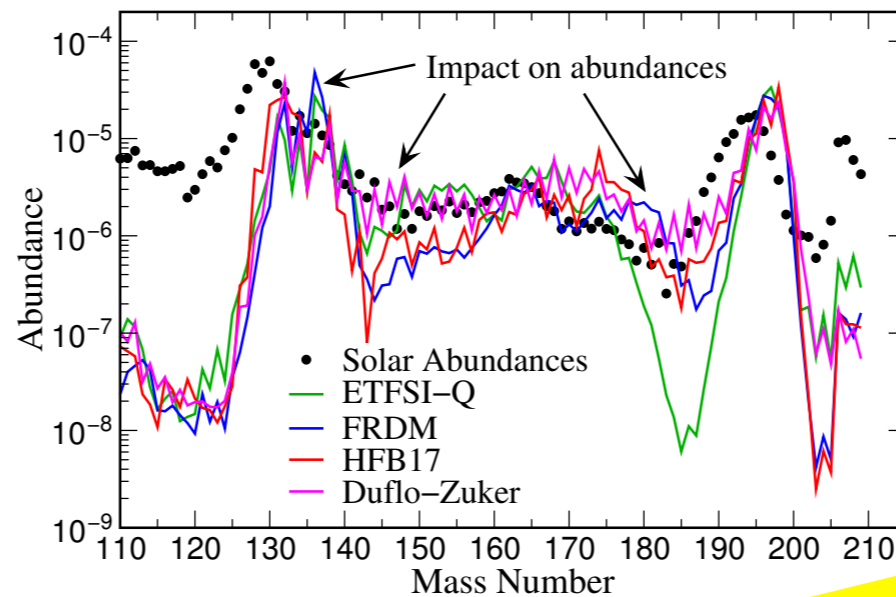
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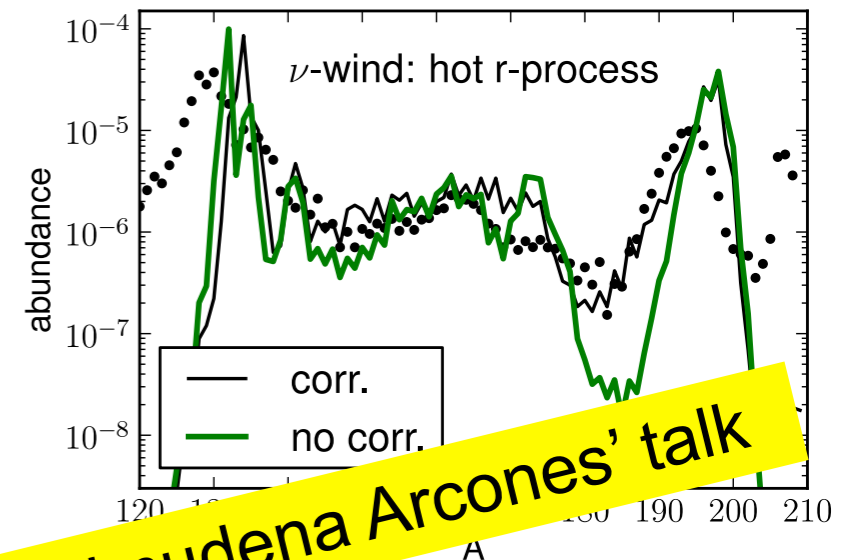
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see Almudena Arcones' talk

Ab-initio nuclear masses

Nuclear binding energies have been computed recently for heavier nuclei using chiral effective field theory interactions

H. Hergert et al., Phys. Rev. C 87, 034307 (2013)

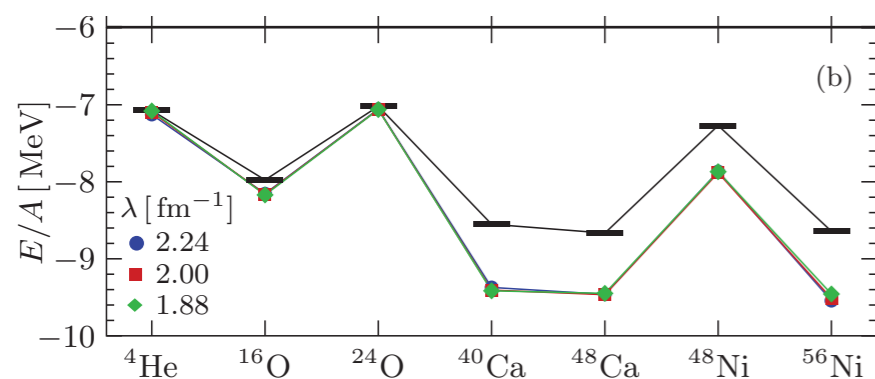
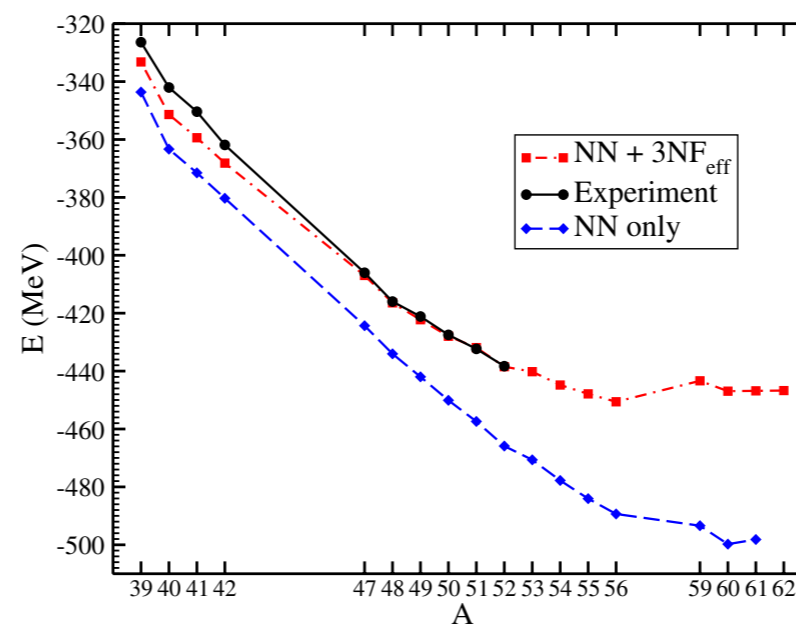
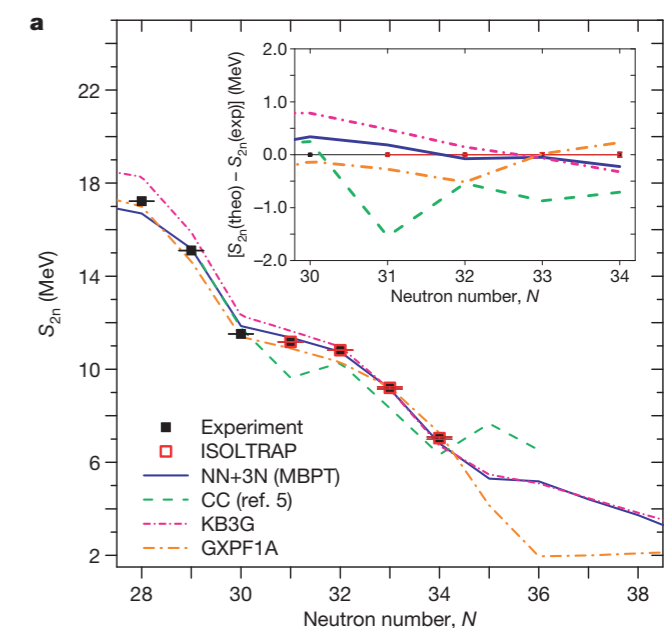


FIG. 7. (Color online) IM-SRG(2) ground-state energy per nucleon of closed-shell nuclei for $NN + 3N$ -induced (top) and $NN + 3N$ -full Hamiltonians (bottom) at different resolution scales λ . Energies are determined at optimal $\hbar\Omega$ for $e_{\text{Max}} = 14$. Experimental energies (black bars) are taken from Ref. [44].

G. Hagen et al., Phys. Rev. Lett. 109, 032502 (2012)



F. Wienholtz et al, Nature 498, 346 (2013)



Ab-initio methods are far from being useful for nucleosynthesis simulations:

- Limited to magic or semi-magic nuclei.
- Limited accuracy so far (too much overbinding).
- Good results in some regions while in other regions are very bad.
- Missing many body forces, uncertainties in the three body coupling constants, etc.

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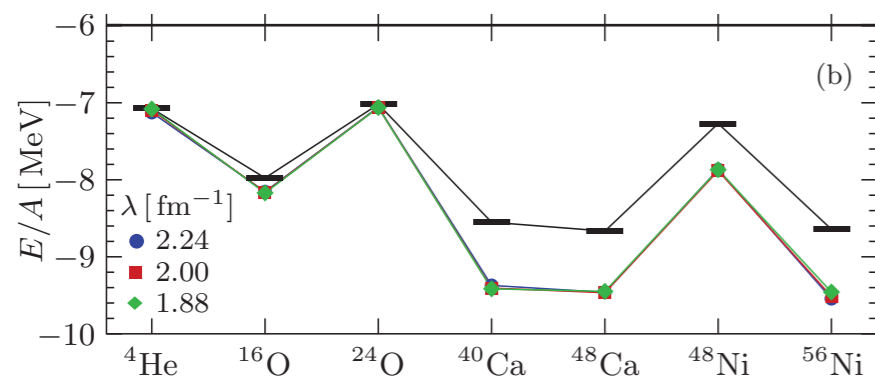
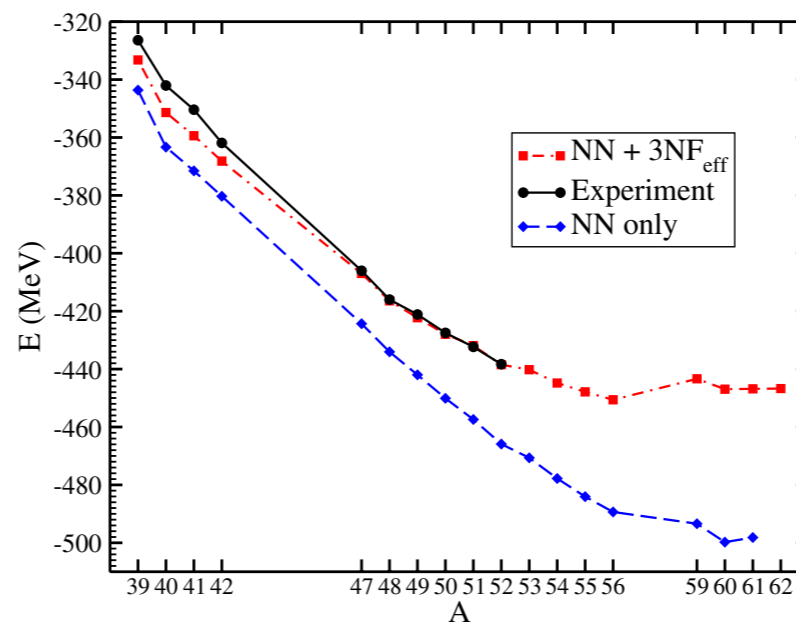
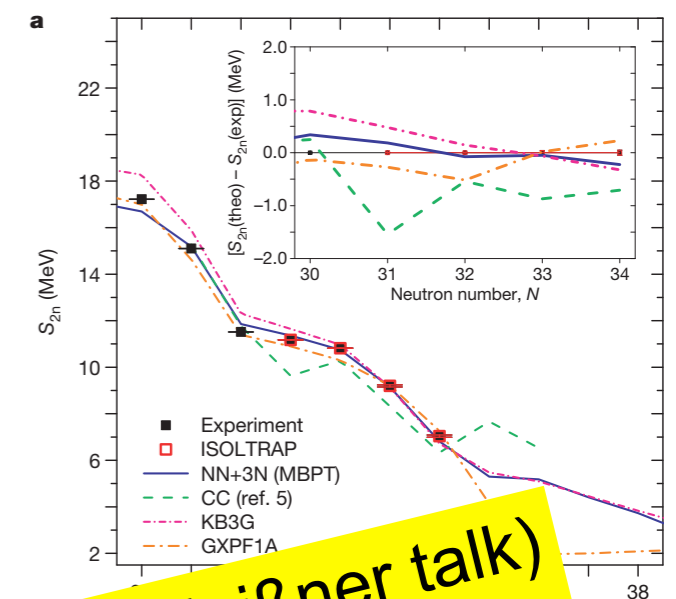


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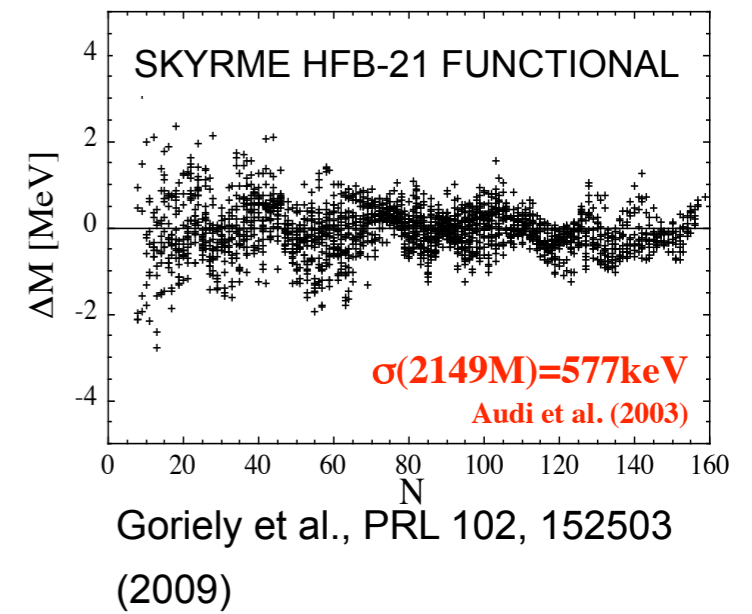
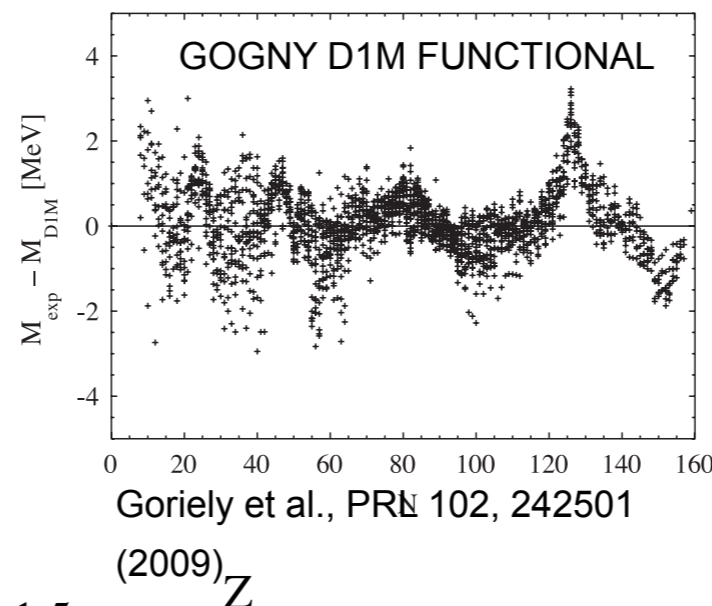
Ab-initio methods are far from being useful for general calculations:

- Limited to magic or semi-magic nuclei
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- Good results in some regions are very bad.
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- Nuclear physics calculations on the lattice (see Ulf G. Meißner talk)
- FMD with UCOM (see T. Neff's talk)

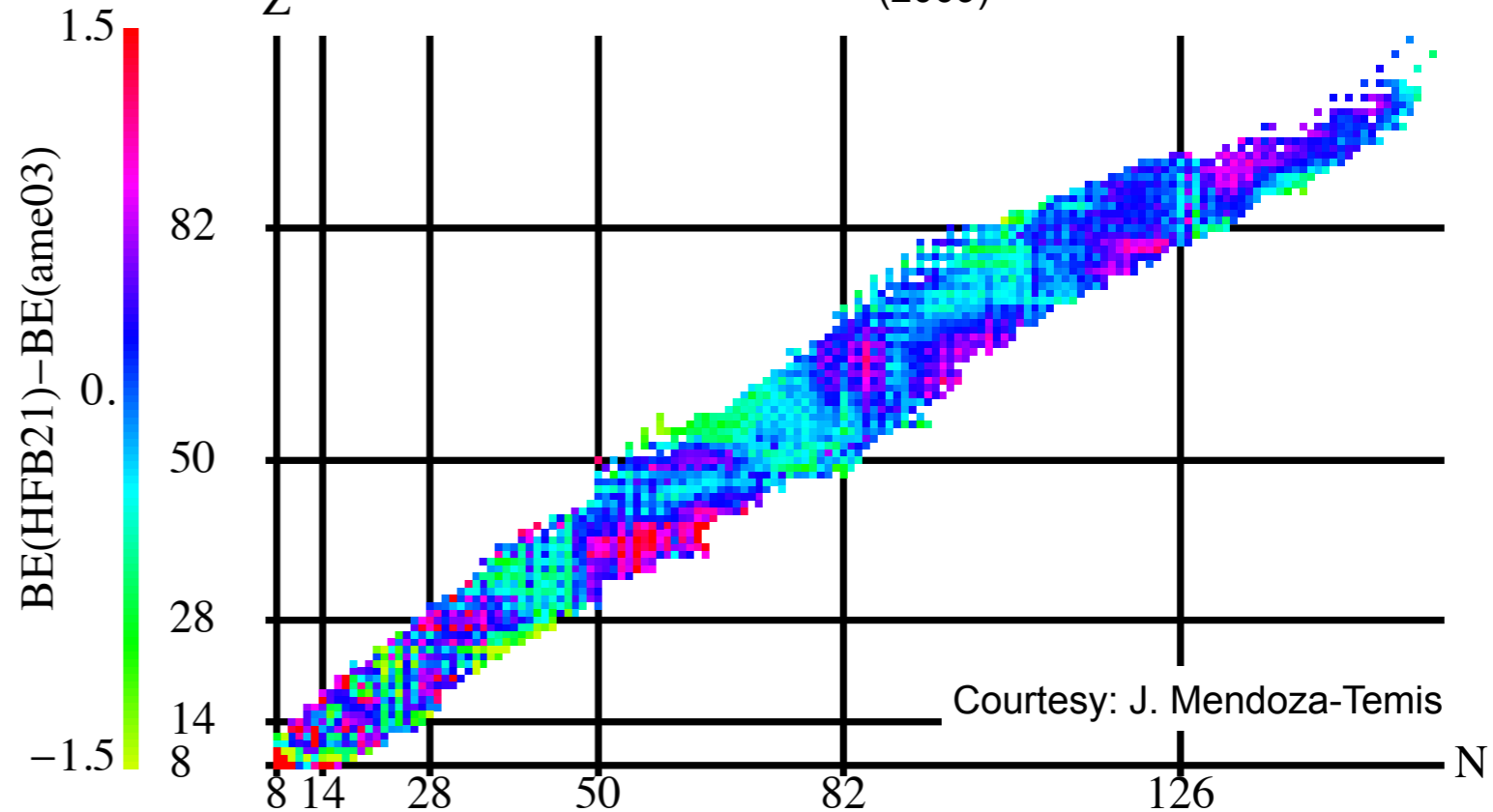
Microscopic mass models with effective interactions

- Self-consistent mean field approximations provide a very good description of known data.



- There are still some problems in transitional regions and local uncertainties:

- Numerical noise.
- Some physics missing: Restoration of broken symmetries and configuration mixing.
- Nuclei with odd number of protons/neutrons are not treated in equal footing as the even-even ones

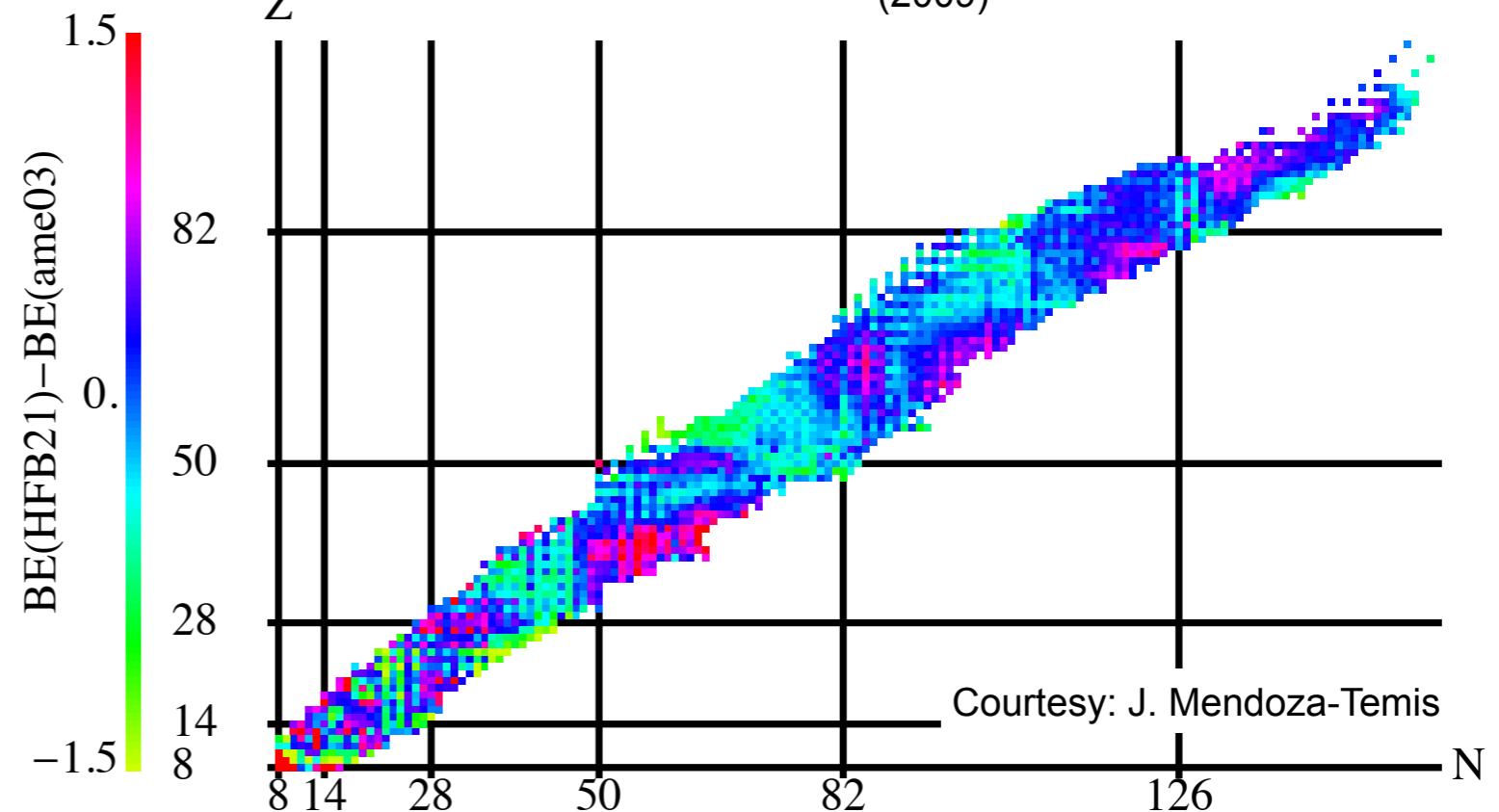
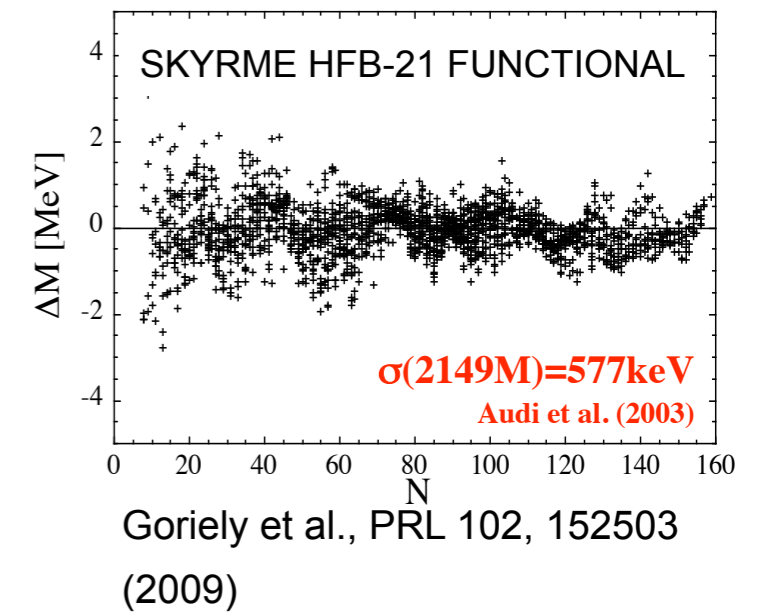
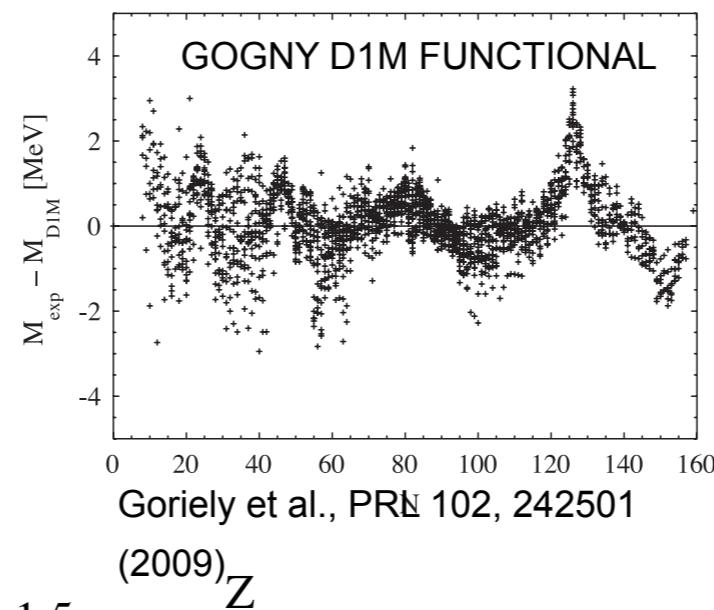


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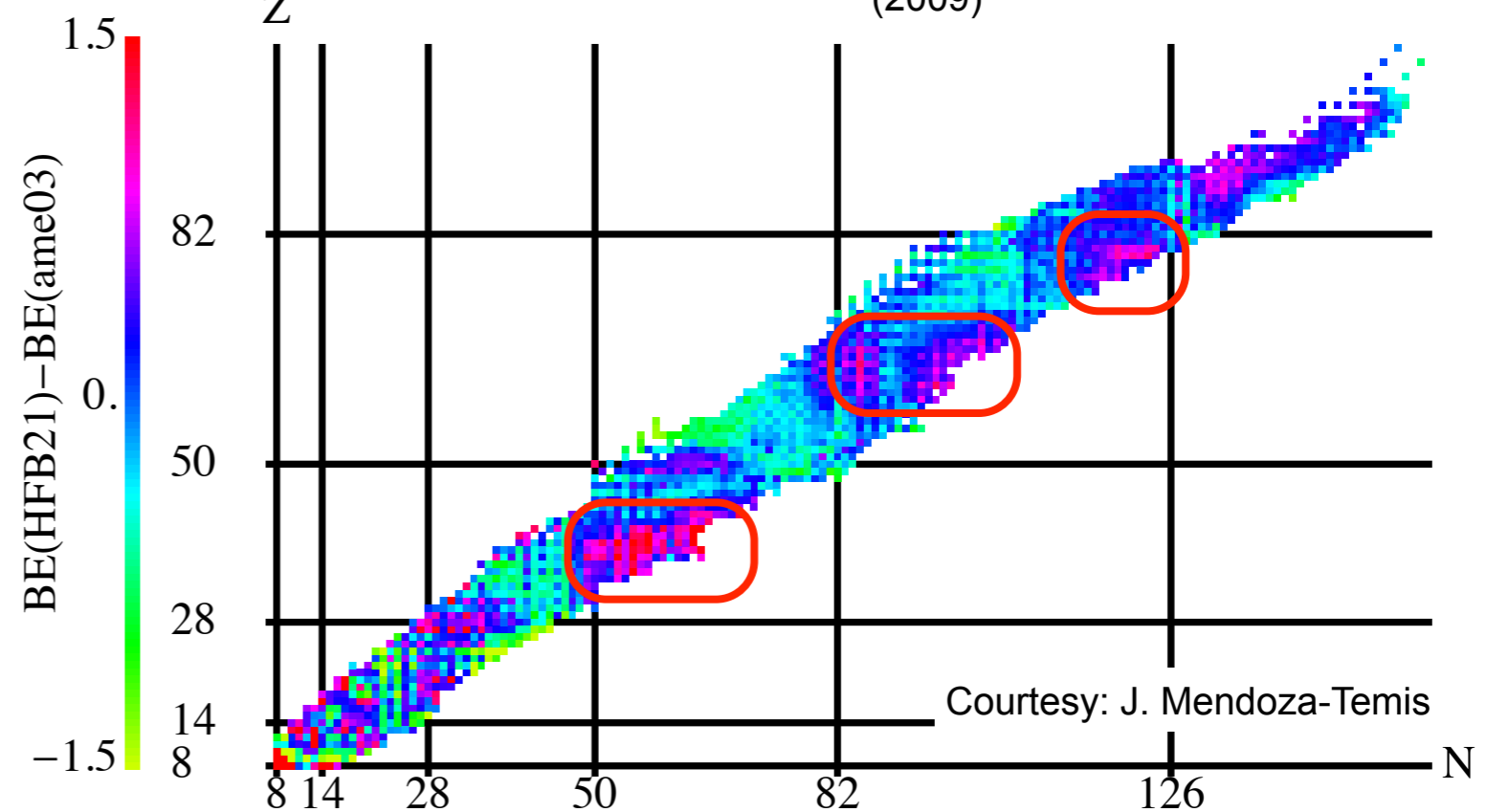
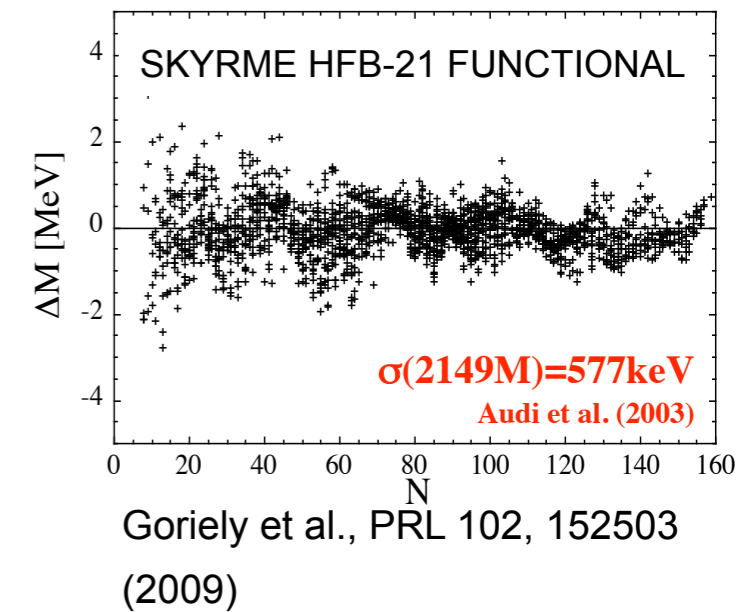
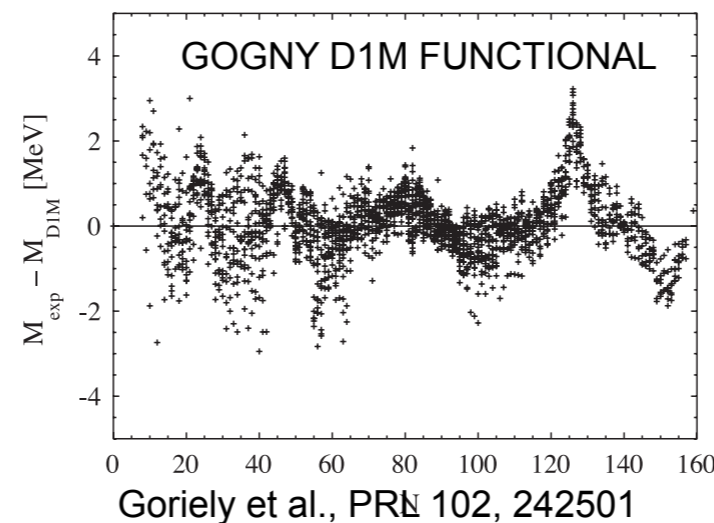


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Self-consistent (beyond) mean field description

- **Effective nucleon-nucleon interaction:**

Gogny force (D1S-D1M) that is able to describe properly many phenomena along the whole nuclear chart.

$$V(1, 2) = \sum_{i=1}^2 e^{-(\vec{r}_1 - \vec{r}_2)^2 / \mu_i^2} (W_i + B_i P^\sigma - H_i P^\tau - M_i P^\sigma P^\tau) \quad \text{central term}$$

spin-orbit term

$$+ i W_0 (\sigma_1 + \sigma_2) \vec{k} \times \delta(\vec{r}_1 - \vec{r}_2) \vec{k} + t_3 (1 + x_0 P^\sigma) \delta(\vec{r}_1 - \vec{r}_2) \rho^\alpha ((\vec{r}_1 + \vec{r}_2)/2)$$

$$+ V_{\text{Coulomb}}(\vec{r}_1, \vec{r}_2) \quad \text{Coulomb term}$$

density-dependent term

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spin-orbit term: $+iW_0(\sigma_1 + \sigma_2)\vec{k} \times \delta(\vec{r}_1 - \vec{r}_2)\vec{k} + t_3(1 + x_0 P^\sigma)\delta(\vec{r}_1 - \vec{r}_2)\rho^\alpha((\vec{r}_1 + \vec{r}_2)/2)$

Coulomb term: $+V_{\text{Coulomb}}(\vec{r}_1, \vec{r}_2)$ density-dependent term

- **Methods of solving the many-body problem: Variational approaches**

Self-consistent (beyond) mean field description

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 \end{aligned}$$

- **Methods of solving the many-body problem: Variational approaches**

➔Parameters of the effective interaction are fitted to reproduce experimental data solving the many-body problem at certain level of approximation (mean field normally).

Self-consistent mean field in a nutshell

Hartree-Fock-Bogoliubov (HFB)

Variational space: $\{|\Phi(\vec{q})\rangle\}$ set of **product-type** wave functions which fulfill:

• Quasiparticle vacua:
$$\alpha_k(\vec{q})|\Phi(\vec{q})\rangle = 0$$

• Most general linear combination of the arbitrary single particle basis:

$$\alpha_k^\dagger(\vec{q}) = \sum_l U_{lk}(\vec{q})c_l^\dagger + V_{lk}(\vec{q})c_l$$

• Fermionic operators:

$$\{\alpha_k^\dagger(\vec{q}), \alpha_{k'}(\vec{q})\} = \delta_{kk'}; \{\alpha_k^\dagger(\vec{q}), \alpha_{k'}^\dagger(\vec{q})\} = \{\alpha_k(\vec{q}), \alpha_{k'}(\vec{q})\} = 0$$

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Variational principle: $\delta \left[E'^{\text{HFB}}(\vec{q}) = \langle \Phi(\vec{q}) | \hat{H} - \lambda_N \hat{N} - \lambda_Z \hat{Z} - \vec{\lambda}_{\vec{q}} \hat{Q} | \Phi(\vec{q}) \rangle \right]_{|\Phi(\vec{q})\rangle = |\text{HFB}(\vec{q})\rangle} = 0$

$$\lambda_N(\vec{q}) \rightarrow \langle \Phi(\vec{q}) | \hat{N} | \Phi(\vec{q}) \rangle = N$$

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$|\text{HFB}(\vec{q})\rangle$ **Product Type**

Self-consistent mean field in a nutshell

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- Most general linear combination of the arbitrary single particle basis: **1. finite basis!! convergence?**

$$\alpha_k^\dagger(\vec{q}) = \sum_l U_{lk}(\vec{q})c_l^\dagger + V_{lk}(\vec{q})c_l$$

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Product Type

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- 1. finite basis!! convergence?**
2. Breaks the symmetries!!

Variational principle: $\delta \left[E'^{\text{HFB}}(\vec{q}) = \langle \Phi(\vec{q}) | \hat{H} - \lambda_N \hat{N} - \lambda_Z \hat{Z} - \vec{\lambda}_{\vec{q}} \hat{Q} | \Phi(\vec{q}) \rangle \right]_{|\Phi(\vec{q})\rangle = |\text{HFB}(\vec{q})\rangle} = 0$

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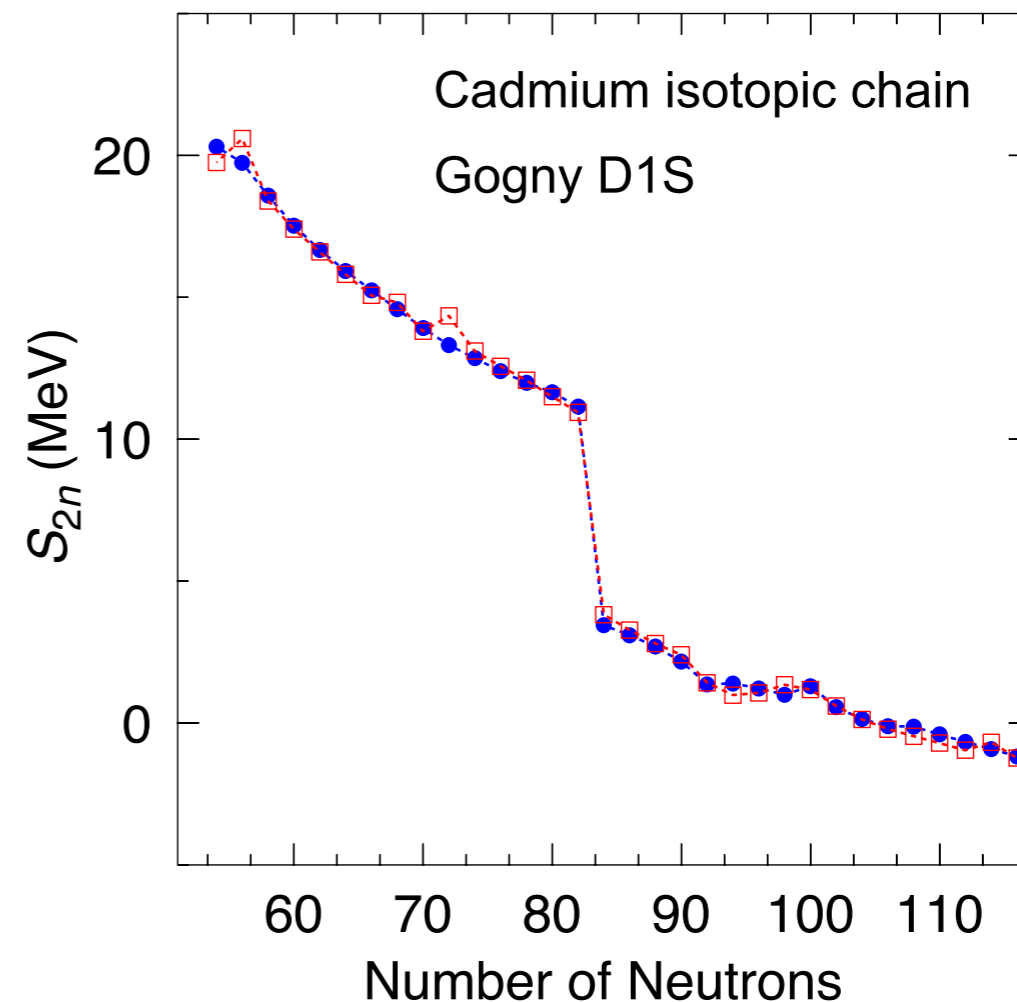
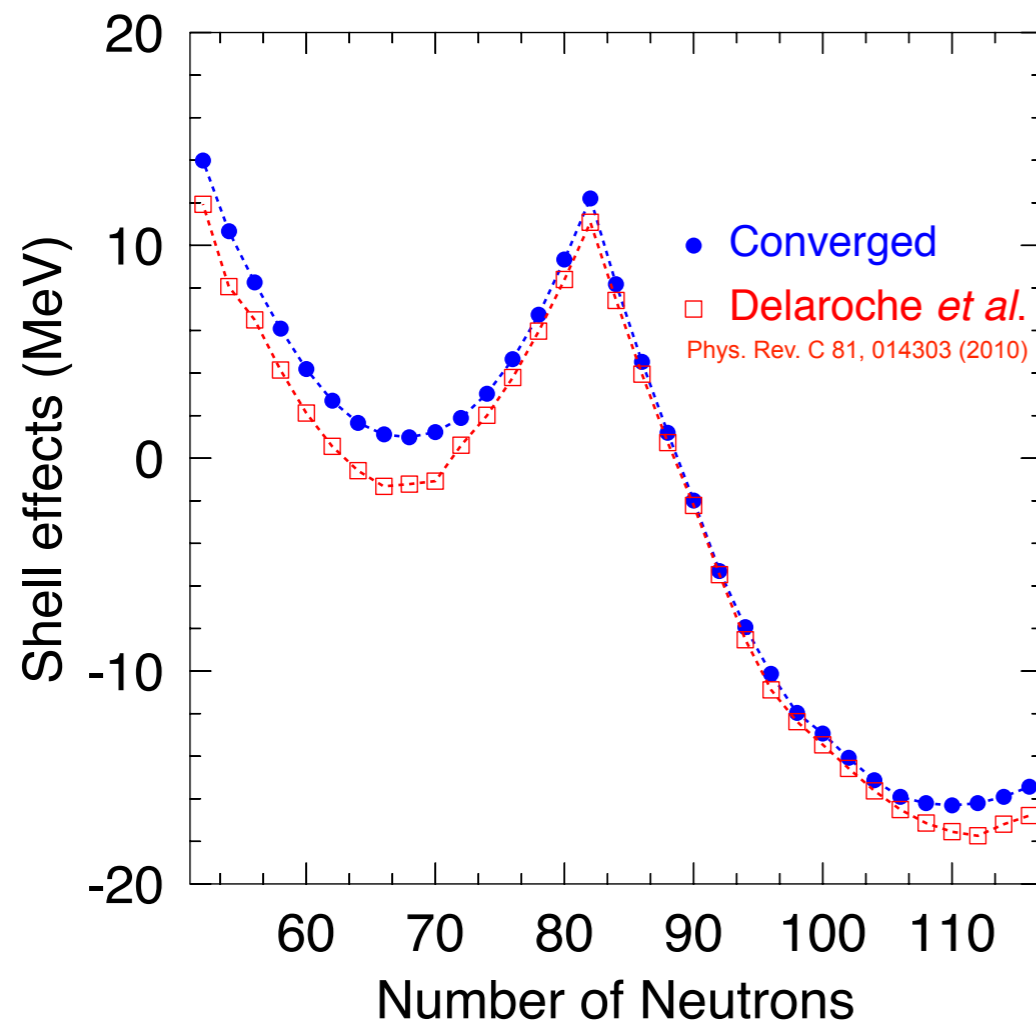
$$\lambda_Z(\vec{q}) \rightarrow \langle \Phi(\vec{q}) | \hat{Z} | \Phi(\vec{q}) \rangle = Z$$

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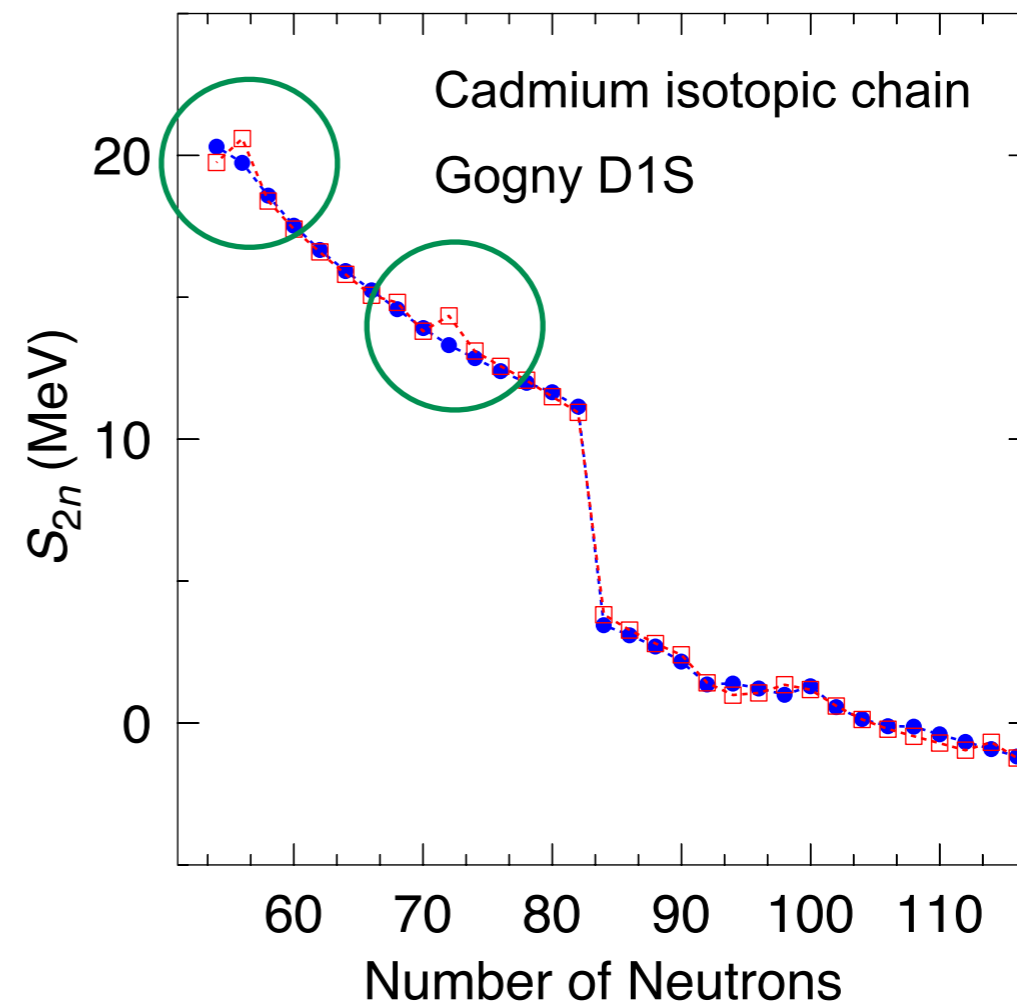
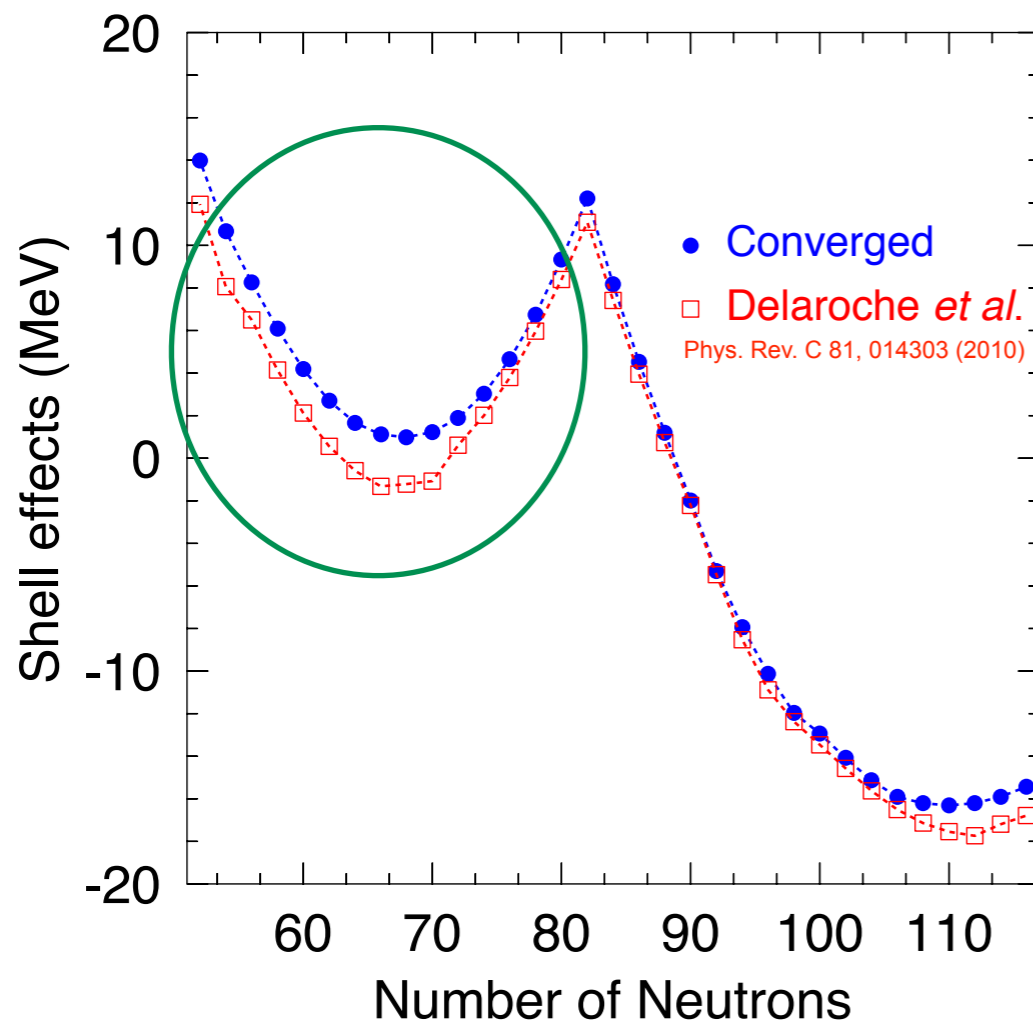
Convergence

- Published tables could contain some lack of convergence in the total binding energy.
- Two neutron separation energies are better converged.
- Artificial 'jumps' or 'noise' could appear in the S_{2n} due to lack of convergence.

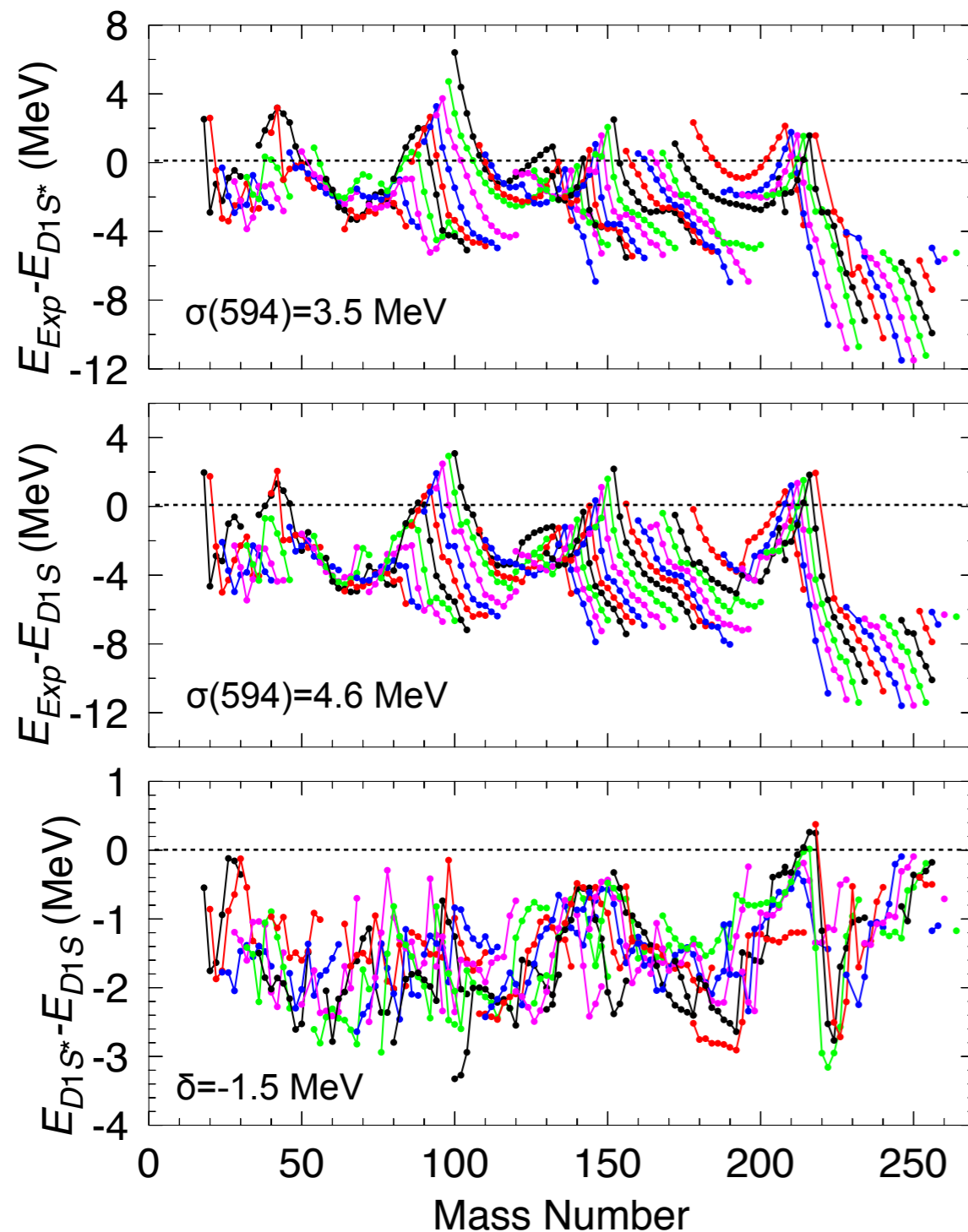


Convergence

- Published tables could contain some lack of convergence in the total binding energy.
- Two neutron separation energies are better converged.
- Artificial 'jumps' or 'noise' could appear in the S_{2n} due to lack of convergence.



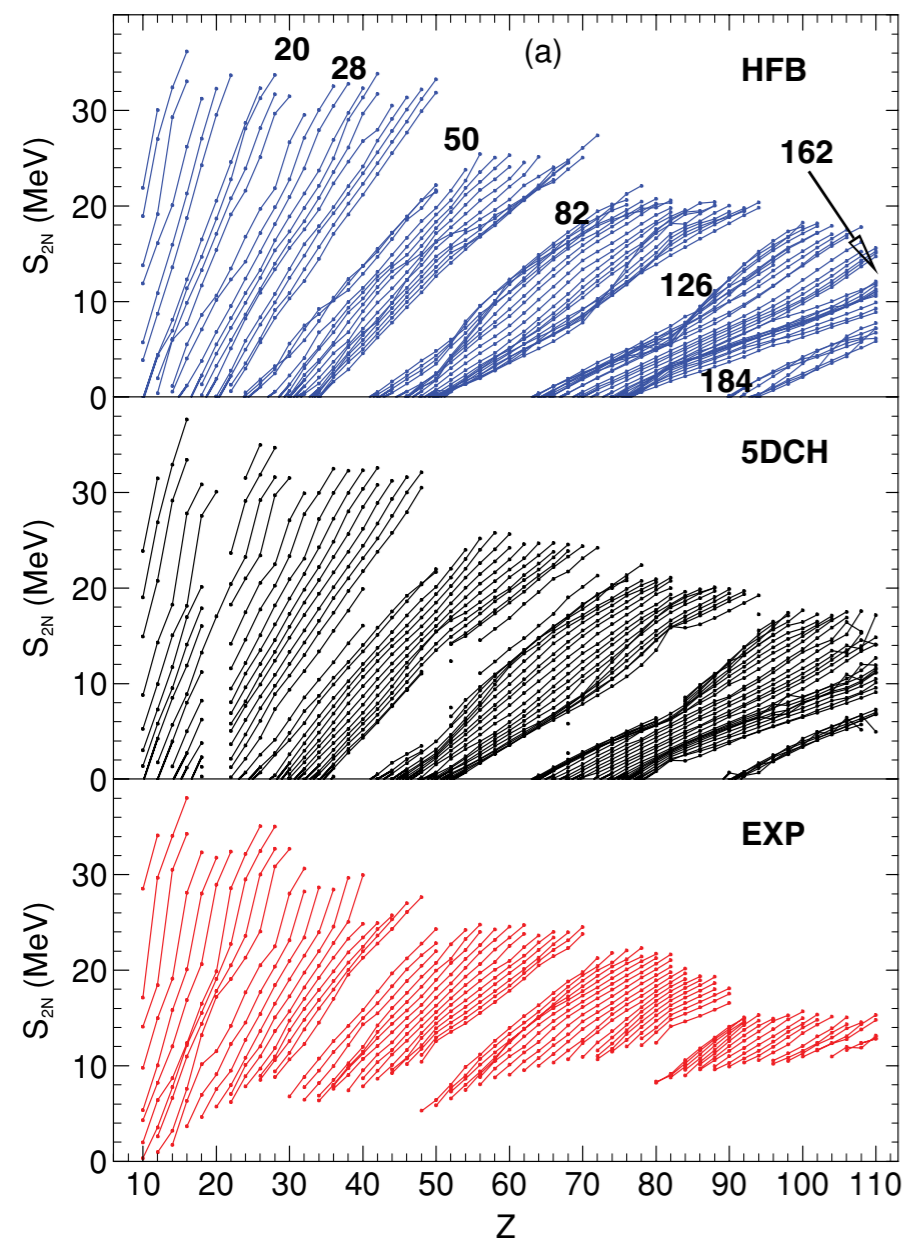
Convergence



- Experimental data: AME12, only even-even.
- Gogny D1S: Delaroche et al., PRC 81, 014303 (2010).
- Gogny D1S*: $N_{osc}=18$, b optimized, β_2 explored.
- Gogny D1S is **not** a good parametrization for masses (overbinding of double magic nuclei, underbinding of neutron rich nuclei, poor r.m.s.).
- Better convergence gives smaller r.m.s. and smoother behavior along the whole AME12 even-even data.
- ~ 1.5 MeV average gain in energy by improving the convergence.

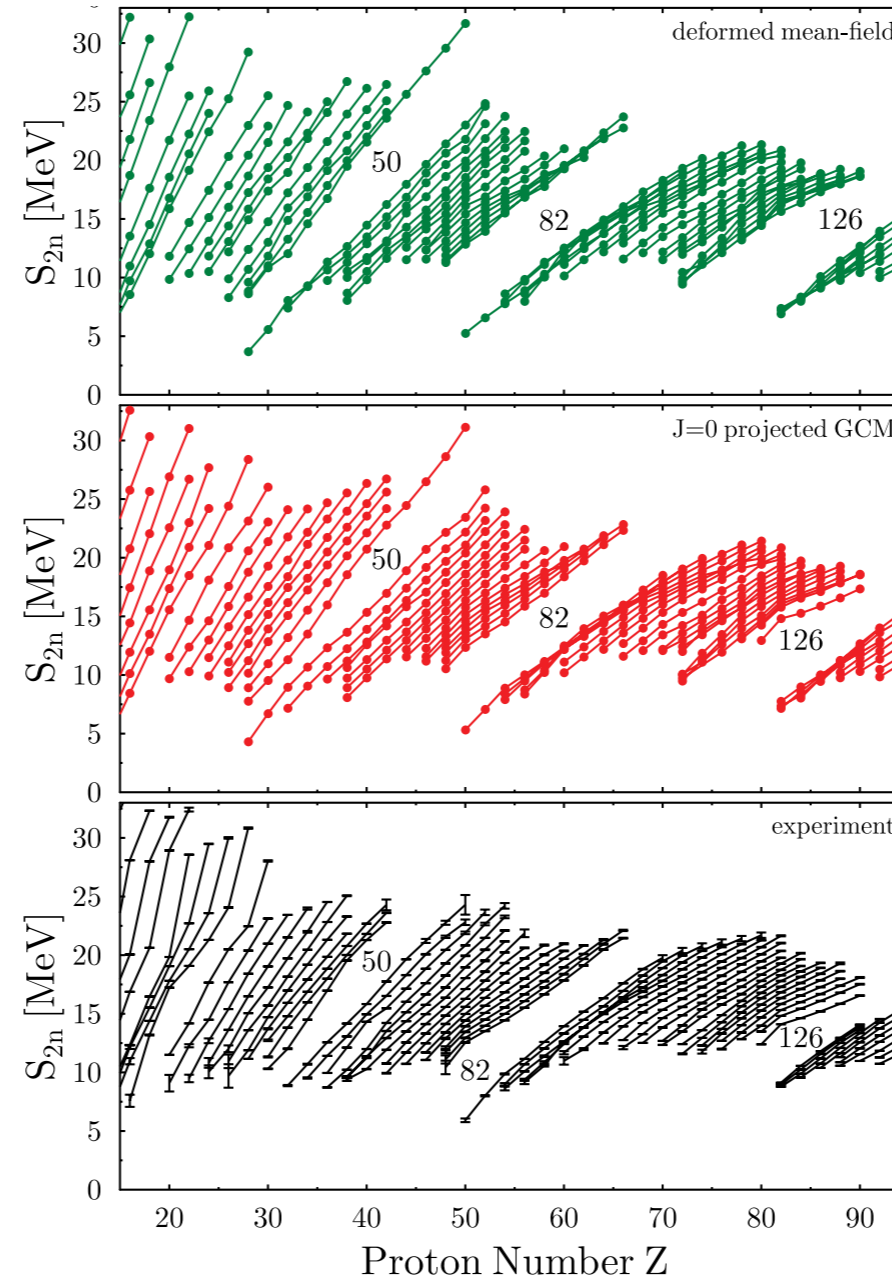
Mean field vs. Beyond mean field. Global systematics

Gogny D1S



Delaroche et al. PRC 81, 014303 (2010)

Skyrme SLy4

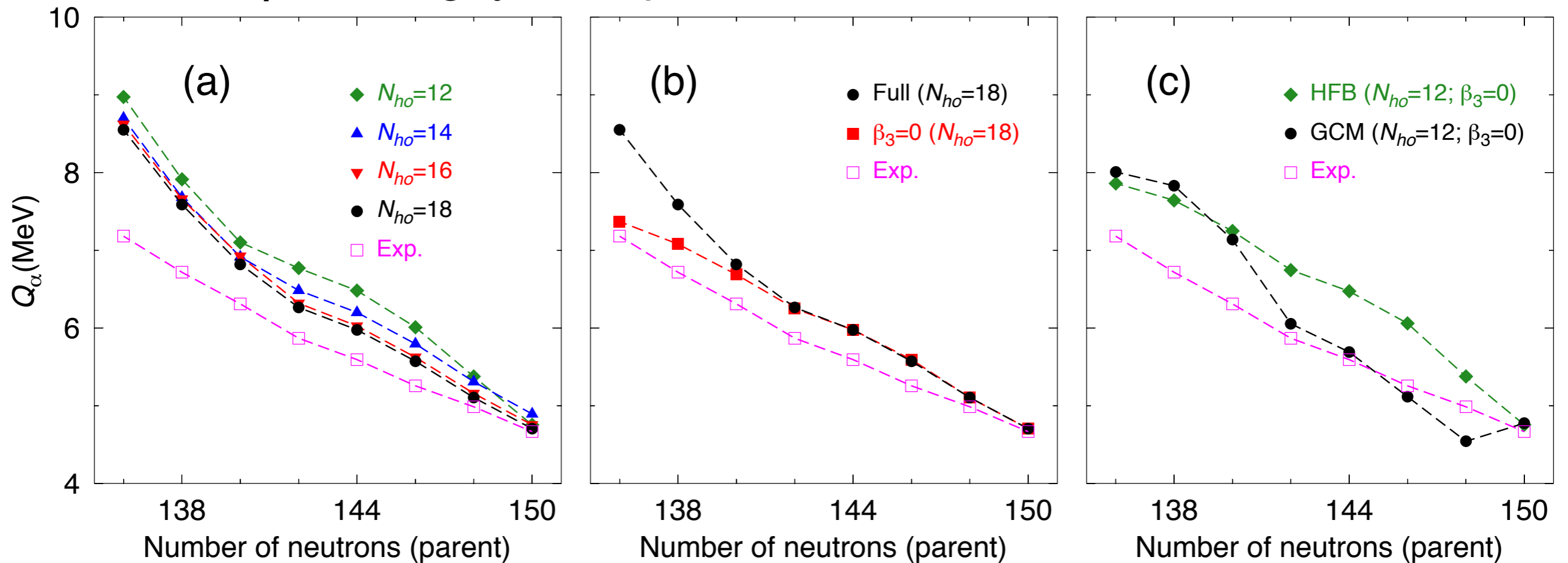


Bender et al., PRC 73, 034322 (2006)

- No **exact** projections/GCM but gaussian overlap approximations (GOA) are used: they are not variational
- Beyond mean field effects tend to reduce the shell gaps
- Separation energies are smoother when beyond mean field are included.

Alpha decay in heavier nuclei

Pu isotopes. Gogny D1M parametrization



Convergence affects the results

Addition of new degrees of freedom affects the results

Beyond mean field effects affects the results

Need to reduce the *physical* and *numerical* uncertainties in energy density functional calculations

T. R. Rodríguez, GSI report 2013

Credits

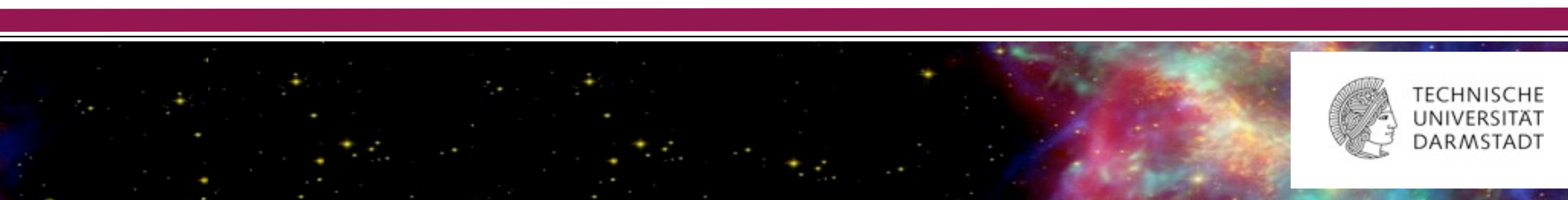


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