

Coupled Channel Analysis with $\bar{p}p$ -Data

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Outline

- Introduction
 - Crystal Barrel at LEAR
 - Reminder: $\bar{p}p \rightarrow \omega\pi^0$
 - Goodness of fit: the energy test
- PWA of CB-LEAR data with relevance for PANDA
 - $\bar{p}p \rightarrow K^+K^-\pi^0$
 - $\bar{p}p \rightarrow \pi^+\pi^-\pi^0$
 - First coupled channel analysis
 - Spin density matrices
- Summary and outlook

Motivations

With regard to the upcoming PANDA experiment, analyses of existing $\bar{p}p$ -data are valuable

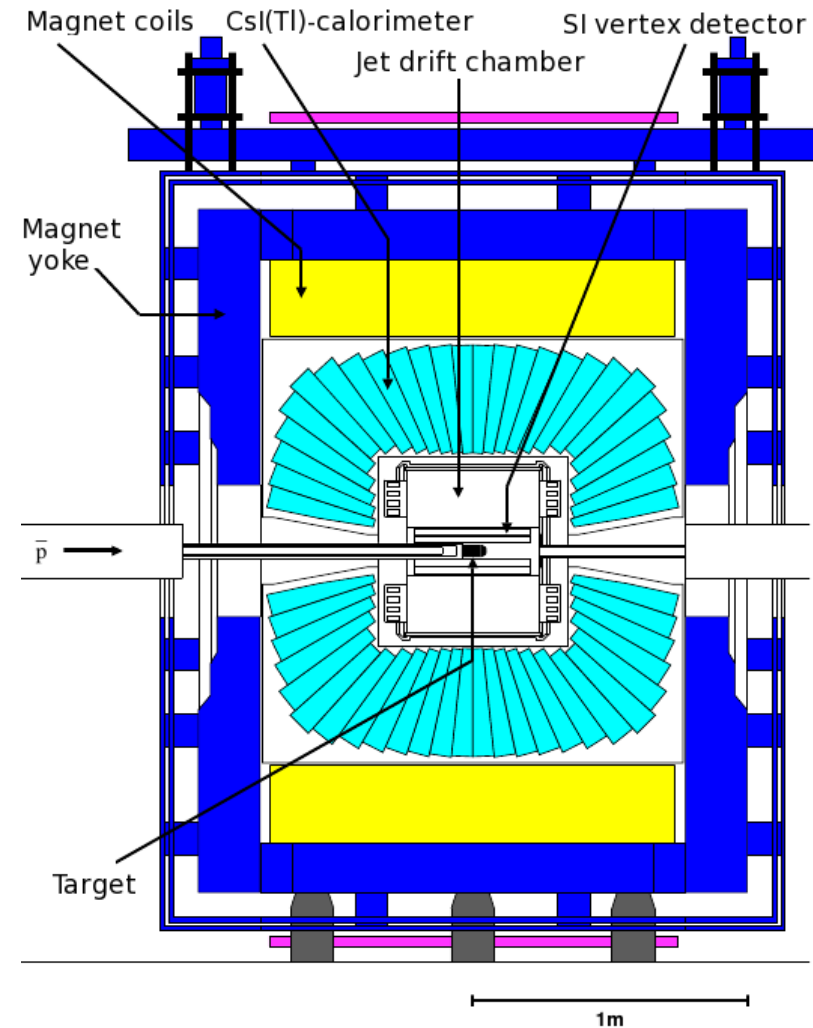
➡ Crystal Barrel at LEAR

- Development and test of analysis tools for PANDA, such as the partial wave analysis (PWA) software
- Gain experience with fitting strategies and identification of resonances
- Study of the production of vector mesons and the initial $\bar{p}p$ -states
- Evaluation of the contributing orbital angular $\bar{p}p$ -momenta
 - $p_{\bar{p},max} = 1.94 \text{ GeV}/c$ @ CB-LEAR ➡ $L_{max} \approx 5$
 - $p_{\bar{p}} = (1.5 - 15) \text{ GeV}/c$ @ PANDA ➡ $L_{max} = ?$
- Evaluation of the spin density matrix for different mesons
- Modern hardware allows more sophisticated analyses of old data

Crystal Barrel

- Fixed target experiment at LEAR (CERN) data taking 1989 - 1996
- $\bar{p}p$ -annihilation in flight and at rest
- $p_{\bar{p}} = 105 \text{ MeV/c} \dots 2 \text{ GeV/c}$
- $94\% \cdot 4\pi$ detector
- Targets: LH_2 , LD_2 , GH_2
- Trigger on 0 or 2 charged particles

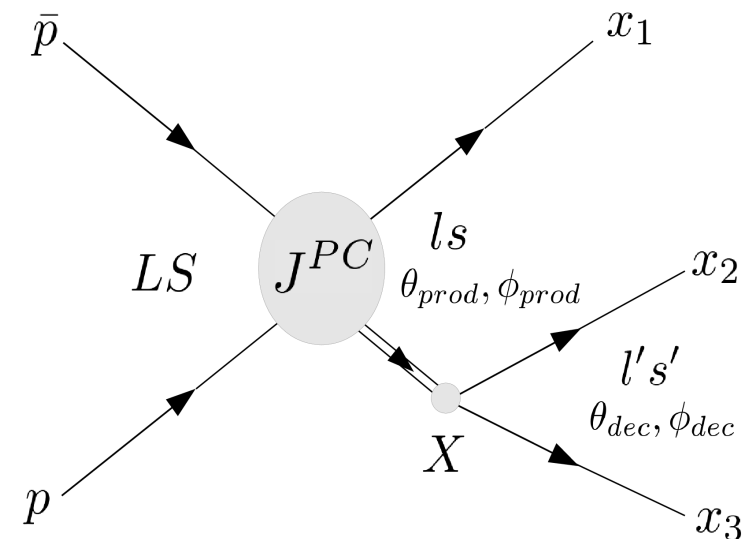
Excellent opportunity for the investigation of specific physics aspects for PANDA



Partial wave analyses of $\bar{p}p$ reactions

$$\begin{aligned}
 \frac{d\sigma}{d\Omega} \propto & \sum_{\lambda_{FS}} \sum_{(2S+1)S} \left| \sum_{J^{PC}} T_{LS}^{\bar{p}p \rightarrow J^{PC}} \times \right. \\
 & \times \left. \sum_X \sum_{l_s} T_{l_s}^{J^{PC} \rightarrow Xx_1} A_{l's'}^{X \rightarrow x_2x_3} \right|
 \end{aligned}$$

FS particle spin \downarrow $\bar{p}p$ Singlet / Triplet states \downarrow J^{PC} prod. amplitudes \downarrow
 Resonances \uparrow Res. prod. amp. \uparrow Res. decay amp. \uparrow



- Amplitudes include angular distributions (D-functions), spin/isospin couplings (Clebsch-Gordan) and dynamics (Breit Wigner, K-Matrix, ...)
- Pawian automatically builds the full amplitude and takes account of spin-, isospin-, C/G-parity conservations
- Maximum contributing orbital $\bar{p}p$ momentum L_{max} is unknown and has to be determined e.g. by significances of likelihood improvements

Reminder: $\bar{p}p \rightarrow \omega\pi^0$ (Meeting June 2013)

- Partial wave analysis of the channels $\omega \rightarrow \pi^0\gamma$ and $\omega \rightarrow \pi^+\pi^-\pi^0$ using CB at LEAR data

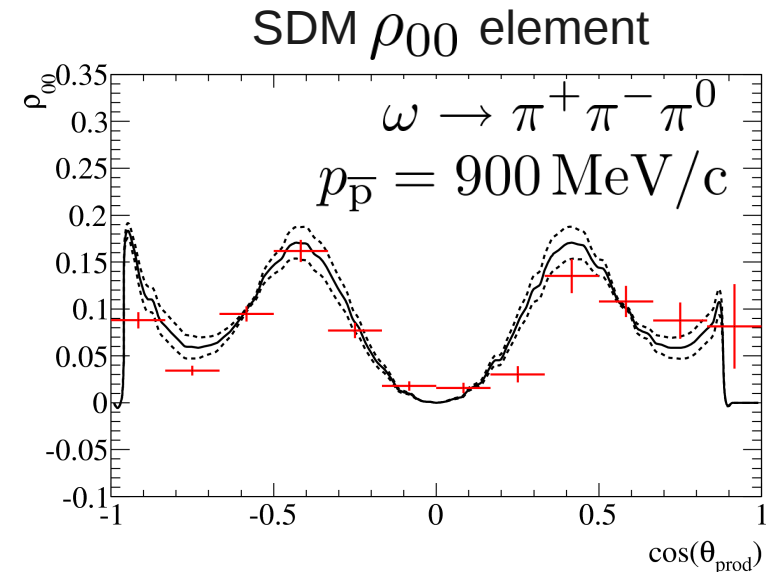
- L_{\max} values found using \mathcal{L} ratios:

$$L_{\max}=3 \text{ @ } p_{\bar{p}} = 600 \text{ MeV/c}$$

$$L_{\max}=4 \text{ @ } p_{\bar{p}} = 900\text{-}1525 \text{ MeV/c}$$

$$L_{\max}=5 \text{ @ } p_{\bar{p}} = 1940 \text{ MeV/c}$$

- Spin density matrix (SDM) revealed strong alignment of the ω in both channels, strongly dependent on production angle
- Hints for intermediate resonances?



Motivation

- ➔ • Further studies of the $K^+K^-\pi^0$ and $\pi^+\pi^-\pi^0$ final states with all intermediate resonances
- Evaluation of L_{\max} and the mass / resonance – dependency
- SDM evaluation of other particles like ϕ , ρ , $f_2(1270)$
- Complicated channels that require a full PWA
- Coupled channel analyses

Goodness of fit – the energy test

- QA of PWA result requires an unbinned, multivariate gof test. One of the most powerful is the **energy test**.

B. Aslan and G. Zech, Nucl. Instrum. Methods A537 (2005) 626-636.

- Data and a sample of the fitted pdf are regarded like electric charges of opposite sign in multivariate space
 ➔ “electrostatic” energy is minimal if the samples originate from the same parent distribution

- Generalized energy:

$$\phi_{NM} = \frac{1}{M(M-1)} \sum_{j>i} R(|\mathbf{y}_i - \mathbf{y}_j|) - \frac{1}{NM} \sum_{i,j} R(|\mathbf{x}_i - \mathbf{y}_j|)$$

Data sample
Fit sample
Metric has to be defined

$N \gg M$

- Different potential functions for different applications:

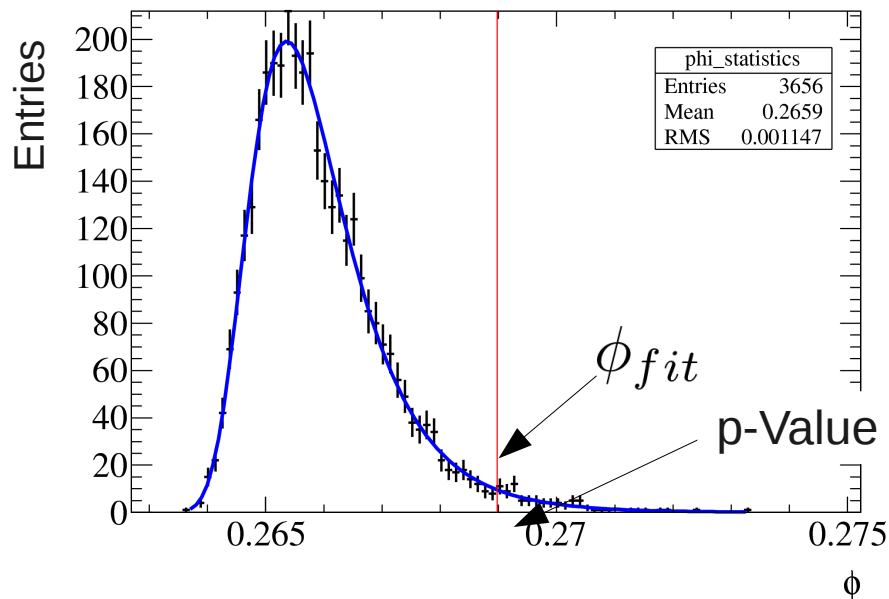
$$R_{\log}(r) = -\ln(r + \epsilon) \quad \text{long range, e.g. linear omnipresent background}$$

$$R_G(r) = e^{-r^2/2s^2} \quad \text{short range, e.g. localized peaking background}$$

Energy Test - p-Value

Unlike for the χ^2 test, the test statistics (the ϕ distribution) has to be generated for each pdf

- **Monte Carlo simulation**: generate new “data” from pdf and calculate energy. May become time consuming due to detector simulation.
- **Resampling**: relabel the N+M events randomly to get different N data and M fit points, calculate energy.

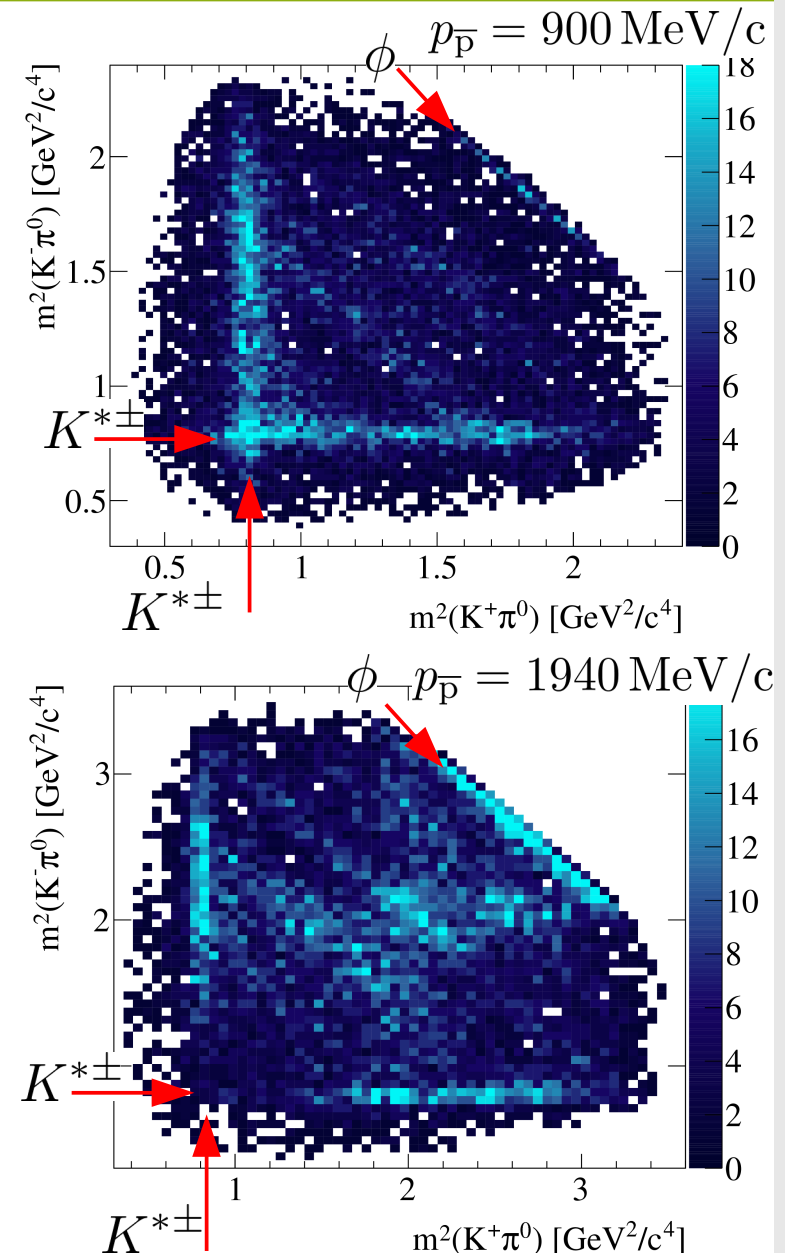


High statistics simulation can be avoided by fitting the distribution:

$$f(x) = \frac{1}{\sigma} \left(1 + \xi \frac{x - \mu}{\sigma} \right)^{-1/\xi - 1} \cdot \exp \left\{ - \left(1 + \xi \frac{x - \mu}{\sigma} \right)^{-1/\xi} \right\}$$

$$\bar{p}p \rightarrow K^+K^-\pi^0$$

- Contains $\phi\pi^0$ and $K^{*\pm}K^\mp$ events
- Production of vector mesons with strangeness
 - different process in comparison to $\bar{p}p \rightarrow \pi^+\pi^-\pi^0$
 - rearrangement vs. annihilation
- Interference of resonances requires a PWA of the complete channel
- Spin density matrix via extraction of the fitted ϕ and $K^{*\pm}$ amplitudes
- Selected CB data:
 - ~18100 events @ 900 MeV / c
 - ~14400 events @ 1940 MeV / c



PWA : $\bar{p}p \rightarrow K^+ K^- \pi^0$

- Full PWA from the initial to the final state
 - Hypotheses based on previous results (Crystal Barrel: Phys. Lett. B639 (2006) 165)
 - $\phi\pi^0$, $\phi(1680)\pi^0$
 - $f_2(1270)\pi^0$, $f_2'(1525)\pi^0$
 - $a_2(1320)\pi^0$
 - $K^{*\pm}K^\mp$, $K^*(1680)^\pm K^\mp$
 - Five $f_0\pi^0$
New: via $(KK)_S$ -wave
 - $K_0^{*\pm}K^\mp$
New: via $(K\pi)_S(I = 1/2)$ - wave
 $[(K\pi)_S(I = 3/2)$ - wave]
- K-matrix parametrization by
 Anisovich and Sarantsev
 Eur. Phys. J. A16, 229(2003)
 5-pole, 5-channel matrix

←

K-matrix parametrization
 used by FOCUS
 Phys. Lett. B653 (2007) 1-11
 1 / 0 -pole, 2-channel matrix

- Generalized K-Matrix support in preparation

Amplitude prefactors

- $K^* K$ systems are no G- and C-parity eigenstates and can have isospin $I=0$ or $I=1$

- Thus, those states have to be symmetrized, e.g. ($J=1$)

$$|I, I_z\rangle^C = |1, 0\rangle^+ = 1/2 \cdot \left[+|K_1^{*0} \bar{K}^0\rangle + |K_1^{*+} K^-\rangle - |\bar{K}_1^{*0} K^0\rangle - |K_1^{*-} K^+\rangle \right]$$

- This yields to amplitude prefactors:

J^{PC}	0^{-+}				
Transition	l	L	I	x	y
$K_0^*(1/2) \bar{K}$	0	0	0	+	+
$K_0^*(1/2) \bar{K}$	0	0	1	-	-
$K_0^*(3/2) \bar{K}$	0	0	1	+	+
$K_1^* \bar{K}$	1	1	0	+	+
$K_1^* \bar{K}$	1	1	1	-	-

J^{PC}	1^{+-}				
Transition	l	L	I	x	y
$K_0^*(1/2) \bar{K}$	0	1	0	-	+
$K_0^*(1/2) \bar{K}$	0	1	1	+	-
$K_0^*(3/2) \bar{K}$	0	1	1	-	+
$K_1^* \bar{K}$	1	0,2	0	-	+
$K_1^* \bar{K}$	1	0,2	1	+	-

Destructive interference

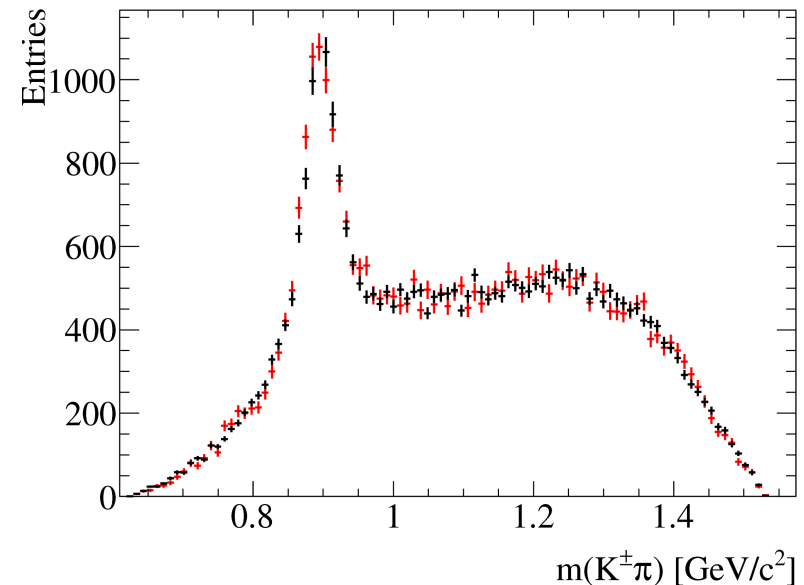
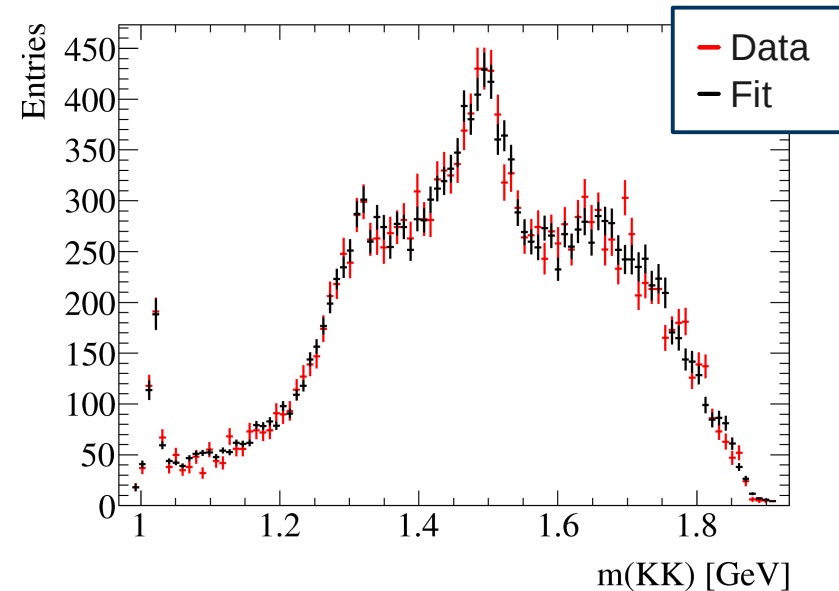
[...]

- $K^{*+} K^-$ and $K^{*-} K^+$ production can be described using the same amplitudes, but the correct prefactors are essential

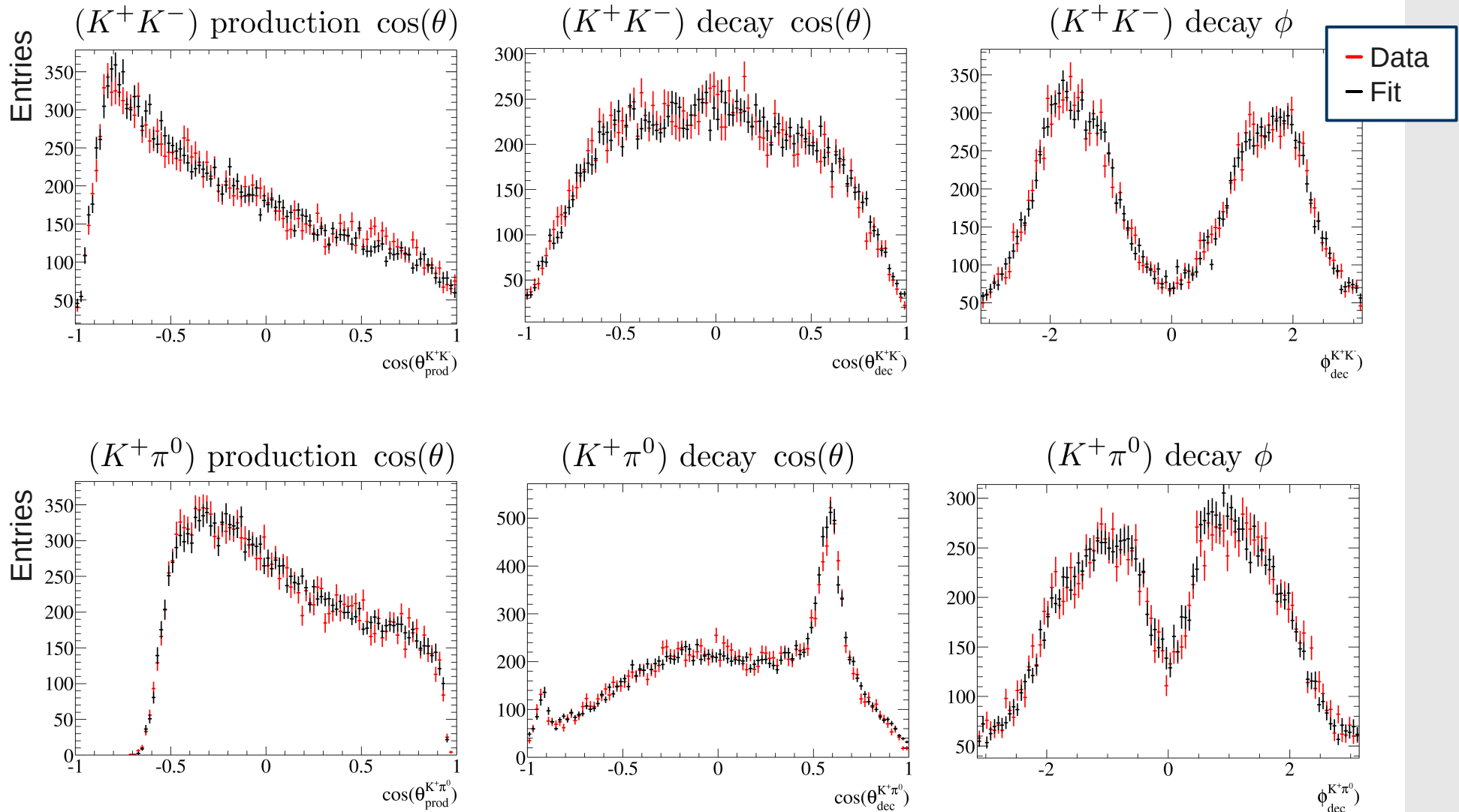
Fit results $p_{\bar{p}} = 900 \text{ MeV}/c$

L_{max}	# free param.	$-\ln \mathcal{L}$	\mathcal{L} -ratio signific.
1	127	-4720.8	-
2	216	-5205.6	$> 10 \sigma$
3	301	-5581.6	$> 10 \sigma$
4	384	running	

- $L_{max} = 3$: $p_g = 0.22$ $p_{log} = 0.38$
easily accepted on 5% significance level
- LH improvements up to $L_{max} = 3$ significant
- Higher global L_{max} values and resonance dependent L_{max} values need to be tested



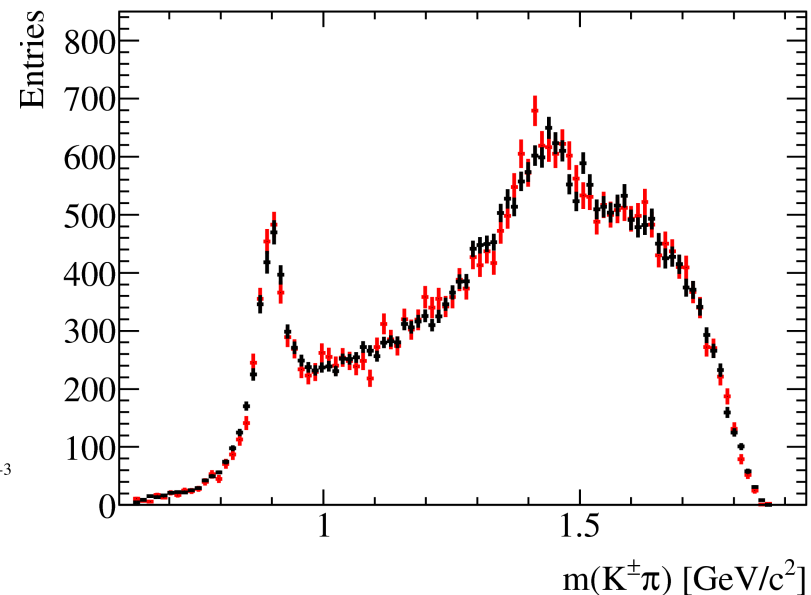
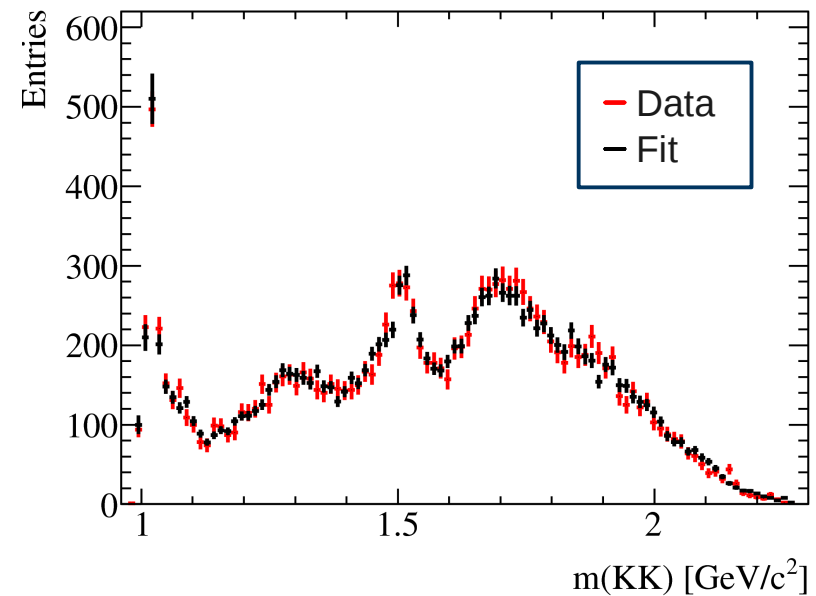
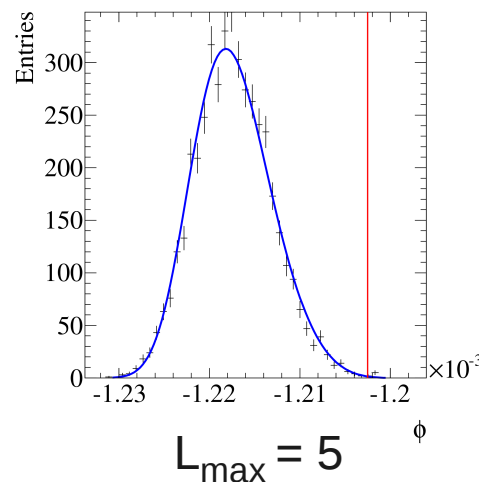
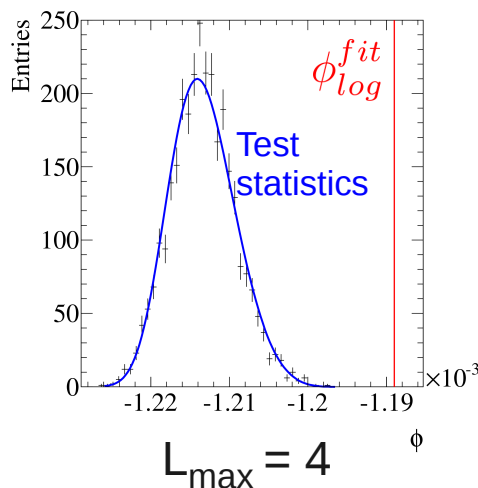
Angular distributions



Fit results $p_{\bar{p}} = 1940 \text{ MeV}/c$

L_{max}	# free param.	$-\ln \mathcal{L}$	\mathcal{L} -ratio signific.
4	428	-3357.4	-
5	529	-3510.9	9.8σ
6	not tested yet		

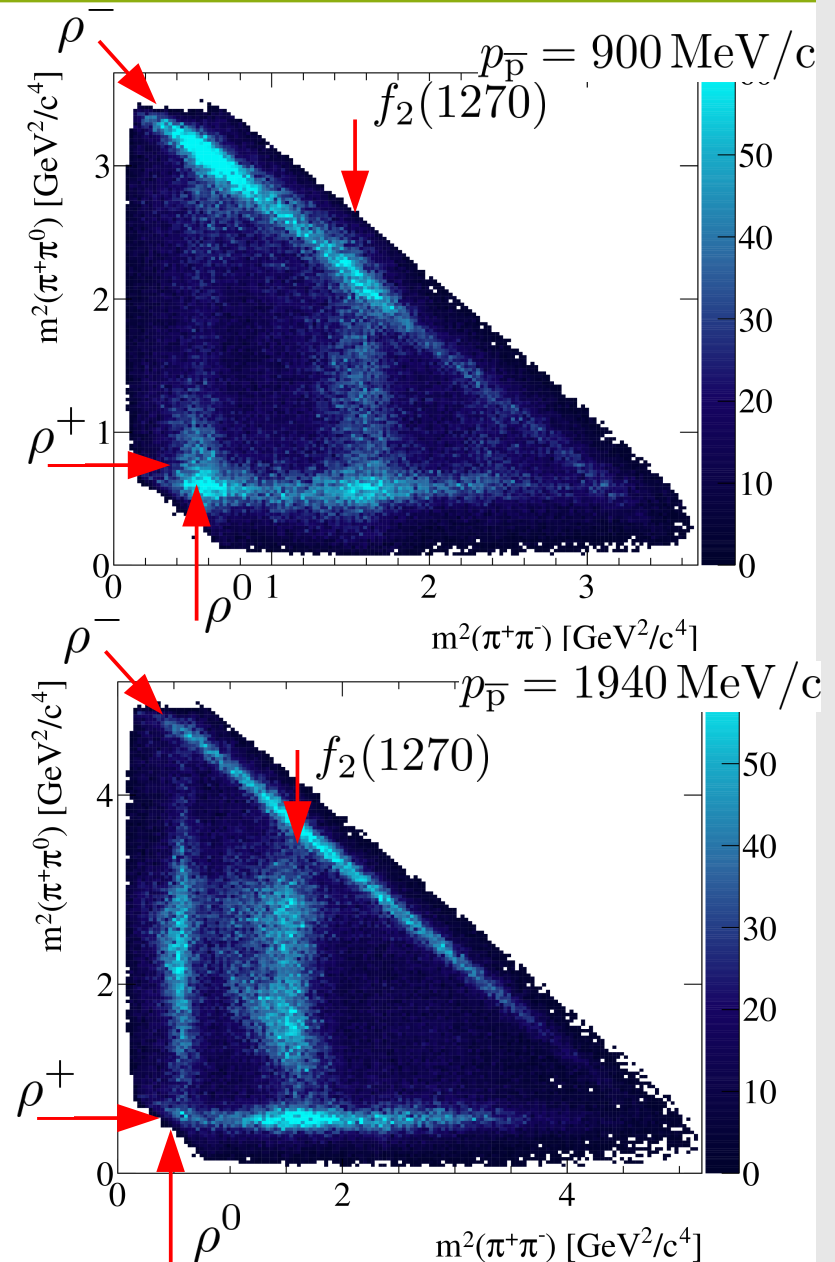
- $L_{max} = 5$:
 $p_g \approx 0.0014$ $p_{log} \approx 0.0090$



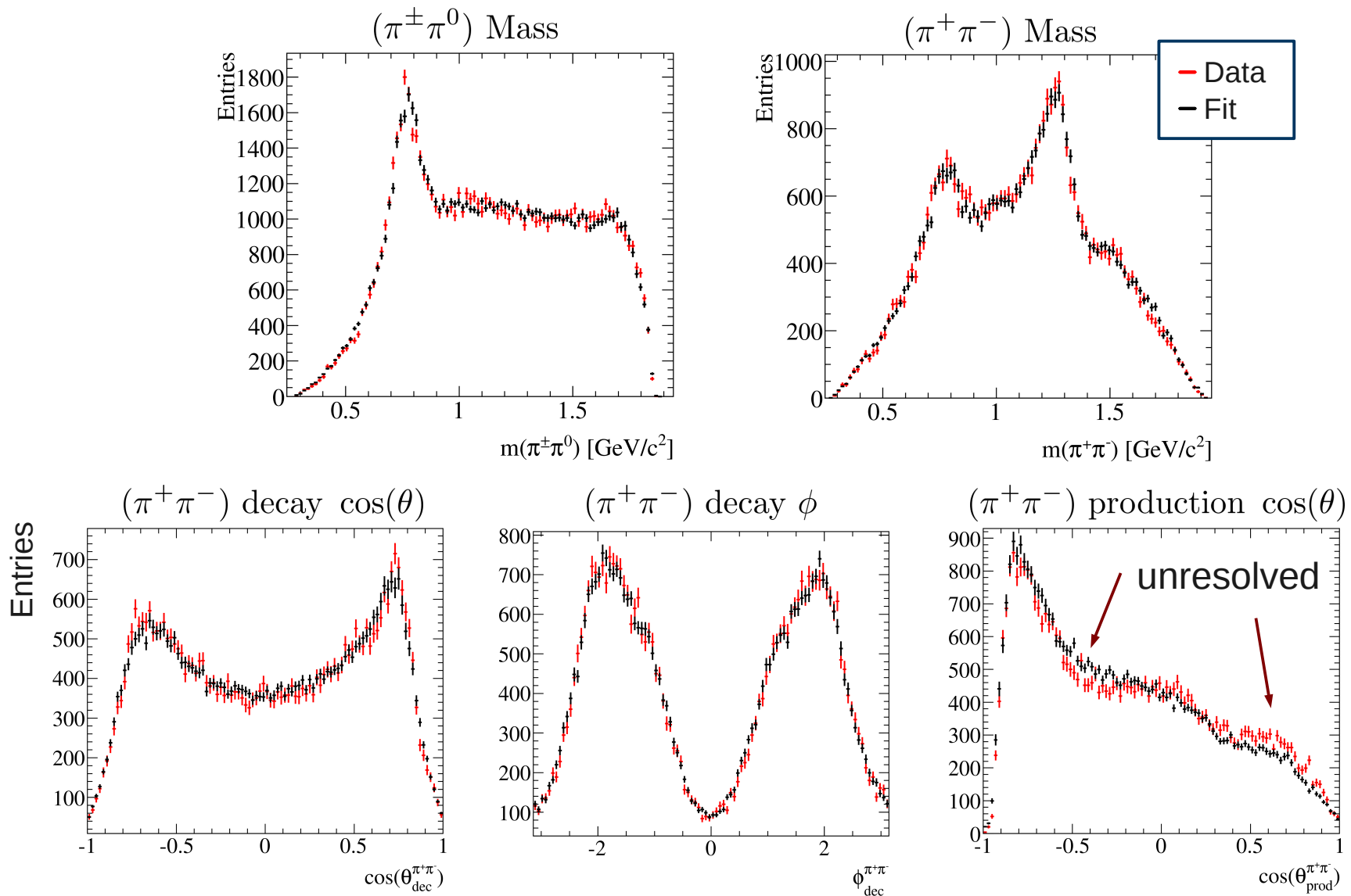
PWA : $\bar{p}p \rightarrow \pi^+\pi^-\pi^0$

- Current hypothesis:
 - $\rho(770)\pi, \rho(1450)\pi, \rho(1700)\pi$
 - $f_2(1270)\pi^0$
 - $(\pi\pi)_S$ -wave
- Possibly also contributing:
 - $\rho_3(1690)\pi^0$ $\omega(\rightarrow \pi^+\pi^-)\pi^0$
 - $f_2'(1525)\pi^0$
- Selected CB Data:
 - ~247000 @ 900 MeV / c
 - ~231000 @ 1940 MeV / c

Temporarily limited to 40000 each



PWA: first fit results $\bar{p}p \rightarrow \pi^+\pi^-\pi^0$




$(p_{\bar{p}} = 900 \text{ MeV}, L_{\text{max}} = 3)$

Coupled channel analysis

- ➔ Simultaneously fitting different reaction channels that share a part of their parameter sets
 - Some parameters might be better accessible in one channel than in another
 - K-Matrix describes dynamics across channels by design, ensures unitarity
 - Hard constraints, less total parameters, better convergence
 - Higher statistics
 - Reduction of systematic effects: different datasets might have different background, detection characteristics, MC quality, ...
 - Check for the physical validity of the parameters

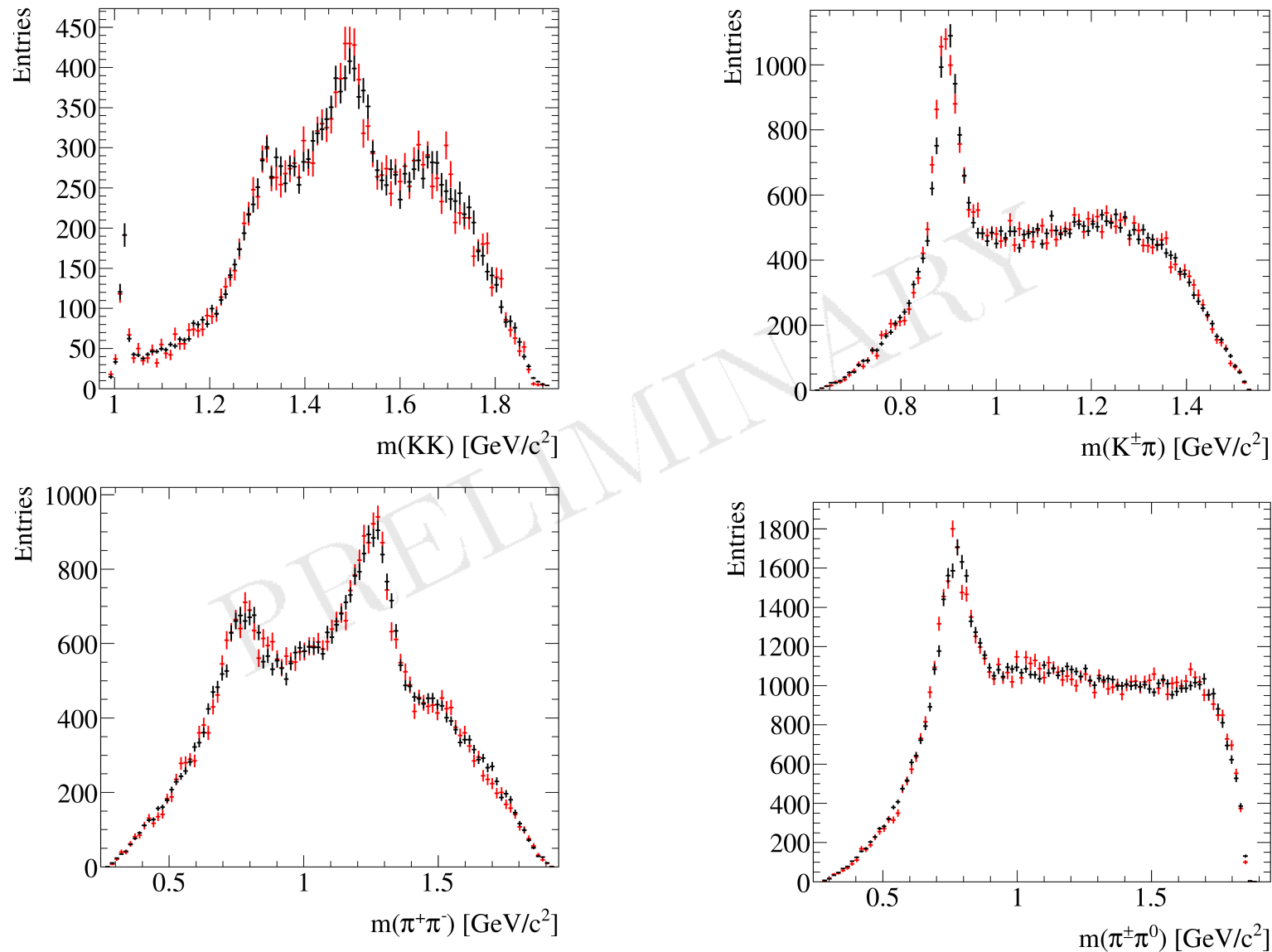
Coupled channel analysis

- Coupled fit of $\bar{p}p \rightarrow K^+ K^- \pi^0$ and $\bar{p}p \rightarrow \pi^+ \pi^- \pi^0$ (and later: $\bar{p}p \rightarrow \pi^+ \pi^- \eta$) in progress
- $f_0(980)$, $f_0(1300)$, $f_0(1500)$, $f_0(1750)$ and $f_0(1200 - 1600)$ present in both channels and described by $(KK/\pi\pi)_S$ -Wave
- $a_2(1320)$ only present in the kaon channel
 can now be separated from $f_2(1270)$
- Current fit status:

Fit	# free param.	$-\ln \mathcal{L}$
separated	301 + 214 = 515	-5581.5 + -9624.2 = -15205.7
coupled	405	-5414.1 + -9599.0 = -15013.1

(running)

Coupled channel analysis – current results



$(p_{\bar{p}} = 900 \text{ MeV}, L_{max} = 3)$

Spin density matrix ρ

- Spin S particle : n x n -matrix with $n = 2S+1$
- Provides full information on production mechanism, diagonal elements give propability of certain spin state ($\text{Tr}(\rho) = 1$)
- $\rho_{00} \neq \rho_{11} = \rho_{-1-1}$ Alignment
 $\rho_{11} \neq \rho_{-1-1}$ Polarization (Spin 1)
- Extraction via particle production amplitudes

$$\rho_{\lambda_X \lambda'_X} = \frac{1}{\sum_{\lambda_{\bar{p}}, \lambda_p, \lambda_x, \lambda_X} |T_{\lambda_{\bar{p}} \lambda_p \lambda_x \lambda_X}|^2} \cdot \sum_{\lambda_{\bar{p}}, \lambda_p, \lambda_x} T_{\lambda_{\bar{p}} \lambda_p \lambda_x \lambda_X}^* T_{\lambda_{\bar{p}} \lambda_p \lambda_x \lambda'_X}$$

H. Koch,
Helicity amplitude for $\bar{p}p \rightarrow \omega \pi^0$,
Internal PANDA Note

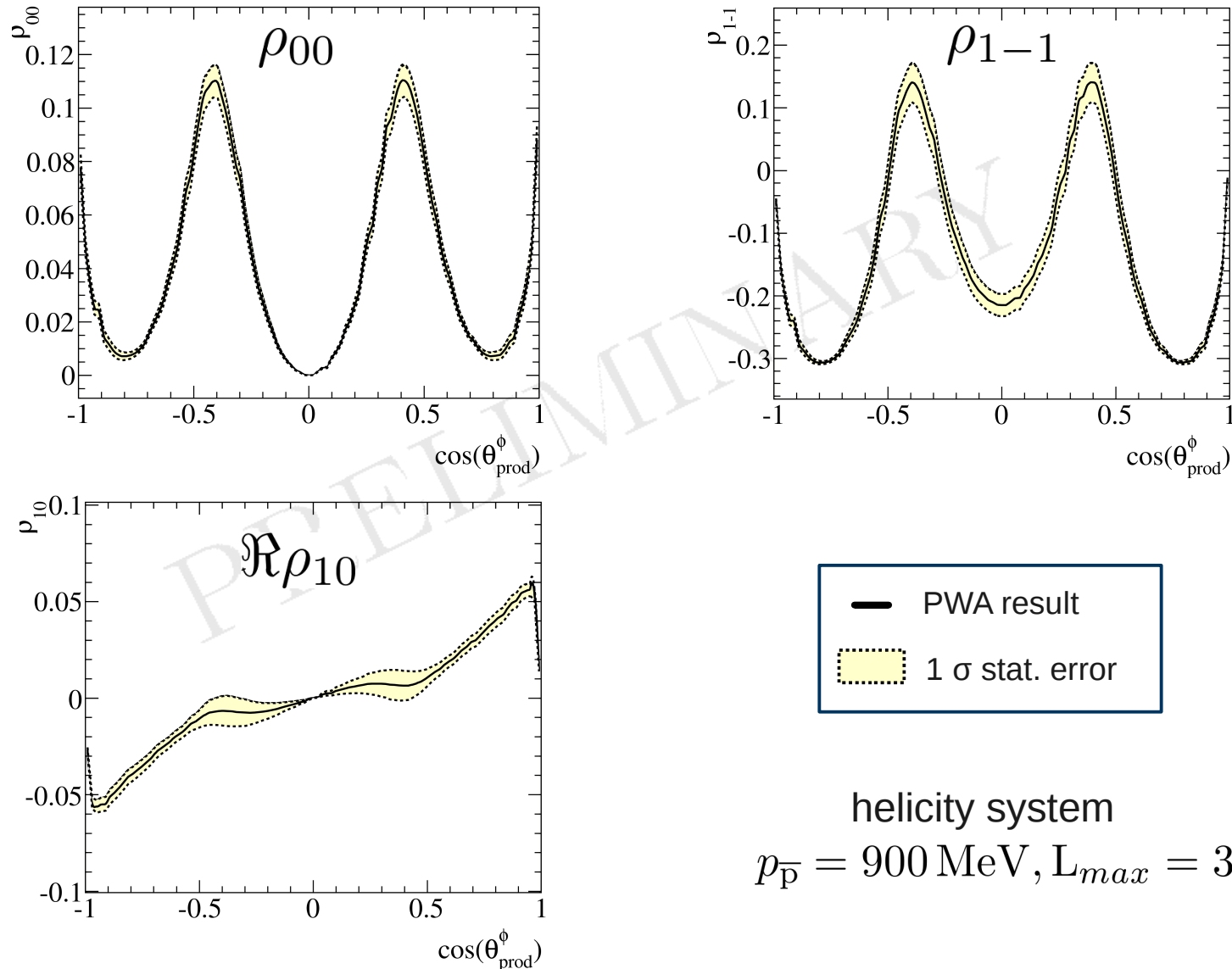
- Or via fit to decay angular distribution

$$W_{\text{pseudoscalars}}(\cos \theta, \phi) = \frac{3}{4\pi} \left(\frac{1}{2}(1 - \rho_{00}) + \frac{1}{2}(3\rho_{00} - 1) \cos^2 \theta \right. \\ \left. - \sqrt{2} \Re \rho_{10} \sin 2\theta \cos \phi - \rho_{1-1} \sin^2 \theta \cos 2\phi \right)$$

Schilling, Seyboth and Wolf,
Nucl.Phys. B15 (1970) 397-412,
Erratum-ibid. B18 (1970) 332

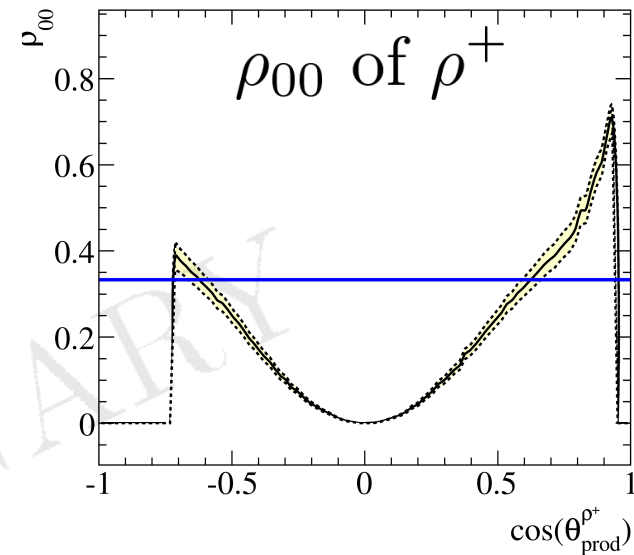
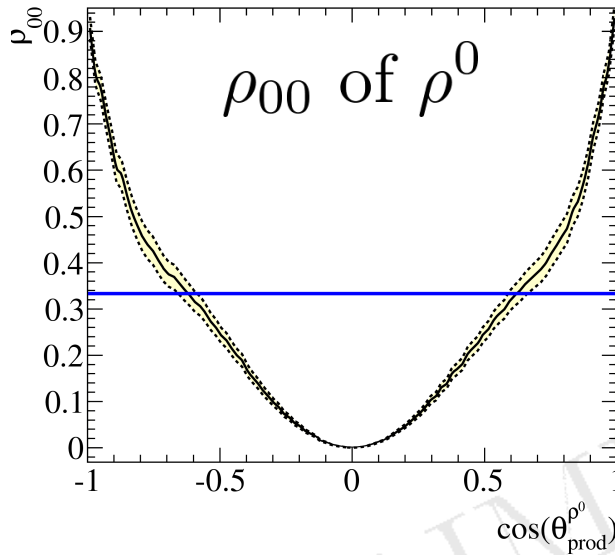
“Schilling's method”

Spin density matrix ($\phi \rightarrow K^+ K^-$)

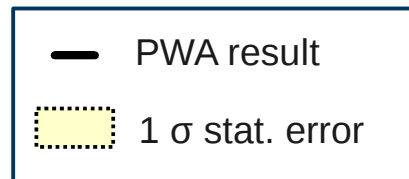


Spin density matrix ($\rho \rightarrow \pi\pi$)

$$I(\bar{p}p) = 0$$

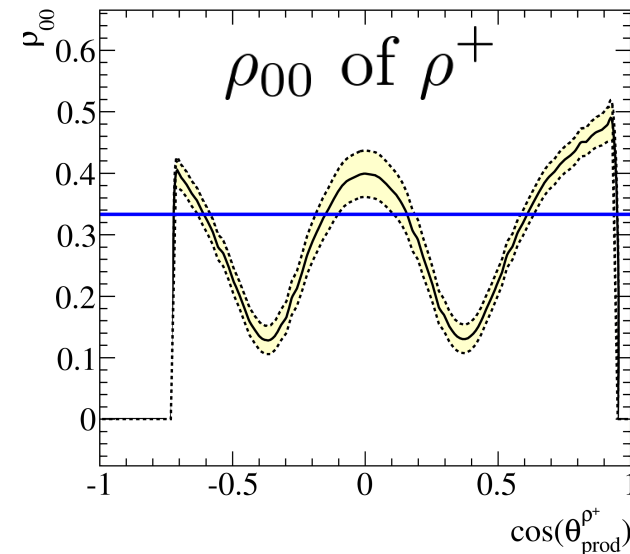


$$I(\bar{p}p) = 1$$

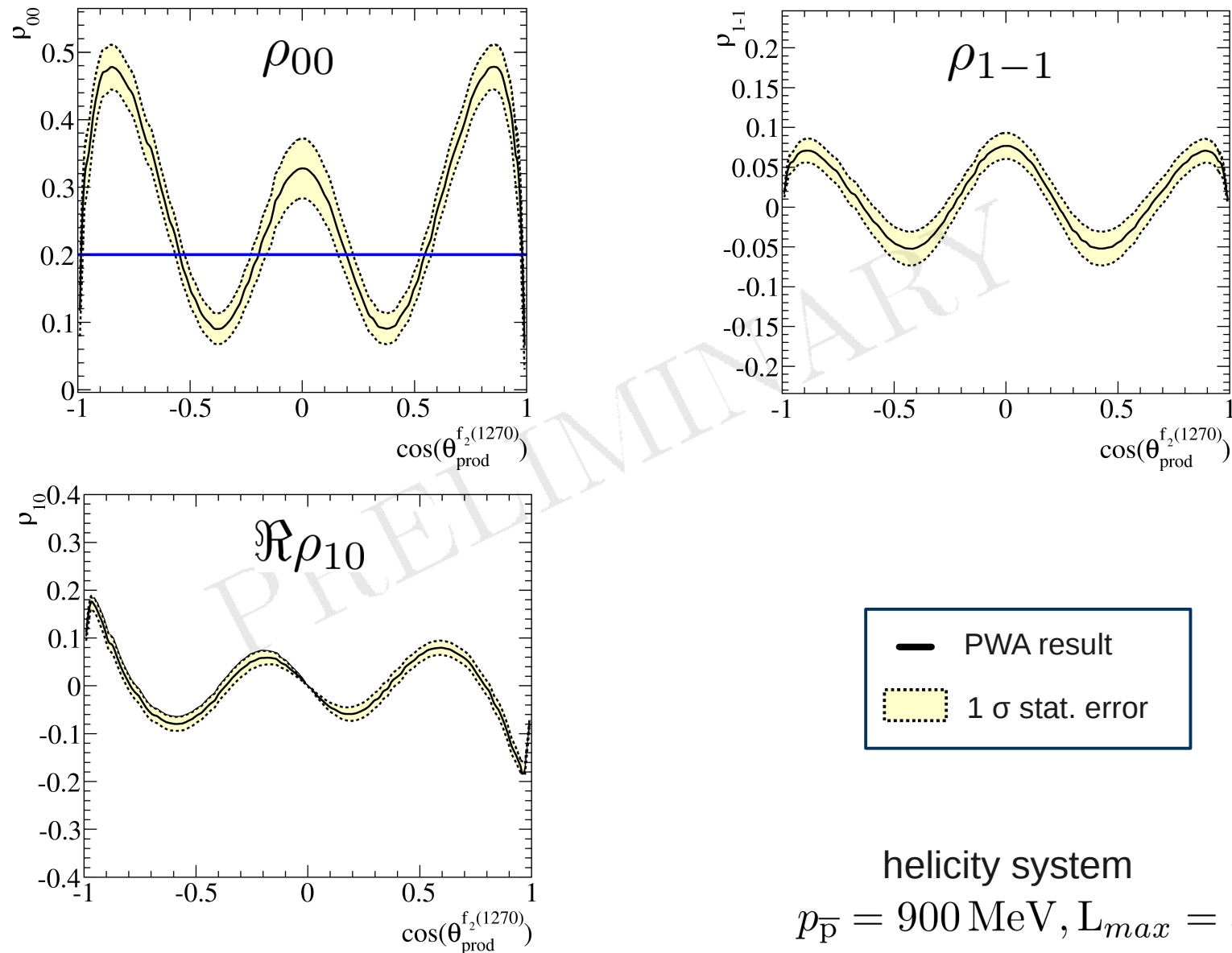


helicity system

$$p_{\bar{p}} = 900 \text{ MeV}, L_{max} = 3$$



Spin density matrix $f_2(1270)$



Summary and outlook

- Analyses of Crystal Barrel LEAR data with relevance for PANDA
- $\bar{p}p$ initial states and production of vector mesons
- Full PWA of the channels $K^+K^-\pi^0$ and $\pi^+\pi^-\pi^0$ in progress
 - Excellent description of the data $K^+K^-\pi^0$ at 900 MeV / c
 - $L_{\max} \geq 3$ for 900 MeV / c and ≥ 5 for 1940 MeV / c
 - First coupled channel analysis shows reasonable results
- Spin density matrix can be extracted from production amplitudes for $\phi, \rho, f_2(1270), a_2(1320), K^* \dots$
- L_{\max} evaluation for each resonance
- $\pi\pi$ production angles need to be understood
- Coupling of more channels like $\pi^0\pi^0\pi^0, \pi^0\pi^0\eta, \pi^0\eta\eta \dots$

Thank you