

Progress on the online tracking algorithm

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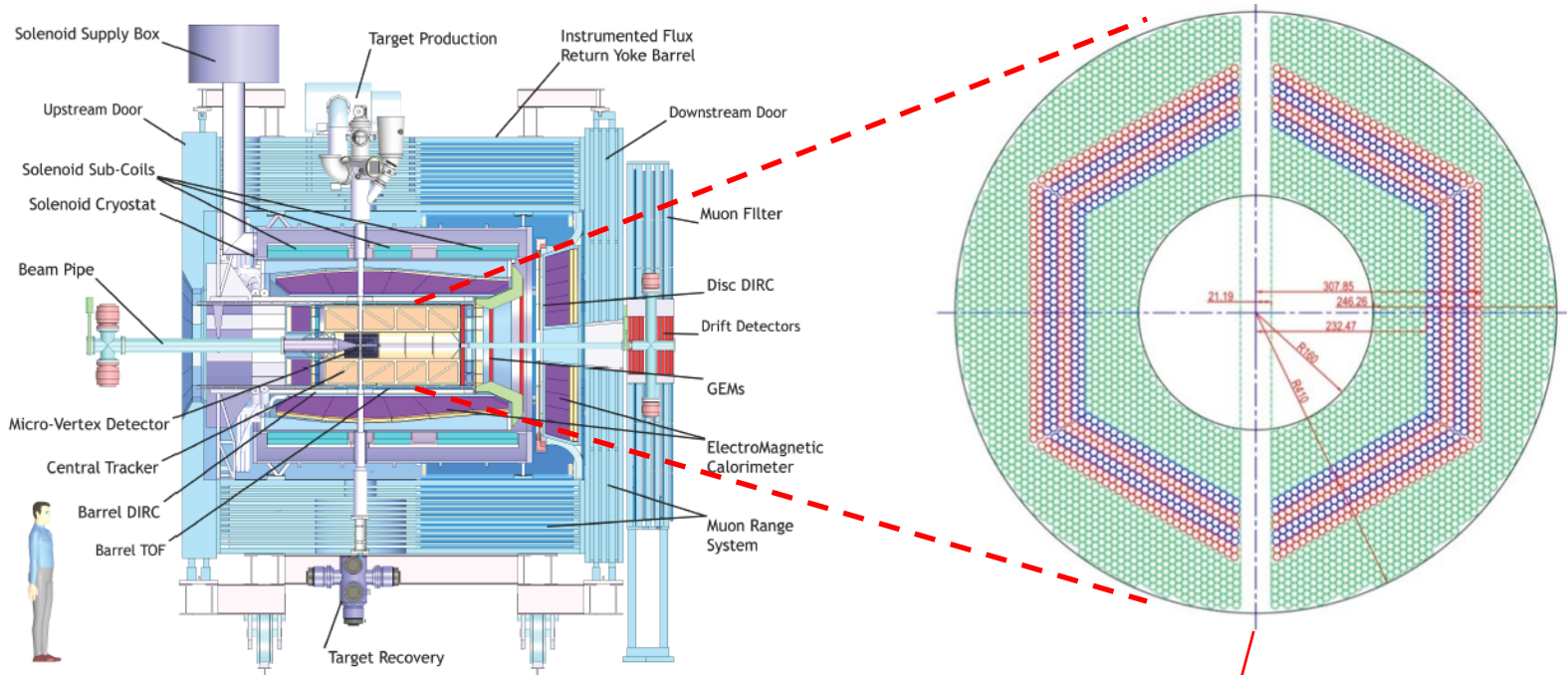
II. Physikalisches Institut, JUSTUS-LIEBIG-UNIVERSITÄT GIESSEN

Dec. 10 2013

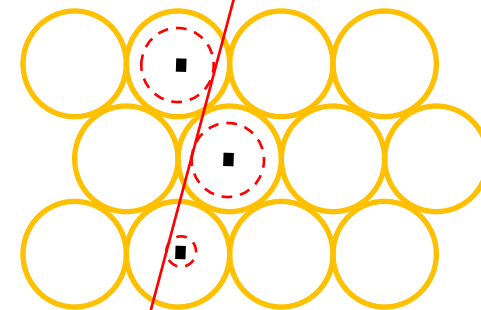
Outline

1. Introduction
2. Road finding and momentum calculation
3. Performance studies
 - Single/multi-track events
 - Dpm (event-based)
 - Dpm (time-based)
4. VHDL implementation
5. Summary and outlook

Straw Tube Tracker(STT)

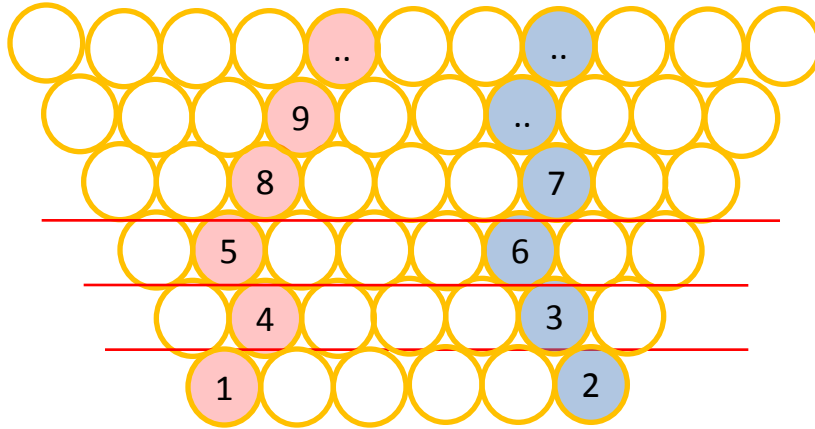


- 4636 Straw tubes
- 23-27 planar layers
 - 15-19 axial layers(**green**) in beam direction
 - 4 stereo double-layers for 3D reconstruction, with ± 2.89 skew angle(**blue/red**)



From STT : Wire position + drift time

Road finding



1: Sort hits, and fill into array
array_layer_0 <= (1, 2)
array_layer_1 <= (3, 4)
array_layer_2 <= (5, 6)

2: Combine hits of two adjacent layers,
keep effective combinations (in red color)

Layer 0 & 1: 1->3 || 2->3 || 1->4 || 2->4

Layer 1 & 2: 3->5 || 4->5 || 3->6 || 4->6

Easy to parallel design.

3: Connect these combinations and
form tracklets

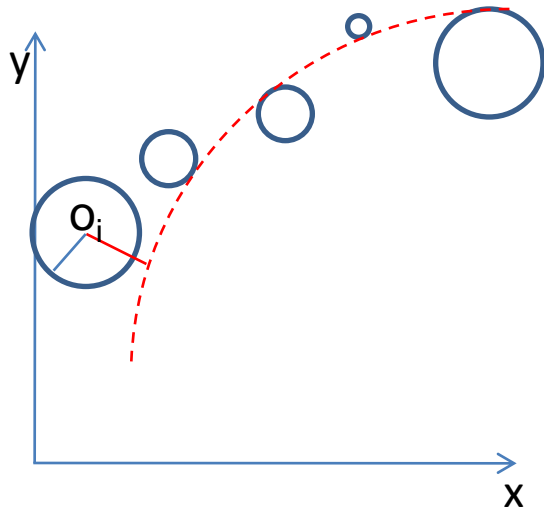
1->4 + 4->5 ... = 1->4->5->8->9

2->3 + 3->6 ... = 2->3->6->7.....

If somewhere broken, a further step to
connect them...

4: Calculate momentum for each tracklet.

Calculation of circle parameters



Known : x_i, y_i, d_i

Question: To determine a circle,

$$x^2 + y^2 + ax + by + c = 0$$

Method: Minimize the equation

$$E^2 = \sum (x_i^2 + y_i^2 + a x_i + b y_i + c)^2 (1/d_i)^2$$

1) Circle para.

$$\begin{pmatrix} S_{xx} & S_{xy} & S_x \\ S_{xy} & S_{yy} & S_y \\ S_x & S_y & N \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} -S_{xxx} - S_{xyy} \\ -S_{xxy} - S_{yyy} \\ -S_{xx} - S_{yy} \end{pmatrix}$$

$$\begin{aligned} S_x &= \sum x_i & \dots \\ S_{xx} &= \sum x_i x_i & \dots \\ S_{xxx} &= \sum x_i x_i x_i & \dots \end{aligned}$$

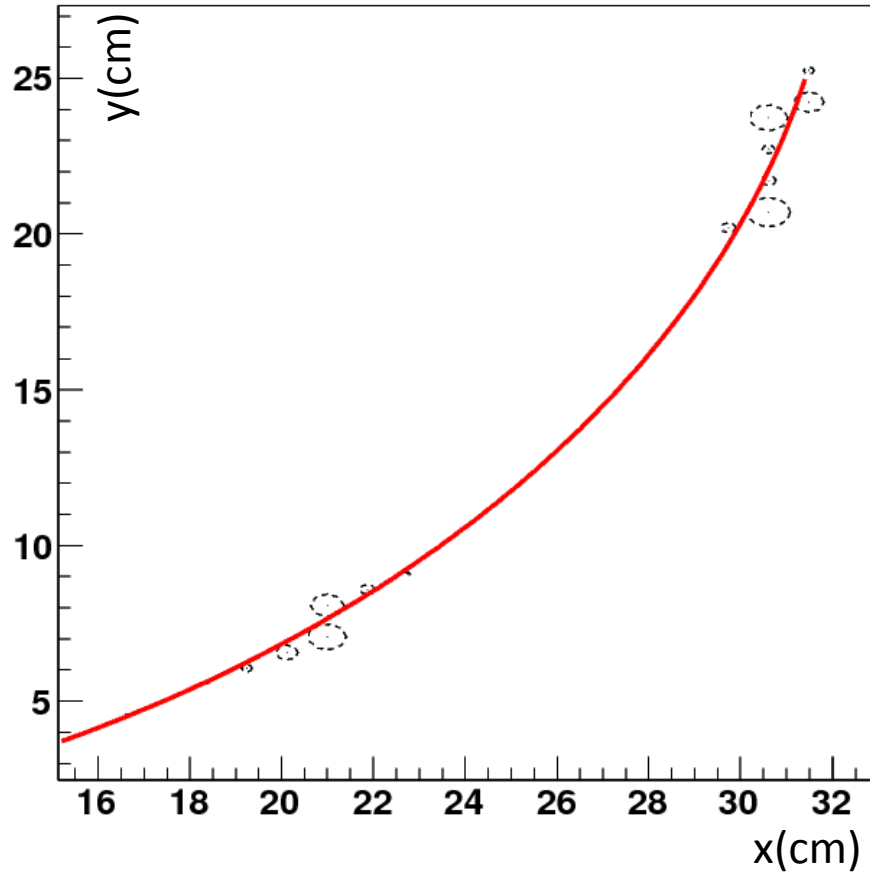
2) Track quality.

$$\chi^2 = 1/n \times \sum_i \frac{(x_i^2 + ax_i + y_i^2 + by_i) / 2r^2}{d_i^2}$$

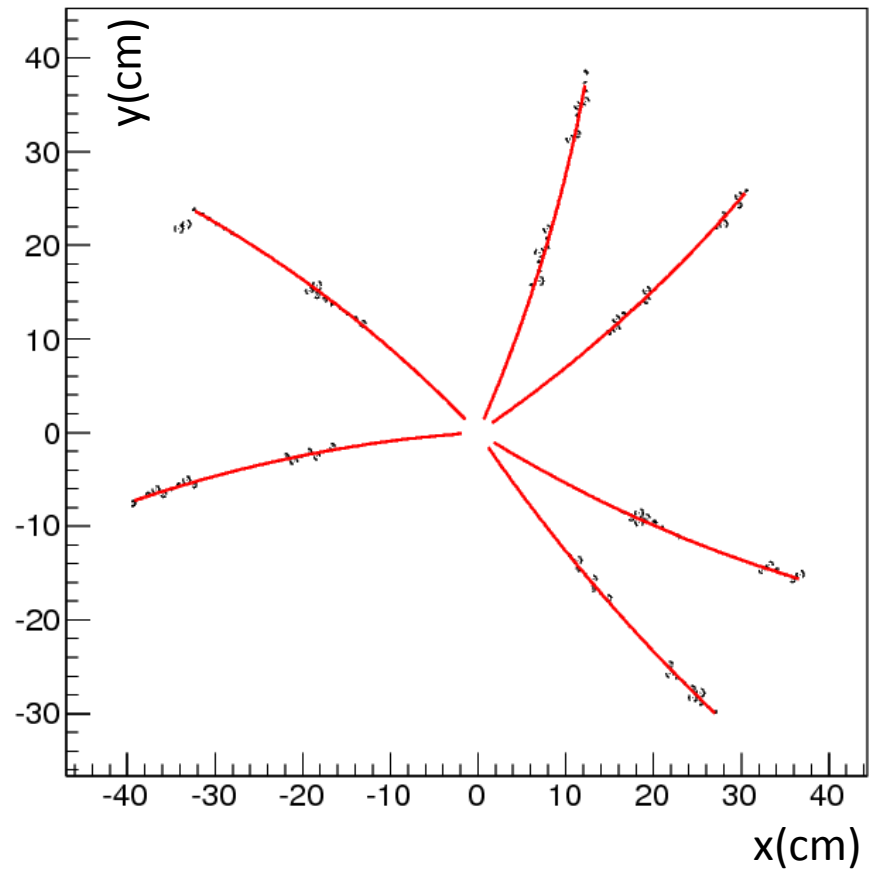
$$= (S_{xxxxdd} + S_{yyyydd} + 2S_{xxyydd} + 2aS_{xxxdd} + 2bS_{yyydd} + 2bS_{xxyydd} + 2aS_{xyydd} + a^2S_{xxdd} + b^2S_{yydd} + 2abS_{xydd}) / 2r$$

Performance study -- single/multi-track event

Single track, 0.2GeV

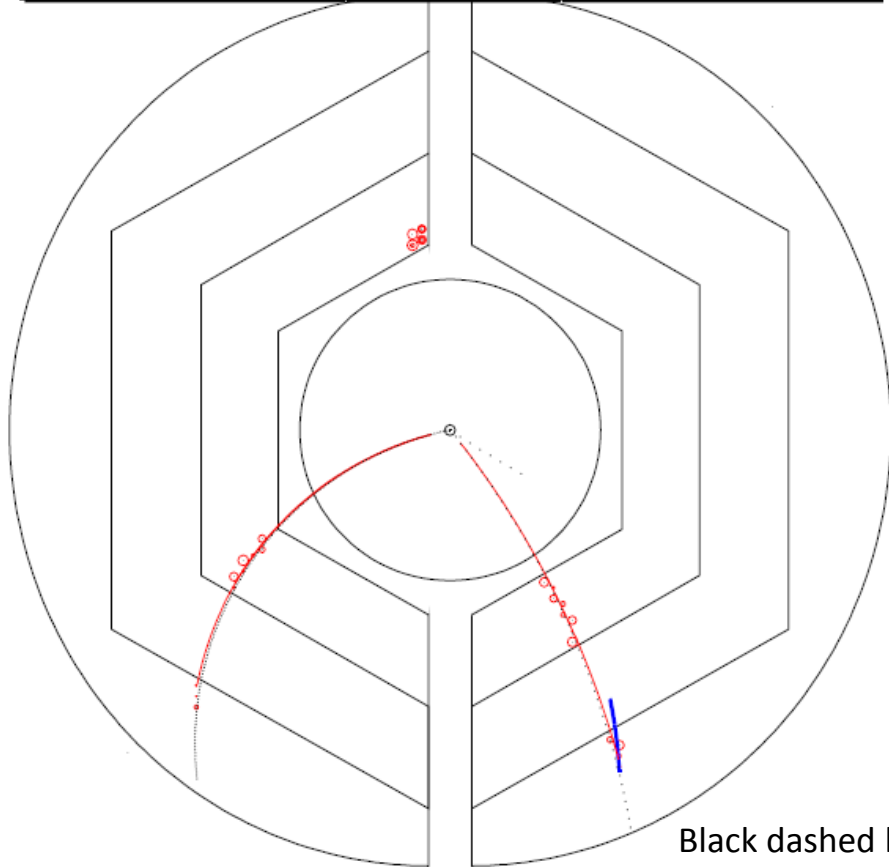


Multi-track

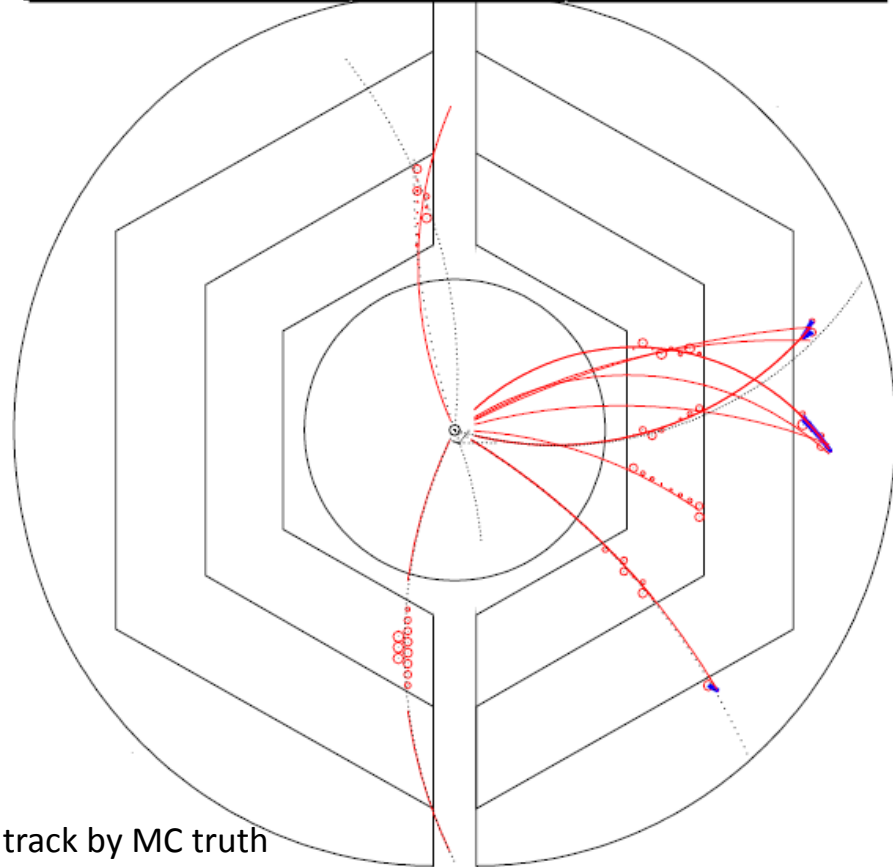


Performance study -- Dpm events

T_0 information: **current event(Red)** or **other events(Green)**



Event #1



Event #2

Black dashed line: track by MC truth

Red line: recon. track

Blue: recon. using outer layers

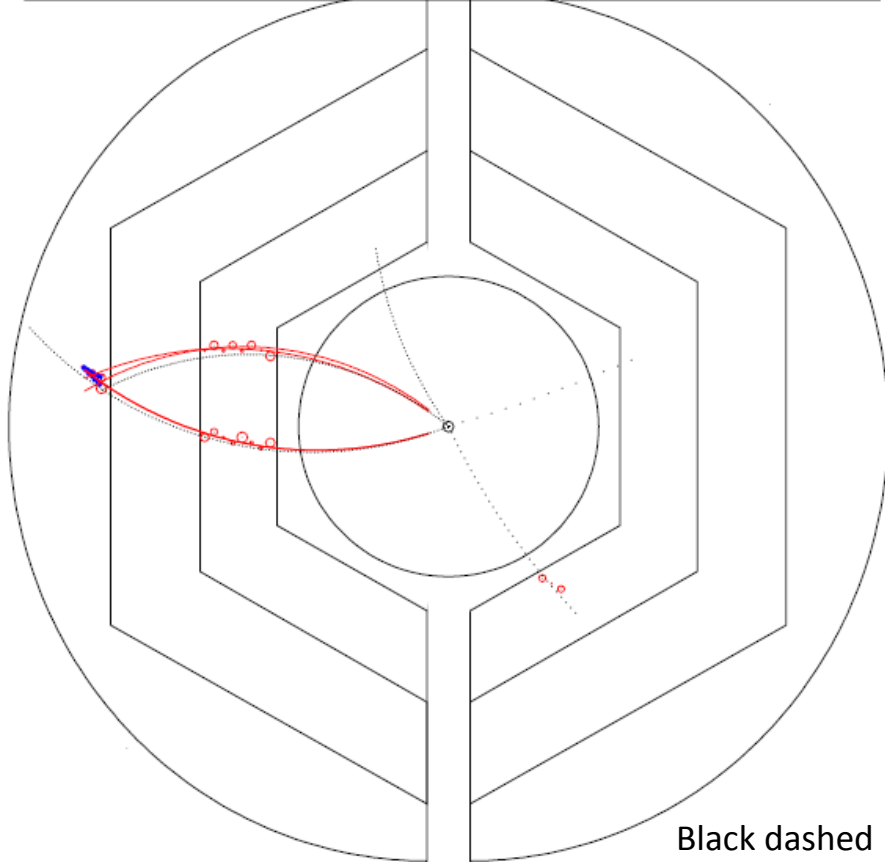
drift circles belong to **current event**

(Red) or **other events** (Green)

Performance study -- Dpm events

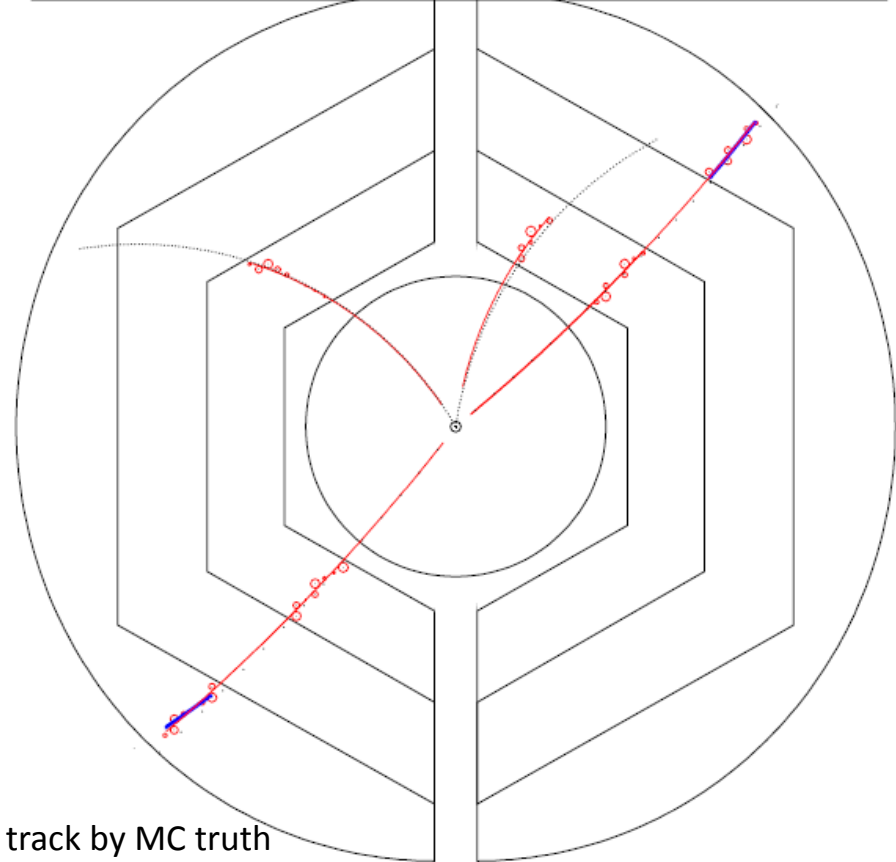
T_0 information: **current event(Red)** or **other events(Green)**

8 → 35 → 114 → 128ns → 138 → 148 → 223 → 235



Event #3

879 → 881 → 976 → 1000 → 1002ns → 1005 → 1101 → 1138 → 1199



Event #4

Black dashed line: track by MC truth

Red line: recon. track

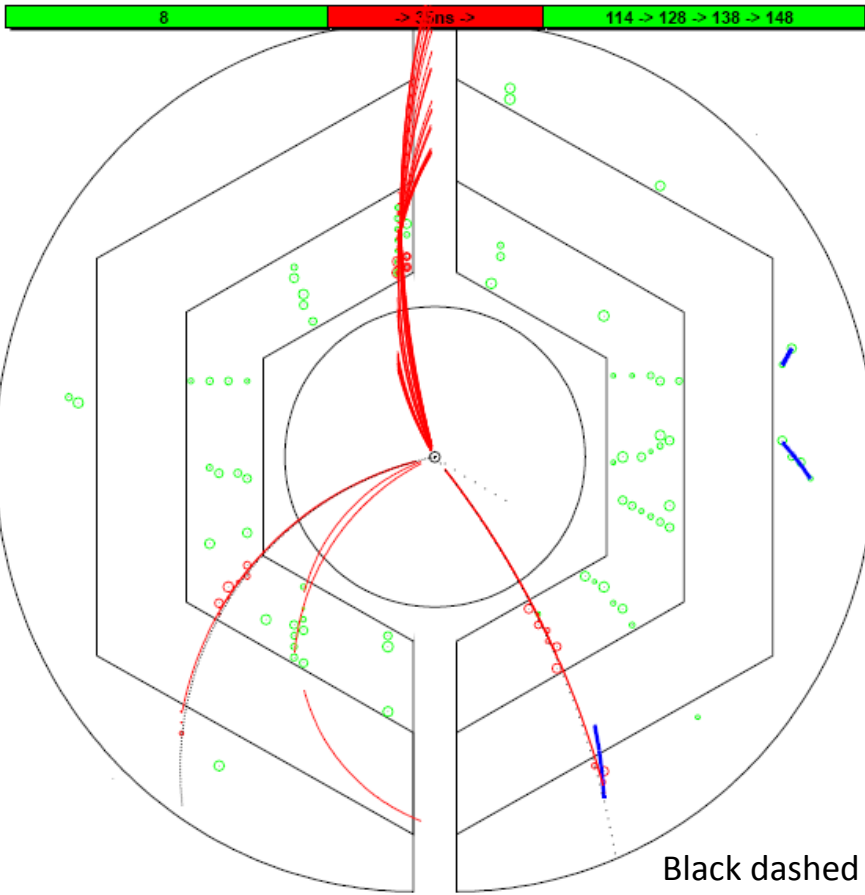
Blue: recon. using outer layers

drift circles belong to **current event**

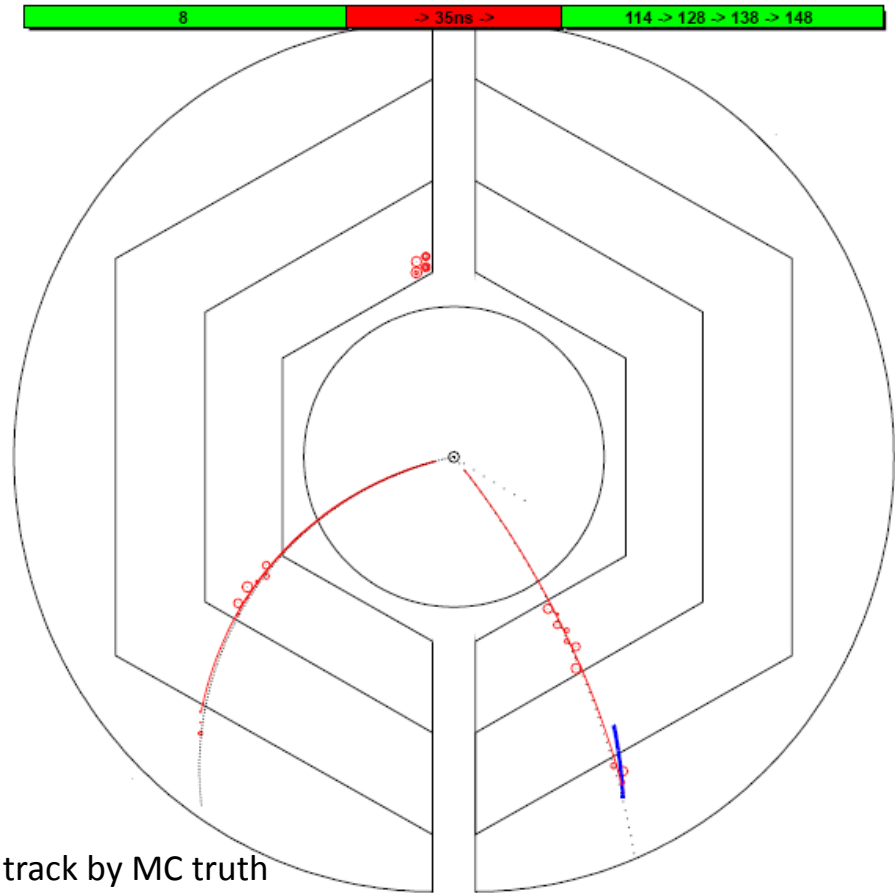
(Red) or **other events** (Green)

Performance study -- Dpm events, time-based

T_0 information: **current event(Red)** or **other events(Green)**



Event #1



Event #1

Black dashed line: track by MC truth

Red line: recon. track

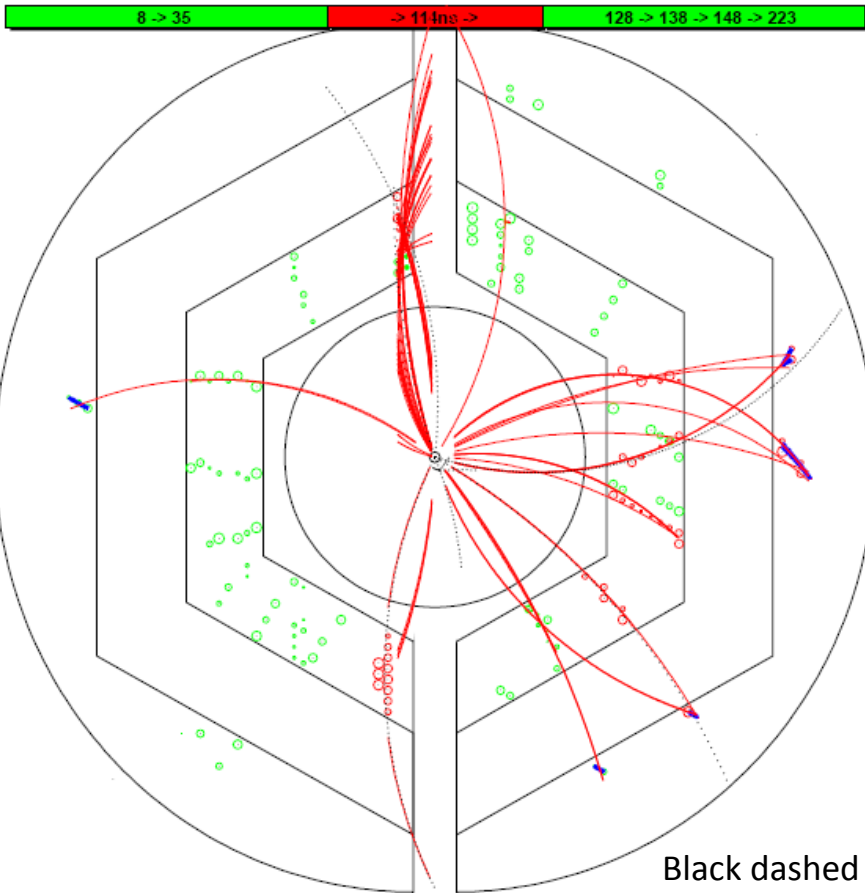
Blue: recon. using outer layers

drift circles belong to **current event**

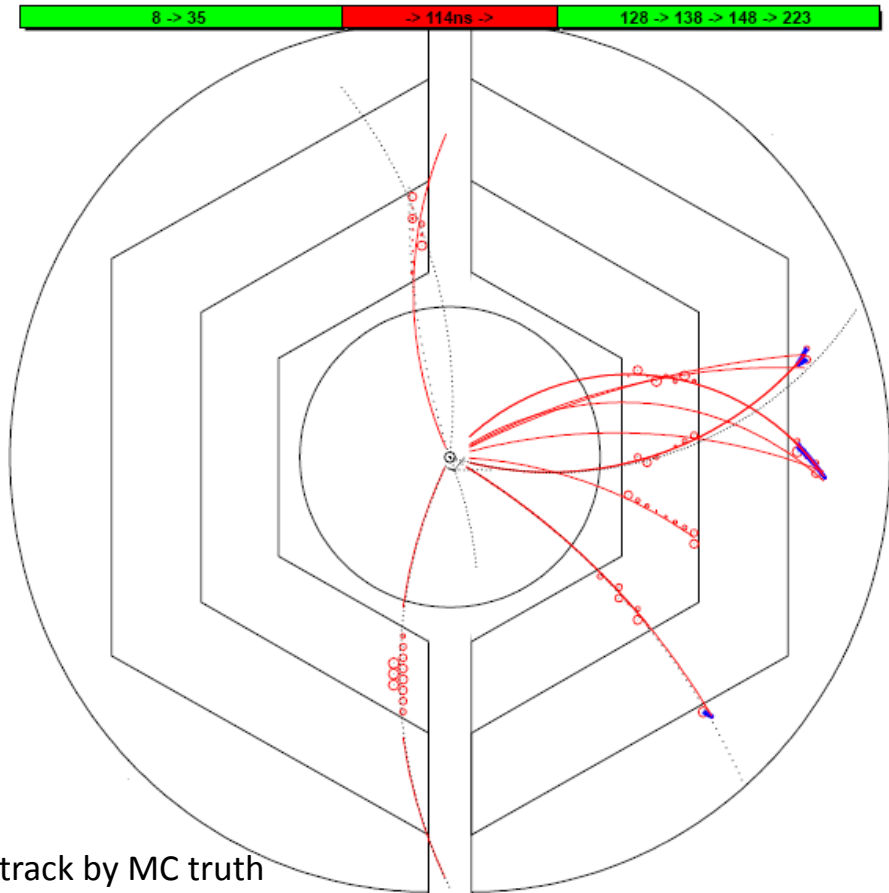
(Red) or **other events (Green)**

Performance study -- Dpm events, time-based

T_0 information: **current event(Red)** or **other events(Green)**



Event #2



Event #2

Black dashed line: track by MC truth

Red line: recon. track

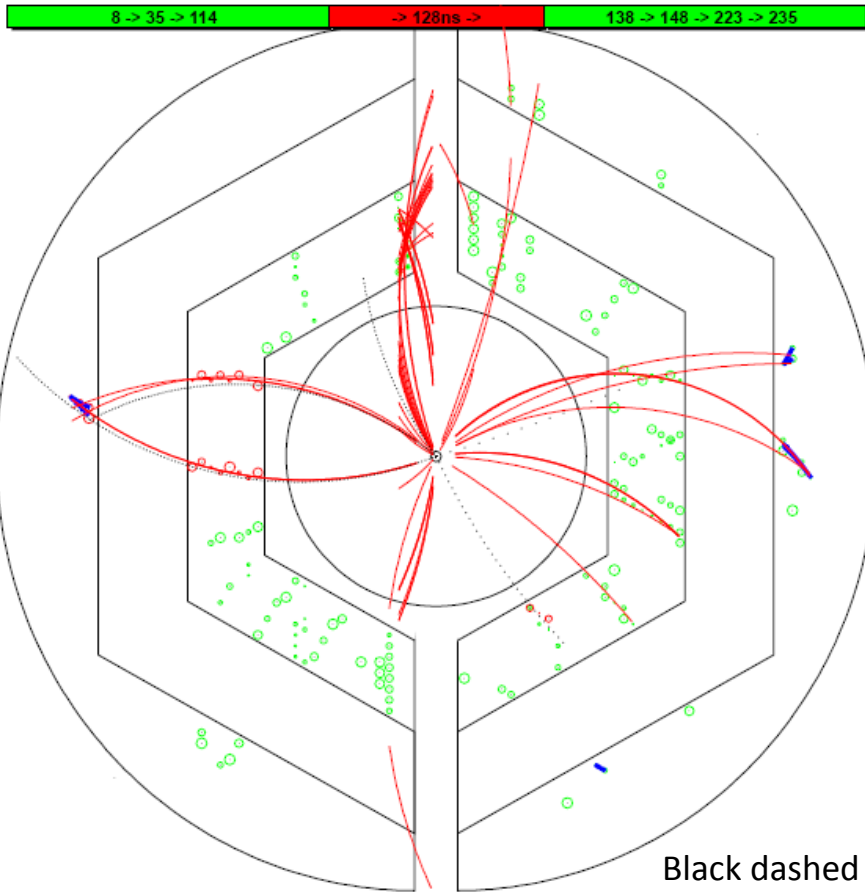
Blue: recon. using outer layers

drift circles belong to **current event**

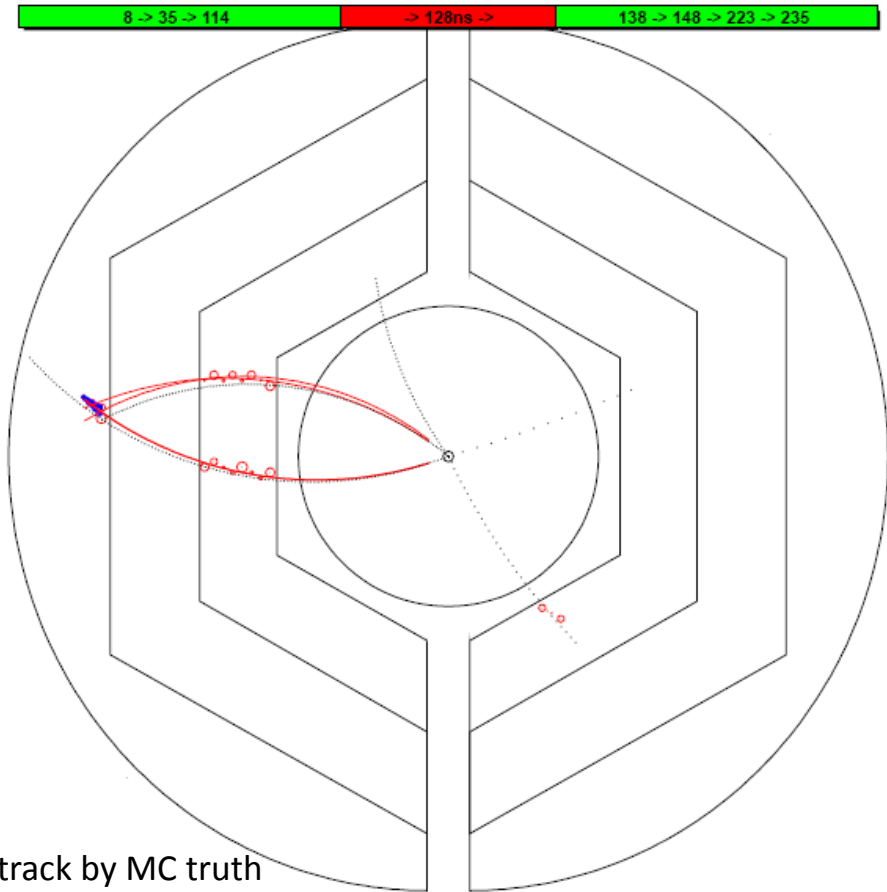
(Red) or **other events (Green)**

Performance study -- Dpm events, time-based

T_0 information: **current event(Red)** or **other events(Green)**



Event #3

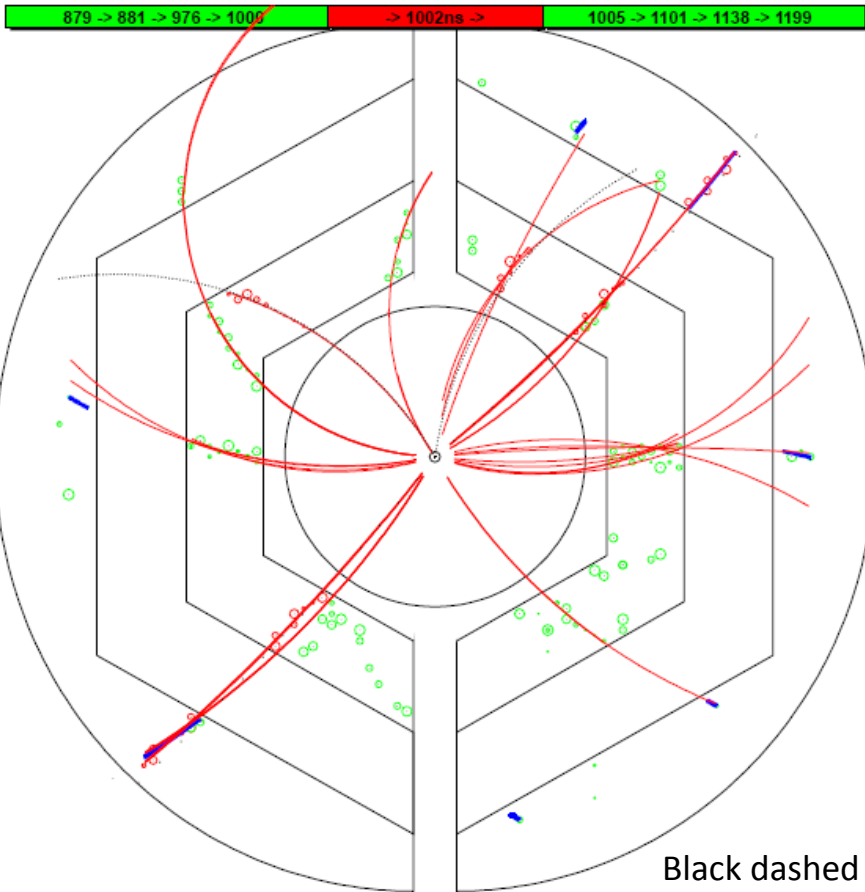


Event #3

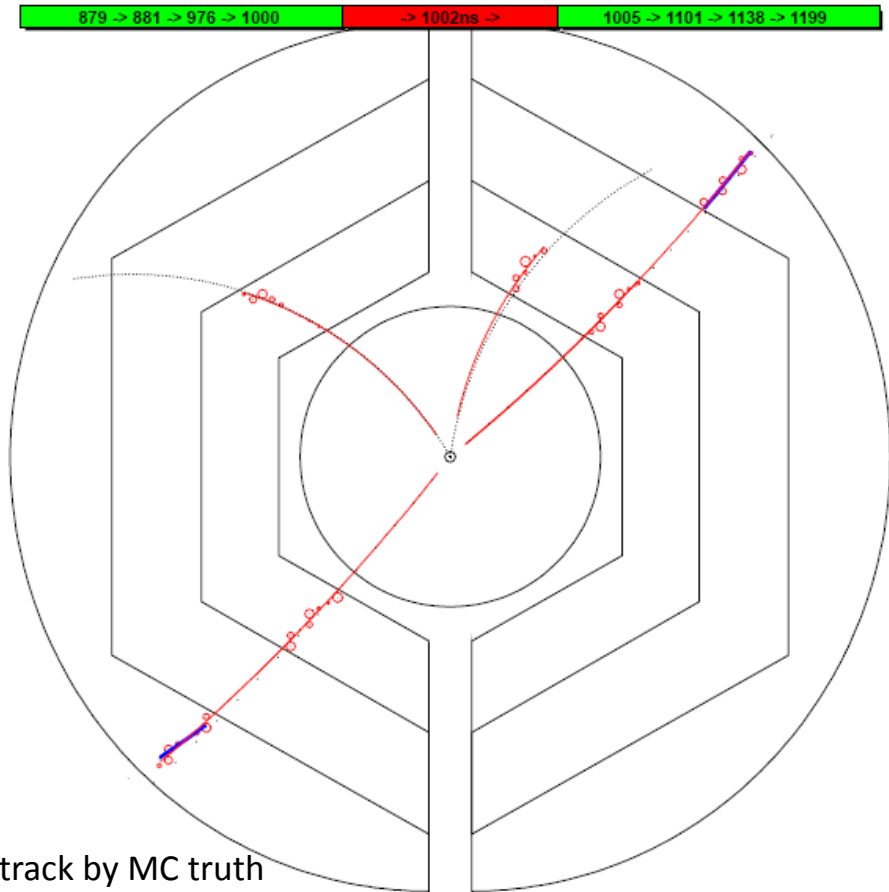
Black dashed line: track by MC truth
Red line: recon. track
Blue: recon. using outer layers
drift circles belong to **current event (Red)** or **other events (Green)**

Performance study -- Dpm events, time-based

T_0 information: **current event(Red)** or **other events(Green)**



Event #4



Event #4

Black dashed line: track by MC truth

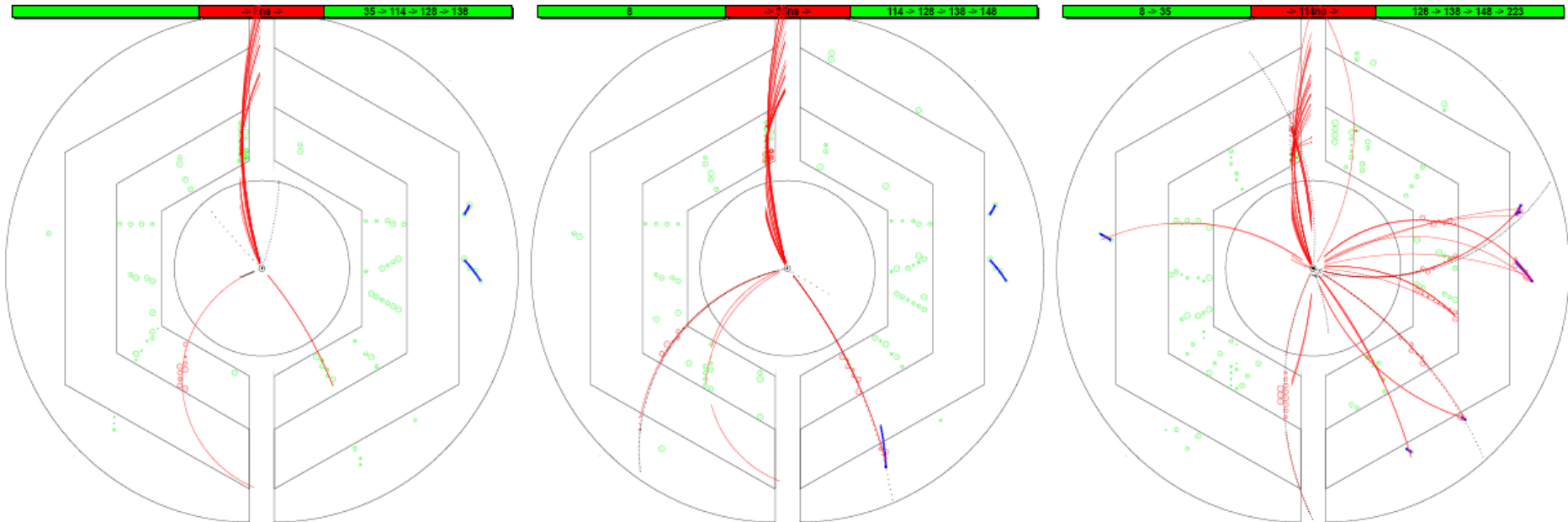
Red line: recon. track

Blue: recon. using outer layers

drift circles belong to **current event**

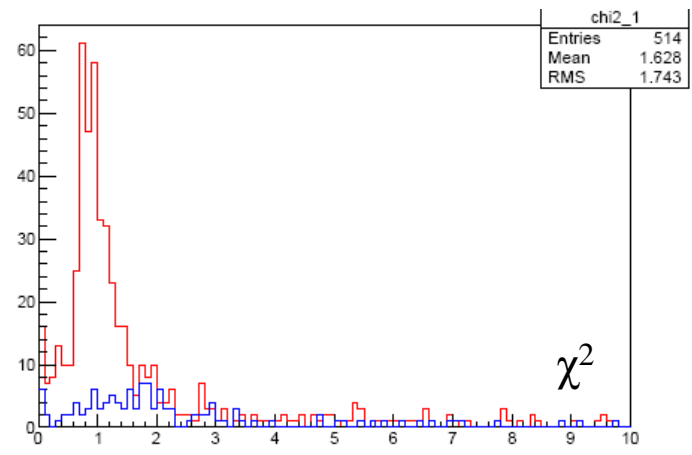
(Red) or **other events (Green)**

Assign a track to the correct event



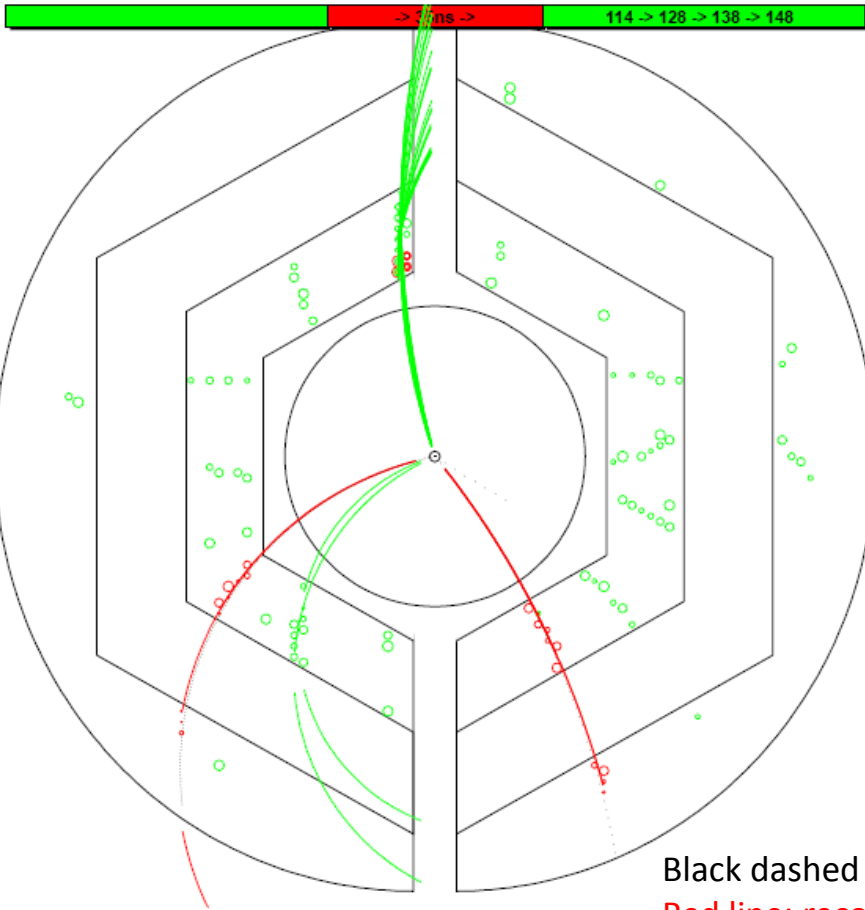
1: Number of hits in the track

2: χ^2 of the track

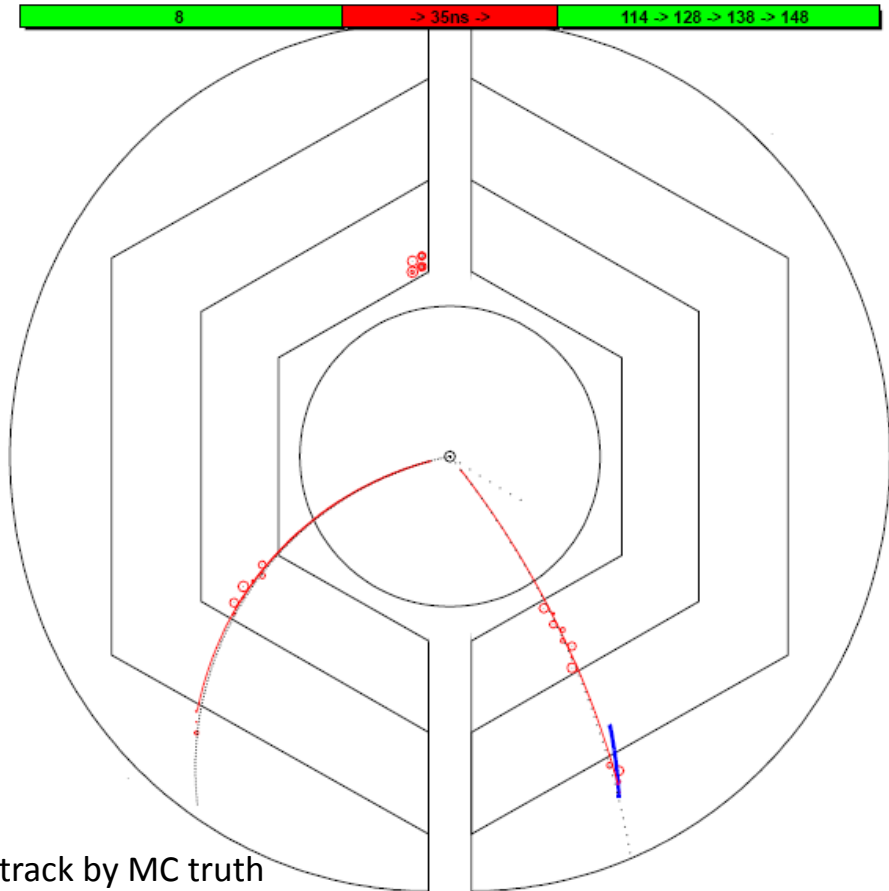


Assign a track to the correct event

T_0 information: **current event(Red)** or **other events(Green)**



Event #1



Event #1

Black dashed line: track by MC truth

Red line: recon. track

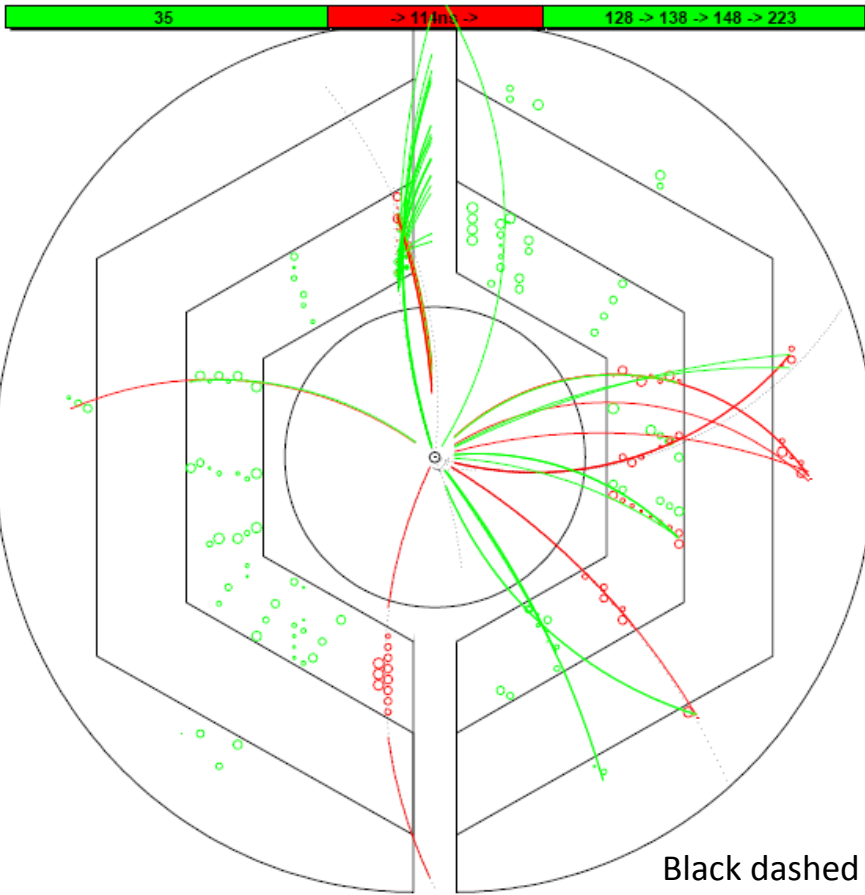
Blue: recon. using outer layers

drift circles belong to **current event**

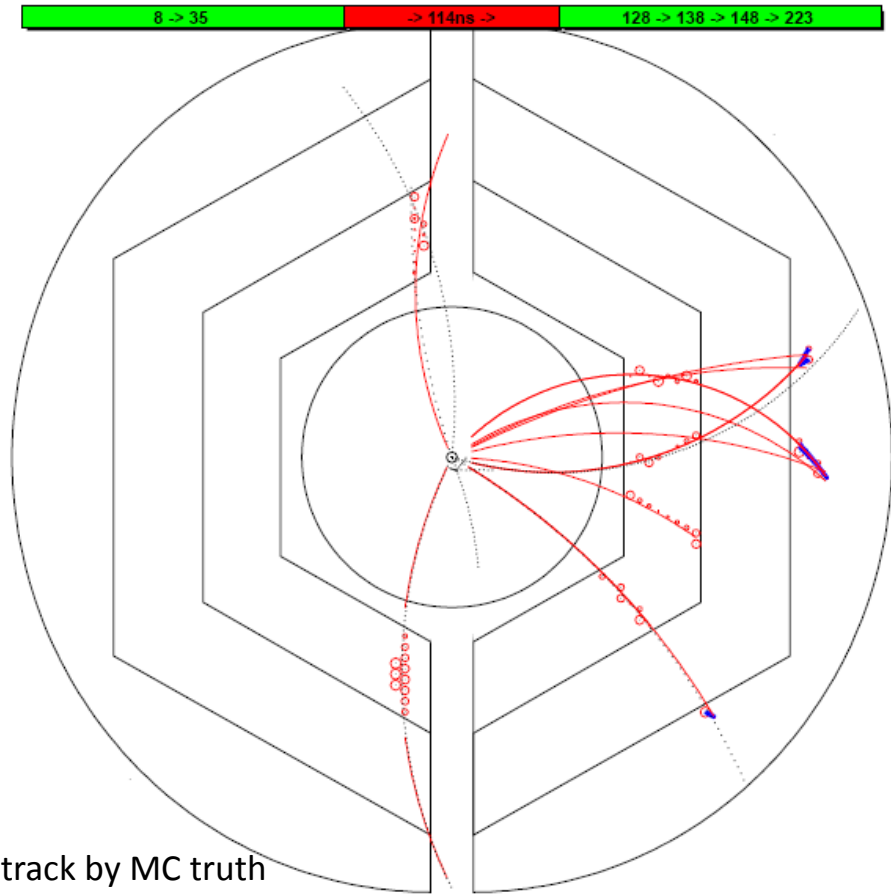
(Red) or **other events** (Green)

Assign a track to the correct event

T_0 information: **current event(Red)** or **other events(Green)**



Event #2



Event #2

Black dashed line: track by MC truth

Red line: recon. track

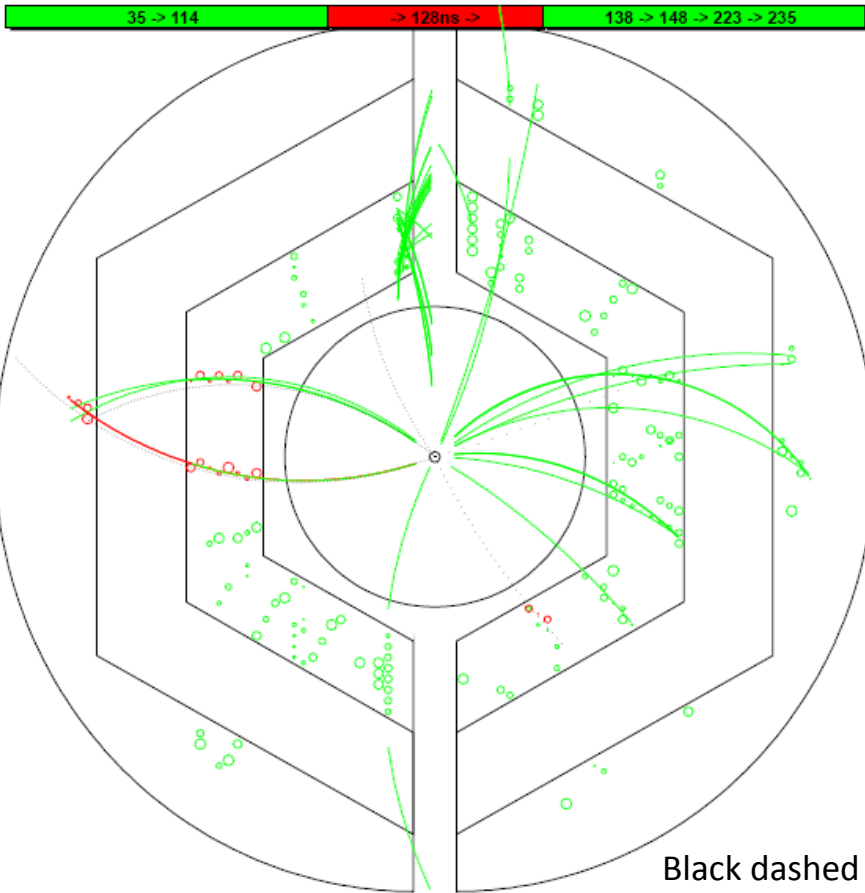
Blue: recon. using outer layers

drift circles belong to **current event**

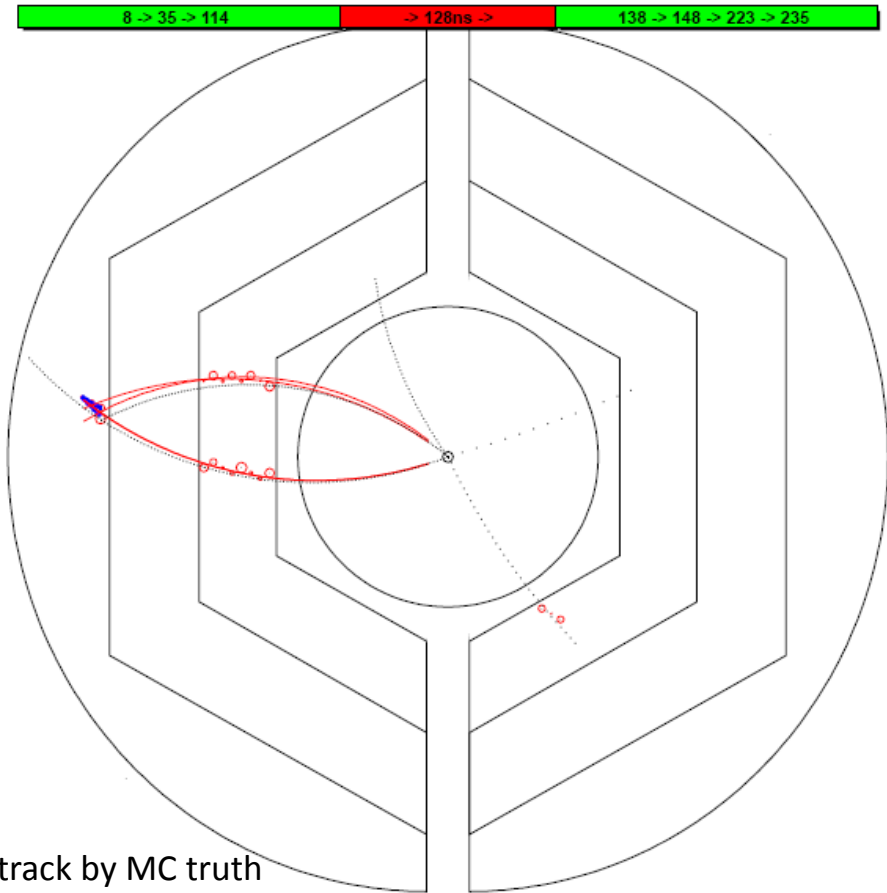
(Red) or **other events** (Green)

Assign a track to the correct event

T_0 information: **current event(Red)** or **other events(Green)**



Event #3



Event #3

Black dashed line: track by MC truth

Red line: recon. track

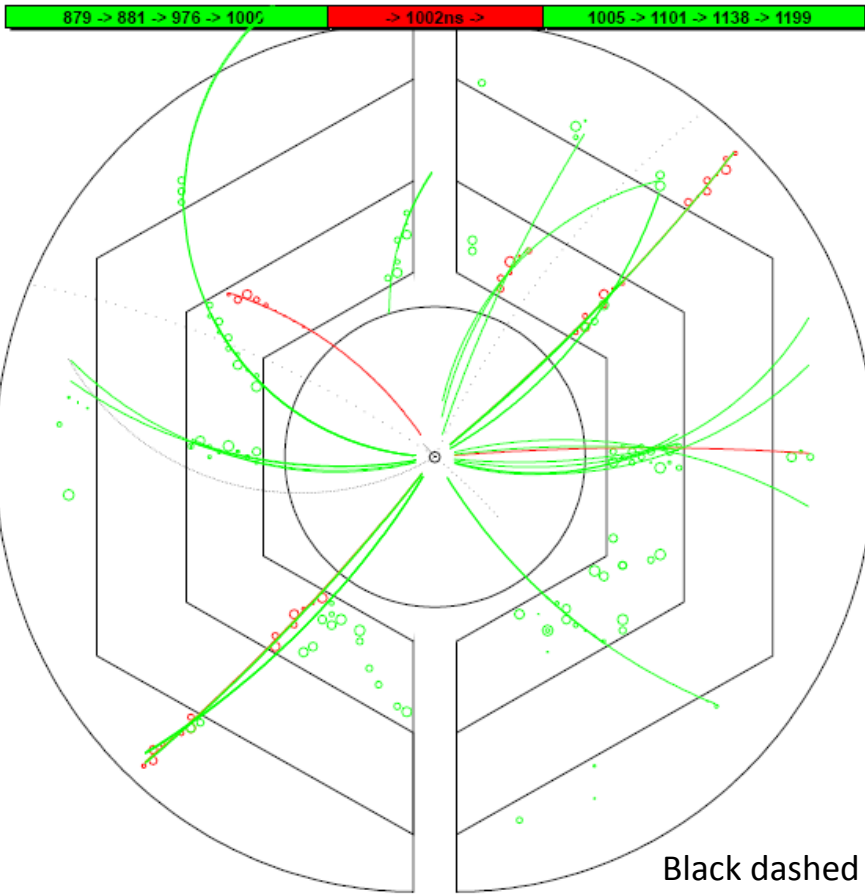
Blue: recon. using outer layers

drift circles belong to **current event**

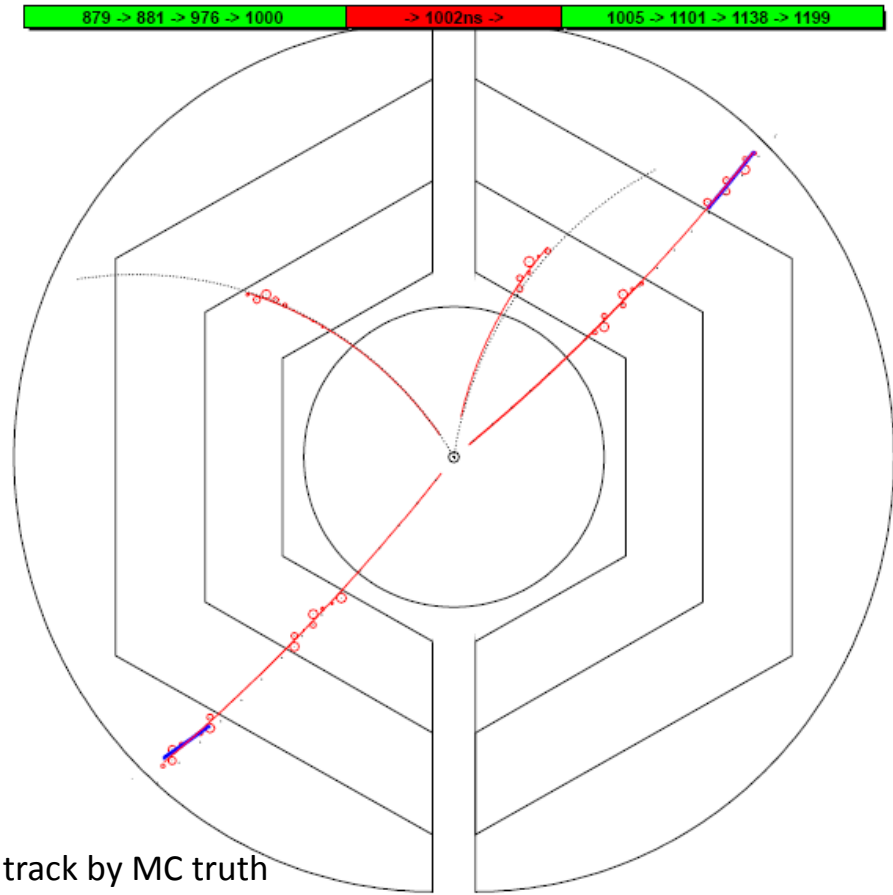
(Red) or **other events** (Green)

Assign a track to the correct event

T_0 information: **current event(Red)** or **other events(Green)**



Event #4



Event #4

Black dashed line: track by MC truth

Red line: recon. track

Blue: recon. using outer layers

drift circles belong to **current event**

(Red) or **other events** (Green)

VHDL implementation

1: Road finding: Using status machine to control the following procedures.

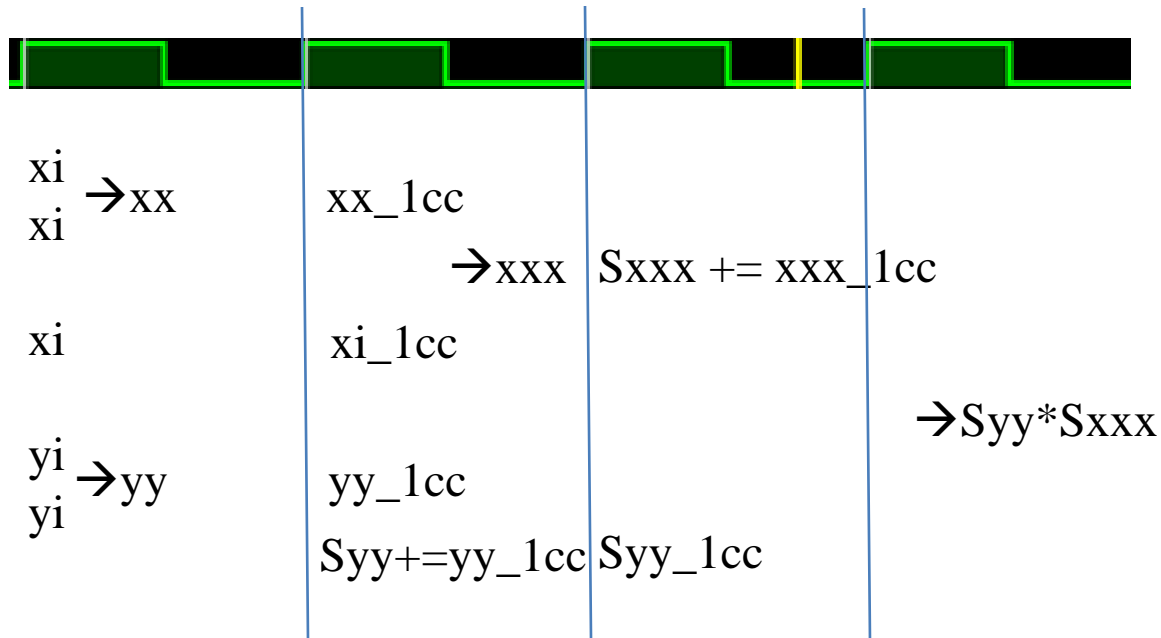
- 1) Hit sorting: fill hit into array_layer_id according to layer ID
- 2) Combine hits from two adjacent layers
- 3) Form a tracklet by attaching hit layer by layer
tracklet_inner : layer 0-7
tracklet_outer: layer 8-15
- 4) Combine tracklet_inner and tracklet_outer.

For one event with 100 hits (6 tracks): 1) 100 clock cycles (cc) 2) ~ 300-600cc 3) ~200cc → several us (if FPGA running at 100MHz)

VHDL implementation

2: Momentum calculation

$$a = S_{yy} * (-S_{xxx} - S_{xyy}) - S_{xy} * (-S_{xxy} - S_{yyy});$$



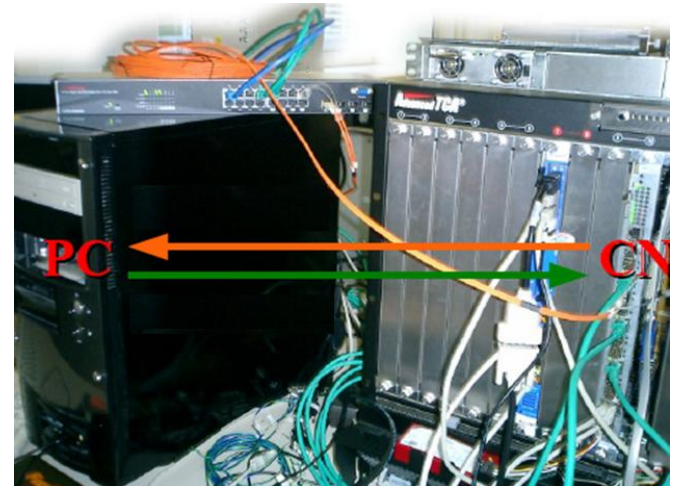
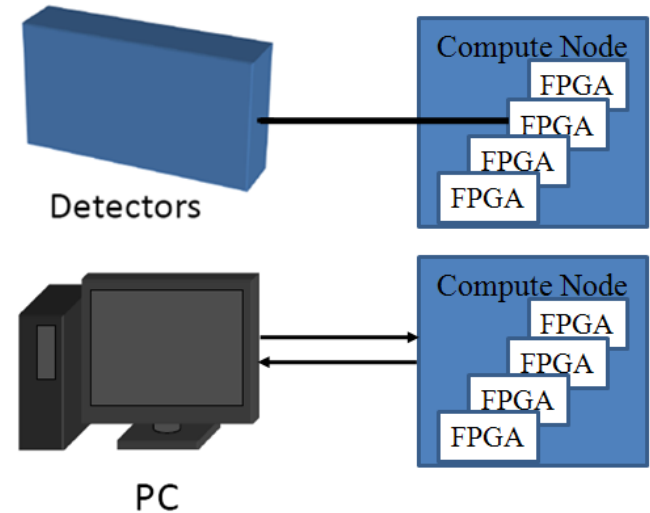
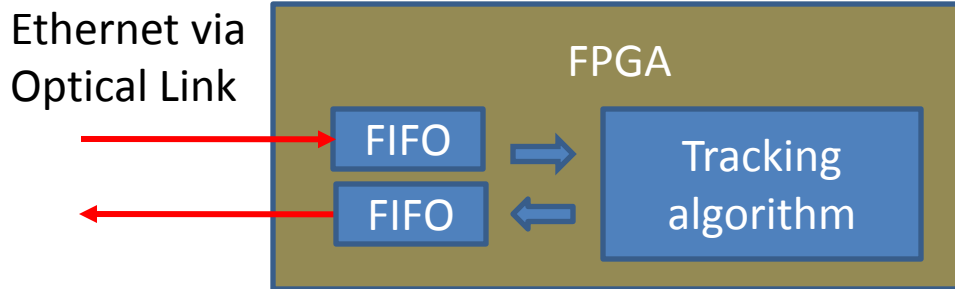
3: χ^2 calculation

24X24 bit not precise enough → 32X32 bit

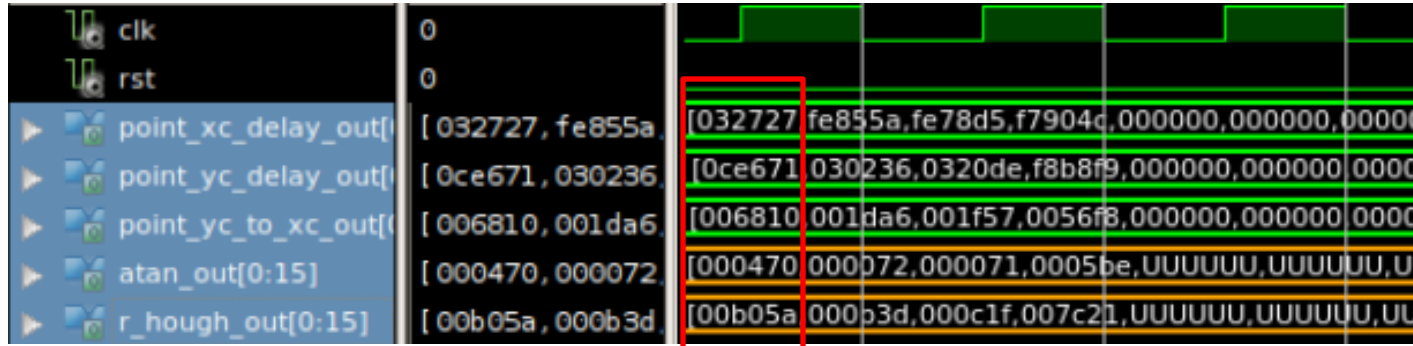
Setup and test

PC as data source and receiver.

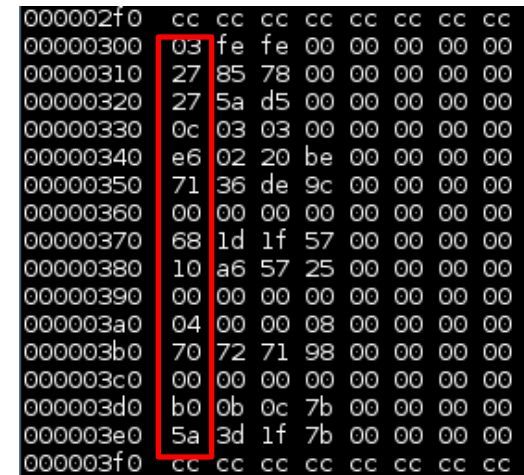
- Ethernet.
- Optical link (UDP by Grzegorz Korcyl)
(not integrated yet)



Simulation with ISim and test at FPGA



Track	#1	#2	#3	#4
Xr (cm):	-38.8	63.9	62.4	124.2
Yr (cm):	-158.7	-129.9	-127.8	107.1
R(cm):	163.3	144.7	142.2	164.0
χ^2 :	0.40	0.63	0.58	0.74



Timing Expectation(4 tracks per event): 200cc+300cc → 300~500cc
 → 3~5 us/event, agrees to the test with 1M events.

Device utilization Summary

Device Utilization Summary				
Logic Utilization	Used	Available	Utilization	Note(s)
Number of Slice Flip Flops	18,301	50,560	36%	
DCM autocalibration logic	14	18,301	1%	
Number of 4 input LUTs	22,934	50,560	45%	
DCM autocalibration logic	8	22,934	1%	
Number of occupied Slices	17,997	25,280	71%	
.....				
Number of DSP48s	124	128	96%	
Number of DCM_ADVs	2	12	16%	
Average Fanout of Non-Clock Nets	2.98			

31 multiplications take too much resource.

Multiplication(32 X 32 bit): 4 DSPs or 1088 LUTs

Need a smarter way to calculate χ^2

Summary and Outlook

- In the road finding module, the match of inner and outer layer is done.
- In momentum calculation module, the χ^2 is calculated.
- One more module is necessary to assign one recon. track to the correct event.

Next to do:

The road finding module is being optimized.

The module to calculate χ^2 need to be improved.

Thank you

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DCM autocalibration logic	14	18,301	1%	
Number of 4 input LUTs	22,934	50,560	45%	
DCM autocalibration logic	8	22,934	1%	
Number of occupied Slices	17,997	25,280	71%	
Number of Slices containing only related logic	17,997	17,997	100%	
Number of Slices containing unrelated logic	0	17,997	0%	
Total Number of 4 input LUTs	23,331	50,560	46%	
Number used as logic	19,002			
Number used as a route-thru	397			
Number used as 16x1 RAMs	8			
Number used for Dual Port RAMs	2,448			
Number used as Shift registers	1,476			
Number of bonded IOBs	36	576	6%	
IOB Flip Flops	3			
IOB Dual-Data Rate Flops	1			
Number of BUFG/BUFGCTRLs	6	32	18%	
Number used as BUFGs	5			
Number used as BUFGCTRLs	1			
Number of FIFO16/RAMB16s	102	232	43%	
Number used as RAMB16s	102			
Number of DSP48s	124	128	96%	
Number of DCM_ADVs	2	12	16%	
Average Fanout of Non-Clock Nets	2.98			

```

00000400 00 00 00 00 00 00 00 00 00 00 00 00 00 00
*
00000490 00 01 02 03 04 05 06 07 00 00 00 00 00 00 00
000004a0 10 11 12 13 14 15 16 17 00 00 00 00 00 00 00
000004b0 1f 20 21 00 00 00 00 00 00 00 00 00 00 00
000004c0 00 00 00 00 00 00 00 00 00 00 00 00 00 00

```

PANDA@20MHz. $2 \cdot 10^7$ events/second

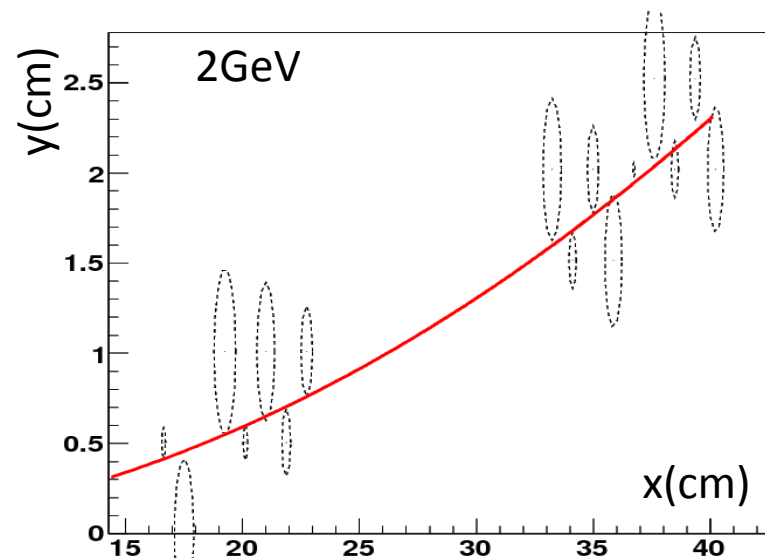
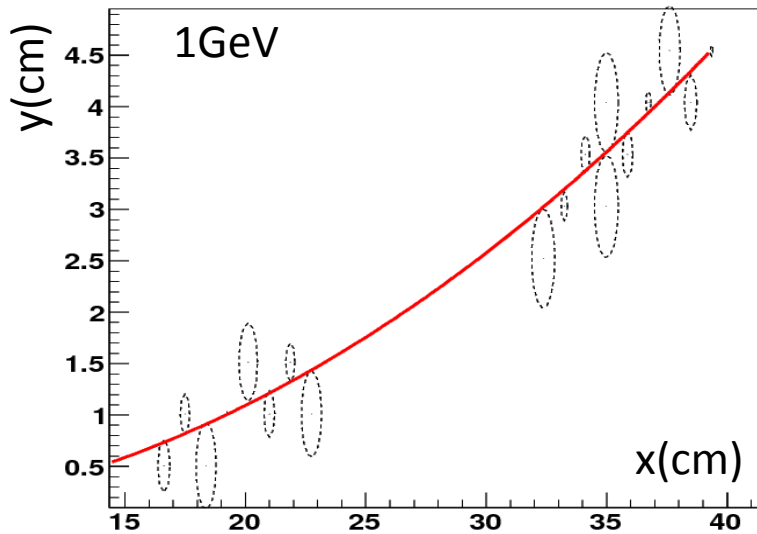
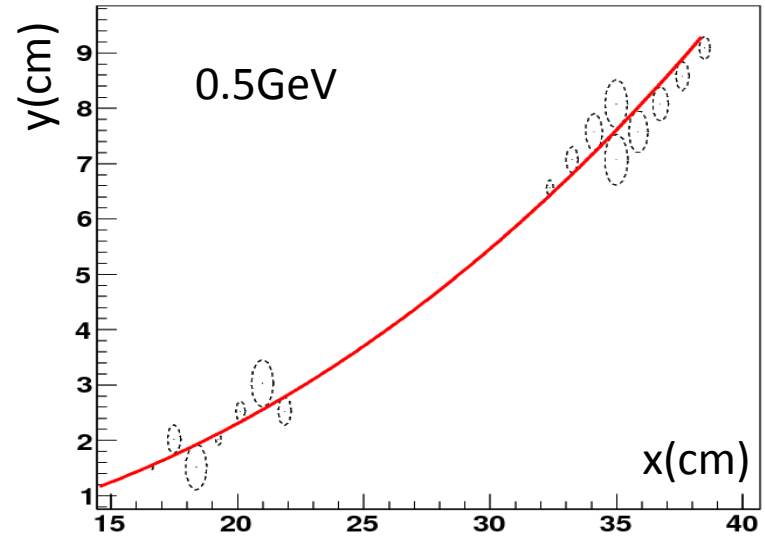
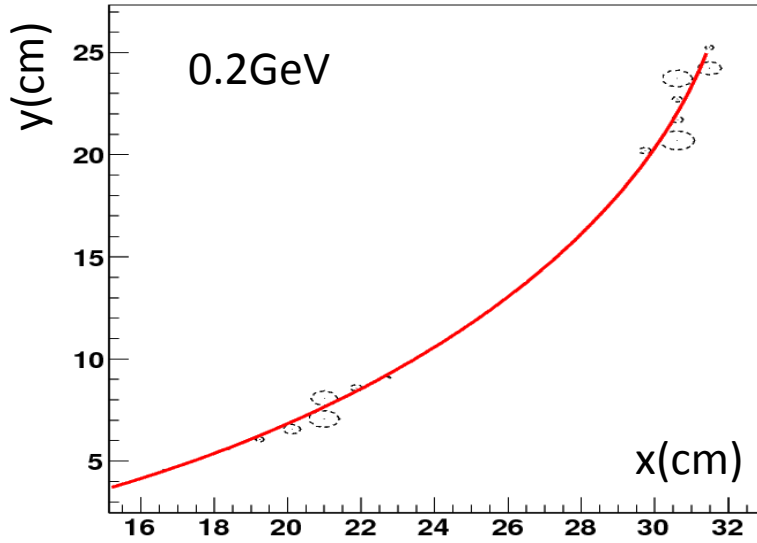
1 event: ~ 3 tracks/event * ~ 16 hits/track * ~ 2 (overlap factor) $\rightarrow \sim 100$ hits/event

When dividing STT into 16 layers, ~ 6 hits/layers. $6 \cdot 6 \cdot 15 = 540$ combinations

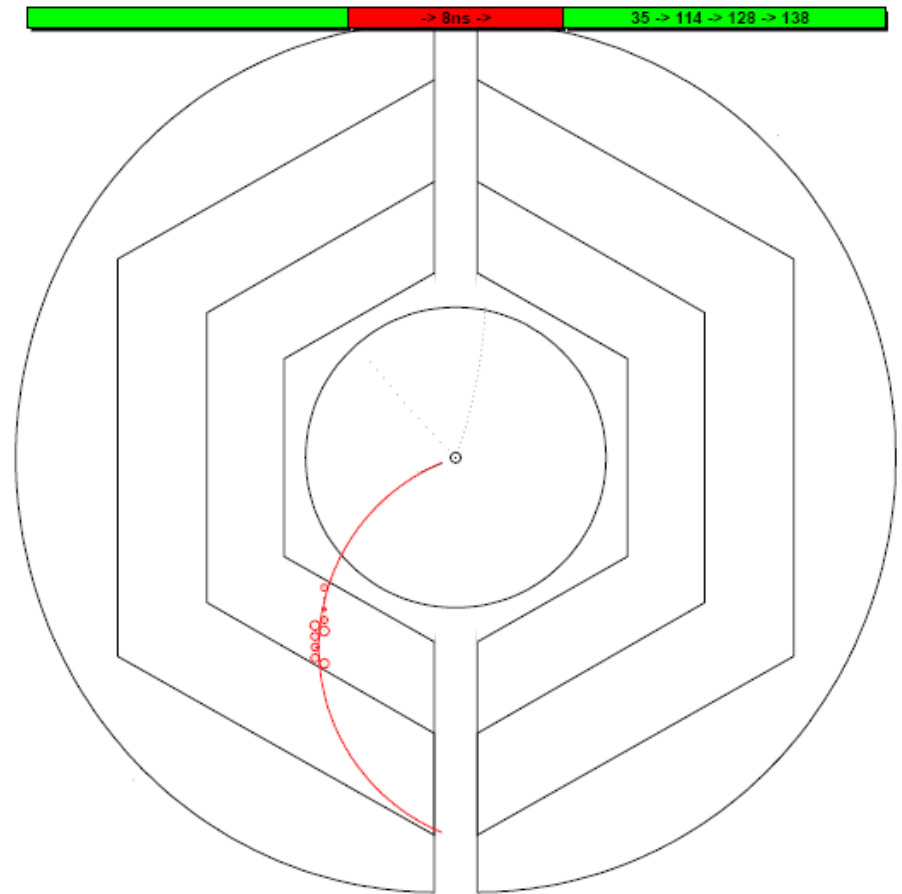
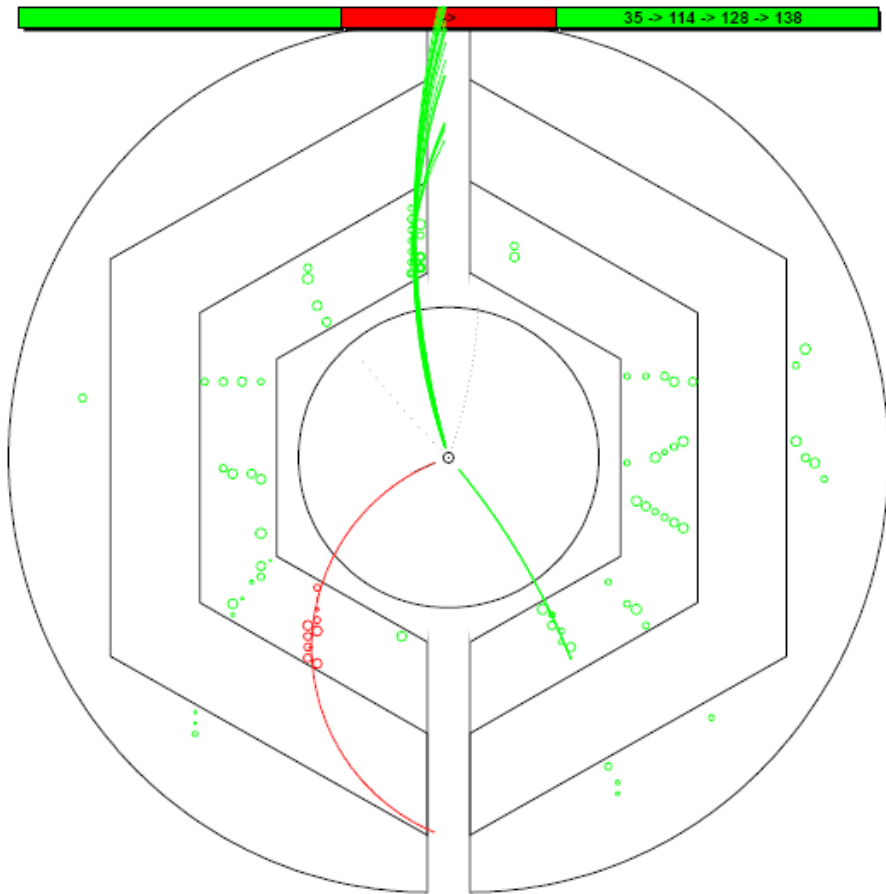
$\sim 1 \sim 2$ clock cycles/combo. $\rightarrow 500 \sim 1000$ clock cycles/event

If FPGA running at 100MHz, $(500 \sim 1000) \cdot 10\text{ns} / 50\text{ns} \rightarrow 100 \sim 200$ FPGA $\rightarrow 25 \sim 50$ CN

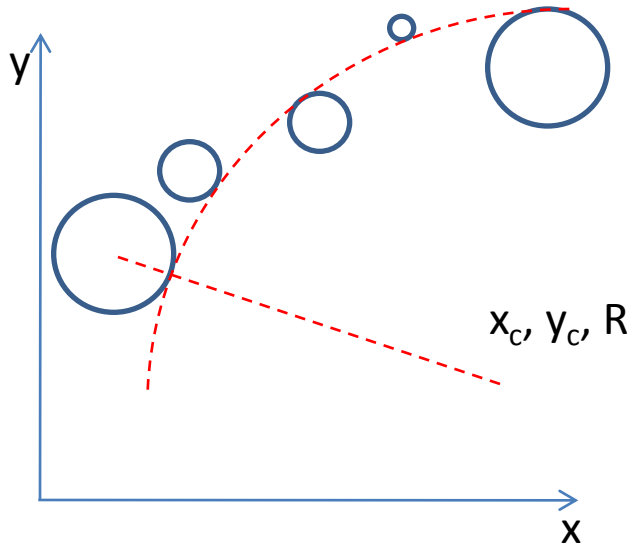
Performance study – single track



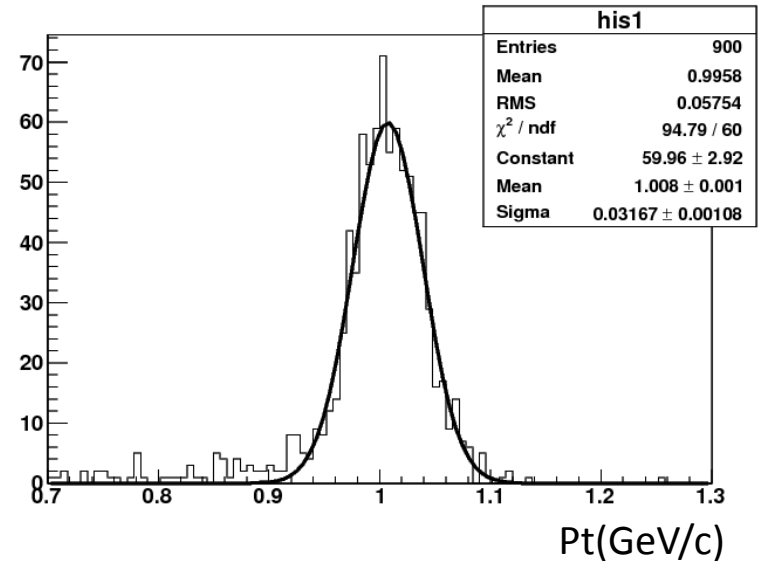
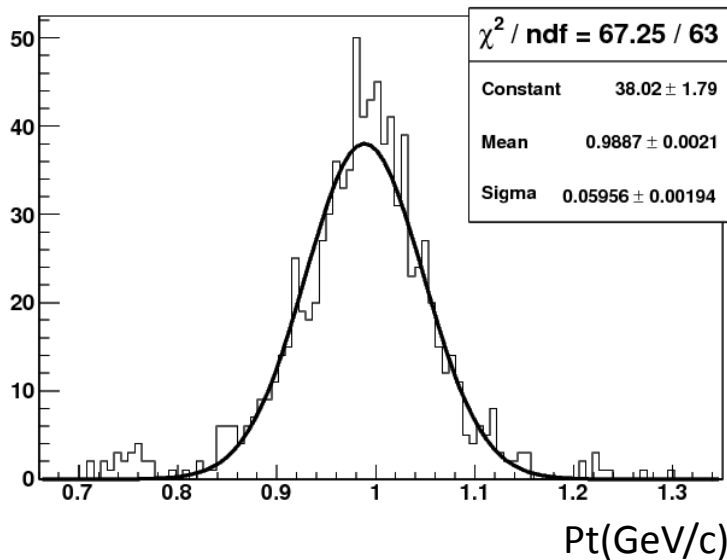
DPM background – Event # 1



To improve the momentum resolution



0.2 GeV/c :	0.195 ± 0.0068	0.195 ± 0.0068
0.5 GeV/c :	0.5 ± 0.0212	0.5 ± 0.0164
1.0 GeV/c :	0.99 ± 0.0595	1.0 ± 0.0317
2.0 GeV/c :	1.85 ± 0.213	2.0 ± 0.073



	VHDL		C++	
S_{xx}	4.26358	✓	4.26378	
S_{xy}	0.226061	✓	0.226091	
S_{yy}	0.012103	✓	0.0121131	
S_{xxx}	8.24079	✓	8.24134	event 2:
S_{xxy}	0.438052	✓	0.43809	det A: 0.00109
S_{xyy}	0.0234513	✓	0.0235531	a: 0.00741
S_{yyy}	0.00127371	✓	0.00127769	b: 0.01307
S_{xxxx}	15.953	✓	15.9542	
S_{xxxxy}	0.0456499	✓	0.0458053	
S_{xxyyy}	0.000137139	✓	0.00013764	
a	-0.00068454		-0.000776344	x 4 VHDL
b	-0.00491509		-0.00475687	-0.00273816
det A	0.000487605		0.000530637	-0.0196604
				0.00195842
$S_{xy}(S_{xyy} - S_{yyx})$	-1.87312		-1.87337	
$S_{yx}(S_{yxx} - S_{xxy})$	-1.86821		-1.86861	

$$2^{**}(-16) = 0.00001526$$