

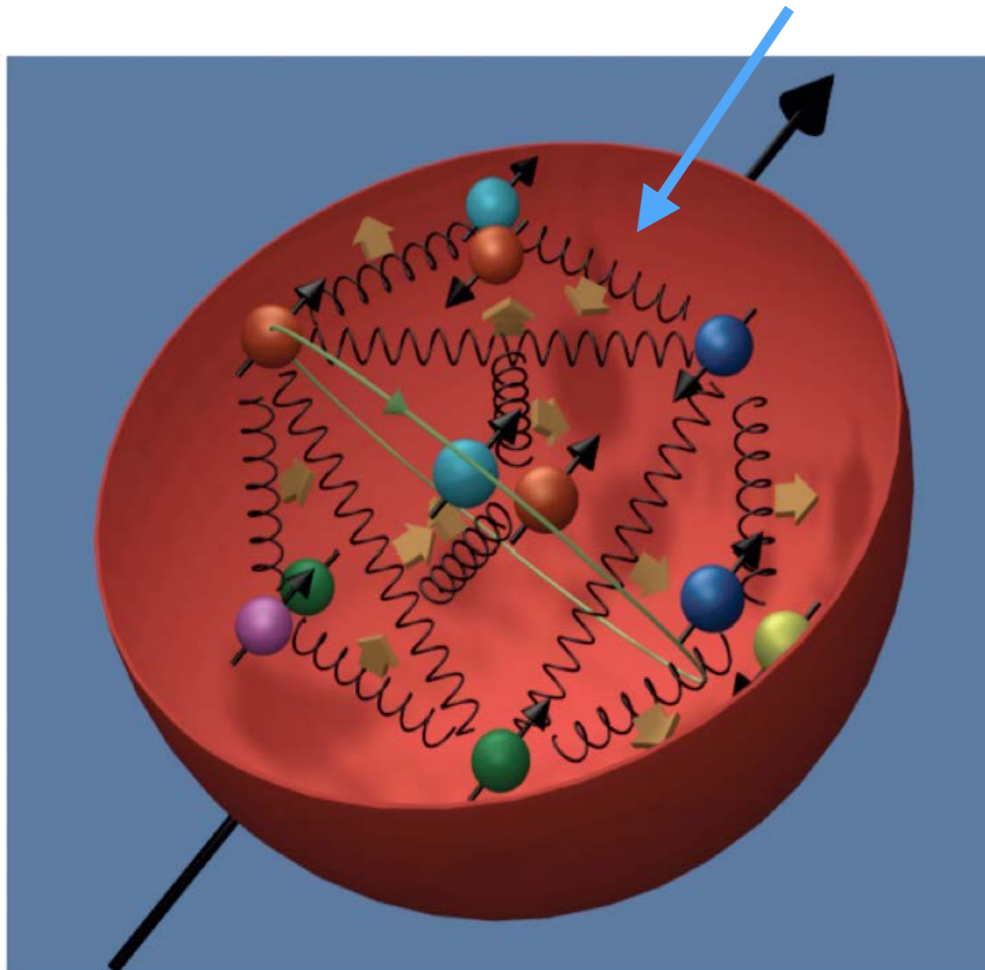
*Glueballs - at the heart of QCD  
but hard to identify*

Ulrich Wiedner  
(Ruhr-University Bochum)

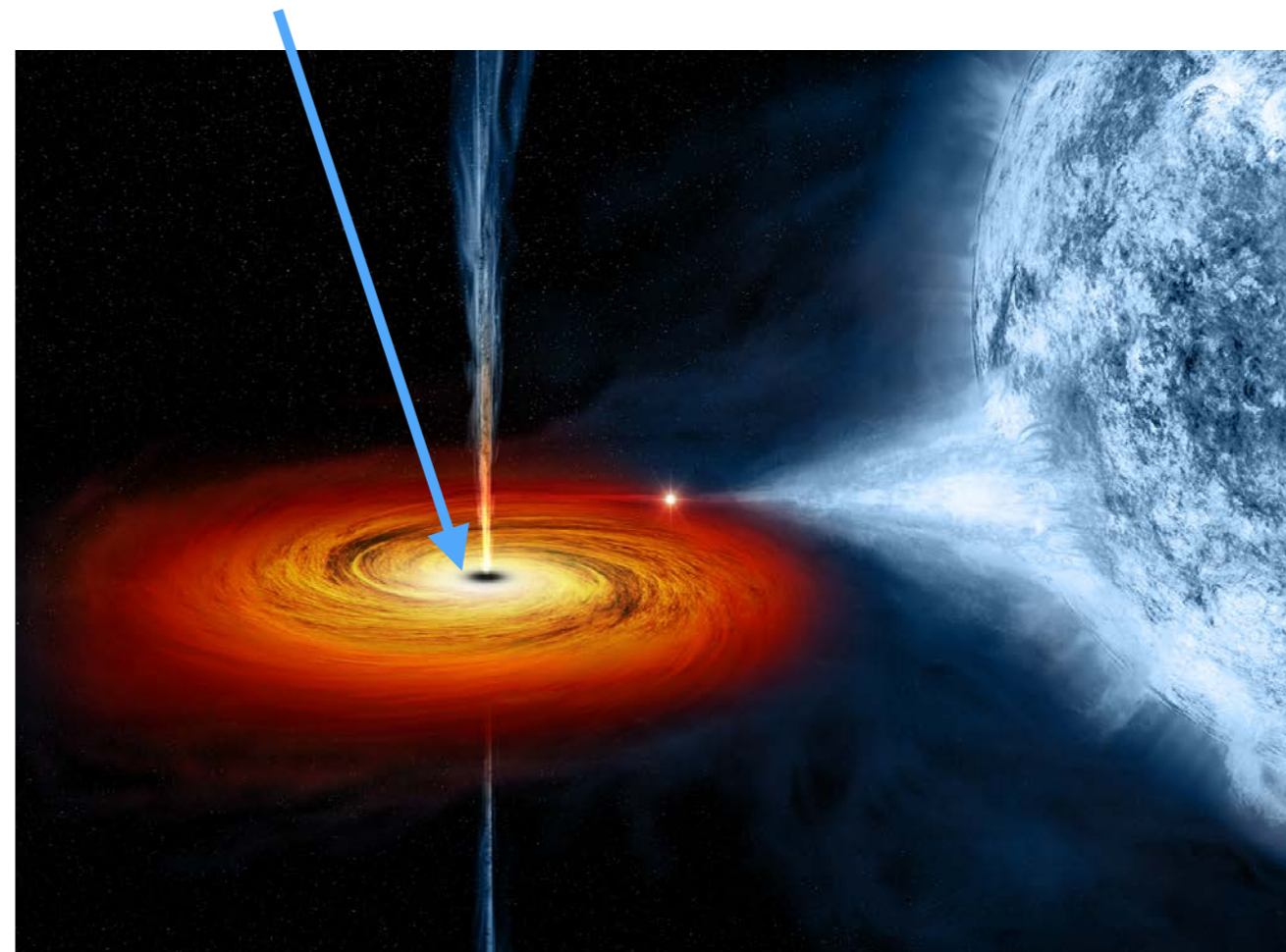
# Binding of masses of confined objects

Confining particles:

Massless gluons



Massless gravitons



*Credits: NASA/CXC/M.Weiss*

Glueballs are one of the most fascinating facets of QCD:

↳ massless gluons come together to form massive states

**Hadron physics is the place on earth to study non-Abelian massless gauge boson - gauge boson interaction in a controlled manner.**

# Feynman lectures on gravitation:

In fact, his work led to two sets of very useful results. The first, purely pedagogical, is embodied in the *Feynman Lectures on Gravitation* (publication [123]). In those lectures, Feynman develops the quantum field theory of a neutral massless spin 2 particle (the *graviton*), emphasizing the special features that arise, in comparison to theories of spin 0 and spin 1 particles, as well as the complications that result for a zero-mass particle in trying to create a self-consistent theory. As in the case of spin 1, masslessness results in redundant degrees of freedom, since Lorentz invariance requires that a *massless* particle can spin only along or opposite to its direction of momentum (positive or negative *chirality*), while a massive spin 2 particle may take up five different orientations relative to any arbitrary quantization direction. Eliminating the unwanted degrees of freedom is achieved by imposing certain “gauge conditions,” which in the gravitational case brings about nonlinearity in the form of **graviton–graviton interaction**. Feynman shows that the classical limit of a properly gauged massless spin 2 theory is described by the Einstein gravitational field equations.<sup>3</sup>

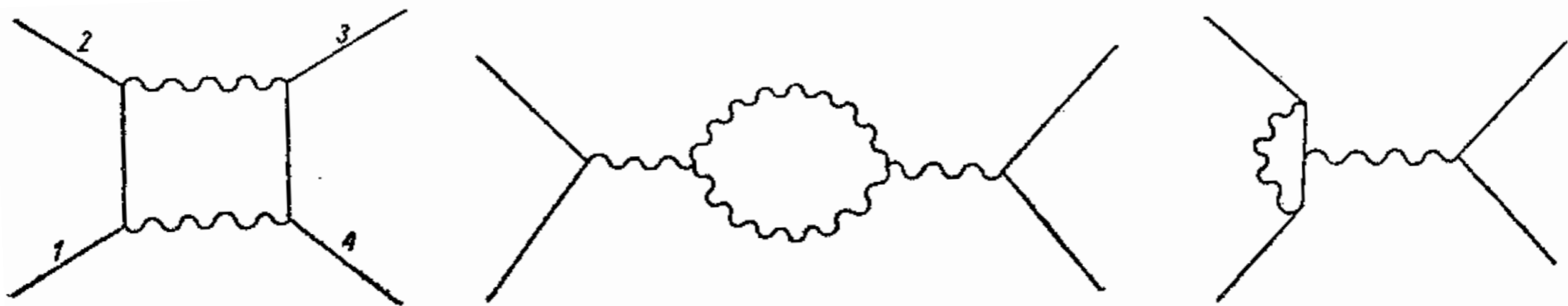


Fig. 5

# The glueball hunter's guide

*Use gluon-rich processes to form and find them*

Glueballs are super-numerous states among the nonets

↳ precise hadron spectroscopy experiments and analyses

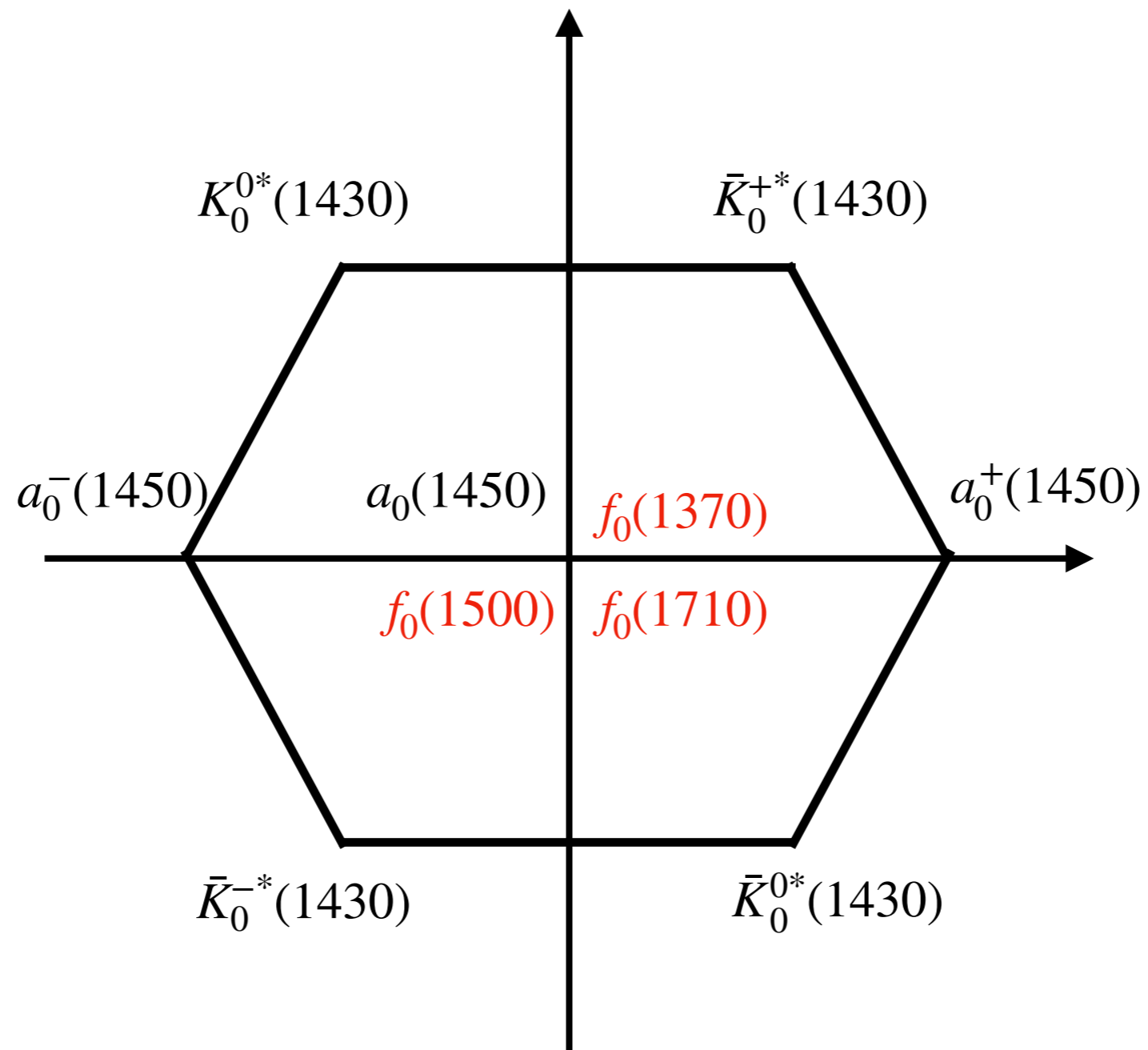
Glueballs decay flavor blind:

↳ study decay patterns to mesons with different quark-(gluon?) content

Glueballs do not couple to photons (at least in first order)

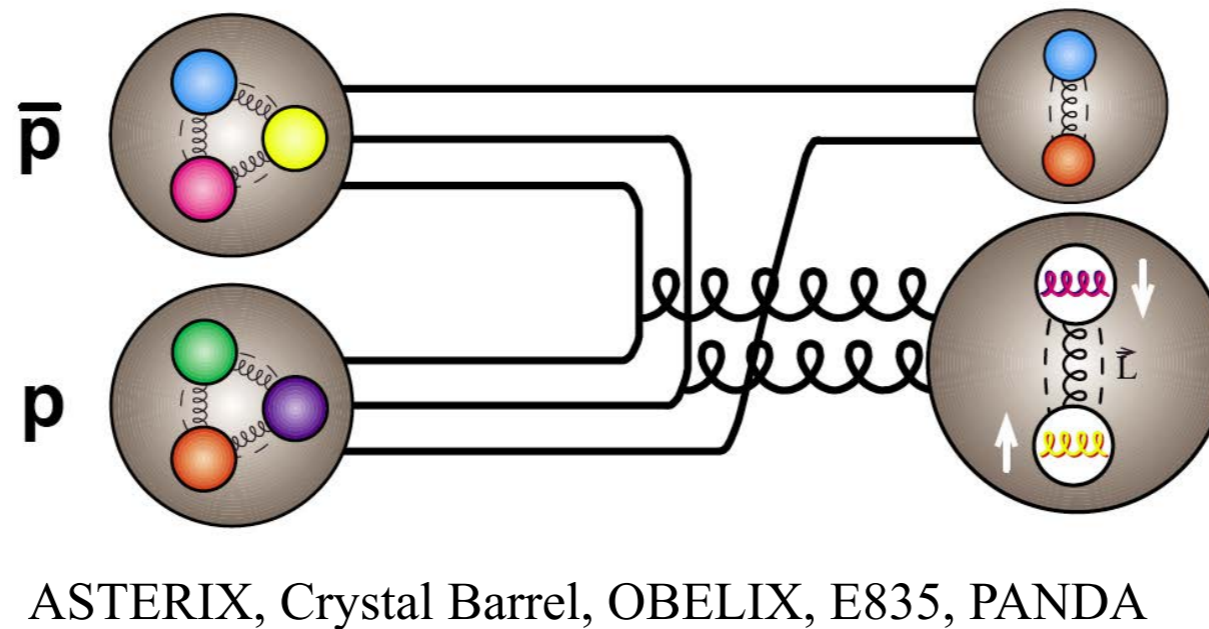
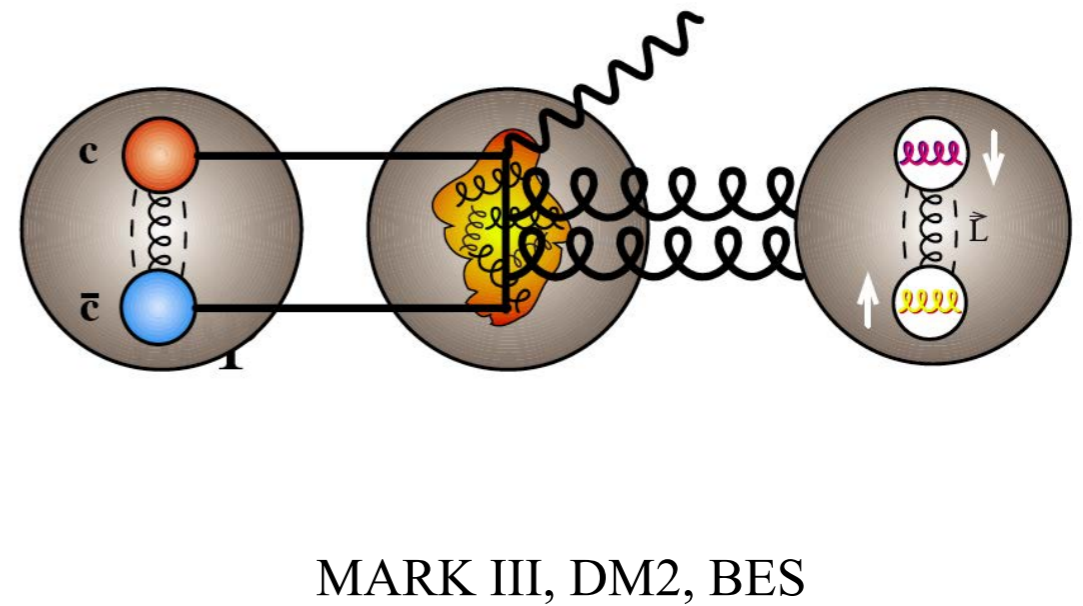
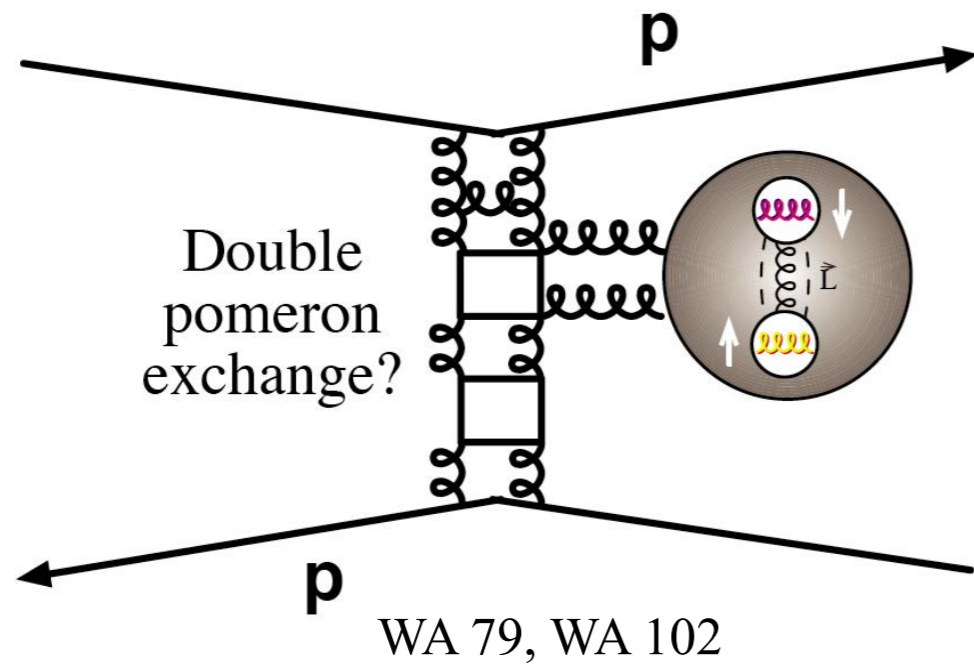
↳ use different beam particles

# The glueball ground state ( $0^{++}$ ) and the scalar nonet

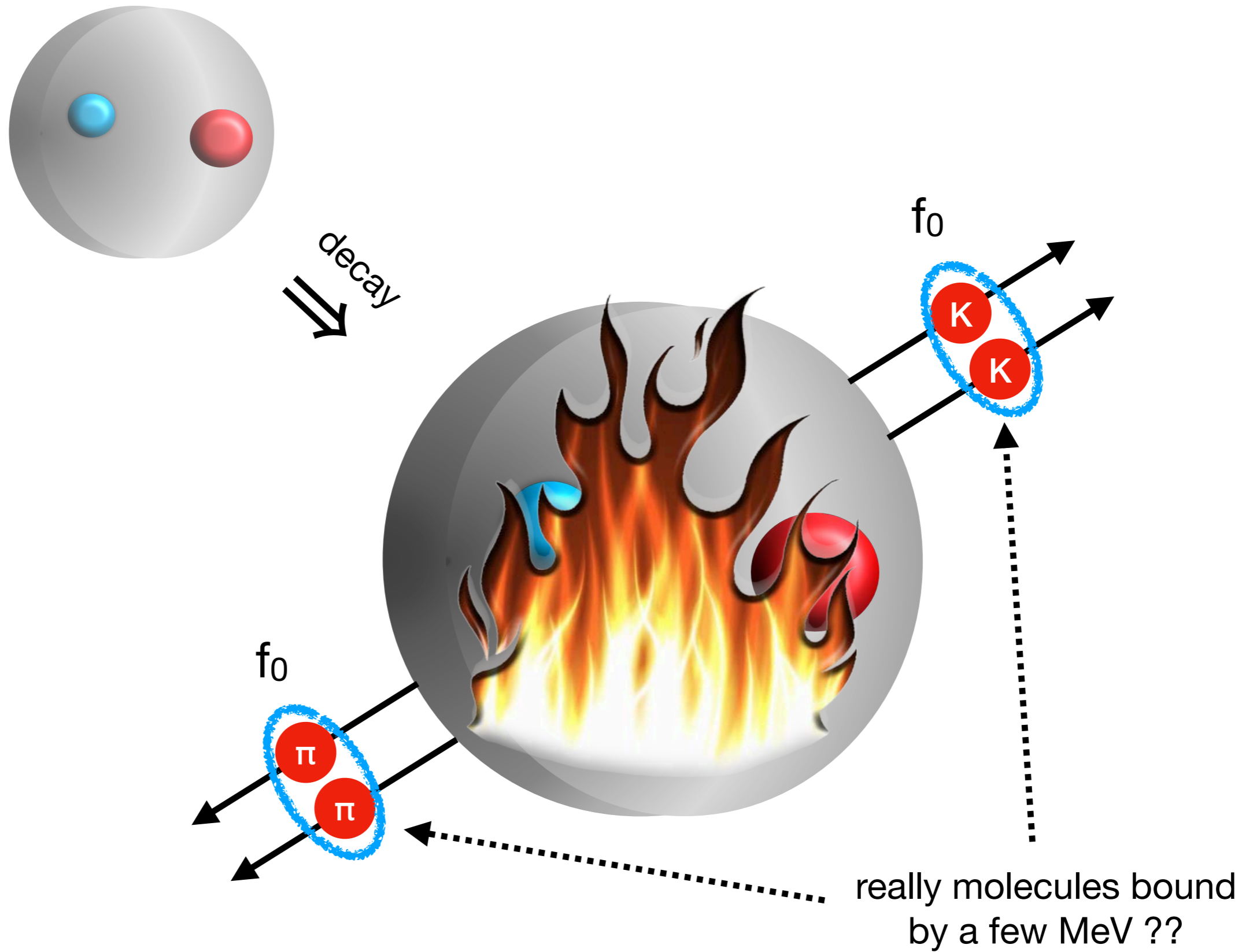


3  $f_0$  ??  $\rightarrow$  1 particle super numerous  $\Rightarrow$  glueball??

# Particle production: “gluon-rich” processes



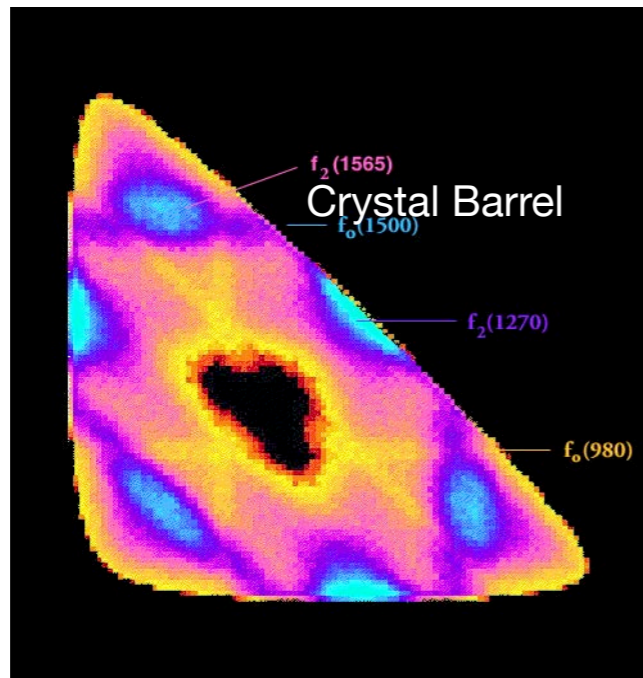
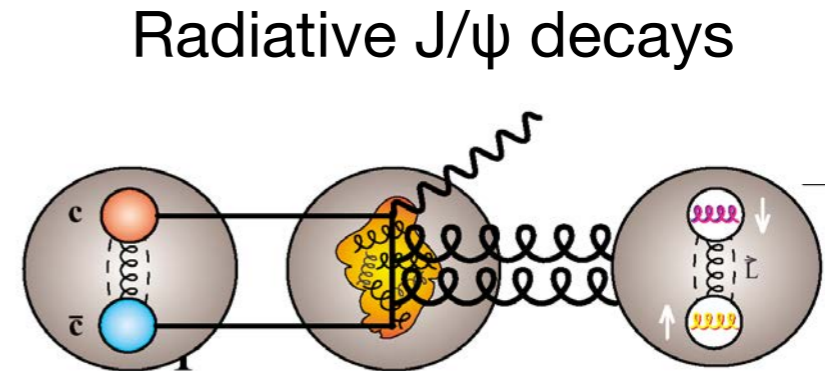
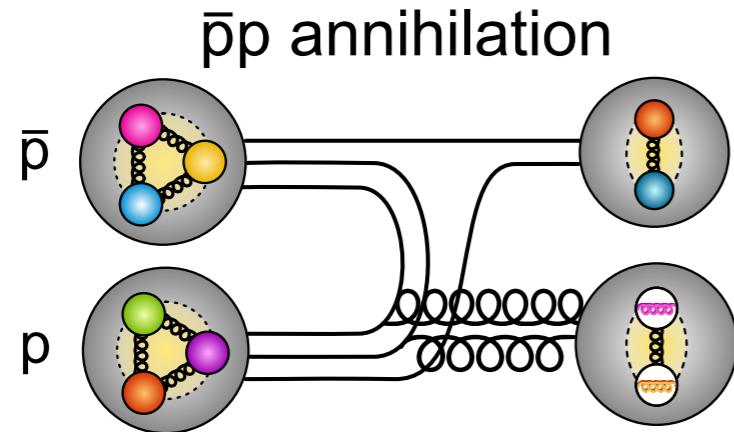
# Charmonium decays



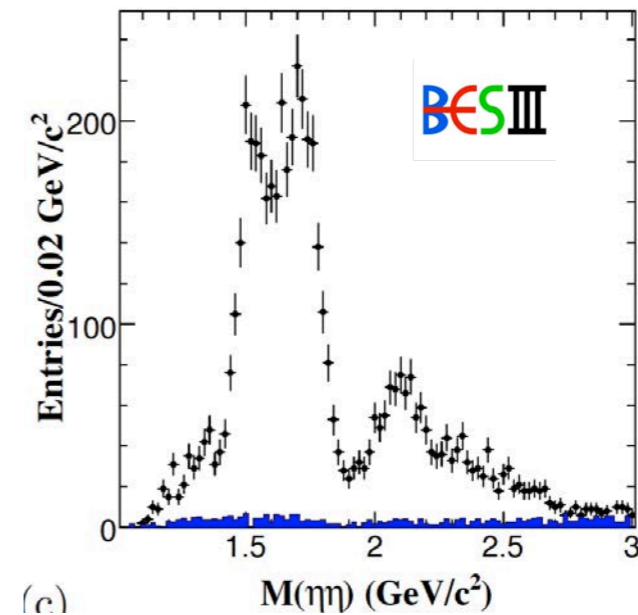
# Glueball searches in gluon-rich reactions

Massless gluons come together to form massive states.

Many candidates are proposed and observed in gluon-rich processes:



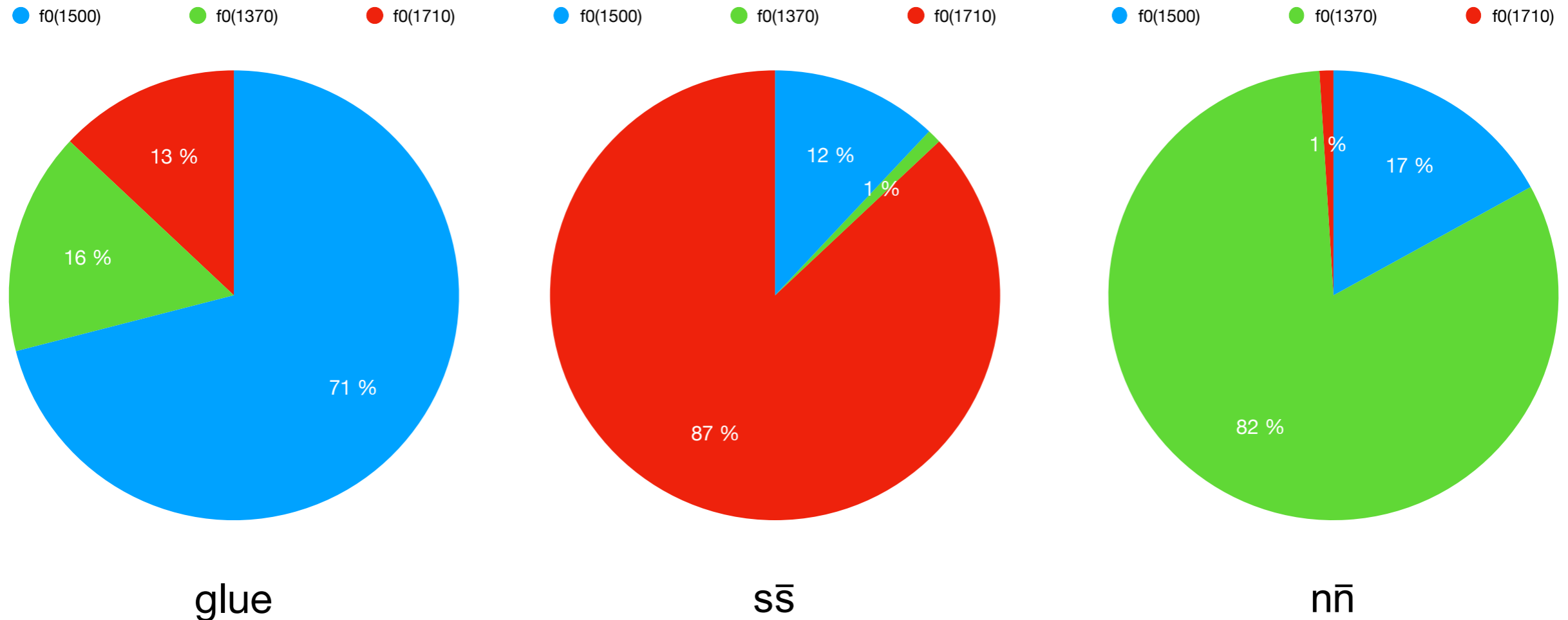
$f_0(1500)$  and  $f_0(1710)$



Primitive glueball decays to mesons:  $\pi\pi : \eta\eta : \eta\eta' : KK = 3 : 1 : 0 : 4$

# The mixing of states

Problem: Overlapping states with the same quantum numbers  $q\bar{q}$  or  $gg$  can mix.

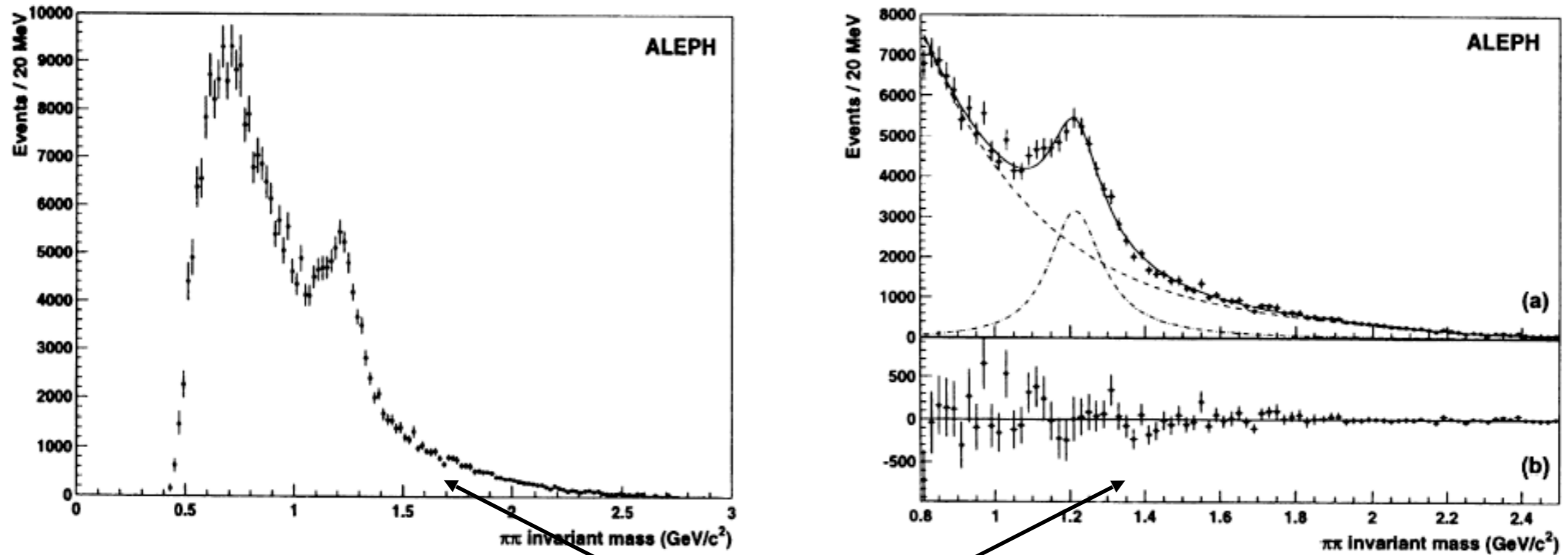


Different mixing schemes exist.

ISSN 0075-8450 ISSN 1616-6361 (electronic)  
Lecture Notes in Physics  
ISBN 978-3-319-98526-8 ISBN 978-3-319-98527-5 (eBook)  
<https://doi.org/10.1007/978-3-319-98527-5>

# $\gamma\gamma$ collisions from ALEPH

(anti-glueball filter)



no  $f_0(1500)$

upper limit:

$$\Gamma(\gamma\gamma \rightarrow f_0(1500)) \cdot BR(f_0(1500) \rightarrow \pi^+\pi^-) < 0.31 \text{ keV}$$

Phys. Lett. B472 (2000) 189.

# Lots of information in the PDG (2025)

$f_0(1500)$   $I^G(J^{PC}) = 0^+(0^{++})$

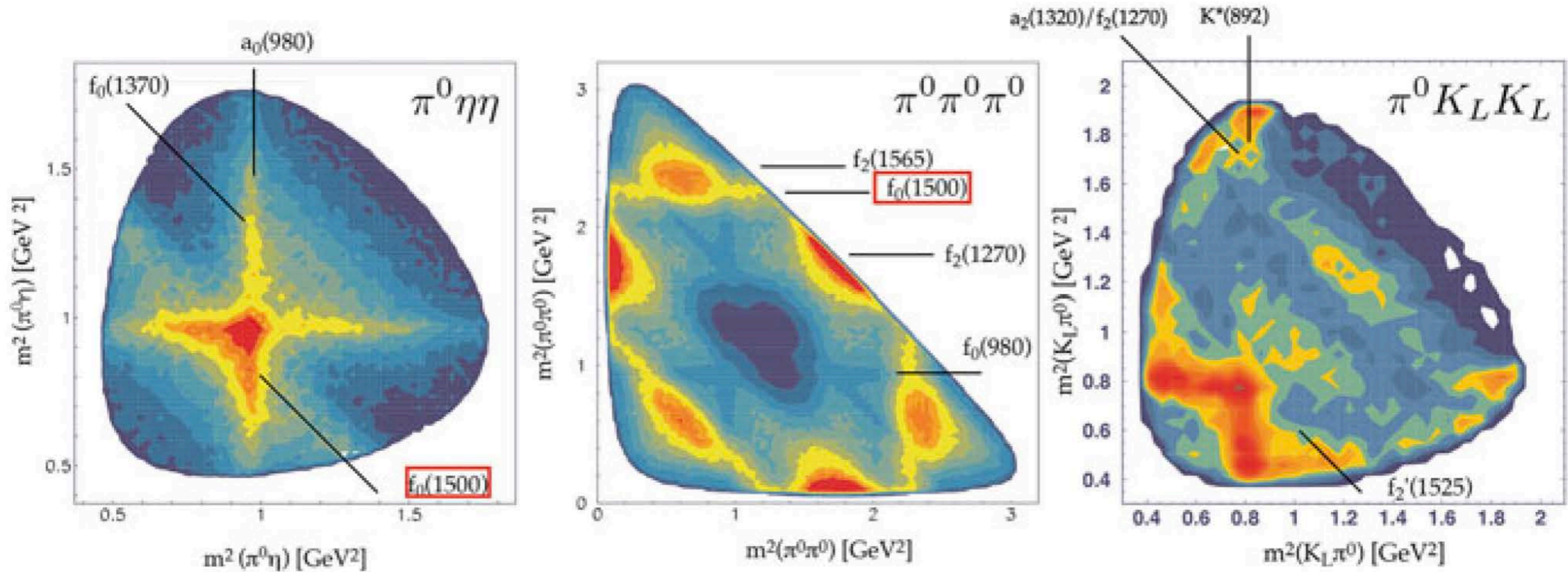
See the review on "Spectroscopy of Light Meson Resonances."

$f_0(1500)$ T-MATRIX POLE $\sqrt{s}$	$(1430 - 1530) - i(40 - 90)$ MeV	▼
$f_0(1500)$ MASS	$1522 \pm 25$ MeV	▼
$f_0(1500)$ WIDTH	$108 \pm 33$ MeV	▼

## $f_0(1500)$ DECAY MODES

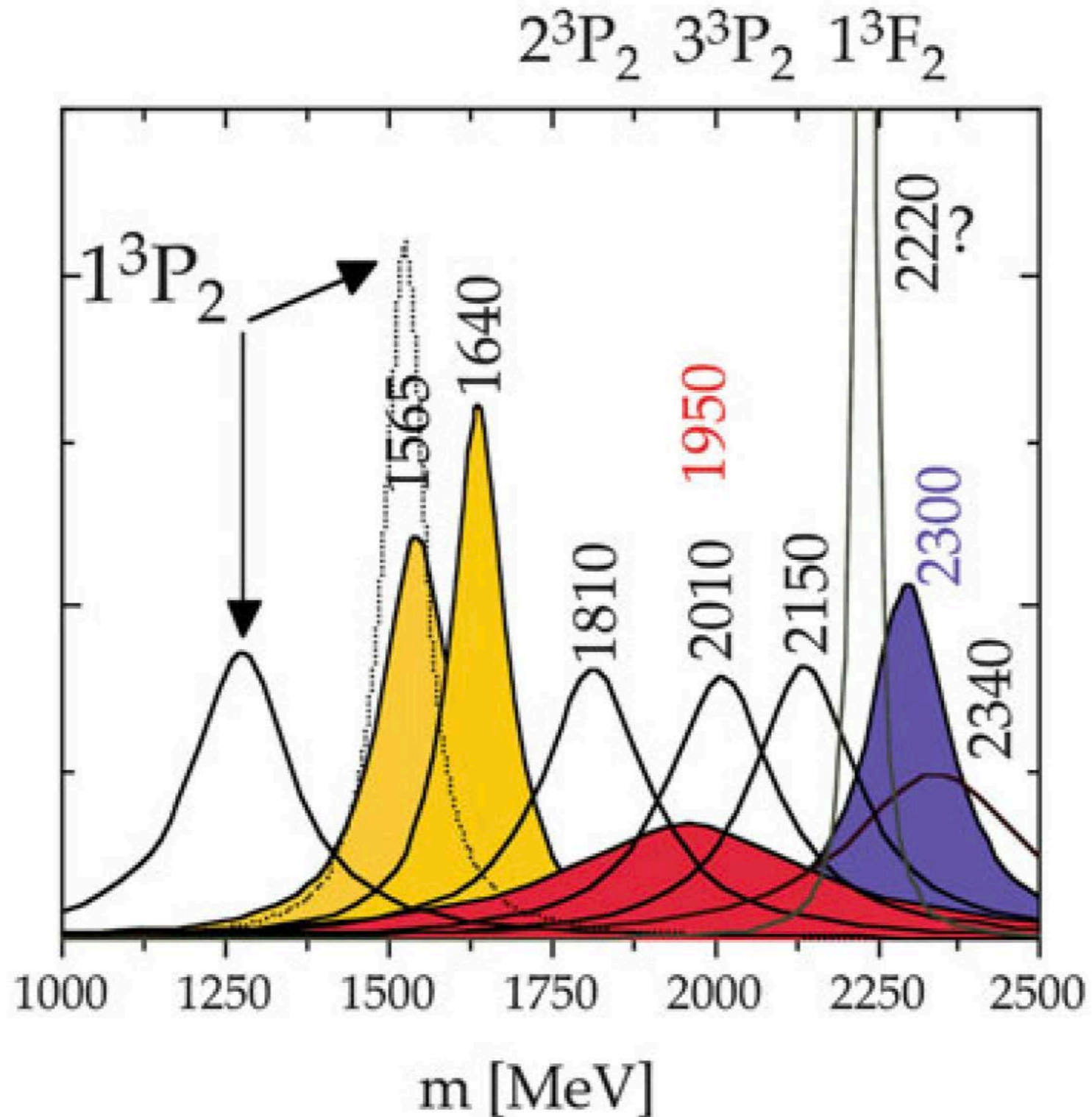
Mode	Fraction ( $\Gamma_i / \Gamma$ )	Scale Factor/ Conf. Level	P(MeV/c)	
$\Gamma_1$ $\pi\pi$	$(34.5 \pm 2.2)$ %	S=1.2	749	▼
$\Gamma_2$ $\pi^+\pi^-$	seen		748	▼
$\Gamma_3$ $2\pi^0$	seen		749	▼
$\Gamma_4$ $4\pi$	$(48.9 \pm 3.3)$ %	S=1.2	700	▼
$\Gamma_5$ $4\pi^0$	seen		700	▼
$\Gamma_6$ $2\pi^+2\pi^-$	seen		696	▼
$\Gamma_7$ $2(\pi\pi)_{S\text{-wave}}$	seen			▼
$\Gamma_8$ $\rho\rho$	seen		-1	▼
$\Gamma_9$ $\pi(1300)\pi$	seen		163	▼
$\Gamma_{10}$ $a_1(1260)\pi$	seen		234	▼
$\Gamma_{11}$ $\eta\eta$	$(6.0 \pm 0.9)$ %	S=1.1	528	▼
$\Gamma_{12}$ $\eta\eta'(958)$	$(2.2 \pm 0.8)$ %	S=1.4	107	▼
$\Gamma_{13}$ $K\bar{K}$	$(8.5 \pm 1.0)$ %	S=1.1	579	▼
$\Gamma_{14}$ $\gamma\gamma$	not seen		761	▼

# Data: $p\bar{p}$ Dalitz plots



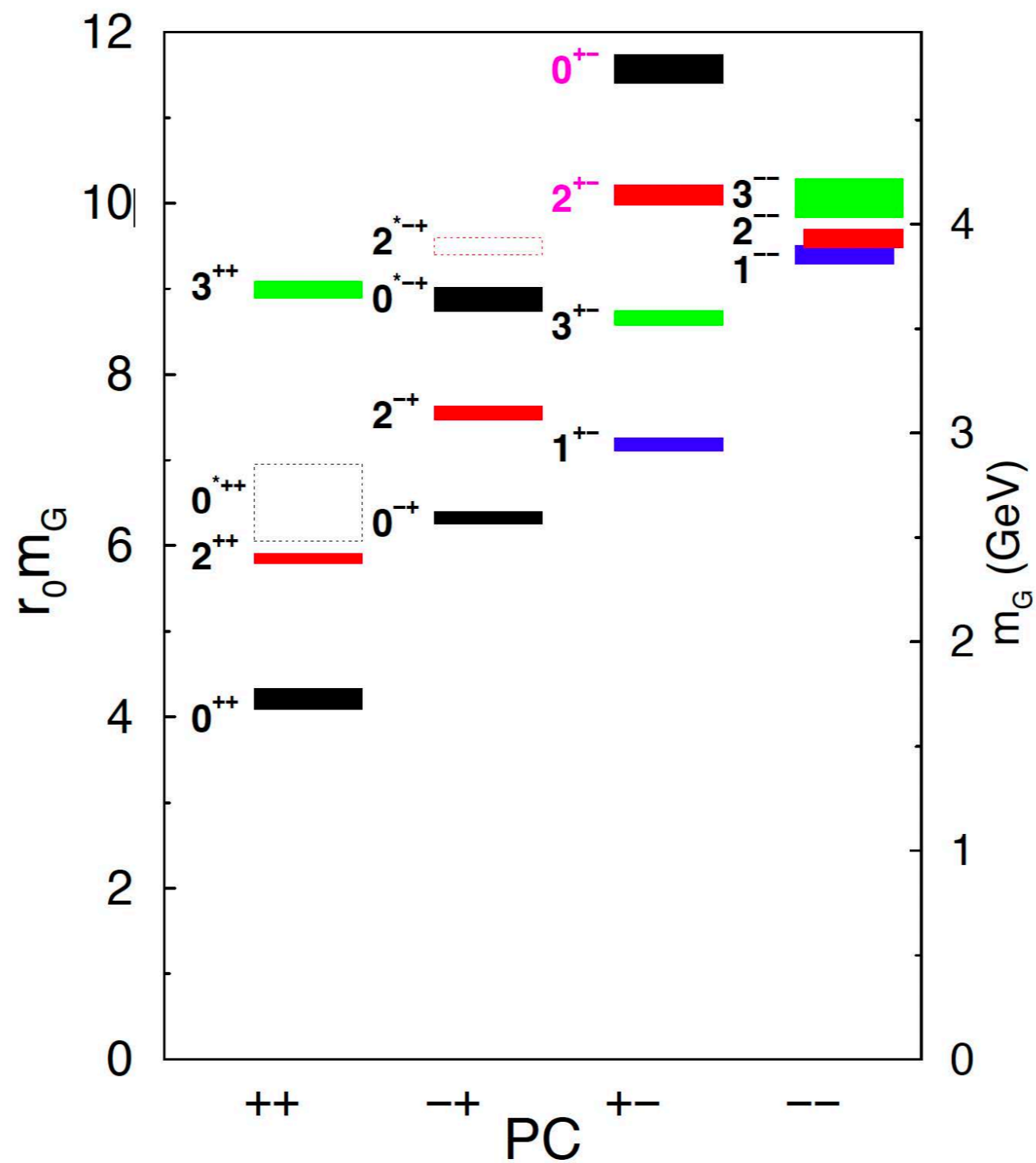
Amsler, C.: Rev. Mod. Phys. 70, 1293 (1998)

# The tensor ( $J^{PC} = 2^{++}$ ) particles



Taken from Claude Amsler: Lecture Notes in Physics  
ISBN 978-3-319-98526-8 ISBN 978-3-319-98527-5 (eBook)

# The lattice glueball spectrum



# Towards the glueball spectrum from unquenched lattice QCD

E. Gregory, A. Irving, B. Lucini, C. McNeile, A. Rago, C. Richards, E. Rinaldi, JHEP10 (2012) 170, arXiv:1208.1858 [hep-lat]

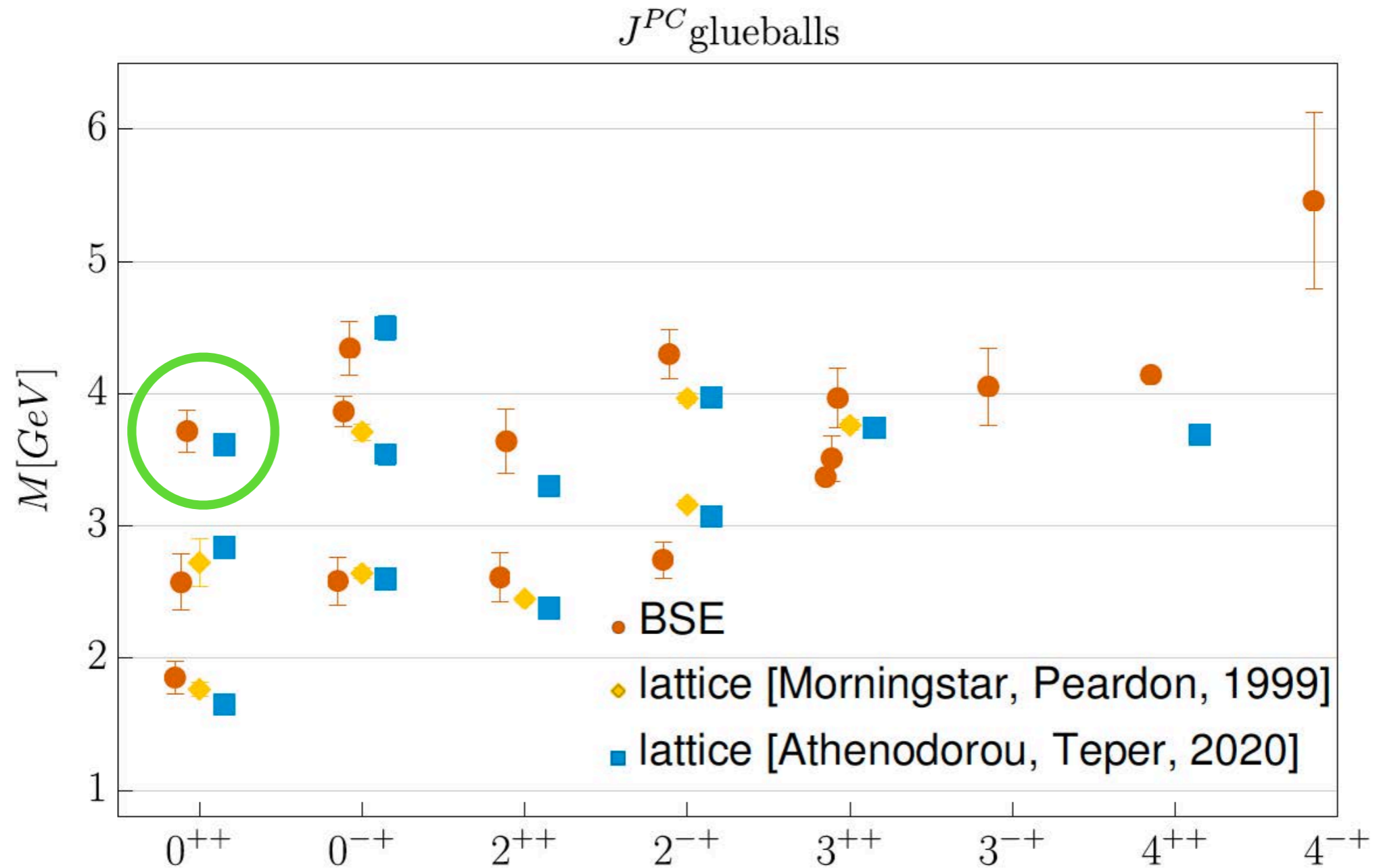
$J^{PC}$	Mass MeV			
	Unquenched This work	Quenched		
		M&P	Ky	Meyer
$0^{-+}$		2590(40)(130)	2560(35)(120)	2250(60)(100)
$2^{-+}$	3460(320)	3100(30)(150)	3040(40)(150)	2780(50)(130)
$0^{-+}$	4490(590)	3640(60)(180)		3370(150)(150)
$2^{-+}$				3480(140)(160)
$5^{-+}$				3942(160)(180)
$0^{--}$ (exotic)	5166(1000)			
$1^{--}$		3850(50)(190)	3830(40)(190)	3240(330)(150)
$2^{--}$	4590(740)	3930(40)(190)	4010(45)(200)	3660(130)(170)
$2^{--}$				3.740(200)(170)
$3^{--}$		4130(90)(200)	4200(45)(200)	4330(260)(200)
$1^{+-}$	3270(340)	2940(30)(140)	2980(30)(140)	2670(65)(120)
$3^{+-}$	3850(350)	3550(40)(170)	3600(40)(170)	3270(90)(150)
$3^{+-}$				3630(140)(160)
$2^{+-}$ (exotic)		4140(50)(200)	4230(50)(200)	
$0^{+-}$ (exotic)	5450(830)	4740(70)(230)	4780(60)(230)	
$5^{+-}$				4110(170)(190)
$0^{++}$	1795(60)	1730(50)(80)	1710(50)(80)	1475(30)(65)
$2^{++}$	2620(50)	2400(25)(120)	2390(30)(120)	2150(30)(100)
$0^{++}$	3760(240)	2670(180)(130)		2755(30)(120)
$3^{++}$		3690(40)(180)	3670(50)(180)	3385(90)(150)
$0^{++}$				3370(100)(150)
$0^{++}$				3990(210)(180)
$2^{++}$				2880(100)(130)
$4^{++}$				3640(90)(160)
$6^{++}$				4360(260)(200)

M&P: C. J. Morningstar and M. J. Peardon, The glueball spectrum from an anisotropic lattice study, Phys. Rev. D60 (1999) 034509, [hep-lat/9901004].

Ky: Y. Chen et al., Glueball spectrum and matrix elements on anisotropic lattices, Phys. Rev. D73 (2006) 014516, [hep-lat/0510074].

H. B. Meyer, Glueball Regge trajectories, hep-lat/0508002. Ph.D. Thesis.

# Glueballs from functional methods



M.Q.Huber, Fischer, Sanchis Alepuz, Eur.Phys.J.C 85, 2503.03821 (2025)

# New approach on scalar glueballs

Look for the excited  $0^{++}$  glueball among the charmonium states.

## Hunting for glueballs in electron-positron annihilation

Stanley J. Brodsky,<sup>2,4</sup> Alfred Scharff Goldhaber,<sup>3,4,5</sup> and Jungil Lee<sup>1,2</sup>

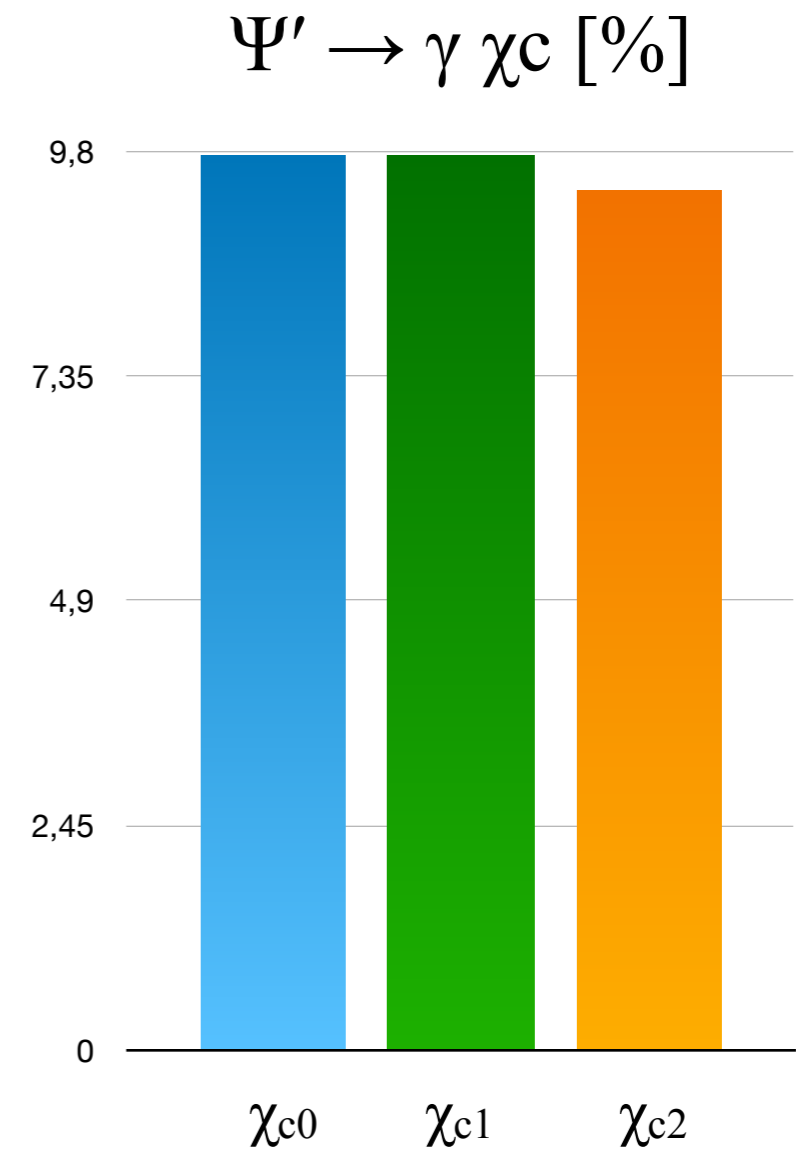
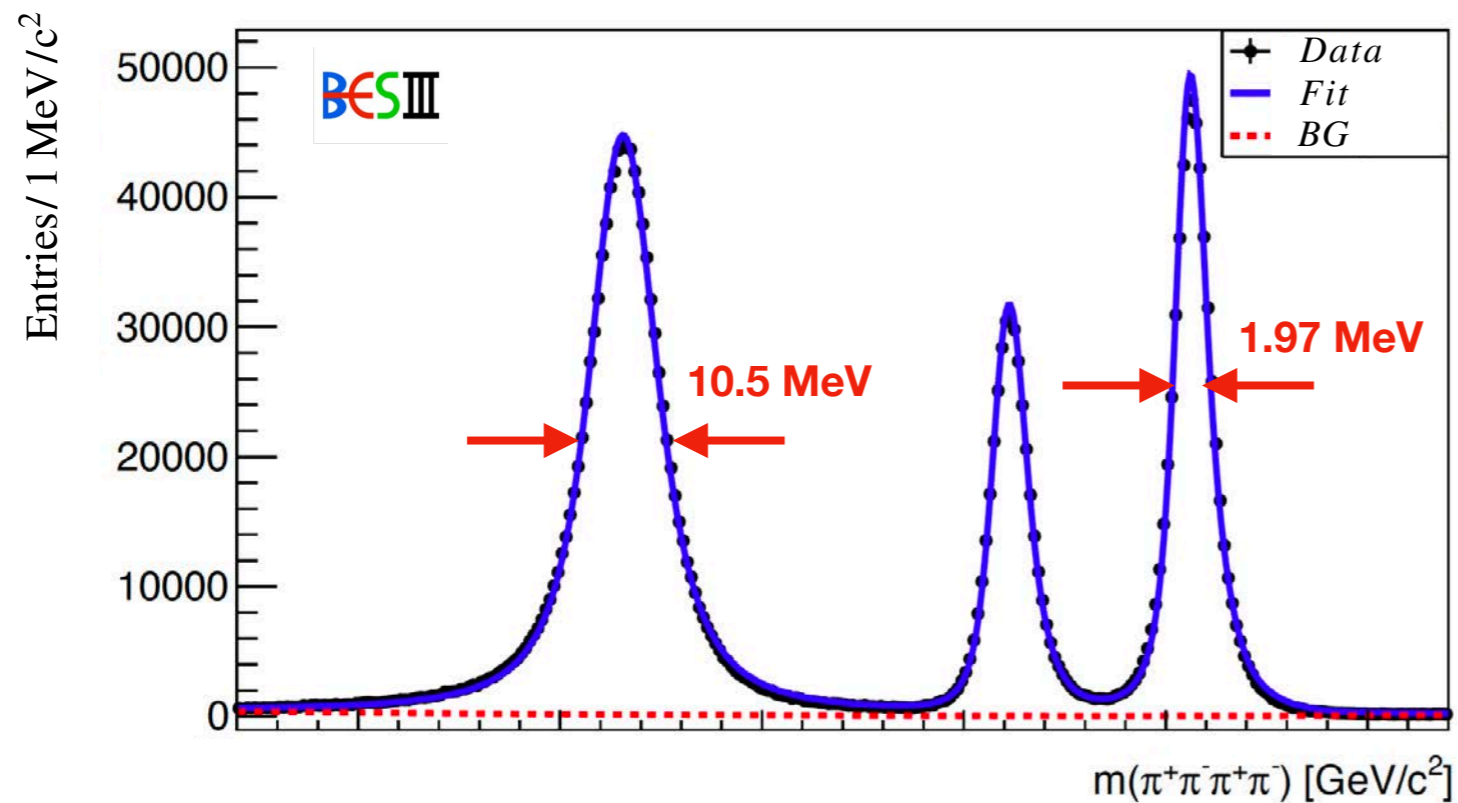
hep-ph/0305269  
ANL-HEP-PR-03-024  
JLAB-THY-03-33  
MIT-CTP 3380  
SLAC-PUB-9861  
YITP-SB-03-23

We calculate the cross section for the exclusive production of  $J^{PC} = 0^{++}$  glueballs  $\mathcal{G}_0$  in association with the  $J/\psi$  in  $e^+e^-$  annihilation using the pQCD factorization formalism. The required long-distance matrix element for the glueball is bounded by CUSB data from a search for resonances in radiative  $\Upsilon$  decay. The cross section for  $e^+e^- \rightarrow J/\psi + \mathcal{G}_0$  at  $\sqrt{s} = 10.6$  GeV is similar to exclusive charmonium-pair production  $e^+e^- \rightarrow J/\psi + h$  for  $h = \eta_c$  and  $\chi_{c0}$ , and is larger by a factor 2 than that for  $h = \eta_c(2S)$ . As the subprocesses  $\gamma^* \rightarrow (c\bar{c})(c\bar{c})$  and  $\gamma^* \rightarrow (c\bar{c})(gg)$  are of the same nominal order in perturbative QCD, it is possible that some portion of the anomalously large signal observed by Belle in  $e^+e^- \rightarrow J/\psi X$  may actually be due to the production of charmonium-glueball  $J/\psi\mathcal{G}_J$  pairs.

$M_{\mathcal{G}_0} = M_h$	$h = \eta_c$	$\chi_{c0}$	$\eta_c(2S)$
$ I_0 _{\max}^2 (10^{-3} \text{ GeV}^2)$	5.2	5.8	6.2
$\sigma_{J/\psi\mathcal{G}_0}^{\max}$	1.4 fb	1.5 fb	1.6 fb
$\sigma_{J/\psi\mathcal{G}_0}^{\max} / \sigma_{J/\psi h}$	0.63	0.72	1.9

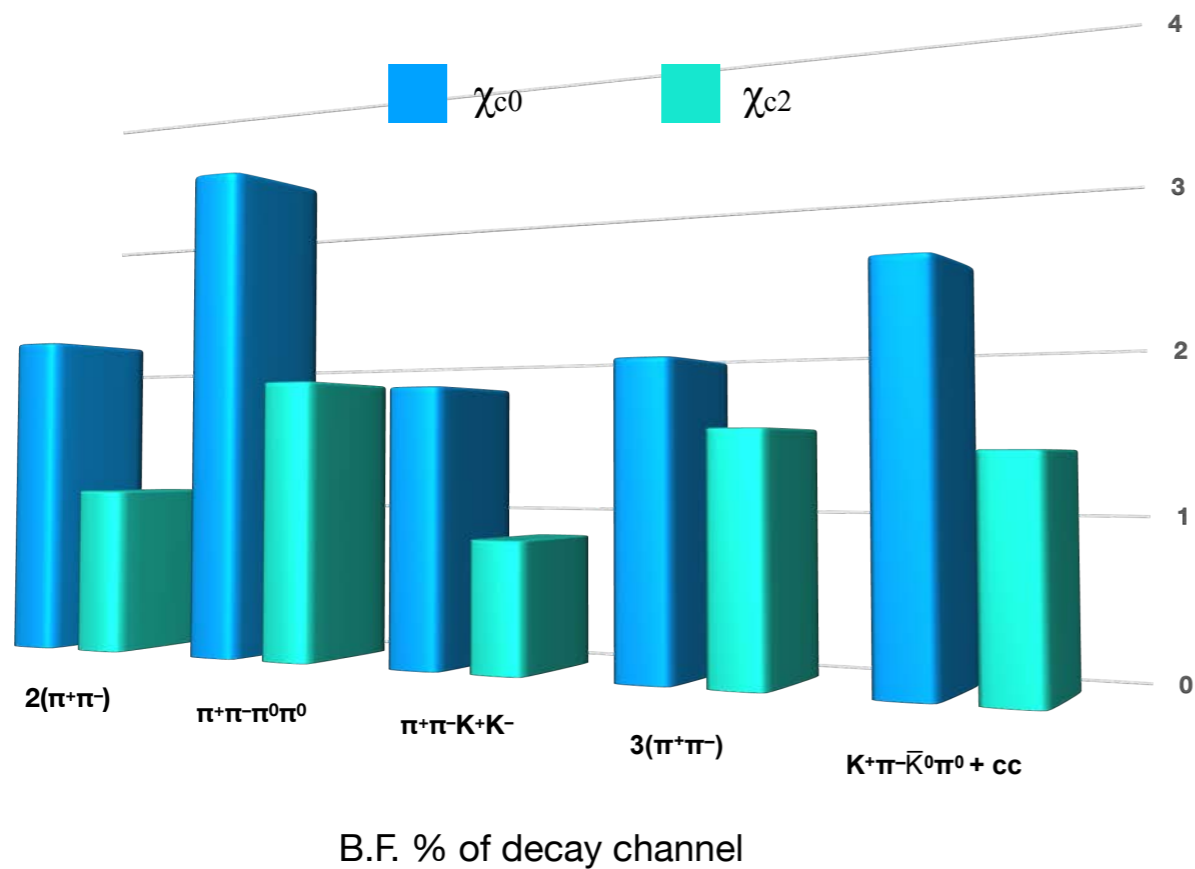
$\Rightarrow$  Study  $\chi_{c0}$  decays (admixture of glueball component)

# The $\chi_{cJ}$ states in radiative $\psi(2S)$ BESIII data

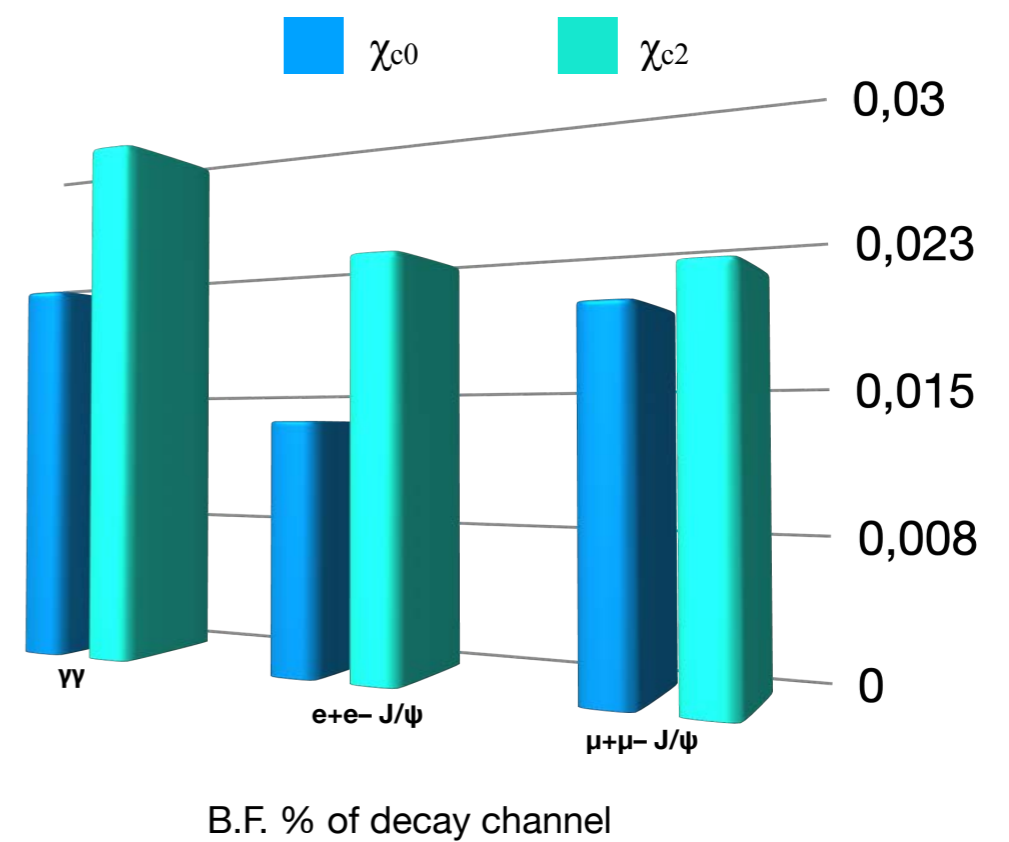


# Decay B.F. of $\chi_{cJ}$ states

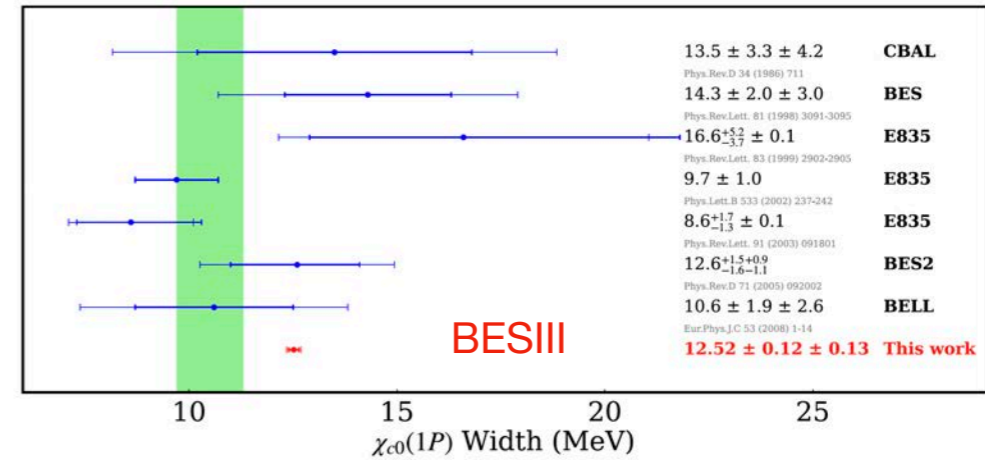
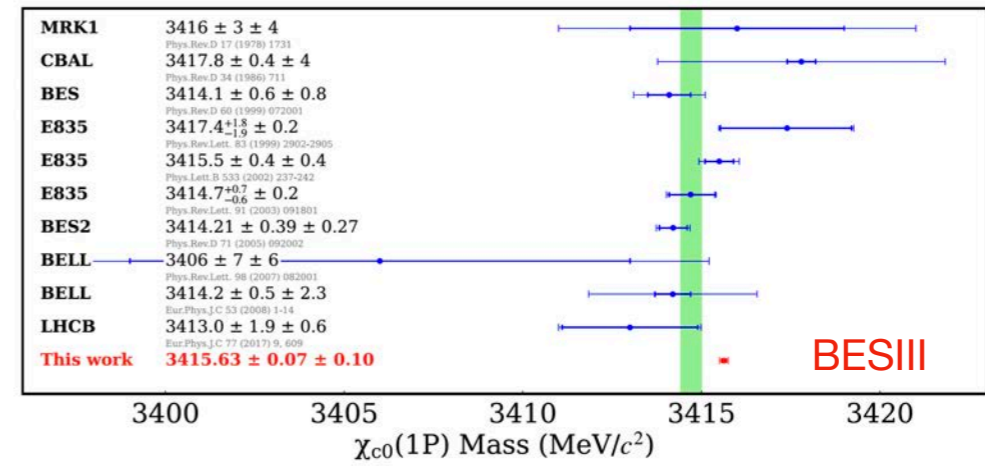
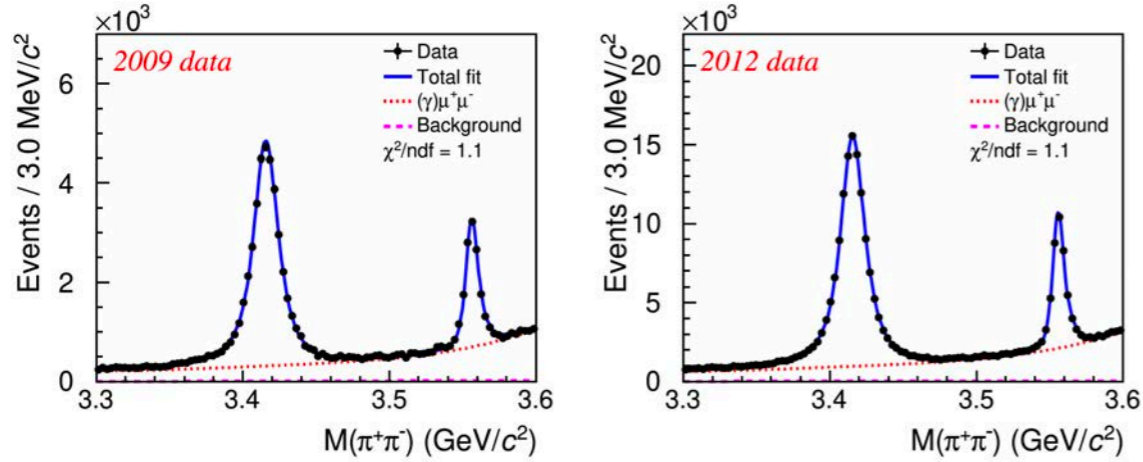
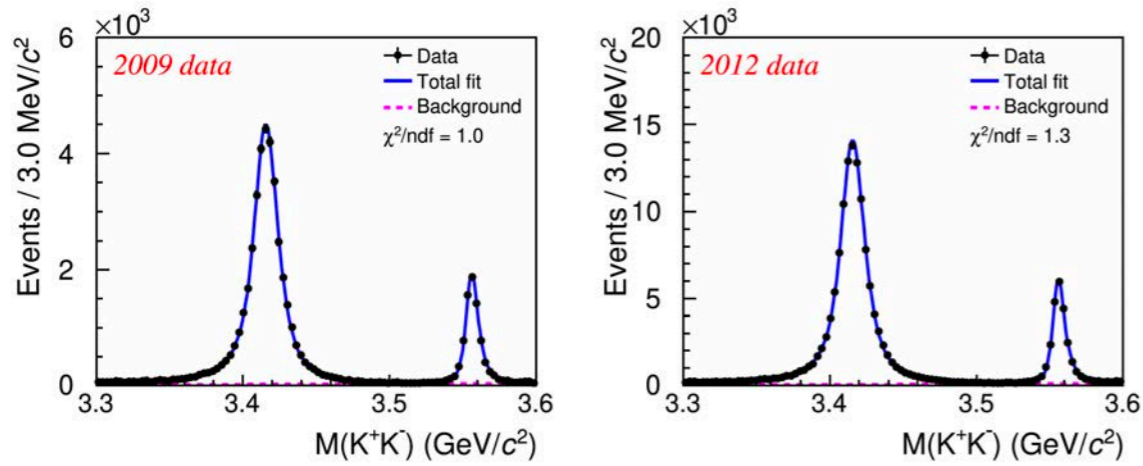
Most prominent hadronic decays of  $\chi_{c0}$  and  $\chi_{c2}$



Electroweak decays of  $\chi_{c0}$  and  $\chi_{c2}$



# Precision charmonium physics and decay B.F. of $\chi_{cJ}$ states



$$\mathcal{B}(\chi_{c0} \rightarrow K^+ K^-) = (6.36 \pm 0.02 \pm 0.08 \pm 0.13) \times 10^{-3}$$

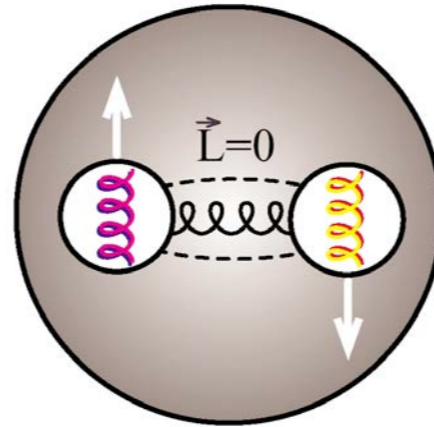
$$\mathcal{B}(\chi_{c0} \rightarrow \pi^+ \pi^-) = (6.06 \pm 0.02 \pm 0.07 \pm 0.13) \times 10^{-3}$$

$$\mathcal{B}(\chi_{c2} \rightarrow K^+ K^-) = (1.22 \pm 0.01 \pm 0.02 \pm 0.03) \times 10^{-3}$$

$$\mathcal{B}(\chi_{c2} \rightarrow \pi^+ \pi^-) = (1.61 \pm 0.01 \pm 0.02 \pm 0.04) \times 10^{-3}$$

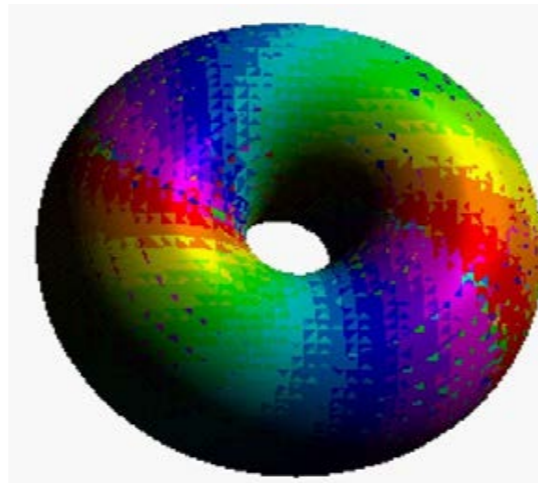
<https://arxiv.org/abs/2502.08929>

# The structure of glueballs



Glueball (gg)

Are glueballs configurations of twisted or knotted colored flux?

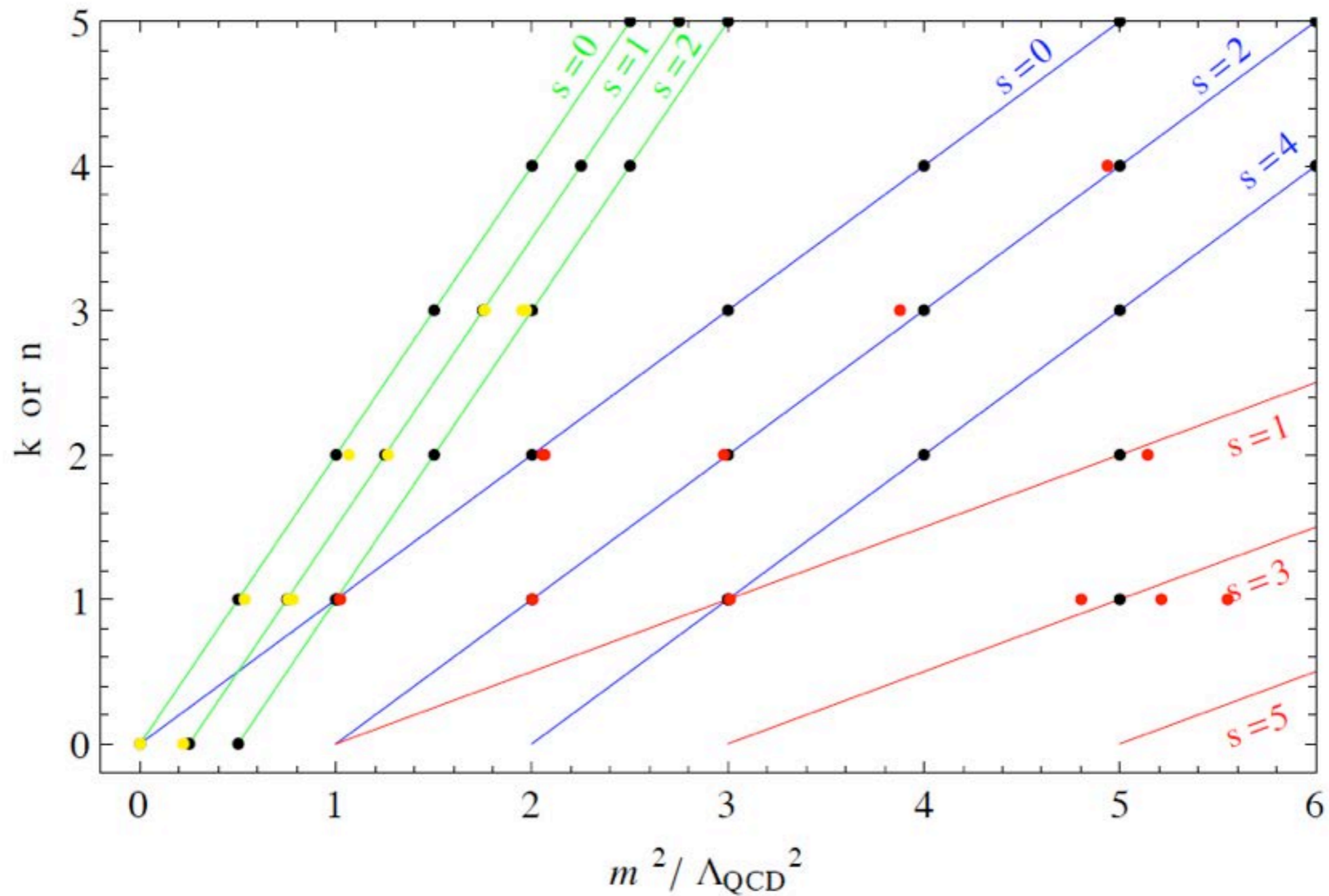


GLUEBALLS, FLUXTUBES AND  $\eta(1440)$ .

L. Fadeev, A. Niemi and U. Wiedner

Phys.Rev.D70:114033, 2004

# Glueballs on Regge trajectories like mesons?

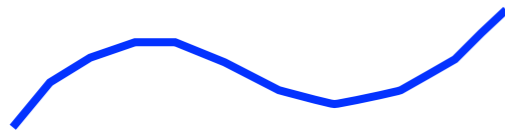


Marco Bochicchio; arXiv:1308.2925

Harvey B. Meyer, Michael J. Teper; Phys.Lett. B605 (2005) 344-354

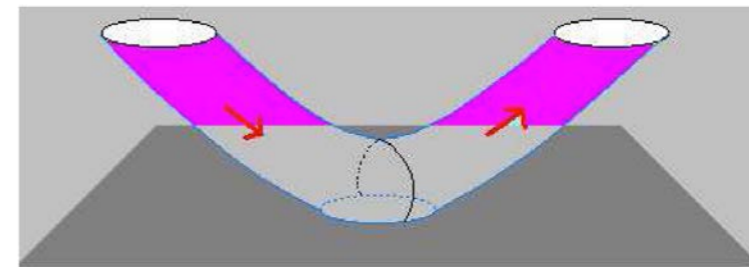
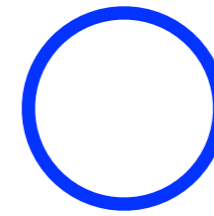
G. S. Bali et al.; arXiv:1302.1502; PoS ConfinementX (2012) 278

# Open Strings



representing gauge theories

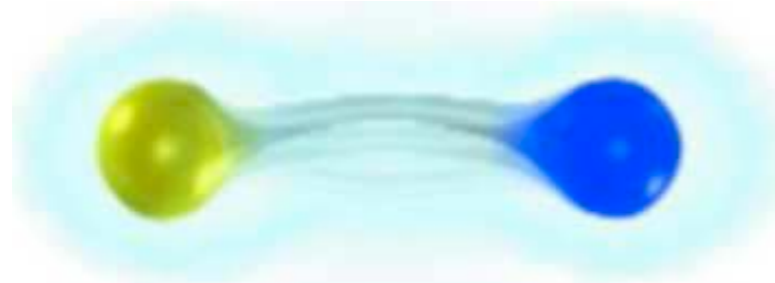
# Closed Strings



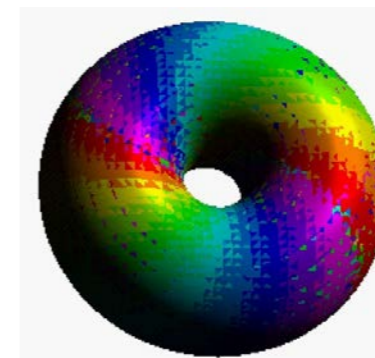
representing gravitation

# String World

# Hadron World



meson



glueball ?

# String theory adds new component through ADS/CFT

## Glueball Mass Spectrum from Supergravity\*

LBNL-42987  
UCB-PTH-99/08  
hep-th/9903142

Csaba Csáki<sup>†</sup> and John Terning

*Theoretical Physics Group*

*Ernest Orlando Lawrence Berkeley National Laboratory*

*University of California, Berkeley, CA 94720*

and

*Department of Physics*

*University of California, Berkeley, CA 94720*

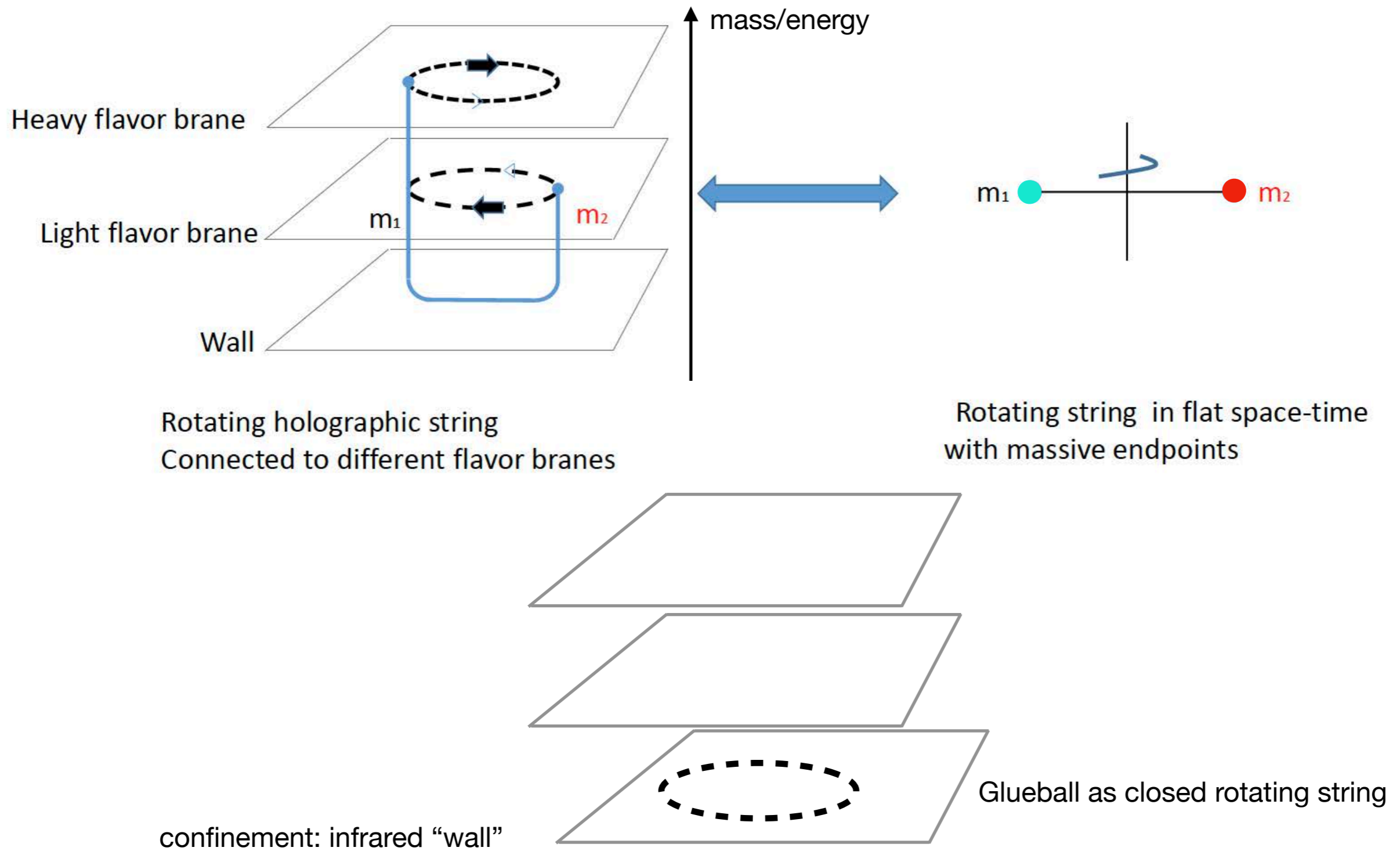
see also: JHEP 9901:017,1999

...

TABLE III. Masses of the first few  $0^{++}$  glueballs in  $\text{QCD}_4$ , in GeV, from supergravity compared to the available lattice results. The first column gives the lattice result [7,16,17], the second the supergravity result for  $a = 0$  while the third the supergravity result in the  $a \rightarrow \infty$  limit. The change from  $a = 0$  to  $a = \infty$  in the supergravity predictions is tiny. Note, that for the excited state the supergravity calculation came before the lattice results.

state	lattice, $N = 3$	supergravity $a = 0$	supergravity $a \rightarrow \infty$
$0^{++}$	$1.61 \pm 0.15$	1.61 (input)	1.61 (input)
$0^{++*}$	$2.48 \pm 0.18$	2.55	2.56
$0^{++**}$	-	3.46	3.48
$0^{++***}$	-	4.36	4.40

# Holography Inspired Stringy Hadron model

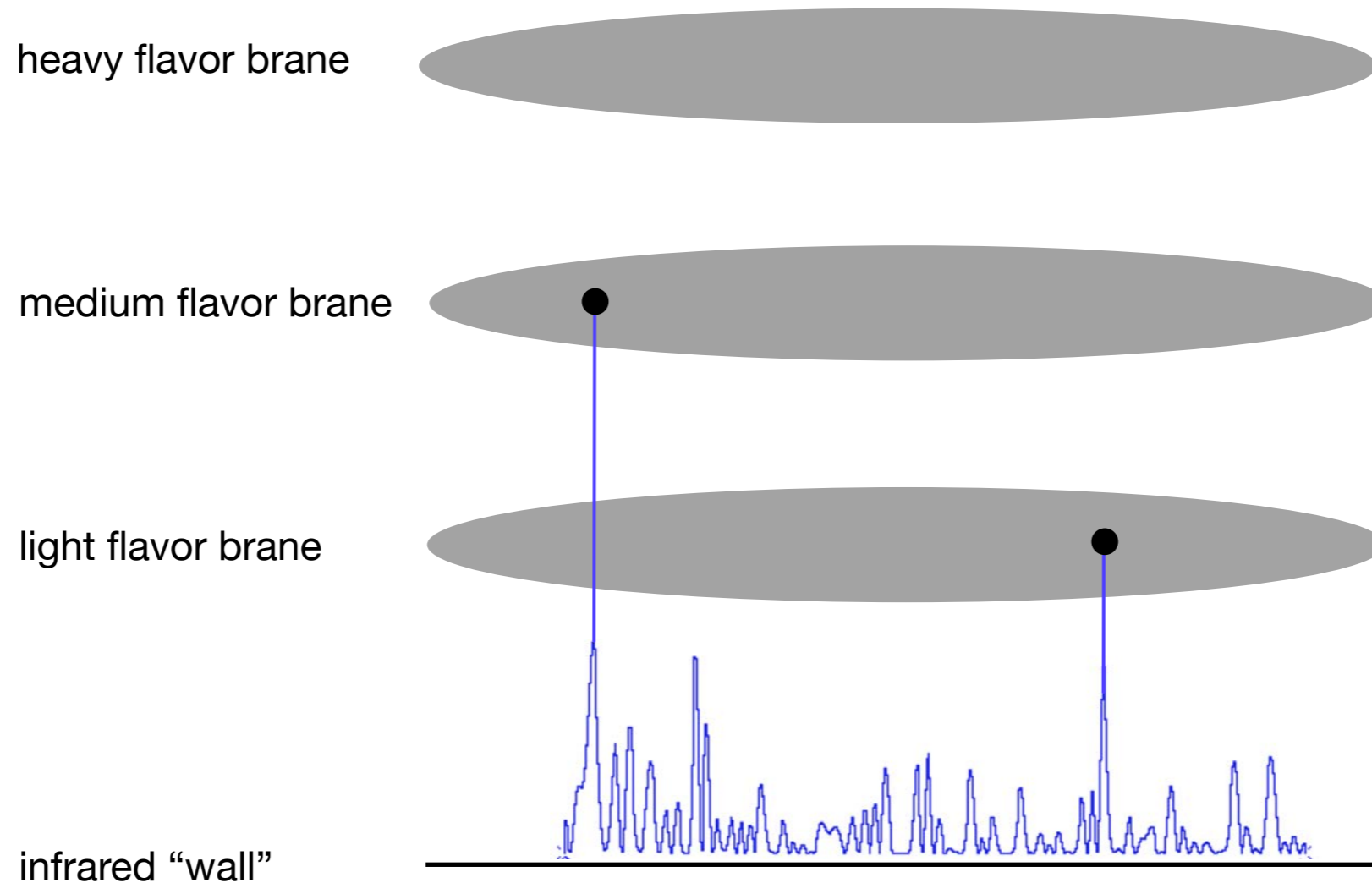


Jacob Sonnenschein, Dorin Weissman, JHEP 1512 (2015) 011, arXiv:1507.01604.

Jacob Sonnenschein, Dorin Weissman, *Eur.Phys.J.C* 79 (2019) 4, 326 • e-Print: [1812.01619](#) [hep-ph]

Jakob Sonnenschein, *Prog.Part.Nucl.Phys.* 92 (2017) 1-49 • e-Print: [1602.00704](#) [hep-th]

# Holography Inspired Stringy Hadron model: decays



Fluctuations of the gluon string reaching flavor branes cause decays

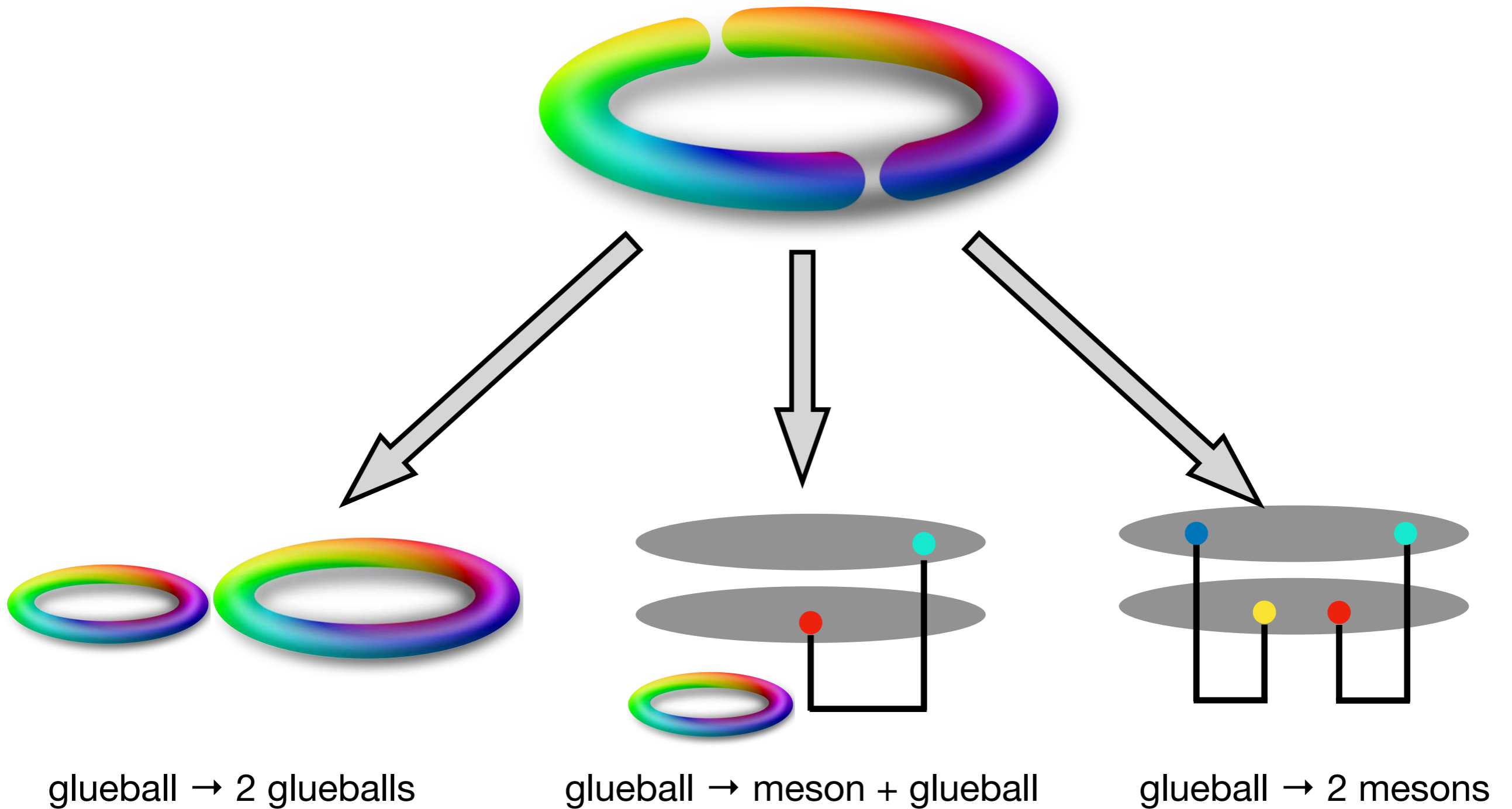
Jacob Sonnenschein, Dorin Weissman, *JHEP* 1512 (2015) 011, arXiv:1507.01604.

Jacob Sonnenschein, Dorin Weissman, *Eur.Phys.J.C* 79 (2019) 4, 326 • e-Print: [1812.01619](#) [hep-ph]

Jakob Sonnenschein, *Prog.Part.Nucl.Phys.* 92 (2017) 1-49 • e-Print: [1602.00704](#) [hep-th]

# Holography Inspired Stringy Hadron model: decay patterns

Glueball decay by string breaking



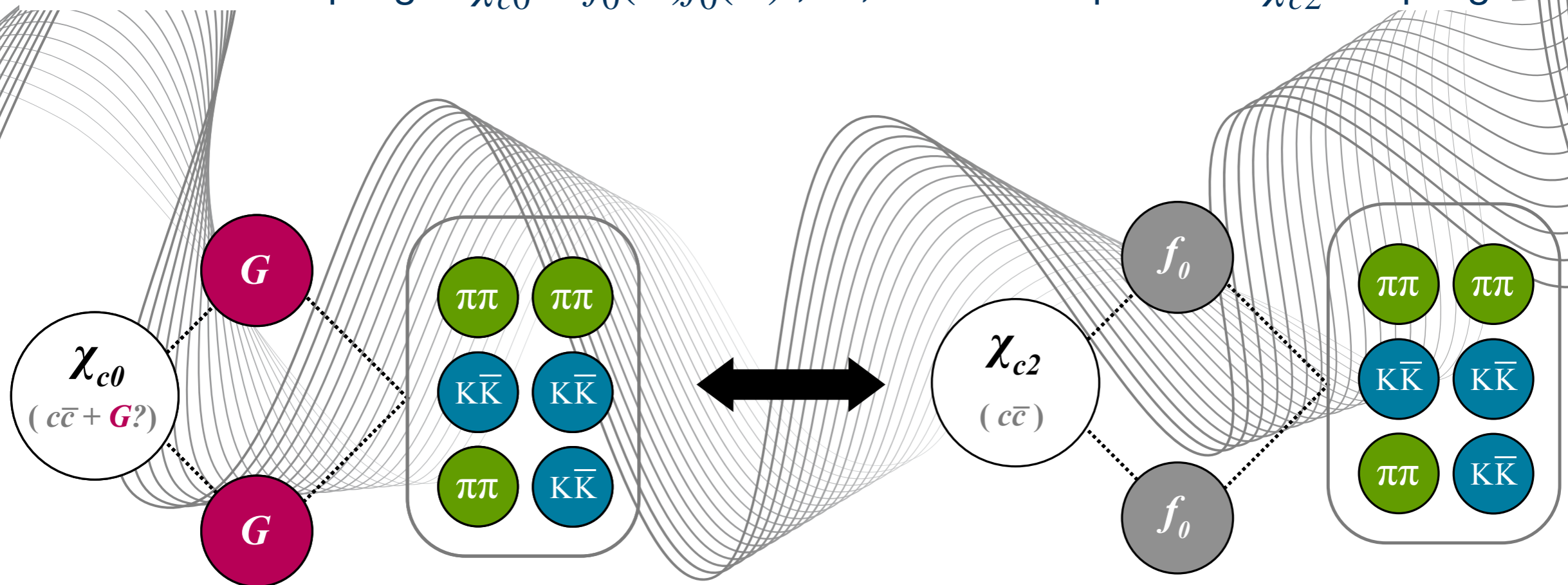
# Possible (leading order?) decays of $\chi_{cJ}$

$\chi_{c0}$ with suspected glueball admixture	$\chi_{c2}$ no glueball admixture
$f_0(980) + f_0$ (or $f_2$ )	$f_0 + f_2(1270)$
$f_0(1370) + f_0$ (or $f_2$ )	$f_0 + f_2'(1525)$
$f_0(1500) + f_0$ (or $f_2$ )	$f_0 + f_2(1565)$
$f_0(1710) + f_0$ (or $f_2$ )	$f_0 + f_2(1640)$
$f_0(1770) + f_0$ (or $f_2$ )	$f_0 + f_2(1810)$
$f_0(2020) + f_0$ (or $f_2$ )	

suspected glue content

# Strategy for improved analysis

- $\chi_c$  channels have not been investigated since 2008 by CLEO
- $\chi_{c0}$  could contain a gluonic admixture due to the presence of a nearby glueball
- Glueballs might decay also into lighter glueballs...
- Measure the coupling of  $\chi_{c0}$  to  $f_0(X)f_0(Y)$ , ..., and  $\rightarrow$  compare it to  $\chi_{c2}$  couplings



# Investigated channels

⇒ Investigate  $\chi_{cJ}$  decays to (gluon-rich)  $f_0 f_0$ . Interesting channels are:

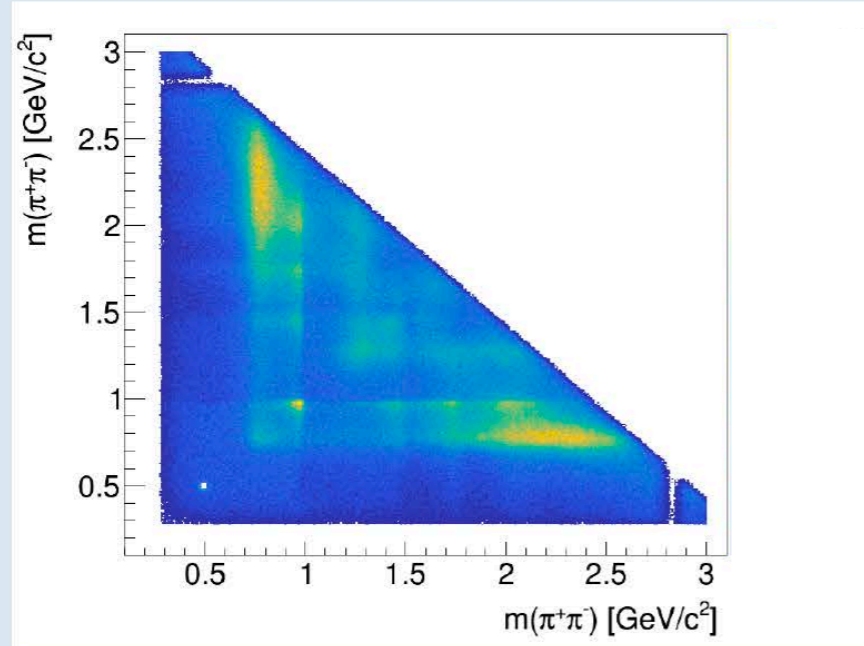
- $\chi_{cJ} \rightarrow \pi^+ \pi^- \pi^0 \pi^0$
- $\chi_{cJ} \rightarrow 2(\pi^+ \pi^-)$
- $\chi_{cJ} \rightarrow \pi^0 \pi^0 \pi^0 \pi^0$
- $\chi_{cJ} \rightarrow \eta \eta \pi^0 \pi^0$
- $\chi_{cJ} \rightarrow \eta \eta' \pi^0 \pi^0$
- $\chi_{cJ} \rightarrow K^+ K^- \pi^0 \pi^0$
- $\chi_{cJ} \rightarrow K^+ K^- \pi^+ \pi^-$
- $\chi_{cJ} \rightarrow K^+ K^- K_S^0 K_S^0$
- $\chi_{cJ} \rightarrow K^+ K^- \pi^0 \pi^0 \pi^0 \pi^0$

Analyses done in Bochum with the goal of comparison of  $\chi_{c0}$  to  $\chi_{c2}$  decays.

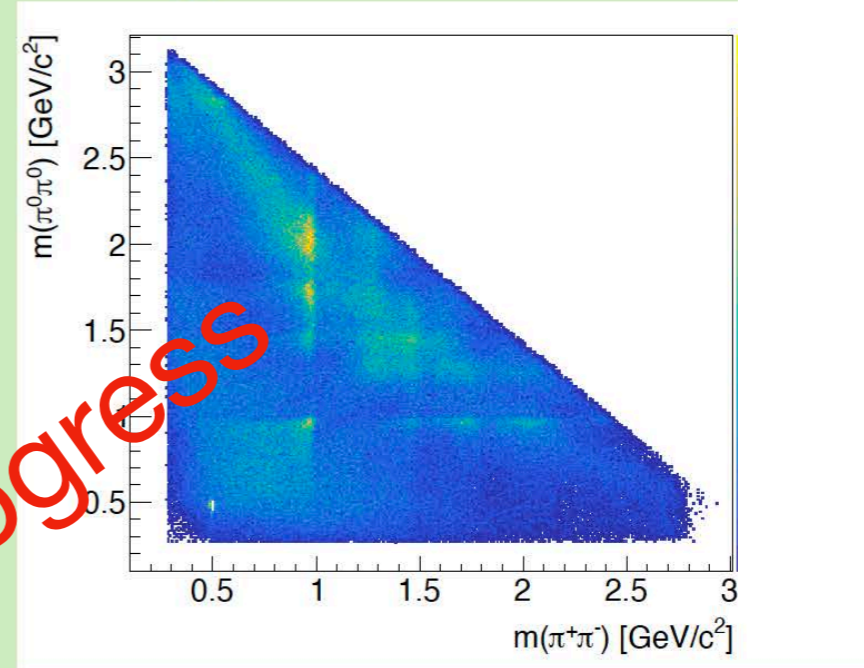
$$\chi_{cJ} \rightarrow 2(\pi^+\pi^-)$$

$$\chi_{cJ} \rightarrow (\pi^+\pi^-\pi^0\pi^0)$$

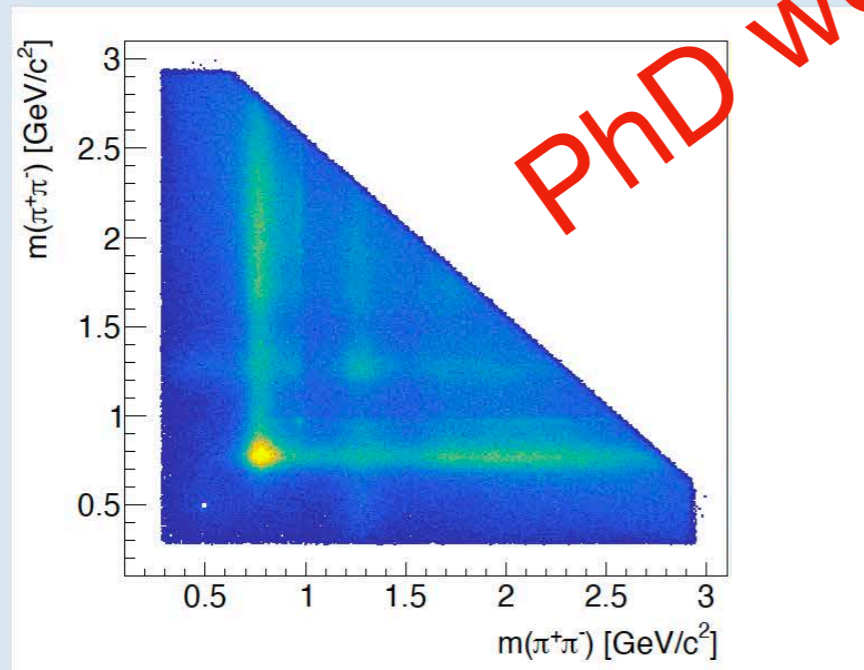
$$\chi_{c0} \rightarrow (\pi^+\pi^-)(\pi^+\pi^-)$$



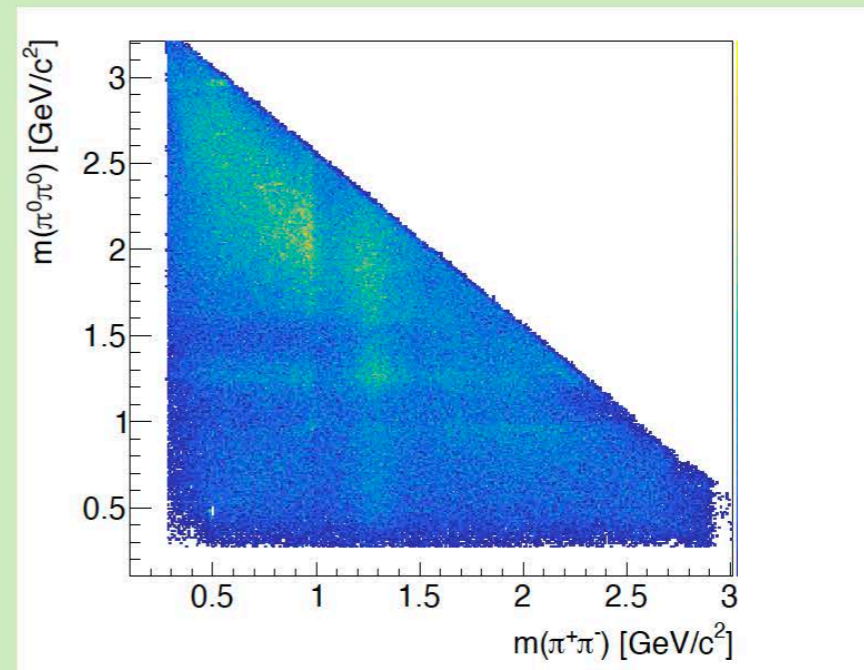
$$\chi_{c0} \rightarrow (\pi^+\pi^-)(\pi^0\pi^0)$$



$$\chi_{c2} \rightarrow (\pi^+\pi^-)(\pi^+\pi^-)$$



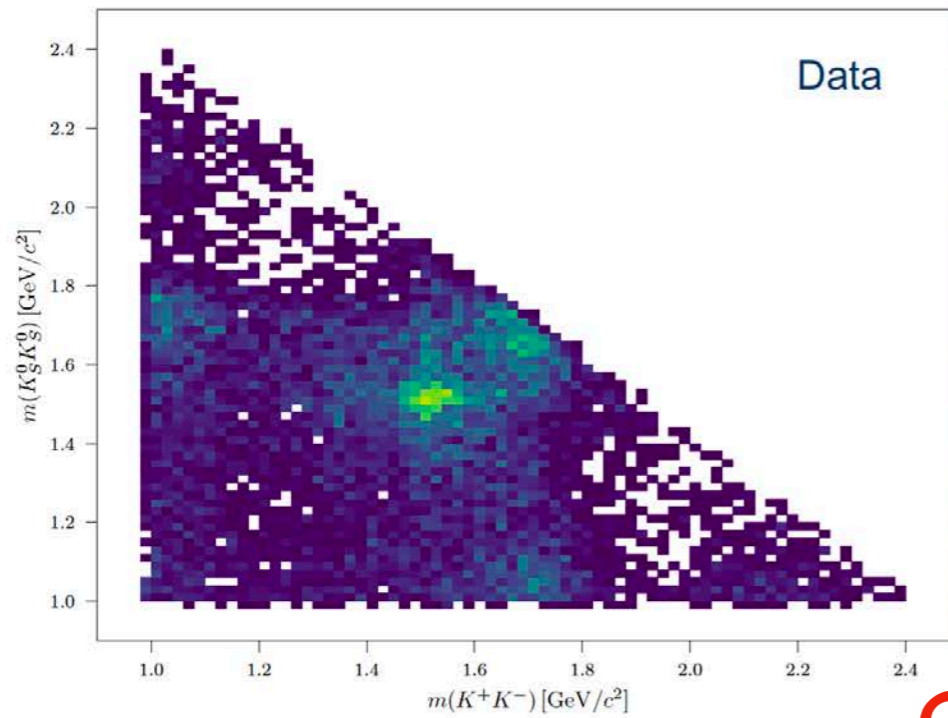
$$\chi_{c2} \rightarrow (\pi^+\pi^-)(\pi^0\pi^0)$$



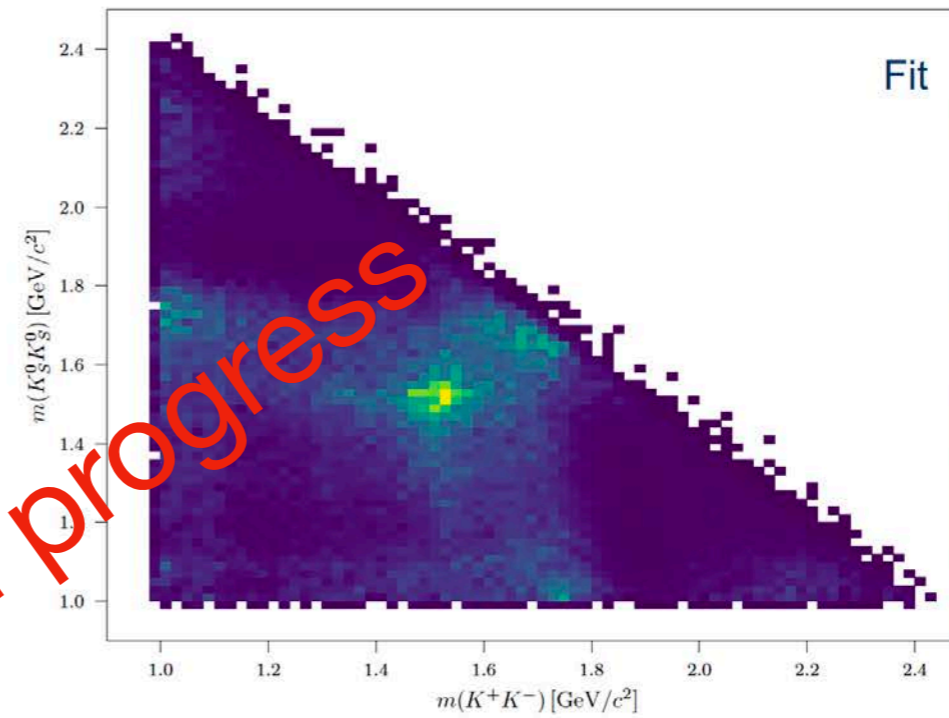
PhD work in progress

# Data and Fit for $\chi_{cJ} \rightarrow K^+K^-K_S^0K_S^0$

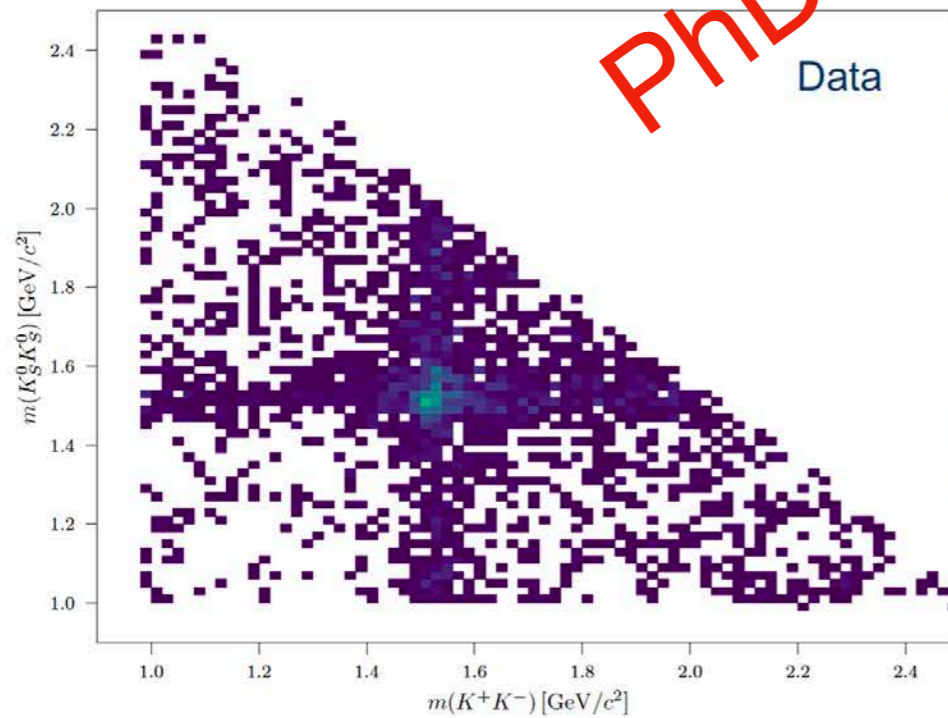
Data  $\chi_{c0} \rightarrow (K^+K^-K_S^0K_S^0)$



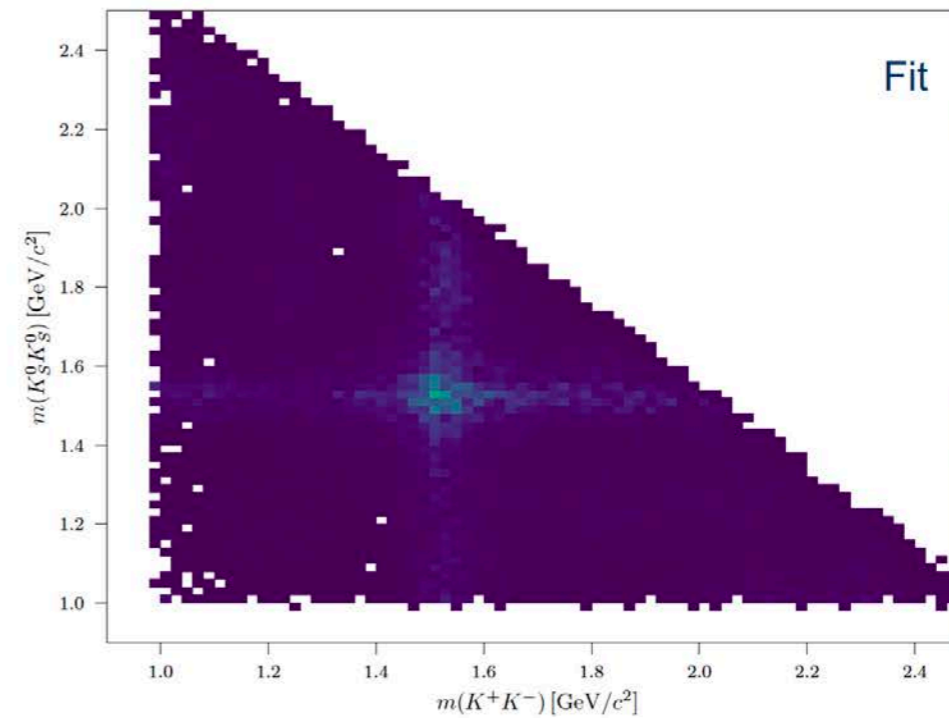
Fit  $\chi_{c0} \rightarrow (K^+K^-K_S^0K_S^0)$



Data  $\chi_{c2} \rightarrow (K^+K^-K_S^0K_S^0)$



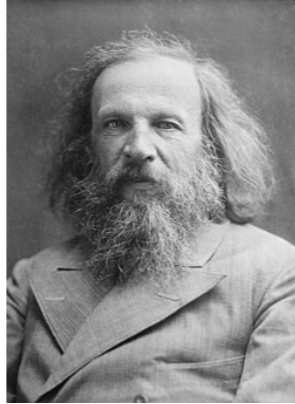
Fit  $\chi_{c2} \rightarrow (K^+K^-K_S^0K_S^0)$



PhD work in progress

# We learned about the nature of the atom due to the periodic system

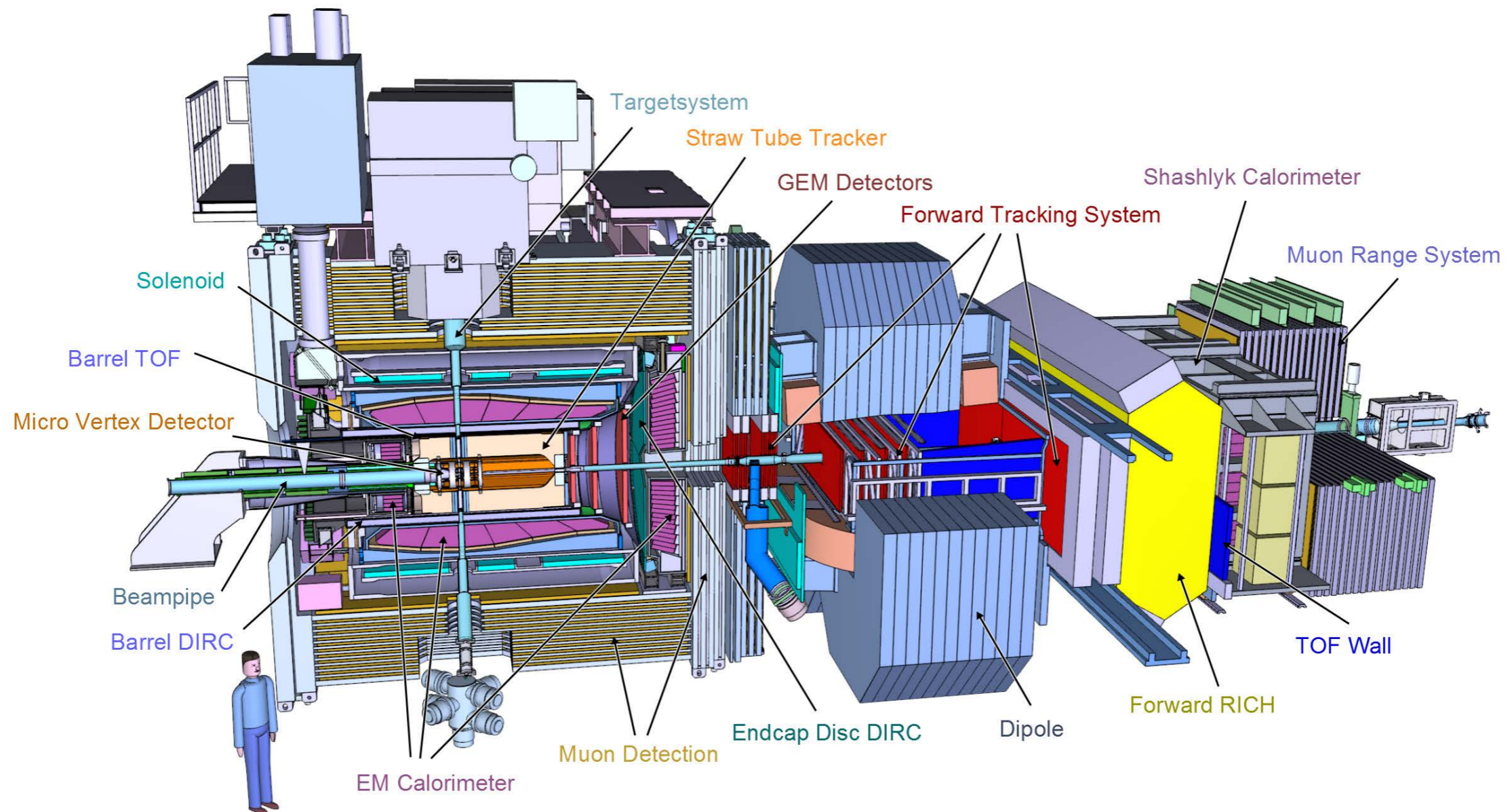
Group→	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
↓Period																		
1	1 H																	2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
6	55 Cs	56 Ba	* 71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
7	87 Fr	88 Ra	* 103 Lr	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Uut	114 Fl	115 Uup	116 Lv	117 Uus	118 Uuo
			* 57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb		
			* 89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No		



Do precision hadron spectroscopy experiments to understand the glueballs!

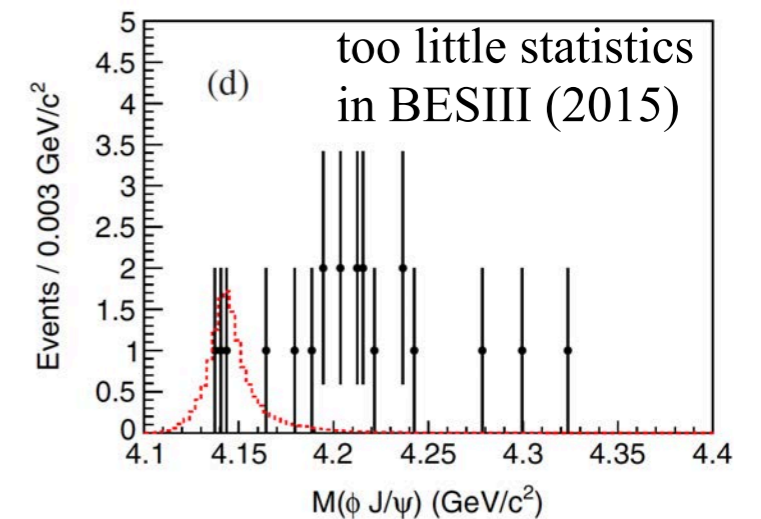
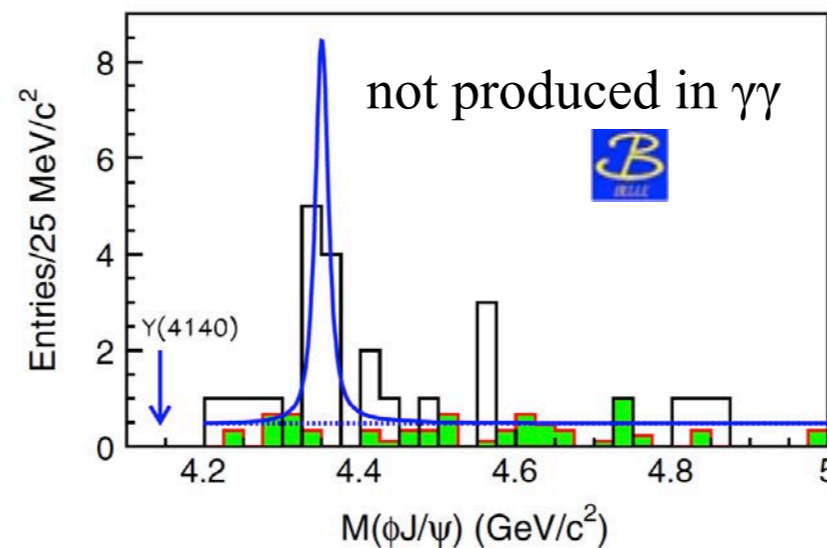
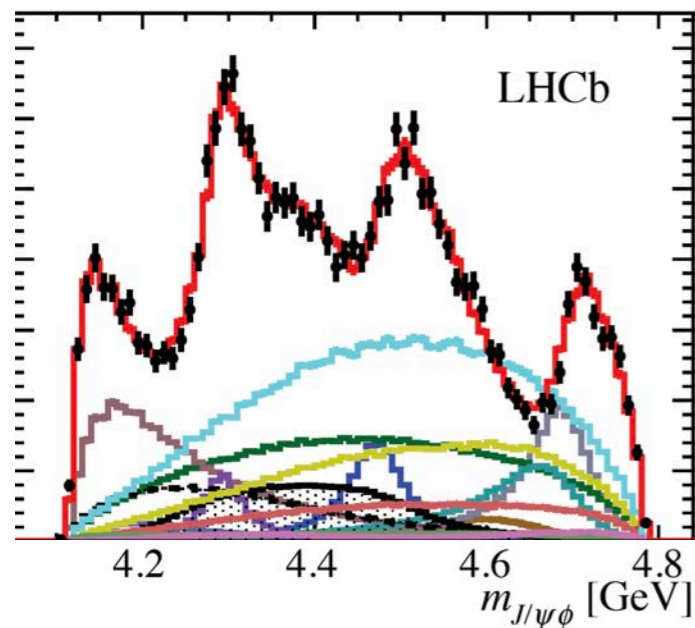
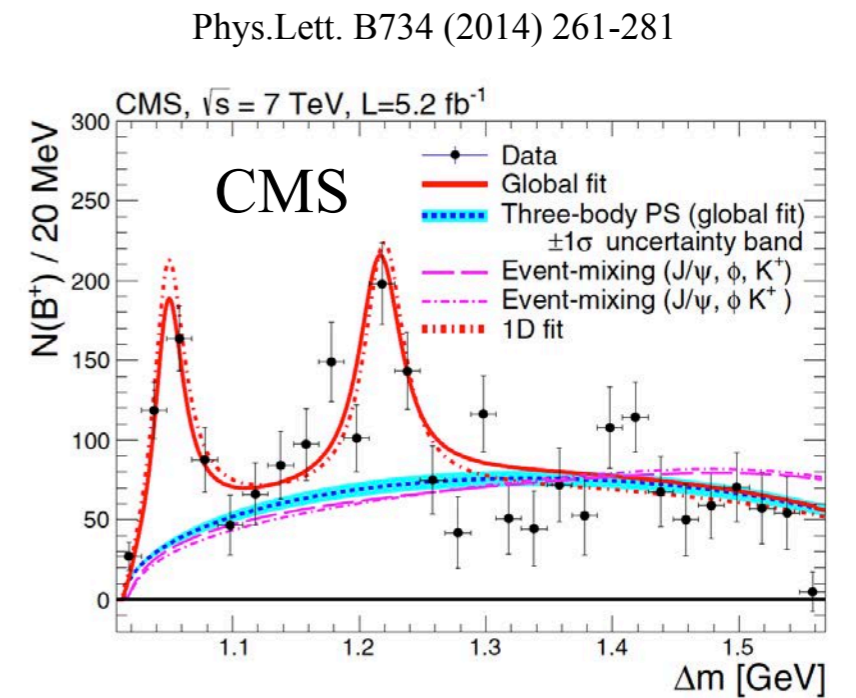
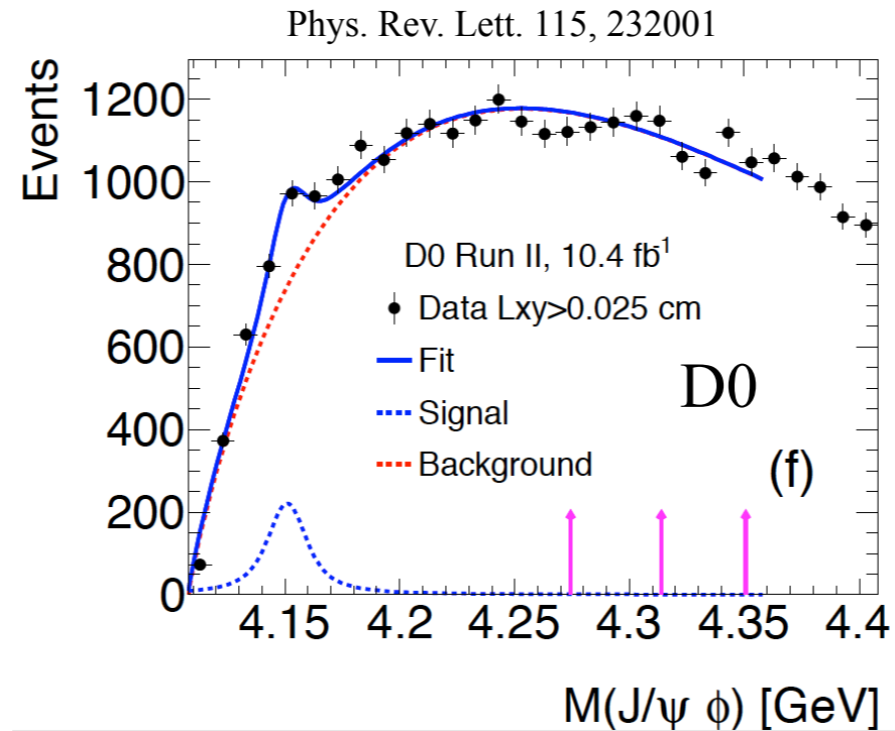
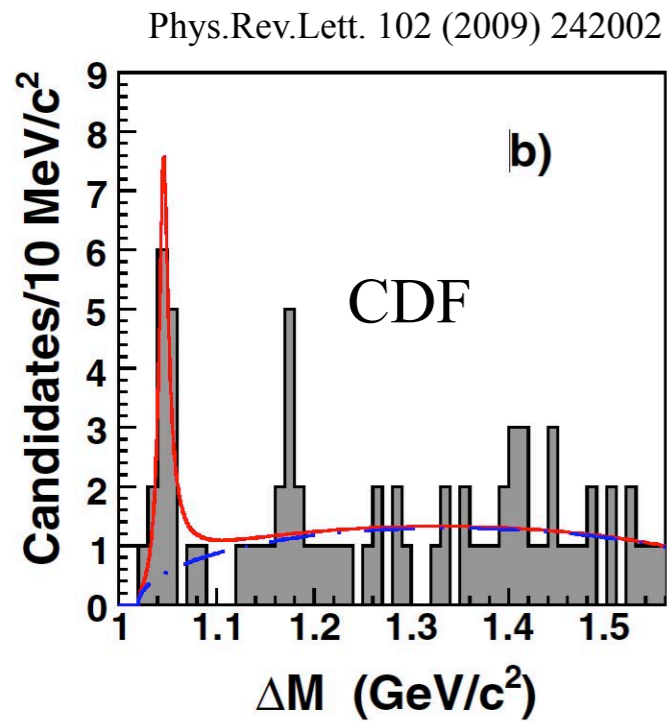
# PANDA @ FAIR

- gluon-rich due to antiprotons-proton annihilations
- no limitations on q.n. of glueballs (even exotic)
- glueballs (and other particles) up to 5.5 GeV
- line shape of resonances



# Glueballs

My personal glueball candidate for  $1^{++}$  glueball:  $X(4140)$   $M = 4147 \text{ MeV}/c^2$ ,  $\Gamma = \sim 19 \text{ MeV}$   
 $\hookrightarrow$  decay mode  $J/\psi \phi$  (flavor blind)



# Summary and conclusions

**BESIII** offers the best opportunity to study glueballs at the moment.

➔ full structure and spectrum to be studied in future by  **PANDA**

There are strong hints for the excited scalar glueball and we have to proof it.

➔ a broad study of 4-body final states is underway.

We might be able to establish glueball to glueball decays.

Our studies will lead to a better understanding of the ground state scalar glueball.

***Glueballs are fundamental for understanding mass creation!***

*Thank you for your attention!*