

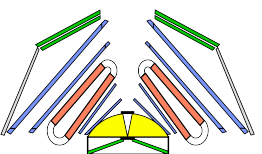
Production Mechanism Studies in $pp \rightarrow NN\pi$: Comparison with SMASH

VIII HADES physics analysis meeting 2026

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Why N^* and Δ ?

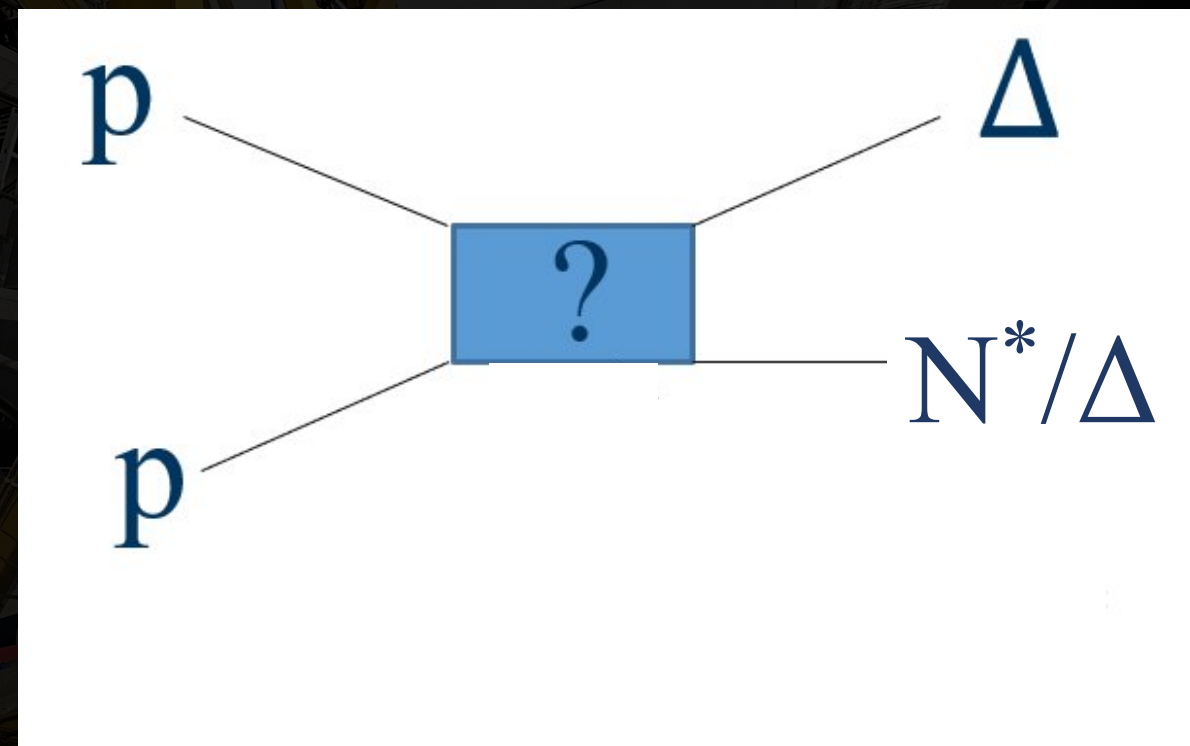
- “They are the simplest system to understand the **non-Abelian nature** of QCD”[1].

1.N. Isgur, in: V. Burkert, L. Elouadrhiri, J. Kelly, R.M. (eds.) (Eds.), NSTAR2000: Excited Nucleons and Hadronic Structure, Newport News, USA, 2000, pp. 422–445, arXiv:nucl-th/0007008.

2.Volker Burkert, Gernot Eichmann, Eberhard Klempt, Progress in Particle and Nuclear Physics, Volume 146, Part 2, 2026, <https://doi.org/10.1016/j.pnnp.2025.104214>.

Why N^* and Δ ?

- “They are the simplest system to understand the **non-Abelian nature** of QCD”[1].
- Understanding the **production mechanisms and dynamical behavior** of these resonances is a key objective of this study.
- What is the relationship between **dynamically generated resonances and quark-model states**[2]?

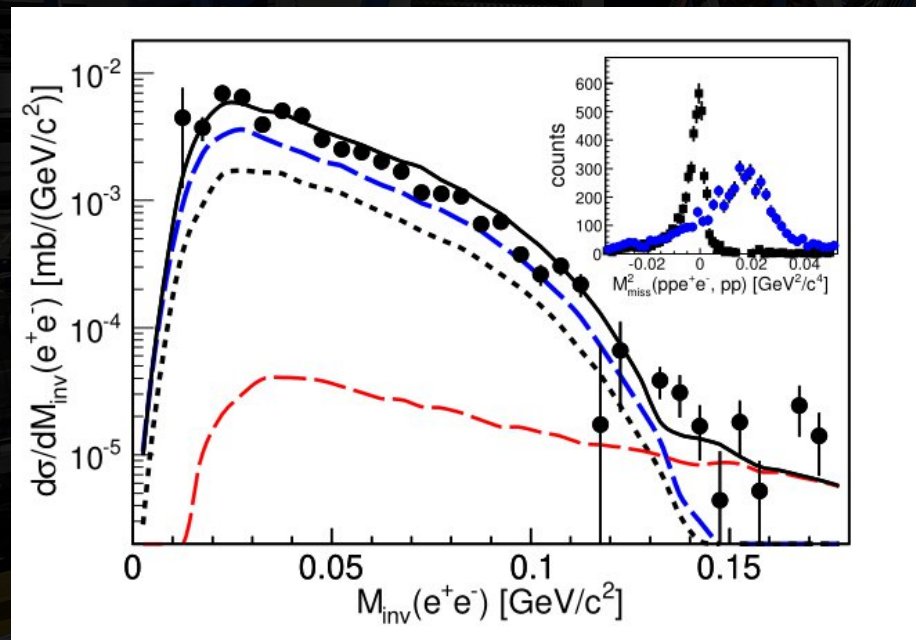


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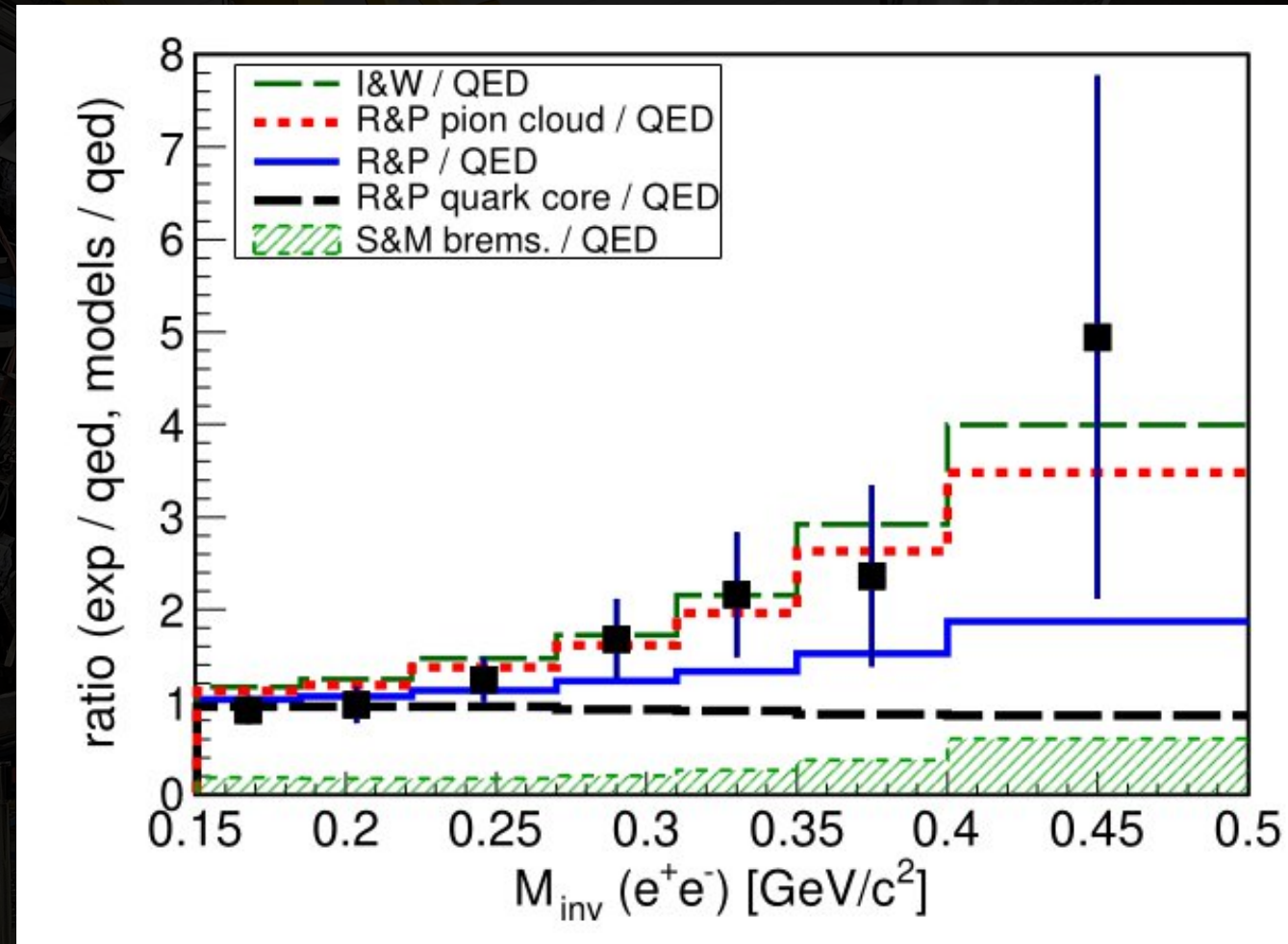
Towards Studying the Electromagnetic Properties of Light Baryons

- Production mechanisms and reaction dynamics of N^* and Δ states in $pp \rightarrow NN\pi$ provide access to their electromagnetic structure through dilepton decays.



contribution of Δ and $N(1440)$ ^[3]

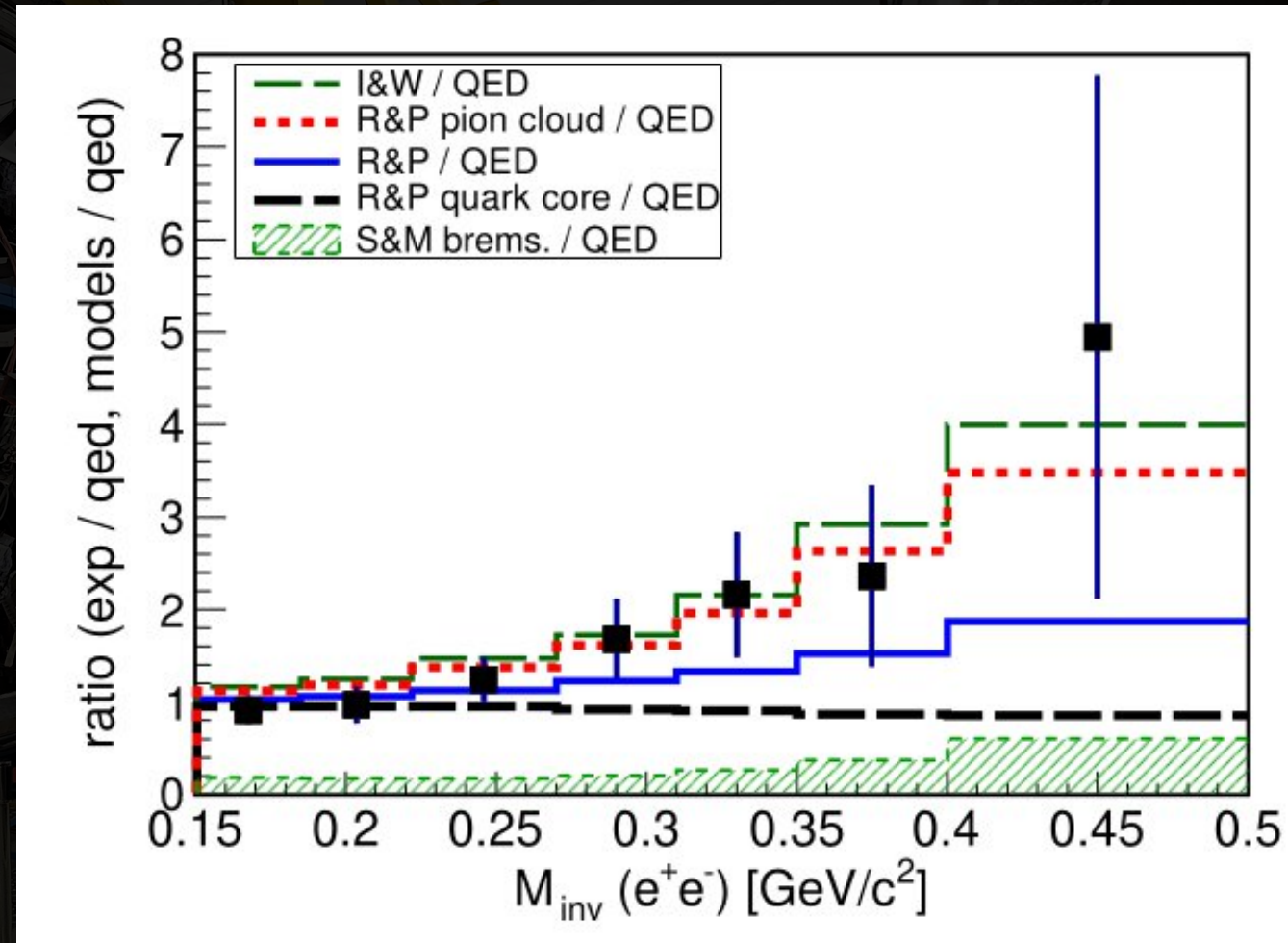
3. Adamczewski-Musch, J. *et al.* $\Delta(1232)$ Dalitz decay in proton-proton collisions at $T=1.25$ GeV measured with HADES at GSI. *Phys. Rev. C* **95**, 065205 (2017).



effective transition form factor for $\Delta \rightarrow pe^+e^-$ ^[3]

Towards Studying the Electromagnetic Properties of Light Baryons

- **Production mechanisms and reaction dynamics** of N^* and Δ states in $pp \rightarrow NN\pi$ provide access to their **electromagnetic structure** through **dilepton decays**.
- Extract differential cross-sections and also the coupling strengths N^* and Δ resonances.
- How do these measurements improve the baseline for transport models and heavy-ion collisions?



effective transition form factor for $\Delta \rightarrow pe^+e^-$ [3]

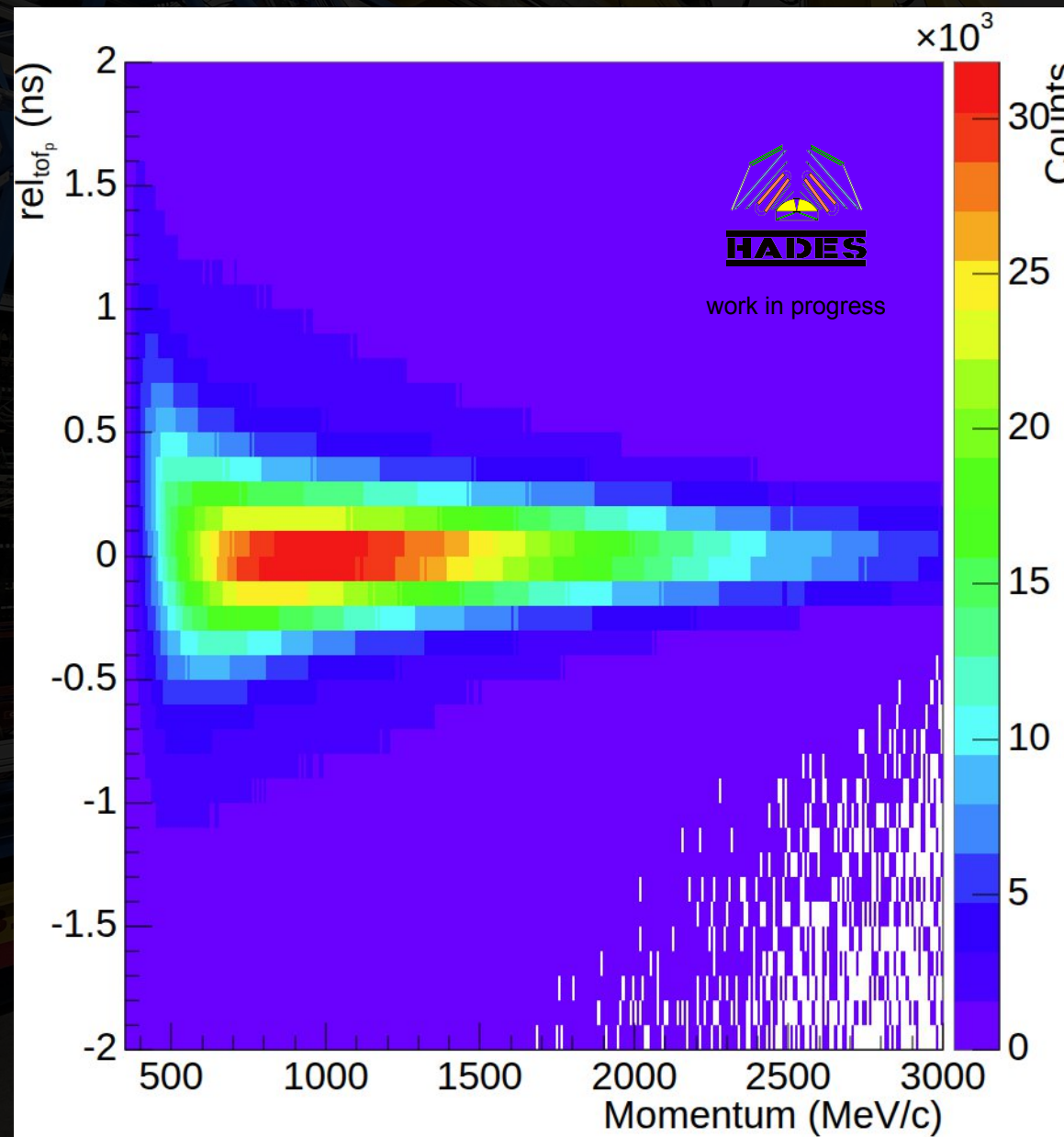
Particle Identification via TOF Residual χ^2

- For each event, four track PID hypotheses are evaluated:
 $pp, p\pi^+, \pi^+p, \pi^+\pi^+$
- For each hypothesis Δt_i is calculated, where $\Delta t_i = \text{measured-expected TOF for track } i$.
- For each event, the four possible values of χ^2 are calculated corresponding to all four possible track combinations.

$$\chi^2 = (\Delta t_1)^2 + (\Delta t_2)^2$$

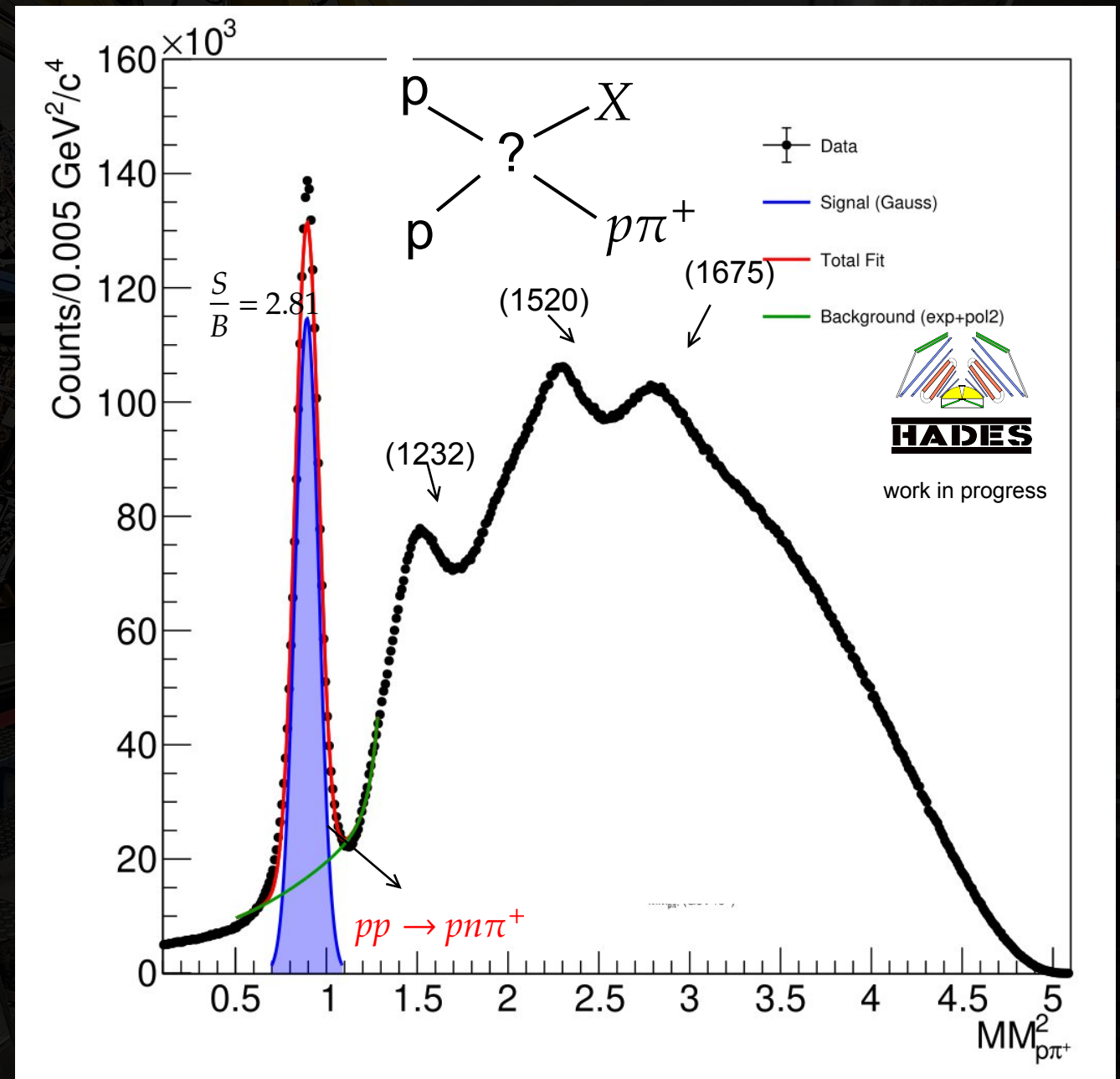
- The track PID hypothesis with the smallest χ^2 value is chosen to identify the PID of the two tracks.

Particle Identification via TOF Residual χ^2



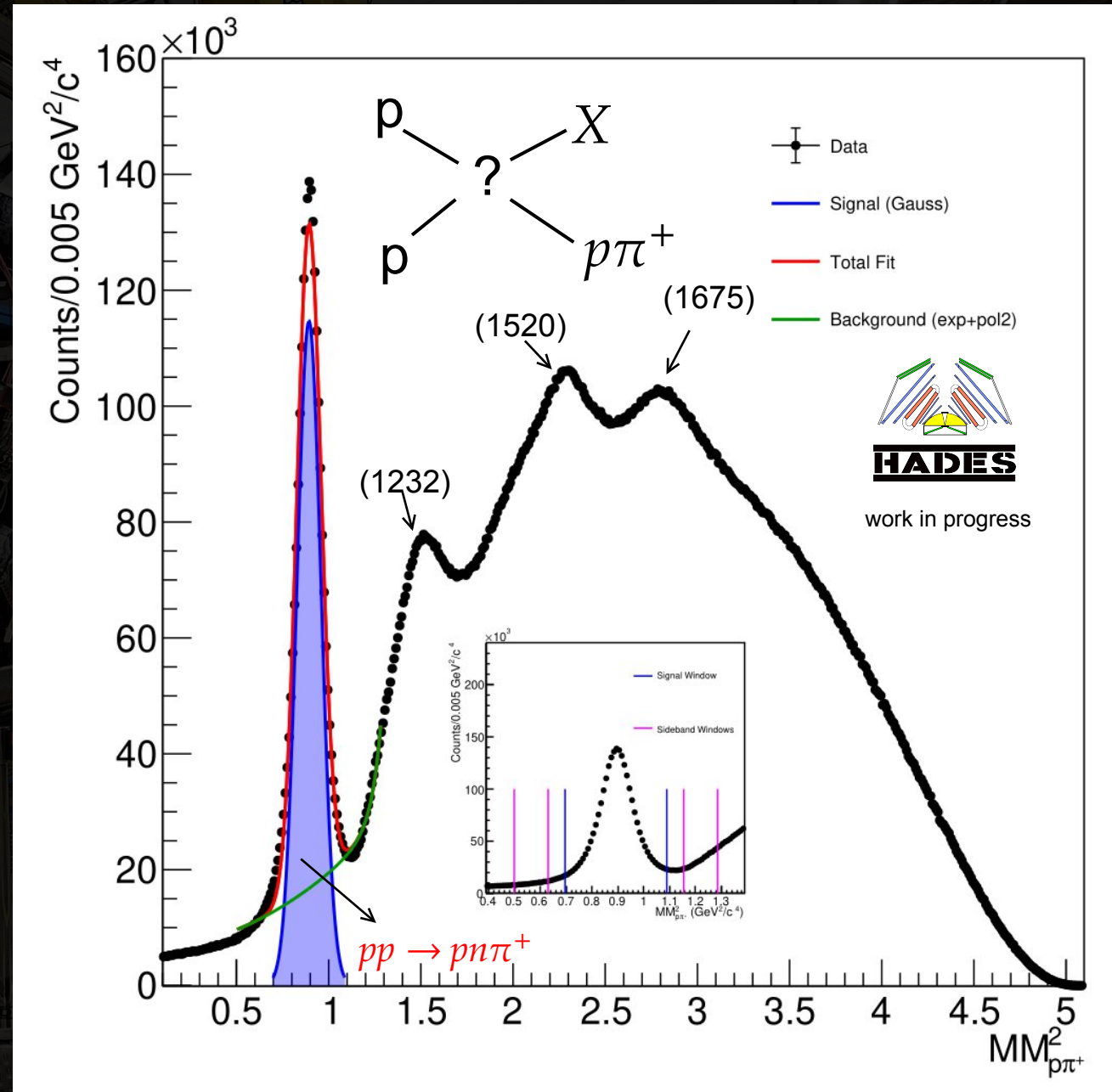
Missing Neutron Identification

- Select missing neutron by applying mass window for further analysis.
- Kinematic fit (Missing Mass Constraint) is applied to signal and sideband regions.

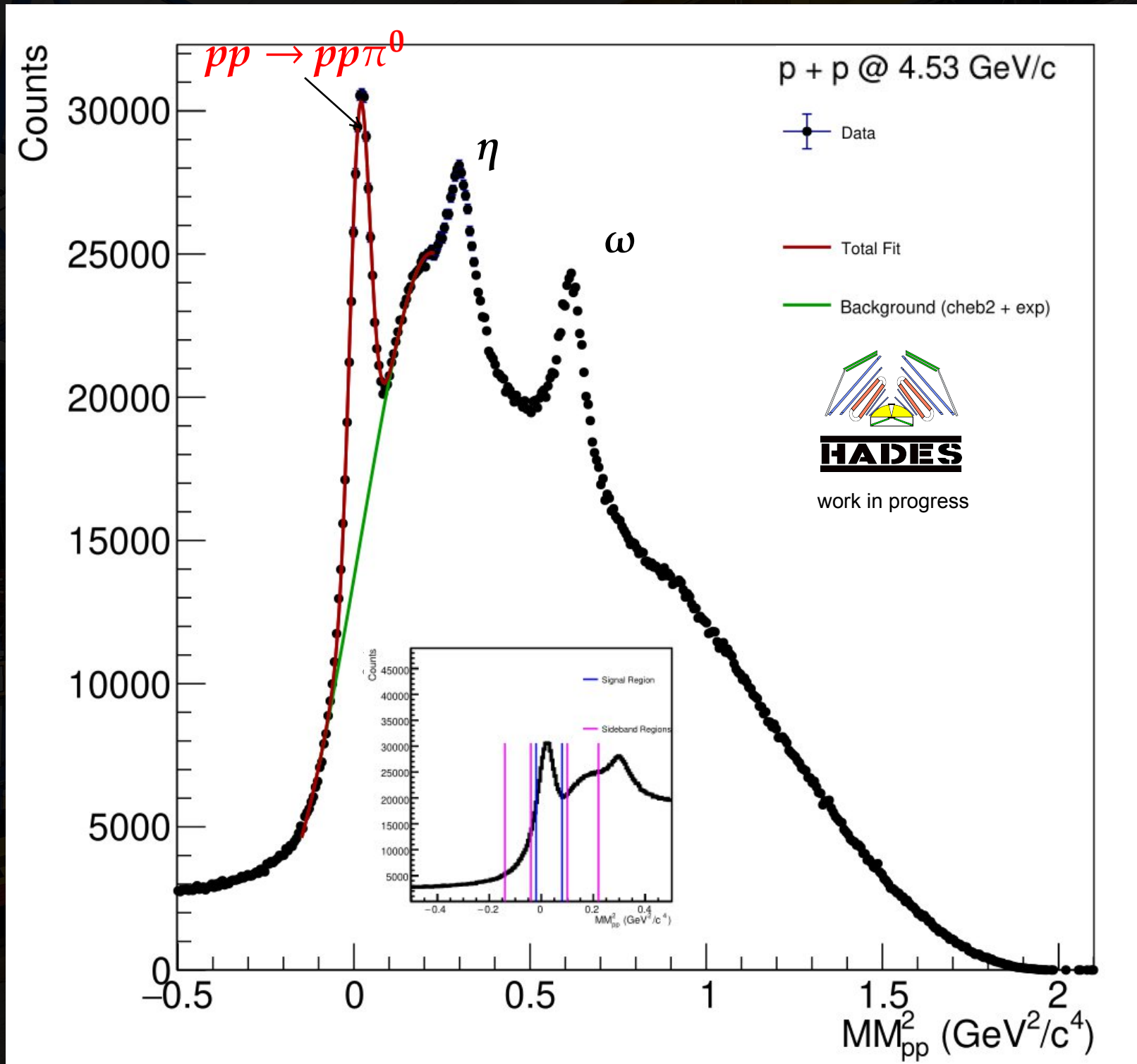


Missing Neutron Identification

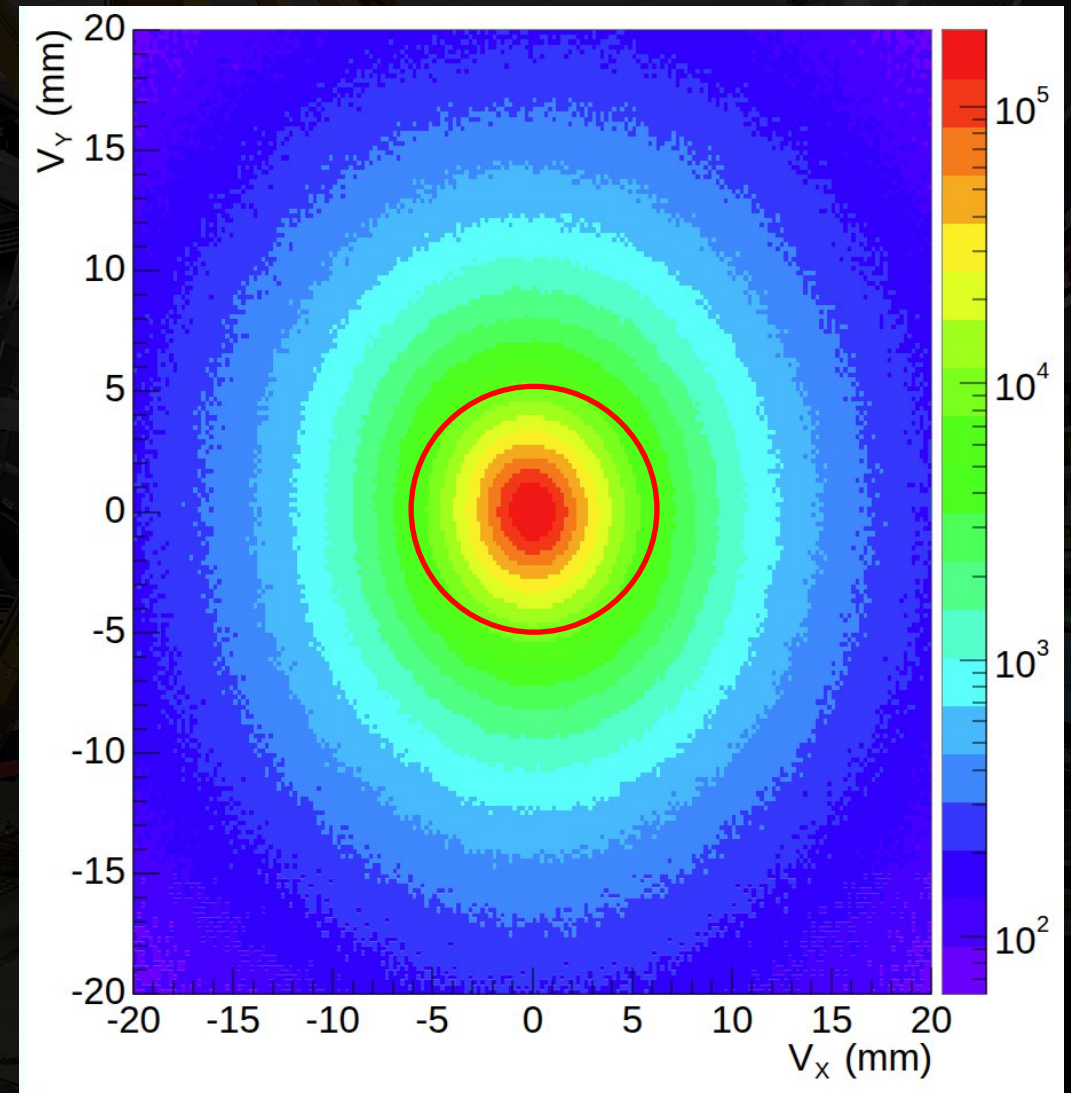
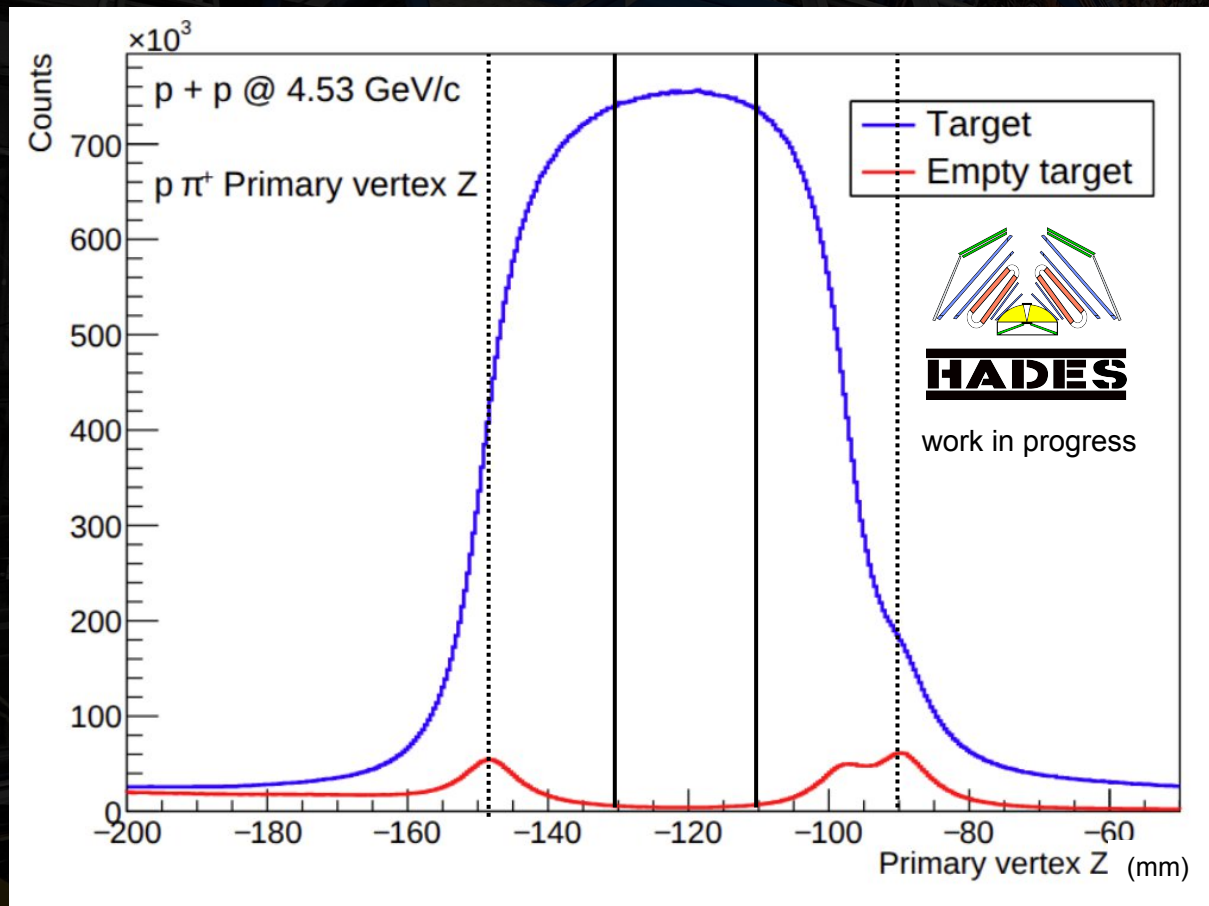
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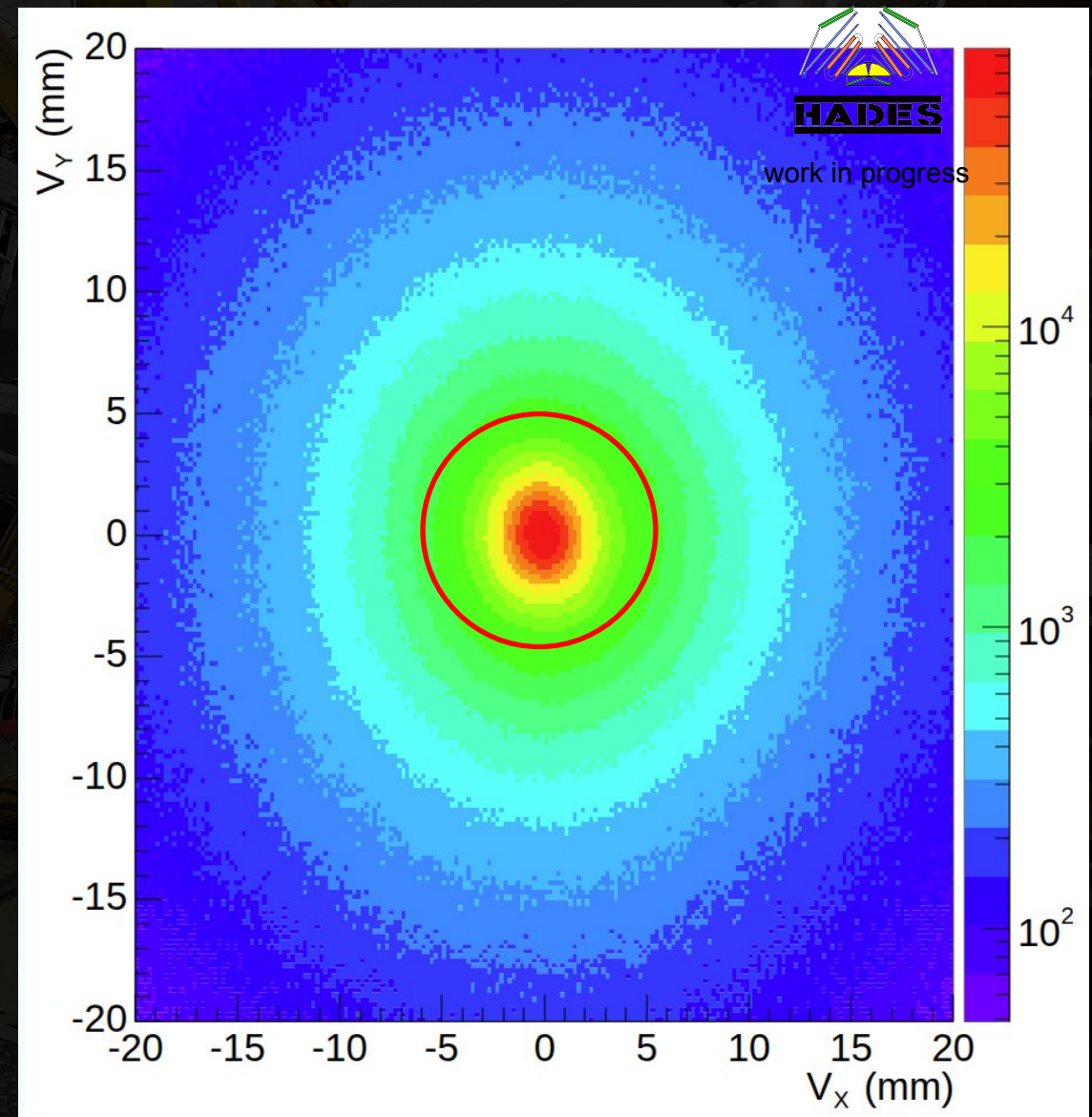
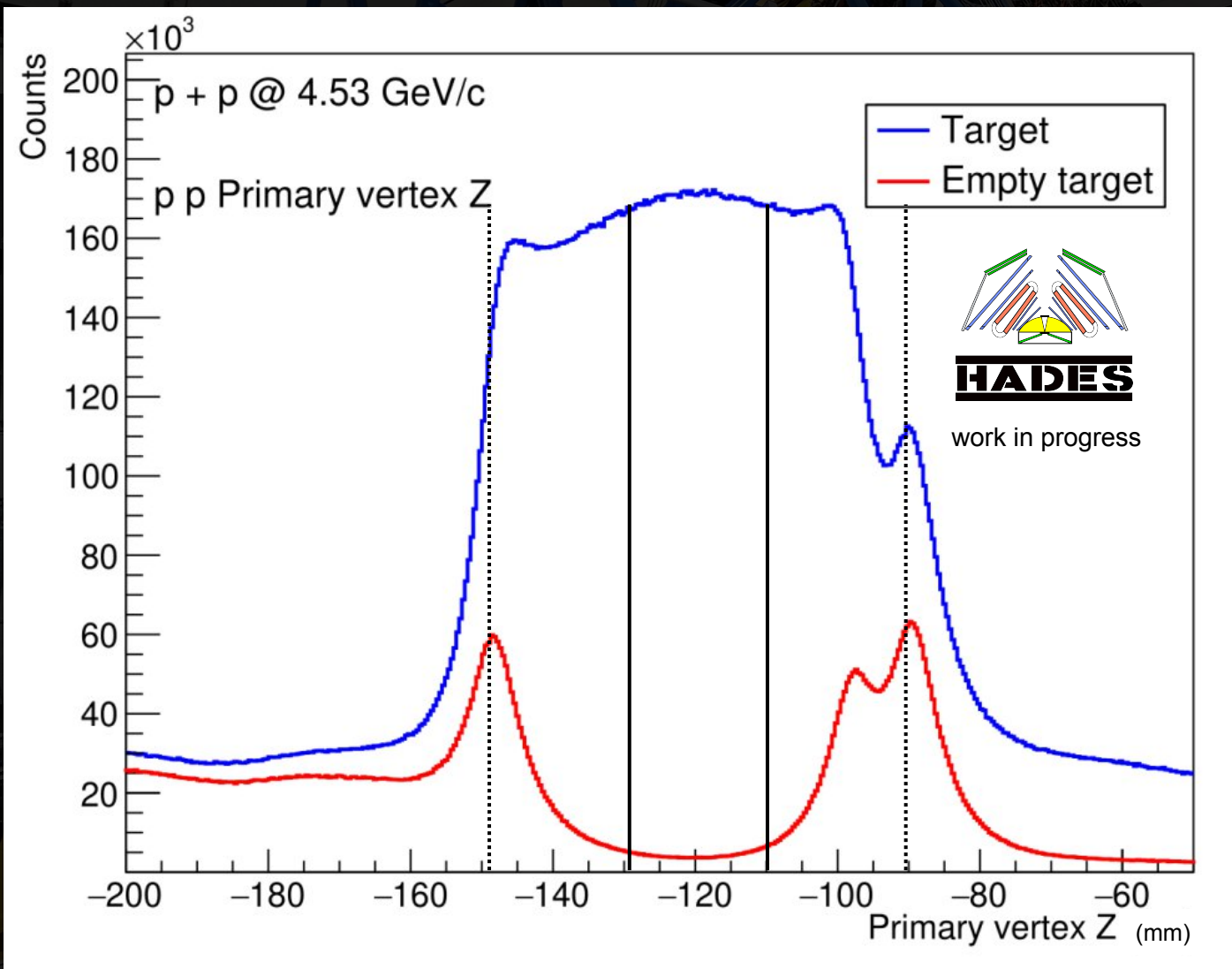
$$pp \rightarrow pp\pi^0$$



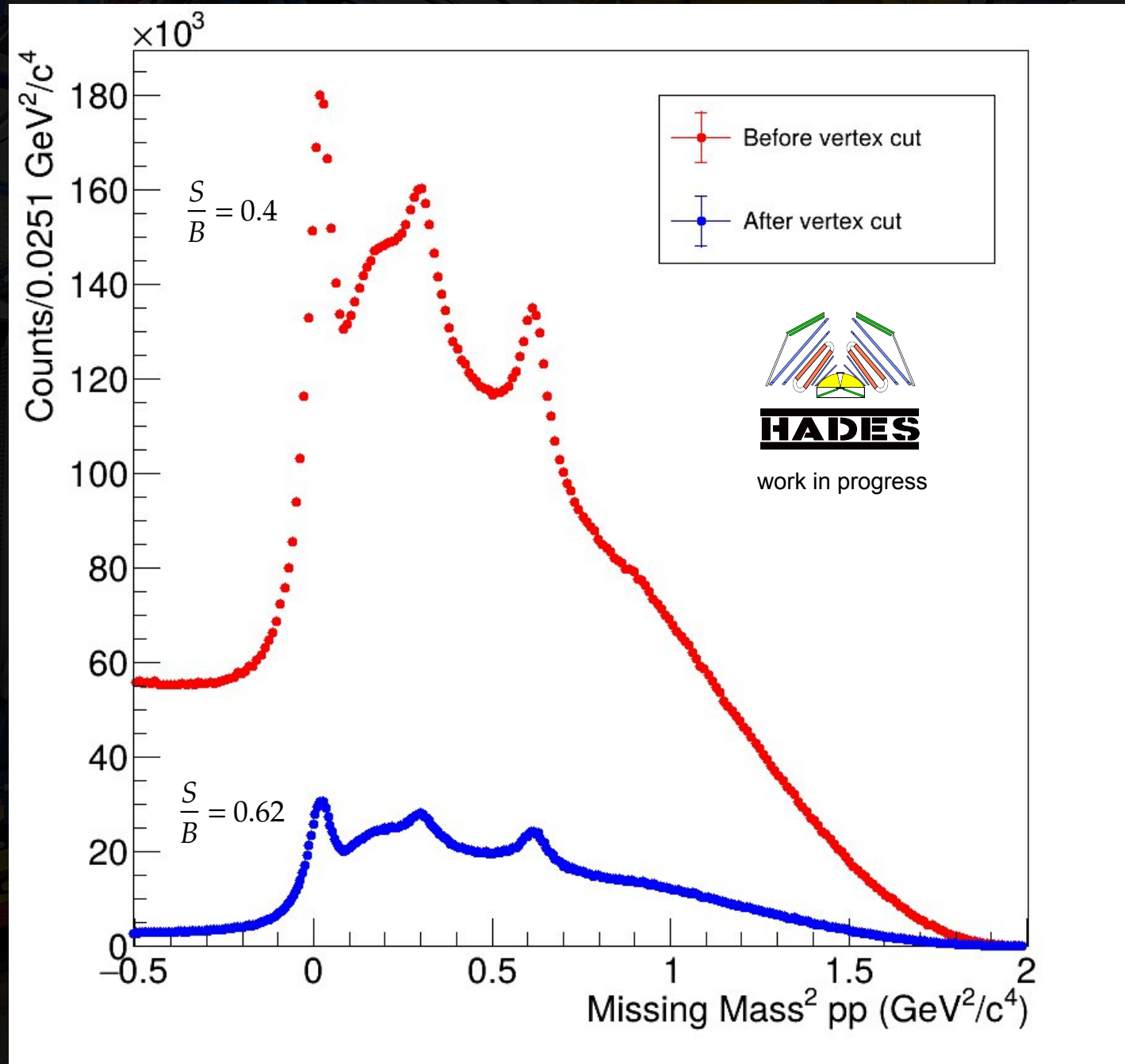
$p n \pi^+$ Vertex Selection



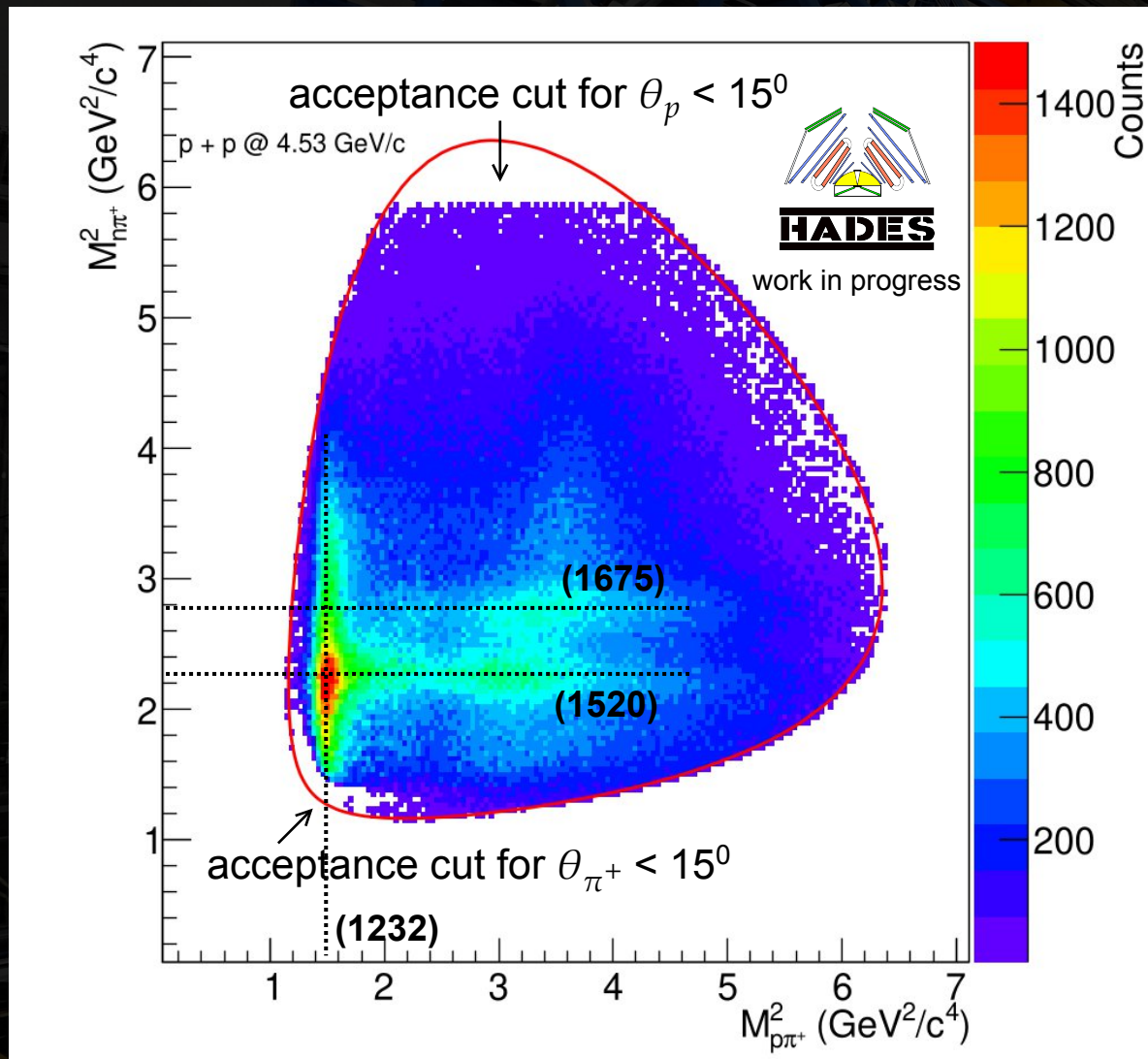
$pp \rightarrow pp\pi^0$ Vertex Selection



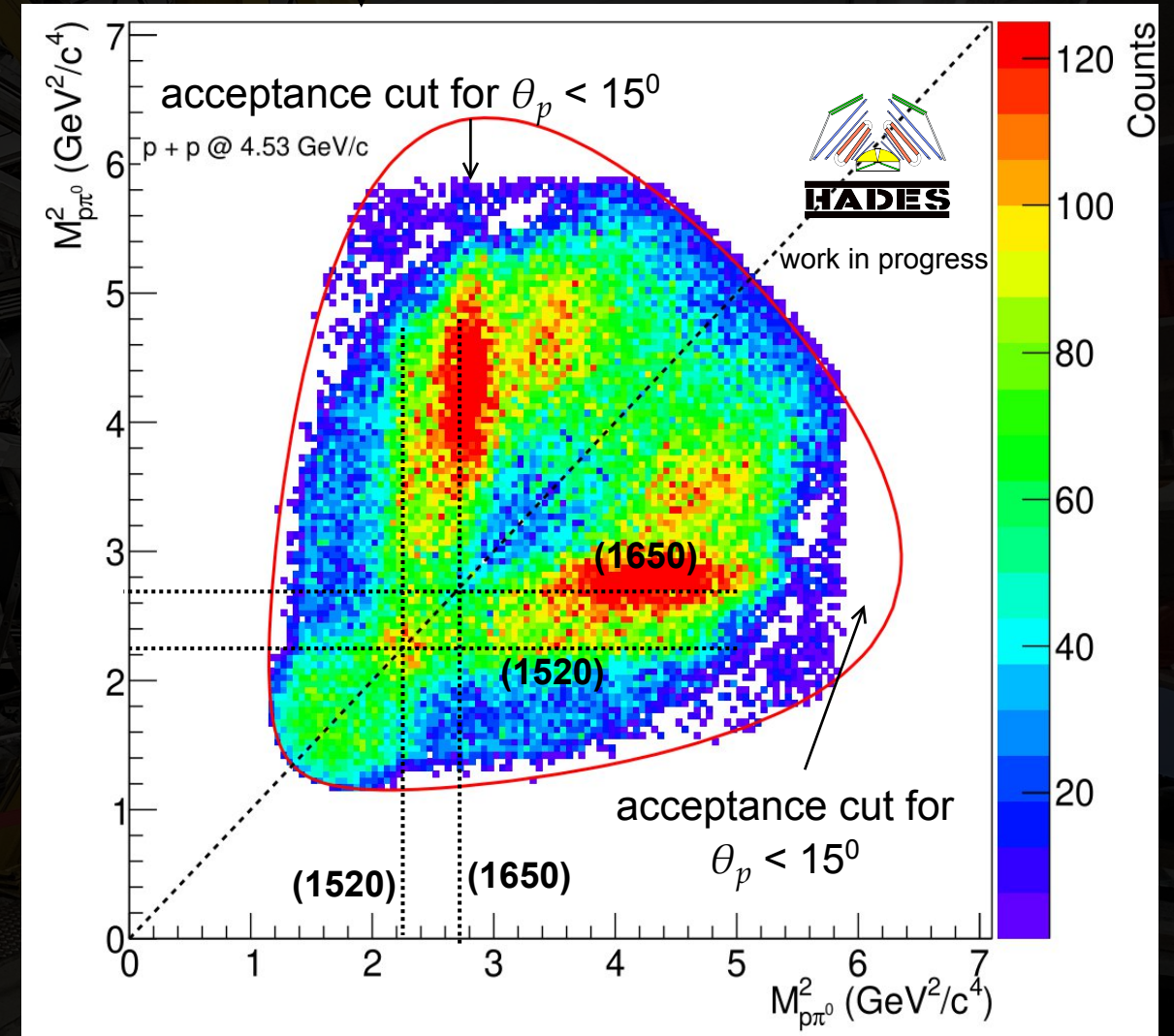
$pp \rightarrow pp\pi^0$ Vertex Selection



Sideband Subtracted Dalitz Plots

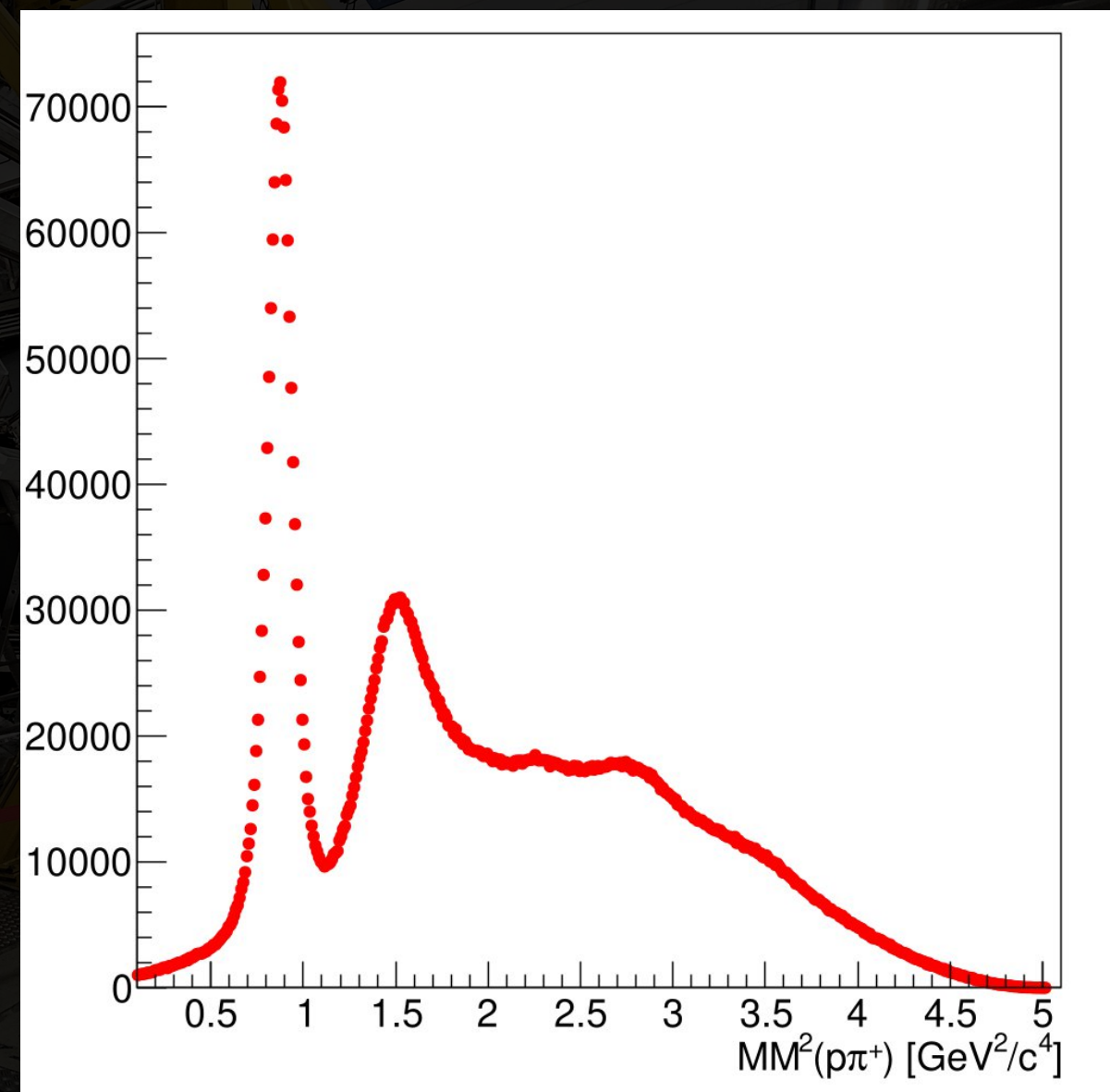
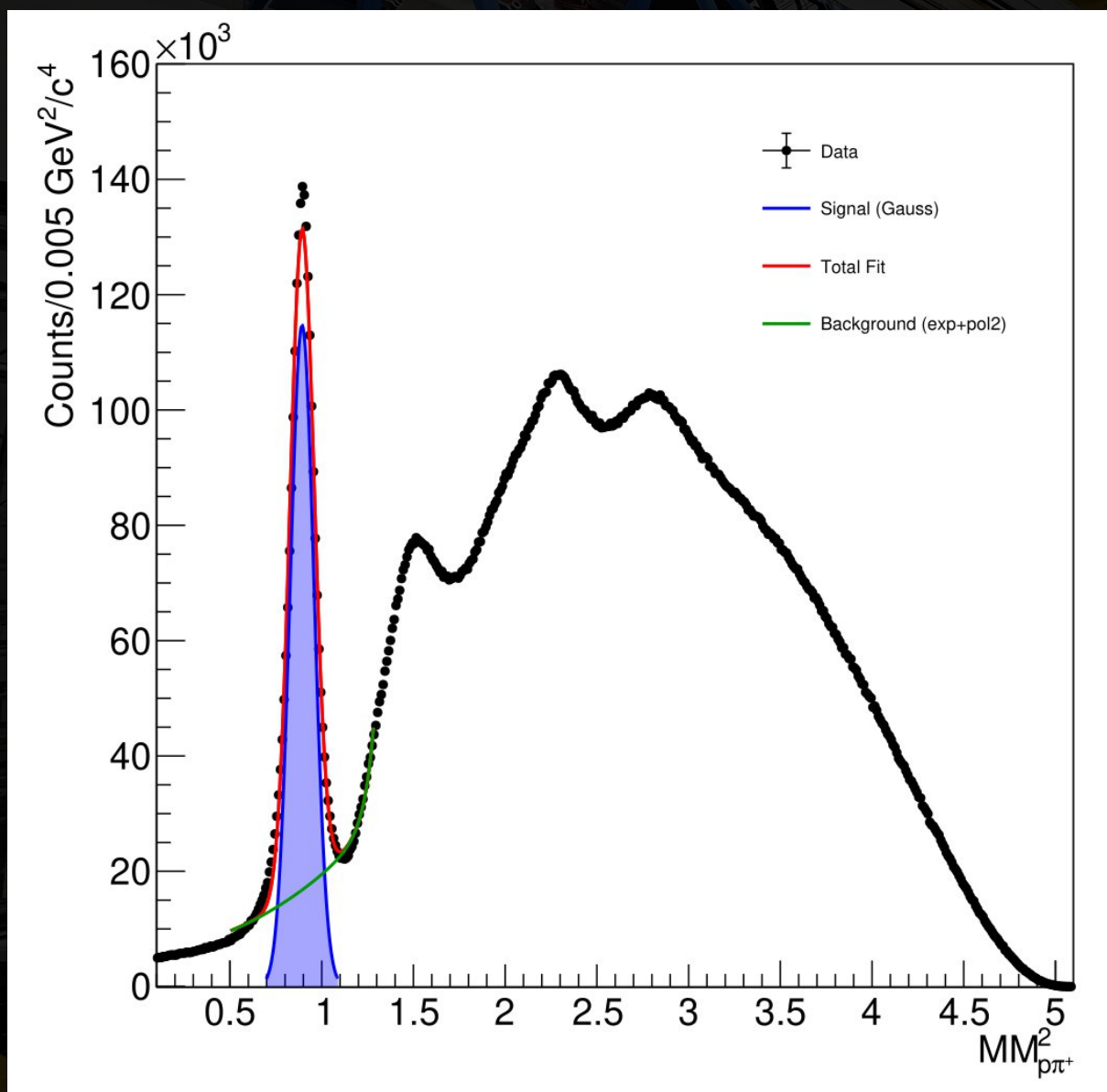


$pn\pi^+$



$pp\pi^0$

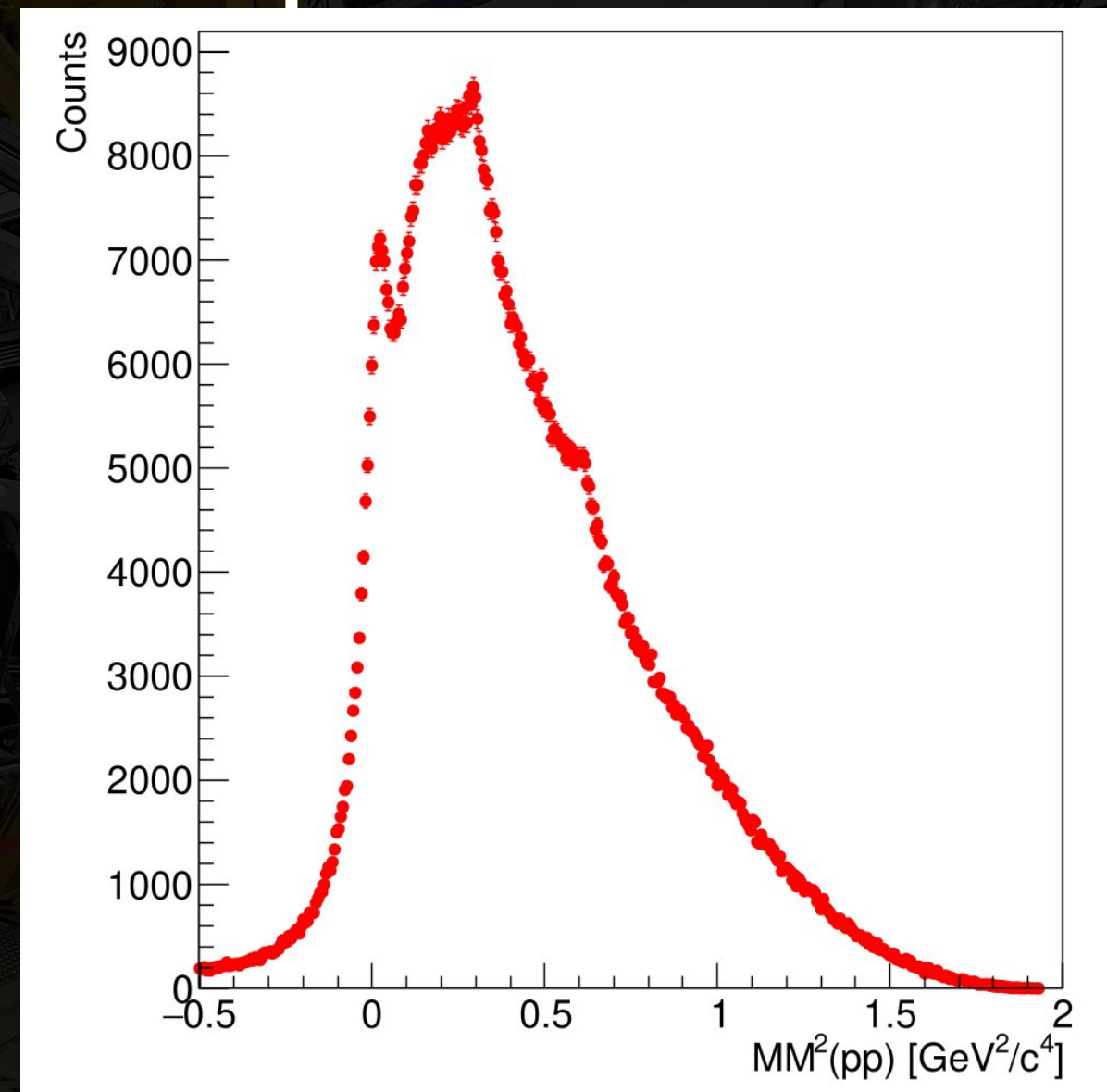
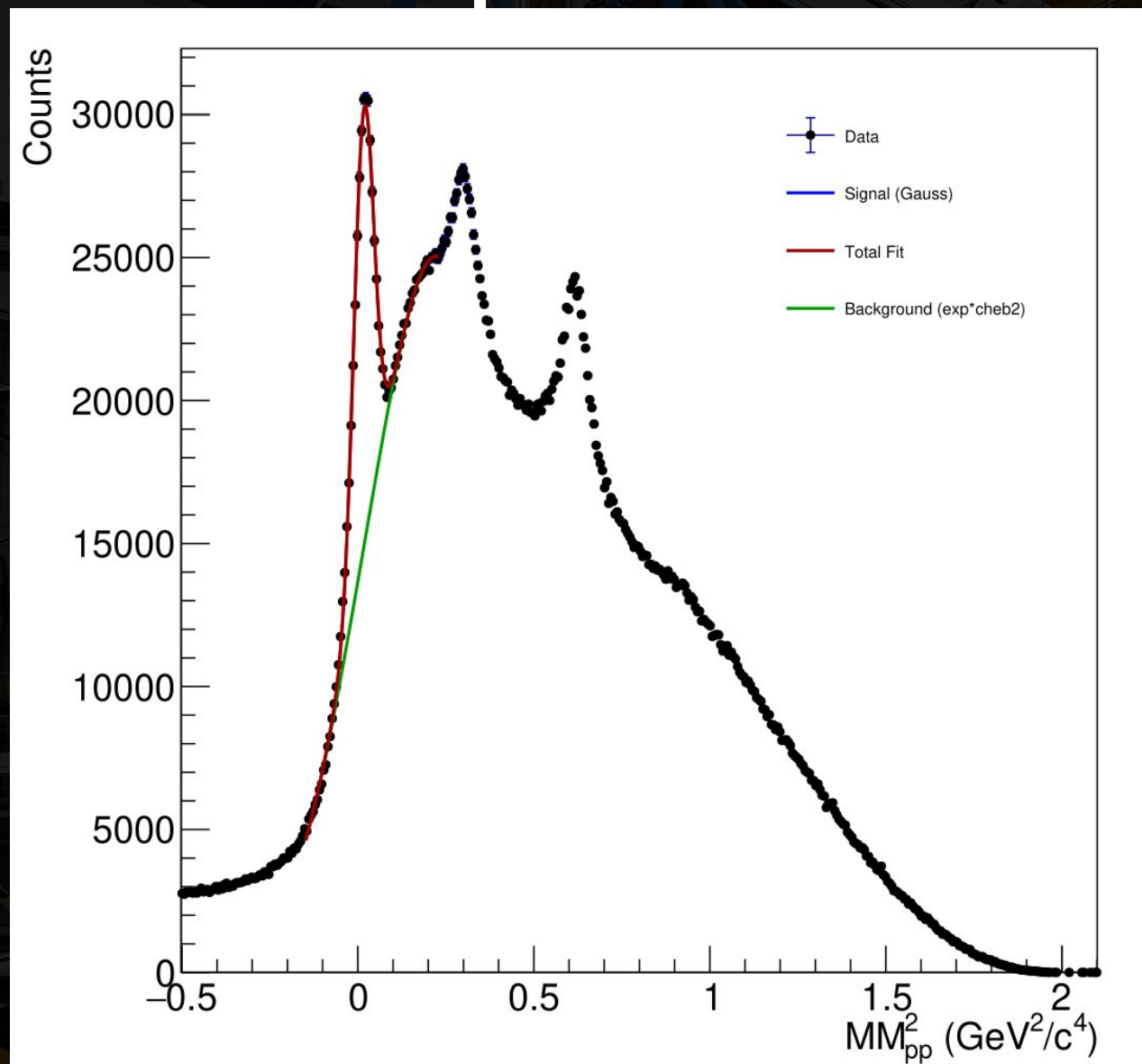
Comparison to Transport Model



$p\eta\pi^+$

SMASH^[6]

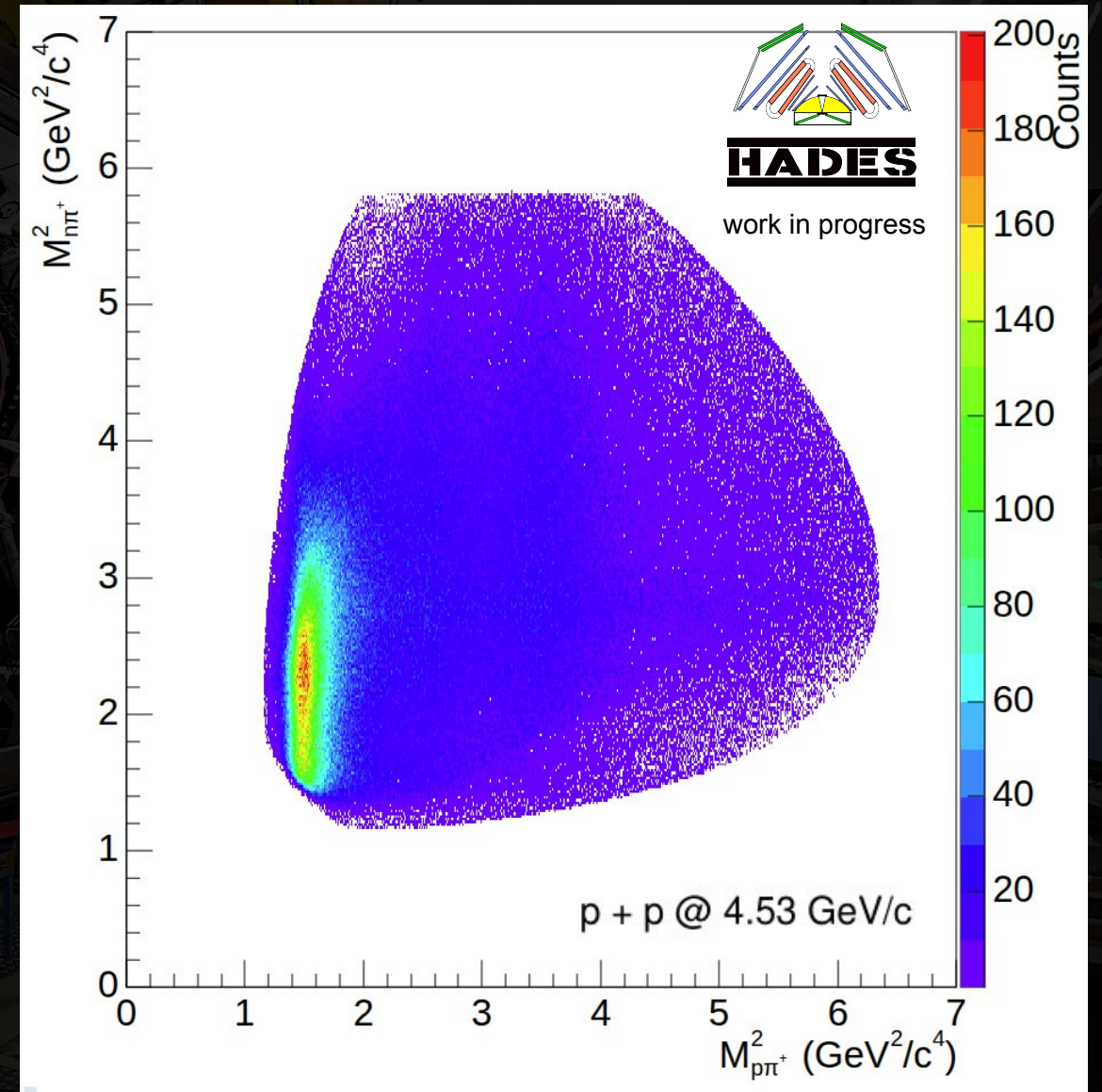
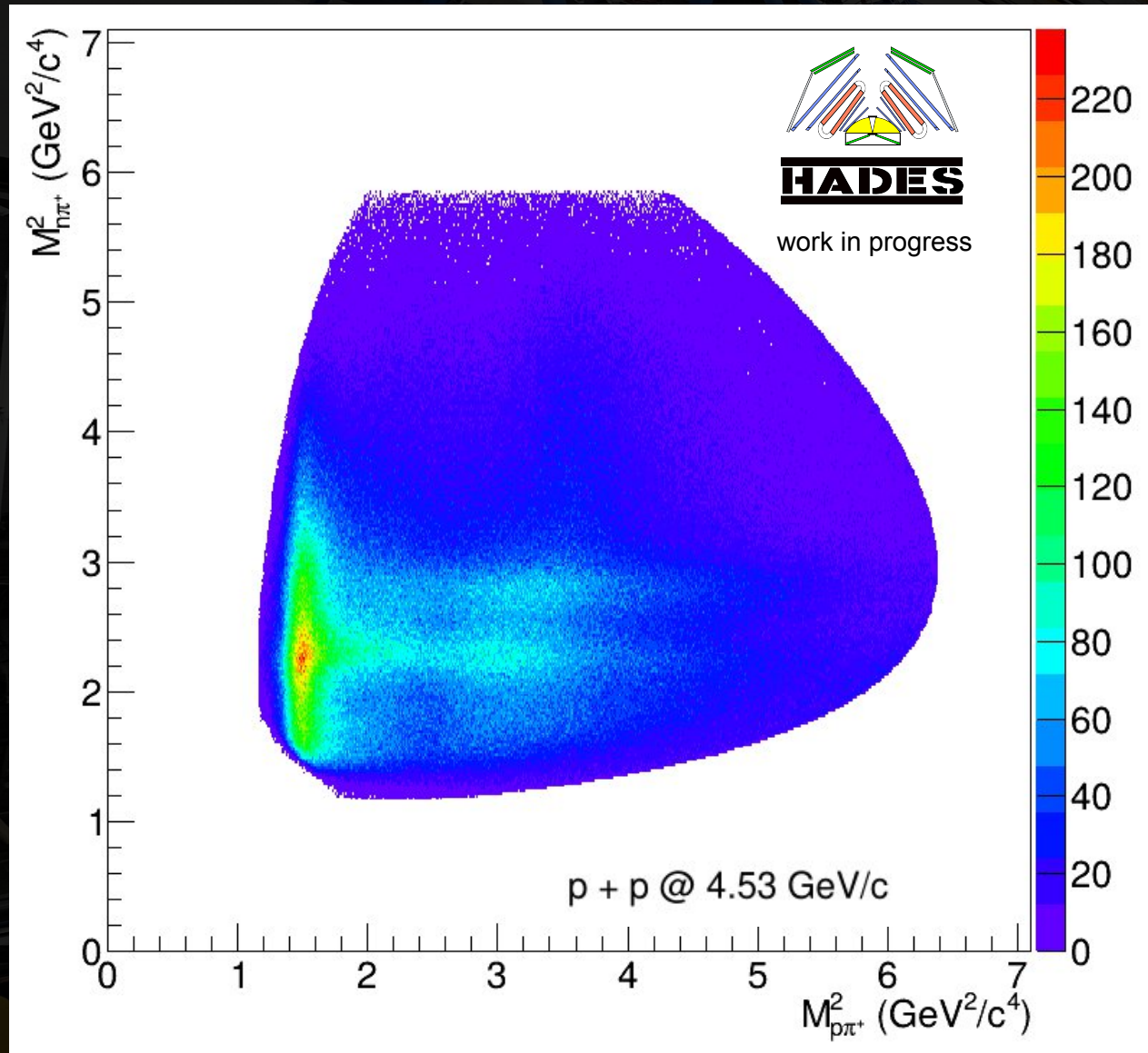
Comparison to Transport Model



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Comparison to Transport Models

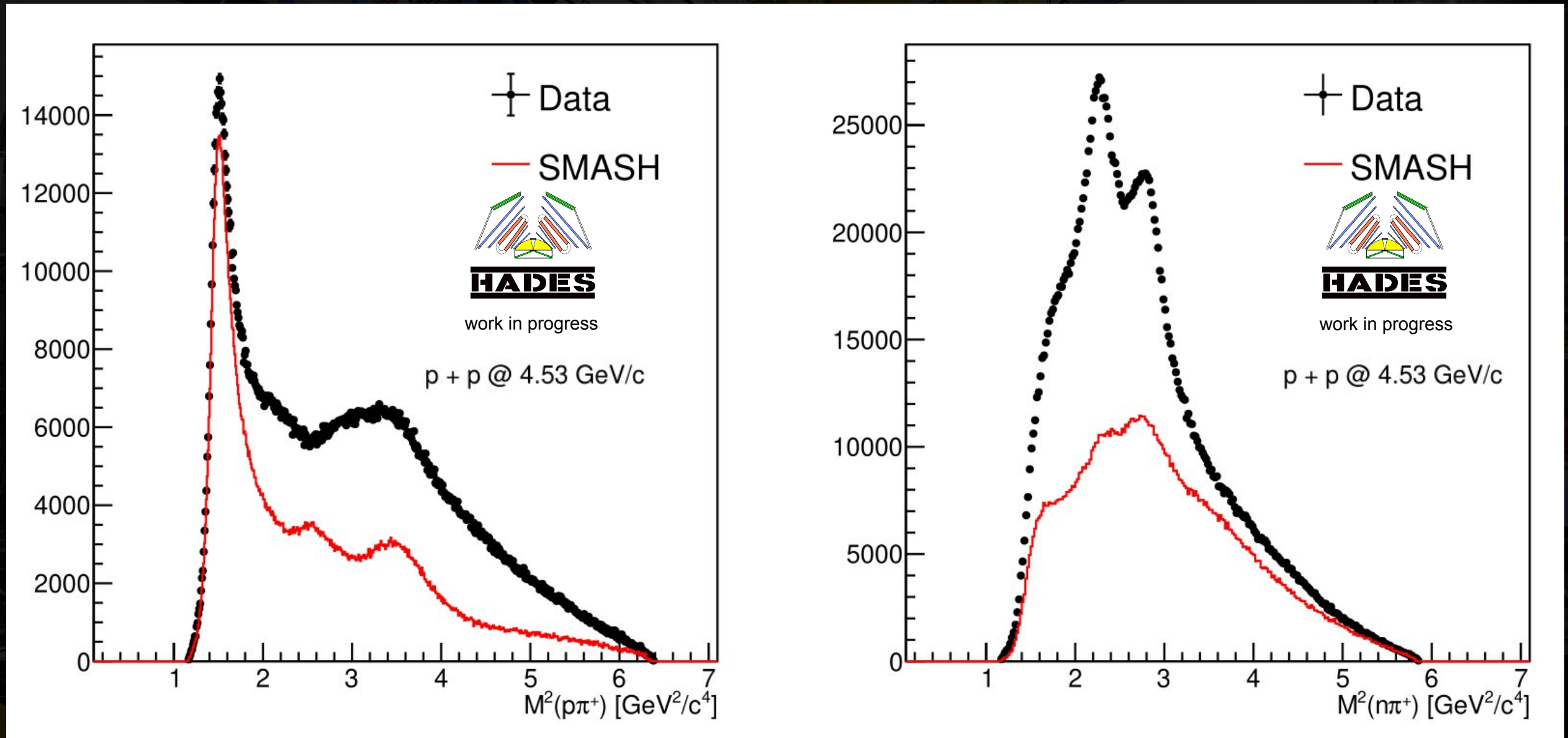


Data

$p\eta\pi^+$

SMASH^[6]

Comparison to Transport Models

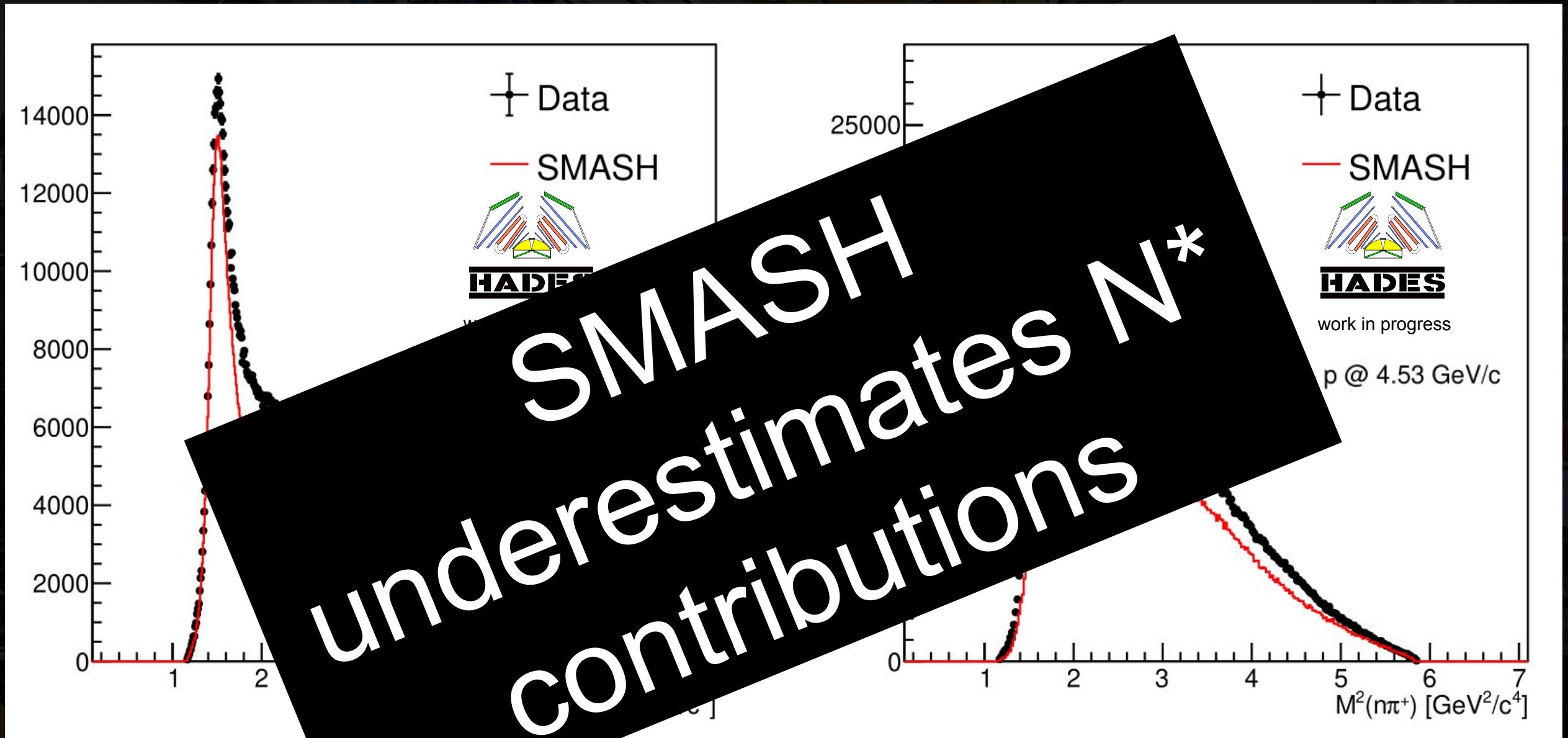


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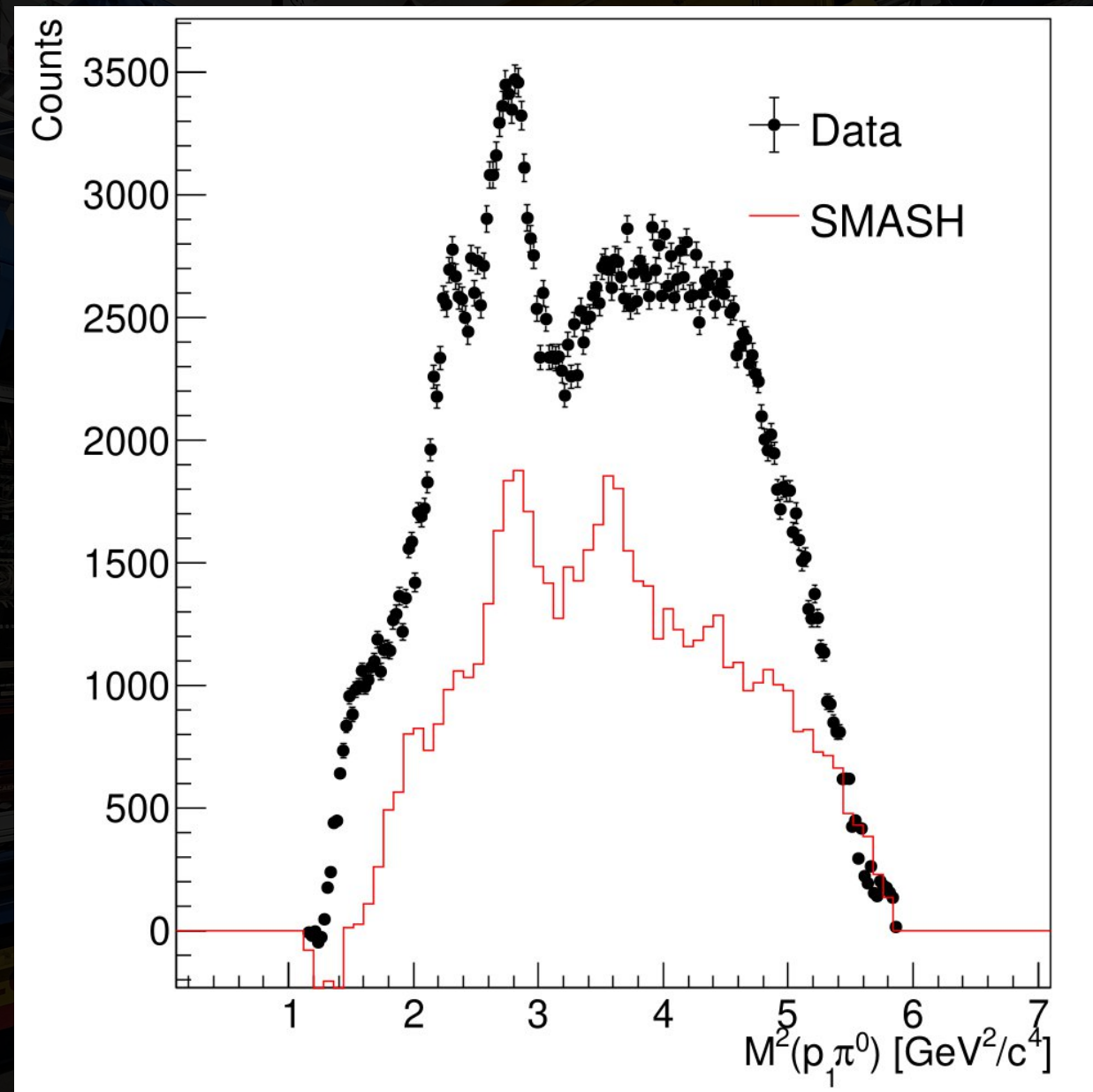
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$pn\pi^+$

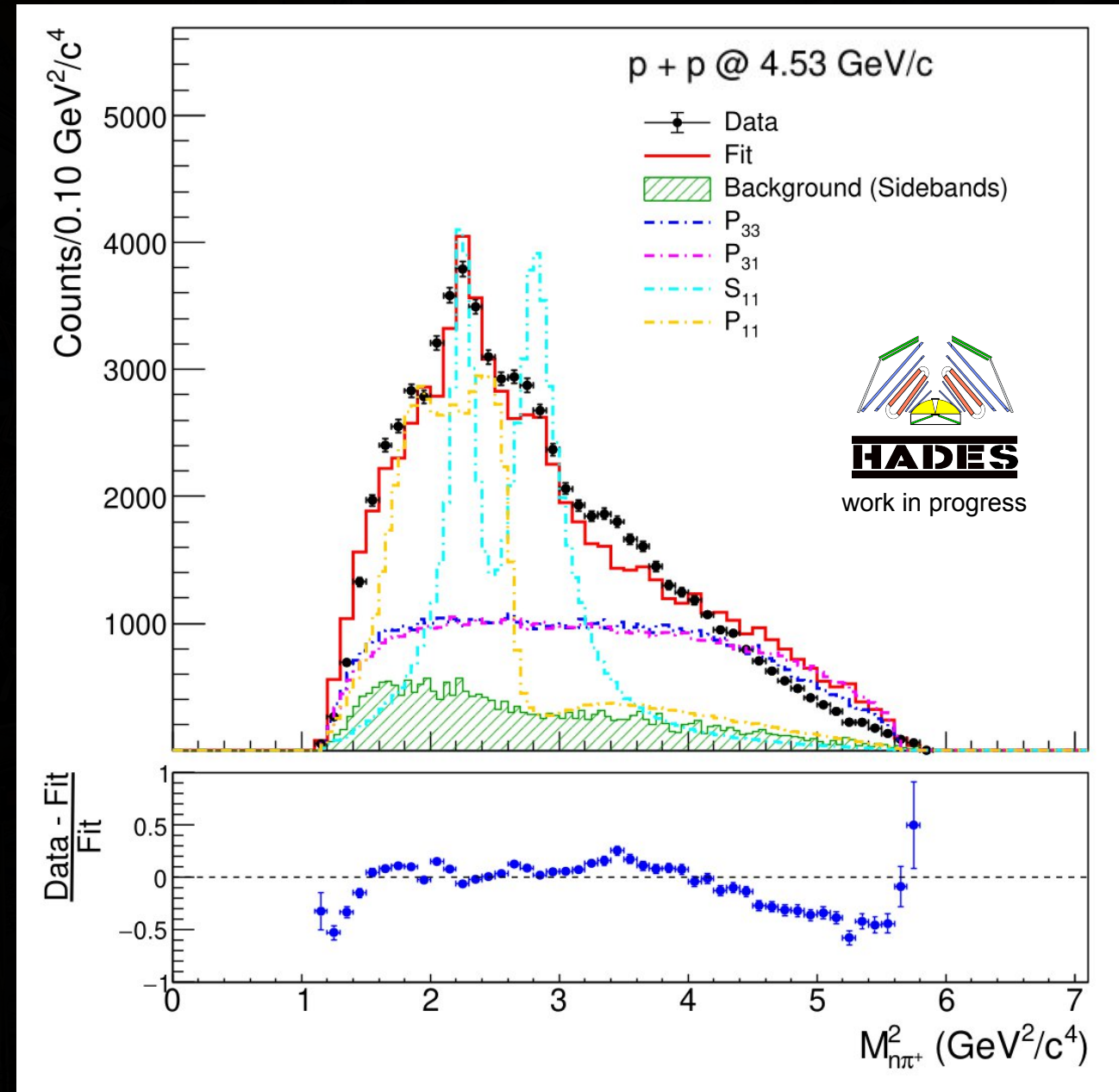
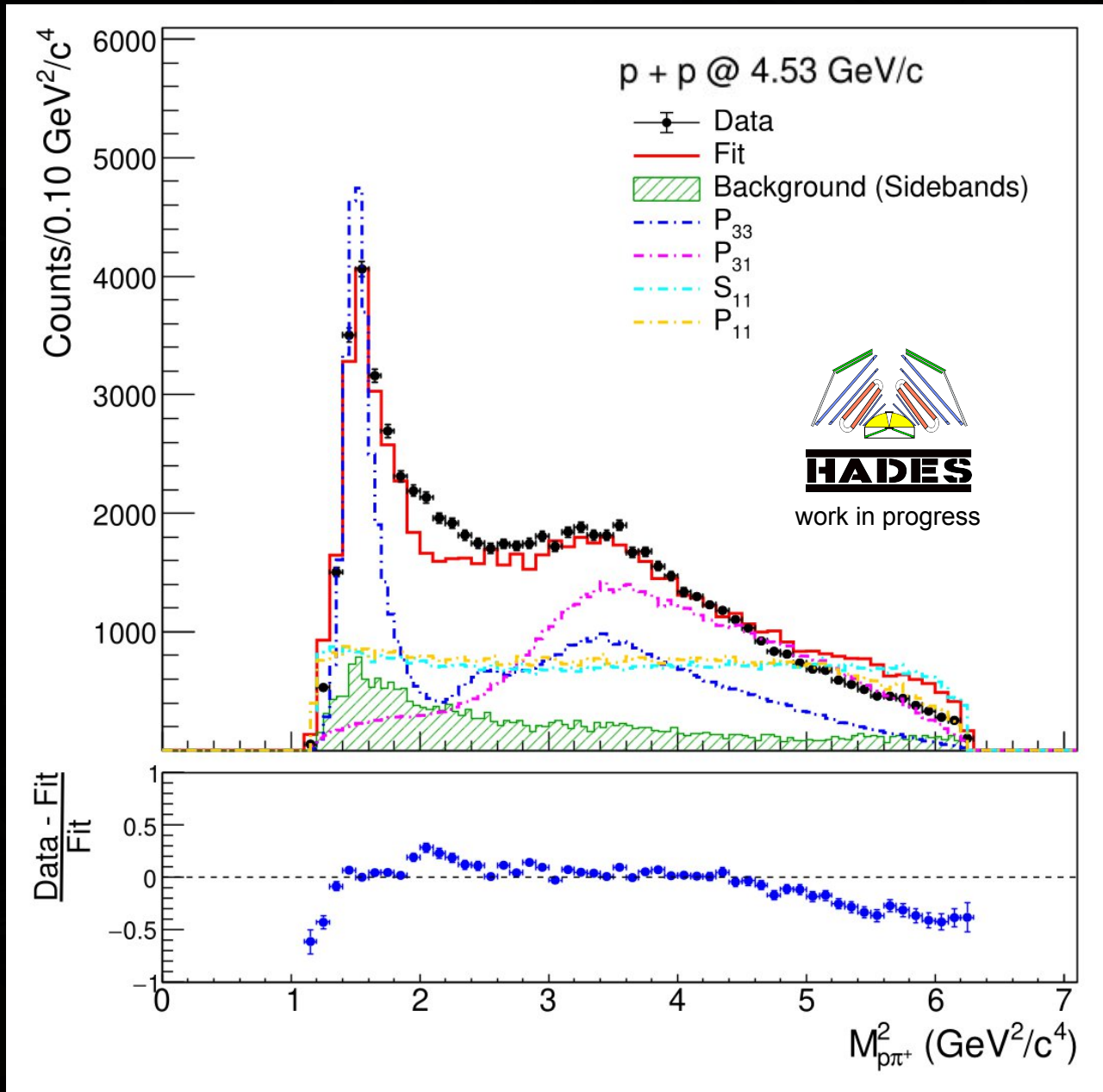
SMASH^[6]

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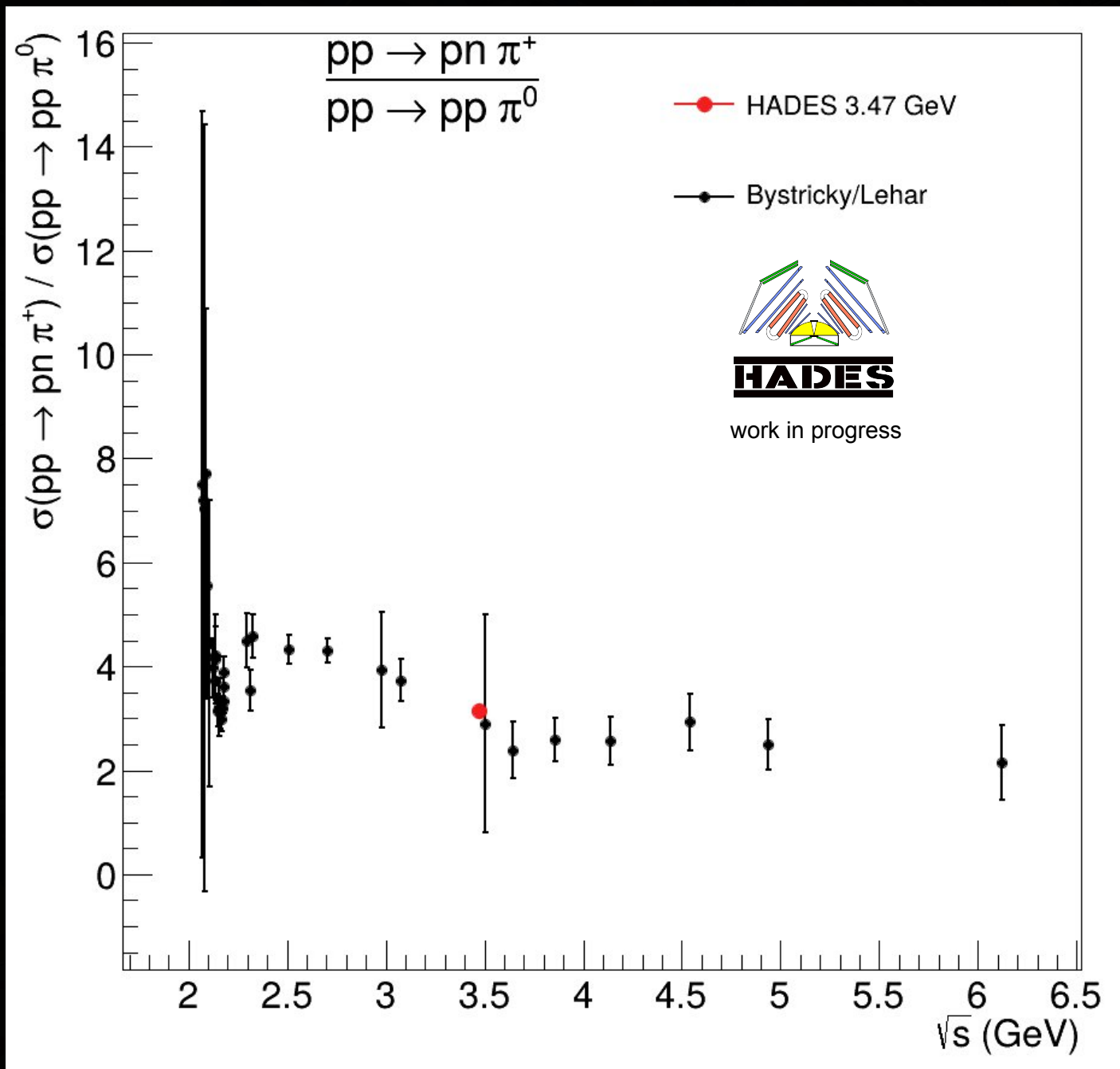
$pp\pi^0$

Preliminary JüBo Fit Results



Fit Result (P_{33}, P_{31}, S_{11} and P_{11})

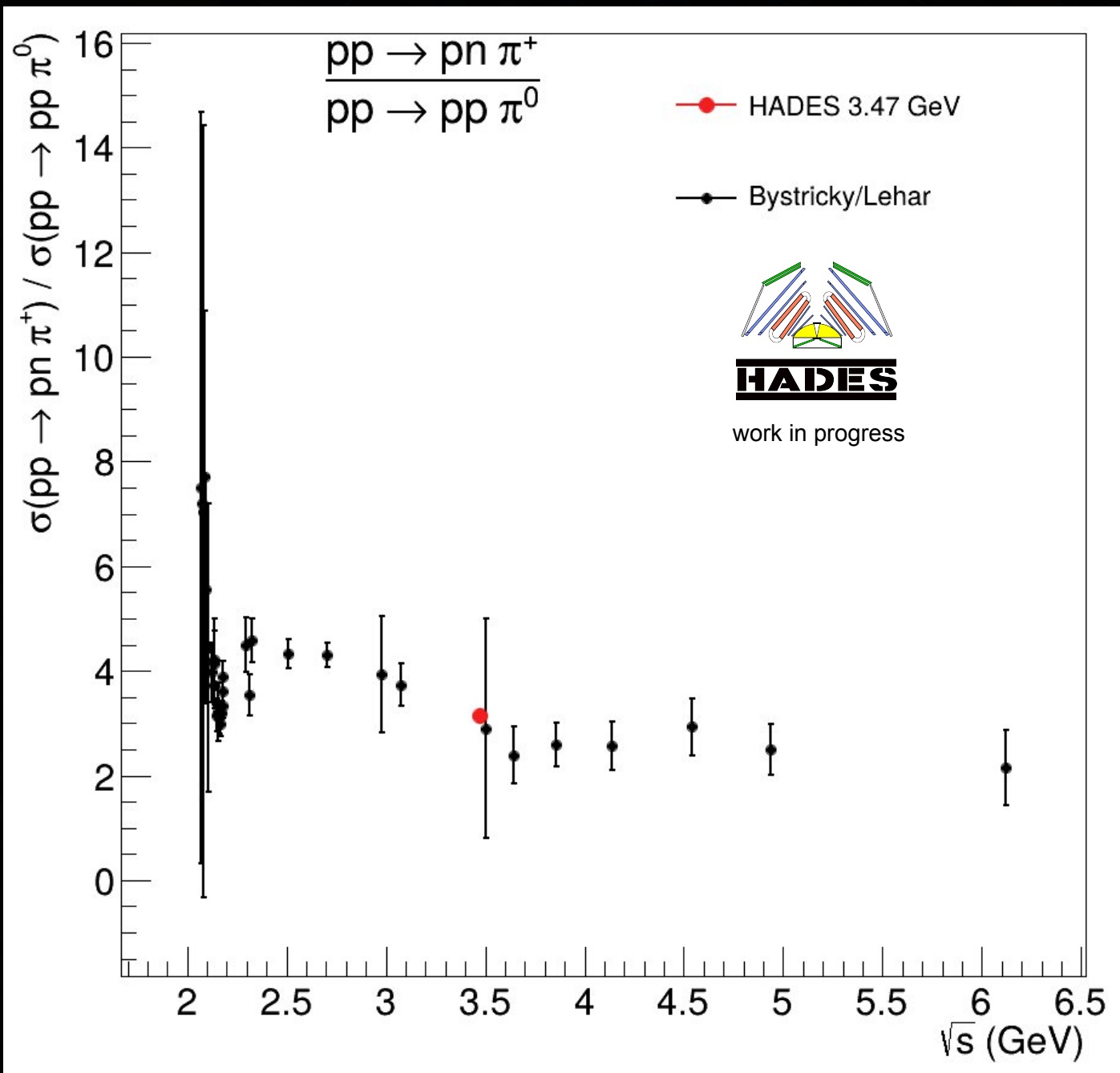
$$\frac{\sigma(pp \rightarrow pn\pi^+)}{\sigma(pp \rightarrow pp\pi^0)}$$



Efficiency Correction based on
 $F(M_{p\pi^+}^2), F(M_{n\pi^+}^2), \cos(\theta_n^{cm}), \phi_{plane}^{cm}$

$$\sigma(pp \rightarrow pn\pi^+)$$

$$\sigma(pp \rightarrow pp\pi^0)$$



$$\frac{\sigma(pp \rightarrow pn \pi^+)}{\sigma(pp \rightarrow pp \pi^0)} = 3.1 \pm 0.005 \text{ (stat)}$$

The decreasing cross-section ratio reflects the transition from $\Delta(1232)$ -dominated pion production to increasing contributions from higher-mass baryon resonances.

Conclusion and Outlook

- The data provides valuable constraints for improving the implementation of baryon-resonance dynamics in transport models such as SMASH.
- Preliminary fit to the $pp \rightarrow pn\pi^+$ case shows the coupled channel machinery works.
- A good benchmark case to validate this machinery and assess whether it can be used to compute the FSI for other channels involving $K\Lambda$ and $K\Sigma$.
- Once the fit for $pp \rightarrow pn\pi^+$ case is finalised, quantify the different MB contribution.
- Also do a combined fit of the $pp \rightarrow pn\pi^+$ and $pp \rightarrow pp\pi^0$ channels.
- Extract cross-sections for $pp \rightarrow pn\pi^+$ and $pp \rightarrow pp\pi^0$ channels

Conclusion and Outlook

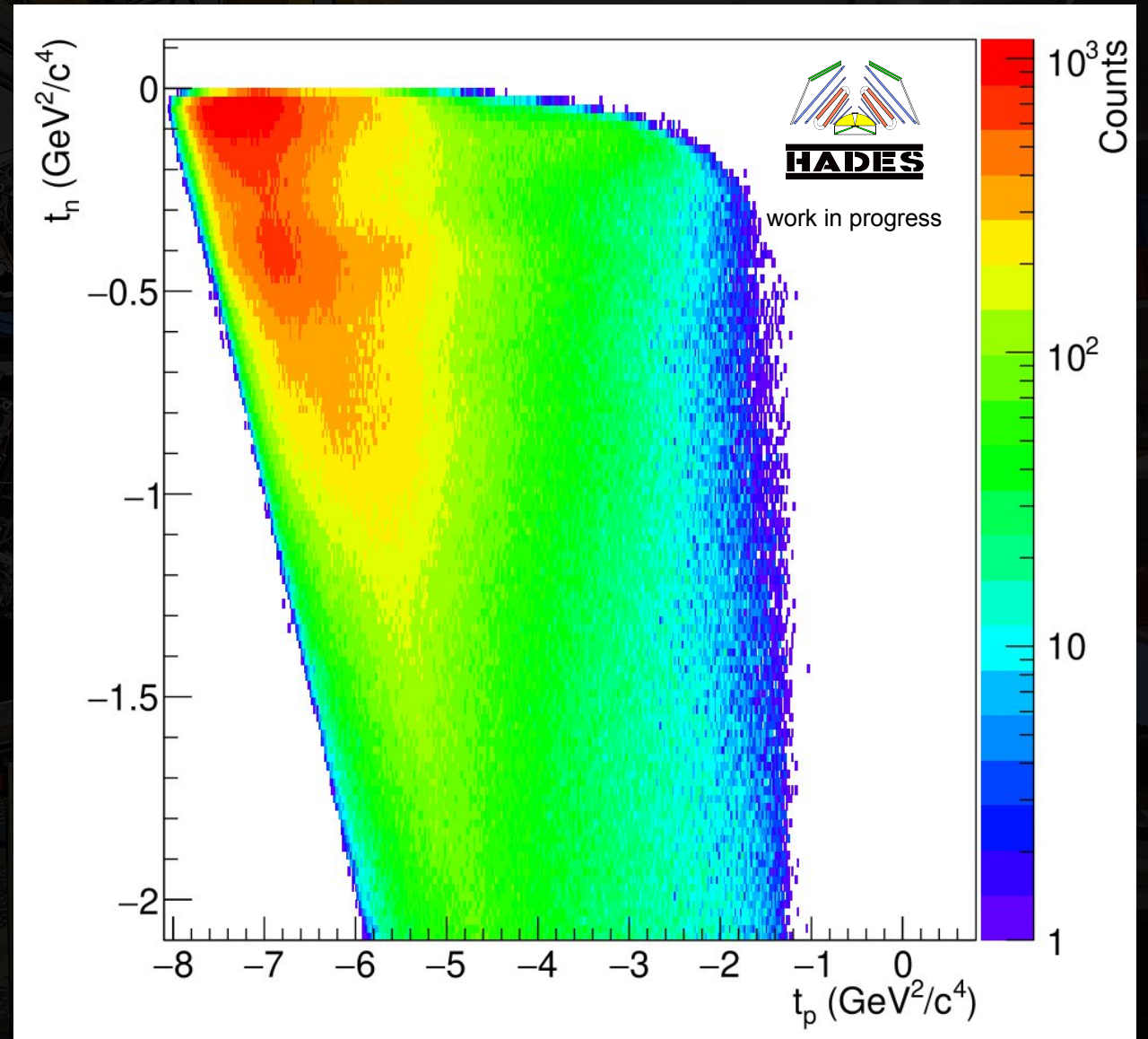
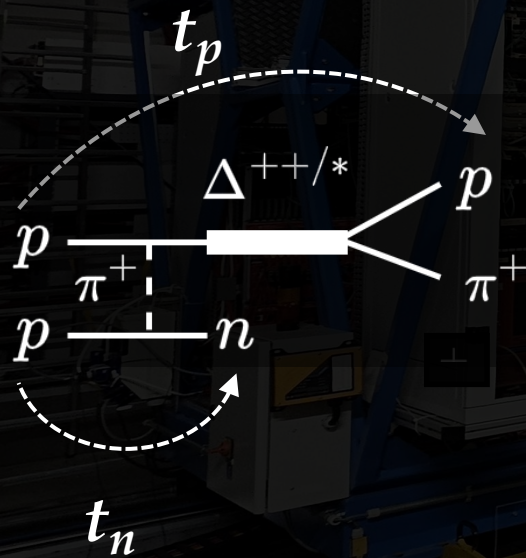
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Δ Thank You Δ

t_p vs t_n

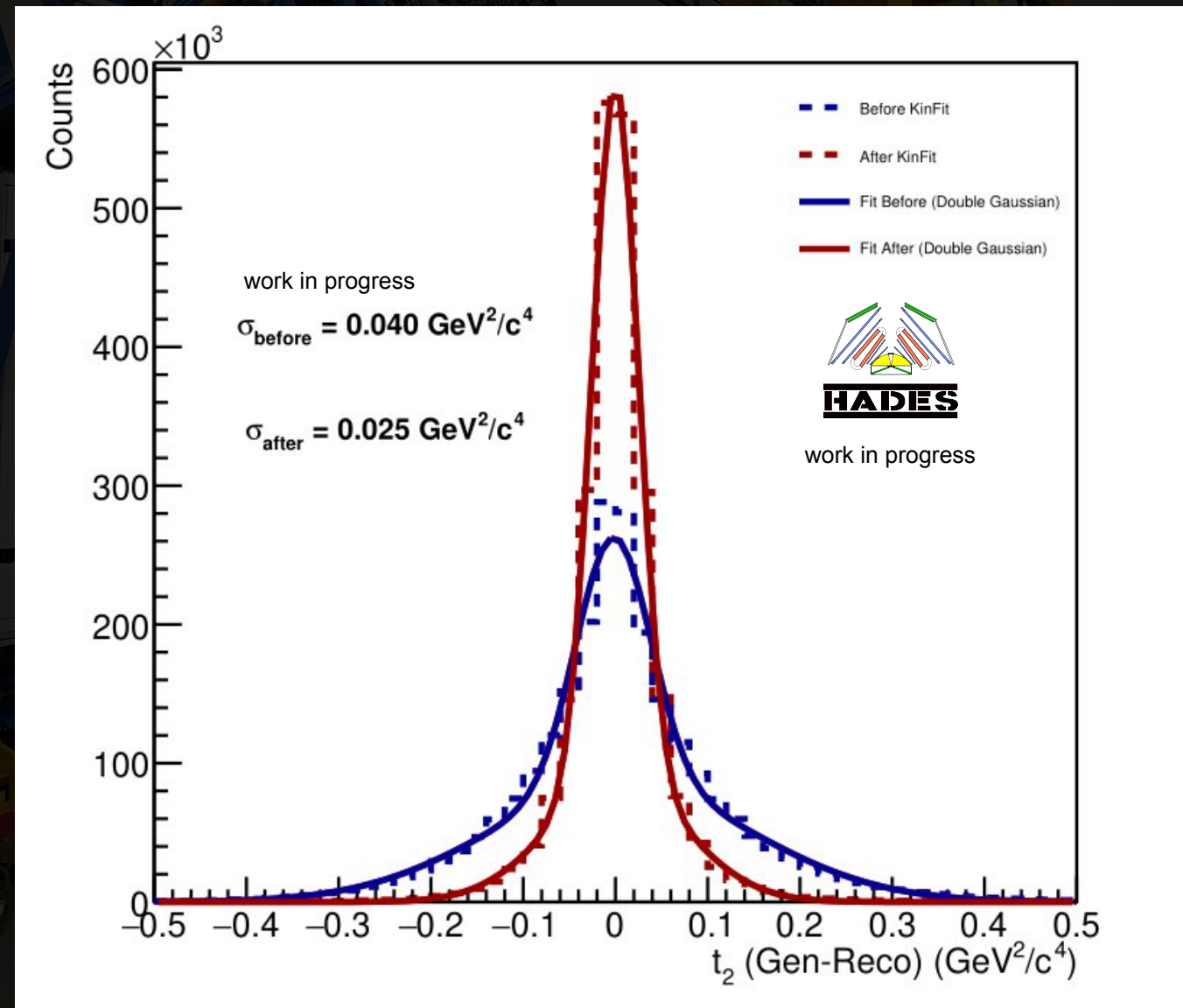
$$t_p = (p_{\text{beam}} - p_{\text{proton}})^2$$

$$t_n = (p_{\text{beam}} - p_{\text{neutron}})^2$$



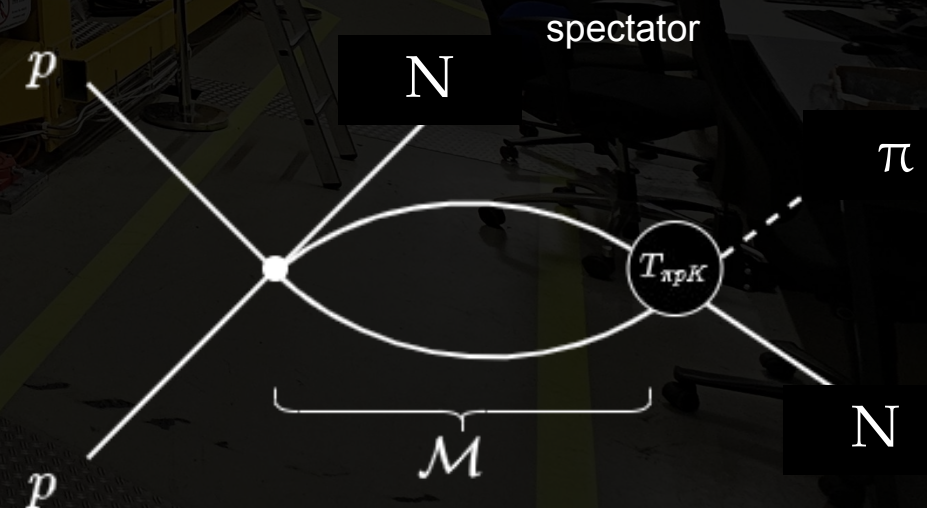
t Resolutions

$$t_2 = (p_{beam} - p_{neutron})^2$$



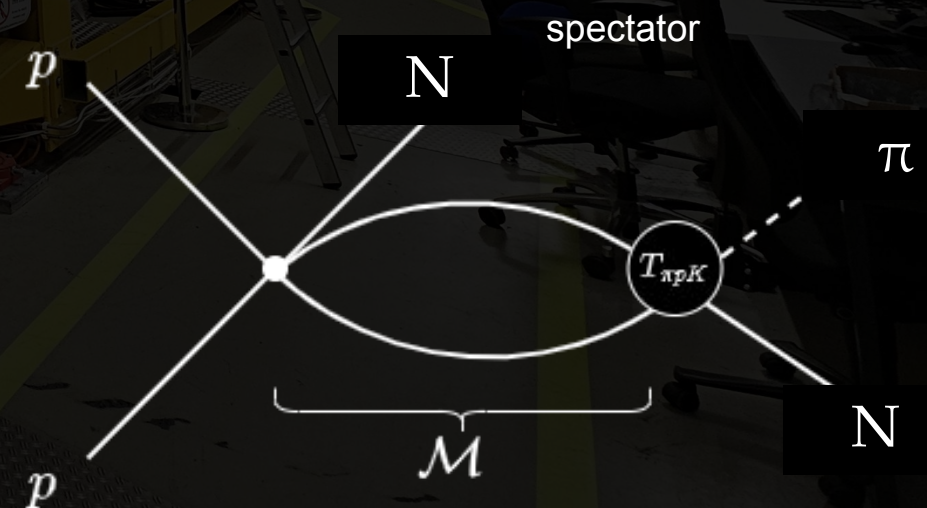
$pp \rightarrow pn\pi^+$ with Jülich-Bonn Dynamic Coupled Channel Approach

- Dynamical Coupled Channel (DCC) ^[2] approach : simultaneous analysis of different reactions.
- Allows for extracting the coupling strength of the resonances to final states.



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- \mathcal{M} is the invariant matrix element for calculating the invariant mass distribution and $T_{\pi p K}$ is the full JüBo T-Matrix for different channels ($K \rightarrow \pi N$), includes s-channel and dynamically generated resonances.



$pp \rightarrow pn\pi^+$ with Jülich-Bonn Dynamic Coupled Channel Approach

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- Allows for extracting the coupling strength of the resonances to final states.
- \mathcal{M} is the invariant matrix element for calculating the invariant mass distribution and $T_{\pi p K}$ is the full JüBo T-Matrix for different channels ($K \rightarrow \pi N$), includes s-channel and dynamically generated resonances.

$$\mathcal{M}_{\mu\nu}(q, p', \epsilon) = V_{\mu\nu}(q, p', \epsilon) + \sum_{\hat{K}} \int_0^{\infty} dp p^2 T_{\mu\hat{K}}(q, p, \epsilon) G_{\hat{K}}(p, \epsilon) V_{\hat{K}\nu}(p, p', \epsilon)$$

Kernel which contains the coupling information of the resonances to the final state

all possible meson baryon channels

ϵ - C.M energy of $pp \rightarrow pn\pi^+$

- MB \rightarrow MB interactions (e.g. FSI) are incorporated by Jülich-Bonn model (fitted through lots of data) within SU(3) dynamics.

$pp \rightarrow pn\pi^+$ with Jülich-Bonn Dynamic Coupled Channel Approach

- Dynamical Coupled Channel (DCC) [2] approach : simultaneous analysis of different reactions.
- Allows for extracting the coupling strengths to all final states.

- \mathcal{M} is the invariant matrix element for the transition from initial state to final state. It includes s-channel meson exchange (e.g. $K \rightarrow \pi N$), t-channel meson exchange (e.g. $K \rightarrow \pi N$), and u-channel meson exchange (e.g. $K \rightarrow \pi N$).

Can we decouple final-state interactions from the production mechanism?

$$\mathcal{M}_{\mu\nu}(p, p', \epsilon)$$

$$V_{K\nu}(p, p', \epsilon) G_K(p, \epsilon) V_{K\nu}(p, p', \epsilon)$$

all possible meson baryon channels

ϵ - C.M energy of $pp \rightarrow pn\pi^+$

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AmpTools – Framework for Amplitude Analysis

Purpose:

- Toolkit for performing Partial Wave Analysis (PWA)^[3].
- Fits complex amplitudes for exclusive reactions.

Key Features:

- Flexible physics model definitions (resonances, backgrounds).
- Coherent and incoherent amplitude combinations.
- Event-based maximum likelihood fitting.

$$-2 \ln \mathcal{L}(\theta) = -2 \left(\sum_{i=1}^N \ln I(x_i; \theta) - \int I(x; \theta) \eta(x) dx \right) + c_1$$

- GPU acceleration for fast computations.
- Interfaces with ROOT.

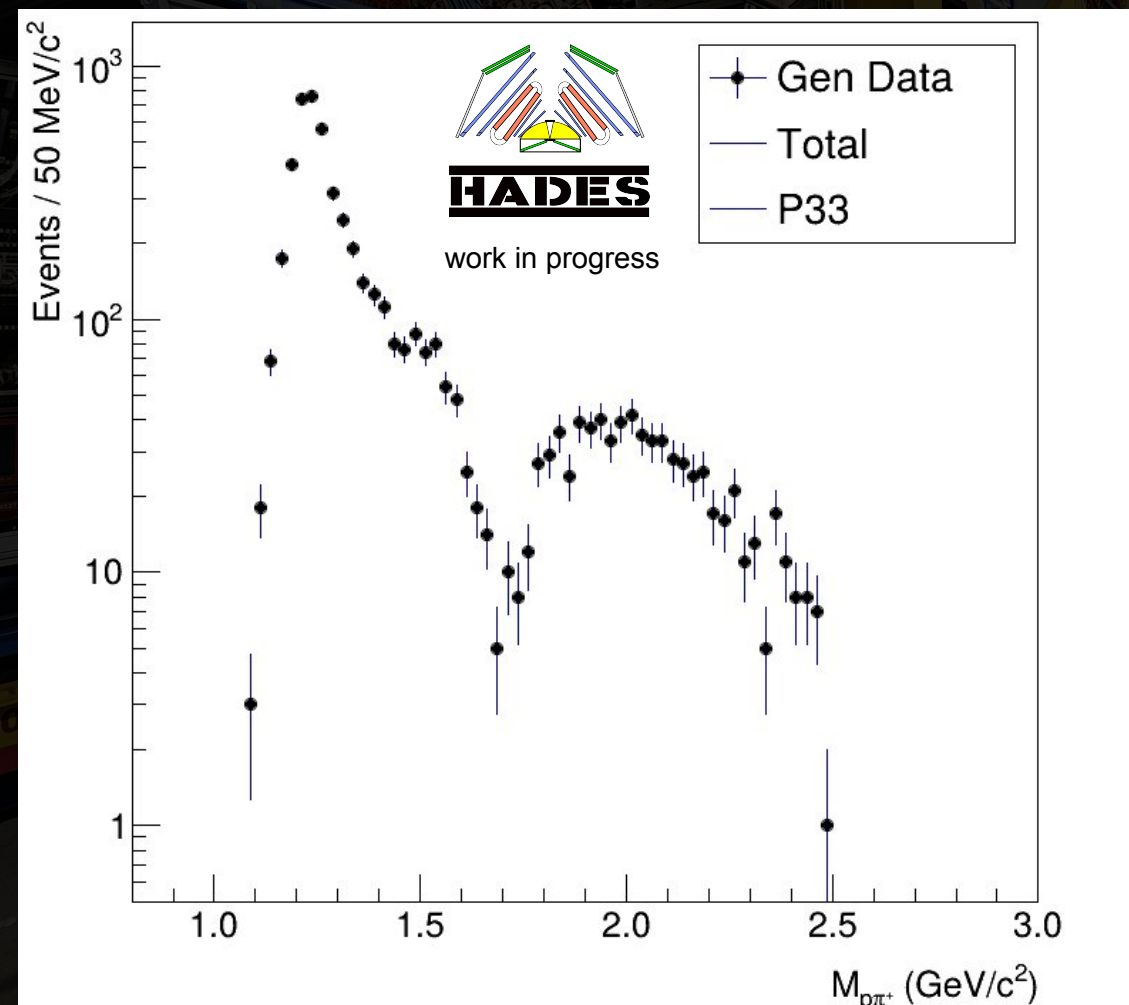
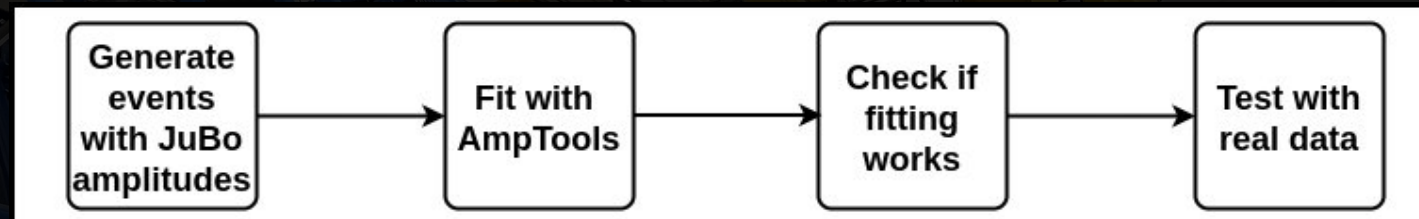
Normalization and Barrier Factors

- The amplitude is normalized and multiplied by a barrier factor:

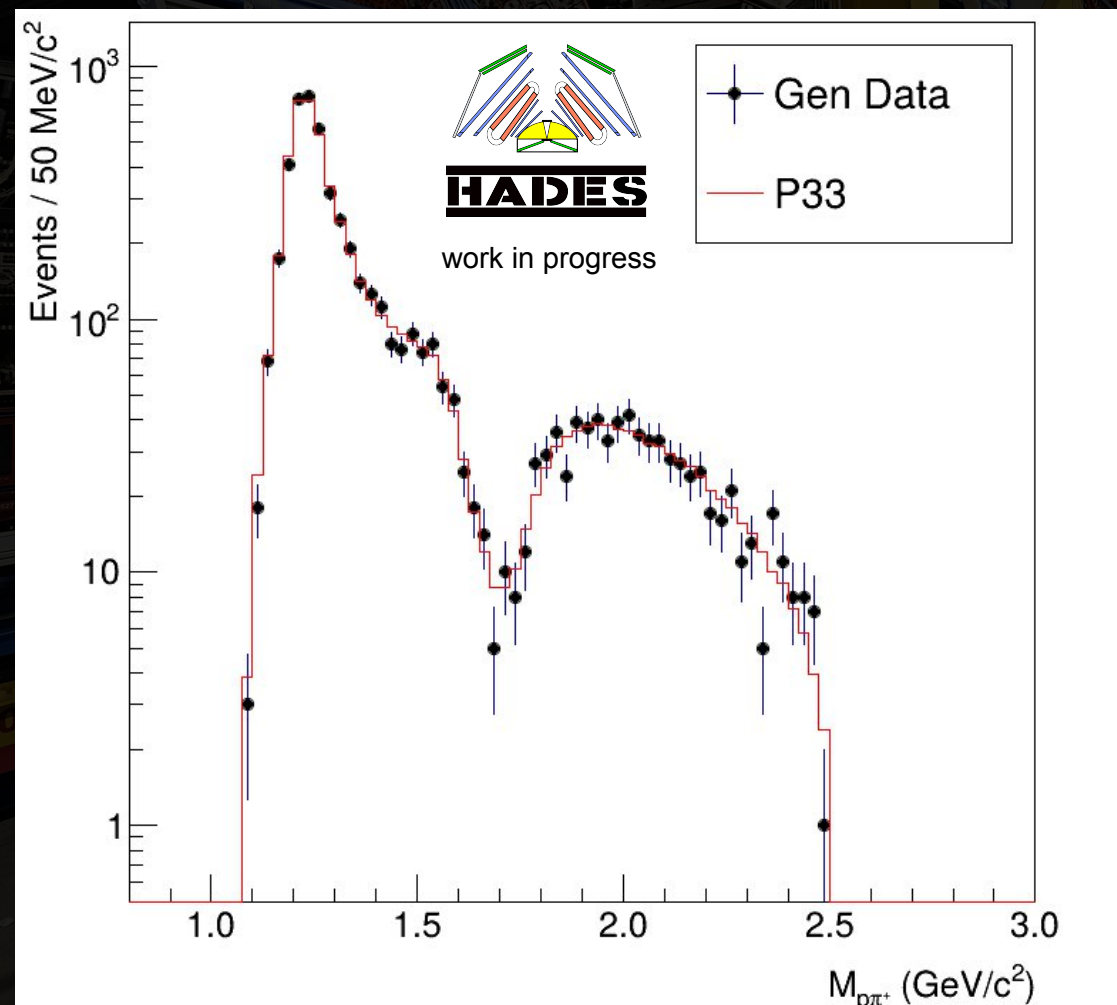
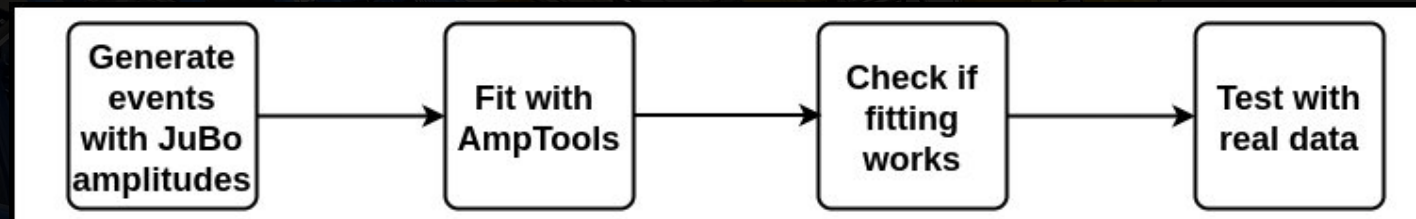
$$A_{JuBo}(L, I, J) = B_L(q) \sqrt{\frac{\rho(s, m_1, m_2) K_f}{K_i}} A_{L, I, J}(\alpha, \gamma)$$

- $B_L(q)$ is the Blatt-Weisskopf barrier factor for a spectator with the orbital angular momentum L .
- K_i, K_f are initial and final momenta in the CM frame.
- ρ is the Meson-Baryon phase space volume.

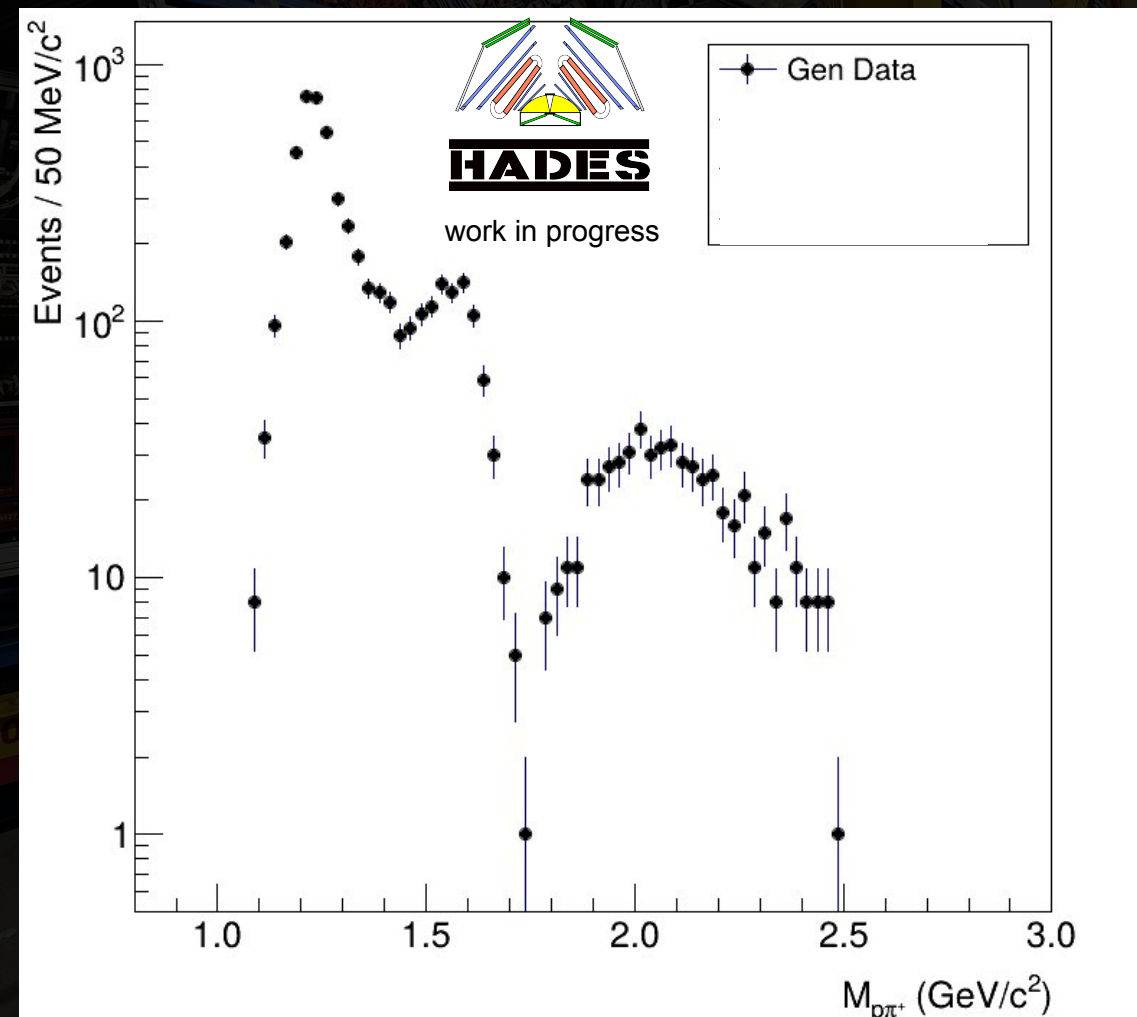
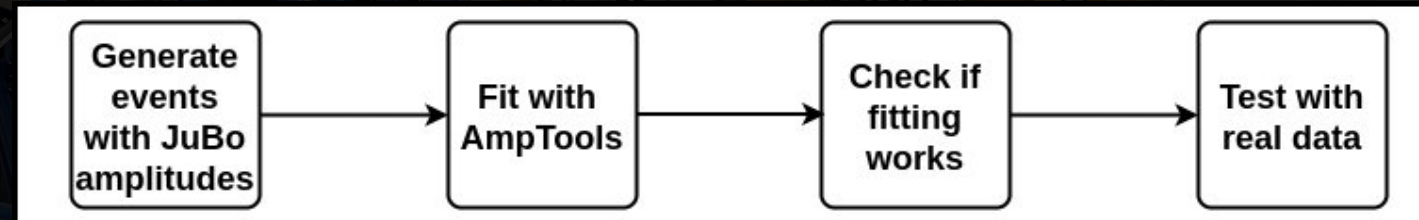
Testing the Machinery



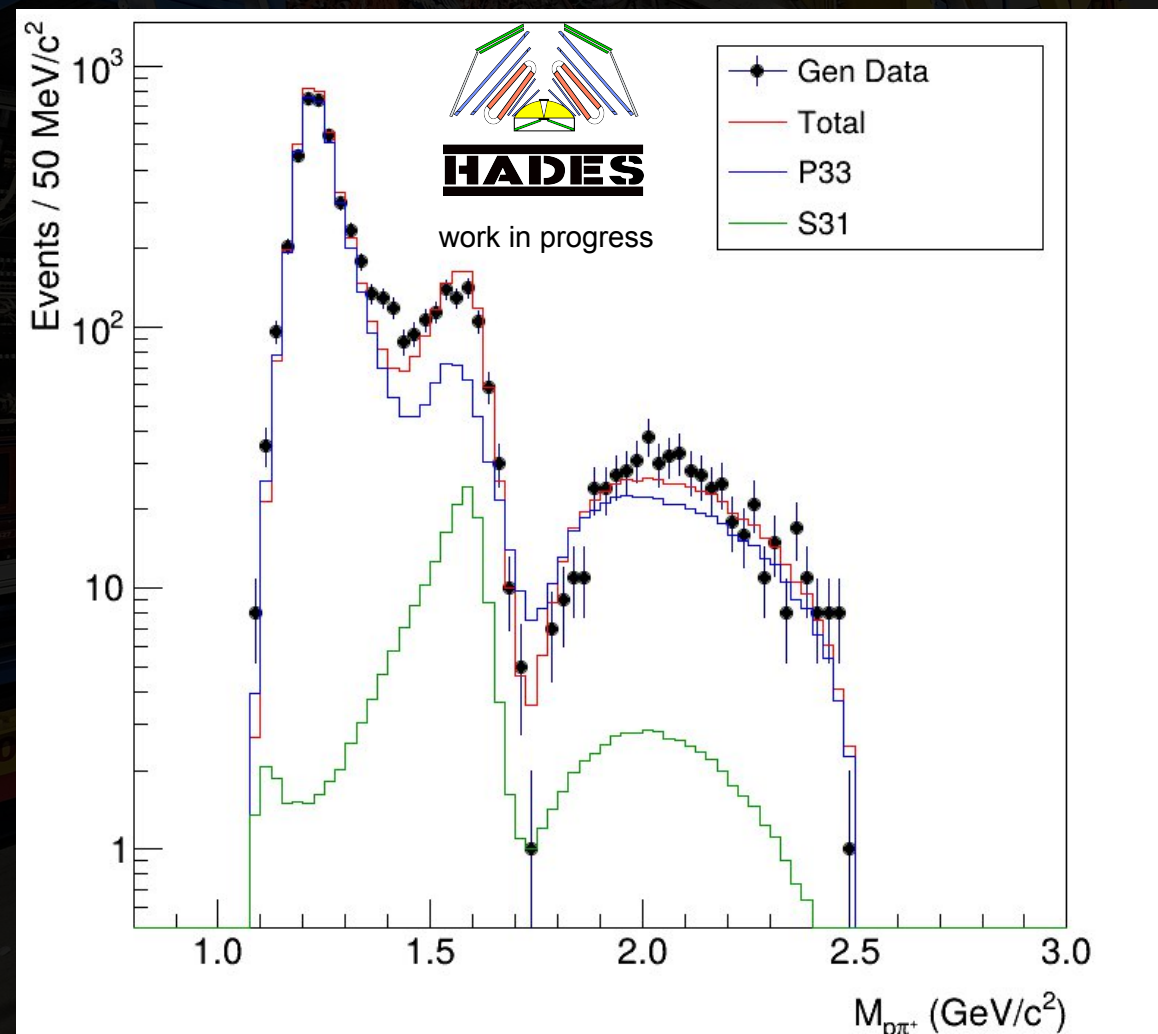
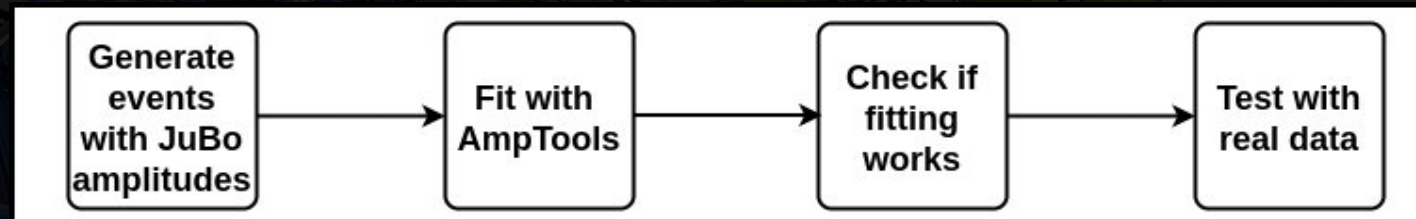
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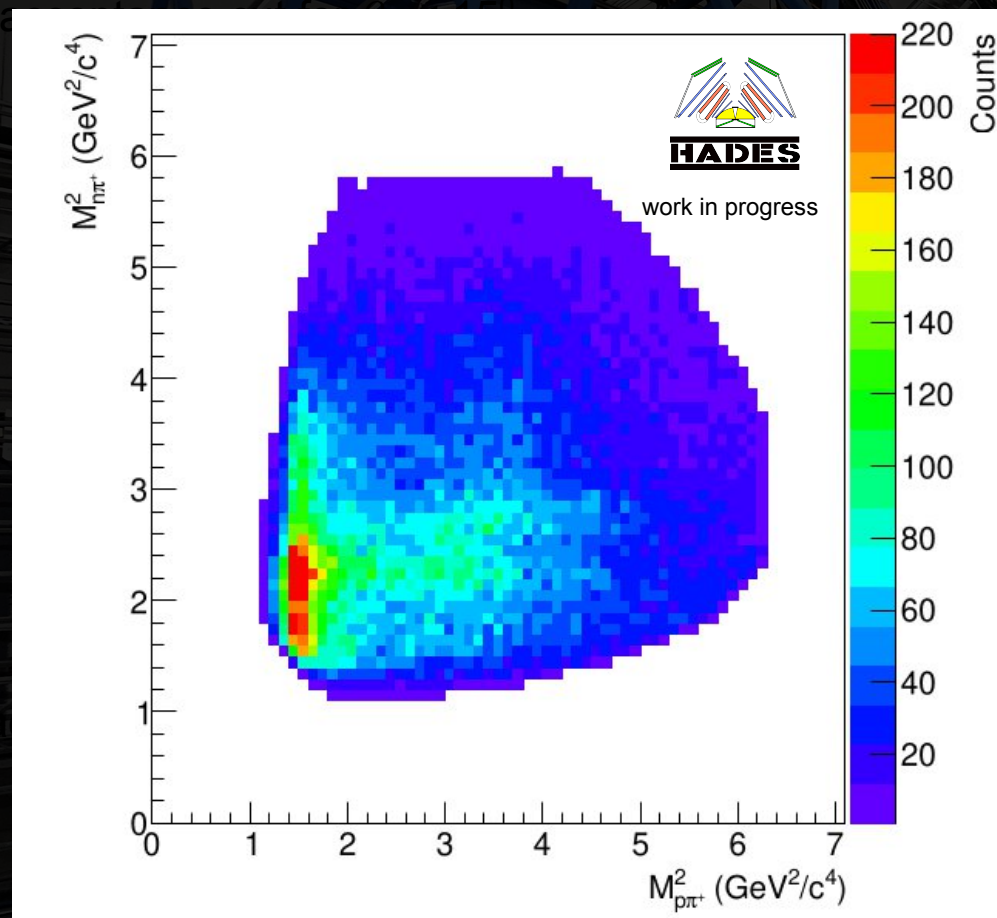
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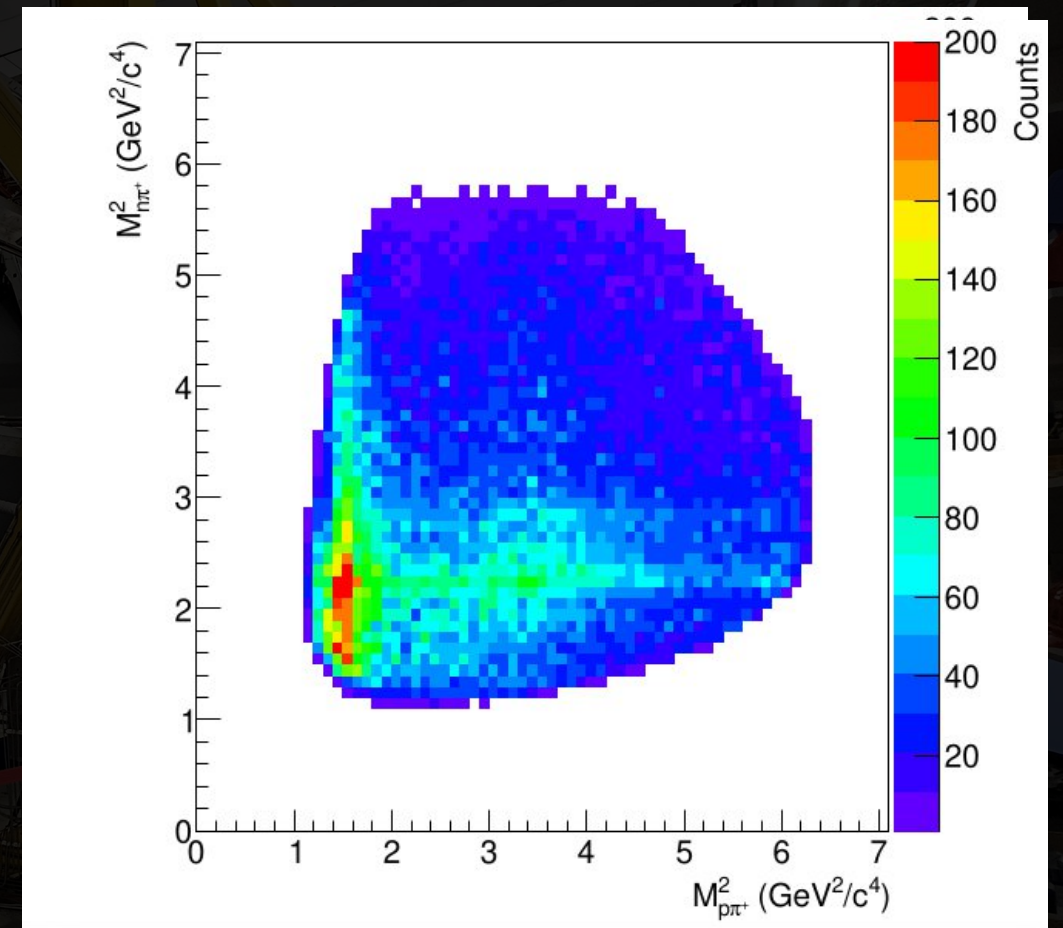
Testing the Machinery



Preliminary Fit Results

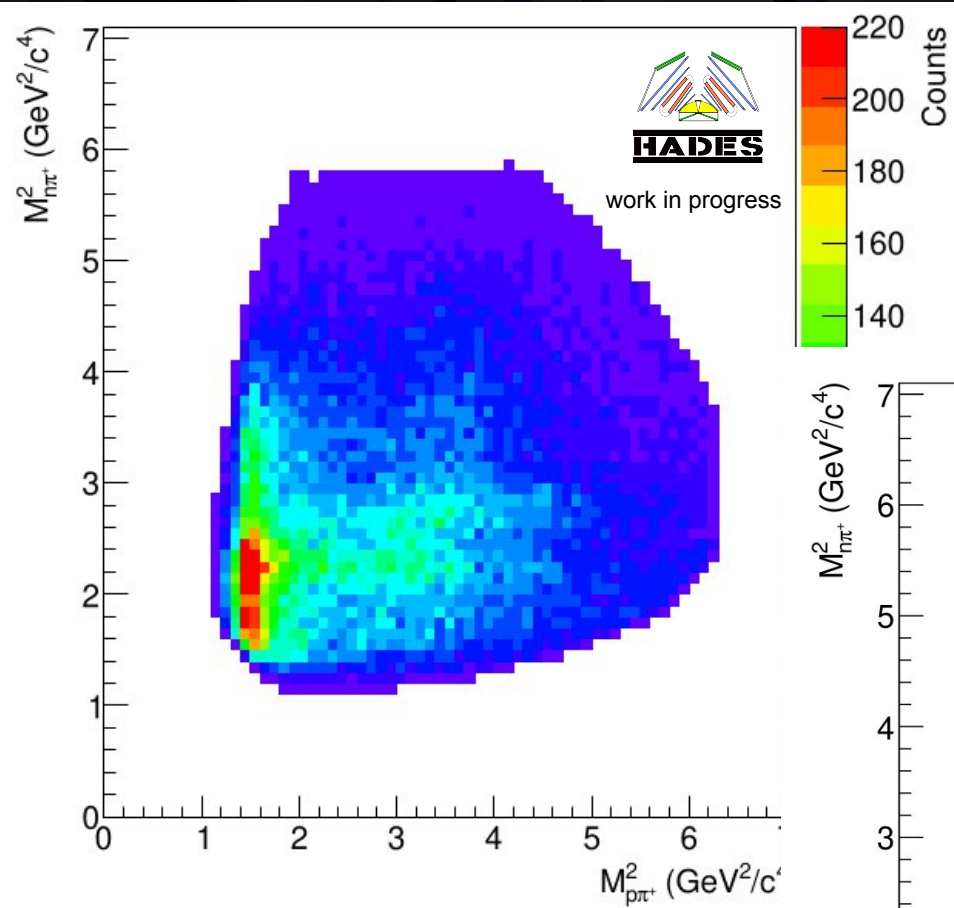


Data

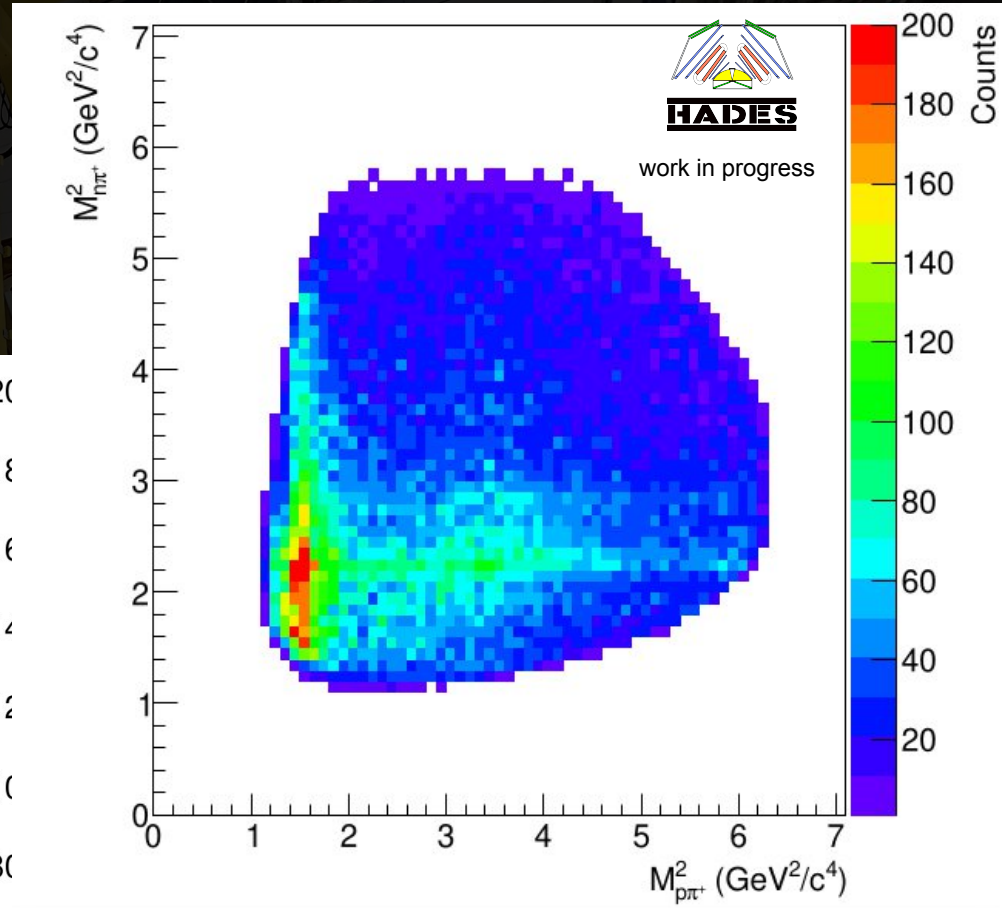
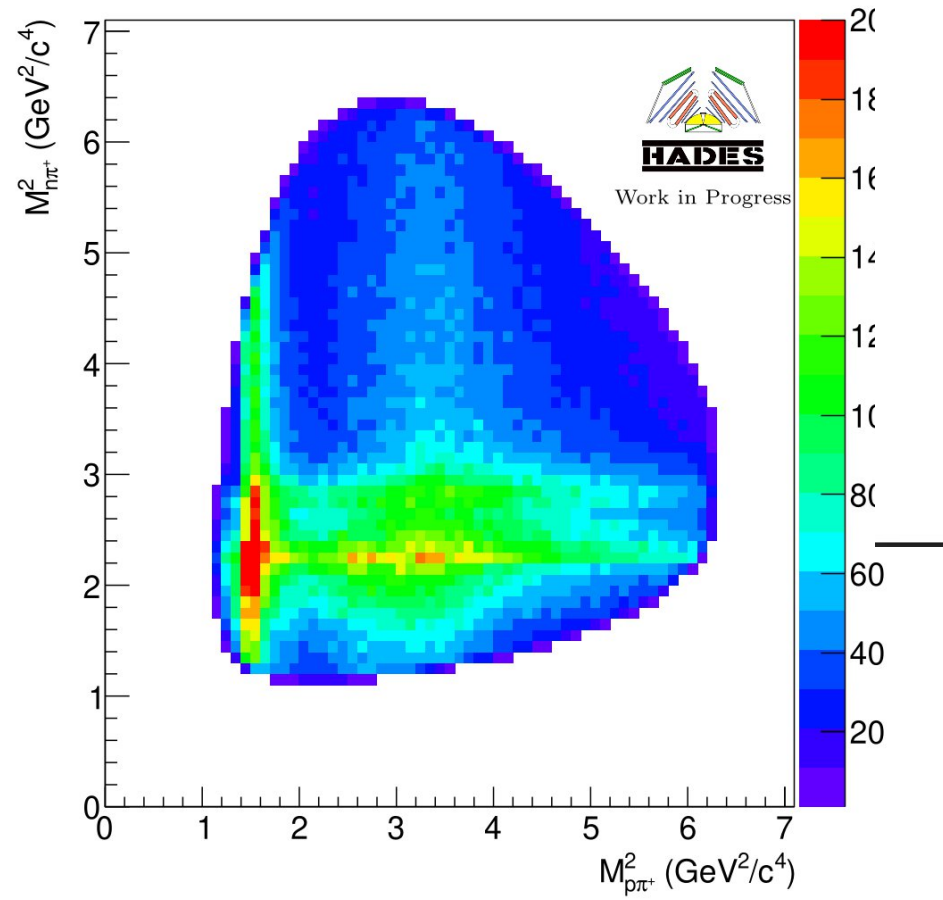


Fit Result (P33,P31,S11 and P11)

Preliminary Fit Results

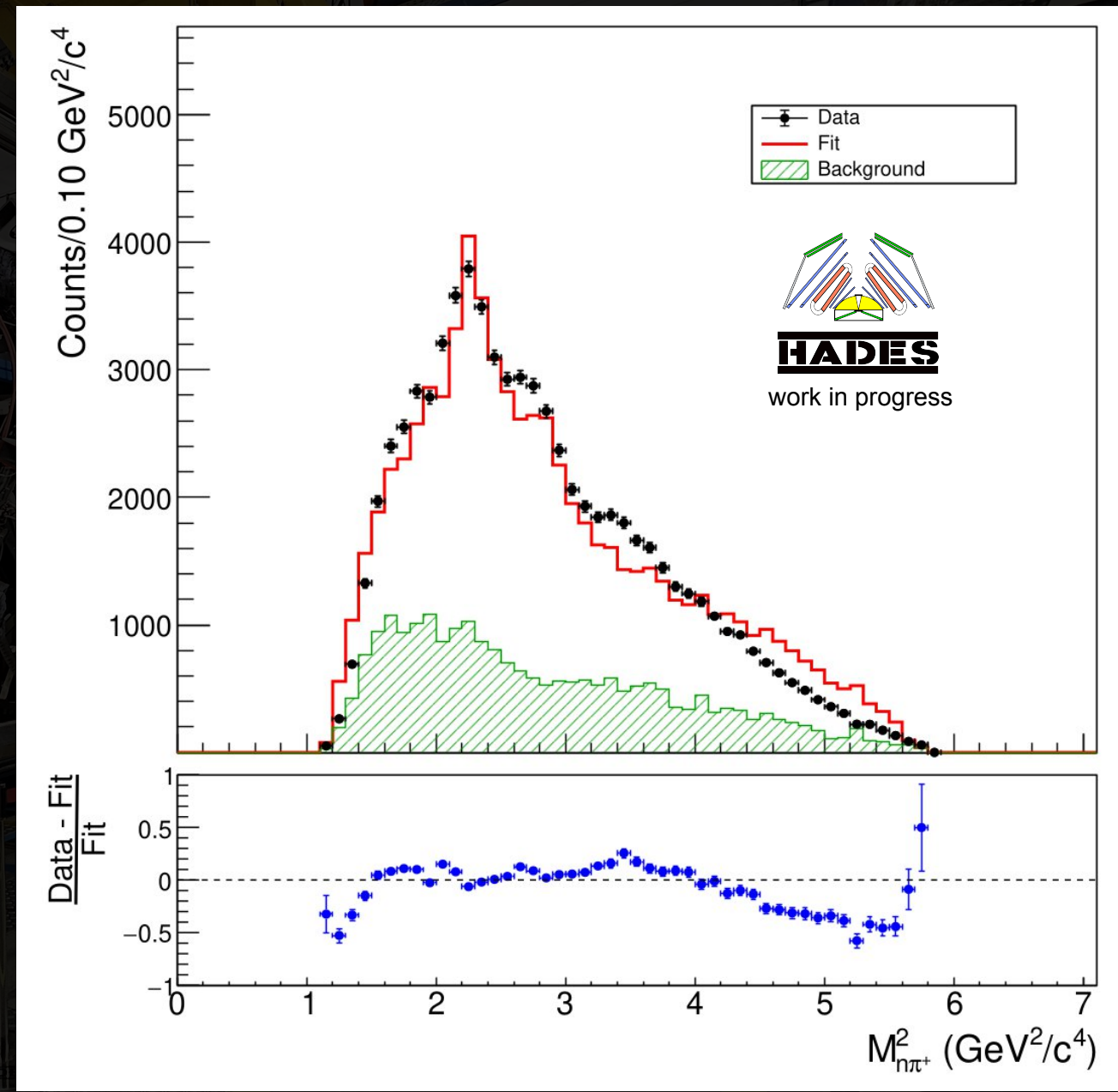
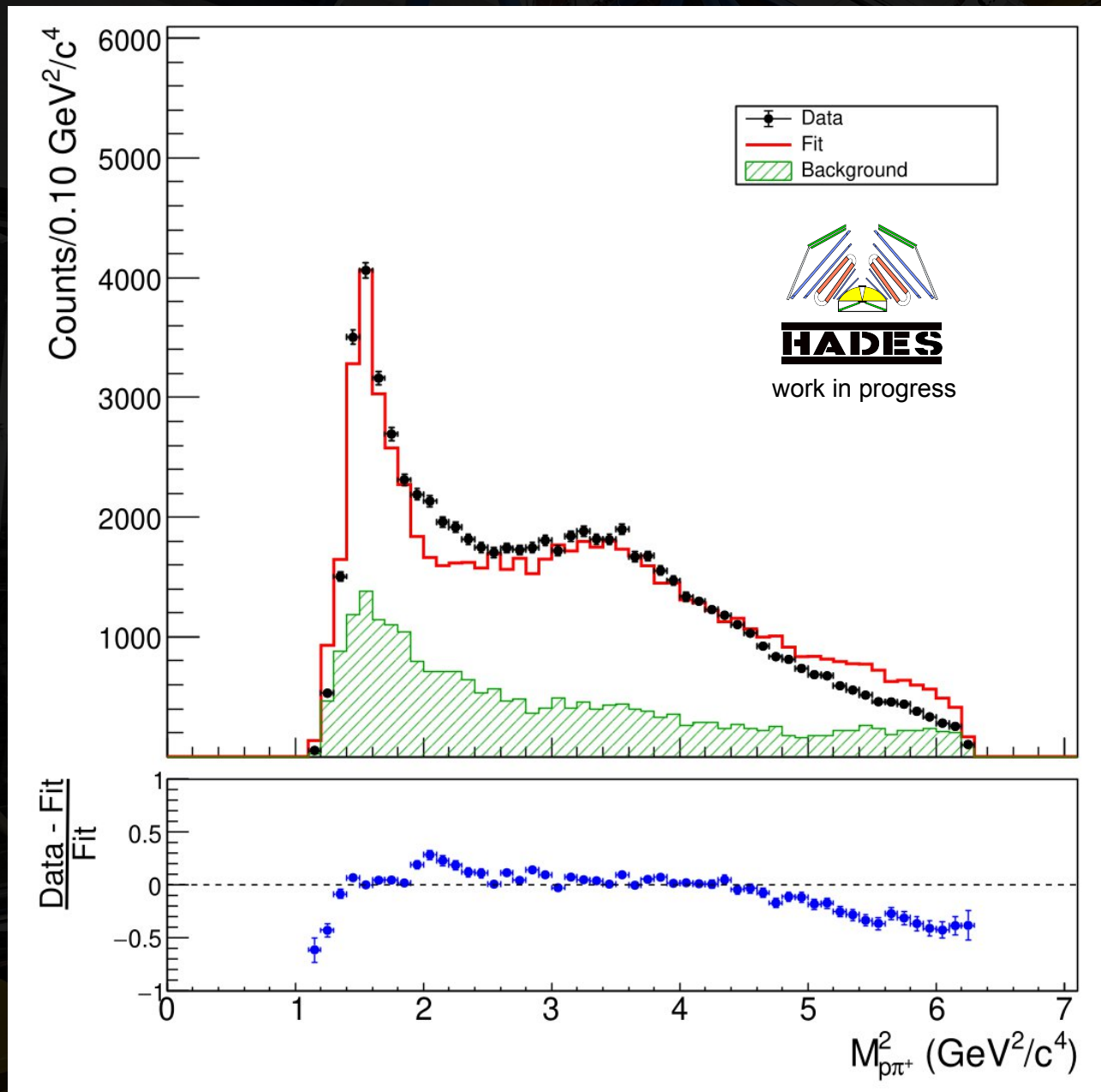


Data



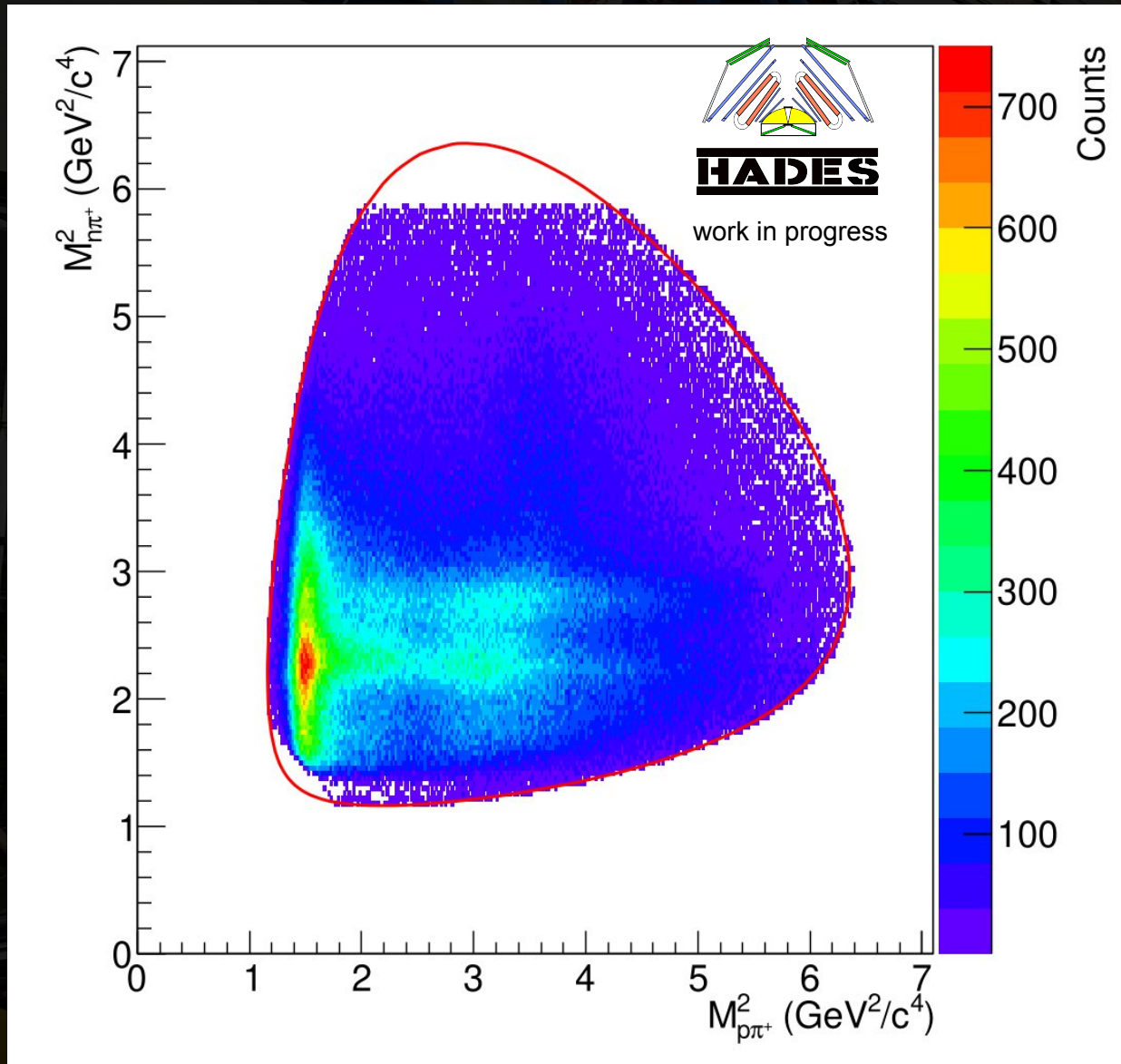
Acceptance Corrected
Fit Result (P33,P31,S11 and P11)

Preliminary Fit Results

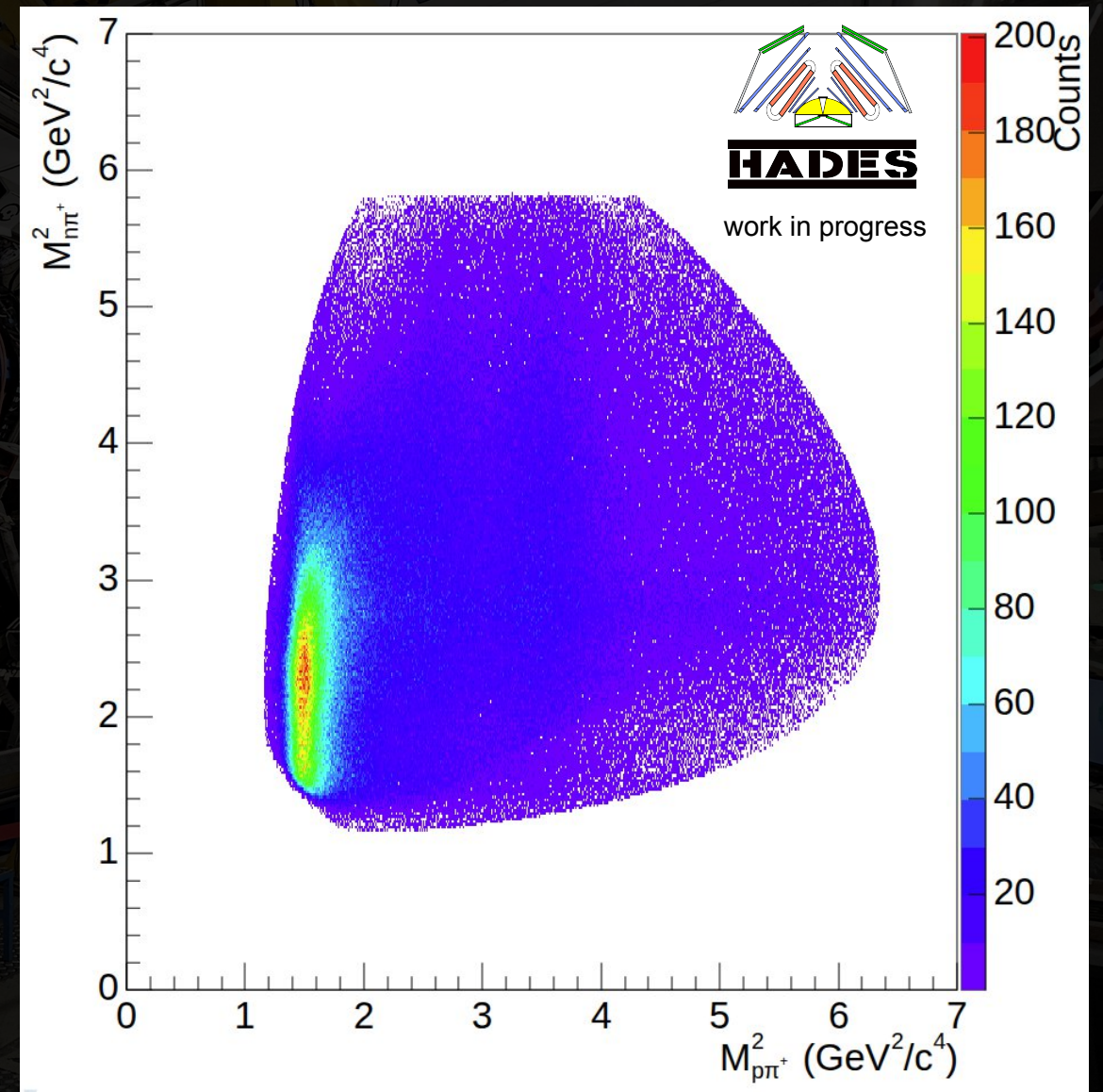


Fit Result (P33,P31,S11 and P11)

Comparison to Transport Models



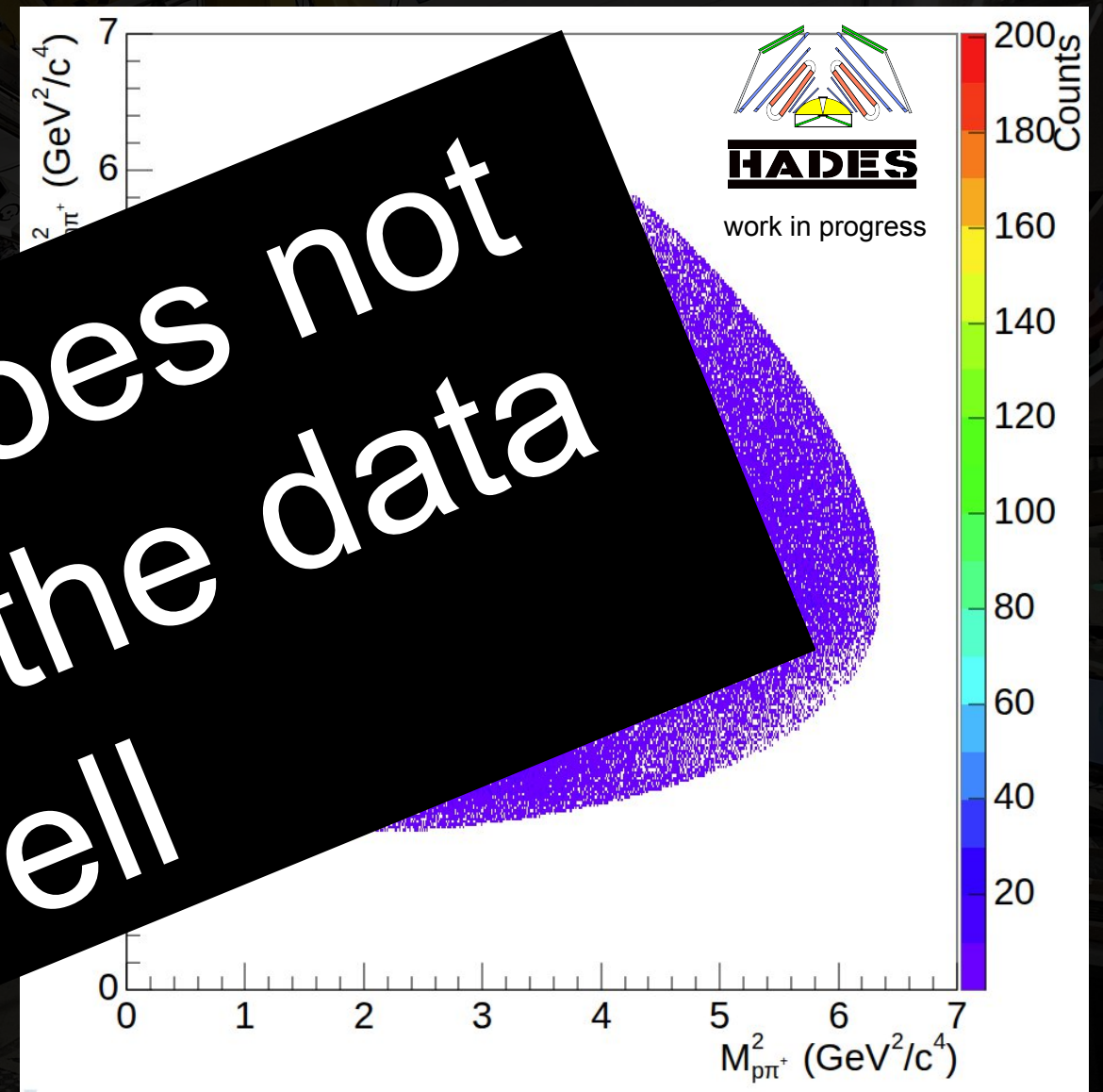
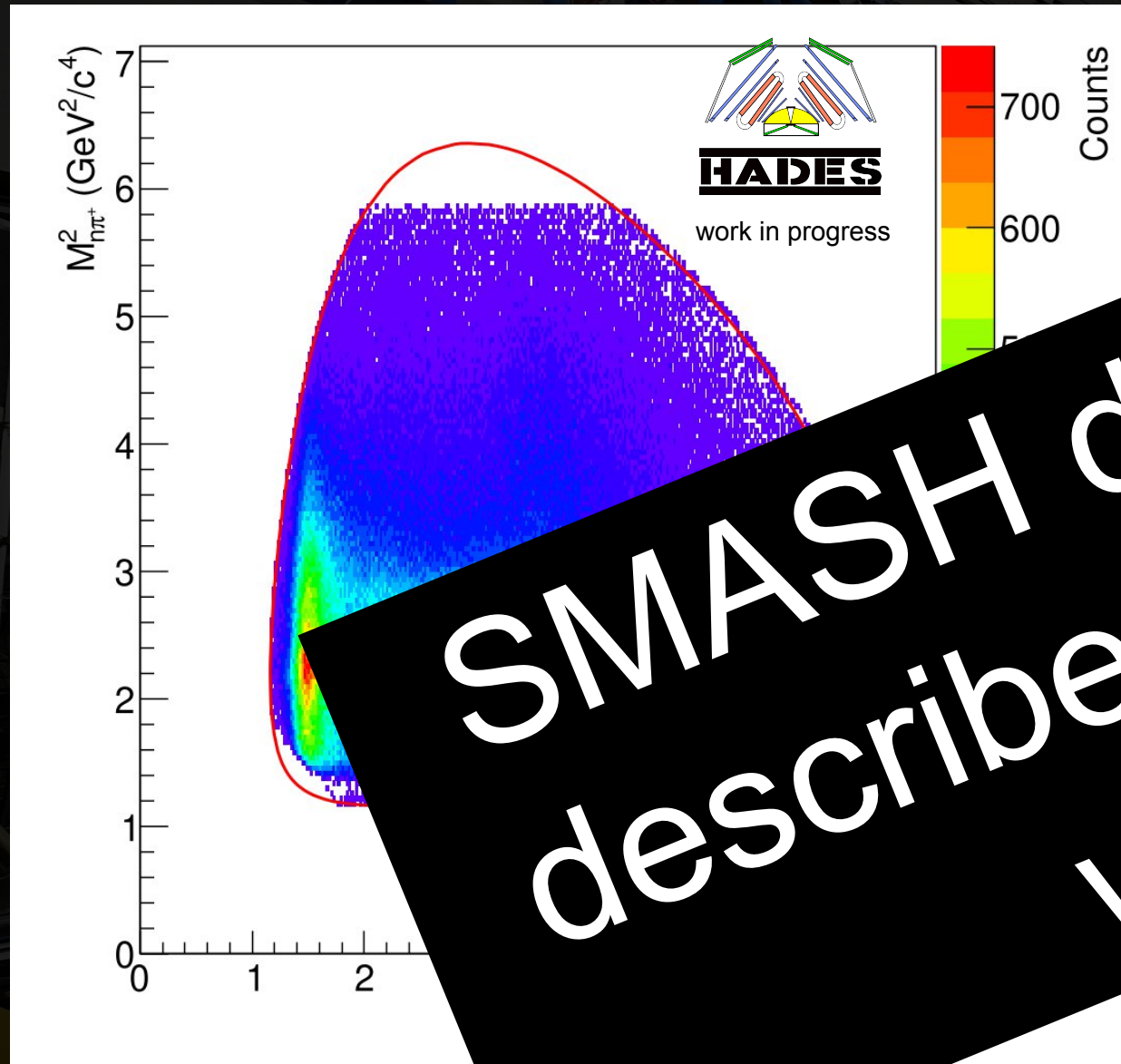
Data



SMASH^[4]



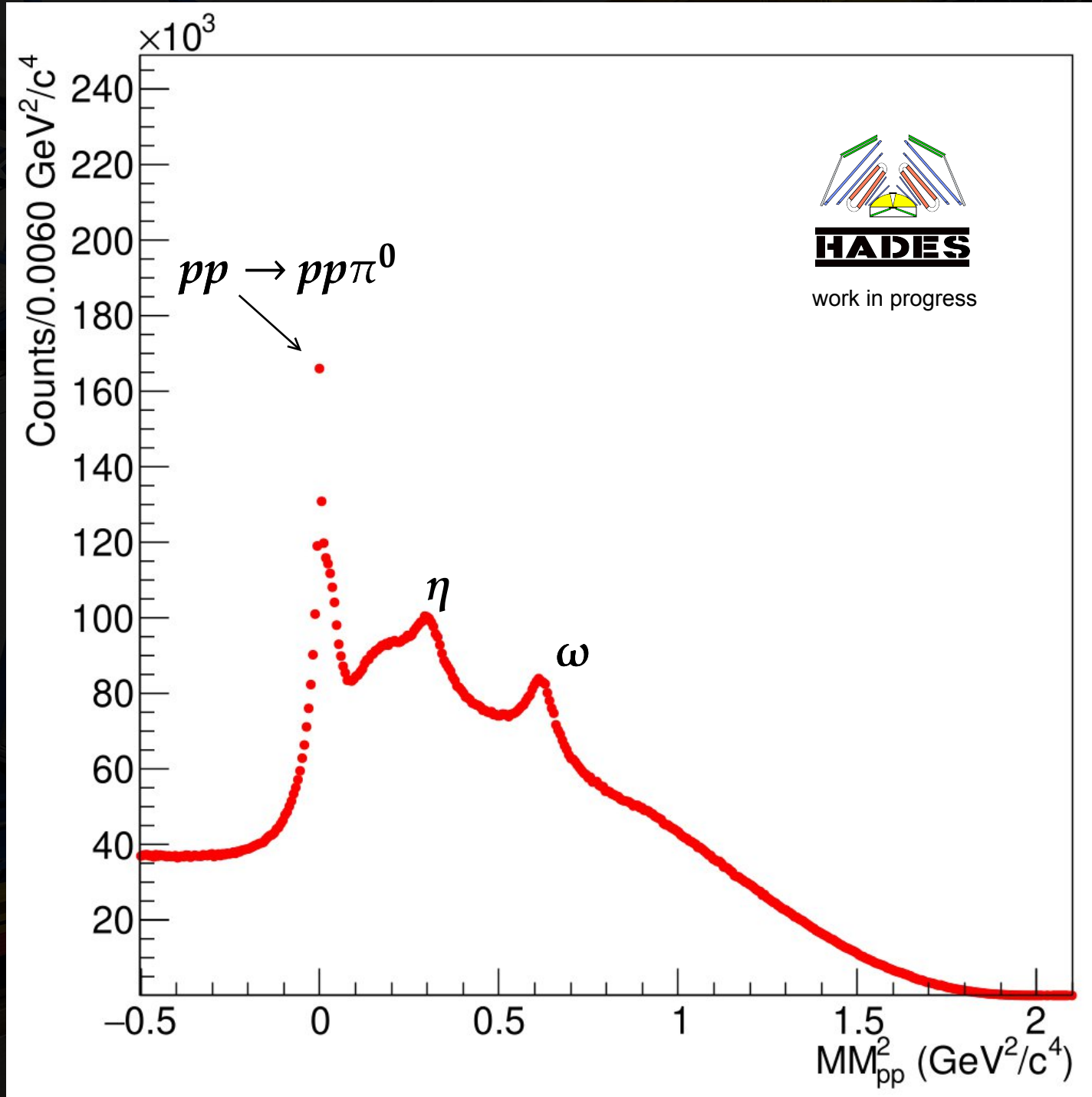
Comparision to SMASH



SMASH does not describe the data well

SMASH

$$pp \rightarrow pp\pi^0$$

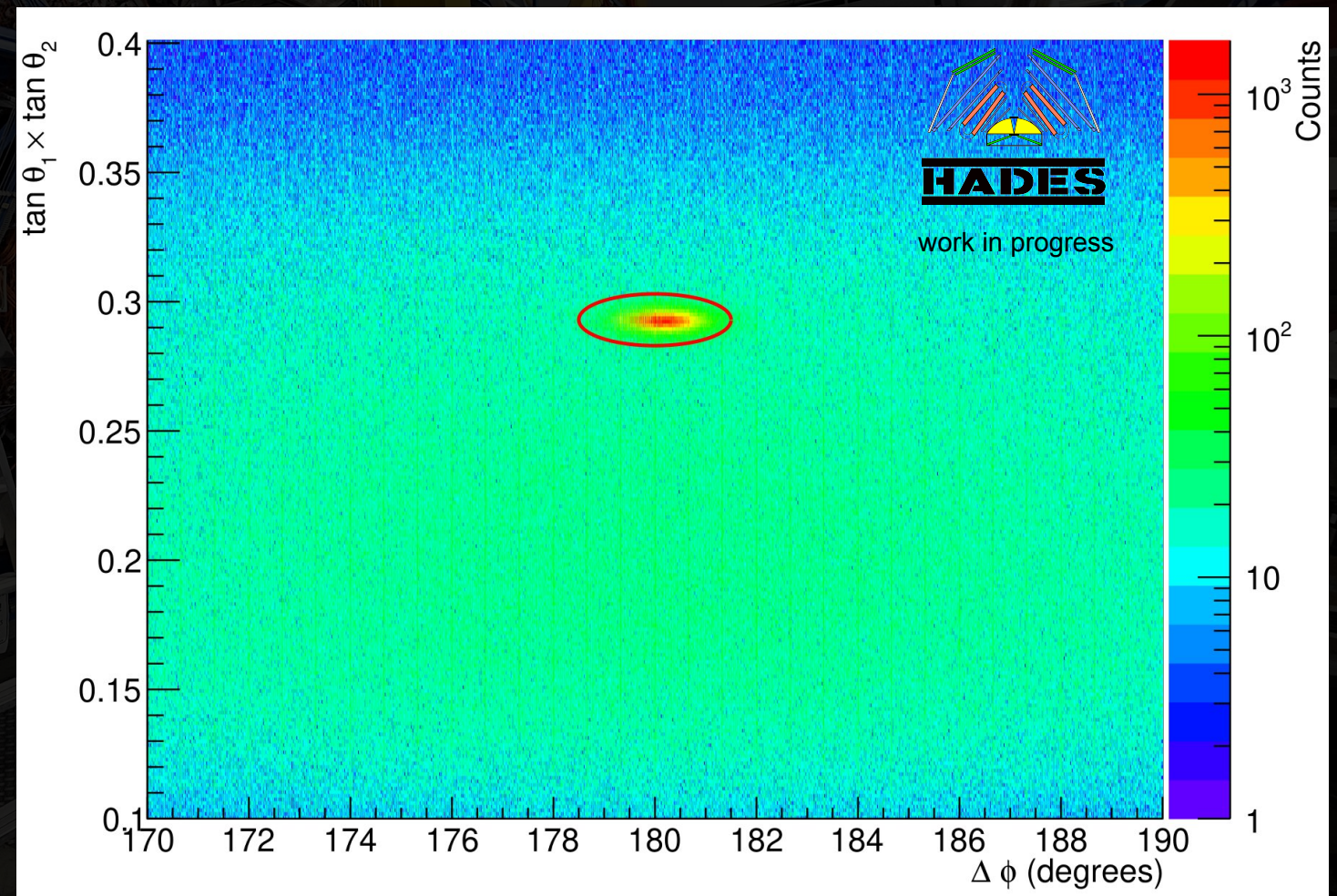


Elastic Cut

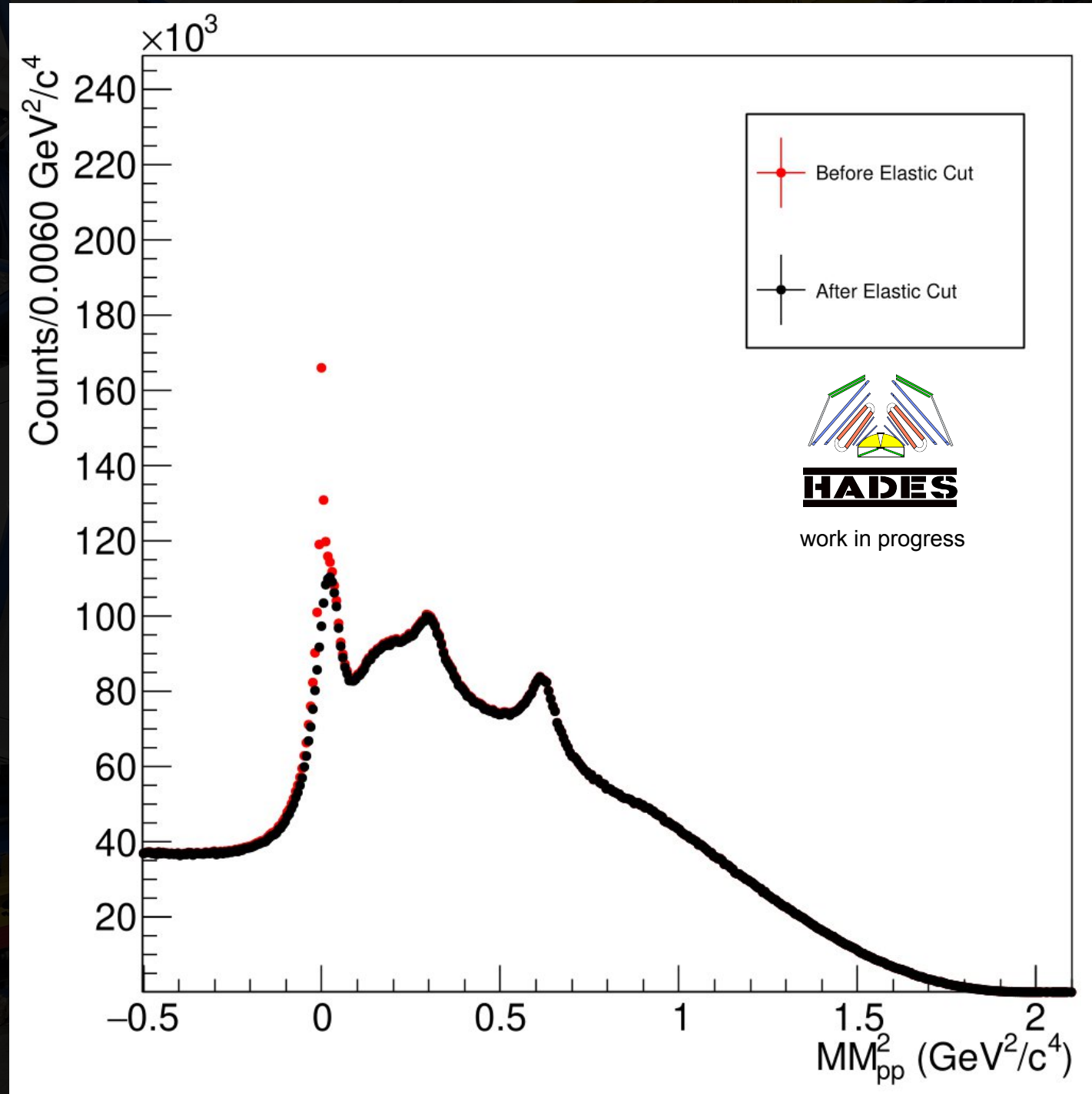
- Inelastic events are selected by applying cuts based on the expected kinematics of elastic scattering.

$$\Delta\phi = |\phi_1 - \phi_2| = 180^\circ$$

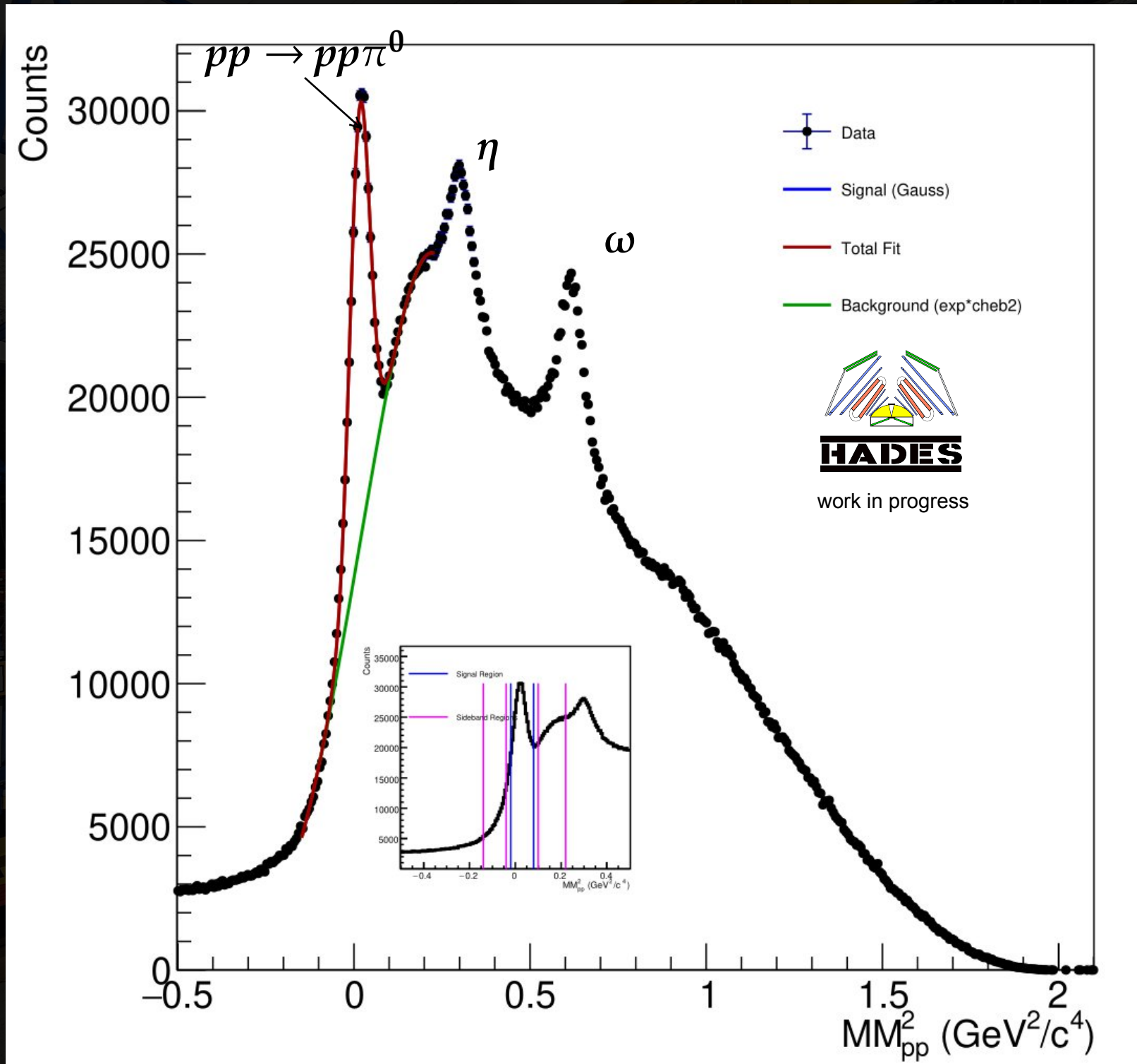
$$\tan\theta_1 \times \tan\theta_2 = \frac{1}{\gamma_{CM}^2}$$



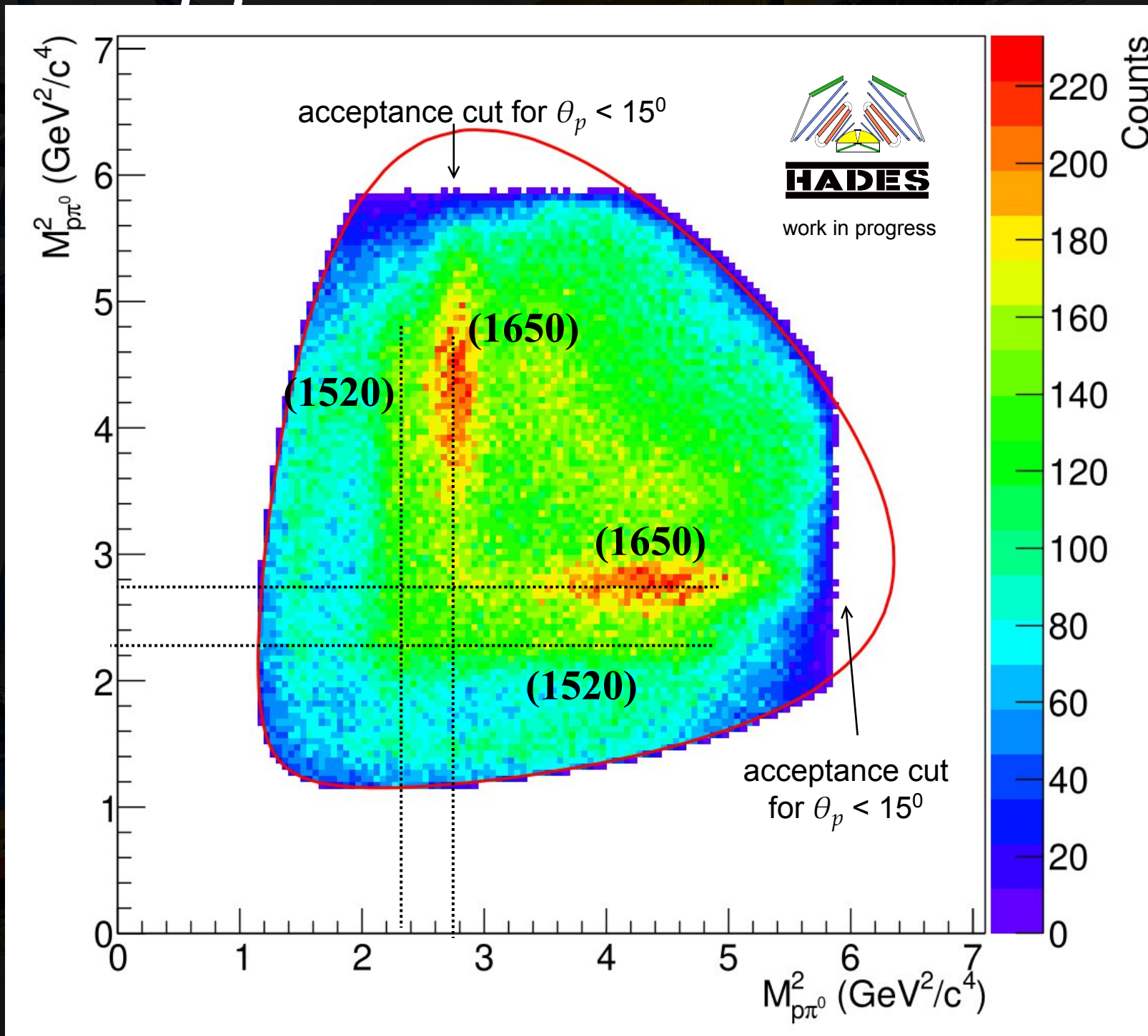
$$pp \rightarrow pp\pi^0$$



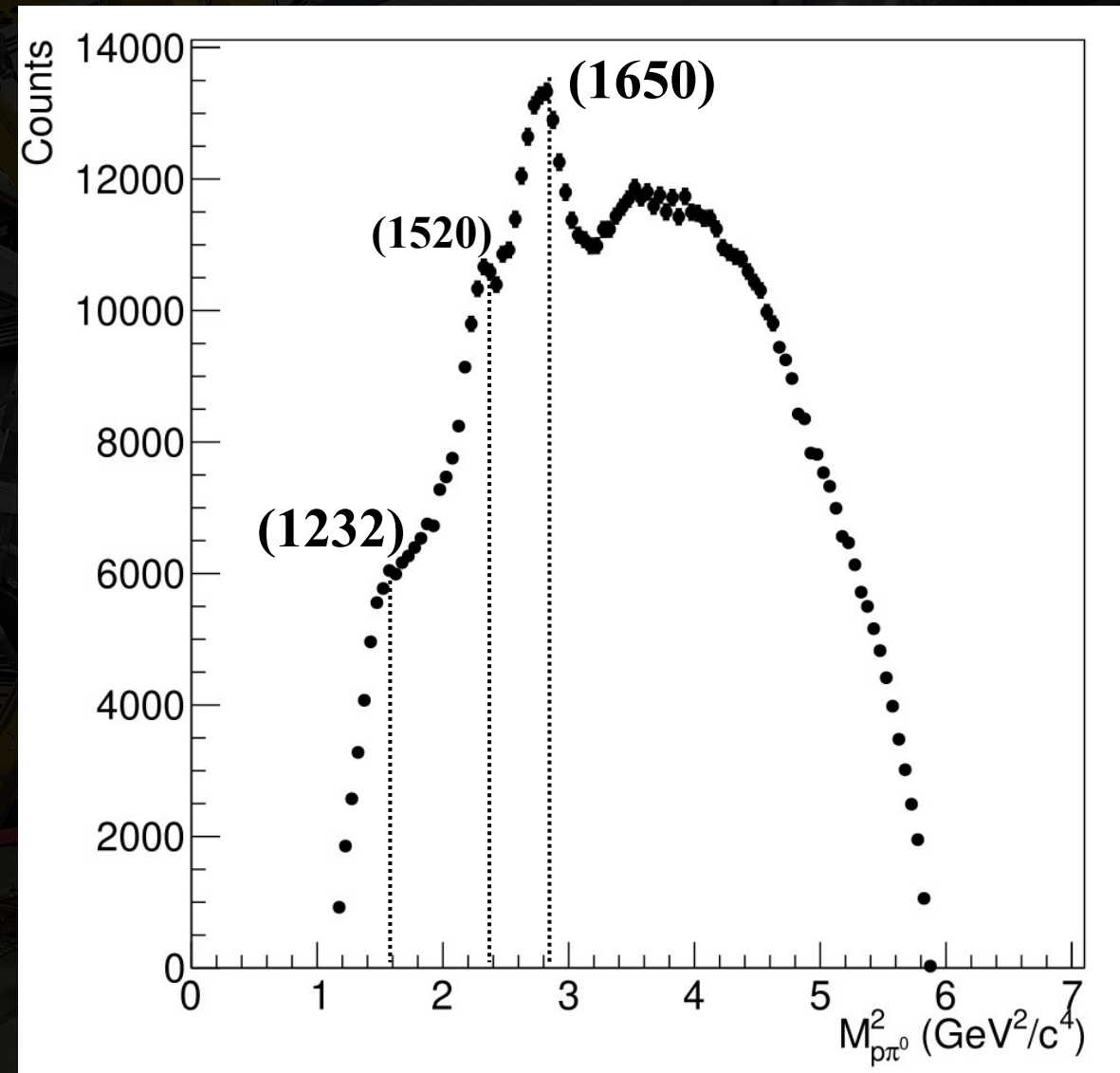
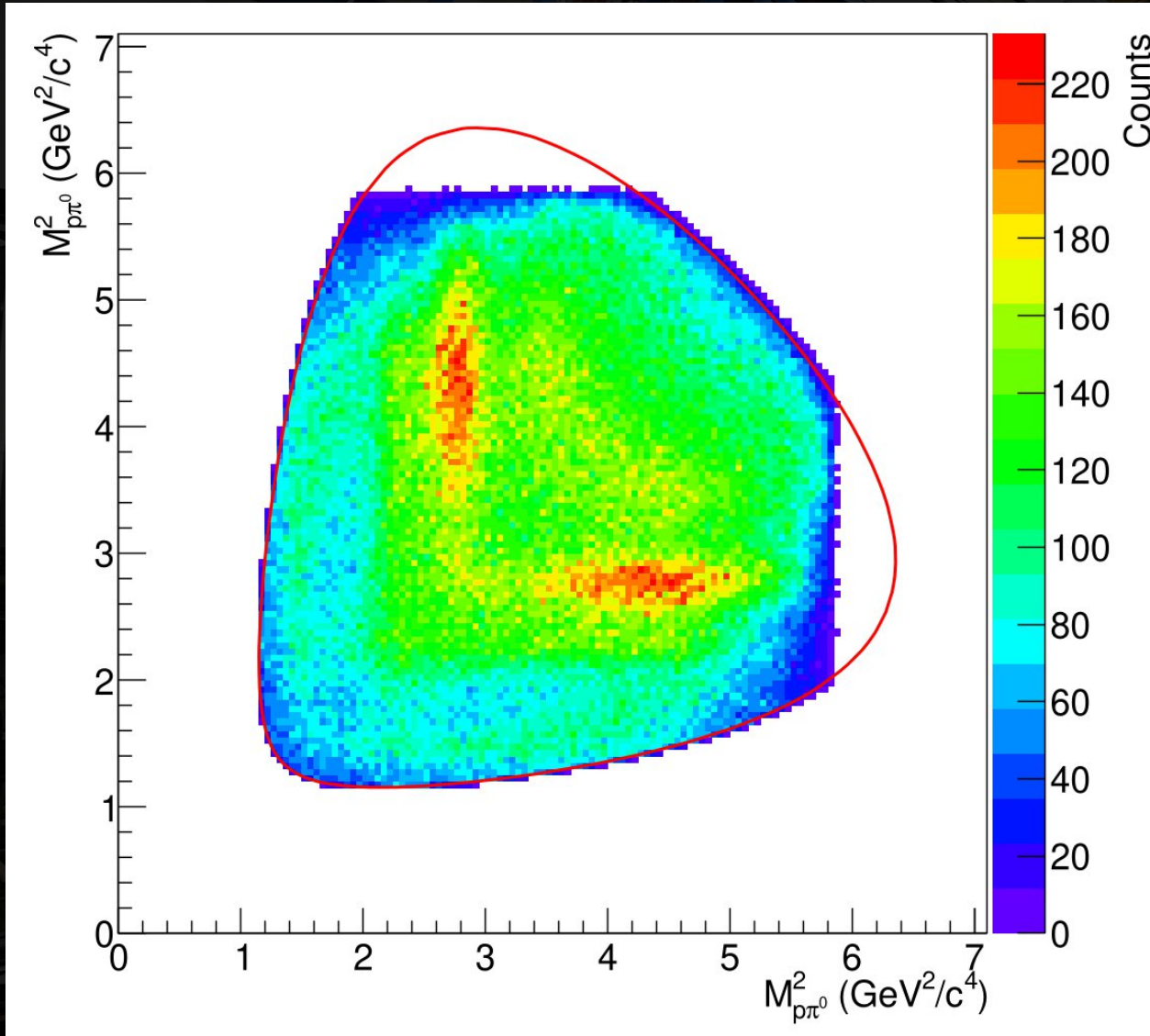
$$pp \rightarrow pp\pi^0$$



$pp\pi^0$ Dalitz Plot

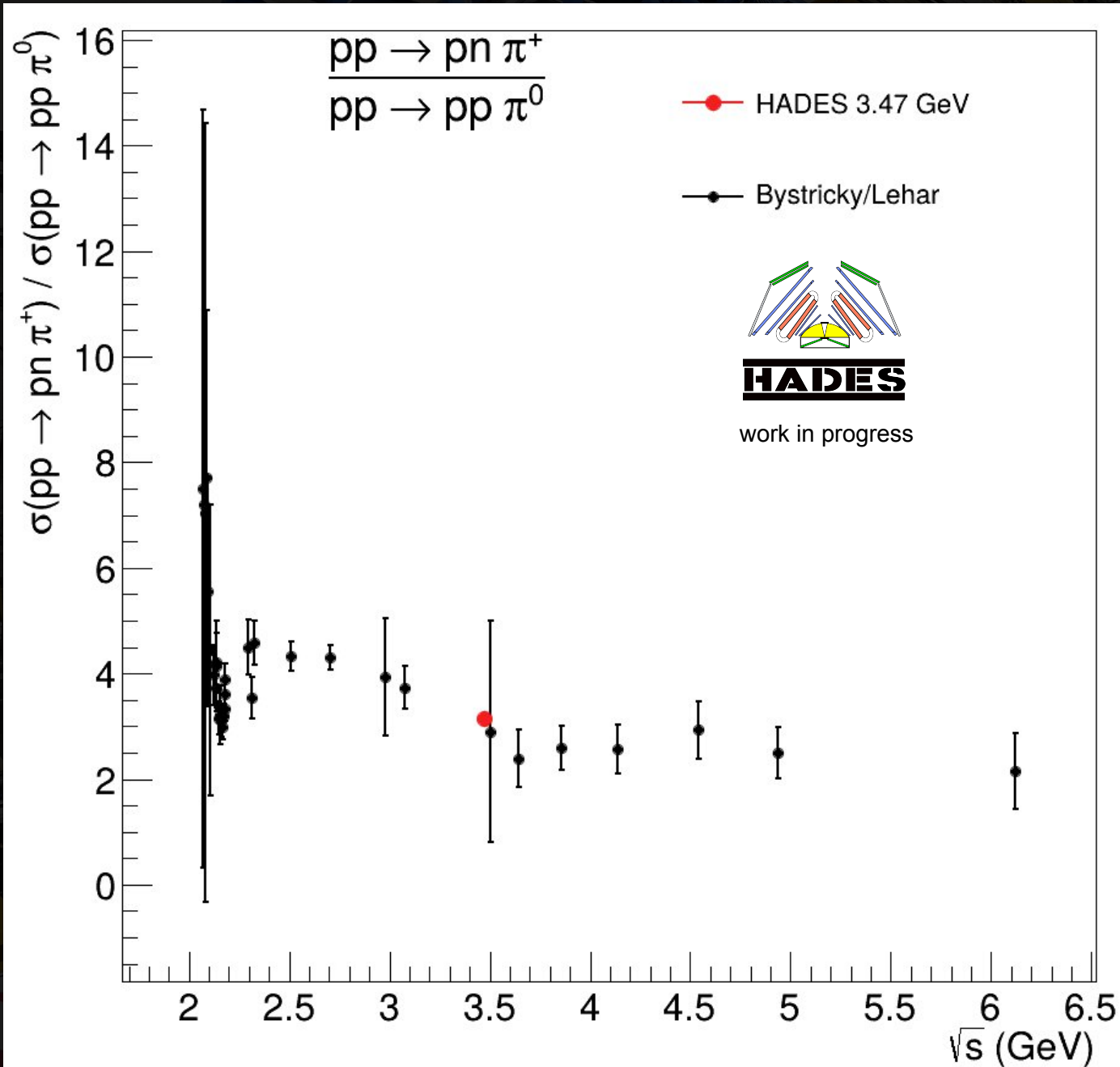


$pp\pi^0$ Dalitz Plot



$$\sigma(pp \rightarrow pn\pi^+)$$

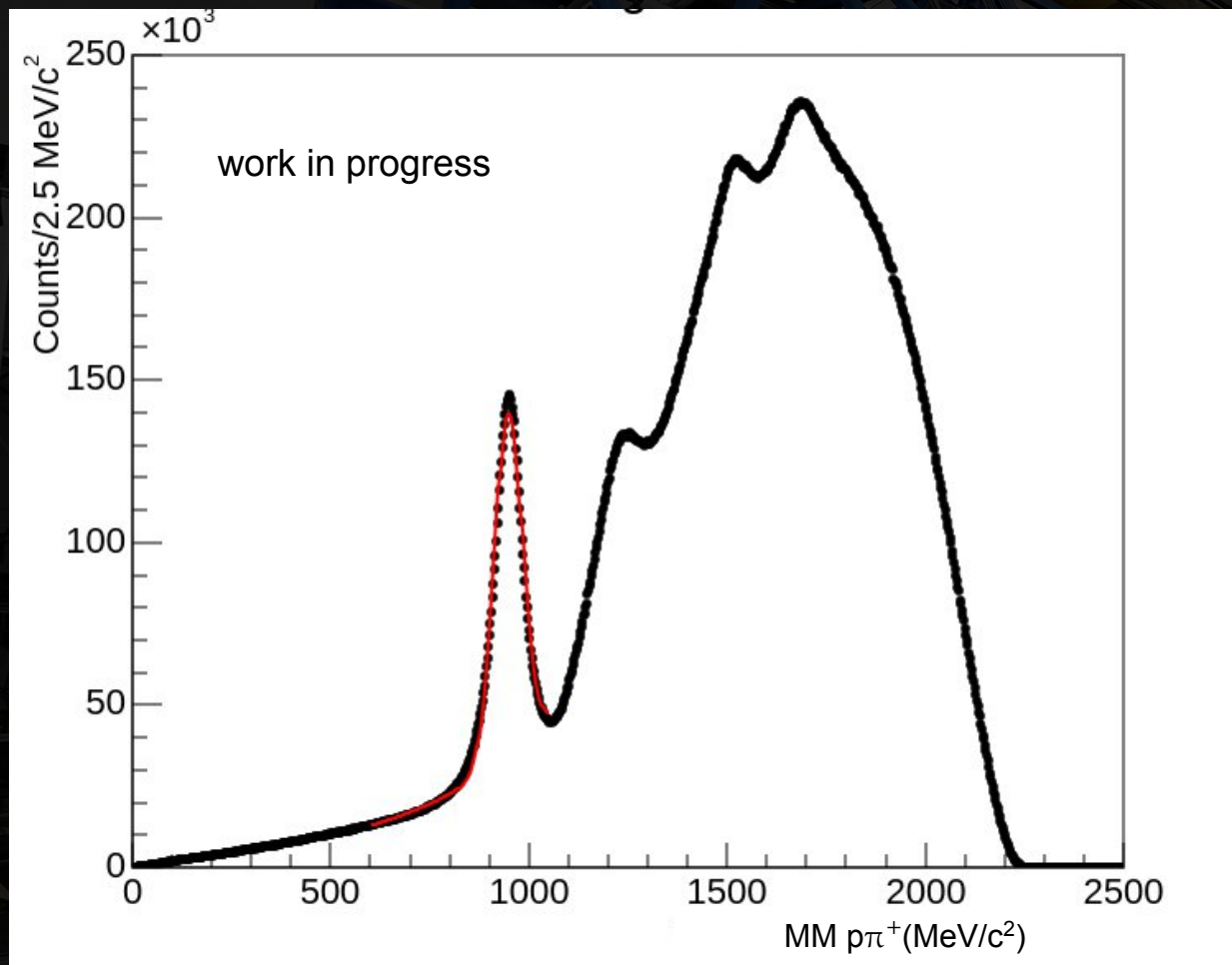
$$\sigma(pp \rightarrow pp\pi^0)$$



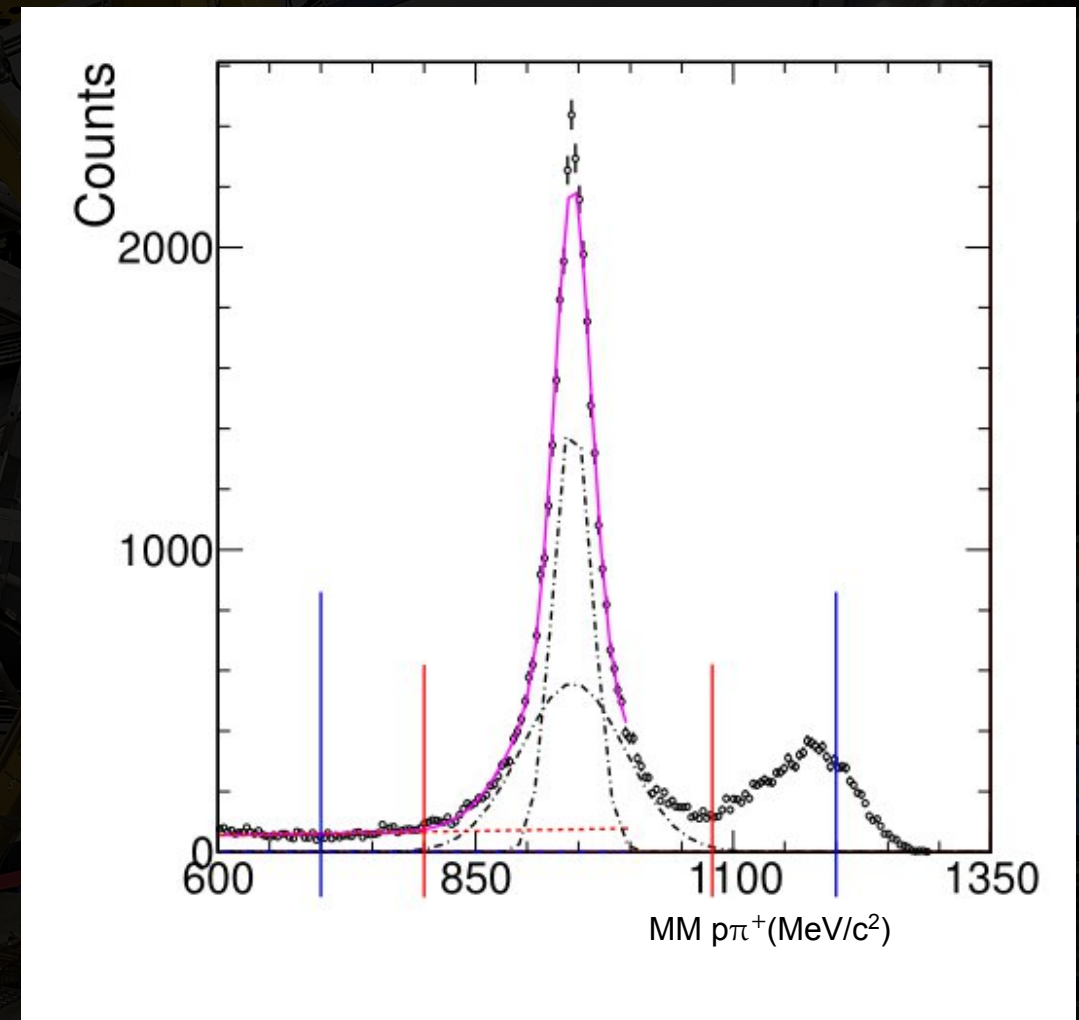
$$\frac{\sigma(pp \rightarrow pn\pi^+)}{\sigma(pp \rightarrow pp\pi^0)} = 3.14 \pm 0.005 \text{ (stat)}$$

The decreasing cross-section ratio reflects the transition from $\Delta(1232)$ -dominated pion production to increasing contributions from higher-mass baryon resonances.

Missing Mass Resolution

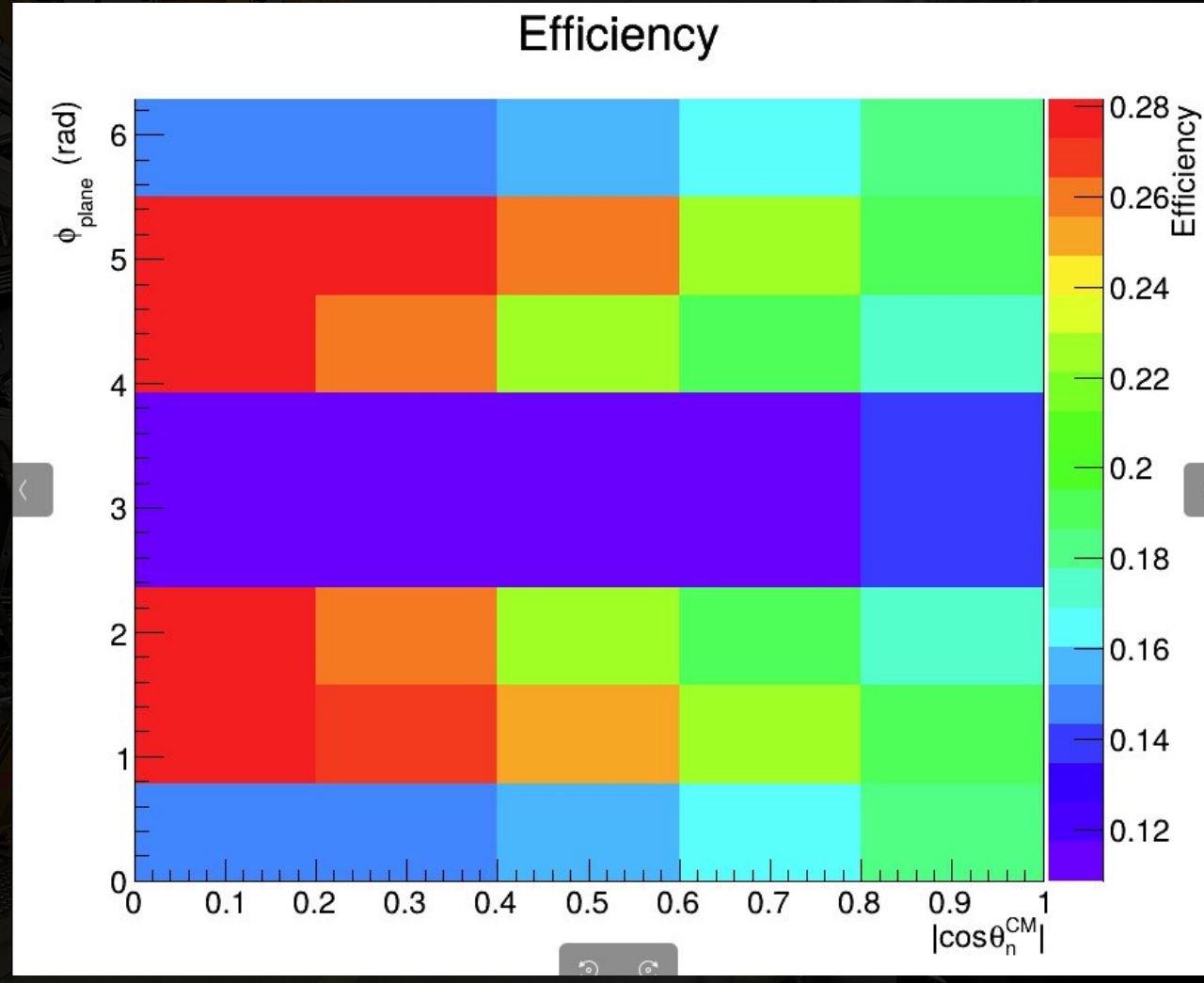
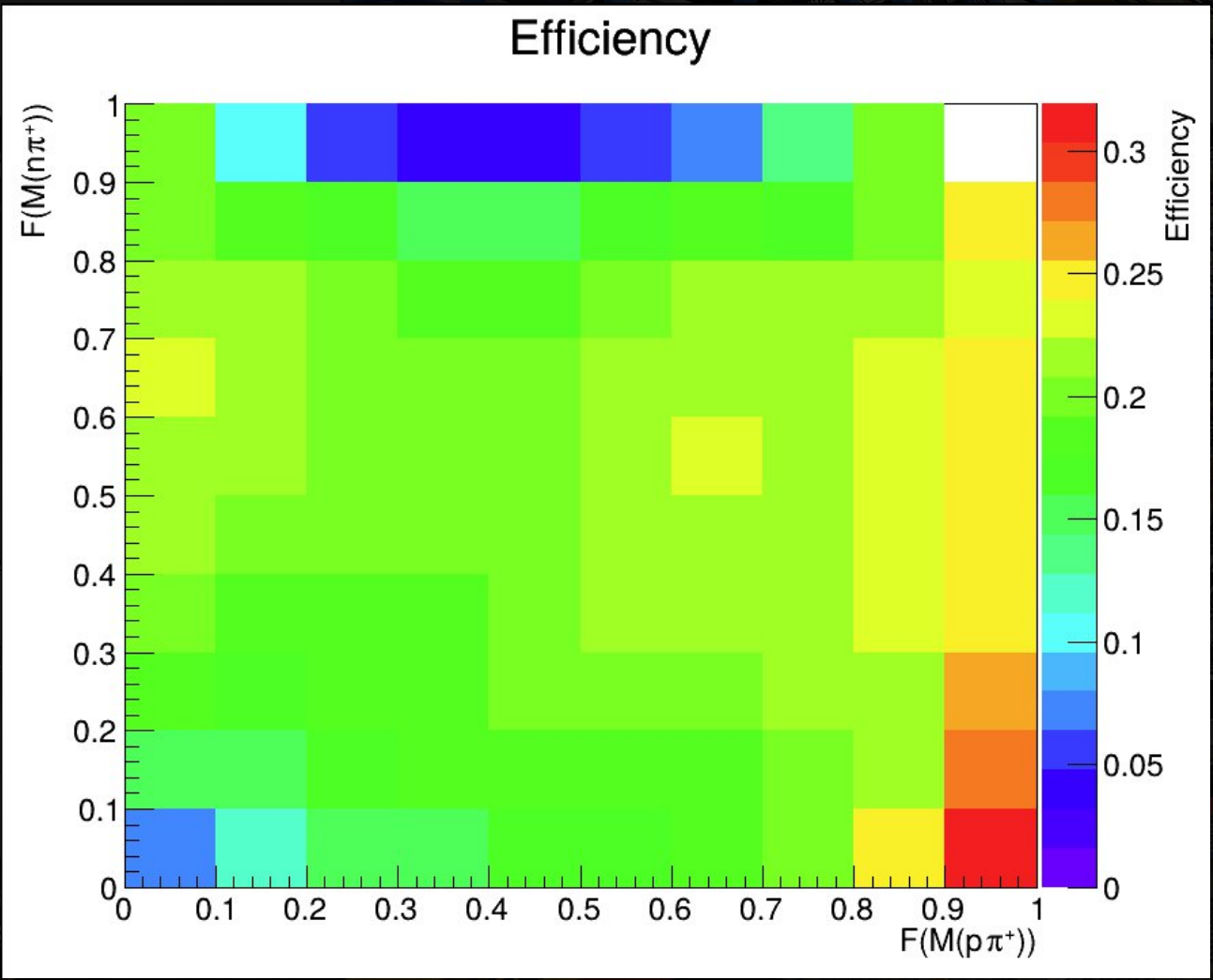


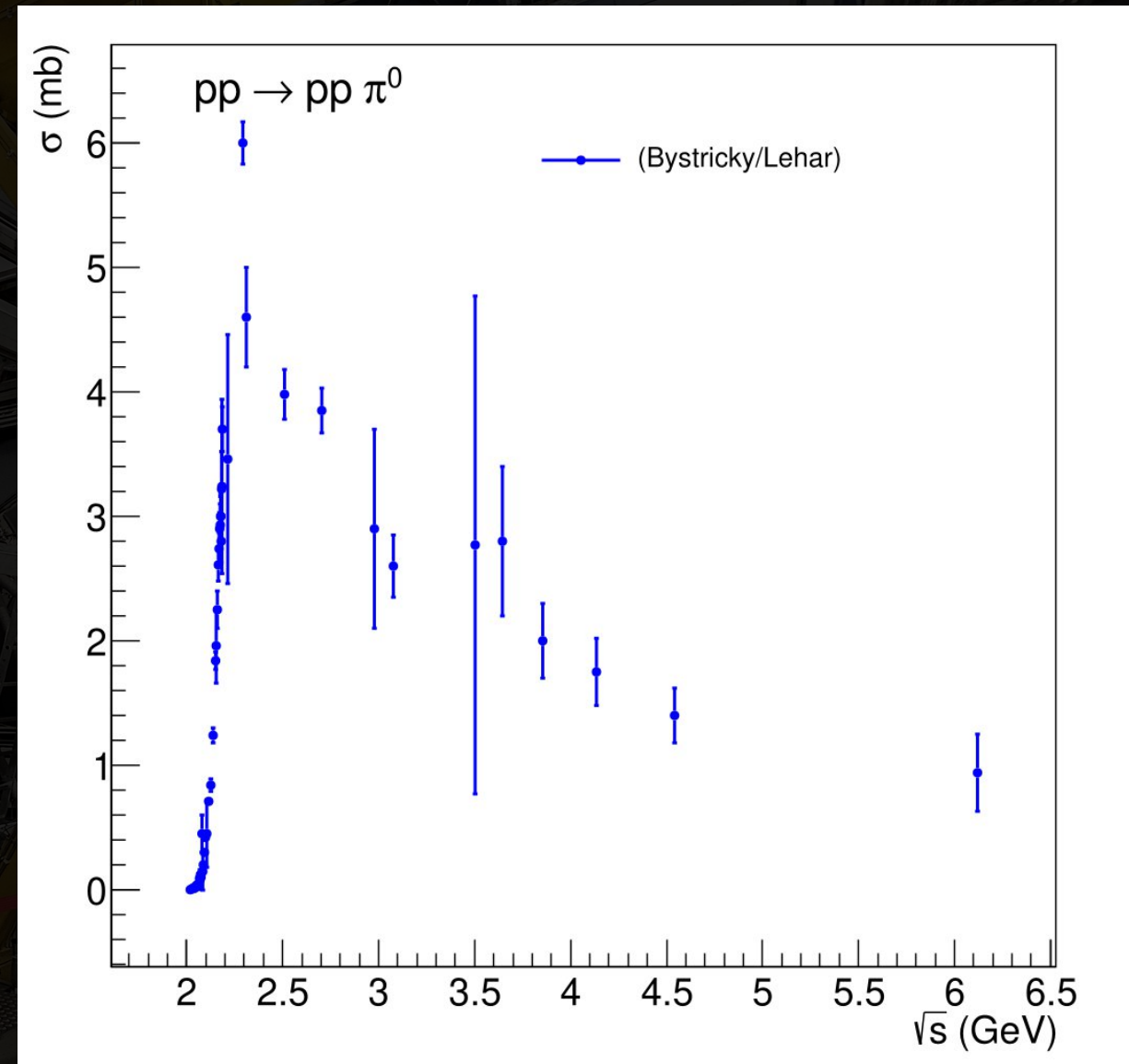
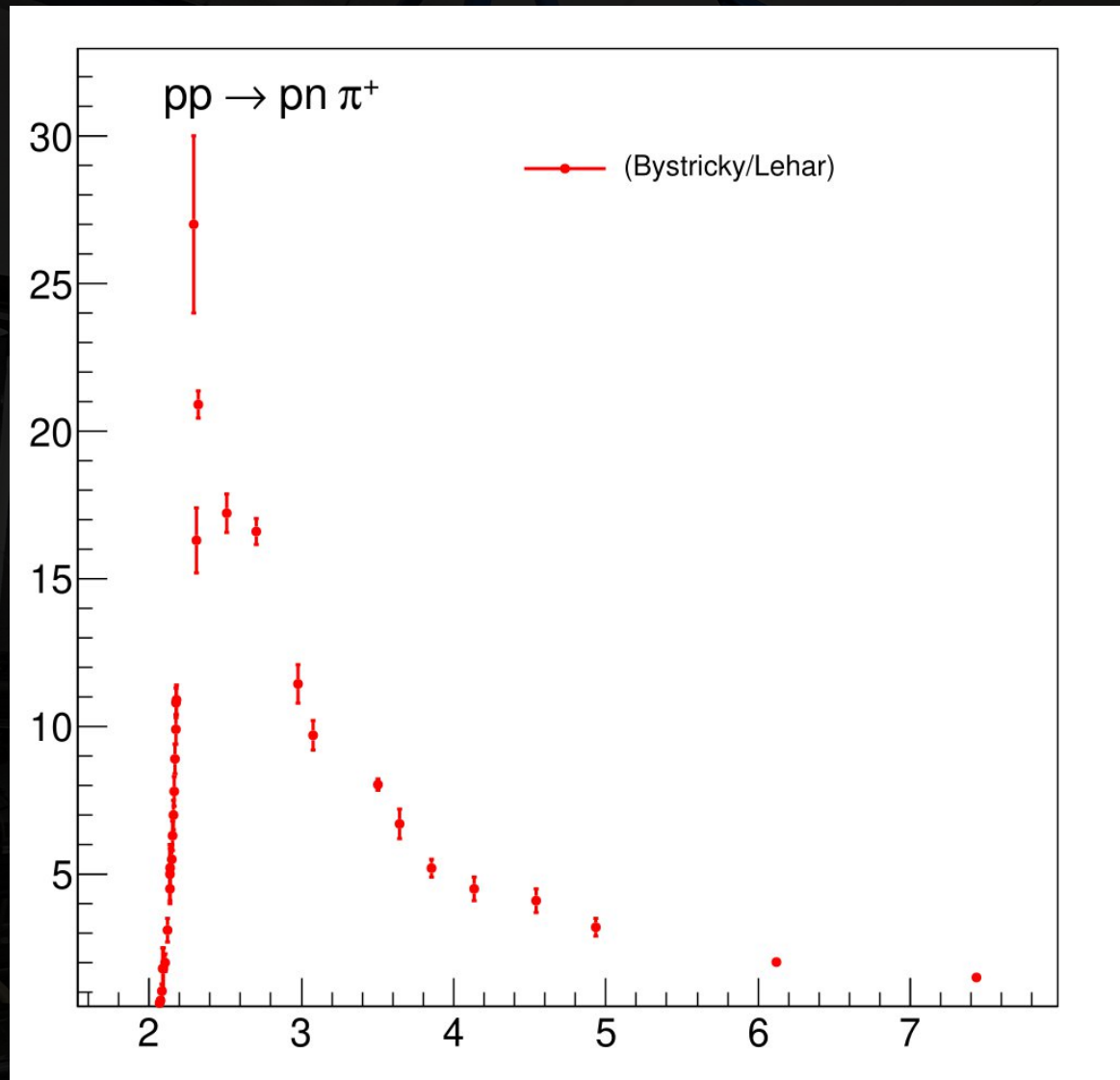
Neutron Peak Resolution $\sim 35 \text{ MeV}/c^2$



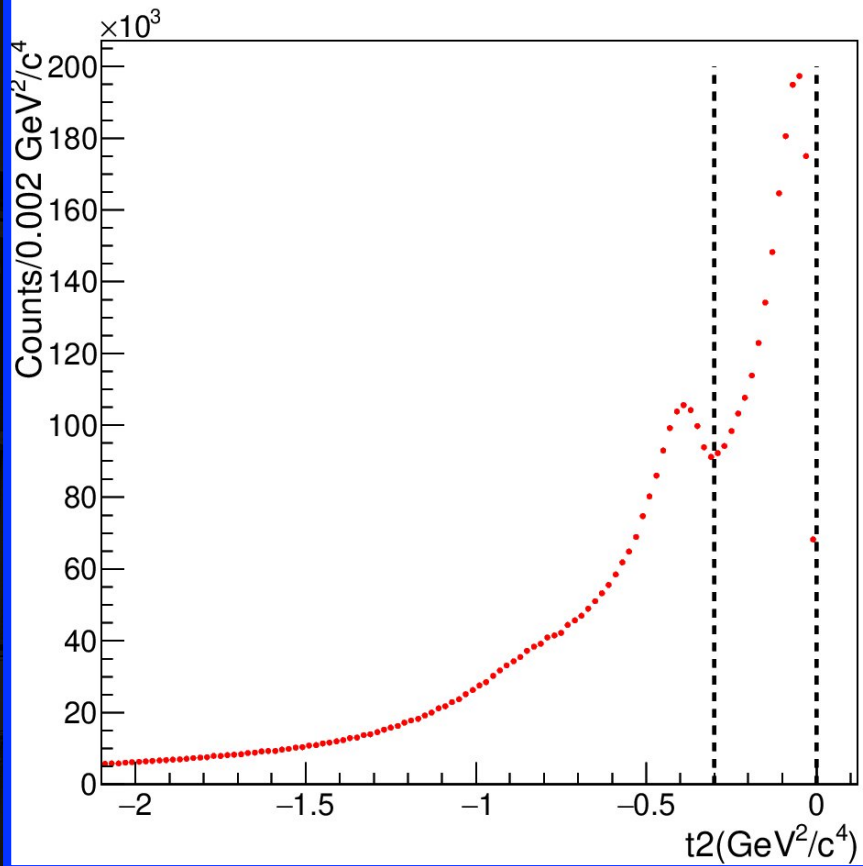
pp at $T = 1.25 \text{ GeV}$
T. Liu, PhD Thesis 2010.

Neutron Peak Resolution $\sim 12 \text{ MeV}/c^2$

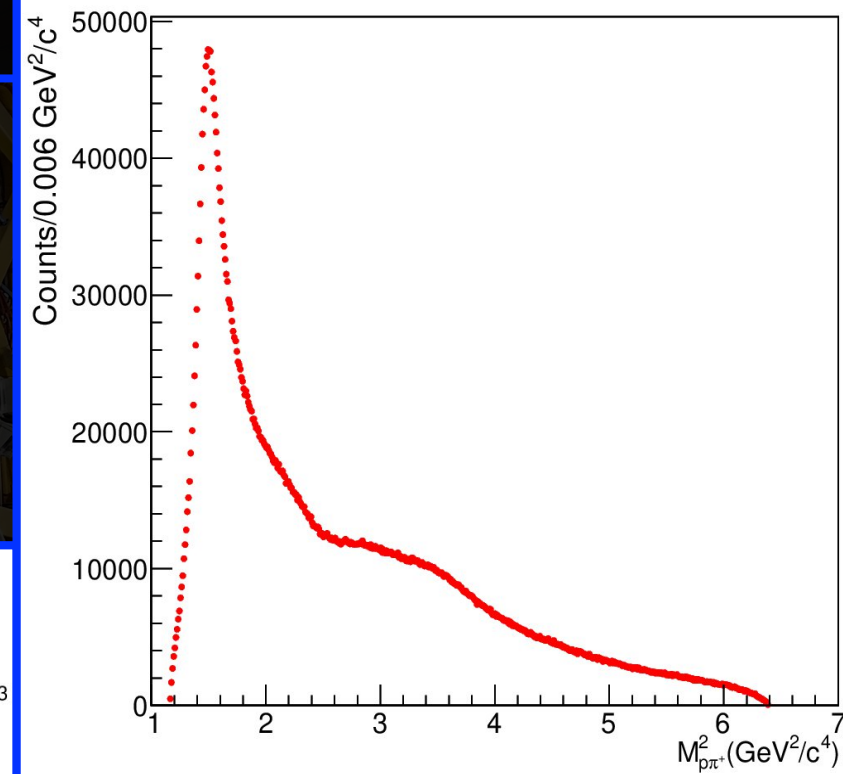
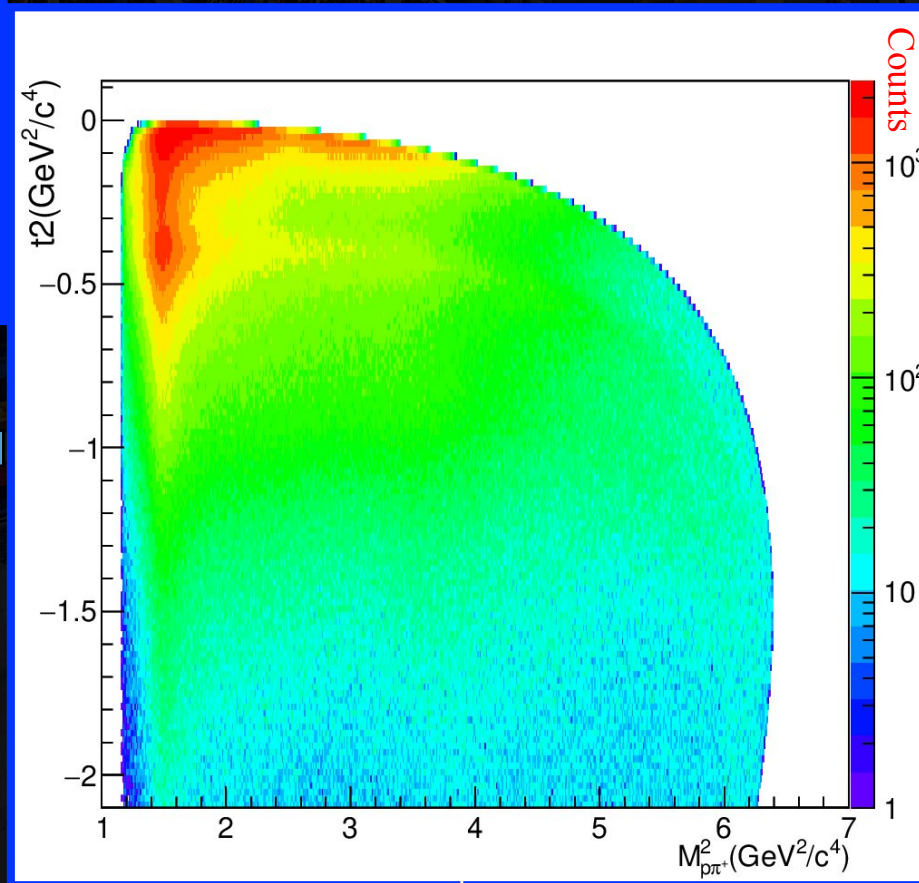
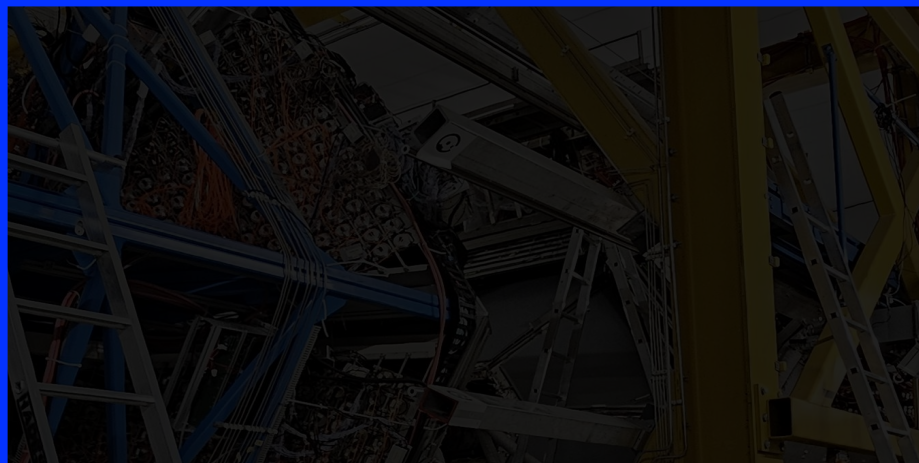




$$M_{p\pi^+}^2 \text{ vs } t_2$$



Y projection



X projection