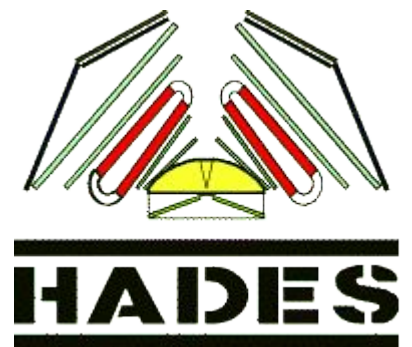


# Quality checks for $pp \rightarrow ppK^+K^-$ reaction analysis

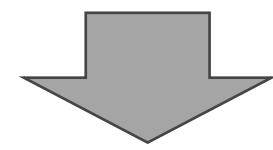
Valentin Kladov

Ruhr-Universität Bochum  
GSI Helmholtzzentrum

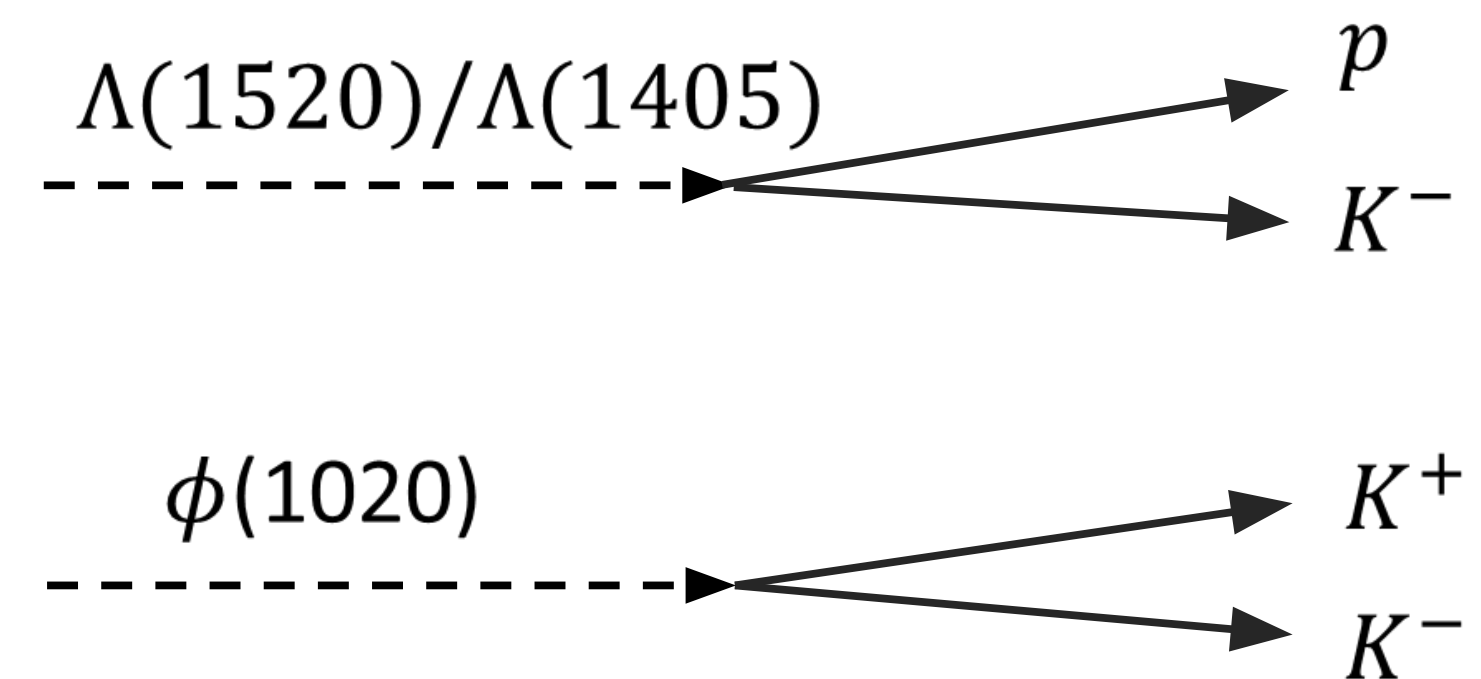
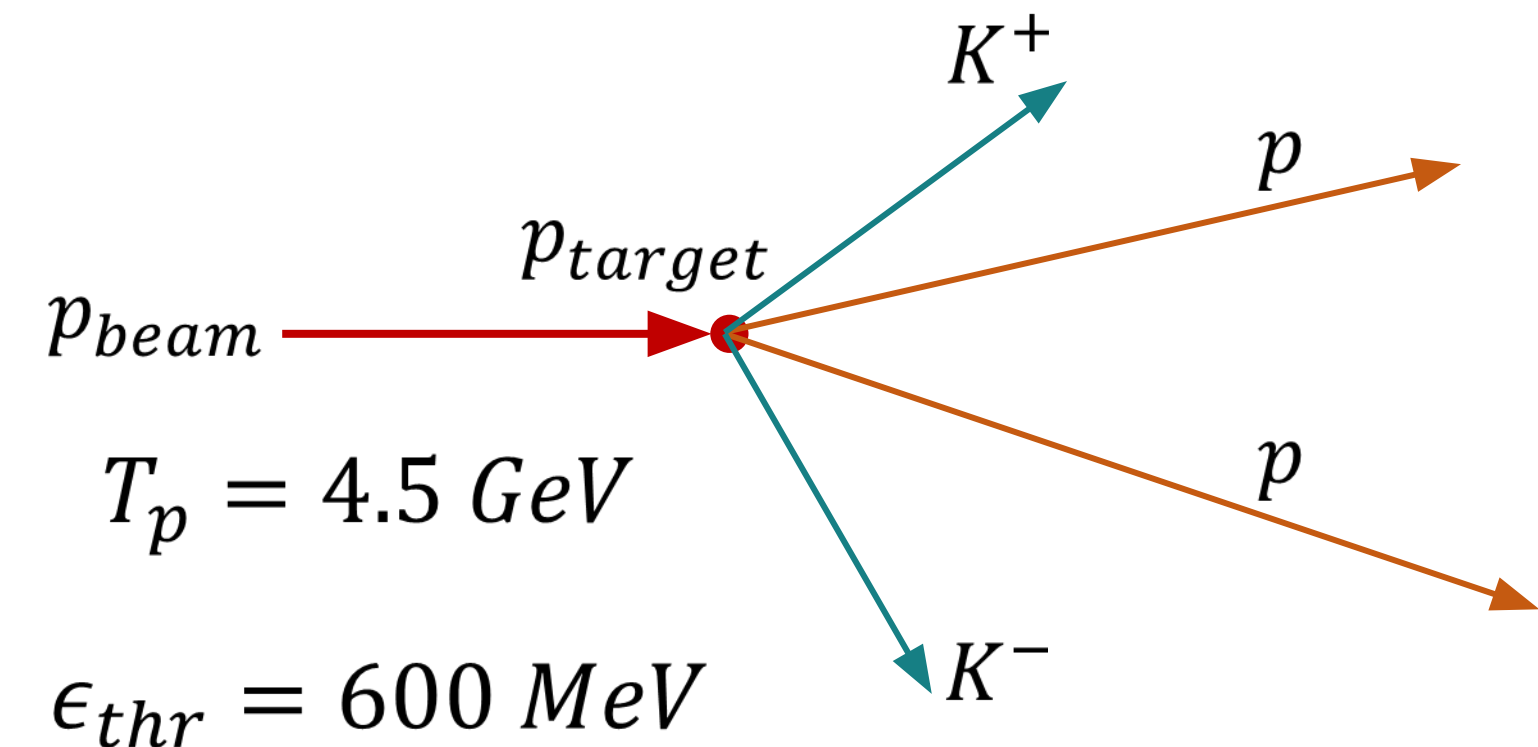


# Motivation

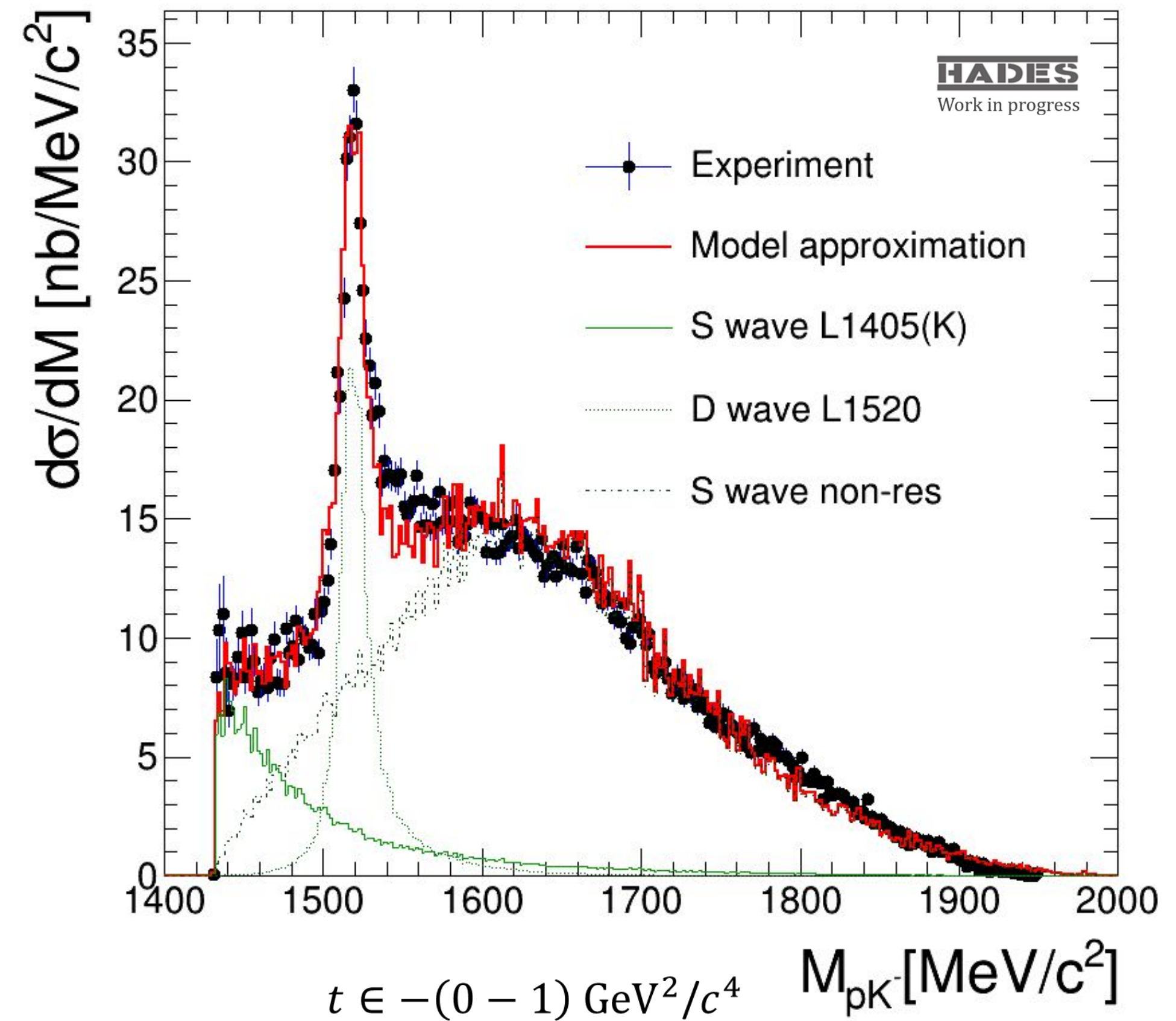
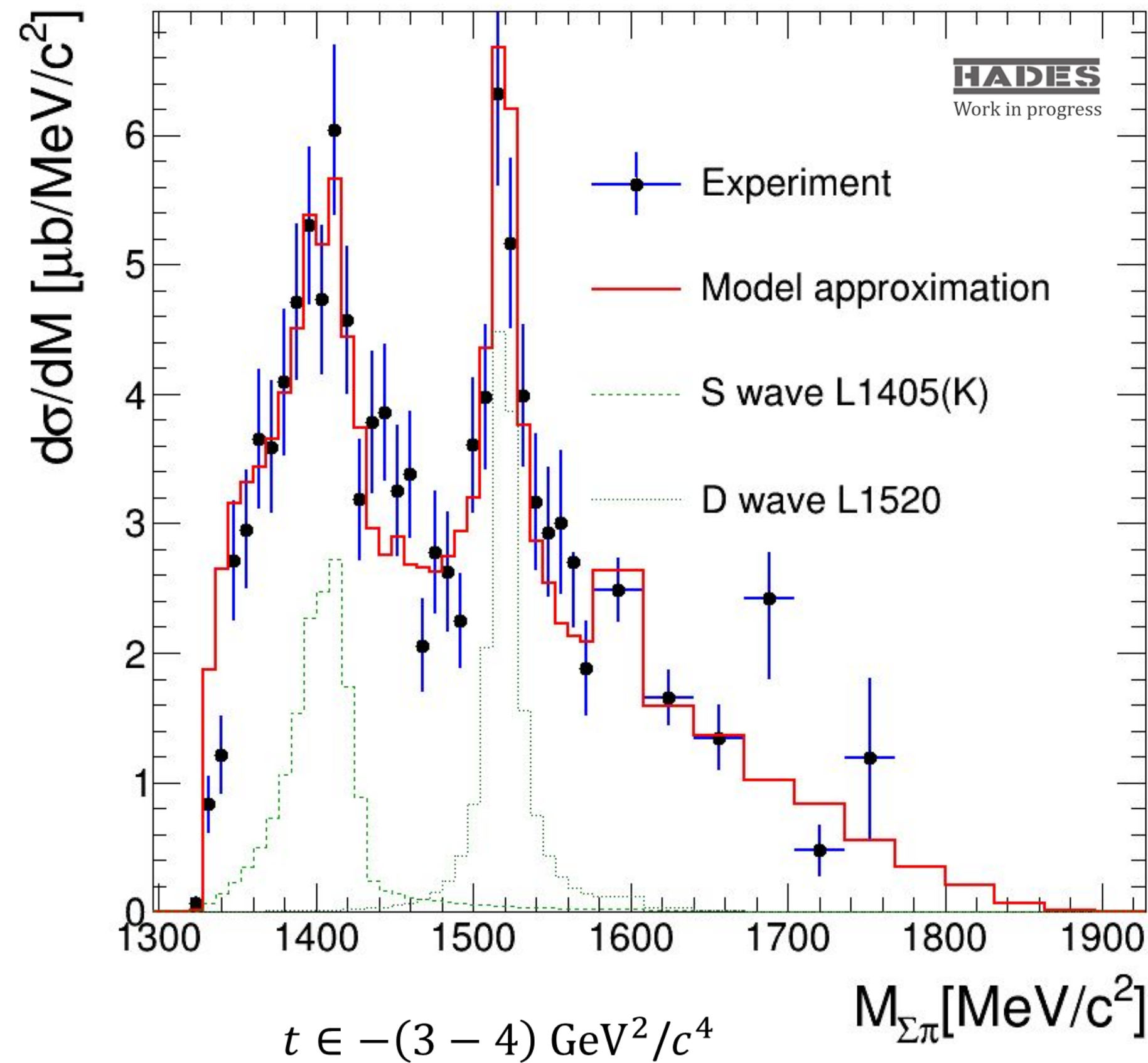
- Strangeness production in a non-strange system?
- Final state interactions in  $pK^-$  and  $K^+K^-$  pairs?
- The role of baryon resonances?  $N^*$  or  $\Lambda(1405)$



- Differential and total cross sections
- Resonance parameters, spin density matrix elements
- Scattering lengths from FSI
- K-matrix formalism pole positions for  $\Lambda(1405)$

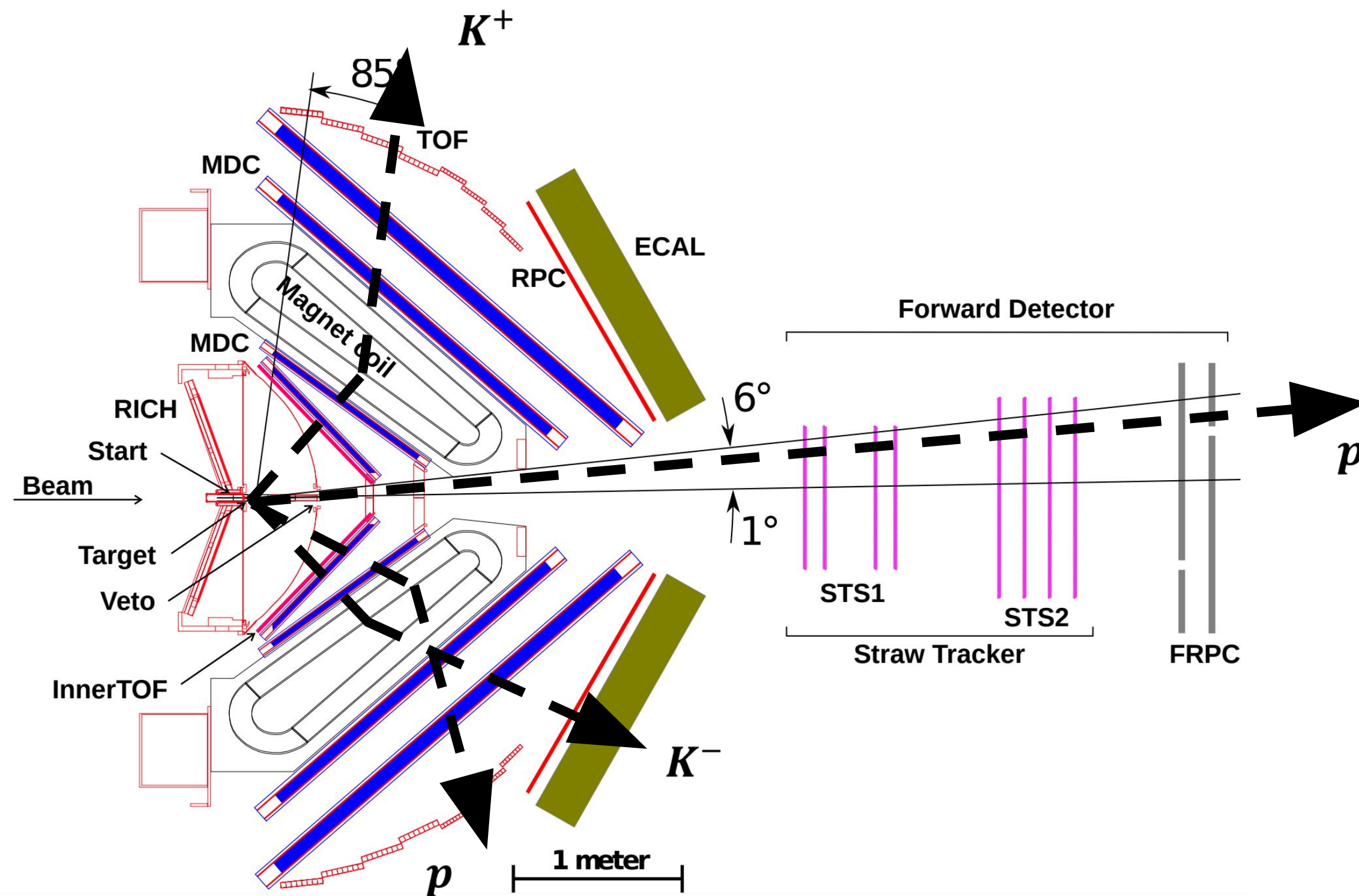


# $\Lambda(1405)$ Analysis in Progress



- Differential cross sections in momentum transfer bins  $t$
- Fit within 2-pole K-matrix formalism to approximate UchPT models
- Will present tomorrow at Meson 2026
- Separate PWG discussion needed?

# Event Selection



*Topology:*

$2K^\pm$  &  $1p$  in HADES,  $1p$  in Forward

• *PID in HADES:*

NN-based,  $\pi^\pm, K^\pm, p$  classification

• *Kinematic refit:*

$\chi^2_{KK} < 20$  &  $\chi^2_{KK} < \chi^2_{\pi\pi}$ , 4C refit

**Signal:**

$pp \rightarrow ppK^+K^-$  ( $\sim 5 \mu b$ )

**Background:**

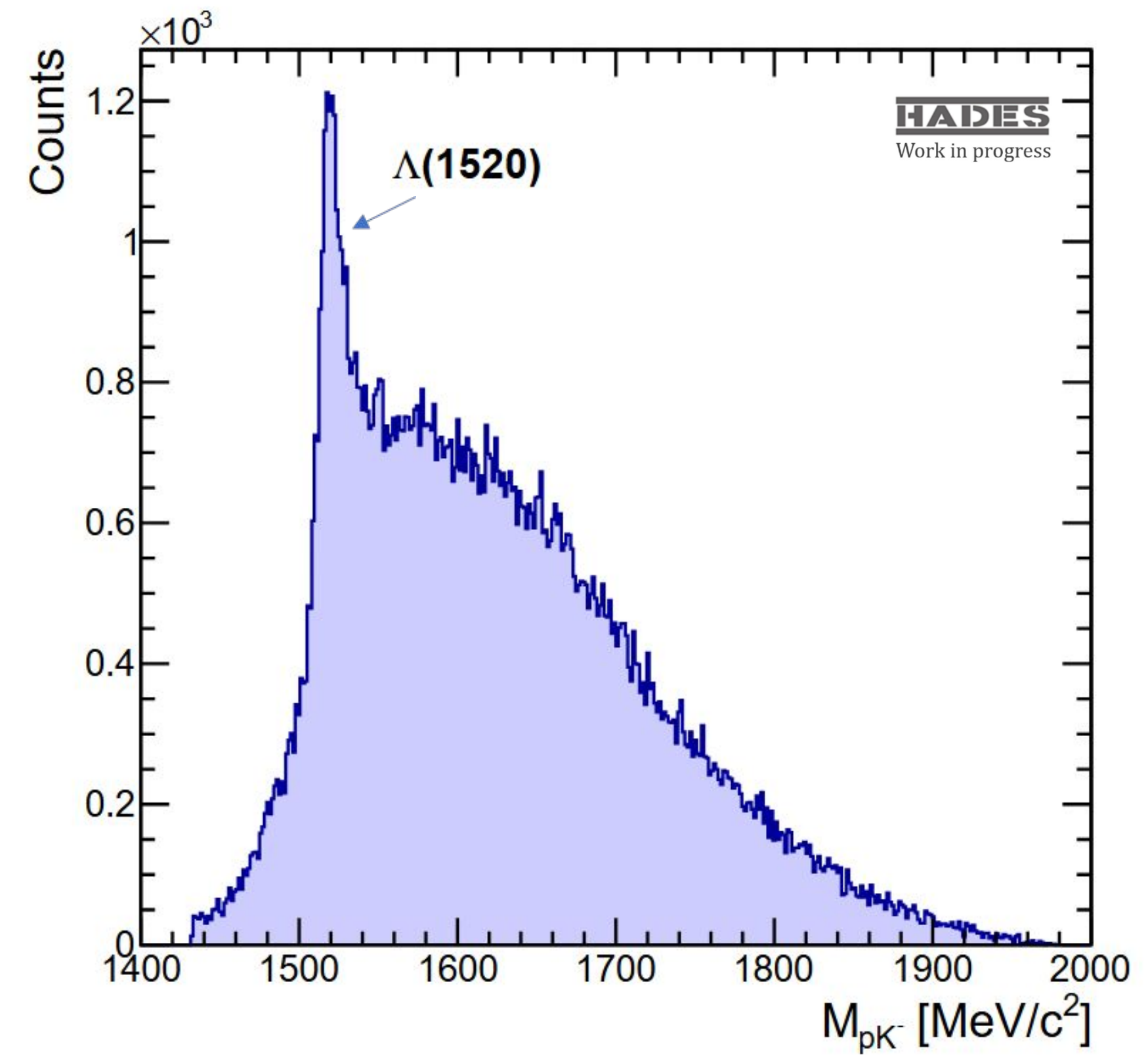
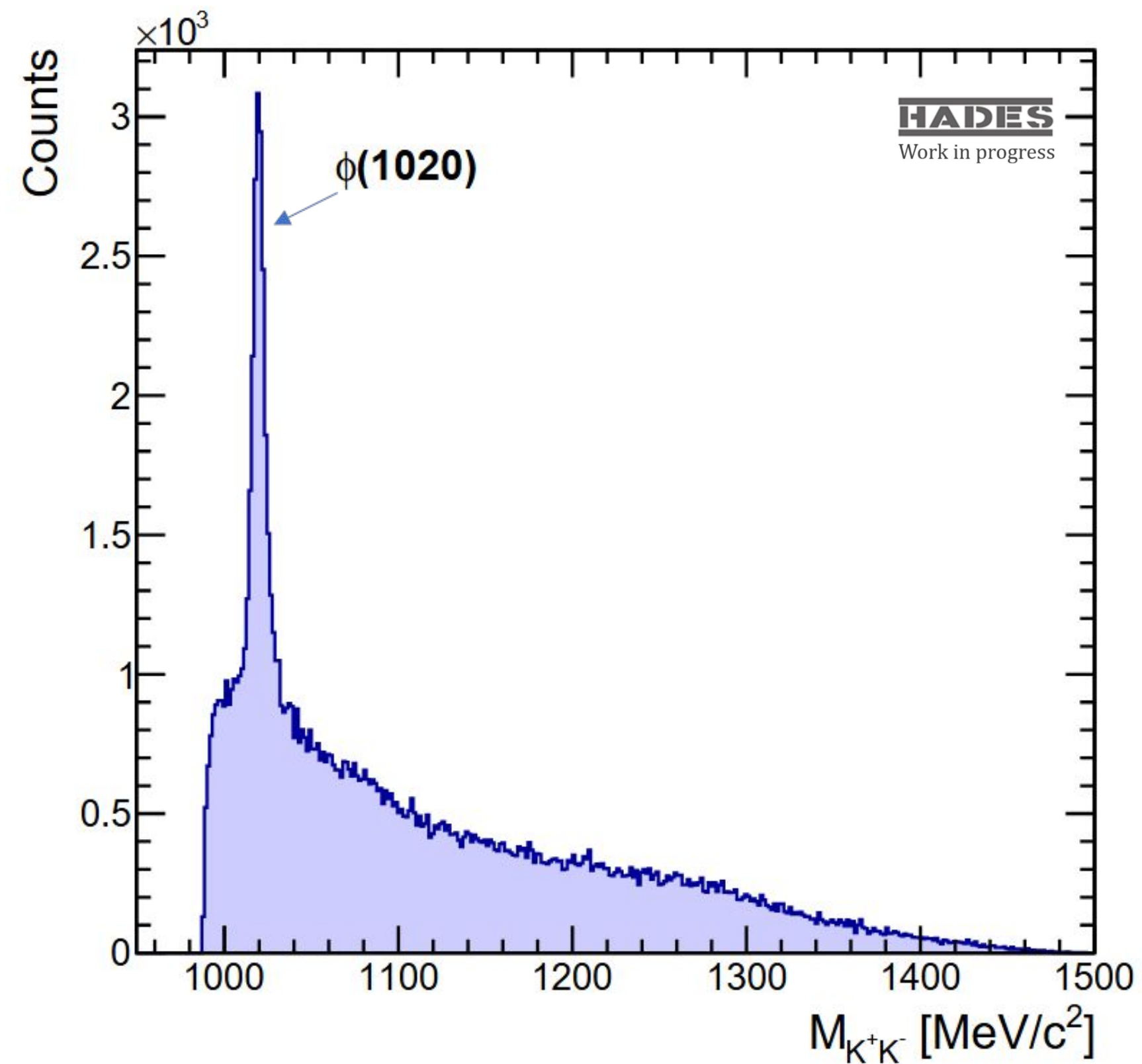
$pp \rightarrow pp\pi^+\pi^-$  ( $\sim 5000 \mu b$ )

$pp \rightarrow pK^+[\Lambda \rightarrow p\pi^-]$  ( $\sim 50 \mu b$ )

...

- February 2022 beam time, HF topology

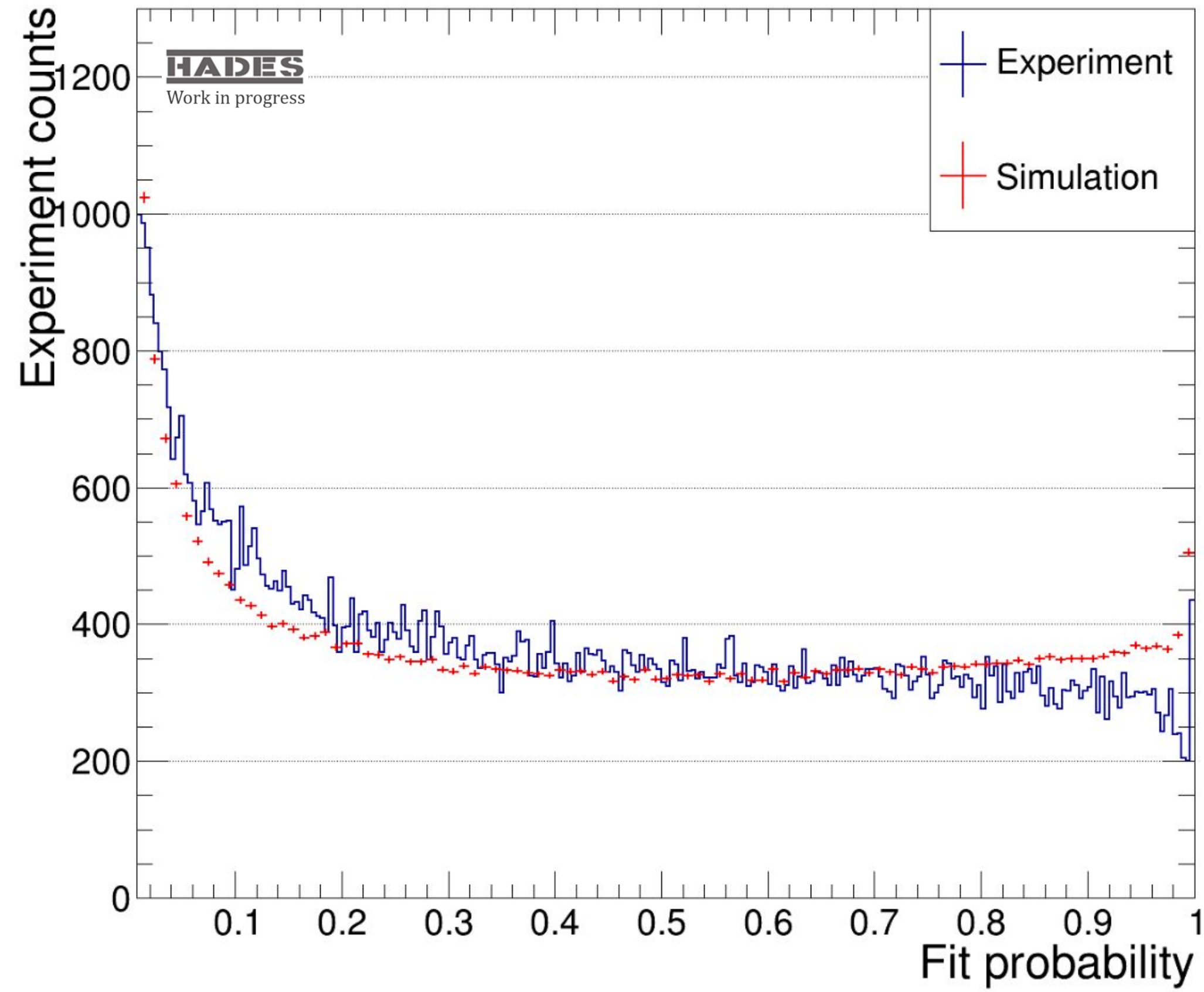
# Raw Distributions



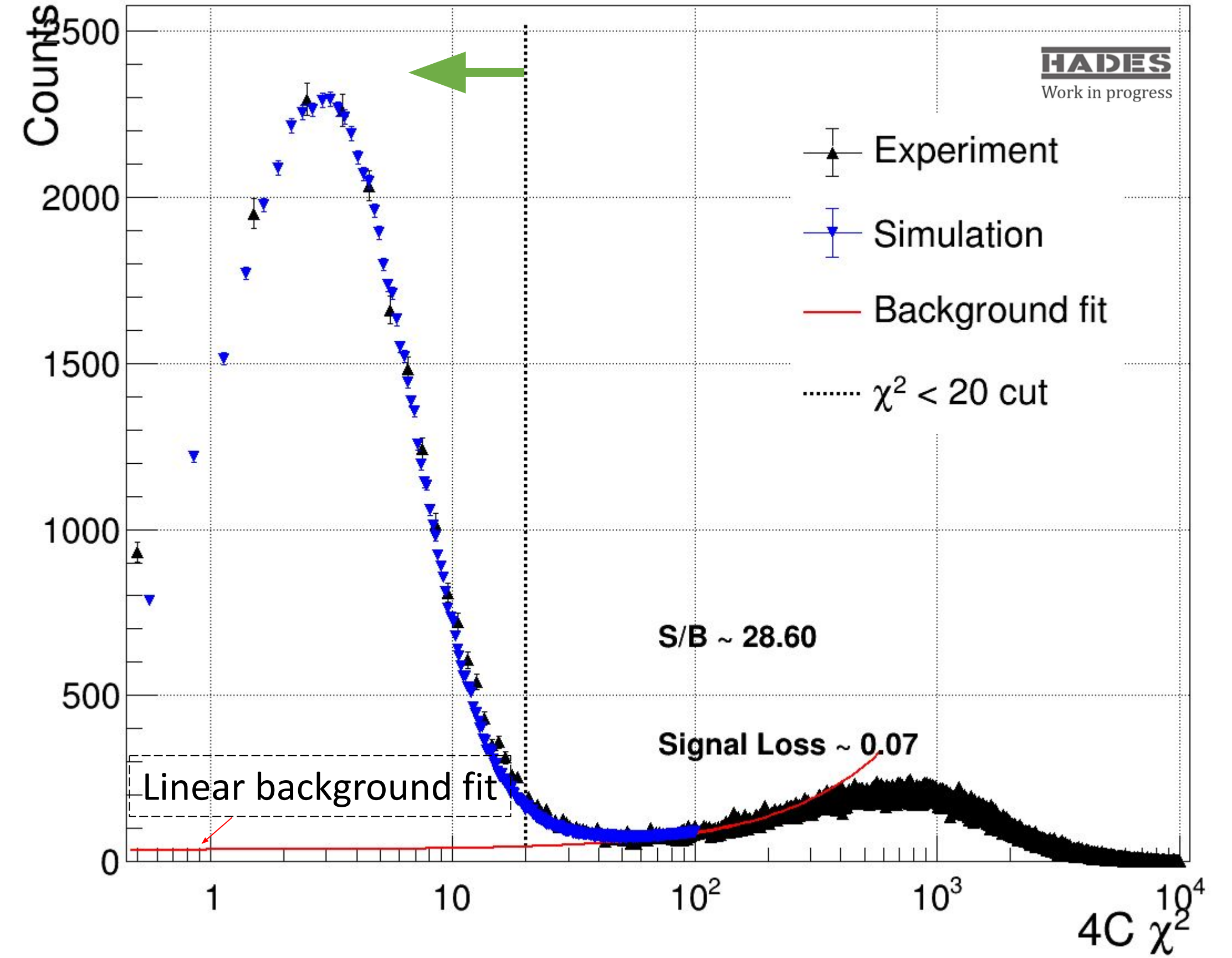
- Obtained after all selection cuts
- Filled with KR-shifted values

- Does kinematic refit (KR) work properly?
- Is background really low?

# Kinematic Refit



Sufficiently flat probability distribution



$S/B \sim 30$ ,  $S = 1.5 \cdot 10^5$

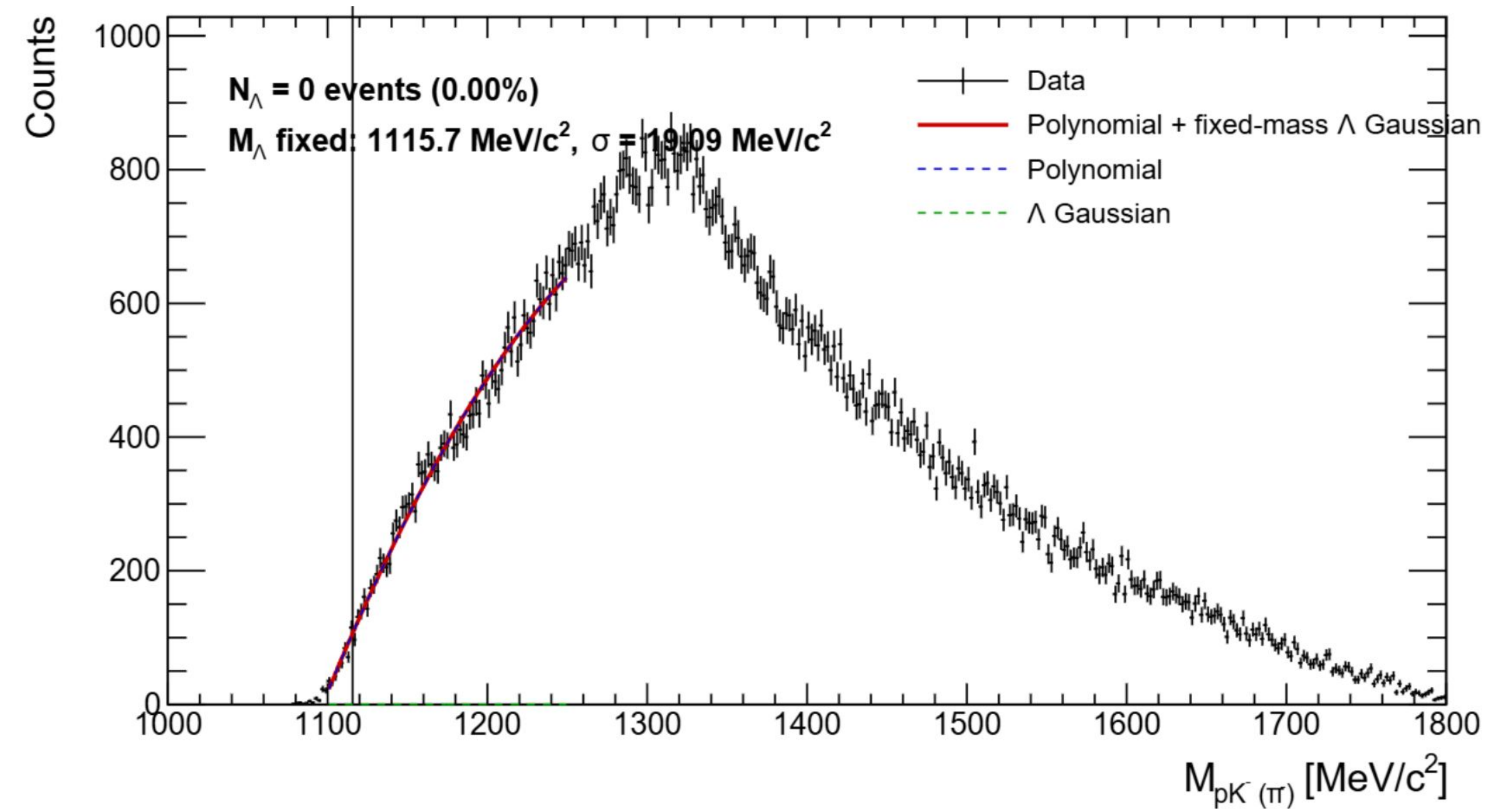
## Remaining Background Studies 1

$$pp \rightarrow pK^+ [\Lambda \rightarrow p\pi^-]$$

Lambda contribution,

Under the assumption of  $\pi - K$  misidentification

No contribution visible



## Remaining Background Studies 2

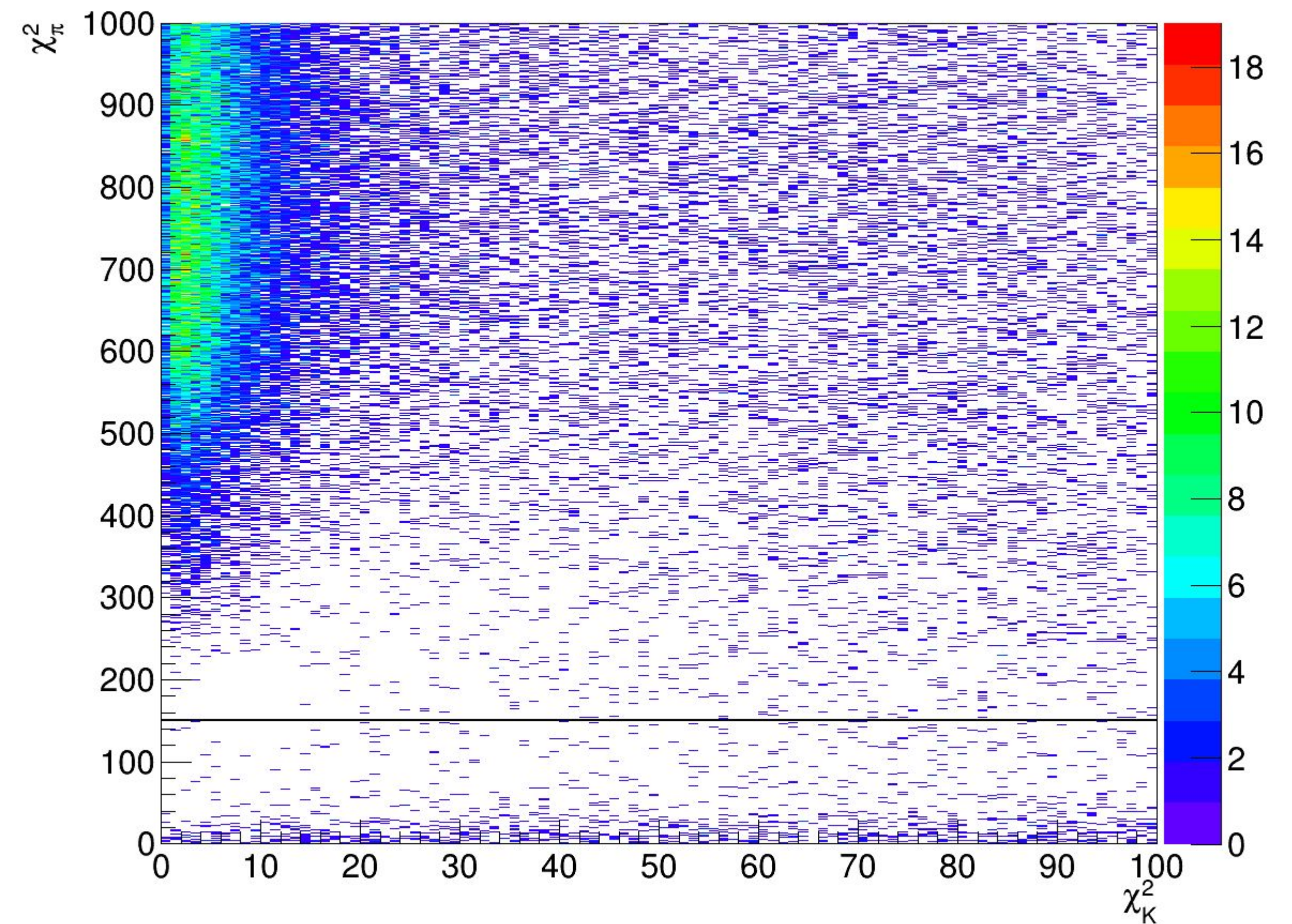


4C fit in a mass hypothesis of double K

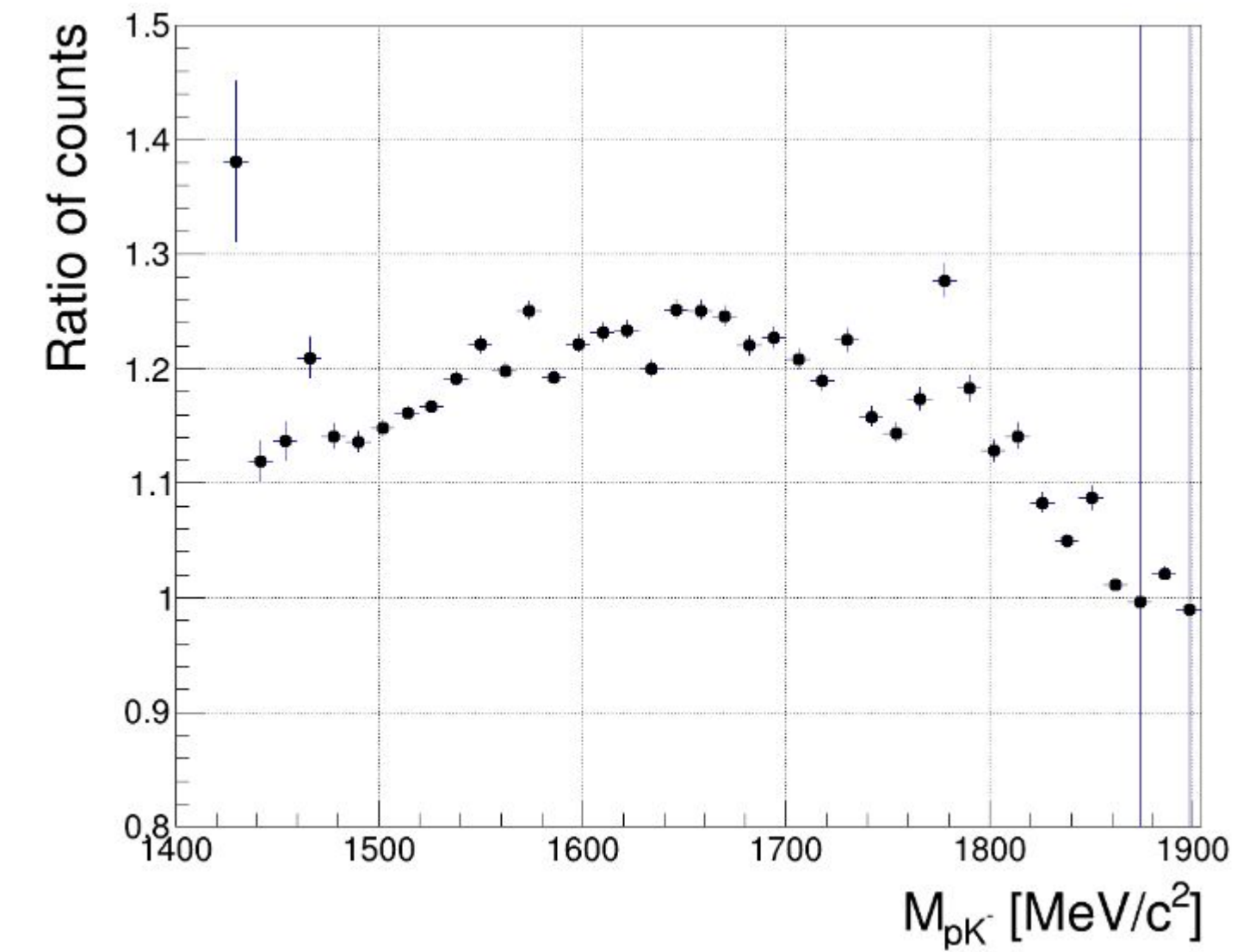
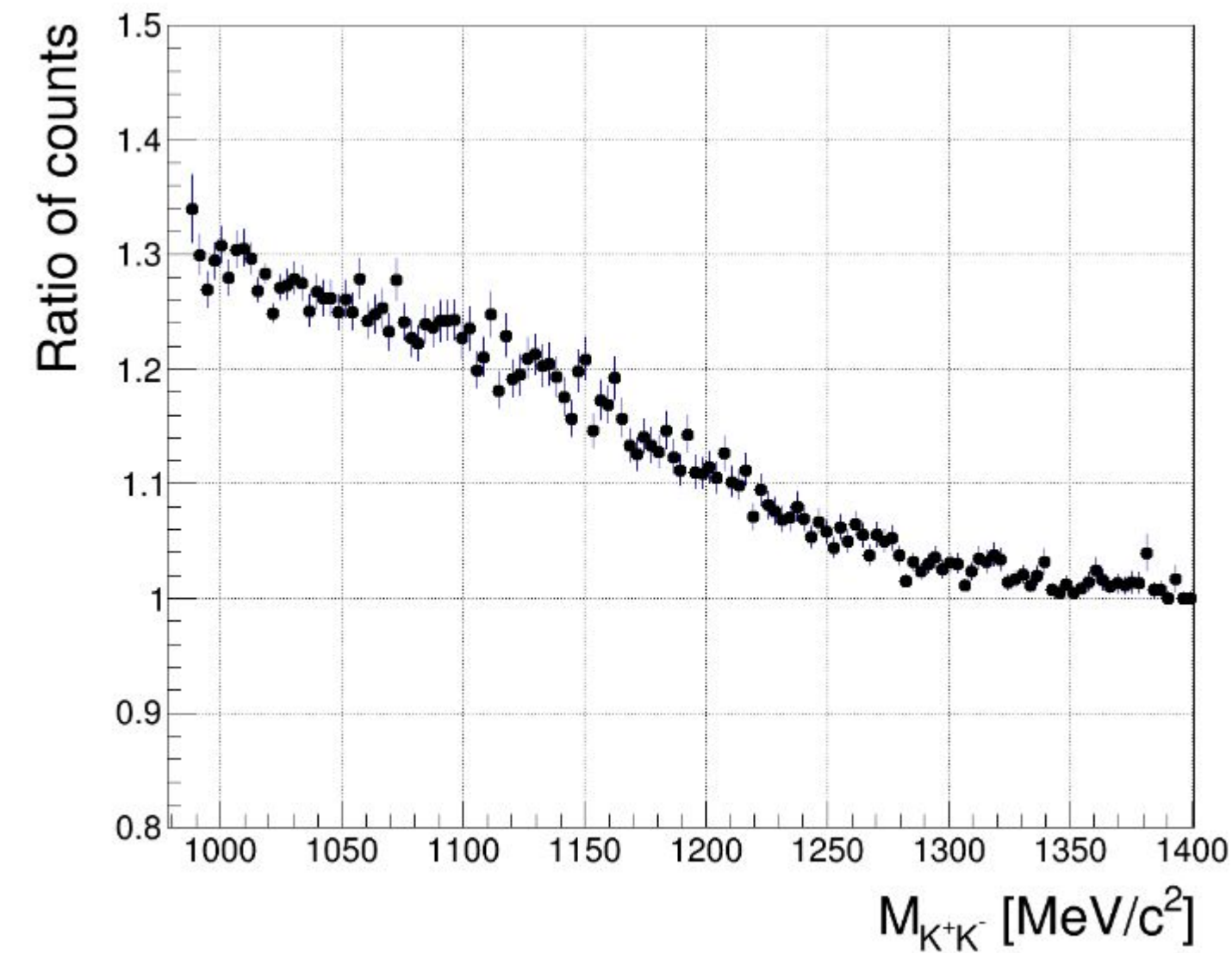
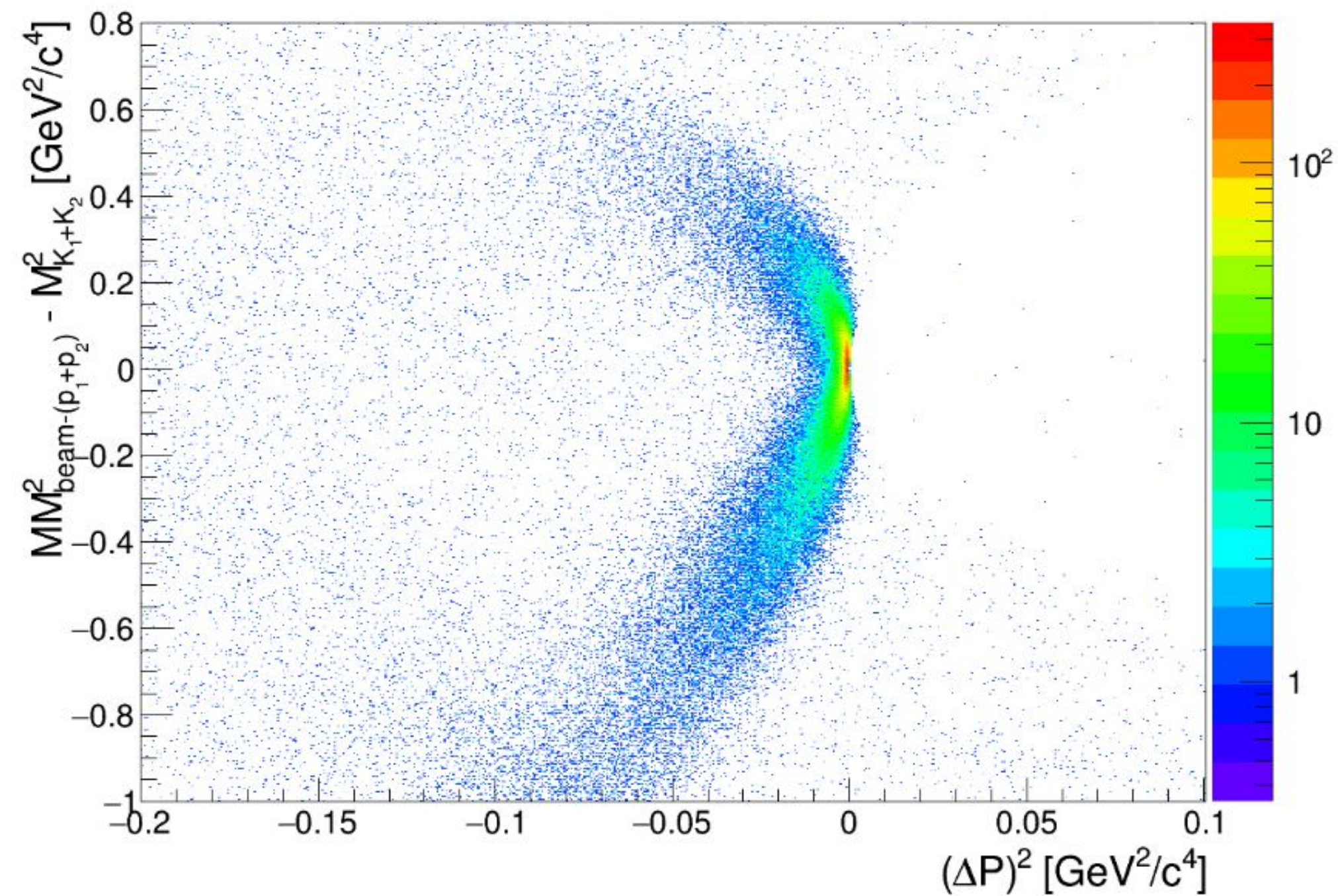
Against the fit with in a hypothesis of double  $\pi$

The line shows the cut that is currently used

Clear contribution is almost completely removed



## Remaining Background Studies 3

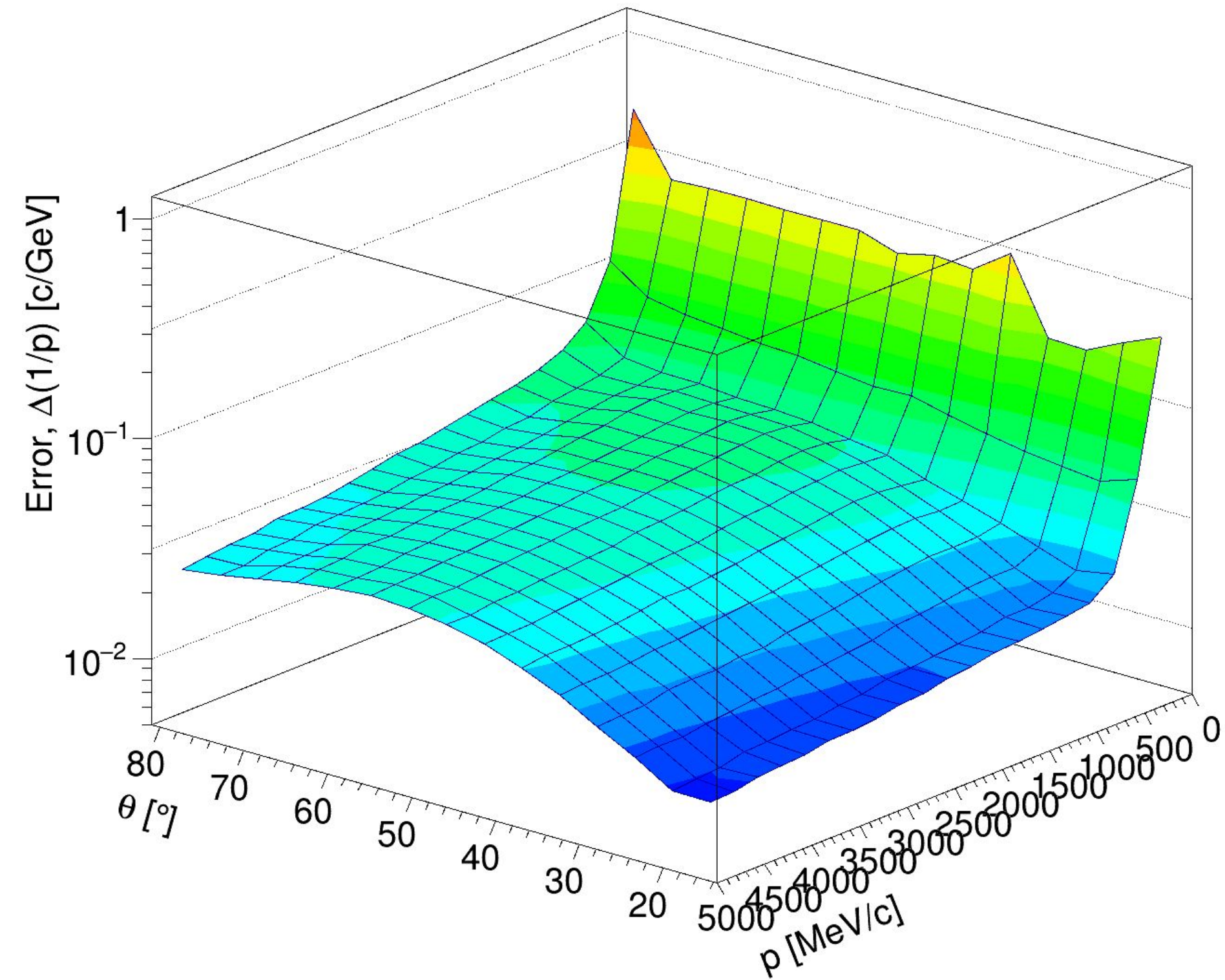


Study of extra kinematic variables

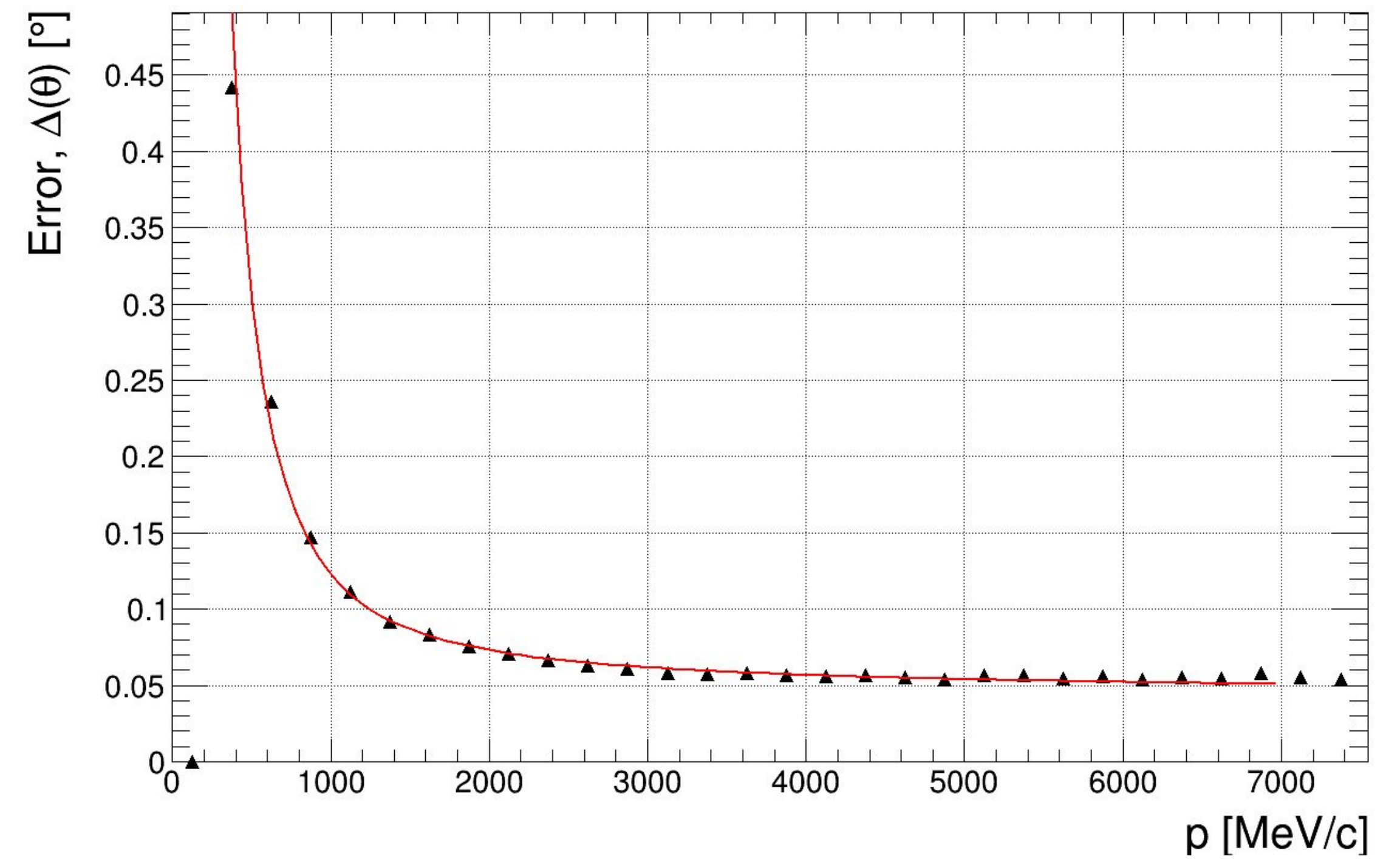
Shows that stricter cuts do not produce noticeable structures in the  $\phi(1020)$  and  $\lambda(1520)$  regions

+ Variations of the primary  $\chi^2$  cut in the backup

# Errors for KR

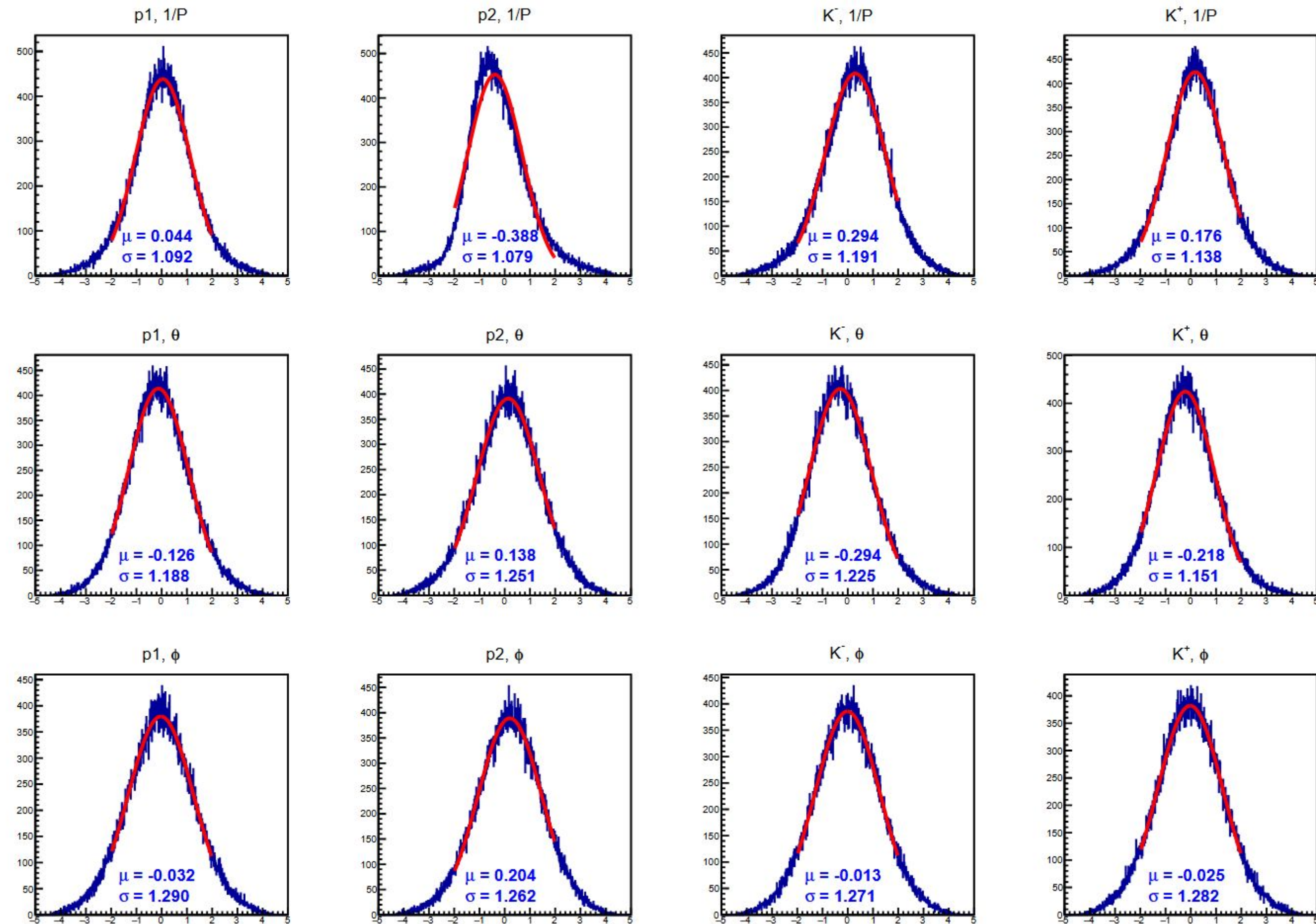


For main HADES particles

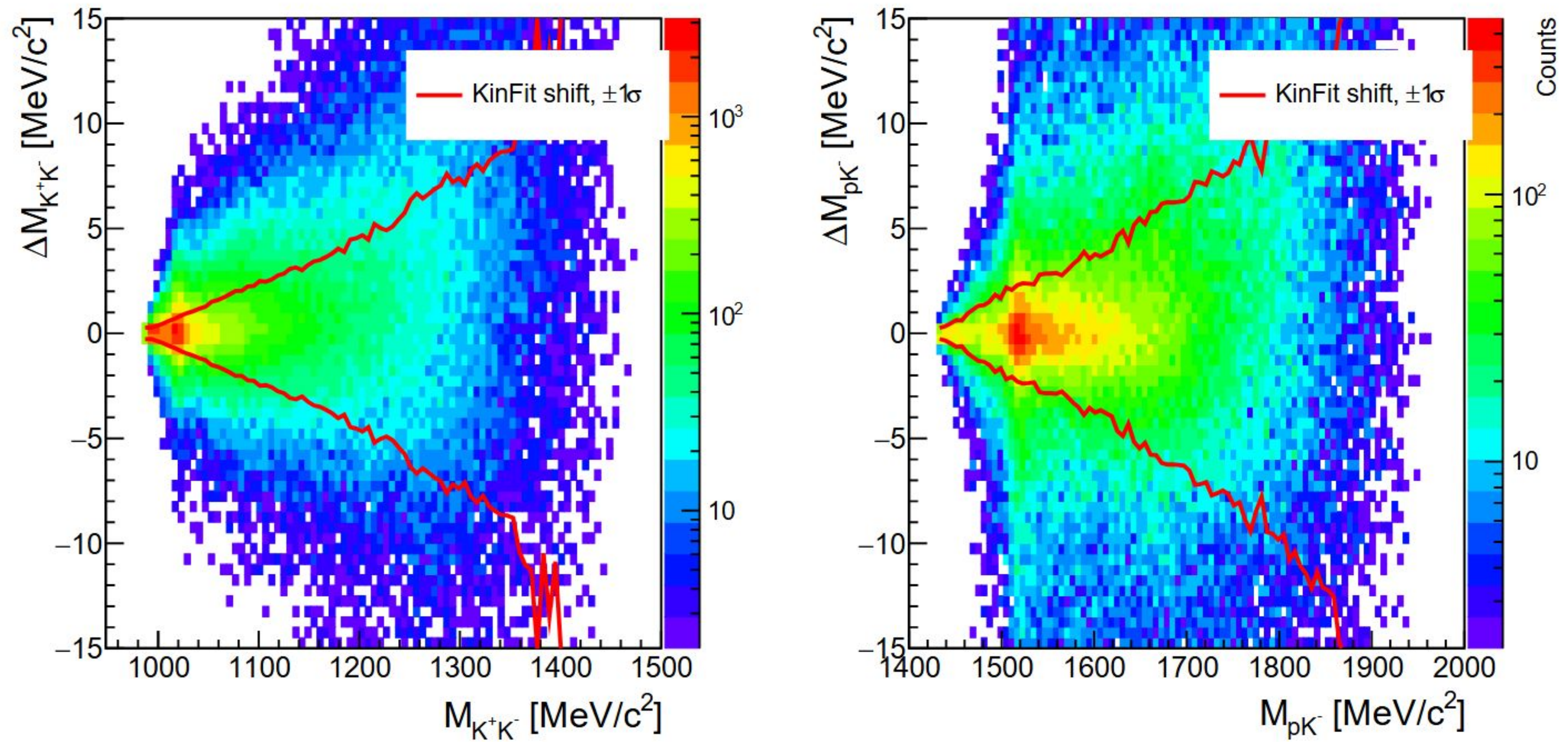


For Forward particles

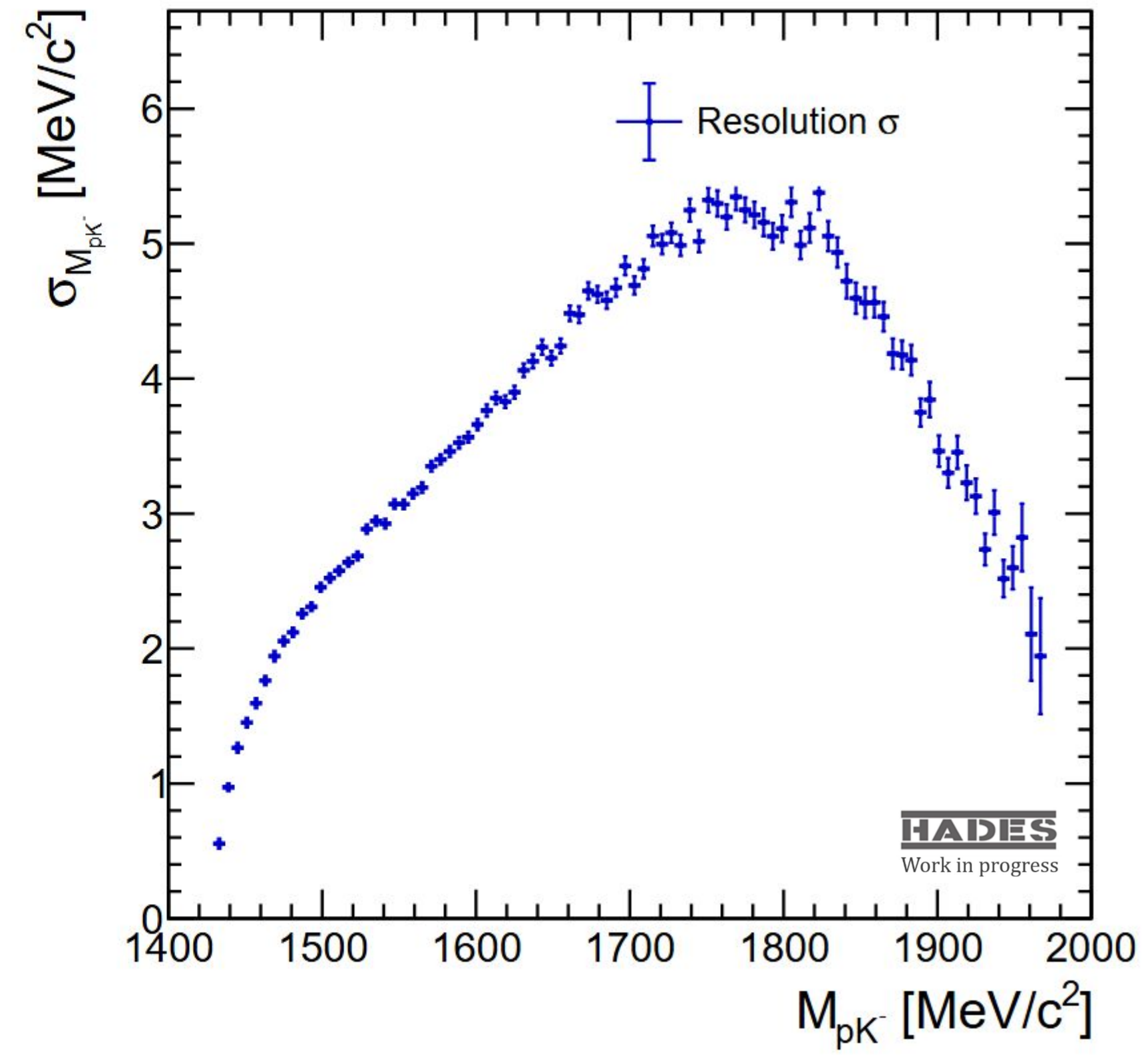
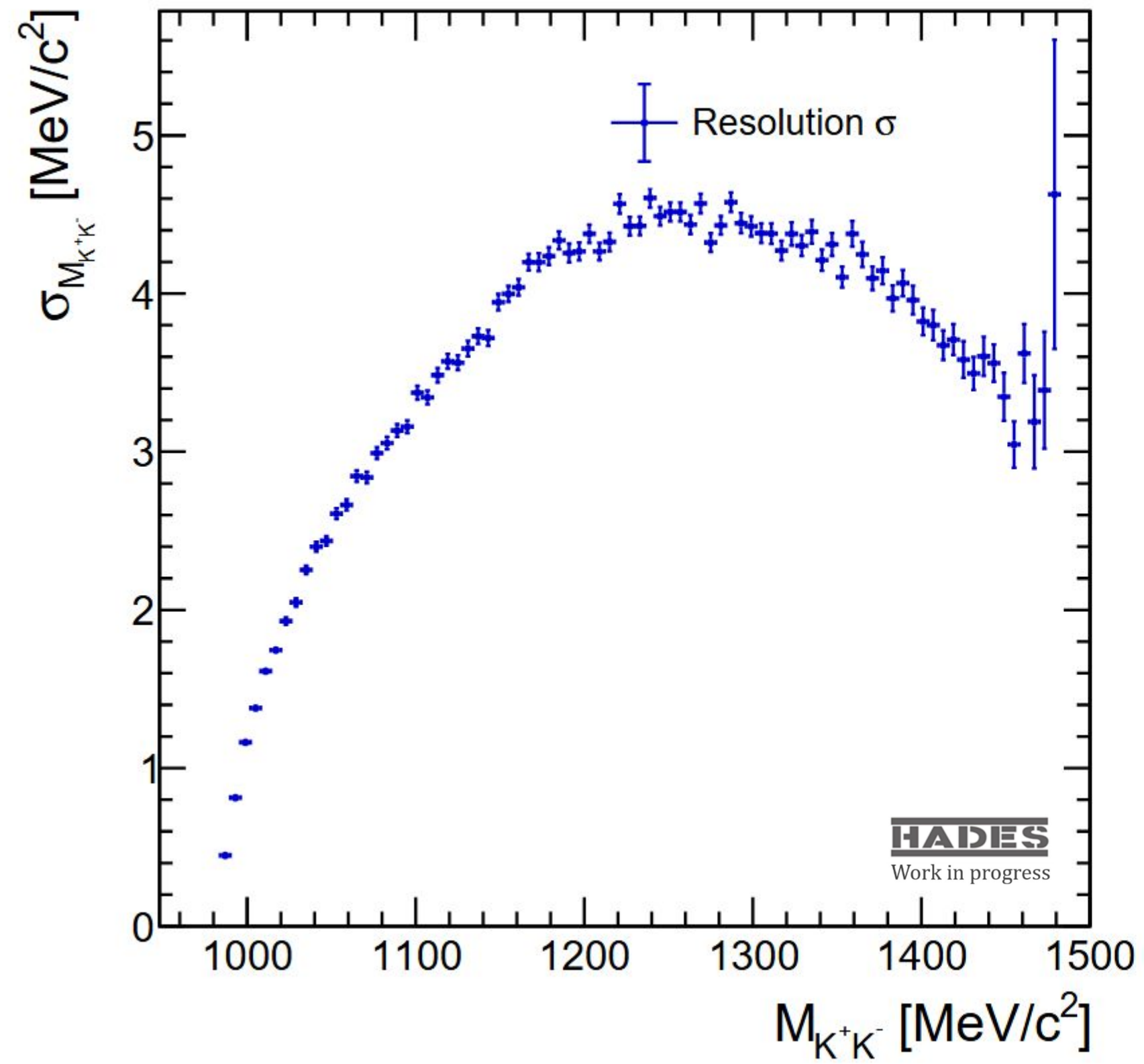
# Experimental Pull Distributions



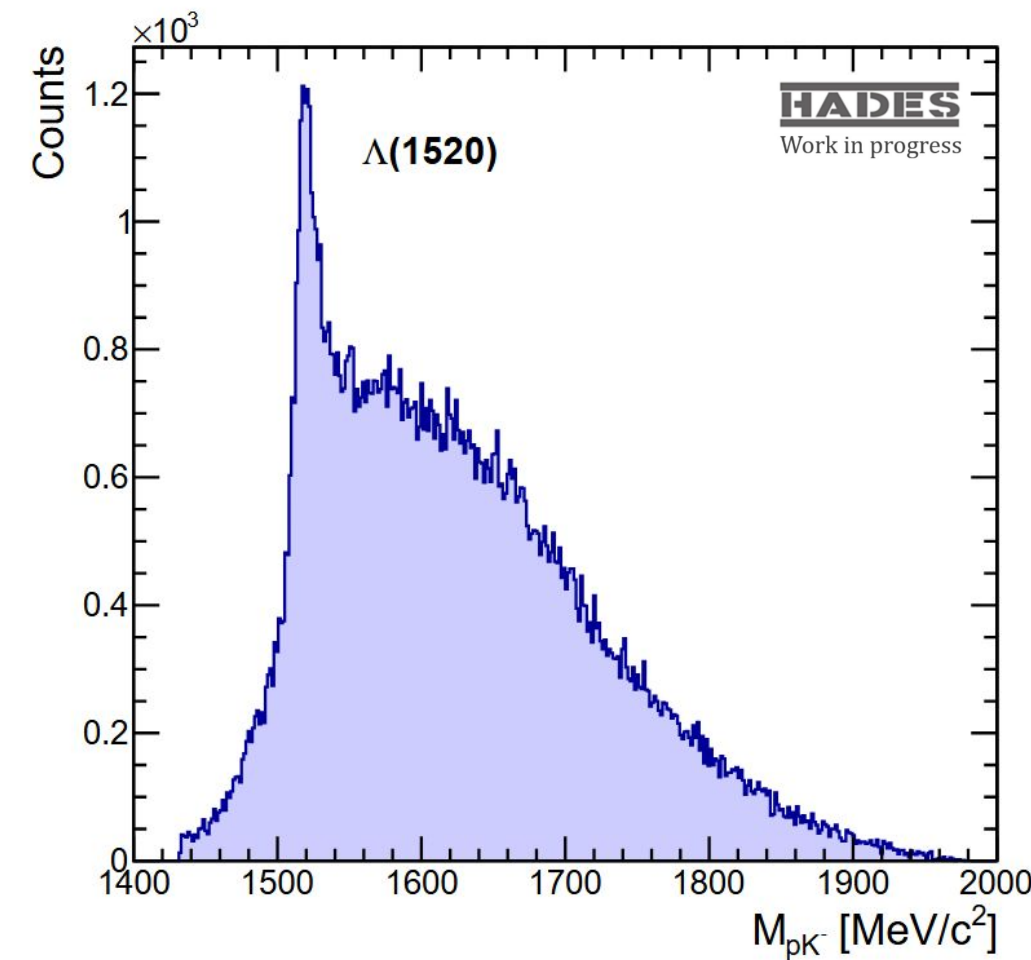
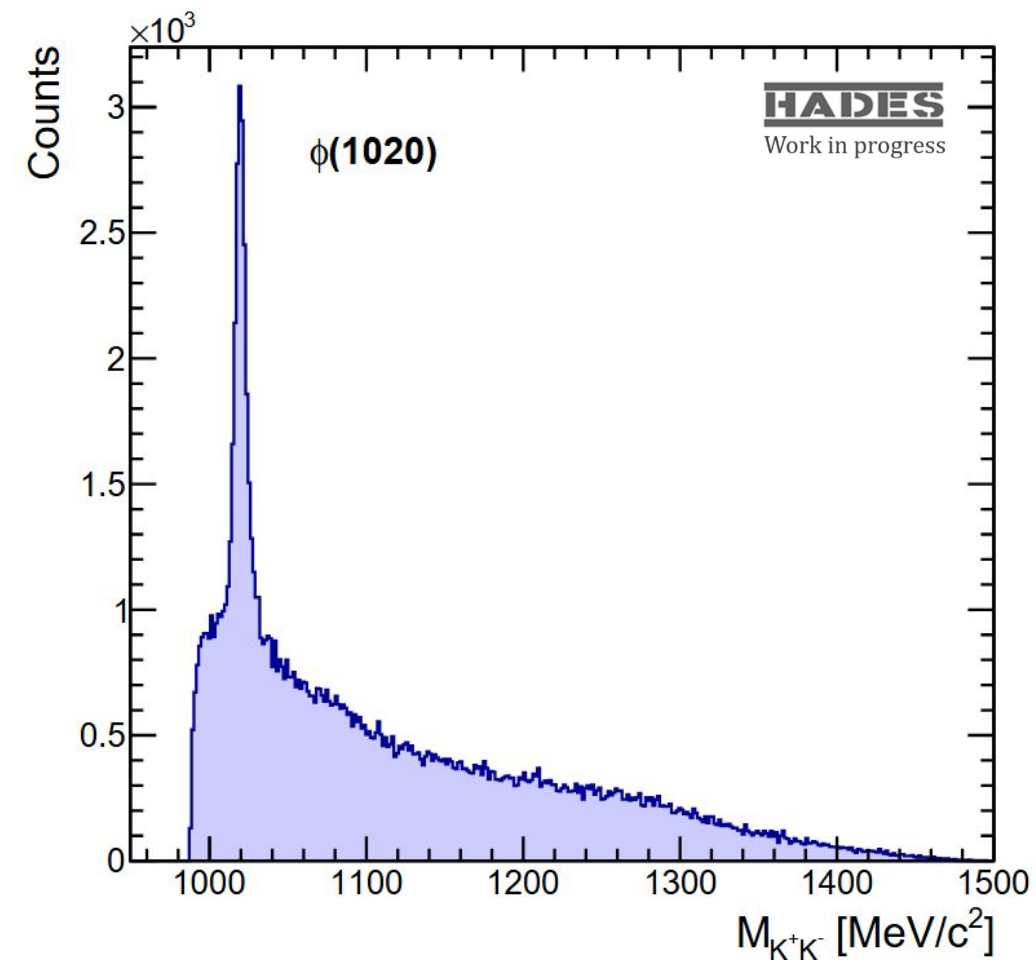
# KR Shifts of Invariant Masses



# Mass Resolutions



# Efficiency Times Acceptance Correction



- *Method:*  
Bin-by-Bin  
Phase Space Simulation

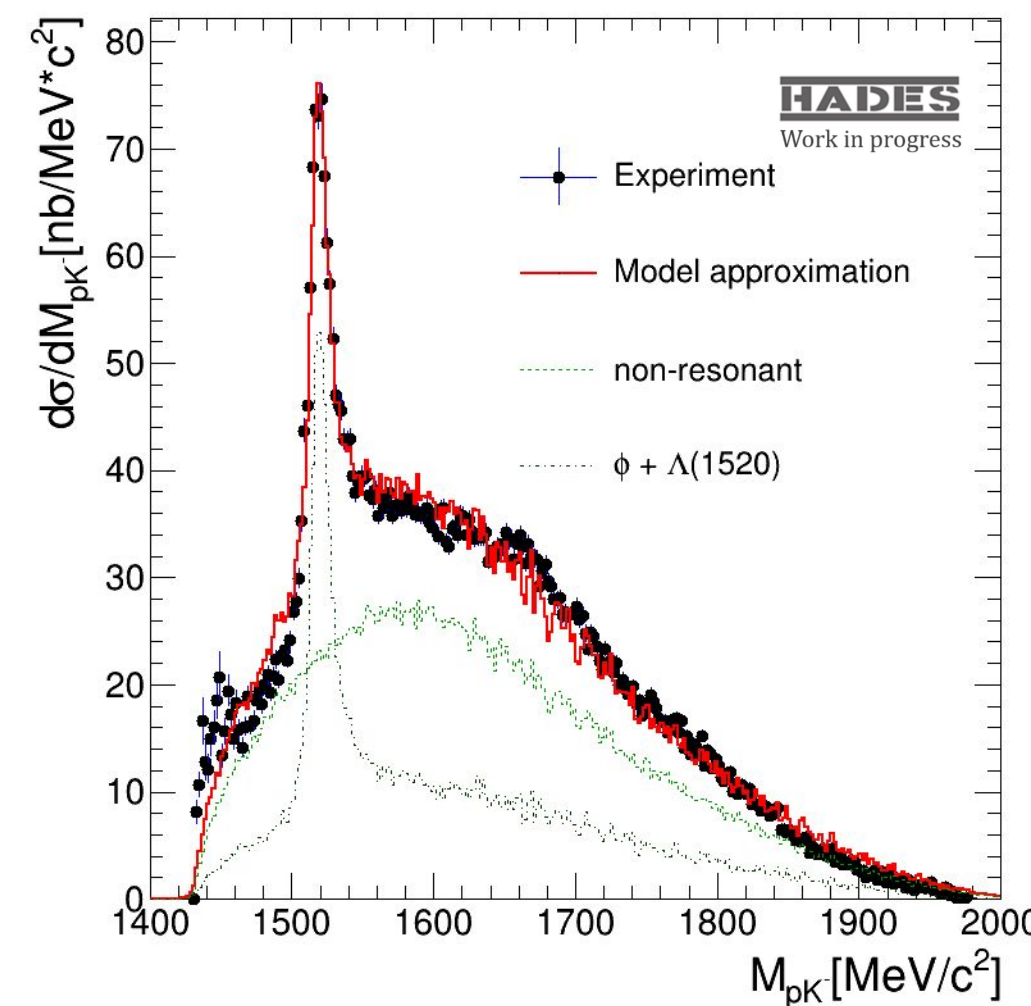
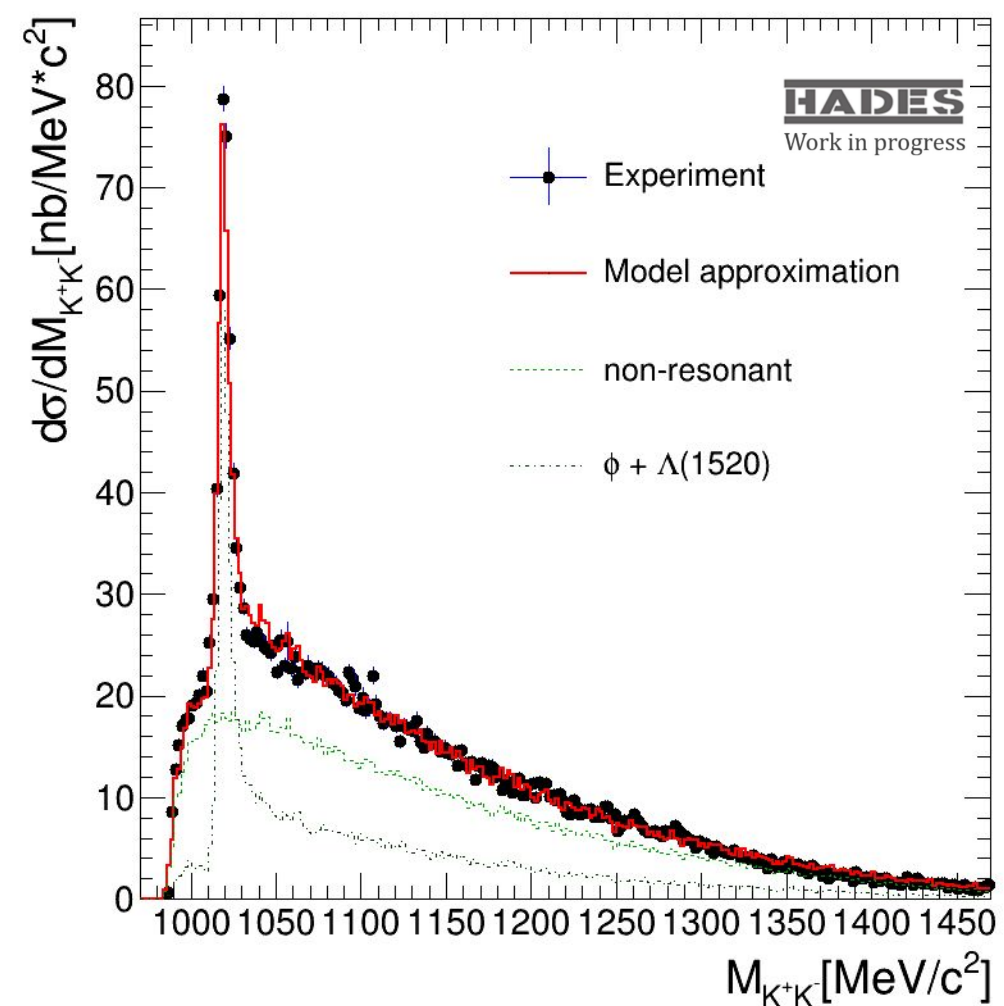
- *Parameterization:*

Main resonances in 2D, 3D, or 4D:

$$M(K^+K^-) + M(pK^-)$$

$$M(K^+K^-) + M(pK^-) + \theta_{\phi \rightarrow KK}^{GJ}$$

$$M(K^+K^-) + M(pK^-) + \theta_{\phi \rightarrow KK}^{GJ} + \varphi_{\phi \rightarrow KK}^{GJ}$$



- What are systematic uncertainties of this correction?  
(from PID, acceptance, parameterization)



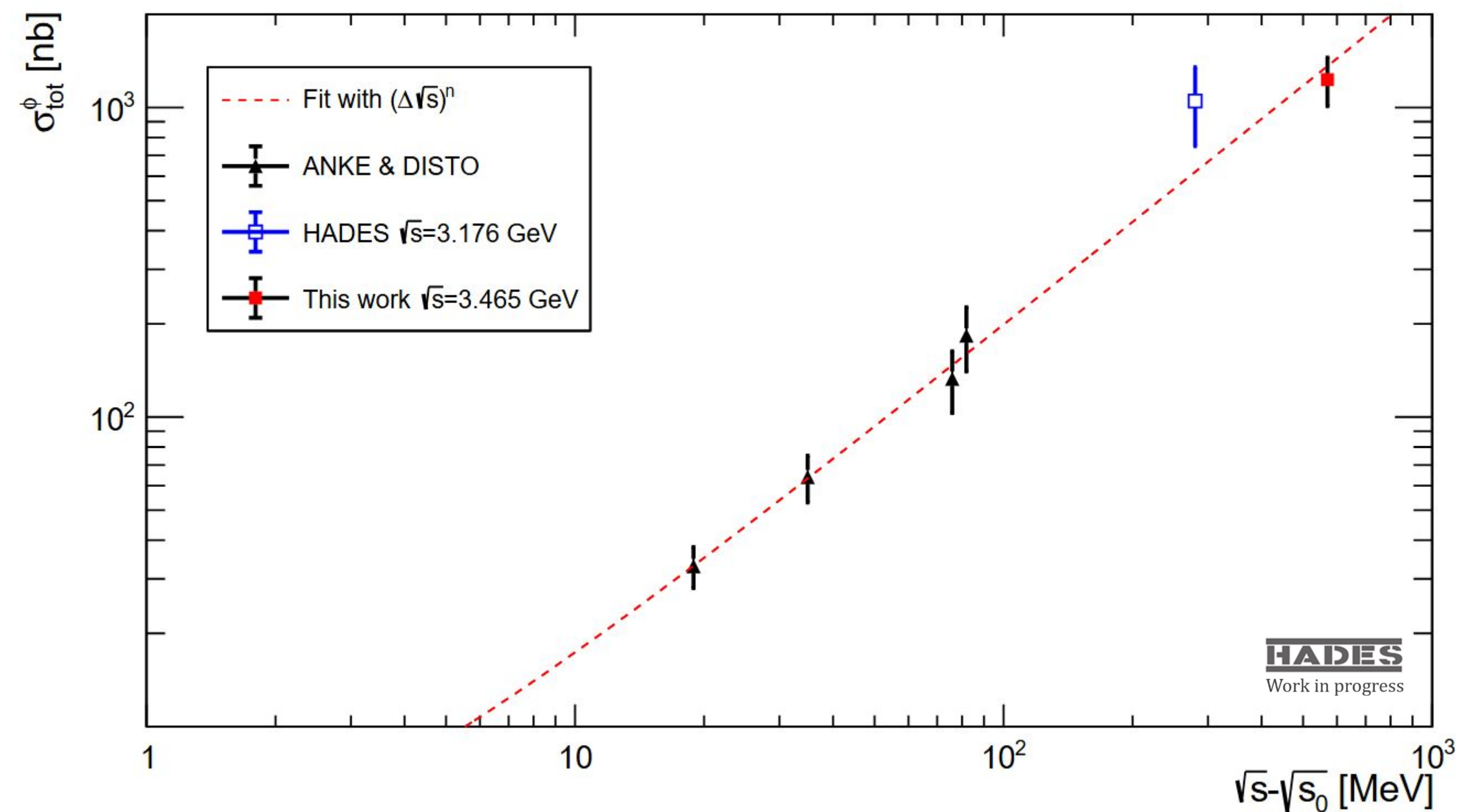
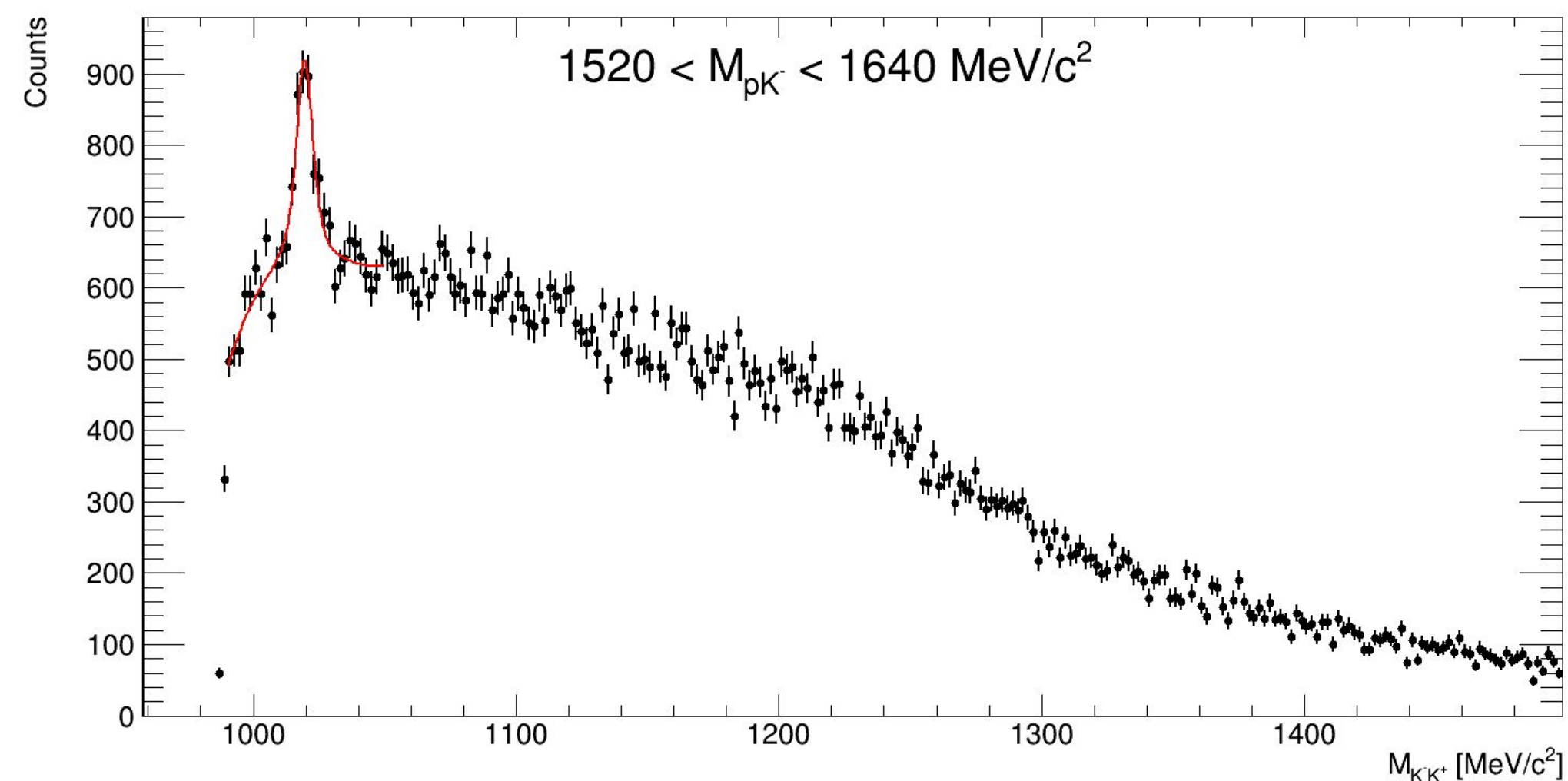
## Test Without KR - pp $\phi$ (1020) Cross Section

### Selection:

1. Same as in the main analysis
2. Before KR
3. Total FS momentum not too small compared to IS

### Calculation:

1. Phase space sim, bin-by-bin, 2D map, M(KK) vs M(pK)
2. Fit M(KK) in each bin of M(pK) for N(exp)
3. Weight efficiency with the Voigt shape from exp



**Cross section normally = 1230 +/- 150 nb**

**Cross section no KR = 1380 +/- 175 nb**

# Particle Identification with DANN

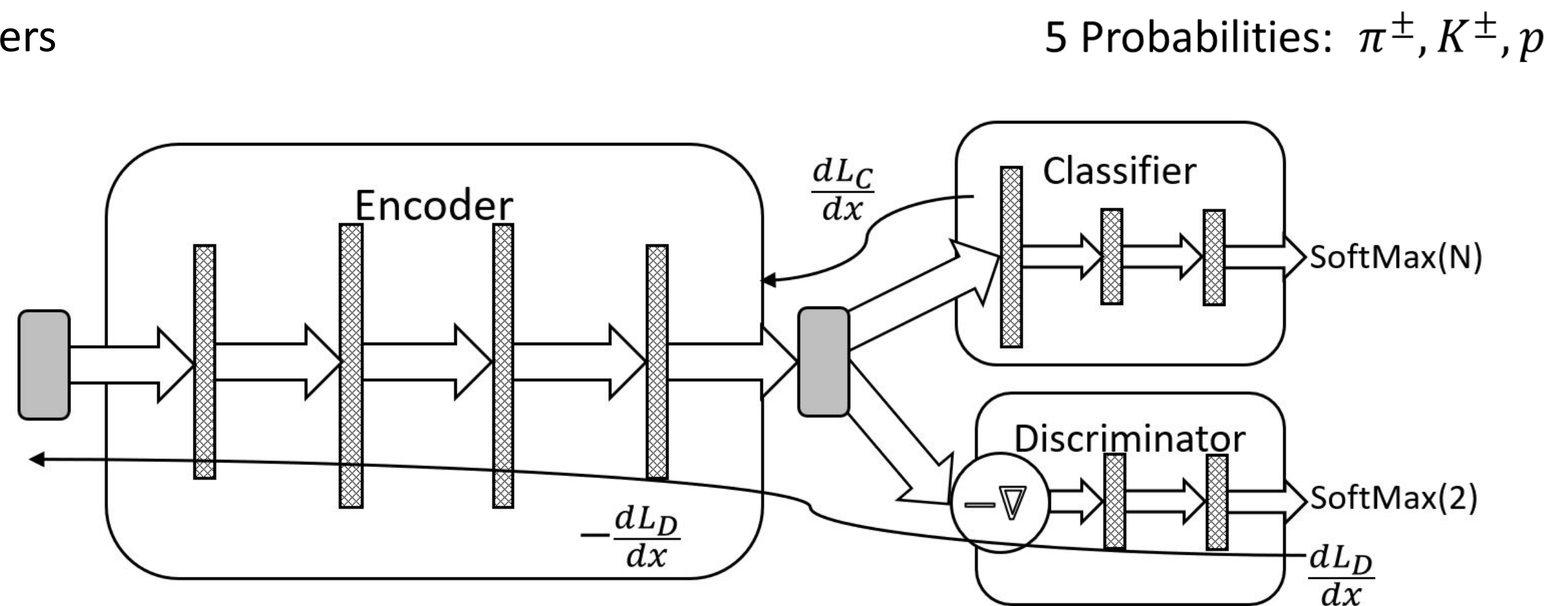
- Traditional PID systematic uncertainties  $\sim 10\%$
- Improve PID and reduce systematic error (Sim-Exp consistency)

✓ All information simultaneously,  
better performance

Input parameters

- *Moment*
- *Charge*
- *Theta*
- $dE/dx_{M1}$
- *Beta*

$$+ \beta_{theory}^i(p) - \beta_{exp}^i \times 3$$



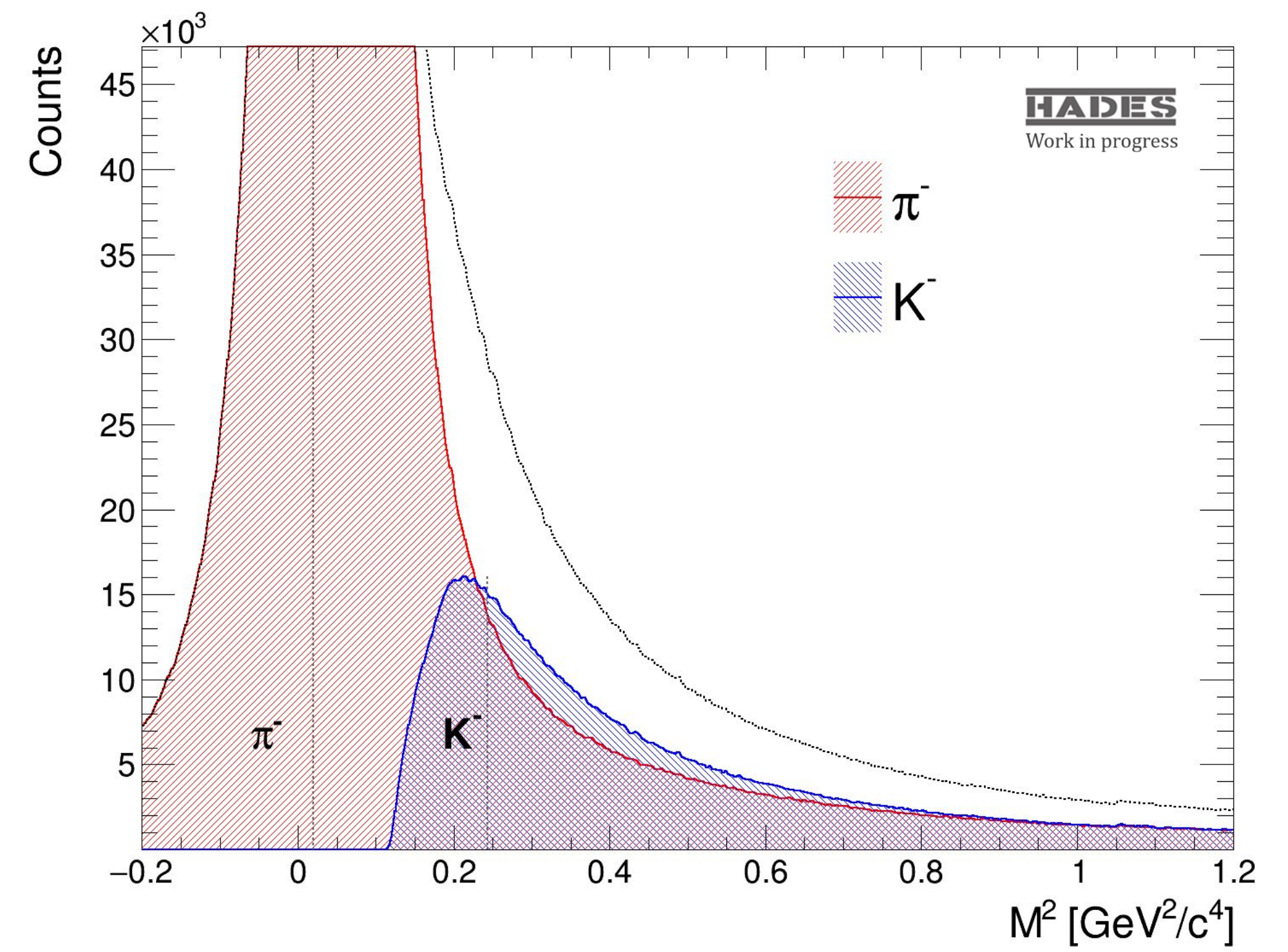
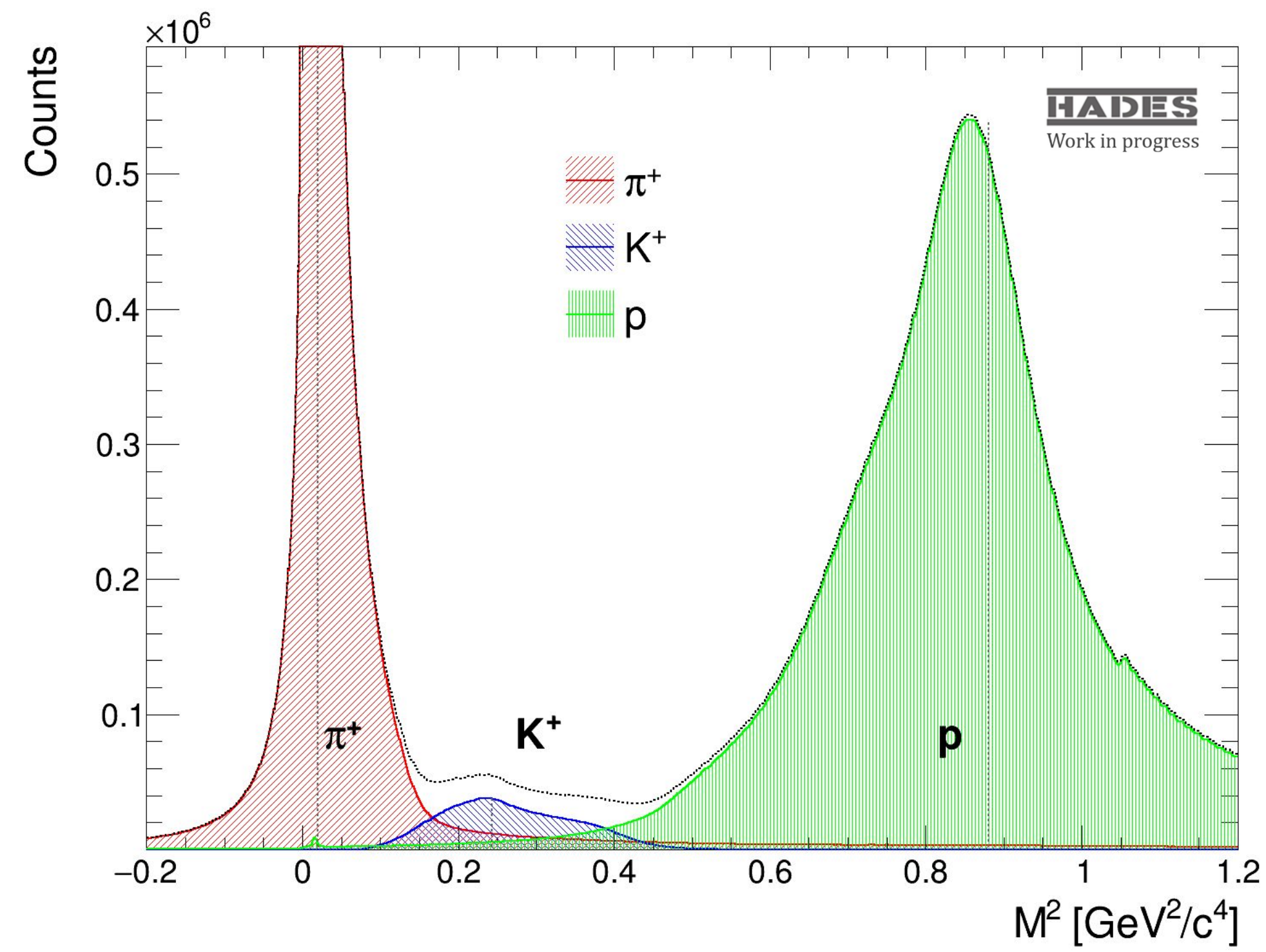
✓ Operates with probabilities,  
flexible classification

✓ Less sim-exp difference

# Mass Distributions

Mass distributions overlap, while keeping contaminations in K low.

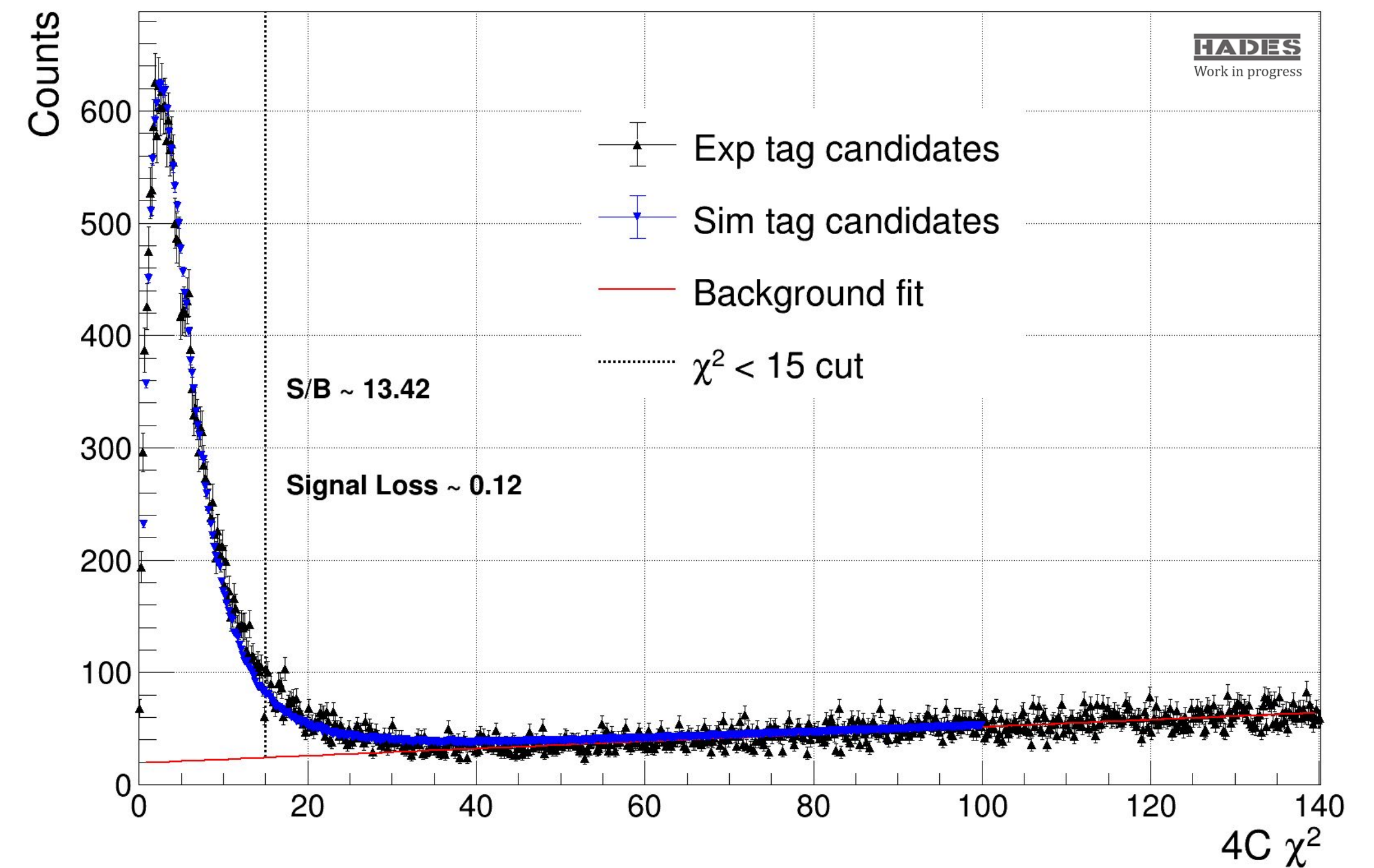
\*Experiment



# ML-PID Tag-and-probe Procedure

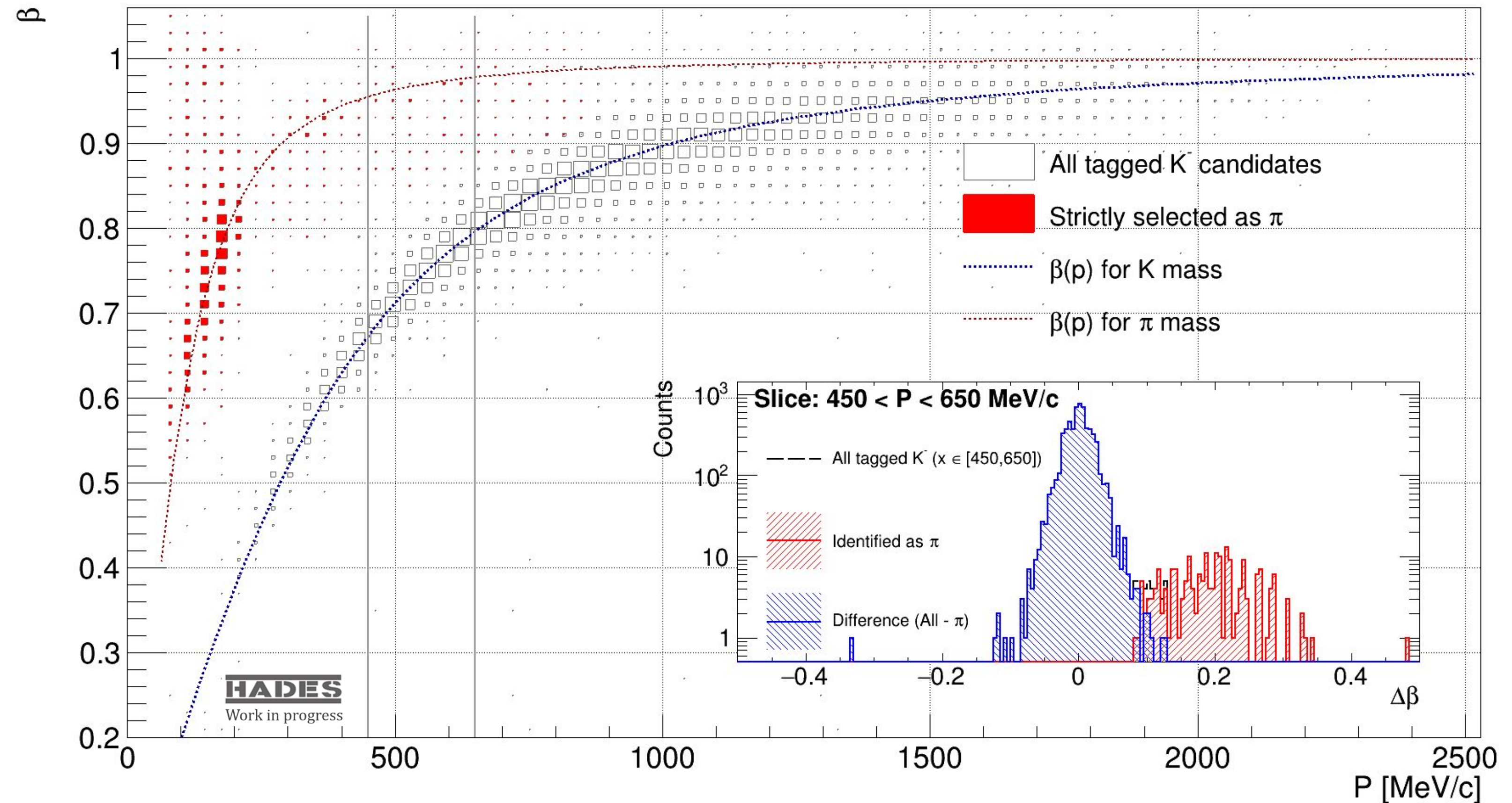
1. Do strict PID for all particles except one:  $ppK^+ / pp\pi^-$  ( $K^- / \pi^+$ ).
2. Select a remaining particle with  $\bar{q}$  as  $K^- / \pi^+$ .
3. Apply 4C kinematic refit ( $ppK^+K^- / pp\pi^+\pi^-$ ).
4. Choose the lowest  $\chi^2$  combination, apply strict cut.
5. Apply PID to the tagged  $K^- / \pi^+$ .

□ Measure efficiency and purity (misidentification rates) vs P



# ML-PID Tag-and-probe Procedure

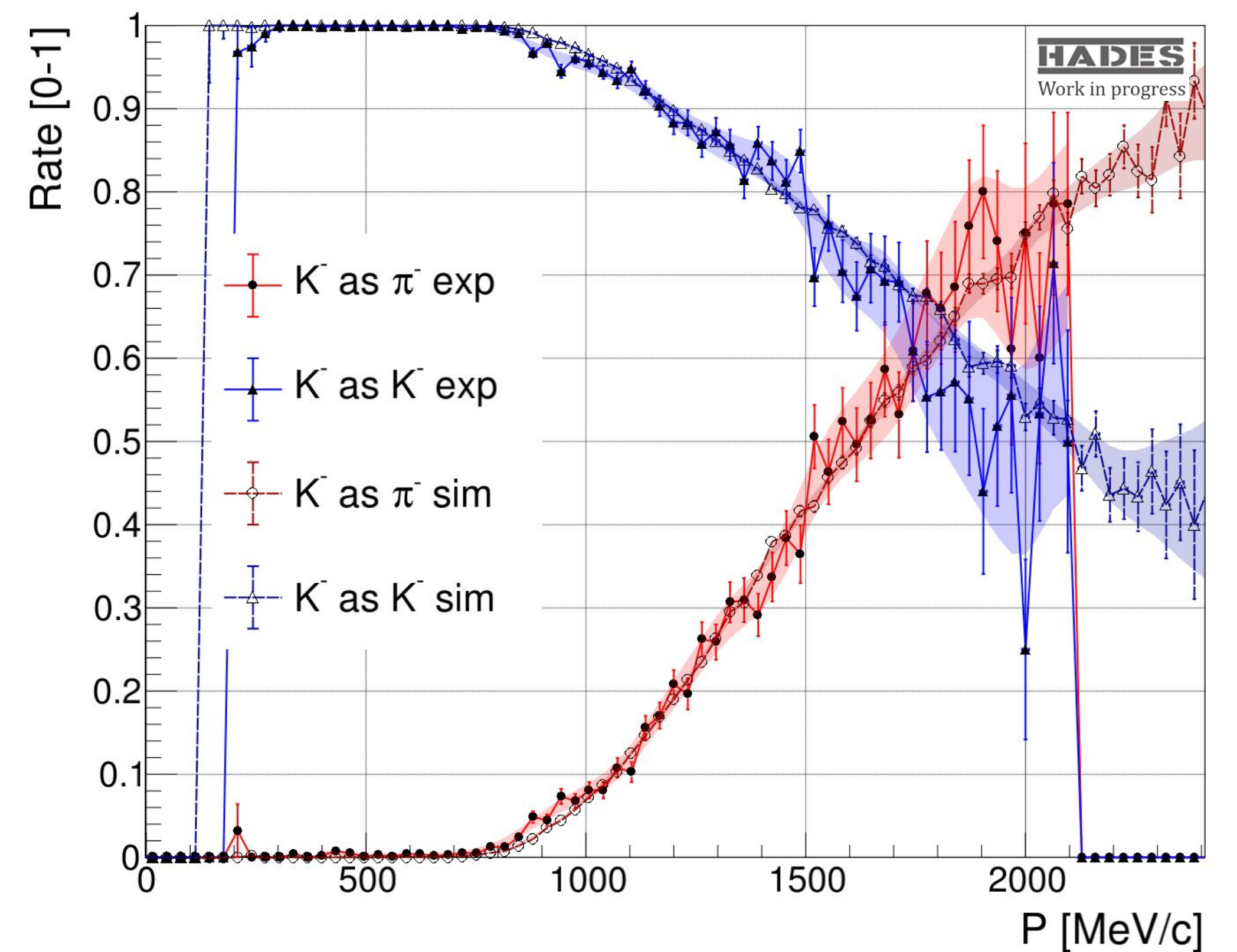
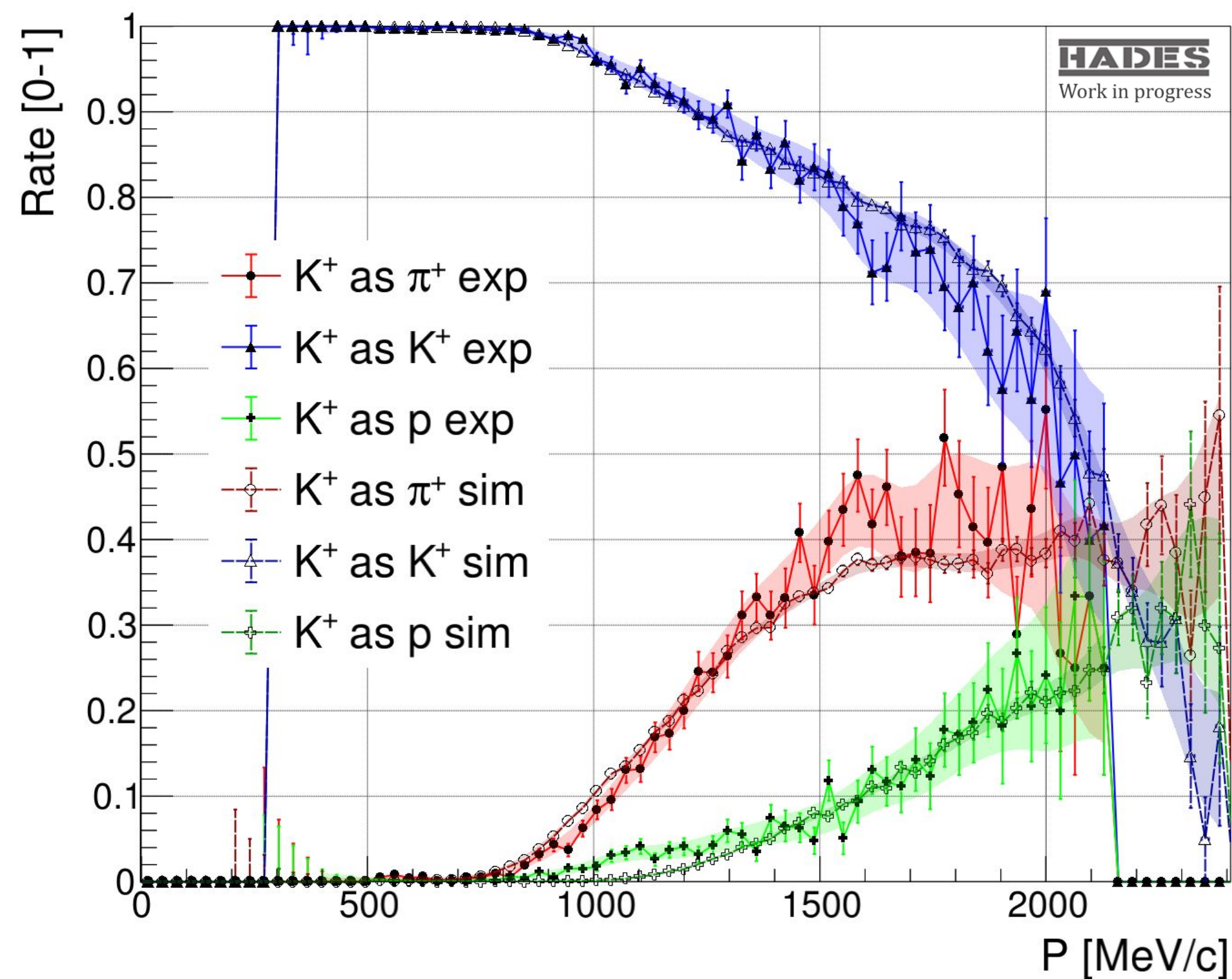
- Remaining kaon tag contamination is efficiently removed (see the inset).
- The mainly background-populated area contains  $\ll 1\%$  kaons (based on sim).
- ✓ Clean datasets for  $\pi, K, p$  obtained.



# Momentum Dependence of Kaon Efficiency and Purity

Selection efficiency and “purity” vs momentum

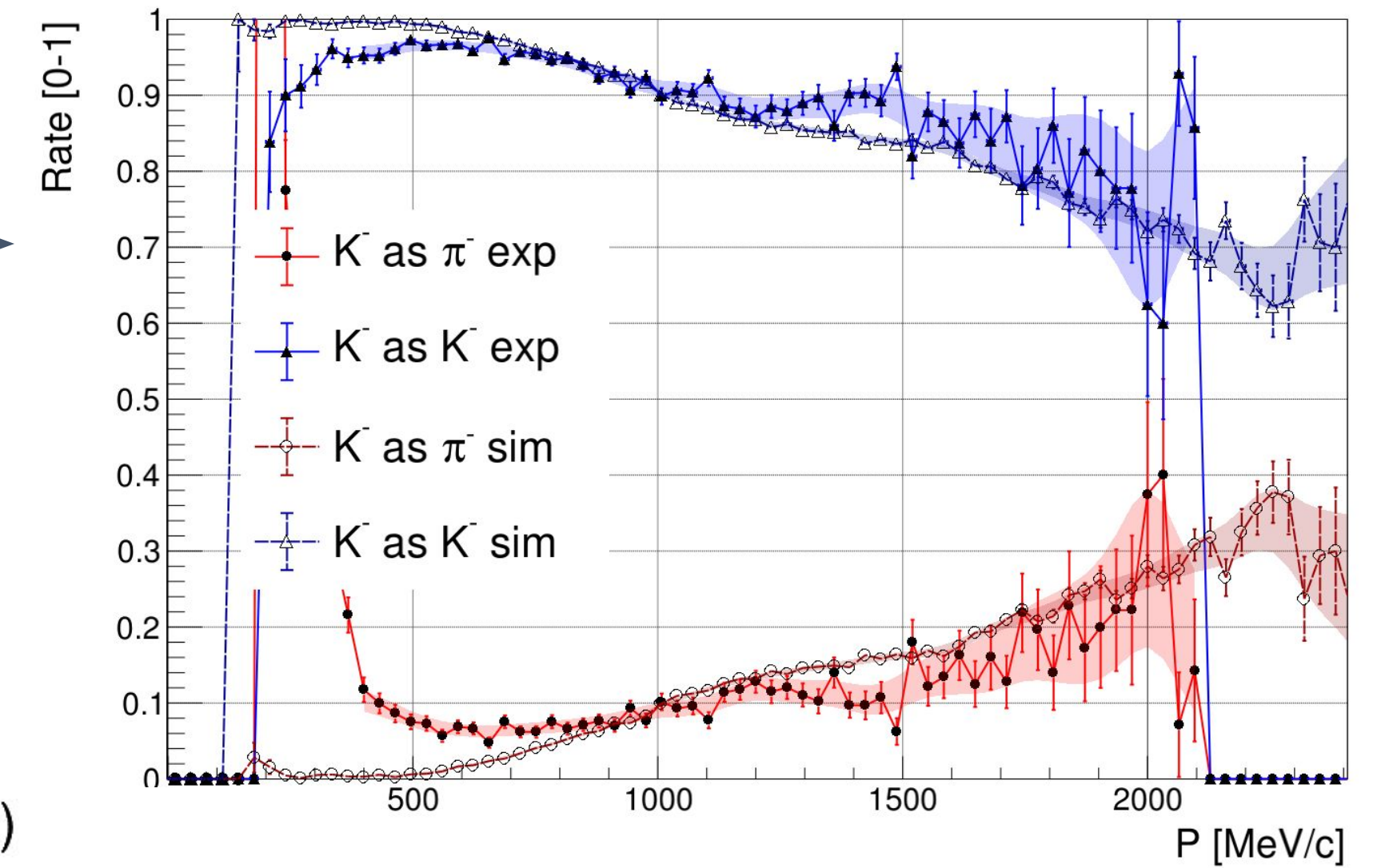
\*Share of particles being identified as  $C_i$  with loose cuts (prob > 35%) → Sum is more than 1



✓ DANN sim-exp agreement (< 1% per particle)

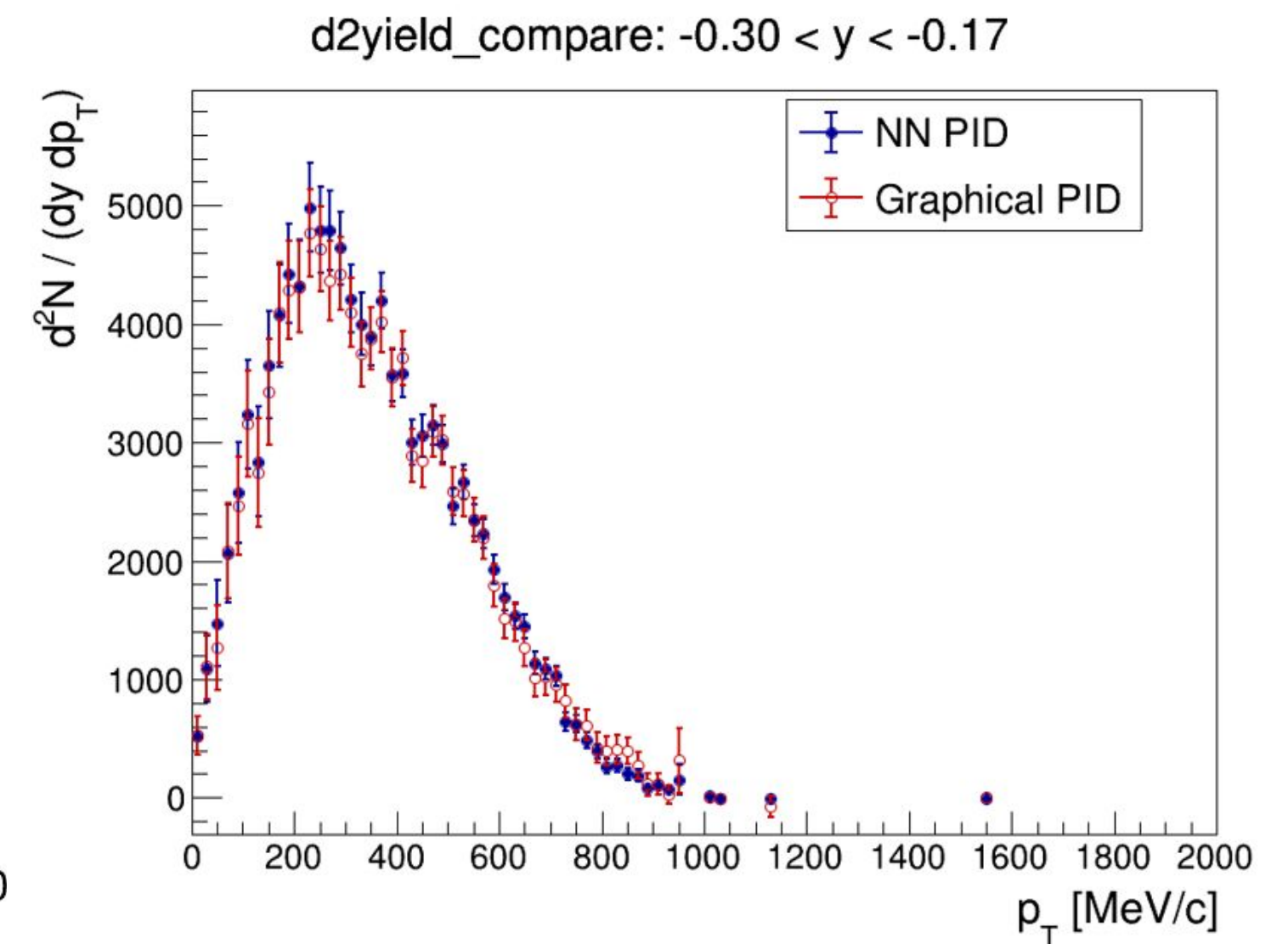
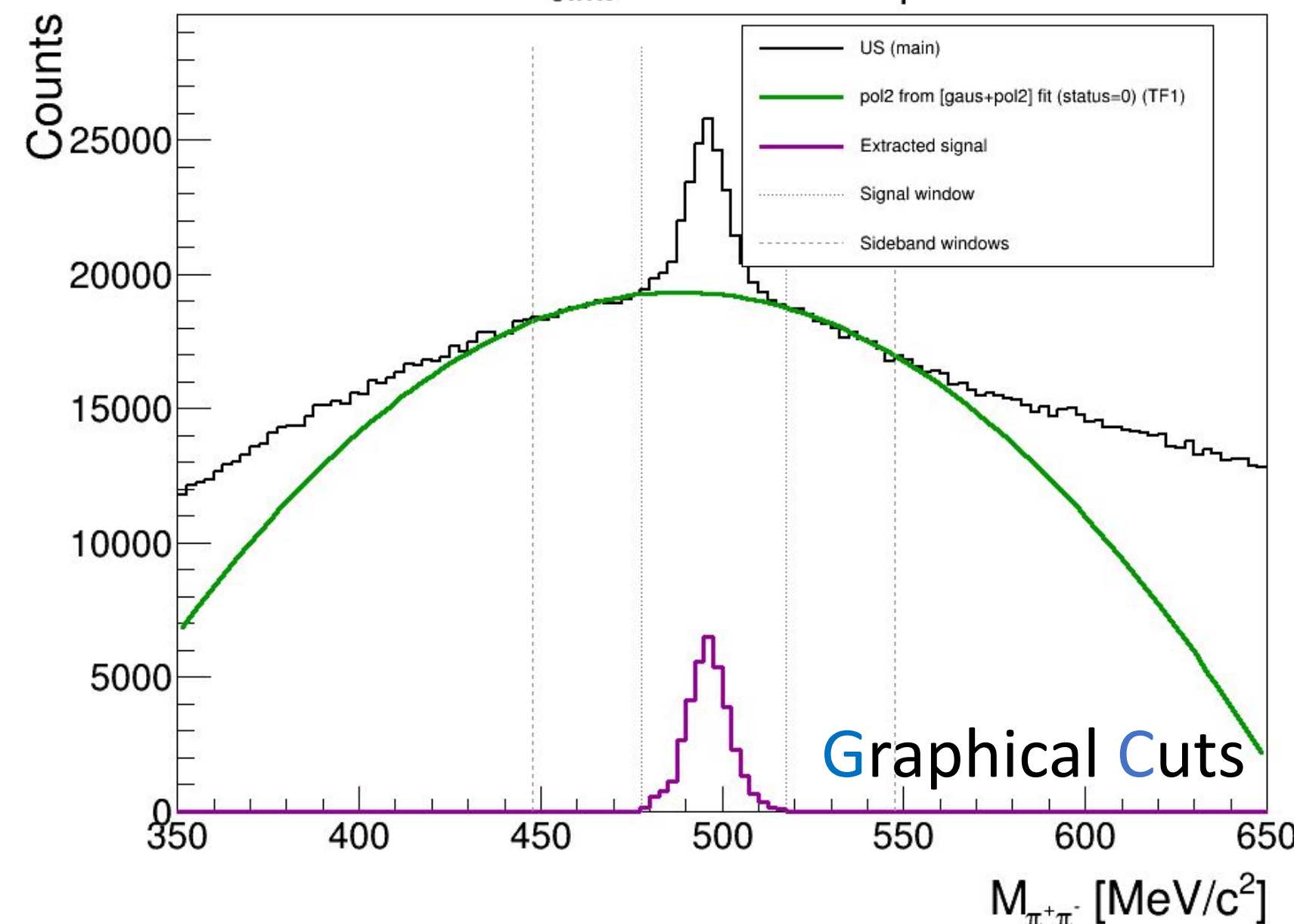
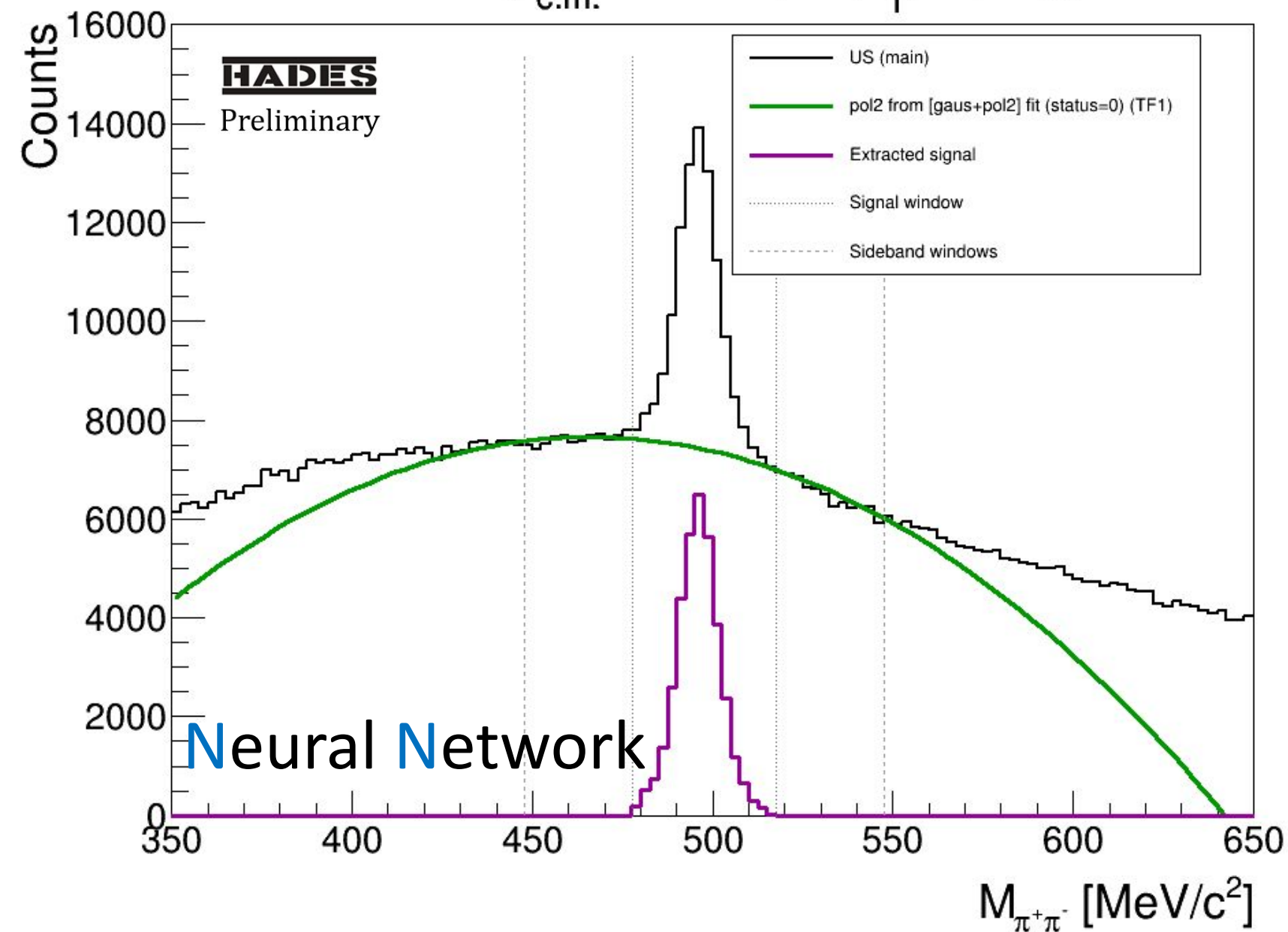
# Comparison to Graphical Cuts: Direct + $\rho$

1. Tested graphical cuts systematic effects as well for DANN validation  $\longrightarrow$
2. Compared results for inclusive resonance analyses without KR (pions)



NN:  $1.43 < y_{c.m.} < 1.55$  (all  $p_T$ , fitpoly)

GR:  $1.43 < y_{c.m.} < 1.55$  (all  $p_T$ , fitpoly)



Comparison to Graphical Cuts:  $\phi(1020)$ 

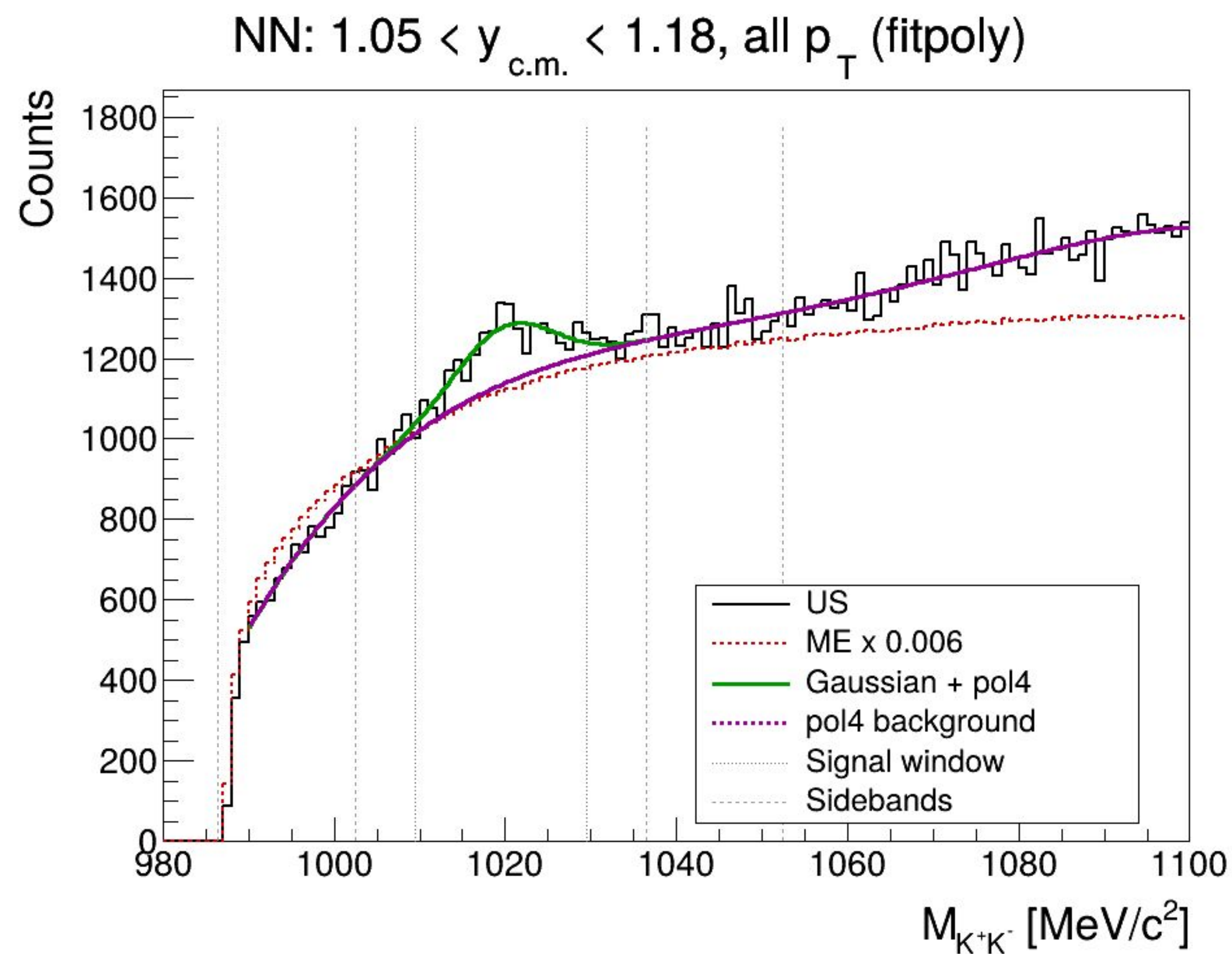
## Potential extensions

1.  $\phi(1020)$  inclusive selection  $\longrightarrow$
2. kaon inclusive selection

They need a special treatment, because background is still too large.

- Multi-differential analysis will require additional selection methods

Only limited amount of good bins



## Comparison to Graphical Cuts: Kaons

### Potential extensions

1.  $\phi(1020)$  inclusive selection
2. kaon inclusive selection  $\longrightarrow$

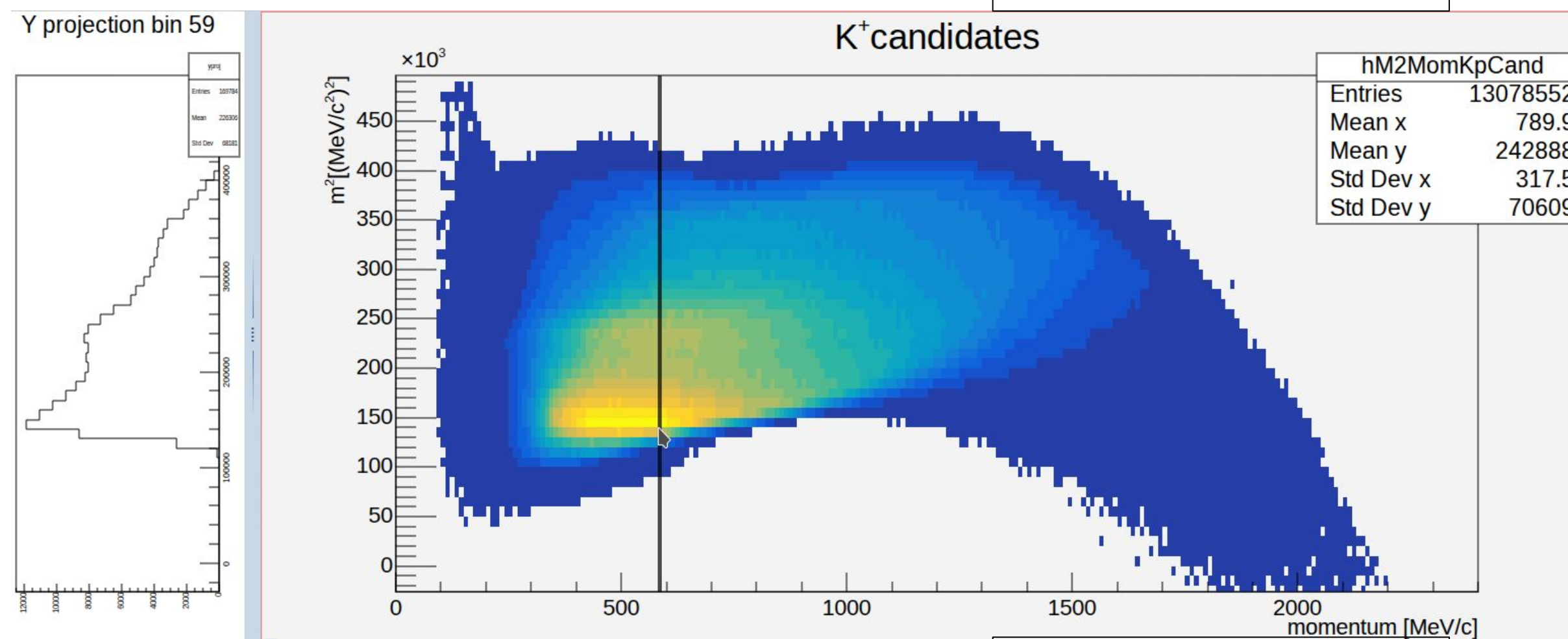
They need a special treatment, because background is still too large.

- Multi-differential analysis will require additional selection methods

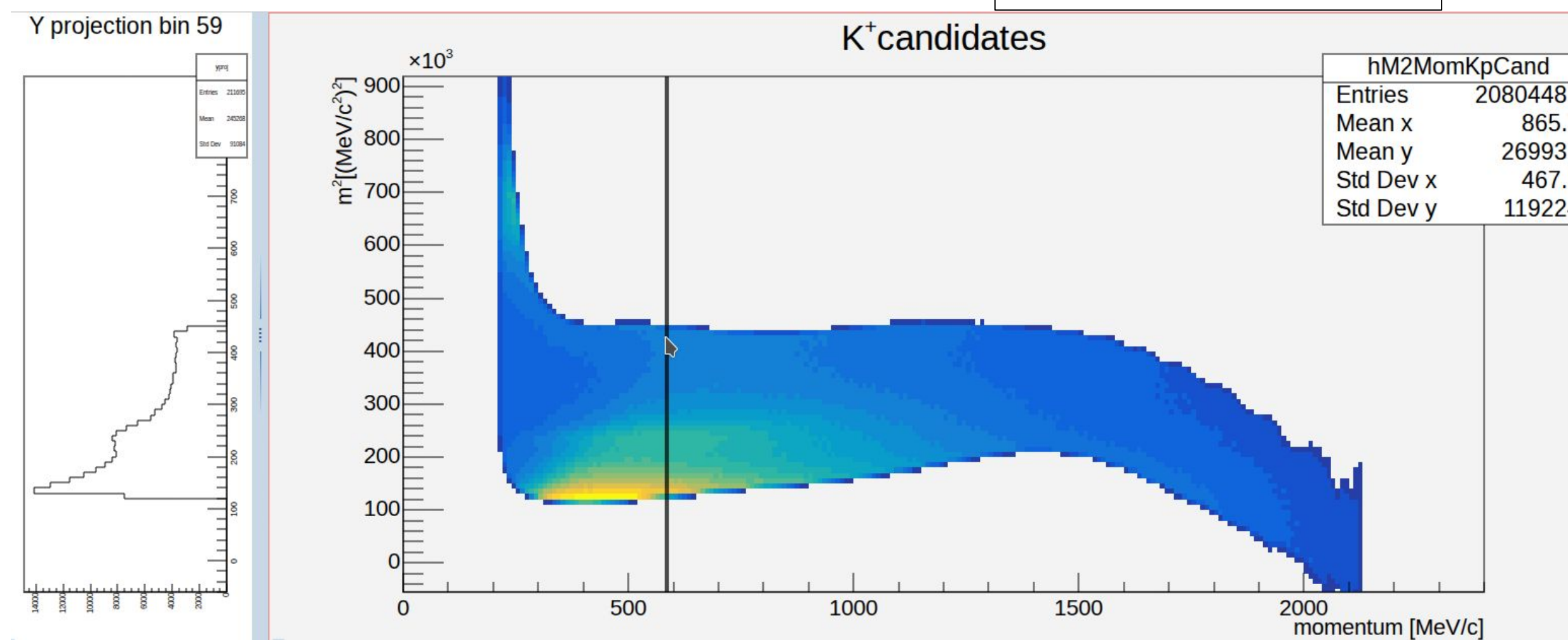
Graphical cuts = no cut at all

- Can try Carl's selection

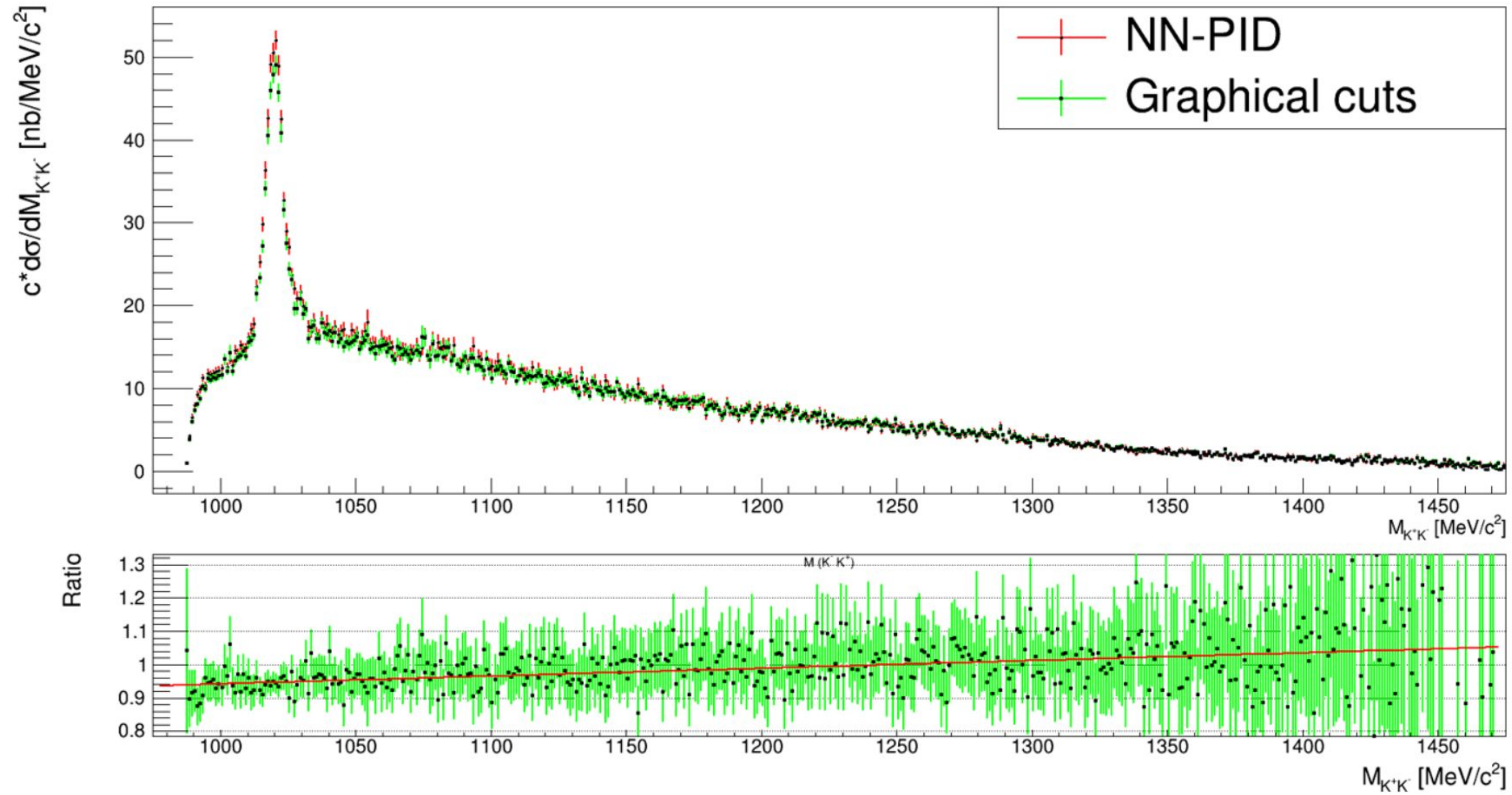
### ML-based PID



### Graphical Cuts

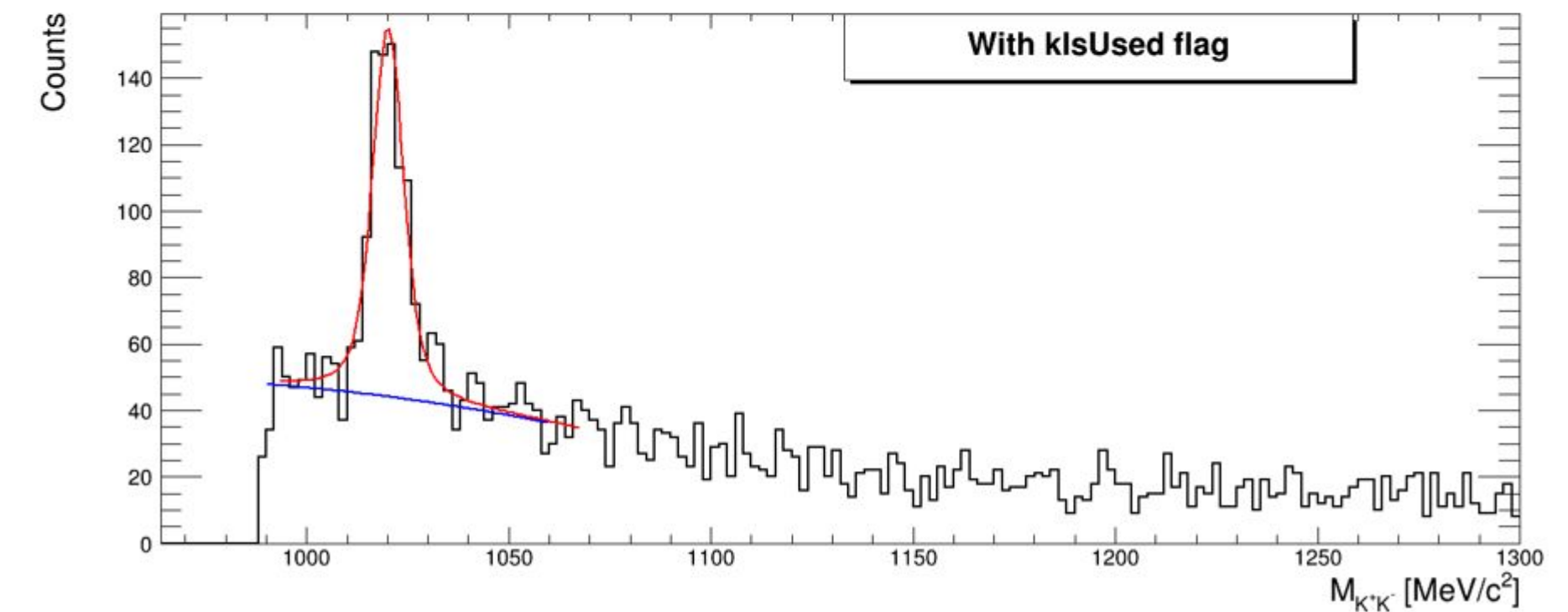
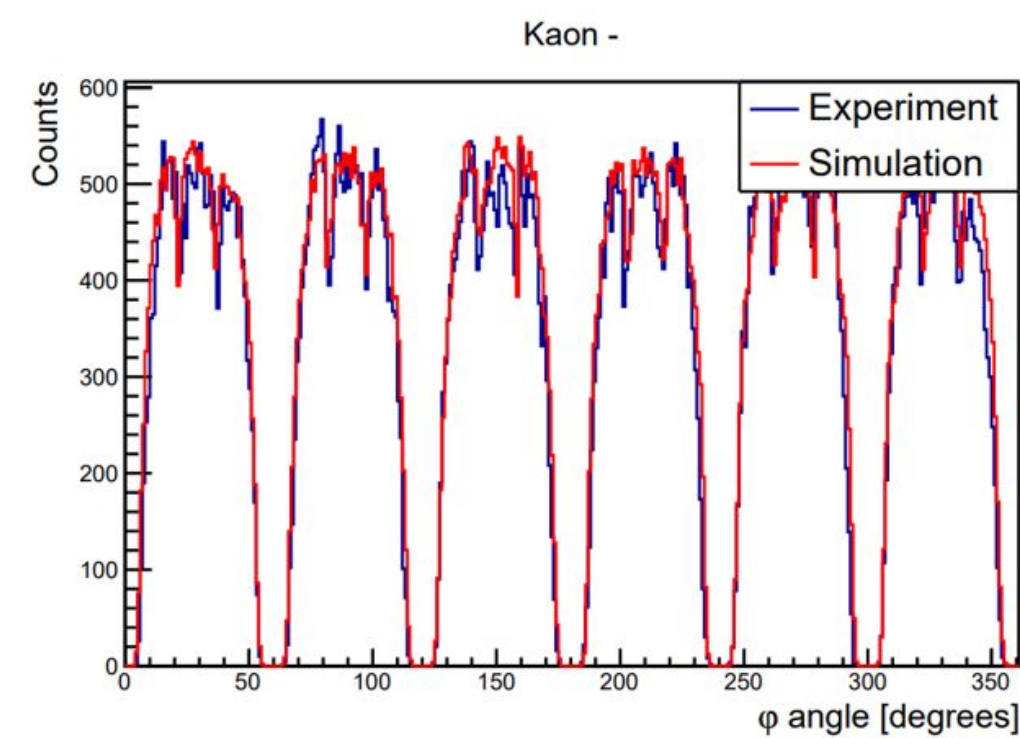
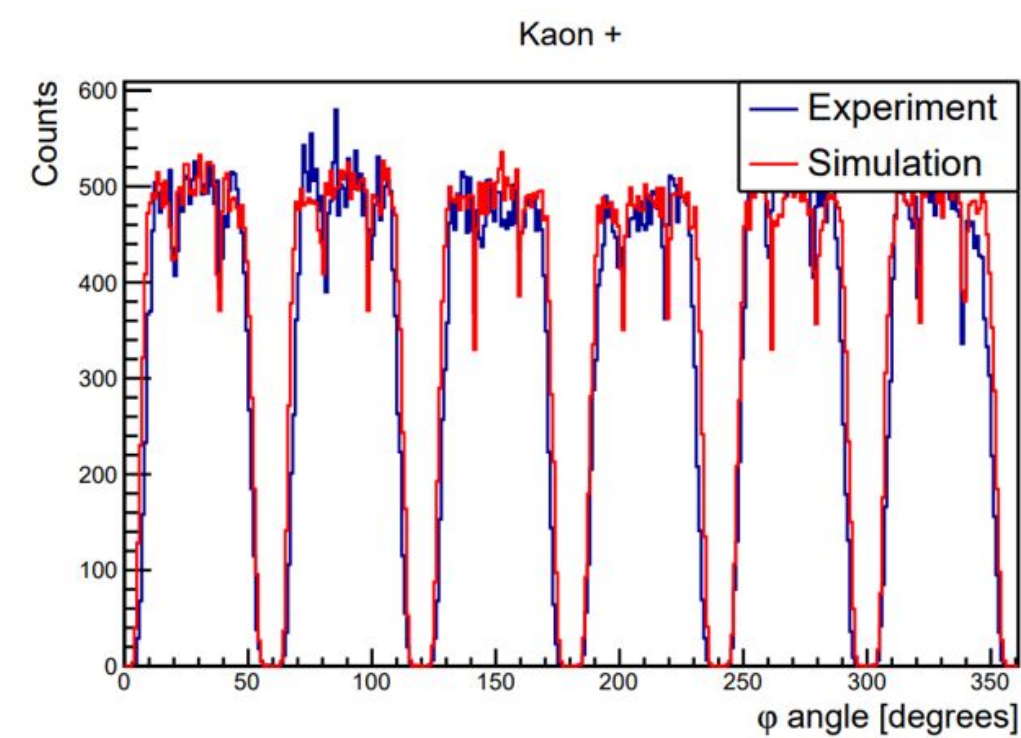
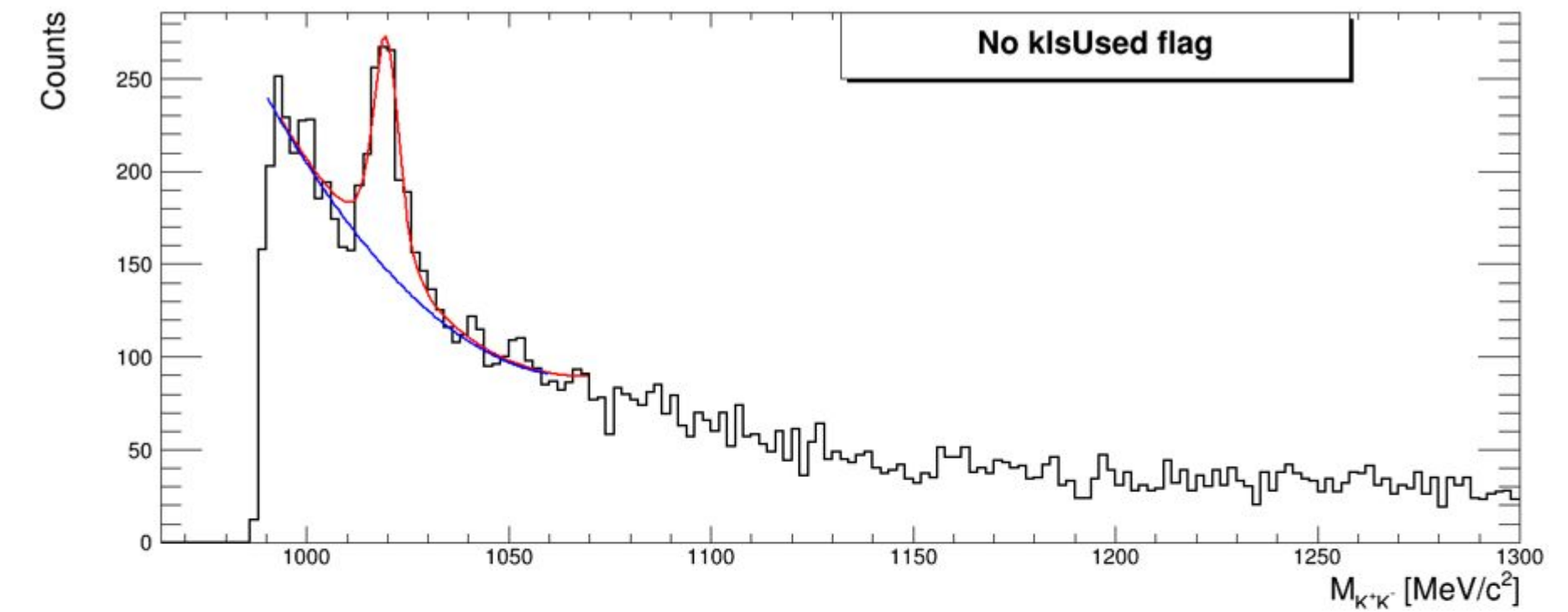
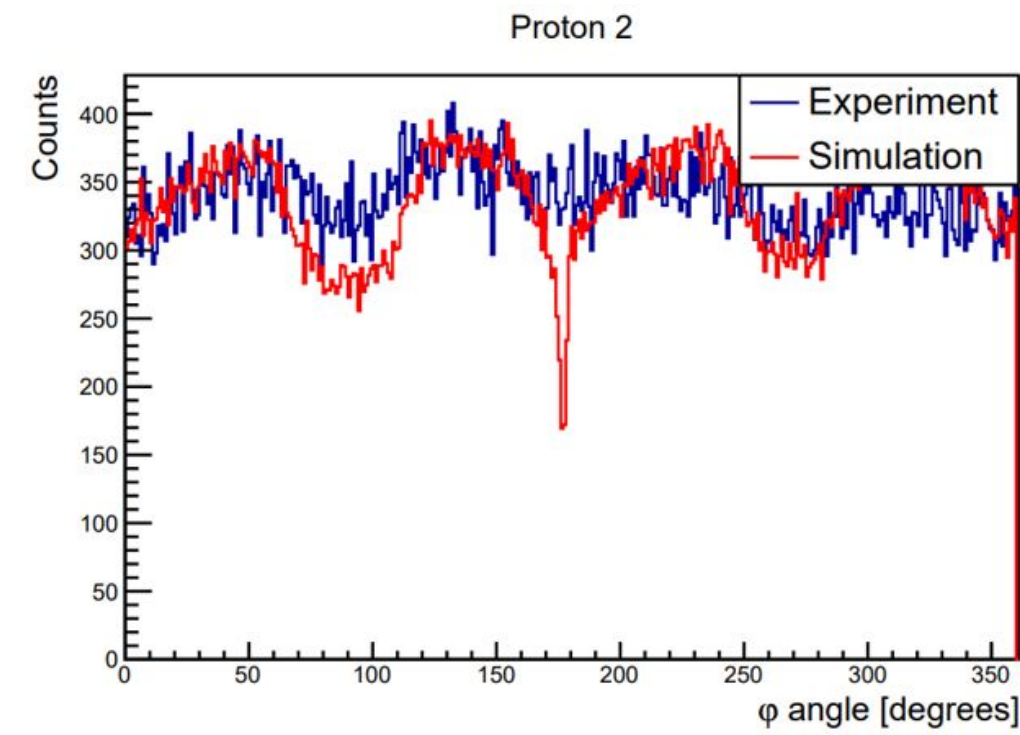
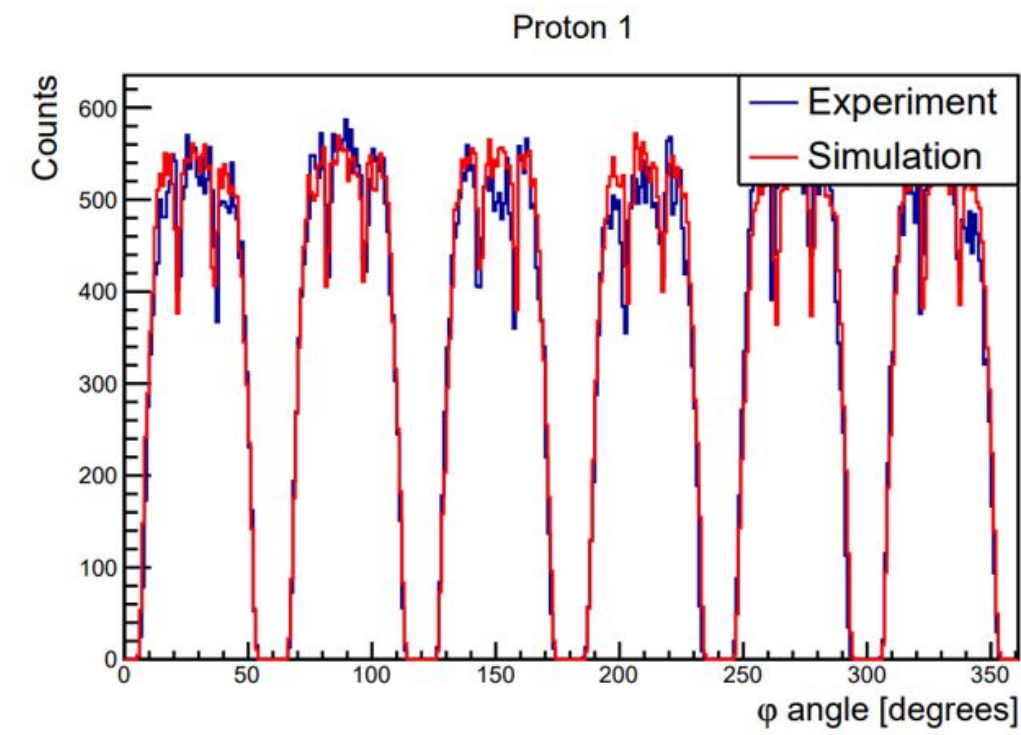


# Systematic Uncertainties: PID



Variations of the systematic bias correction calculation + comparison with the graphical cuts

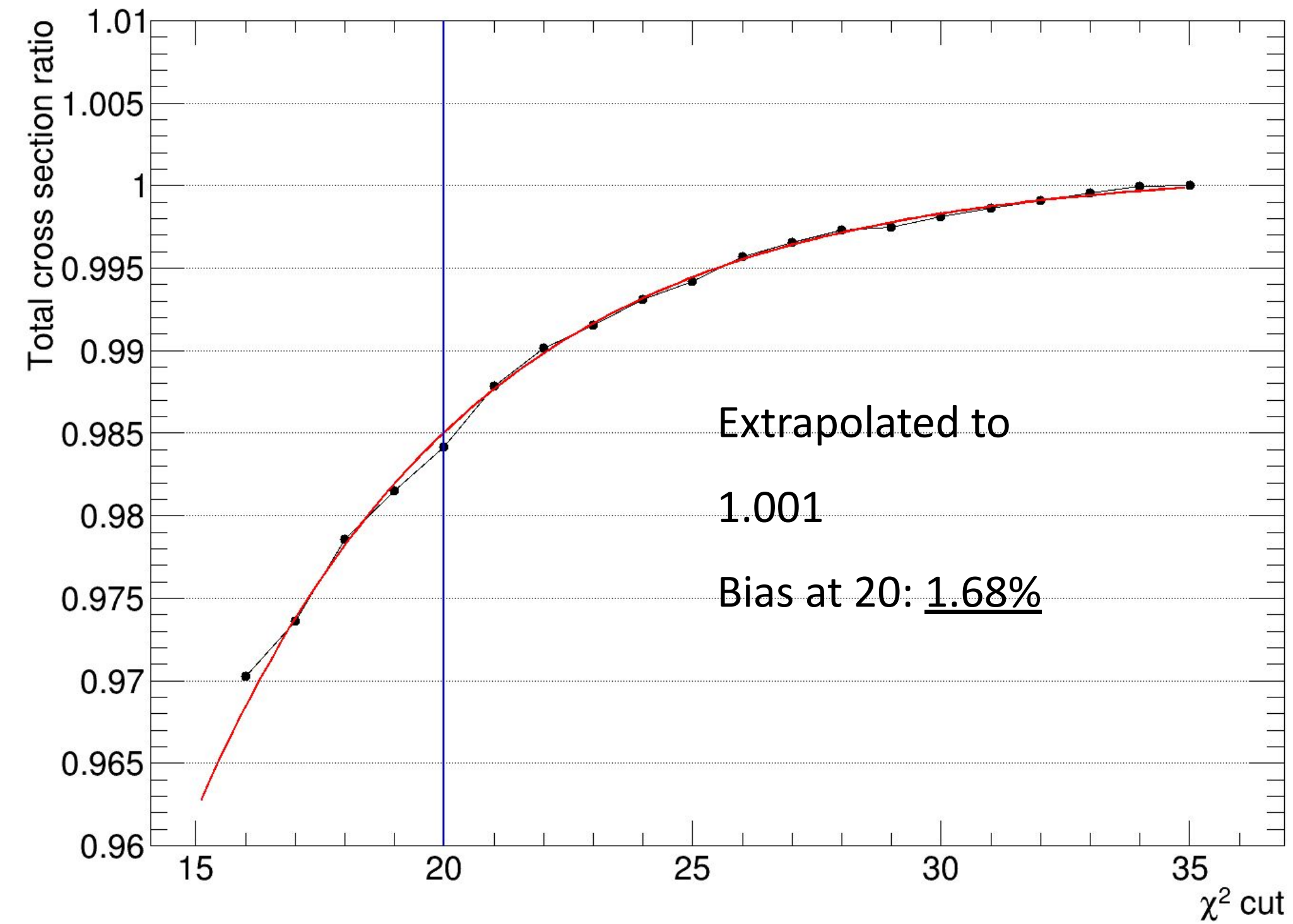
# Systematic Uncertainties: Acceptance and Global Cuts



Estimated via

- Varying the methods, selection cuts, and models
- Comparing Sim to Exp efficiencies

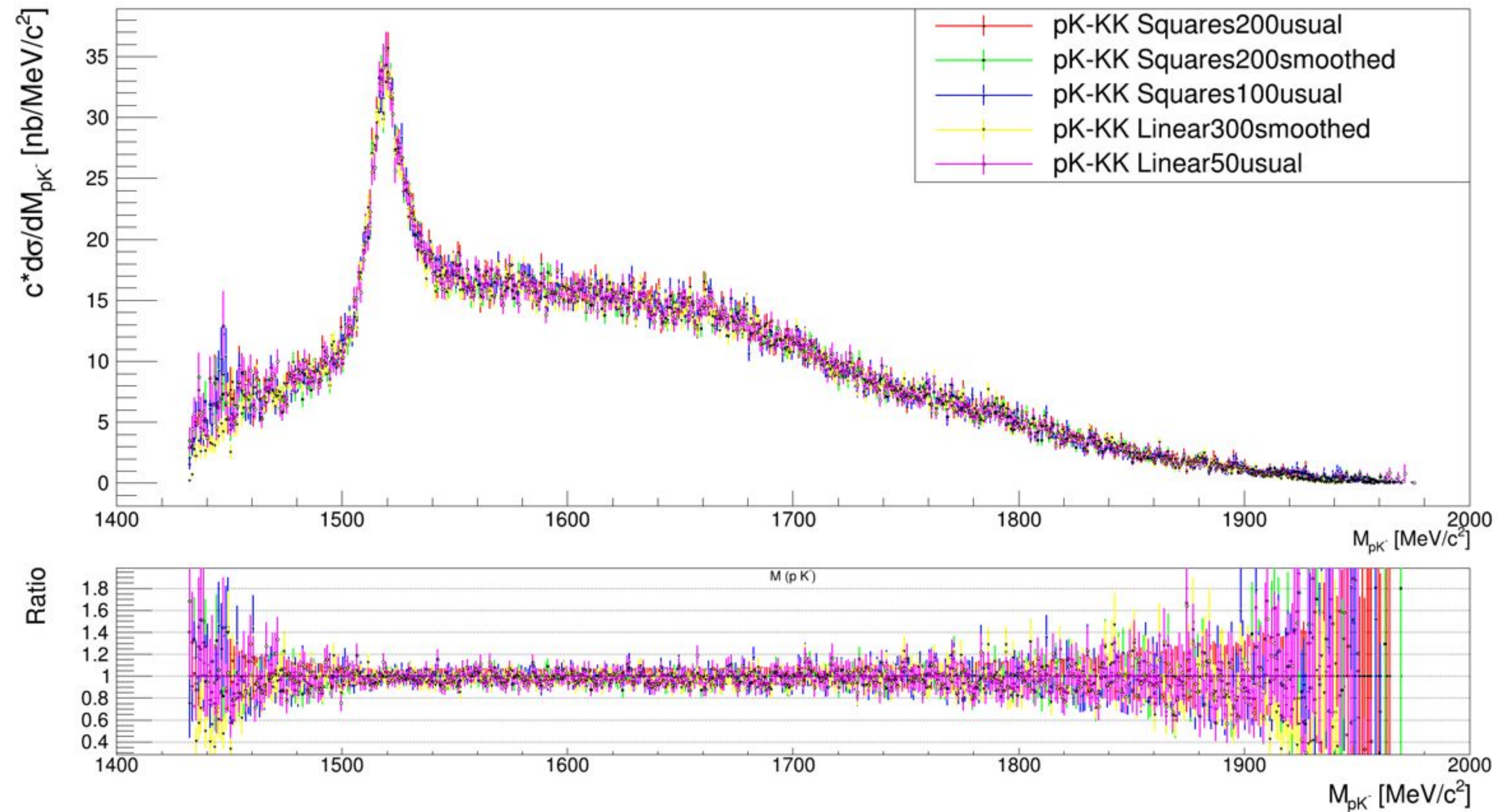
# Systematic Uncertainties: KR cuts



Estimated via

- Varying the methods, selection cuts, and models
- Comparing Sim to Exp efficiencies

# Systematic Uncertainties: Efficiency Correction



Estimated via

- Varying the methods, selection cuts, and models
- Comparing Sim to Exp efficiencies

# Systematic Errors and Uncertainties

Source	Correction [Y/N]	Uncertainty [%]
Start detector	Y	1.5
kIsUsed flag	N	5
NN-PID	Y	2
Kinematic refit and $\chi^2$ cuts	Y	3
Efficiency parametrization	N	5
Acceptance	Y	10
Remaining background	Y	3
Integrated luminosity	N	7
Total	-	$\sim 15$

Estimated via

- Varying the methods, selection cuts, and models
- Comparing Sim to Exp efficiencies

## Summary:

- Clean dataset  $S/B = 30$ , refined over the years
- A number of physics results obtained
- Kinematic refit works properly
- ML-based PID works properly
- Background and efficiency correction under control
- Systematic Uncertainties  $\sim 15\%$

## Outlook:

- Gen4 - Gen3 difference
- Further work on inclusive analyses
- Improvements of PID
- Improvements of physics analysis

Thank you for your attention

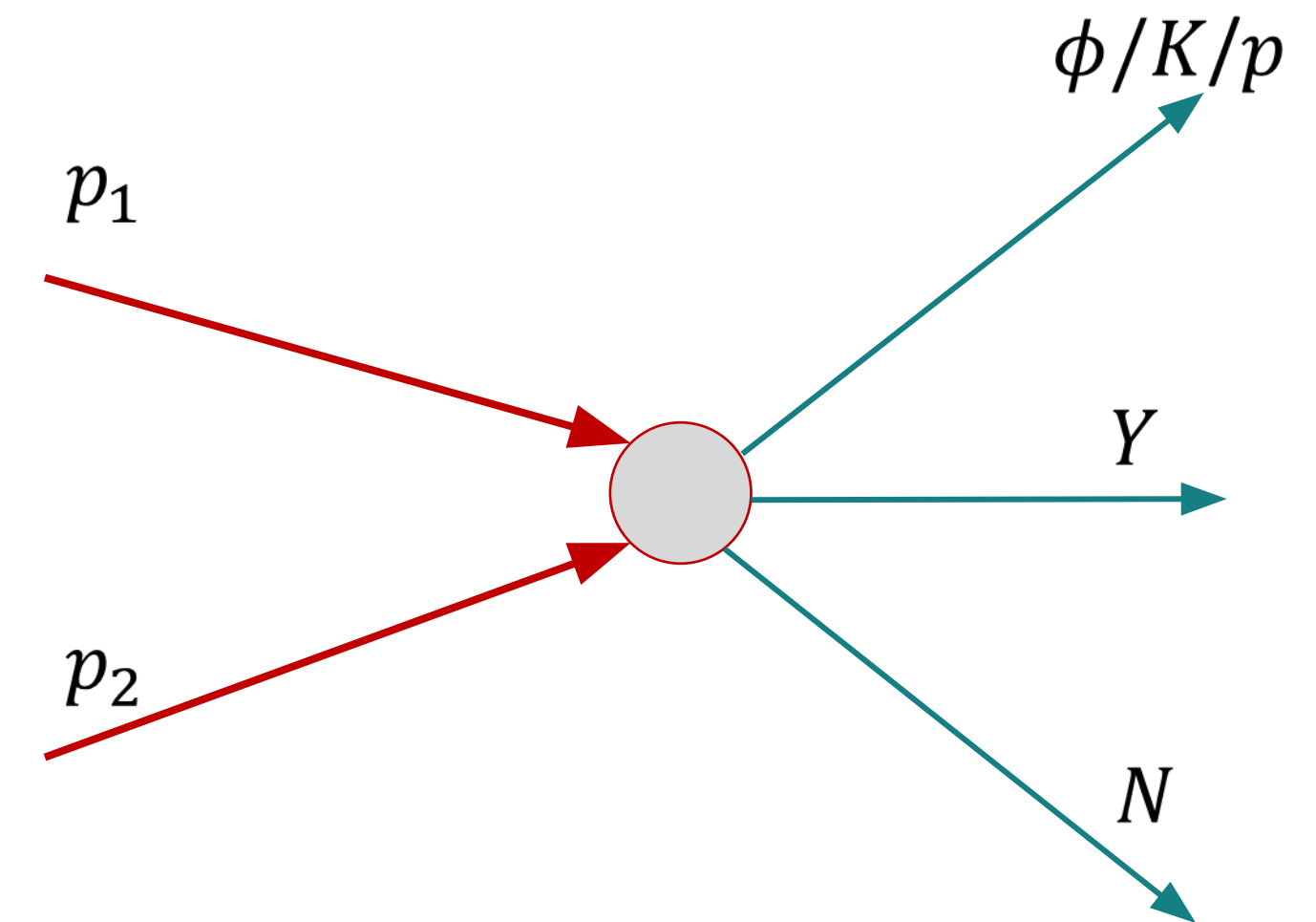
Backup

# Strangeness Production

Studies of strangeness in p-p collisions

Up to a few GeV above thresholds:

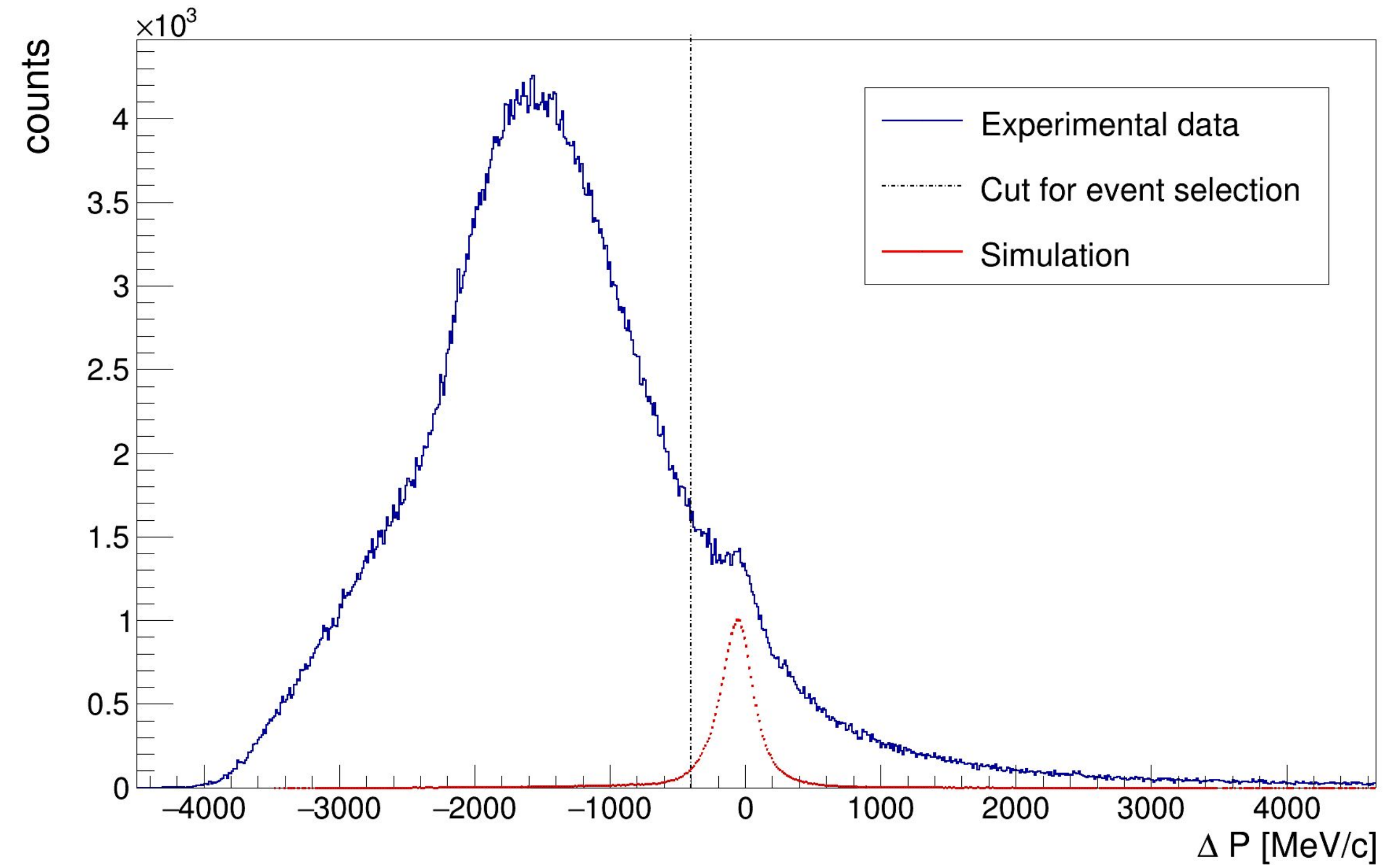
- Production mechanism in nonperturbative regime
- Spectroscopy of baryons with strangeness
- Hadron-hadron interactions
- Exotic states and resonances
- ...



# Selection of events for no KR tests

Particle identification with strict PID

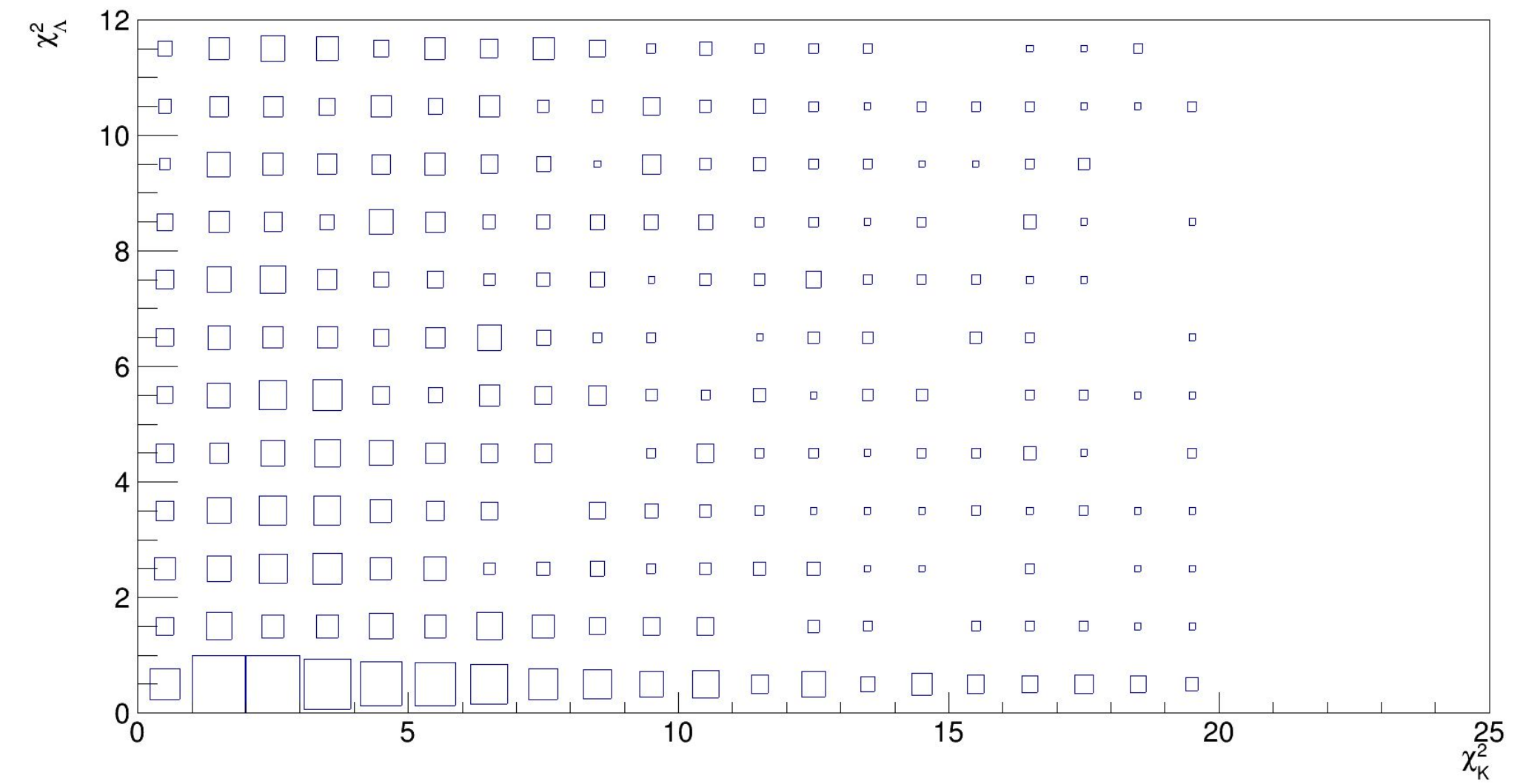
Total momentum of final state is not significantly lower than that of initial state



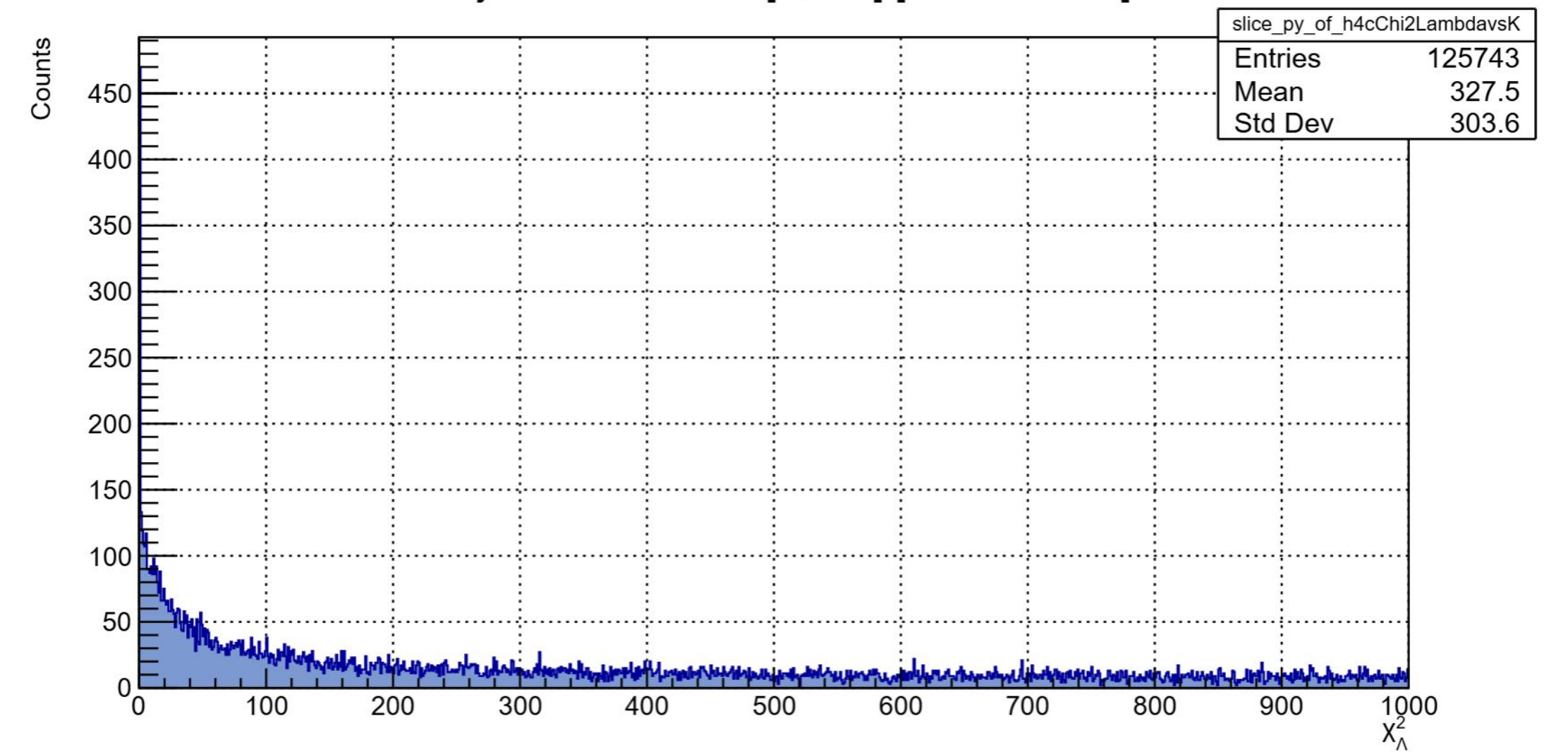
# Remaining Background Studies 2

3C fit for Lambda candidate.

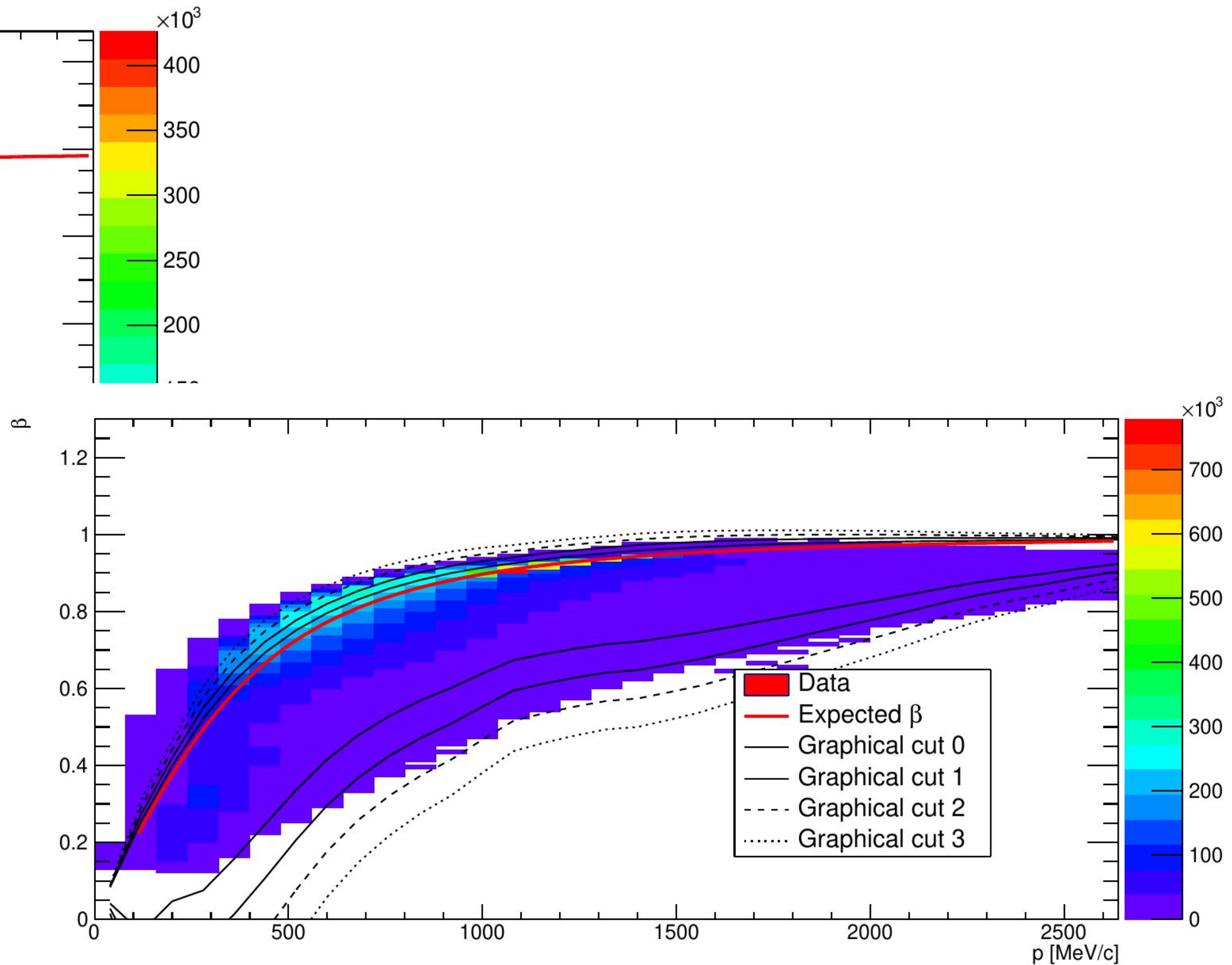
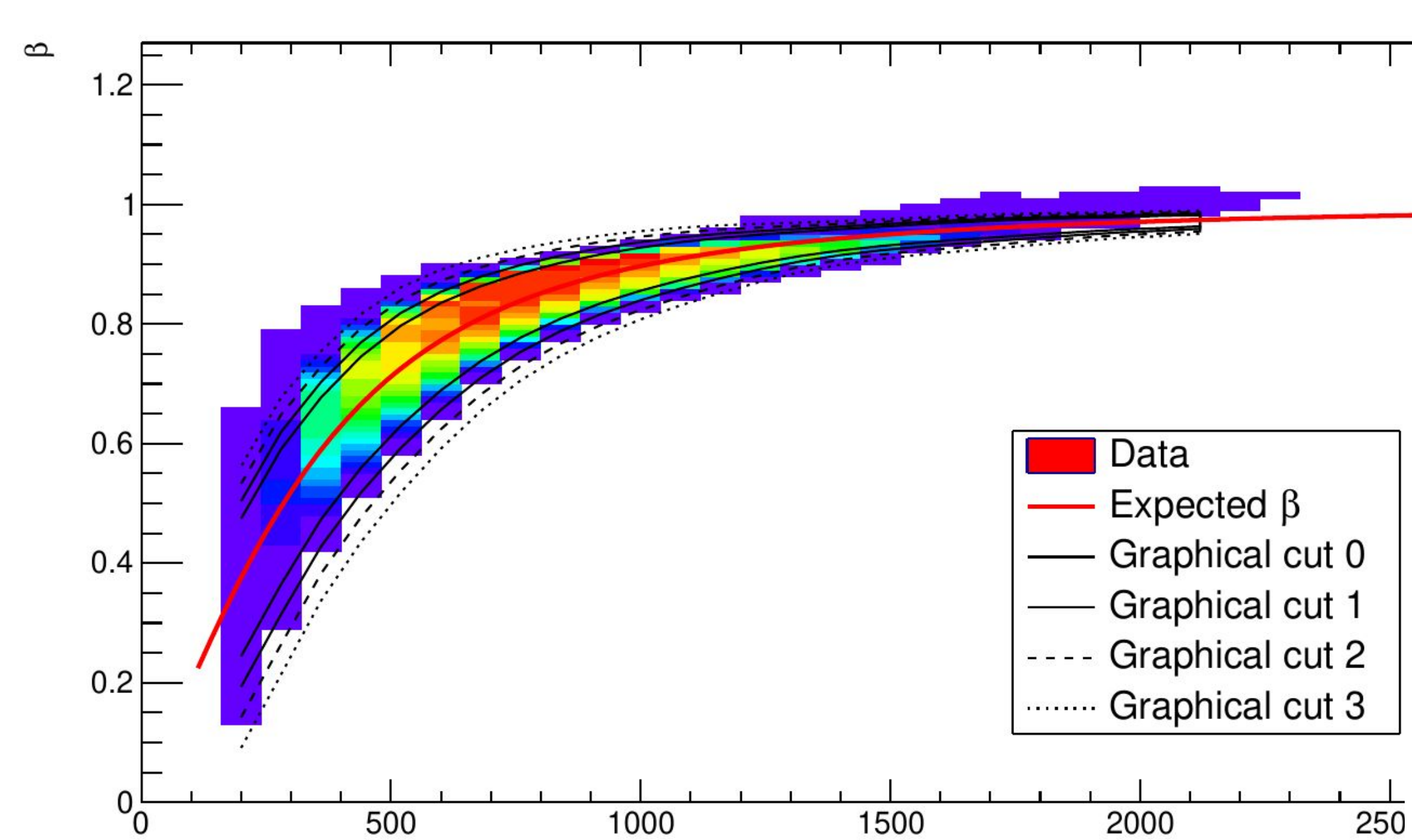
(no peak, consistent numbers)



ProjectionY of binx=[1,100] [x=0.0..100.0]



# Graphical cuts windows

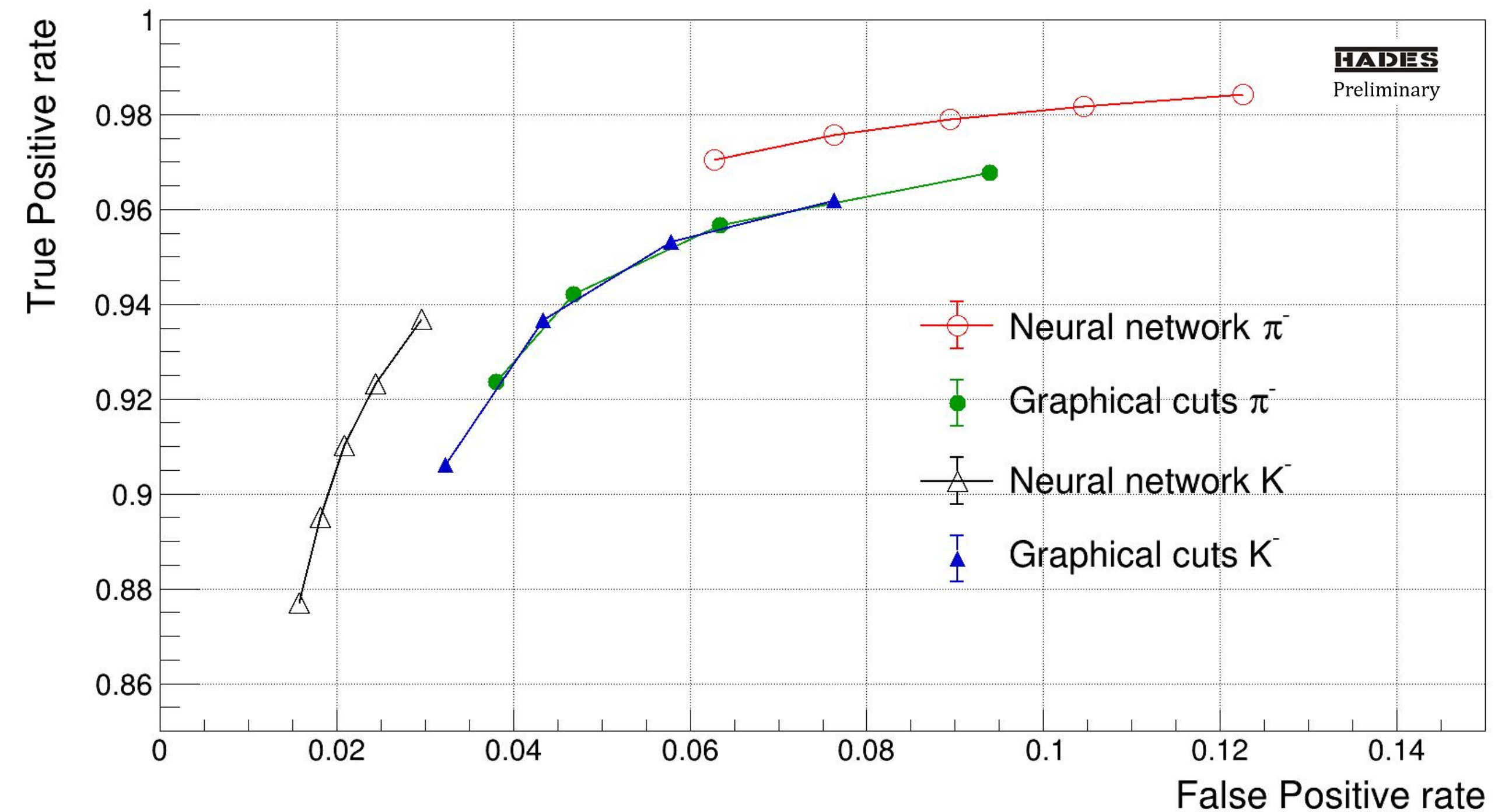


# Comparison With the Graphical Cuts ( $\beta - P$ )

DANN PID has ~1.5 times better  
purity at the same efficiency:

$$\text{TPR}_i \equiv \frac{N(\text{true } i \text{ selected as } i)^*}{N(\text{true } i)}$$

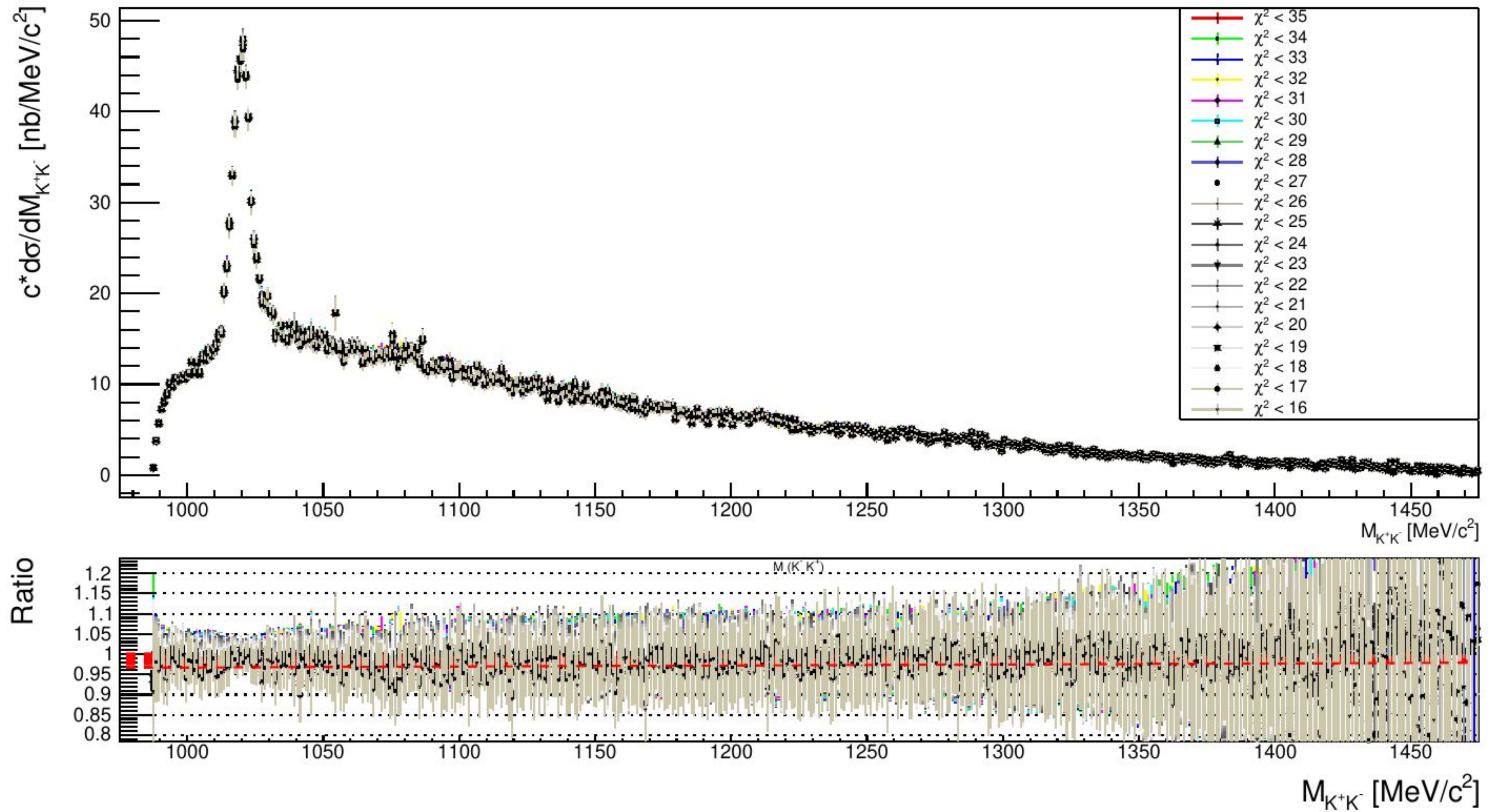
$$\text{FPR}_i \equiv \frac{N(\text{true } j \neq i \text{ selected as } i)^*}{N(\text{true } j \neq i)}$$



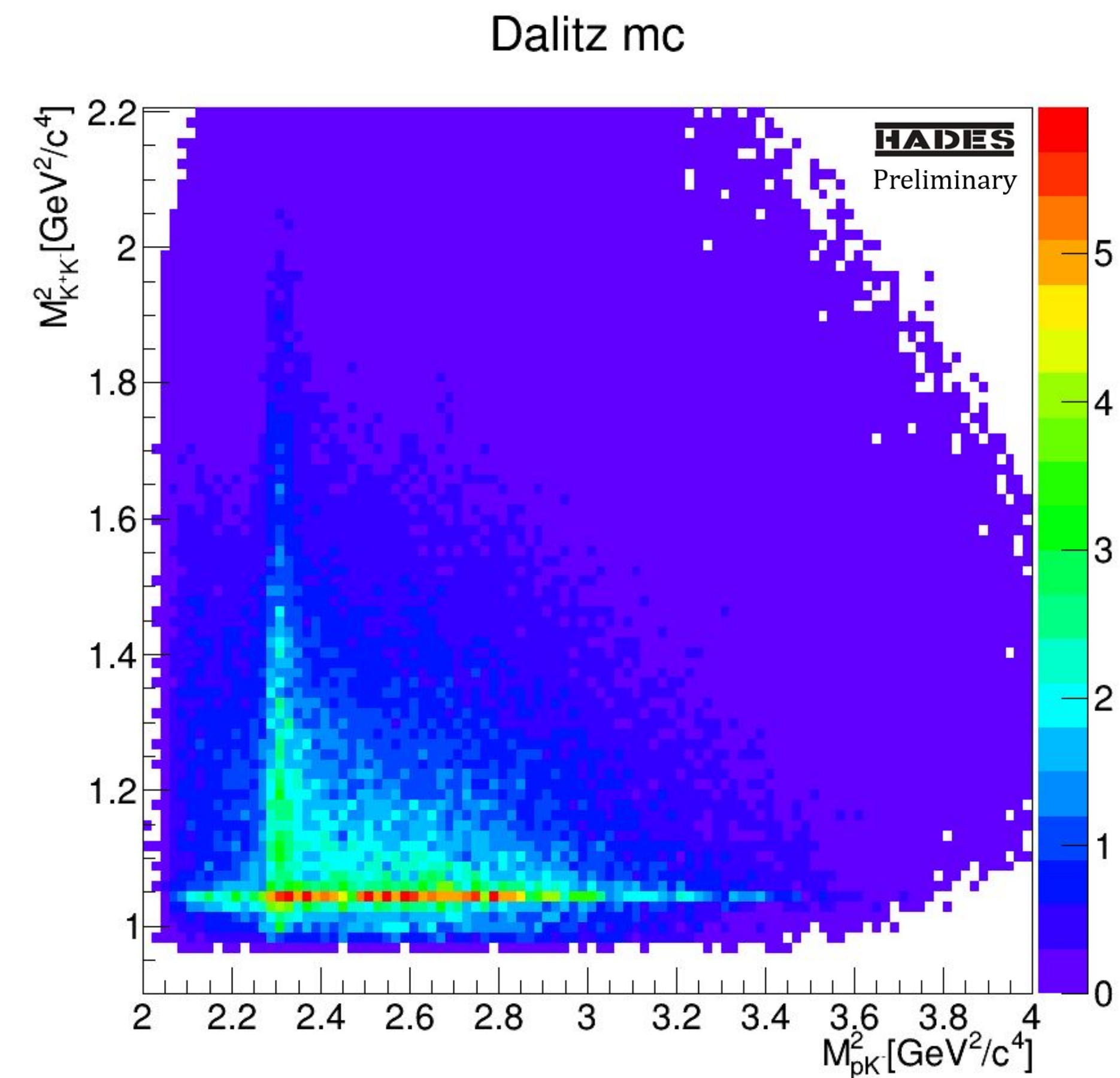
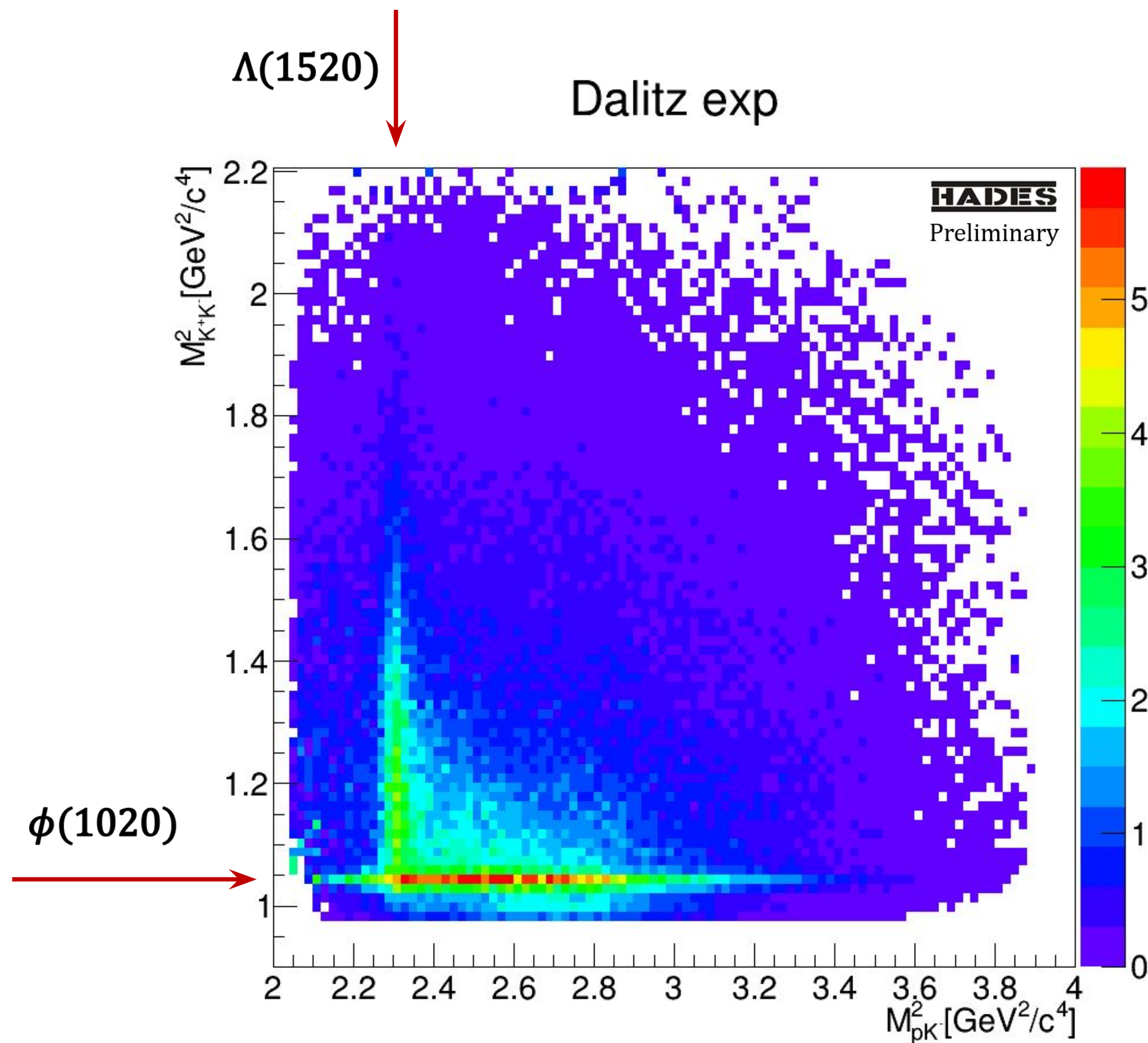
✓ *Performance improvements*

\*Both TPR and FPR are self-contained for the case of two classes and thus insensitive to the fractions of events

# Varying the chi2 cut



# Mass Distributions and Model Approximations



- Efficiency and luminosity corrected counts
- 2 combinations per event (2 protons)

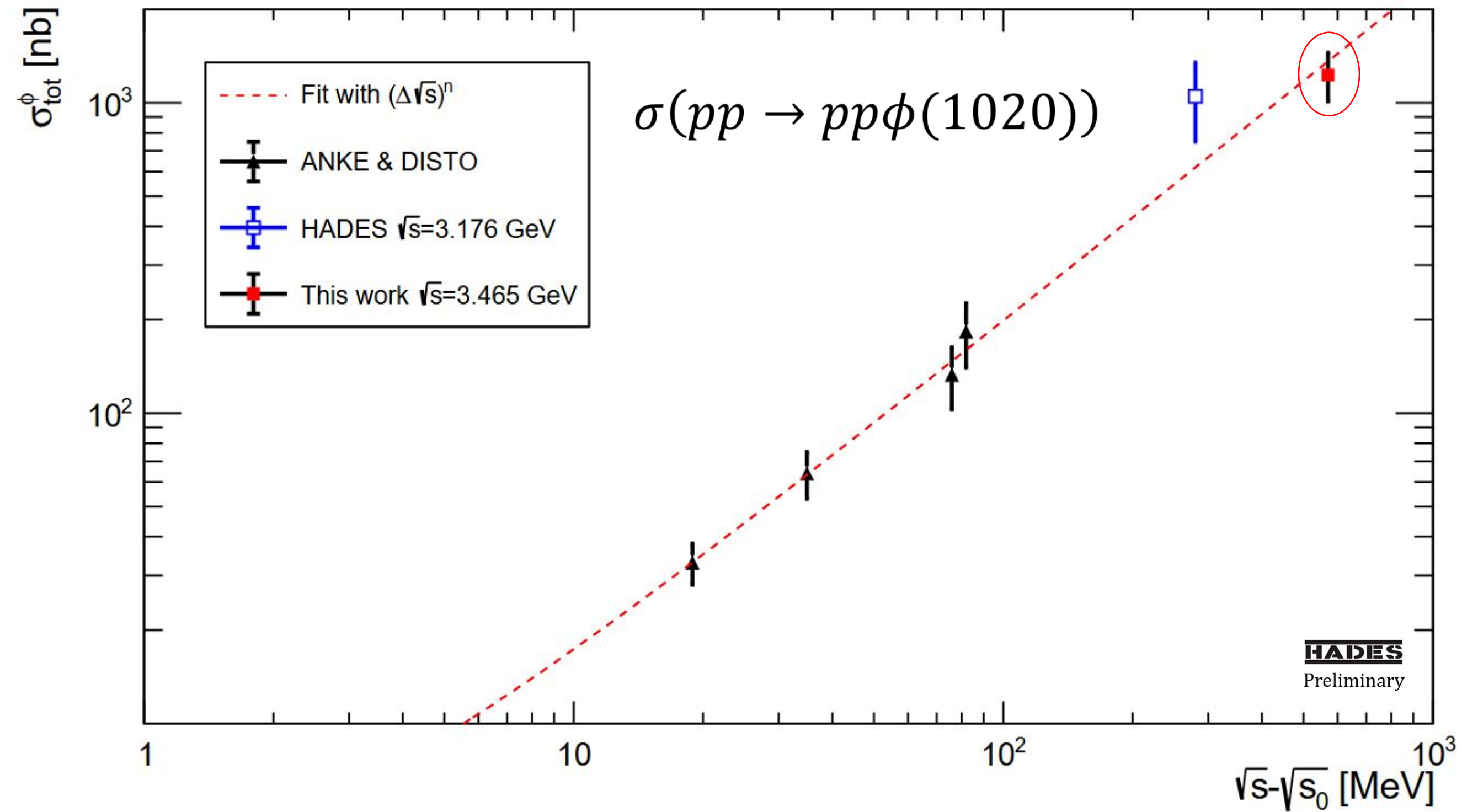
- MC events based on phase space distribution reweighted by a model

# Total and Resonance Cross Sections

- $\sigma(pp \rightarrow ppK^+K^-) = 2800 \pm 400 \text{ nb}$
- $\sigma(pp \rightarrow pp\phi(1020)) = 613 \pm 90 \text{ nb}$
- $\sigma(pp \rightarrow pK^+\Lambda(1520)) = 1372 \pm 200 \text{ nb}$

At  $\sqrt{s} = 3465 \pm 5 \text{ MeV}$

Systematic uncertainty  $\sim 15\%$   
mainly from global acceptance

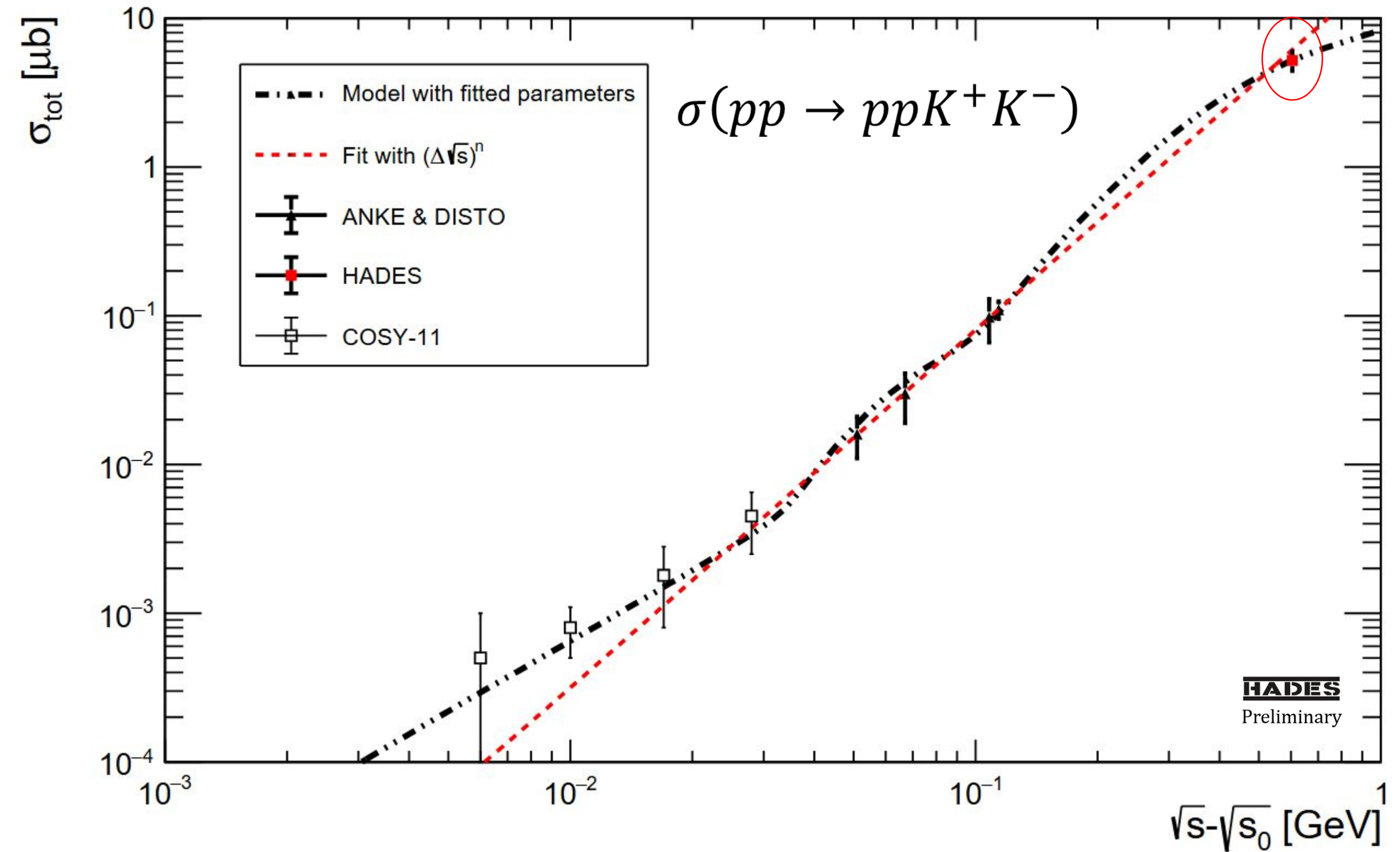


# Total and Resonance Cross Sections

- $\sigma(pp \rightarrow ppK^+K^-) = 2800 \pm 400 \text{ nb}$
- $\sigma(pp \rightarrow pp\phi(1020)) = 613 \pm 90 \text{ nb}$
- $\sigma(pp \rightarrow pK^+\Lambda(1520)) = 1372 \pm 200 \text{ nb}$

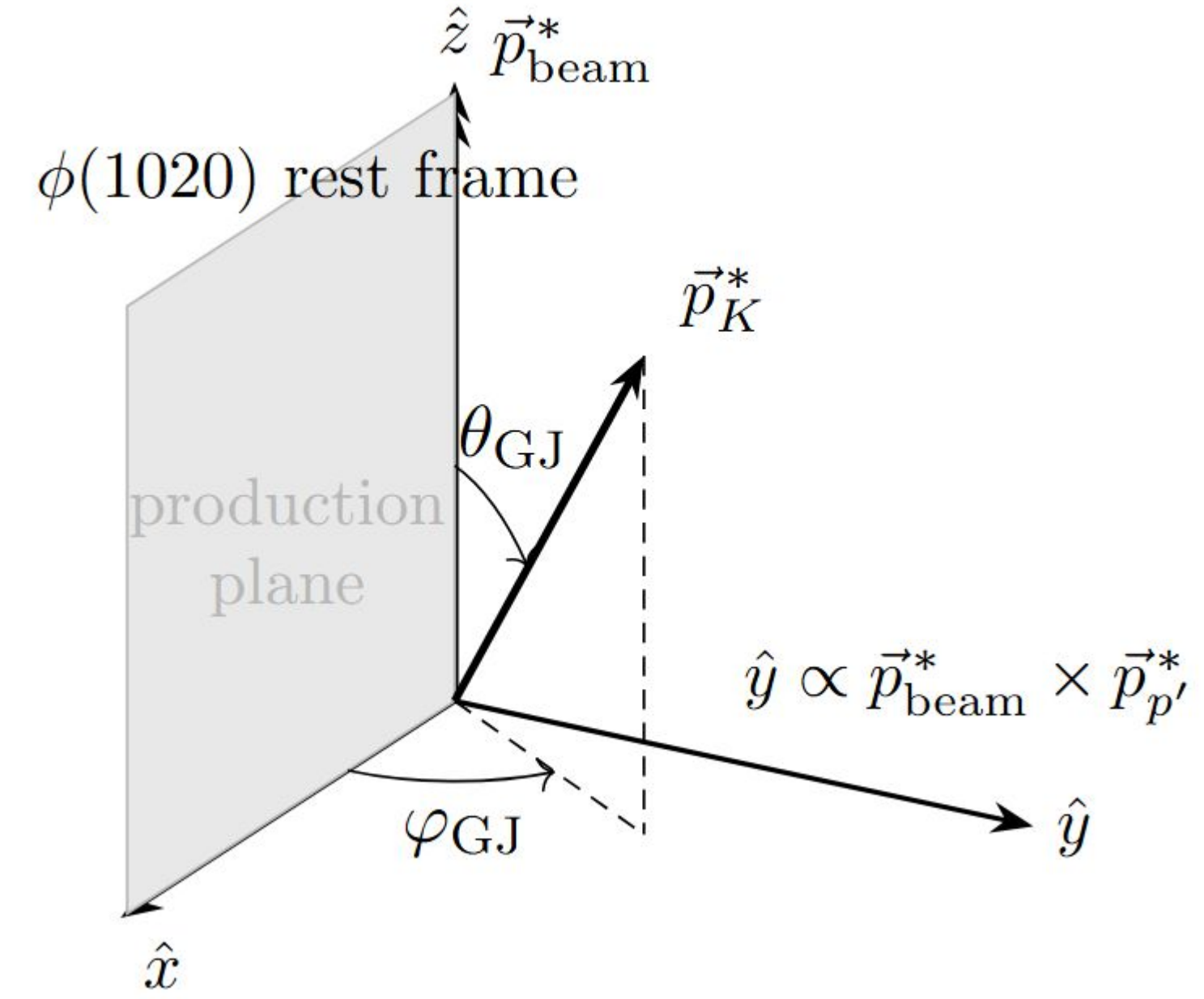
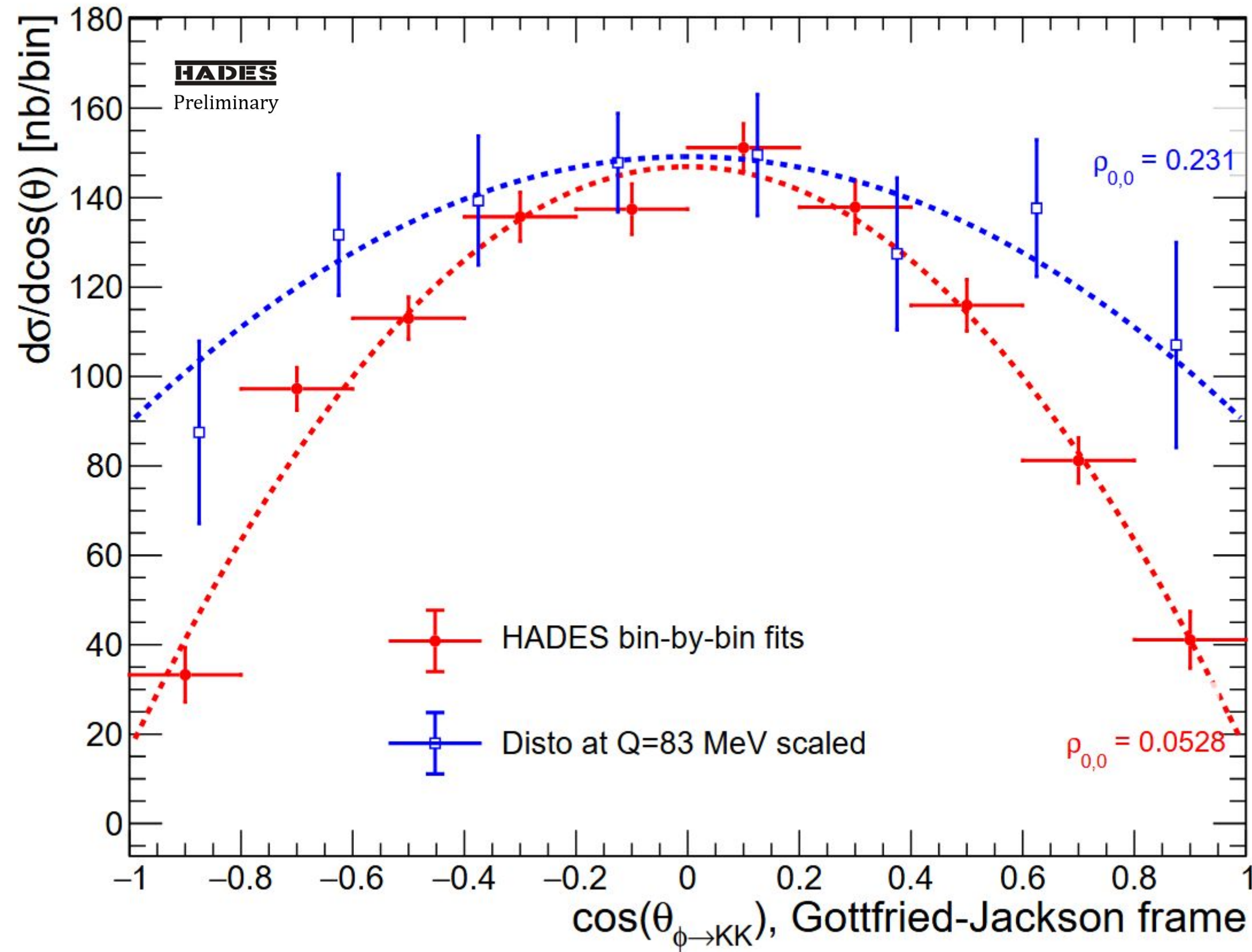
At  $\sqrt{s} = 3465 \pm 5 \text{ MeV}$

Systematic uncertainty  $\sim 15\%$   
mainly from global acceptance



- ✓ Inclusion of FSI increases the low-energy cross section, and the measurements align.

# Angular Analysis for $\phi(1020)$ spin



$\rho_{00} = 0.04 \pm 0.02$  - This measurement at 600 MeV

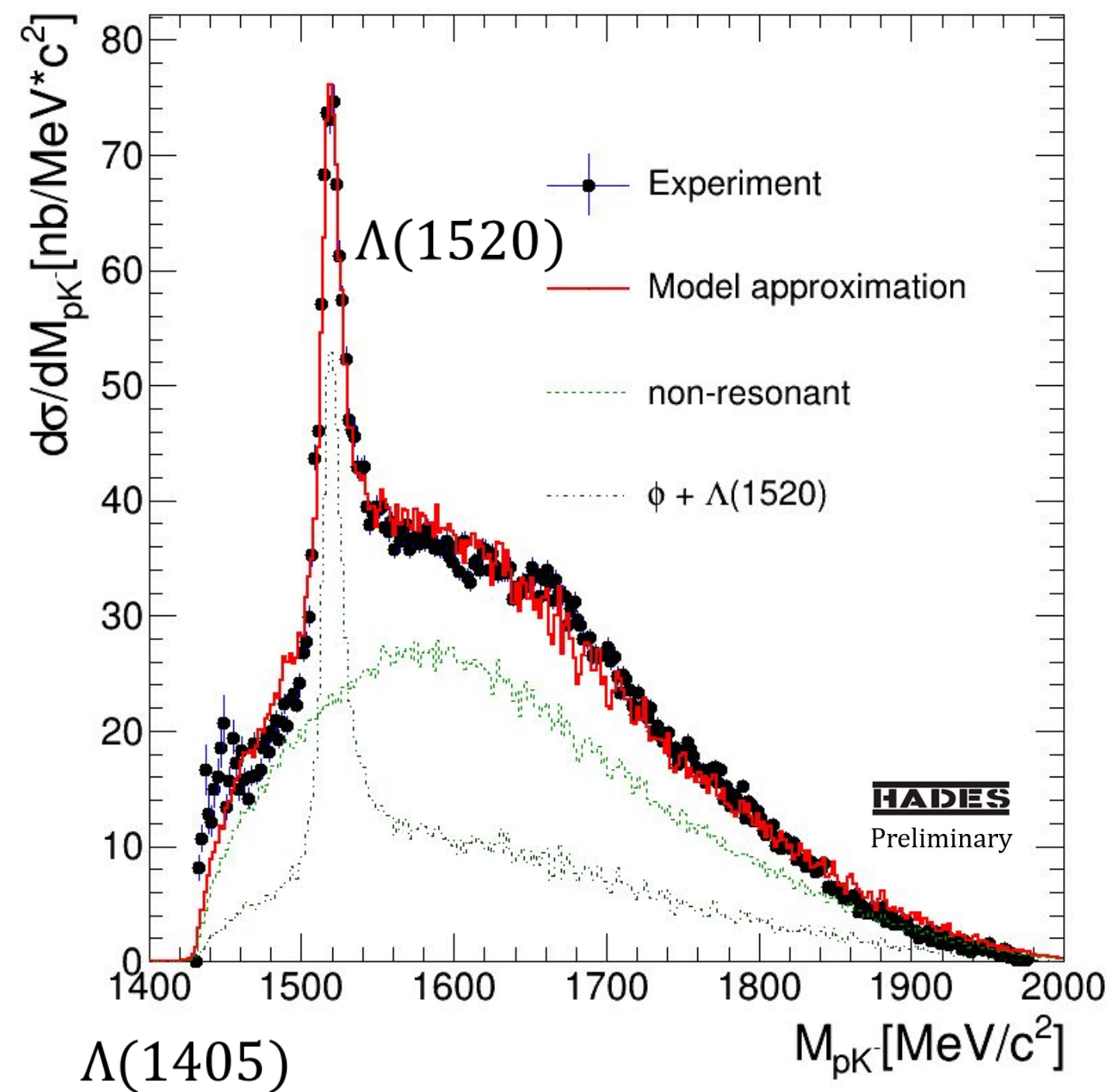
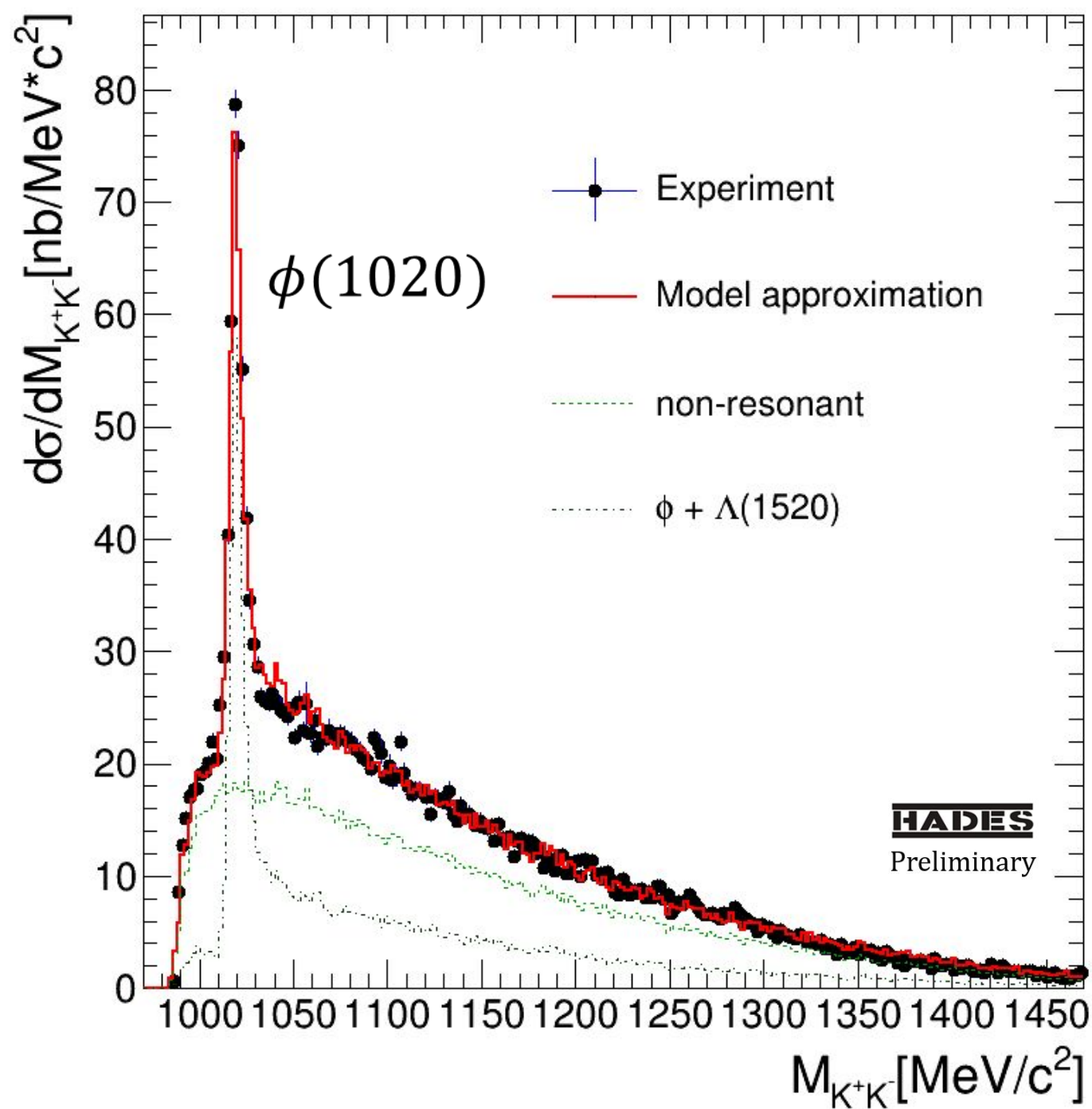
$\rho_{00} = 0.23 \pm 0.04$  - DISTO at  $\sim 100$  MeV above  $E_{thr}$

Longitudinal polarization (1/3 for unpolarized)

$$\frac{dN}{d\Omega} = \frac{3}{4\pi} \left[ \frac{1}{2}(1 - \rho_{00}) + \left(\frac{3}{2}\rho_{00} - \frac{1}{2}\right) \cos^2 \theta - \rho_{1-1} \sin^2 \theta \cos 2\varphi - \sqrt{2} \operatorname{Re}(\rho_{10}) \sin 2\theta \cos \varphi - \sqrt{2} \operatorname{Im}(\rho_{10}) \sin 2\theta \sin \varphi \right].$$

- ✓ A transition from unpolarized to transverse production?
- Inclusion of  $\varphi$  diagonal elements is underway

# Amplitude Analysis



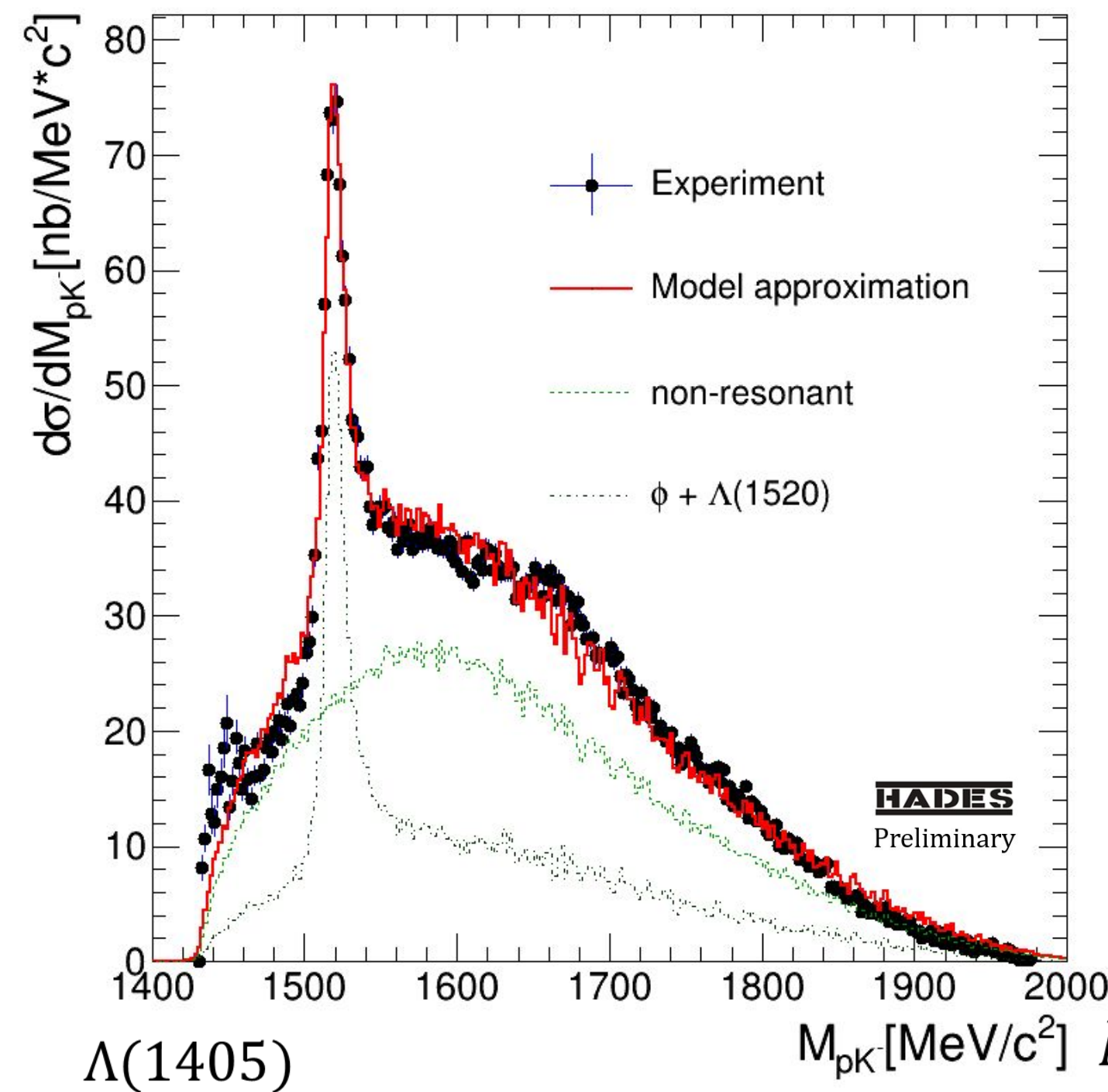
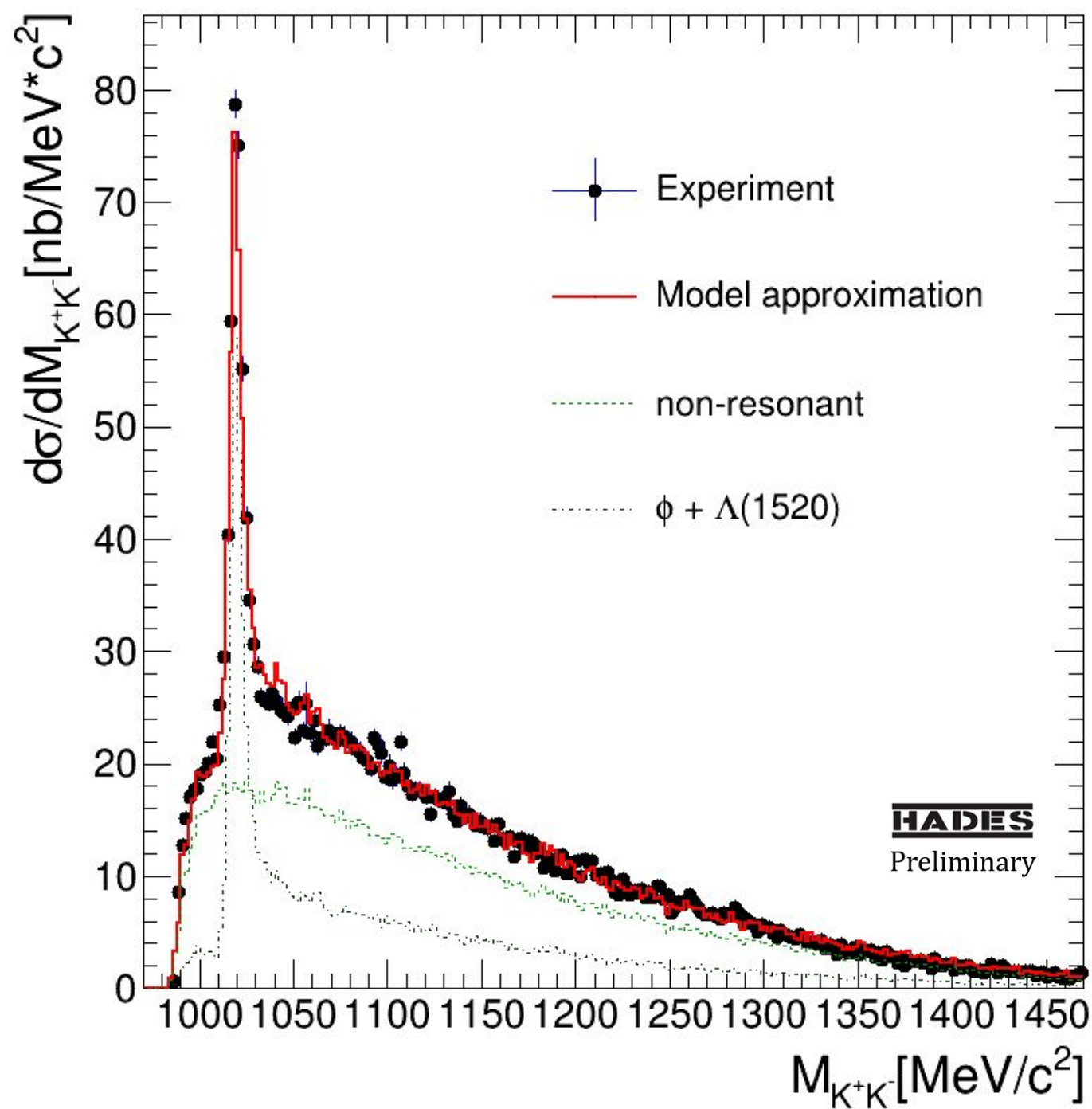
- MC phase space simulation, reweight events with the complex “amplitude” squared:

$$A = \frac{1}{1-iq_1 a_{pK}} \cdot \frac{1}{1-iq a_{KK}} \cdot (1 + c_1 BW_{\phi(1020)} + c_2 BW_{\Lambda(1520)})$$

- Simultaneous fit of  $M_{K^+K^-}$  and  $M_{pK^-}$
- Fit parameters:  $c_1, c_2, c_3$  and phases,  $\Lambda/\phi$  parameters,  $a_{pK}, a_{KK}$  scattering lengths

✓ Valid description of the experiment with FSI encapsulating different effects

# Amplitude Analysis



- $a_{KK} = (0.47 \pm 0.05) + i(0.0 \pm 0.1)$  fm  
- previous results\* poorly constrained:  
 $a_{KK} = (0.50_{-0.5}^{+4}) + i(3.0_{-3.0}^{+3.0})$  fm
- $a_{pK} = (0.09 \pm 0.02) + i(-0.22 \pm 0.05)$  fm

$$M_\phi = (1019.5 \pm 0.1) \text{ MeV}$$

$$M_\Lambda = (1519 \pm 0.5) \text{ MeV}$$

$$\Gamma_\phi = (4.5 \pm 0.1) \text{ MeV}$$

$$\Gamma_\Lambda = (14 \pm 0.5) \text{ MeV}$$

✓ The best fit includes  $\Lambda(1405) \rightarrow pK$  subthreshold production

$$M_\phi^{PDG} = (1019.461 \pm 0.016) \text{ MeV}$$

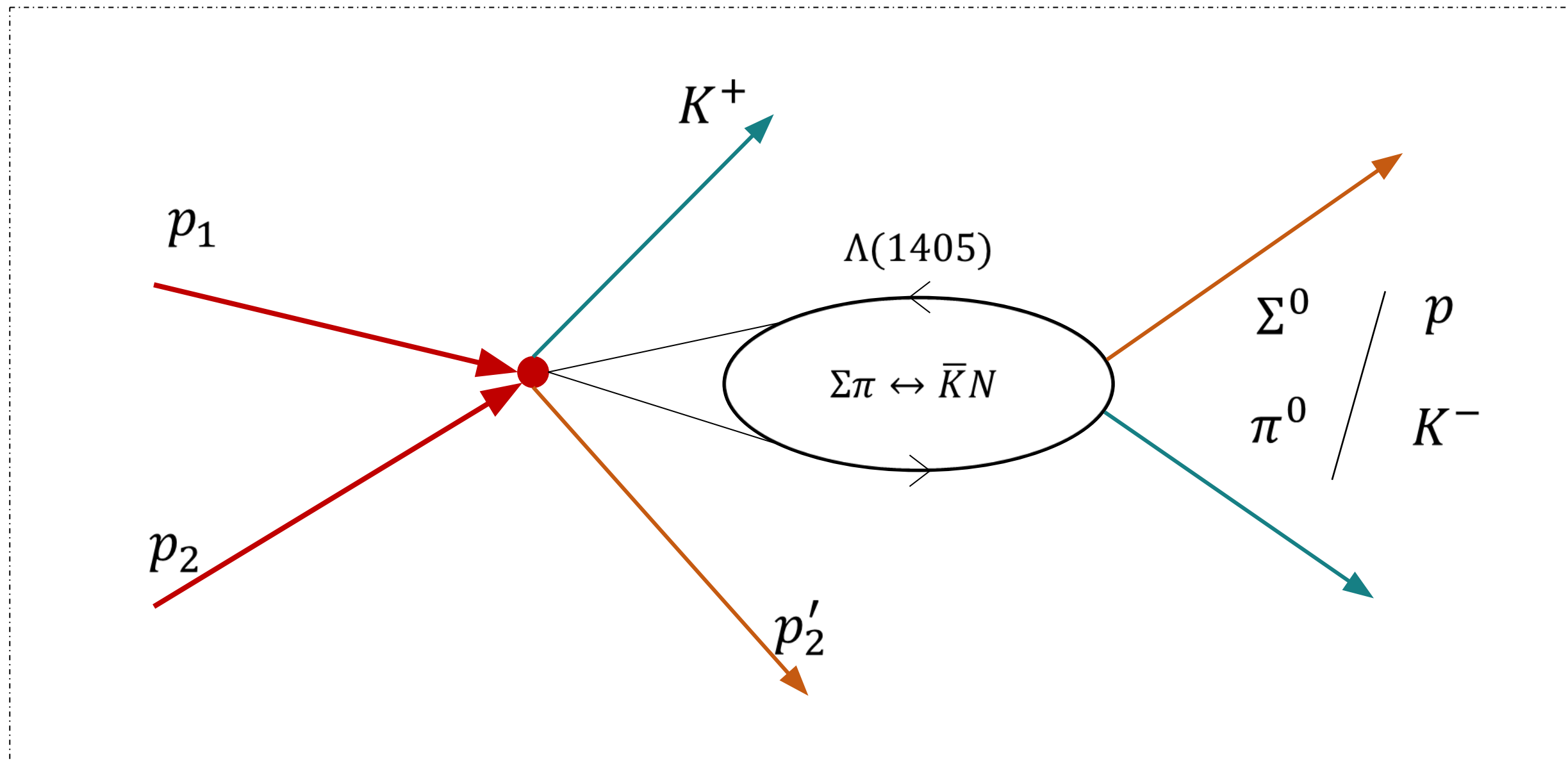
$$M_\Lambda^{PDG} = (1519 \pm 1) \text{ MeV}$$

$$\Gamma_\phi^{PDG} = (4.249 \pm 0.013) \text{ MeV}$$

$$\Gamma_\Lambda^{PDG} = (15 \pm 1) \text{ MeV}$$

\*<https://arxiv.org/abs/1003.4504>

# Coupled Channels Analysis in K-Matrix Formalism



$\Sigma\pi$  analysis described in the previous talk, done by Anna Władyszewska ( $\Sigma^0 \rightarrow \gamma[\Lambda \rightarrow p\pi^-]$ )

Simplified procedure:

1. Measure two raw distributions:

$$M_{pK^-} \text{ \& \ } M_{\Sigma^0\pi^0}$$

2. Re-weight Phase Space simulation within a common coupled amplitude

3. Fit  $M_{\Sigma\pi}$  and  $M_{pK^-}$  simultaneously

$$K_{ij}(s) = \sum_R \frac{g_{R,i}g_{R,j}}{m_R^2 - s}$$

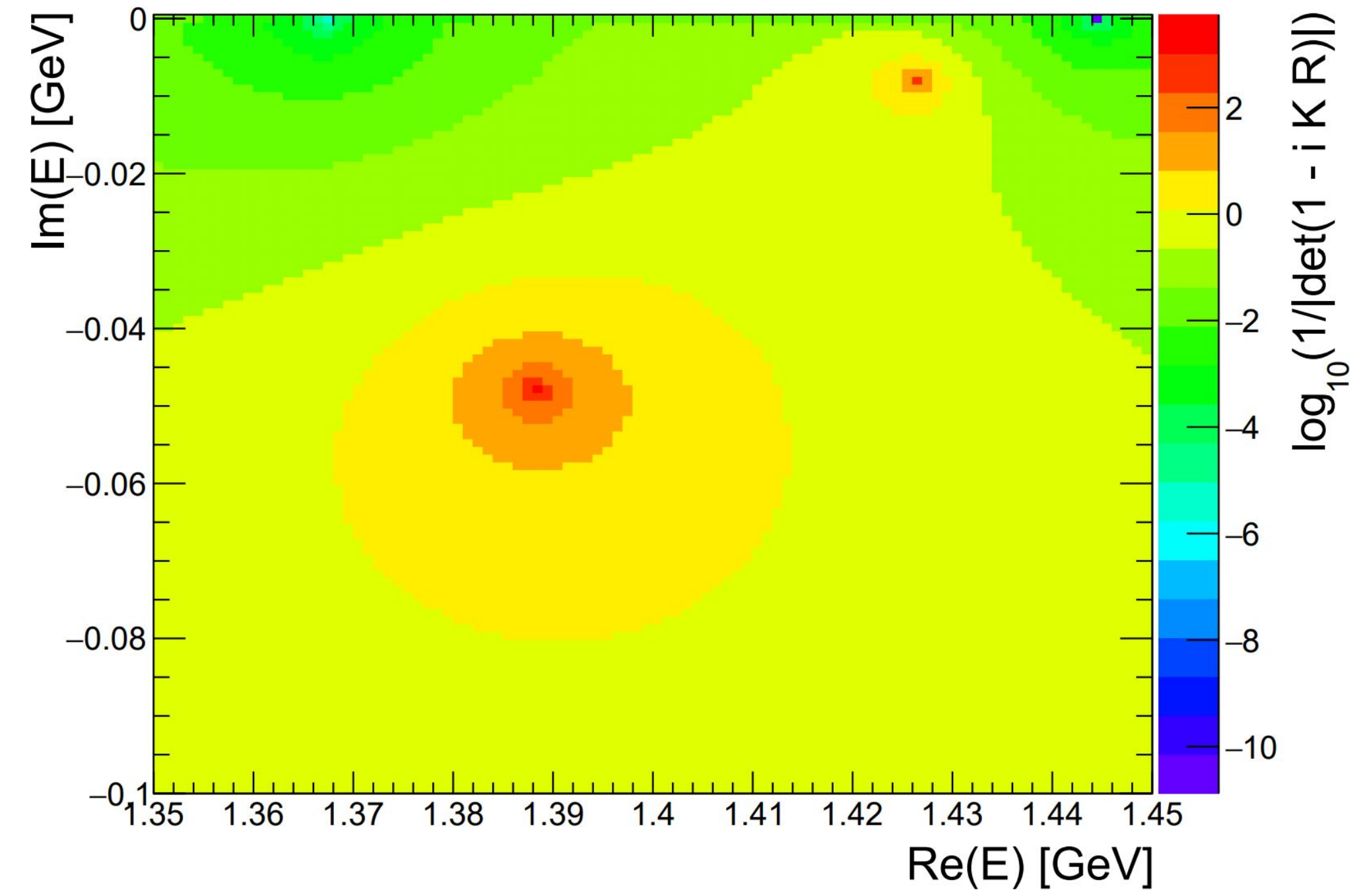
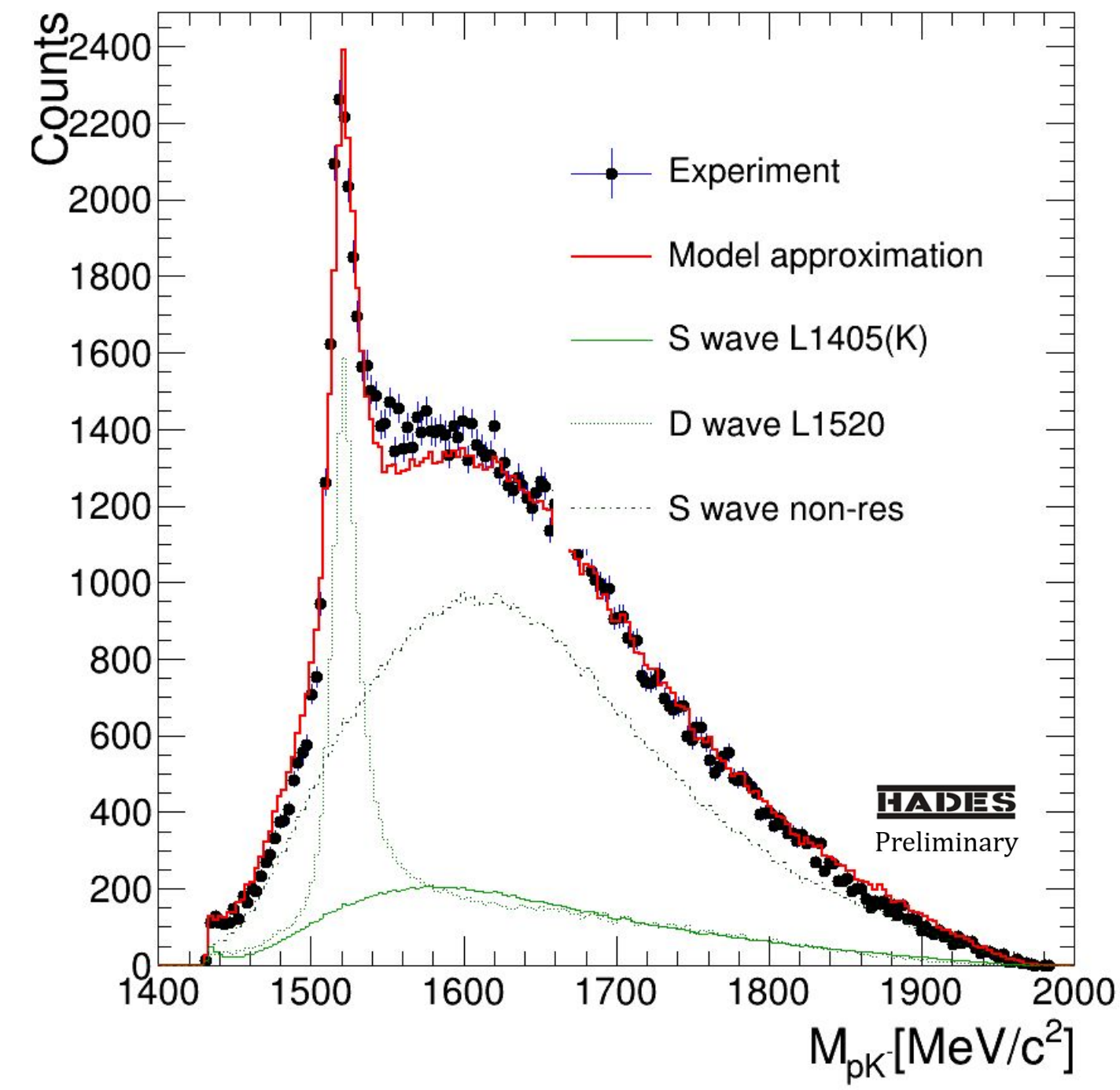
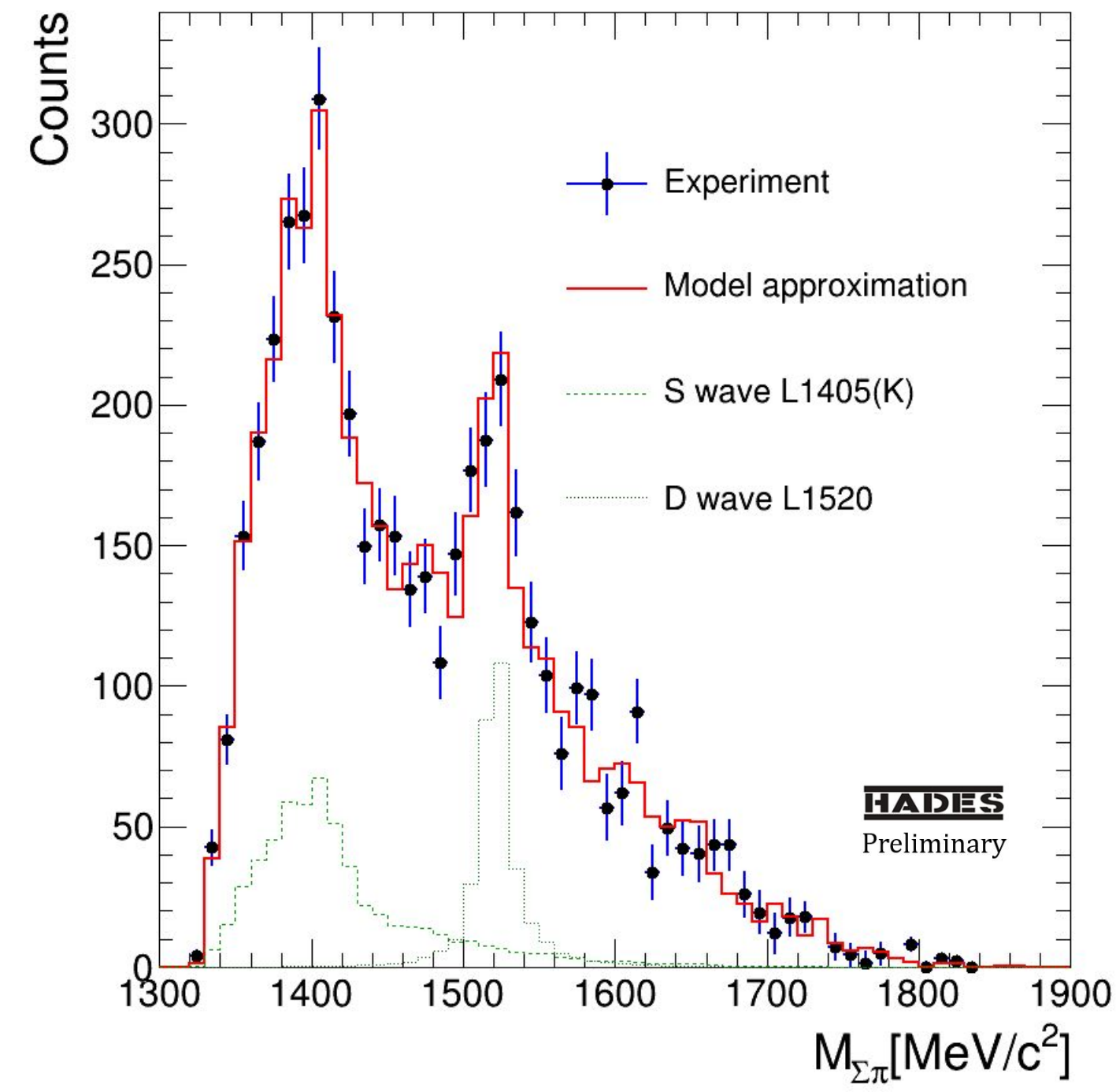
Two-pole description of  $\Lambda(1405)$  – Dynamically generated  $\Sigma\pi - \bar{K}N$  state?

$$A_i(s) = [(I - iK\rho)^{-1}]_i^k P_k$$

(Poles of the amplitude)

\*Efficiency is encoded in the approximation model (phase space simulated, reconstructed and reweighted)

# Raw Data Averaged over Momentum Transfer

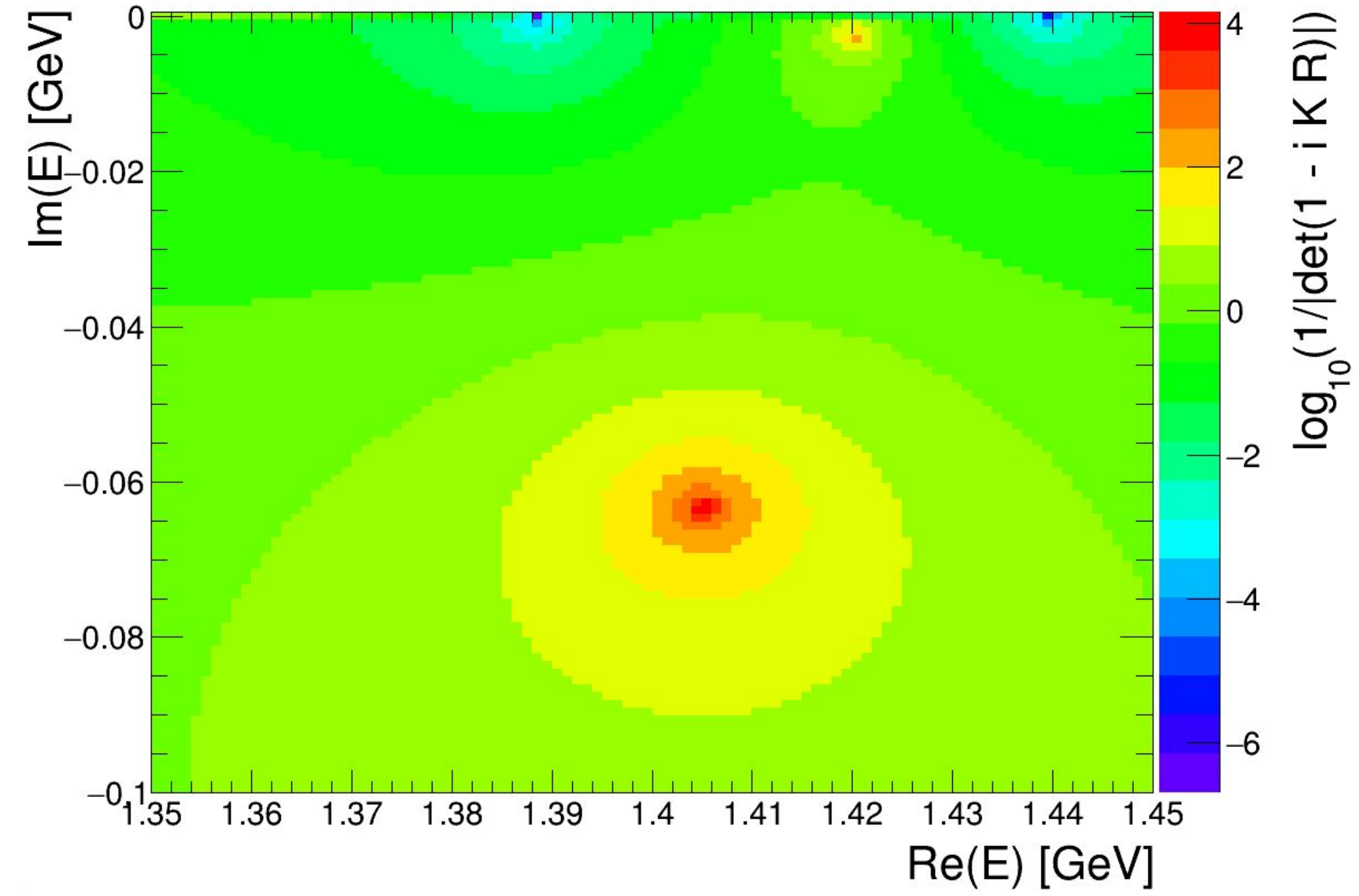
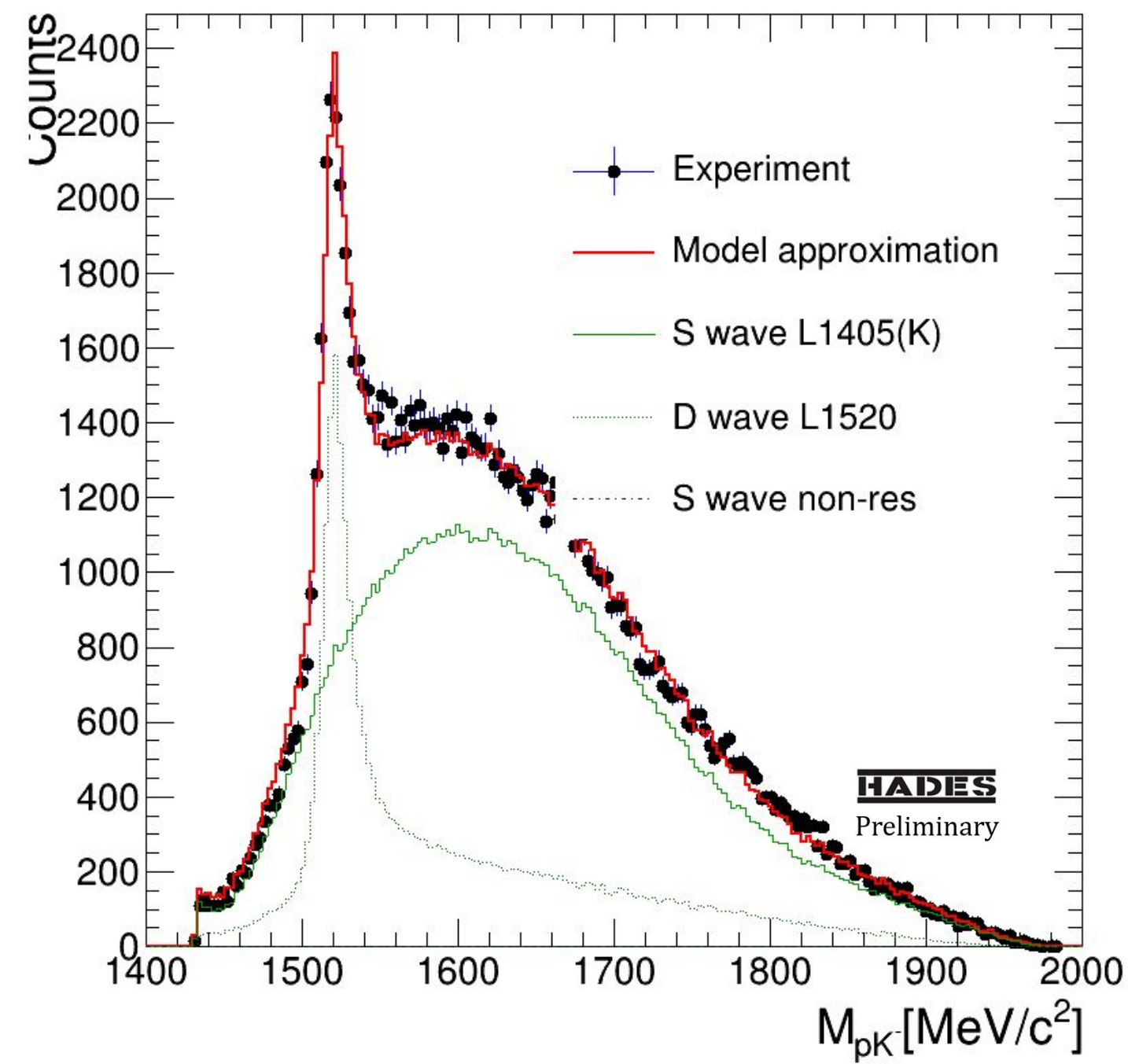
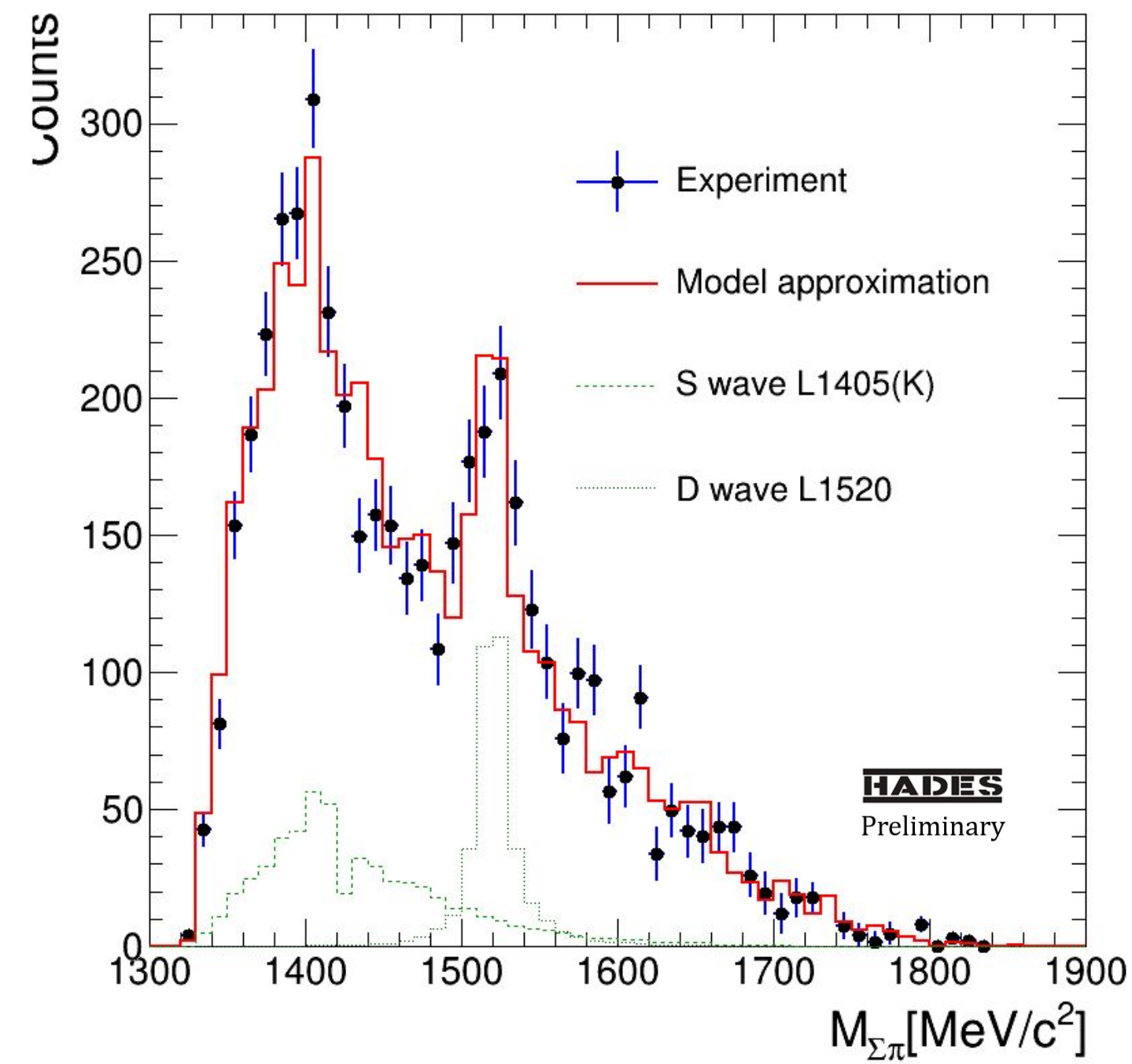


Total intensities with  $\Lambda(1405)$  contribution:

- $I_{pK} = \left| \frac{1}{1 - iq_1 a_{pK}} \right|^2 + c_1 |((1 - IKR)^{-1} P)_1|^2 + |C_{\Lambda(1520)}^{\Sigma\pi} BW_{\Lambda(1520)}|^2$
- $I_{\Sigma\pi} = |1 + c_2 ((1 - IKR)^{-1} P)_2|^2 + |C_{\Lambda(1520)}^{pK} BW_{\Lambda(1520)}|^2$

✓ Fit consistent with this hypothesis

# Raw Data Averaged over Momentum Transfer



- $I_{pK} = \left| \frac{1}{1 - iq_1 a_{pK}} \right|^2 + c_1 |((1 - IKR)^{-1} P)_1|^2 + |C_{\Lambda(1520)}^{\Sigma\pi} BW_{\Lambda(1520)}|^2$
- $I_{\Sigma\pi} = |1 + c_2 ((1 - IKR)^{-1} P)_2|^2 + |C_{\Lambda(1520)}^{pK} BW_{\Lambda(1520)}|^2$

✓ Fit consistent with this hypothesis

# Pole Positions and Theory

Pole positions, \*Recent theory predictions (2000+)

!Not directly comparable (calculations vs parametrization)

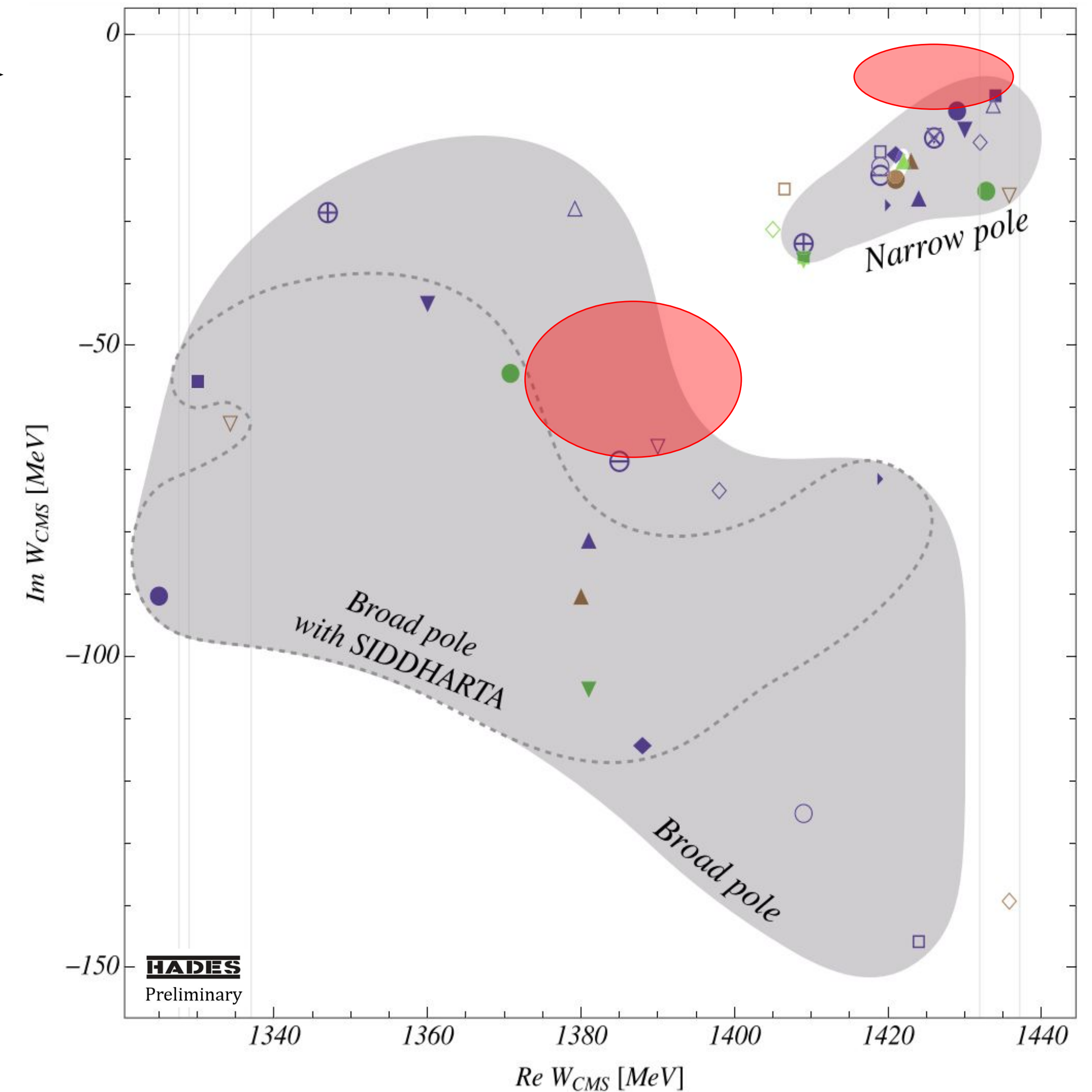
Red areas – poles from this work

Obtained by varying:

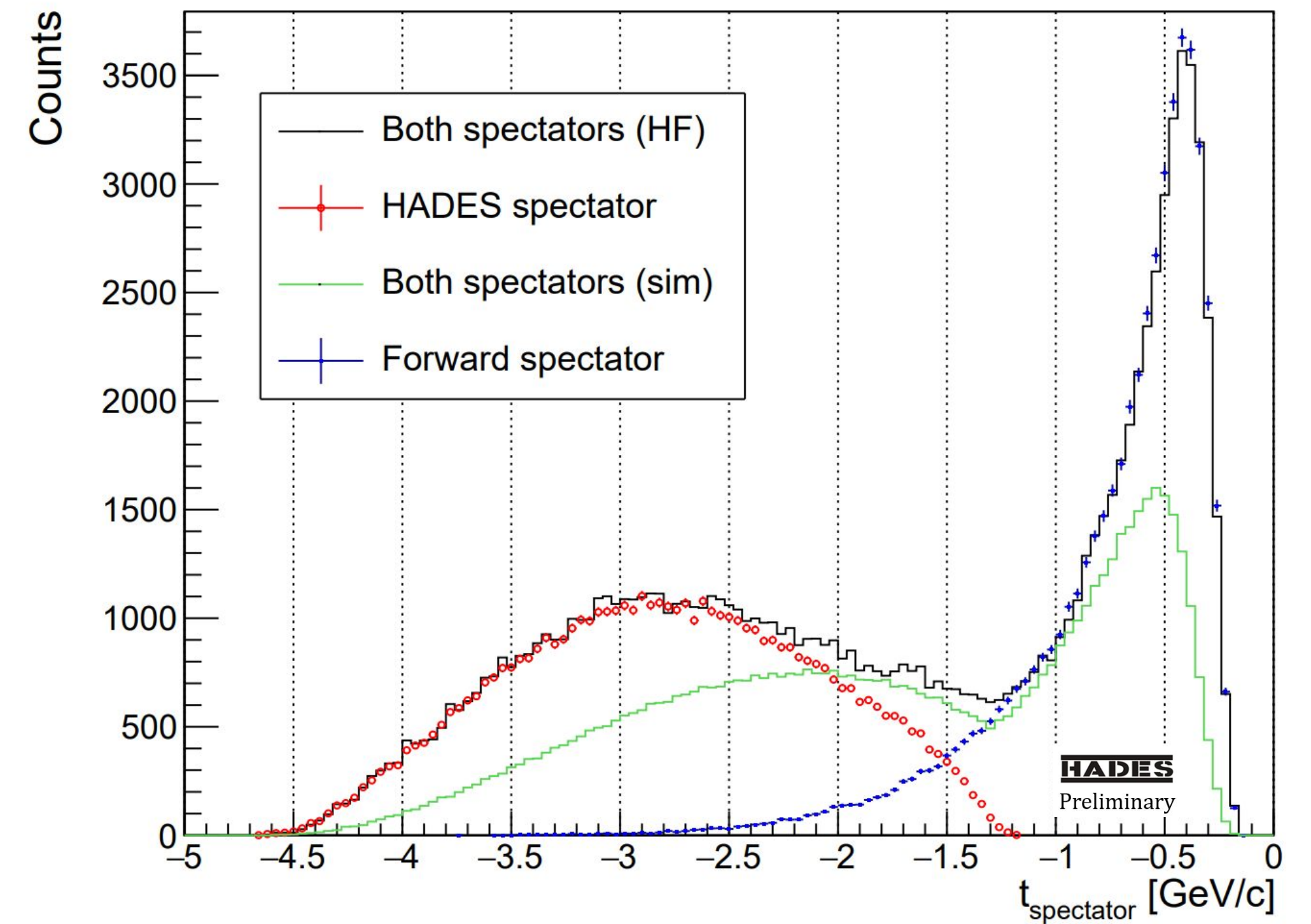
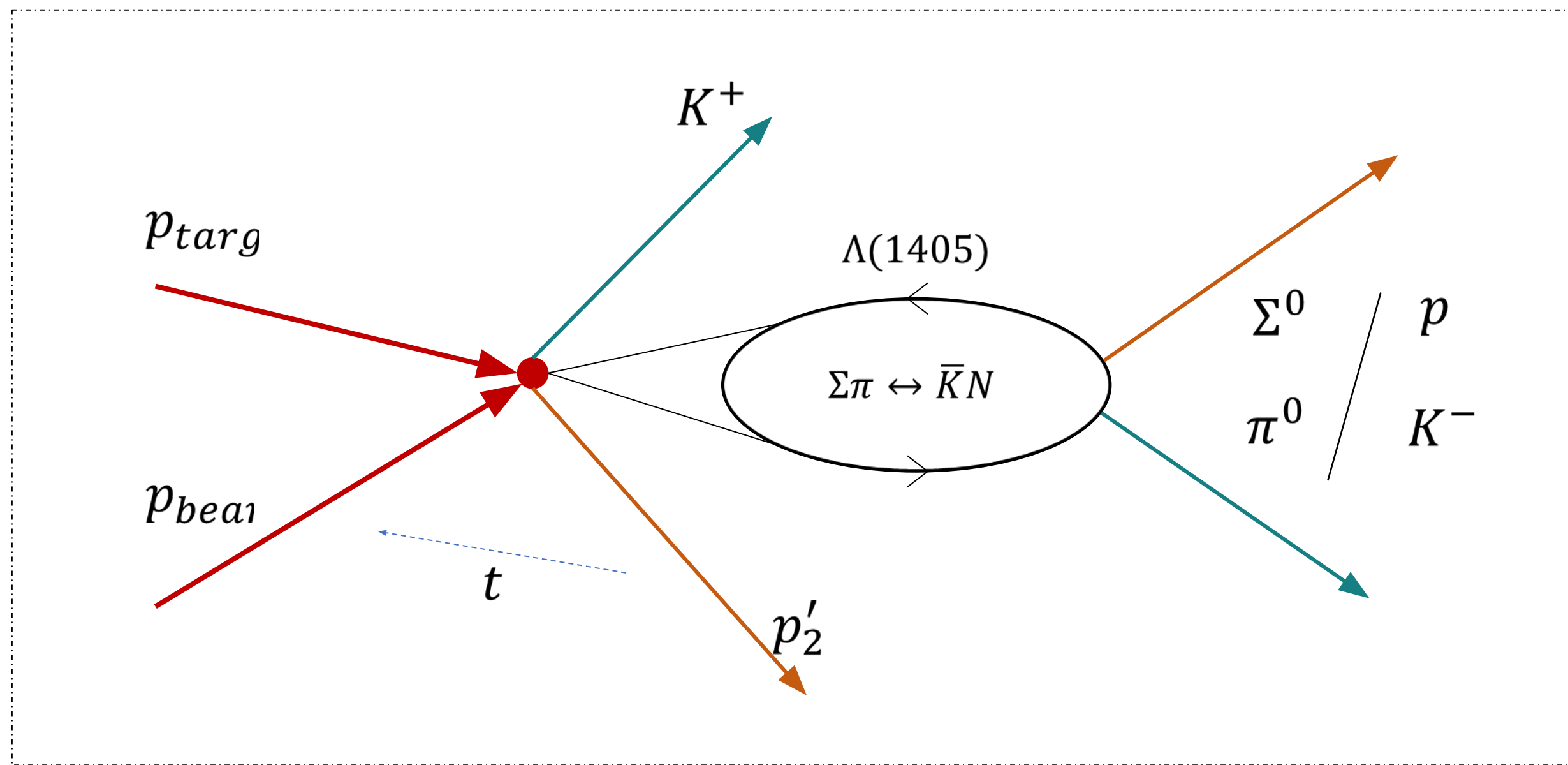
- Global amplitude model
- Production vector
- Fit procedure

Compared to single pole and no Lambda(1405)

✓ Clear fit improvements



# Cross Sections in Momentum Transfer bins



- ✓ Solves proton ambiguity for efficiency correction
- ✓ Can enhance Lambda(1405) visibility
- ✓ Access to branching ratios