

# $2 M_{\odot}$ hybrid stars from metastable hadronic stars

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# Motivation

- ▶ Will the nucleation forbid the appearance of QM in  $2M_{\odot}$  neutron stars?
- ▶ Which constraints are set by the existence of QM in a NS?





# Outline

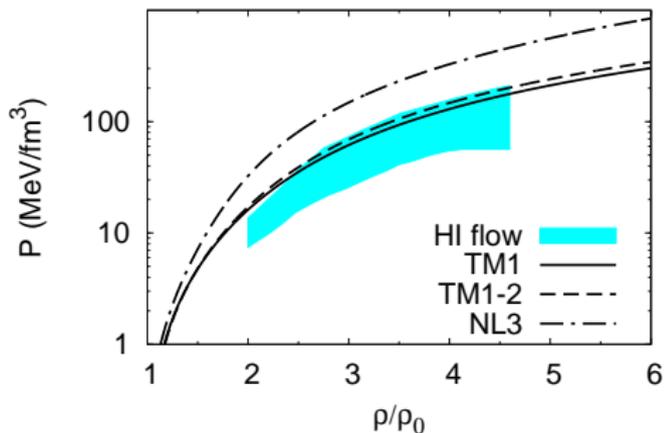
- ▶ EOS: hadron and quark phases
- ▶ Hadron-quark phase transition
- ▶ Including nucleation
- ▶ Discussion



# Framework

## Hadronic Matter

- ▶ Hadronic matter: NL3, TM1, TM1-2
  - ▶ behaviour at large  $\rho$
- ▶ Heavy ion flow data constraints



- ▶ Effect of the inclusion of hyperons



# Framework

## Quark matter

- ▶  $su(3)$  NJL quark model

$$\begin{aligned}\mathcal{L}_{NJL} &= \bar{\psi}(i\gamma^\mu\partial_\mu - \hat{m})\psi + G_S \sum_{a=0}^8 [(\bar{\psi}\lambda_a\psi)^2 + (\bar{\psi}i\gamma_5\lambda_a\psi)^2] \\ &- K \{ \det_f[\bar{\psi}(1 + \gamma_5)\psi] + \det_f[\bar{\psi}(1 - \gamma_5)\psi] \} \\ &- G_V \sum_{a=0}^8 [(\bar{\psi}\gamma_\mu\lambda_a\psi)^2 + (\bar{\psi}\gamma_5\gamma_\mu\lambda_a\psi)^2]\end{aligned}$$

- ▶ no color superconductivity
- ▶ vector term contribution



# Framework

Quark matter: su(3) NJL quark model

## ► Total pressure

$$p = \sum_{i=u,d,s} \int_{k_{Fi}}^{\Lambda} \frac{dk k^2}{2\pi^2} |\epsilon_i| - 2G_s \sum_{i=u,d,s} \sigma_i^2 \\ + 4K\sigma_u\sigma_d\sigma_s + 2G_V \sum_{i=u,d,s} n_i^2 - p_0 - B^* + \sum_{l=e^-, \mu^-} p_l,$$

## ► vector term, extra effective bag parameter

- $B^*$  → defines hadron-quark phase transition (Plagiara&Schaffner-Bielich2008)
- with vector contribution → stiffer quark EOS



# Hadron-quark matter transition

## Gibbs criteria for phase equilibrium

- ▶ **time scale of the deconfinement transition** is determined by the **strong interaction**
- ▶ **quark flavor must be conserved** during the deconfinement transition
- ▶ **Q\* phase**: the deconfined quark matter with flavor content equal to that of the  $\beta$ -stable hadronic phase at the same pressure and temperature.



# Hadron-quark matter transition

## Gibbs criterion

- ▶ **Metastable phase:** starts at the transition point defined by Gibbs criterion

$$\mu_H = \mu_Q \equiv \mu_0, \quad P_H(\mu_0) = P_Q(\mu_0) \equiv P_0,$$

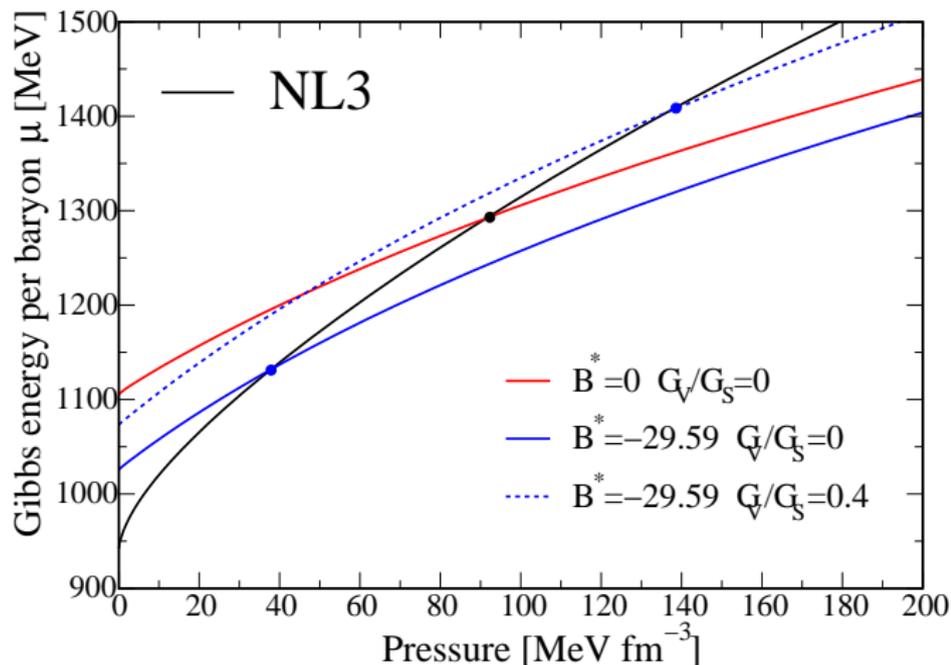
$$\mu_H = \frac{\epsilon_H + P_H}{n_H}, \quad \mu_Q = \frac{\epsilon_Q + P_Q}{n_Q}$$

- ▶ **central pressure  $P > P_0$ :** hadronic phase is metastable  
→ stable quark matter as result of a nucleation process



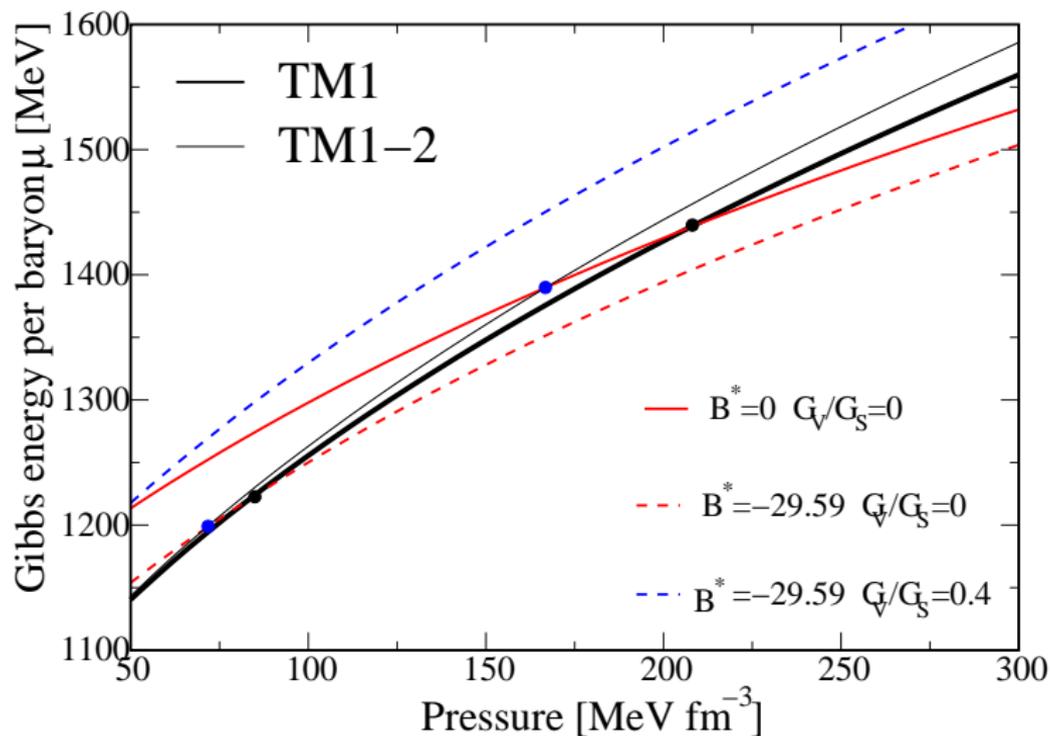
# Hadron-quark matter transition

NL3 - effect of  $B^*$  and  $G_V$



# Hadron-quark matter transition

TM1



# Quantum nucleation

Lifshitz& Kagan 1972, Iida& Sato 1998, Bombaci et al. 2004

- ▶ if  $P > P_0 \rightarrow$  formation of  $Q^*$  phase
- ▶ Free energy difference between system with/without  $Q^*$  droplet

$$U(\mathcal{R}) = \frac{4}{3}\pi n_{Q^*}(\mu_{Q^*} - \mu_H)\mathcal{R}^3 + 4\pi\sigma\mathcal{R}^2$$

- ▶ Curvature and Coulomb effects are neglected



# Critical mass

Lifshitz& Kagan 1972, Iida& Sato 1998, Bombaci et al. 2004

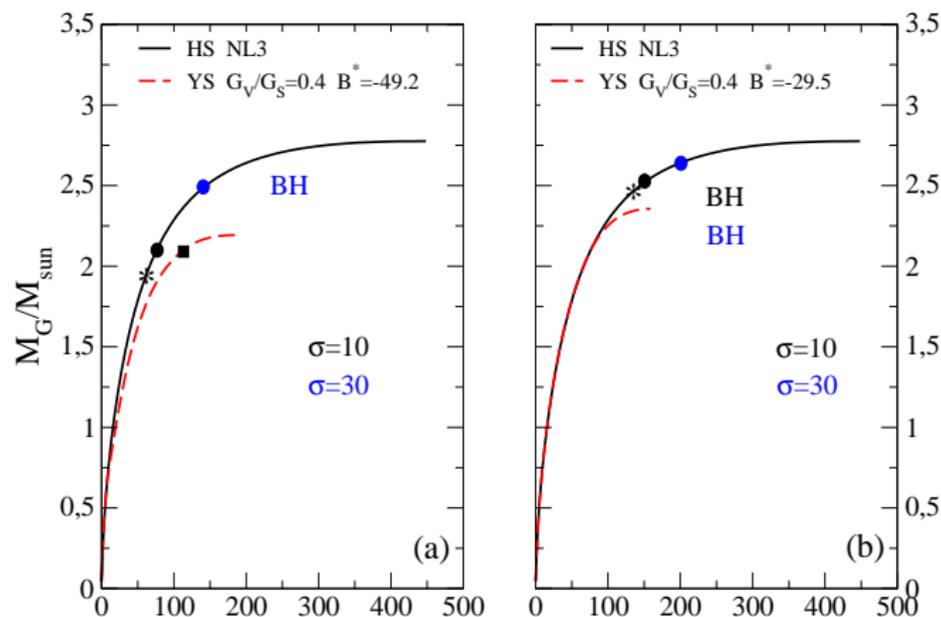
- ▶ WKB gives for quantum nucleation time

$$\tau_q = (\nu_0 \rho_0 N_c)^{-1},$$

- ▶  $\rho_0$ : probability of tunneling
- ▶  $N_c \sim 10^{48}$ : number of nucleation centers in  $r \leq R_{nuc} \sim 100$  m
- ▶  $\nu_0$ : oscillation frequency of the drop in  $U(\mathcal{R})$
- ▶ **Critical mass  $M_{cr}$ : gravitational mass of cold and deleptonized of the metastable hadronic star with  $\tau \sim 1$  yr.**



# Star evolution

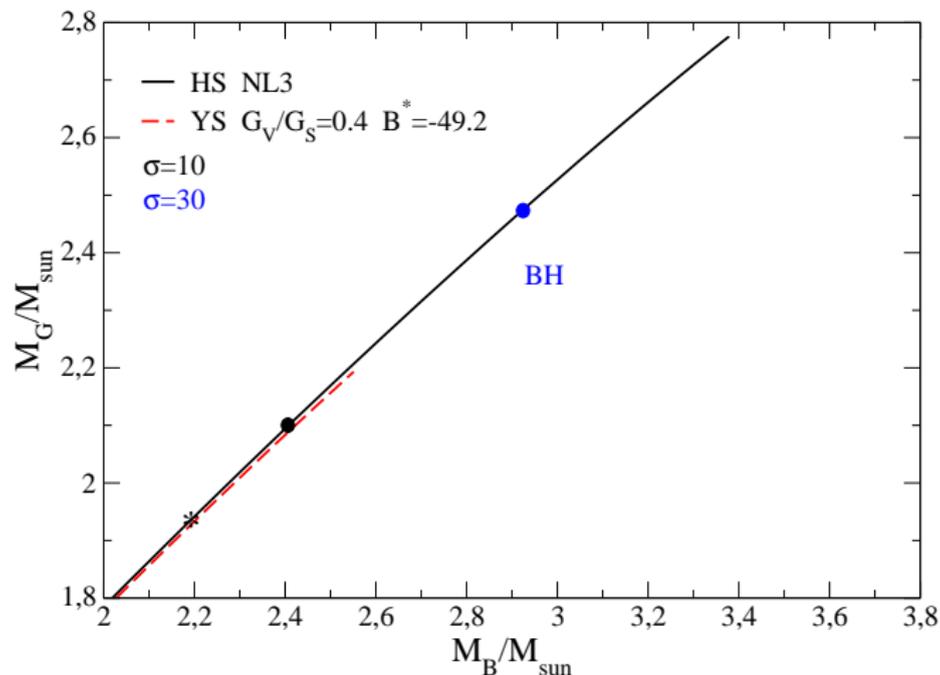


- ▶ Final configuration is not a blackhole if
  - ▶  $G_V$  is strong enough: stiff quark EOS
  - ▶  $B^*$  allows a hadron-quark phase transition a low enough  $\rho$
- ▶ if  $B^* > -49.2$  MeV/fm<sup>3</sup>: transition to BH



# Star evolution

## Surface energy effect



- ▶ Evolution of a star occurs along a vertical line: constant baryonic mass



# Final configuration: surface energy effect

NL3+NJL

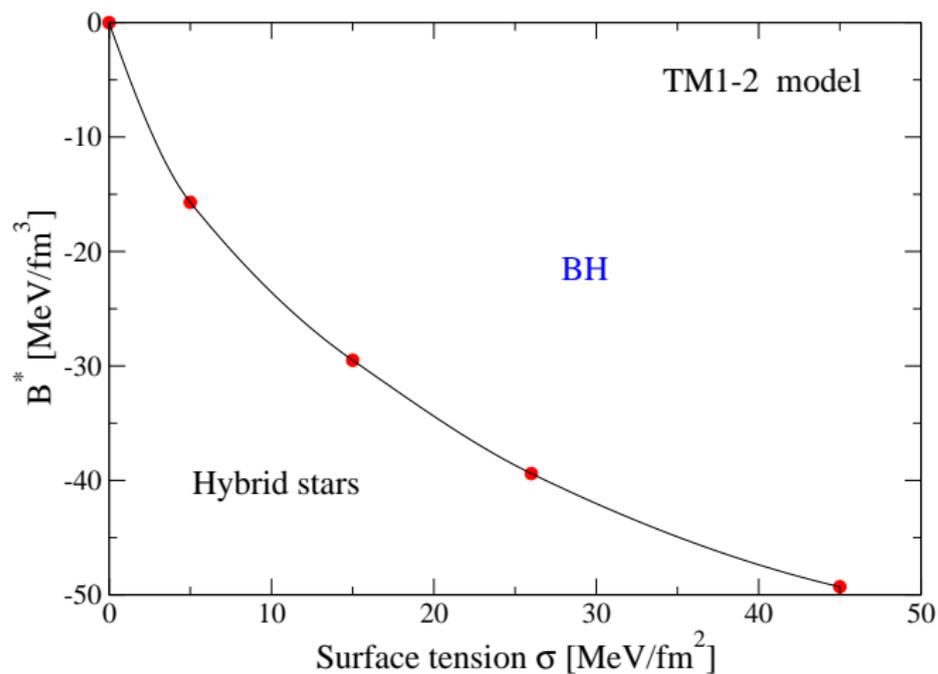
- ▶ Final configuration: hybrid stars with a quark core
- ▶  $B^* = -49.23 \text{ (MeV/fm}^3)$  ,  $G_V/G_S = 0.4$
- ▶  $M(P_0) = 1.92M_\odot$

NL3	$\sigma$ (MeV/fm <sup>2</sup> )	$M_{cr}$ ( $M_\odot$ )	$M_{cr}^b$ ( $M_\odot$ )	$M_{fin}$ ( $M_\odot$ )	$M_{max}^{YS}$ ( $M_\odot$ )
	5	2.00	2.27	1.99	2.19
	10	2.09	2.40	2.08	2.19
	15	2.20	2.54	2.18	2.19
	30	2.45	2.89	BH	2.19



# Stable final configurations

Surface energy vs  $B^*$



# Final configuration

Hybrid star or blackhole

- ▶ TM1+NJL: hybrid star with a mixed phase core,  $G_V = 0$

$\sigma$ $\left(\frac{\text{MeV}}{\text{fm}^2}\right)$	$B^*$ $\left(\frac{\text{MeV}}{\text{fm}^3}\right)$	$P_0$ $\left(\frac{\text{MeV}}{\text{fm}^3}\right)$	$M(P_0)$ $(M_\odot)$	$M_{cr}$ $(M_\odot)$	$M_{fin}$ $(M_\odot)$	$M_{max}^{YS}$ $(M_\odot)$
5	0	206.71	2.08	2.09	BH	1.97
5	-15.78	147.53	2.01	2.03	BH	1.95
10	-29.59	82.89	1.76	1.88	1.87	1.92
30				1.93	BH	1.92
20	-39.46	37.92	1.31	1.85	1.84	1.90
25				2.03	BH	1.90
30	-49.33	26.75	1.11	1.36	1.35	1.88
50				1.87	1.86	1.88
70				2.11	BH	1.88



# Final configuration

Hybrid star or blackhole

TM1-2+NJL: Hybrid stars have a mixed phase core,  $G_V = 0$

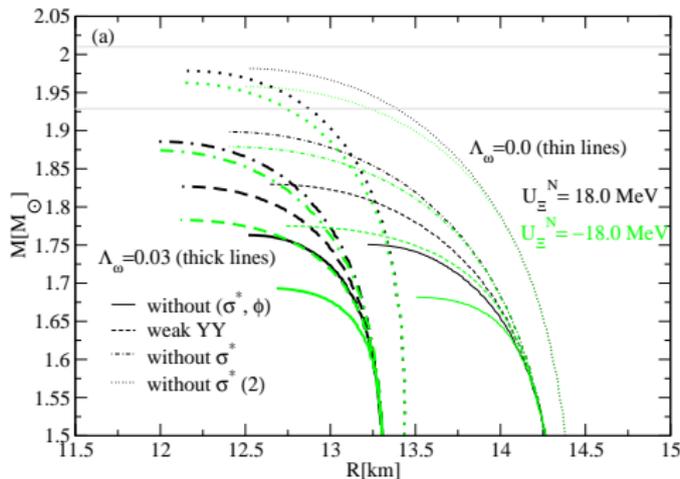
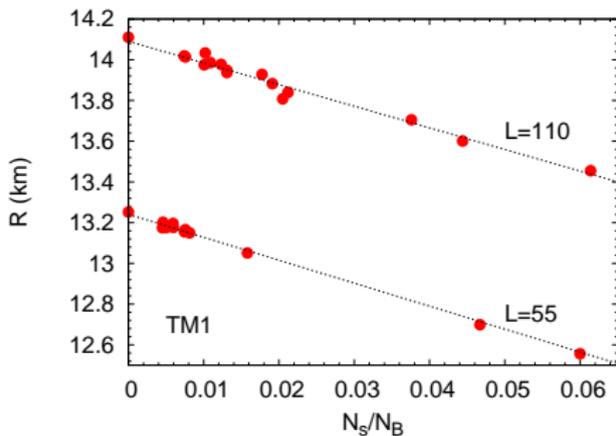
$\sigma$ $\left(\frac{\text{MeV}}{\text{fm}^2}\right)$	$B^*$ $\left(\frac{\text{MeV}}{\text{fm}^2}\right)$	$P_0$ $\left(\frac{\text{MeV}}{\text{fm}^2}\right)$	$M(P_0)$ $(M_\odot)$	$M_{Cr}$ $(M_\odot)$	$M_{fin}$ $(M_\odot)$	$M_{max}^{YS}$ $(M_\odot)$
5	0	166.69	2.12	2.14	BH	2.05
5	-15.78	120.30	2.00	2.03	1.86	2.02
8				2.05	BH	2.02
10	-29.59	70.30	1.73	1.87	1.86	1.99
15				1.93	1.92	1.99
20				2.00	BH	1.99
25	-39.46	35.93	1.31	1.94	1.95	1.97
30				2.04	BH	1.97
45	-49.33	26.39	1.12	1.92	1.92	1.94
50				2.03	BH	1.94



# Effect of the strangeness

## Hadronic EOS with hyperons

- ▶ Include hyperons in the RMF
- ▶  $g_{\omega H}$ ,  $g_{\rho H}$ , and  $g_{\phi H}$  are determined from SU(6) symmetry
- ▶  $U_{\Lambda} = -28\text{MeV}$ ,  $U_{\Sigma} = 30\text{ MeV}$ ,  $U_{\Xi} = 18\text{ MeV}$ ,  $g_{\sigma^* \gamma} = 0$



# Effect of the strangeness

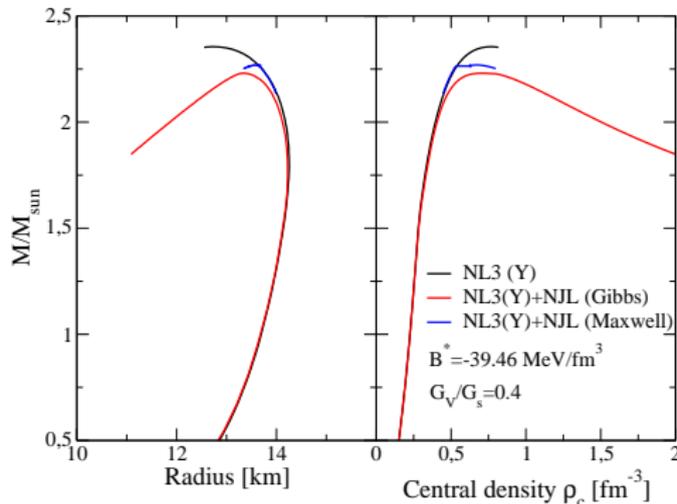
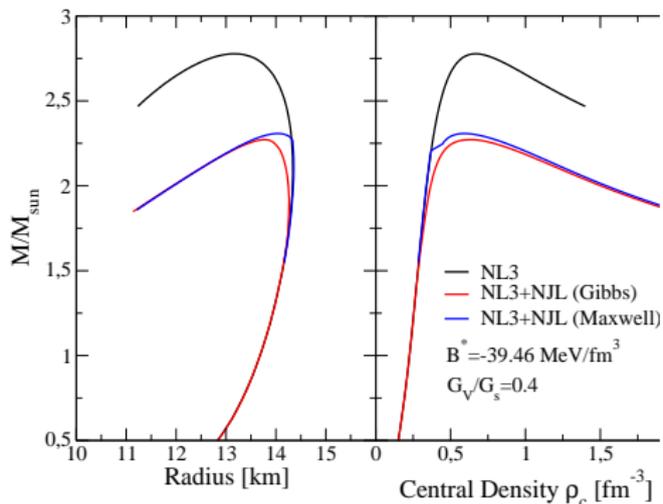
►  $B^* = -39.46 \text{ (MeVfm}^3\text{)}$

Model	$\sigma$ $\left(\frac{\text{MeV}}{\text{fm}^2}\right)$	$P_0$ $\left(\frac{\text{MeV}}{\text{fm}^3}\right)$	$M(P_0)$ $(M_\odot)$	$M_{cr}$ $(M_\odot)$	$M_{fin}$ $(M_\odot)$	$M_{max}^{YS}$ $(M_\odot)$
NL3						
N	5	97.87	2.27	2.33	BH	2.27
N	30			2.57	BH	2.27
<b>NY</b>	<b>29</b>	<b>21.63</b>	<b>1.19</b>	<b>2.22</b>	<b>2.20</b>	2.23
TM1-2						
N	25	35.93	1.31	1.94	1.95	1.97
N	30			2.04	BH	1.97
<b>NY</b>	<b>11.5</b>	<b>14.16</b>	<b>0.925</b>	<b>1.83</b>	<b>1.82</b>	1.90



# Gibbs vs Maxwell construction

- ▶ **Finite size effects and Coulomb interaction:** close to Maxwell const  $\gtrsim 50 \text{ MeV/fm}^2$  (Endo et al, PTP 2006, Maruyama et al PRD76 (2007))



# Discussion

## Very stiff hadronic EOS

### NL3, very stiff hadronic EOS, Hybrid stars with quark core

- ▶  $G_V = 0$ 
  - ▶ nucleation  $\rightarrow$  BH if  $|B^*| \leq |B_c^*|$
  - ▶ if  $|B^*| > |B_c^*|$ , nucleation to stable hybrid stars but  $M < 2M_\odot$
- ▶  $G_V > G_{Vc}$ 
  - ▶ hadron-quark transition at larger  $\rho$
  - ▶ nucleation  $\rightarrow$  BH if  $|B^*| \leq |B_c^*|$
  - ▶ if  $|B^*| > |B_c^*|$ , nucleation to stable hybrid stars and  $M \gtrsim 2M_\odot$
  - ▶ however if  $\sigma$  too large  $\rightarrow$  BH



# Discussion

## Stiff hadronic EOS

### TM1: stiff hadronic EOS, hybrid stars with mixed phase

- ▶  $G_V < 0.2$ 
  - ▶ quark EOS too stiff
  - ▶ no hadron-quark transition or at too large  $\rho$
- ▶  $G_V = 0$ 
  - ▶ if  $|B^*| > |B_c^*|$  nucleation to stable hybrid stars (mixed phase in core)
  - ▶ Maximum  $M$  depends on  $\sigma$
  - ▶ TM1 with  $\sigma \lesssim 5 - 50 \text{ MeV/fm}^2$ ,  $M_{max} \sim 1.92 - 1.88 M_\odot$
  - ▶ TM1-2 with  $\sigma \lesssim 5 - 15 \text{ MeV/fm}^2$ ,  $M_{max} \sim 2.02 - 1.99 M_\odot$



# Conclusions

- ▶ Not all stable hybrid stars are populated after nucleation!
- ▶ Hadronic EOS with hyperons
  - ▶ if repulsive YY interaction included only slightly smaller maximum mass ( [more information about hyperon-hyperon interaction needed!](#) )
- ▶ Could nucleation occur at finite T to massive stable hybrid stars? [needs checking!](#)
- ▶ HI flow constraints  $\rightarrow \sim 2 - 2.1 M_{\odot}$  but not  $2.4 M_{\odot}$
- ▶ How much confidence on HI constraints? [More precise high density constraints are need!](#)
- ▶ Better knowledge of surface tension  $\sigma$

