

# Electromagnetic Radiation from Heavy-Ion Collisions: From Microscopic Aspects to Bulk Dynamics

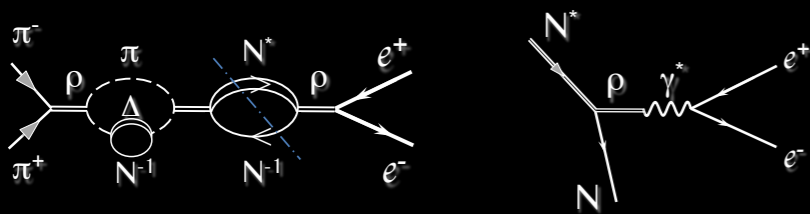
Helmholtz Alliance  
Extremes of Density and Temperature: Cosmic Matter in the Laboratory

## ExtreMe Matter Institute EMMI

EMMI Rapid Reaction Task Force

Emissivity of matter under extreme conditions, dileptons and chiral symmetry: established connections and missing links

October 5-15, 2013, GSI, Darmstadt, Germany



### Key Topics

- Baryon resonances: present status and understanding of vector-meson (mainly rho)-resonance couplings
- Electromagnetic transition form factors of baryonic resonances in the time- and space-like regions: theoretical treatment and experimental approaches
- Dielectron and photon radiation from dense nuclear matter
- New theoretical developments in the context of electromagnetic decays of baryonic resonances

### Information

<http://www.gsi.de/emmi/rrtf>

### Organizers

Tetyana Galatyuk, TU Darmstadt  
Piotr Salabura, Jagiellonian University, Kraków  
Joachim Stroth, Frankfurt University

### Symposium

October 9th, 2013; 10:00 a. m.  
GSI, Lecture Hall (KBW)

### More about EMMI

[www.gsi.de/emmi](http://www.gsi.de/emmi)



Charles Gale  
McGill University



## OUTLINE

- Sources & EM emissivity: Rates
- Modelling the evolving system:
  - 3D hydro
  - 3D viscous hydro
  - Fluctuating initial states
- How are the photon yields dependent on the dynamics?
- Status of our interpretation of the data

# Sources of photons in a relativistic nuclear collision:

Hard direct photons. pQCD with shadowing  
Non-thermal

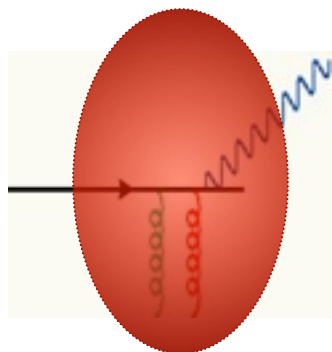
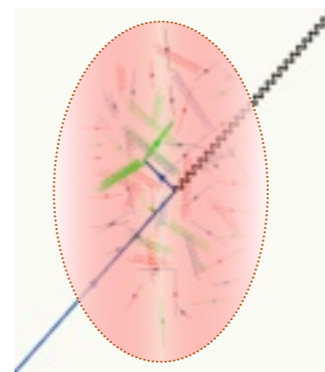
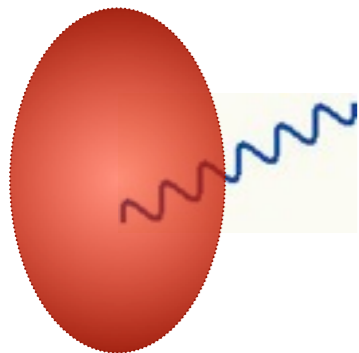
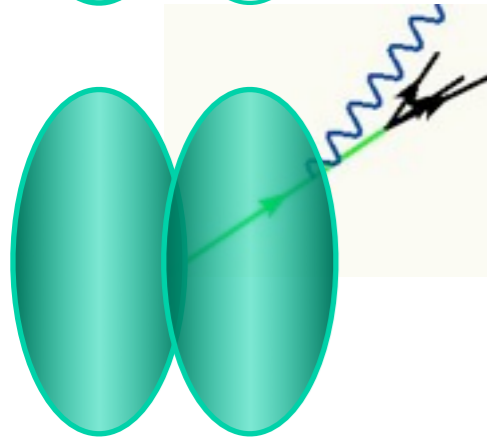
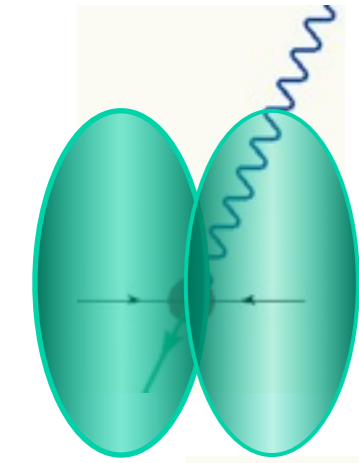
Fragmentation photons. pQCD with shadowing  
Non-thermal

Thermal photons  
Thermal

Jet-plasma photons  
Thermal

Jet in-medium bremsstrahlung  
Thermal

Pre-equilibrium?



# INFO CARRIED BY THE RADIATION

$$dR = -\frac{g^{\mu\nu}}{2\omega} \frac{d^3k}{(2\pi)^3} \frac{1}{Z} \sum_i e^{-\beta K_i} \sum_f (2\pi)^4 \delta(p_i - p_f - k) \\ \times \langle j | J_\mu | i \rangle \langle i | J_\nu | j \rangle$$

Thermal ensemble average of the current-current correlator

Emission rates:

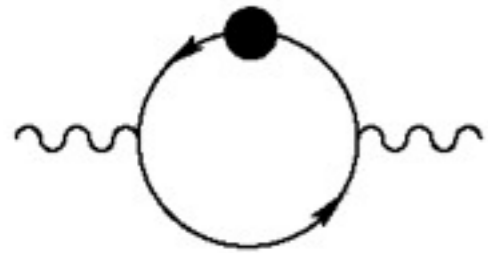
$$\omega \frac{d^3R}{d^3k} = -\frac{g^{\mu\nu}}{(2\pi)^3} \text{Im}\Pi_{\mu\nu}^R(\omega, k) \frac{1}{e^{\beta\omega} - 1} \quad (\text{photons})$$

$$E_+ E_- \frac{d^6R}{d^3p_+ d^3p_-} = \frac{2e^2}{(2\pi)^6} \frac{1}{k^4} L^{\mu\nu} \text{Im}\Pi_{\mu\nu}^R(\omega, k) \frac{1}{e^{\beta\omega} - 1} \quad (\text{dileptons})$$

McLerran, Toimela (85), Weldon (90), Gale, Kapusta (91)



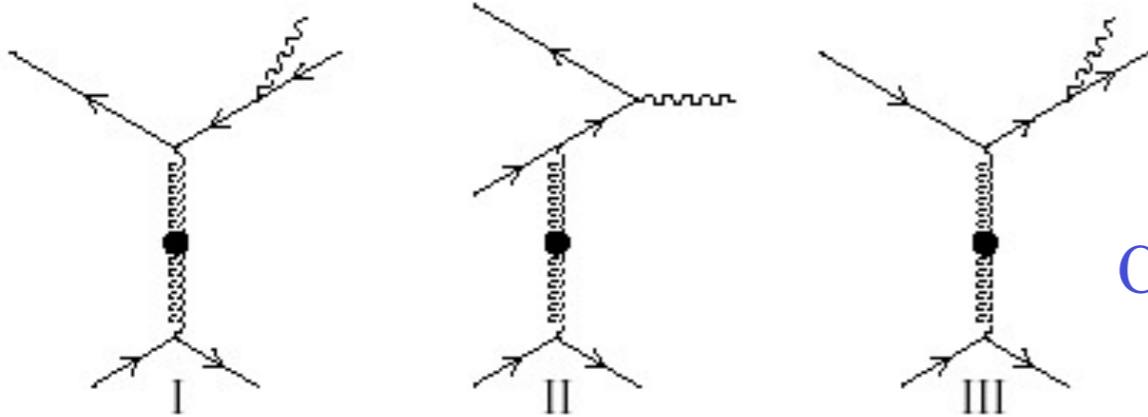
# Thermal Photons from hot QCD: HTL program (Klimov (1981), Weldon (1982), Braaten & Pisarski (1990); Frenkel & Taylor (1990))



$$\text{Im } \Pi_{R\mu}^{\mu} \sim \ln \left( \frac{\varpi T}{(m_{th} (\sim gT))^2} \right)$$

Kapusta, Lichard, Seibert (1991)  
Baier, Nakkagawa, Niegawa, Redlich (1992)

Going to two loops: Aurenche, Kobes, Géelis, Petitgirard (1996)  
Aurenche, Géelis, Kobes, Zaraket (1998)



Co-linear singularities:

$$\alpha_s^2 \left( \frac{T^2}{m_{th}^2} \right) \sim \alpha_s$$

2001: Results complete at  $O(\alpha_s)$

Arnold, Moore, and Yaffe JHEP **12**, 009 (2001); JHEP **11**, 057 (2001)  
Incorporate LPM; Inclusive treatment of collinear enhancement,  
photon and gluon emission



## Going beyond LO AMY rates?

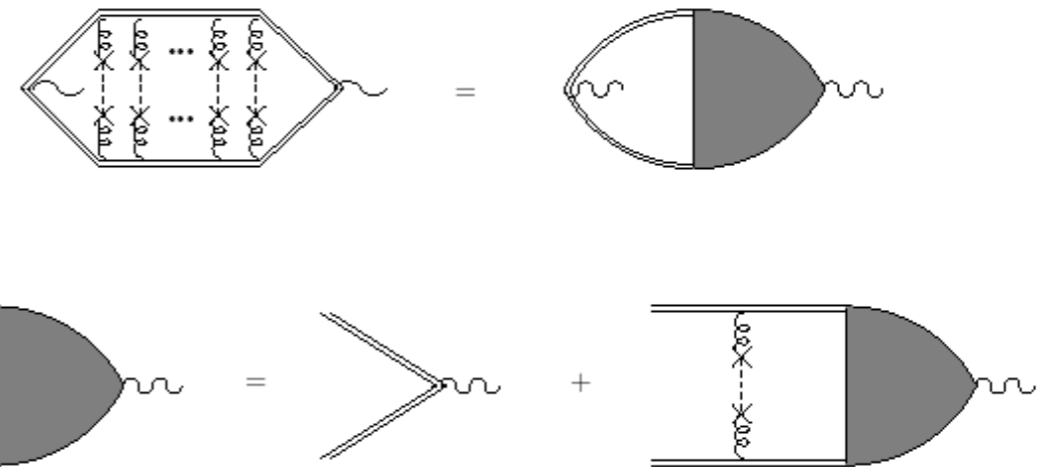
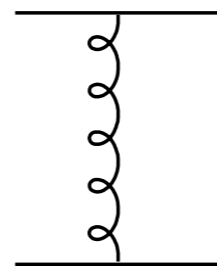
- Approach is LO, but

$$\alpha_s \sim 0.2 - 0.3$$

- Integral equation can be written in terms of a Dyson-Schwinger type iteration...

which contains a scattering kernel:

$$C(q_{\perp})|_{\text{LO}} = g^2 C_R T \frac{m_D^2}{q_{\perp}^2 (q_{\perp}^2 + m_D^2)}$$



Aurenche, Gélis, Zaraket (2002)

The techniques used to derive this - and all results in perturbative, finite-temperature field theory - rely on the scale separation:

$$gT \ll T$$

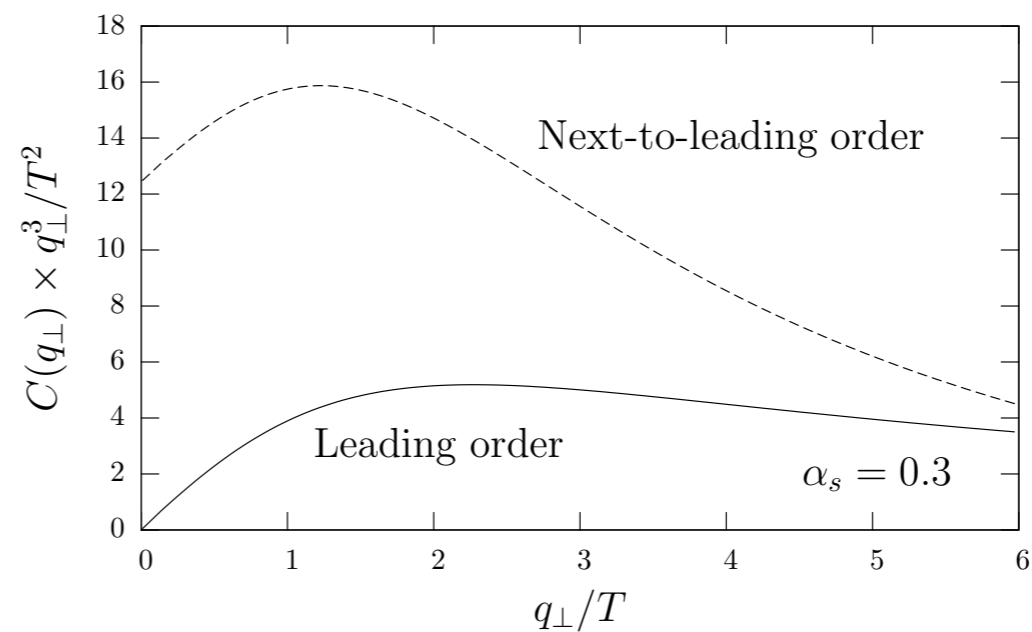
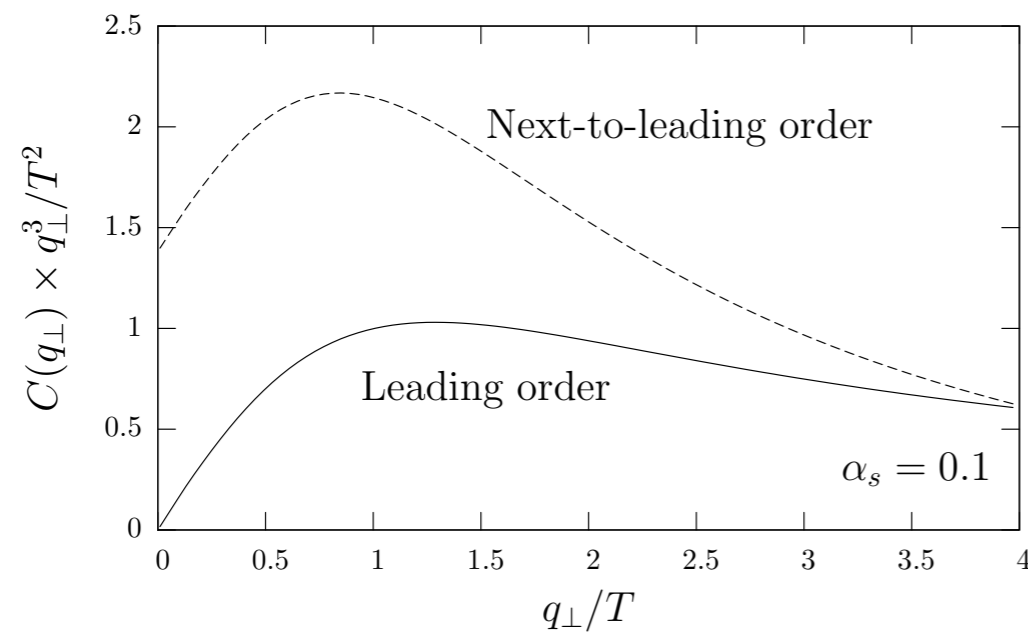
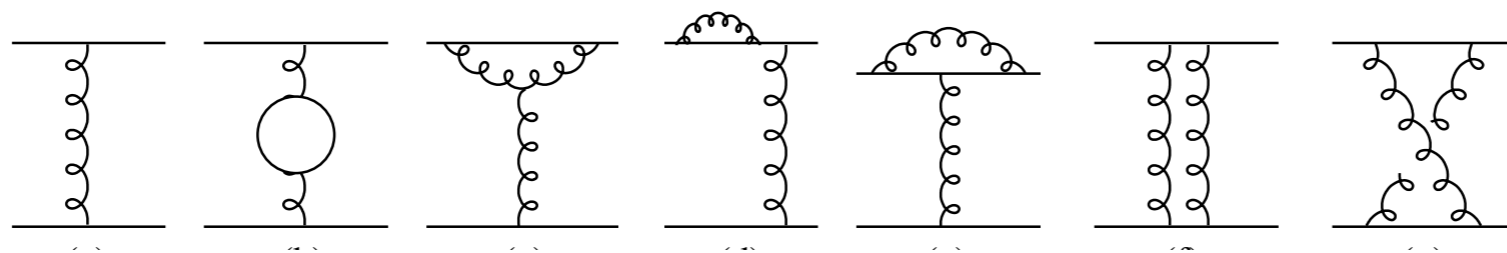
$$\text{soft} \ll \text{hard}$$

# The LO-NLO scattering kernel(s)

Clue that NLO effects might be important: Heavy quark diffusion

$$C(q_{\perp})|_{\text{LO}} \rightarrow C(q_{\perp})|_{\text{NLO}}$$

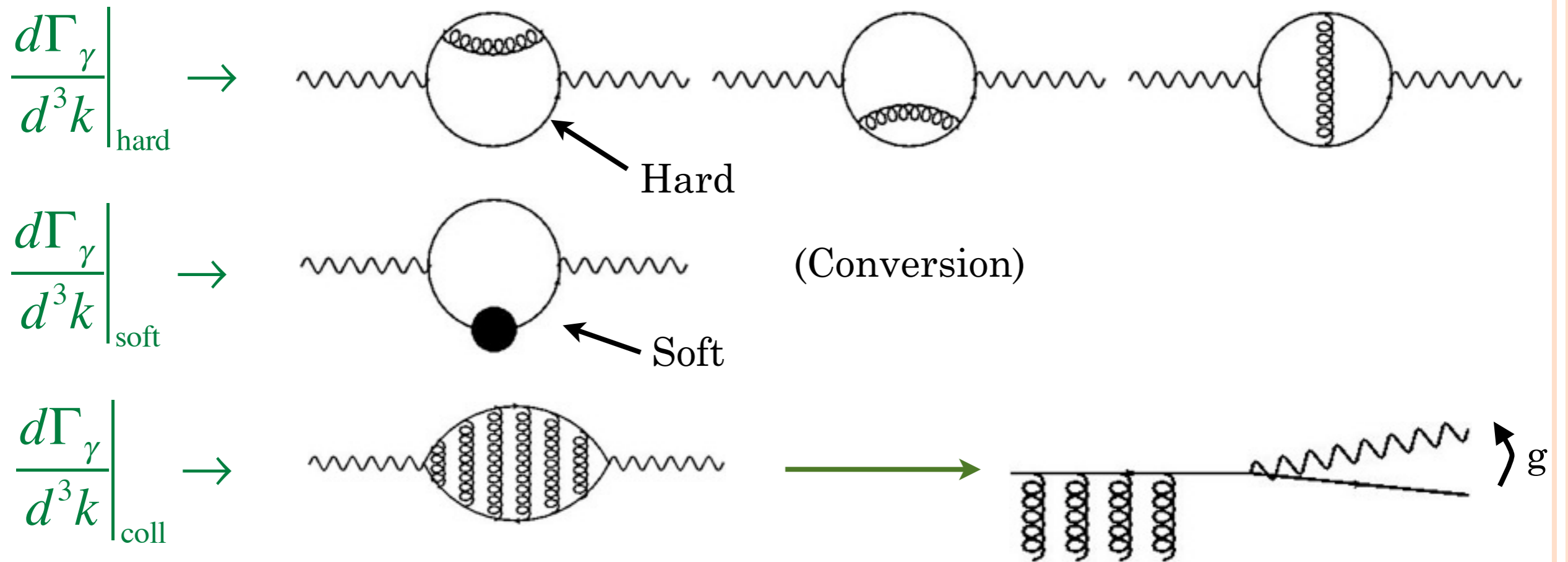
Simon Caron-Huot PRD (2009)



Possible large effects on photon production!?

# Photon emission at LO

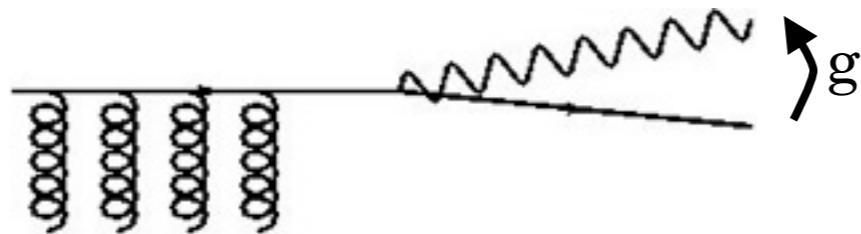
$$\left. \frac{d\Gamma_\gamma}{d^3k} \right|_{\text{LO}} = \left. \frac{d\Gamma_\gamma}{d^3k} \right|_{\text{hard}} + \left. \frac{d\Gamma_\gamma}{d^3k} \right|_{\text{soft}} + \left. \frac{d\Gamma_\gamma}{d^3k} \right|_{\text{coll}}$$



# The LO-NLO scattering kernels

Ghiglieri, Hong, Kurkela, Lu, Moore, Teaney, JHEP (2013)

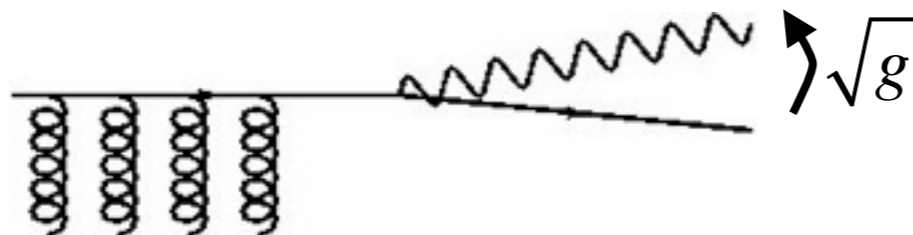
The two main contributions:



$$C(q_T)_{\text{LO}} = \frac{Tg^2 m_D}{q_T (q_T + m_D)} \Rightarrow \text{NLO}$$

Simon Caron-Huot PRD (2009)

Enhanced at NLO



Larger angle bremsstrahlung

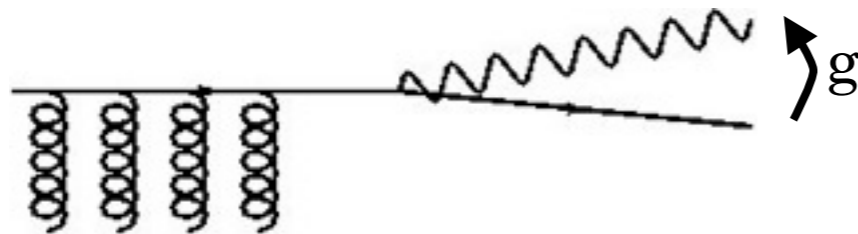
Suppressed at NLO



# The LO-NLO scattering kernels

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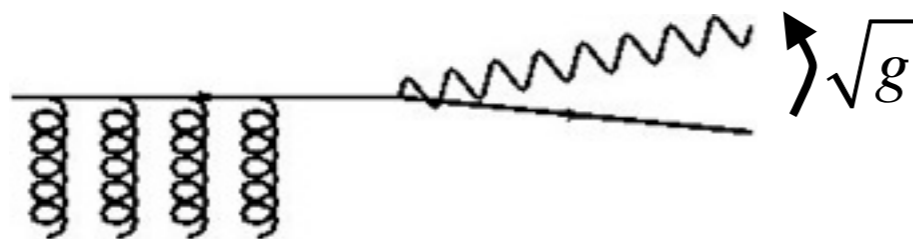
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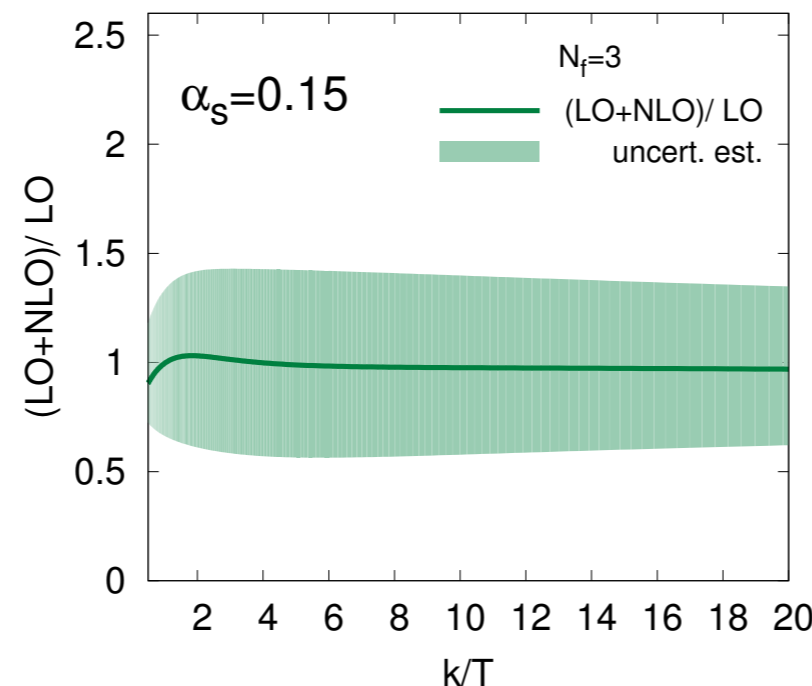
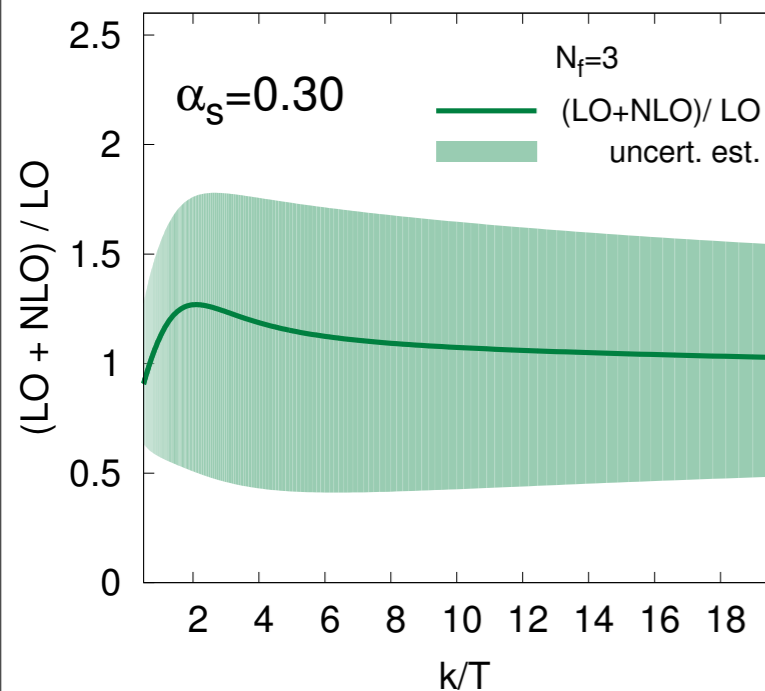
Simon Caron-Huot PRD (2009)

Enhanced at NLO



Larger angle bremsstrahlung

Suppressed at NLO



- Net correction to photon production rate is modest up to high  $k/T$
- Techniques developed here have many more applications in FTFT

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# ELECTROMAGNETIC RADIATION FROM HADRONS

## Chiral, Massive Yang-Mills:

O. Kaymakcalan, S. Rajeev, J. Schechter, PRD 30, 594 (1984)

$$\mathcal{L} = \frac{1}{8} F_\pi^2 \text{Tr} D_\mu U D^\mu U^\dagger + \frac{1}{8} F_\pi^2 \text{Tr} M (U + U^\dagger) \\ - \frac{1}{2} \text{Tr} (F_{\mu\nu}^L F^{L\mu\nu} + F_{\mu\nu}^R F^{R\mu\nu}) + m_0^2 \text{Tr} (A_\mu^L A^{L\mu} + A_\mu^R A^{R\mu}) \\ + \text{non-minimal terms}$$

Parameters and form factors are constrained by hadronic phenomenology:

- Masses & strong decay widths
- Electromagnetic decay widths
- Other hadronic observables:

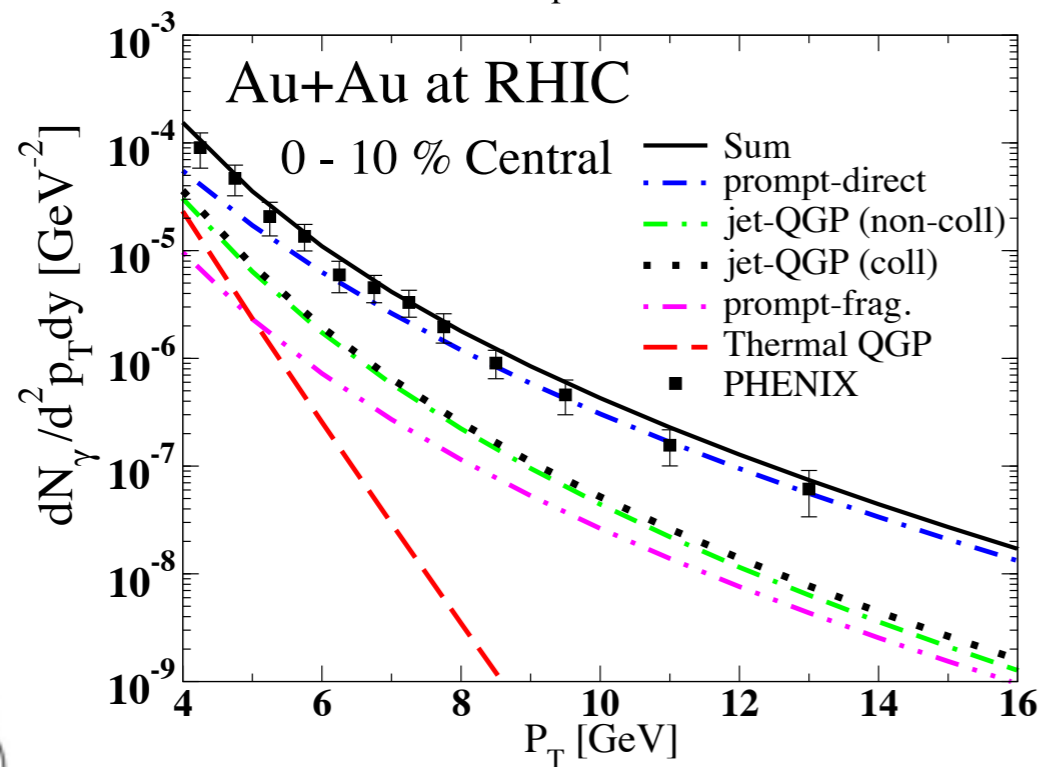
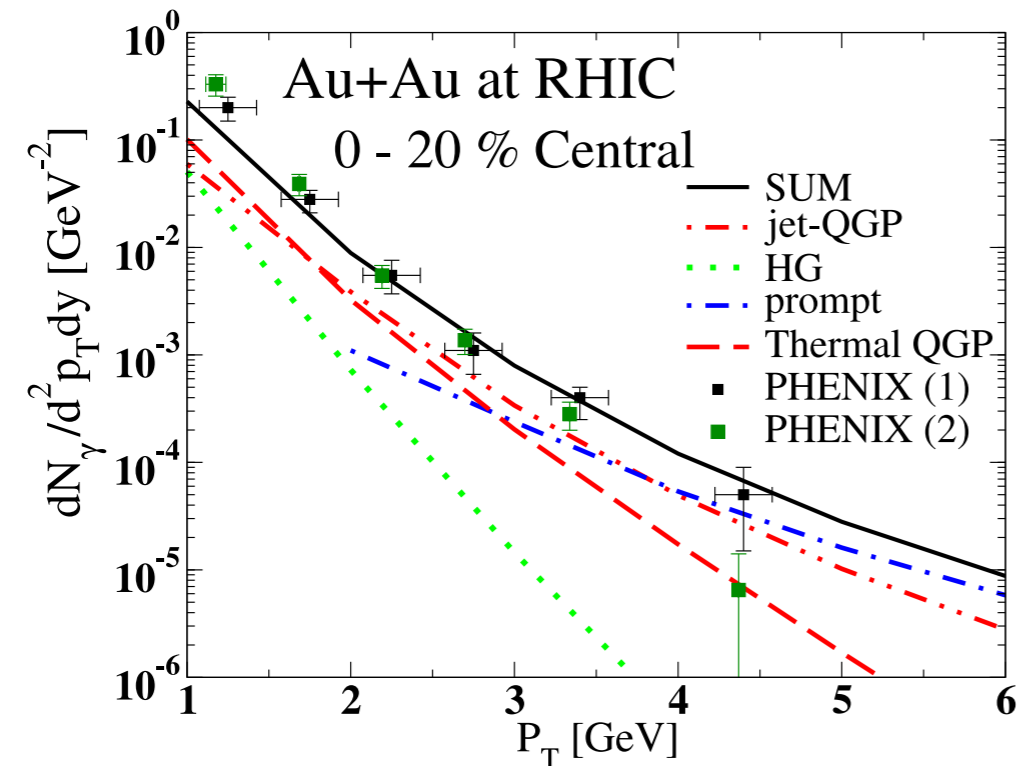
• *e.g.*  $a_1 \rightarrow \pi \rho$   $D/S$  (See also, Lichard and Vojik, Nucl. Phys. (2010); Lichard and Juran, PRD (2008))

EM emissivities computed: Turbide, Rapp, Gale, PRC (2004);  
Turbide, McGill PhD (2006)

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# APPLYING THIS TO INTERPRET PHOTONS MEASURED @ RHIC: RATES ARE INTEGRATED USING RELATIVISTIC HYDRODYNAMIC MODELING



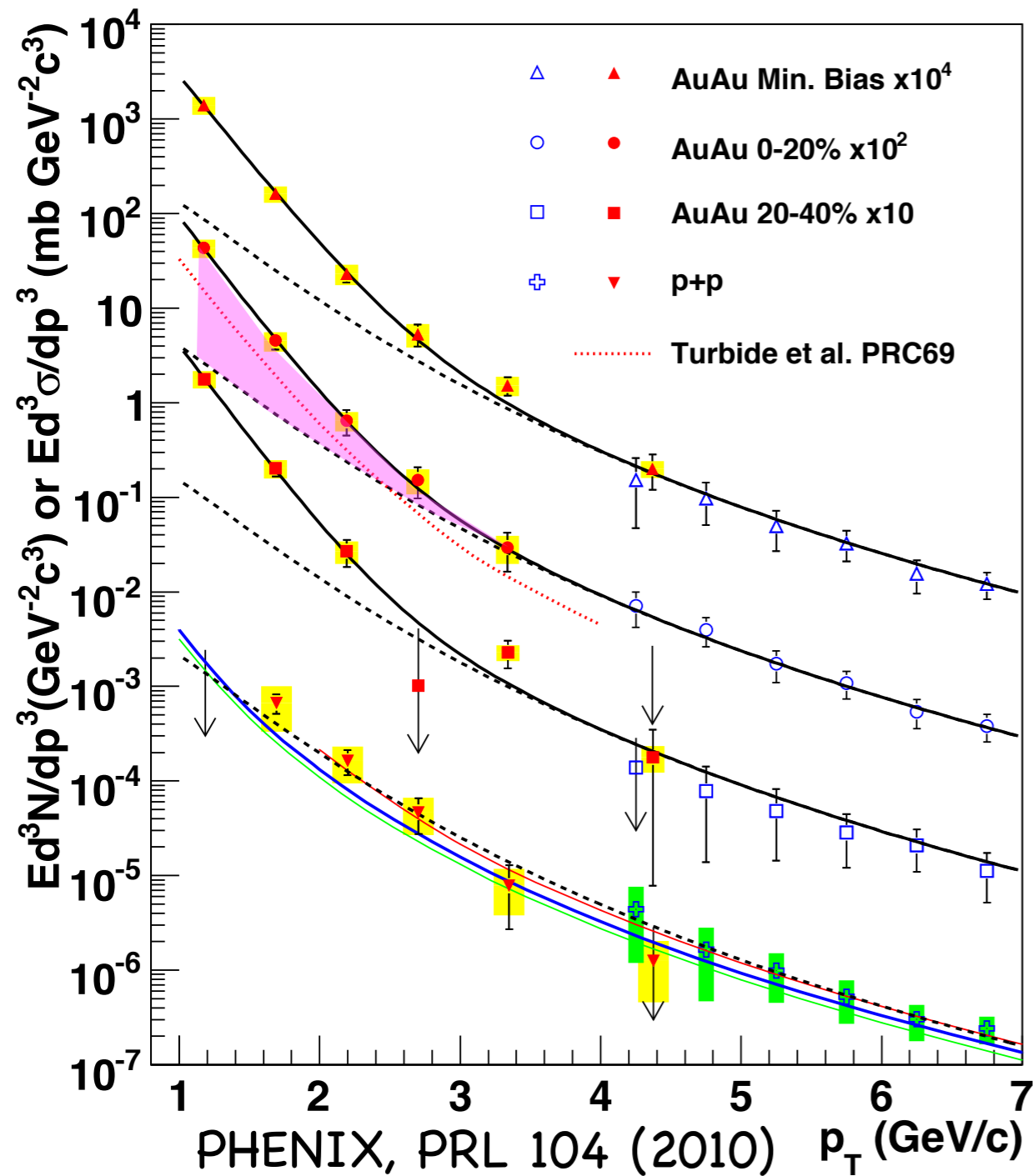
- At low  $p_T$ , spectrum dominated by thermal components (HG, QGP)
- At high  $p_T$ , spectrum dominated by pQCD
- Window for jet-QGP contributions at mid- $p_T$ ?

Turbide, Gale, Frodermann, Heinz, PRC (2008);  
Higher  $p_T$ : G. Qin et al., PRC (2009)

10

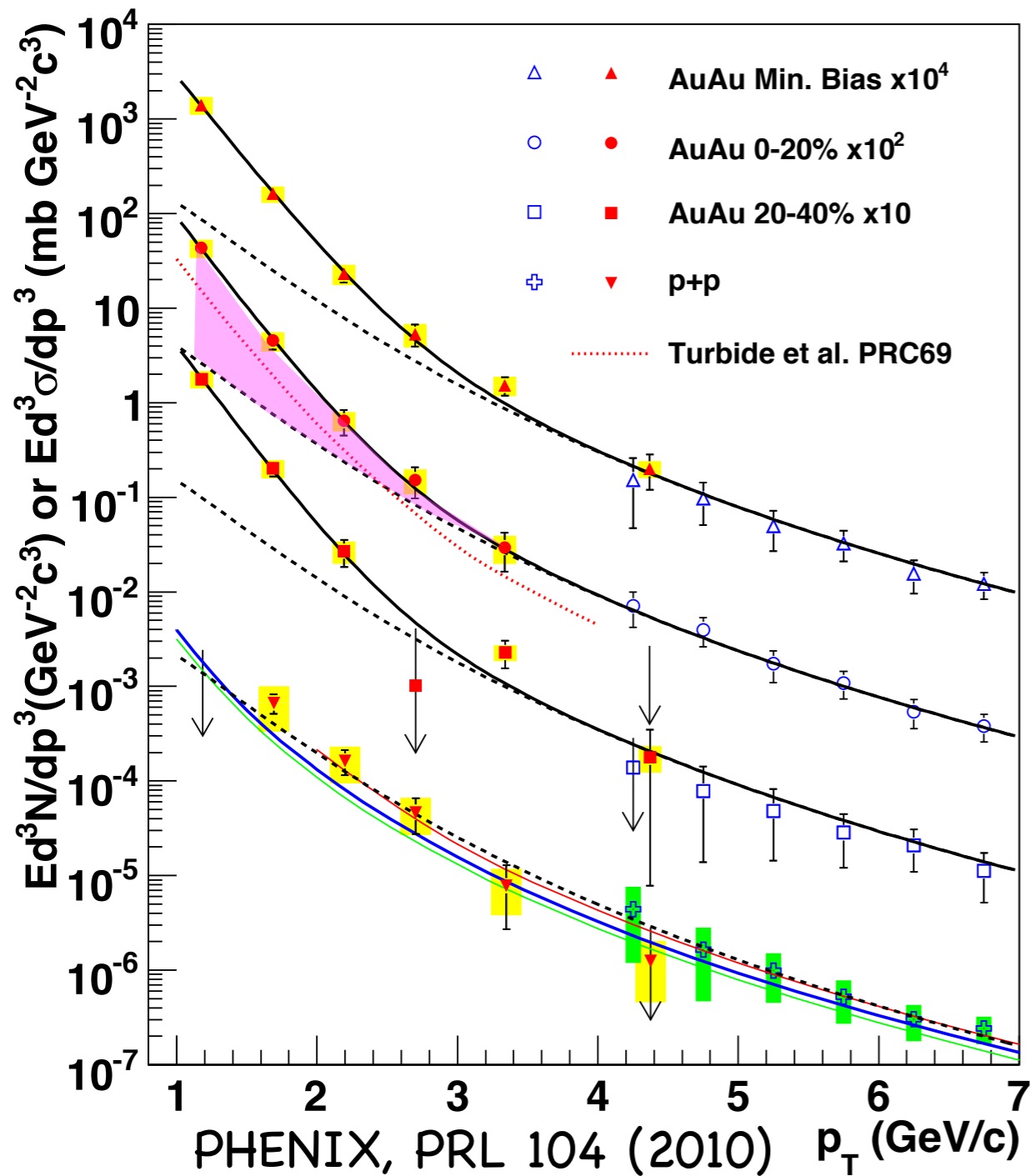


# ONE OF THE USES OF PHOTONS: CHARACTERIZING THE HOT MATTER CREATED AT RHIC



$$T_{\text{excess}} = 221 \pm 19 \pm 19 \text{ MeV}$$

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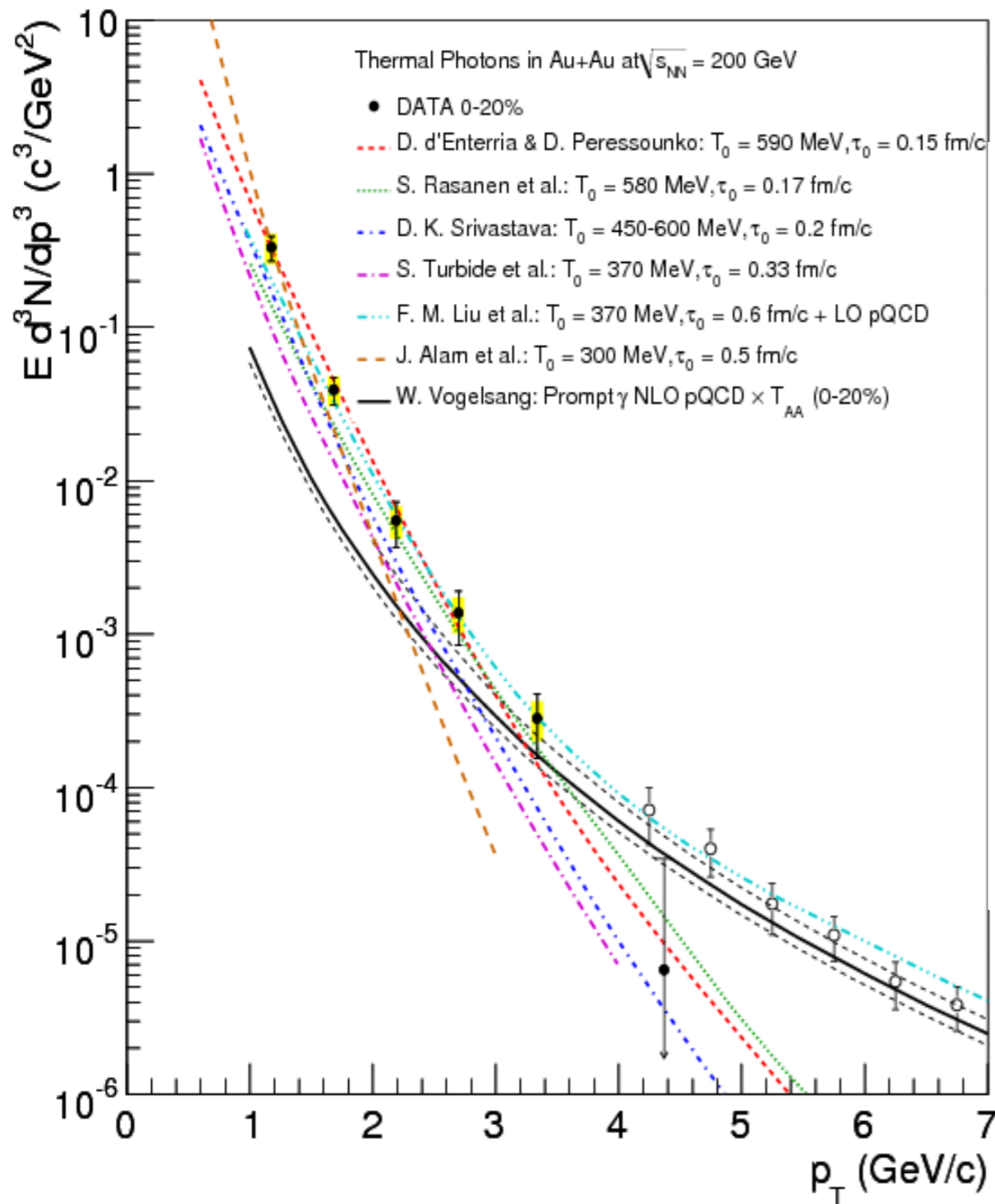
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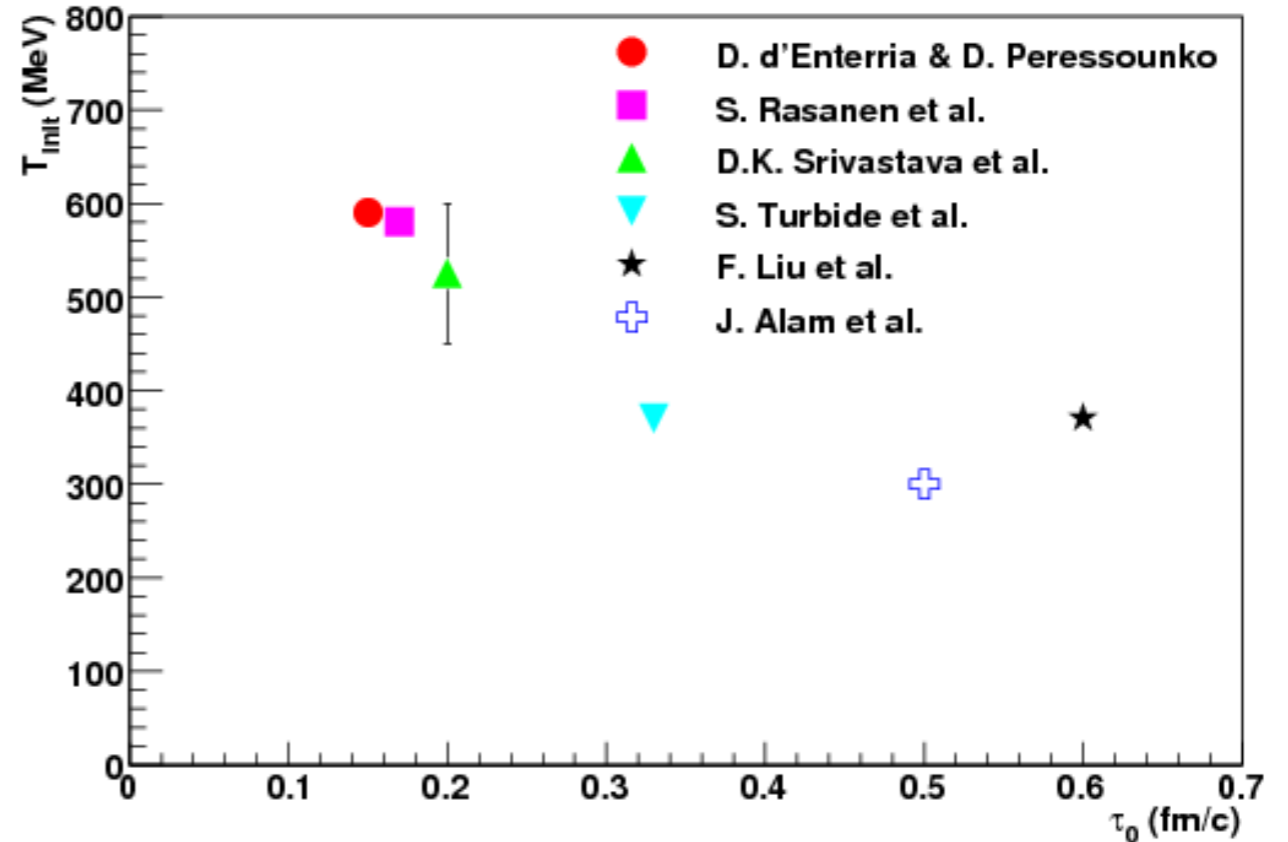
Flow effects will be important

- van Hees, Gale Rapp, PRC (2011)
- Shen, Heinz, Paquet, Gale, arXiv:1308.2440

# ONE OF THE USES OF PHOTONS: CHARACTERIZING THE HOT MATTER CREATED AT RHIC



$$T_{\text{excess}} = 221 \pm 19 \pm 19 \text{ MeV}$$



$T_{\text{ini}} = 300 \text{ to } 600 \text{ MeV}$   
 $t_0 = 0.15 \text{ to } 0.5 \text{ fm/c}$

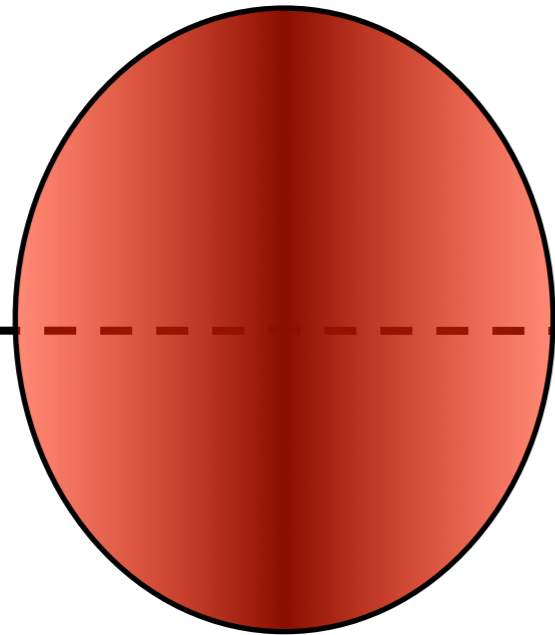
D'Enterria & Peressounko, Eur. Phys. J. (2006)

Knowing rates alone is not enough to guarantee predictive power or even characterization ability

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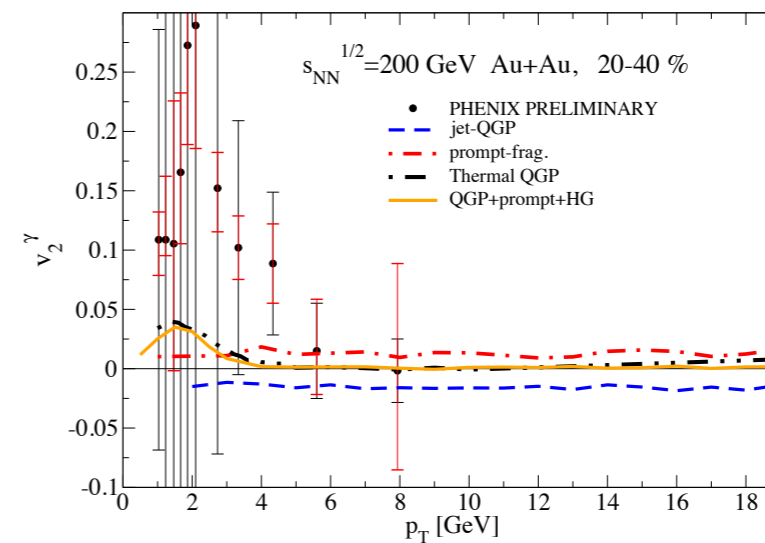


# BEYOND SIMPLE SPECTRA: FLOW AND CORRELATIONS



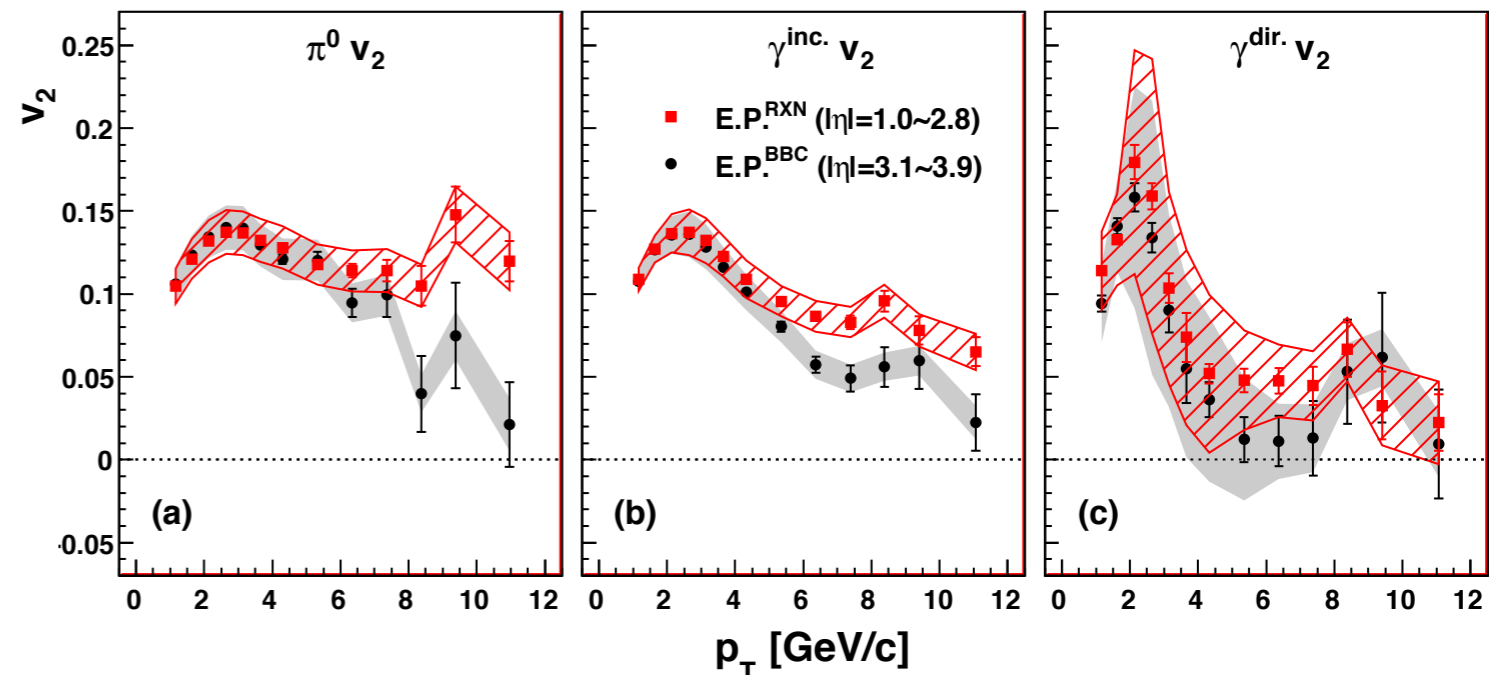
$$\frac{dN}{p_T dp_T d\phi} = \frac{dN}{2\pi p_T dp_T} \left[ 1 + \sum_n 2v_n \cos(n\phi) \right]$$

- Soft photons will go with the flow
- Jet-plasma photons: a negative  $v_2$
- Details will matter: flow,  $T(t)$ ...



(2008)

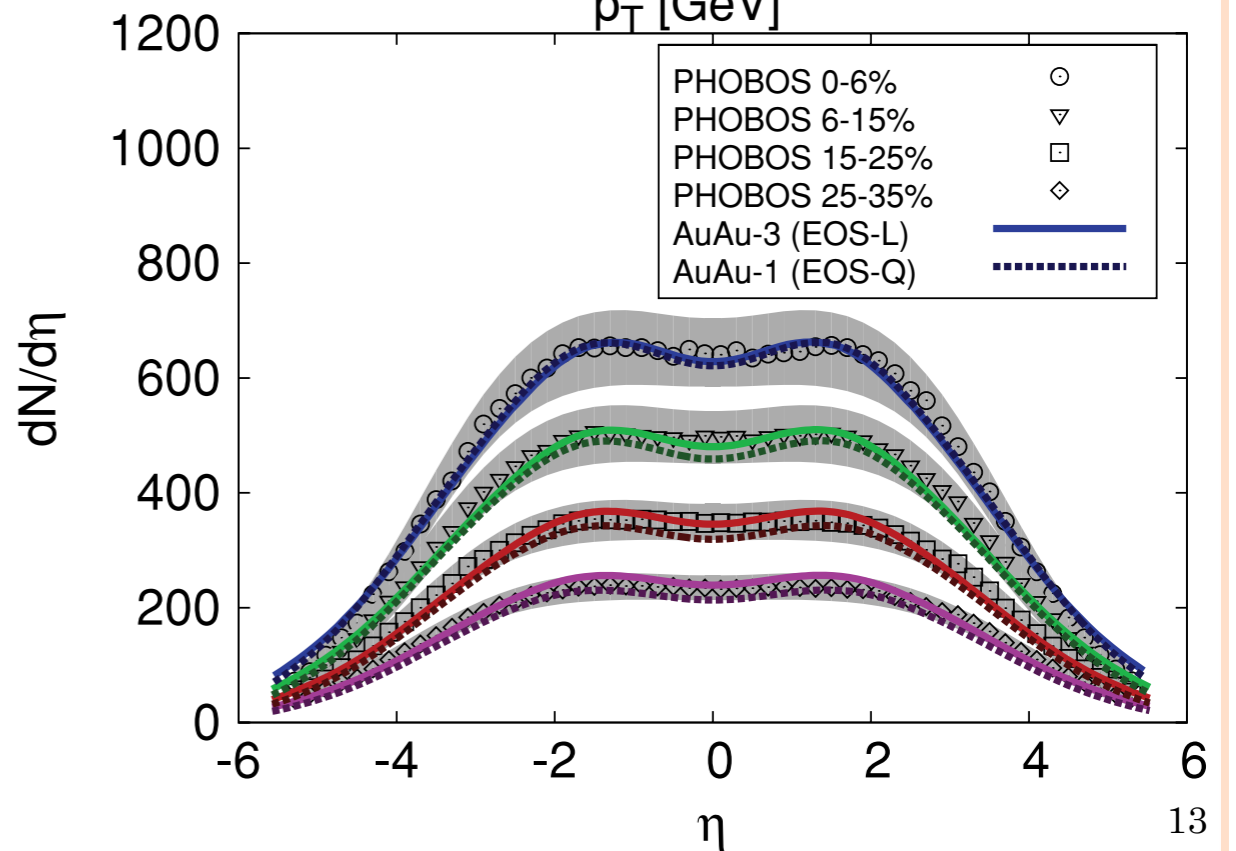
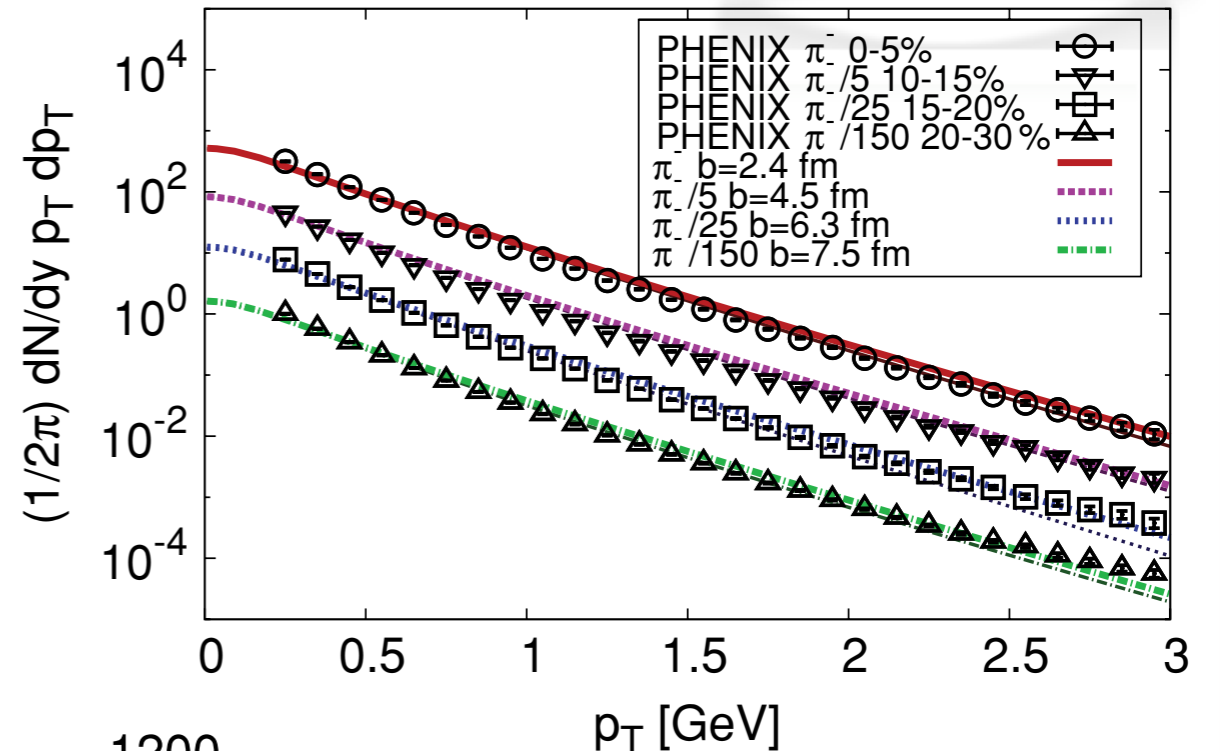
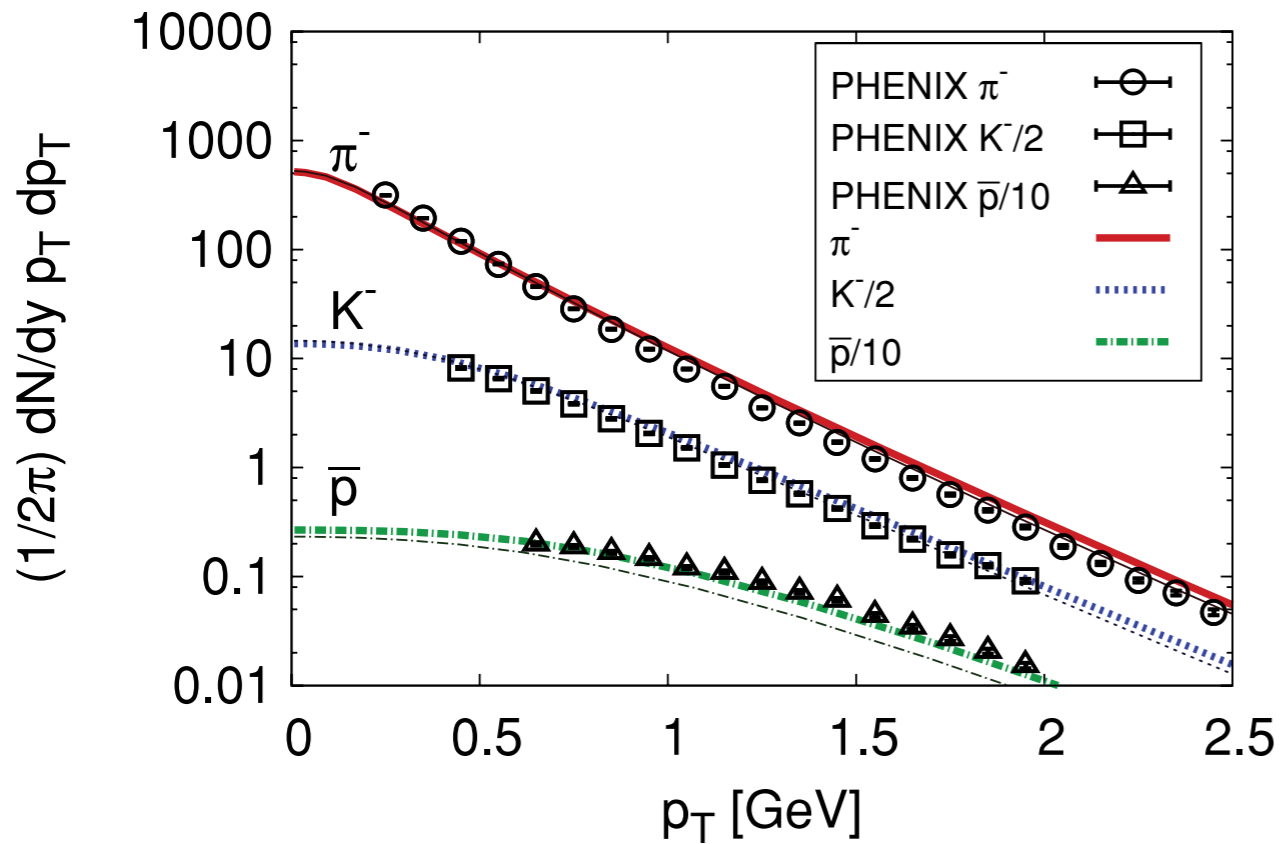
Turbide, Gale, Fries PRL (2006)  
 Low  $p_T$ : Chatterjee *et al.*, PRL (2006)  
 All  $p_T$ : Turbide *et al.*, PRC (2008)



(2011)



# PROGRESS IN CHARACTERIZATION TOOL: 3D VISCOUS RELATIVISTIC HYDRODYNAMICS



## MUSIC: 3D relativistic hydro

- Ideal: Schenke, Jeon, and Gale, PRC (2010)
- FIC and Viscous: Schenke, Jeon, Gale, PRL (2011)

Viscosity effects on EM observables?

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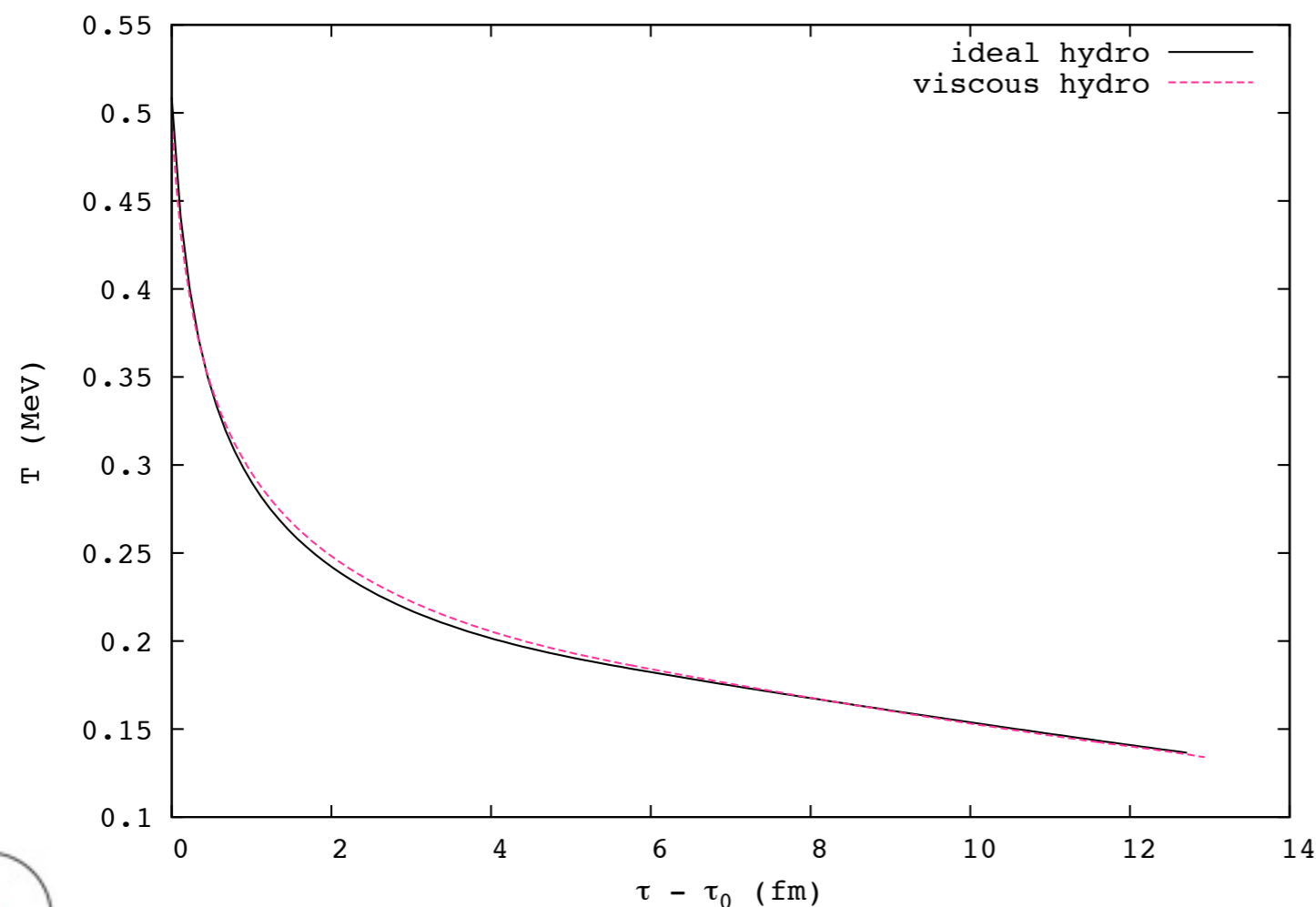
# THE EFFECTS OF SHEAR VISCOSITY ON BULK DYNAMICS

$$T_{\text{ideal}}^{\mu\nu} = (\varepsilon + P)u^\mu u^\nu - Pg^{\mu\nu}$$

$$T^{\mu\nu} = T_{\text{ideal}}^{\mu\nu} + \pi^{\mu\nu}$$

Israël & Stewart, Ann. Phys. (1979), Baier et al., JHEP (2008), Luzum and Romatschke, PRC (2008)

$$\partial_\mu (su^\mu) \propto \eta$$



- Viscous evolution starts with a lower T
- T drop is slower than ideal case

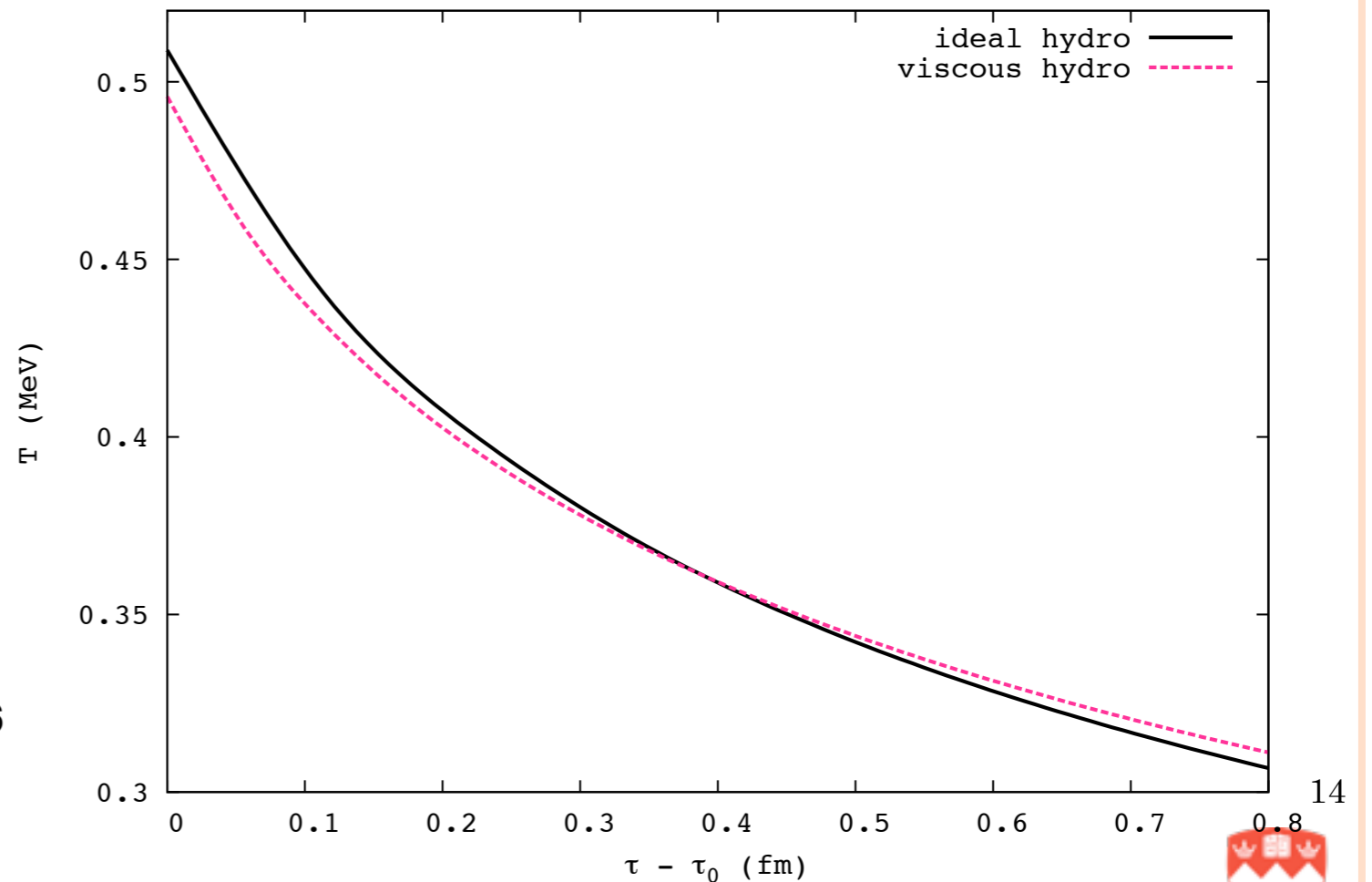
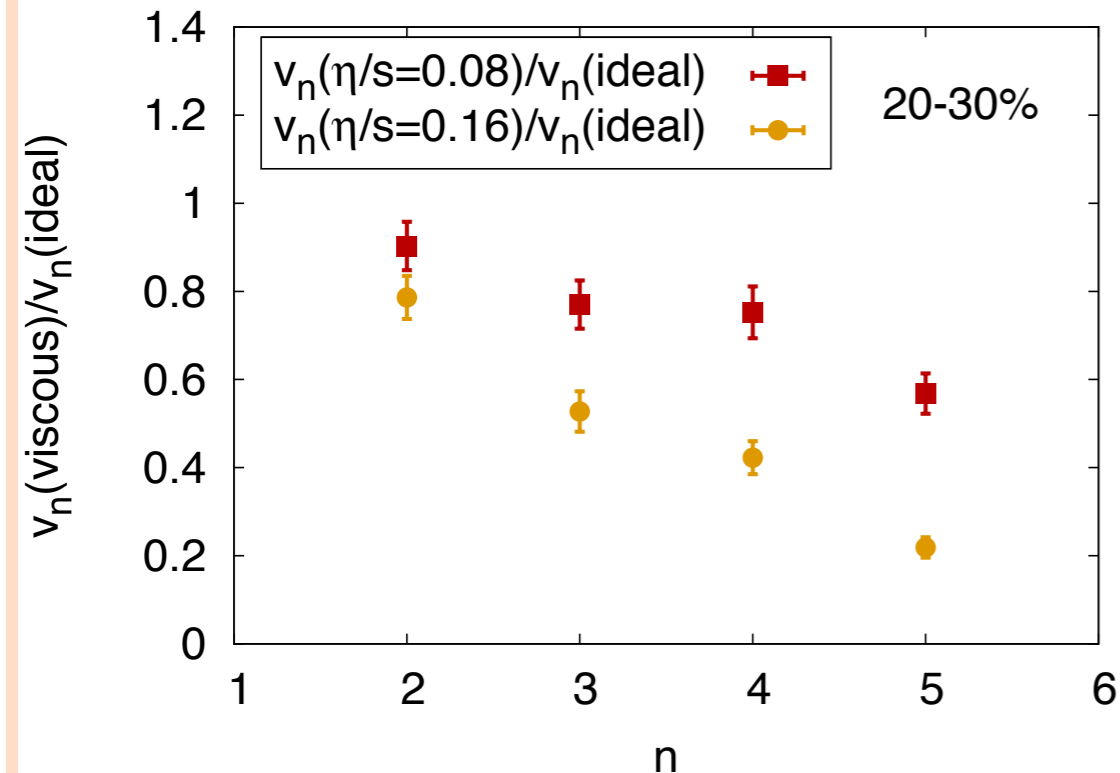
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$$\partial_\mu (su^\mu) \propto \eta$$



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# THE EFFECTS OF SHEAR VISCOSITY ON THE PHOTON DISTRIBUTION

In-medium **hadrons**:

$$f_0(u^\mu p_\mu) = \frac{1}{(2\pi)^3} \frac{1}{\exp[(u^\mu p_\mu - \mu)/T] \pm 1}$$

$$f \rightarrow f_0 + \delta f, \quad \delta f = f_0 (1 \pm (2\pi)^3 f_0) p^\alpha p^\beta \pi_{\alpha\beta} \frac{1}{2(\varepsilon + P)T^2}$$

$$q_0 \frac{d^3 R}{d^3 q} = \int \frac{d^3 p_1}{2(2\pi)^3 E_1} \frac{d^3 p_2}{2(2\pi)^3 E_2} \frac{d^3 p_3}{2(2\pi)^3 E_3} (2\pi)^4 |M|^2 \delta^4(\dots) \frac{f(E_1) f(E_2) [1 \pm f(E_3)]}{2(2\pi)^3}$$

One considers all the reaction and radiative decay channels of external state combinations of:

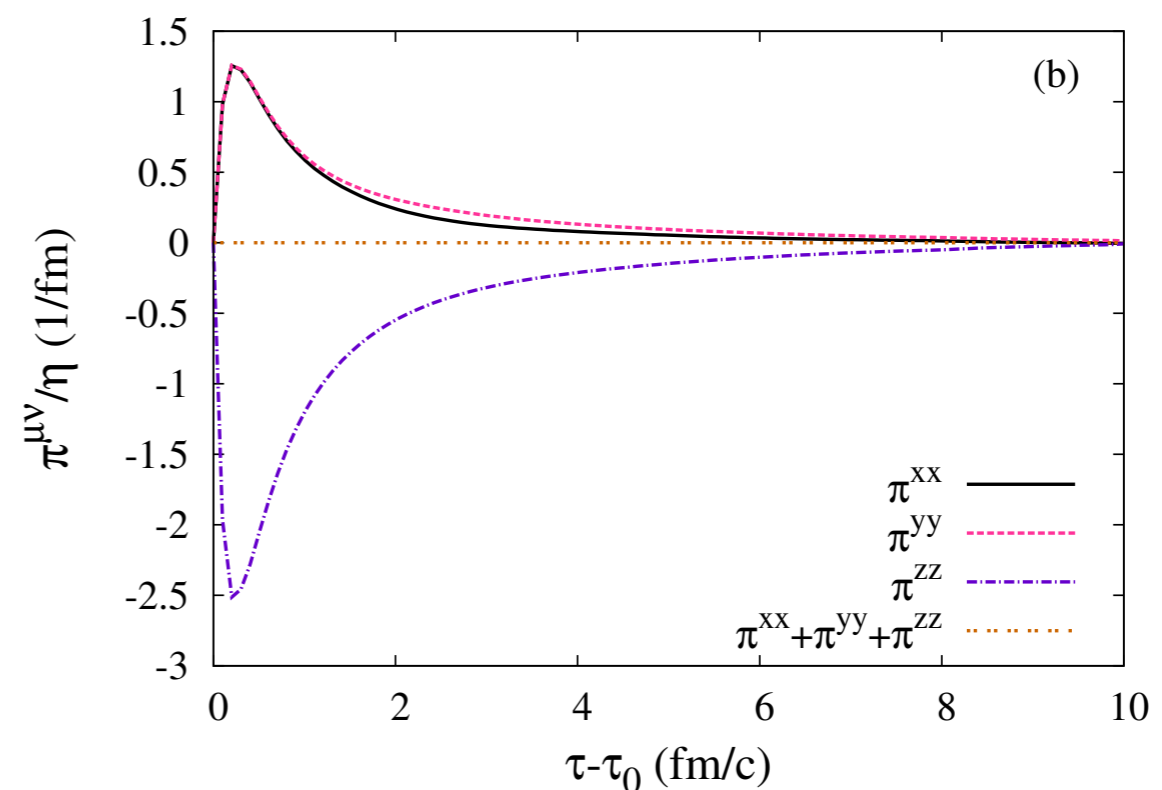
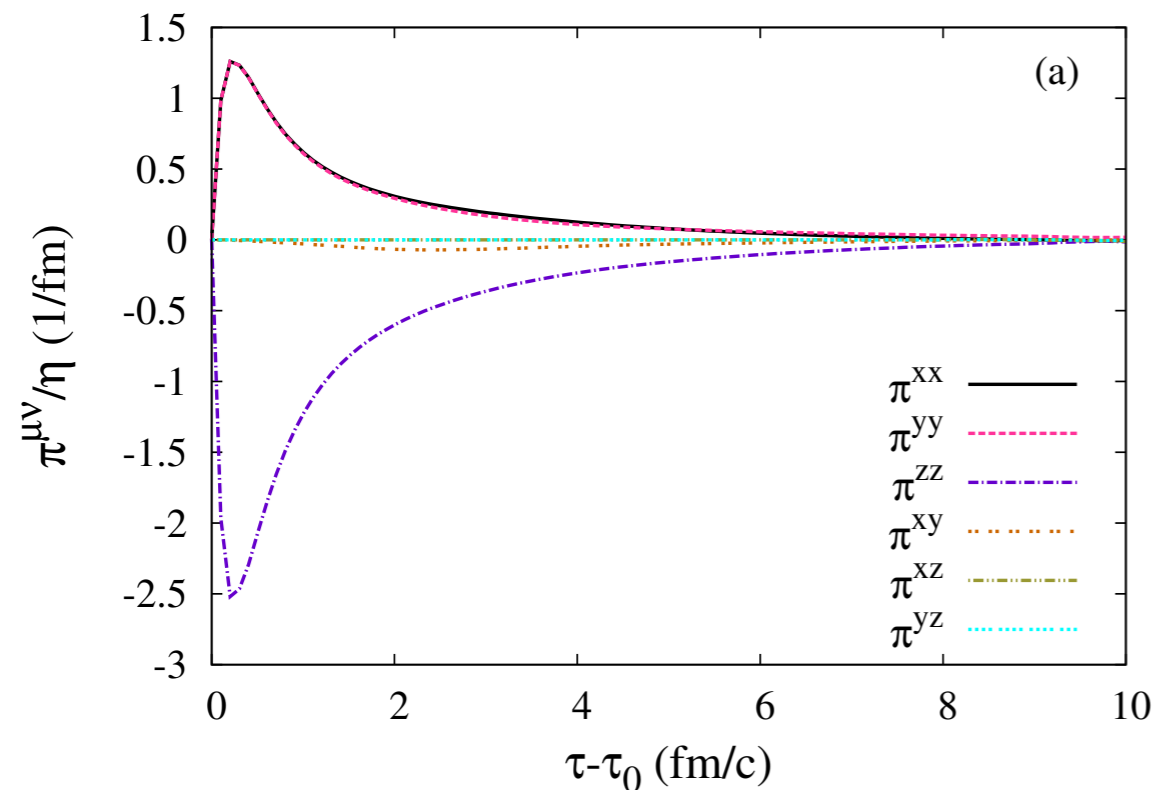
$\{\pi, K, \rho, K^*, a_1\}$

With hadronic form factors

+ QGP Photons

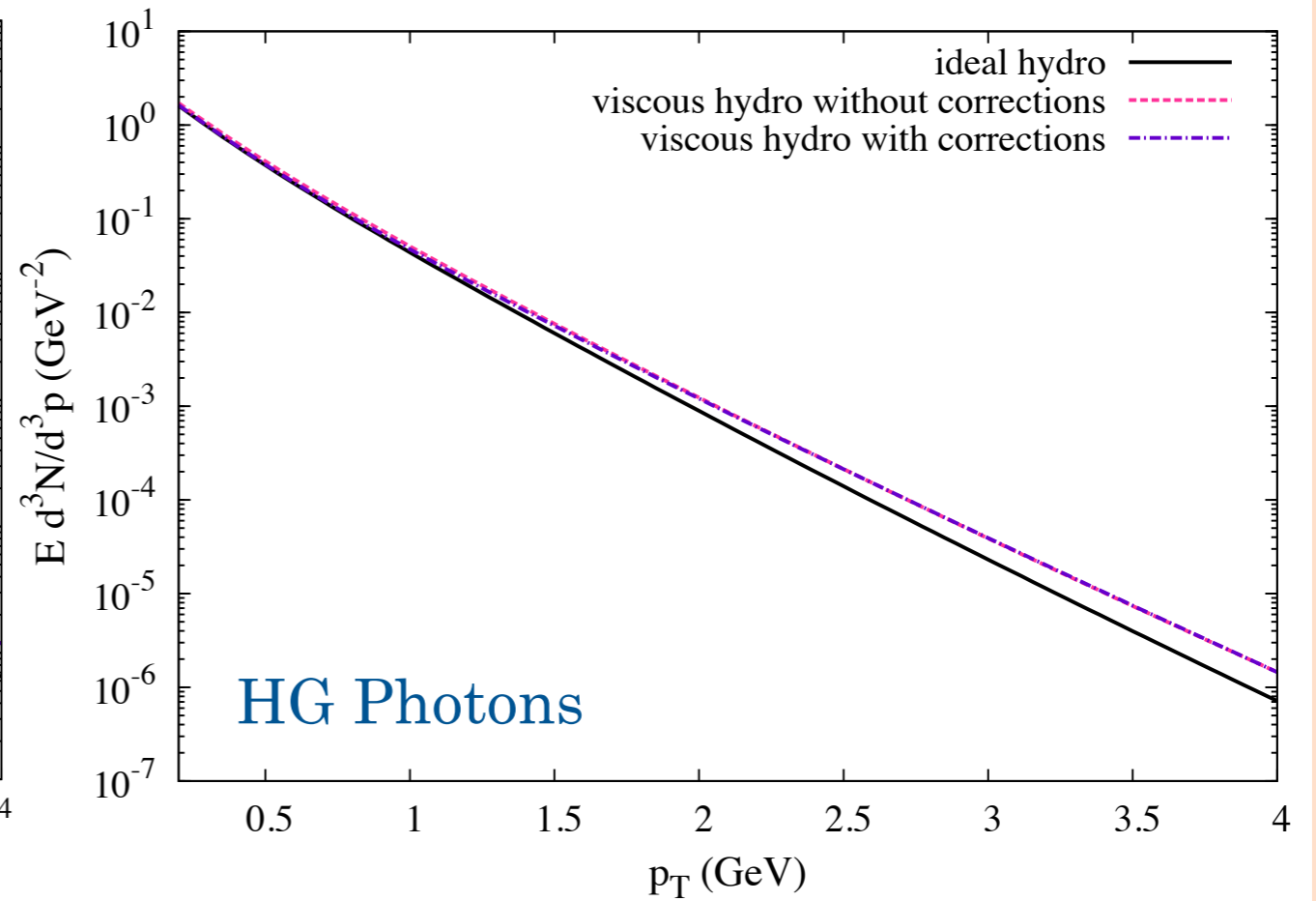
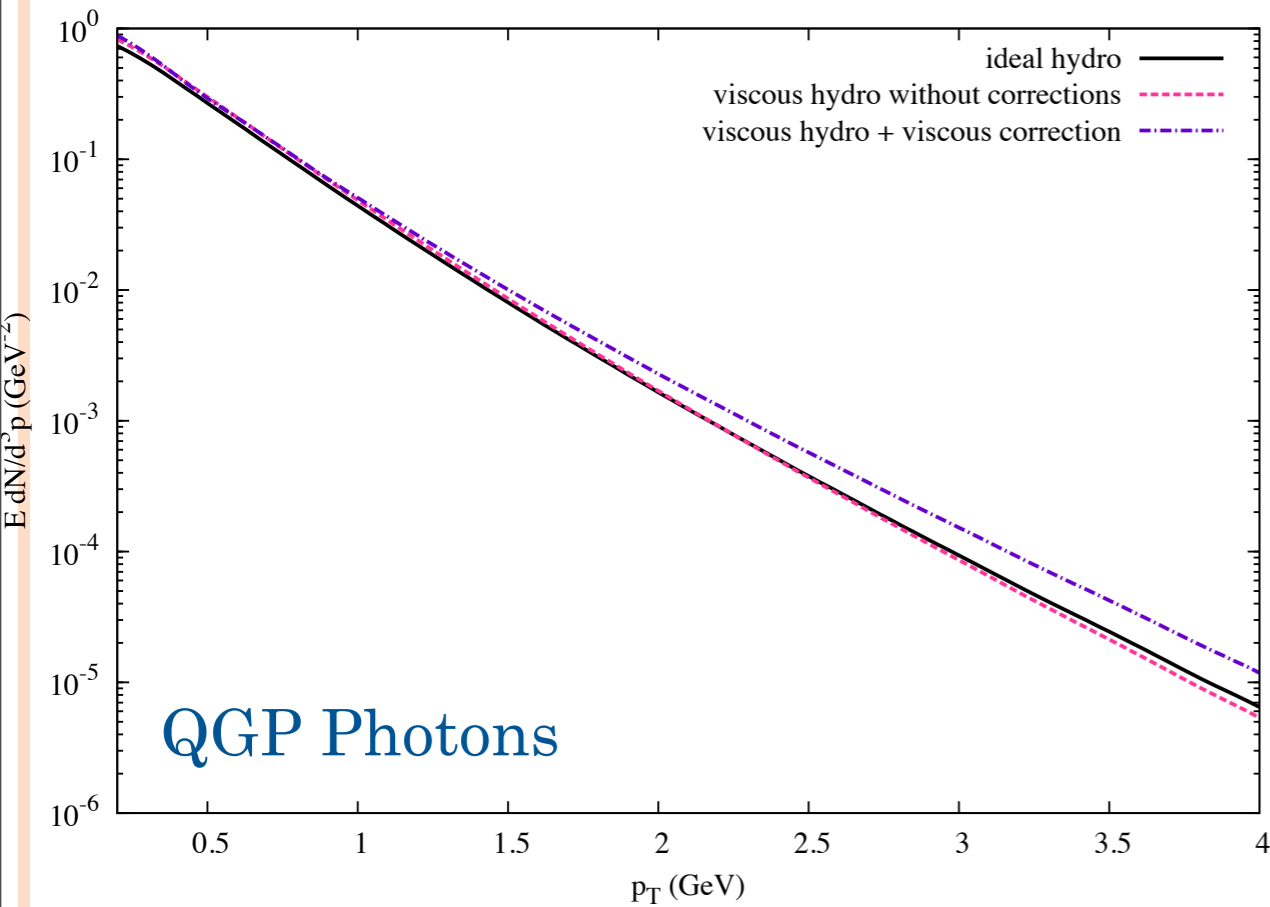


# THE EFFECTS OF SHEAR VISCOSITY ON THE BULK DYNAMICS



- Large at early times
- Small at later times: viscosity corrections to the distribution functions will also vanish

# THE EFFECTS OF SHEAR VISCOSITY ON THE PHOTON DISTRIBUTION



K. Dusling NPA (2010)  
Chaudhuri & Sinha, PRC (2011)

Viscous effects harden  
the photon spectrum

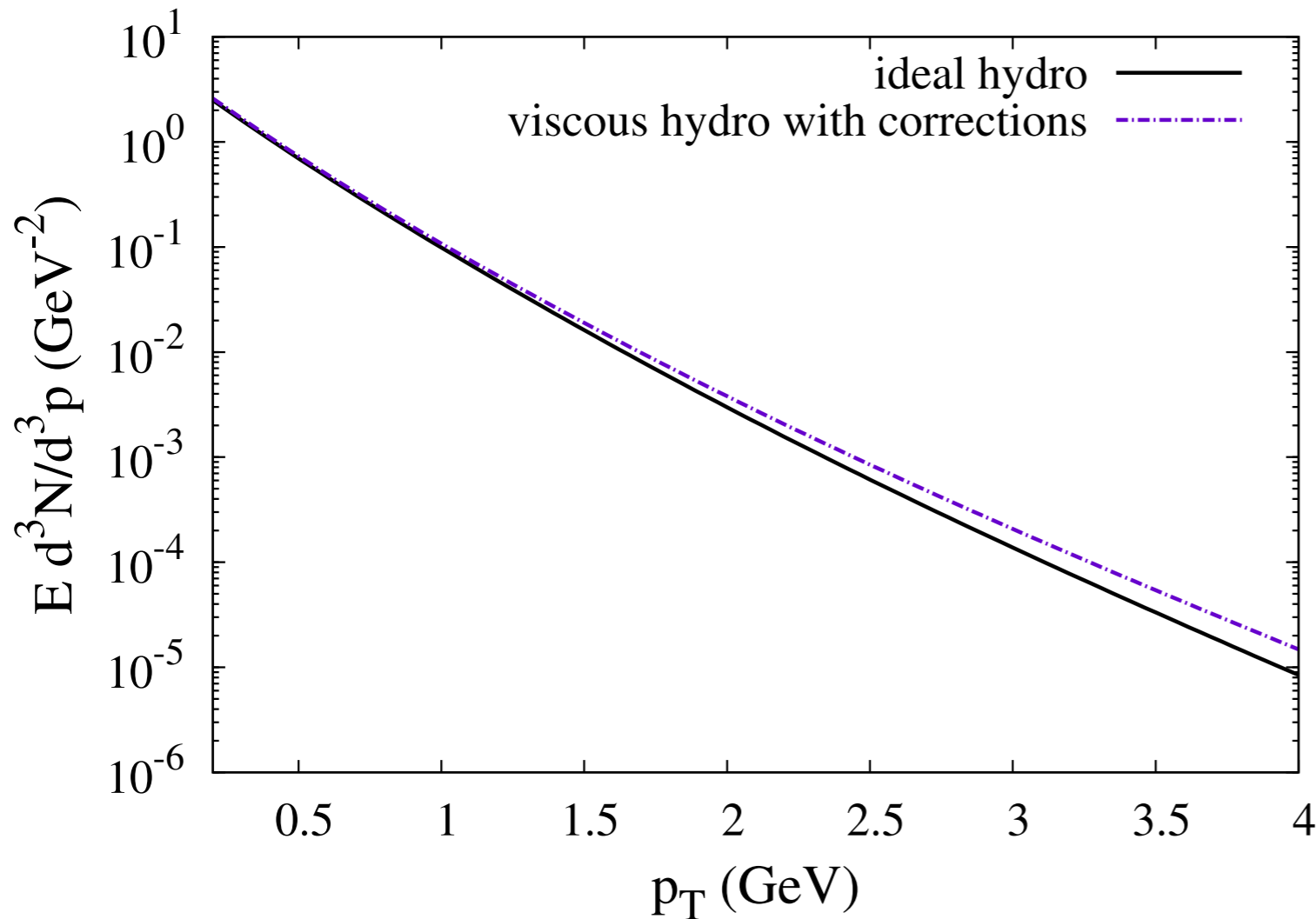
M. Dion et al., PRC (2011)



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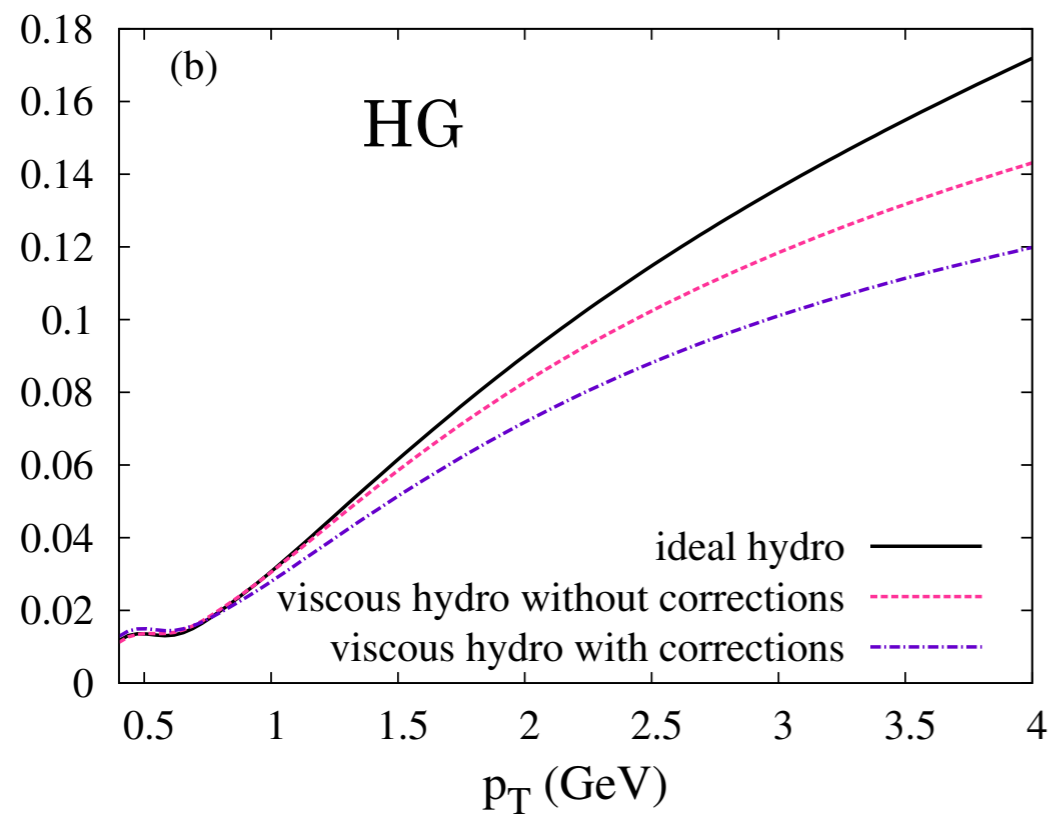
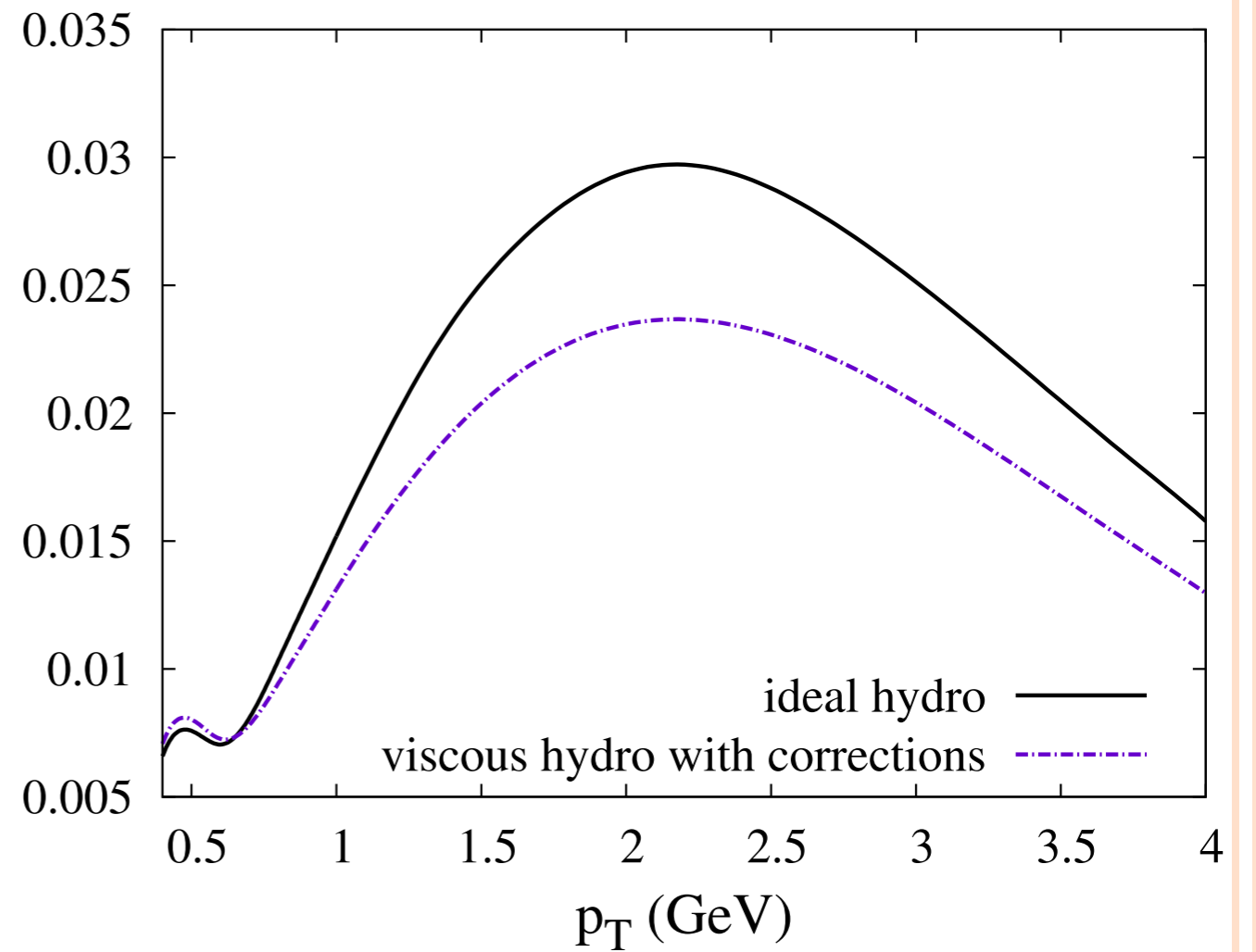
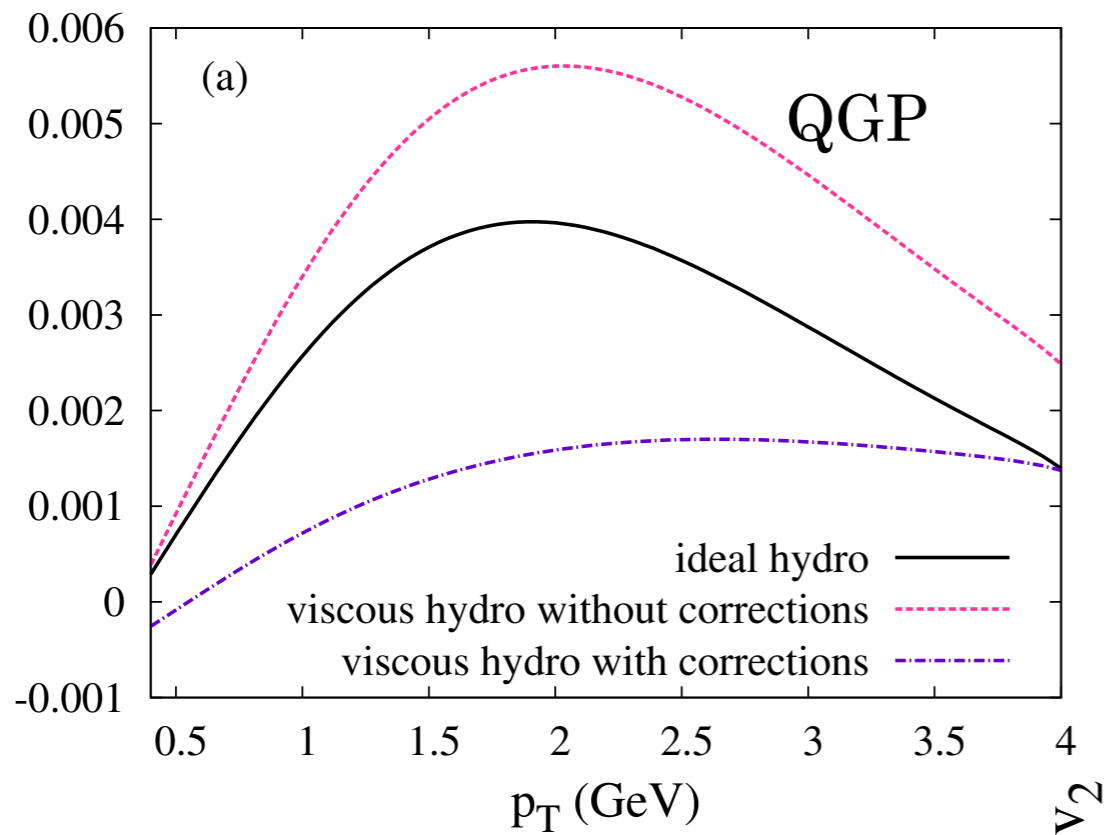


# THE NET THERMAL PHOTON YIELD

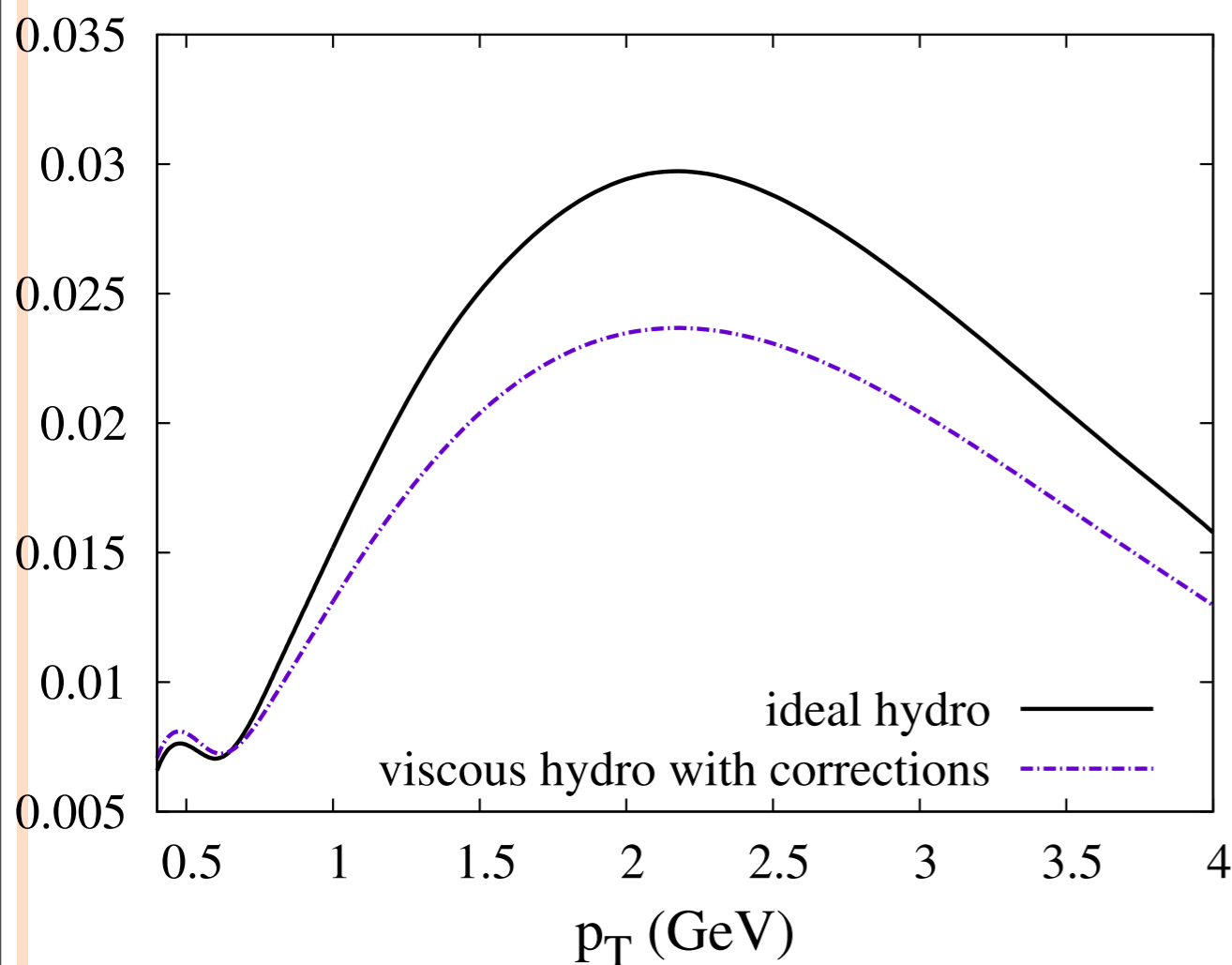


- Viscous corrections make the spectrum harder,  $\approx 100\%$  at  $p_T = 4 \text{ GeV}$ .
- Increase in the slope of  $\approx 15\%$  at  $p_T = 2 \text{ GeV}$ .
- Extracting the viscosity from the photon spectra will be challenging
- Once pQCD photons are included: a few % effect from viscosity
- More work is still needed to properly include all photon sources in a consistent way

# SHEAR VISCOSITY AND PHOTON $V_2$



# SHEAR VISCOSITY AND PHOTON $v_2$

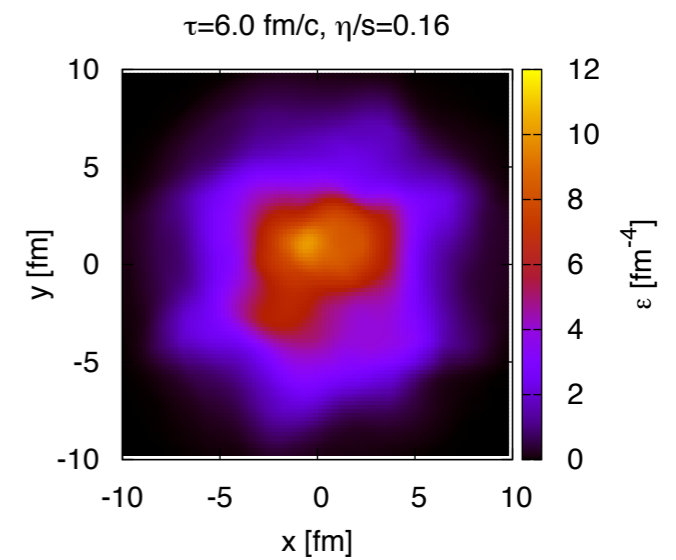
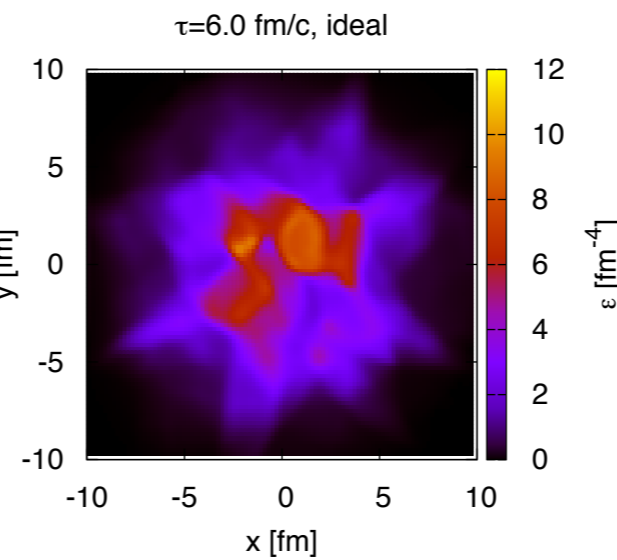
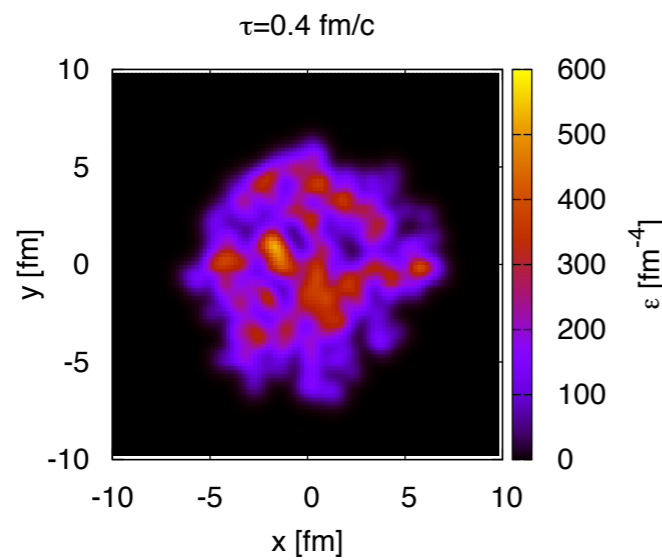
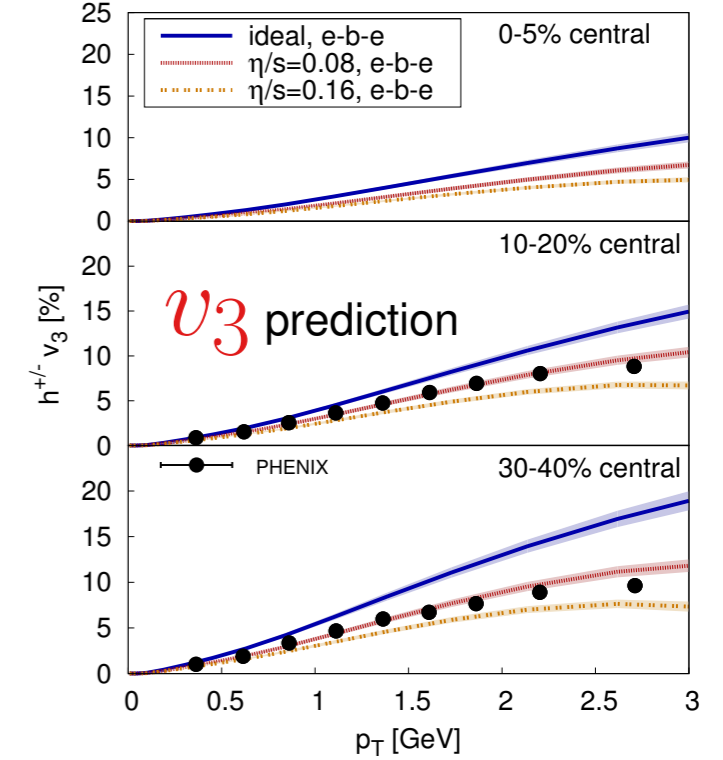
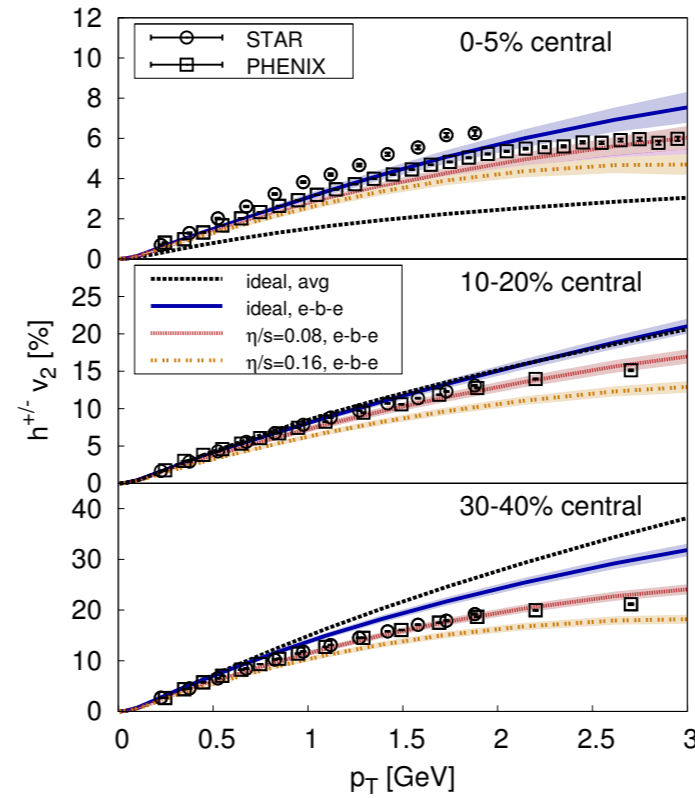
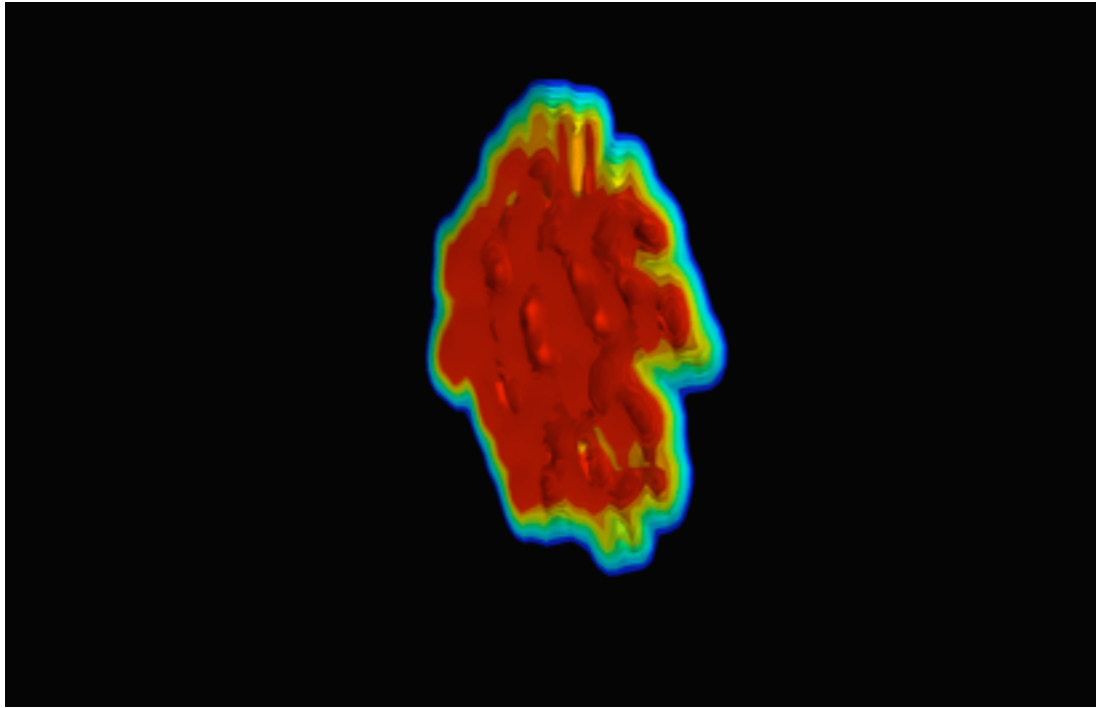


- The net elliptic flow is a *weighted average*. A larger QGP yield will yield a smaller  $v_2$ . Same story - *mutatis mutandis* - for the HG
- The turnover at  $p_T \approx 2$  GeV could be QGP-driven and/or pQCD-driven
- The net effect of viscous corrections makes the photon elliptic flow *smaller*, as it does for hadrons



# INITIAL STATE FLUCTUATIONS: A PARADIGM SHIFT IN HEAVY ION ANALYSES

Lumpy  
MUSIC



Schenke, Jeon, Gale, PRL (2011)

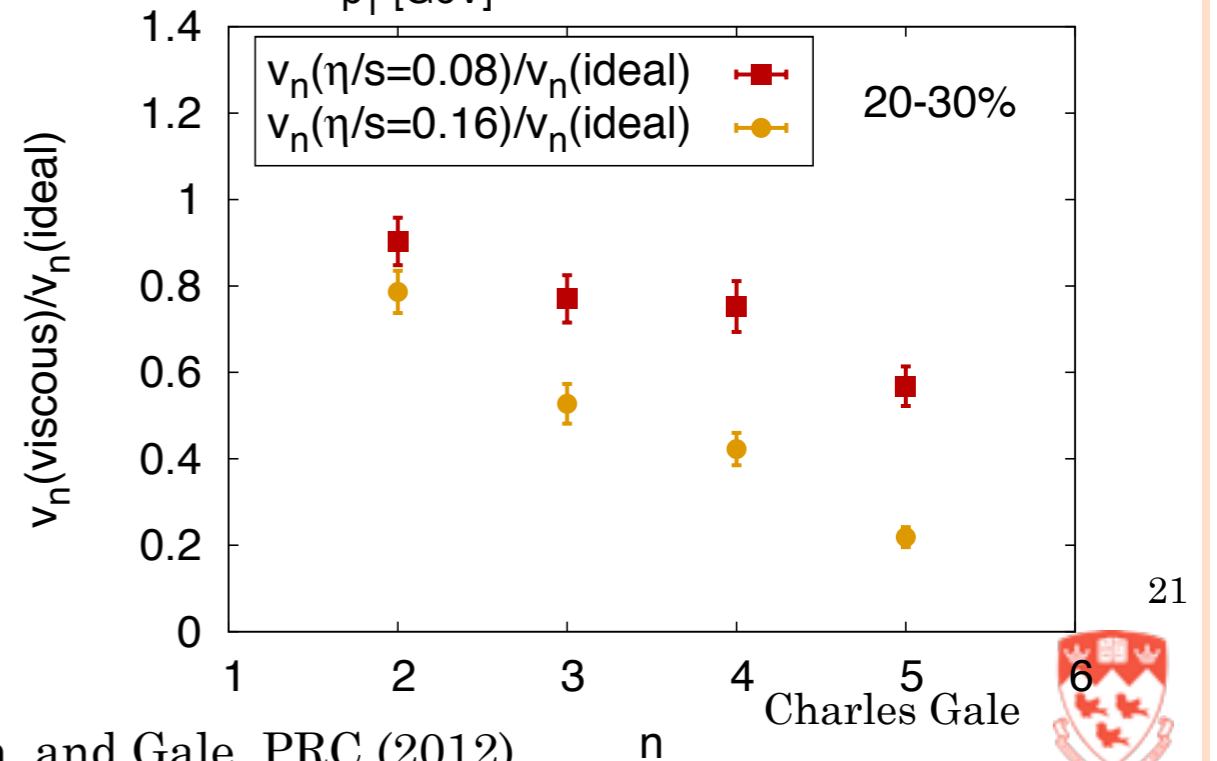
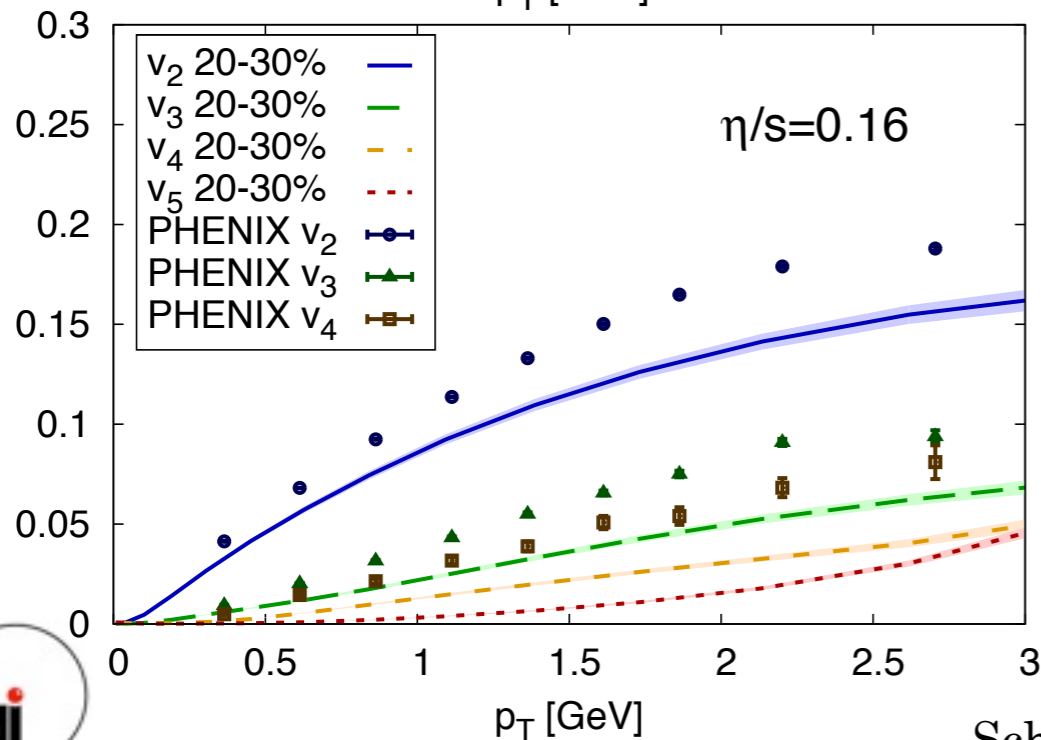
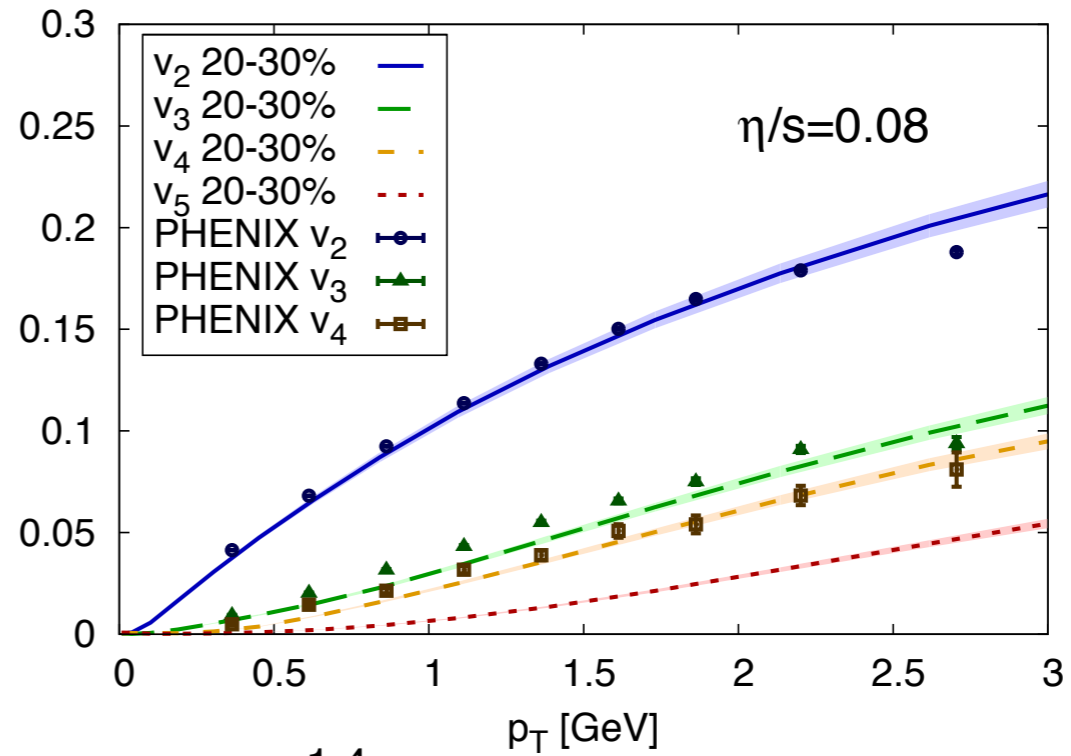
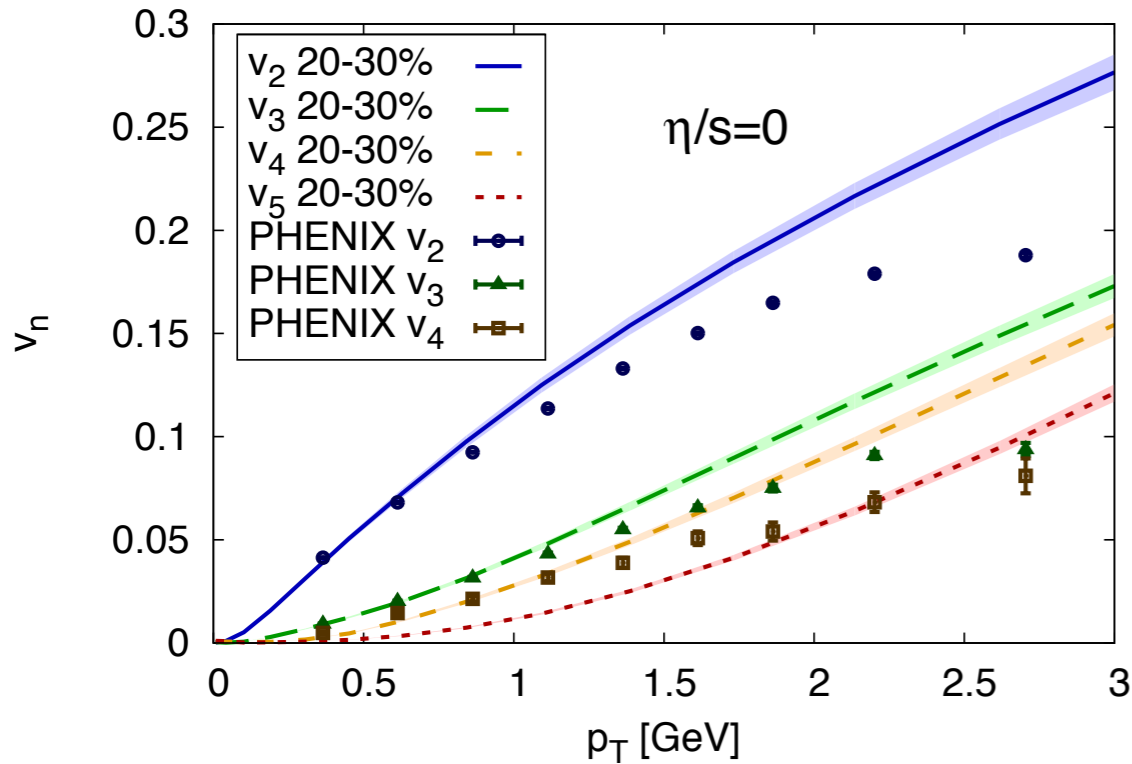
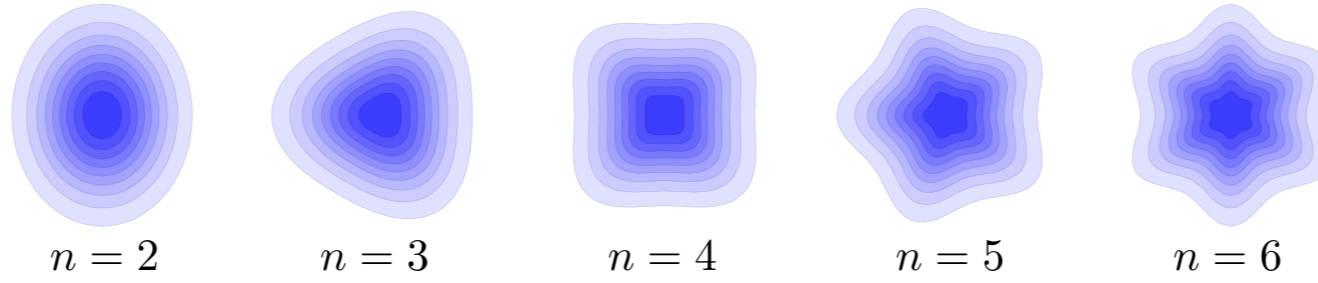
20



Charles Gale



# MOVING INTO THE "CHARACTERIZATION" PHASE...

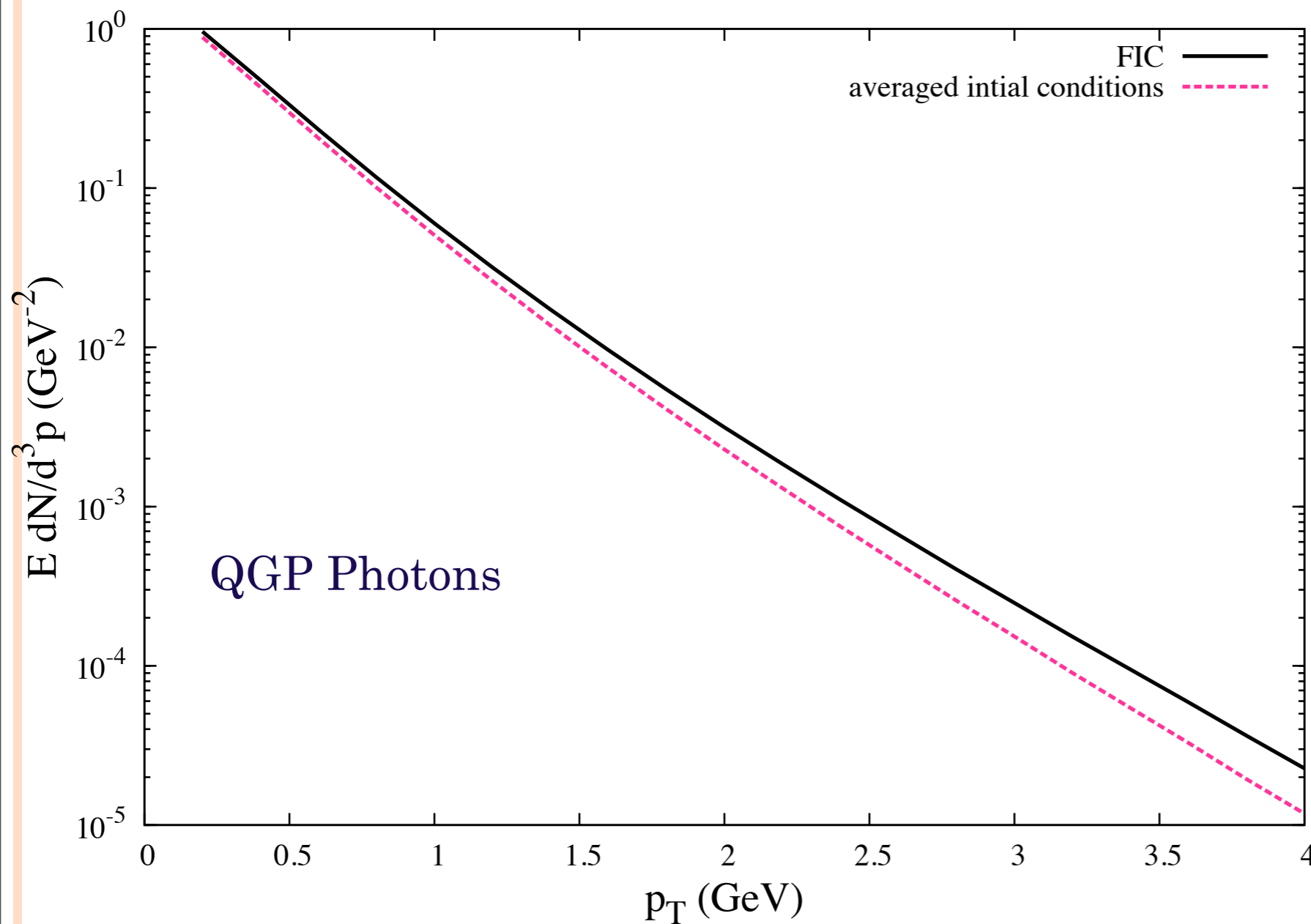


Schenke, Jeon, and Gale, PRC (2012)

Charles Gale



# THE EFFECT OF FIC ON THE THERMAL PHOTON SPECTRUM



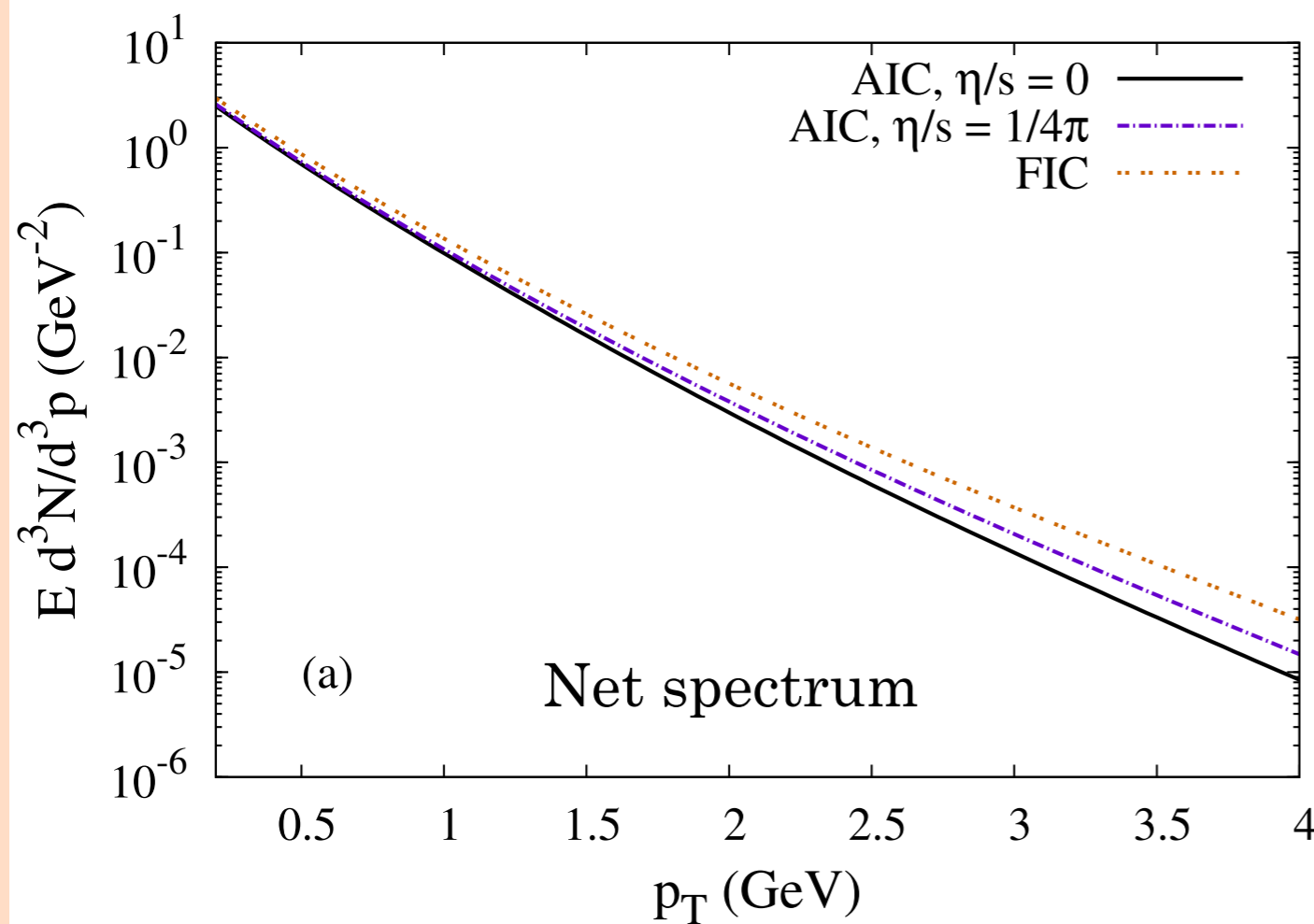
- FIC produces higher initial  $T$  (hot spots), and higher initial gradients
- FIC conditions are demanded by hadronic data ( $v_{\text{odd}}$ )
- These lead to a harder spectrum, *as for hadrons*

Dion et al., PRC (2011)  
Chatterjee et al., PRC (2011)

# ALL TOGETHER: FICs + VISCOSITY

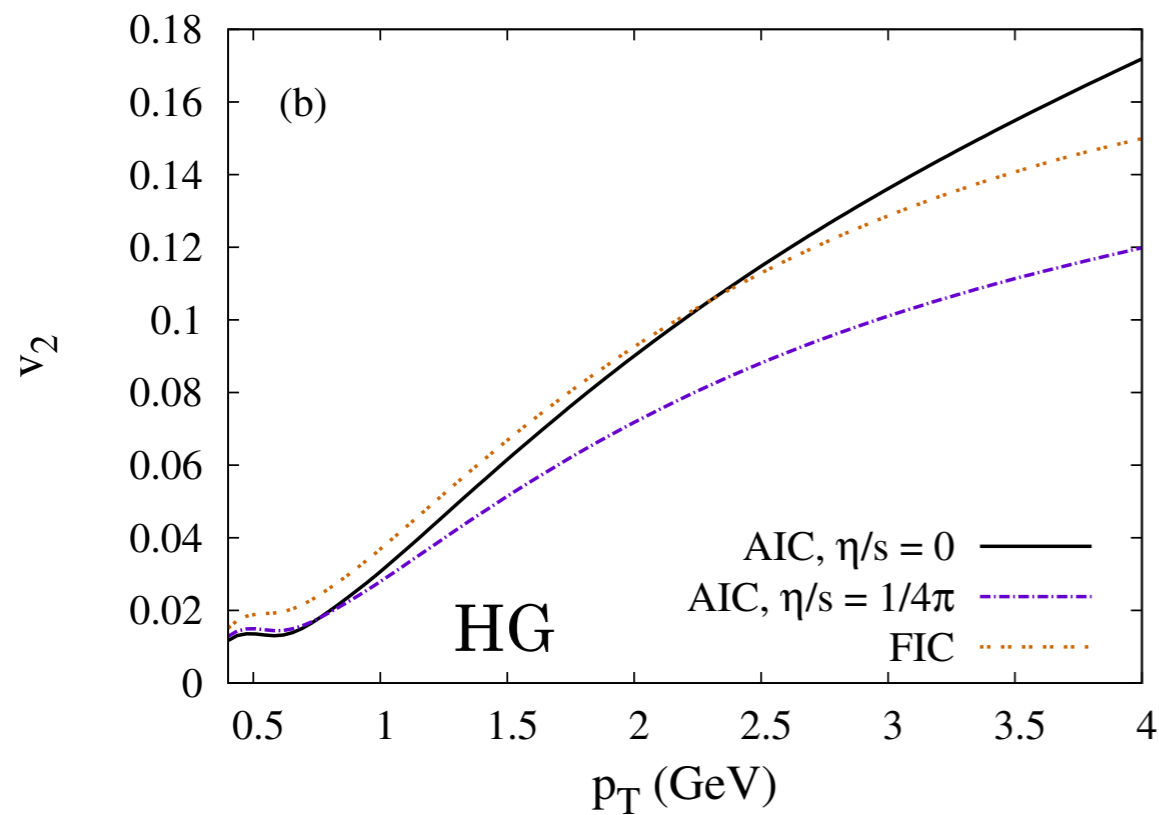
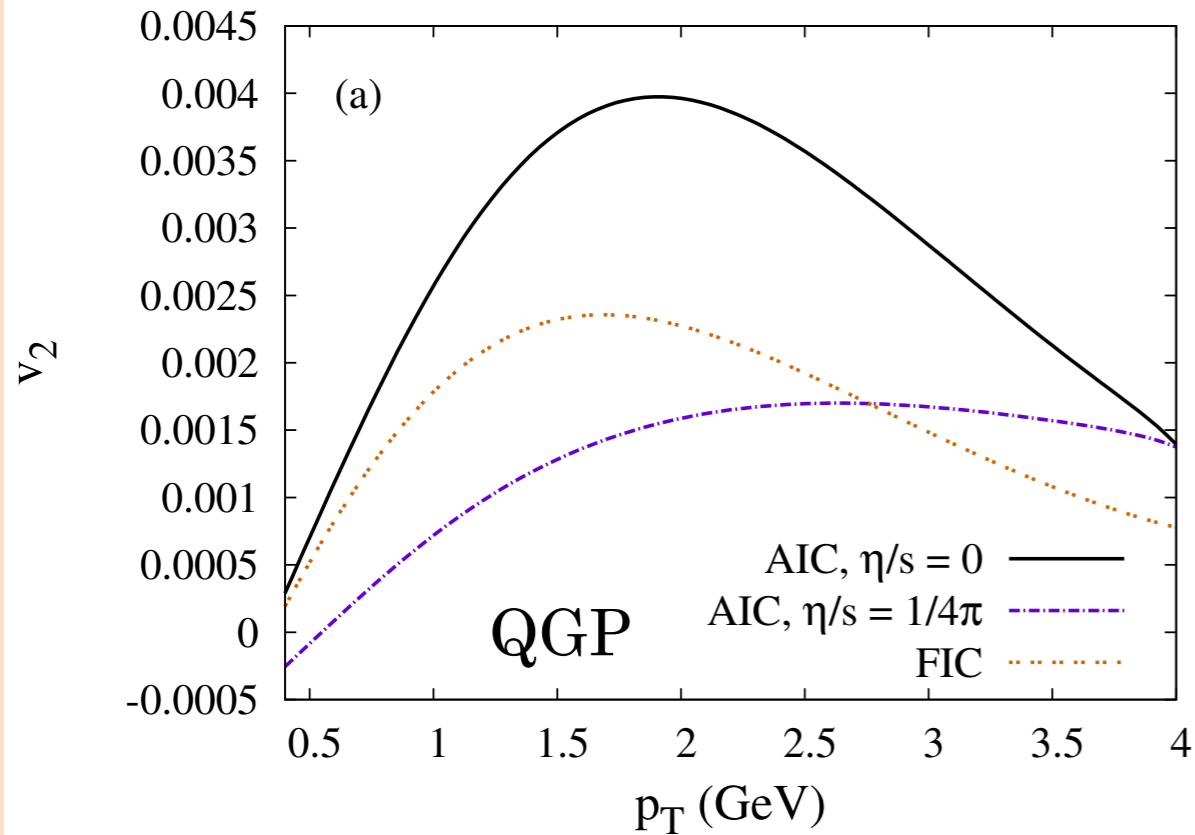
- Combined with viscous corrections, FIC yield an enhancement by  $\approx 5$  @ 4 GeV, and  $\approx 2$  @ 2 GeV
- Temperature estimated by slopes can vary considerably
- A combination of hot spots and blue shift hardens spectra
- Once pQCD photons are included: only modest changes from viscous corrections + FICs

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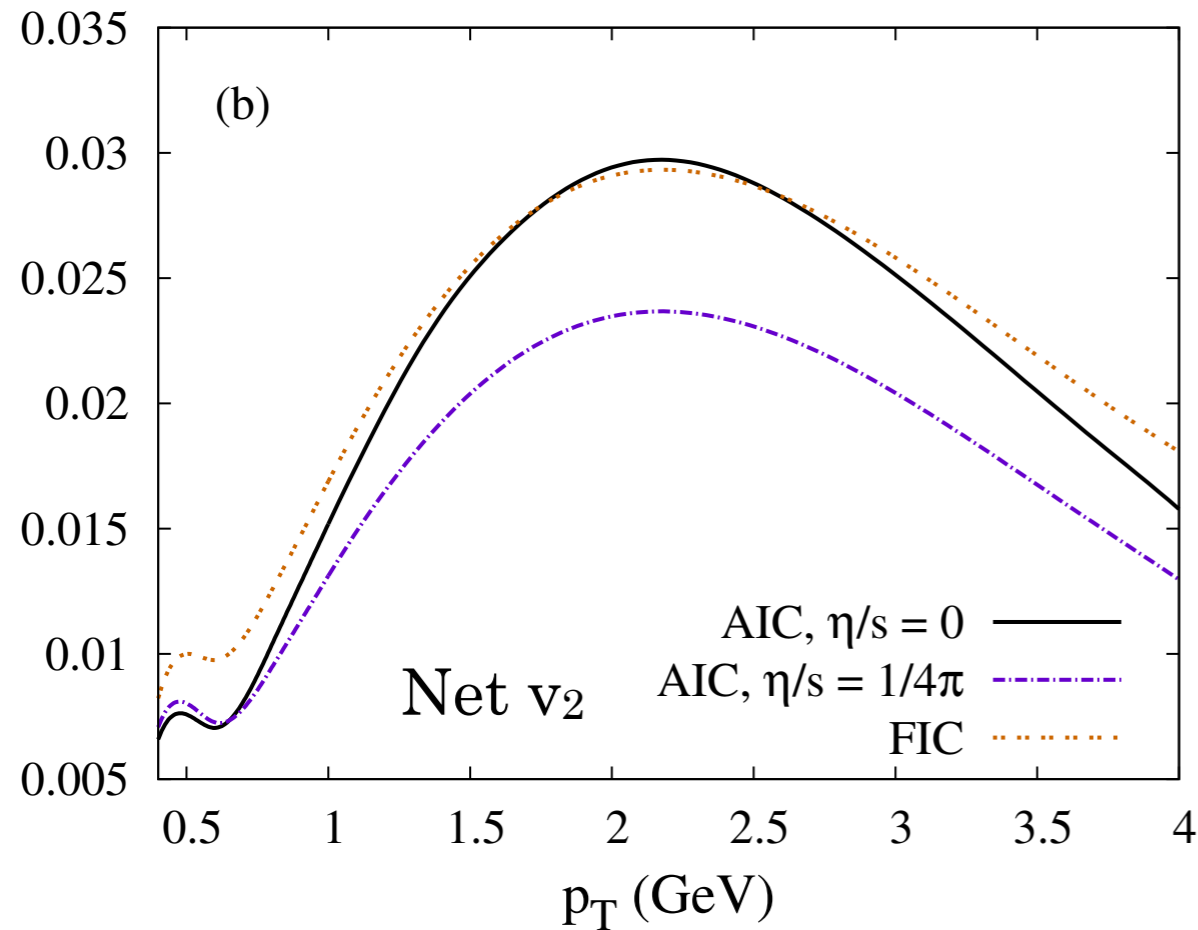
# FICs AND THERMAL PHOTON $v_2$



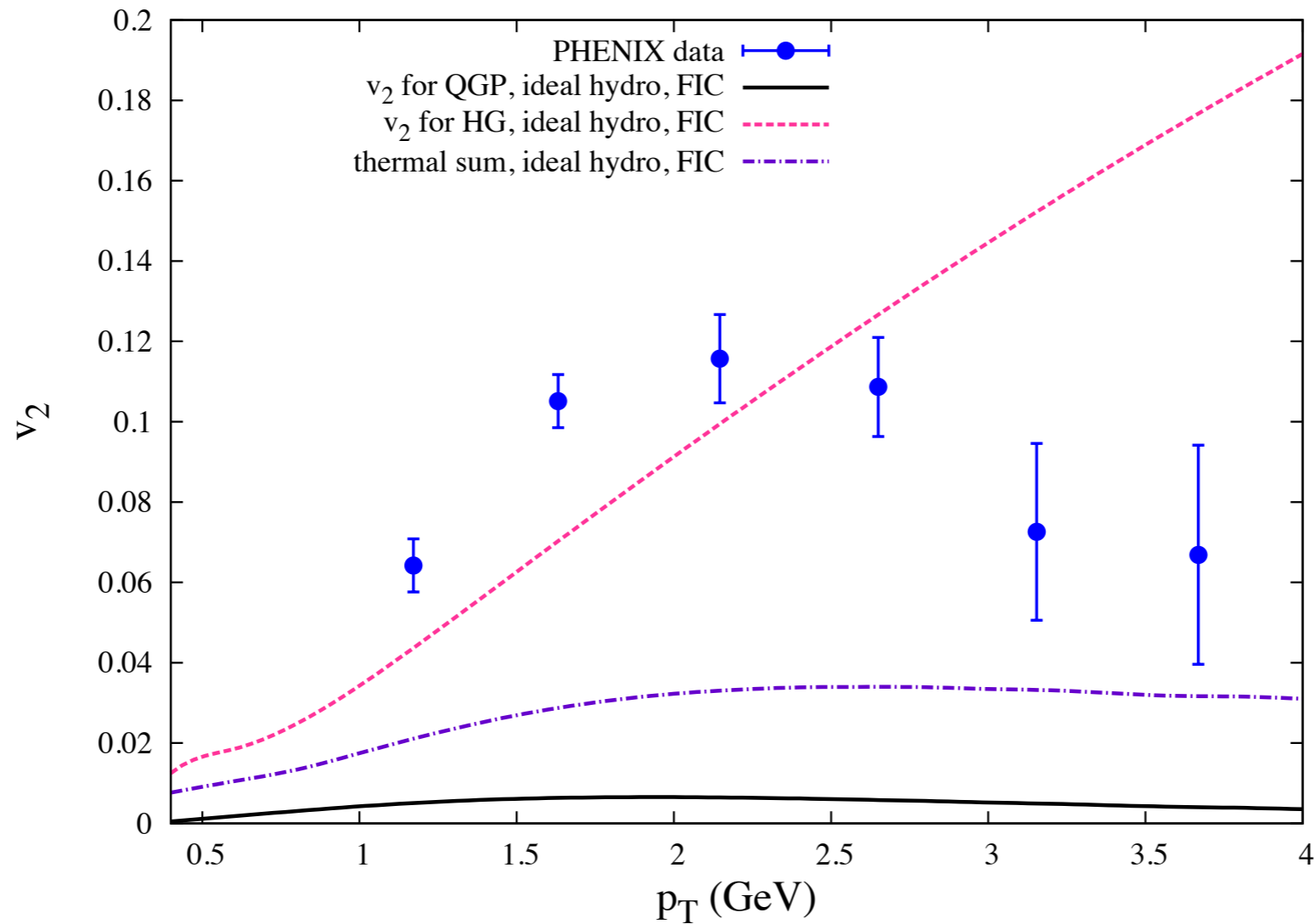
- FICs enhance  $v_2$  in this centrality class (0-20%), as for hadrons
- For hadrons measured in events belonging to large centrality, FICs will *decrease*  $v_2$
- HG elliptic flow is much larger than QGP elliptic flow, but remember net  $v_2$  is a weighted average

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- Net  $v_2$  is comparable in size to that with ideal medium.



# PHOTON $v_2$ DATA?

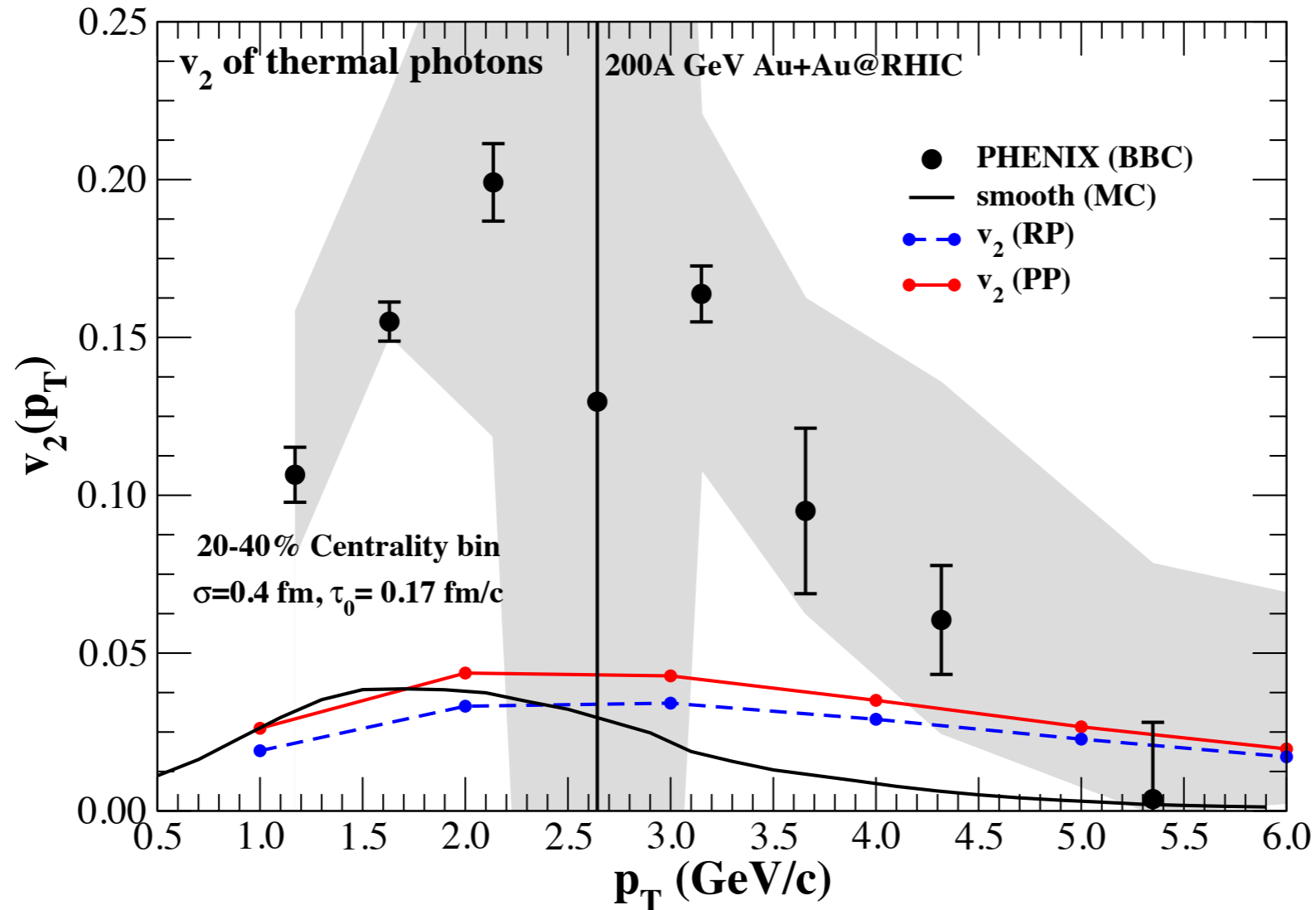


Dion et al. (2011)

- Data is higher than calculation, even with e-b-e initial state fluctuations, and ideal hydro
- Size comparable with HG  $v_2$



# PHOTON $v_2$ DATA?



Chatterjee et al. (2013)

Dion et al. (2011)

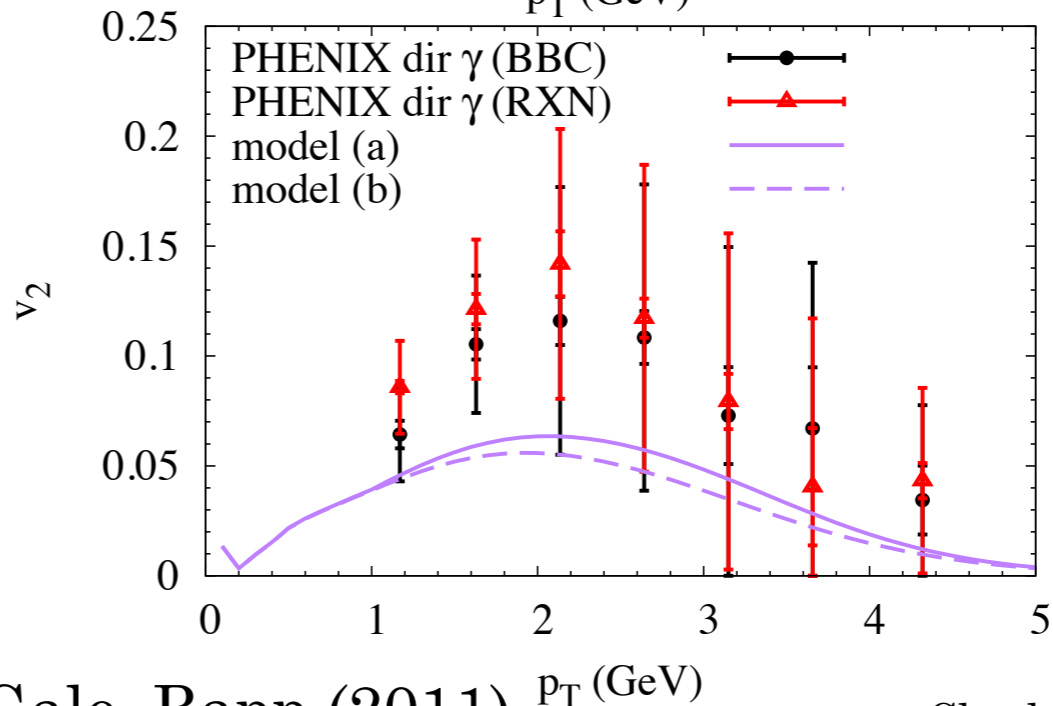
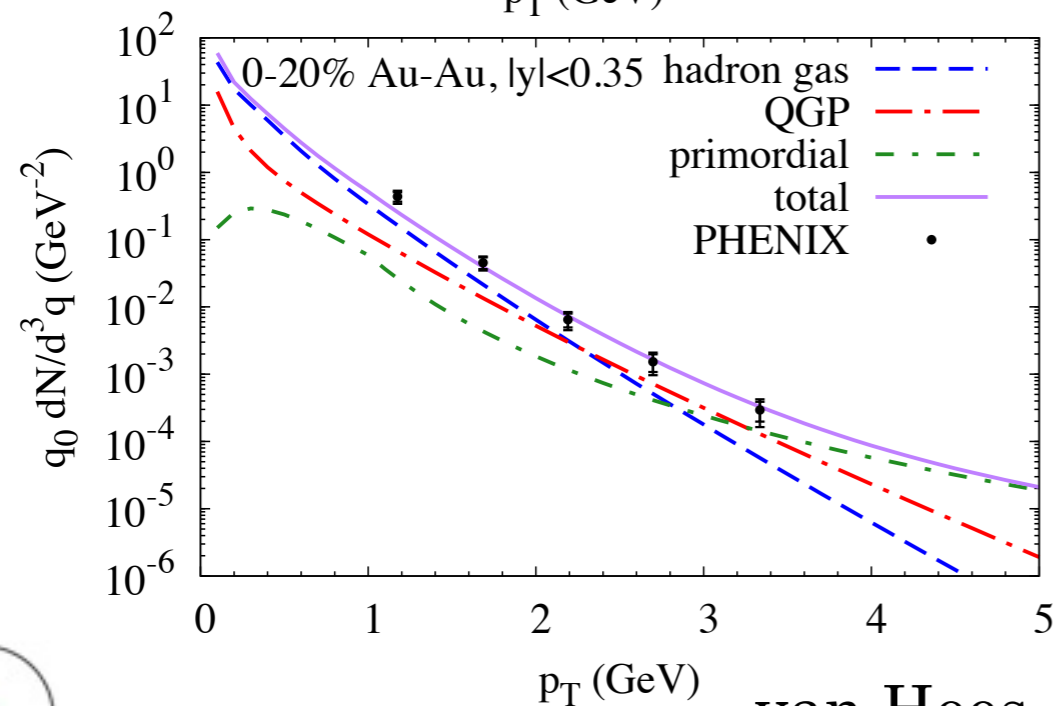
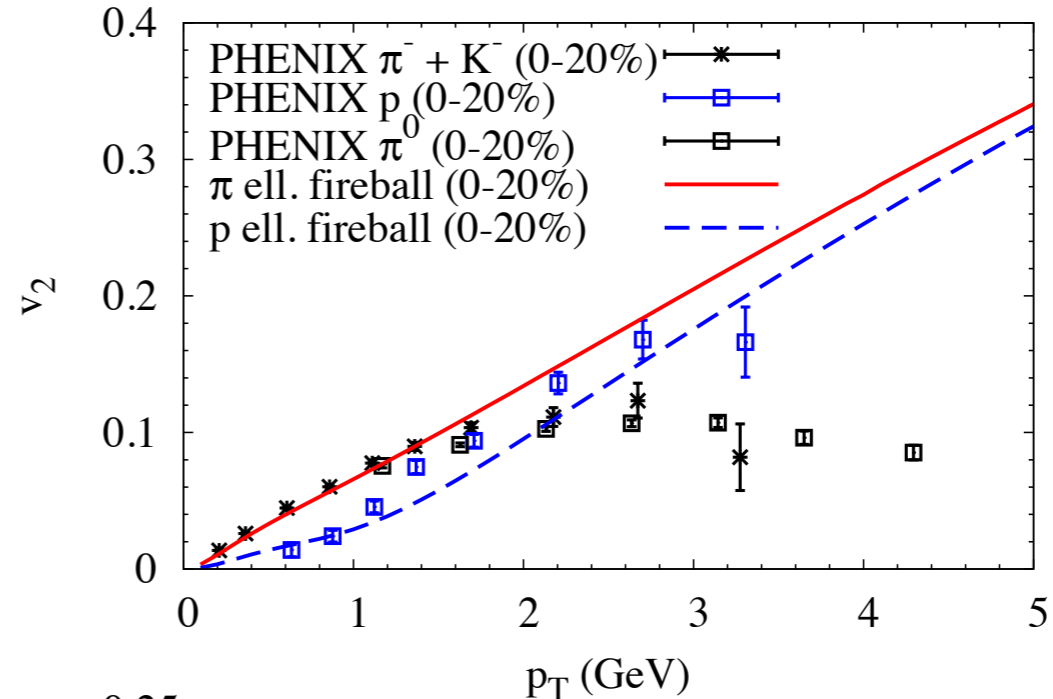
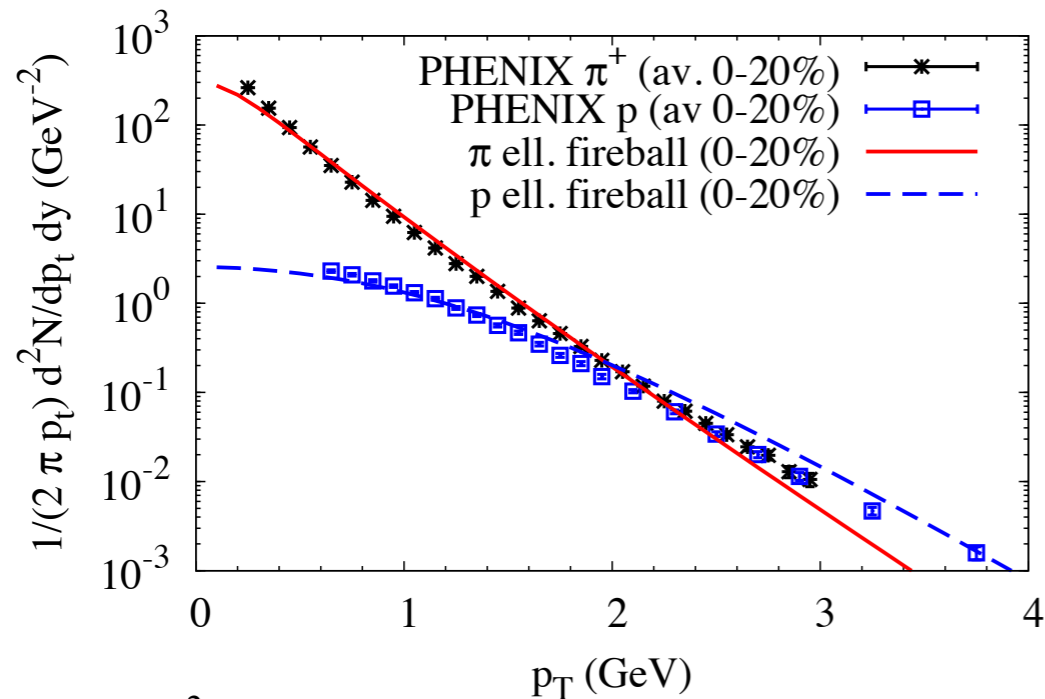
- Data is higher than calculation, even with e-b-e initial state fluctuations, and ideal hydro
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# SOME FACTS AND SOME LEADS

- FICs are here to stay. The meaning of “initial temperature” is altered.
- (Some?) Room to explore systematically hydro initialization and parameters. This requires consistency with the hadronic data.
- Making the QGP signal larger will *decrease* the  $v_2$ . The  $T=0$  photons, *decrease*  $v_2$ .
- Early-times magnetic field effects? (Basar, Kharzeev, Skokov, PRL (2012))
- Is the large photon elliptic flow telling us about the dynamics? Baryons?
- Non-zero initial shear tensor? Primordial flow? Can we improve on the hydro initial states?
- Can we improve on the hydrodynamic evolution?

# ELLIPTIC FLOW AND SPACE-TIME DYNAMICS

- In a thermal fireball picture, the net photon yield is sensitive to the value of the acceleration parameter, and to details of the initial state. The photons **do** report on the details of the dynamics.
- How uniquely determined are these? How unique is the entire evolution?



van Hees, Gale, Rapp (2011)

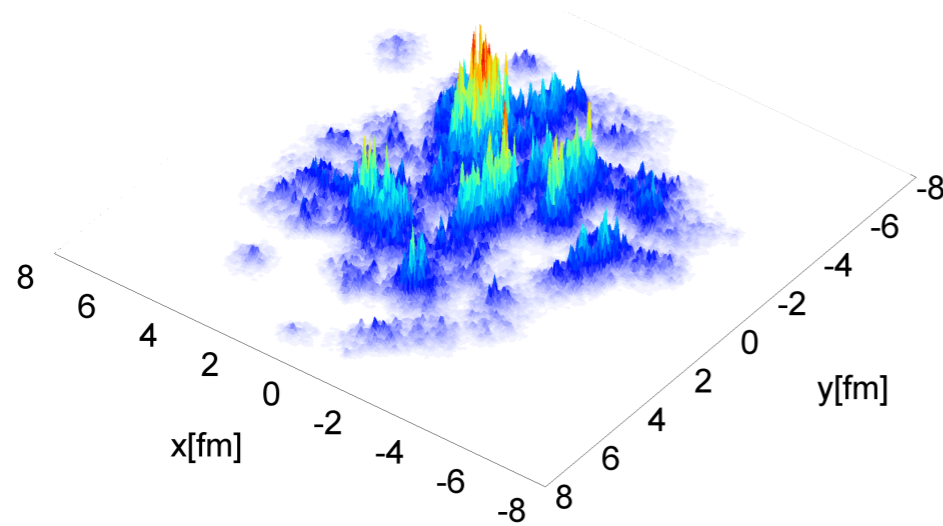
Charles Gale



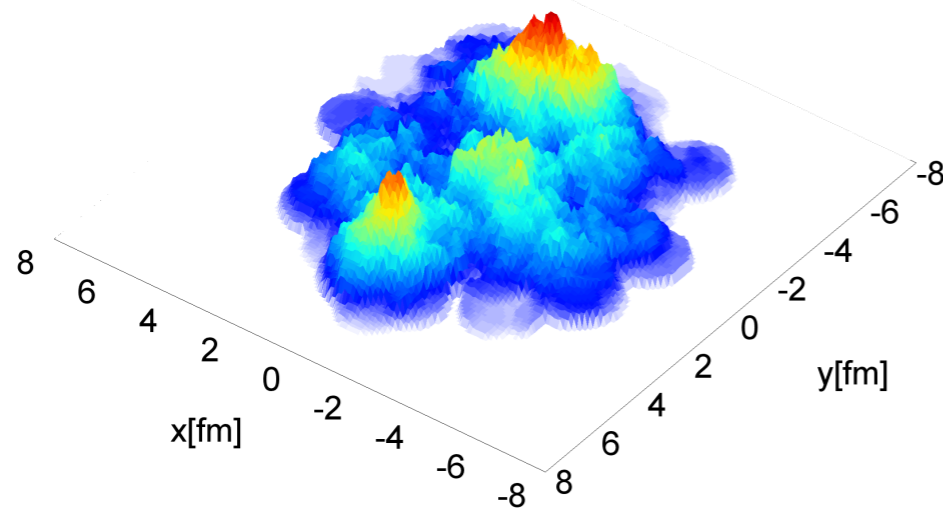
# FICs: BEYOND GLAUBER, ADDRESSING INITIAL/PRIMORDIAL FLOW

- Several sources of quantum fluctuations:
  - Fluctuations of nucleon distributions in the nuclear wave function
  - Fluctuations of the colour charges inside a nucleon:  
Depends on the nuclear saturations scale  $Q_s$
- Using fluctuating glasma initial states: IP-Sat + CYM.  
Implementation of CGC initial state.
- Couple the IP-Glasma initial state to MUSIC

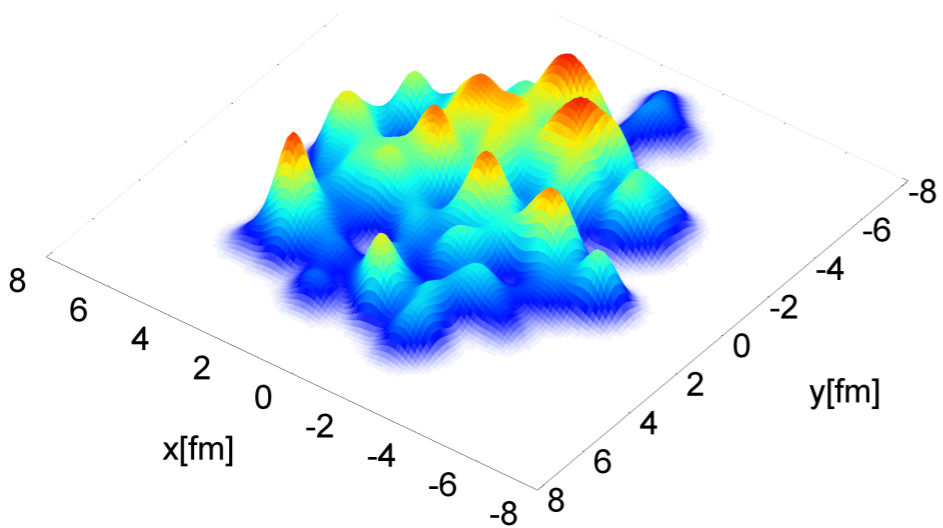
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IP-Glasma



MC-KLN



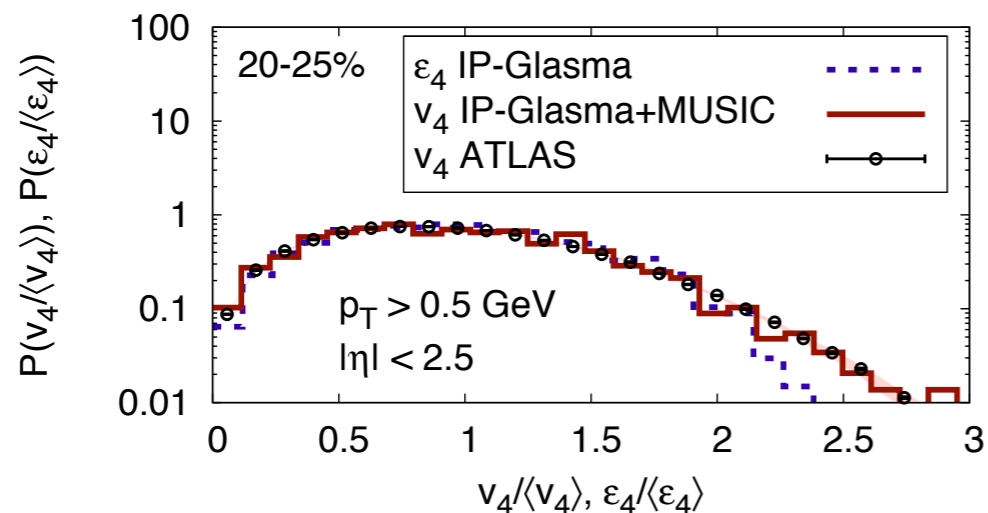
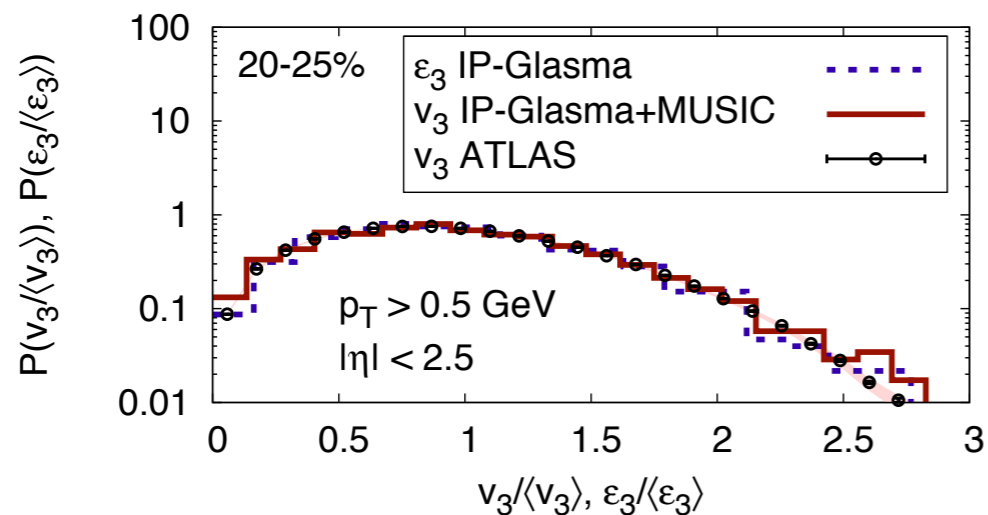
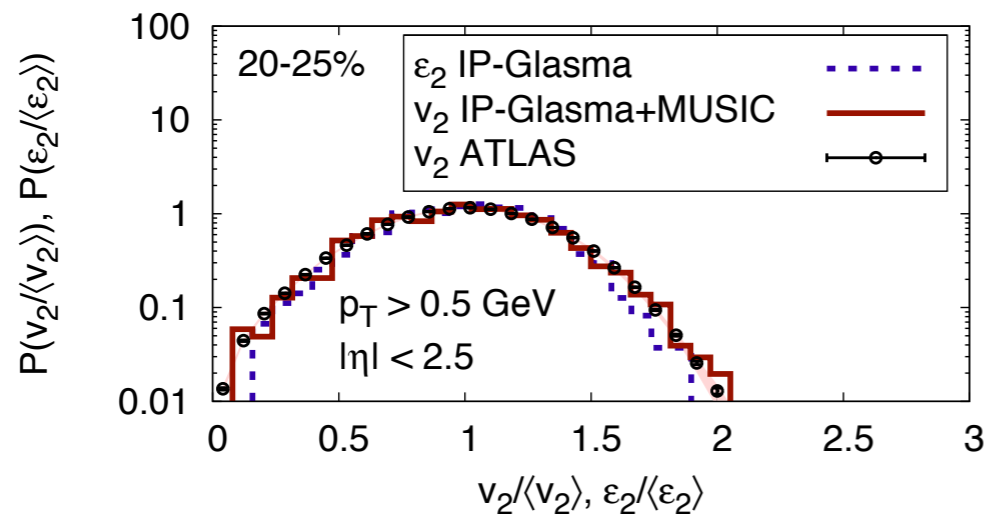
Glauber

IP-Glasma initial states show structure absent in Glauber

# IP-GLASMA + MUSIC

## EFFECT ON HADRONIC OBSERVABLES

- Flow harmonics reproduced up to  $v_5$  at RHIC and LHC
- Distributions of  $v_n$  at LHC:



- Initial eccentricity distributions a good approximation to  $v_n$ 's
- IP-Glasma + MUSIC provides consistent flow systematics at RHIC & LHC
- Investigating the effects on EM variables

Gale, Jeon, Schenke, Tribedy, Venugopalan  
PRL (2013)

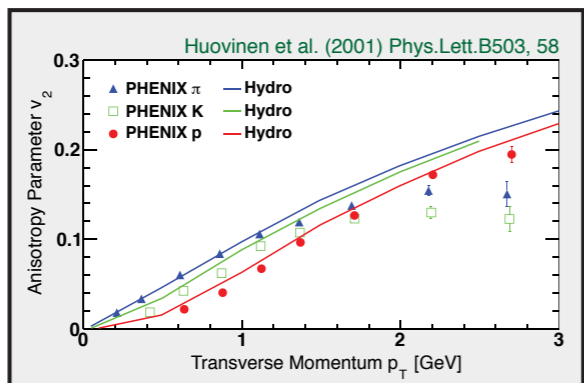


# Is the hydrodynamic modeling complete?

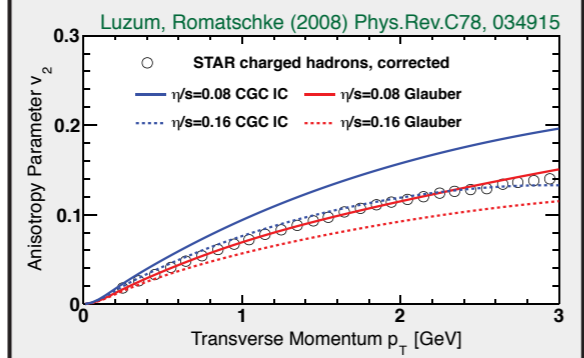
- In the last ~5-8 years, relativistic hydrodynamics has undergone a revolution
  - 3D
  - 3D - Shear viscosity
  - 3D - Shear viscosity - Fluctuating initial conditions
  - 3D - Shear viscosity - Fluctuating initial conditions also in  $y$
- What's left?

# Important experimental and theoretical developments

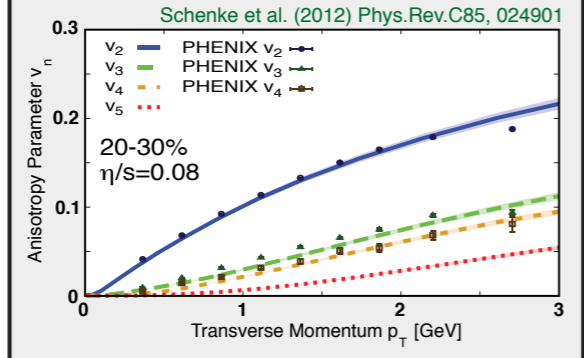
# Increasing precision of key observable



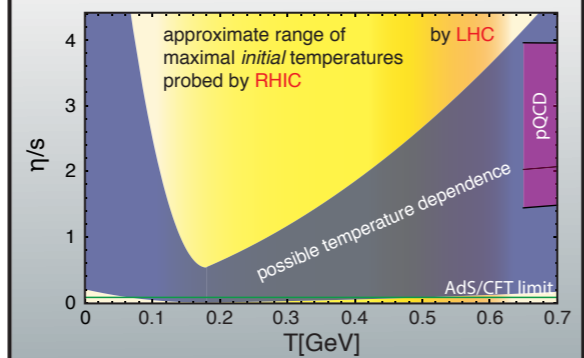
Early success of hydrodynamics missing physics of lattice QCD equation of state and viscosity.



Bounds on shear viscosity but large uncertainties from initial conditions.



Higher moments constrain viscosity and fluctuating initial conditions better, but temperature dependence of  $\eta/s$  is not yet determined.



To determine  $(\eta/s)(T)$  different initial temperatures need to be accessible. Only possible with combined data from LHC and RHIC beam energy scan.

2000 experimental techniques developed

2002  $v_2$  systematics developed

2004 analysis improved errors reduced

2006 fluctuations important for  $v_2$  analysis in small systems

2008 first flow results from viscous fluid-dynamics

2010 reliable QCD equation of state from the lattice included

2012  $v_3$

2012  $v_n$

2012  $v_n$  correlations

2012  $P(v_n)$

2014

RHIC BES-II upgrade required to

2022

0 0.5 1 1.5 2

$\frac{\eta}{s} \sim \frac{1}{\alpha_s^2 \ln(\alpha_s^{-1})}$

ideal hydro

LO pQCD

$\frac{1}{4\pi}$  AdS/CFT limit

viscous hydro

- kinetic theory
- lattice QCD
- AdS/CFT limit
- viscous hydro + flow data

$\frac{\eta}{s}(T), \frac{\zeta}{s}(T)$

$\tau_\eta, \tau_\zeta, \dots$

$\eta/s$  near  $T_c$

2000

2002

2004

2006

2008

2010

2012

2014

2022





$$T^{\mu\nu} = -Pg^{\mu\nu} + \omega u^\mu u^\nu + \Delta T^{\mu\nu}$$

A general form for the dissipative terms:

$$\Delta T^{\mu\nu} = \eta \left( \Delta^\mu u^\nu + \Delta^\nu u^\mu \right) + \left( \frac{2}{3} \eta - \zeta \right) H^{\mu\nu} \partial_\rho u^\rho - \chi \left( H^{\mu\alpha} u^\nu + H^{\nu\alpha} u^\mu \right) Q_\alpha$$

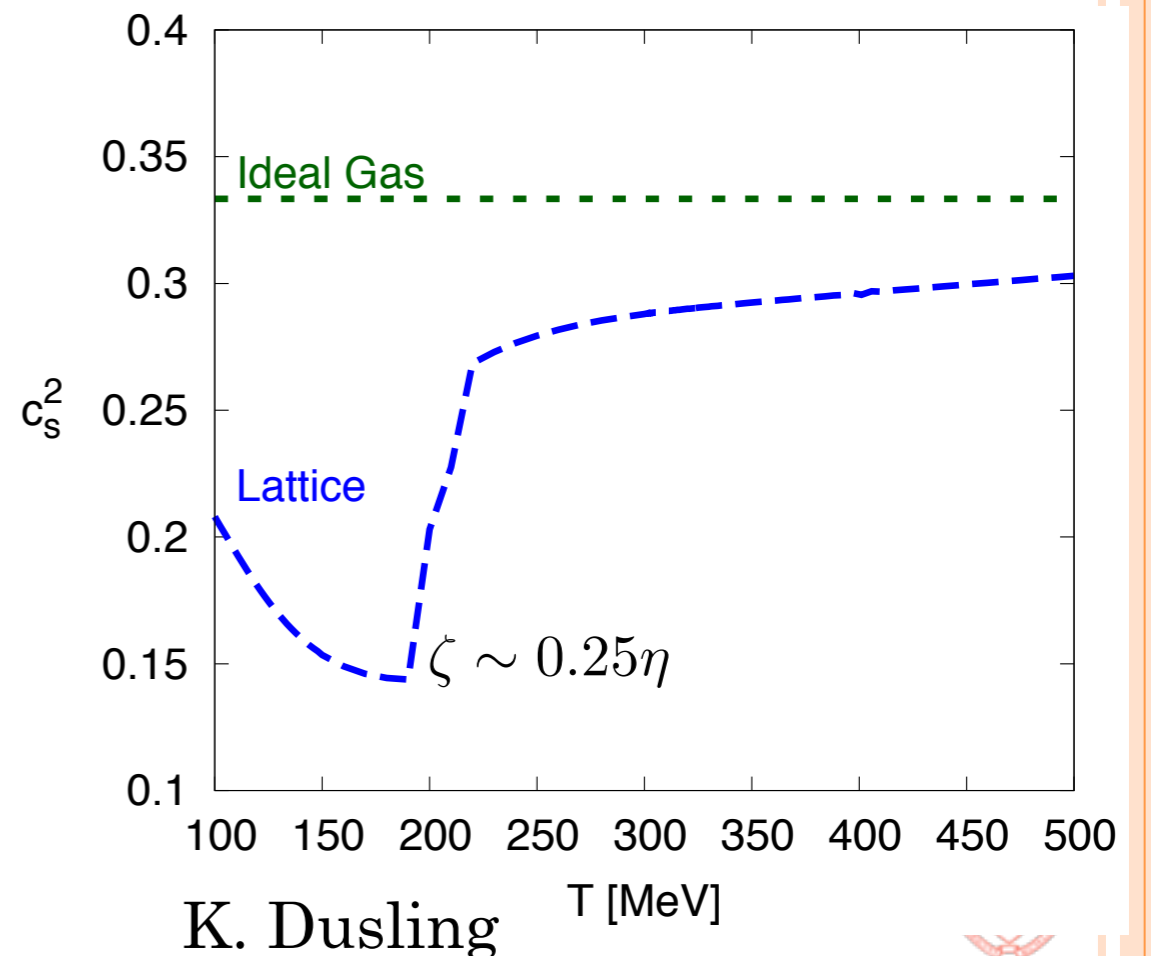
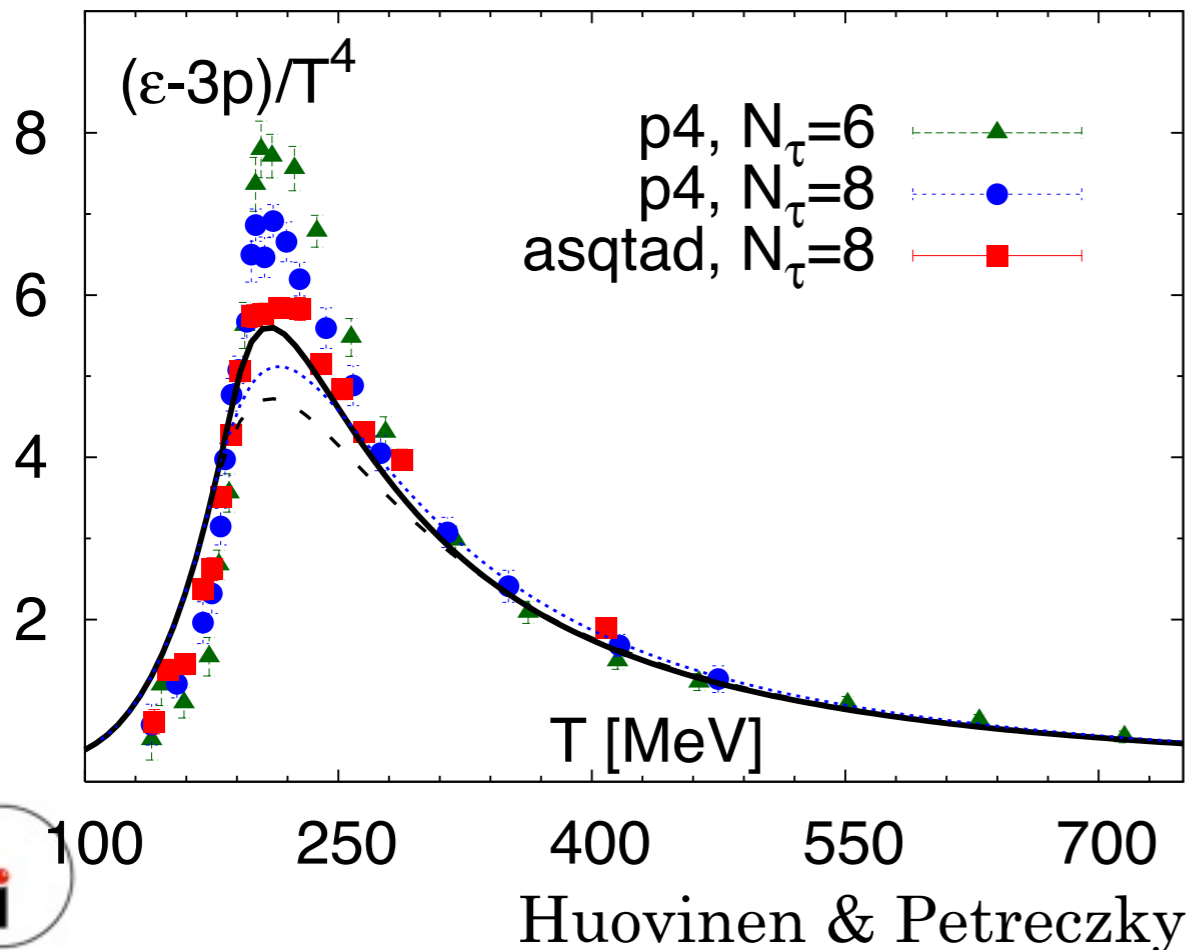
No simulation incorporates all of these

# BULK VISCOSITY?

$$\zeta \approx 15\eta \left( \frac{1}{3} - c_s^2 \right)^2 \quad \text{S. Weinberg, Ap. J (1971)}$$

$$\zeta \gtrsim 2\eta \left( \frac{1}{3} - c_s^2 \right) \quad \text{A. Buchel, Phys. Lett. (2008)}$$

Bulk viscosity vanishes in conformal fluids. QCD is only very approximately conformal:



# BULK VISCOSITY?

- Quantifies deviations from equilibrium, when the fluids expands or contracts more quickly than the time needed to relax back to equilibrium

$$\Delta T^{\mu\nu} = \eta \left( \Delta^\mu u^\nu + \Delta^\nu u^\mu \right) + \left( \frac{2}{3} \eta - \zeta \right) H^{\mu\nu} \partial_\rho u^\rho - \chi \left( H^{\mu\alpha} u^\nu + H^{\nu\alpha} u^\mu \right) Q_\alpha$$

$$\frac{\delta f}{f_0} \sim p_T^2 \left( \frac{1}{3} - c_s^2 \right)^2 (\partial_\mu u^\mu) \quad \text{Relaxation Time Approximation, Dusling \& Schäfer (2012)}$$

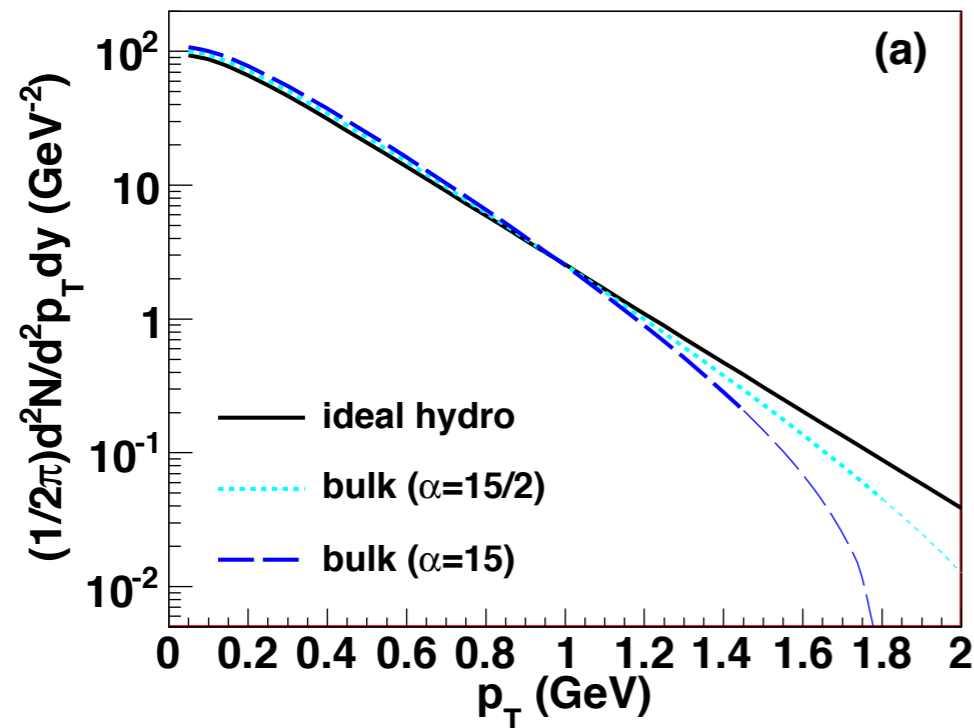
$$\frac{\delta f}{f_0} \sim \zeta (\partial_\mu u^\mu) \left[ \alpha + \beta u \cdot k + \gamma (u \cdot k)^2 \right] \quad \text{Modified Moment Expansion Noronha-Hostler, Denicol, et al., (2013)}$$

- Acts as a “negative pressure”

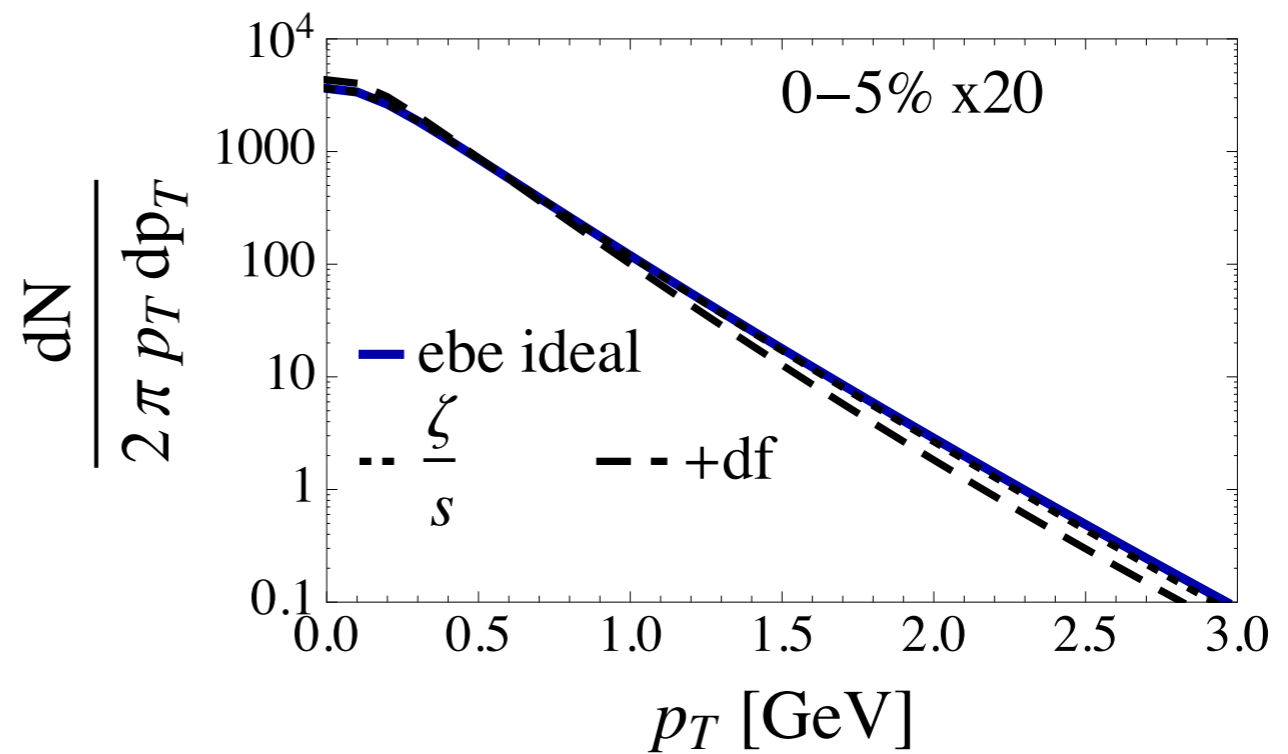
$$P \rightarrow P - |\Pi|$$



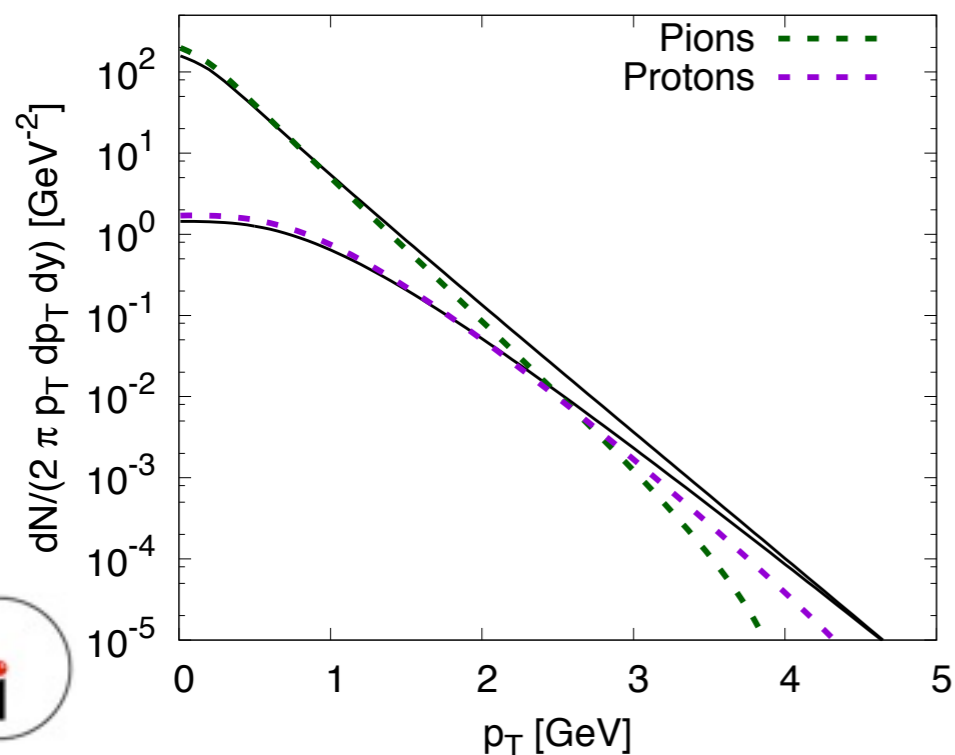
# BULK VISCOSITY EFFECTS ON HADRON SPECTRA @ RHIC



Monnai and Hirano (2009)  
3+1D Hydro



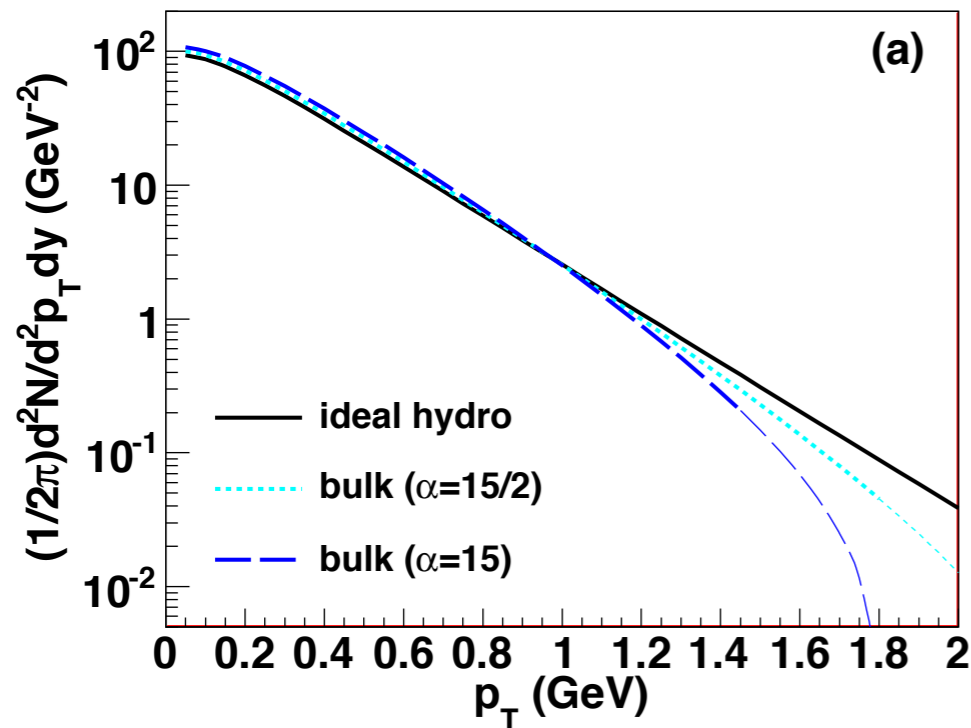
Noronha-Hostler, Denicol, Andrade,  
Grassi (2013), 2+1D Hydro



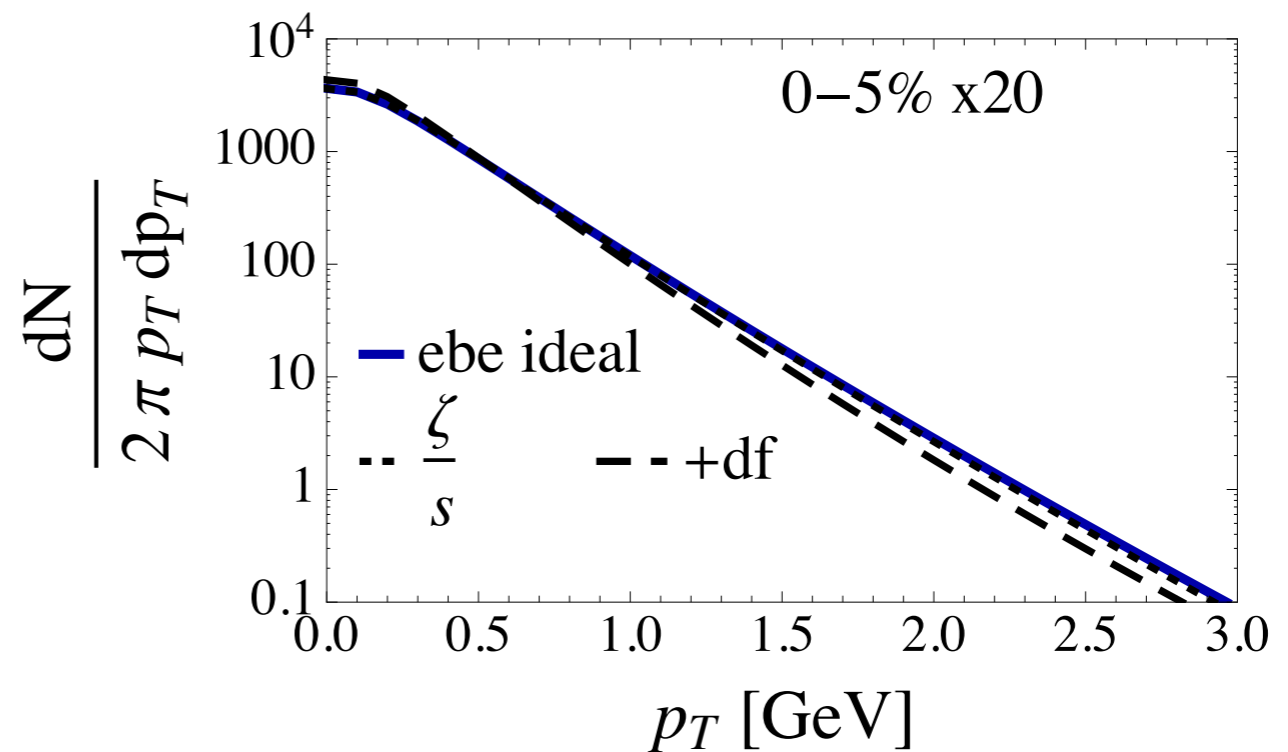
Dusling and Schäfer, (2012) —  $\eta/s = 0.16$   
2+1D Hydro      --  $\eta/s = 0.16, \zeta/s = 0.005$



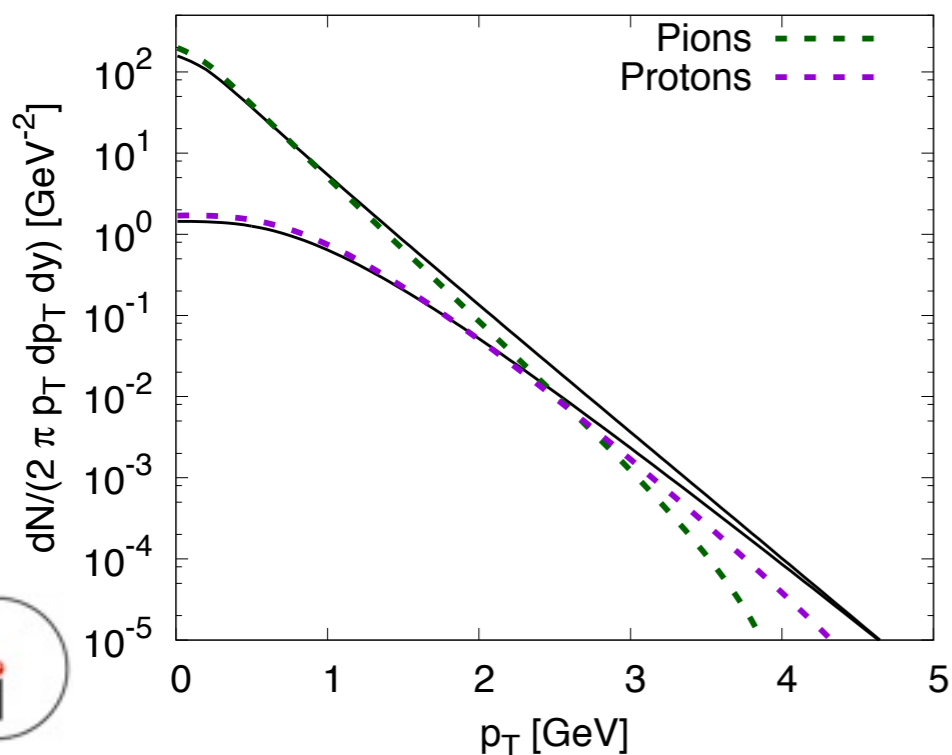
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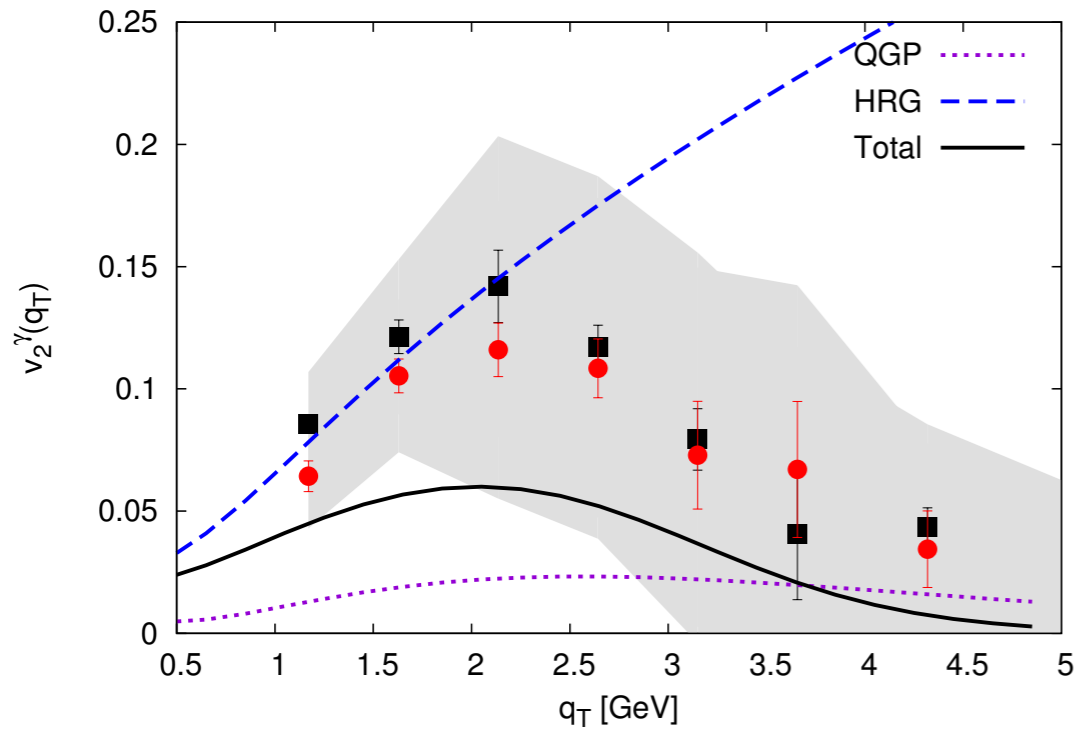
Dusling and Schäfer, (2012) —  $\eta/s = 0.16$   
2+1D Hydro —  $\eta/s = 0.16, \zeta/s = 0.005$

- Spectra are systematically softer
- Details depend on the scheme to implement the viscosity correction(s)
- Some cancellation between shear and bulk effects

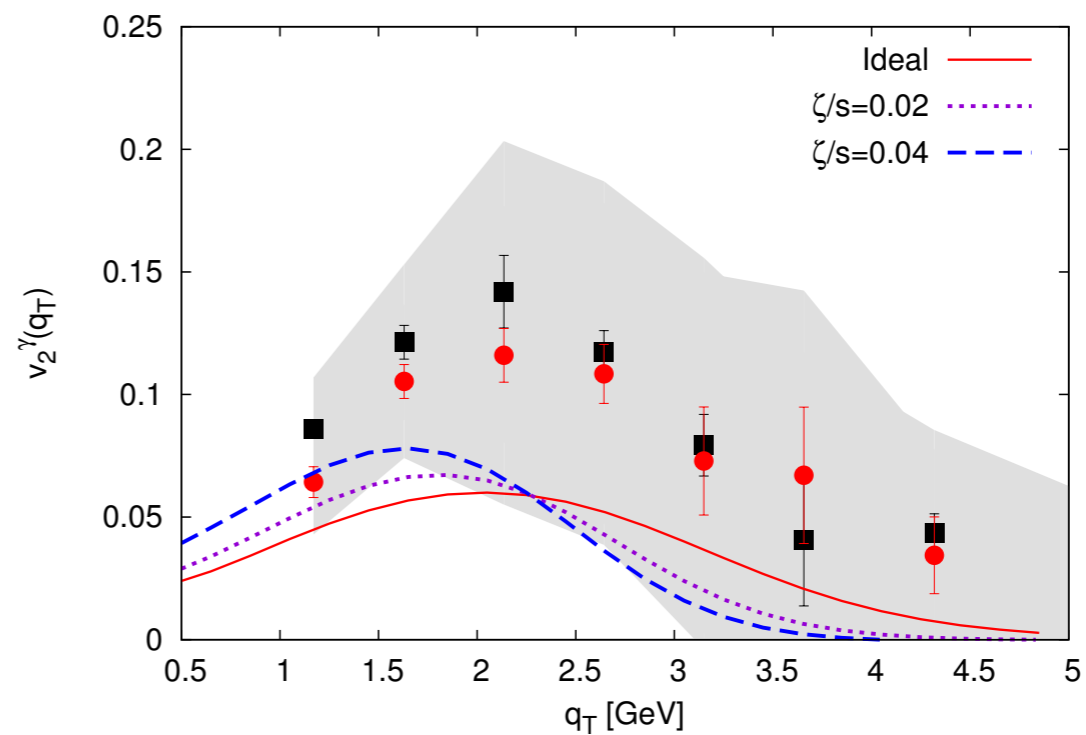


# BULK VISCOSITY EFFECTS ON PHOTONS?

Ideal photon  $v_2(q_T)$



Viscous photon  $v_2(q_T)$



K. Dusling

- Bulk viscosity seems to help, but perhaps not enough?
- Effects are however large enough: a consistent inclusion of bulk is warranted.

- $\frac{\zeta}{s}(T)$  etc...

# CONCLUSIONS

- The status of EM rates and their integration in dynamical models is still in flux
- Photon  $v_2$  is sensitive to the EOS, and to various hydro parameters such as viscosity, and initial conditions (time and FICs). Current  $v_2$  data: new physics? Measuring photon  $v_3, v_n$  at RHIC and LHC will help complete this picture
- FICs and viscosity(ies) make a difference in photon (and dilepton) characterization of the HICs: one must be consistent with hadronic data
- Jet-plasma photons need to be included: MARTINI
- Known unknowns: pre-equilibrium radiation

# Thanks to

- \* G. Denicol
- \* S. Jeon
- \* I. Kozlov
- \* M. Luzum
- \* J.-F. Paquet
- \* R. Rapp (Texas A&M)
- \* B. Schenke
- \* C. Shen (OSU-U. Heinz)
- \* H. van Hees (Frankfurt)
- \* G. Vujanovic