

# Heavy Ion Collisions



# In Medium Dileptons

- Intro (VK)
- From pp to pA to AA (Tetyana)
- Various details of the in medium rho/omega spectral function calculation (Ralf)
- Transport (Theory vs reality) Stefan
- Ingredients to the Gumbo ( how dileptons are calculated in a transport code) Janus
- Effects of time evolution (Hendrik)
- Photons and  $v_2$  (Hendrik)
- What do we need to declare success (VK, all)

# Thermodynamics and Resonances

Resonances are nothing but interactions among the long lived particles (pions, nucleons):

Virial Expansion a la Beth Uhlenbeck

(see e.g. Landau, Stat.Mech, or Prakash et al. PLB 245 (1990))

$$\Delta P = \frac{\int d^3 q}{(2\pi)^3} \int d\epsilon \exp(-\beta \sqrt{q^2 + \epsilon^2}) \sum_i \frac{1}{\pi} g_i \frac{\partial \delta_i(\epsilon)}{\partial \epsilon}$$

Limit of narrow width

Phase shift resonance

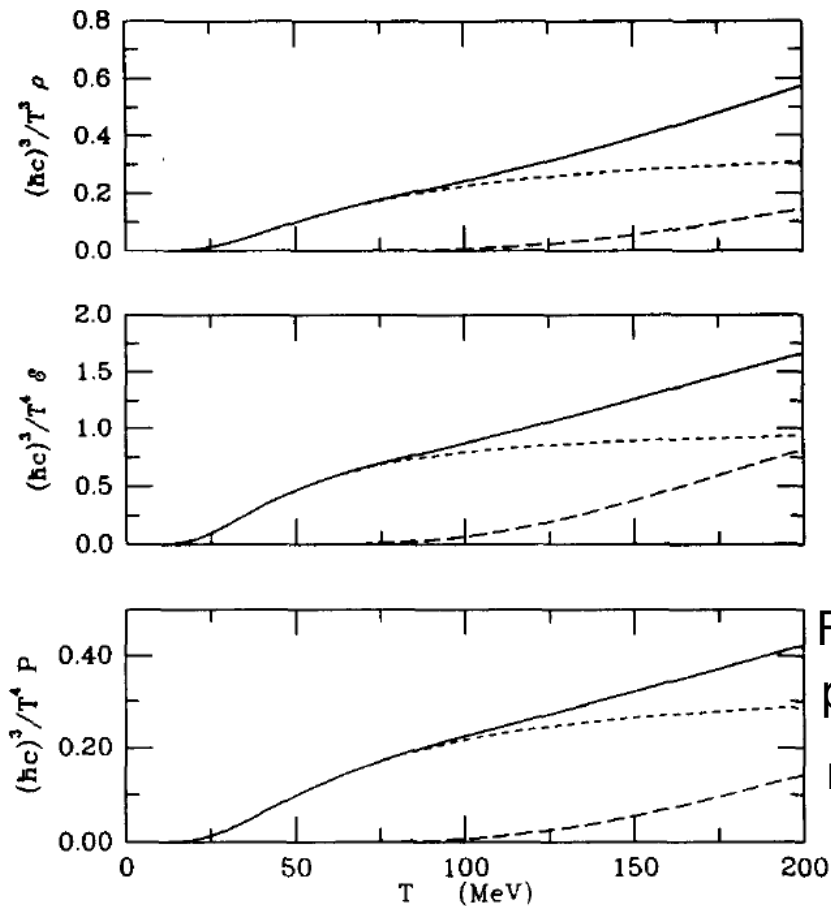
$$\delta(E) = \frac{\pi}{2} + \arctan\left(\frac{E - M_R}{\Gamma/2}\right) \rightarrow \pi \delta(M_R - E)$$

$$\Delta P \rightarrow \sum_i g_i \int \frac{d^3 q}{(2\pi)^3} \exp(-\beta \sqrt{q^2 + M_R})$$

Appears just as a gas of resonances

Necessary ingredients: Narrow width, “proper” resonances

# Thermodynamics and Resonances

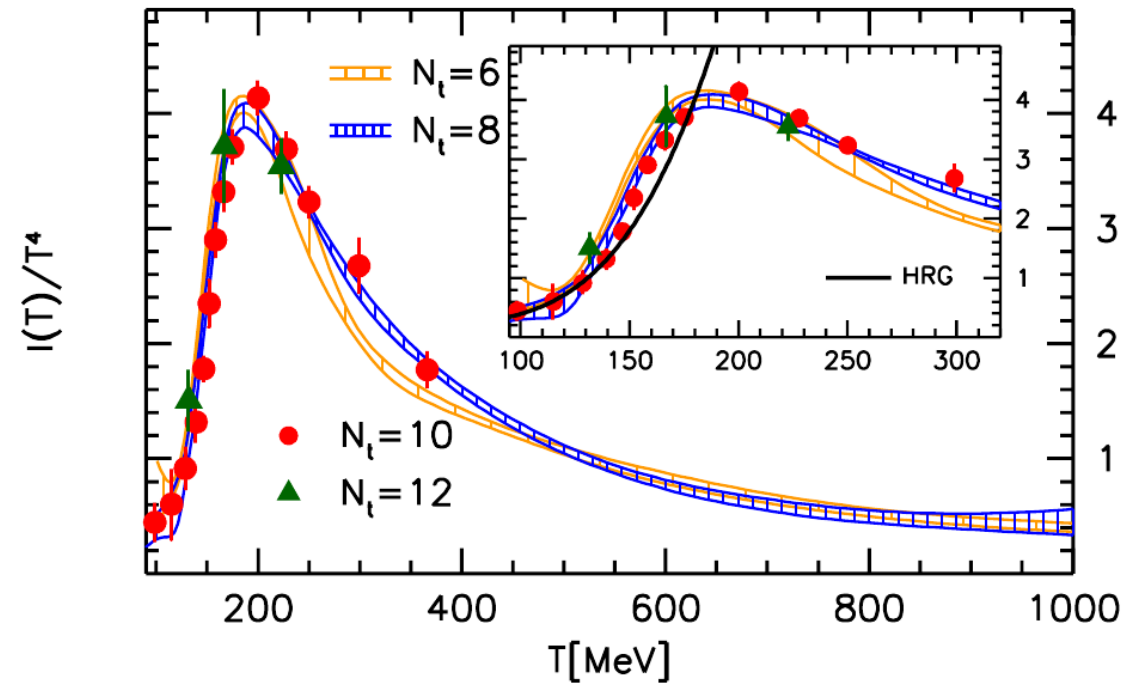
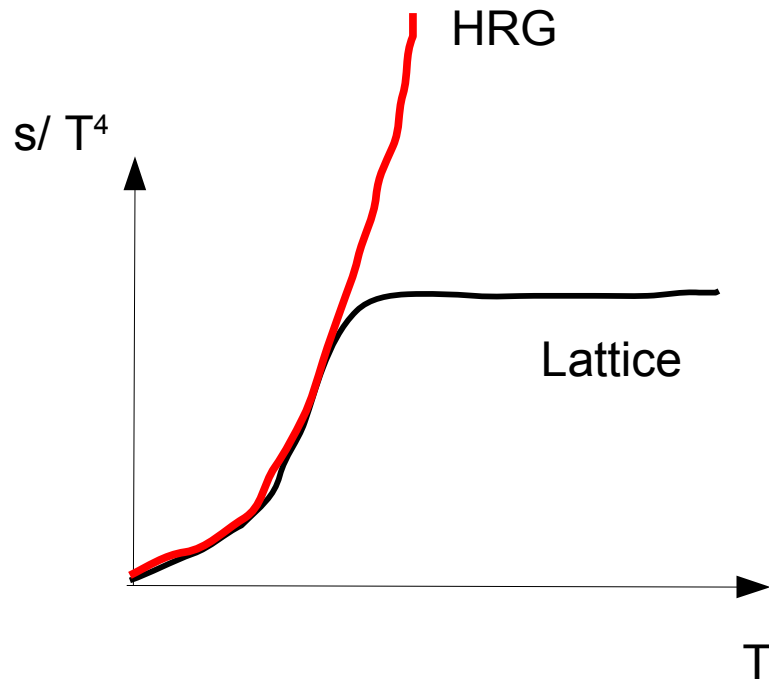


Works well for the rho meson!

Fully interacting system  
pions  
rhos

Prakash et al, PLB 245 (1990)

# Resonances and the EOS

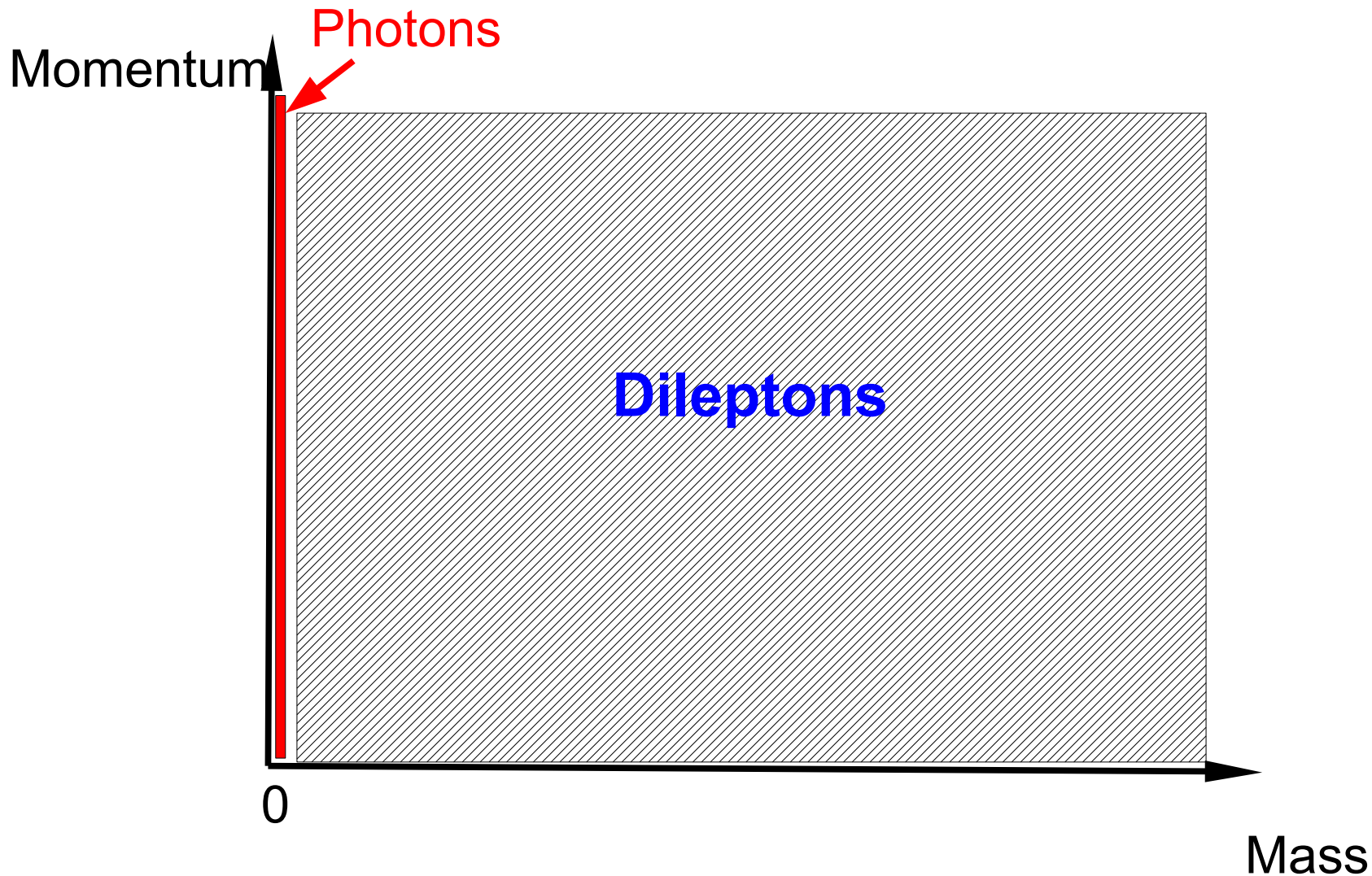


Wuppertal/Budpest LQCD

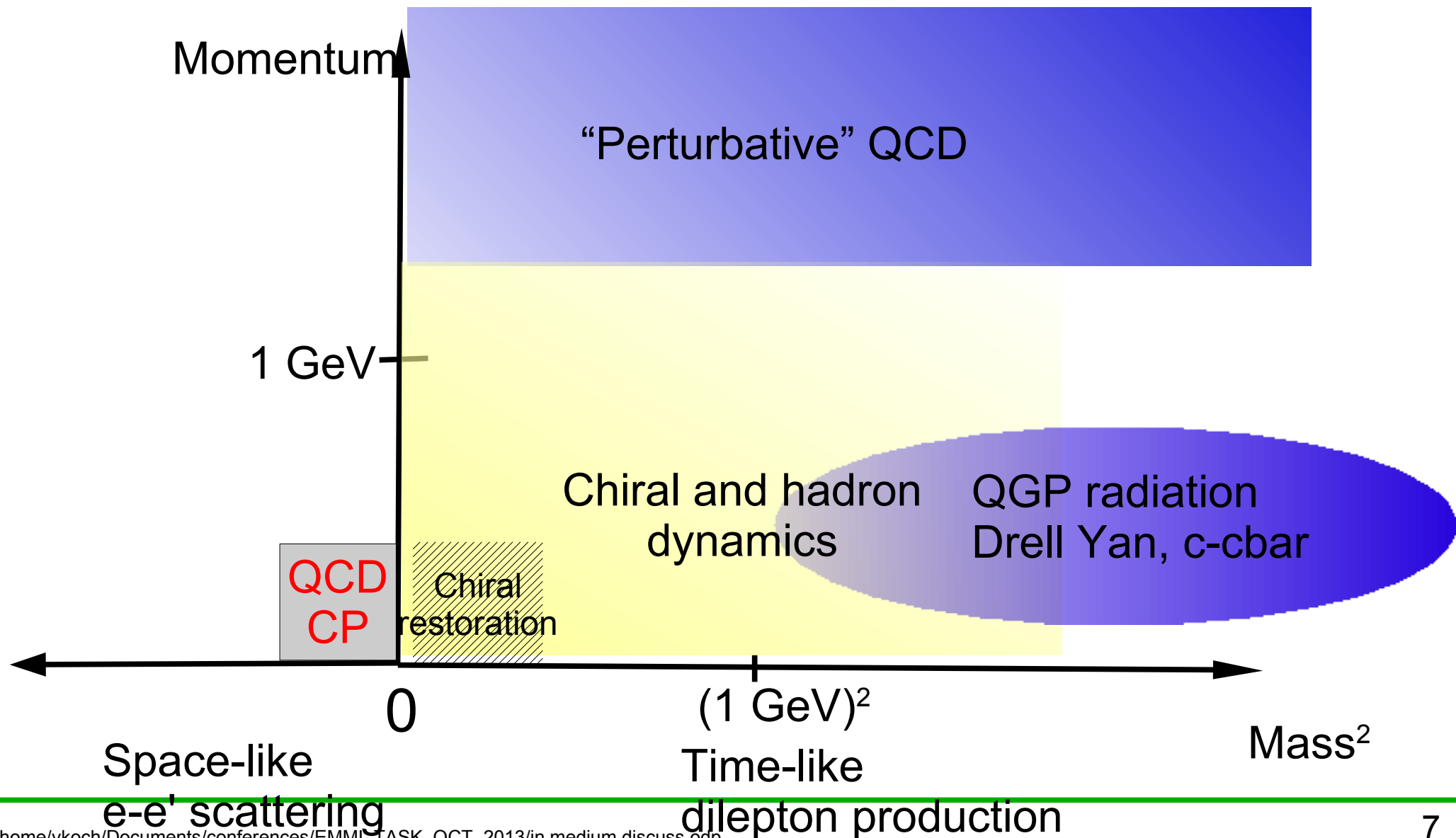
EOS reasonably well described by HRG up to  $T \sim T_c$   
For  $T > T_c$  QCD predicts **LESS** degrees of freedom than HRG

# Dilepton

## The versatile photon



# The Dilepton production landscape



# Dileptons (dis) advantages

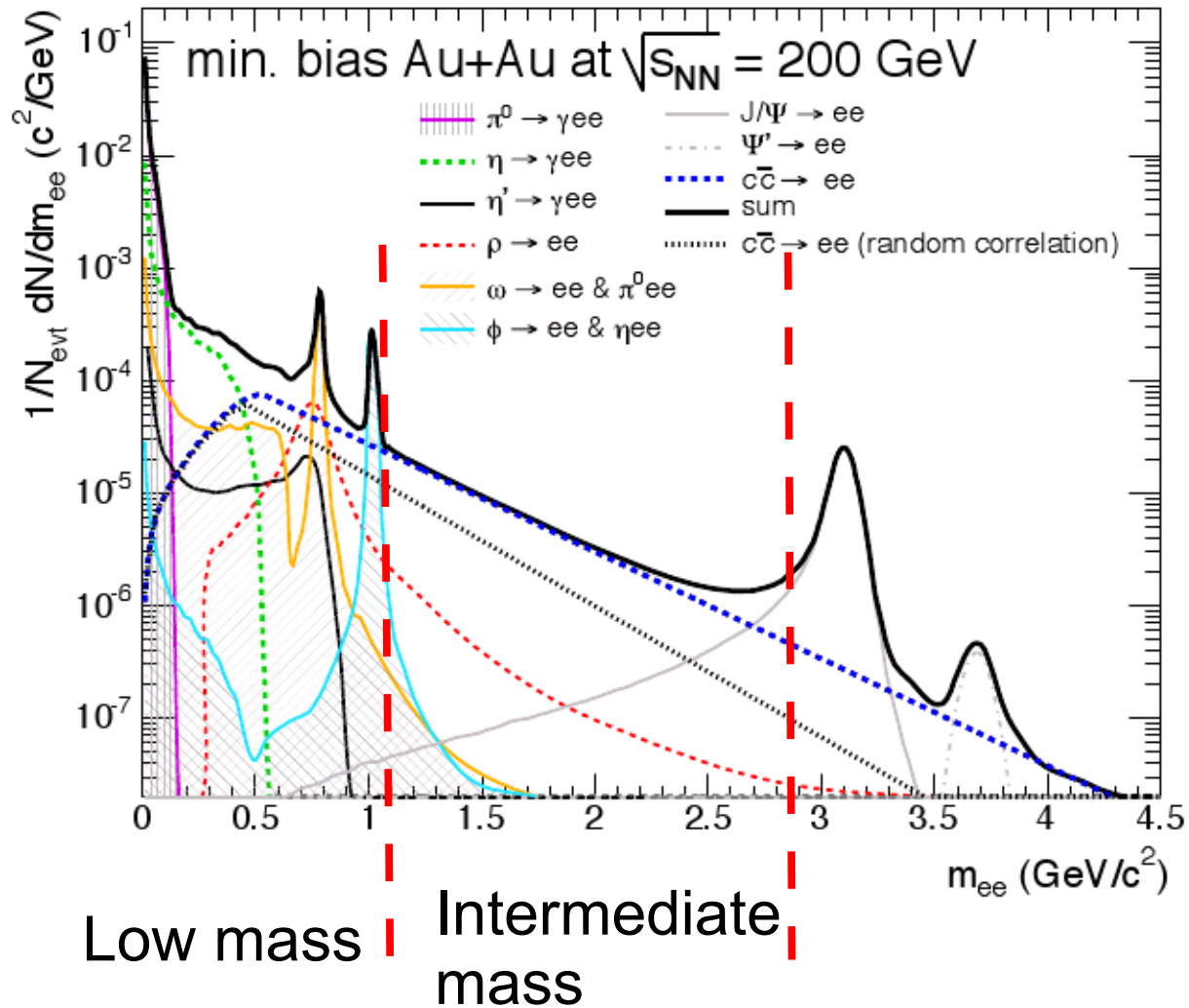
- Good:
  - Penetrating probe
  - Dynamic range ( $M$ ,  $p_t$ )
- Bad:
  - Penetrating probe: Measure only time integrals
  - Rare



# Production channels

- Quark annihilation (the holy grail?)
- Pion annihilation (the dull background?)
- Resonance decays
  - $N(1520)$ ,  $a_1$ ,  $\omega$ , etc. (Note: many are 3 body decay)
- Multi-particle channels
- Exotica
  - DCC, collective Bremsstrahlung
- Drell-Yan
- “ $c\text{-}c_{\text{bar}}$  decays”

# Elementary Production channels



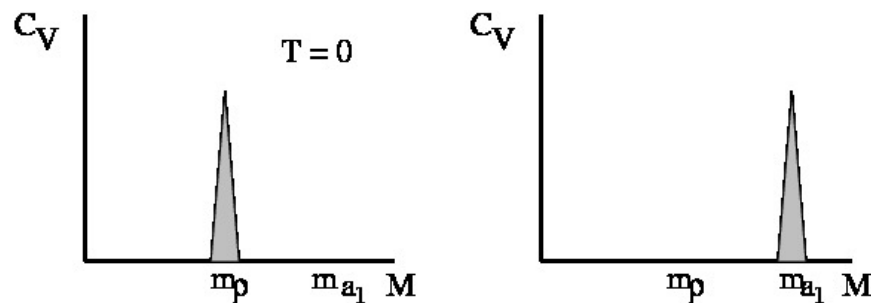
Thanks to  
T. Ullrich

# Low mass dileptons

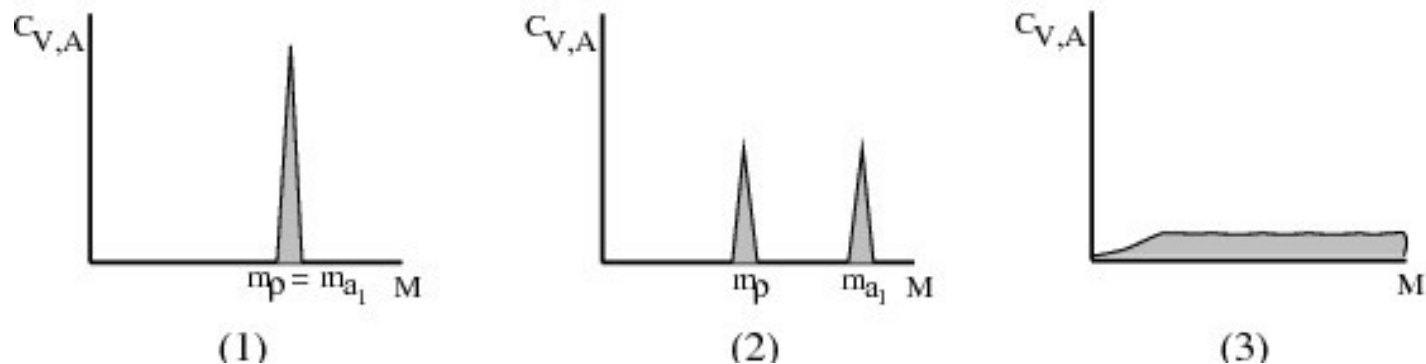
Chiral symmetry restoration:

QCD vacuum: Chiral symmetry spontaneously broken!

$T=0$



$T > T_c$



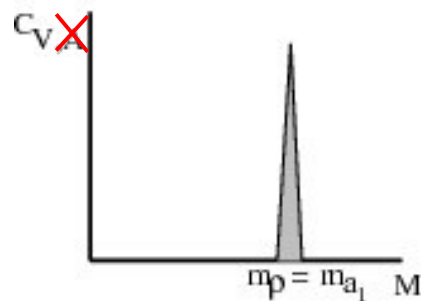
# Dileptons and chiral symmetry

Dileptons measure both **isovector-vector** and **isoscalar vector** current

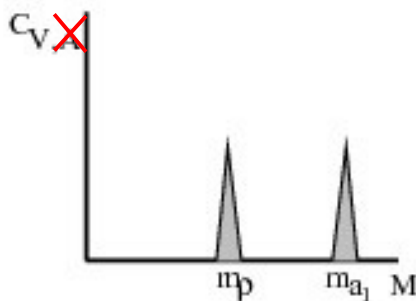
Good!!

Not so good

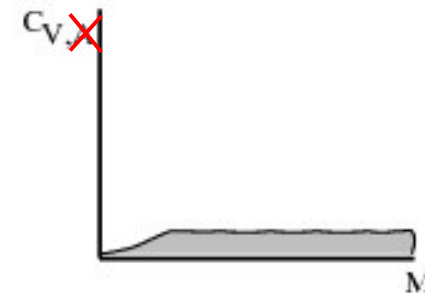
Dileptons do **NOT** measure the isovector **AXIAL** current



(1)



(2)



(3)

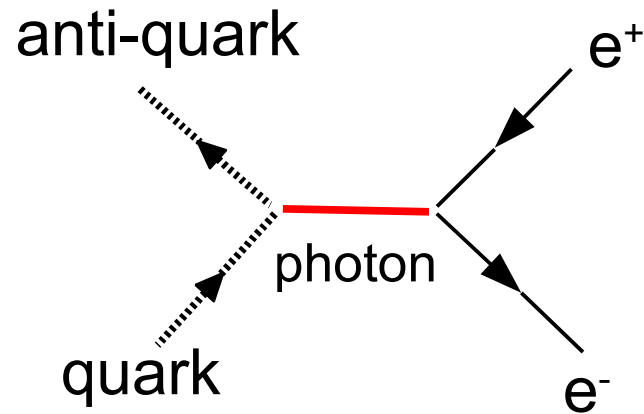
# Calculating Dilepton Production

- Elementary production channels
- Many body (medium) effects
- Collision / Expansion dynamics

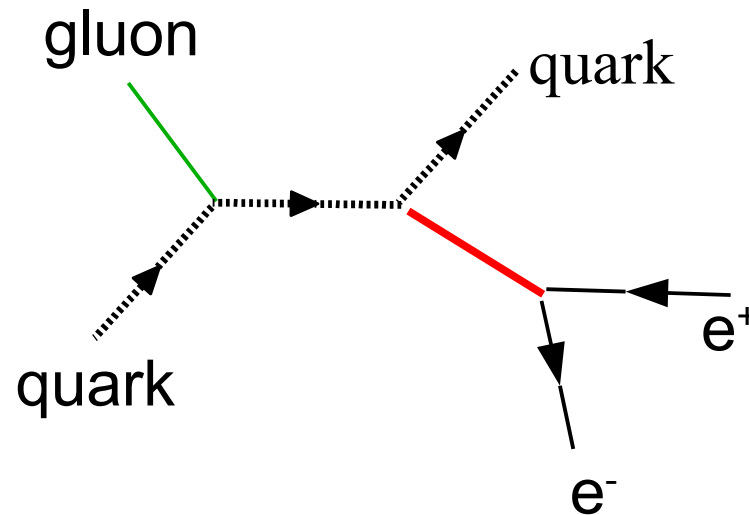
# Elementary channels

(partons)

q-qbar annihilation:



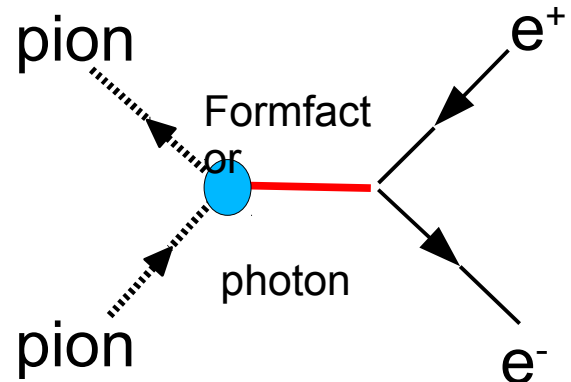
Compton  
"scattering"



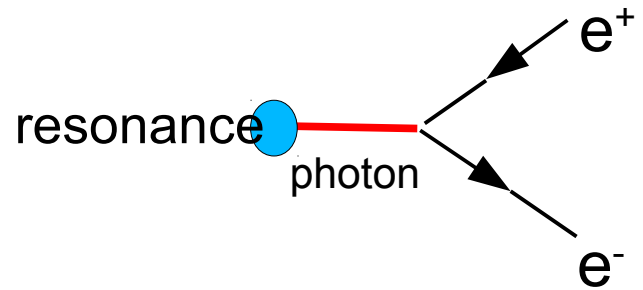
# Elementary channels

(hadrons)

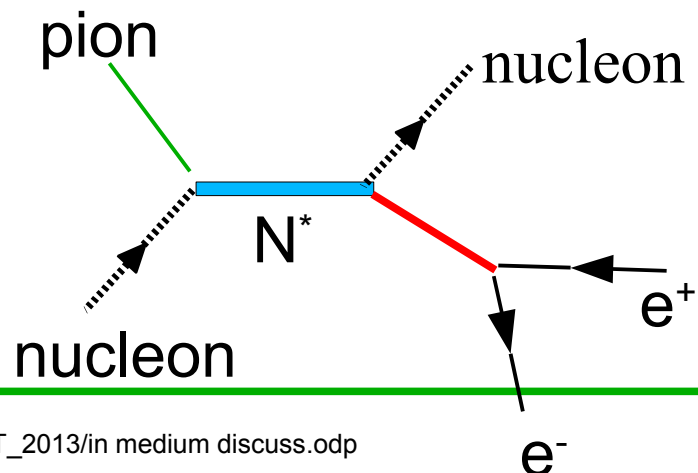
Pion annihilation



“Direct decay”



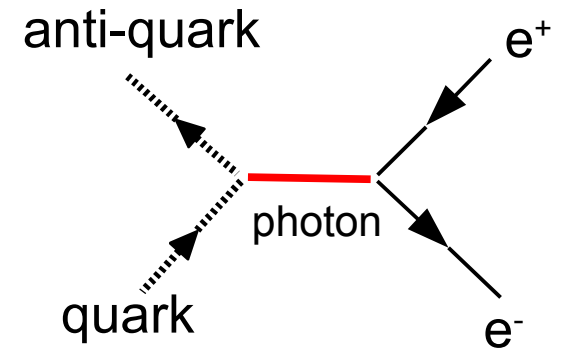
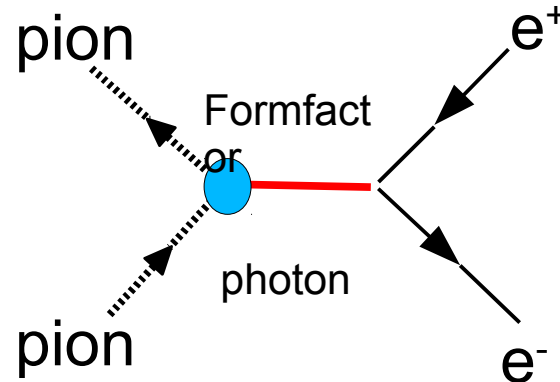
Dalitz decay



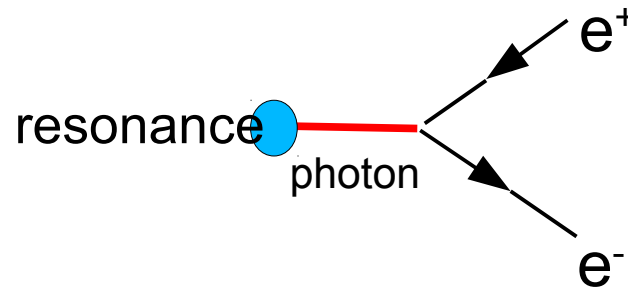
# Elementary channels

(hadrons)

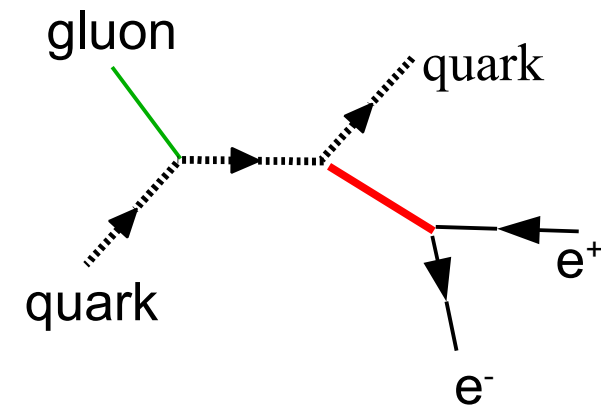
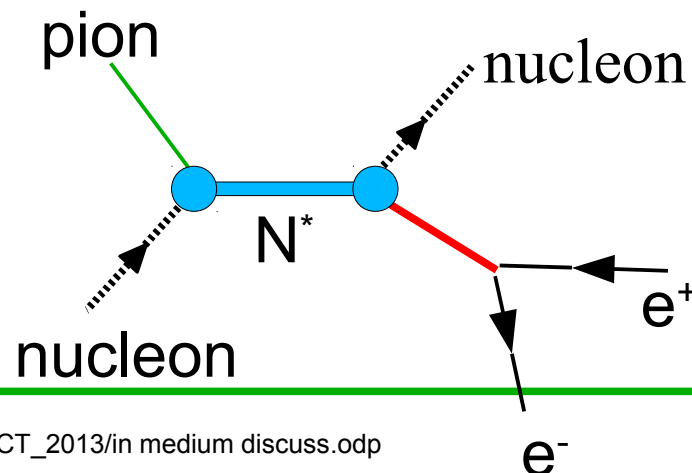
Pion annihilation



Direct decay



Dalitz decay





# Many body / medium effects

## General approach:

- Calculate dilepton production from current-current correlator (e.g. Gale&Kapusta)

$$E_+ E_- \frac{d^6 R}{d^3 p_+ d^3 p_-} = \frac{2}{(2\pi)^6} \frac{e^2}{k^4} \left[ p_+^\mu p_-^\nu + p_+^\nu p_-^\mu - g^{\mu\nu} (p_+ \cdot p_- + m_l^2) \right] \underline{\text{Im } \Pi_{\mu\nu}^R(k)} \frac{1}{e^{\beta\omega} - 1}$$

“Trivial” QED + kinematics

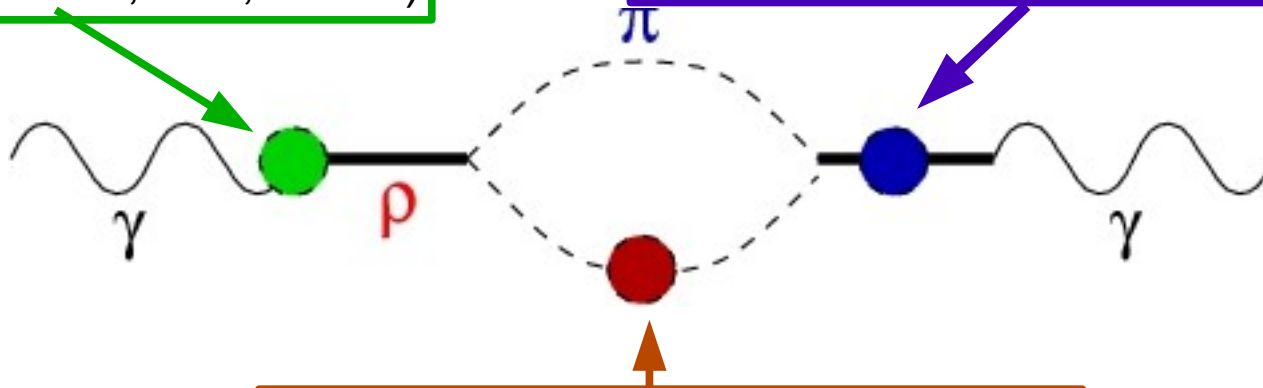
All the good stuff:

- Strong interaction physics
- Manybody physics

# In medium correlator

Coupling of  $\rho$  to photon  
(gauge invariance)  
(Song et al, Harada, Rho, Brown)

Dressing of the  $\rho$  itself  
(s-wave resonances)  
 $a_1$ , baryon resonances (N 1520)  
(Song et al, Friman et al, Mosel et al, Rapp et al)



Dressing of intermediate  
pion states  
(Delta-hole, thermal pions,...)  
(Friman et al, Ko et al, Rapp et al)

# Dressing of the rho

- microscopic calculation of self energy ( C. Song et al, Chanfray et al, Leupold et al,...
  - dominant channel: coupling to N(1520) (Mosel et al)
    - support from photo absorption data
- impulse/low density approximation for rho optical potential (Kapusta et al.)

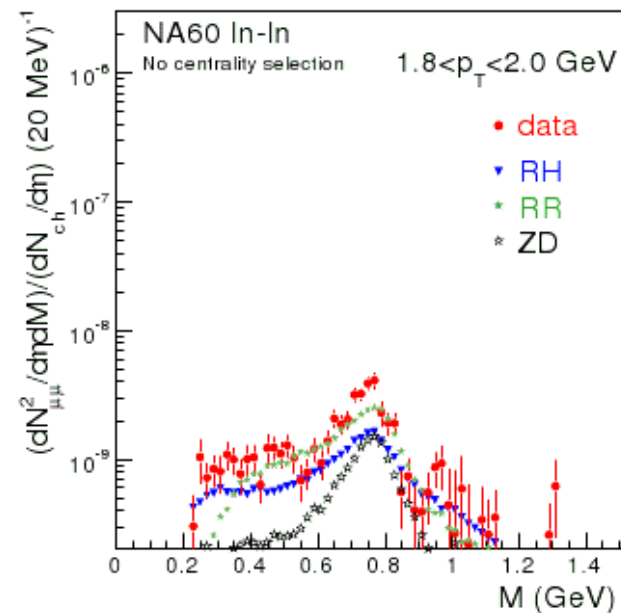
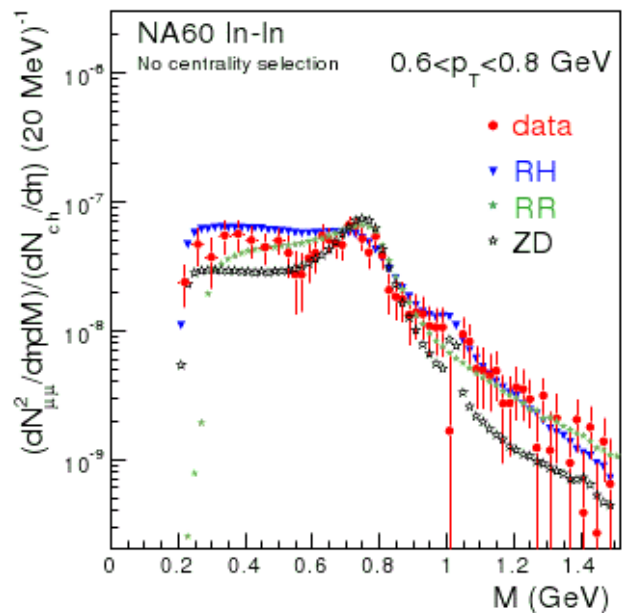
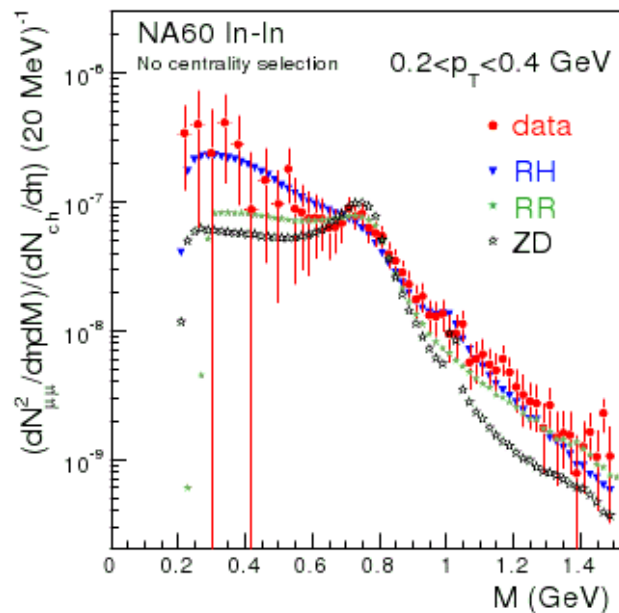
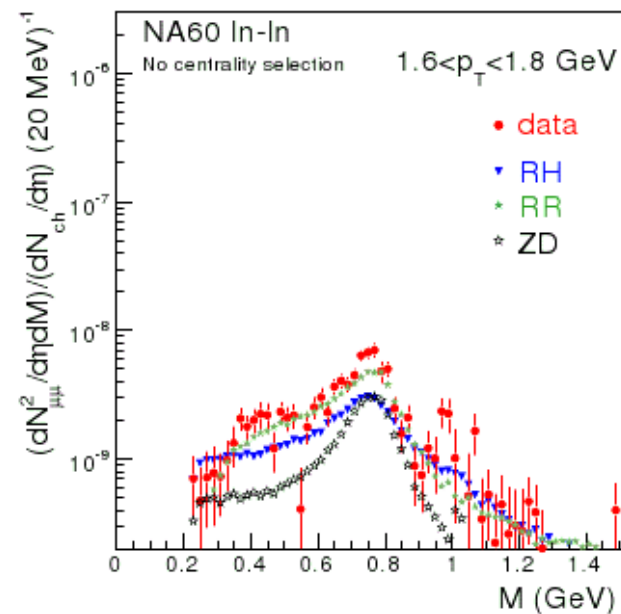
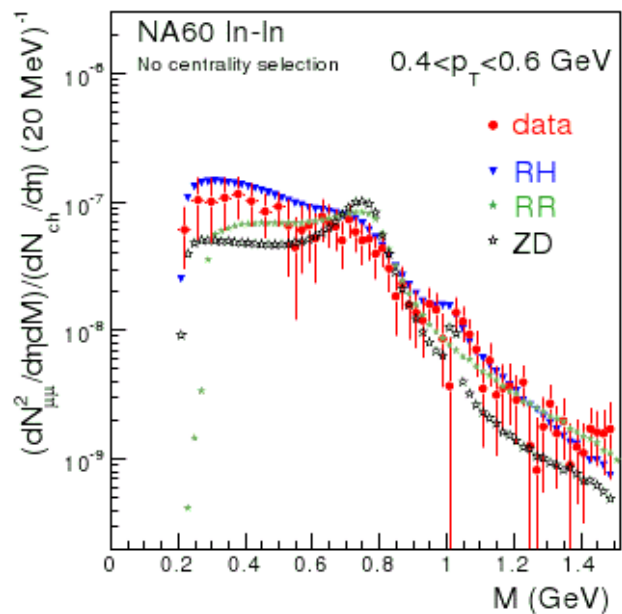
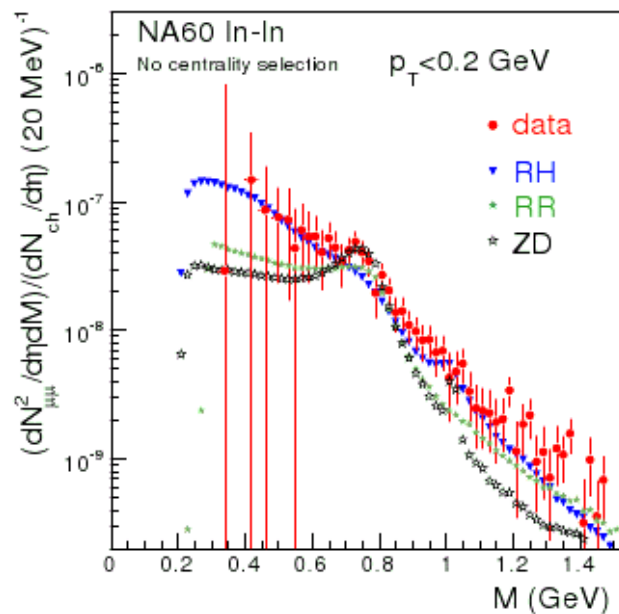
$$\Pi_{ab}(E, \mathbf{p}) = -4\pi \int \frac{d^3 \mathbf{k}}{(2\pi)^3} n_b(\omega) \frac{\sqrt{s}}{\omega} f_{ab}^{(cm)}(s)$$

Non-relativistically::  $\Pi_{ab} = -4\pi f_{ab}^{(b \text{ rest frame})} \rho_b$

# Expansion dynamics

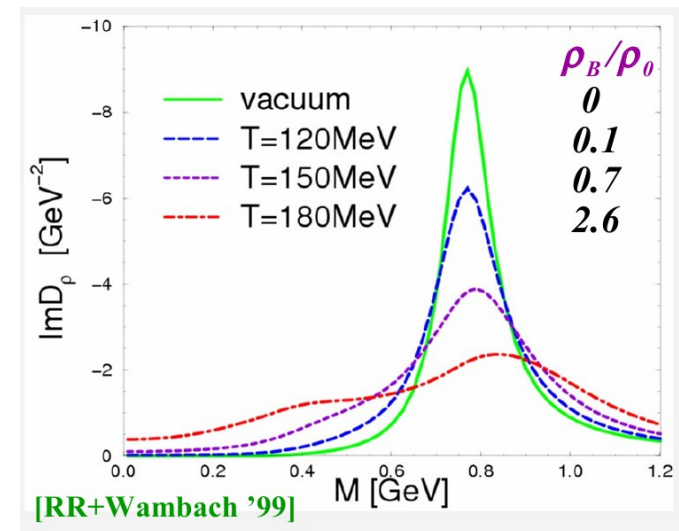
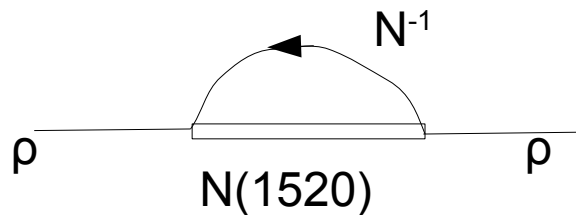
- Fireball, constrained by entropy
  - $V(t), T(t), \mu(t)$
  - constant  $T, \mu, \mu_\pi, \mu_{K,eta,\dots}$  over Volume
  - NO longitudinal flow field
- Hydro (valid at SPS energies ?)
- Transport

# NA 60 favors broadening

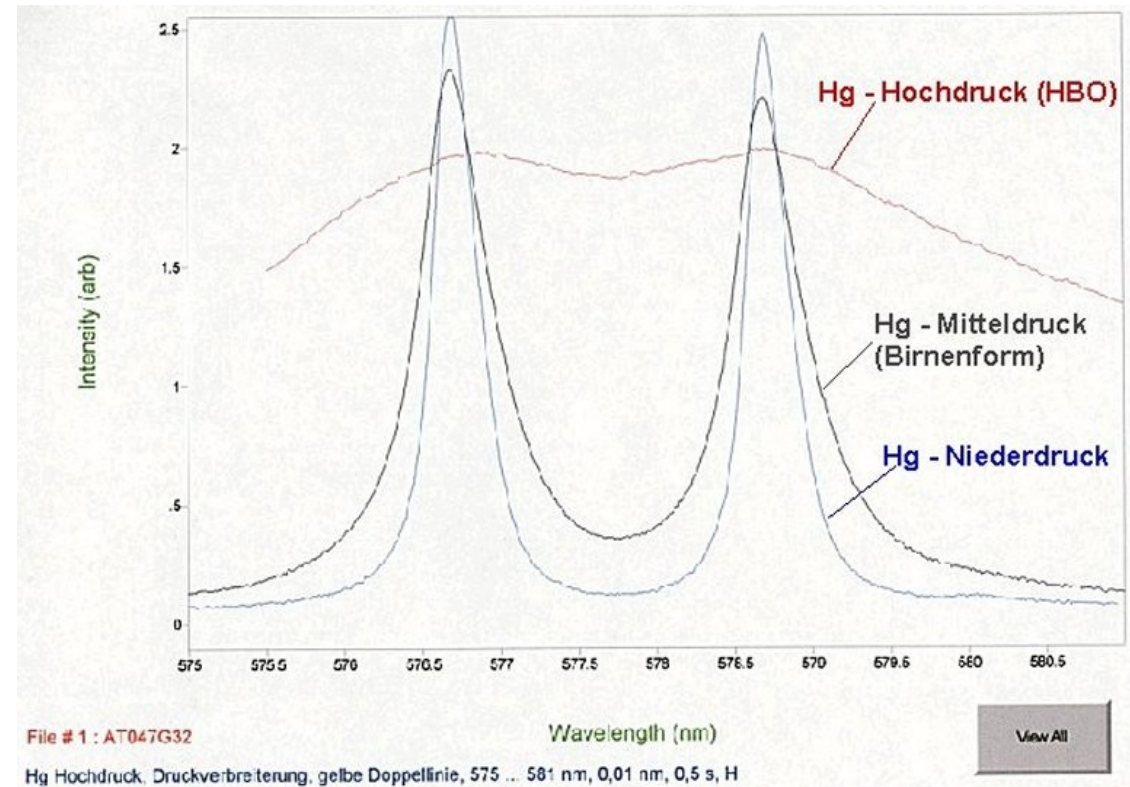


# Melting/Broadening of Resonances

- Deconfinement
- Change of hadronic part of the wave function
  - Example  $\Lambda(1405)$ , rho?
- Mixing with other hadrons
  - Example rho



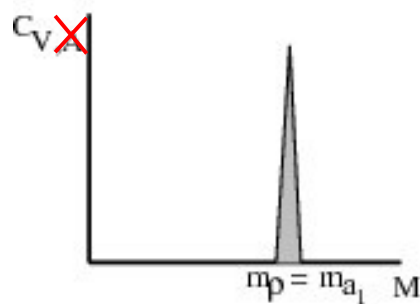
# Broadening of Resonances



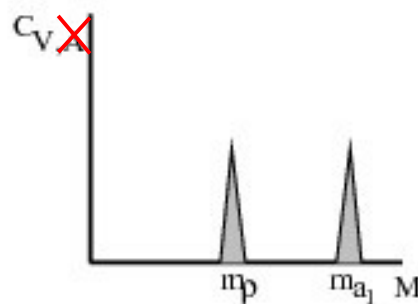
“Chiral restoration” in real life ....

# Low mass dileptons

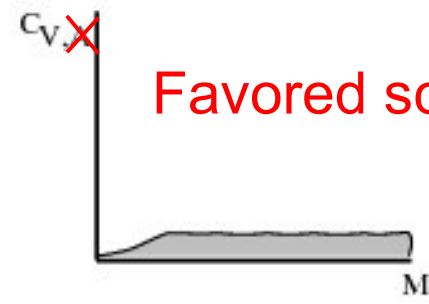
- Well explained by broadening of  $\rho$ 
  - Baryons are essential
- Dropping masses dis-favored
- What about chiral symmetry?



(1)



(2)



(3)



# Closing the deal

- Are we done ? SPS RHIC (PHENIX?) described by in medium spectral function
- HADES? Looks as if resonances play important role (see Tetayana's talk)
- What do we need to declare success?
  - Expansion dynamics controlled
  - Channels controlled
  - Are we treating the resonances correctly?
  - Re-tune spectral function approach to incorporate p-p, p-A, pi-N ....

# Resonance $\rightarrow N\rho$ Branching Ratios

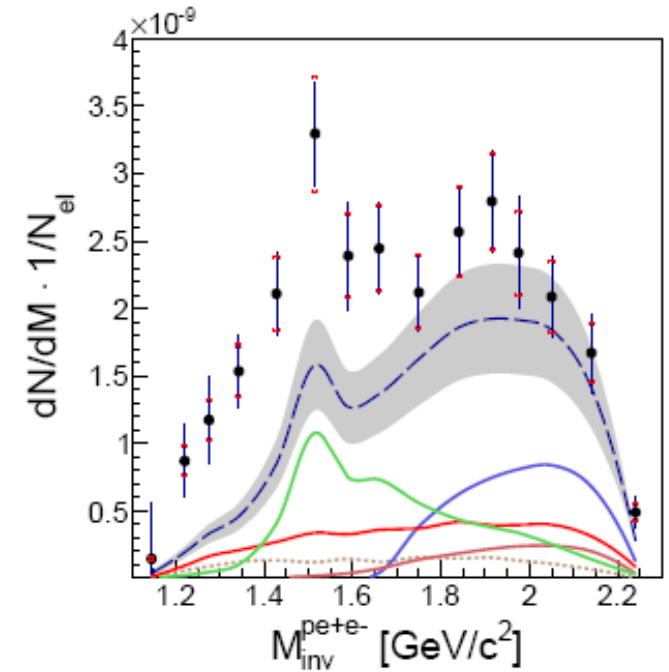
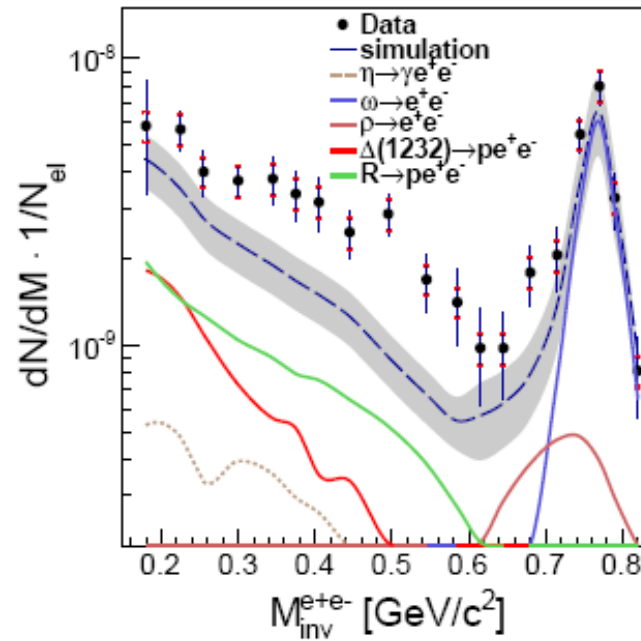
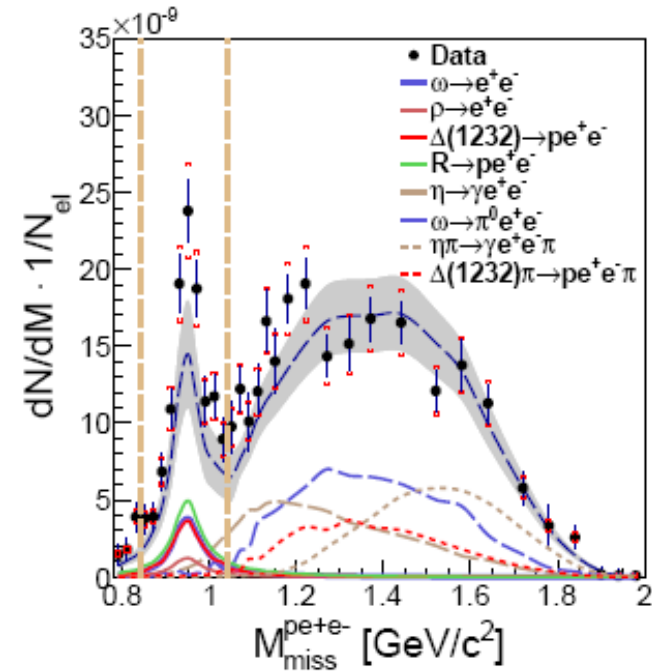
	GiBUU12	UrQMD09	KSU12	KSU92	BnGa12	CLAS12	PDG12	
$N(1520)3/2^-$	21	15	20.9(7)	21(4)	10(3)	12.7(4.3)	20(5)	D13
$N(1720)3/2^+$	87	73	1.4(5)	87(5)	10(13)	47.5(21.5)	77.5(7.5)	P13
$\Delta(1620)1/2^-$	29	5	26(2)	25(6)	12(9)	37(12)	16(9)	S31
$\Delta(1905)5/2^+$	87	80	<6	86(3)	42(8)		>60	F35

Partial courtesy of Piotr Salabura, Sept 2013

**CLAS12:** V. Mokeev *et al*, Phys Rev C **86**, 035203 (2012); V. Mokeev, PC  
**BnGa12:** A.V. Anisovich *et al*, Eur Phys J A **48**, 15 (2012)  
**GiBUU12:** J. Weil *et al*, Eur Phys J A **48**, 111 (2012); J. Weil, PC  
**KSU92:** D.M. Manley and E.M. Saleski, Phys Rev D **45**, 055203 (1992)  
**KSU12:** M. Shrestha and D.M. Manley, Phys Rev D **86**, 055203 (2012)  
**PDG12:** J. Beringer *et al* [RPP] Phys Rev D **86**, 010001 (2012)  
**UrQMD09:** K. Schmidt *et al*, Phys Rev C **79**, 4002 (2009)

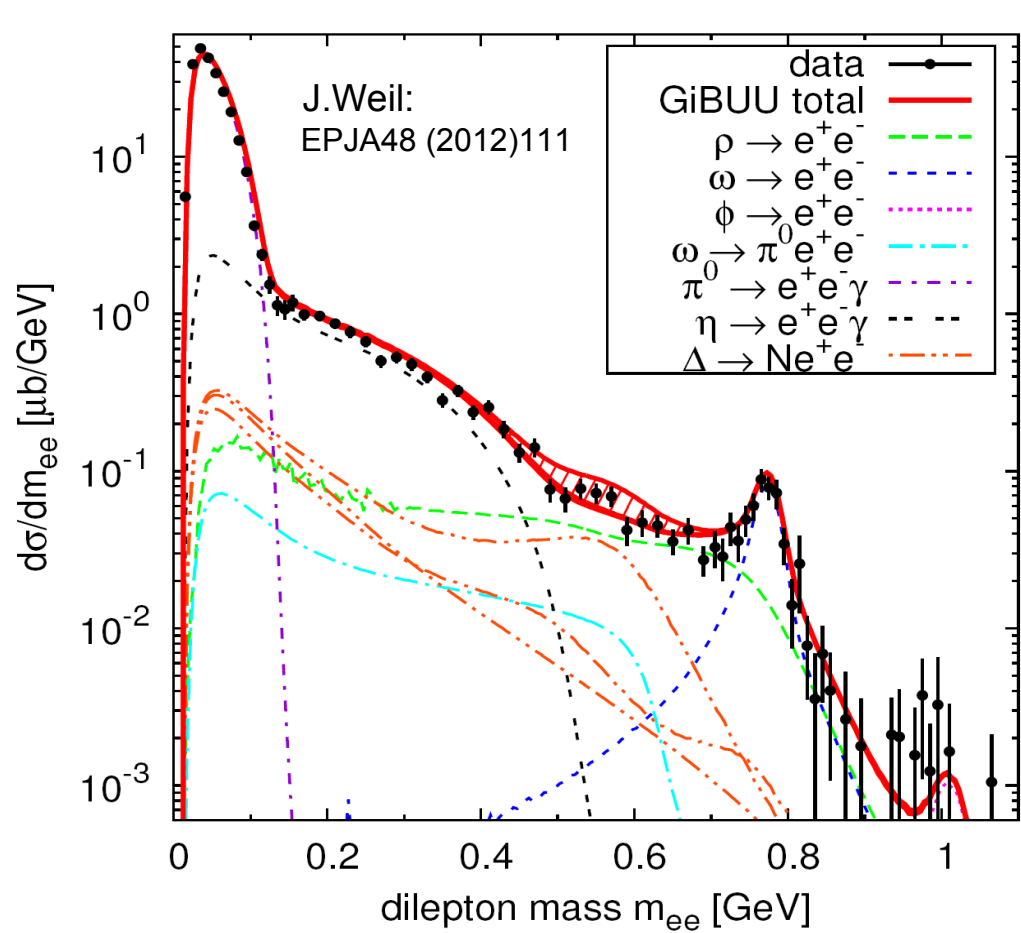
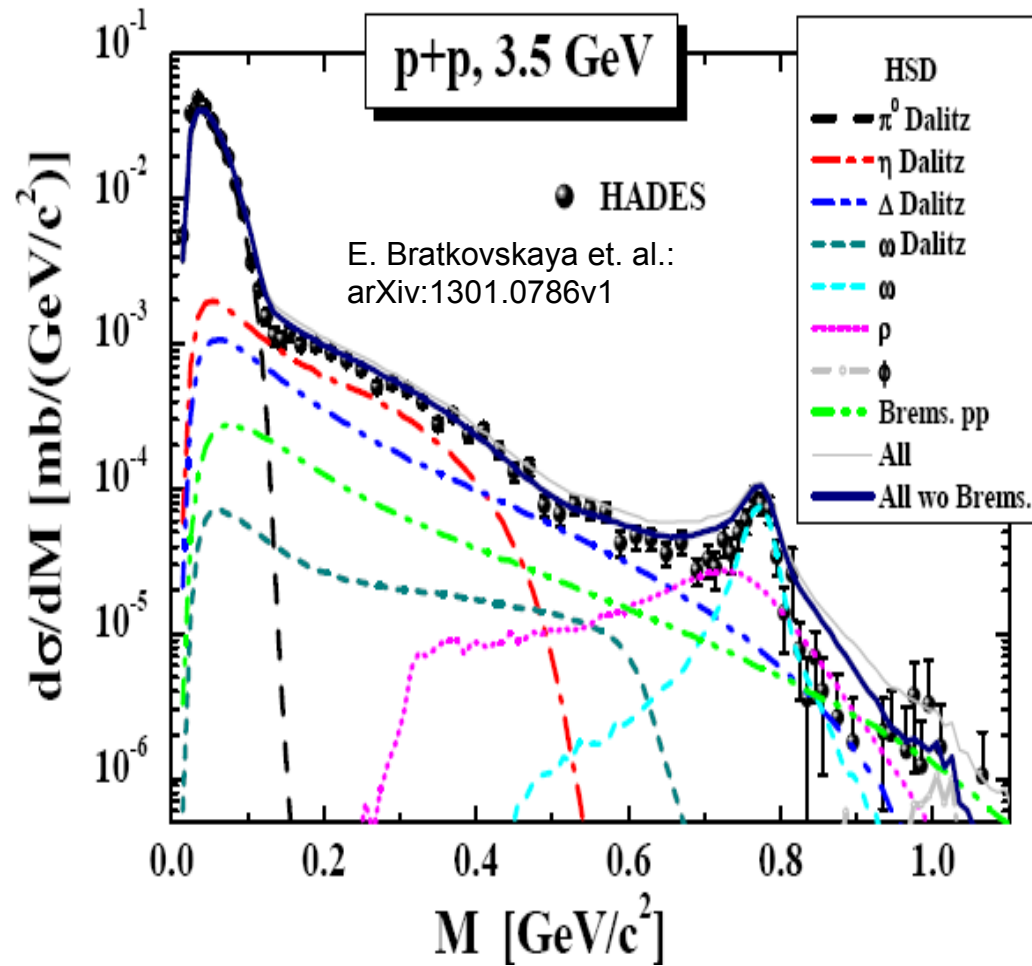
# Results for ppe+e- channel

„QED” : point like  $R \rightarrow N\gamma^*$  vertex



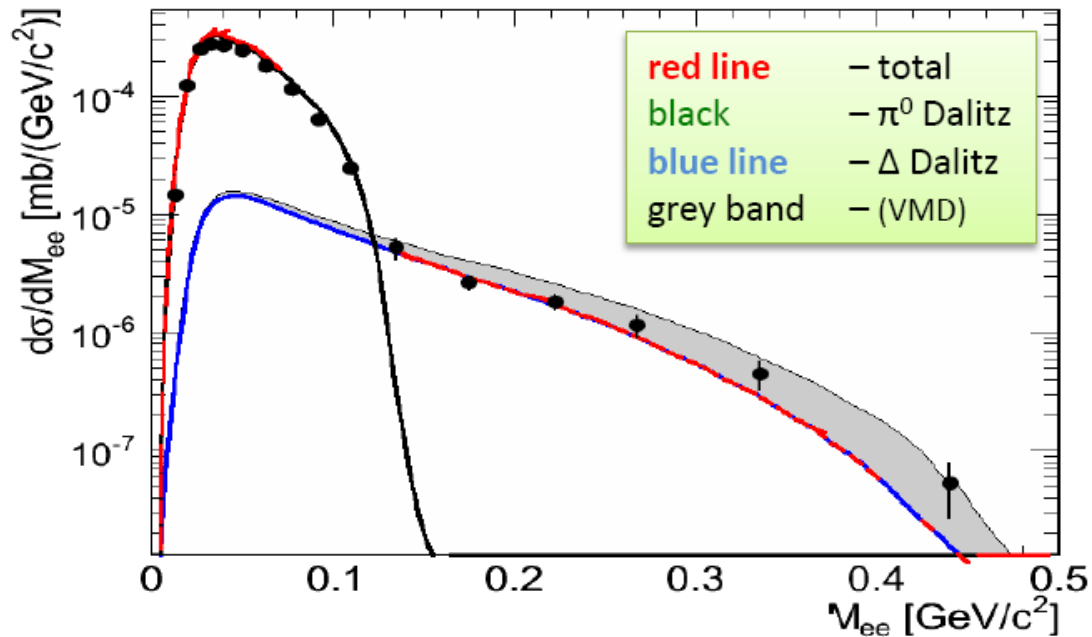
- Significant contribution from higher (than  $\Delta$ ) mass resonances
- Additional strength below VM pole needed – off shell  $\rho$  meson coupling ! – extended interaction vertex
- low mass resonances :  $\Delta(1232)$ ,  $N(1440)$ ,  $N(1520)$  ?

# e+e- sources in pp @ 3.5 GeV



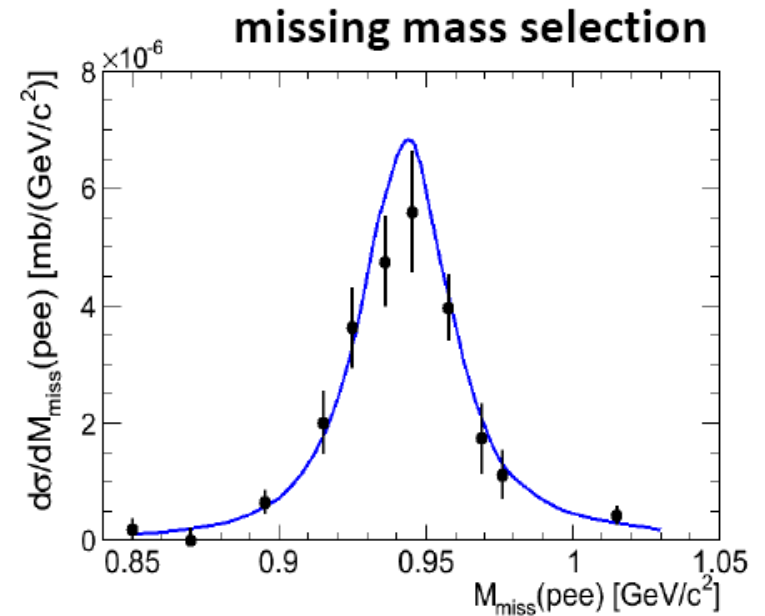
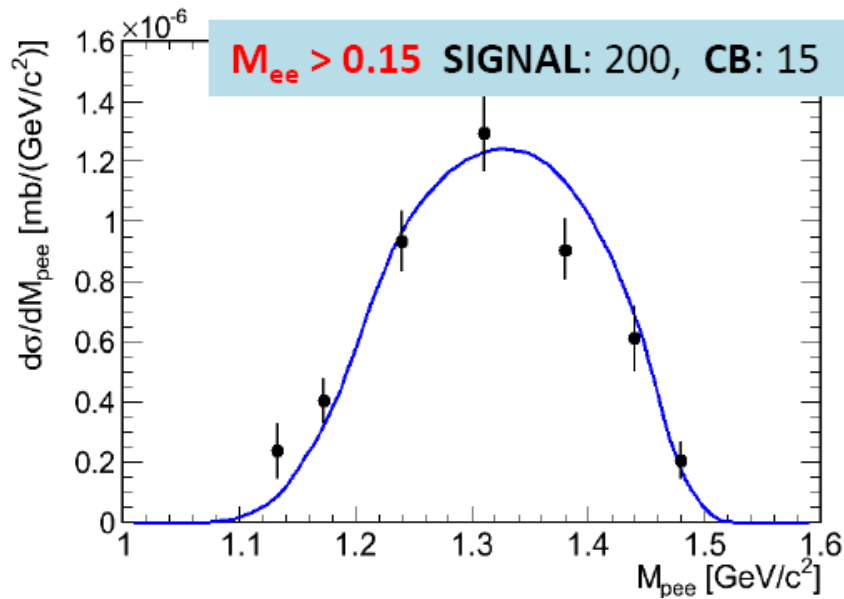
- Many uncertainties: inclusive cross sections  $\pi$ ,  $\Delta$ ,  $\eta$ ,  $\omega/\rho$  (fixed now by HADES)  
 $\Delta \rightarrow \pi e^+e^-$  transition (Dalitz decay); rates, em. Transition Form-Factors  
 $\rho$  - spectral function !

# $p+p \rightarrow p\Delta^+ \rightarrow p\ p e^+e^-$ Dalitz decay

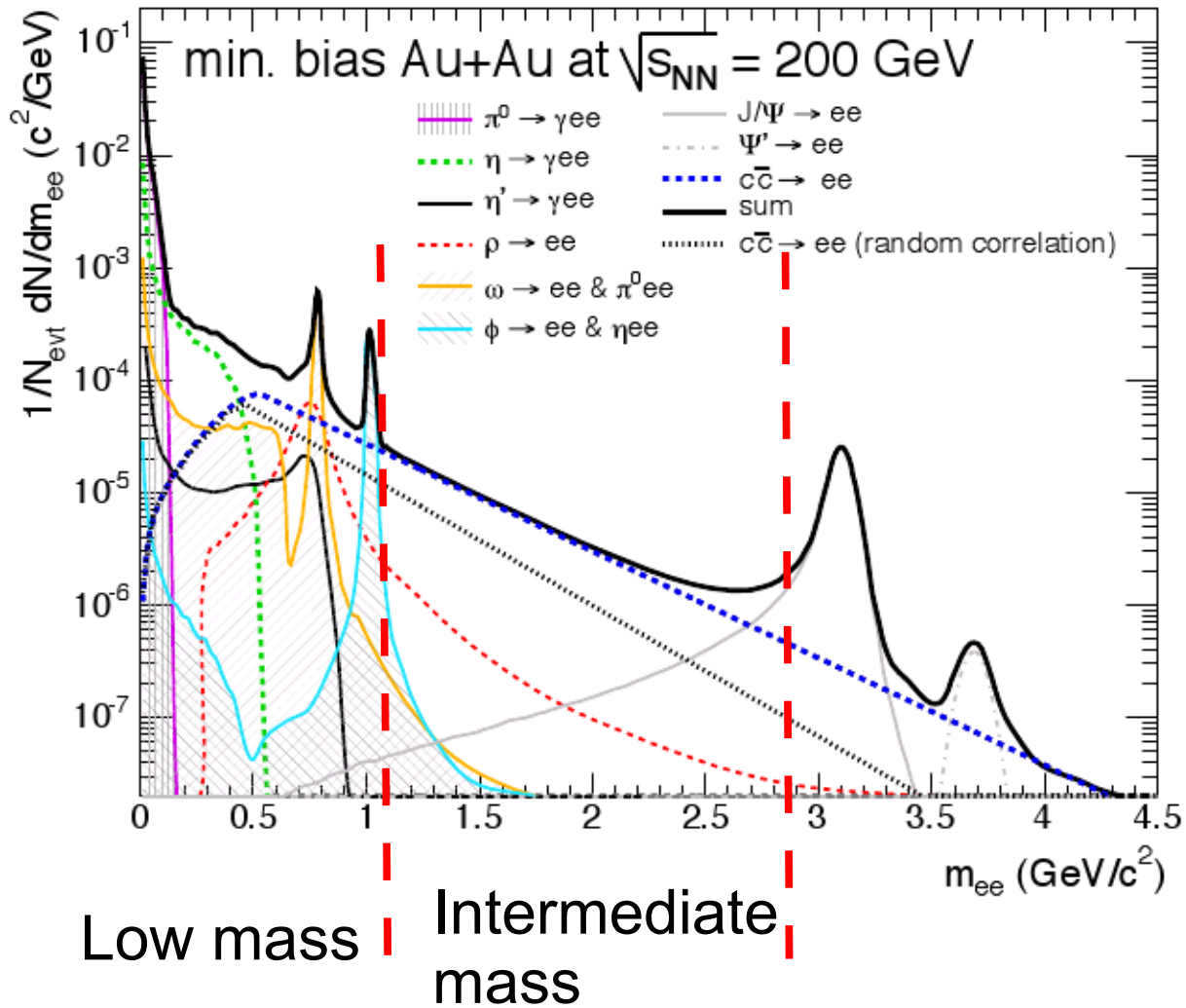


Mass distributions

$G_M(q^2)$  impact moderate



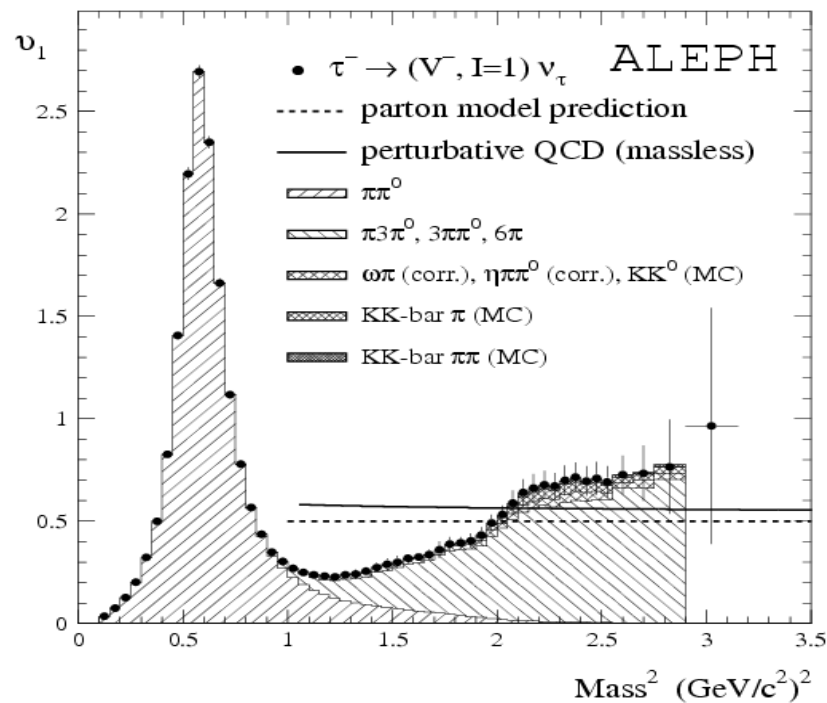
# Intermediate mass



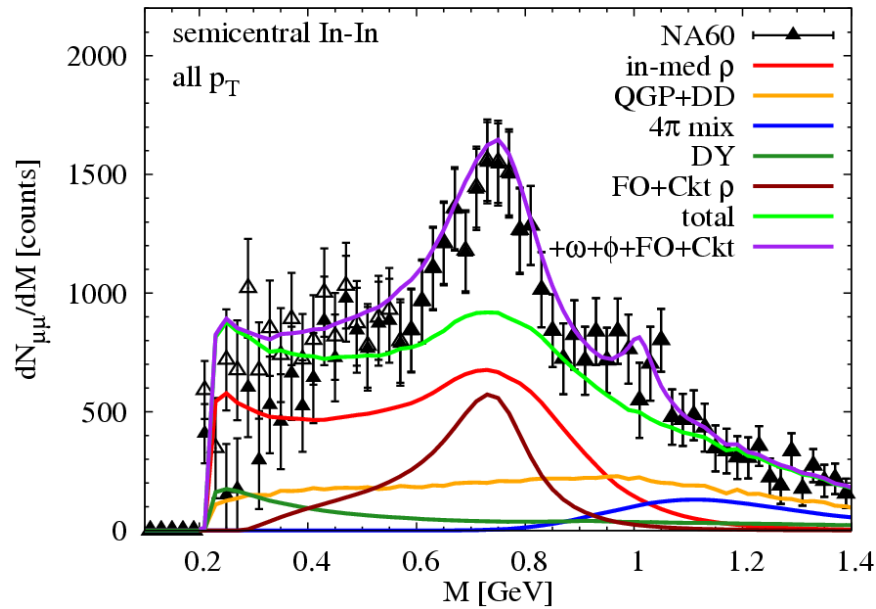
Thanks to  
T. Ullrich

# Intermediate mass

- Contributions from both q-qbar and multi-pion ( $a_1$  etc) channels
  - Can we disentangle this?



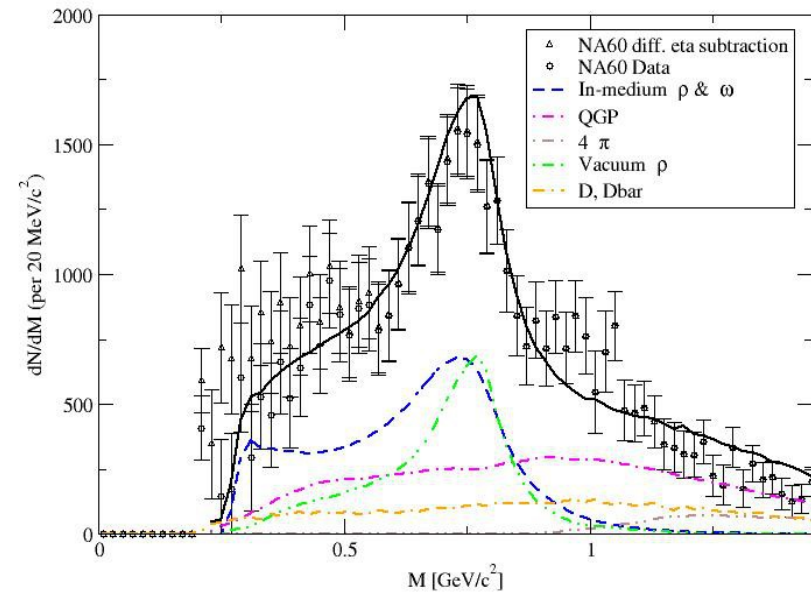
# Intermediate Mass $M > 1 \text{ GeV}$



van Hess, Rapp

“multi pion”

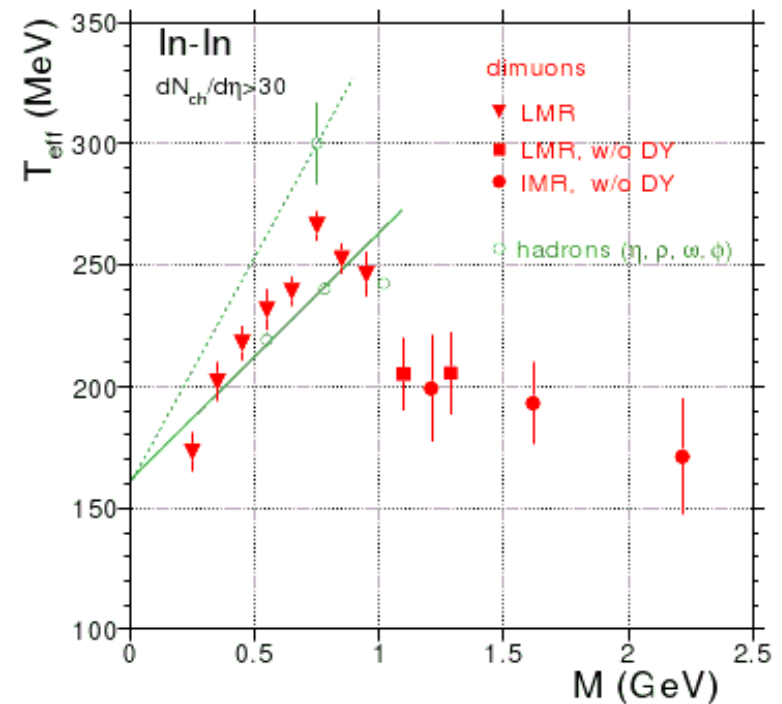
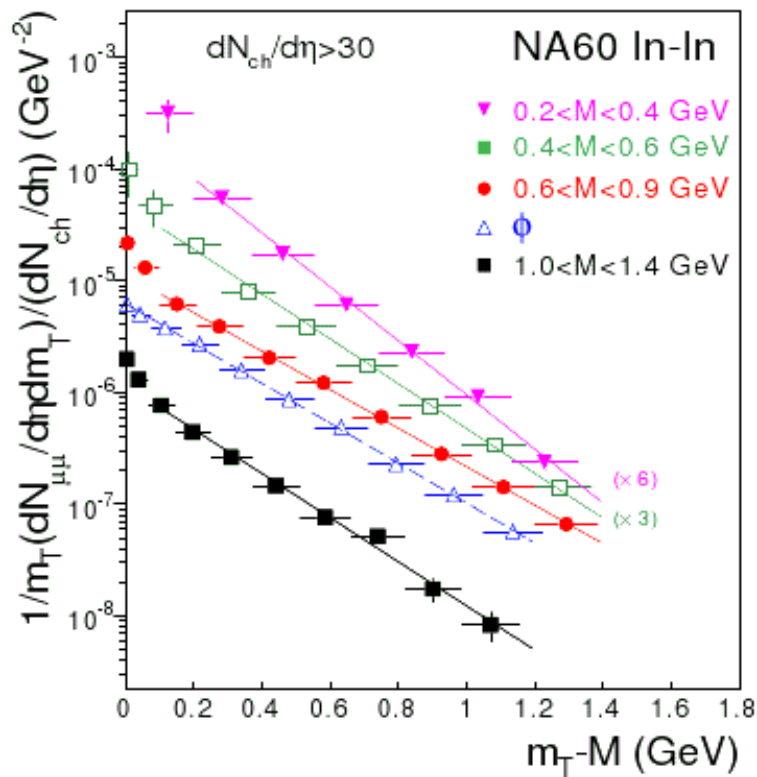
vs



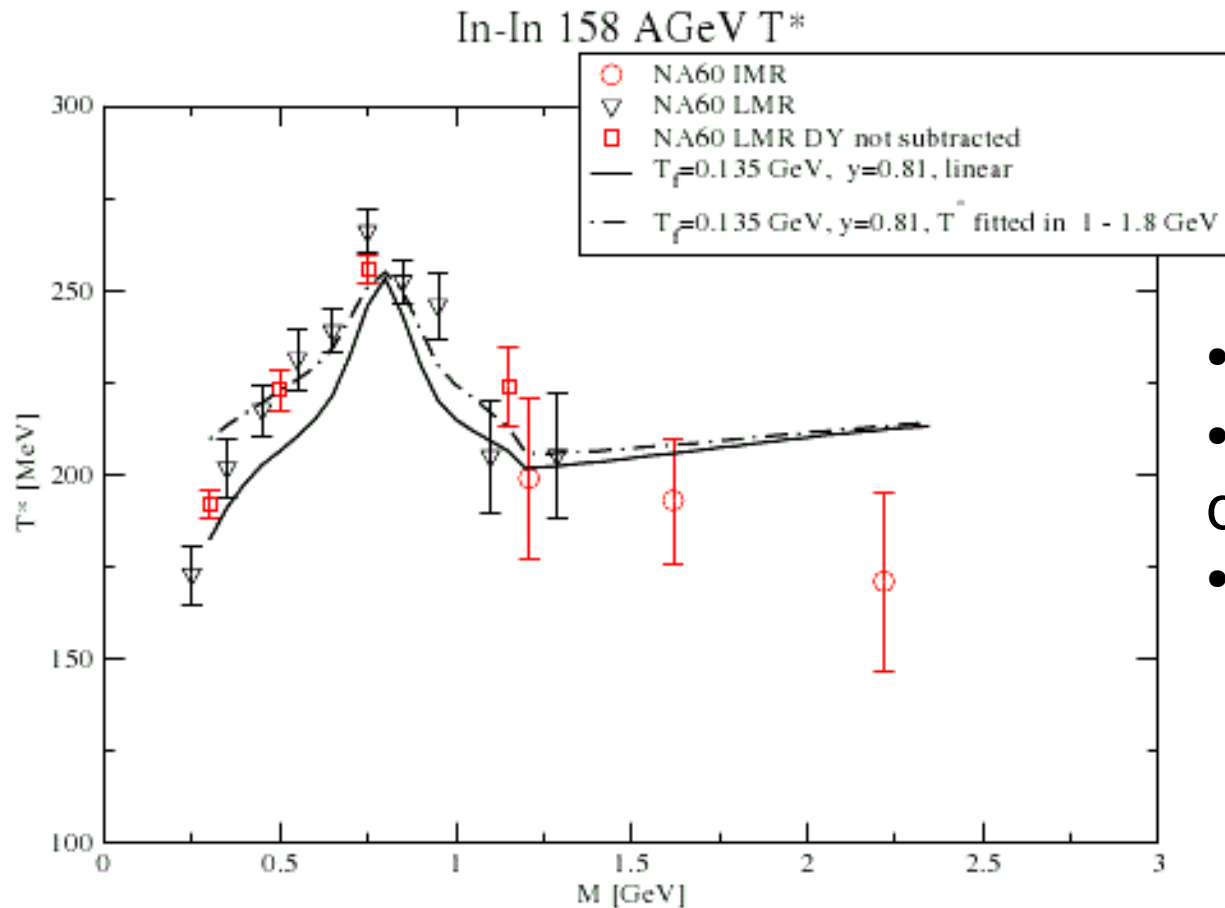
Renk,  
Rupert  
QGP



# NA60 $p_t$ slopes

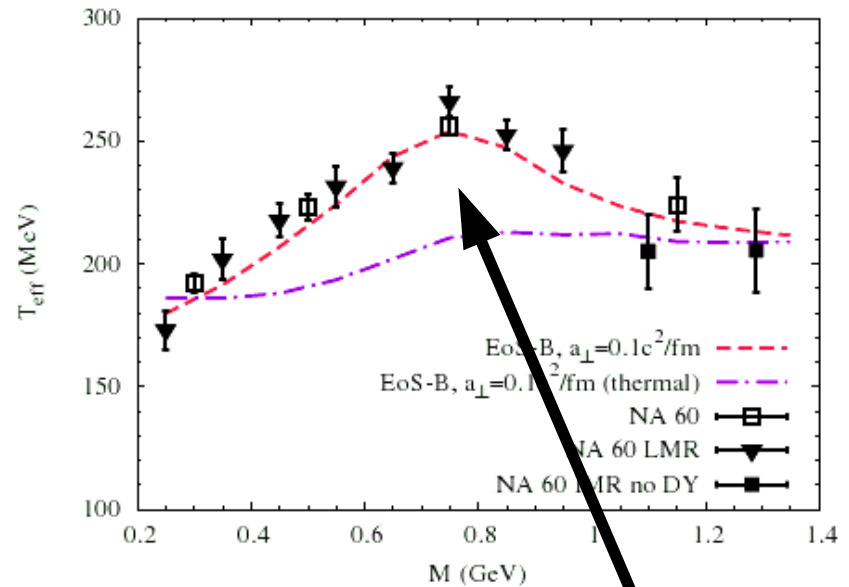
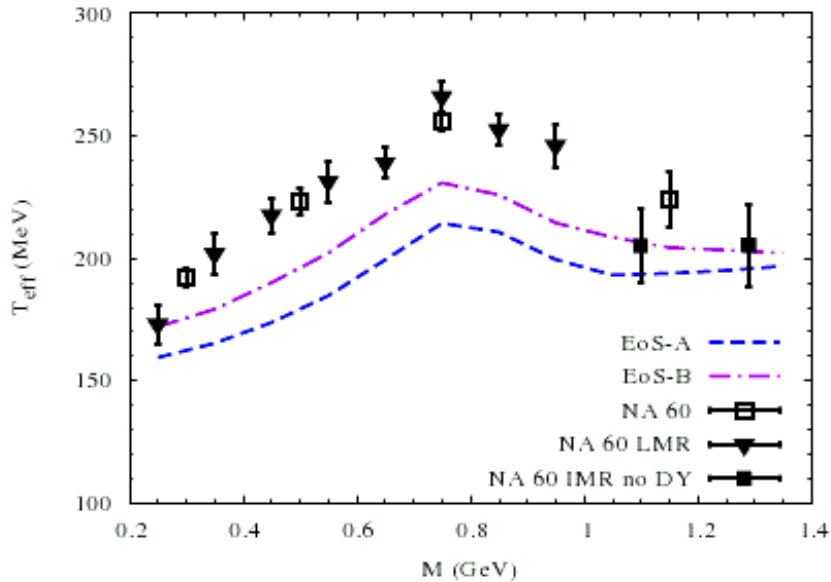


# Renk, Ruppert et al



- Deviation for  $p_t < 1$  GeV
- $M > 1$  GeV dominated by  $q$ - $\bar{q}$
- initial high Temp is essential

# van Hees and Rapp



Data can be reproduced with:

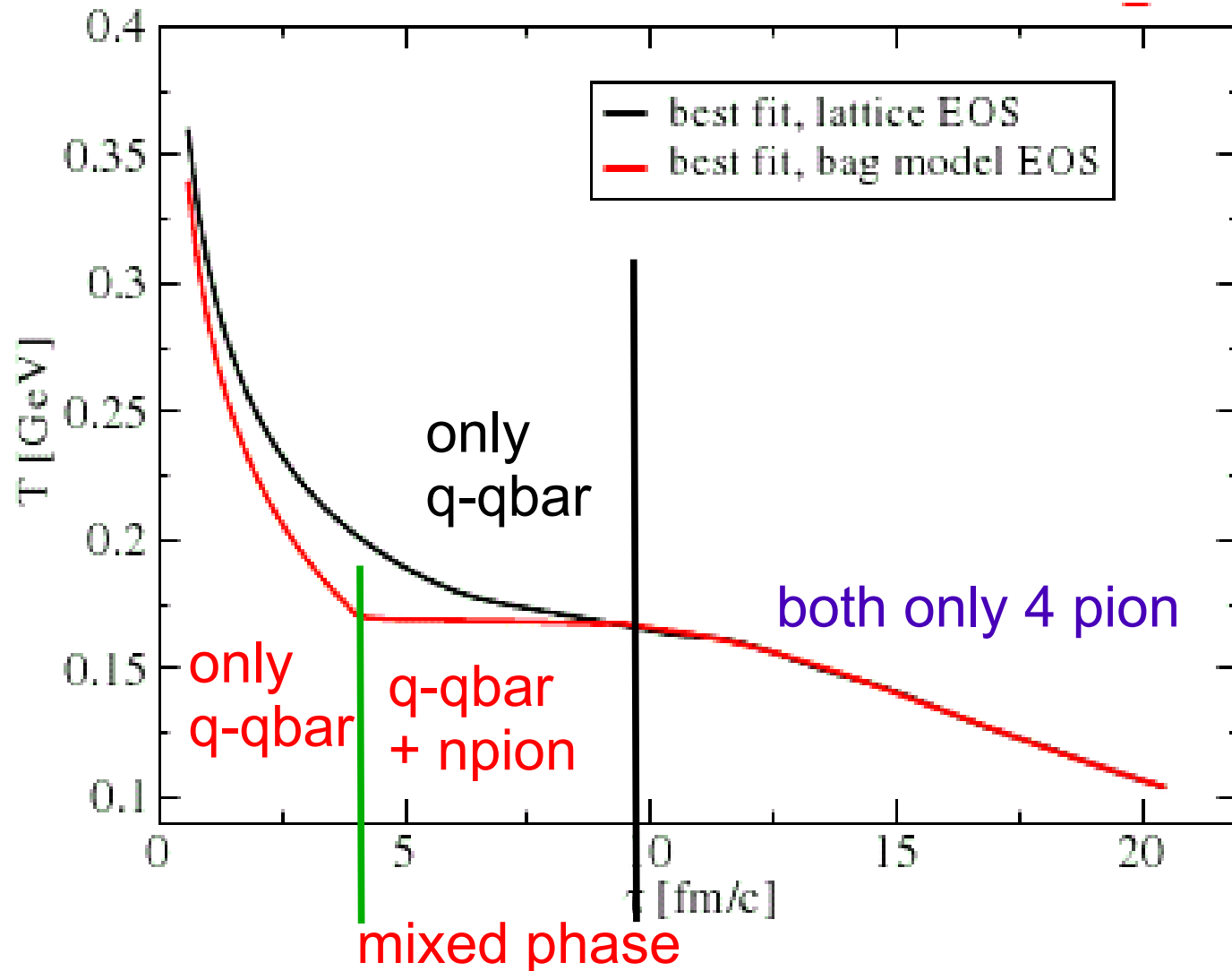
- **primordial** rho-meson
- increased initial acceleration
- EOS with low  $T_c=160$  MeV (EOS B)

Primordial (“hard”) rho  
absolutely essential

(equivalent hard *pion*  
equally important for  
pion spectrum)

# Expansion dynamics and intermediate mass

T. Renk

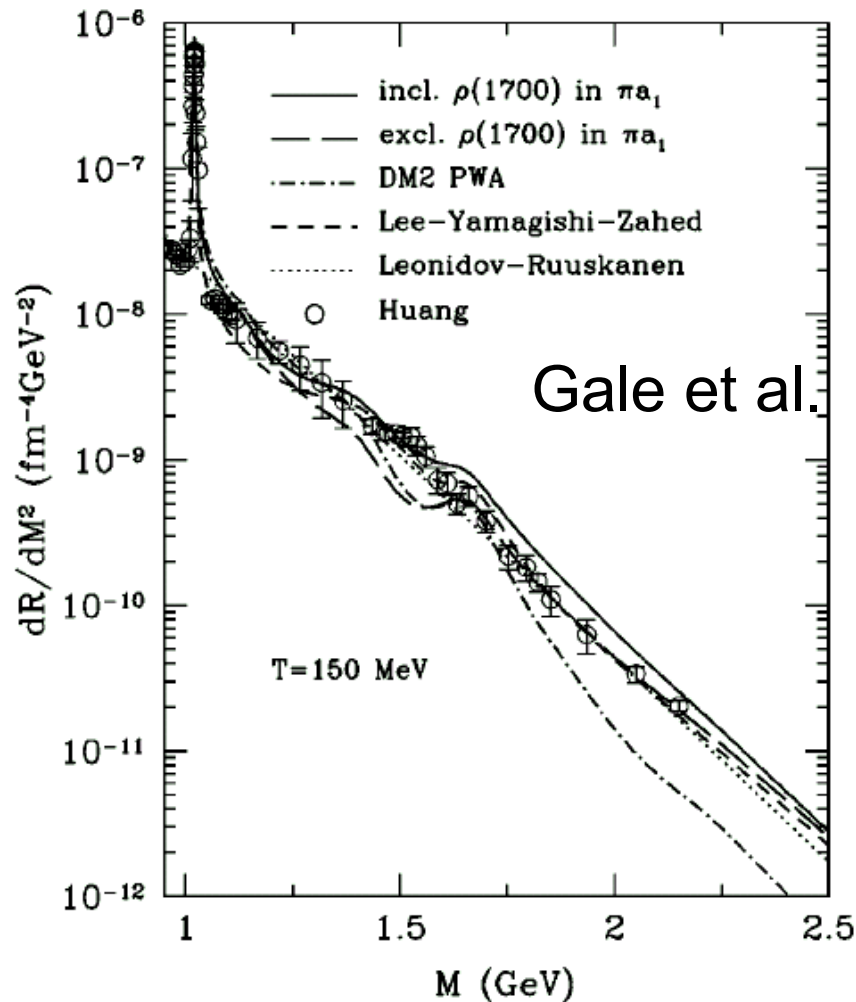


# So what is it?

q-q\_bar annihilation ?

Multi-pion hadronic reactions?

# Meet Bob (aka Duality)



Rate(QGP) = Rate(Hadrons) = **Bob**

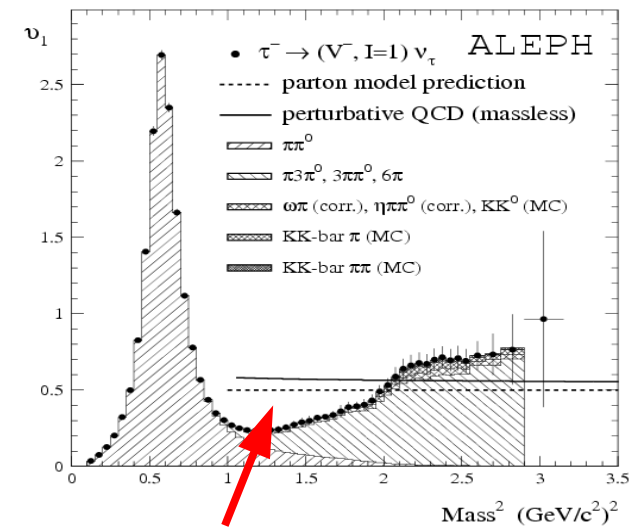
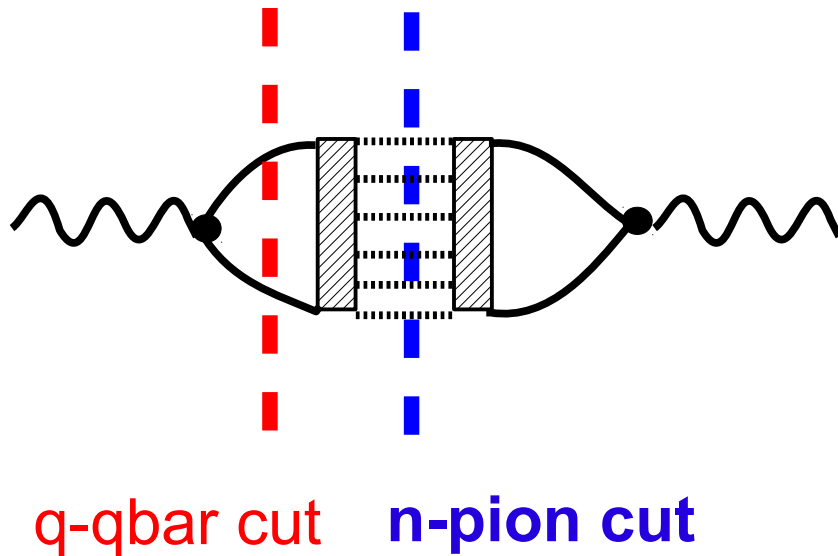
Renk, Rupert et al: **Bob Q-qbar**

Van Hees and Rapp: **Bob Multipion**

# Duality

$$E_+ E_- \frac{d^6 R}{d^3 p_+ d^3 p_-} = \frac{2}{(2\pi)^6} \frac{e^2}{k^4} \left[ p_+^\mu p_-^\nu + p_+^\nu p_-^\mu - g^{\mu\nu} (p_+ \cdot p_- + m_1^2) \right] \text{Im} \Pi_{\mu\nu}^R(k) \frac{1}{e^{\beta\omega} - 1}$$

Extract from  $e^+e^-$  or tau-decay data  
(Z. Huang PLB 95)

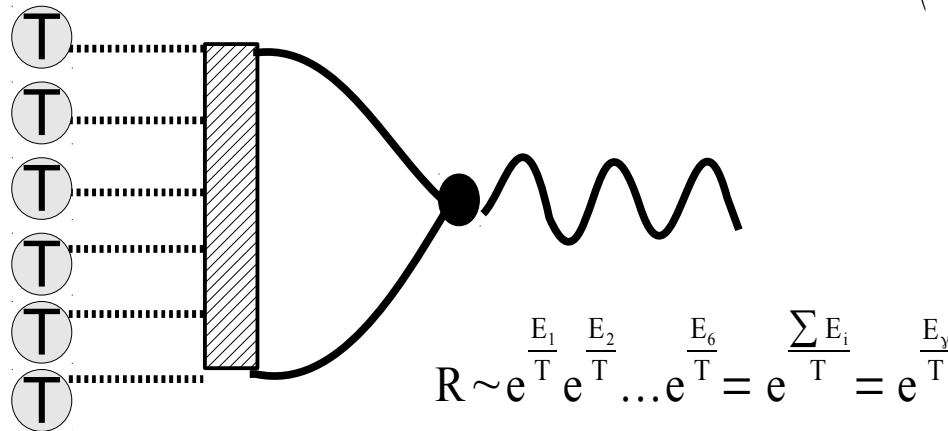


Location of break  
in  $p_t$ -slopes

# Production Rate

$$\frac{dR}{d^4q} \sim \int d^3 p_1 \dots d^3 p_n |M(p_1, \dots, p_n; e^+ e^-)|^2 f(p_1) \dots f(p_n) \delta^4(p_1^\mu + \dots + p_n^\mu - q^\mu)$$

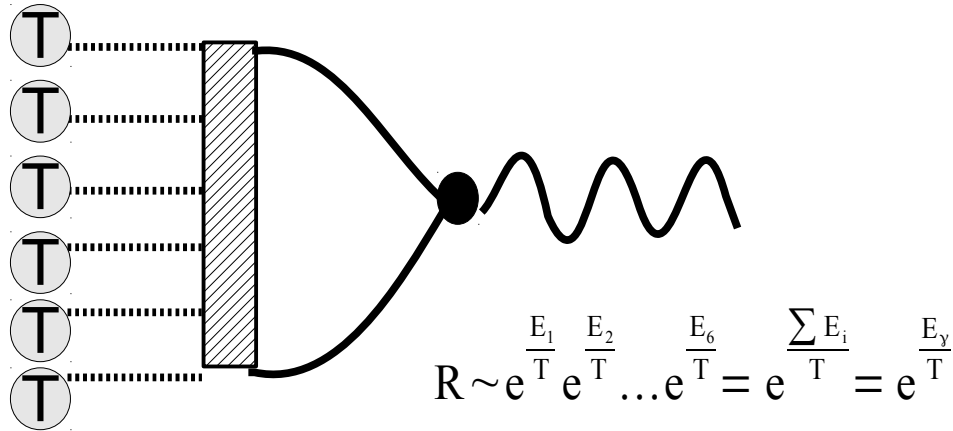
$$f(p) \sim \exp\left(\frac{-E(p)}{T}\right)$$



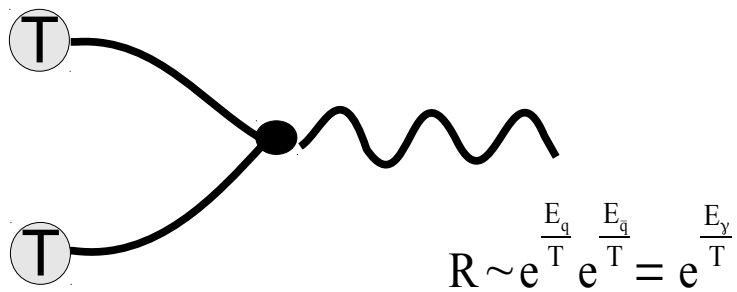


# Duality

n-pion



q-qbar



# Dilepton and the QCD CP

- Massless “modes” at CP since it is a second order phase transition
- Mode is mixture of “sigma” and “omega”
- However these may likely be space-like modes
  - $M^2 \rightarrow 0^-$

# Nambu model

(Fuji et al, hep-ph/0401028,0403039)

Sigma remains massive at CP; CP driven by **spacelike** p-h excitations

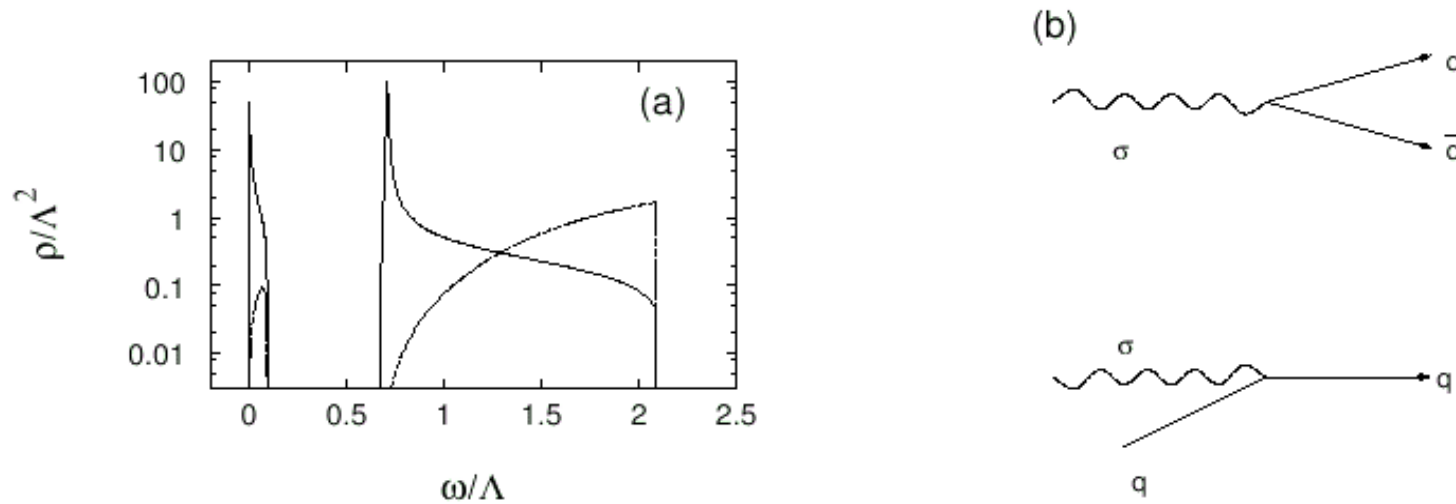


Fig. 2. (a) Spectral function in the scalar channel (solid) with  $|\mathbf{q}|/\Lambda = 0.1$  at a CEP with  $m/\Lambda = 0.01$ . The free gas spectrum (dashed) is also shown for reference. (b) Typical processes contributing to the spectrum.

# Nambu model p-h excitations

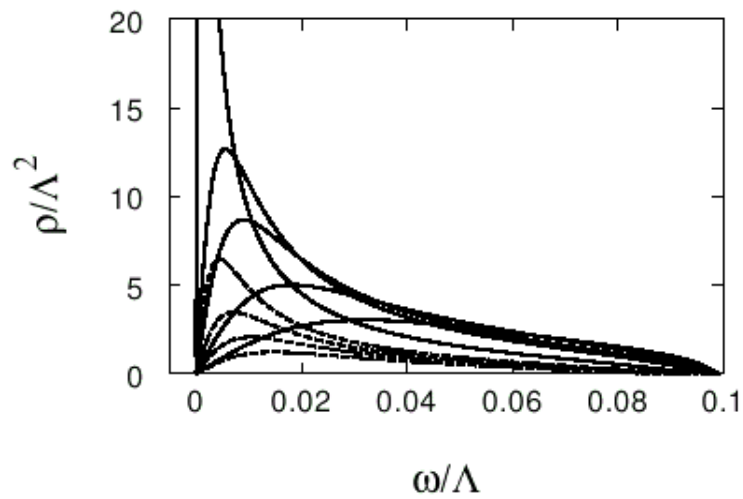
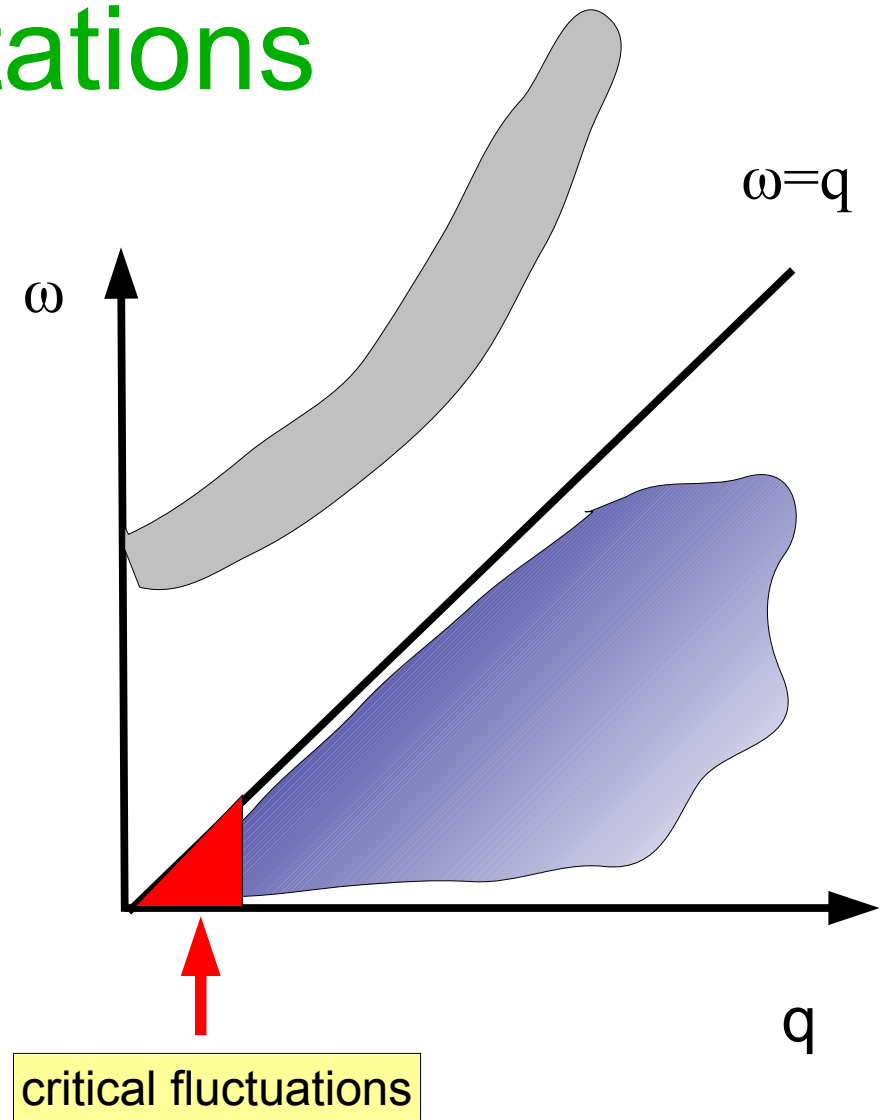


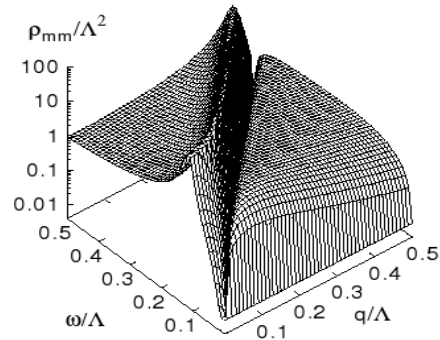
Fig. 3. Spectral function in the spacelike momentum region with  $|\mathbf{q}|/\Lambda = 0.1$ ,  $T = T_c$  and  $m/\Lambda = 0.01$  for several  $\mu$  (see text).



# CP is and the chiral transition

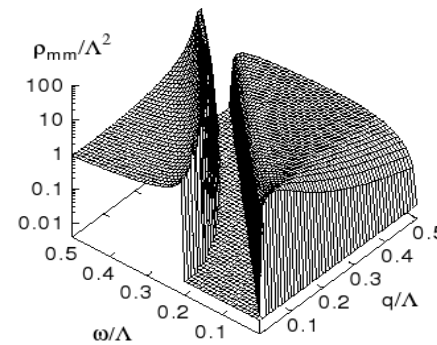
Chiral transition  $m_q=0$

$T > T_c$



(a)

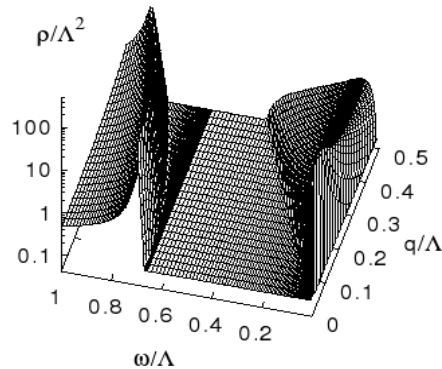
$T < T_c$



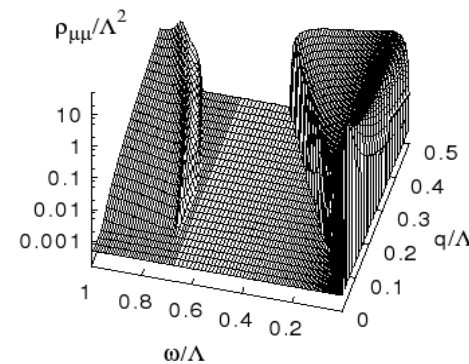
(b)

Critical point  $m_q > 0$

Massive Scalar



Scalar



Vector (Baryon-density)

# Dileptons and Critical Point

- Not accessible since fluctuations are space-like
- Same for charge fluctuations!
- May provide model constraints
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# The Dilepton production landscape

