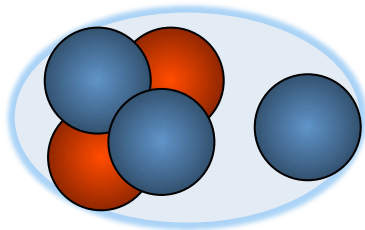


Studying nuclei at the dripline and unbound nuclei

NUSTAR Week 2013
University of Helsinki (Kumpula Campus)
October 10, 2013

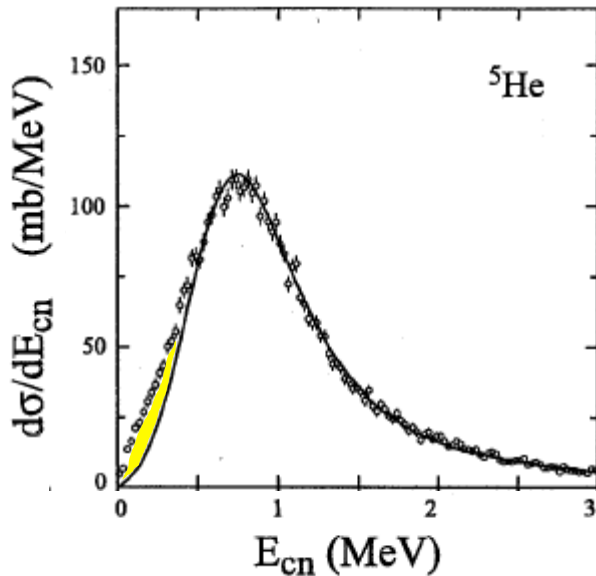
Jürgen

^3He	^4He	^5He unbound	^6He 808 ms	^7He unbound	^8He 119 ms	^9He unbound	^{10}He unbound
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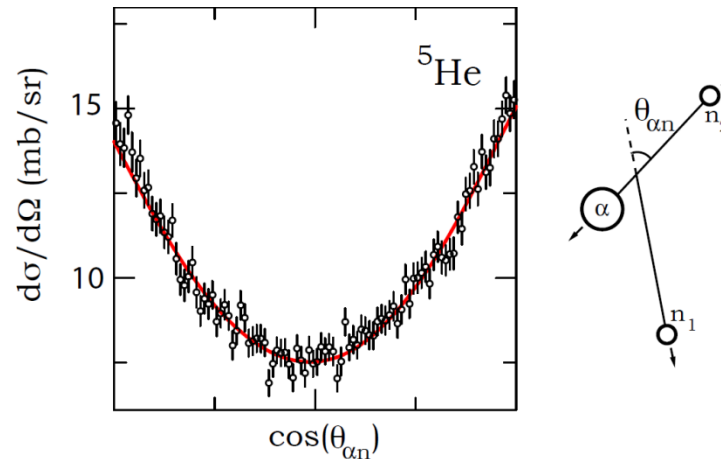


$$^6\text{He} : ^4\text{He} \otimes (\nu p_{3/2})^2$$

K. Markenroth *et al.*, NPA **679** (2001) 462



$$(\mathbf{p}_n = -\mathbf{p}_f)$$

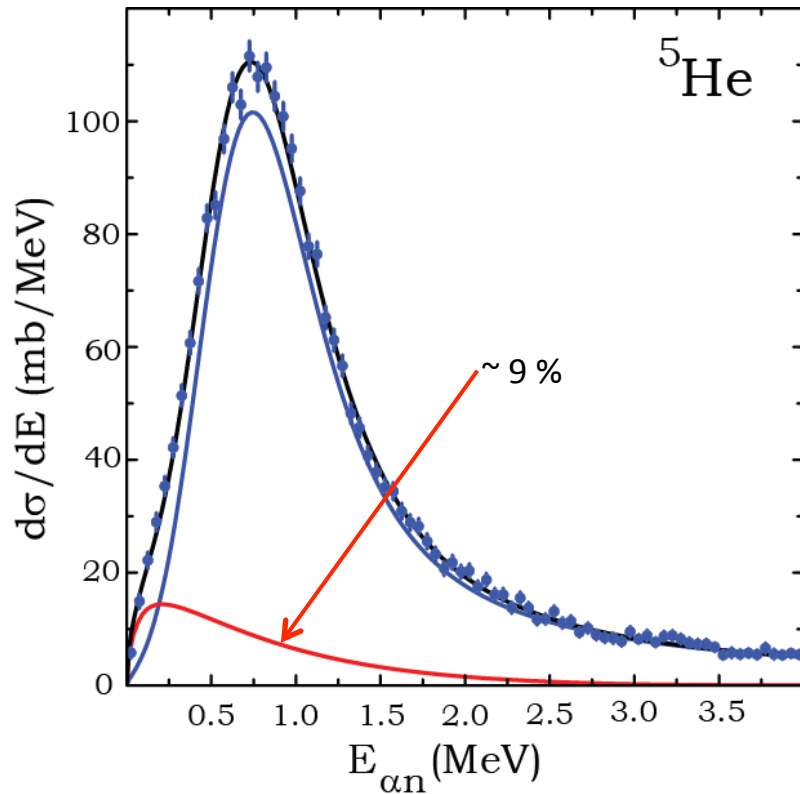


L.V. Chulkov *et al.*, PRL **79** (1997) 201

$$W(\theta_{\alpha n}) = 1 + 1.5 \cos^2(\theta_{\alpha n})$$

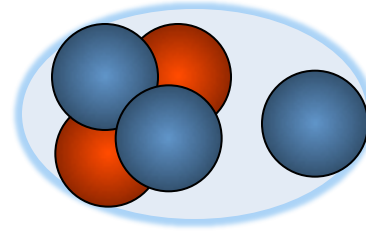
$$(p_{1/2})^2 \sim 7\%$$

L.V. Chulkov, G. Schrieder, Z. Phys **A359** (97) 231



Yu. Aksyutina et al., PLB **679** (2009) 191

$$\begin{aligned}
 k &= \sqrt{2\mu\varepsilon} \\
 \varepsilon &= 0.94(23) \text{ MeV} \\
 a &= 3.37(38) \text{ fm}
 \end{aligned}$$



$$\frac{d\sigma}{dE_{fn}} \propto \frac{\Gamma_l(E_{fn})}{[E_r + \Delta_l(E_{fn}) - E_{fn}]^2 + \frac{1}{4} \Gamma_l^2(E_{fn})}$$

s-wave: Effective-range approximation

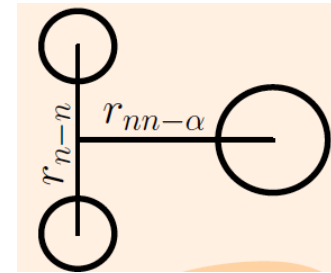
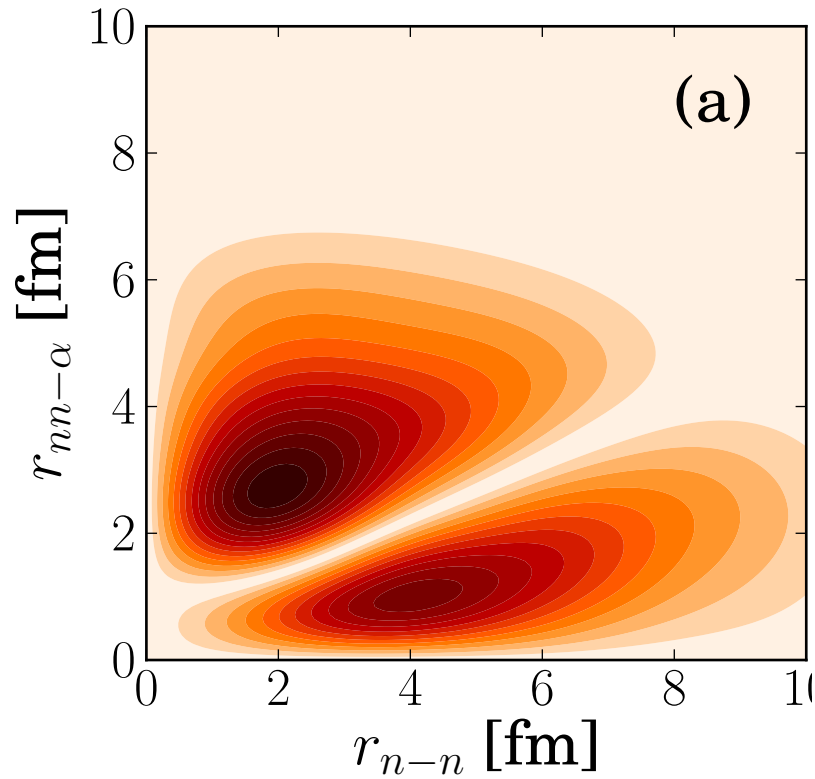
$$\begin{aligned}
 \frac{d\sigma}{dE_{fn}} &\propto p_{fn} \left[\frac{1}{k^2 + p_{fn}^2} \right]^2 \left[\cos(\delta) + \frac{k}{p_{fn}} \sin(\delta) \right]^2 \\
 p_{fn} \cot(\delta) &= -\frac{1}{a} + \frac{1}{2} r_0 p_{fn}^2 + O(p_{fn}^4)
 \end{aligned}$$

Bertch et al., PRC **57** (1998) 1366

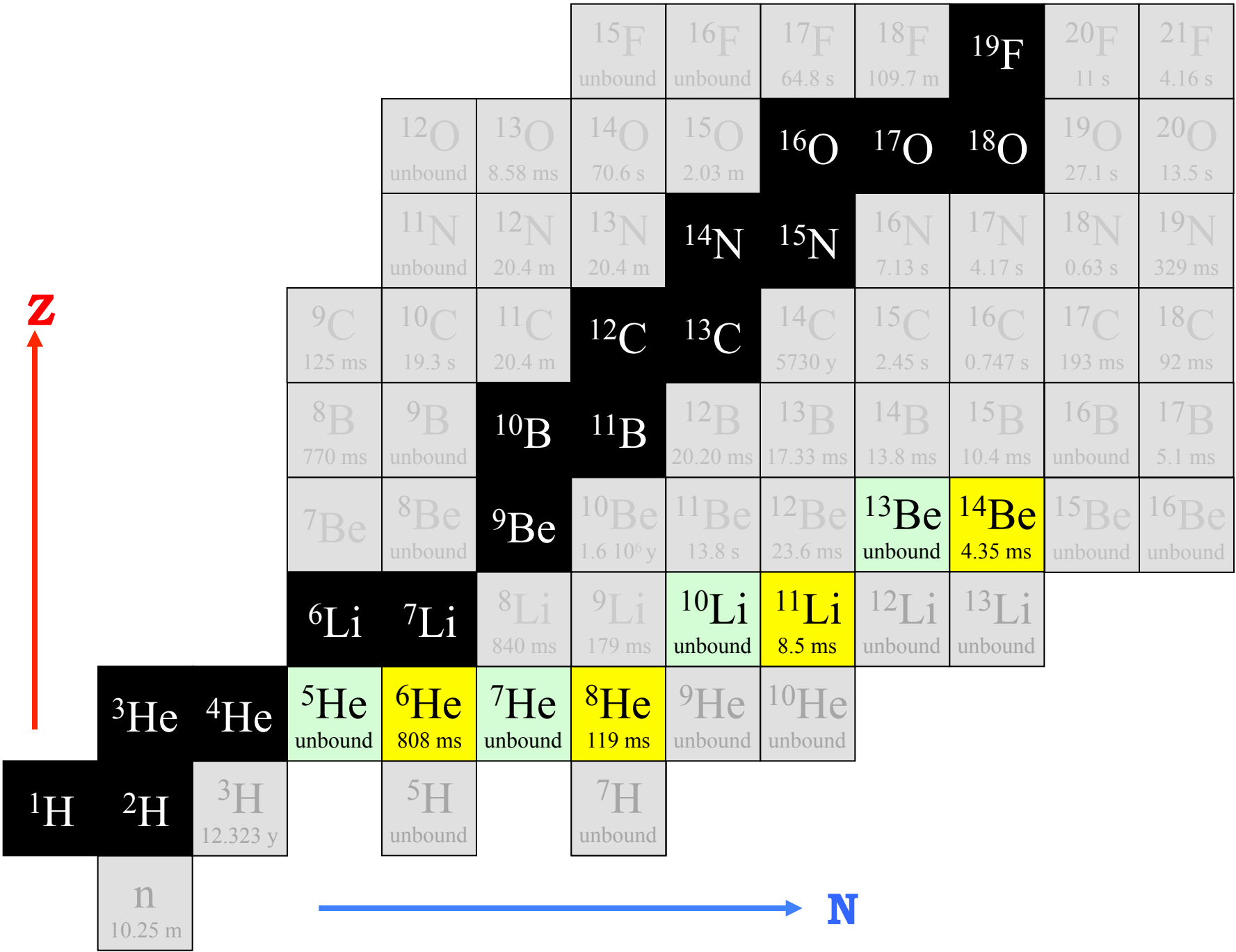
$$\begin{aligned}
 (p_{3/2})^2 &\sim 86\% \\
 (p_{1/2})^2 &\sim 5\% \\
 (s_{1/2})^2 &\sim 7\%
 \end{aligned}$$

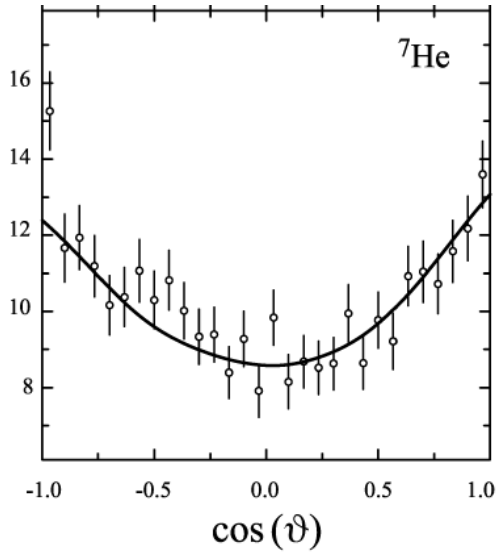
B.V. Danilin et al., NPA **632** (98) 383

Ab initio no-core shell model



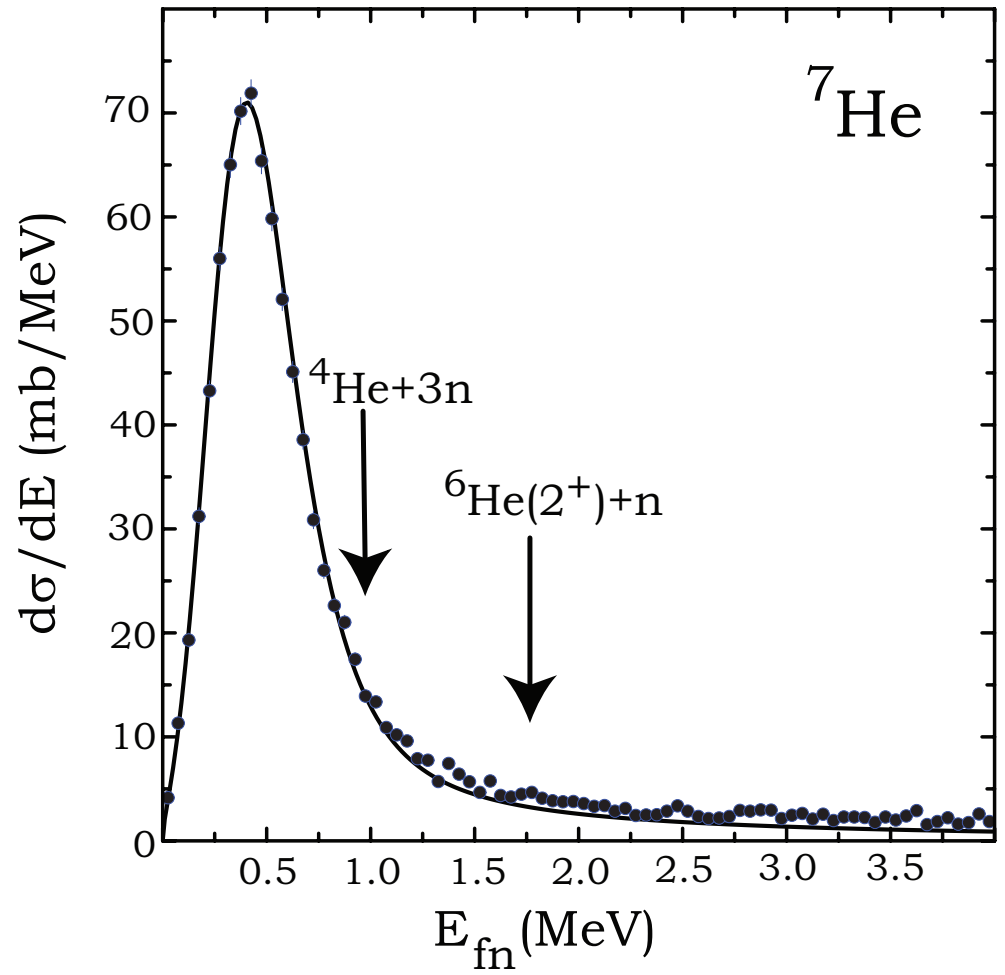
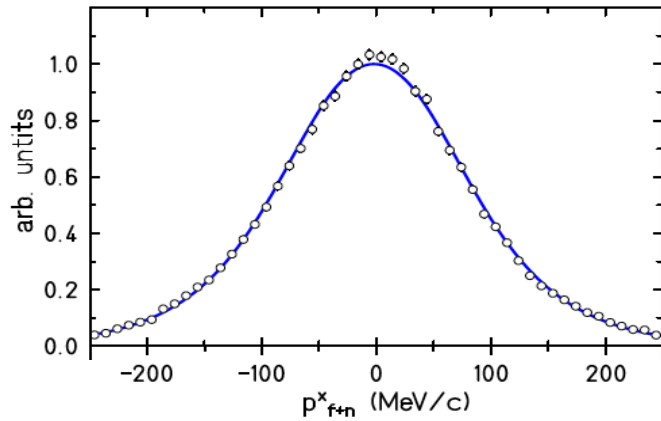
$$(1s_{1/2})^2 \approx 4\%$$





K. Markenroth *et al.*, NP **A679** (2001) 462

$$W(\vartheta_{6\text{He}-n}) \sim 1 + 0.7(1) \cos^2(\vartheta_{6\text{He}-n})$$



Yu. Aksyutina *et al.*,
PLB **679** (2009) 191

$$\frac{d\sigma}{dE_{\text{fn}}} \propto \frac{\Gamma_l(E_{\text{fn}})}{[E_r + \Delta_l(E_{\text{fn}}) - E_{\text{fn}}]^2 + \frac{1}{4}\Gamma_l^2(E_{\text{fn}})}$$

$$\Gamma_l = 2P_l(E_{\text{fn}})\gamma^2$$


$$\gamma_{\text{sp}}^2 = \frac{2}{3}\hbar^2 / \mu R^2$$

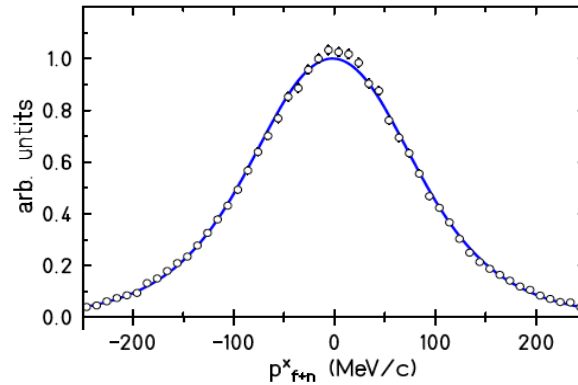
$$S_n = \gamma_{\text{obs}}^2 / \gamma_{\text{sp}}^2$$

Yu. Aksyutina *et al.*,
PLB **679** (2009) 191

$${}^5\text{He} \quad \gamma_{\text{obs}}^2 = \gamma_{\text{sp}}^2$$

$${}^7\text{He}: {}^6\text{He}(0^+) + n \quad S_n = 0.61(3)$$

 not a pure single-particle $p_{3/2}$ -state.



Momentum Profile Function

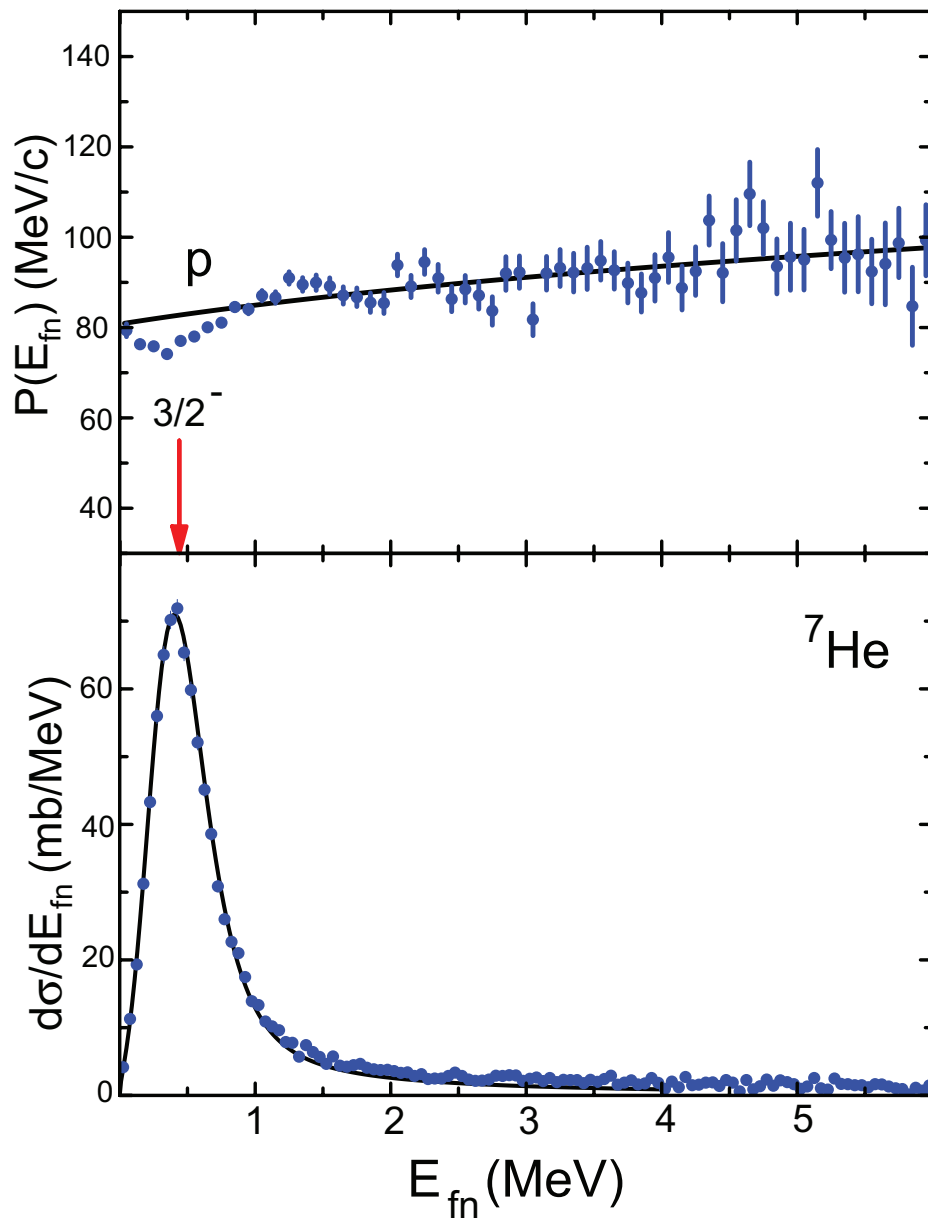
$$P(E_{fn}) = \sqrt{\langle (p_f^x + p_n^x)^2 \rangle - \langle (p_f^x + p_n^x) \rangle^2}$$

Transverse Momentum Distribution

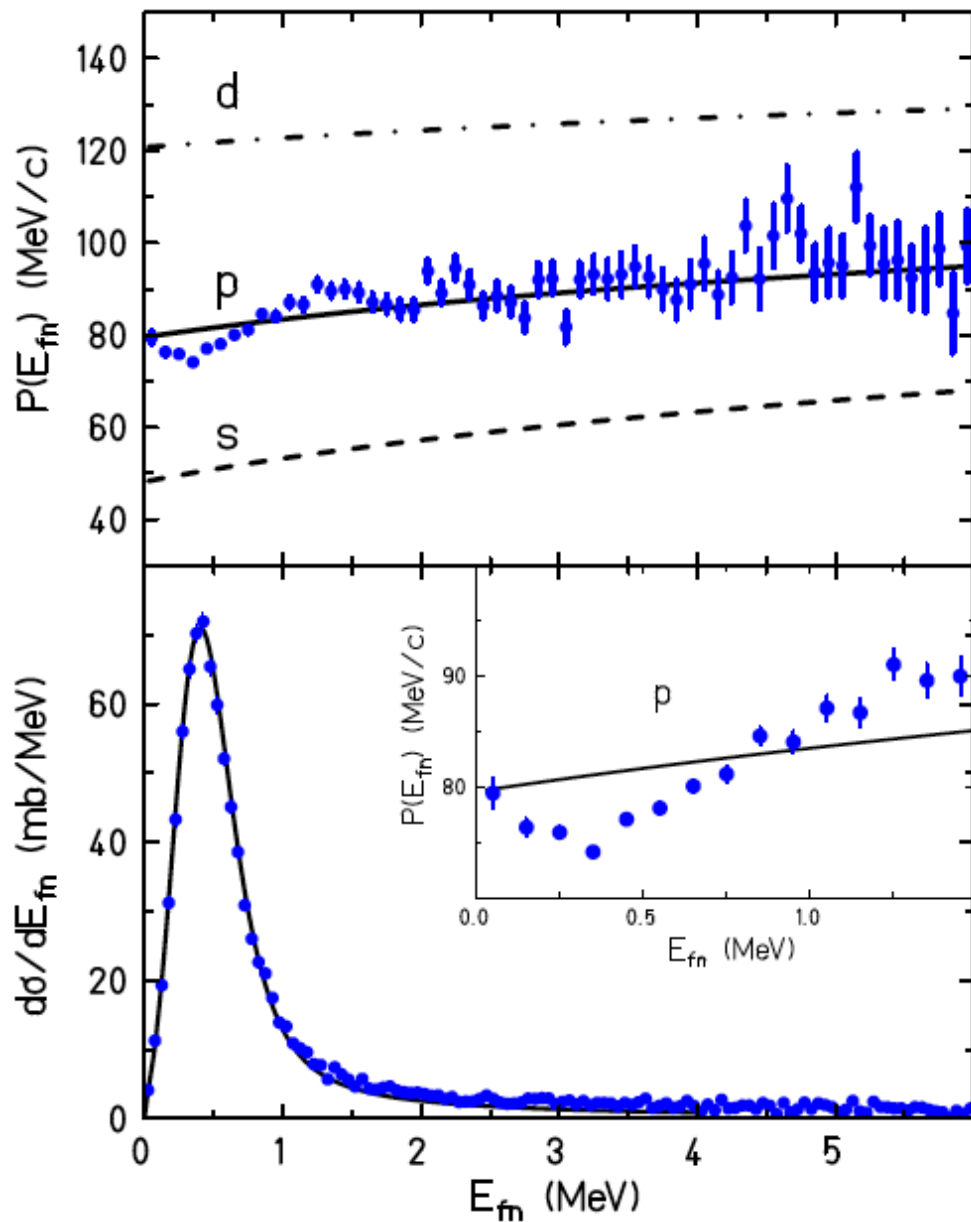
$$\frac{dN}{dp}(l=0) \propto K_1^2(\xi) - K_0^2(\xi)$$

P.G. Hansen, PRL **77** (1996) 1016

D. Basin et al., Phys. Rev. **57** (1998) 2156



Yu. Aksyutina *et al.*,
PLB **718** (2013) 1309



$$P_{r.e.}(E_{fn}) =$$

$$\sqrt{\alpha_s \sigma_s^2 + (1 - \alpha_s) \sigma_p^2}$$

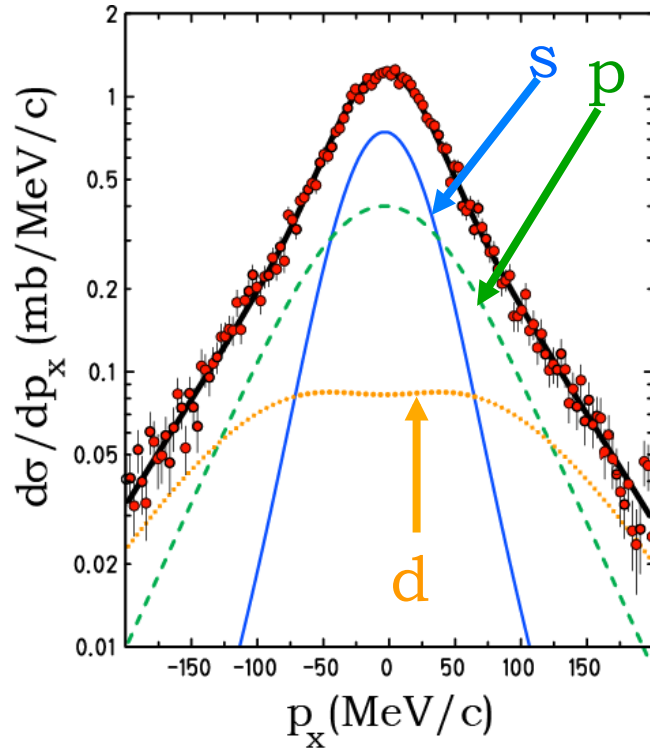
$$l = 0$$

$$l = 1$$

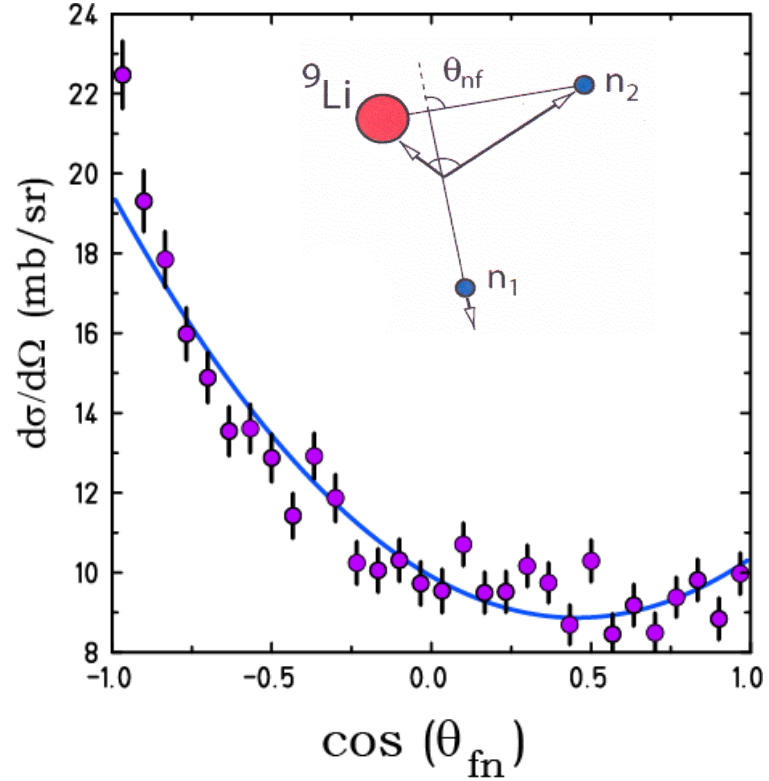


$$12\% (1s_{1/2})^2$$

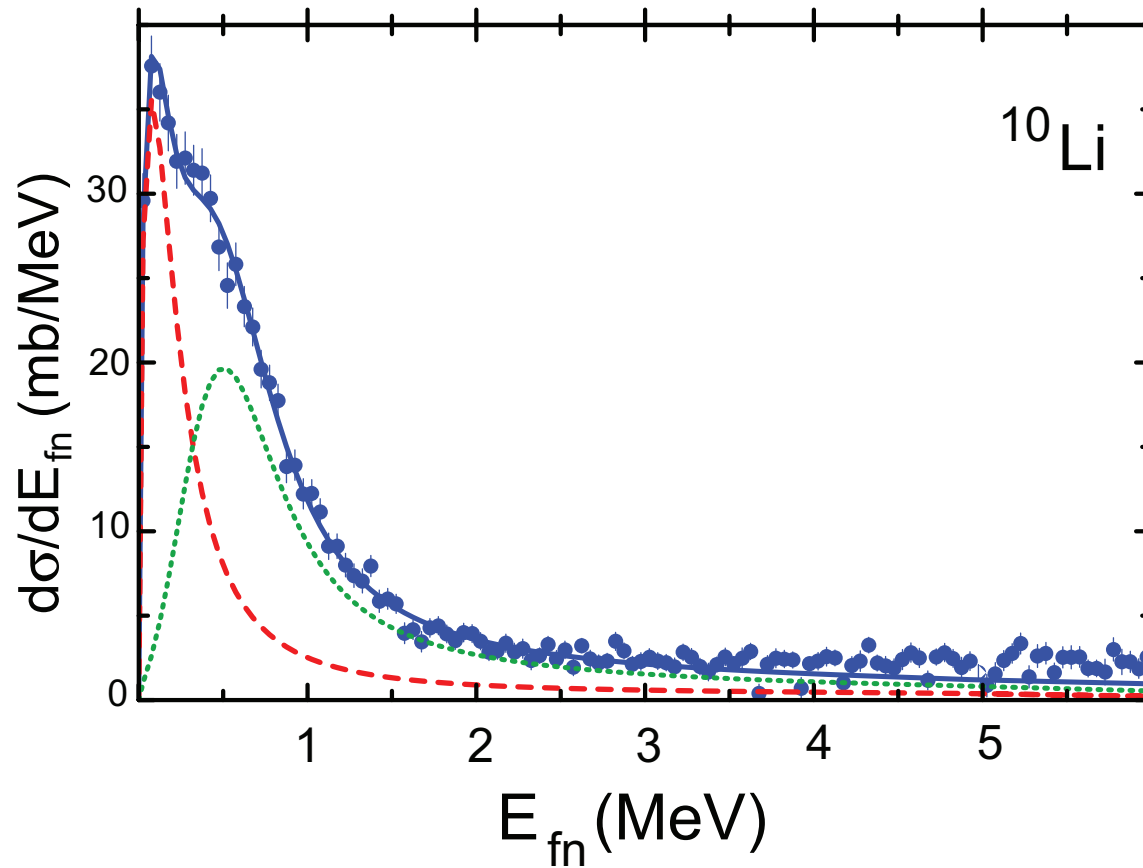
GSI, 287 MeV/u ^{11}Li



$$\mathbf{p}_{n1} = -(\mathbf{p}_{n2} + \mathbf{p}_{9\text{Li}})$$

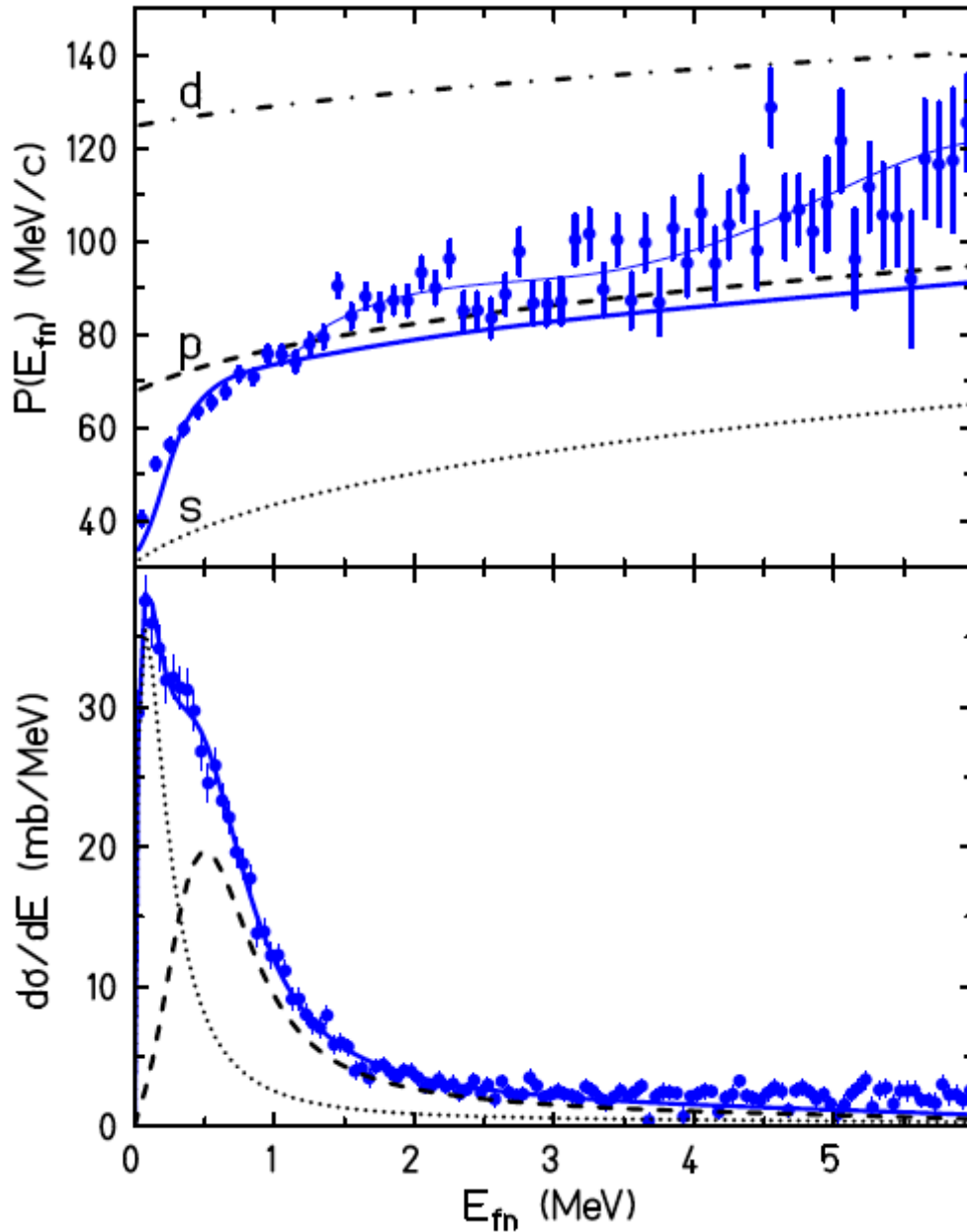


$$W(\theta_{nf}) = 1 - 1.03 \cos(\theta_{nf}) + 1.41 \cos^2(\theta_{nf})$$



Momentum Profile Function

$$P(E_{fn}) = \sqrt{\langle (p_f^x + p_n^x)^2 \rangle - \langle (p_f^x + p_n^x) \rangle^2}$$



$$P_{r.e.}(E_{fn}) = \sqrt{\alpha_s \sigma_s^2 + (1 - \alpha_s) \sigma_p^2}$$

$$\alpha_d = (P_{exp}^2 - P_{r.e.}^2) / (\sigma_d^2 - P_{r.e.}^2)$$

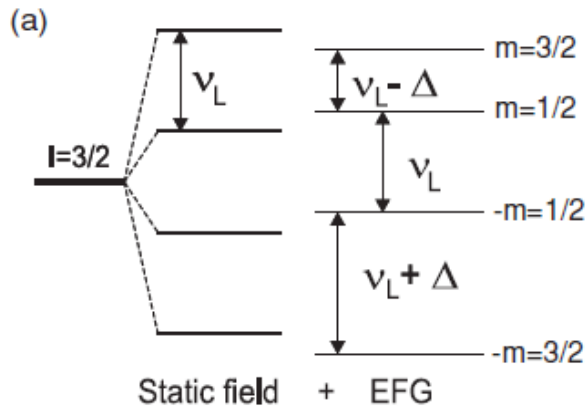
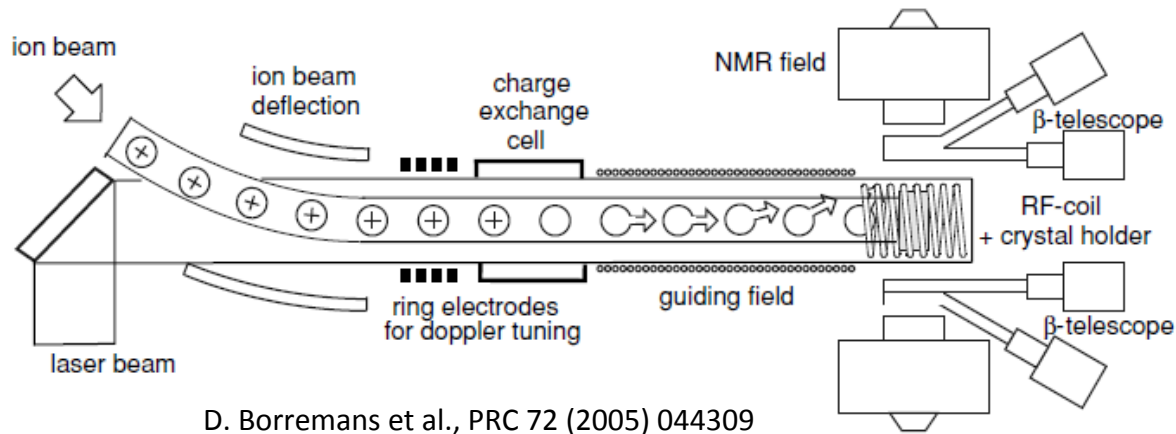
$(0d_{5/2})^2$
11(2) %

Aksyutina *et al.*
PLB 718 (2013) 1309

${}^6\text{Li}$	${}^7\text{Li}$	${}^8\text{Li}$ 840 ms	${}^9\text{Li}$ 179 ms	${}^{10}\text{Li}$ unbound	${}^{11}\text{Li}$ 8.5 ms	${}^{12}\text{Li}$ unbound	${}^{13}\text{Li}$ unbound
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$|\pi=3/2^-$

$|\pi=3/2^-$



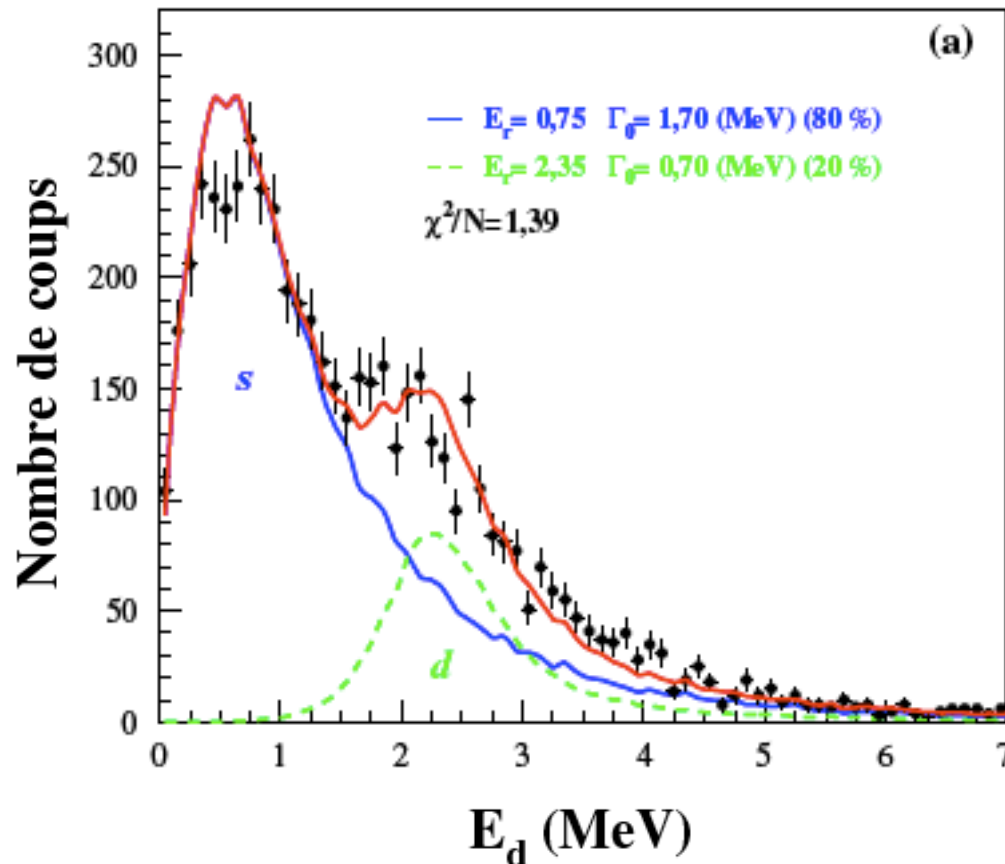
R. Neugart et al., PRL 101(2008) 132502

$|Q({}^{11}\text{Li})/Q({}^9\text{Li})| = 1.088(15)$

${}^7\text{Be}$	${}^8\text{Be}$ unbound	${}^9\text{Be}$	${}^{10}\text{Be}$ $1.6 \cdot 10^6 \text{ y}$	${}^{11}\text{Be}$ 13.8 s	${}^{12}\text{Be}$ 23.6 ms	${}^{13}\text{Be}$ unbound	${}^{14}\text{Be}$ 4.35 ms	${}^{15}\text{Be}$ unbound	${}^{16}\text{Be}$ unbound
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GANIL

41 MeV/u ${}^{14}\text{B}$, C target



${}^{16}\text{Be}$

Spyrou *et al.*,
PRL 108(2012) 102501

${}^{15}\text{Be}$

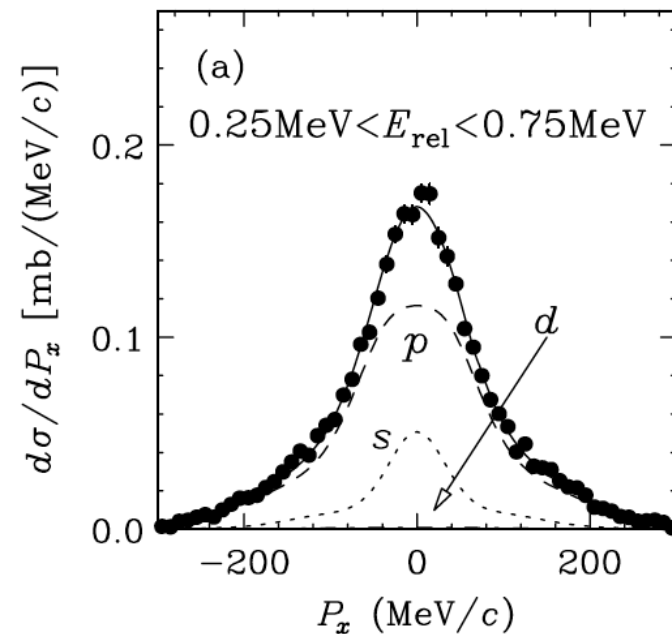
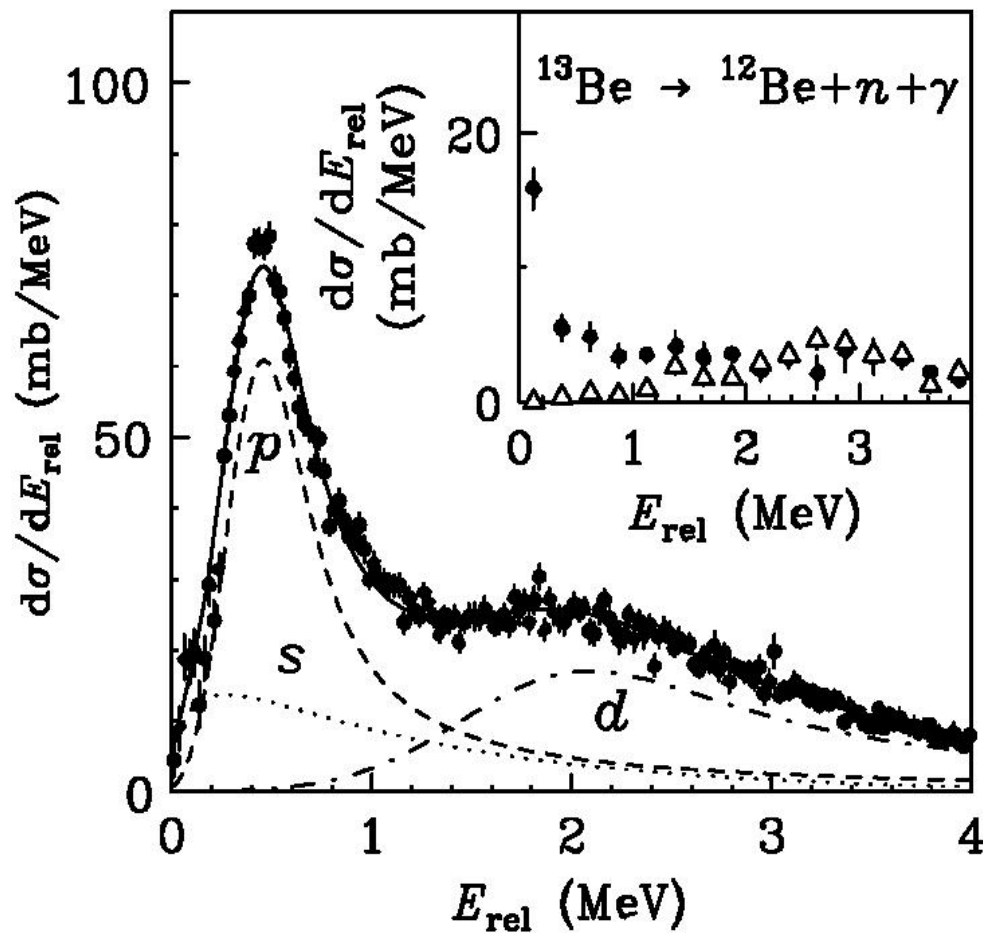
Snyder *et al.*,
PRC 88(2013) 031303

${}^{14}\text{B}$

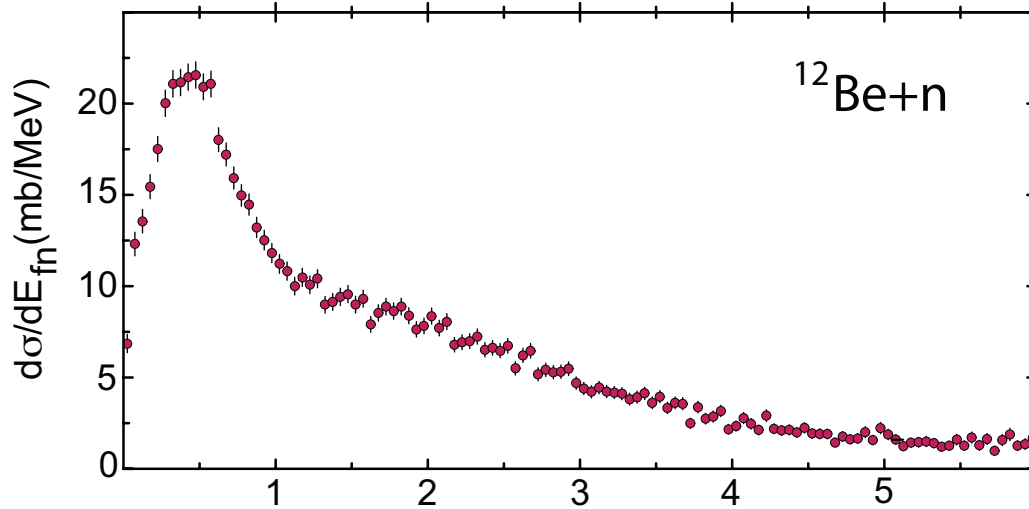
${}^{13}\text{B}(3/2^-) \otimes (sd)$

RIKEN

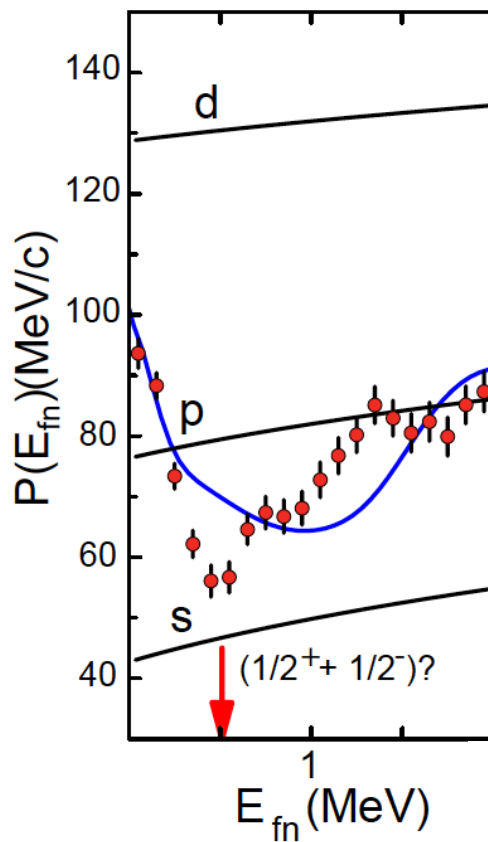
69 MeV/u ^{14}Be , Lq H target



n - γ coincidences
2.11 MeV and 2.71 MeV

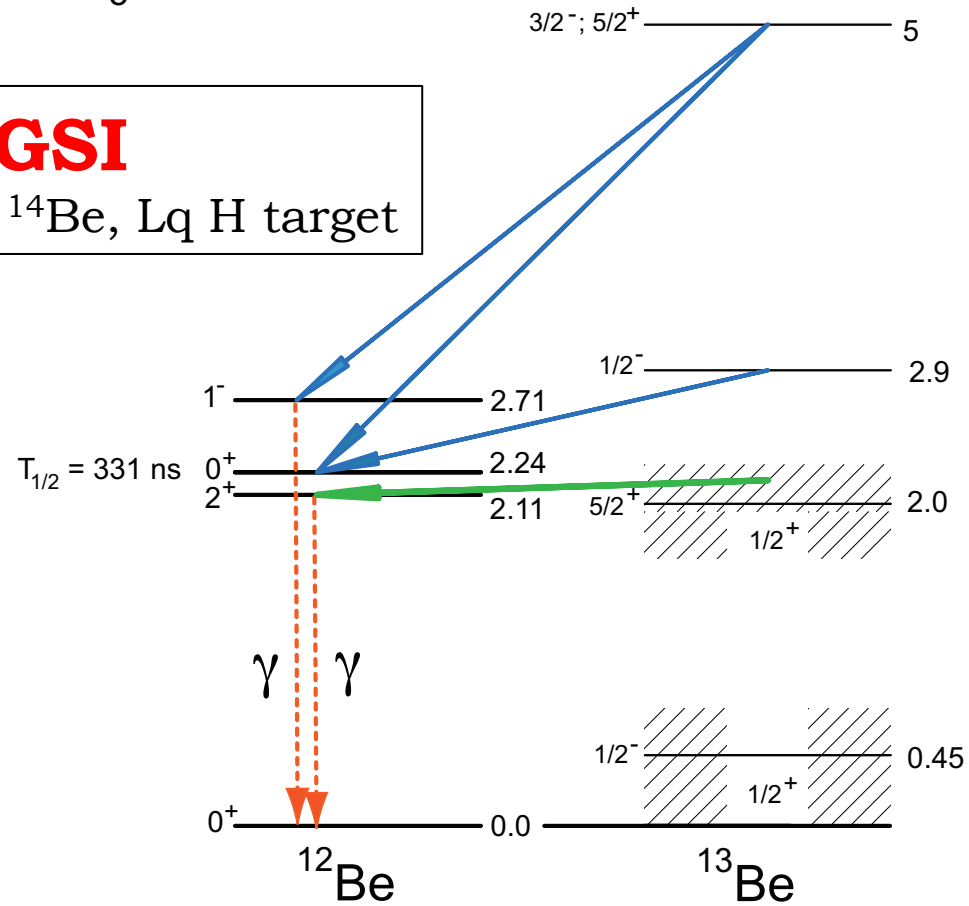


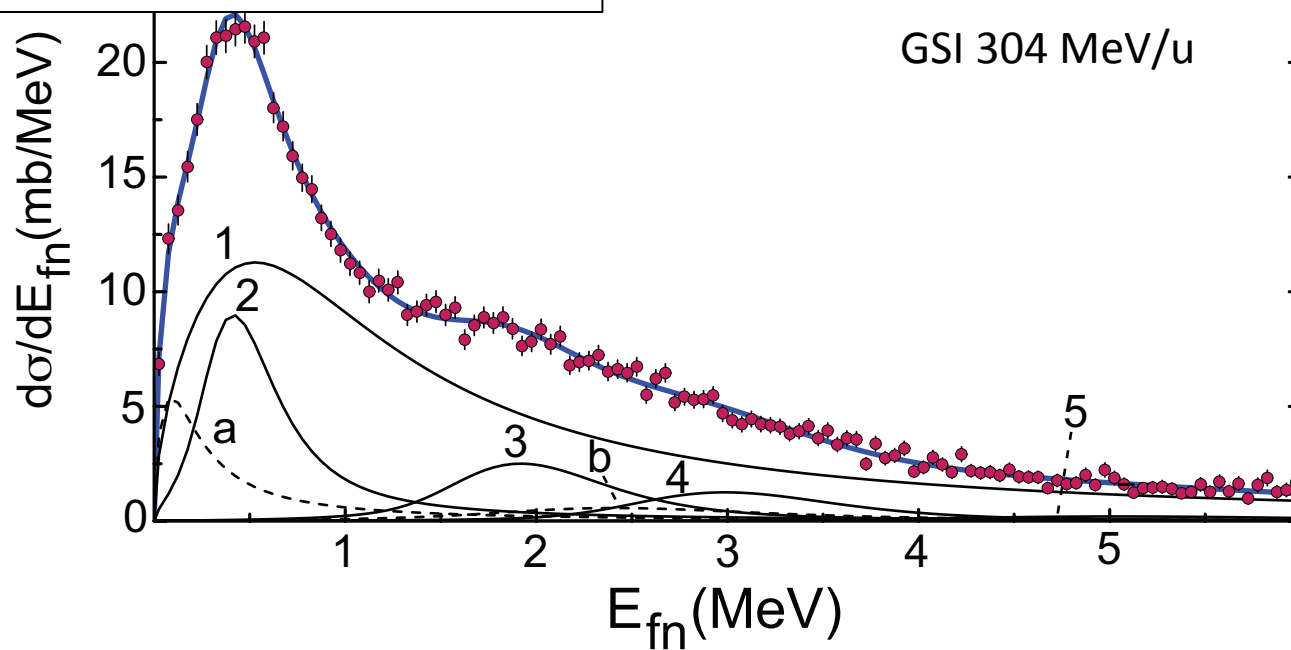
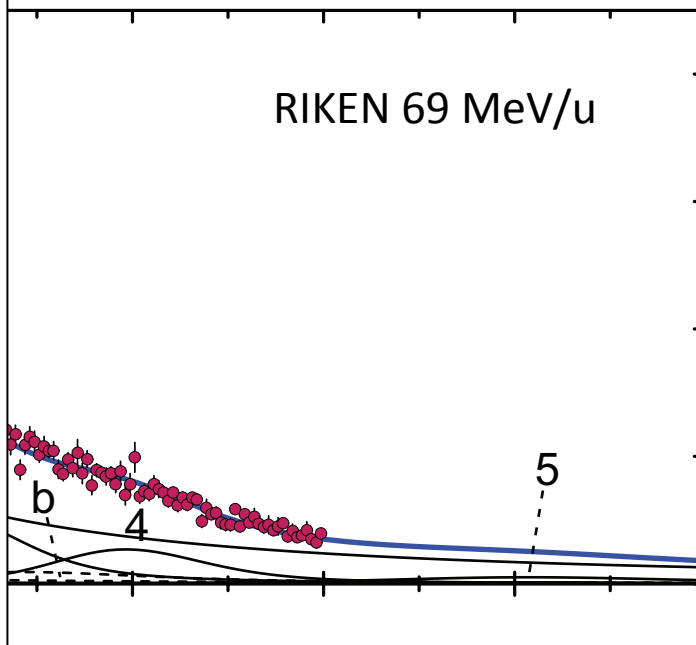
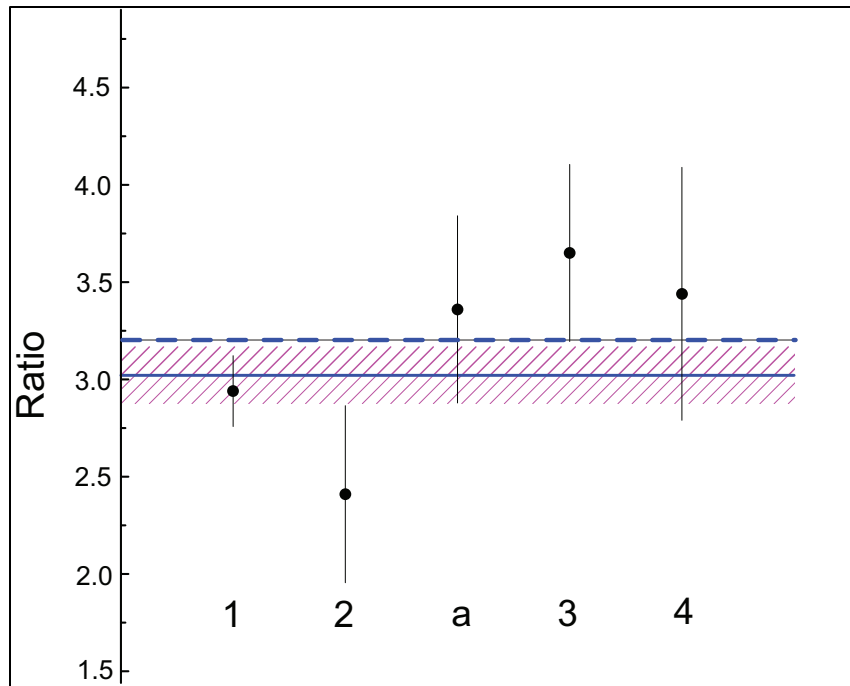
Yu. Aksyutina *et al.*,
 Phys. Rev. C **87** (2013) 064316



$E_{fn}(\text{MeV})$

GSI
 304 MeV/u ^{14}Be , Lq H target





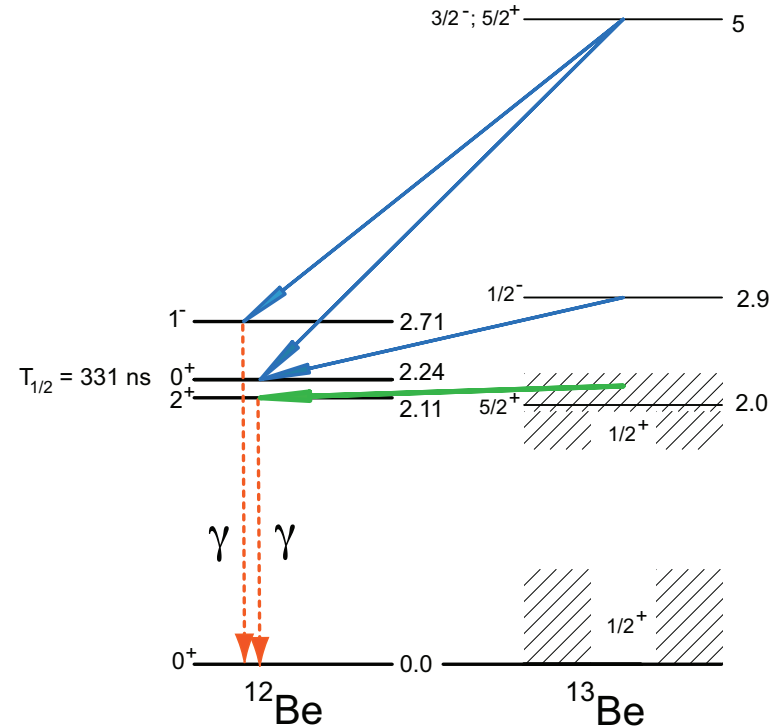
INTERFERENCE ?

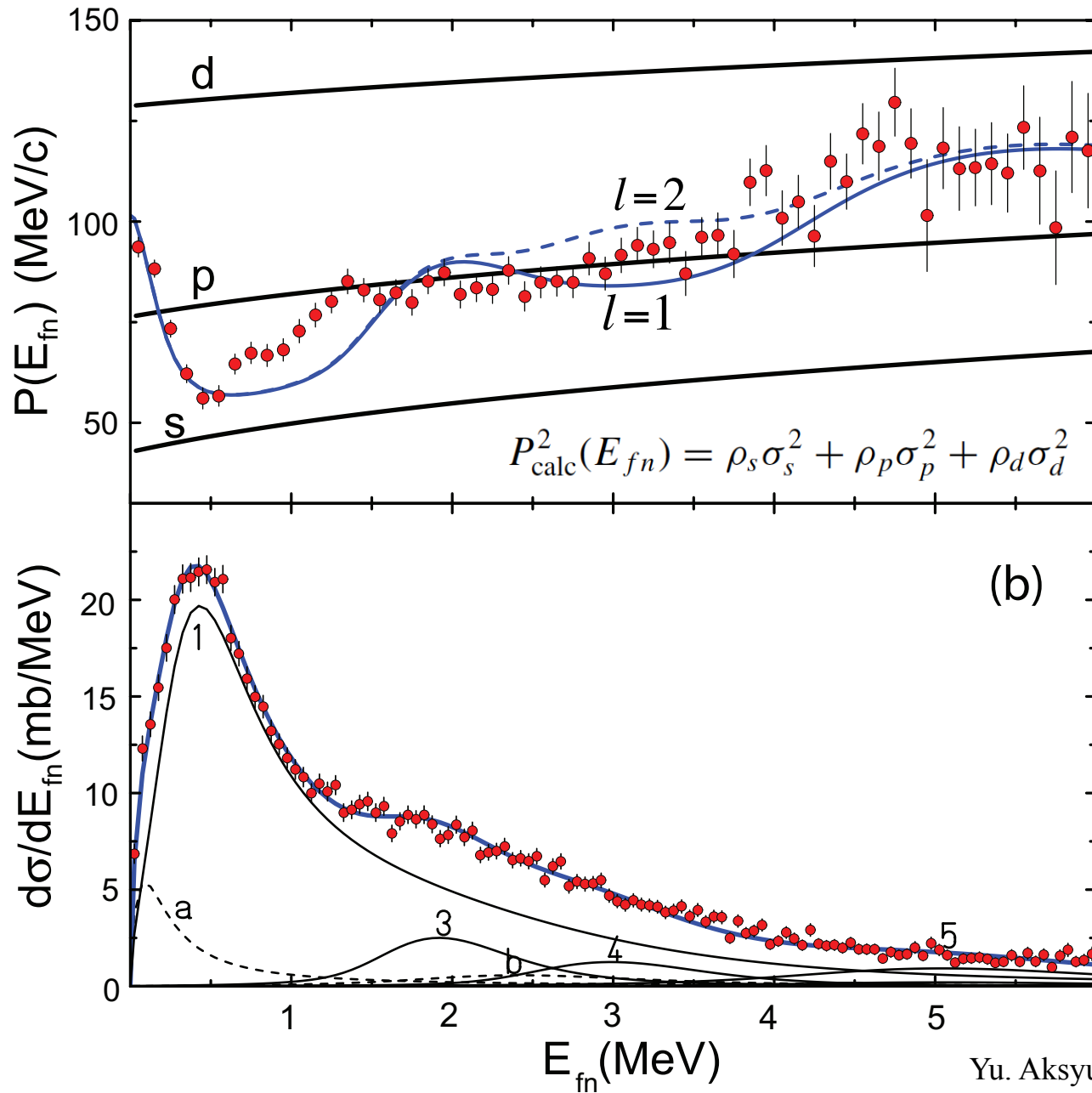
$${}^{12}\text{Be}(0^+) = \alpha[{}^{10}\text{Be} \otimes (1s_{1/2})^2] + \beta[{}^{10}\text{Be} \otimes (0p_{1/2})^2] + \gamma[{}^{10}\text{Be} \otimes (0d_{5/2})^2],$$

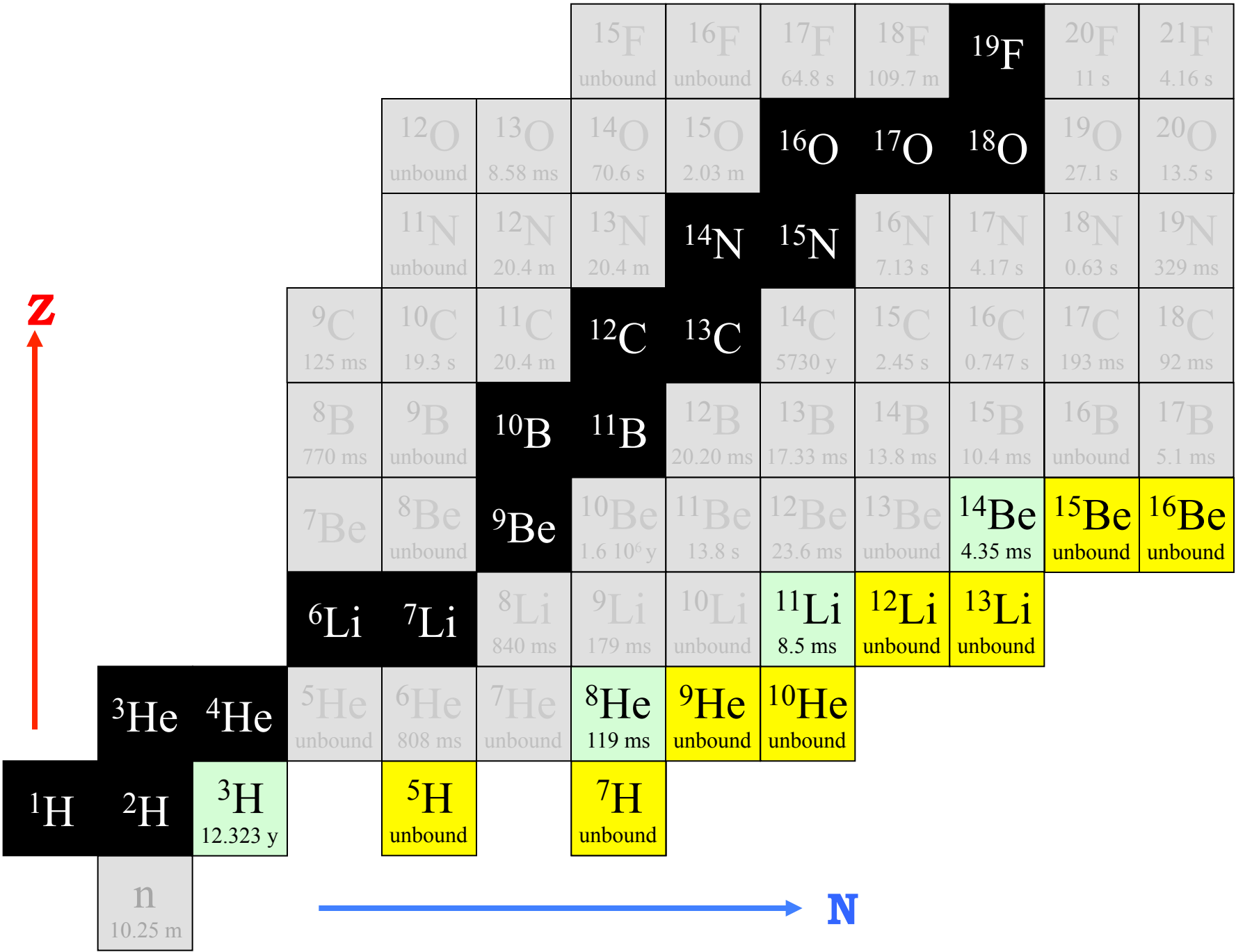
$$\alpha^2 = 0.35, \beta^2 = 0.31, \gamma^2 = 0.34$$

$${}^{13}\text{Be}(1/2_2^+) = \mu[{}^{10}\text{Be} \otimes (0p_{1/2})^2 \otimes (1s_{1/2})] - \lambda[{}^{10}\text{Be} \otimes (0d_{5/2})^2 \otimes (1s_{1/2})]$$

$${}^{13}\text{Be}(1/2_1^+) = \lambda[{}^{10}\text{Be} \otimes (0p_{1/2})^2 \otimes (1s_{1/2})] + \mu[{}^{10}\text{Be} \otimes (0d_{5/2})^2 \otimes (1s_{1/2})].$$







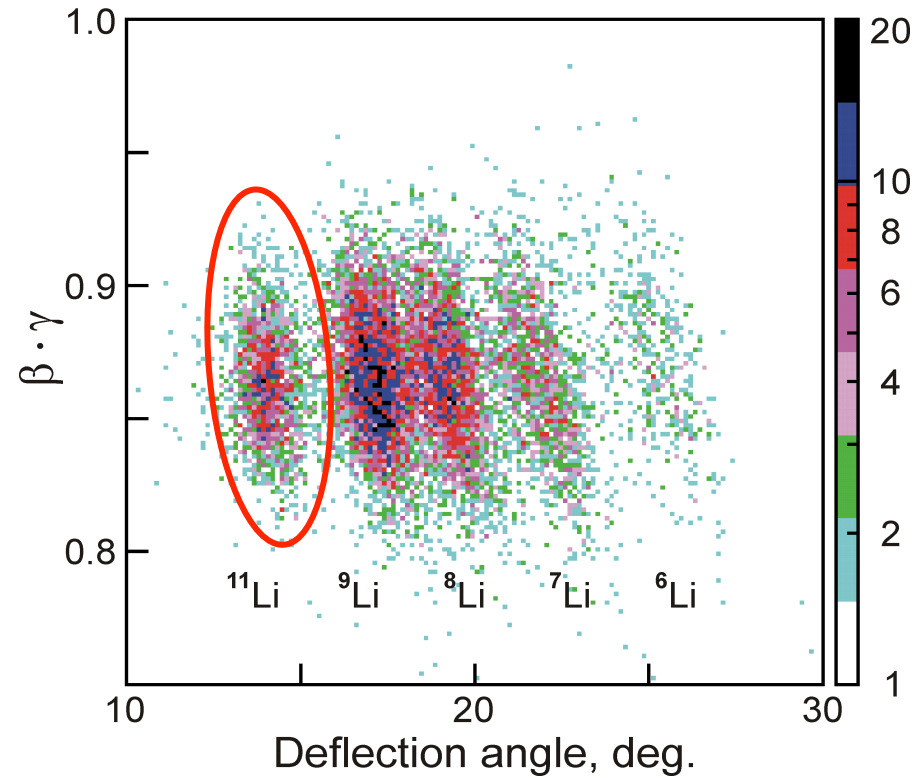
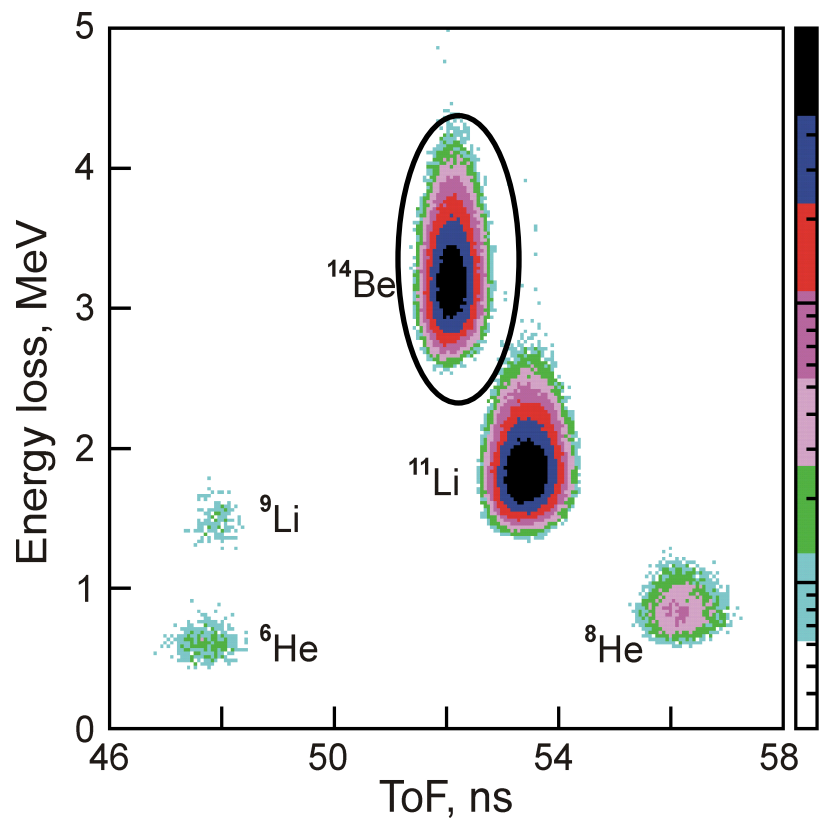
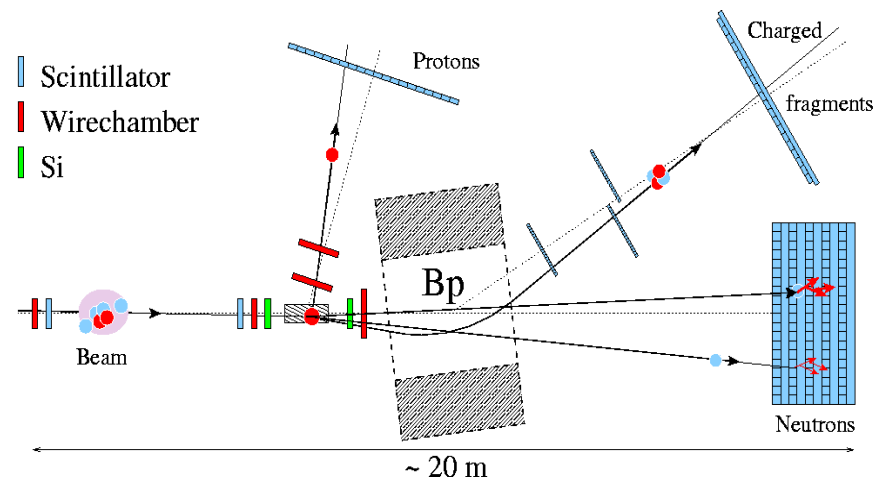
Dripline nuclei as stepping stones towards the unbound

	${}^7\text{Be}$	${}^8\text{Be}$ unbound	${}^9\text{Be}$	${}^{10}\text{Be}$ 1.6 10^6 y	${}^{11}\text{Be}$ 13.8 s	${}^{12}\text{Be}$ 23.6 ms	${}^{13}\text{Be}$ unbound	${}^{14}\text{Be}$ 4.35 ms
	${}^6\text{Li}$	${}^7\text{Li}$	${}^8\text{Li}$ 840 ms	${}^9\text{Li}$ 179 ms	${}^{10}\text{Li}$ unbound	${}^{11}\text{Li}$ 8.5 ms	${}^{12}\text{Li}$ unbound	${}^{13}\text{Li}$ unbound
${}^4\text{He}$	${}^5\text{He}$ unbound	${}^6\text{He}$ 808 ms	${}^7\text{He}$ unbound	${}^8\text{He}$ 119 ms	${}^9\text{He}$ unbound	${}^{10}\text{He}$ unbound		
				${}^7\text{H}$ unbound				

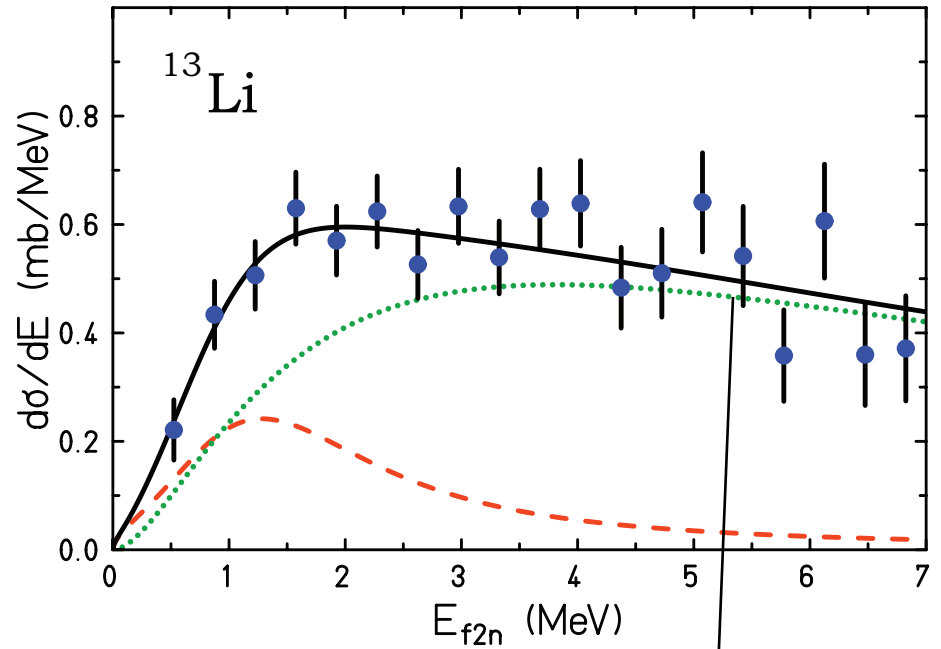
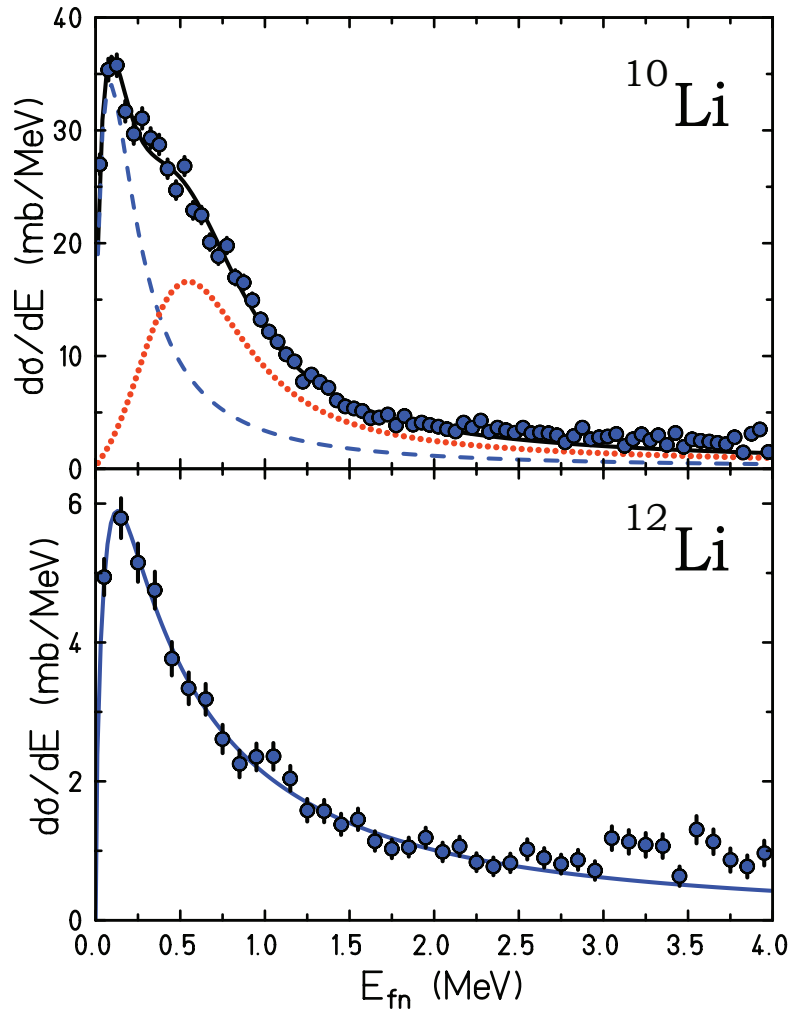
${}^{11}\text{Li}$: Neutron knock-out reaction \rightarrow ${}^{10}\text{Li}$
 Proton knock-out reactions \rightarrow ${}^9, {}^{10}\text{He}$

${}^{14}\text{Be}$: Neutron knock-out reaction \rightarrow ${}^{13}\text{Be}$
 Proton knock-out reactions \rightarrow ${}^{12}, {}^{13}\text{Li}$

${}^8\text{He}$: Neutron knock-out reaction \rightarrow ${}^7\text{He}$
 Proton knock-out reaction \rightarrow (${}^7\text{H}$)



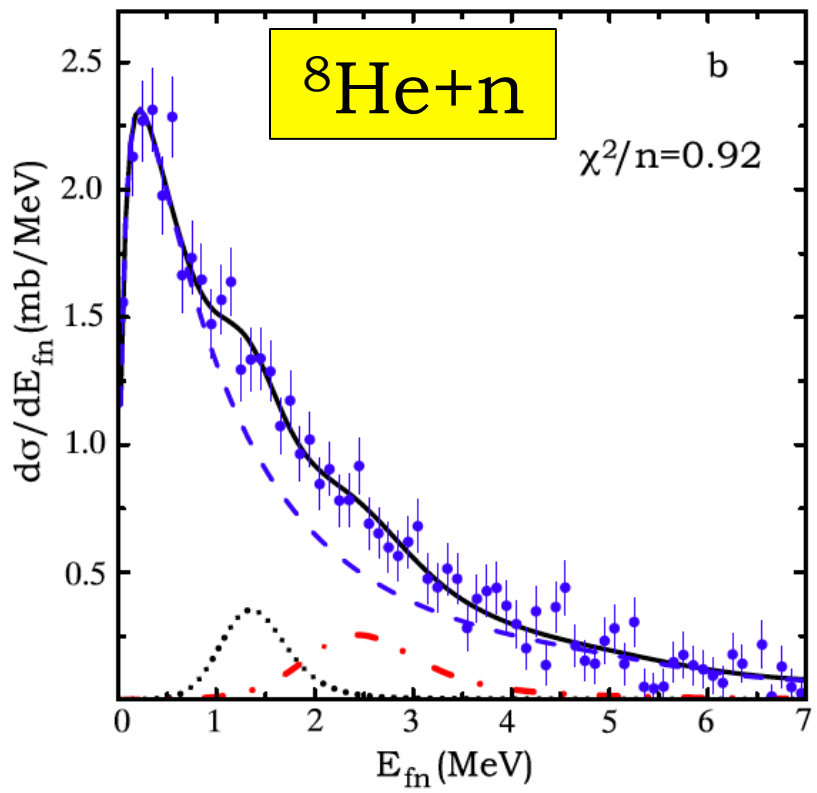
${}^6\text{Li}$	${}^7\text{Li}$	${}^8\text{Li}$ 840 ms	${}^9\text{Li}$ 179 ms	${}^{10}\text{Li}$ unbound	${}^{11}\text{Li}$ 8.5 ms	${}^{12}\text{Li}$ unbound	${}^{13}\text{Li}$ unbound
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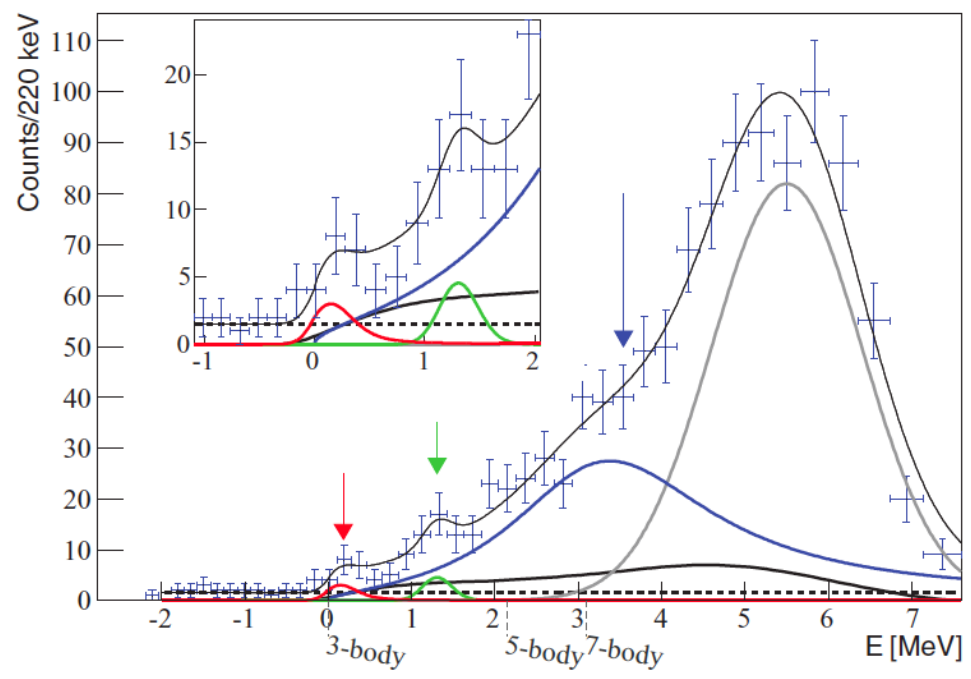
Forssén *et al.* Nucl. Phys. A **673**(2000) 143

^3He	^4He	^5He unbound	^6He 808 ms	^7He unbound	^8He 119 ms	^9He unbound	^{10}He unbound
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$^8\text{He}(d,p)^9\text{He}$

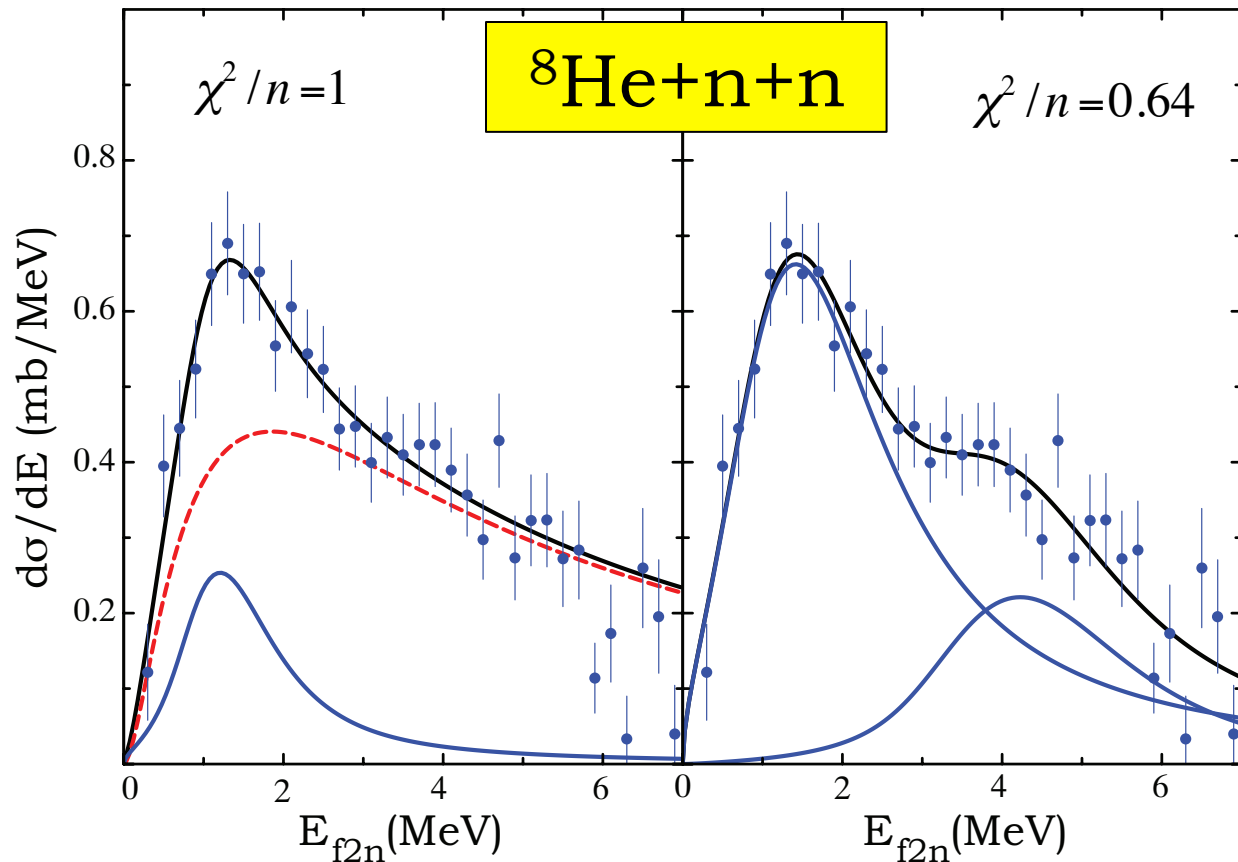


Johansson et al., Nucl. Phys. **A842** (2010) 15



Al Kalanee et al., PRC **88** (2013) 034301

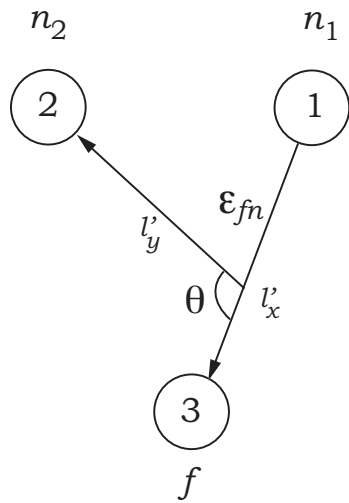
^3He	^4He	^5He unbound	^6He 808 ms	^7He unbound	^8He 119 ms	^9He unbound	^{10}He unbound
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$$\sqrt{2\chi^2} - \sqrt{2n-1} = -1.56$$

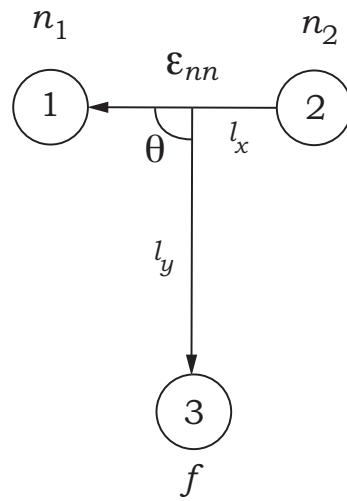
Neyman-Pearson test

$^8\text{He}+n+n$



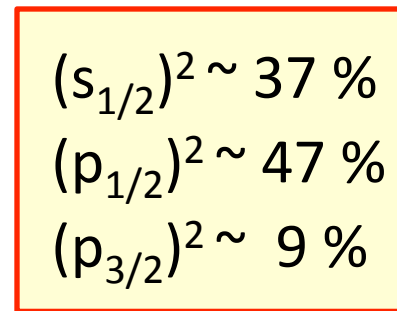
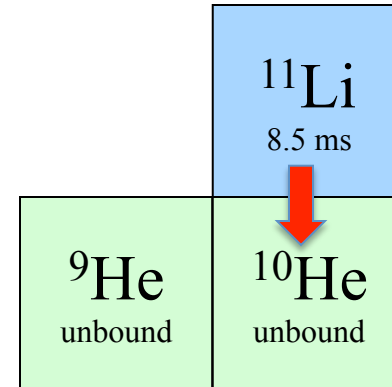
Y-system

$$\epsilon_{fn} = E_{fn}/E$$

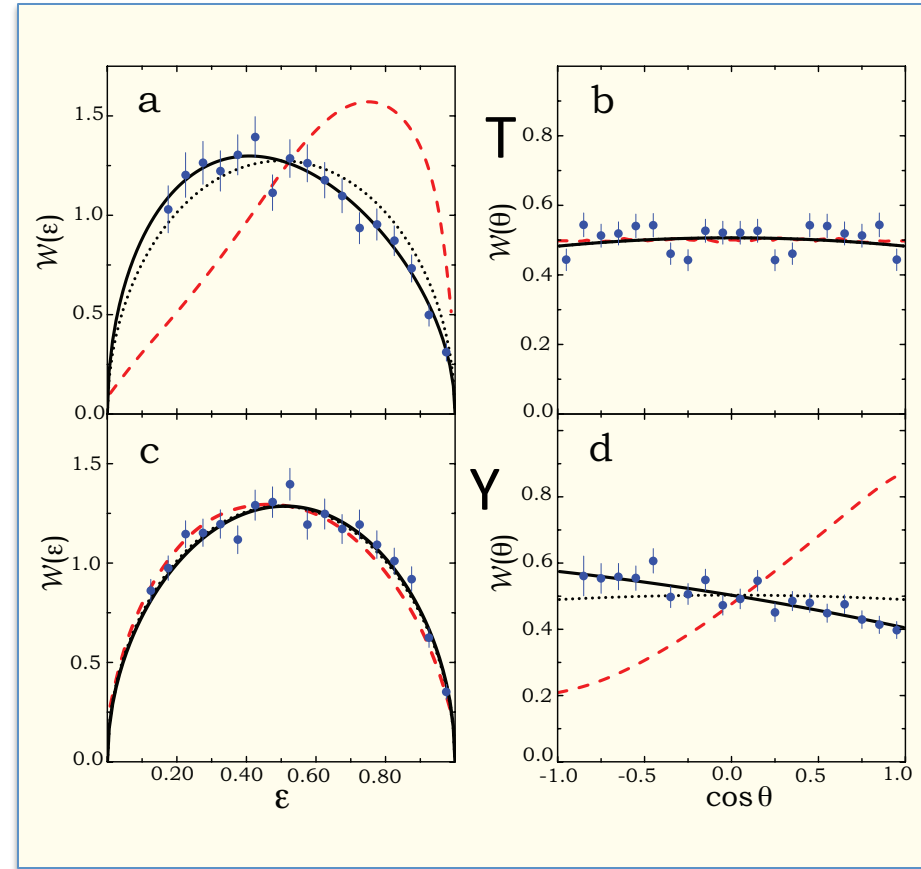
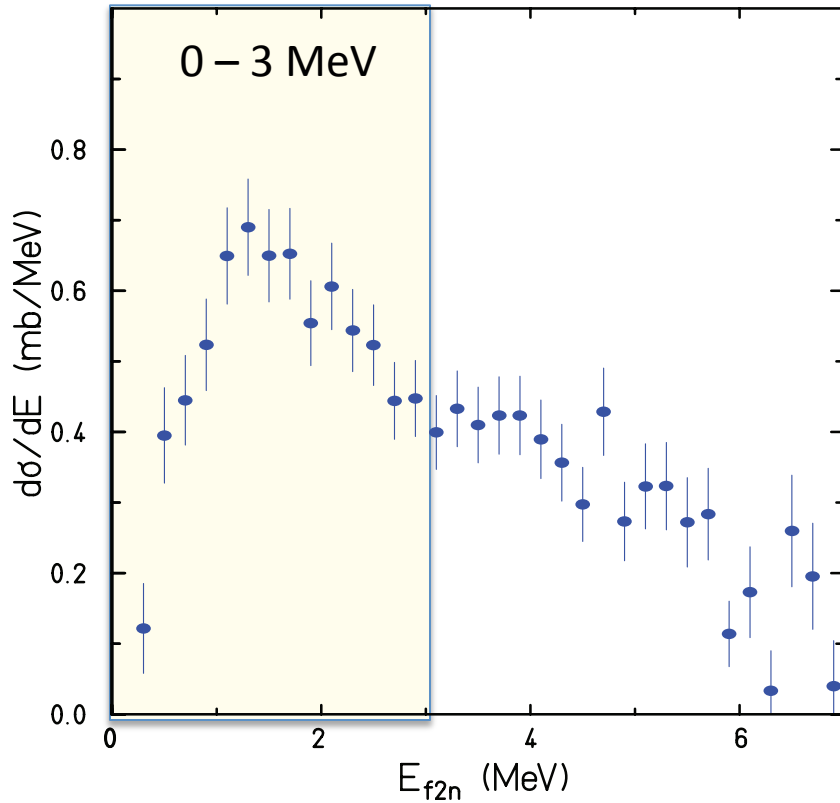


T-system

$$\epsilon_{nn} = E_{nn}/E$$



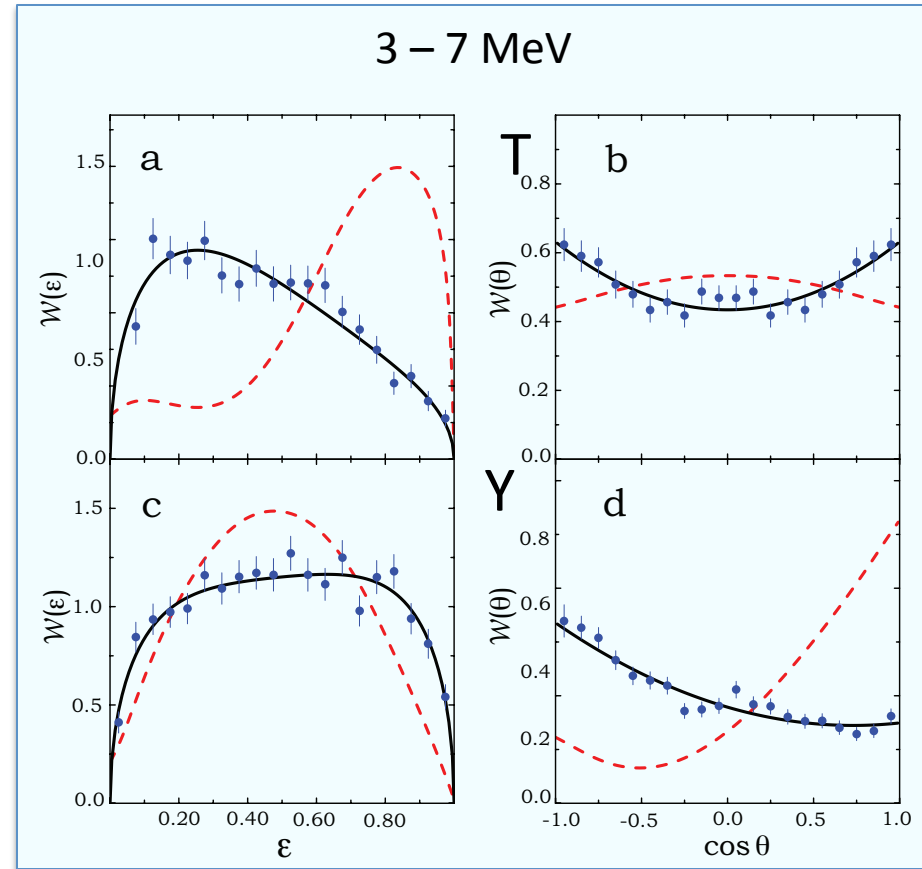
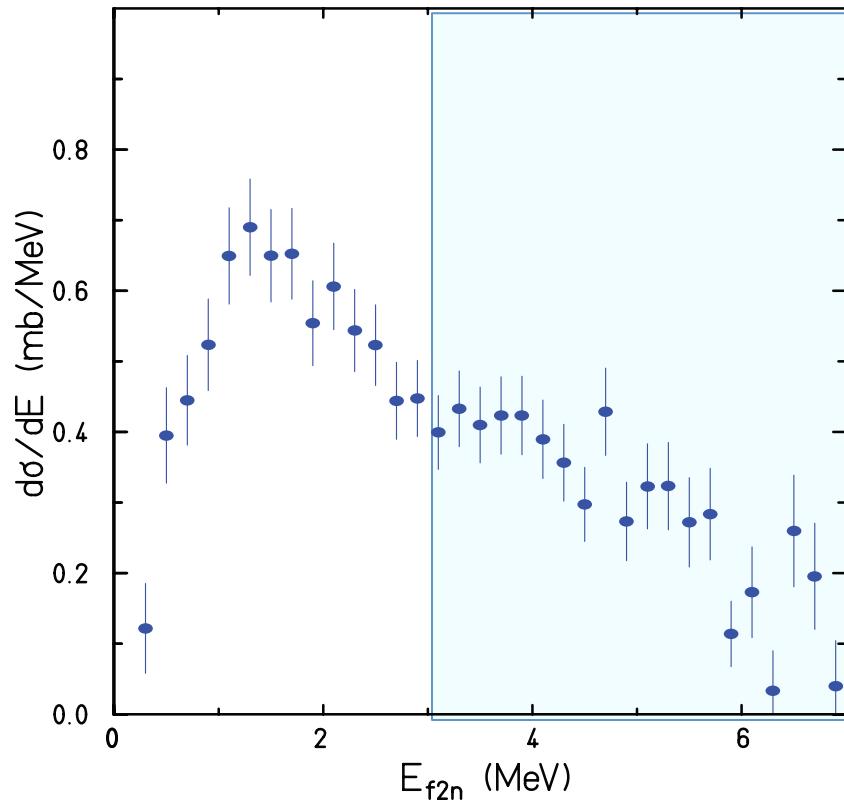
Energy and angular correlations



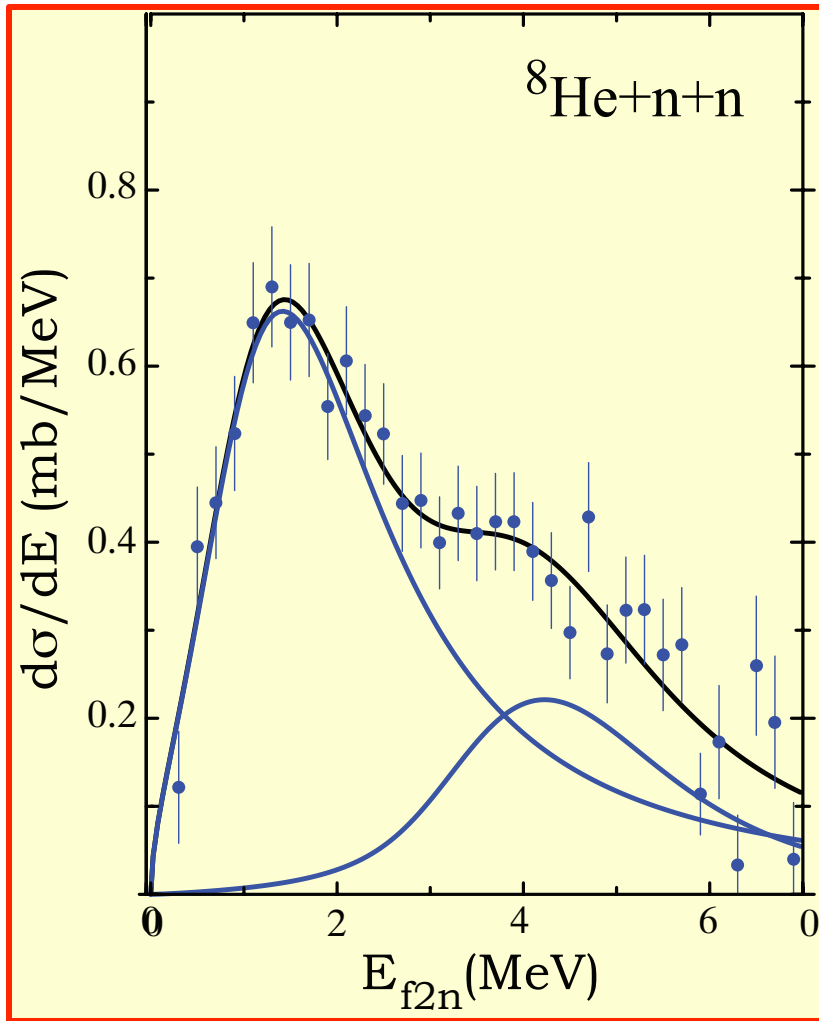
Restricted series of hyperspherical harmonics assuming $I^\pi = 0^+$ and $K \leq 2$

$$\begin{aligned}
 & \mathcal{W}_{0^+}(\varepsilon, \cos \theta) \\
 &= \frac{4}{\pi} \sqrt{\varepsilon(1-\varepsilon)} (|A_{00}^{000}|^2 + 4|A_{00}^{000}| [(1-2\varepsilon)|A_{00}^{200}| \cos \varphi_{00}^{200} \\
 & \quad - 2\sqrt{2}\varepsilon(1-\varepsilon)(1-3\cos^2\theta)|A_{22}^{400}| \cos \varphi_{22}^{400}] + 4[(1-2\varepsilon)|A_{00}^{200}|^2 \\
 & \quad - 4\sqrt{2}\varepsilon(1-\varepsilon)(3-2\varepsilon)(1-3\cos^2\theta)|A_{00}^{200}||A_{22}^{400}| \cos(\varphi_{00}^{200} - \varphi_{22}^{400}) \\
 & \quad + 2\varepsilon(1-\varepsilon)((1-\cos^2\theta)|A_{11}^{211}|^2 + 4\varepsilon(1-\varepsilon)(1-3\cos^2\theta)^2|A_{22}^{400}|^2)])
 \end{aligned}$$

Energy and angular correlations

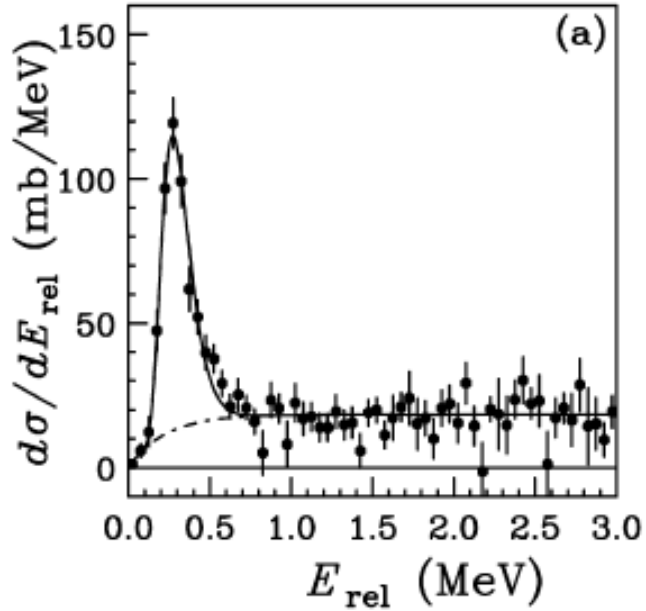


Restricted series of hyperspherical harmonics assuming $I^\pi = 2^+$ and $K \leq 4$

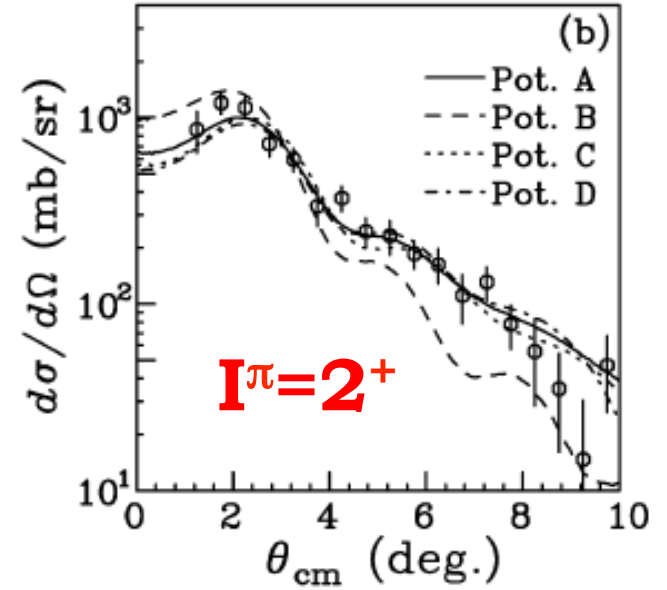


${}^8\text{He} + n + n$
Ground state $I^\pi = 0^+$
Excited state $I^\pi = 2^+$

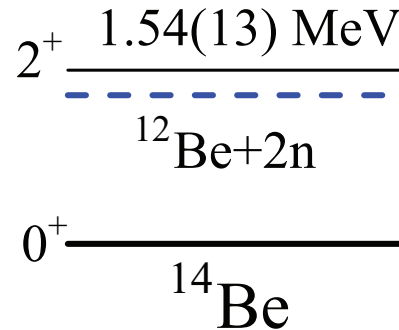
${}^7\text{Be}$	${}^8\text{Be}$ unbound	${}^9\text{Be}$	${}^{10}\text{Be}$ $1.6 \cdot 10^6 \text{ y}$	${}^{11}\text{Be}$ 13.8 s	${}^{12}\text{Be}$ 23.6 ms	${}^{13}\text{Be}$ unbound	${}^{14}\text{Be}$ 4.35 ms	${}^{15}\text{Be}$ unbound	${}^{16}\text{Be}$ unbound
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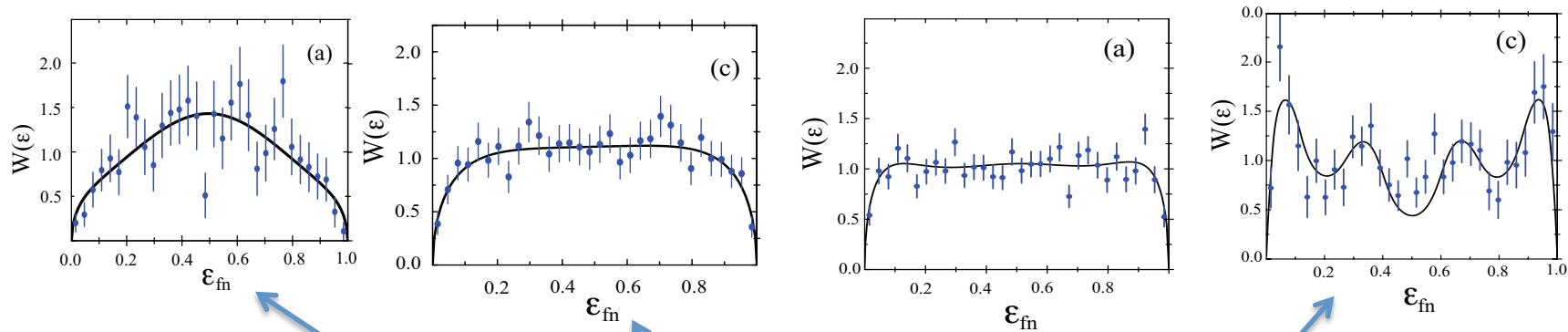


RIKEN
68 MeV/u ${}^{14}\text{Be}$,
 ${}^{12}\text{C}$ target

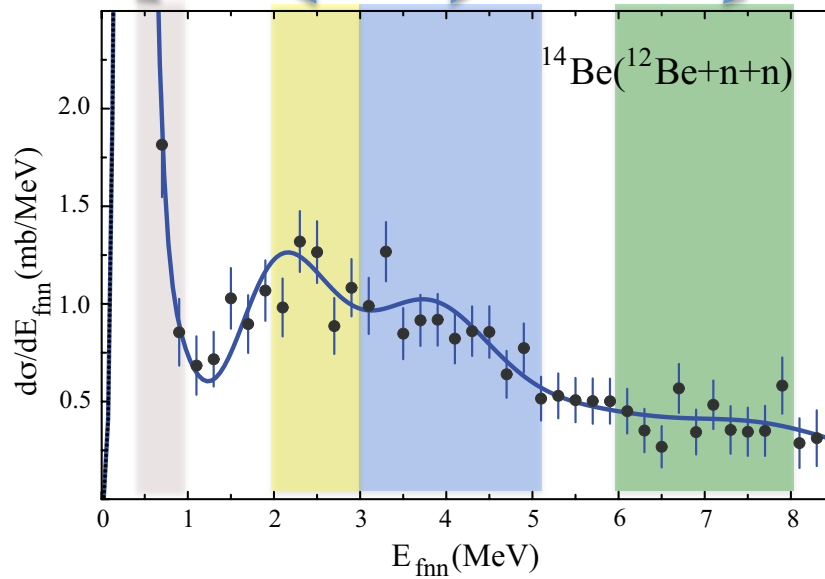


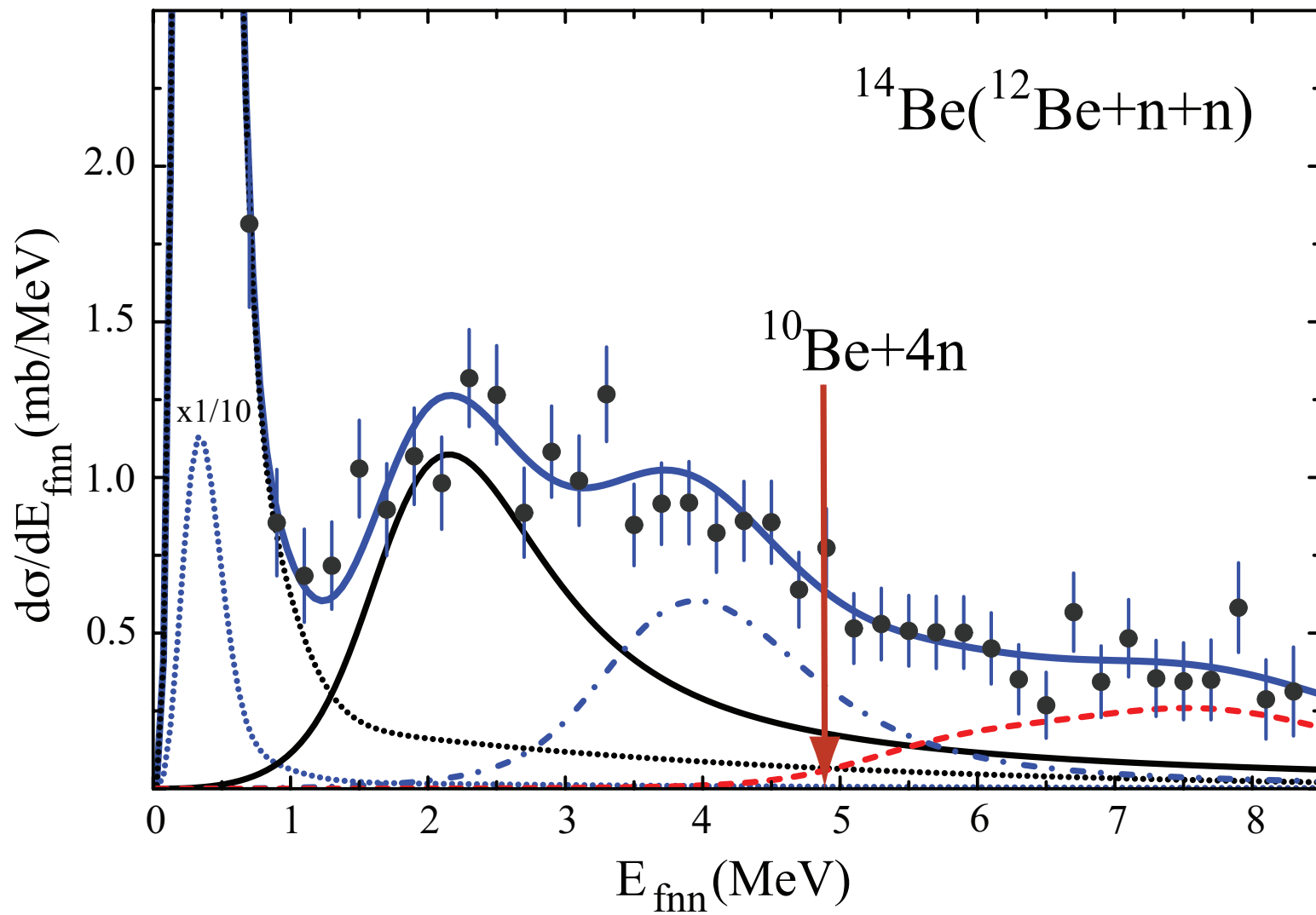
Sugimoto *et al.*,
Phys. Lett. **B654** (2007) 160



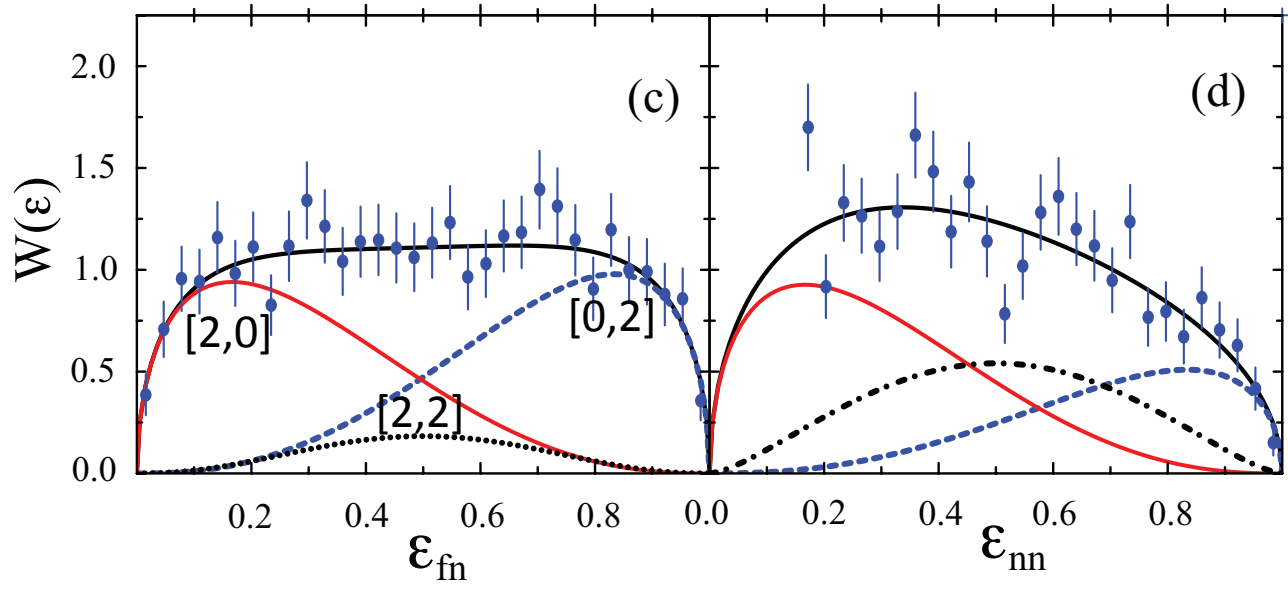


$$\varepsilon_{\text{fn}} = E_{\text{fn}}/E$$





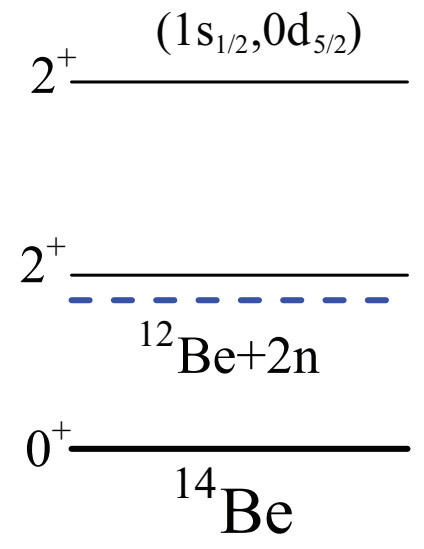
2 MeV < E_{fnn} < 3 MeV



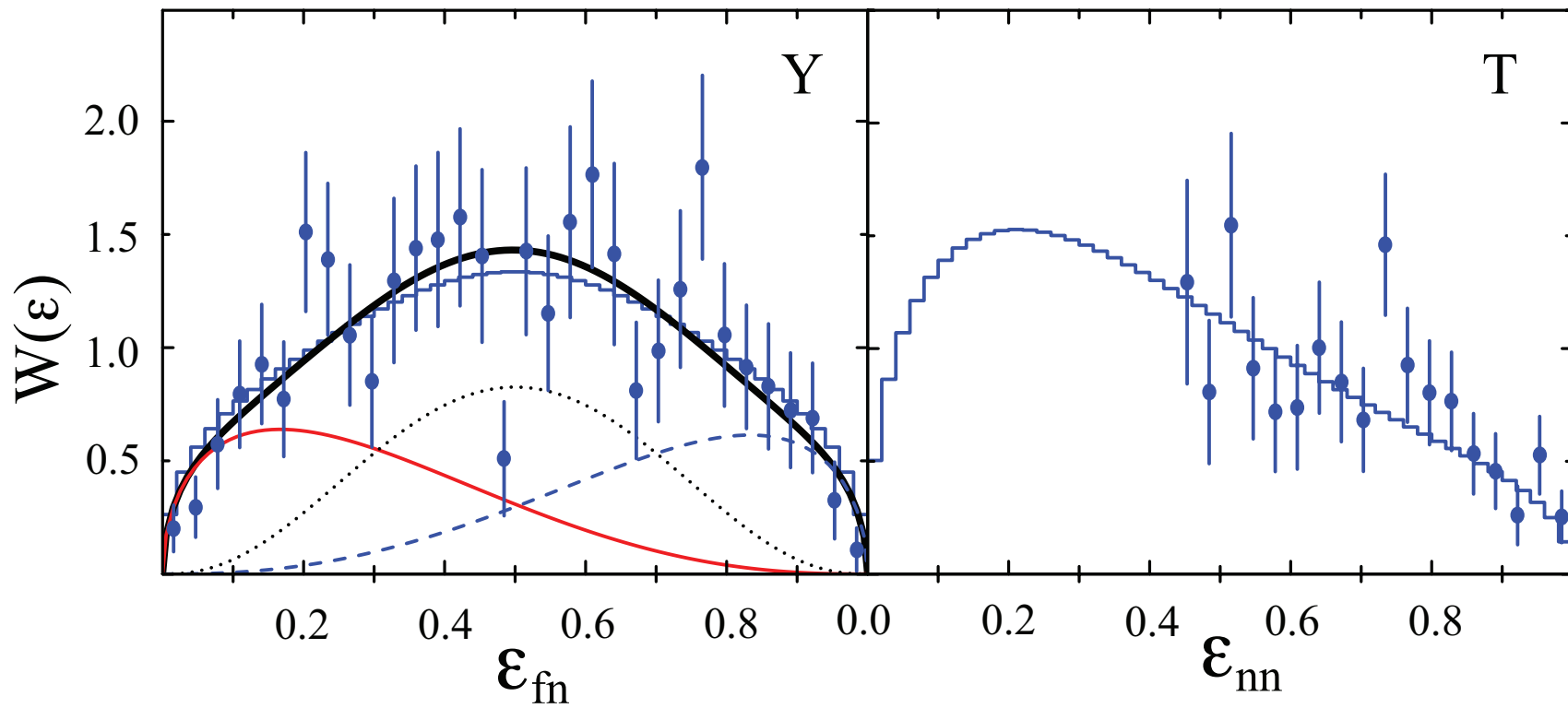
L.M. Delves, Nucl. Phys. **20** (1960) 275

$$W(\epsilon) \sim \sum_i A_i^2 \epsilon^{l_x^i + \frac{1}{2}} (1 - \epsilon)^{l_y^i + \frac{1}{2}}$$

E* = 3.54(16) MeV, Γ = 1.5 MeV
 I^π = 2⁺
 (1s_{1/2}, 0d_{5/2}) ≈ 90 %



$0.5 \text{ MeV} < E_{\text{fmn}} < 1.0 \text{ MeV}$



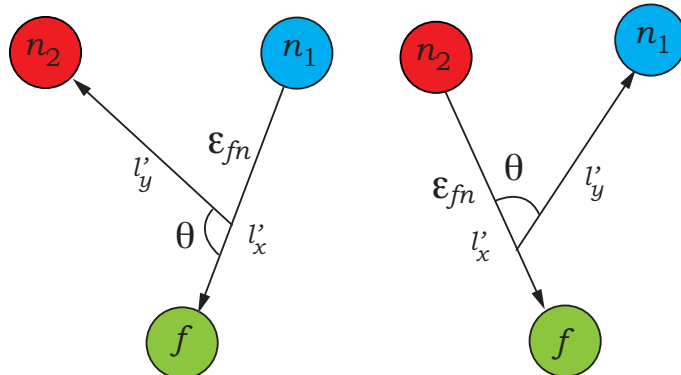
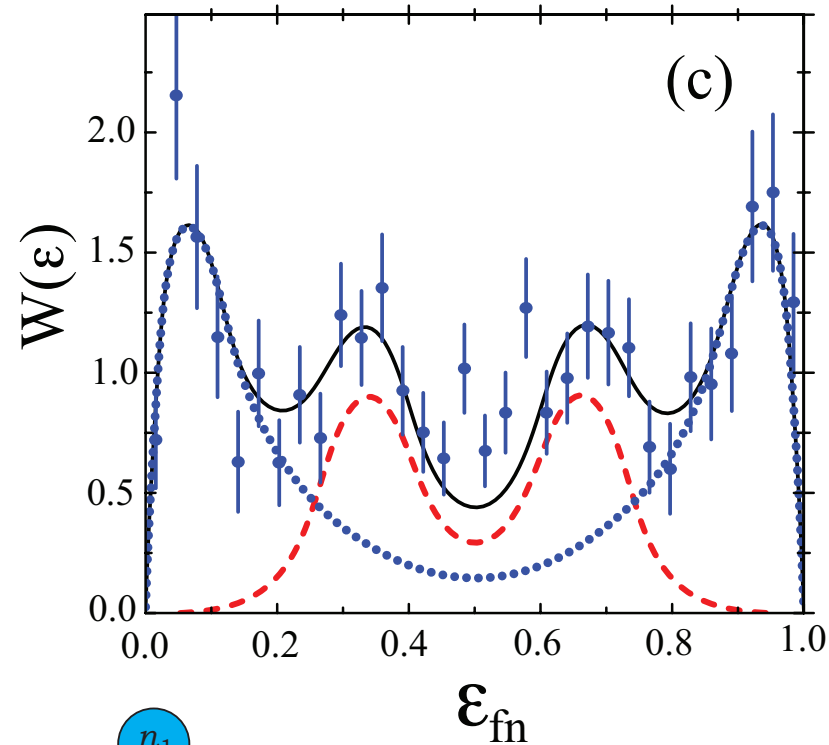
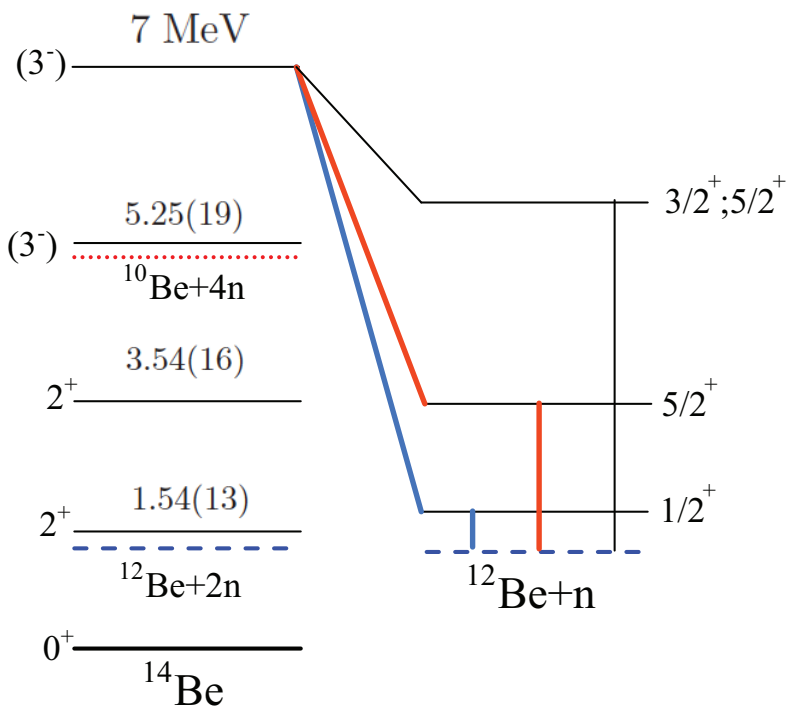
$${}^{12}\text{Be}(0^+) = {}^{10}\text{Be} \otimes \left[\alpha(1s_{1/2})_{I=0}^2 + \beta(0p_{1/2})_{I=0}^2 + \gamma(0d_{5/2})_{I=0}^2 \right]$$

$${}^{14}\text{Be}(2^+) = {}^{10}\text{Be} \otimes \left[\left\{ \begin{array}{l} \alpha_1(1s_{1/2})_{I=0}^2 \\ \alpha_2(0p_{1/2})_{I=0}^2 \\ \alpha_3(0d_{5/2})_{I=0}^2 \end{array} \right\} (0d_{5/2})_{I=2}^2 + \left\{ \begin{array}{l} \beta_1(0p_{1/2})_{I=0}^2 \\ \beta_2(0d_{5/2})_{I=0}^2 \end{array} \right\} (1s_{1/2}, 0d_{5/2})_{I=2} \right]$$

$$\alpha_1\alpha + \alpha_2\beta + \alpha_3\gamma \quad l = 2$$

$$\beta_1\beta + \beta_2\gamma \quad l = 0, 2$$

Sequential Decay

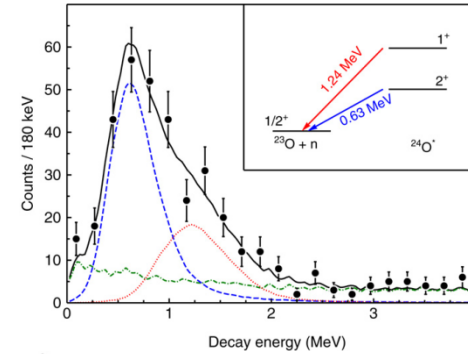
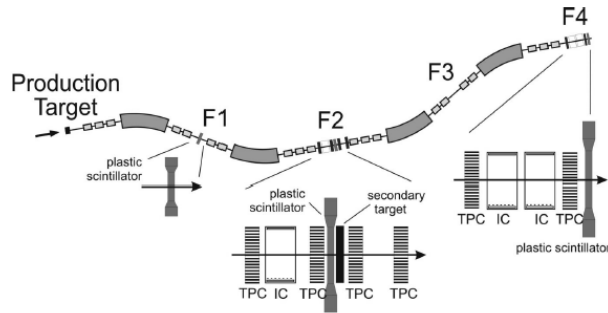


^{20}F 11 s	^{21}F 4.16 s	^{22}F 4.236 s	^{23}F 2.23 s	^{24}F 0.34 s	^{25}F 50 ms	^{26}F 10.2 ms	^{27}F 4.29 ms
^{19}O 27.1 s	^{20}O 13.5 s	^{21}O 3.4 s	^{22}O 2.25 s	^{23}O 82 ms	^{24}O 61 ms		
^{18}N 0.63 s	^{19}N 329 ms	^{20}N 142 ms	^{21}N 95 ms	^{22}N 24 ms	^{23}N 14.5 ms		
^{17}C 193 ms	^{18}C 92 ms	^{19}C 49 ms	^{20}C 14 ms		^{22}C 6.2 ms		

^{29}F
2.6 ms

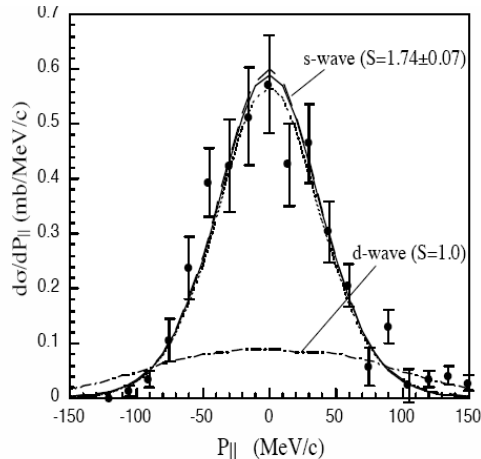
^{28}O
unbound

^{31}F
>260 ns

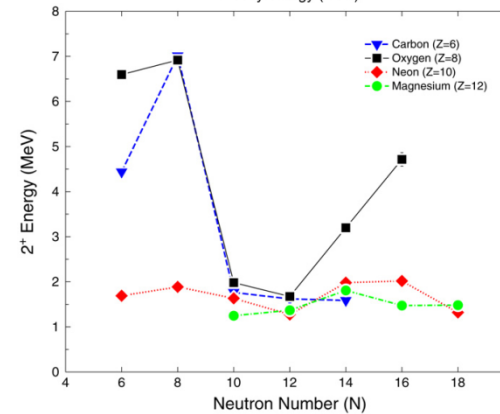


MSU

GSI



S=1.74(19)



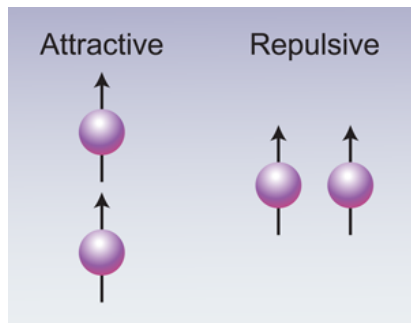
2⁺: 4.7 MeV

C.R. Hoffman et al.,
PLB **672** (2009) 17

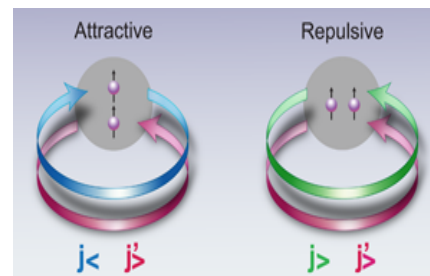
Shell evolution and nuclear forces

N.A. Smirnova *et al.*, PLB **686** (2010) 109

Novel Features of Nuclear Forces and Shell Evolution in Exotic Nuclei

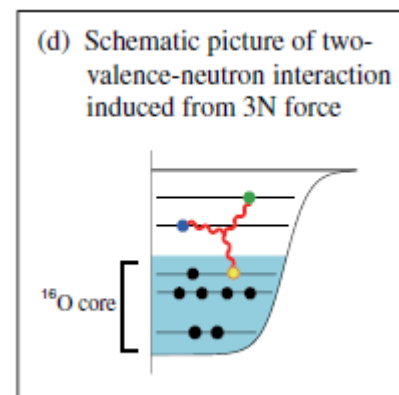
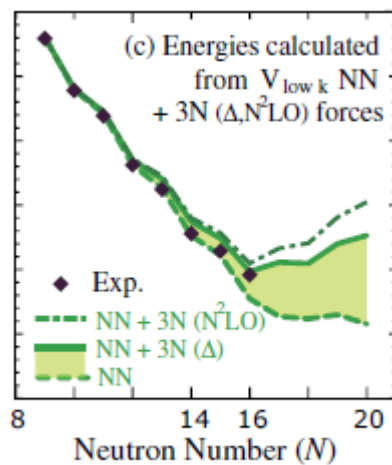
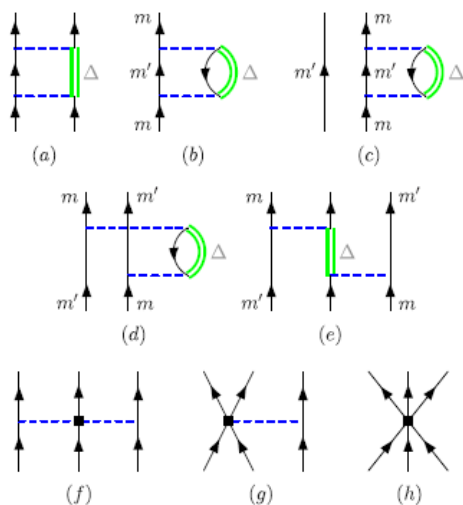


T. Otsuka *et al.*, PRL **104** (2010) 032501



Three-Body Forces and the Limit of Oxygen Isotopes

T. Otsuka *et al.*, PRL **105** (2010) 032501

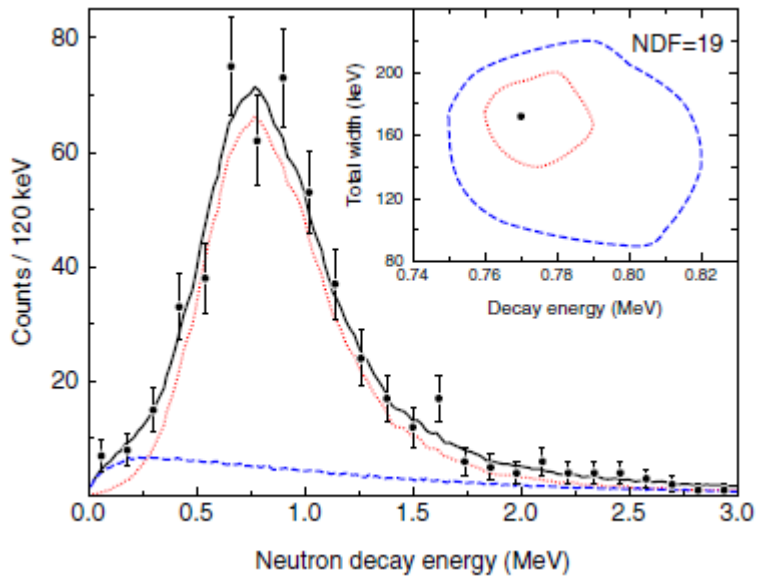


GSI : Data September 2010

^{24}F 0.34 s	^{25}F 50 ms	^{26}F 10.2 ms	^{27}F 4.9 ms	^{28}F unbound	^{29}F 2.6 ms	^{30}F unbound	^{31}F >260 ns
^{23}O 82 ms	^{24}O 61 ms	^{25}O unbound	^{26}O unbound		^{28}O unbound		



MoNA

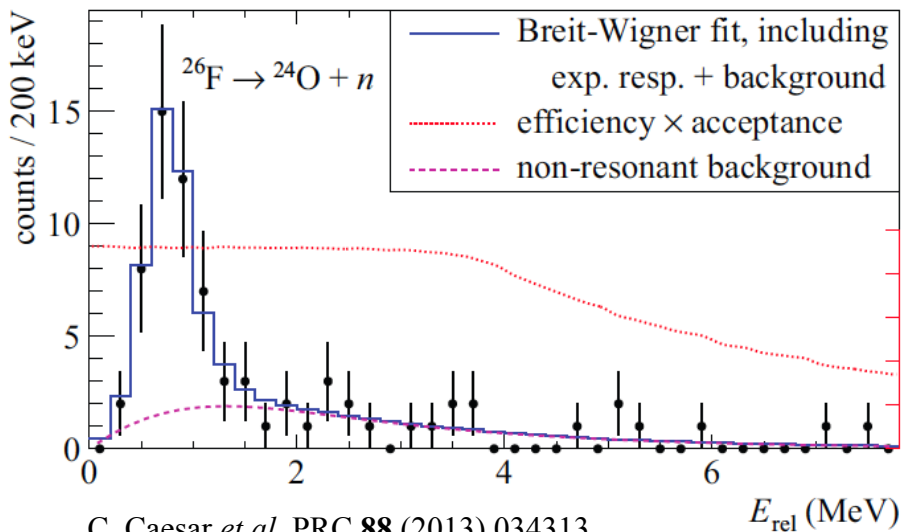
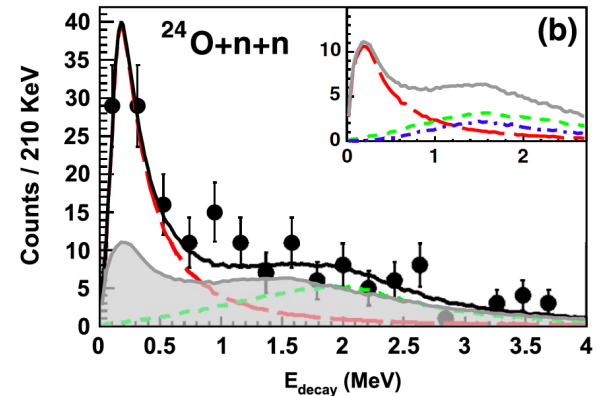


$E_{\text{decay}} = 770 \text{ keV}$,
 $\Gamma = 172 \text{ keV}$, $l=2$

Shell gap $\nu 1s_{1/2} - \nu 0d_{3/2}$
 4.86(13) MeV

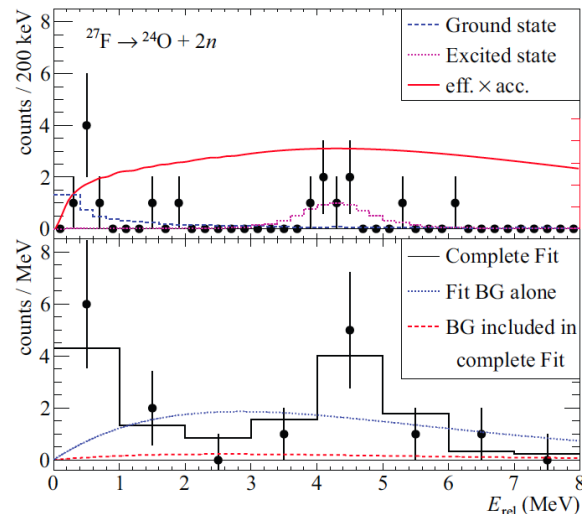
GSI : Data September 2010

^{24}F 0.34 s	^{25}F 50 ms	^{26}F 10.2 ms	^{27}F 4.9 ms	^{28}F unbound	^{29}F 2.6 ms	^{30}F unbound	^{31}F >260 ns
^{23}O 82 ms	^{24}O 61 ms	^{25}O unbound	^{26}O unbound		^{28}O unbound		



C. Caesar *et al.* PRC **88** (2013) 034313

E. Lunderberg *et al.* PRL **108** (2012) 142503



Two-neutron radioactivity ?

L.V. Grigorenko *et al.* PRL **111** (2013) 042501

Z. Kohley *et al.* PRL **110** (2013) 152501 ← $4.5^{+1.1}_{-1.5} \pm 3 \text{ ps}$



Nobelpriset i fysik 2013



François Englert
Université libre de
Bruxelles, Belgium

Peter W. Higgs
University of
Edinburgh,
UK

“For the theoretical discovery of a mechanism that contributes to our understanding of the origin of mass of subatomic particles, and which recently was confirmed through the discovery of the predicted fundamental particle, by the ATLAS and CMS experiments at CERN’s Large Hadron Collider.”

