

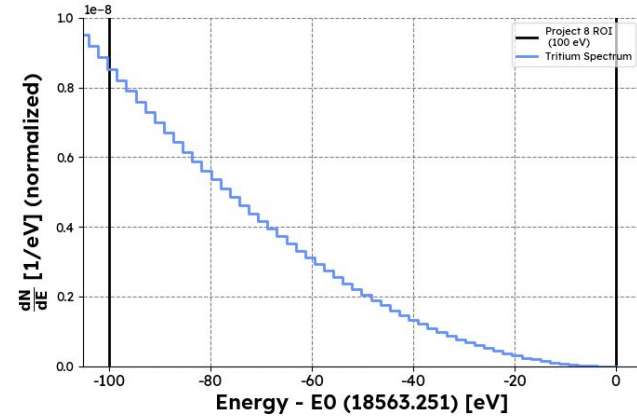
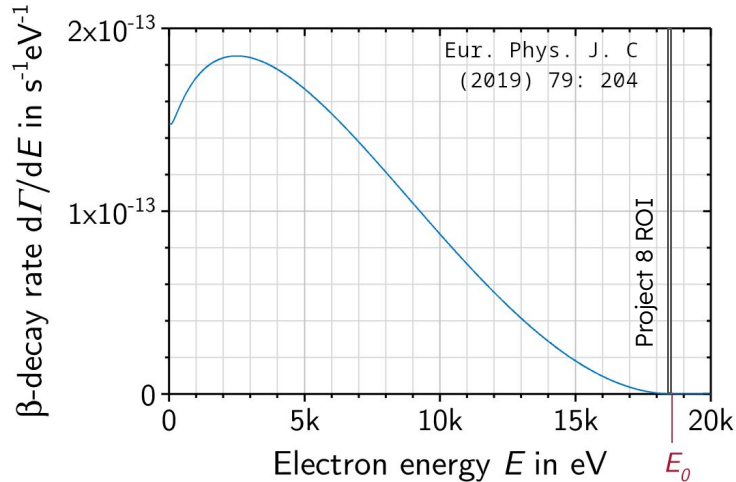
Exploring Cyclotron Radiation Emission Spectroscopy (CRES) Features in Project 8

Jan Küpperbusch

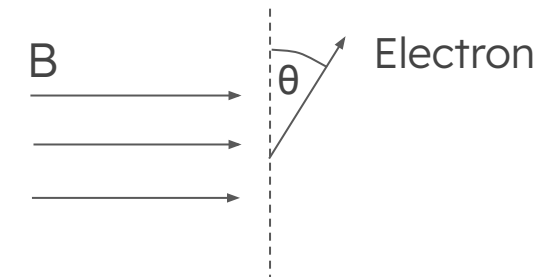
September 18th, 2026

INTERNATIONAL SCHOOL OF NUCLEAR PHYSICS, 47th Course

Measure the electron energy
Idea: spectrum from atomic tritium
beta decays

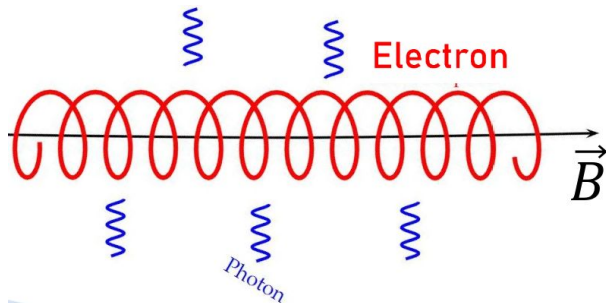


Rate in the final eV makes up $\sim 10^{-6}$ of
the total amount of signals
(assuming no endpoint effects of the neutrino mass)



Measure Frequency to reconstruct the energy: **C**yclotron **R**adiation **E**mission
Spectroscopy

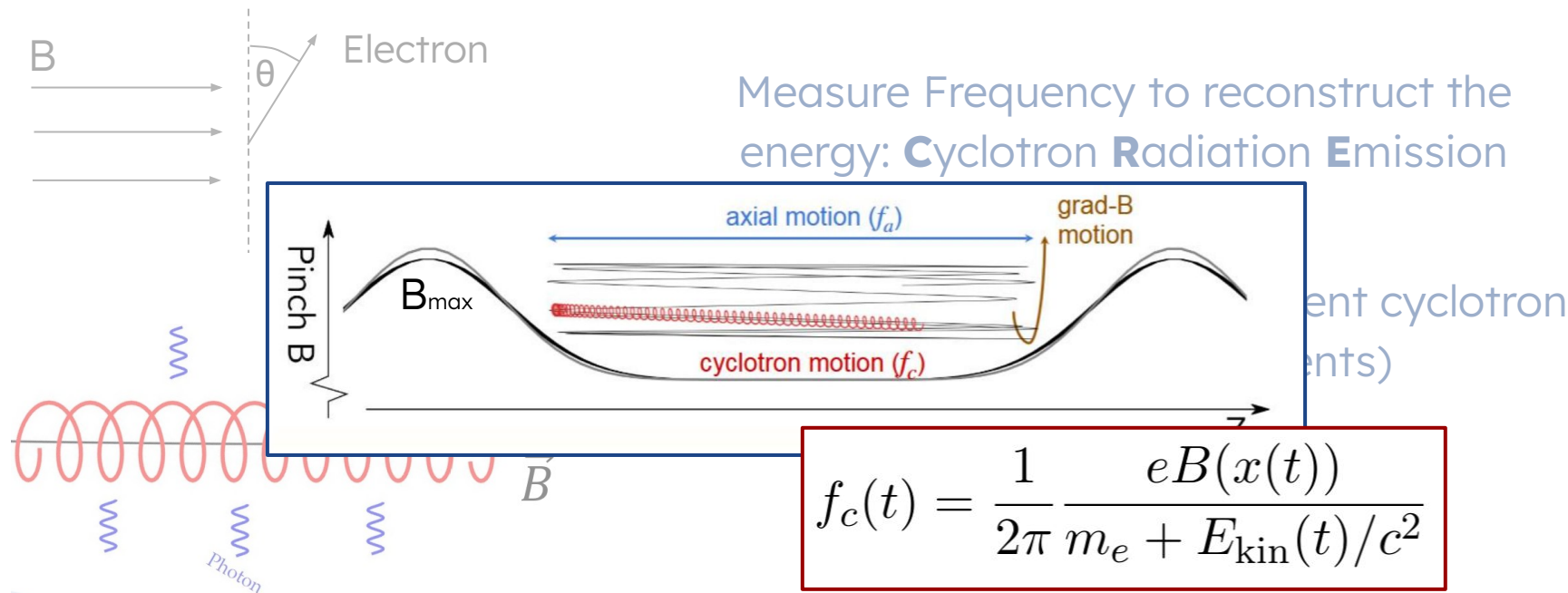
(Non-destructive time-dependent cyclotron frequency measurements)



$$f_c(t) = \frac{1}{2\pi} \frac{eB(x(t))}{m_e + E_{\text{kin}}(t)/c^2}$$

The CRES technique

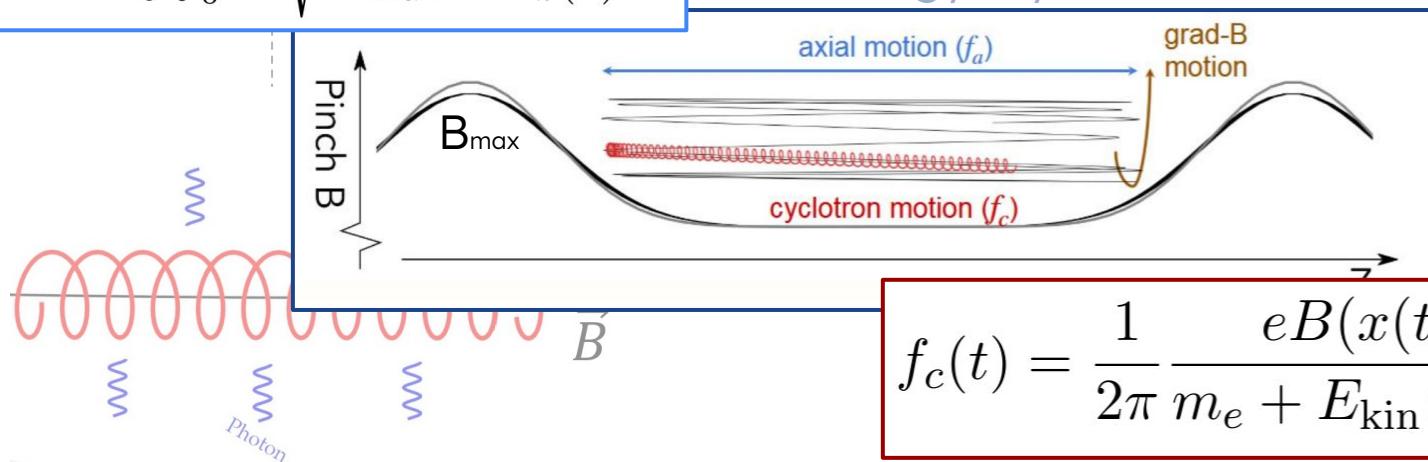
Measure Frequency to reconstruct the energy: **Cyclotron Radiation Emission**



The CRES technique

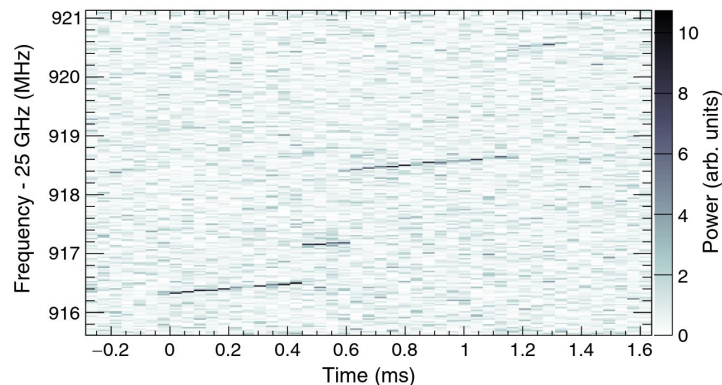
$$f_a = \frac{4}{v_0} \int_0^{z_m} \sqrt{\frac{B_{\max}}{B_{\max} - B_z(z)}} dz$$

Measure Frequency to reconstruct the energy: **Cyclotron Radiation Emission**



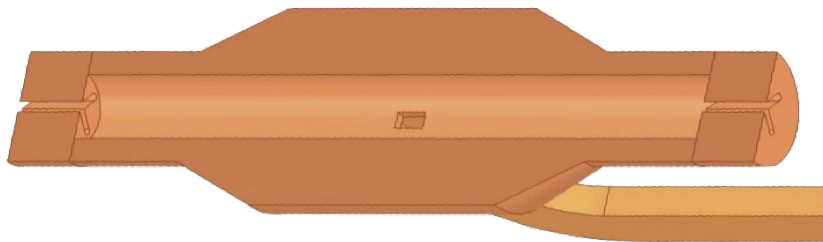
$$f_c(t) = \frac{1}{2\pi} \frac{eB(x(t))}{m_e + E_{\text{kin}}(t)/c^2}$$

The Cavity CRES Apparatus (CCA)



Project 8 Waveguide Spectrogram

Phys. Rev. Lett. 131 (2023) 10, 102502



Project 8 CCA Cavity + Waveguide readout (Credits:
J. Peña)

CCA involves a first resonant cavity
read out by a waveguide

- Axial frequency reconstruction possible
- Purcell enhancement of the radiated power

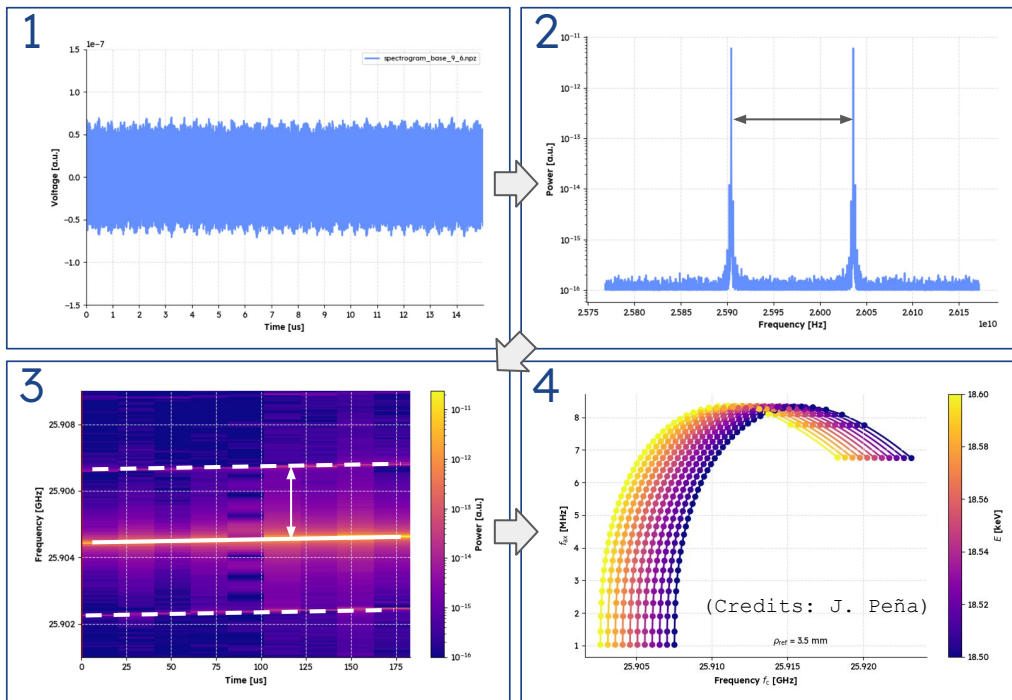
but also strong reliance on

- Correct alignment
- Magnetic field modelling
- Simulation-based reconstruction

The CCA reconstruction

Voltage
Timeseries

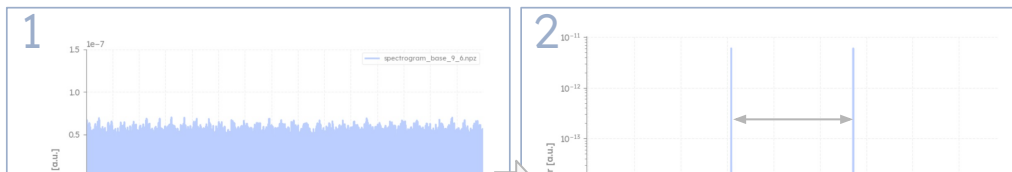
Spectrogram
and track ID
(Dependent on
the TE mode)



Short-scale
frequency
spectrum

Map axial and
cyclotron
frequency to
energy

The CCA reconstruction



What happens once we go to bigger volumes?

How to achieve large volume and high power?

Resonant cavities provide an attractive way of scaling Project 8 to large volumes

- High volume efficiency
- Power enhancement on resonance

LFA (Low Frequency Apparatus)

Magnetic field ~ 21mT
Frequency ~ 560MHz

Neutrino mass sensitivity

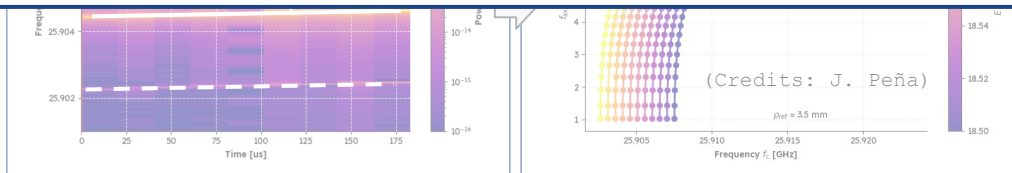
need more endpoint electrons

Previous talk from S. Hoienko

Stefanie Hoienko

INTERNATIONAL SCHOOL OF NUCLEAR PHYSICS

6



Pileup in the Low Frequency Apparatus (LFA)

Lower radiation power $P \sim f^2$
(560 MHz, currently 25.9 GHz)
Probability of signal pileup
will increase
(higher statistics)



<https://www.arsmundi.de>

How to achieve large volume and high power?

Resonant cavities provide an attractive way of scaling Project 8 to large volumes

- High volume efficiency
- Power enhancement on resonance

LFA
(Low Frequency Apparatus)

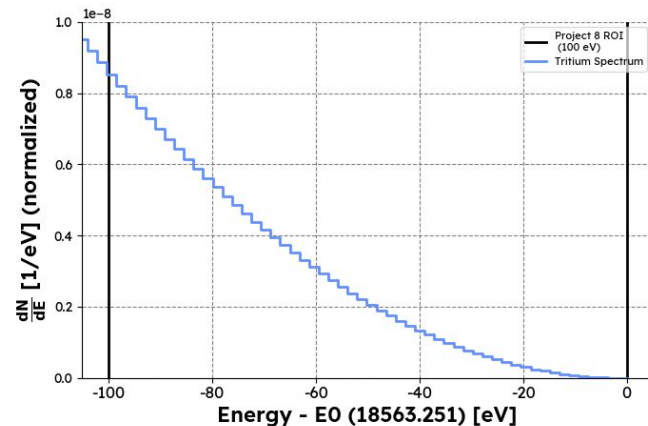
Magnetic field ~ 21 mT
Frequency ~ 560 MHz

Neutrino mass sensitivity

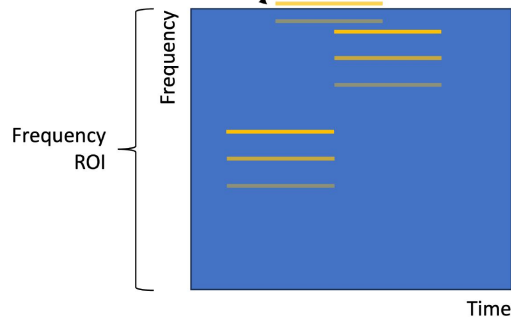
need more endpoint electrons

need larger

Previous talk from S. Hoenko



Electron outside of energy ROI generates a pileup event

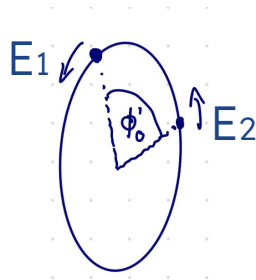


<- how does this pileup look like?

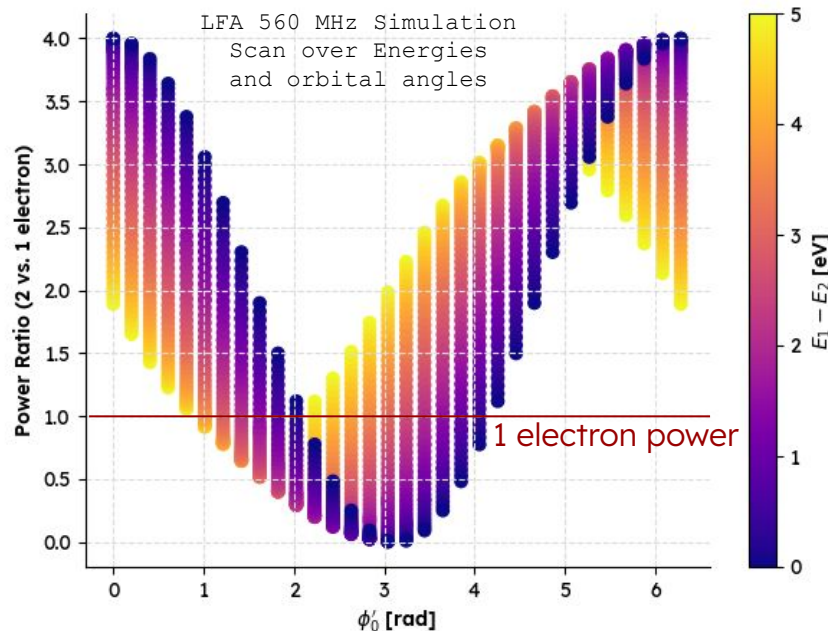
Credit:
H. Binney

LFA: Parametrization of power in pileup events

Scenario: Two
“chasing” electrons



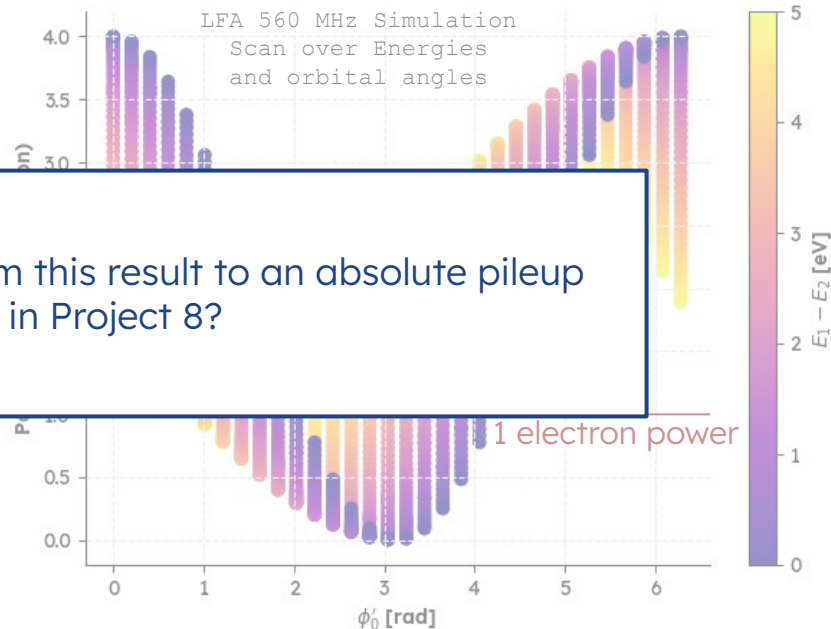
Mean power calculation and
simulational result agree on a
(dimensionless) power ratio factor
 $\Psi(\Delta f)$ (or equivalently, $\Psi(\Delta E)$)



$$\Psi = 2 + 2\alpha \cos(\varphi_0 + \beta) \quad \text{with } \alpha = \text{sinc}(\Delta\omega T/2), \beta = \Delta\omega T/2$$

LFA: Parametrization of power in pileup events

Scenario: Two
“chasing” electrons

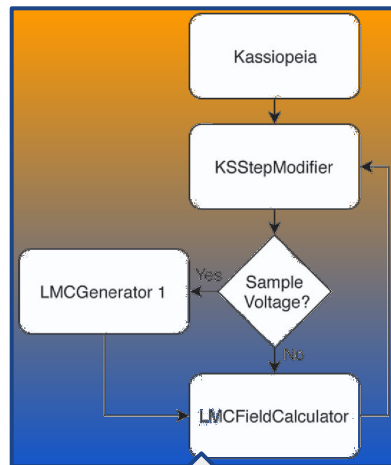


How do we abstractly move from this result to an absolute pileup
description in Project 8?

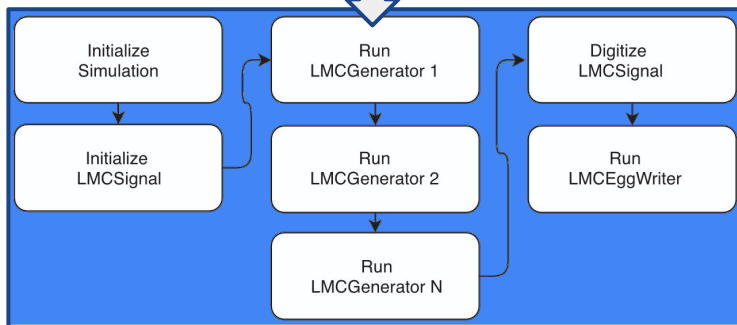
Mean power
simulation
(dimensionless) power ratio factor
 $\Psi(\Delta f)$ (or equivalently, $\Psi(\Delta E)$)

$$\Psi = 2 + 2\alpha \cos(\varphi_0 + \beta) \quad \text{with } \alpha = \text{sinc}(\Delta\omega T/2), \beta = \Delta\omega T/2$$

Project 8 simulations: Locust/Kassiopeia



Electron track
simulation:
Interface between
Locust (Simulation
of Trap/Cavity/
Readout) and
Kassiopeia (Track
building and EM
field simulation)



Locust: C++ software for simulation of RF detection

A Ashtari Esfahani¹, S Böser², N Buzinsky³, R Cervantes⁴, C Claessens⁵, L de Viveiros⁶, M Fertl^{1,2}, J A Formaggio⁷, L Gladstone⁸, M Guigue⁹, K M Heeger¹⁰, J Johnston¹¹, A M Jones¹², K Kazkaz¹³, B H LaRoque¹⁴, A Lindman¹⁵, E Machado¹⁶, B Monreal¹⁷, E C Morrison¹⁸, J A Nikkel¹⁹, E Novitski²⁰, N S Oblath²¹, W Pettus²², R G H Robertson²³, G Rybka²⁴, L Saldaña²⁵, V Sibille²⁶, M Schram²⁷, P L Slocum²⁸, Y-H Sun²⁹, J R T Desch³⁰, T Thümmel³¹, B A VanDevender³², M Wachtendonk³³, M Walter³⁴, T E Weiss³⁵, T Wendler³⁶ and E Zayas³⁷

¹ Center for Experimental Nuclear Physics and Astrophysics and Department of Physics, University of Washington, Seattle, WA 98195, United States of America

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⁴ Department of Physics, Pennsylvania State University, State College, PA 16802, United States of America

⁵ Department of Physics, Case Western Reserve University, Cleveland, OH 44106, United States of America

⁶ Pacific Northwest National Laboratory, Richland, WA 99354, United States of America

⁷ Wright Laboratory and Department of Physics, Yale University, New Haven, CT 06520, United States of America

⁸ Lawrence Livermore National Laboratory, Livermore, CA 94550, United States of America

⁹ Institut für Kernphysik, Karlsruher Institut für Technologie, Karlsruhe, Germany

E-mail: penny.slocum@yale.edu

Keywords: RF, radiation detection, simulation, antenna, C++

New J. Phys. 21 113051 (2019)

Kassiopeia: a modern, extensible C++ particle tracking package

Daniel Furse¹, Stefan Groh², Nikolaus Trost³, Martin Babutzka⁴, John P Barrett⁵, Jan Behrens⁶, Nicholas Buzinsky⁷, Thomas Corona^{8,9}, Sanshiro Enomoto¹⁰, Moritz Erhard¹¹, Joseph A Formaggio¹², Ferenc Glück¹³, Fabian Harms¹⁴, Florian Heizmann¹⁵, Daniel Hilk¹⁶, Wolfgang Käfer¹⁷, Marco Kleesiek¹⁸, Benjamin Leiber¹⁹, Susanne Mertens²⁰, Noah S Oblath²¹, Pascal Renschler²², Johannes Schwarz²³, Penny L Slocum²⁴, Nancy Wandkowsky²⁵, Kevin Wierman²⁶ and Michael Zacher²⁷

¹ Laboratory for Nuclear Science, Massachusetts Institute of Technology, Cambridge, MA 02139, United States of America

² Institute of Experimental Nuclear Physics (IEKP), Karlsruhe Institute of Technology (KIT), Wolfgang-Gaede-Str. 1, D-76131 Karlsruhe, Germany

³ Institute for Nuclear Physics (IKP), Karlsruhe Institute of Technology (KIT), Hermann-von-Helmholtz-Platz 1, D-76344 Eggenstein-Leopoldshafen, Germany

⁴ Institut für Kernphysik, Westfälische Wilhelms-Universität Münster, D-48149 Münster, Germany

⁵ Department of Physics and Astronomy, University of North Carolina, Chapel Hill, NC 27599, United States of America

⁶ Triangle Universities Nuclear Laboratory, Durham, NC 27708, United States of America

⁷ Center for Experimental Nuclear Physics and Astrophysics, Department of Physics, University of Washington, Seattle, WA 98195, United States of America

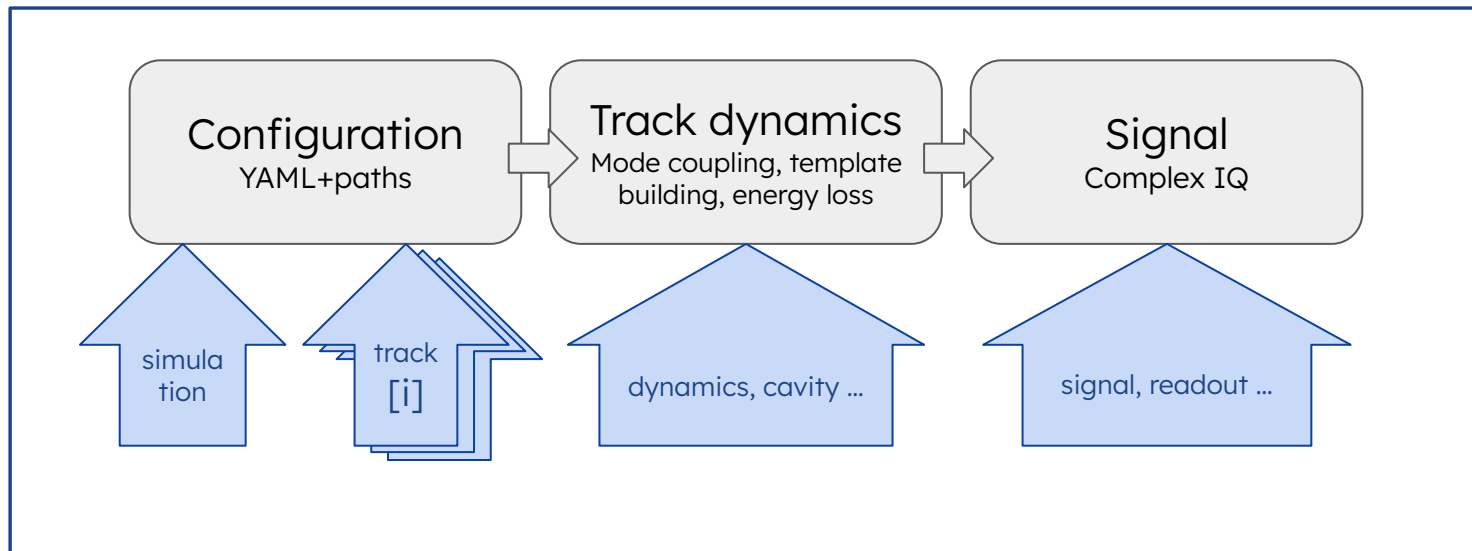
⁸ Wigner Research Institute for Physics, Budapest POB 49, Hungary

⁹ Max Planck Institute for Physics, Munich & Technical University Munich, D-80333 Munich, Germany

¹⁰ Department of Physics, Yale University, PO Box 208120, New Haven, CT 06520, United States of America

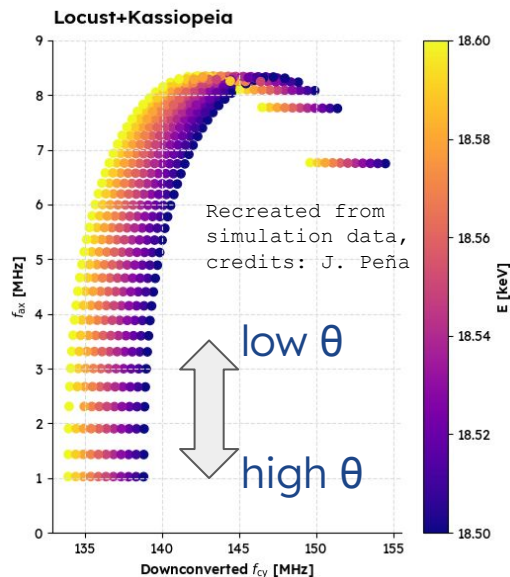
New J. Phys. 19 053012 (2017)

Project 8 simulations: Hopper, the new Kid in town

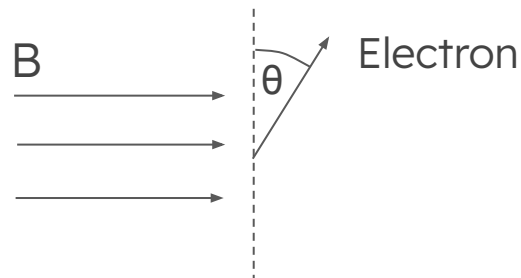


Recent development - Written in python - Capable of multi-electron pileup
Currently benchmarked against Locust/Kassiopeia

Comparing two simulation packages

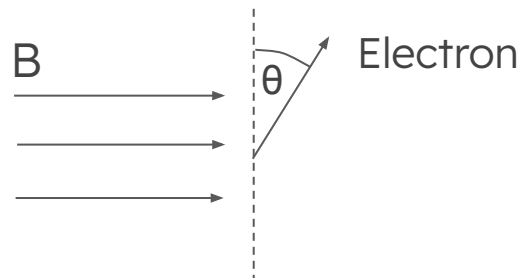
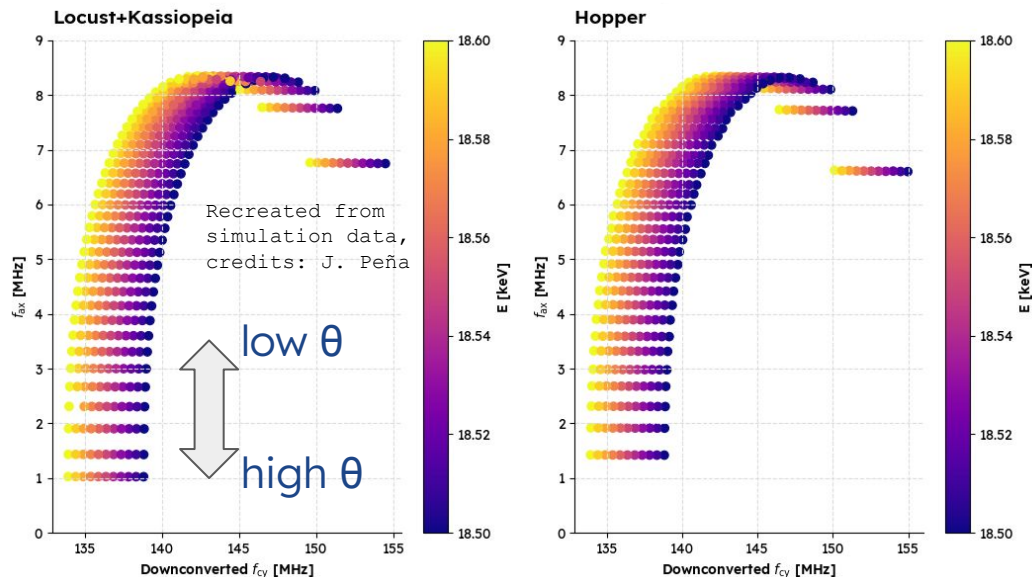


Locust: Given pitch angle and energy configuration results in specific axial and cyclotron frequency



Scan over Pitch angle θ
and electron energy E

Comparing two simulation packages

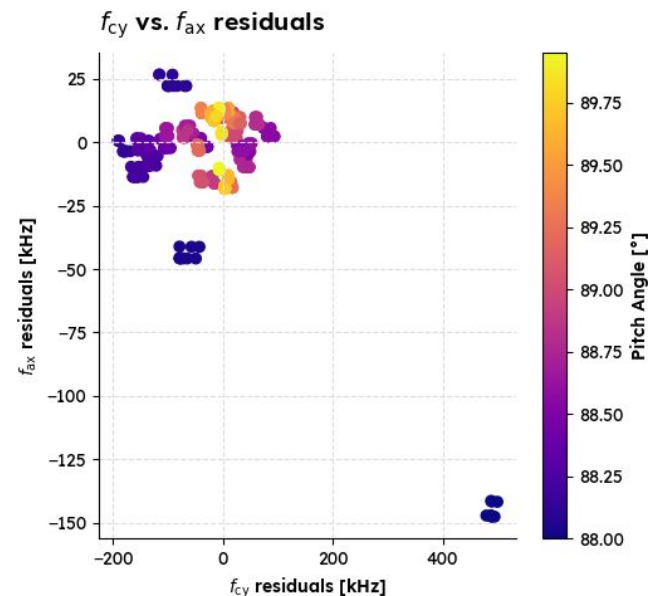
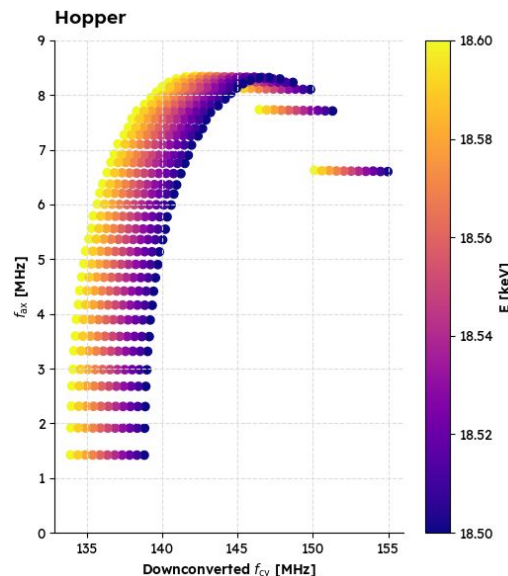
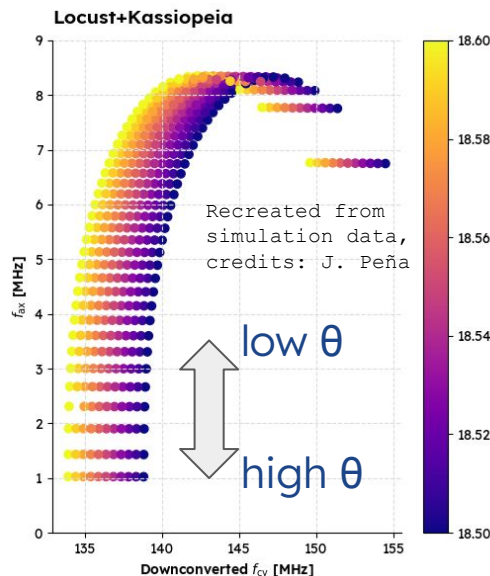


Scan over Pitch angle θ
and electron energy E

Locust: Given pitch angle and energy configuration results in specific axial and cyclotron frequency

Hopper may create these results much faster, but is it correct?

Comparing two simulation packages



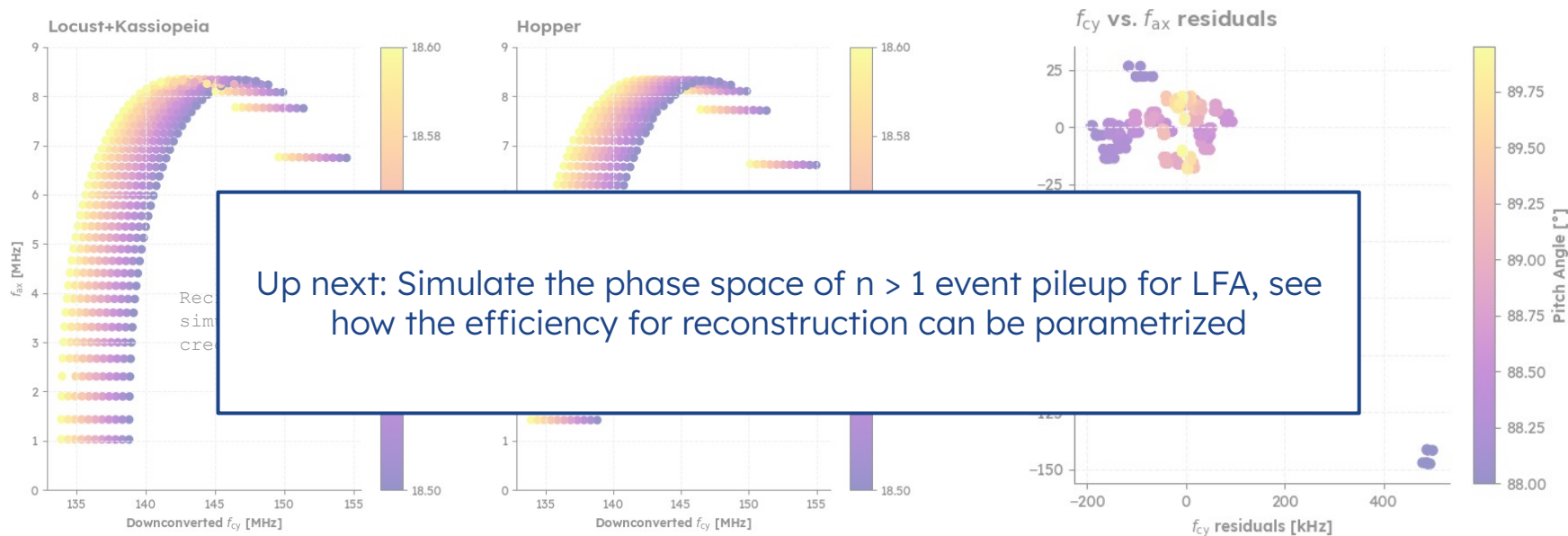
Locust: Given pitch angle and energy configuration results in specific axial and cyclotron frequency

Hopper may create these results much faster, but is it correct?

Current results show bigger residuals towards low pitch angles (high axial frequency)

Residuals: <2.5 % (f_{ax}), <0.4 % (f_{cy})

Comparing two simulation packages



Locust: Given pitch angle and energy configuration results in specific axial and cyclotron frequency

Hopper may create these results much faster, but is it correct?

Current results show bigger residuals towards low pitch angles (high axial frequency)
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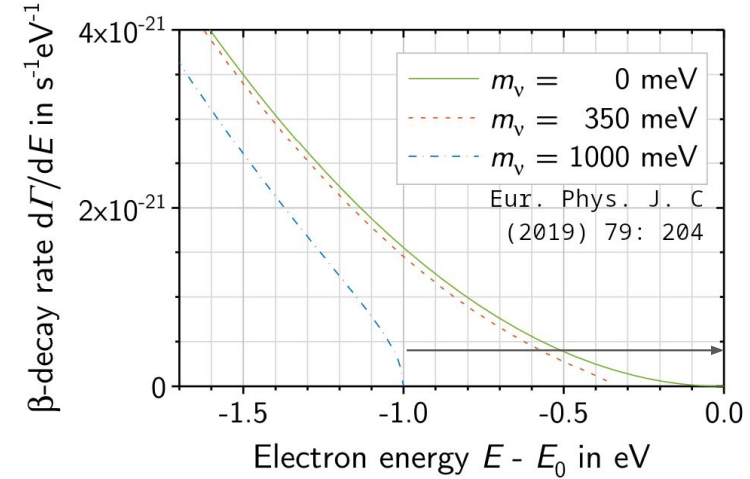
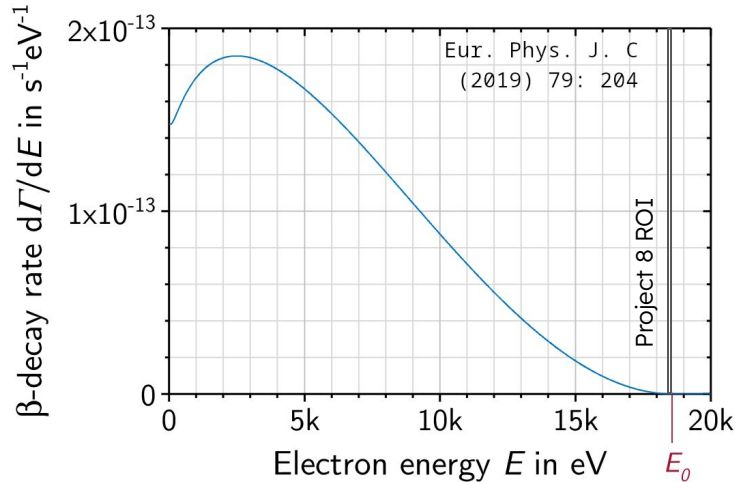
- Project 8: Non-destructive electron spectrometry
- Cavities:
 - Increase information gain through resonant amplification
 - allow axial frequency measurement
- Challenges:
 - Power decreases with lower frequency
 - High statistics require a well-prepared reconstruction
- Simulation:
 - Locust/Kassiopeia: Physics-wise gold standard, workhorse
 - Hopper: Developed for large simulation sets

A scenic landscape view from a hilltop. In the foreground, a black lamppost is visible on the left, and a metal railing runs along the edge of the hill. The middle ground shows a vast valley with a city and a large body of water. The background features distant mountains under a clear blue sky with some light clouds on the right.

Thank you for your attention!
Questions?

Backup

Measure the electron energy
Idea: spectrum from atomic Tritium
beta decays



Distortion of the high energy tail is
related to the neutrino mass

$$\left. \frac{dN}{dE} \right|_{\text{End}} \sim (E - E_0) \sqrt{(E - E_0)^2 - m_\beta^2}$$

The **PROJECT 8** Experiment



UWashingon, Spring 2026

21 Institutions, three countries, over 60 graduate- or higher researchers

Multi-stage experiment aiming to lower the experimental limit for m_β using atomic tritium

Tritium Beta Spectrum and Neutrino Mass Limit from Cyclotron Radiation Emission Spectroscopy

A. Ashtari Esfahani,^{1,2} S. Böser,² N. Buzinsky,² M. C. Carmona-Benitez,⁴ C. Claessens,^{1,2} L. de Viveiros,⁴ P. J. Doe,¹ M. Forti,² J. A. Formaggio,³ J. K. Gibson,⁵ L. Gladstone,⁶ M. Grando,⁵ M. Guigue,⁷ J. Hartse,¹ K. M. Heeger,⁸ X. Huyen,⁹ J. Johnson,² A. M. Jones,¹⁰ K. Kazkaz,² B. H. LaRoque,² M. Li,¹ A. Lindman,² E. Machado,¹ A. Marsteller,¹ C. Matthé,² R. Mohiuddin,⁶ B. Mourel,⁶ R. Mueller,⁴ J. A. Nikkel,⁸ E. Novitski,¹ N. S. Oblath,⁵ J. I. Peña,³ W. Pettus,¹⁰ R. Reinsman,² R. G. H. Robertson,¹ D. Ross De Jesus,⁵ G. Rybka,¹ L. Saldaña,⁸ M. Schram,⁵ P. L. Slomum,⁸ J. Stachurska,³ Y.-H. Sun,⁶ P. T. Surukuchi,⁸ J. R. Tedeschi,⁵ A. B. Telles,⁸ F. Thomas,² M. Thomas,¹² L. A. Thorne,² T. Thümmel,¹ L. Tvrznikova,⁹ W. Van De Pontseele,³ B. A. VanDevender,^{1,5} J. Weintroub,¹² T. E. Weiss,⁸ T. Wendler,⁴ A. Young,¹² E. Zayas,³ and A. Ziegler⁴
(Project 8 Collaboration)

¹Center for Experimental Nuclear Physics and Astrophysics and Department of Physics, University of Washington, Seattle, WA 98195, USA

²Institute for Physics, Johannes Gutenberg University Mainz, 55128 Mainz, Germany

³Laboratory for Nuclear Science, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

⁴Department of Physics, Pennsylvania State University, University Park, PA 16802, USA

⁵Pacific Northwest National Laboratory, Richland, WA 99354, USA

⁶Department of Physics, Case Western Reserve University, Cleveland, OH 44106, USA

⁷Laboratoire de Physique Nucléaire et de Hautes Energies, Sorbonne Université, Université Paris Cité, CNRS/IN2P3, 75005 Paris, France

⁸Wright Laboratory and Department of Physics, Yale University, New Haven, CT 06520, USA

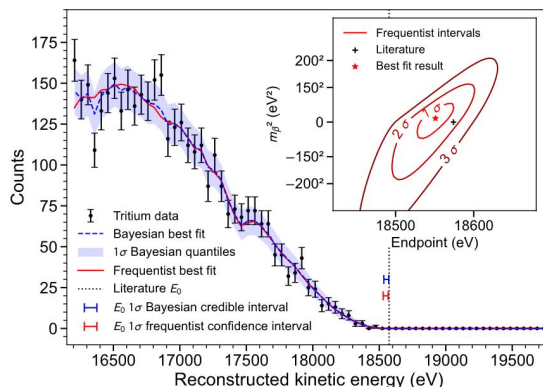
⁹Lawrence Livermore National Laboratory, Livermore, CA 94550, USA

¹⁰Center for Exploration of Energy and Matter and Department of Physics, Indiana University, Bloomington, IN, 47405, USA

¹¹Institute of Astroparticle Physics, Karlsruhe Institute of Technology, 76035 Karlsruhe, Germany

¹²Center for Astrophysics | Harvard & Smithsonian, Cambridge, MA 02138, USA

(Dated: March 20, 2023)

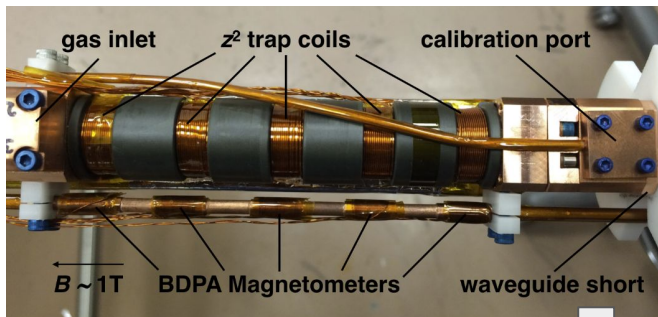


First two stages proved that:

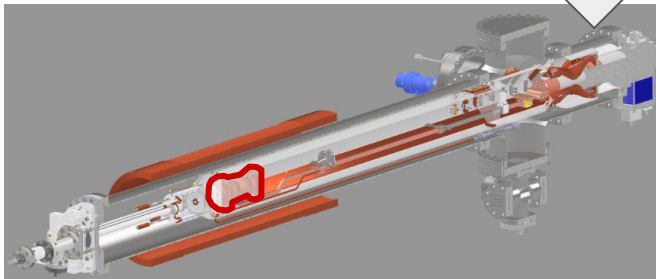
- CRES works using antennas and waveguides
- upper neutrino limits can be extracted

Phys. Rev. Lett. 131 (2023) 10, 102502

Transition from Waveguides to Cavities



Project 8 Phase II Waveguide insert
(J. Phys. G 44 (2017) 5, 054004)



Project 8 Phase III Experimental Apparatus
(Credits: S. Kuenstner)

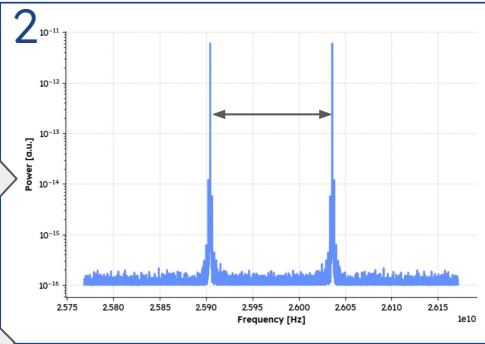
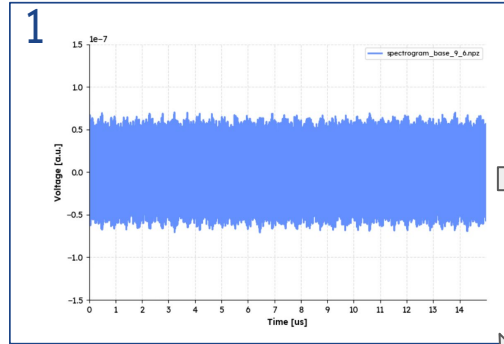
Phase 2 was executed in a WR-42 waveguide

Phase 3 involves a first resonant cavity read out by a waveguide

- Axial frequency reconstruction possible
- First use of cryogenic amplifiers

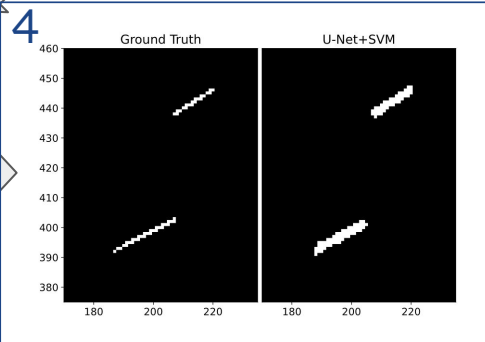
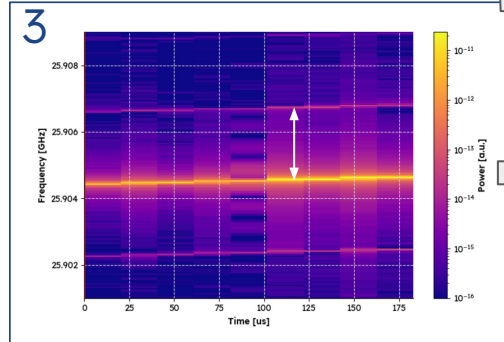
The Project 8 Phase III reconstruction (2nd approach)

Voltage
Timeseries



Short-scale
frequency spectrum

Spectrogram

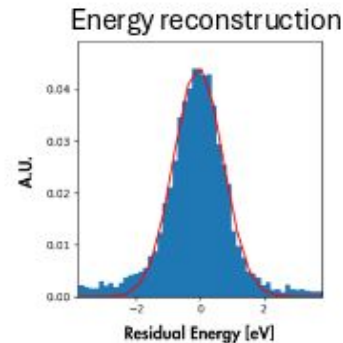
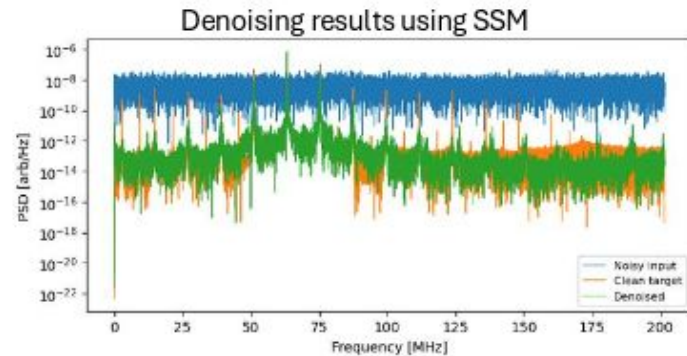


Map axial and
cyclotron frequency
to energy over
machine learning
(U-NET, GNN, SSM)

Mach. Learn. Sci. Tech. 5
(2024) 2, 025026

State Space Model (SSM):

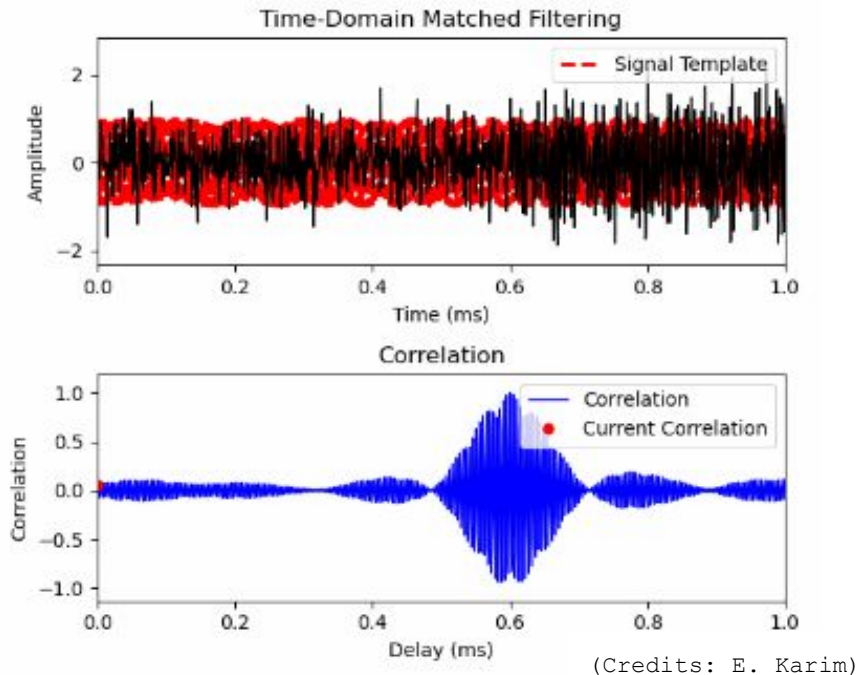
- Machine-learning propelled time series reconstruction
- More dynamically usable than the current reconstruction
- Currently explored both in frequency and in pure time domain reconstruction



(Credits:
H. Binney,
C. Reissel,
L. Felipe Koehler
Domingues)

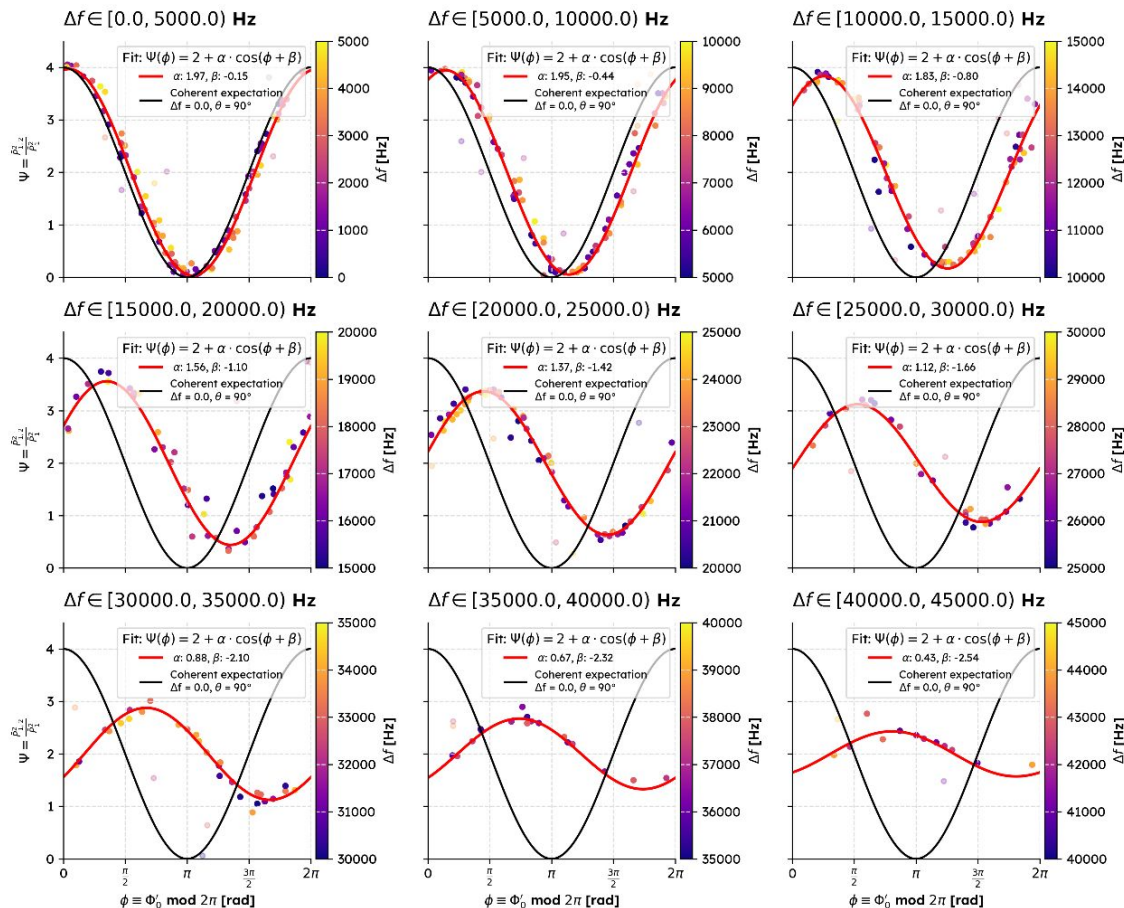
Time domain matched filtering:

- Simulation-informed template fitting
- More conventional approach
- Computation power!



Disect sampled Locust simulations into Δf slices

- Power ratio curve shift
chronically to the right
- loses coherent
interference pattern



$$P(t) \propto (s_1 + s_2)^2 = 2A^2 [1 + \cos(\Delta\omega t + \varphi_0)]$$

$$\begin{aligned} \langle P \rangle &= \frac{1}{T} \int_0^T P(t) dt \\ &= 2A^2 \left[1 + \frac{1}{\Delta\omega T} (\sin(\Delta\omega t T + \varphi_0) - \sin(\varphi_0)) \right] \end{aligned}$$

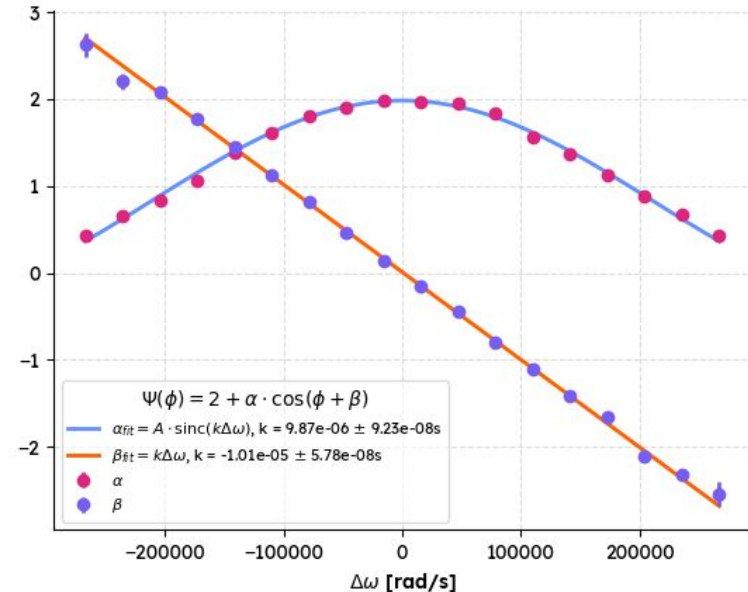
using $\sin(x + y) - \sin(x) = 2 \cos(x + y/2) \sin(y/2)$, we find

$$\begin{aligned} \langle P \rangle &= 2A^2 \left[1 + \frac{2}{\Delta\omega T} (\cos(\varphi_0 + \Delta\omega T/2) \sin(\Delta\omega T/2)) \right] \\ &= 2A^2 \left[1 + \frac{\sin(\Delta\omega T/2)}{\Delta\omega T/2} \cos\left(\varphi_0 + \frac{\Delta\omega T}{2}\right) \right] \end{aligned}$$

Dividing that by the average power of one particle, $\langle P_1 \rangle = A^2$, the ratio of the average powers Ψ may sufficiently be simplified to

$$\Psi = 2 + 2\alpha \cos(\varphi_0 + \beta) \quad \text{with } \alpha = \text{sinc}(\Delta\omega T/2), \beta = \Delta\omega T/2$$

$\alpha = 2\text{sinc}(k\Delta\omega), \beta = -k\Delta\omega$
expected $k = 8192/(2 * 403\text{e}6 \text{ Hz}) = 1.02\text{e-}05\text{s}$



$$S(t) = \sum_i a(\omega_i) e^{i(\omega_i t + \varphi_i)}$$

Spectrogram FFT

$$P(\omega) = |\mathcal{F}\{S(t)\}_T|^2$$

$$= \left| \int_0^T dt \sum_i a(\omega_i) e^{i(\omega_i - \omega)t} e^{i\varphi_i} \right|^2$$

$$= \left| \sum_i a(\omega_i) \operatorname{sinc}\left(\frac{(\omega - \omega_i)T}{2}\right) e^{i(\varphi_i + (\omega_i - \omega)\frac{T}{2})} \right|^2$$