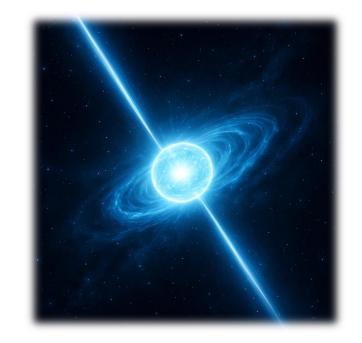
Observational Probes of the Neutron Star Equation of State with Hyperons, Sexaquarks, and Quark Matter

Avraham's talk: deeply bound H-dibaryon

Davood Rafiei Karkevandi

Institute of Theoretical Physics, Wroclaw University, Poland

EMMI Workshop 5th Workshop Anti-Matter, Hyper-Matter and Exotica Production at the LHC, Nov 10-14, 2025, Salerno, Italy















Observational Probes of the Neutron Star Equation of State with Hyperons, Bosonic Dark Matter, and Quark Matter

Mahboubeh Shahrba $f^{1,2,3\star}$, Davood Rafiei Karkevandi 1** , Alexander Ayriyan 1,4*** , and Stefan Typel 5,6

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- Frankfurt Institute for Advanced Studies, Giersch Science Center, D-60438 Frankfurt am Main, Germany
- ⁴ Alikhanyan National Science Laboratory (Yerevan Institute of Physics), Alikhanyan Brothers St 2, 0036 Yerevan, Armenia
- ⁵ Technische Universität Darmstadt, Fachbereich Physik, Institut für Kernphysik, Schlossgartenstraße 9, D-64289 Darmstadt, Germany
- ⁶ GSI Helmholtzzentrum für Schwerionenforschung GmbH, Theorie, Planckstraße 1, D-64291 Darmstadt, Germany

arXiv:2402.18686v2

Accepted for publication in Astronomy & Astrophysics

Probing Strange Dark Matter through f-mode Oscillations of Neutron Stars with Hyperons and Quark Matter

Mahboubeh Shahrbaf¹,* Prashant Thakur²,† and Davood Rafiei Karkevandi¹† Institute of Theoretical Physics, University of Wroclaw, 50-204 Wroclaw, Poland and ²Department of Physics, Yonsei University, Seoul, 03722, South Korea

arXiv:2510.08115

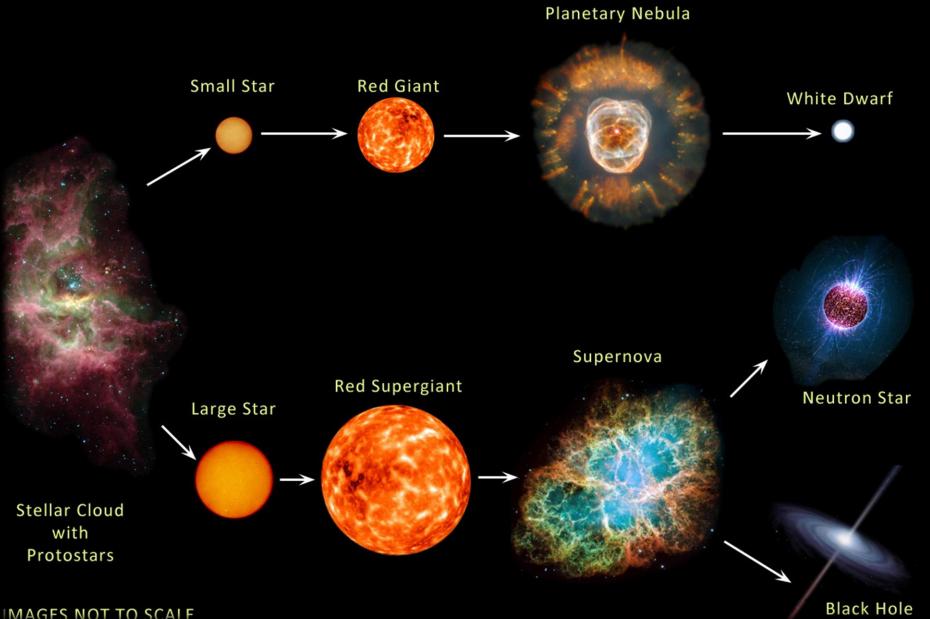




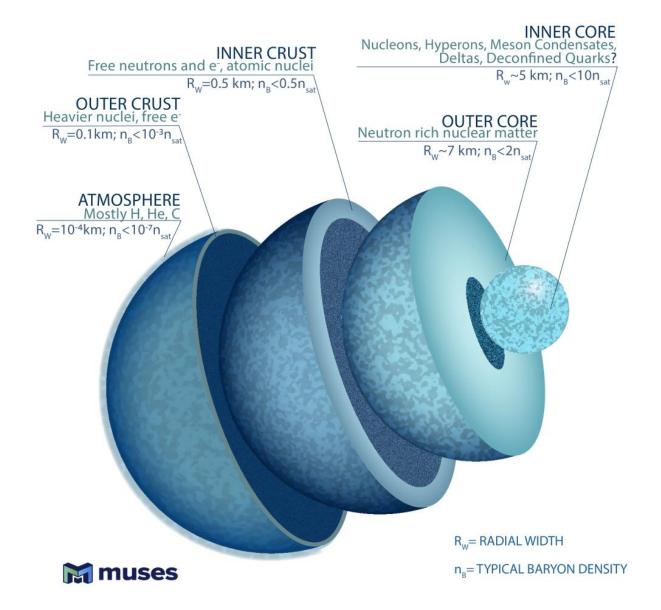


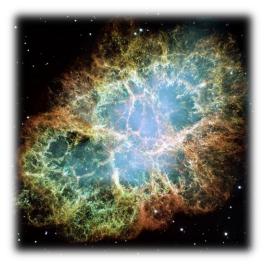


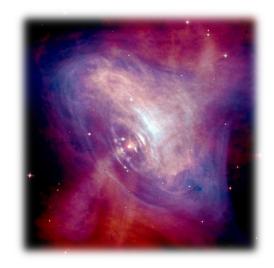
EVOLUTION OF STARS



Crab Pulsar





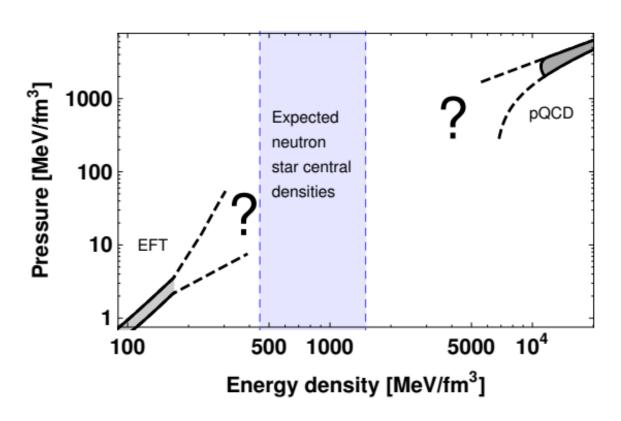


Mass \sim 1.4 – 2 solar mass ($M\odot$)

Radius $\sim 10 - 13$ km

Neutron stars as a natural laboratory for high density matter

Equation of state of ultra-high density matter $oldsymbol{P} = oldsymbol{P}(oldsymbol{arepsilon})$



10⁴ $Max(c_s^2) \leq$ 10³ 1.0 Pressure (MeV fm⁻³) 8.0 10² 0.6 10¹ 0.4 1/3 10⁰ 10² 10³ 10⁴ Energy density (MeV fm⁻³)

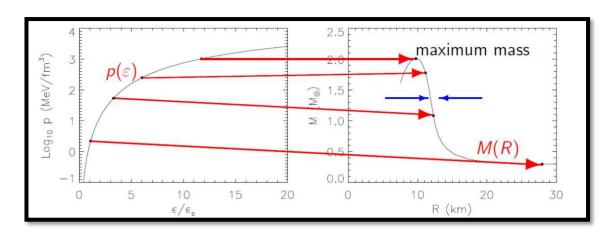
Matti Järvinen, *Eur. Phys. J. C (2022) 82:282*

Eemeli Annala, *Nature Phys. 16 (2020) 9, 907-910*

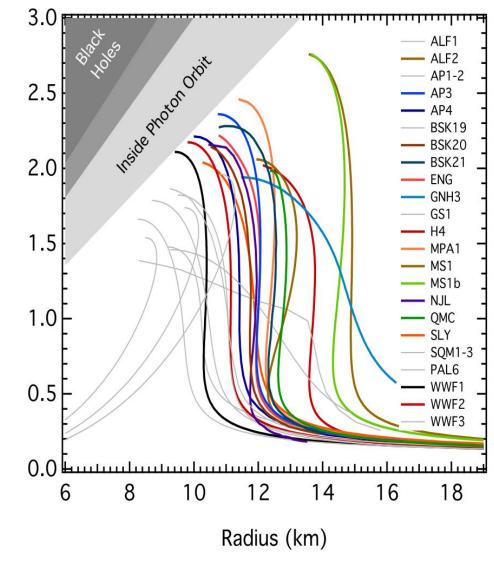
Tolman-Oppenheimer-Volkof (TOV) equations

$$\frac{dP(r)}{dr} = -\frac{GM(r)\,\varepsilon(r)}{c^2r^2} \left[1 + \frac{P(r)}{\varepsilon(r)}\right] \left[1 + \frac{4\pi r^3 P(r)}{M(r)c^2}\right] \left[1 - \frac{2GM(r)}{c^2r}\right]^{-1}$$
R. C. Tolman, Phys. Rev. 55, 364 (1939).

$$\frac{dM(r)}{dr} = \frac{4\pi r^2 \varepsilon(r)}{dr}$$
J. R. Oppenheimer and G. M. Volko, Phys. Rev. 55,374 (1939).



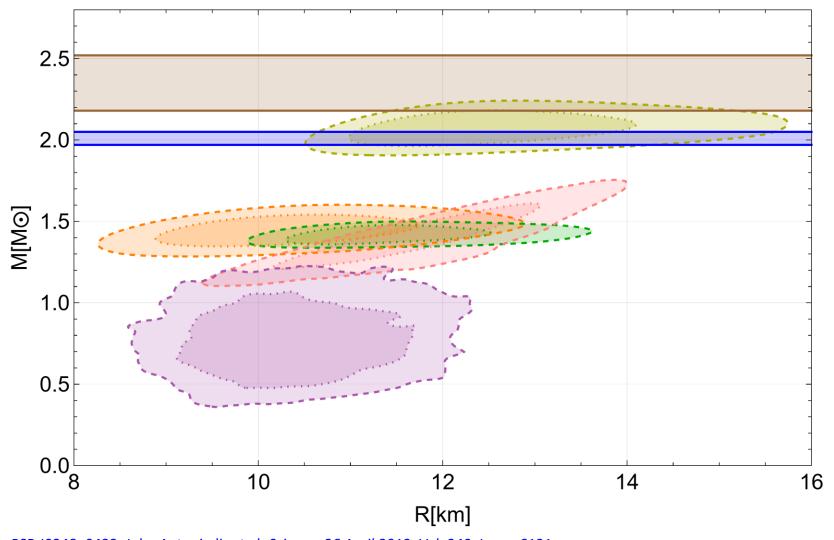
James Latimer, EPJ Web of Conferences 109, 07004 (2016)



Mass (M_☉)

Feryal Özel & Paulo Freire Ann.Rev.Astron.Astrophys. 54 (2016) 401-440

Mass-Radius observational constraints



PSR J0348+0432, John Antoniadis et al, *Science, 26 April 2013, Vol: 340, Issue: 6131*

PSR J0030+0451, S. Vinciguerra et al., <u>Astrophys. J. 961, 62 (2024)</u>
PSR J0740+6620, T. Salmi et al., <u>Astrophys. J. 974, 294 (2024)</u>
PSR J0614-3329, Lucien Mauviard et al, <u>arXiv:2506.14883</u>

HESS J1731-347, Doroshenko et al, *Nature Astron., 6, 1444, 2022*PSR J0437–4715, D. Choudhury et al., *Astrophys. J. Lett. 971, L20 (2024)*PSR J0952–0607, W. Romani et al, *ApJL 934 L17, 2022*

NICER X-ray Telescope



Keck Optical Telescopes



Green Bank Radio Telescope





week ending 20 OCTOBER 2017

GW170817: Observation of Gravitational Waves from a Binary Neutron Star Inspiral

B. P. Abbott et al.*

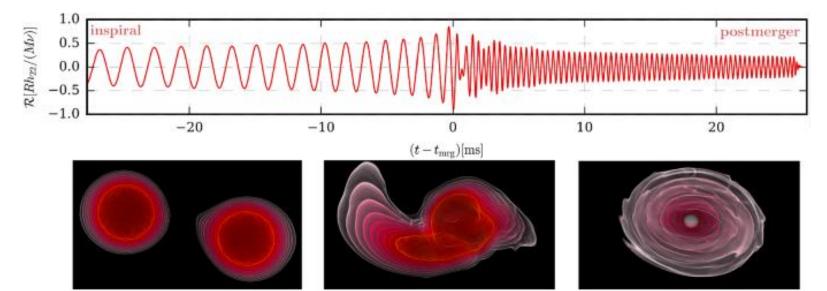
(LIGO Scientific Collaboration and Virgo Collaboration)

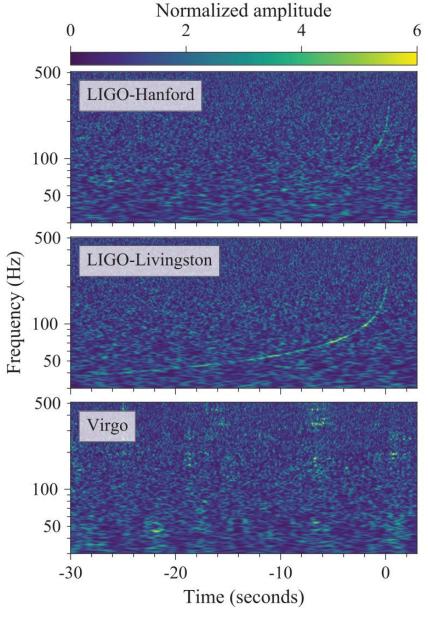
(Received 26 September 2017; revised manuscript received 2 October 2017; published 16 October 2017)



LIGO-Virgo Gravitational-Wave detectors





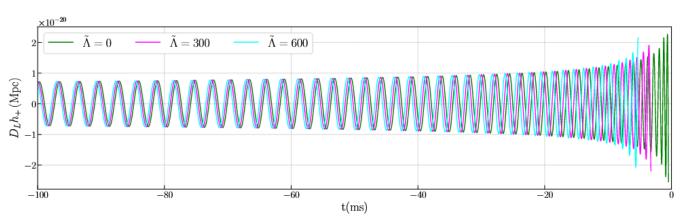


Deformation of the neutron star in the binary systems due to the tidal force

Dimensionless tidal deformability:
$$\Lambda = \frac{\lambda_t}{M^5} = \frac{2}{3} k_2 \left(\frac{R}{M}\right)^5$$

R and M are the mass and radius of star k_2 : Dimensionless tidal love number

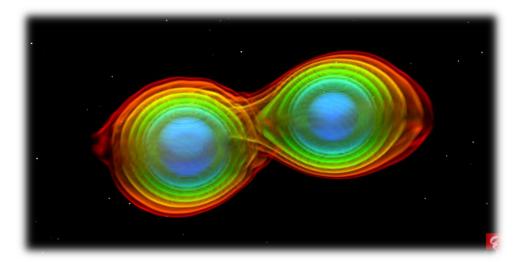
Tanja Hinderer, et al. Phys. Rev. D81:123016,2010



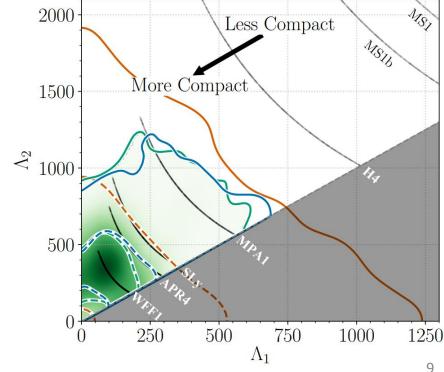
Katerina Chatziioannou, Gen. Rel. Grav. 52 (2020) 11, 109

Dimensionless tidal deformability GW170817 $70 \le \Lambda \le 580 \text{ for } M = 1.4M\odot$

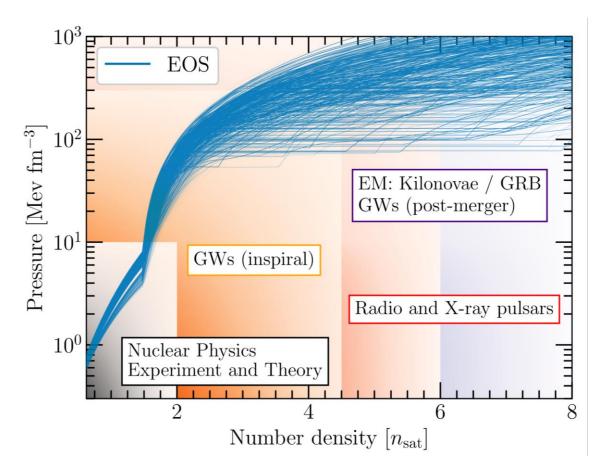
LIGO Scientific and Virgo Collaborations, Phys. Rev. Lett. 121 (2018) 16



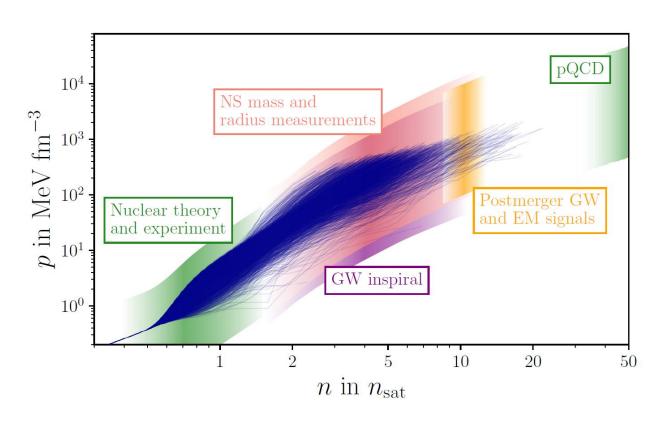
Tim Dietrich et al. Max Planck Institute



Constraining the EOS of high-density matter by multi-messenger observations of neutron stars

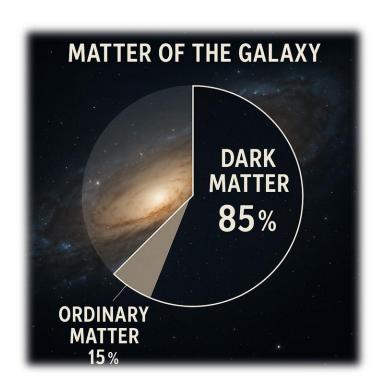


Peter T. H. Pang, et al., Nature Commun. 14 (2023) 1, 8352



Hauke Koehn et al. Phys. Rev. X 15 (2025) 2, 021014

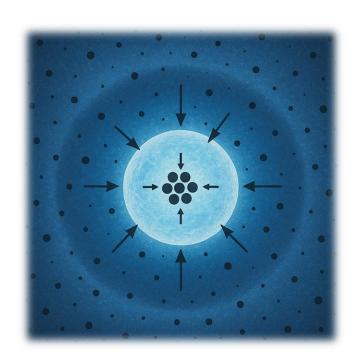
Dark matter constitutes about 85% of the matter in the universe, yet it remains a challenging puzzle in physics.





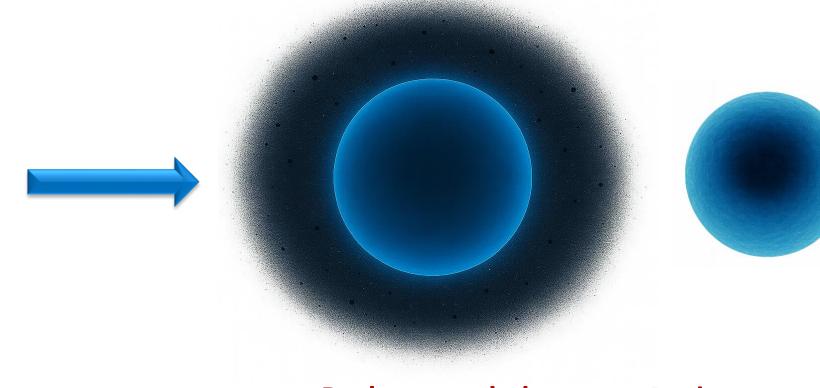
Main goal is to <u>constrain the parameter space</u> of the dark matter models and looking for signature

Neutron stars, due to their <u>high densities</u> and <u>strong gravity</u>, are promising astrophysical laboratories for probing the properties of dark matter.





Dark matter production in the neutron star matter or supernova explosions



<u>Dark matter halo</u> around neutron star **Dark matter core** inside neutron star

Jürgen

D.R.K, S. Shakeri, V. Sagun, O. Ivanytskyi,

Bosonic dark matter in neutron stars and its effect on gravitational wave signal

Phys. Rev. D 105, 023001 (2022) [159 citations]

D.R.K, S. Shakeri, V. Sagun, O. Ivanytskyi,

Tidal deformability as a probe of dark matter in neutron stars

World Scientific pp. 3713-3731 (2023) [21 citations]

S. Shakeri, D.R.K

Bosonic Dark Matter in Light of the NICER Precise Mass-Radius Measurements

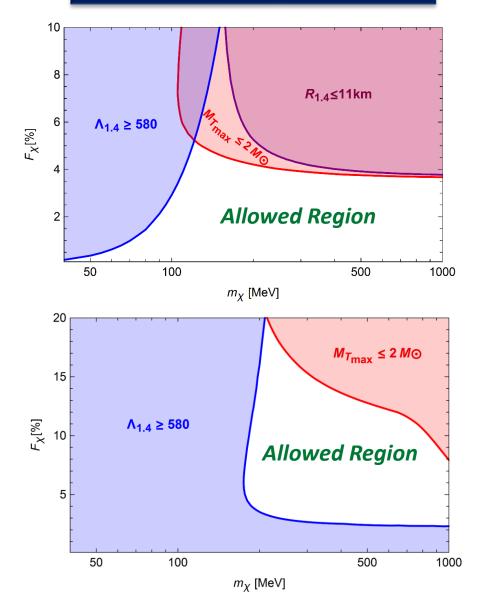
Phys. Rev. D 109, 043029 (2024) [77 citations]

D.R.K, M. Shahrbaf, S. Shakeri, S. Typel

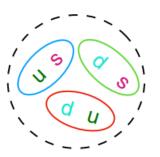
Exploring the distribution and impact of bosonic dark matter in neutron stars

Particles 7 1, 201-213 (2024) [25 citations]

Accretion of dark matter inside neutron stars



Sexaquark a bosonic dark matter candidate



Glennys R. Farrar

arXiv:2201.01334, review paper

Home > International Journal of Theoretical Physics > Article

A Stable H-Dibaryon: Dark Matter,
Candidate Within QCD?

Published: June 2003

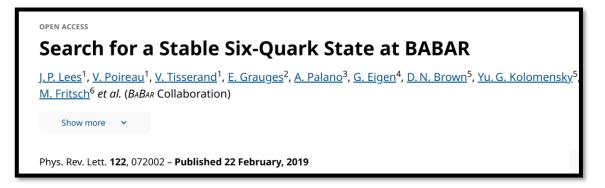
Volume 42, pages 1211–1218, (2003) Cite this article

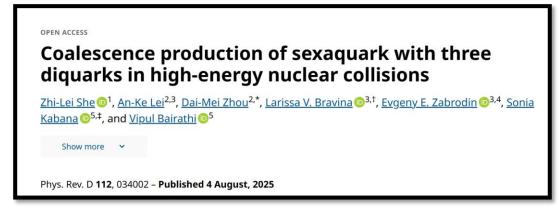
Sexaguark (Mass: ~2 GeV)

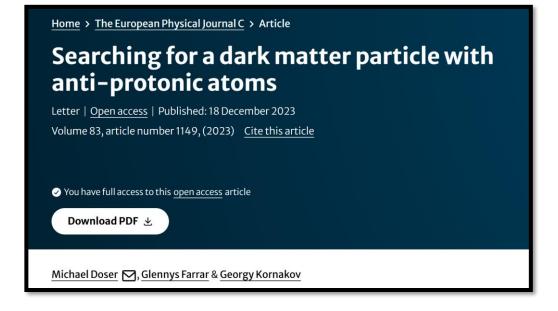
(S=uuddss): bosonic, spin-color-flavor singlet, deeply bound

Q=0, B=2, s=-2

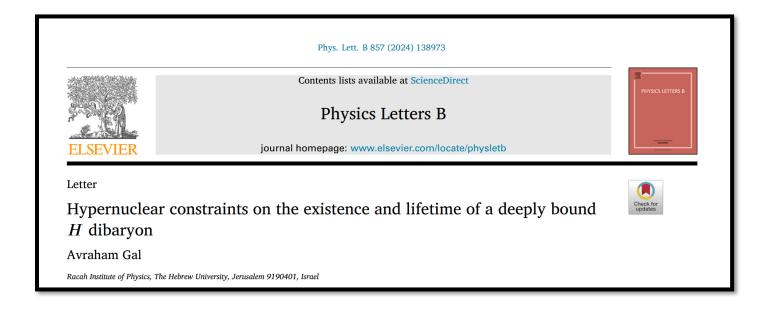
If $m_s \le (m_A + m_p + m_e) = 2054$ MeV, it will decay with a lifetime more than the age of the universe.







Sexaquark cannot be a dark matter candidate





Sexaquark dilemma in neutron stars and its solution by quark deconfinement

M. Shahrbaf 1,*, D. Blaschke 1,2,3,†, S. Typel 1,5,‡, G. R. Farrar 1,6,§, and D. E. Alvarez-Castillo 1,2,3,†

Show more 💙

Phys. Rev. D **105**, 103005 – **Published 4 May, 2022**

For the first time Sexaquark dark matter (?) or exotic particle was investigated via its production in high density matter of neutron stars

Hadronic EOS:

- ➤ A generalized relativistic density functional (GRDF) approach
- DD2Y-T (includes hyperons) Mon. Not. Roy. Astron. Soc., 502, 3476 2021
- Exotic matter component: sexaquark (S) included in hadronic sector

$$m_S^* = m_S(1 + x_S \frac{n_b}{n_0})$$

- Parameters: $m_S \in [\mathbf{1885} \mathbf{2054}] \mathit{MeV}$, $x_S = \mathbf{0.03}$
- $\succ x_S$ is the slope parameter and represents the coupling strength

Quark matter EOS:

nINJL model

- The most likely parameters were selected within a Bayesian analysis (BA)
- ➤ Mapped to the constant speed of sound (CSS) parameterization

M. Shahrbaf, et al. 2023, Phys. Rev. D, 107, 054011

Two sets of Parameters (η_D, η_V, c_S^2) have been used (0.70, 0.10, 0.44) & (0.70, 0.11, 0.44)

The model RIC-DD2Y-T- S_{m_s} describes a neutron star that includes Nucleons, Hyperons, Sexaquark dark matter (?) or exotic particle and Quark matter

Phase transition:

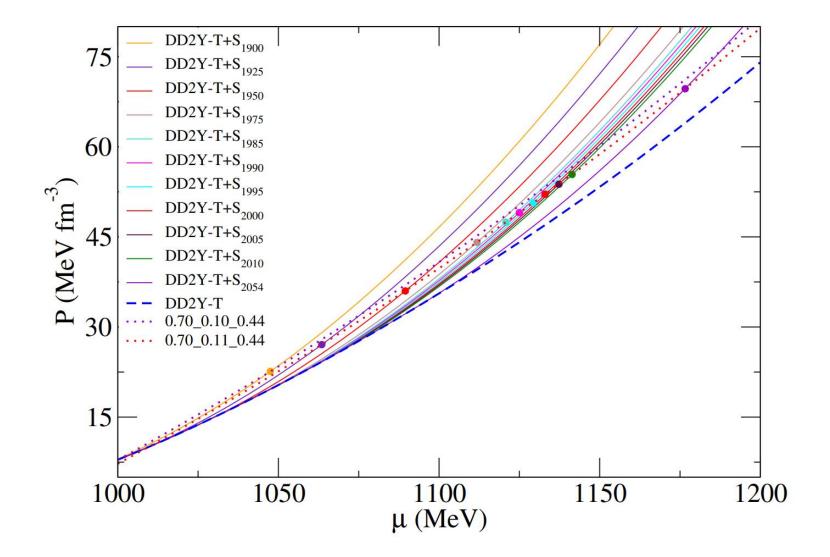
- Smooth crossover phase transition from hadronic matter to deconfined quark matter
- Replacement Interpolation Construction (RIC)

M. Shahrbaf, D. Blaschke, S. Khanmohamadi, J. Phys. G: Nucl. Part. Phys. 47 (2020) 115201

A. Ayriyan et al. <u>Phys. Rev. C 97, 045802</u>

Observational Probes of the Neutron Star Equation of State with Hyperons, Bosonic Dark Matter, and Quark Matter

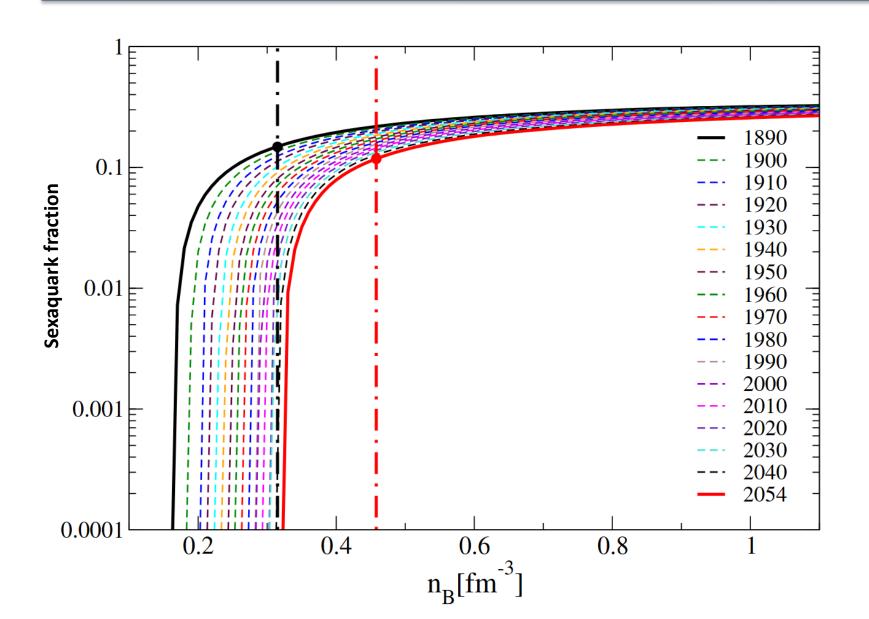
Mahboubeh Shahrbaf^{1,2,3*}, Davood Rafiei Karkevandi^{1**}, Alexander Ayriyan^{1,4***}, and Stefan Typel^{5,6}



<u>arXiv:2402.18686v2</u> <u>Accepted for publication in</u> Astronomy & Astrophysics

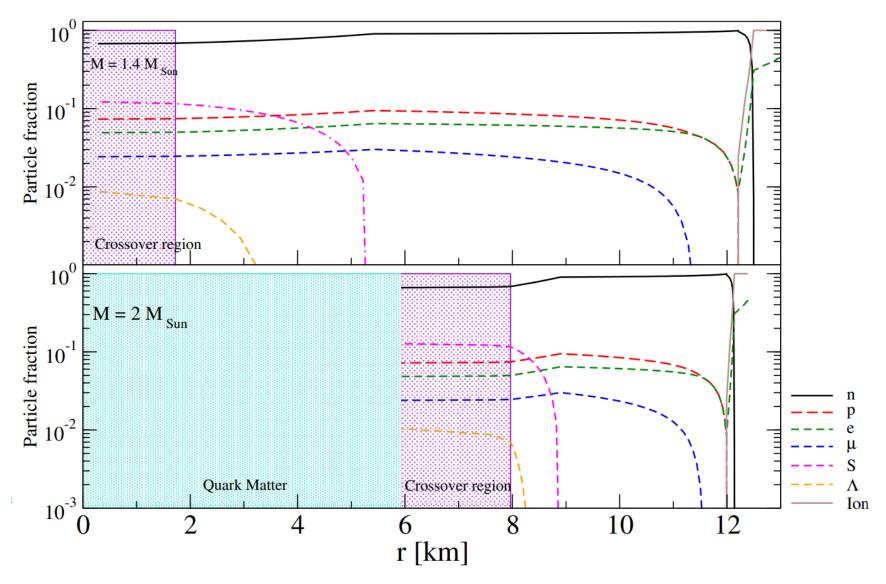
Different masses of Sexaquark particles were considered for its the lowest value of coupling strength with the medium.

The maximum Sexaquark fraction allowed in our models varies from about 12% for the highest S-particle mass to 15% for the lightest one.

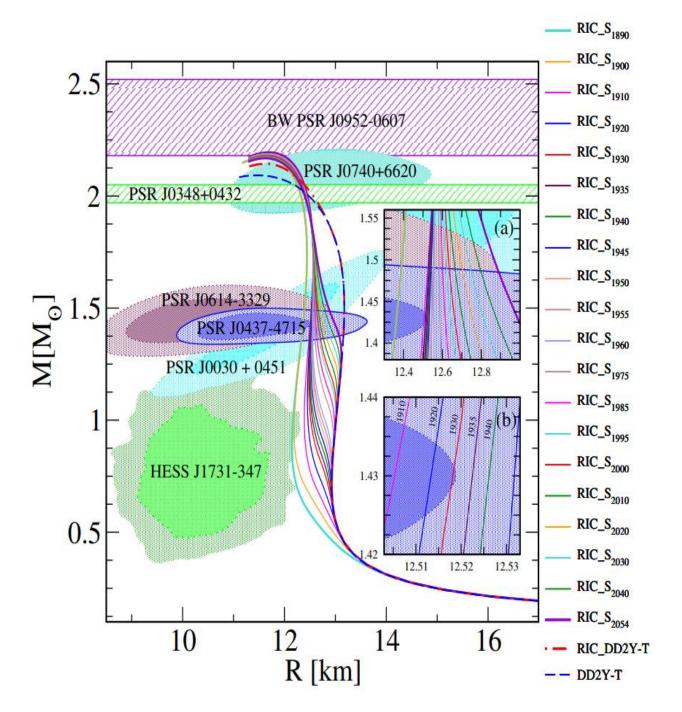


RIC-DD2Y-T+S₂₀₅₀, x = 0.03

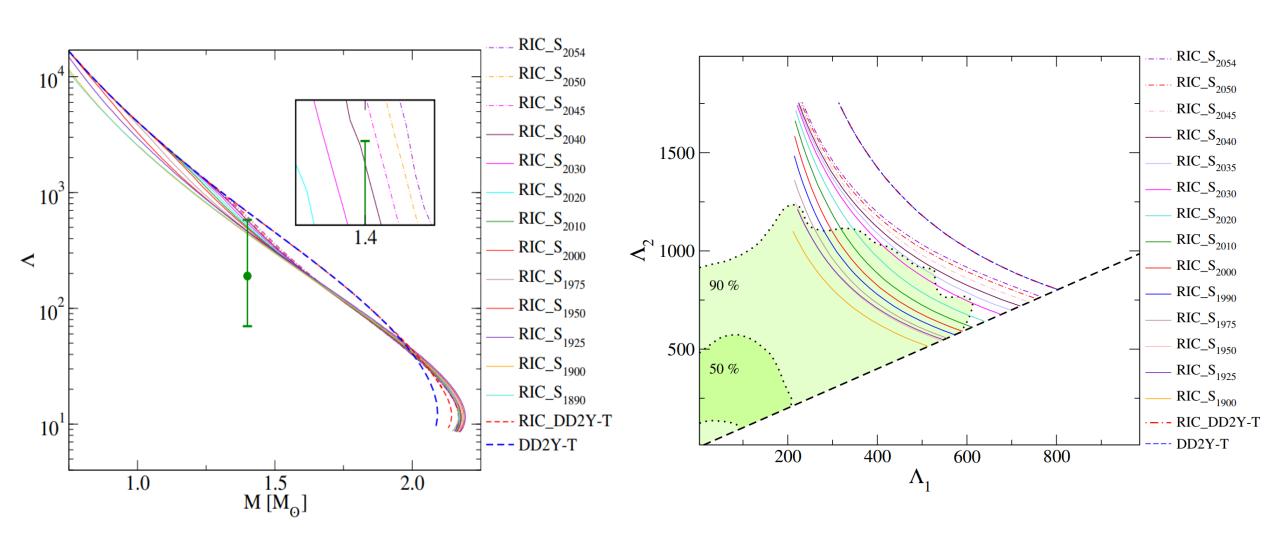
Particle fraction inside the neutron star for $1.4M_{\odot}$ (up) and $2M_{\odot}$ (down)



Mass-Radius
observational constraints
for neutron stars are
considered to probe the
model and different
masses of Sexaquarks

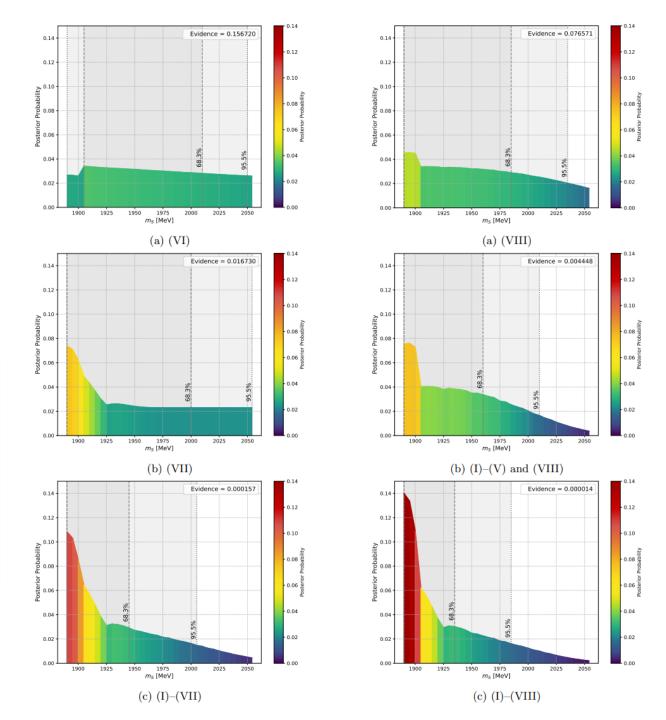


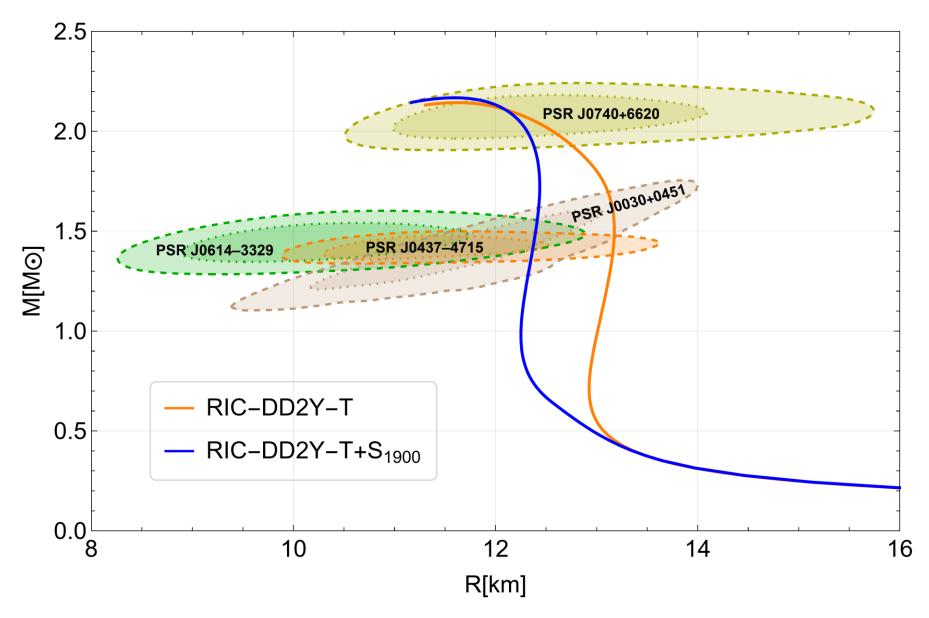
Tidal deformability constraints from gravitational waves of neutron stars merger



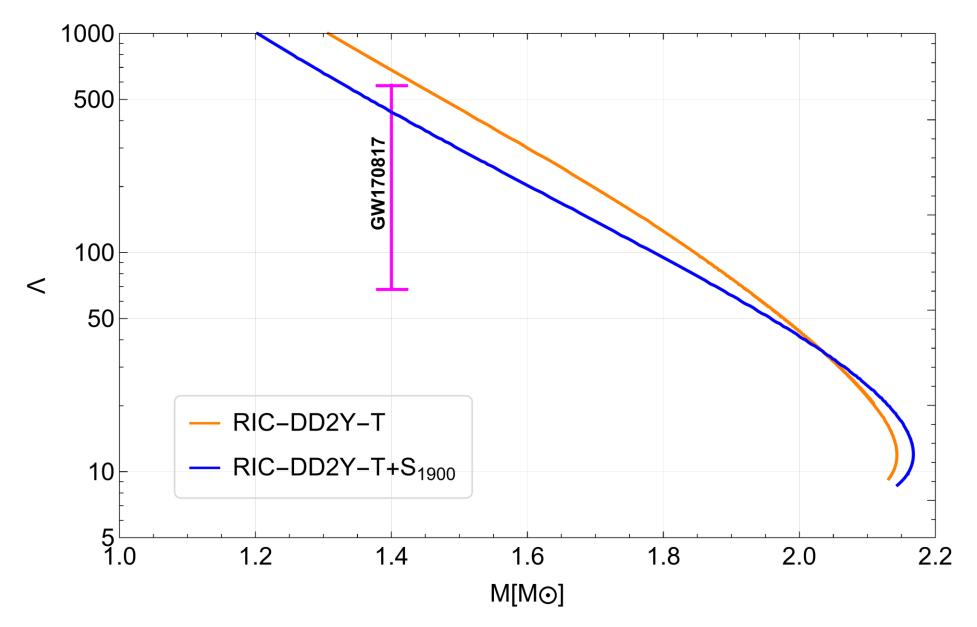
Bayesian analysis based on all available observational constraints for neutron stars

Our results <u>disfavors</u> Sexaquark particle masses <u>higher than 1980 MeV</u> strongly favors $m_S \lesssim$ 1935 MeV for the lowest of coupling strength



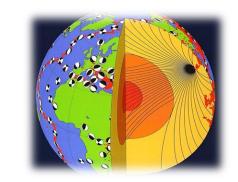


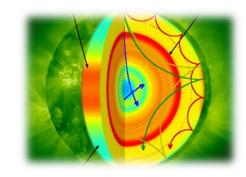
Presence of sexaquark softens the equation of the sate and make it consistent with $\Lambda_{1.4}$ limit



Radial and non-radial oscillations in neutron stars

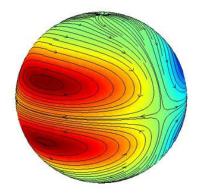
Seismology and Helioseismology for earth and sun





Asteroseismology for neutron stars
the interior structure and
the equation of state can be probed





Of particular interest are the <u>non-radial</u> <u>modes</u>, they distort the star's spherical shape and thus serve as a sources of <u>gravitational waves</u>.

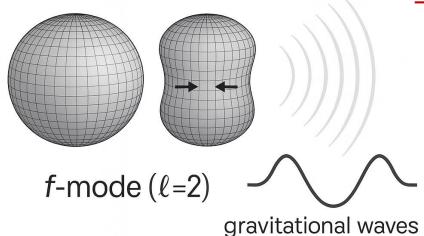
THE ASTROPHYSICAL JOURNAL, Vol. 149, September 1967

NON-RADIAL PULSATION OF GENERAL-RELATIVISTIC STELLAR MODELS. I. ANALYTIC ANALYSIS FOR $l \ge 2^*$

KIP S. THORNE†
California Institute of Technology, Pasadena

AND

ALFONSO CAMPOLATTARO University of California, Irvine Received February 24, 1967



The fundamental mode (f-mode) oscillation in a neutron star

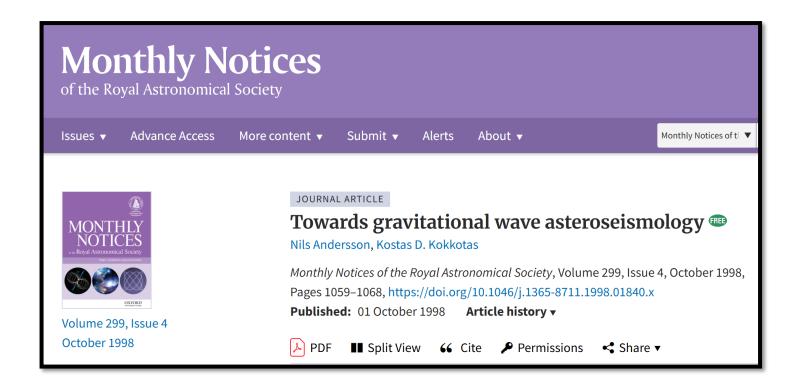
The frequency is between 1.3 and 2.8 kHz could be detectable by current and future gravitational wave detectors

The f-mode oscillations are expected to be damped over time

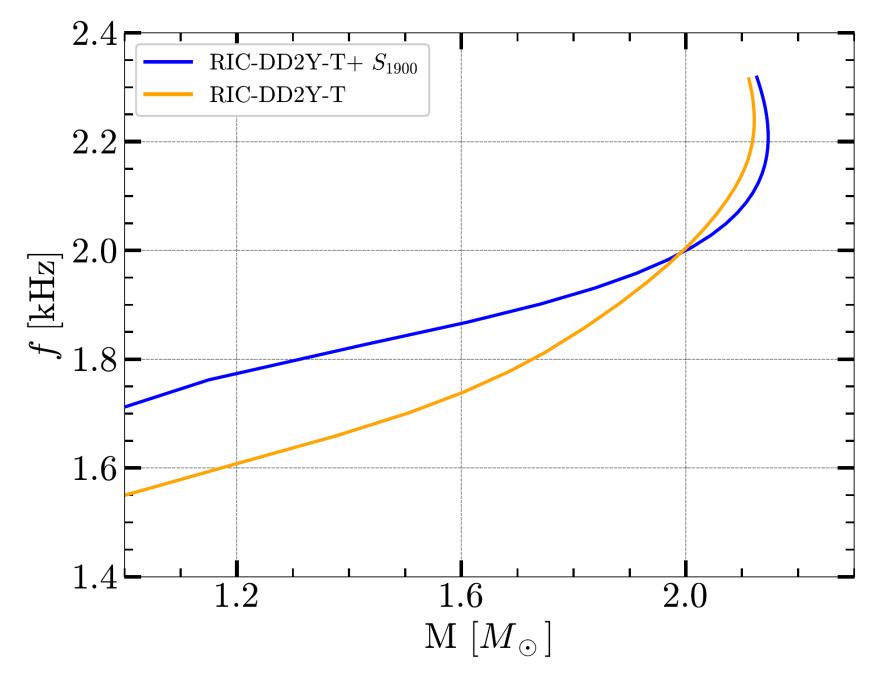
mainly through the emission of gravitational waves
The damping time is predicted to be relatively short,
around 0.1–0.5 seconds.

Gravitational wave asteroseismology

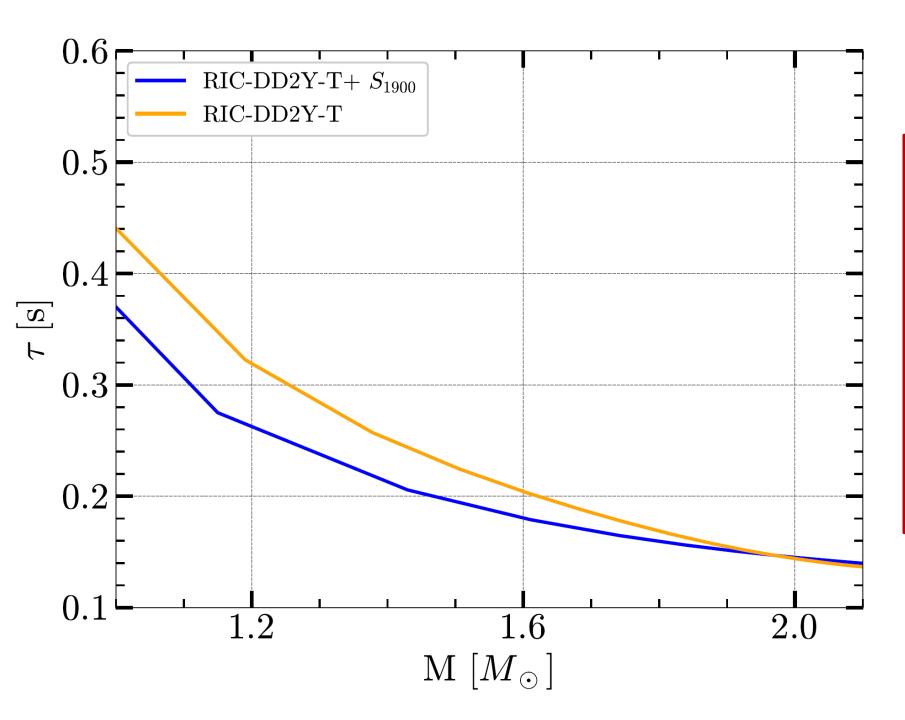
By calculating the universal relation between the <u>f-mode frequency (and damping time)</u> and the <u>star's fundamental properties</u> (mass, radius, tidal, EOS).



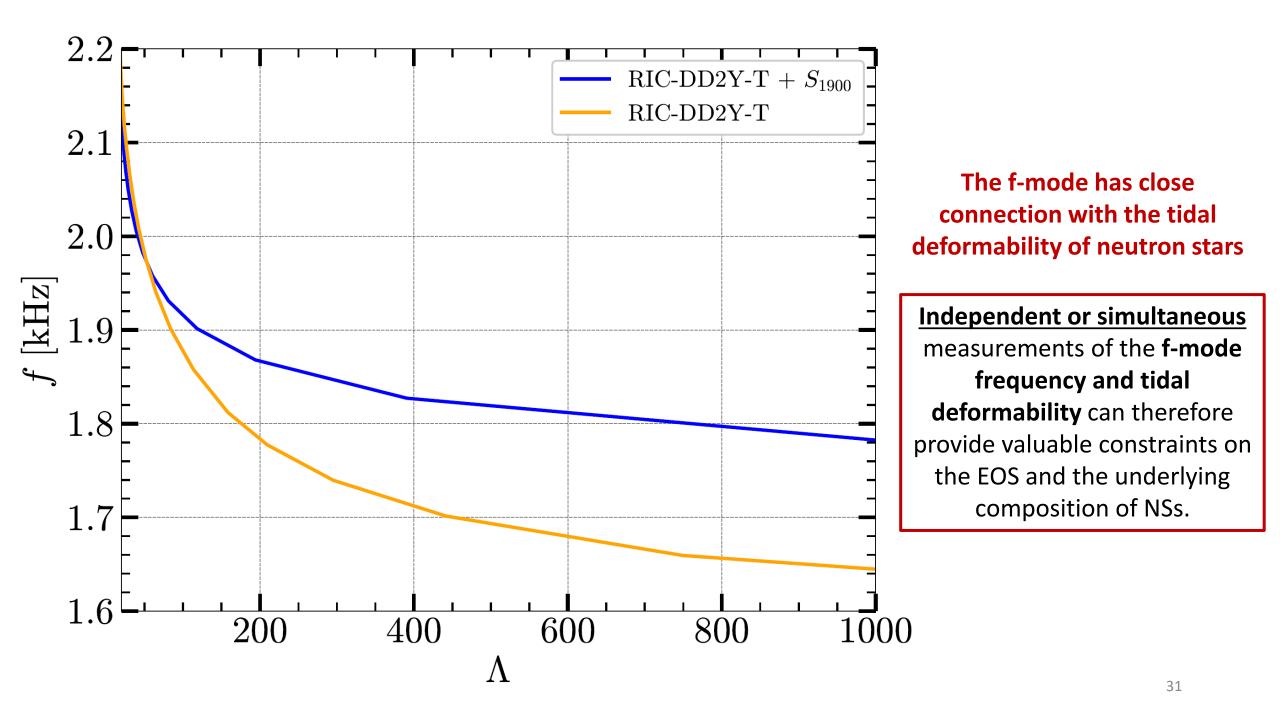
Andersson and Kokkotas
opening up the field of
gravitational wave
asteroseismology in which
they propose the first
asteroseismological universal
relations for oscillation
modes of neutron stars.

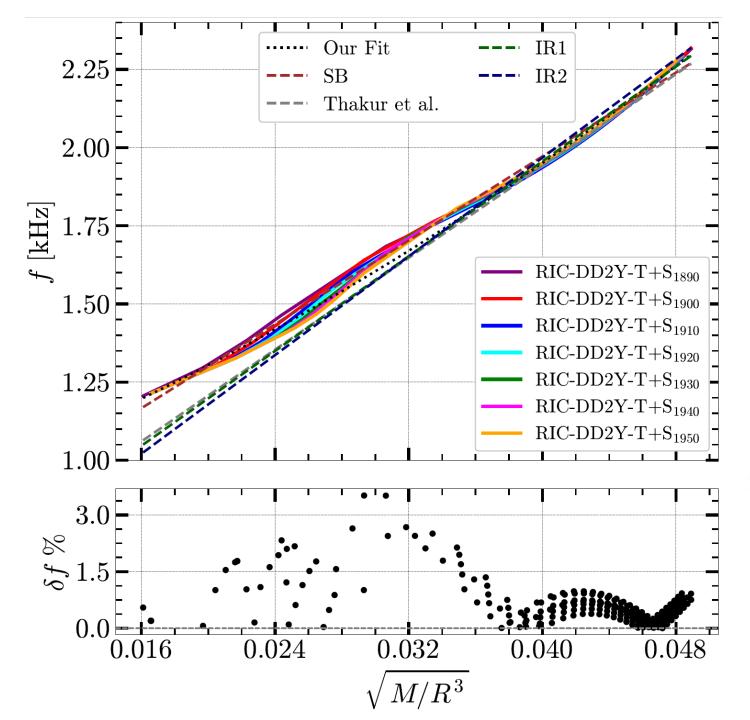


The presence of
Sexaquark directly
contributes to the
softening of the EOS
and higher f-mode
frequencies.



The increased compactness caused by Sexaquark enhances metric perturbations, and enables more efficient emission of gravitational waves, so that **shortens** the damping time



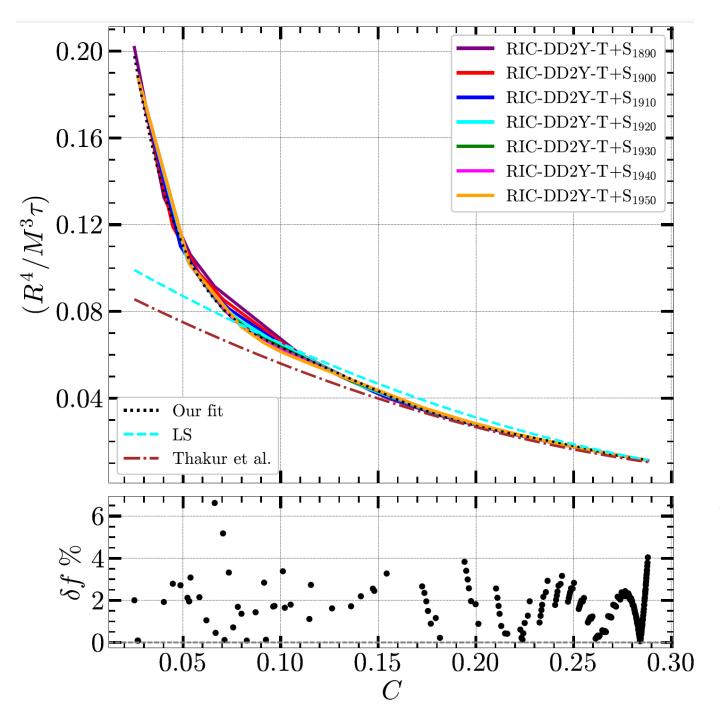


The f-mode frequency scales approximately with the square root of the neutron star's average density.

$$\frac{f}{\text{kHz}} = a + b \left(\sqrt{\frac{M}{R^3}} \right) + c \left(\sqrt{\frac{M}{R^3}} \right)^2$$

where a = 0.840846, b = 18.569058 and c = 229.339724

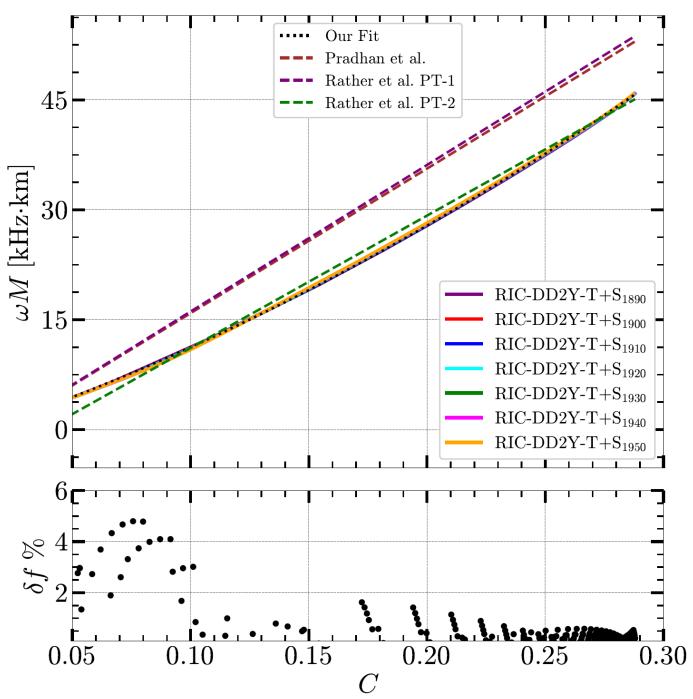
M. Shahrbaf, P. Thakur, D.R.K, arXiv:2510.08115



The quasi-universal relation between the scaled damping-time variable and the compactness

$$\frac{R^4}{M^3\tau} = a + bC + cC^2 + dC^3 + eC^4 + fC^5 + gC^6$$

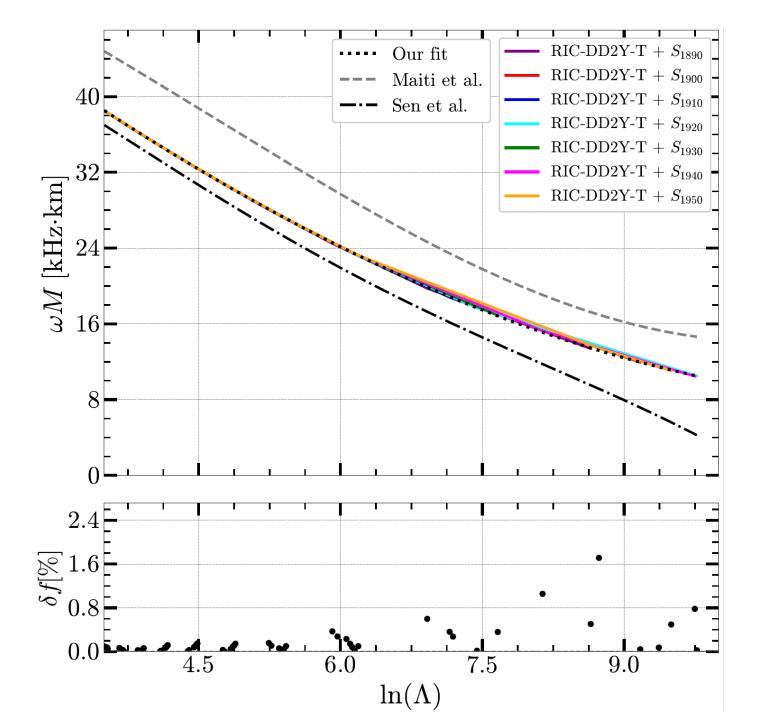
where, $a=0.4095642,\ b=-12.26236,\ c=186.0756,\ d=-1505.978,\ e=6603.648,\ f=-14837.04$ and g=13389.98



The mass scaled angular frequency of f-mode, ωM (with $\omega = 2\pi f$), as a function of the stellar compactness

$$\omega M = a C^2 + b C + c$$

where a = 199.734977, b = 106.082697, c = -1.365759 have units of kHz·km



The variation of the scaled frequency, ωM , as a function of the dimensionless tidal deformability parameter (Λ)

$$\omega M = a + b(\ln \Lambda) + c(\ln \Lambda)^2 + d(\ln \Lambda)^3$$

where a=67.426668, b=-9.797683, c=0.470981, and d=-0.006726







EINSTEIN







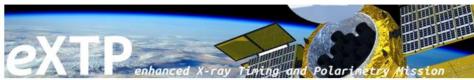


















Golden Age of neutron stars research

Investigating the properties of ultra high density matter

We may shed light on the nature of dark matter



What we know is a drop What we do not know is an ocean