



EXPLORING QUARK MASS DEPENDENT THREE-NUCLEON FORCES IN MEDIUM MASS-NUCLEI

Urban Vernik with Kai Hebeler and Achim Schwenk

arXiv:2512.20454, submitted to PRC

Challenges in effective field theory descriptions of nuclei, Hrischegg, Austria.



Exzellente Forschung für
Hessens Zukunft

OUTLINE



INTRODUCITON

- Enhanced 3N forces
- Choice of interaction and calculational details

REFITTING STRATEGIES

- Comparison of fitting strategies
- Why is the effect of F_2 large?

RESULTS

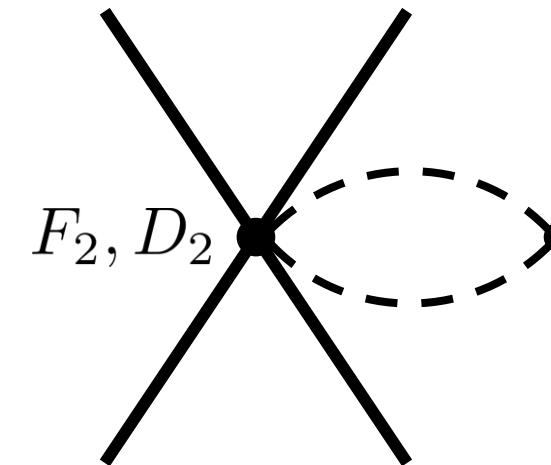
CONCLUSIONS

ENHANCED 3N FORCES



V. Cirigliano et al., Phys. Rev. Lett. 135, (2025)

- Using **KSW** power counting scheme, 3N vertices were identified that:
 - should contribute at $N^3\text{LO}$ rather than $N^5\text{LO}$ (enhanced by Q^{-2} compared to naive dimensional analysis)
 - include a quark-mass dependant $m_\pi^2 (\bar{N}N)^2 \pi^2$ vertex (D_2),
 - and a momentum dependent $(\bar{N}N)^2 \pi^2$ vertex (F_2)
 - seem to play an important role in symmetric and neutron matter
- The suggested range is $\pm 1/(5f_\pi^4) \rightarrow$ our renormalization $\pm 1/5 = \pm 0.2$

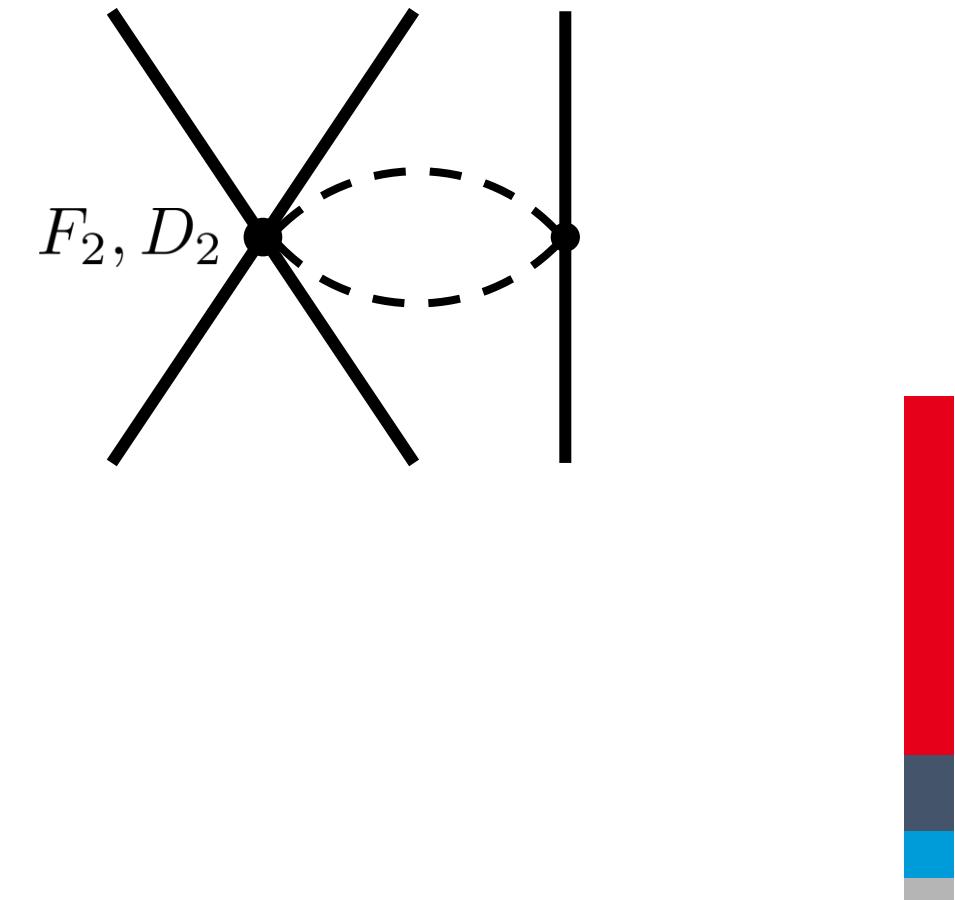
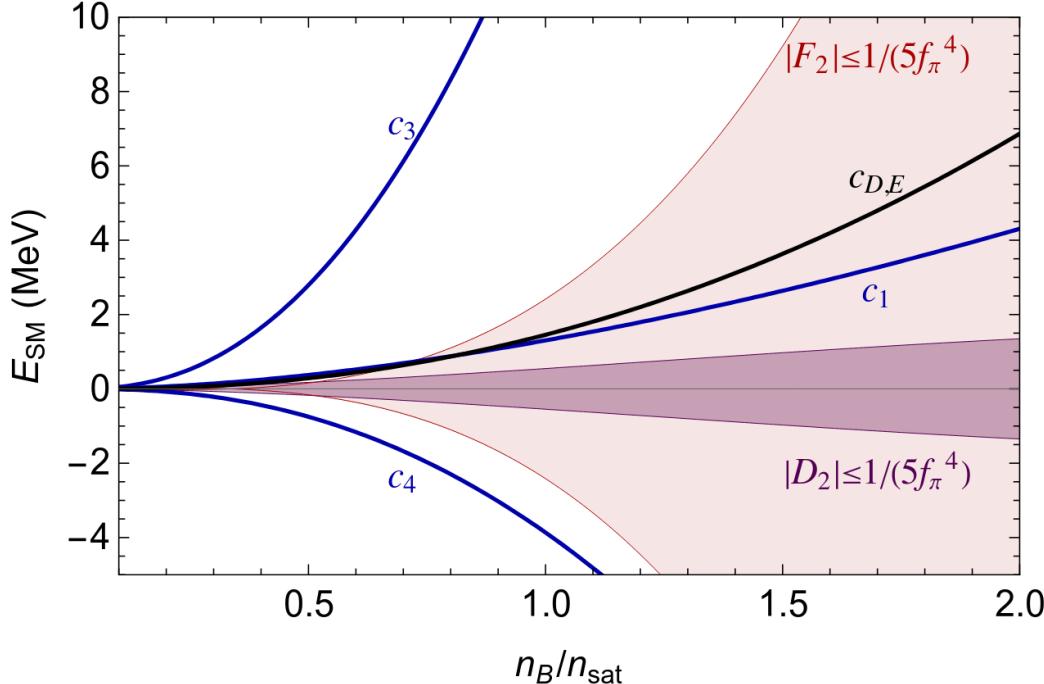


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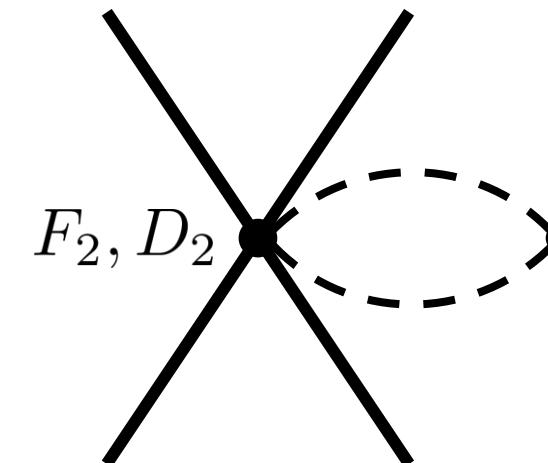
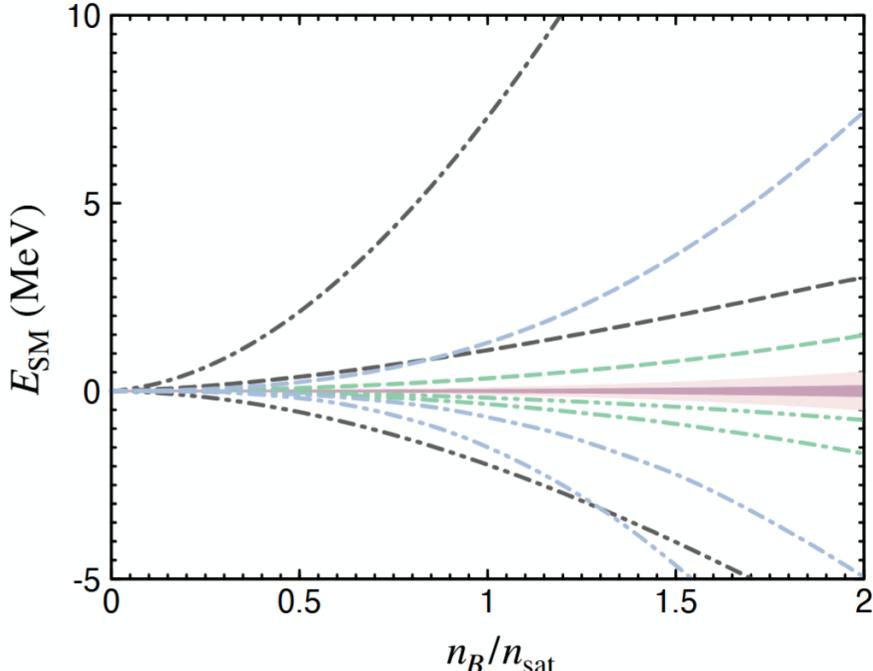


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- The effect is however scheme and regulator dependent
- By removing the dependence, the contributions are within the expectations of Weinberg PC and NDA.

E. Epelbaum et al., arXiv:2512.14117 [nucl-th] (2025)

CHOICE OF INTERACTION & CALCULATION DETAILS



INTERACTION: EMN

D. R. Entem, R. Machleidt, and Y. Nosyk, Phys. Rev. C 96, (2017).

- 2N and 3N treated a consistent chiral order → here: both N²LO and N³LO
- Bare ($\lambda_{\text{SRG}} = \infty$, $\Lambda_{2N} = \Lambda_{3N} = 450$ MeV) and SRG-evolved ($\lambda_{\text{SRG}}^{2N} = 1.8$ fm⁻¹, $\Lambda_{3N} = 2.0$ fm⁻¹ $\approx 394. \dots$ MeV)

LEC	c ₁	c ₃	c ₄	c _D	c _E	F ₂
N ² LO/N ³ LO	-0.74/-1.20	-3.61/-4.43	2.44/2.67	<i>to fit</i>	<i>to fit</i>	<i>to fit</i>

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CALCULATION DETAILS

- IMSRG(2), $e_{\text{max}} = 14$, $E_{3\text{max}} = 24$, $\hbar\omega = 16$



REFITTING



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FITTING PROCEDURE

1. Choose a value of F_2
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3. Constrain c_D
4. Compute observables



Approach	Constraint on c_D
few-body	${}^3\text{H}$ half-life (GT)
many-body	${}^{16}\text{O}$ charge radius (and BE) (${}^{16}\text{O}$)

D. Gazit et al., Phys. Rev. Lett. 103, (2009); P. Klos et al Eur. Phys. J. A 53, (2017).
P. Arthuis et al., arXiv:2411.00097 [nucl-th] (2024)

REFITTING



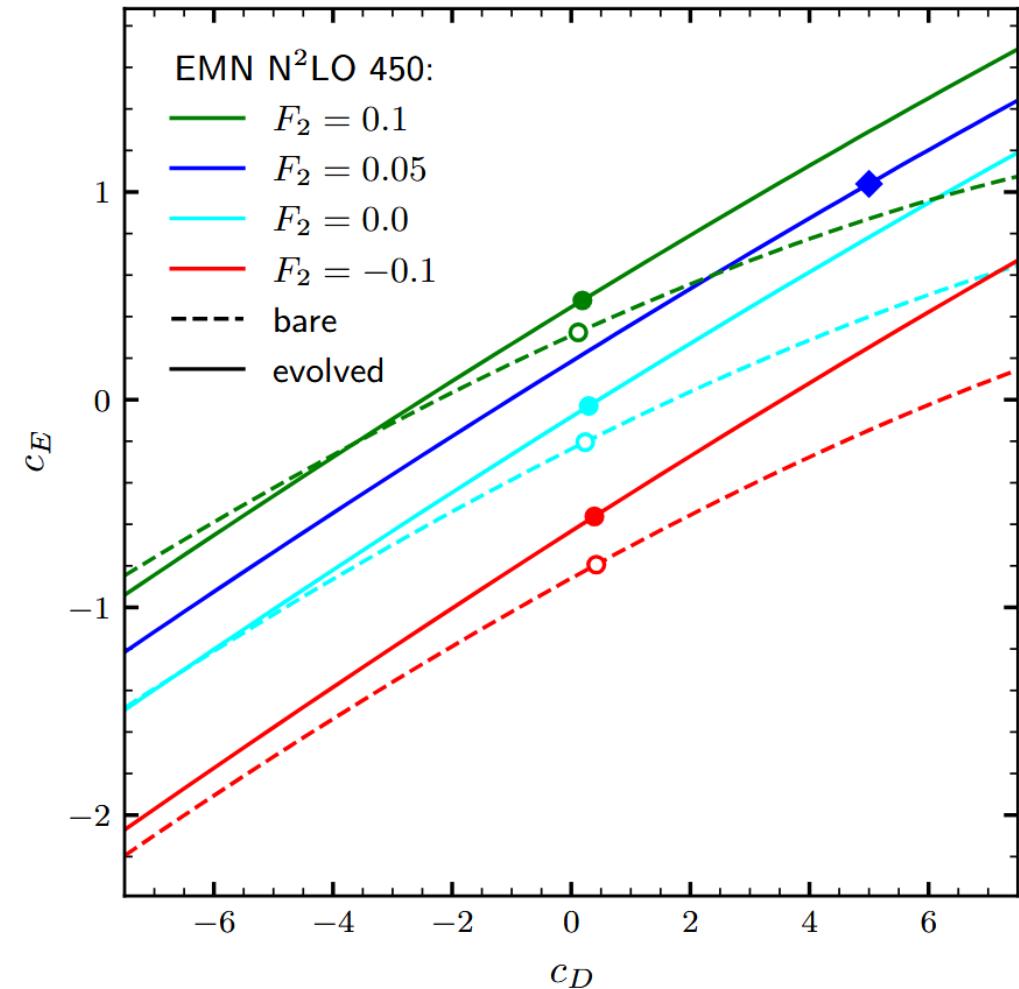
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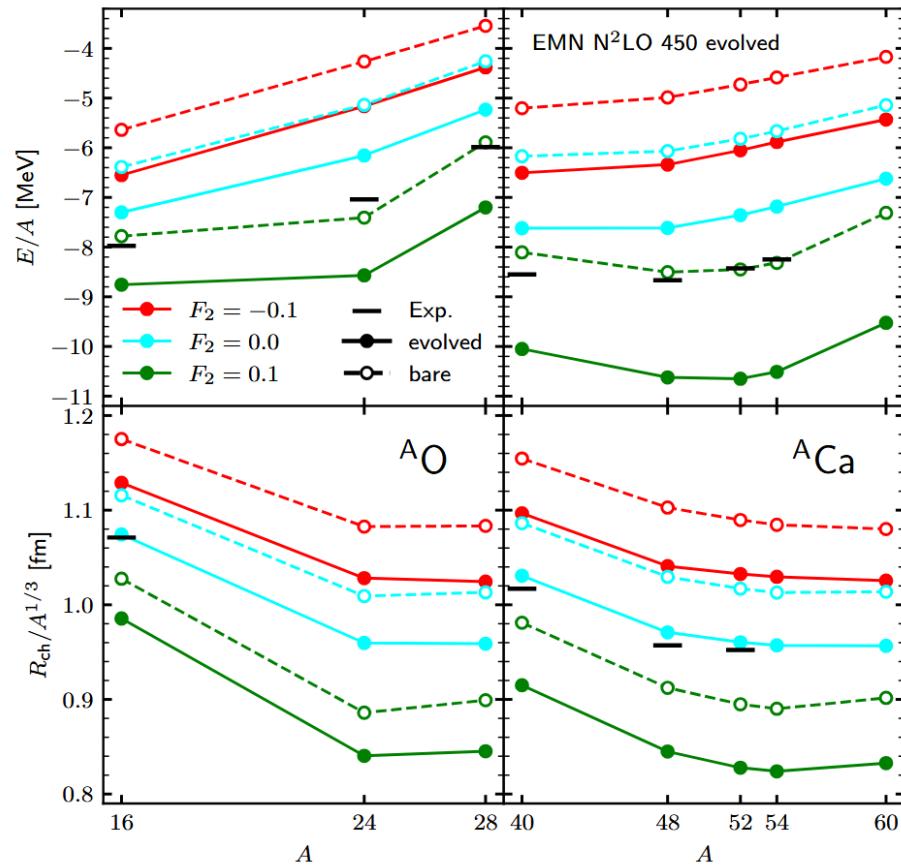
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COMPARISON OF FITTING STRATEGIES

GT STRATEGY

- Both observables cannot be reproduced at the same time
- c_D is fixed and thus changes in radii and ground state energies are very correlated

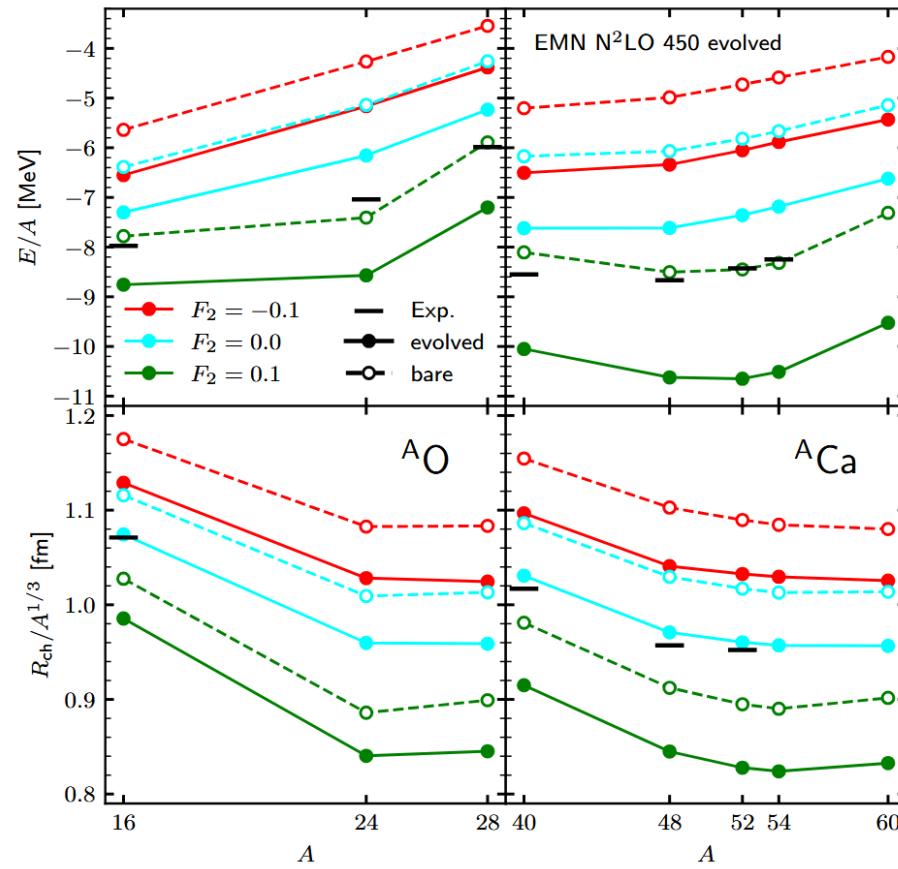


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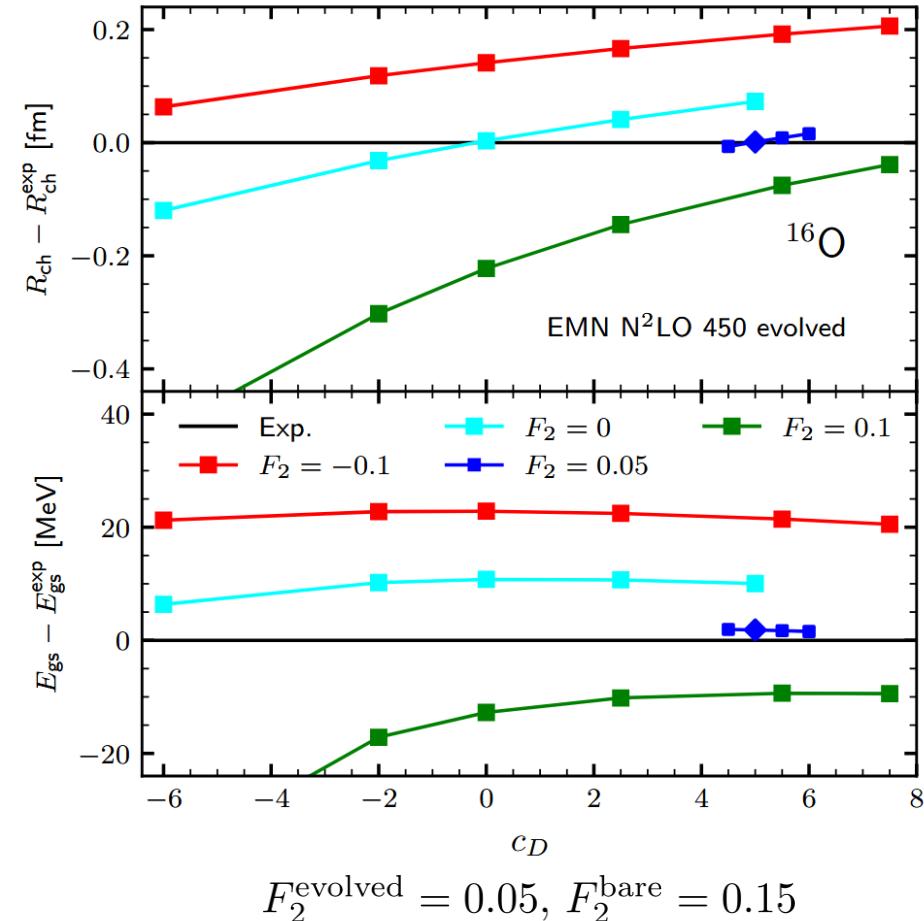
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¹⁶O STRATEGY

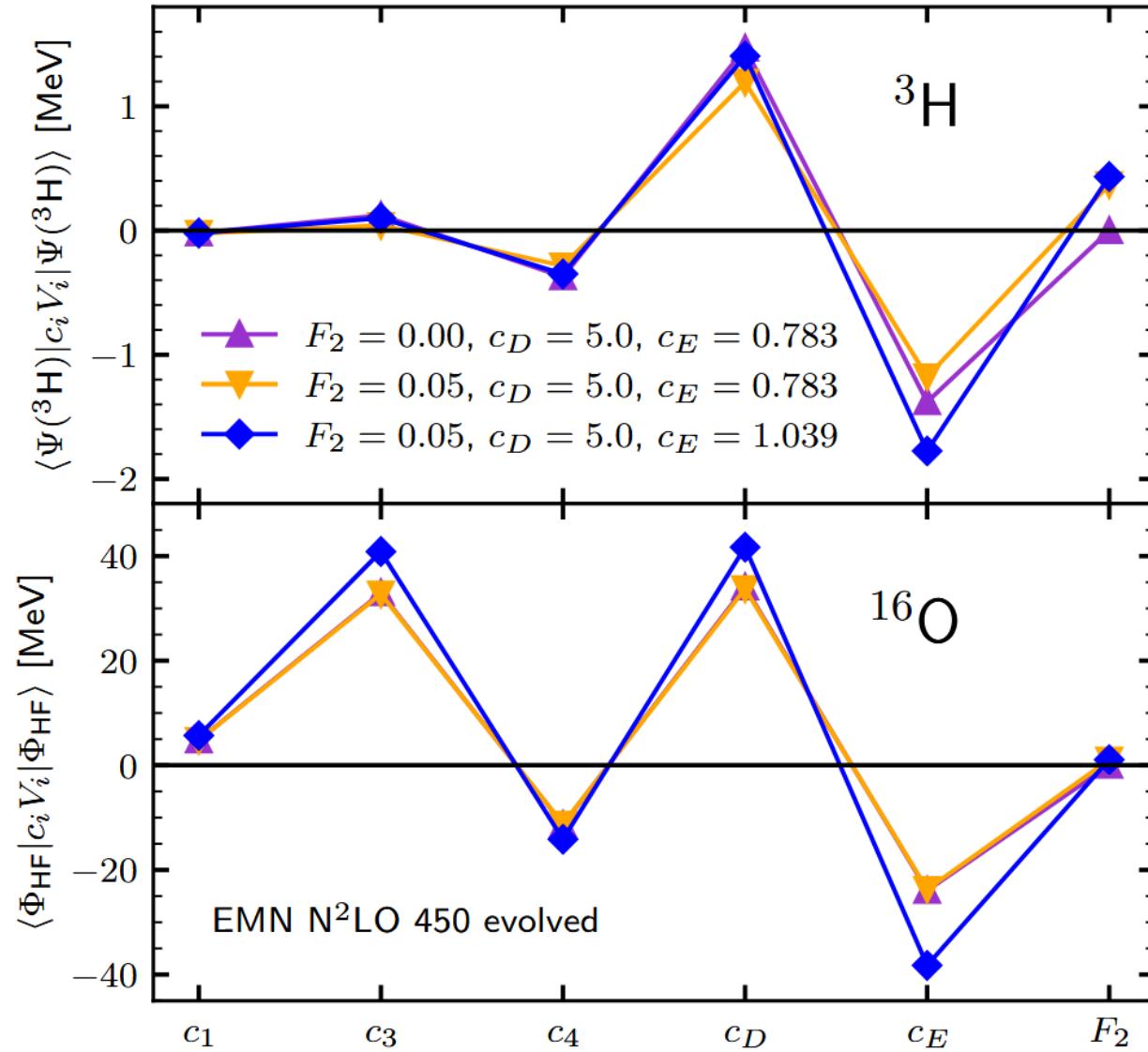
- Is more sensitive to c_D
- Both observables can be reproduced at the same time
- Works similarly well for both chiral orders for the same F_2



WHY IS THE EFFECT OF F_2 SO LARGE?



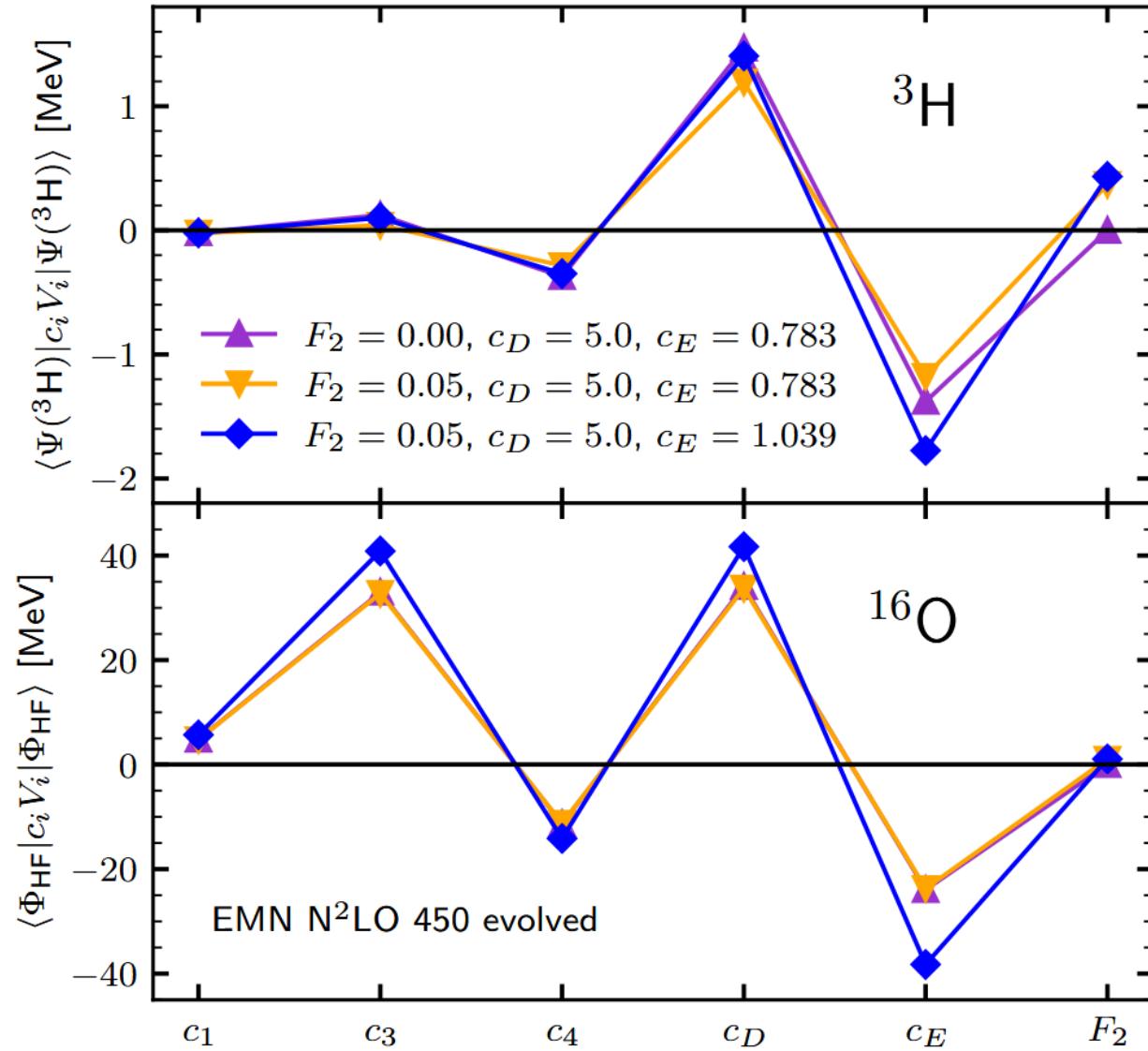
- Is it safe/consistent to promote individual topologies?
 - case study: c_D and c_E exhibit fine cancellations
 - counter terms to F_2 might need to be promoted
- Addition of F_2 to ^3H reshuffles c_D and c_E contributions
- F_2 has a small contribution to the energy but the fitting rearranges other topologies significantly



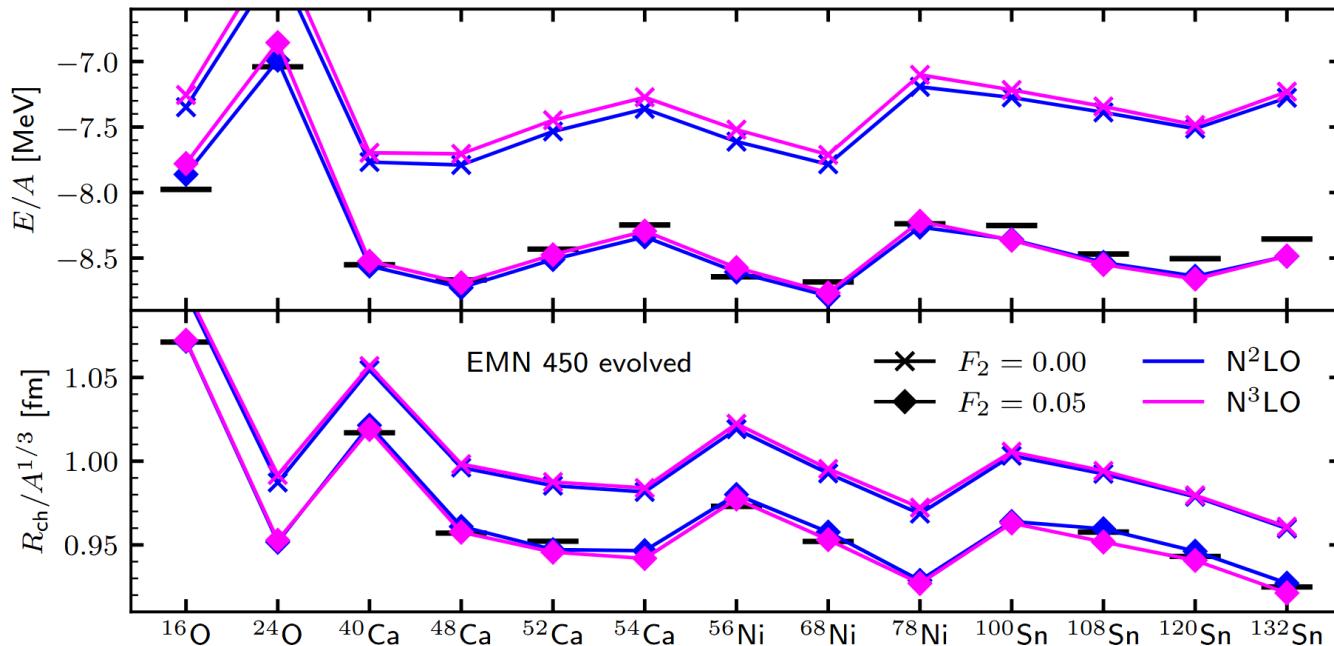
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- It is the refitted c_E that affects the observables

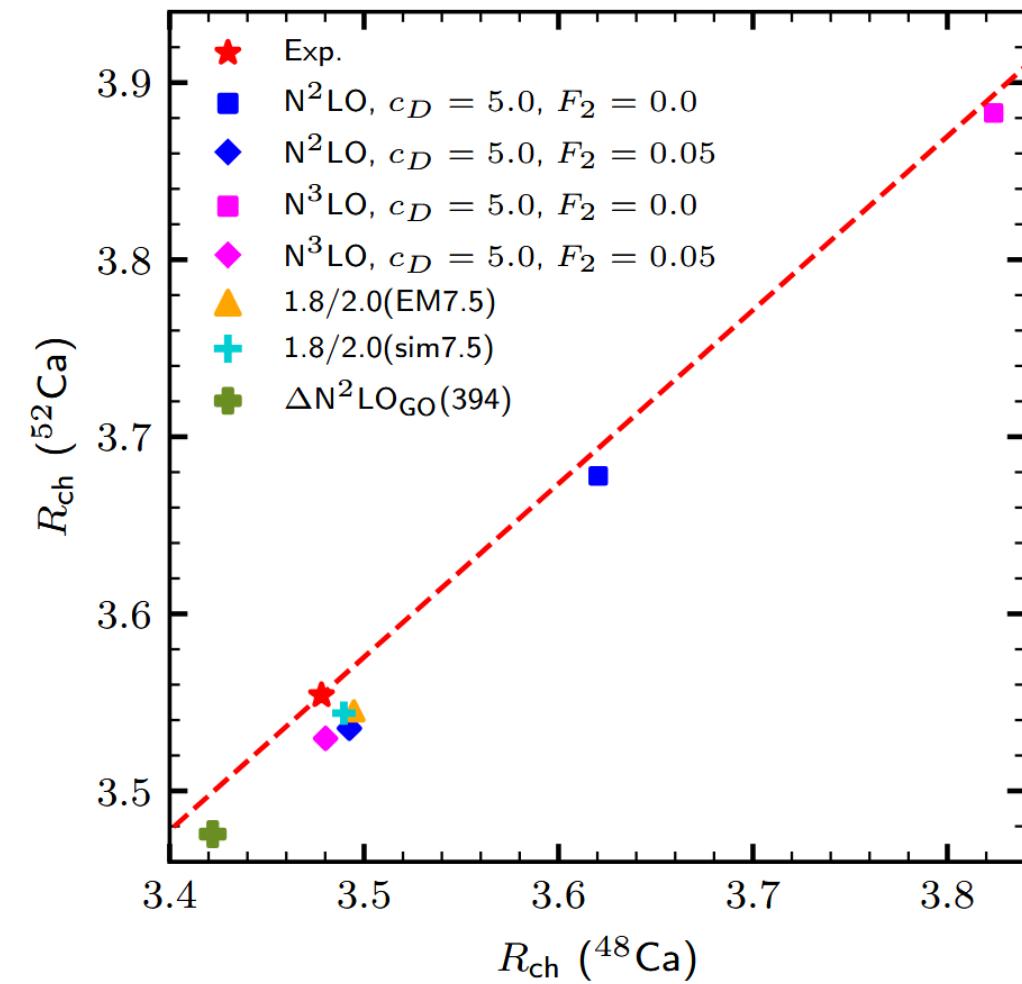
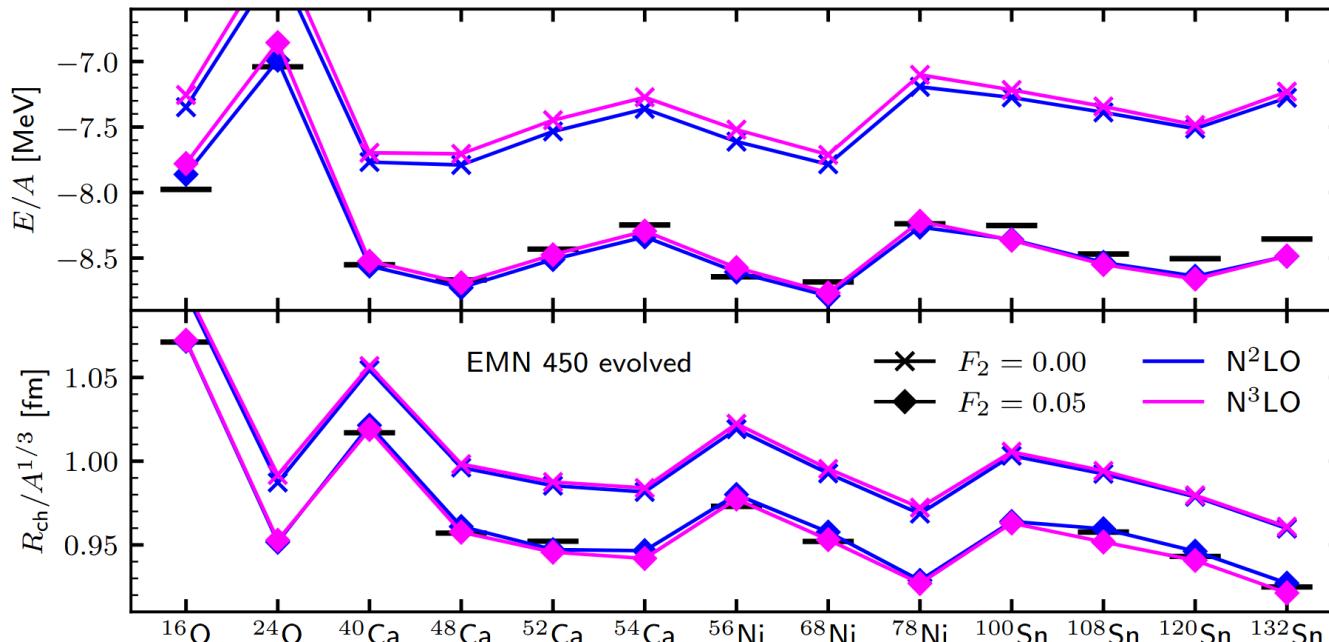


RESULTS FOR ^{16}O - ^{132}Sn



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- Both energies and charge radii are very well reproduced at both chiral orders
- No significant changes in trends as a function of mass and proton-to-neutron ratio
- Inclusion of F_2 cannot resolve the theoretical discrepancy to the experimental value of $\delta\langle R_{\text{ch}}^2 \rangle^{48,52}$

CONCLUSIONS



- We investigated the impact of new 3N forces on the properties of medium-mass nuclei.
- Observables and nuclear states are noticeably impacted by $F_2 \rightarrow$ but due to refit and c_E .
- Employing the ^{16}O fitting strategy and adding F_2 to the EMN interactions brings it in a very good agreement with the experimental results along the chain of closed-shell nuclei.
- Adding F_2 serves more as a 'reparametrization' of the interaction rather than introduction of new physics.



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THANK YOU FOR YOUR ATTENTION!