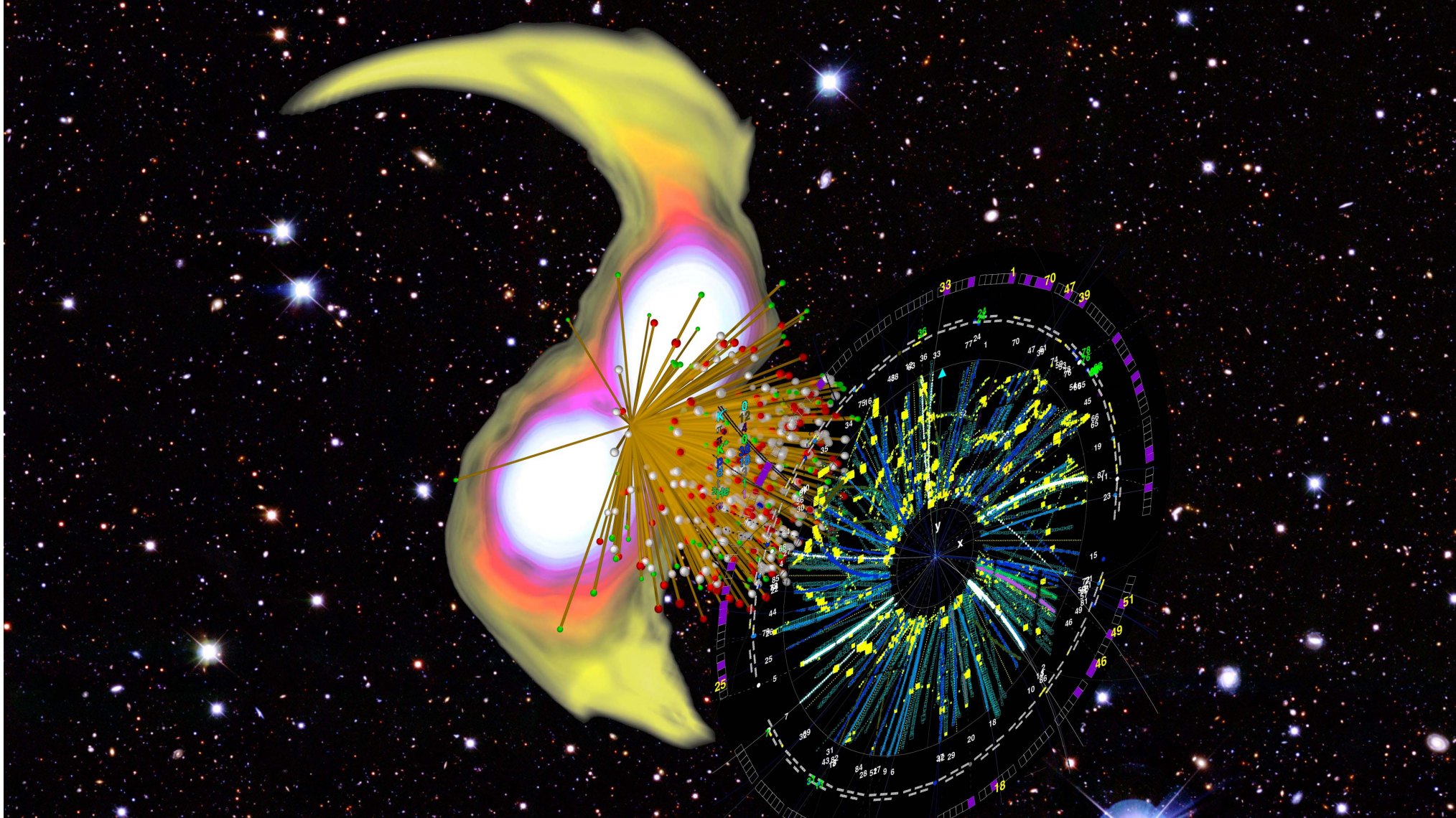


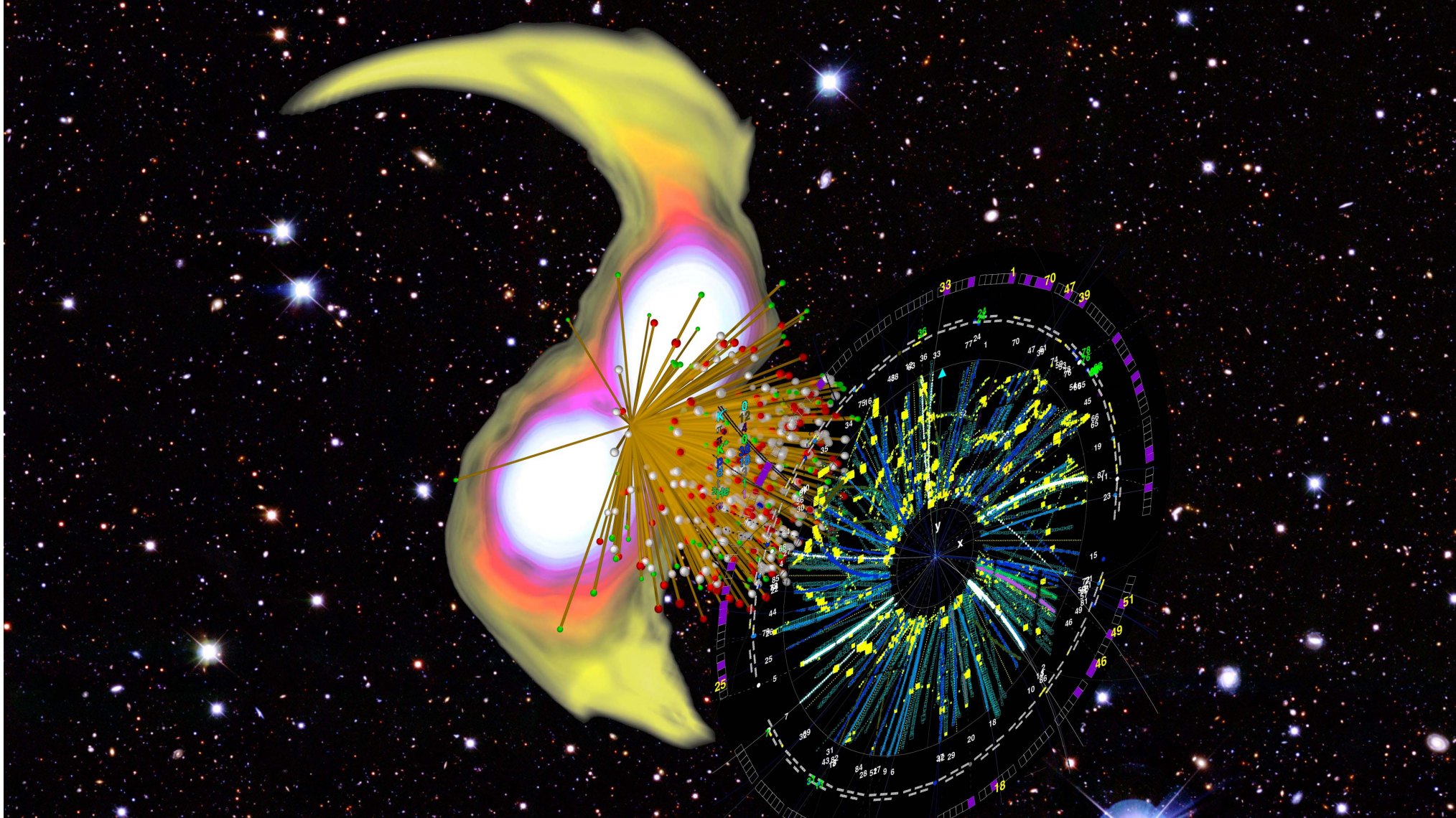


Equation-of-state constraints from FOPI and ASY-EOS flow measurements

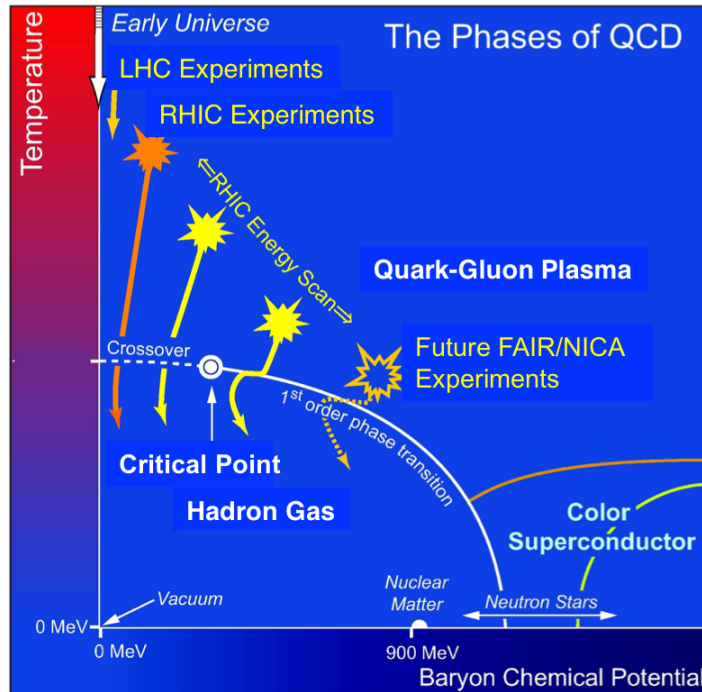




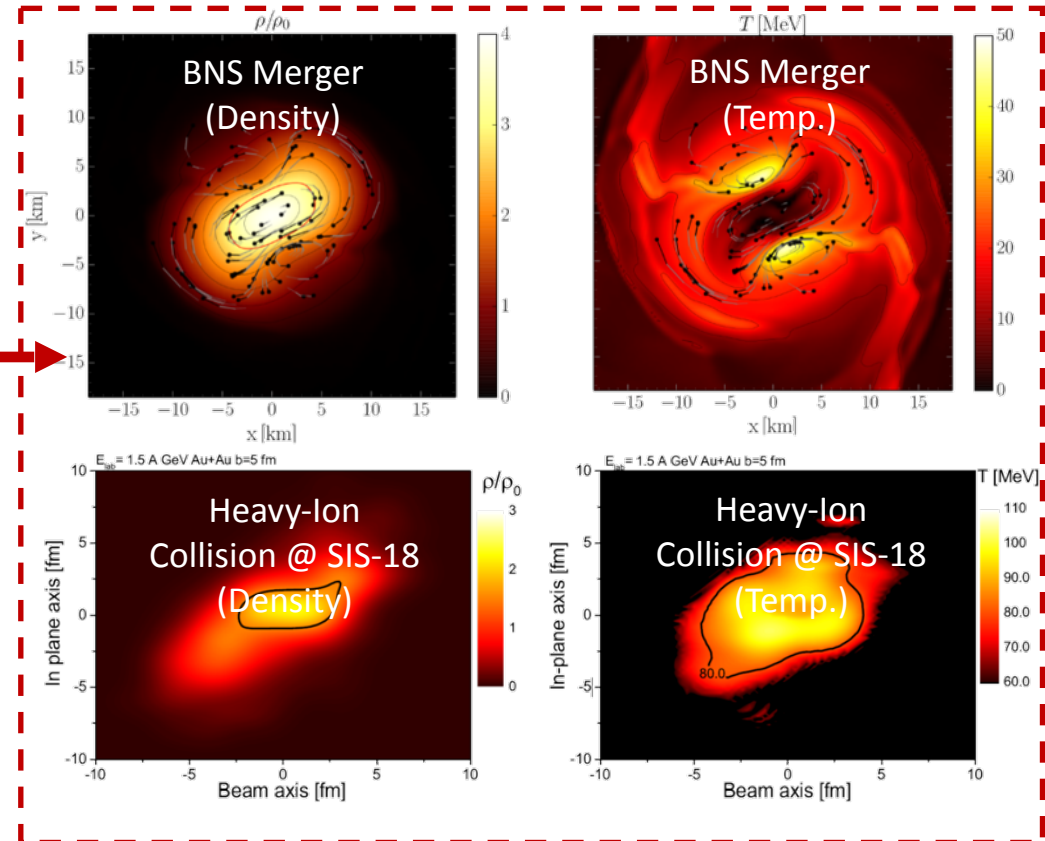
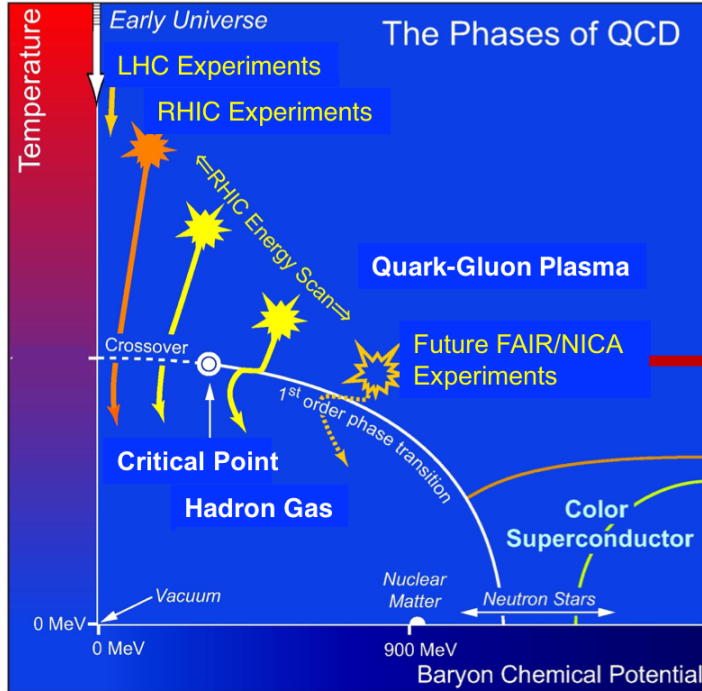
Equation-of-state constraints from FOPI and ASY-EOS flow measurements



[STAR], Studying the Phase Diagram of QCD Matter at RHIC, STAR Note 598 (2014)

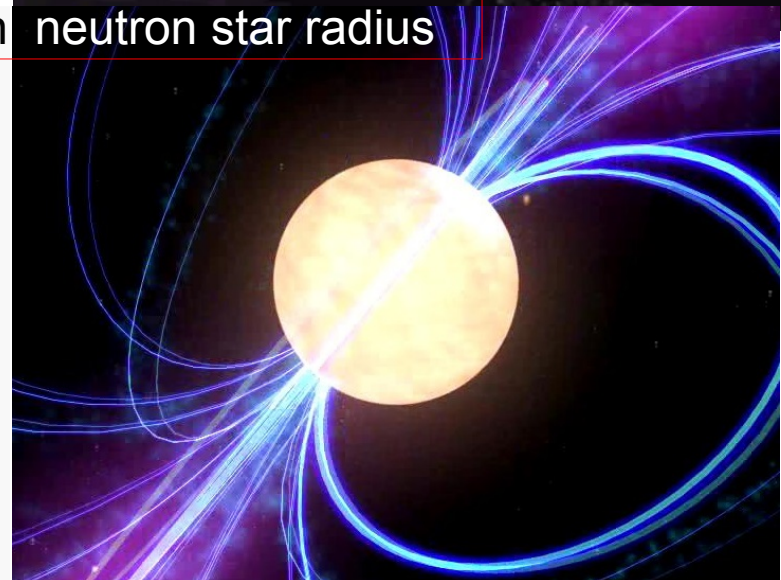
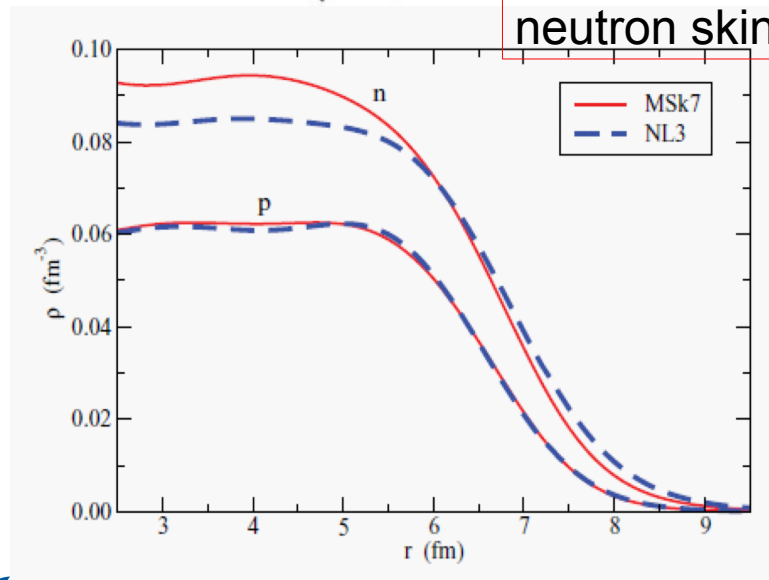
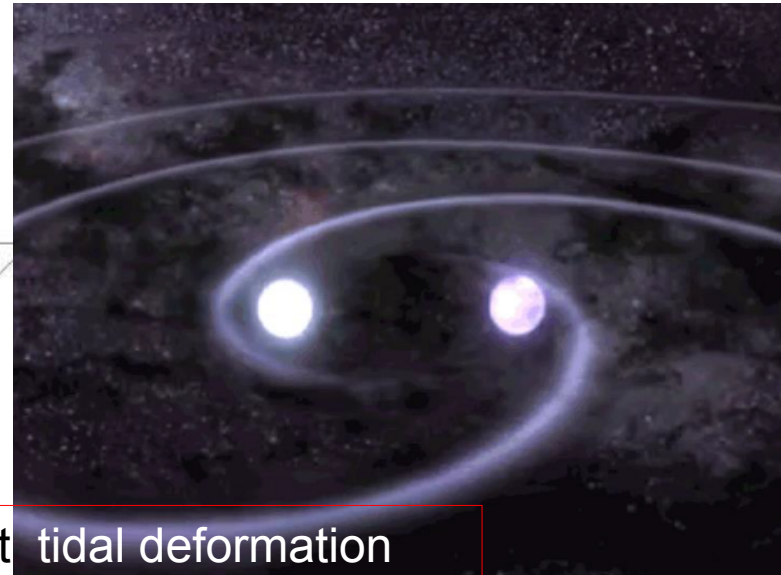
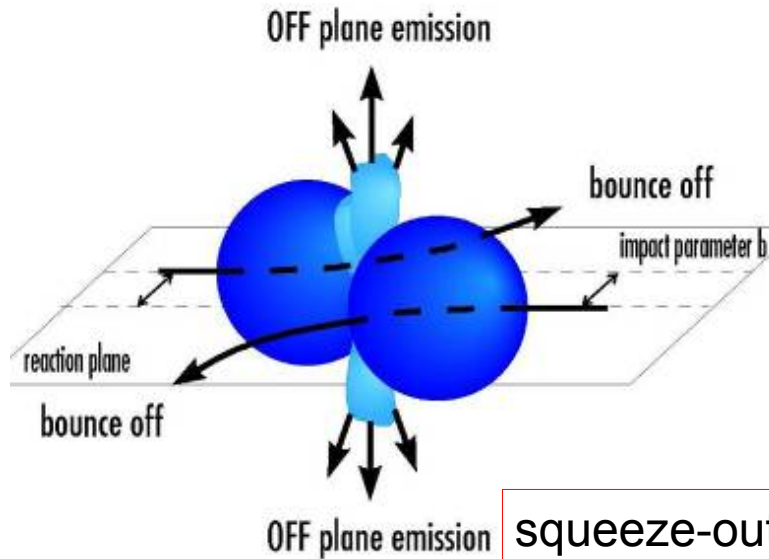


[STAR], Studying the Phase Diagram of QCD Matter at RHIC, STAR Note 598 (2014)

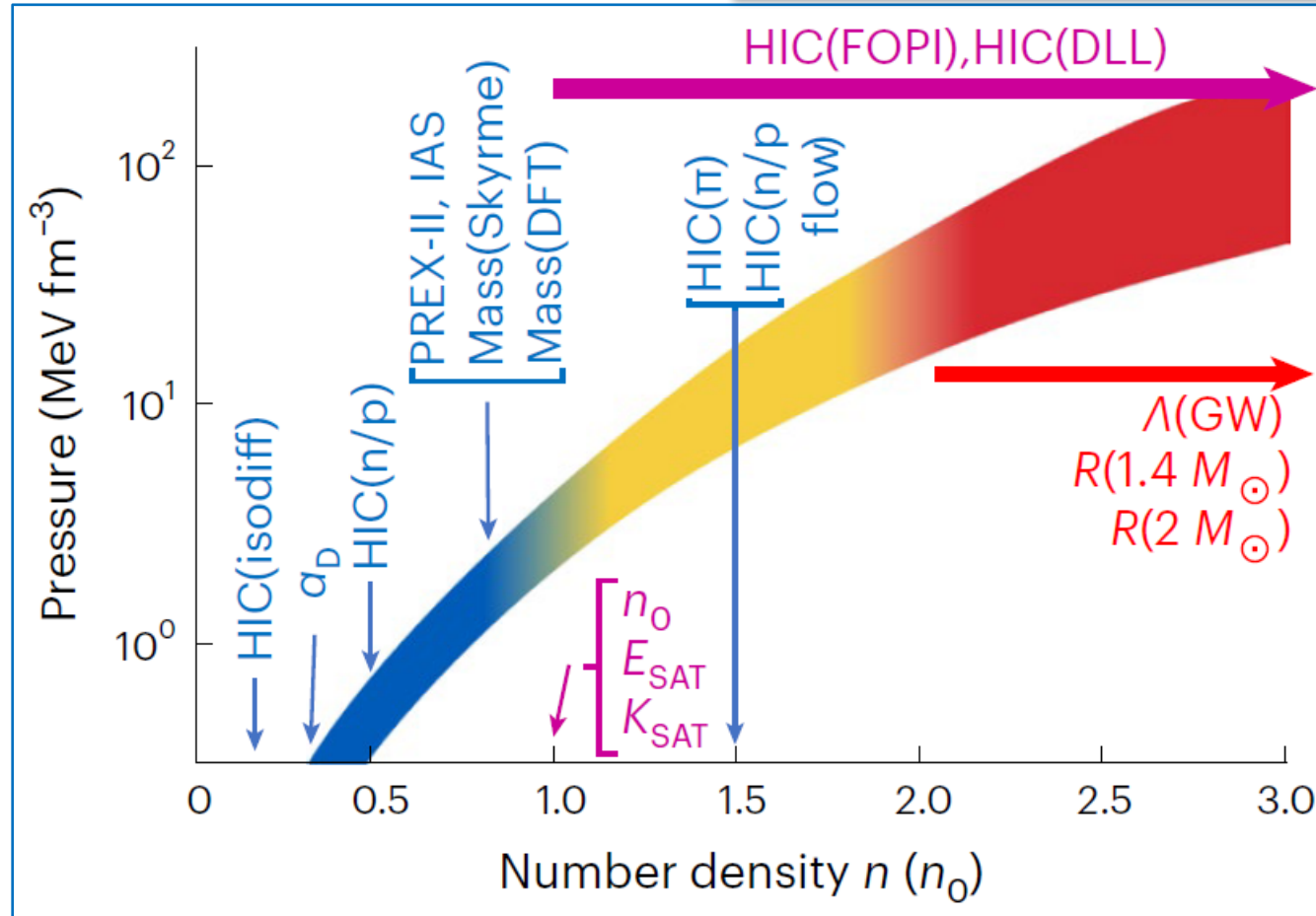


Temperature and density created in the fireball in HIC's at intermediate energies ($E_{\text{inc}} \approx 0.1 - 10 \text{ A GeV}$) mimic the density and temperature conditions created in binary neutron star mergers

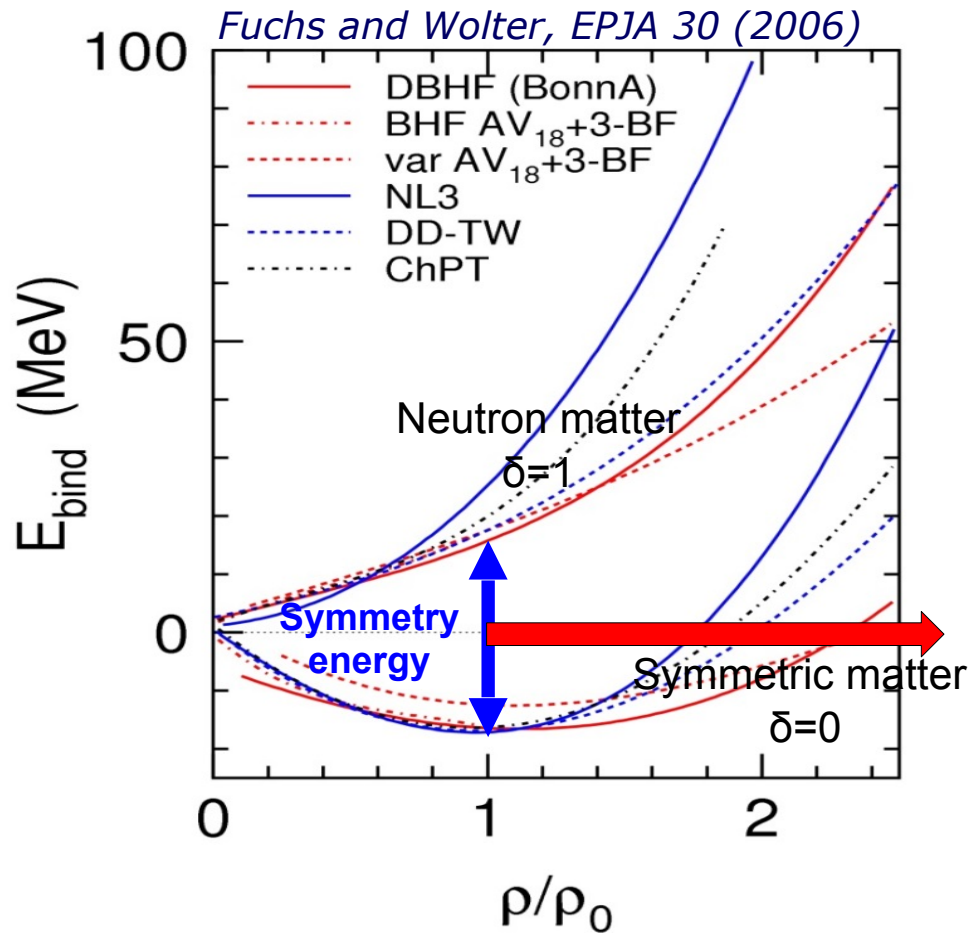
M. Hanauske et al., 2017 J. Phys.: Conf. Ser. 878 012031



Tsang+, Nature Astronomy (2024)



DLL: Danielewicz, Lacey, Lynch, Science - DFT: Density Functional Theory



EOS in thermodynamics pressure $P(\rho, T)$

$$P = \rho^2 \left. \frac{\partial E/A}{\partial \rho} \right|_{T=\text{const}}$$

Nuclear physics EOS

$$\frac{E}{A} = E/A(\rho) \Big|_{T=0}$$

Nuclear incompressibility K

$$K = 9 \rho^2 \left. \frac{\partial^2 E/A}{\partial^2 \rho} \right|_{\rho=\rho_0}$$

Asymmetry parameter $\delta = \frac{\rho_n - \rho_p}{\rho_n + \rho_p}$

Symmetry energy E_{sym}

$$E(\rho, \delta) = E_{\text{SNM}}(\rho, \delta = 0) + \delta^2 E_{\text{sym}}(\rho) + O(\delta^4)$$

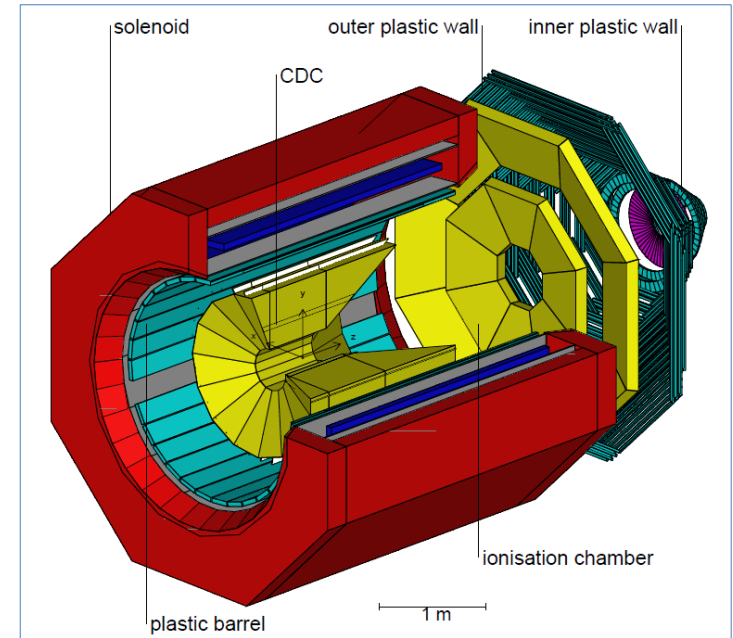
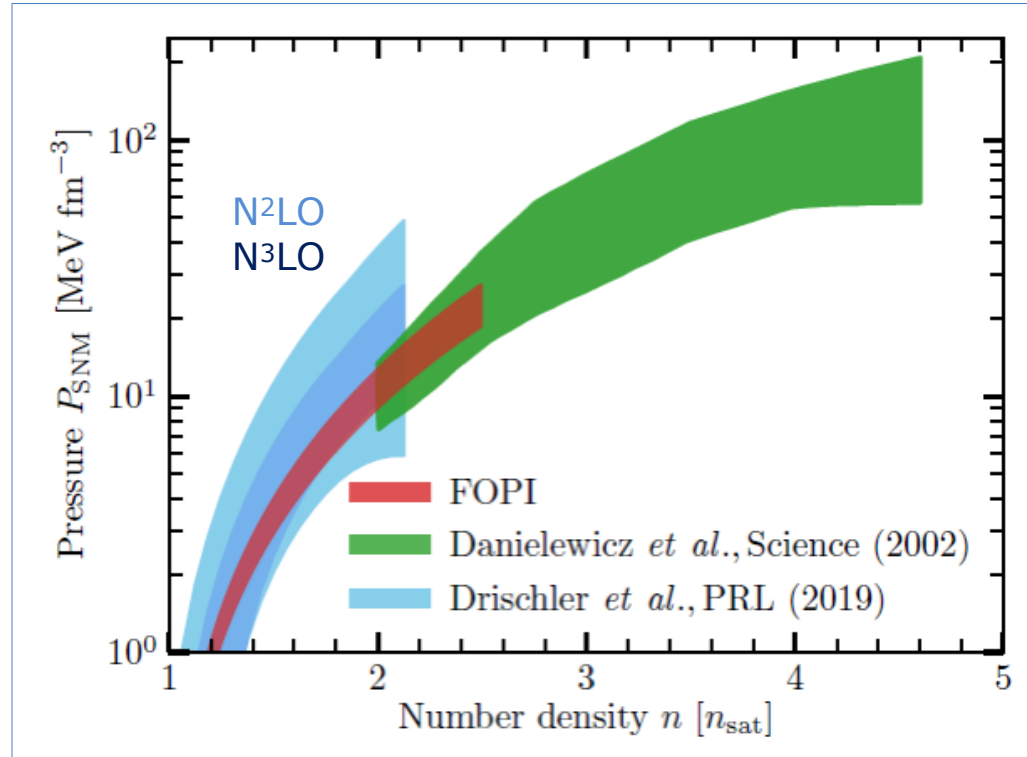
mit

$$E_{\text{sym}} = E_{\text{sym},0} + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{\text{sym}}}{18} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2 + \dots$$

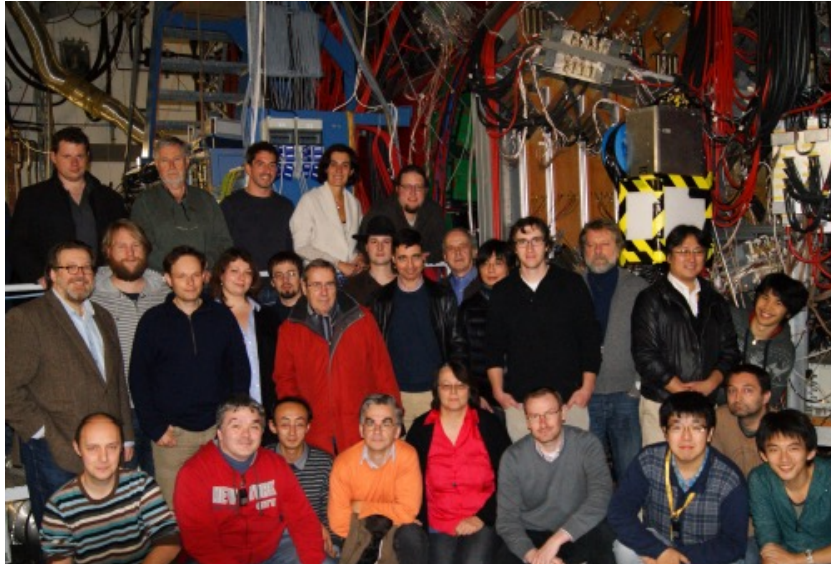
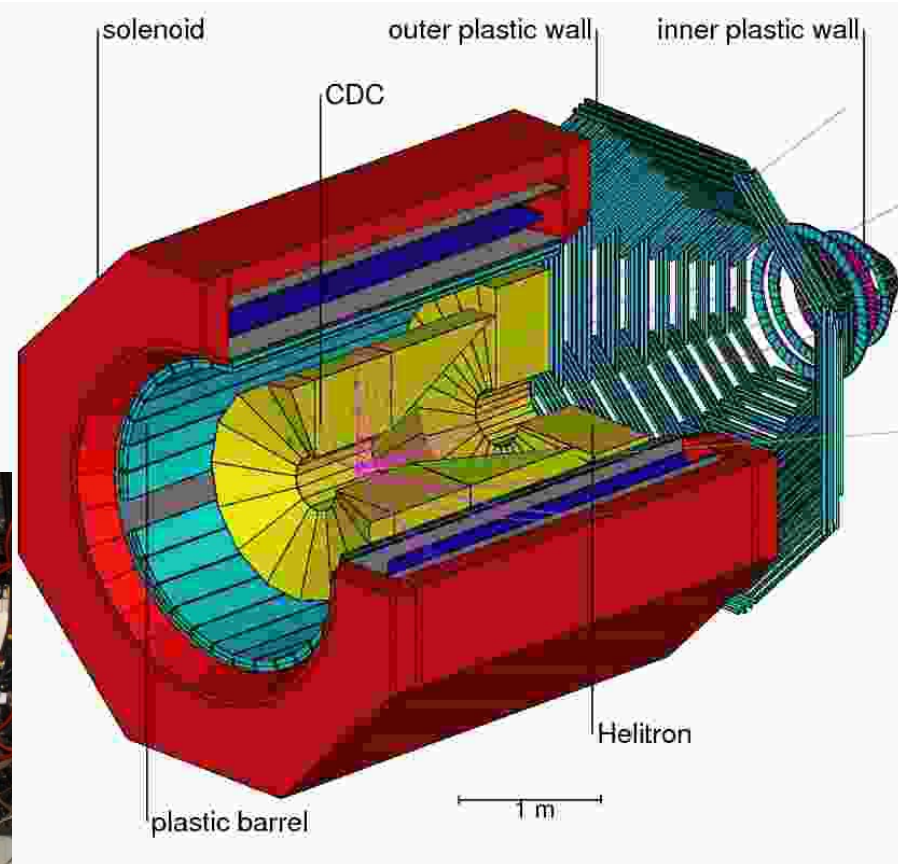
Slope $L = 3\rho_0 \frac{\partial E_{\text{sym}}}{\partial \rho}$

Pressure vs density for symmetric nuclear matter

Extended Data Fig. 5 Huth et al., Nature 606 (2022)

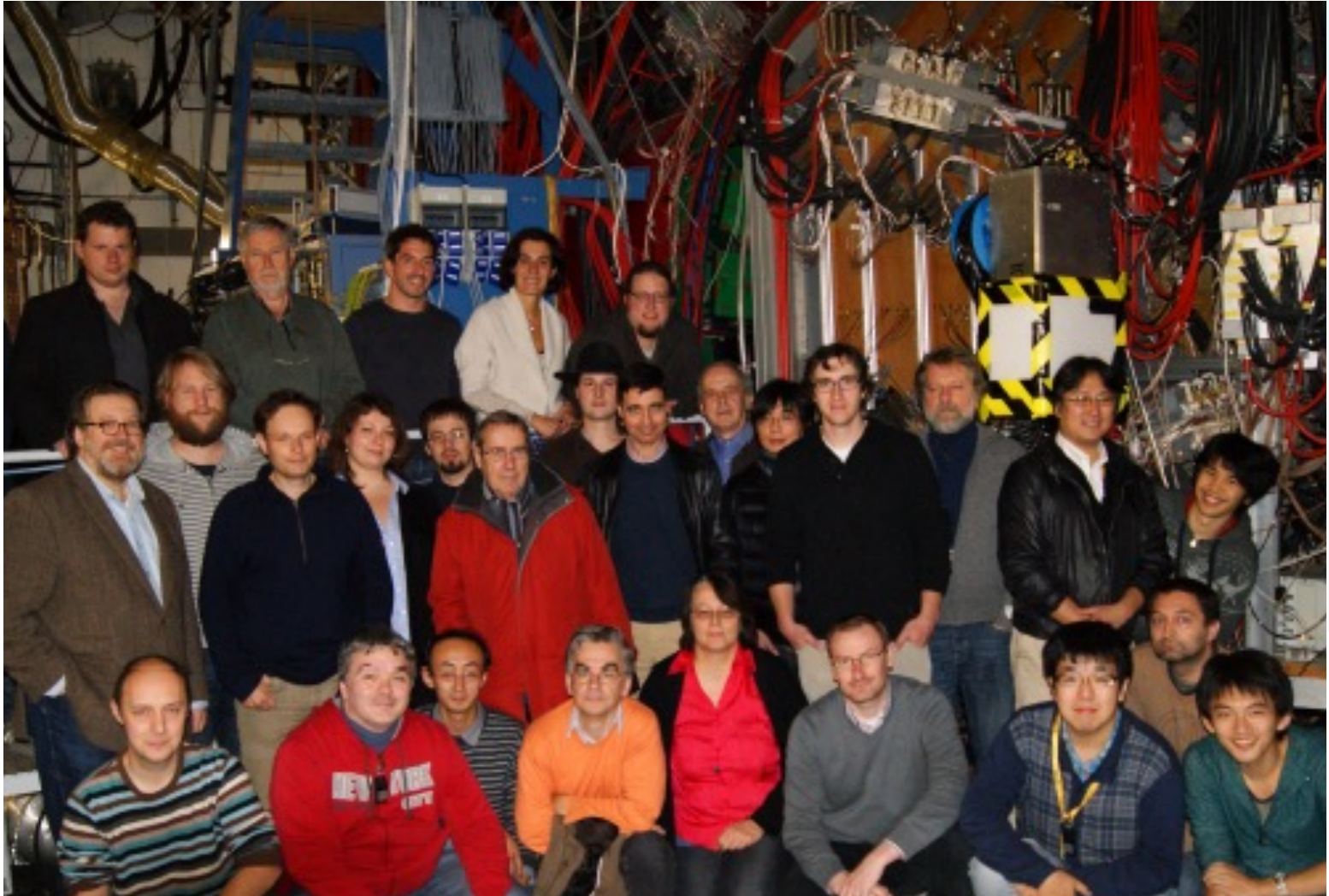


Measurements of FOPI



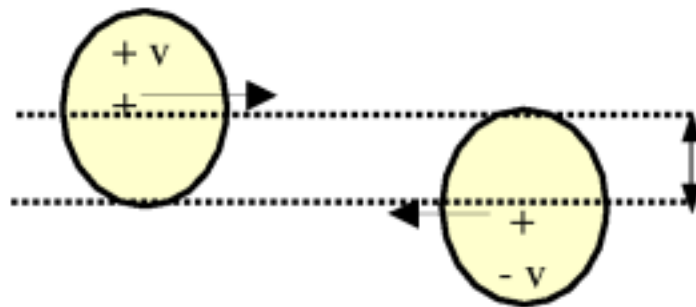
41

Measurements of FOPI



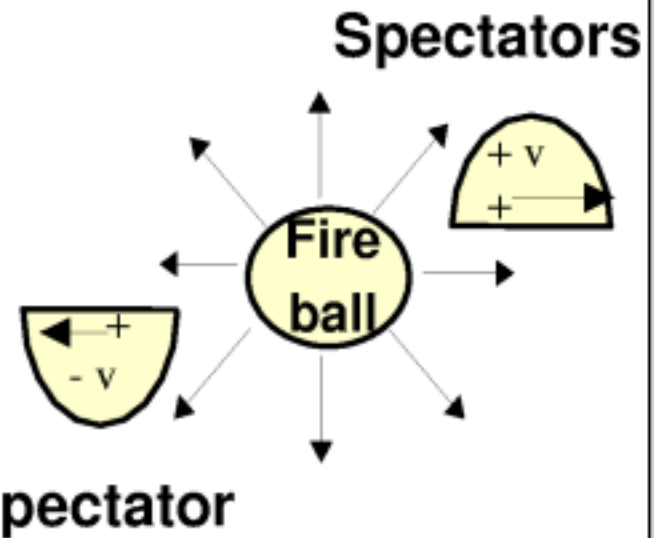
Elliptic flows of particles out of the participant region (« fireball »)

Before the collision



**Overlapping
zone**

after the collision



Elliptic flows of particles out of the participant region (« fireball »)

Flows at high density in heavy-ion collisions

$$\frac{dN}{d(\phi - \phi_R)}(y, p_t) = \frac{N_0}{2\pi} \left(1 + 2 \sum_{n \geq 1} v_n \cos n(\phi - \phi_R) \right)$$

y = rapidity

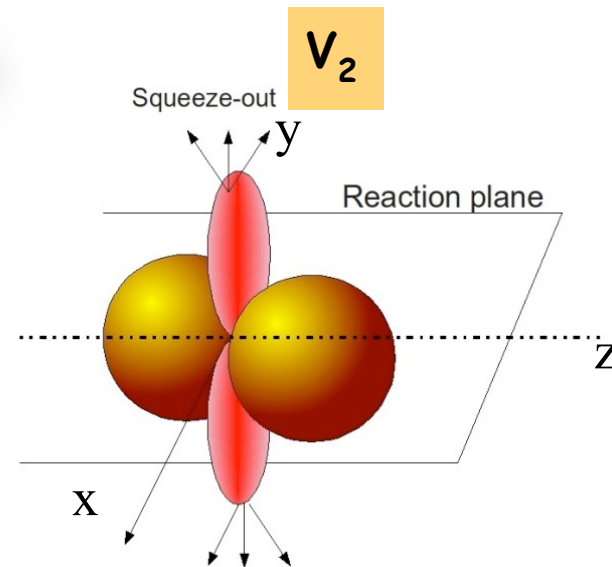
p_t = transverse momentum

ϕ_R = reaction plane azimuthal angle

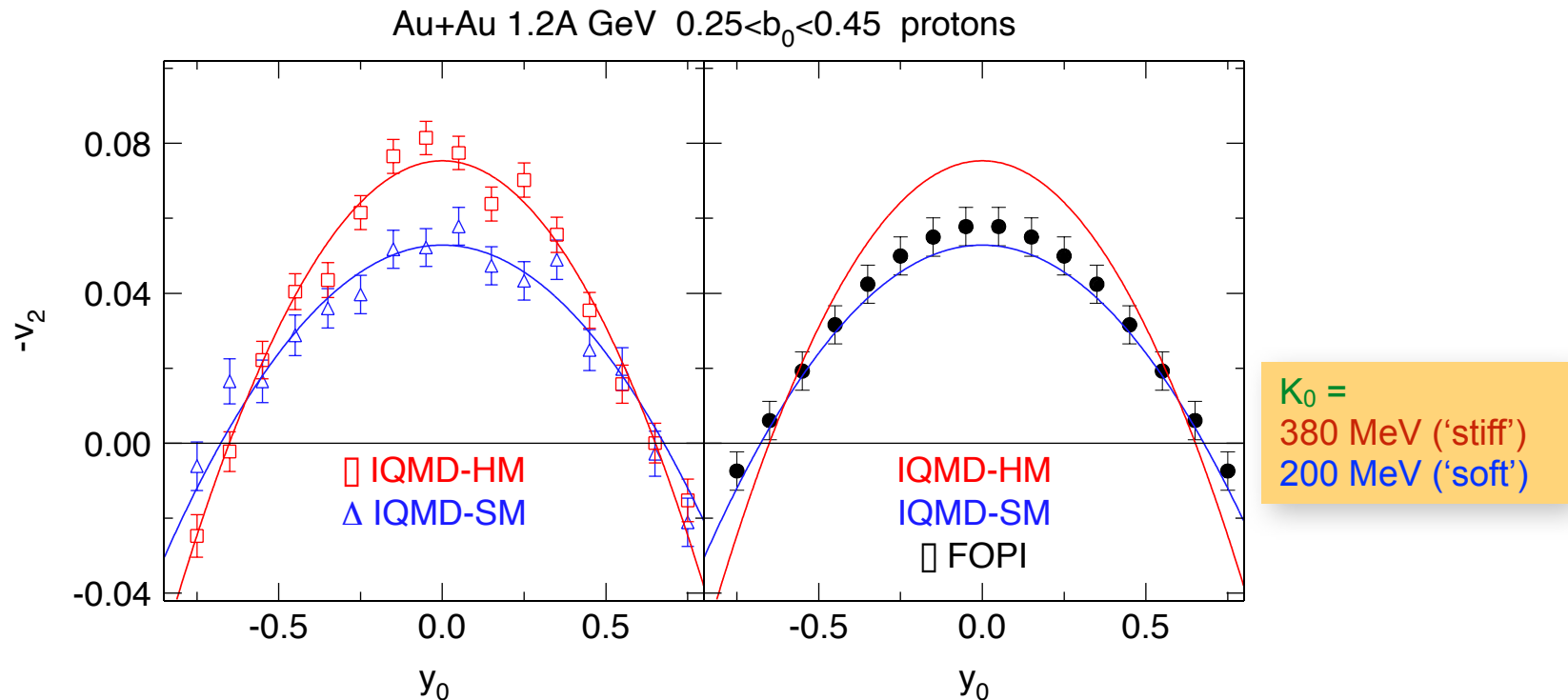
V_1 = 'side/directed flow', $\cos(\Phi - \Phi_R)$ mode

$$V_2(y, p_t) = \left\langle \frac{p_x^2 - p_y^2}{p_t^2} \right\rangle$$

'Elliptic flow': $\cos(2(\Phi - \Phi_R))$ mode, competition between 'in-plane' ($V_2 > 0$) and 'out-of-plane' ejection ($V_2 < 0$).



Elliptic flow



Elliptic flow

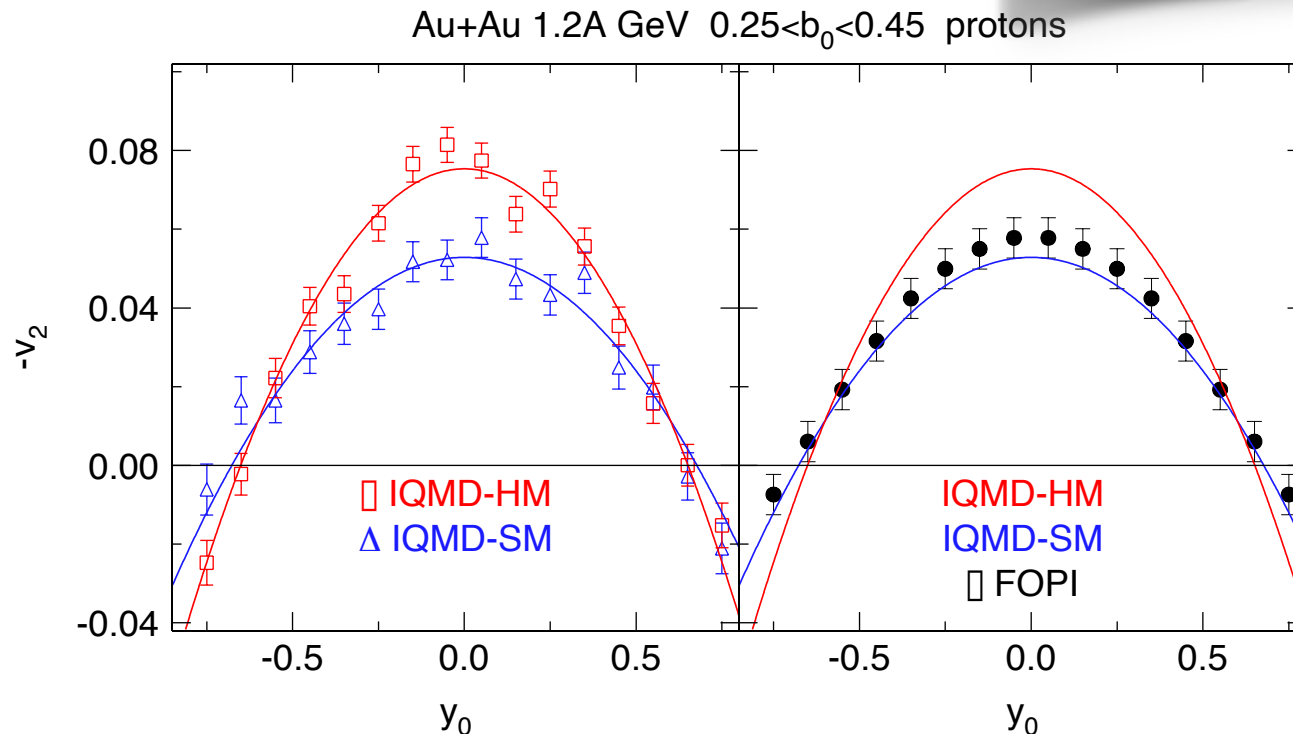
Complete shape of $v_2(y_0)$:

a new observable:

$$v_{2n} = |v_{20}| + |v_{22}|,$$

from fit

$$v_2(y_0) = v_{20} + v_{22} \cdot y_0^2$$

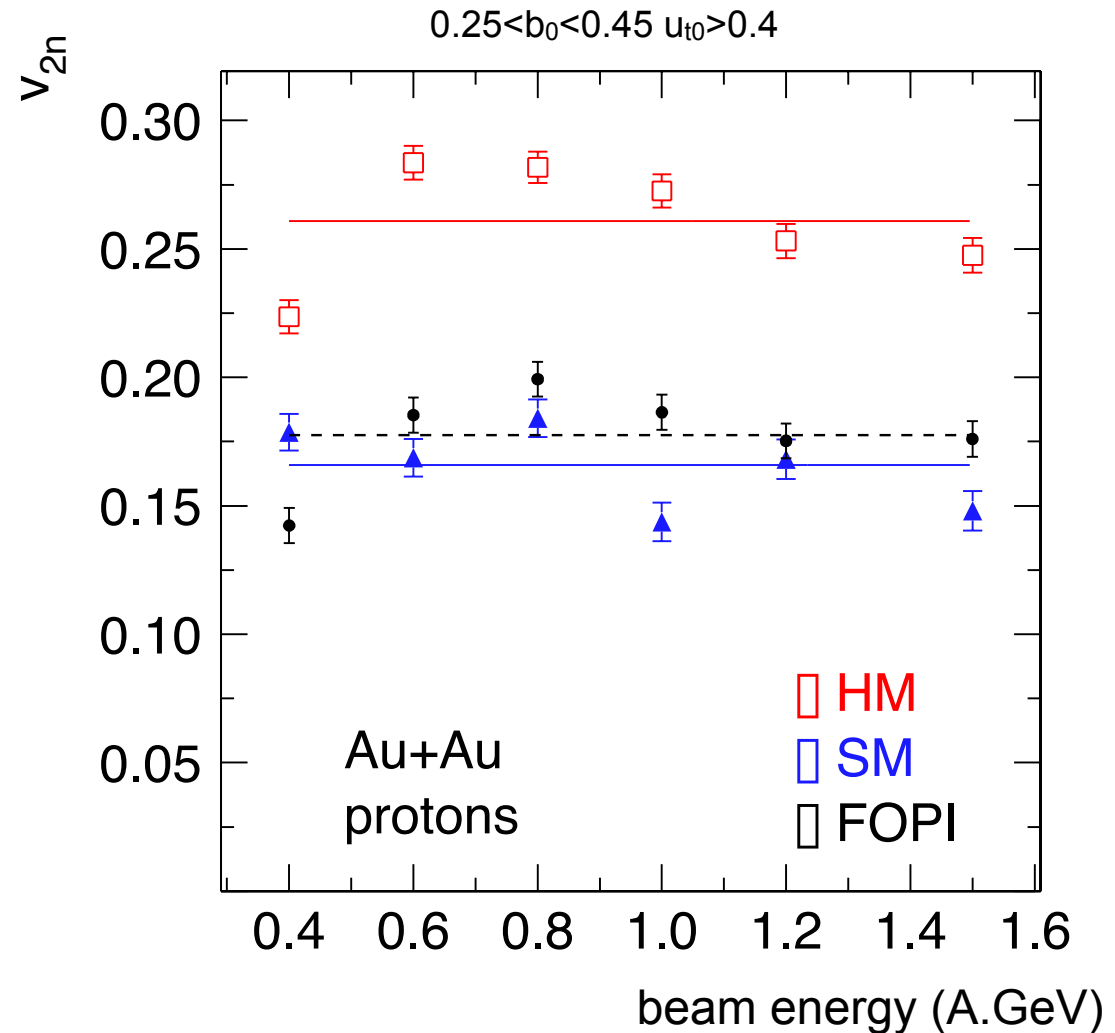


$K_0 =$
380 MeV ('stiff')
200 MeV ('soft')

A. Le Fèvre et al., NPA 945 (2016) 112–133

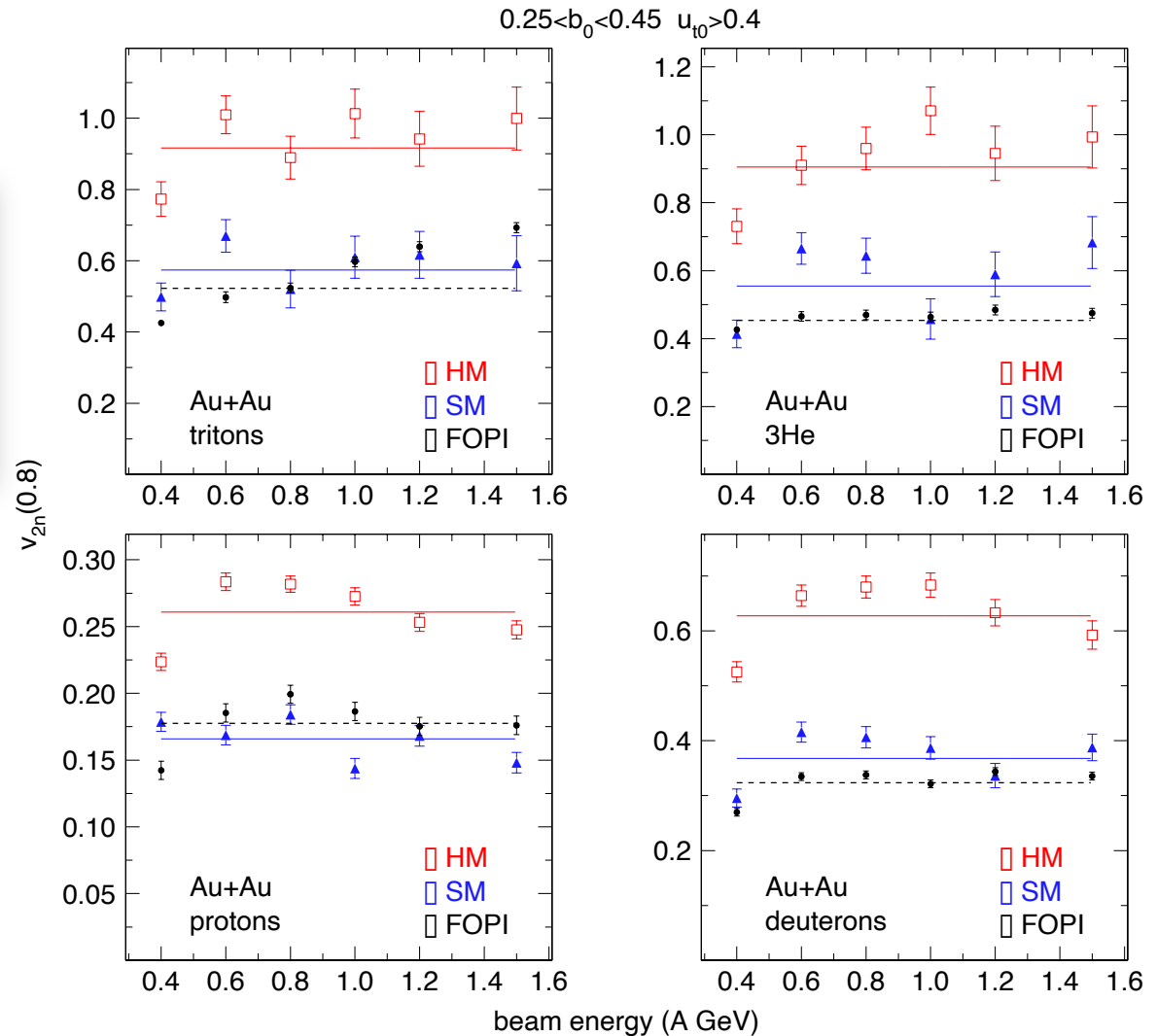
Elliptic flow method: FOPI and the incompressibility K_0

→ $v_{2n}(E_{\text{beam}})$ varies by a factor ≈ 1.6 , $\gg$ measured uncertainty (≈ 1.1)
→ clearly favors a 'soft' EOS.



A. Le Fèvre et al., NPA 945 (2016) 112–133

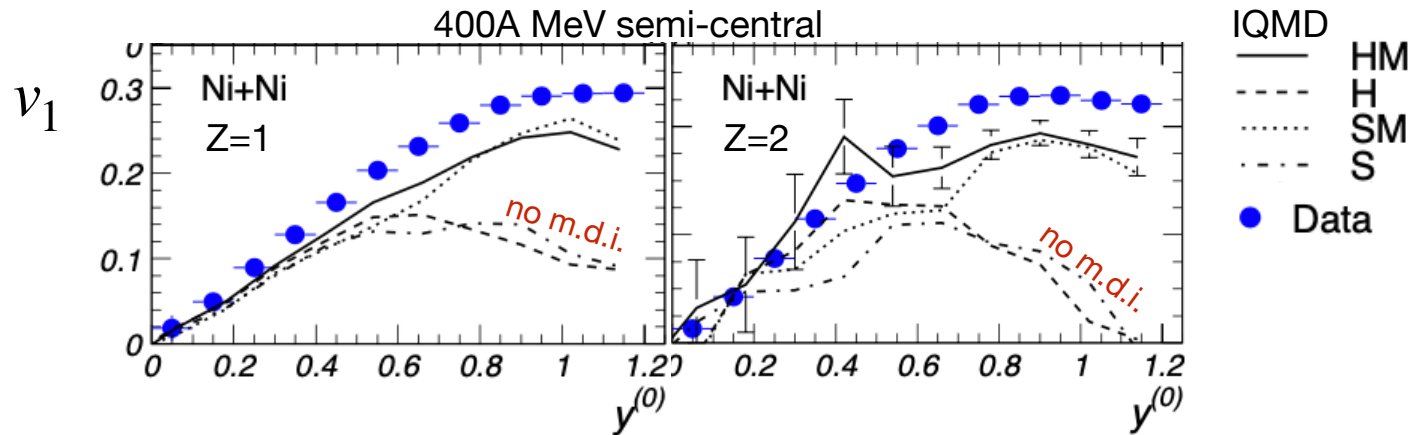
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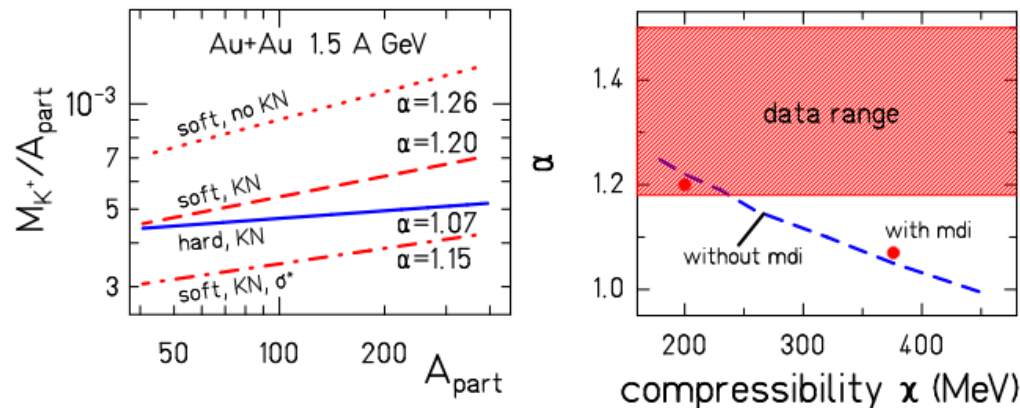
A. Le Fèvre et al., NPA 945 (2016) 112–133

Historical evidences of the need for momentum dependent interaction

- Directed flow (v_1) in semi-central collisions:
A. Andronic et al. (FOPI Collaboration), PRC 67, 034907 (2003)



- Subthreshold kaon data (KaoS) clearly advocate a **soft** EoS :
« Hadronic Matter is Soft », Ch. Hartnack, H. Oeschler and J. Aichelin, PRL 96, 012302 (2006)

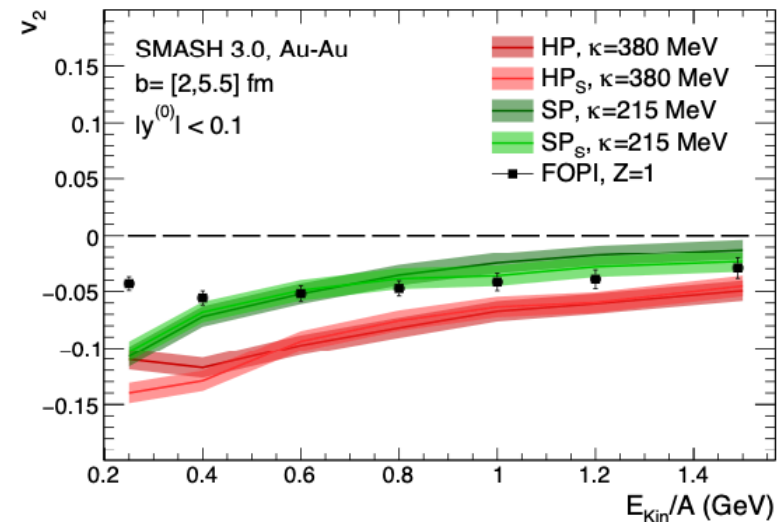
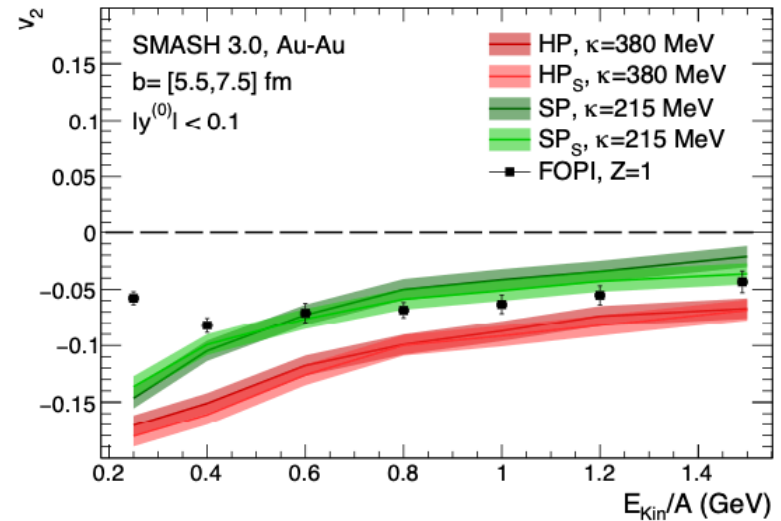
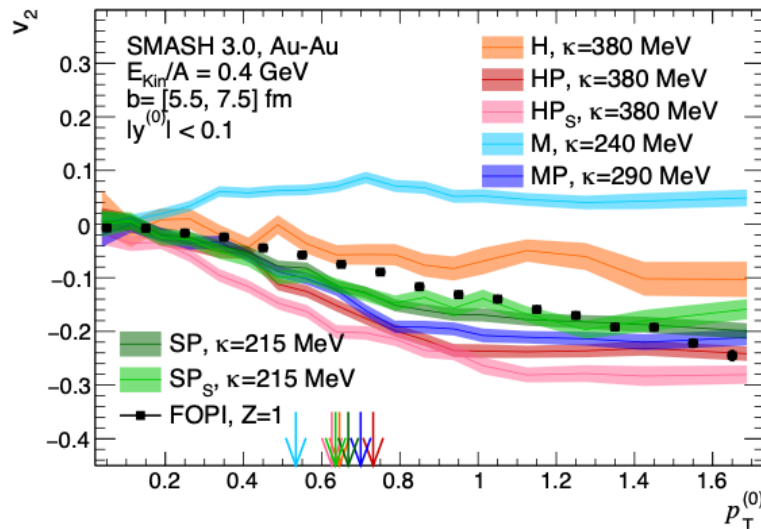


- Elliptic flow data can be explained by a **soft** EoS only if m.d.i. is included

SMASH:

- Soft momentum-dependent interaction (SP) favoured.
- At the highest inc. energies, harder EoS required
- Weakness of this analysis : restricted to $Z=1$

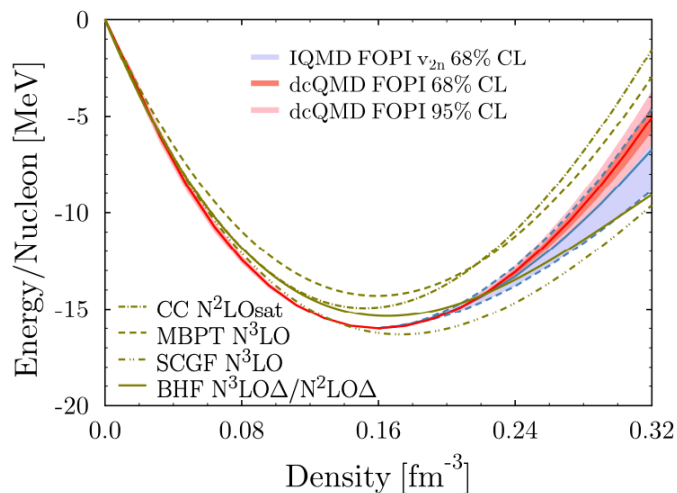
Tarasovicova et al., Eur. Phys. J. A 60, 232 (2024)



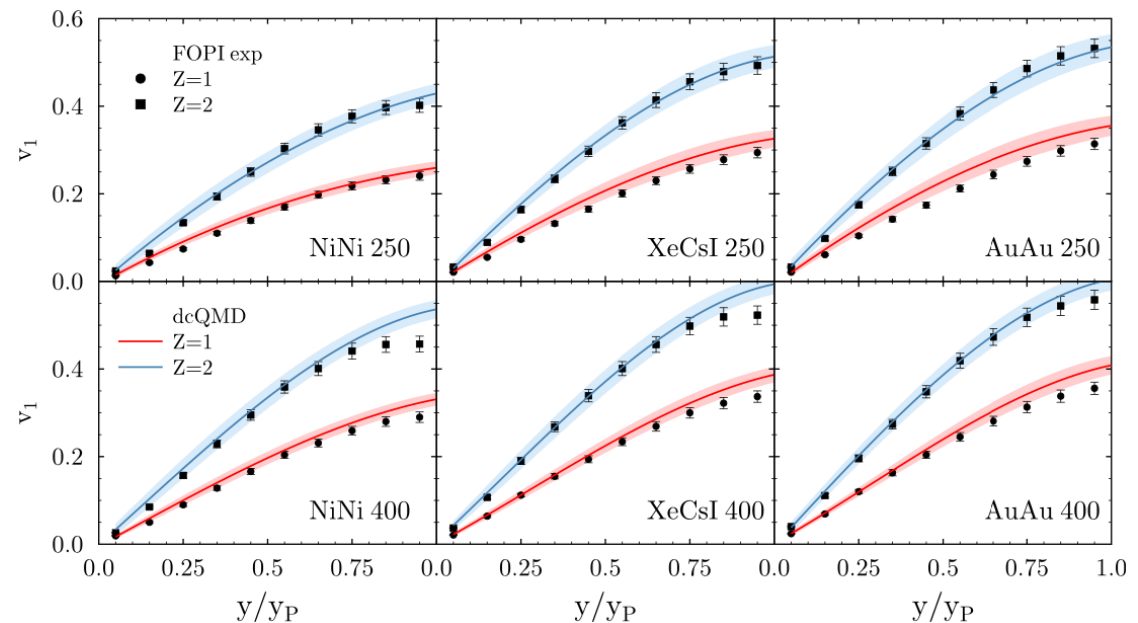
dcQMD:

M.D. Cozma, Phys. Rev. C 110 (2024) 0649111

- A comprehensive data analysis
- Optimisation on various parameters, assumptions, such as to narrow down constraints



$$dcQMD \rightarrow K_0 = 230^{+9}_{-11} \text{ MeV}$$



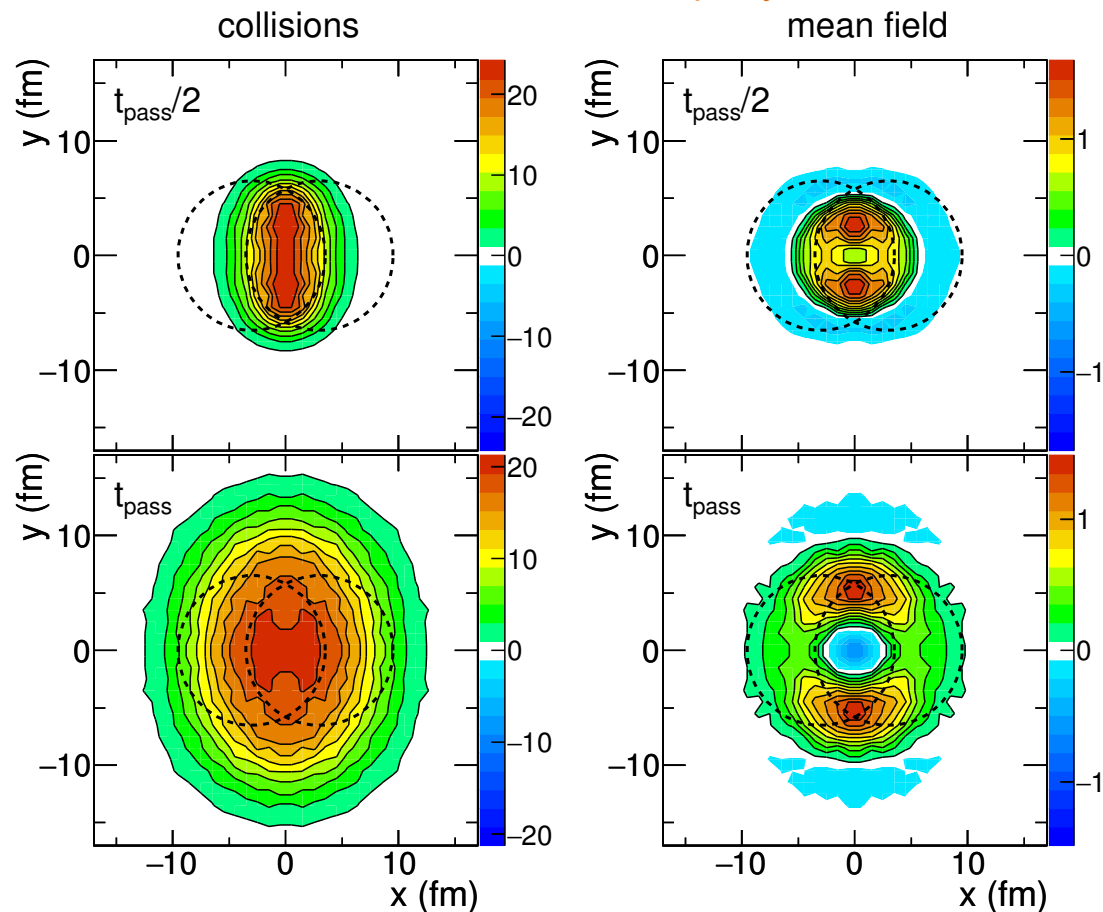
Cf. M.D. Cozma's talk on Thursday

Origin of elliptic flow: collisions versus mean field

An observable to quantify their respective contribution to it: transverse momentum modification induced projected on the direction of the final momentum:

$$\langle \Delta P_t^o(t) \rangle = \langle \Delta \mathbf{P}_t(t) \cdot \frac{\mathbf{p}_{final}}{|\mathbf{p}_{final}|} \rangle$$

IQMD, Au+Au, mid-central
0.6 A.GeV, mid-rapidity, $u_{t0} > 0.4$



A. Le Fèvre et al., PRC98 (2016) 034901

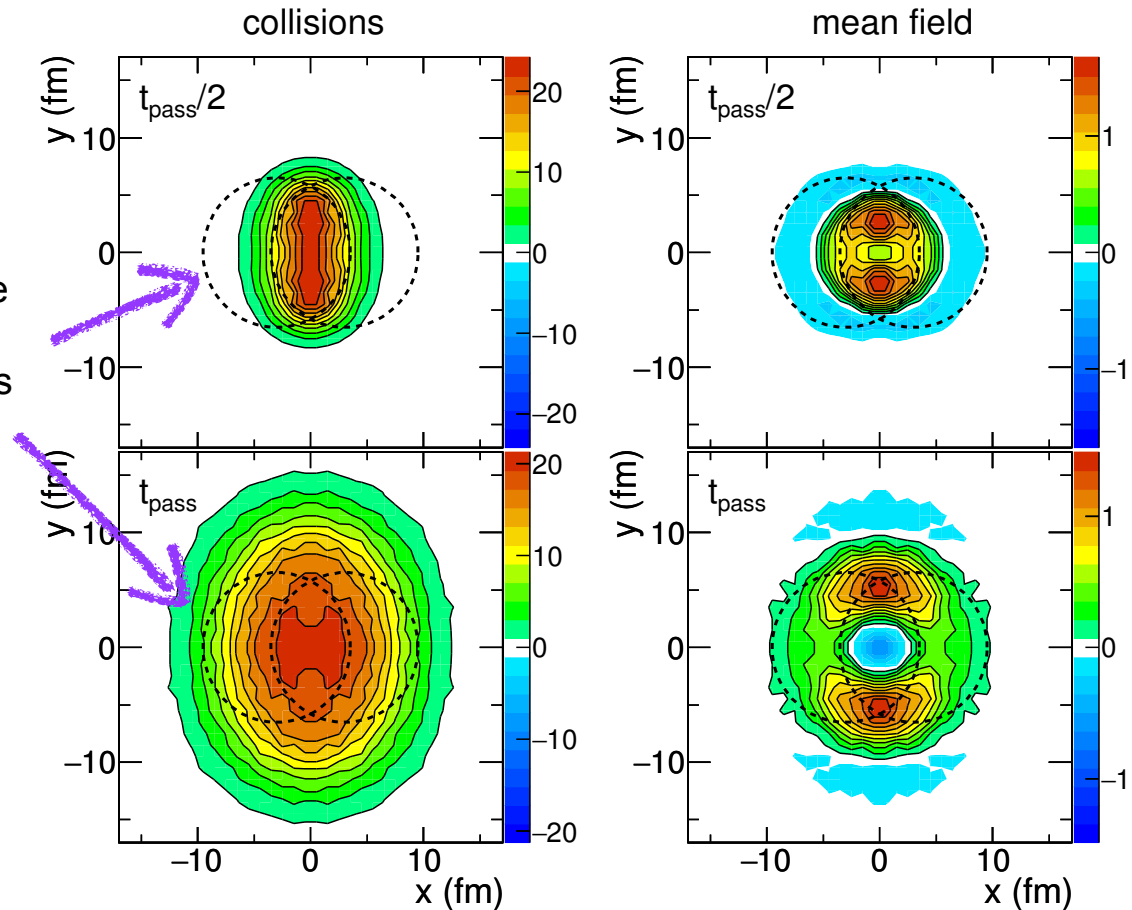
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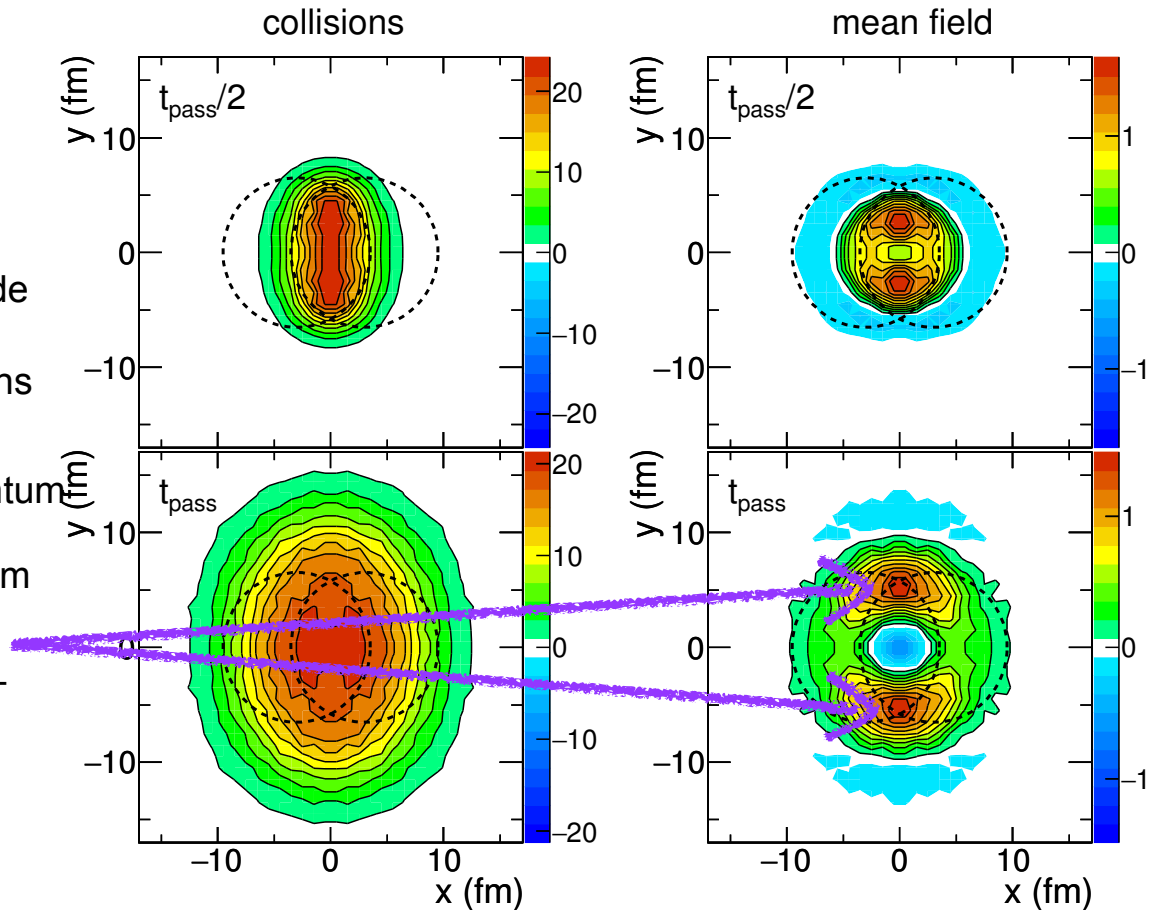
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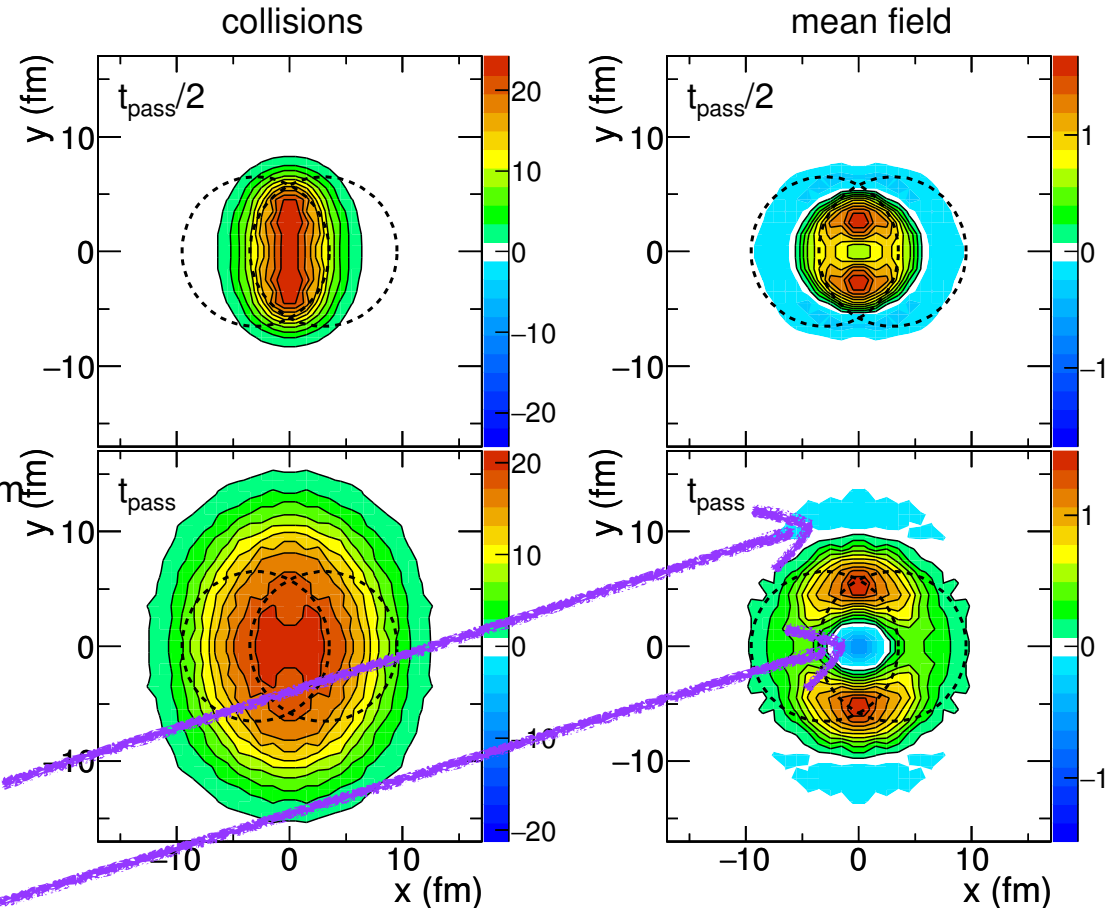
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Outer blue areas $\Leftarrow$ attractive potential of the remnant, deceleration.

Inner blue area: inner density decreases and attraction by the moving spectators $\Rightarrow$ transverse velocity decreases

IQMD, Au+Au, mid-central
0.6 A.GeV, mid-rapidity, $u_{t0} > 0.4$

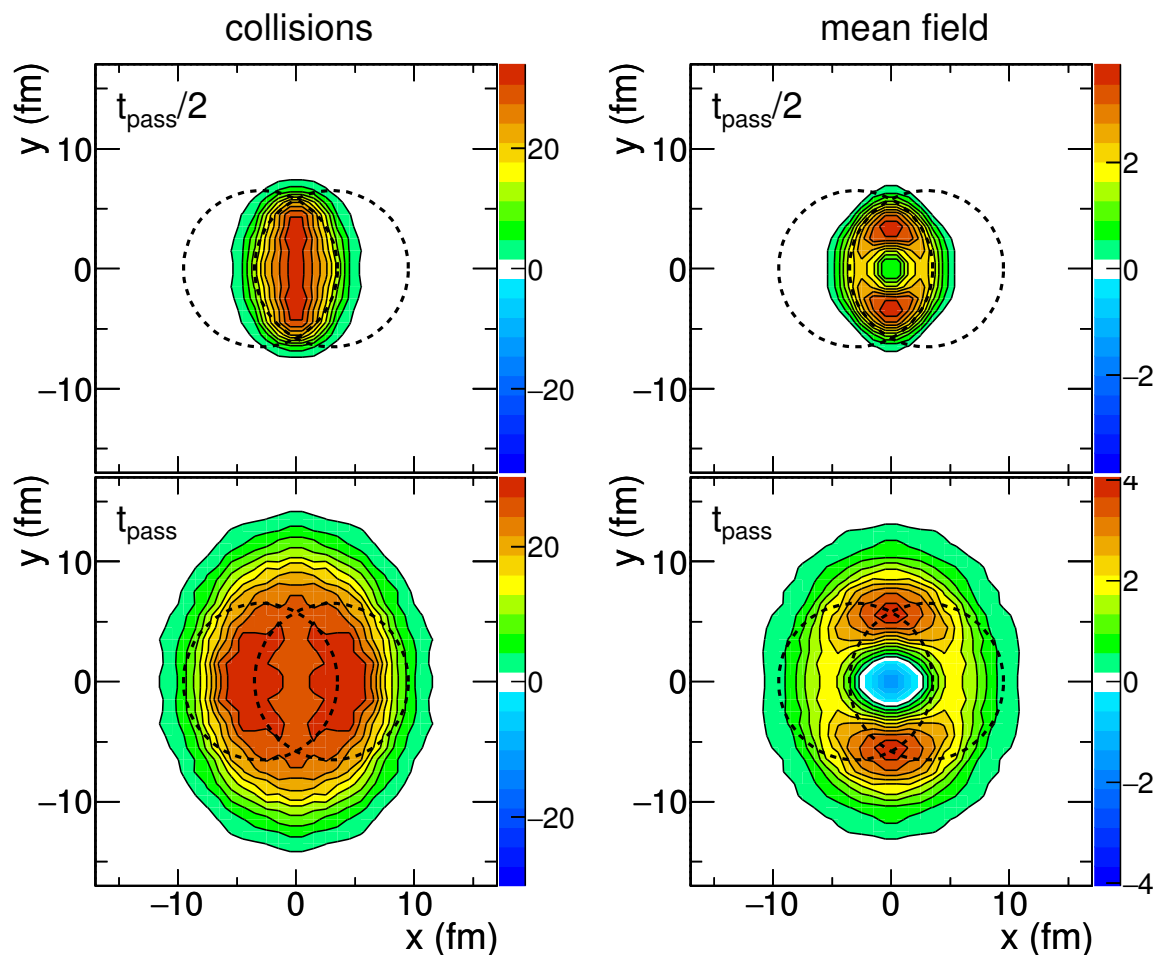


A. Le Fèvre et al., PRC98 (2016) 034901

Origin of elliptic flow: collisions versus mean field

1.5 A.GeV, mid-rapidity, $u_{t0} > 0.4$

Little difference between 0.6 AGeV
and at 1.5 AGeV.



A. Le Fèvre et al., PRC98 (2016) 034901



Origin of elliptic flow: collisions versus mean field





Origin of elliptic flow: collisions versus mean field



- ❖ The elliptic flow observed in the reactions around $E_{\text{kin}} \approx 1$ AGeV for protons at mid-rapidity ($|y_0| < 0.2$) has two origins:



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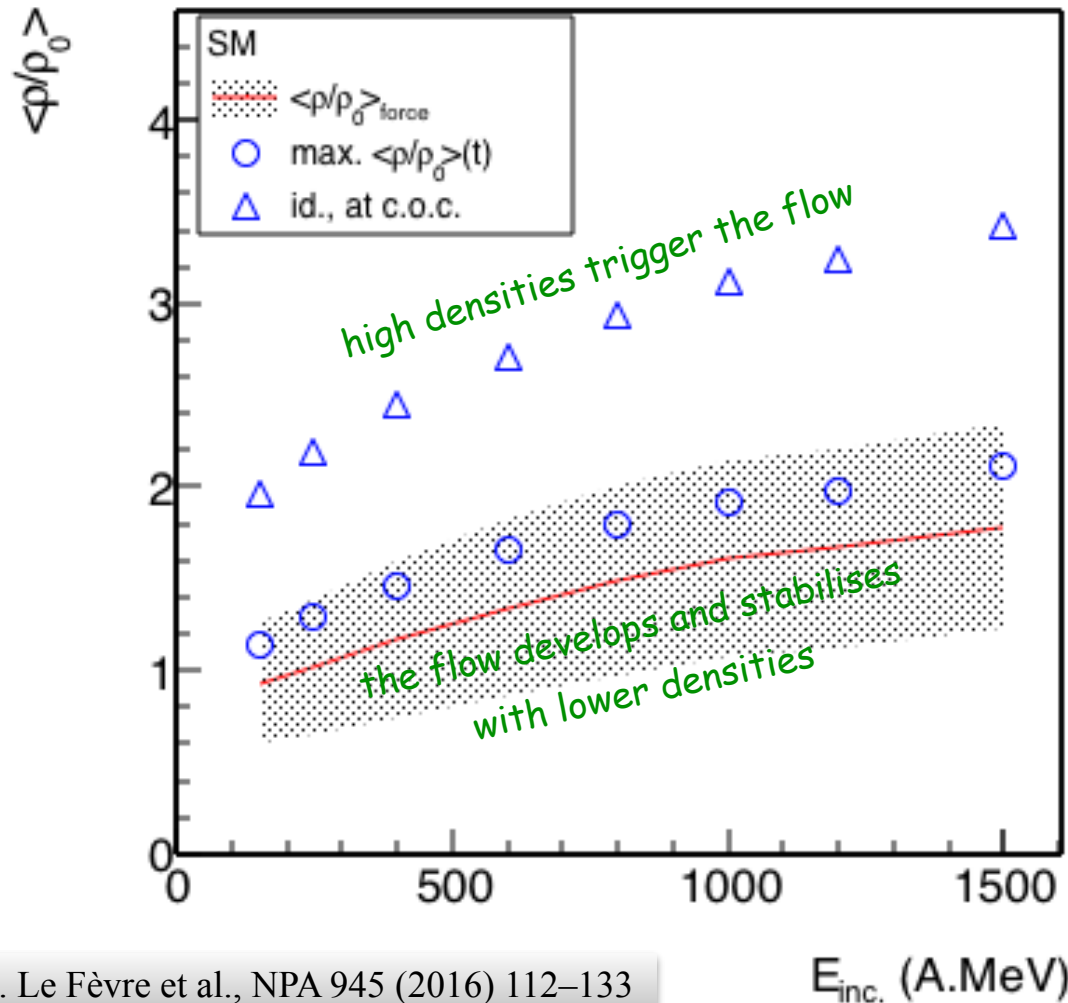
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- ❖ This effect is amplified if one selects particles with a high transverse velocity.

Determining densities probed by an experiment with a given observable is capital !



- In the QMD model, the EOS must be correct over a broad range of densities in order to predict the observed elliptic flow.
- The density range, relevant to the EOS evidenced by the FOPI Collaboration, spans in the range $\rho \approx (1 - 3) \rho_0$.

A. Le Fèvre et al., NPA 945 (2016) 112–133

- K_0 as from FOPI flow data

$$IQMD \rightarrow K_0 = 190 \pm 30 \text{ MeV}$$

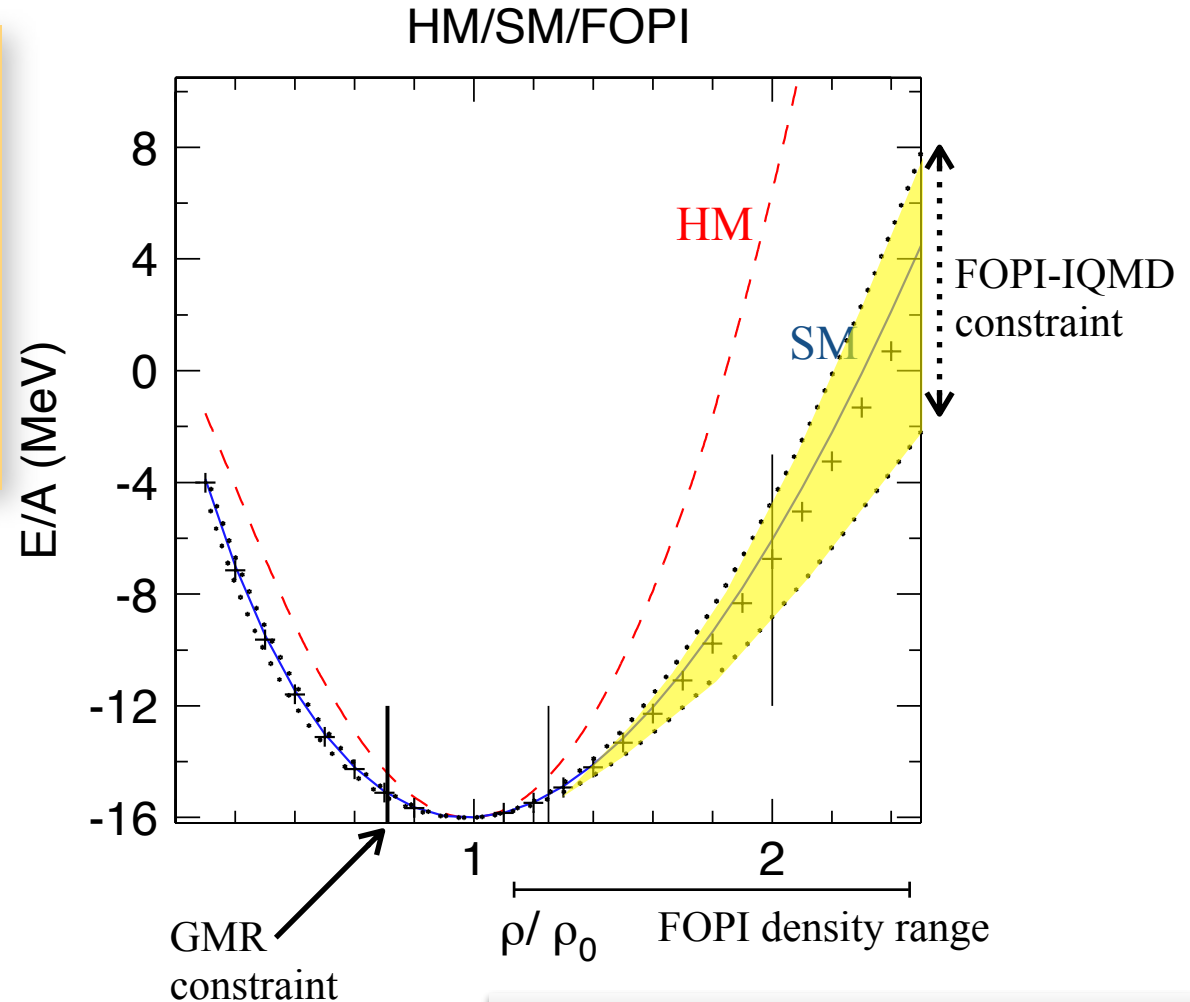
[A. Le Fèvre et al., NPA945(2016)112-133]

$$UrQMD \rightarrow K_0 = 220 \pm 40 \text{ MeV}$$

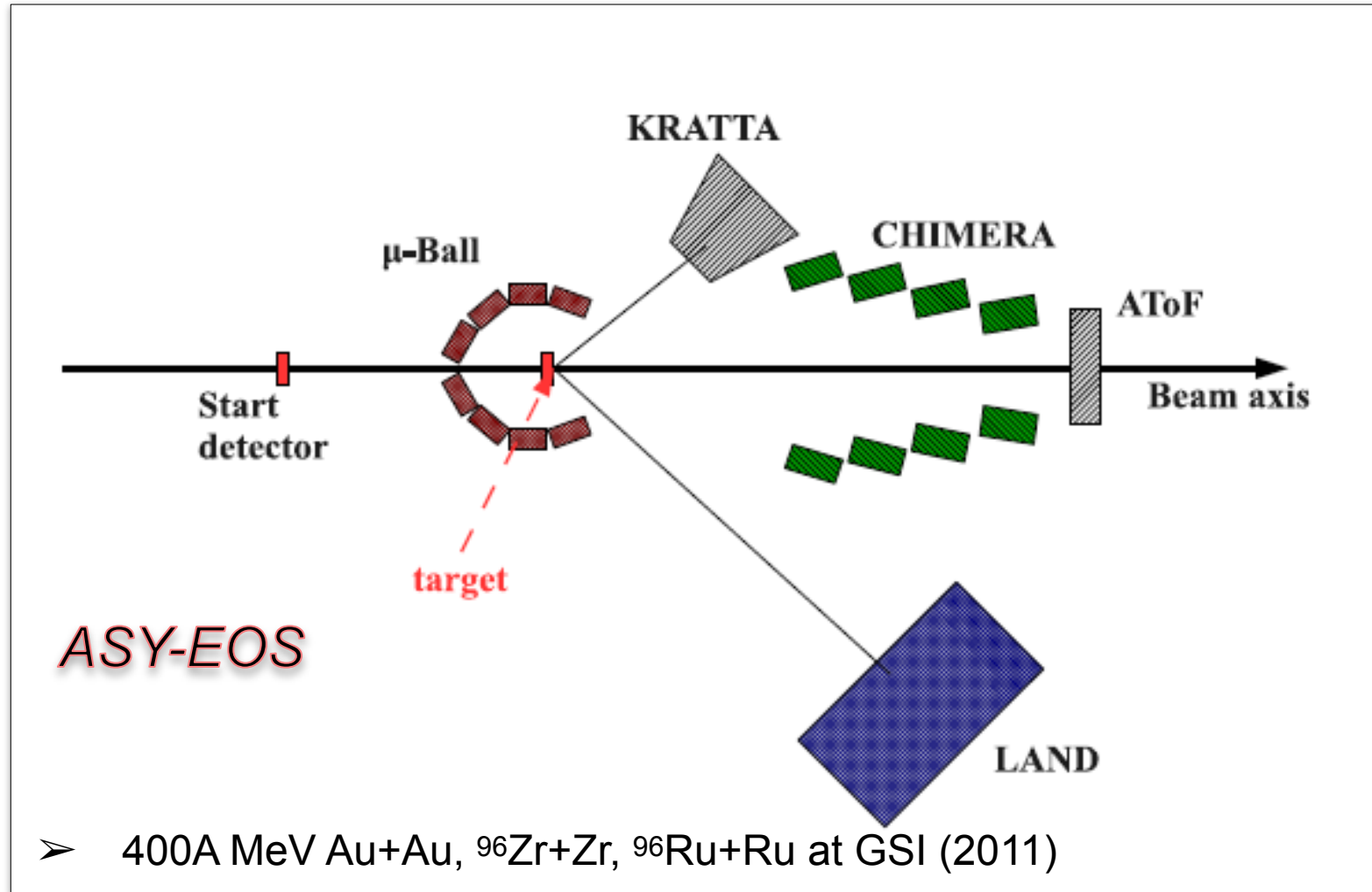
[Y. Wang et al., PLB-778(2018)207-212]

$$dcQMD \rightarrow K_0 = 230^{+9}_{-11} \text{ MeV}$$

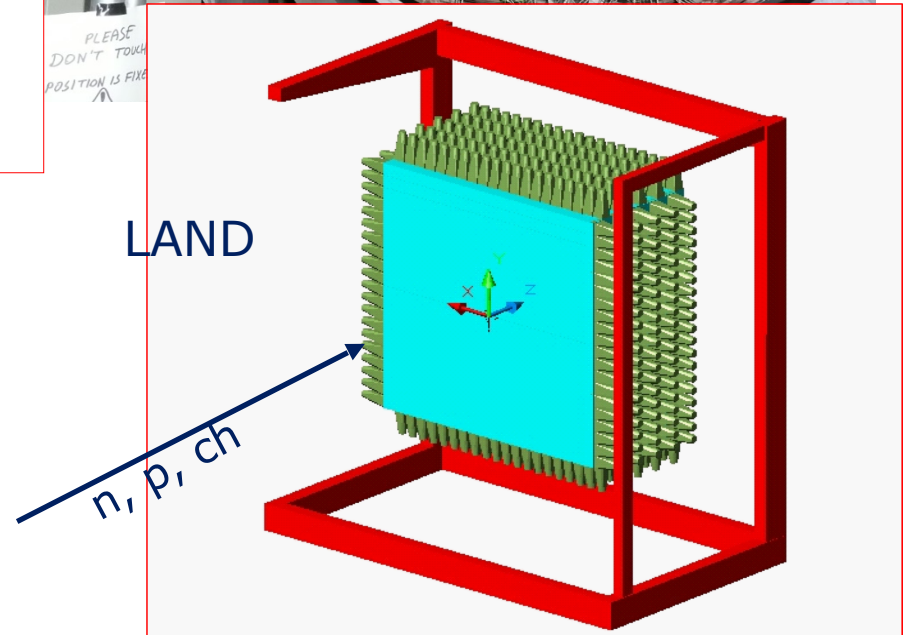
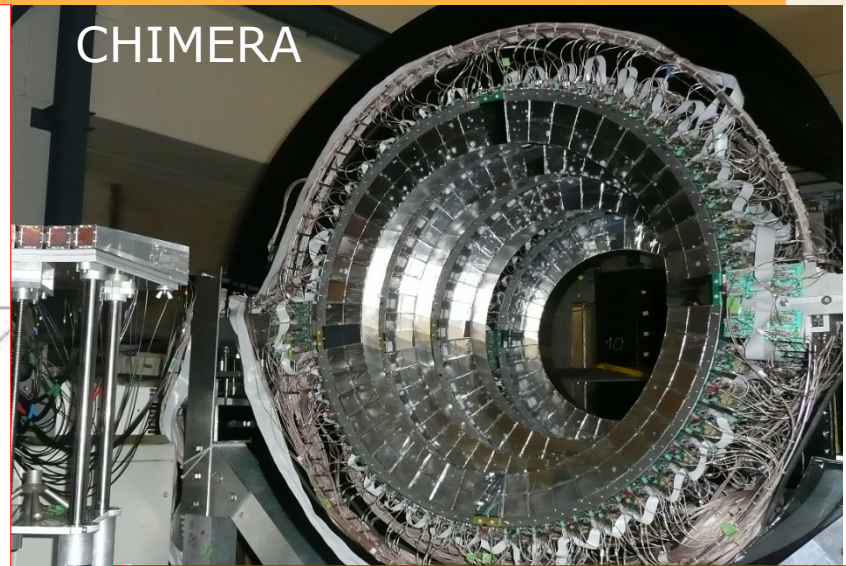
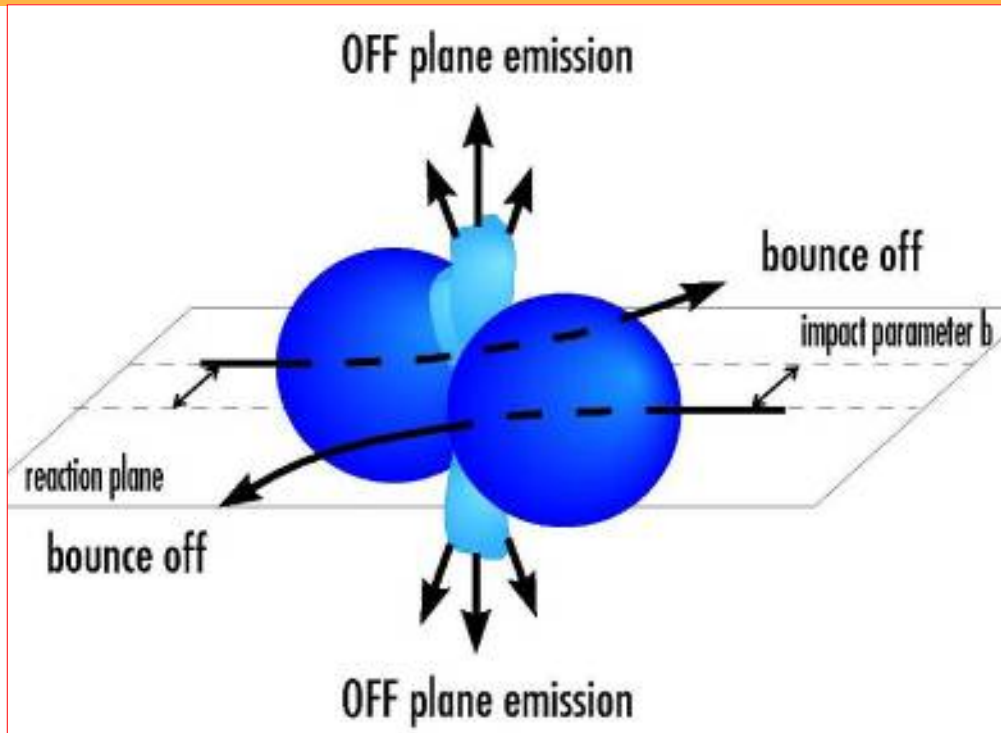
[M.D. Cozma, PRC 110 (2024) 0649111]



A. Le Fèvre et al., NPA 945 (2016) 112–133



Elliptic flow and symmetry energy constraint with ASY-EOS I

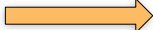


tested with existing **FOPI-LAND** data
 $^{197}\text{Au} + ^{197}\text{Au}$ @ 400 A MeV
 Russotto+ PLB 697 (2011)

ASY-EOS experiment in 2011
 $^{197}\text{Au} + ^{197}\text{Au}$ @ 400 A MeV
 Russotto+ PRC 94 (2016)

Differential elliptic flow v_2 of n/p

UrQMD* (Q. Li et al.) predicts:

“hard” $E_{\text{sym}}(\rho)$ protons unchanged

 “soft” $E_{\text{sym}}(\rho)$ neutron and proton flow inverted

Towards model invariance:

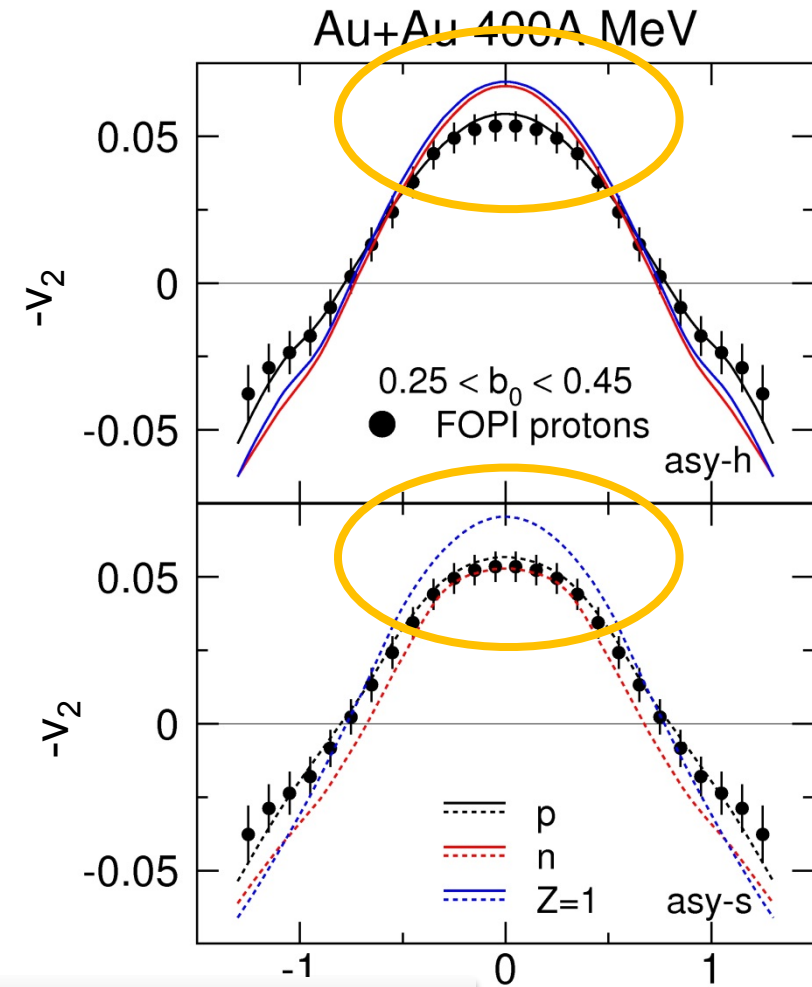
tested stability with different models:

- soft vs. hard EoS: $190 < K_0 < 260$ MeV
- density dependance of $\sigma_{NN,elastic}$
- asymmetry dependance of $\sigma_{NN,elastic}$
- optical potential
- momentum dependence of isovector potential

M.D. Cozma et al., PRC 88 (2013) 044912,
[PRC 110 \(2024\) 0649111](#)

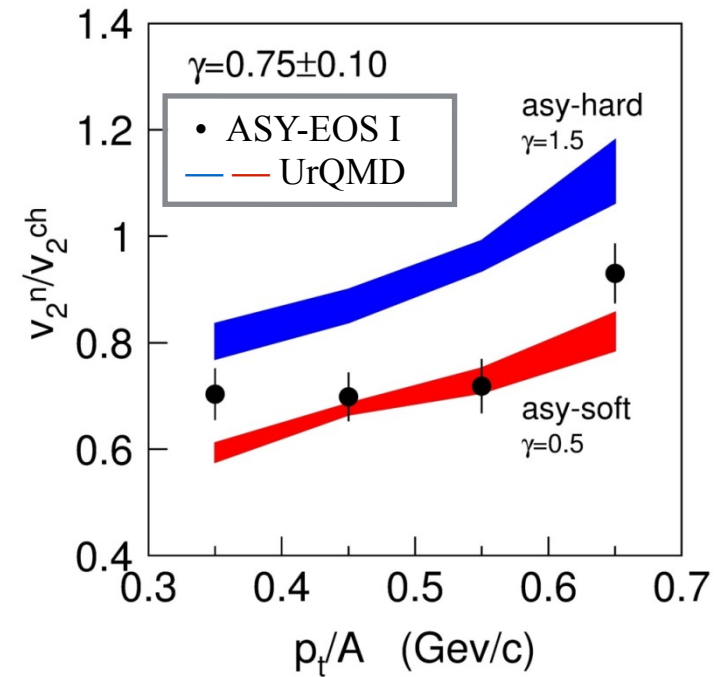
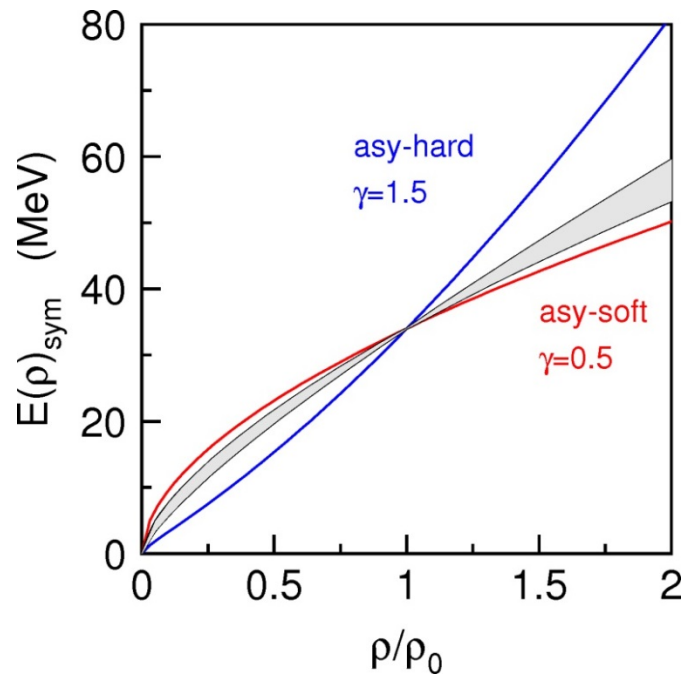
P. Russotto et al., PLB 267 (2010)

Y. Wang et al., PRC 89, 044603 (2014)



*UrQMD: Qingfeng Li et al.
 Data. W. Reisdorf et al.

y_0



P. Russo et al., PRC (2017)

- parametrization for E_{asy} used in the **UrQMD** model:

$$E_{\text{sym}} = E_{\text{sym}}^{\text{pot}} + E_{\text{sym}}^{\text{kin}} = 22 \text{ MeV} \cdot (\rho/\rho_0)^\gamma + 12 \text{ MeV} \cdot (\rho/\rho_0)^{2/3}$$

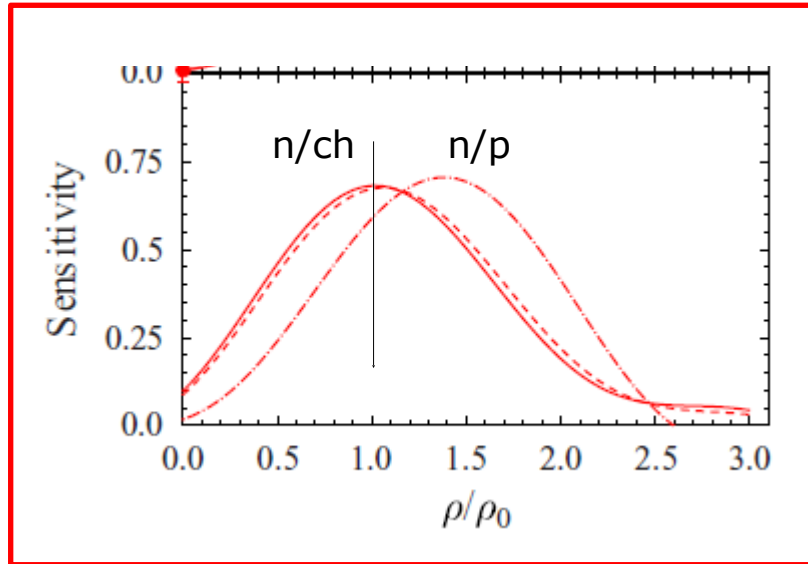
- systematic errors corrected: $\gamma = 0.72 \pm 0.19$
- slope parameter: $L = 72 \pm 13 \text{ MeV}$, $E_{\text{sym}}(\rho_0) = 34 \text{ MeV}$
- slope parameter: $L = 63 \pm 11 \text{ MeV}$, $E_{\text{sym}}(\rho_0) = 31 \text{ MeV}$

- A more recent analysis of M.D. Cozma with **dcQMD** has concluded
 $L = 63_{-13}^{+10} \text{ MeV}$, $E_{\text{sym}}(\rho_0) = 35 \pm 1 \text{ MeV}$

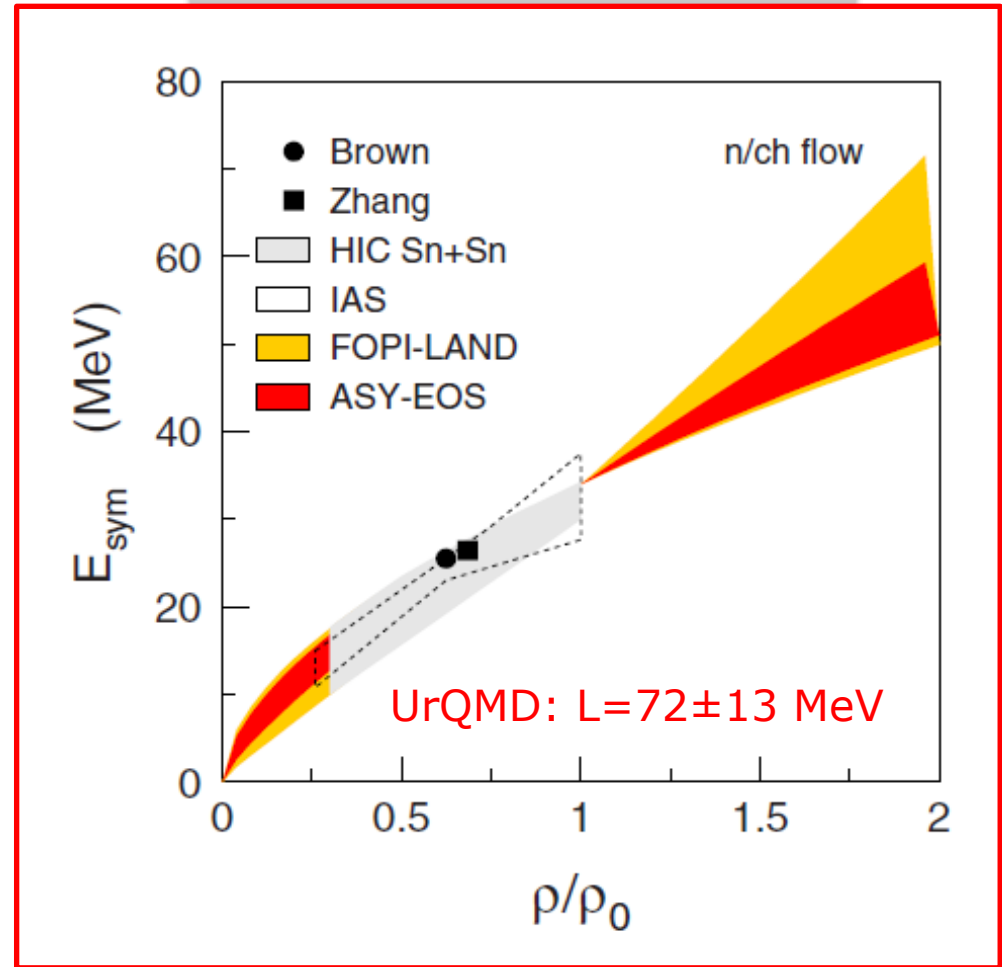
M.D. Cozma, PRC 110 (2024) 0649111

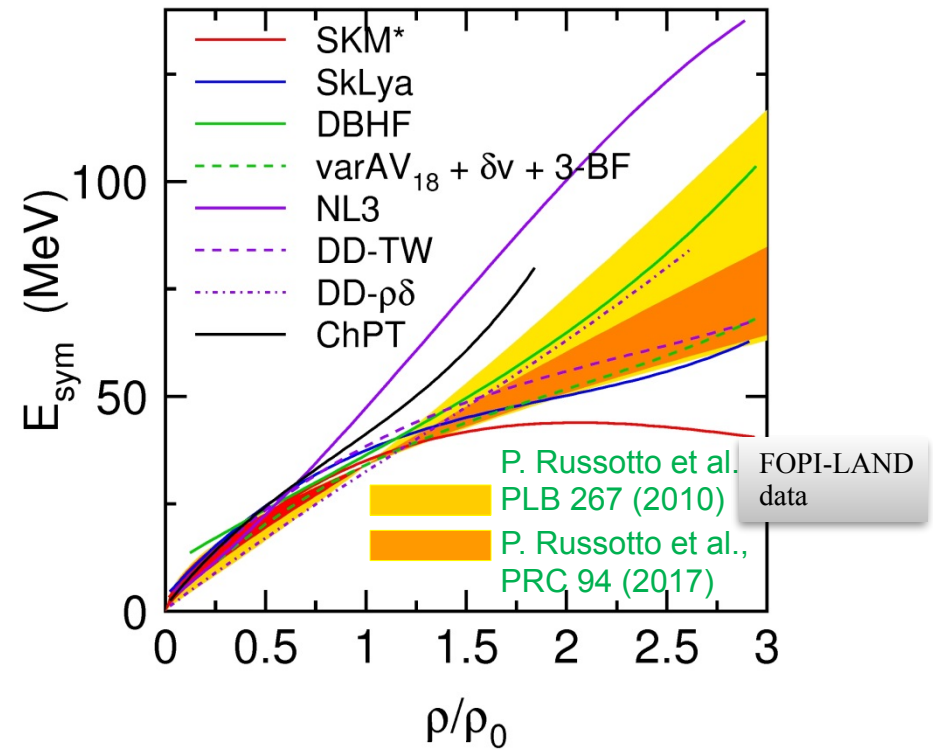
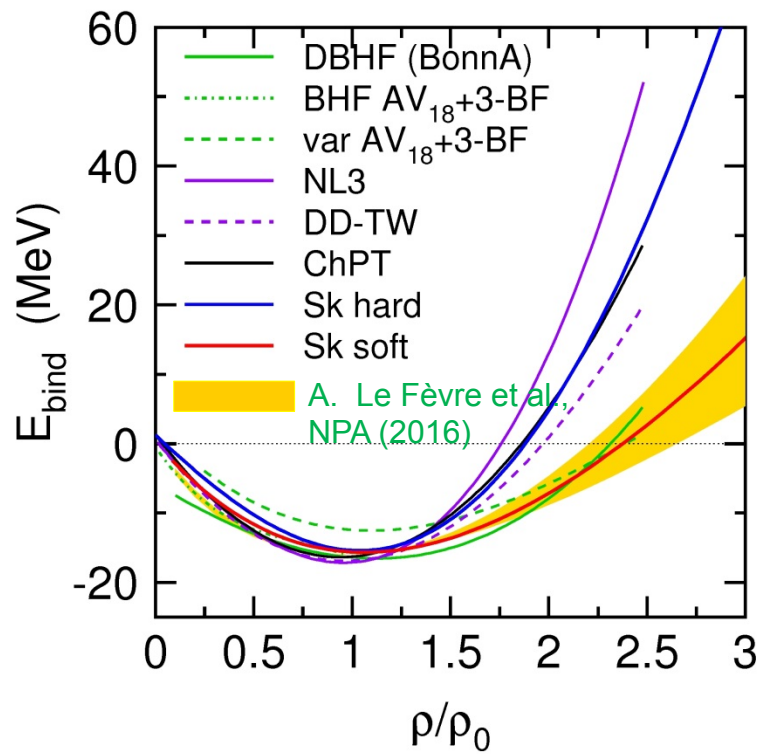
sensitivity to density

P. Russotto+ PRC 94, 034608 (2016)

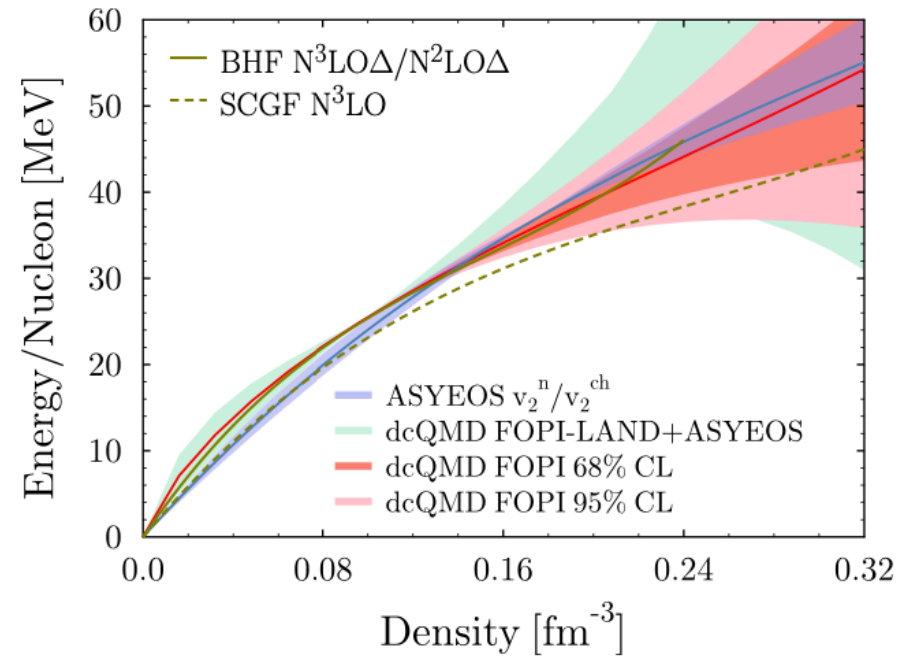
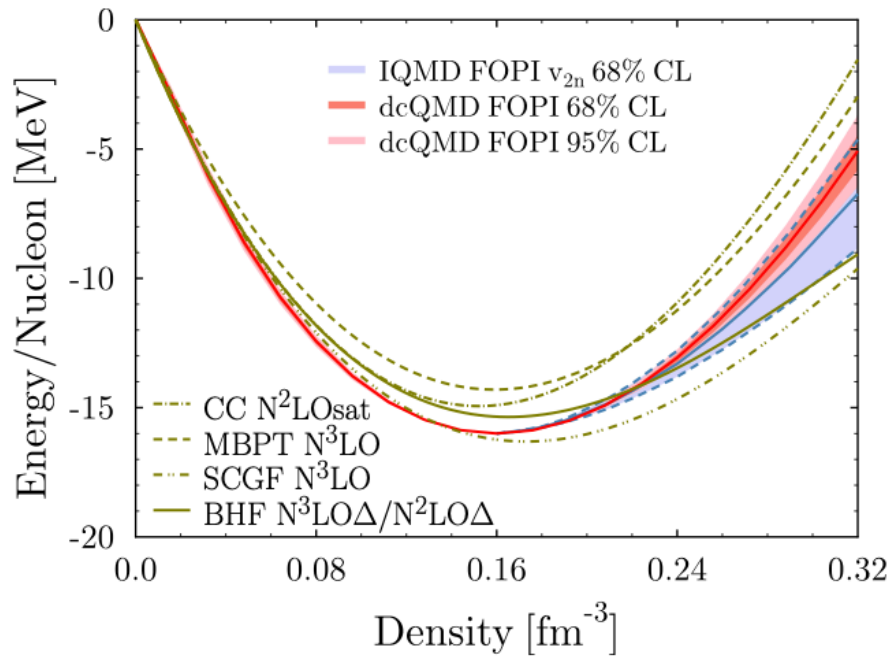


density probed extends to $2.5 \rho_0$
maximum near **saturation density**





M.D. Cozma, PRC 110 (2024) 0649111

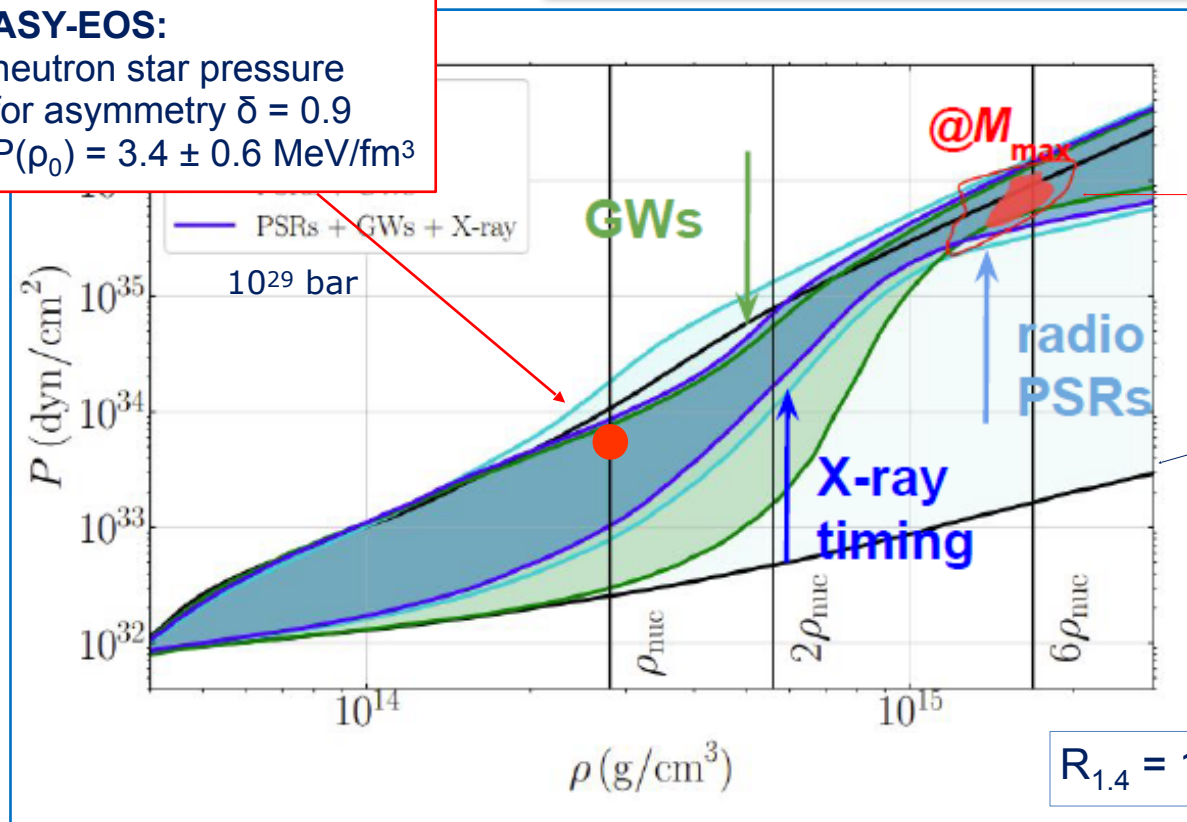


Cf. M.D. Cozma's talk on Thursday

Reed Essick at NuSym22 in Catania

ASY-EOS:

neutron star pressure
for asymmetry $\delta = 0.9$
 $P(\rho_0) = 3.4 \pm 0.6 \text{ MeV/fm}^3$



Legred+, PRD 104, 063003 (2021)

50%/90% contours

model-agnostic prior

$$R_{1.4} = 12.6 \pm 1.1 \text{ km (68\%)}$$

$$R_{1.4} P_{\text{sat}}^{-1/4} = 9.5 \pm 0.5 \Rightarrow R_{1.4} = 12.9 \pm 0.6 \text{ km} \pm 0.7 \text{ km (68\%)}$$

(stat.) (correl.)

for ASY-EOS: Russotto+, PRC 94, 034608 (2016)

for correlation: Lattimer, arXiv:2308.08001

Cf. W. Trautmann's talk on Wednesday



Combining heavy-ion experiments, astrophysical observations, and nuclear theory



Nature 606, 276 (2022)

Article

Constraining neutron-star matter with microscopic and macroscopic collisions

<https://doi.org/10.1038/s41586-022-04750-w>

Received: 13 July 2021

Accepted: 11 April 2022

Published online: 8 June 2022

Open access

Check for updates

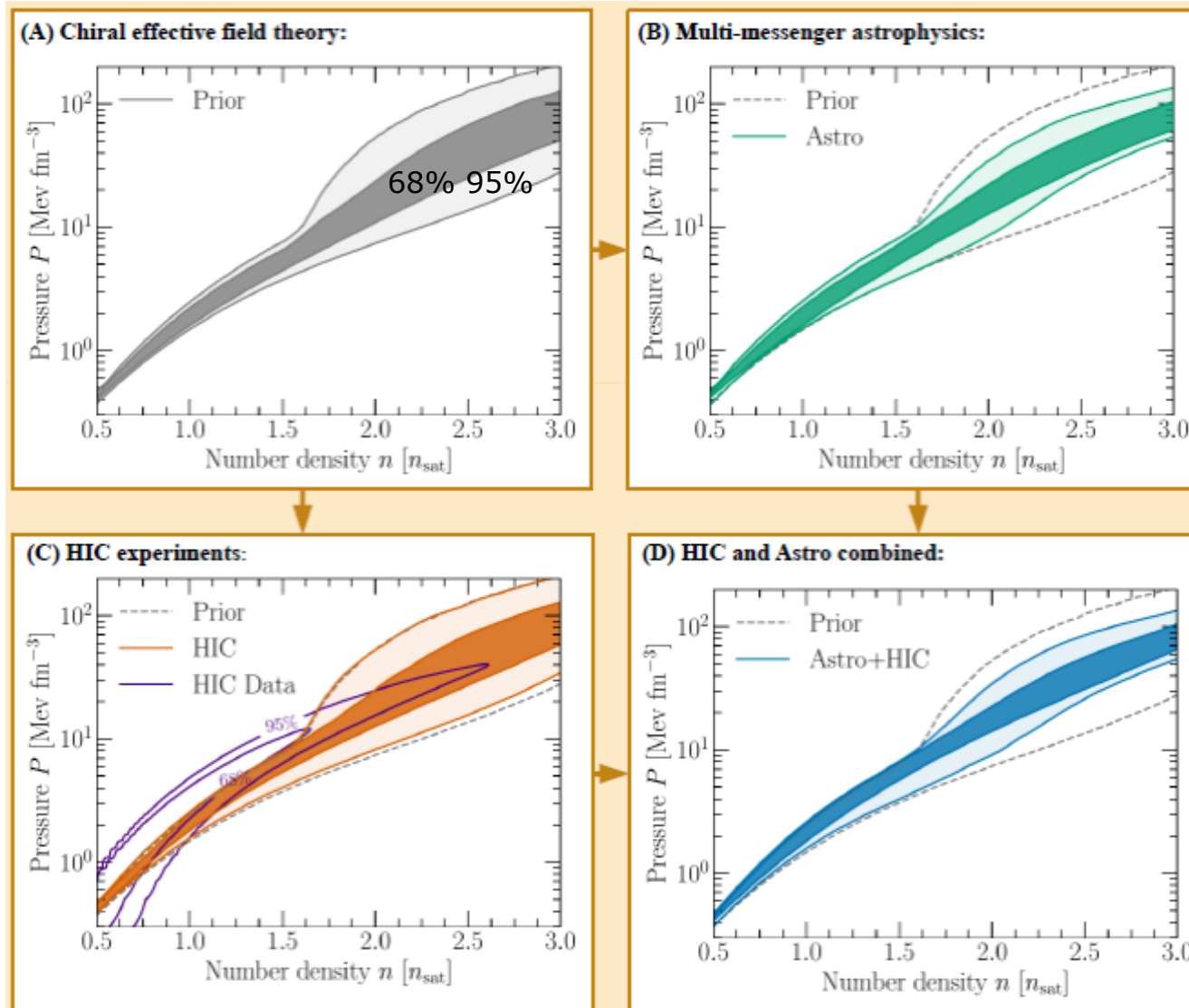
Sabrina Huth^{1,2,13}✉, Peter T. H. Pang^{3,4,13}✉, Ingo Tews⁵, Tim Dietrich^{6,7}, Arnaud Le Fèvre⁸, Achim Schwenk^{1,2,9}, Wolfgang Trautmann⁸, Kshitij Agarwal¹⁰, Mattia Bulla¹¹, Michael W. Coughlin¹² & Chris Van Den Broeck^{3,4}

Interpreting high-energy, astrophysical phenomena, such as supernova explosions or neutron-star collisions, requires a robust understanding of matter at supranuclear densities. However, our knowledge about dense matter explored in the cores of neutron stars remains limited. Fortunately, dense matter is not probed only in

11 authors from nuclear theory, heavy ion reactions, and astrophysics

iments.
messenger

Bayesian inference as in Dietrich+, Science 370, 1450 (2020)



2022 Huth+ Nature
Fig. 1

neutron star matter

contours at
68% and 95%
credibility

prior:

χ EFT up to $1.5 \rho_0$

$M_{\text{max}} \geq 1.9 M_{\text{sun}}$

astro:

GW170817

+kilonova

GW190425

NICER 2 stars

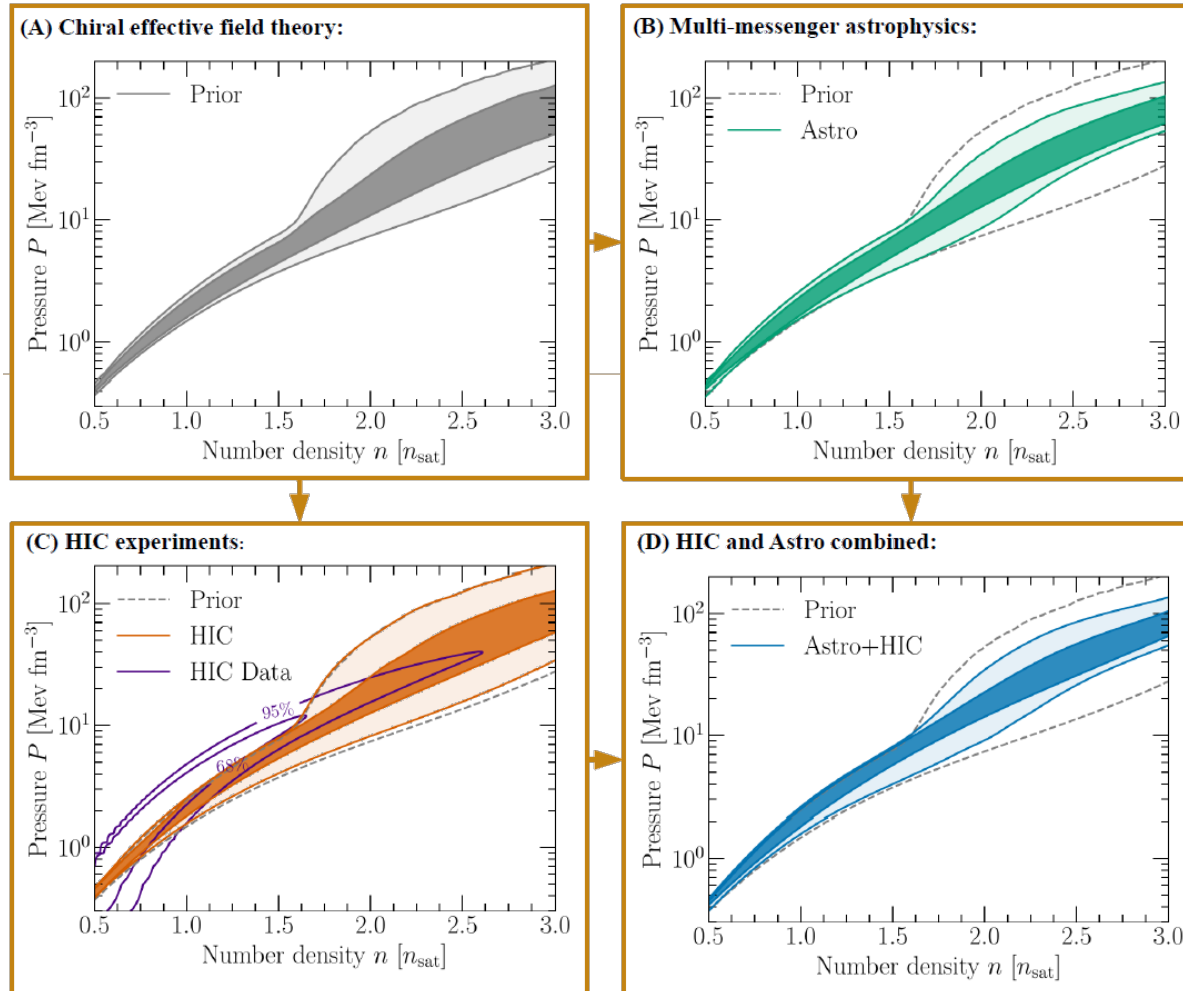
XMM-Newton

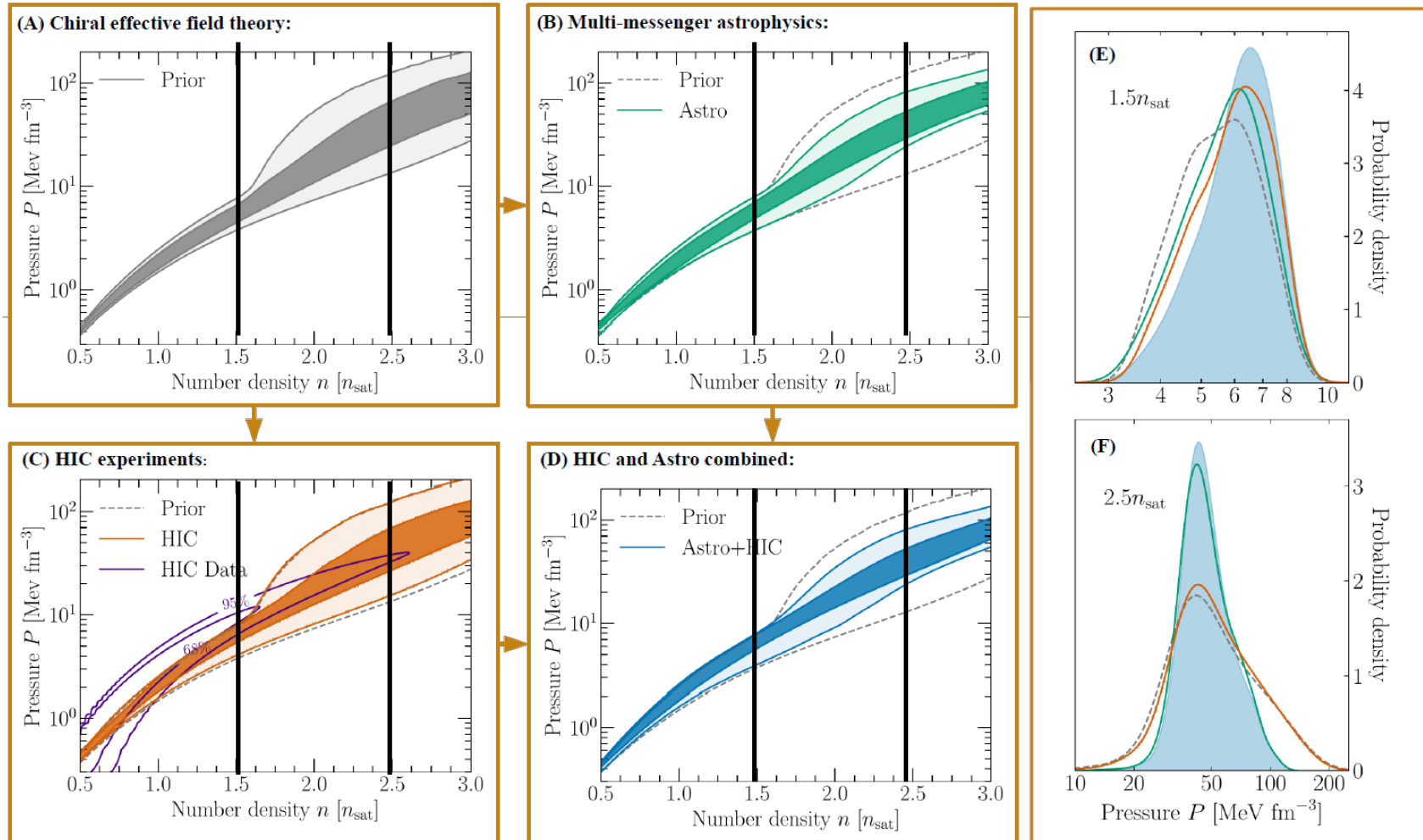
$M_{\text{max}} \leq 2.17 M_{\text{sun}}$

HIC:

PNM: ASY-EOS

SNM: FOPI, AGS





nature astronomy

Article

<https://doi.org/10.1038/s41550-023-02161-z>

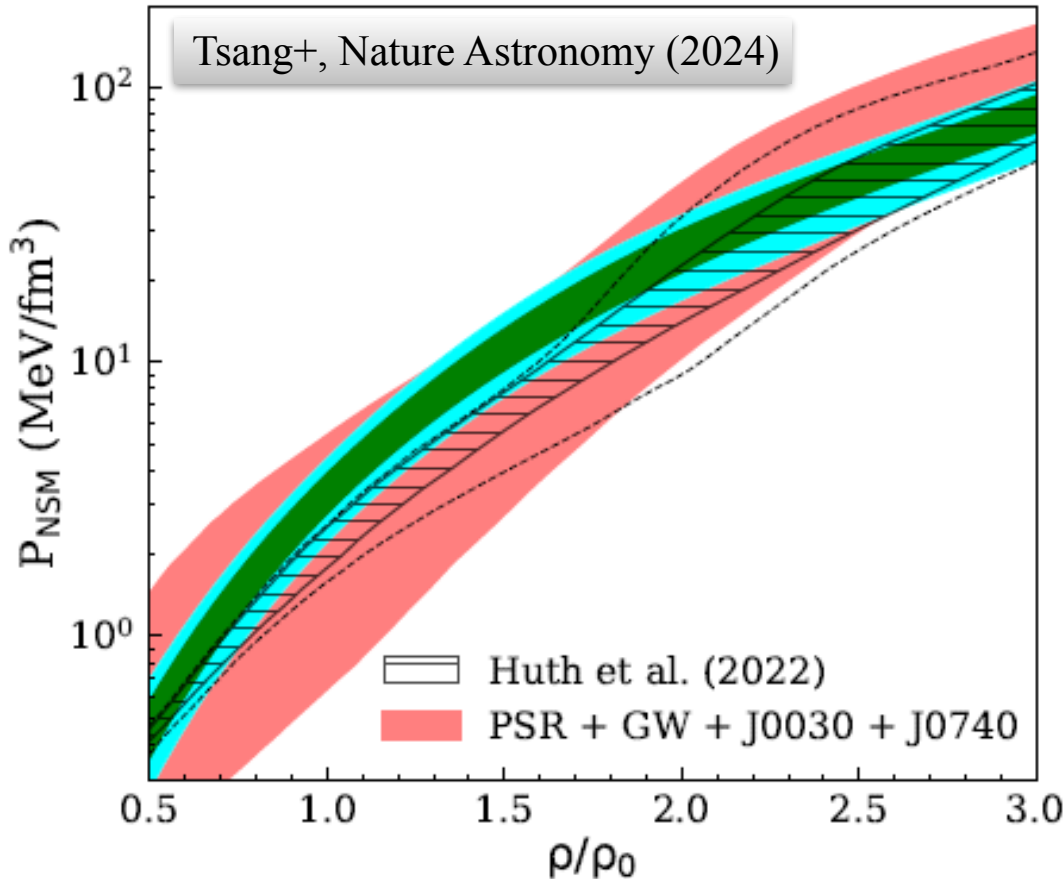
Determination of the equation of state from nuclear experiments and neutron star observations

Received: 22 February 2023

Accepted: 6 November 2023

Published online: 05 January 2024

Chun Yuen Tsang^{1,2}, ManYee Betty Tsang ^{1,2} , William G. Lynch^{1,2}, Rohit Kumar¹ & Charles J. Horowitz ^{1,3}



Legred et al., Phys. Rev. D 104, 063003 (2021)

- Non-parametric equation of states as priors.
- Astrophysical observations are used as constraints

Huth, Pang et al., Nature 606, 279 (2022)

- Prior distribution from the Chiral Effective Field theory (up to $1.5n_0$); constant speed of sound model $>1.5n_0$.
- Include HIC(FOURPI) & astrophysical observations as constraints

χ EFT seems to generate a **bias** as a prior, forcing artificially the posterior EoS to be **too soft** in the $0.5 - 1.5\rho_0$ density range

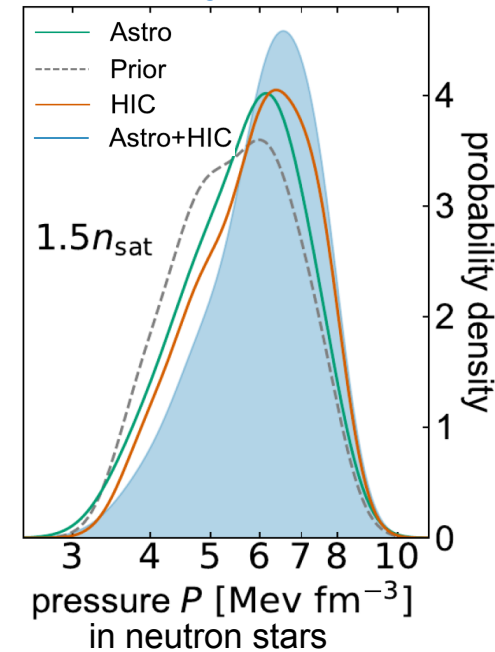
R3B - ASY-EOS II experiment (Cave C, March 2025)



Supported by European Union's Horizon Europe and Horizon 2020 Research and Innovation programmes under Grant Agreements no. 101057511 (EURO-LABS) and no. 824093 (STRONG2020)

● **Goal:** measure the **symmetry energy** of nuclear matter at **high density** ($\gg \rho_0$, world record with HIC) and with **high precision**, to constrain **neutron star properties** (maximum mass, radius, pressure versus density relation)

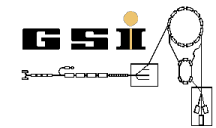
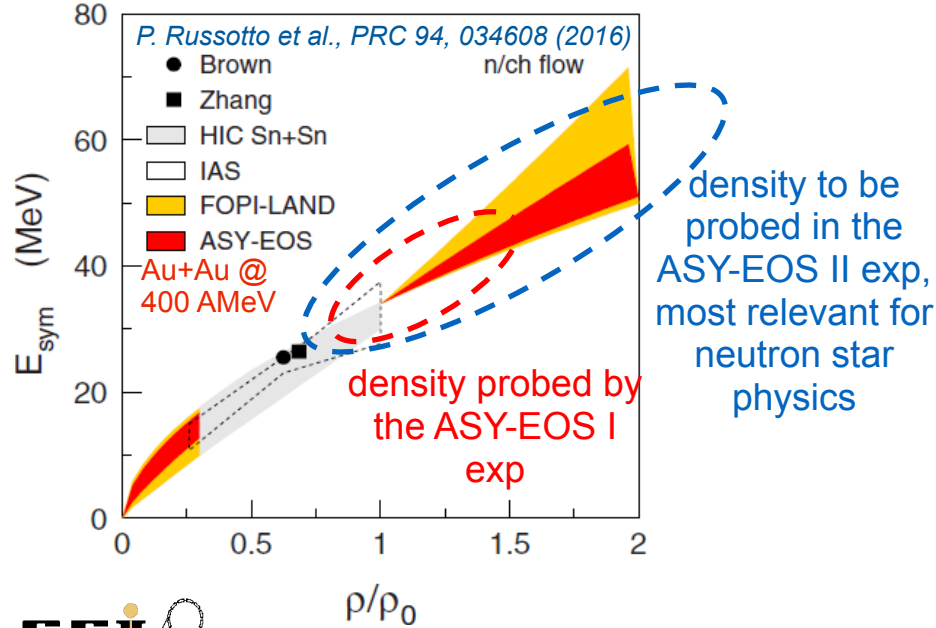
● **Method:** comparison of the strength of the **out-of-plane emission** (« elliptic flow ») of **protons** and **neutrons** in **heavy- and neutron-rich-ion collisions** at relativistic incident energies



Huth, Pang et al., *Nature* 606 (2022)

● March 2025 measurements at GSI Darmstadt:

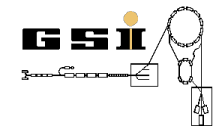
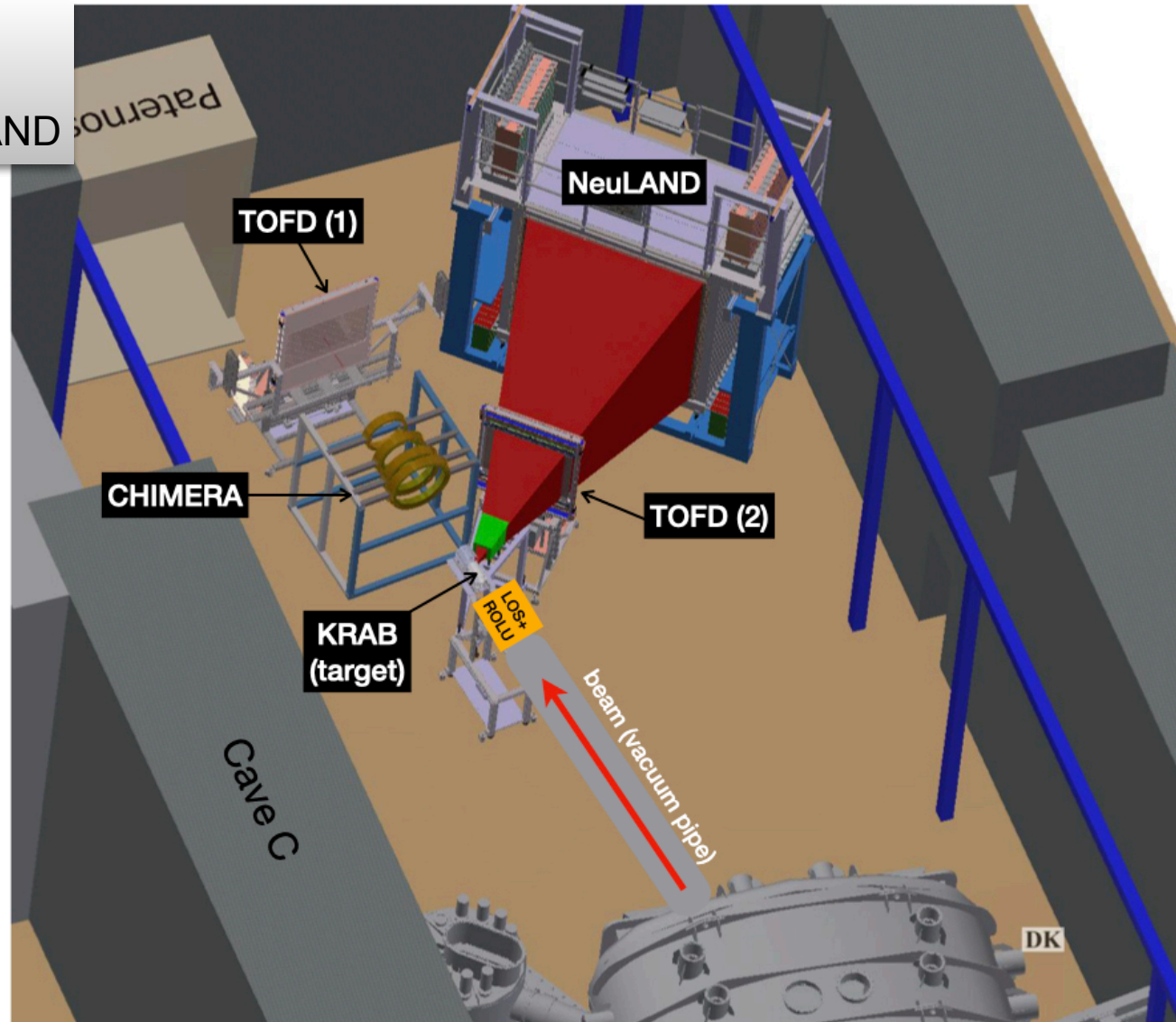
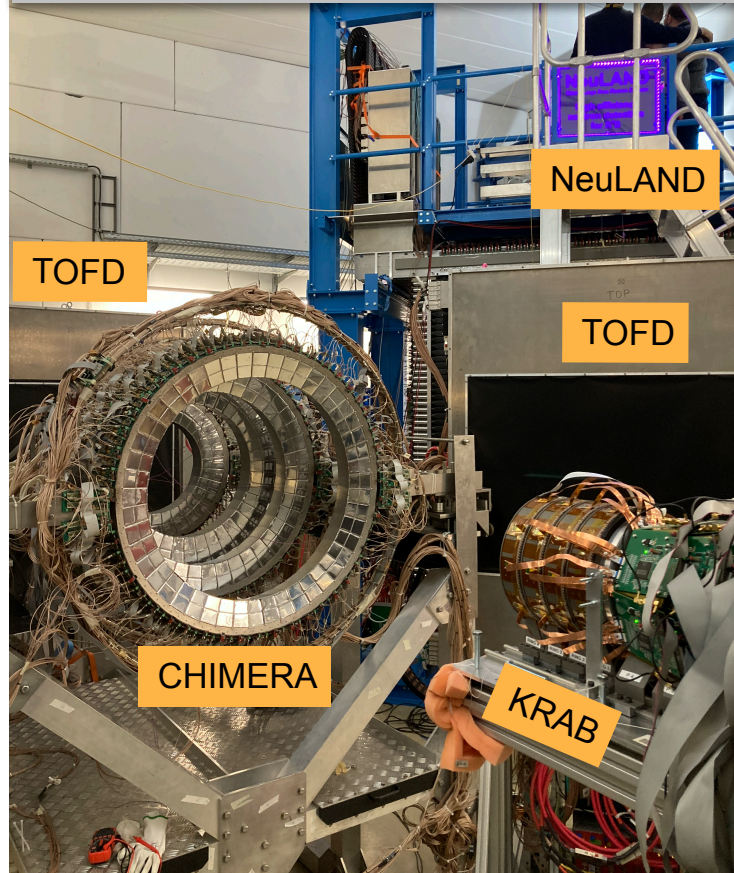
- Au+Au @ 280, 400, 600, 1000A MeV.
- 10^5 pps, high multiplicity (>80)
- precise reaction plane determination
- large neutron and proton acceptance
- optimised (macro & micro-) spill structure allowed about 30% more statistics.
- large statistics (about 100M clean events)



R3B - ASY-EOS II experiment (Cave C, March 2025)



Reaction plane: KRAB, CHIMERA
Impact parameter: TOFD
Neutron/proton flow: TOFD+NeuLAND



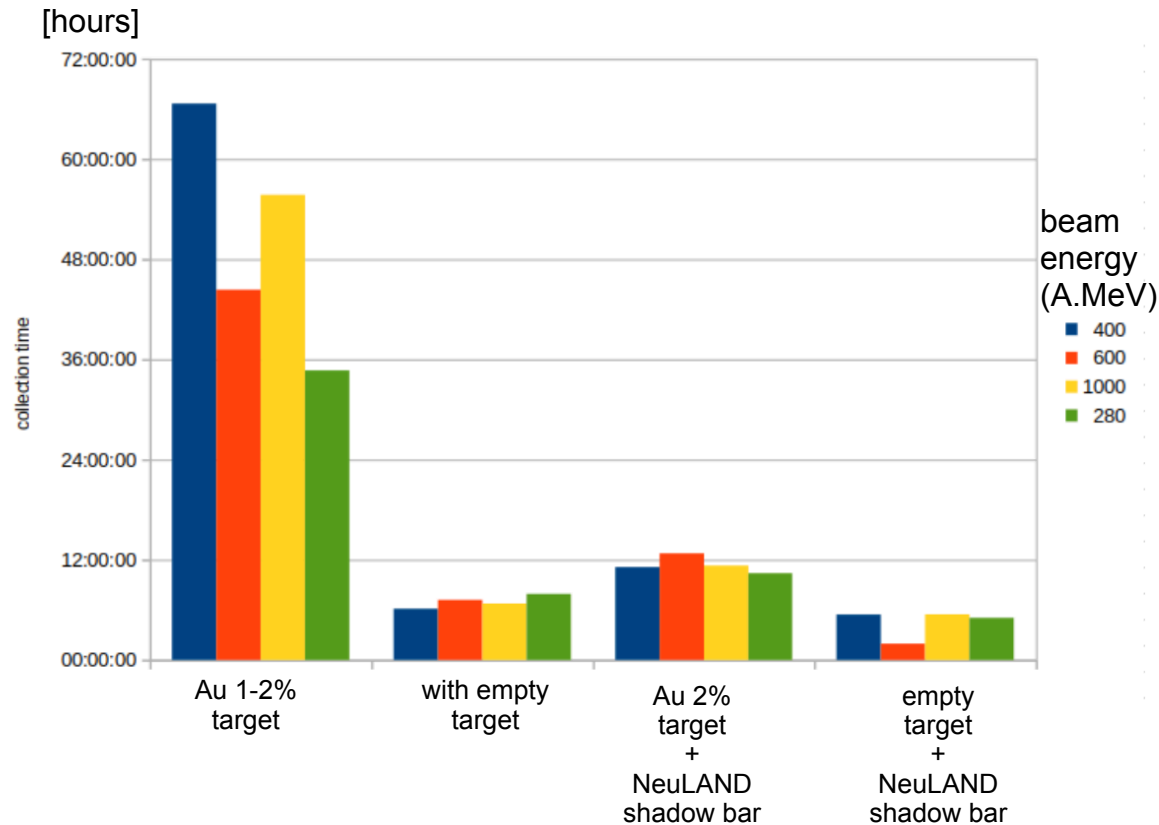
R3B - ASY-EOS II experiment (Cave C, March 2025)



Statistics

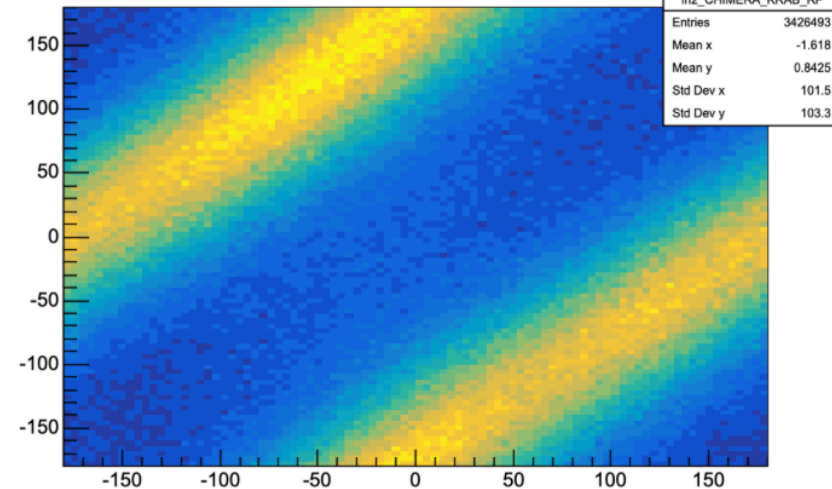
Reaction plane accuracy:
CHIMERA - KRAB correlations

collection times for different runs and energies



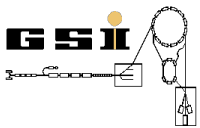
in CHIMERA

CHIMERA_KRAB_RP



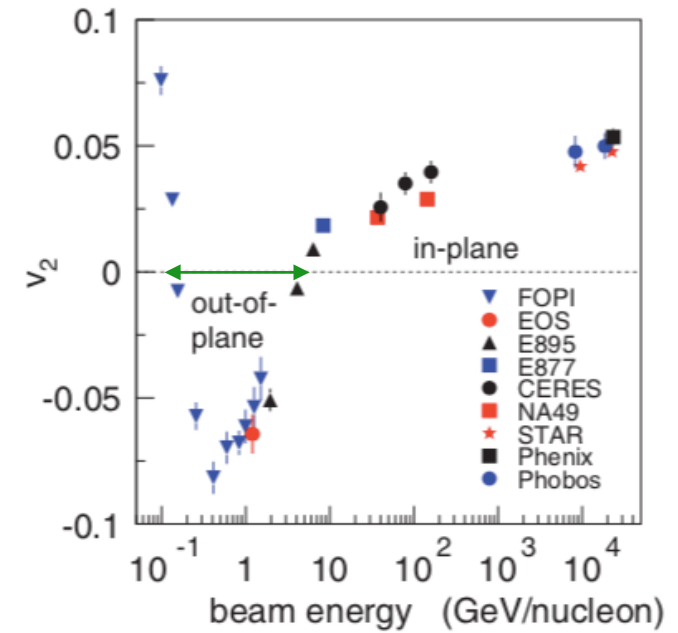
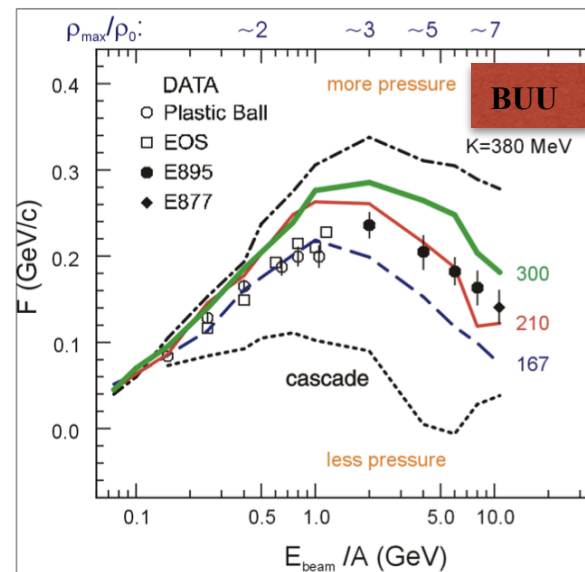
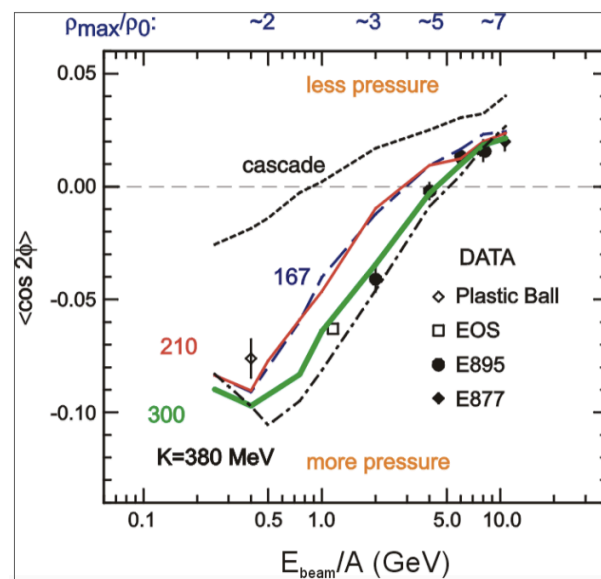
in KRAB

Reaction plane azimuthal angle (°)
anti-correlation between KRAB and
CHIMERA for **reactions in the target**
(**yellow bands**); **else**: mostly reactions in
air (**blue background**)
=> good signal/noise ratio.



Symmetric nuclear matter EoS

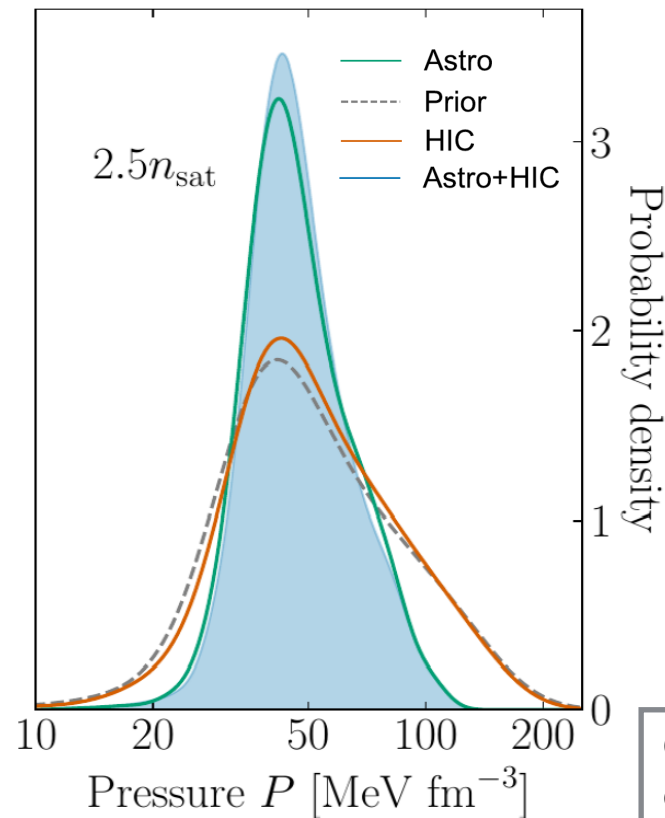
- Constrained so far up to about $3\rho_0$ at GSI
- Above $3\rho_0$, AGS data have presumably constrained it up to around $3-7\rho_0$
- ... using the proton **directed flow** (F or v_1). But inconsistencies with experimental proton **elliptic flow** data comparing with FOPI data (up to 1.5A GeV)
- => **should be remeasured at FAIR and re-analysed with other transport models.**
- Above 1A GeV, elliptic flow still sensitive on K_0 , up to around 3A GeV. **Directed flow is more constraining at higher incident energies.**



Pawel Danielewicz, *et al.* *Science* **298**, 1592 (2002); DOI: 10.1126/science.1078070

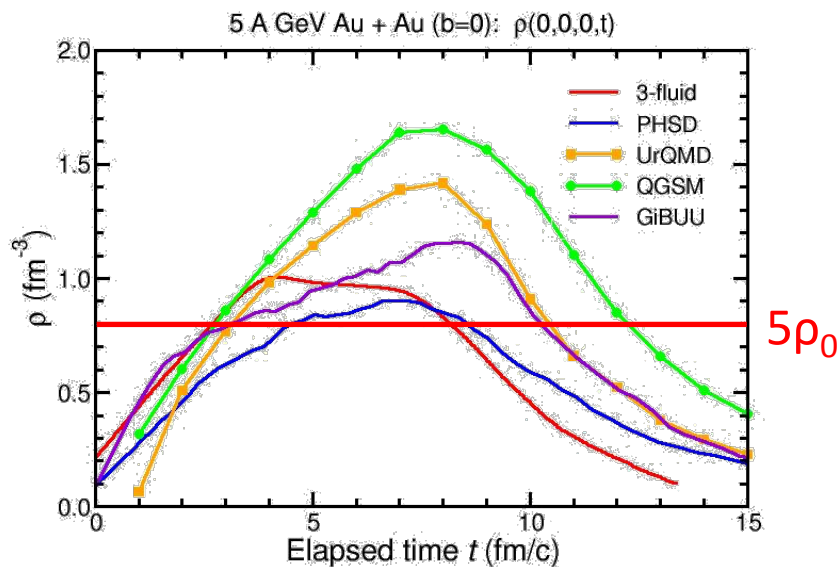
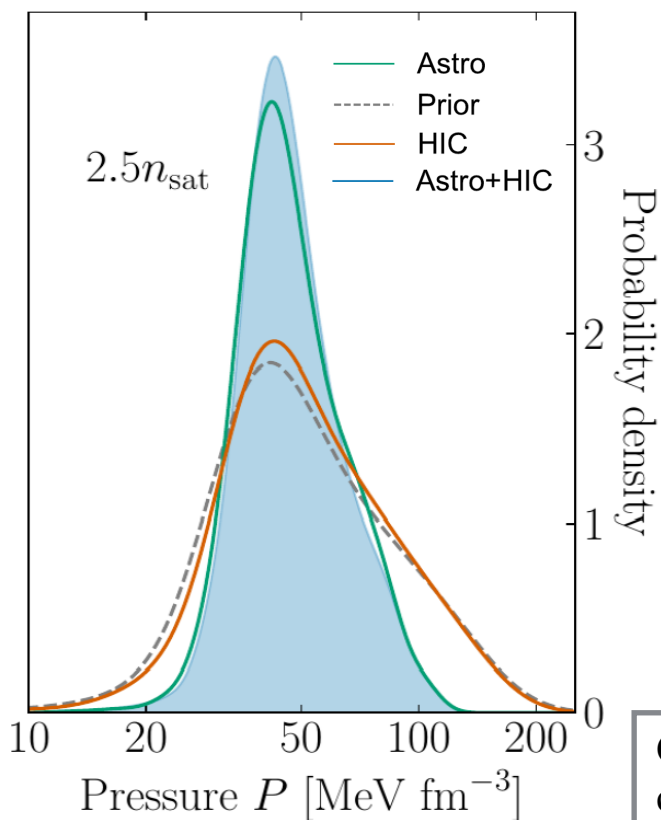
A. Le Fèvre *et al.*, *Phys. Rev. C* **98**, 034901 (2018)

Present situation: Above $\approx 2\rho_0$, the posterior distribution of the pressure in a neutron star is primarily driven by astronomical observations.
Reason: reliable HIC data (symmetry energy) not yet available at higher densities.



Challenge: which HIC observables will be able to constrain the symmetry energy at higher densities?
Cf. Dan Cozma's talk.

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Reason: reliable HIC data (symmetry energy) not yet available at higher densities.



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J. Randrup & J. Cleymans, PRC 74 (2006) 047901
I.C. Arsene et al., PRC 75 (2007) 034902
Friman et al., The CBM Physics Book, Springer (2010)

A common HIC EoS with well-defined errors consistent with all transport codes



Progress in Particle and Nuclear Physics

Volume 134, January 2024, 104080



Review

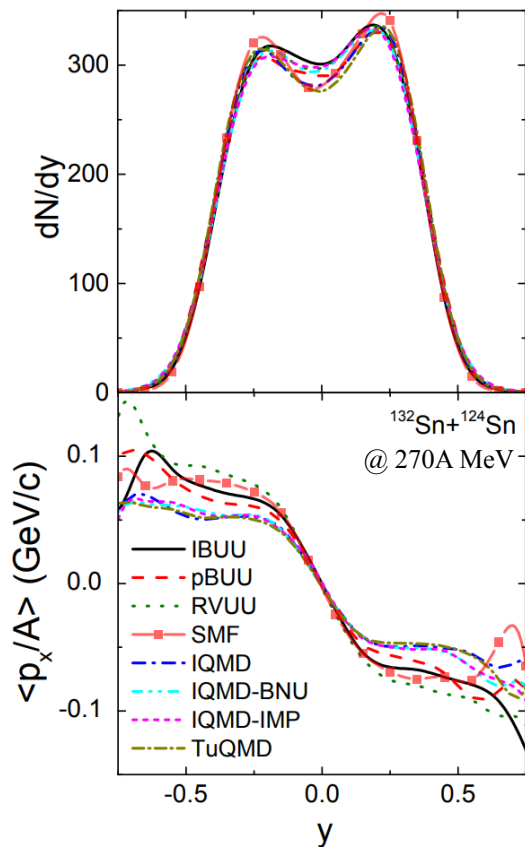
Dense nuclear matter equation of state from heavy-ion collisions

Agnieszka Sorensen¹ , Kshitij Agarwal², Kyle W. Brown^{3,4}, Zbigniew Chajęcki⁵, Paweł Danielewicz^{3,6}, Christian Drischler⁷, Stefano Gandolfi⁸, Jeremy W. Holt^{9,10}, Matthias Kaminski¹¹, Che-Ming Ko^{9,10}, Rohit Kumar³, Bao-An Li¹², William G. Lynch^{3,6}, Alan B. McIntosh¹⁰, William G. Newton¹², Scott Pratt^{3,6}, Oleh Savchuk^{3,13}, Maria Stefania^{14,15}, Ingo Tews⁸, ManYee Betty Tsang^{3,6}, Ramona Vogt^{16,17}, Hermann Wolter¹⁸, Hanna Zbroszczyk¹⁹, Navid Abbasi²⁰, Jörg Aichelin^{21,22}, Anton Andronic²³, Steffen A. Bass²⁴, Francesco Becattini^{25,26}, David Blaschke^{27,28,29}, Marcus Bleicher^{30,31}, Christoph Blume³², Elena Bratkovskaya^{15,30,31}, B. Alex Brown^{3,6}, David A. Brown³³, Alberto Camaiani^{25,26}, Giovanni Casini²⁶, Katerina Chatziioannou^{34,35}, Abdelouahad Chbihi³⁶, Maria Colonna³⁷, Mircea Dan Cozma³⁸, Veronica Dexheimer³⁹, Xin Dong⁴⁰, Travis Dore⁴¹, Lipei Du⁴², José A. Dueñas⁴³, Hannah Elfner^{15,30,22,31}, Wojciech Florkowski⁴⁴, Yuki Fujimoto¹, Richard J. Furnstahl¹⁴, Alexandra Gade^{3,6}, Tetyana Galatyuk^{15,45}, Charles Gale⁴², Frank Geurts⁴⁶, Fabiana Gramegna⁶⁸, Sašo Grozdanov^{47,48}, Kris Hagel¹⁰, Steven P. Harris¹, Wick Haxton^{49,40}, Ulrich Heinz¹⁴, Michal P. Heller⁵⁰, Or Hen⁵¹, Heiko Hergert^{3,6}, Norbert Herrmann⁵², Huan Zhong Huang⁵³, Xu-Guang Huang^{54,55,56}, Natsumi Ikeno^{57,10}, Gabriele Inghirami¹⁵, Jakub Jankowski²⁷, Jiangyong Jia^{58,59}, José C. Jiménez⁶⁰, Joseph Kapusta⁶¹, Behruz Kardan³², Iurii Karpenko⁶², Declan Keane³⁹, Dmitri Kharzeev^{63,59}, Andrej Kugler⁶⁴, Arnaud Le Fèvre¹⁵, Dean Lee^{3,6}, Hong Liu⁶⁵, Michael A. Lisa¹⁴, William J. Llope⁶⁶, Ivano Lombardo⁶⁷, Manuel Lorenz³², Tommaso Marchi⁶⁸, Larry McLerran¹, Ulrich Mosel^{69,70}, Anton Motornenko²², Berndt Müller²⁴, Paolo Napolitani⁷¹, Joseph B. Natowitz¹⁰, Witold Nazarewicz^{3,6}, Jorge Noronha⁷², Jacquelyn Noronha-Hostler⁷², Grażyna Odyniec⁴⁰, Panagioti Papakonstantinou⁷³, Zuzana Paulinyová⁷⁴, Jorge Piekarewicz⁷⁵, Robert D. Pisarski⁵⁹, Christopher Plumberg⁷⁶, Madappa Prakash⁷, Jørgen Randrup⁴⁰, Claudia Ratti⁷⁷, Peter Rau¹, Sanjay Reddy¹, Hans-Rudolf Schmidt^{2,15}, Paolo Russotto³⁷, Radosław Ryblewski⁷⁸, Andreas Schäfer⁷⁹, Björn Schenke⁵⁹, Srimoyee Sen⁸⁰, Peter Senger⁸¹, Richard Seto⁸², Chun Shen^{66,83}, Bradley Sherrill^{3,6}, Mayank Singh⁶¹, Vladimir Skokov^{84,83}, Michał Spaliński^{85,86}, Jan Steinheimer²², Mikhail Stephanov⁸⁷, Joachim Stroth^{32,15}, Christian Sturm¹⁵, Kai-Jia Sun⁸⁸, Aihong Tang⁵⁹, Giorgio Torrieri^{89,90}, Wolfgang Trautmann¹⁵, Giuseppe Verde⁹¹, Volodymyr Vovchenko⁷⁷, Ryoichi Wada¹⁰, Fuqiang Wang⁹², Gang Wang⁵³, Klaus Werner²¹, Nu Xu⁴⁰, Zhangbu Xu⁵⁹, Ho-Ung Yee⁸⁷, Sherry Yennello^{10,9,93}, Yi Yin⁹⁴

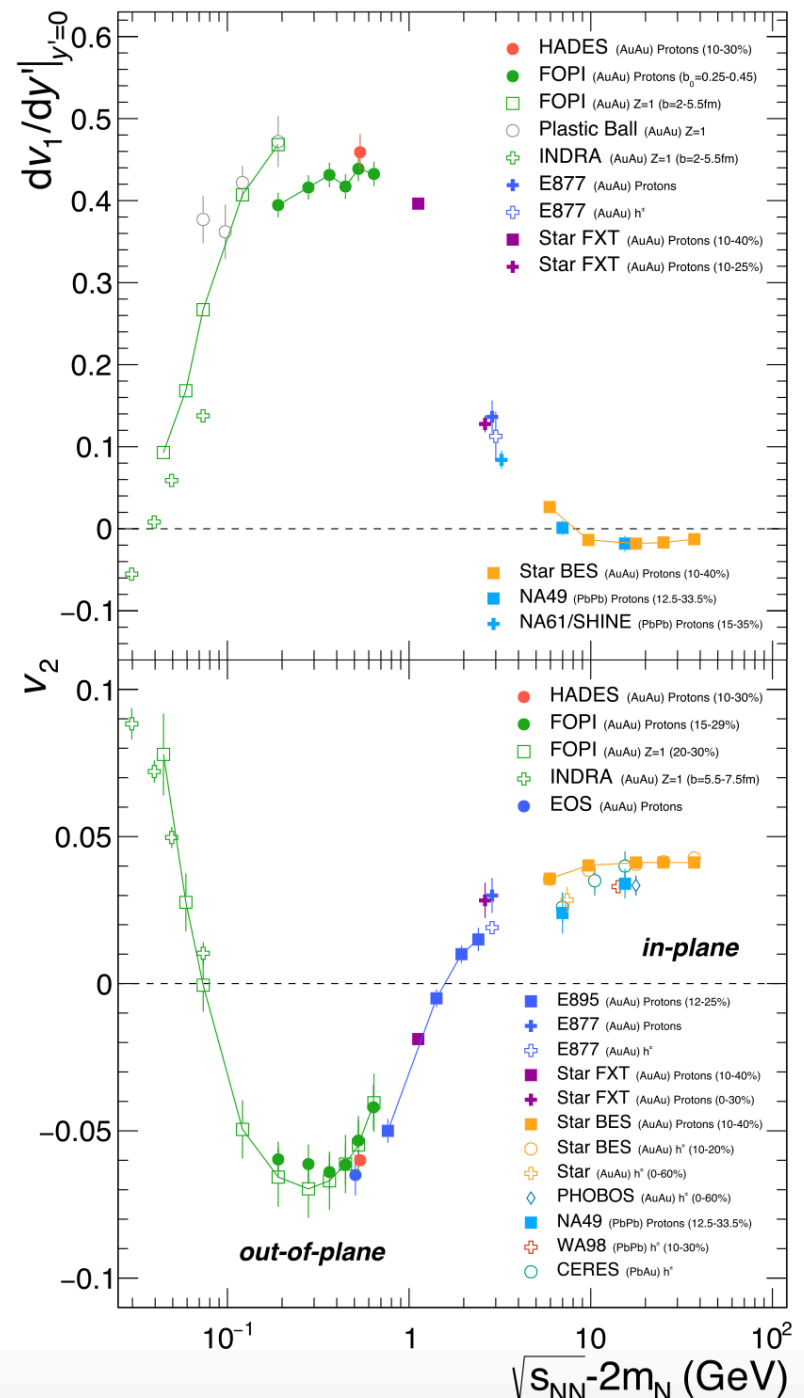


Perspectives: transport mod

A common HIC EoS with well-defined errors consistent with all transport codes



In line with the international Transport Model Evaluation Project (TMEP)



A promising multi-messenger era for the next 15+ years...

K. Agarwal

2022 2023 2024 2025 2026 2027 2028 2029 2030 2031 2032 2033 2034 2035 2036 2037

Heavy-Ion
Collisions

STAR-FXT@RHIC ^[1]

HADES@SIS-18 ^[2]

ASY-EOS-II@SIS-18 ^[3]

MPD@NICA* ^[4]

CBM(HADES)@SIS-100 ^[5]

GW
Observations

LIGO (O4, O5) ^[6]

Einstein Telescope ^[7]

LISA ^[8]

X-Ray
Observations

NICER (Cycles 5, 6) ^[9]

eXTP ^[10]

STROBE-X ^[11]

ATHENA ^[12]

[1] D. Morrison, Quark Matter 2022 | [Link](#)

[2] Proposal for Beamtime in 2023-24, GSI G-PAC (2022)

[3] Proposal for Beamtime in 2023-24, GSI G-PAC (2022)

[4] I. Maldonado, A. Ayala, EuNPC 2022 | [Link](#)

[5] First-Science and Staging Review of the FAIR Project (2022) |

[Link](#)

[6] LIGO-Virgo-KAGRA Observing Run Plan | [Link](#)

[7] Einstein Telescope Homepage | [Link](#)

[8] LISA ESA Factsheet | [Link](#)

[9] NICER Proposals Guide – Cycle 5 | [Link](#)

[10] eXTP Homepage | [Link](#)

[11] STROBE-X White Paper for the Astro 2020 Decadal Survey | [Link](#)

[12] ATHENA ESA Factsheet | [Link](#)





















