



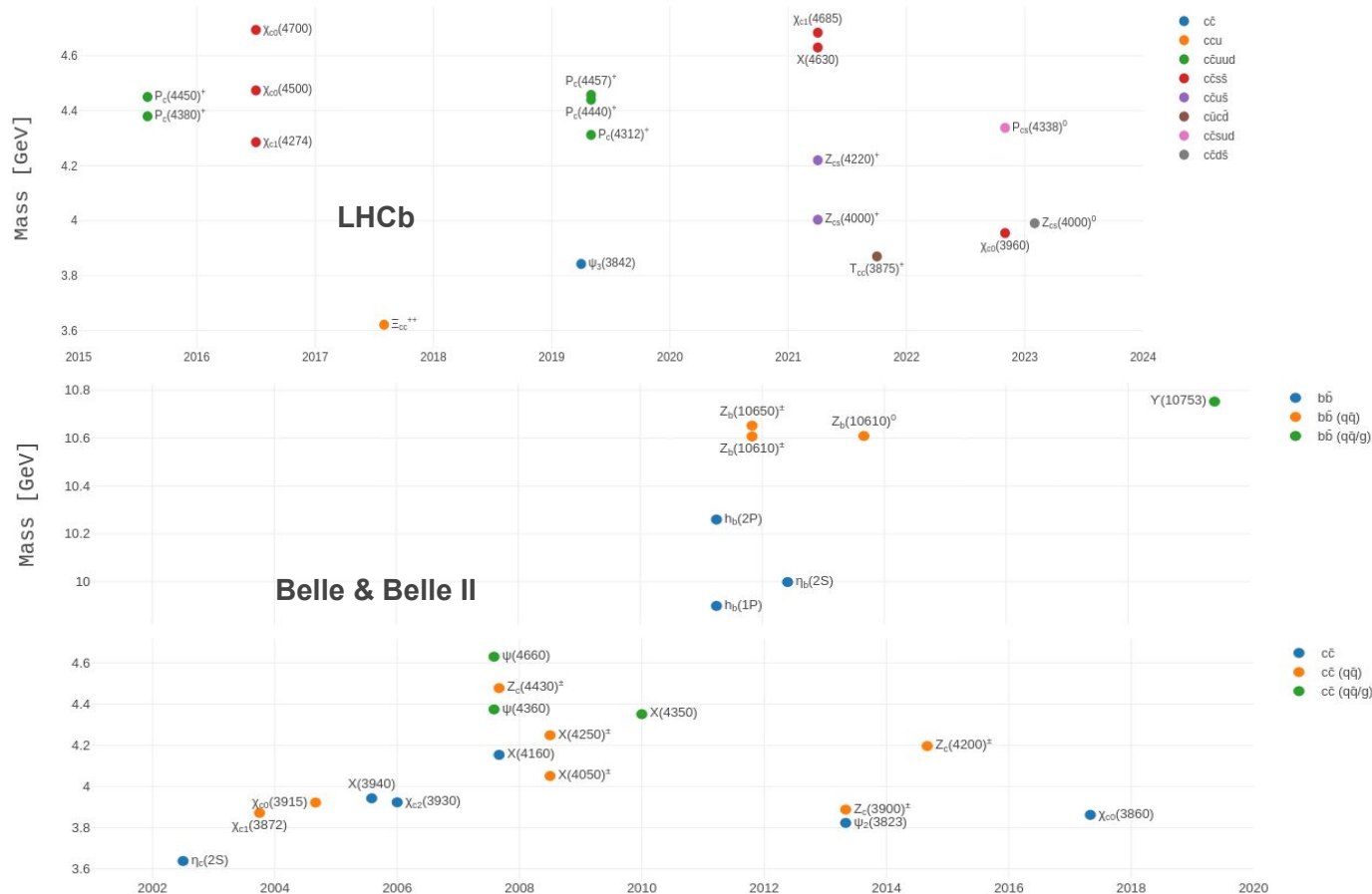
Aci Castello,
22–27 June 2025

Hadron spectroscopy at B factories

A. Boschetti



The rebirth of hadron spectroscopy



18



+



22

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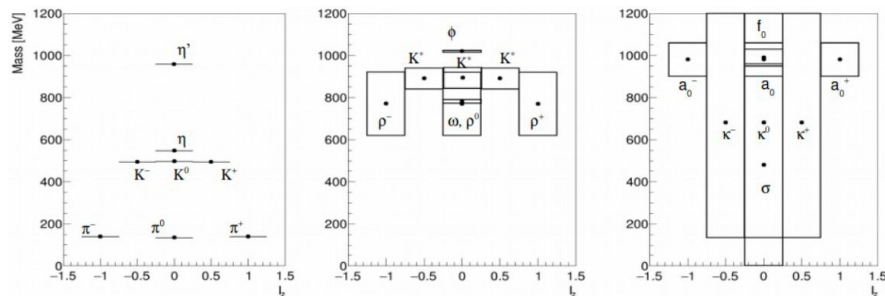


40 new states!

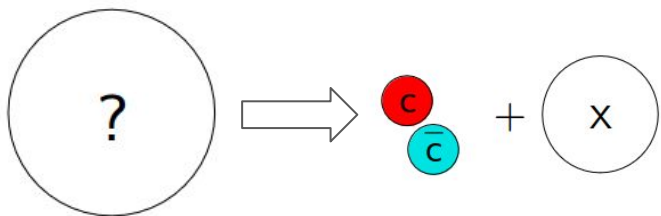
Why heavy quarkonia?

Multi-quark systems are possible at any energy [Jaffe, Wilczek, PRL 91 232003 (2003)]

However, experimentally challenging to distinguish $q\bar{q}$ from $q\bar{q}q\bar{q}$ in light sector



With heavy quarks separating conventionals and exotics is much simpler, *e.g.*



- Mass $> 3 \text{ GeV}/c^2$
- Small width ($\Gamma/M < 0.1$)
- Large BF for J/ψ (or $D\bar{D}$) + X decay

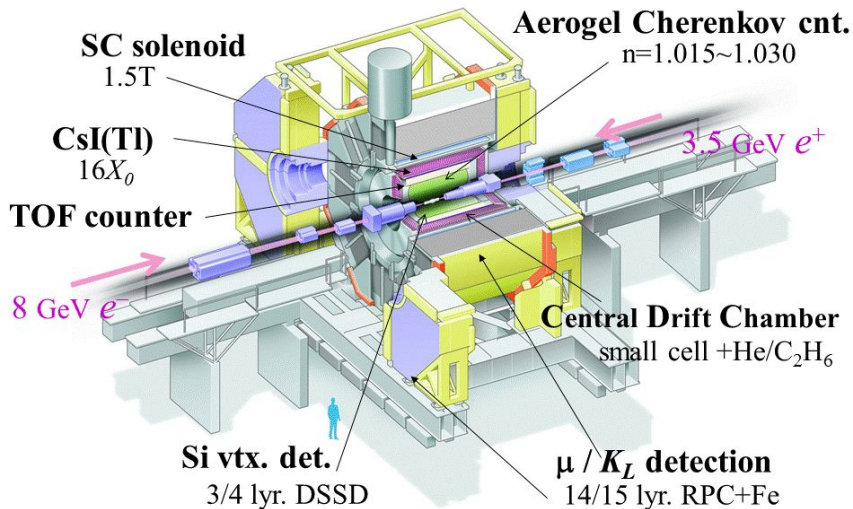
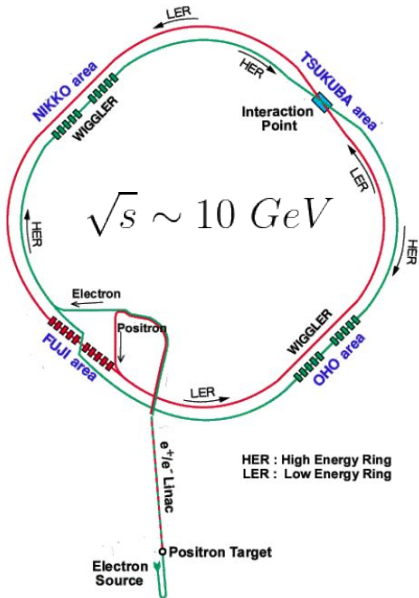
\Rightarrow Must contain $c\bar{c}$ pair

Belle at KEKB

B-factory \Rightarrow optimized for $\Upsilon(4S)$ production

Quarkonium spectroscopy

\Rightarrow **Tunable beam energy:** from $\Upsilon(1S)$ to $\Upsilon(6S)$

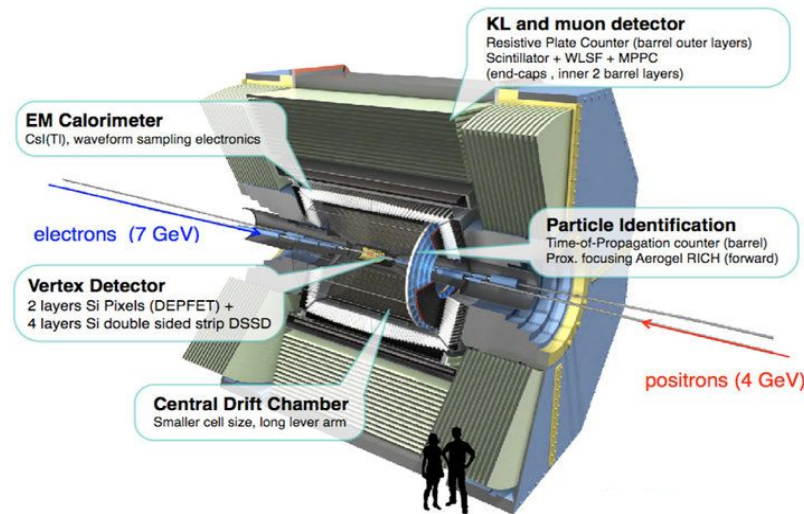
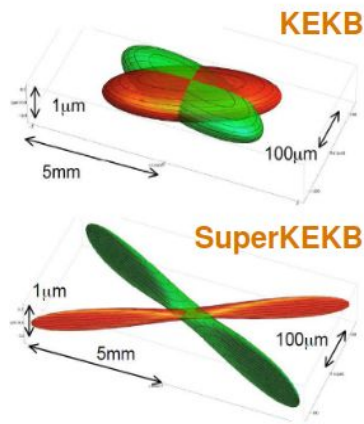
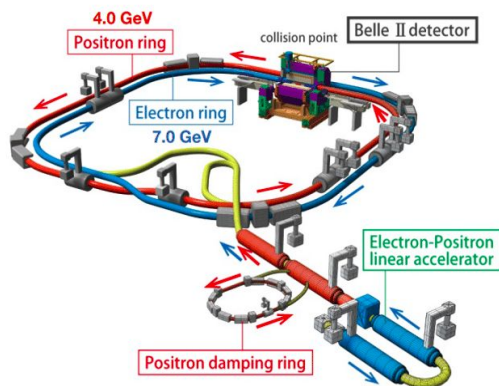


Belle II at SuperKEKB

Improved tracking and PID performance

Implementation of the nano-beam scheme for collisions

⇒ projected luminosity ~ 30xBelle



The LHCb detector

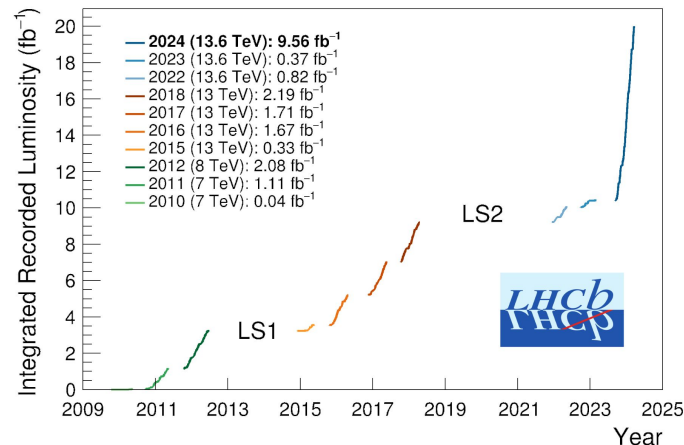
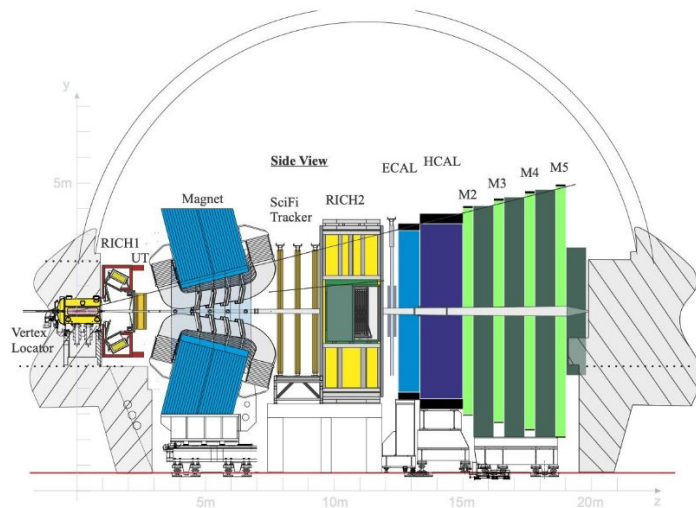
Single arm spectrometer (forward)

15 to 300 mrad coverage

Larger cross sections, higher boost, more b hadrons

Large background:

- worse flavor tagging
- difficulties with missing/neutral particles



- Vertex reconstruction:
 - $\Delta P = (15 + 29/p_T) \mu\text{m}$
- Momentum resolution:
 - $\Delta p/p = \sim 0.5\text{--}1\%$ (from 2 to 200 GeV)
- Hadronic PID:
 - $\epsilon_{K \rightarrow K} \sim 95\%$,
 - $\epsilon_{K \rightarrow \pi} \sim 10\%$ (from 2 to 200 GeV)
- Muon trigger efficiency:
 - $\epsilon > 90\%$

The doubly charmed tetraquark T_{cc}

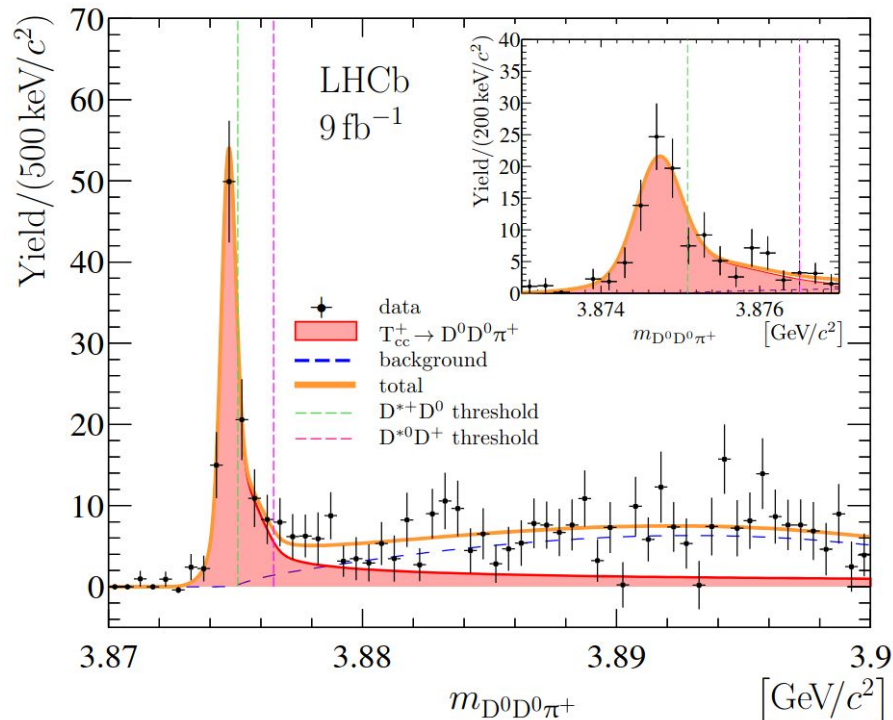
- Observation of narrow state in $M(D^0 D^0 \pi^+)$ near $D^0 D^{*+}$ threshold
- Minimal quark content $[cc\bar{u}\bar{d}]$
- $J^P = 1^+$

Unitarised model, signal \sim Flatté

- $\delta m_{\text{pole}} = -360 \pm 40_{-0}^{+4} \text{ keV}/c^2$
- $\Gamma_{\text{pole}} = 48 \pm 2_{-14}^{+0} \text{ keV}$
- Excellent description of $M(D^0 \pi^+)$
- Absence of signal in $M(D^0 D^0)$ and $M(D^+ D^0 \pi^+)$

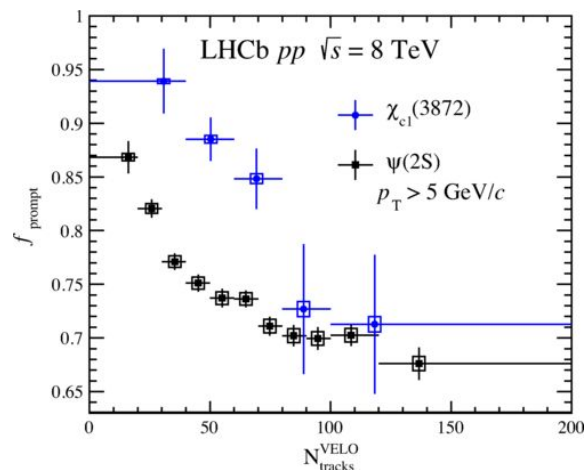
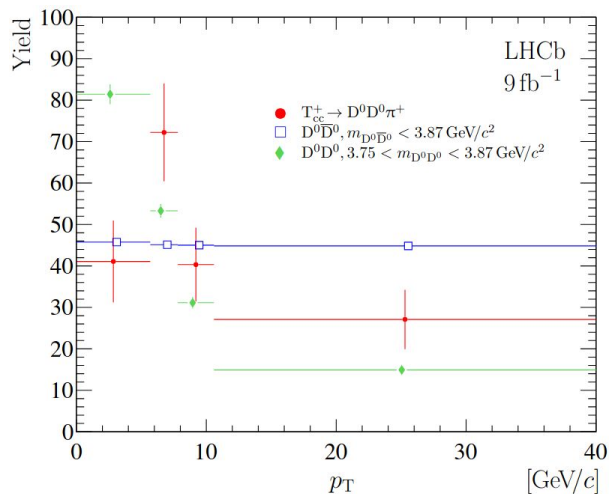
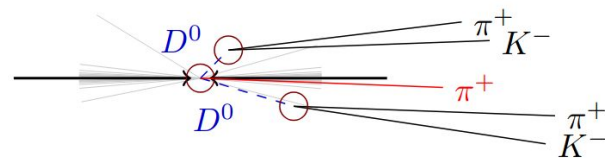
$\Rightarrow T_{cc}$ consistent with isoscalar tetraquark

[Nat Commun 13, 3351 \(2022\)](#)



Prompt production

The analysis shows **large prompt production** at high p_T

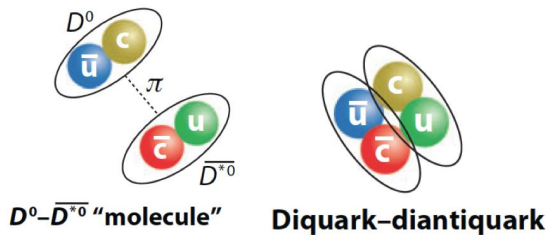


Same property is shared by $\chi_{c1}(3872)$

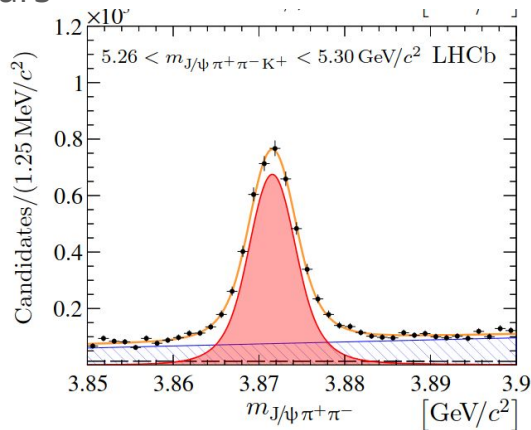
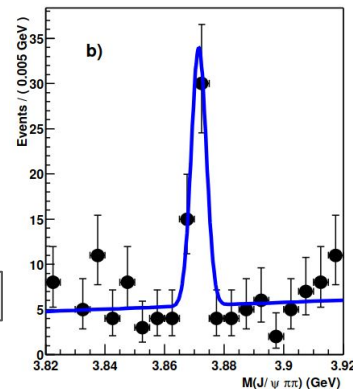
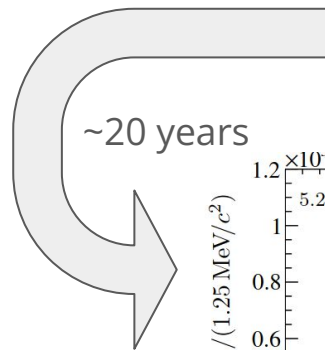
[Phys. Rev. Lett. 126, 092001](#)

Large prompt production at high p_T disfavors molecular interpretation

The $\chi_{c1}(3872)$ state



- $m(\chi_{c1}(3872)) - (m(D^0) + m(\bar{D}^{*0})) = -0.07 \pm 0.12 \text{ MeV}$
- $J^{PC} = 1^{++}$
- **Production:**
 - B decays
 - prompt pp, $p\bar{p}$, pPb, PbPb !
 - $e^+e^- \rightarrow \gamma\chi_{c1}(3872), \omega\chi_{c1}(3872)$
- **Decay:**
 - $J/\psi\pi\pi, J/\psi\omega, D\bar{D}^*, \dots$



Proximity to threshold, dominant decay modes, $J^{PC} = 1^{++}$
 \Rightarrow molecular picture is favored

Suppression of $\chi_{c1}(3872)$: compact state?

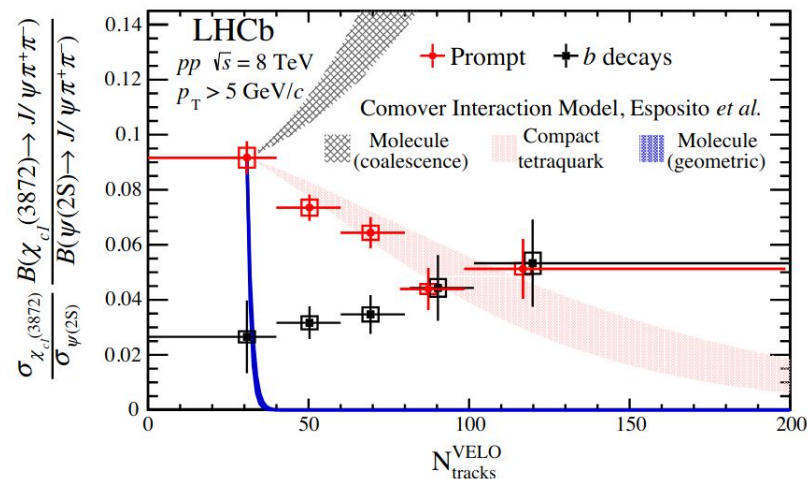
Study behaviour of states immersed in QCD matter \Rightarrow estimate the spatial size

Comover Interaction Model (CIM)

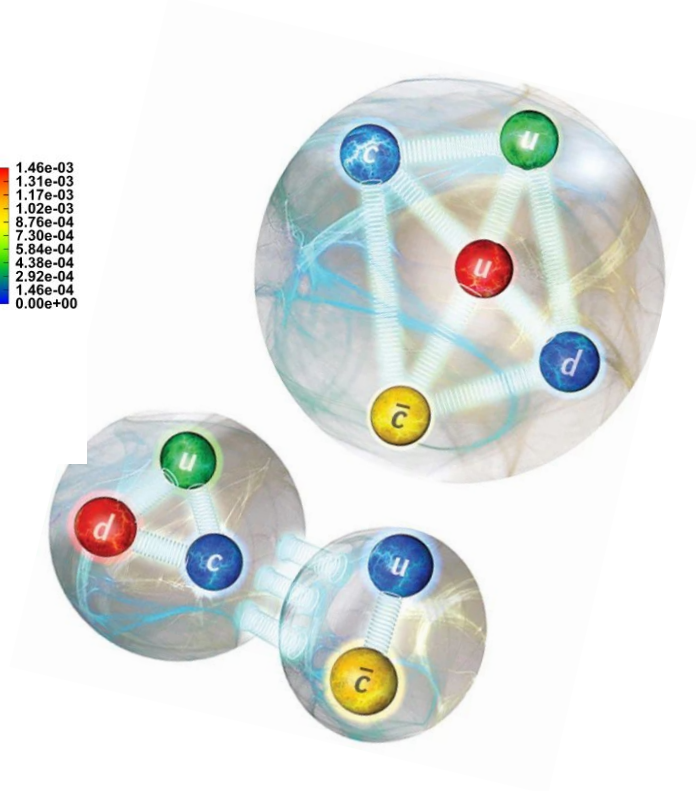
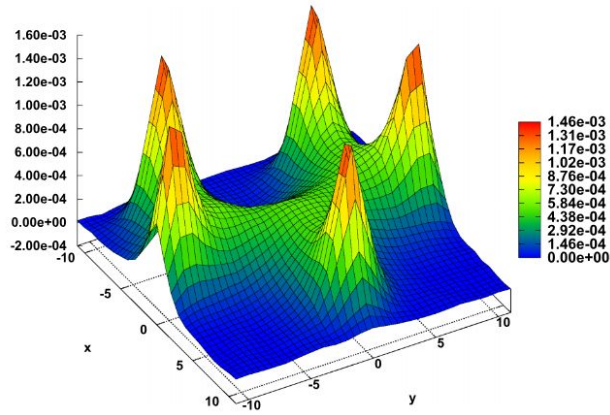
[Eur. Phys. J. C 81, 669 \(2021\)](#)

- Quarkonia broken by collision with comovers in nuclear medium
 - Breakup cross section depends on radius and binding energy
- Pure molecule:
 - large radius \Rightarrow quick dissociation
 - reformation by coalescence $\Rightarrow \sigma_{\chi_{c1}(3872)} / \sigma_{\psi(2S)}$ rises with multiplicity
- Compact state:
 - radius of $\chi_{c1}(3872)$ slightly larger than ψ' $\Rightarrow \sigma_{\chi_{c1}(3872)} / \sigma_{\psi(2S)}$ decreases

[Phys. Rev. Lett. 126, 092001](#)



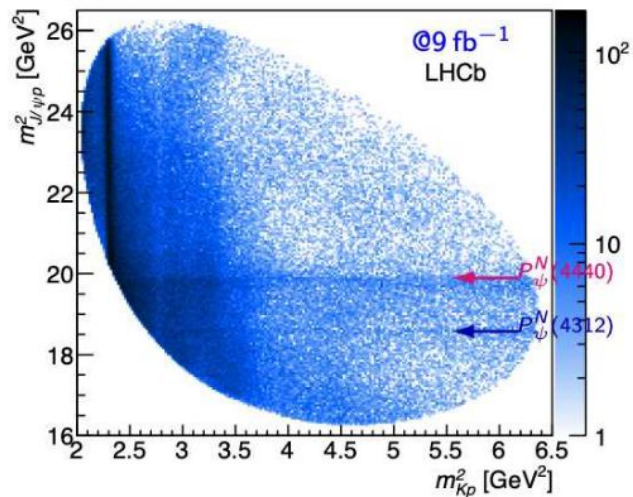
Pentaquarks



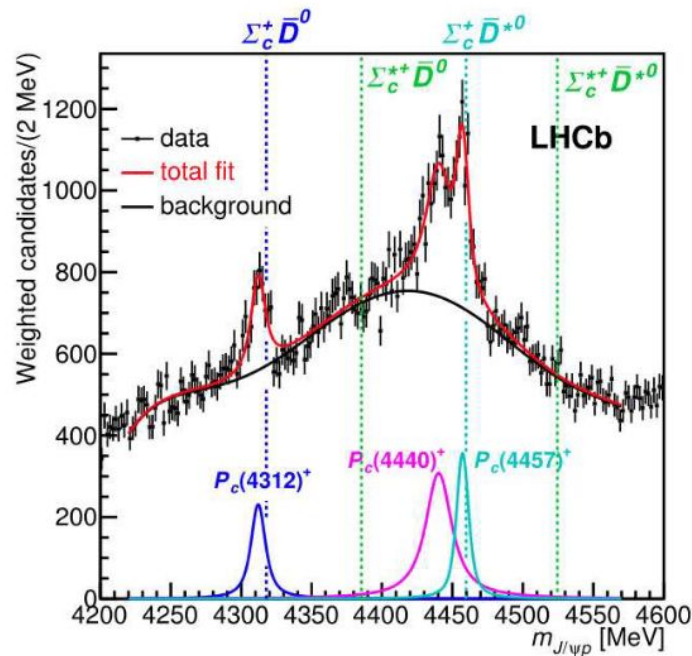
First discovery of pentaquarks

Dalitz plot analysis of

$\Lambda_b \rightarrow K^- p J/\psi$



State	M [MeV]	Γ [MeV]
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	$9.8 \pm 2.7^{+3.7}_{-4.5}$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	$6.4 \pm 2.0^{+5.7}_{-1.9}$

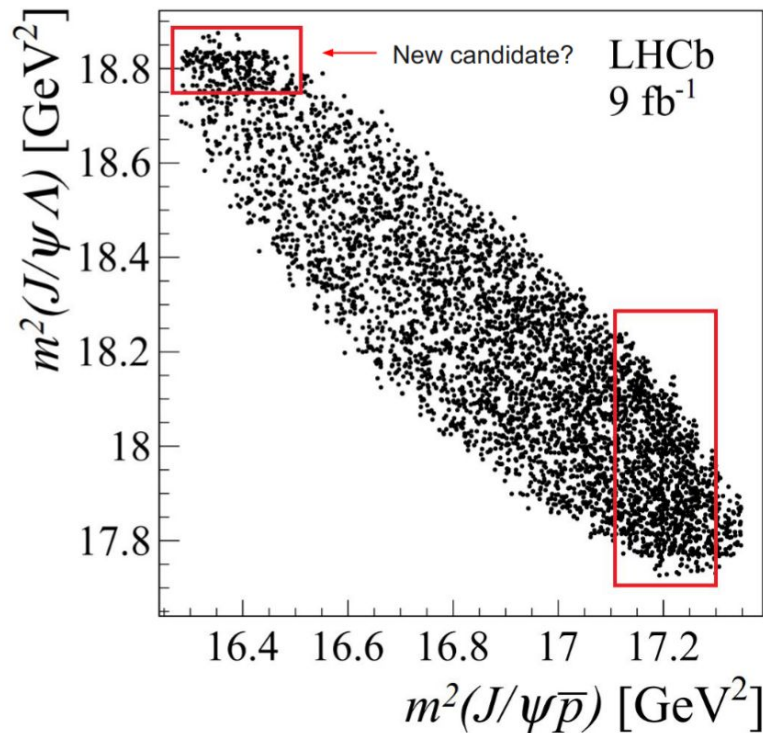


[Phys. Rev. Lett. **122**, 222001](#) (2019)

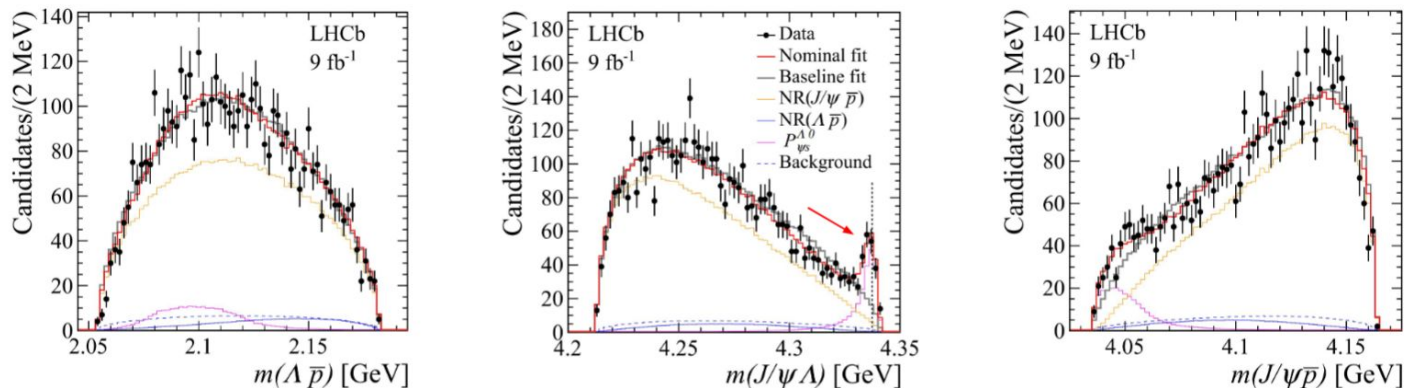
New strange pentaquark candidate $P_{\psi_s}^\Lambda$

- Amplitude analysis of $B^- \rightarrow J/\psi \Lambda \bar{p}$
 - pp collisions, $9 \text{ fb}^{-1} \Rightarrow \sim 4400$ events
 - High signal purity (93%)
- Fit model
 - Non-resonant $J/\psi \bar{p}$
 - Non-resonant $\Lambda \bar{p}$
 - Virtual $K_4^*(2045)^-, K_2^*(2250)^-, K_3^*(2320)^-$
 - Combinatorial background
 - Signal $P_{\psi_s}^\Lambda \rightarrow J/\psi \Lambda$

[*Phys. Rev. Lett.* **131**, 031901](#) (2023)



New strange pentaquark candidate $P_{\psi_s}^\Lambda$



Results of the fit:

[Phys. Rev. Lett. **131**, 031901 \(2023\)](#)

$$m(P_{\psi_s}^\Lambda) = 4338.2 \pm 0.7 \pm 0.4 \text{ GeV}$$

$$m(\Xi_c^+) + m(D^+) = 4337.2 \text{ MeV}$$

$$\Gamma(P_{\psi_s}^\Lambda) = 7.0 \pm 1.2 \pm 1.3 \text{ MeV}$$

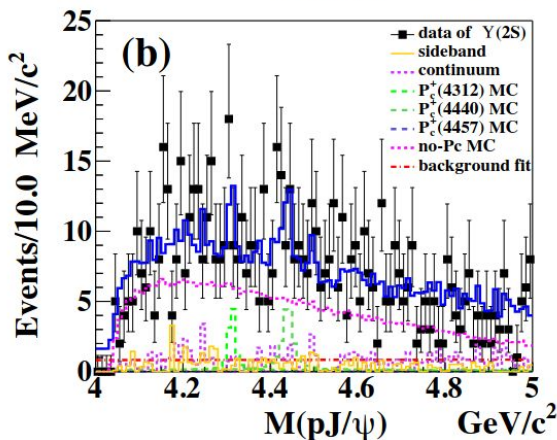
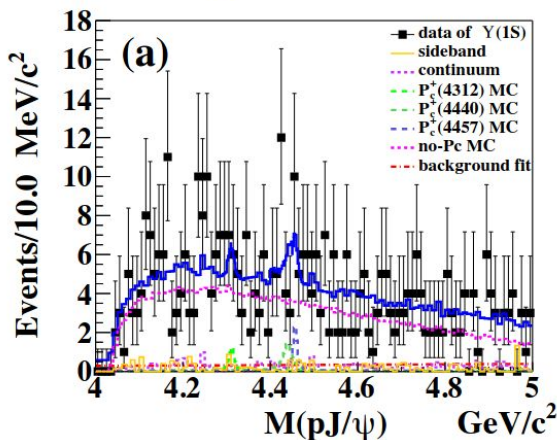
Preferred $J^P = 1/2^-$

First observation of $[c\bar{c}uds]$ pentaquark!

Significance $> 10\sigma$

Pentaquarks in Υ decays ?

arXiv:2403.04340 (submitted to JHEP)



Reconstruct inclusive $p J/\psi$
in $\Upsilon(1S)$ & $\Upsilon(2S)$ Belle data

No pentaquark signals found;
only slight excesses at LHC-b masses

Inclusive $p J/\psi$
BF results

$$\mathcal{B}(\Upsilon(1S) \rightarrow pJ/\psi + X) = (4.27 \pm 0.16 \pm 0.20) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow pJ/\psi + X) = (3.59 \pm 0.14 \pm 0.16) \times 10^{-5}$$

$$\sigma(pJ/\psi + X) = (57.5 \pm 2.1 \pm 2.5) \text{ fb at } 10.52 \text{ GeV}$$

Pentaquark Limits:

$$\mathcal{B}[\Upsilon(1S) \rightarrow P_c(4312)^+ + \text{anything}] \cdot \mathcal{B}[P_c(4312)^+ \rightarrow pJ/\psi] < 3.9 \times 10^{-6},$$

$$\mathcal{B}[\Upsilon(1S) \rightarrow P_c(4440)^+ + \text{anything}] \cdot \mathcal{B}[P_c(4440)^+ \rightarrow pJ/\psi] < 6.2 \times 10^{-6},$$

$$\mathcal{B}[\Upsilon(1S) \rightarrow P_c(4457)^+ + \text{anything}] \cdot \mathcal{B}[P_c(4457)^+ \rightarrow pJ/\psi] < 5.5 \times 10^{-6},$$

$$\mathcal{B}[\Upsilon(2S) \rightarrow P_c(4312)^+ + \text{anything}] \cdot \mathcal{B}[P_c(4312)^+ \rightarrow pJ/\psi] < 4.7 \times 10^{-6},$$

$$\mathcal{B}[\Upsilon(2S) \rightarrow P_c(4440)^+ + \text{anything}] \cdot \mathcal{B}[P_c(4440)^+ \rightarrow pJ/\psi] < 7.2 \times 10^{-6},$$

$$\mathcal{B}[\Upsilon(2S) \rightarrow P_c(4457)^+ + \text{anything}] \cdot \mathcal{B}[P_c(4457)^+ \rightarrow pJ/\psi] < 2.6 \times 10^{-6},$$

Pentaquarks in Υ decays!

[arXiv:2502.09951](https://arxiv.org/abs/2502.09951) (accepted by PRL)

Reconstruct inclusive $J/\psi \Lambda$ in $\Upsilon(1S)$ & $\Upsilon(2S)$
Belle data

3.3 σ evidence for LHCb state

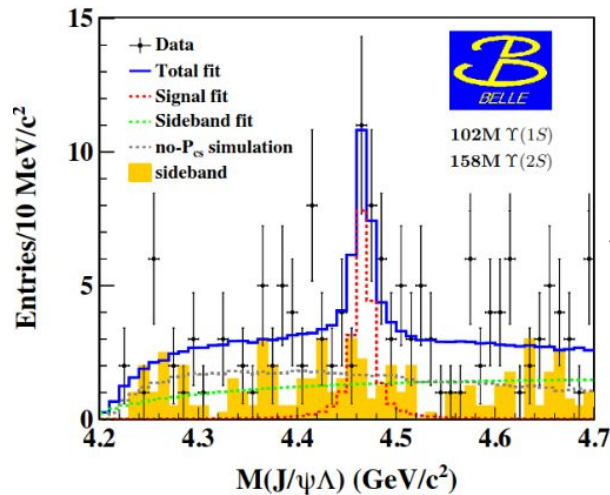
$P_{ccs}(4459)^0 \rightarrow J/\psi \Lambda$

– OR –

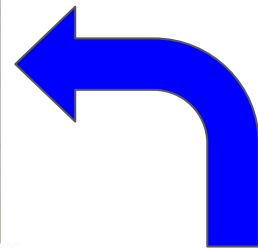
3.8 σ for a slightly more massive state

$M = 4471.7 \pm 4.8 \pm 0.6 \text{ MeV}/c^2$

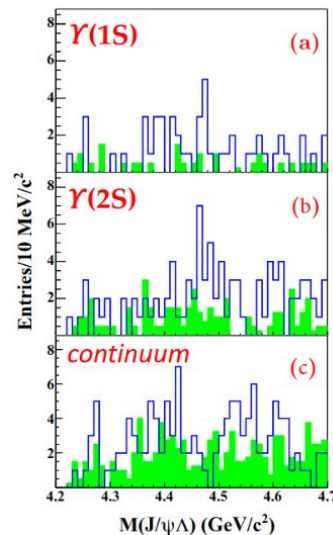
$\Gamma = 21.9 \pm 13.1 \pm 2.7 \text{ MeV}$



sum of the
resonance data



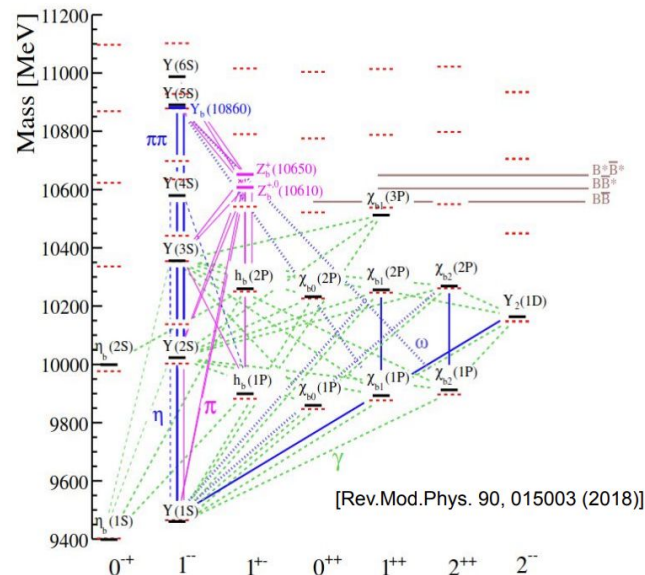
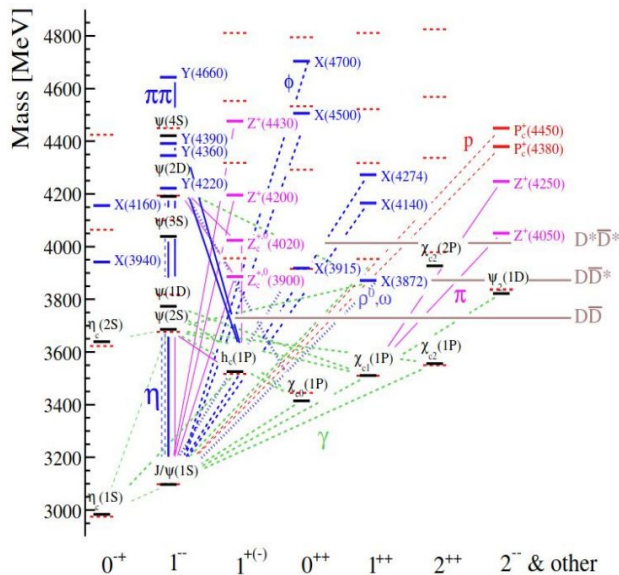
note that LHCb found
 $M = 4458.8 \pm 2.9^{+4.7}_{-1.1} \text{ MeV}/c^2$
 $\Gamma = 17.3 \pm 6.5^{+8.0}_{-4.7} \text{ MeV}$



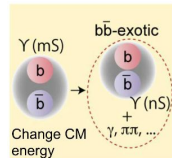
The $b\bar{b}$ spectrum

QCD is symmetric w.r.t. quark flavor

Compact charmonium-like states \Rightarrow should find **partners in the bottomonium region**

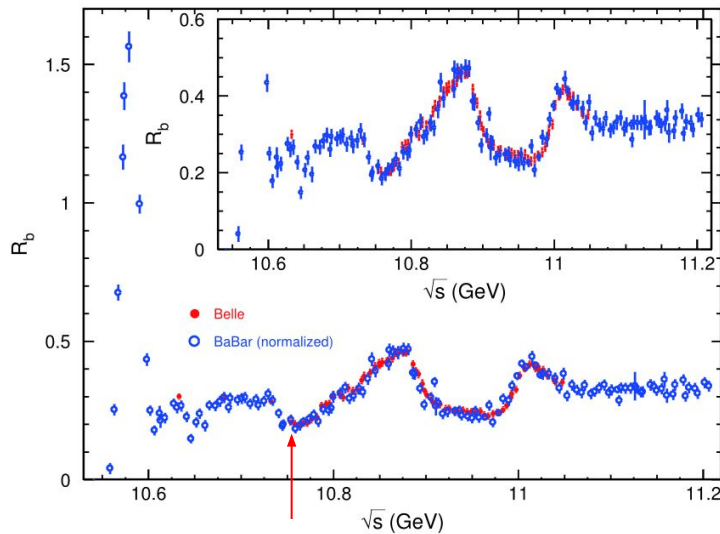


Belle: above $\Upsilon(4S)$



High energy scans @ Belle and BaBar $\Rightarrow R_b$

- Peaks at 10.86 and 11.02 GeV
 $\Rightarrow \Upsilon(5S), \Upsilon(6S)$
- Dips at 10.65, 10.75 GeV

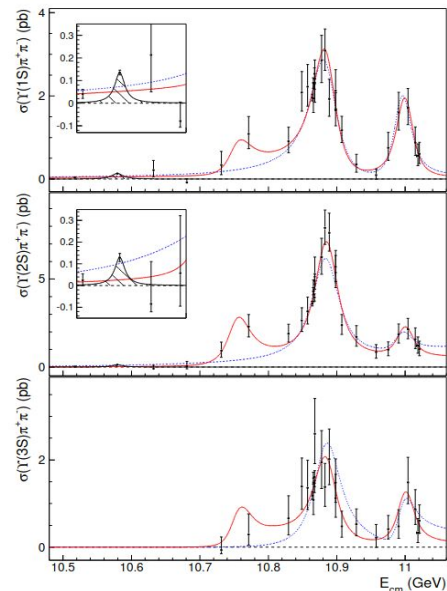


[Dong *et al.*, Chin. Phys. C 44 (2020) 8, 083001]

Discovery of $\Upsilon(10753)$ ($\pi\pi$ transitions)

We want to

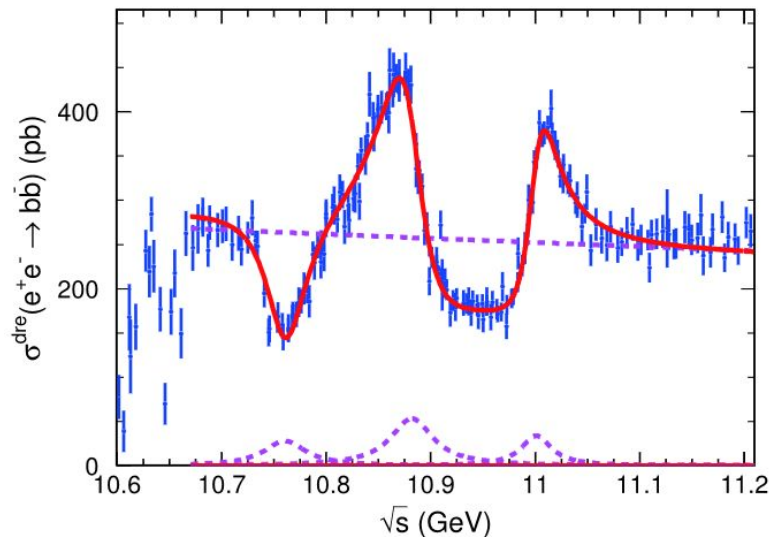
- know more about its nature
- explore transitions to lower states



[Belle, JHEP 10 (2019) 220]

Fitting the R_b scans

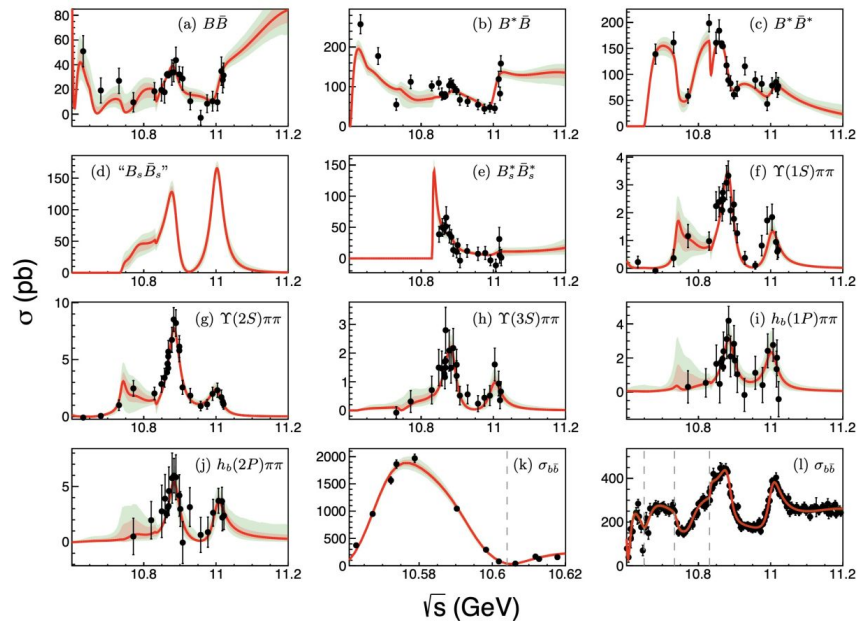
Coherent sum of continuum and 3 BW functions
 [Dong *et al.*, Chin. Phys. C 44 (2020) 8, 083001]



Parameter	$Y(10750)$	$\Upsilon(5S)$	$\Upsilon(6S)$
Mass/(MeV/c ²)	10761 ± 2	10882 ± 1	11001 ± 1
Width/MeV	48.5 ± 3.0	49.5 ± 1.5	35.1 ± 1.2

Coupled channel analysis using the K matrix formalism

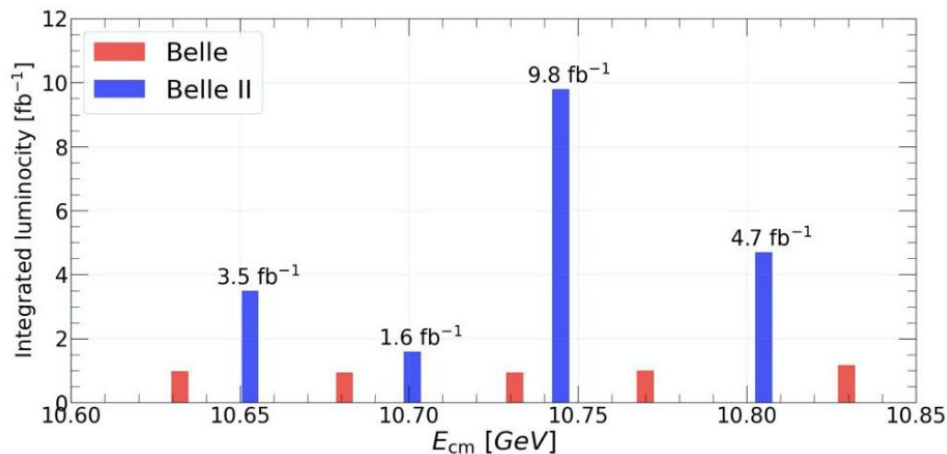
[Hüsken *et al.*, PRD 106 (2022) 9, 094013]



Belle II: new scan points (Nov. 2021)

Motivations:

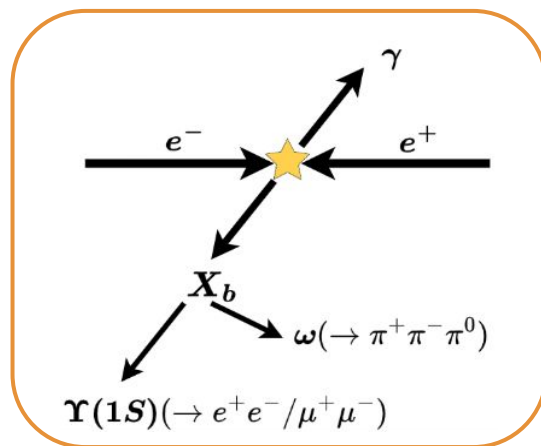
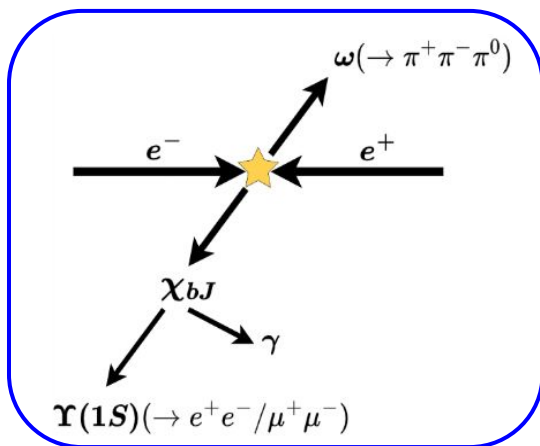
- **confirm** existence and properties of the $Y(10753)$ state
- update the R_b scan, $e^+e^- \rightarrow BB$, $Y(10753) \rightarrow \pi^+\pi^-Y(nS)$
- observe **new transitions** / **new states**!



Observation of $Y(10753) \rightarrow \omega \chi_{bJ}(1P)$ and search for X_b

Same final state $\gamma \omega Y(1S)$

$\omega \rightarrow \pi^+ \pi^- \pi^0$, $Y(1S) \rightarrow l^+ l^-$



Inspired by observations at **BESIII**

$$Y(4230) \rightarrow \chi_{c0}(1P) \omega$$

$$Y(4230) \rightarrow \gamma X(3872)$$

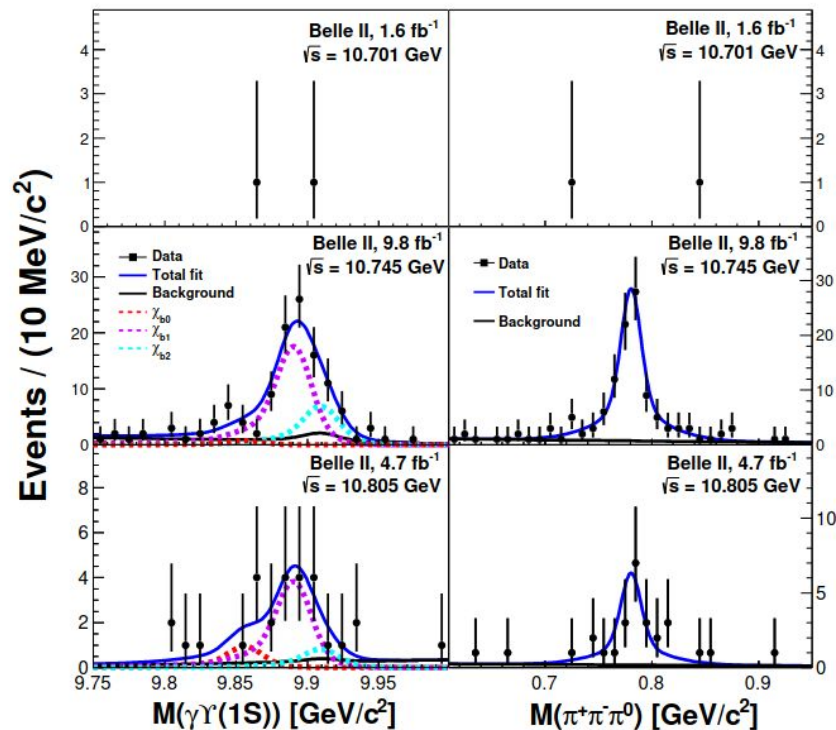
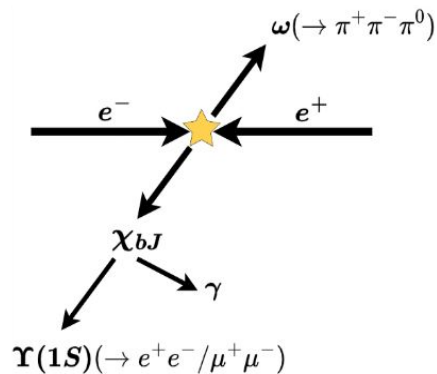
Observation of $Y(10753) \rightarrow \omega \chi_{bJ}(1P)$

Prediction for S-D mixed state

[PRD 104 034036 (2021)]

BR comparable with
 $Y_b \rightarrow \pi^+ \pi^- Y(nS)$

$$\frac{\mathcal{B}(\omega \chi_{b1})}{\mathcal{B}(\omega \chi_{b2})} \sim \frac{1}{5}$$

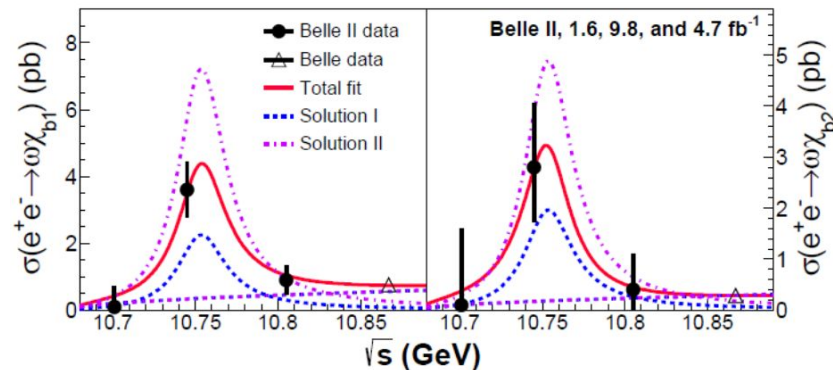


PRL 130, 091902 (2023)

Observation of $Y(10753) \rightarrow \omega \chi_{bJ}(1P)$

Signal is larger than in $Y(10753) \rightarrow Y(2S)\pi^+\pi^-$

Signal at $Y(5S)$ (Belle \triangle) is likely a **tail**



PRL 130, 091902 (2023)

Two $J^{PC} = 1^-$ states, $\Delta M = 120$ MeV, 1 order of magnitude diff in $\sigma \Rightarrow$ hints at **different structure**

$$\frac{\sigma(e^+e^- \rightarrow \chi_{b1}(1P)\omega)}{\sigma(e^+e^- \rightarrow \chi_{b2}(1P)\omega)} = 1.3 \pm 0.6$$

Pure $Y(3D)$ would give 15 [Guo *et al.*, PLB 738 (2014), 172]
Slight tension with mixed 4S-3D state
[Li *et al.*, PRD 104 (2021) 034036]

Search for X_b

Bottomonium analogue of $X(3872)$

Existence predicted in both molecular and tetraquark models

- **Molecule** \Rightarrow M close to $B\bar{B}^*$ threshold
- **Tetraquark** $\Rightarrow 10 < M < 11 \text{ GeV}/c^2$

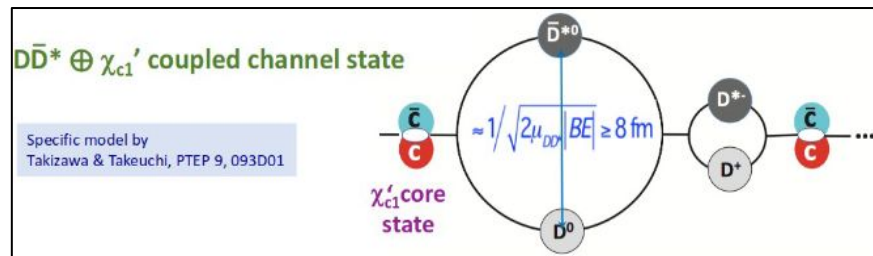
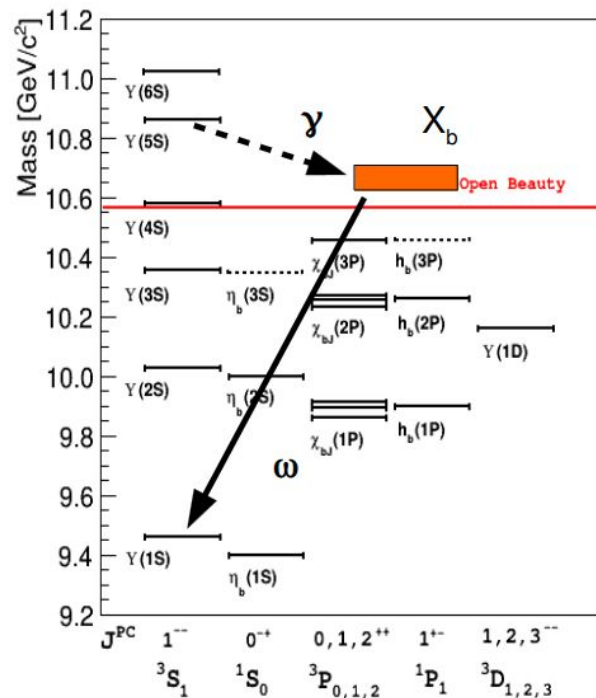
Dynamical effect (cusp)?

No χ_b near $B\bar{B}^*$ threshold \Rightarrow No X_b ?

Strong UL on $\sigma \Rightarrow$ exclude tetraquark hypothesis

Negligible isospin breaking for X_b

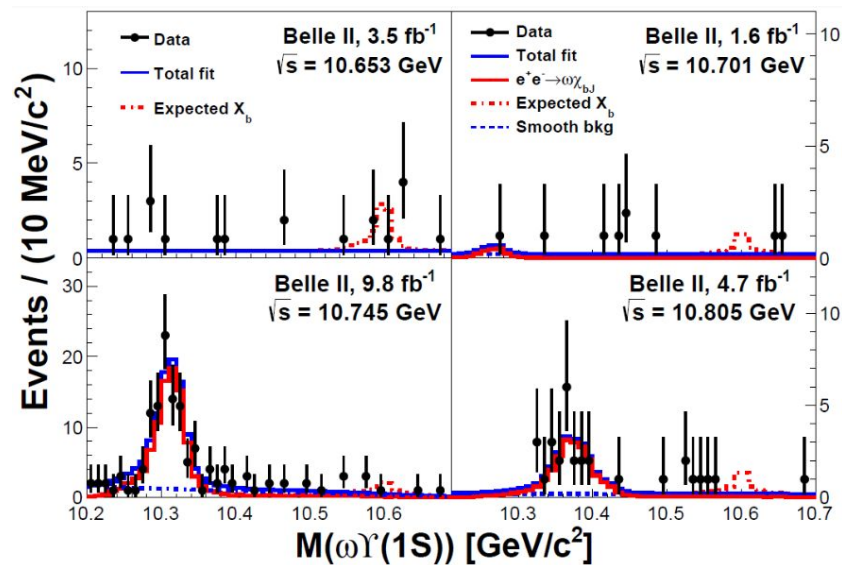
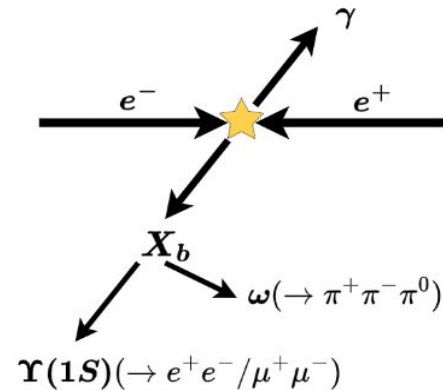
\Rightarrow **3π mode enhanced** wrt 2π



Search for X_b

- Same $Y(1S) \pi^+ \pi^- \pi^0 \gamma$ final state
- Search for resonances in $M(Y(1S)\omega)$
- Reflection from $Y(10753) \rightarrow \omega \chi_{bJ}(1P)$
- **No evidence for X_b signal**

\sqrt{s} (GeV)	M_{X_b} (GeV)	$\sigma_{X_b}^{UL}$ (pb)
10.653	10.59	0.55
10.701	10.45	0.84
10.745	10.45	0.14
10.805	10.53	0.47

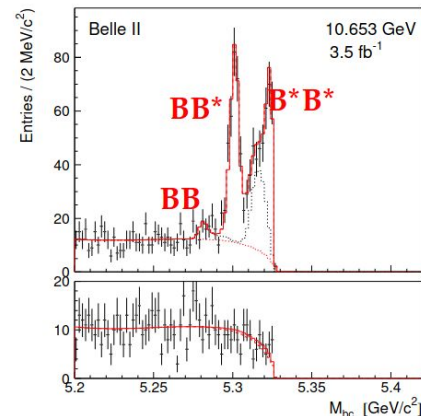
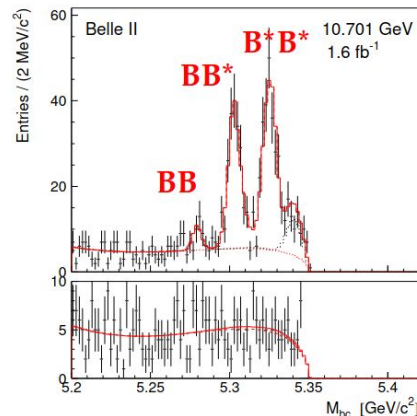
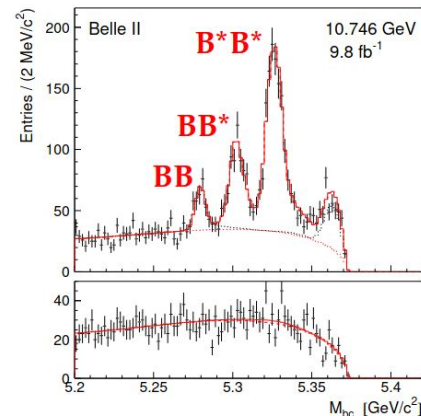
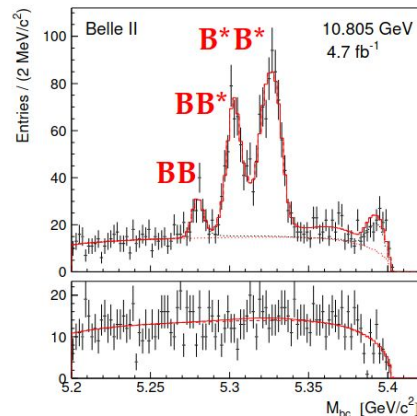


$e^+e^- \rightarrow B\bar{B} + B\bar{B}^* + B^*\bar{B}^*$ cross sections

Method

- FEI: fully reconstruct one B
[Comput.Softw.Big Sci. 3 (2019) 1, 6]
- Identify signals with M_{bc}
- Combine with Belle measurement
[JHEP 06, 137 (2021)]

$$M_{bc} = \sqrt{(E_{cm}/2)^2 - p_B^2}$$

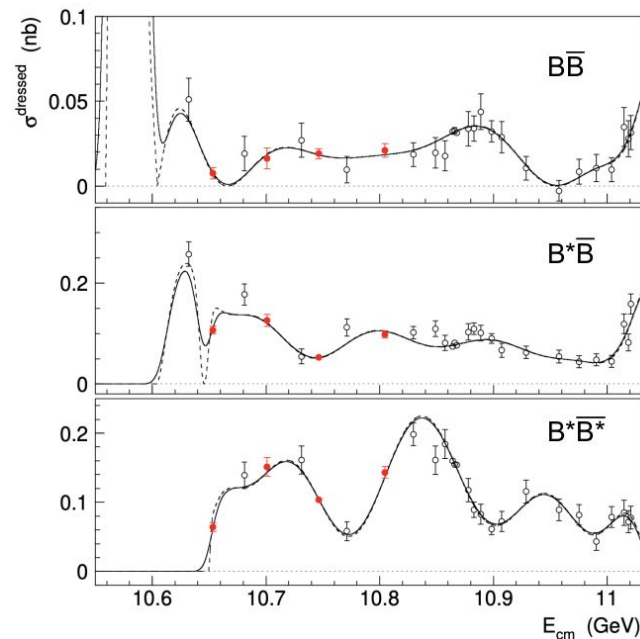


$e^+e^- \rightarrow B\bar{B} + B\bar{B}^* + B^*\bar{B}^*$ cross sections

2-body cross sections fit with
Chebychev polynomials

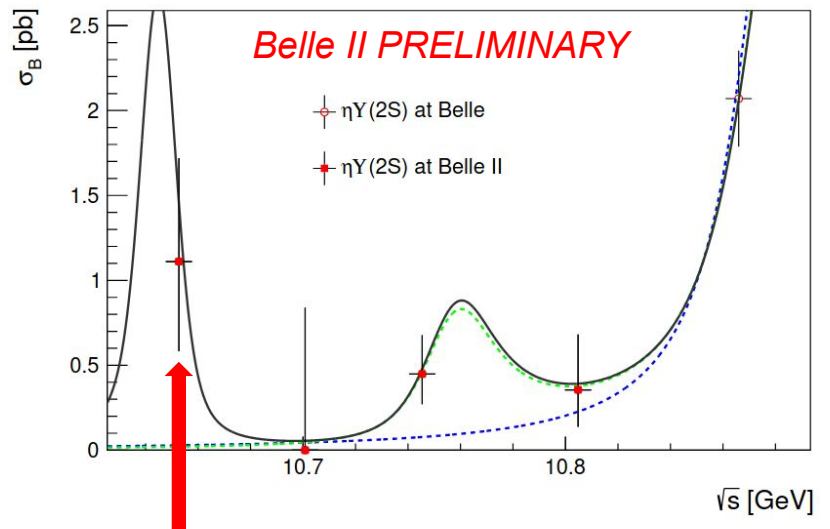
Steep rise of the $B^*\bar{B}^*$ cross section
at threshold

⇒ hint at existence of **bound state**



[JHEP 10 \(2024\) 114](#)

Search for $e^+e^- \rightarrow \eta Y(1, 2S)$ near $Y(10753)$



— $B^*\bar{B}^*$ bound state near threshold

--- Fit with $Y(5S)$ and $Y(10753)$

--- Fit with $Y(5S)$ only

Belle II PRELIMINARY

Mode	$N_{\text{signal}}/\mathcal{B}\epsilon$	\mathcal{L} (pb^{-1})	$(1 + \delta)$	$ 1 - \Pi ^2$	σ_B (pb)
(10653.30 ± 1.14) MeV					
$\eta Y(2S)$	$(3.71^{+1.6}_{-1.3}) \times 10^3$	3521	0.881	0.929	$1.11^{+0.49}_{-0.39} \pm 0.36$
$\eta Y(1S)$	$< 0.4 \times 10^3$	3521	0.895	0.929	< 0.10
γX_b	$< 0.3 \times 10^3$	3521	0.784	0.929	< 0.14
(10700.90 ± 0.63) MeV					
$\eta Y(2S)$	$(0.00^{+1.0}_{-0.0}) \times 10^3$	1632	1.832	0.928	$0.00^{+0.31}_{-0.00} \pm 0.53$
$\eta Y(1S)$	$< 0.4 \times 10^3$	1632	0.901	0.928	< 0.22
γX_b	$< 0.1 \times 10^3$	1632	0.803	0.928	< 0.09
(10746.30 ± 0.48) MeV					
$\eta Y(2S)$	$(3.25^{+1.6}_{-1.2}) \times 10^3$	9818	0.687	0.930	$0.45^{+0.22}_{-0.17} \pm 0.05$
$\eta Y(1S)$	$< 0.9 \times 10^3$	9818	0.906	0.930	< 0.09
γX_b	$< 1.4 \times 10^3$	9818	0.817	0.930	< 0.17
(10804.50 ± 0.70) MeV					
$\eta Y(2S)$	$(1.52^{+1.4}_{-0.9}) \times 10^3$	4690	0.848	0.931	$0.36^{+0.32}_{-0.21} \pm 0.04$
$\eta Y(1S)$	$< 0.4 \times 10^3$	4690	0.912	0.931	< 0.08
γX_b	$< 1.3 \times 10^3$	4690	0.833	0.931	< 0.32

Also search for

$X_b \rightarrow \pi^+\pi^-\chi_{b1,2}(1P)$, $\chi_{b1,2} \rightarrow \gamma Y(1S)$

No signal \Rightarrow UL on σ_B are set

Conclusion and prospects

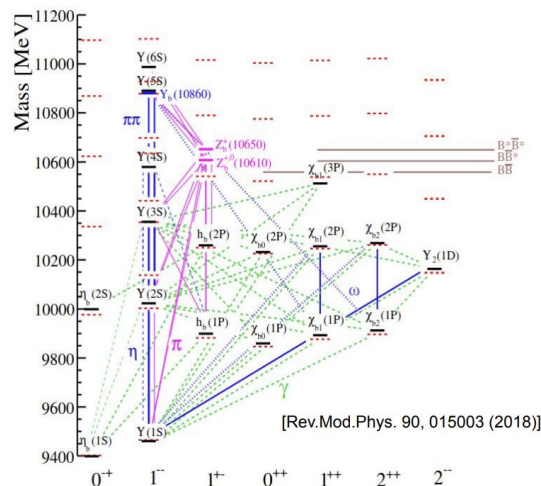
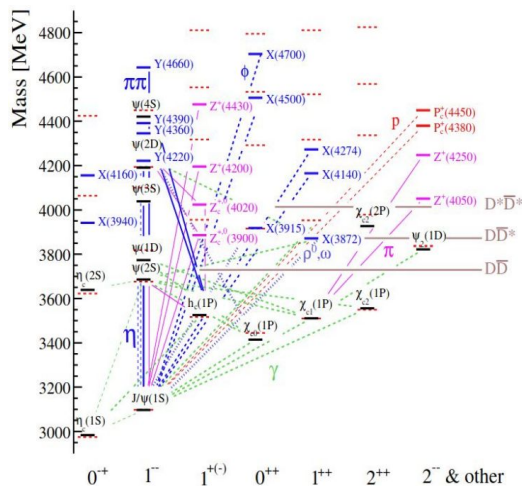
- The advent of B factories has led to a renaissance of hadron spectroscopy
 - Tens of new state discovered, more are expected to come
- Properties of T_{cc} are being studied in detail at LHCb
 - Belle II could be able to produce T_{cc} in double charmonium production with larger statistics
- Pentaquarks have been discovered in beauty hadron decays, but we are seeing the first evidence of inclusive production of these states also in $Y(nS)$ decays
- The nature of the recently discovered vector bottomonium-like state $Y(10750)$ still unclear
 - The recent scan data above $Y(4S)$ is showing interesting results
- Implementing femtoscopy in $e^+e^- \rightarrow Y(nS) \rightarrow ppX$ at Belle

Stay tuned!

Backup

The rebirth of hadron spectroscopy

- Lots of unexpected, puzzling experimental results
 - especially in heavy quarkonium sector
- Difficulties in QCD calculations hinder accurate predictions for spectra
- Interplay of **experimental results** and **effective models/LQCD** is needed



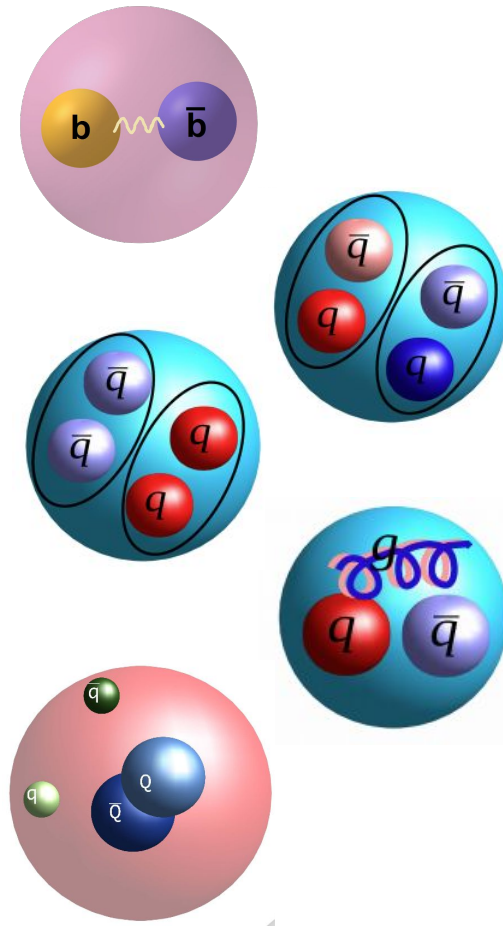
Exotic heavy quarkonia

What are they? Competition between several models:

- **Standard quarkonia** [Swanson, PRD 91, 034009 (2015)]
- **Meson molecules**: shallow bound states of two mesons [Guo *et al.*, Rev.Mod.Phys.90,015004 (2018)]
- **Compact tetraquarks**: diquark-antidiquark states bound by the color force [Polosa *et al.*, PRD89, 114010 (2014)]
- **Hybrids**: colored QQbar states with bound excited gluon [Meyer and Swanson, Prog.Part.Nucl.Phys. 82, 21 (2015)]
- **Hadroquarkonium**: QQbar state surrounded by a cloud of light quarks [Dubinskij *et al.*, PLB 666, 344 (2008)]

Comprehensive reviews:

- Brambilla *et al.*, Eur. Phys. J. C (2011) 1534
- Olsen *et al.*, Rev. Mod. Phys. 90 (2018) 015003

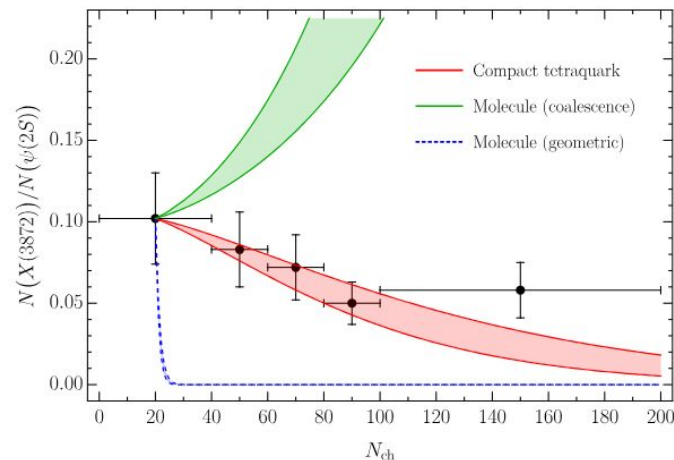


Suppression of $\chi_{c1}(3872)$

Study behaviour of states immersed in QCD matter \Rightarrow estimate the spatial size

Comover Interaction Model (CIM):

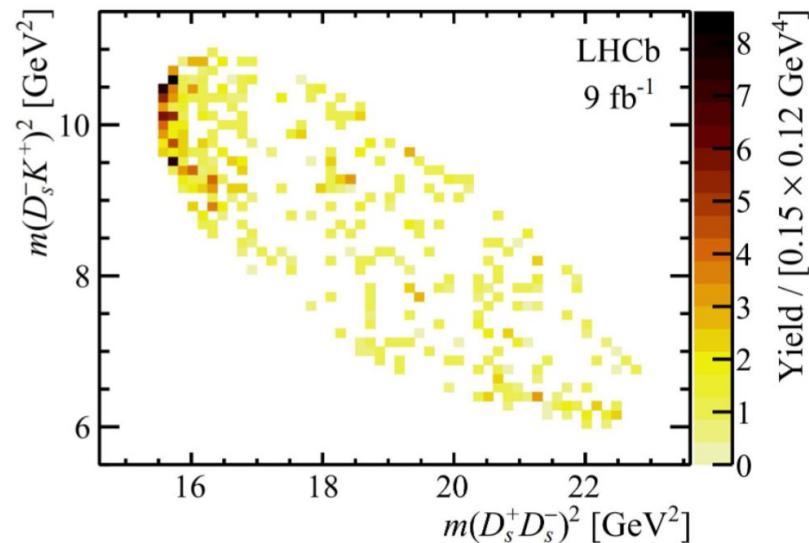
- Quarkonia broken by collision with comovers in nuclear medium
- Breakup cross section depends on radius and binding energy
- Pure molecules:
 - large radius \Rightarrow quick dissociation
 - reformation by coalescence \Rightarrow σ increases



Modeling (3872) as a compact tetraquark ($r=1.3$ fm) well reproduces experimental data [arXiv:[2006.15044](https://arxiv.org/abs/2006.15044)]

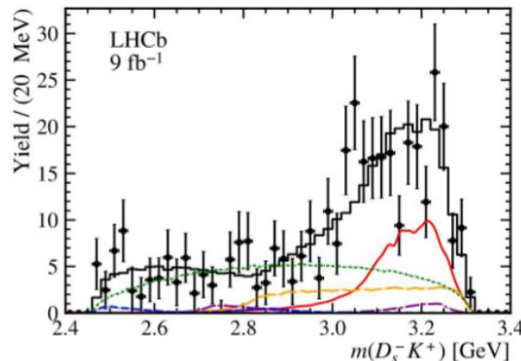
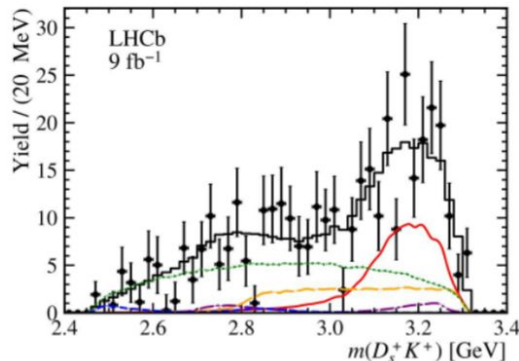
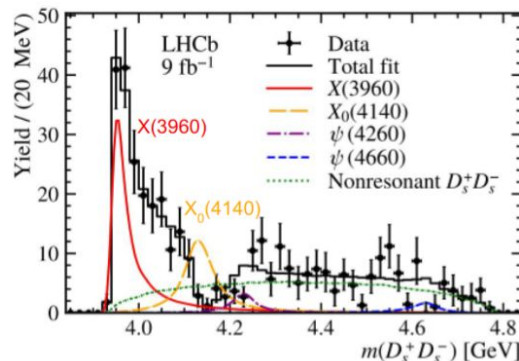
Observation of X(3960) and search for X(4140)

- Amplitude analysis of $B^+ \rightarrow D_s^+ D_s^- K^+$
 - 360 events
 - Enhancement close to threshold in $M(D_s^+ D_s^-)$
- Fit model
 - $\psi(4260)$, $\psi(4660)$ contributions
 - Non-resonant $D_s^+ D_s^- K^+$ component
 - X(3960), X(4140) signals



[Phys. Rev. Lett. 131, 071901 (2023)]

Observation of X(3960) and search for X(4140)

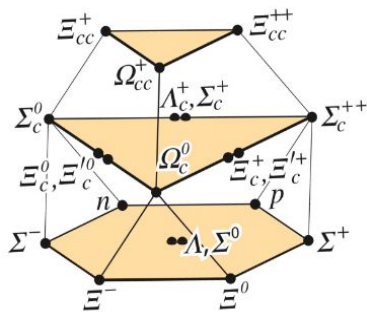


- X(3960)
 - Significance > 12 σ
 - $M = 3956 \pm 5 \pm 10$ MeV, $\Gamma = 43 \pm 13 \pm 8$ MeV
 - Minimal quark content [ccss]
- X(4140)
 - Significance = 3.9 σ
 - Dip around 4140 MeV: X(4140) or $J/\psi \rightarrow D_s + D_{s^-}$ rescattering?
- Both states with preferred $J^{PC} = 0^{++}$

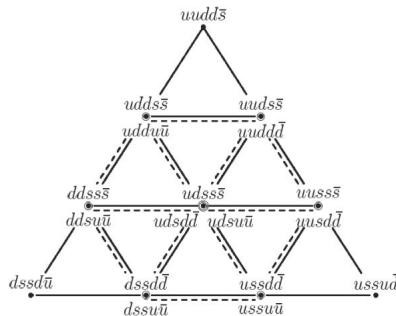
Compact objects?

If so, symmetry should imply existence of tetra- and penta-quark multiplets

e.g. can we find partners of \mathbf{T}_{cc} ?



Spin 1/2 $SU(4)_f$
multiplet



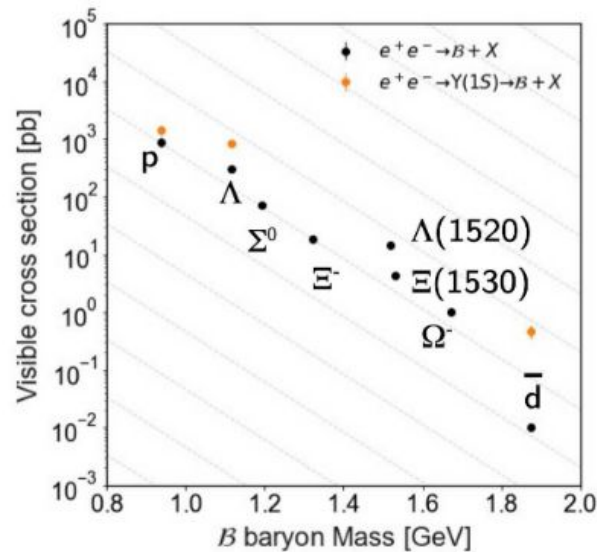
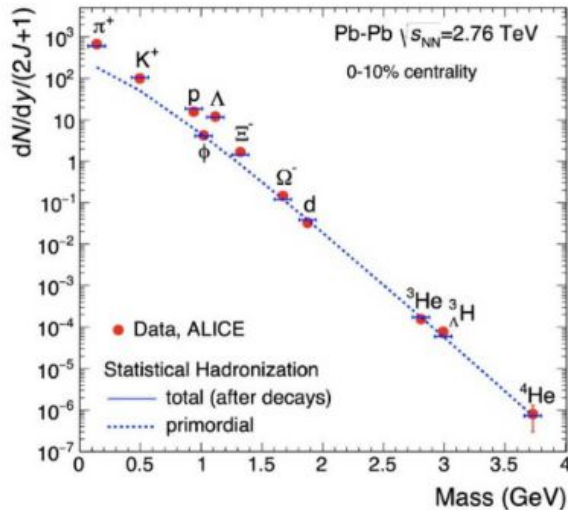
Light pentaquark
multiplet

[2411.08429]

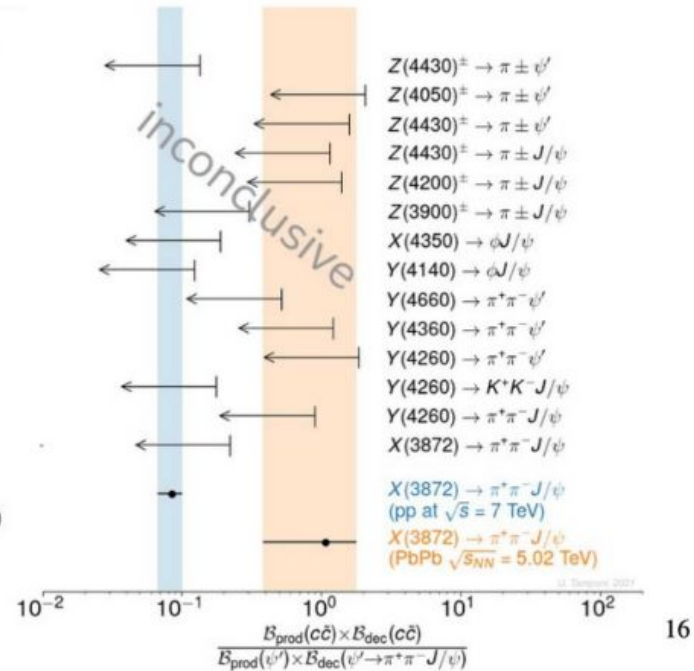
Heavy quarkonia: **non-perturbative QCD**: rely on EFTs / lattice / potential models

Production of exotica in Y decays at Belle

ALICE has been doing many studies on scaling laws to describe inclusive production of hadrons in heavy ion collisions.



Enhanced production of hyperons and even nuclei in bottomonium decays is known since ARGUS times and has been exploited by B factories to search for dibaryons.



BELLE has been searching for inclusive production of many tetraquarks in Y decays, but further data are needed to reach solid conclusions.

What about pentaquarks in Y decays?

The $\chi_{c1}(3872)$ state

N. Hüsken, E. S. Norella, I. Polyakov

4.2. The $\chi_{c1}(3872)$ (also known as $X(3872)$)

MESON-LIKE/HIDDEN CHARM/ISOSCALAR

quantum numbers: $I^G(J^{PC}) = 0^+(1^{++})$

minimal quark content: $[c\bar{c}]$, more likely $[c\bar{c}(u\bar{u} + d\bar{d})]$

experiments: Belle, CDF, D0, BaBar, LHCb, CMS, ATLAS, BESIII (and potentially E705, COMPASS)

production: B^+ , B^0 , B_s^0 and Λ_b^0 decays, prompt pp , $p\bar{p}$, pPb (Pbp) and PbPb collisions, $e^+e^- \rightarrow \gamma\chi_{c1}(3872)$, $\omega\chi_{c1}(3872)$ potentially via ψ - or χ_c -like states

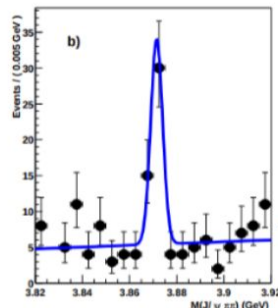
decay modes: $\pi^+\pi^-J/\psi$, $\omega J/\psi$, $D^{*0}\bar{D}^0$, $\pi^0\chi_{c1}(1P)$, $\gamma J/\psi$, $\gamma\psi(2S)$

nearby threshold: $D^{*0}\bar{D}^0$

width: 1.19 ± 0.21 MeV (*Breit-Wigner*)

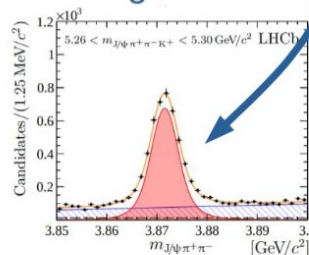
$$m(\chi_{c1}(3872)) - m(D^{*0}\bar{D}^{*0}) = -0.07 \pm 0.12 \text{ MeV}$$

LHCb, JHEP 08 (2020) 123

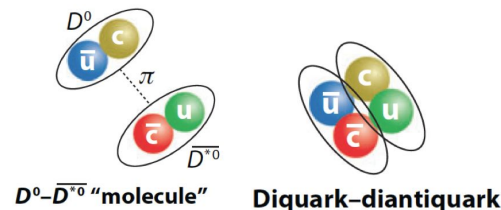


Belle, PRL 91 (2003) 262001

36 \rightarrow 20x10³
signal events



LHCb, JHEP 08 (2020) 123



Proximity to threshold, dominant decay modes, $J^{PC} = 1^{++}$

\Rightarrow molecular picture is favored

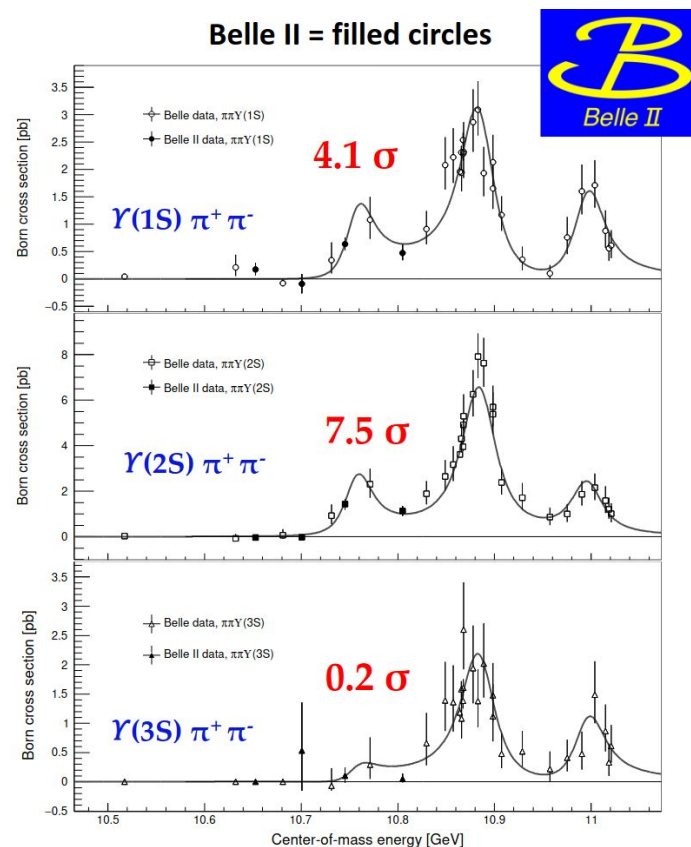
Di-pion transitions

Analysis of di-pion transitions:
excellent confirmation of $\Upsilon(10753)$
properties

$$M = 10756.6 \pm 2.7 \pm 0.9 \text{ MeV}$$

$$\Gamma = 29.0 \pm 8.8 \pm 1.2 \text{ MeV}$$

$$\Upsilon(10753) \rightarrow \pi^+ \pi^- \Upsilon(nS), n=1,2,3$$



[JHEP 07, 116 (2024)]

Femtoscopy

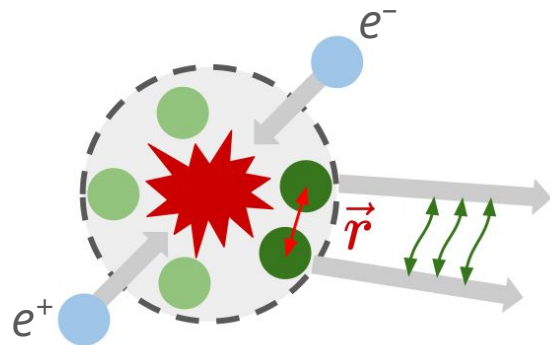
Method to probe **geometric** and **dynamic** properties of a **source of hadrons**

They are affected by

- quantum statistics
- interaction potential
- hadronization process

Key observable: 2-particle correlation function $C(k^*)$

(k^* = relative momentum)
$$C(k^*) = \int S(r) |\Psi(\vec{k}^*, \vec{r})|^2 d^3r$$

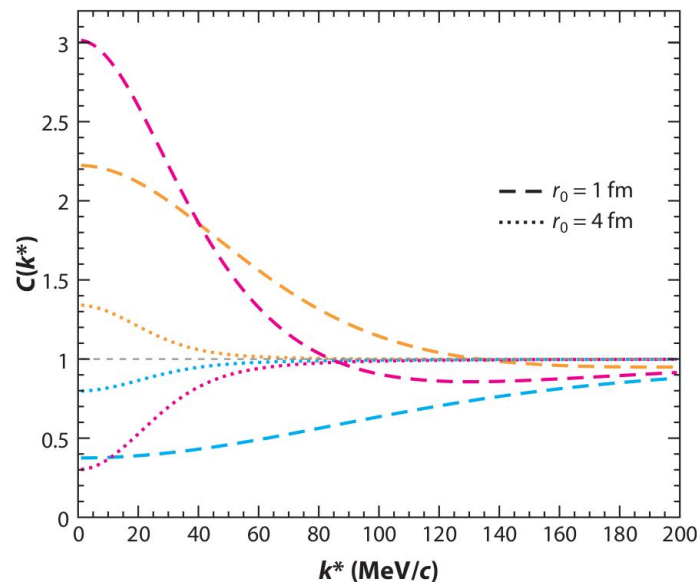


- known interaction \Rightarrow study source geometry
- known source \Rightarrow study the interaction

Correlation function

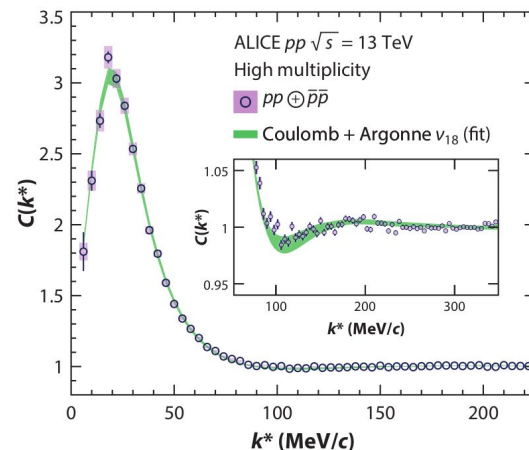
$$C(k^*) = \int S(r) |\Psi(\vec{k}^*, \vec{r})|^2 d^3r$$

Expectations from theory for 2 different **source sizes** (r_0)



[Phys. Atom. Nucl. 71 (2008) 1572-1578]

- **Orange**: attractive potential
- **Blue**: repulsive potential
- **Magenta**: shallow bound state

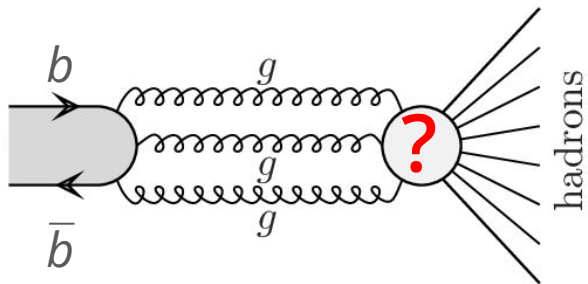


[Phys.Lett.B 805 (2020) 135419]

Goal of the analysis

The pp interaction potential is well known (Coulomb + Argonne v_{18})

But we know nothing about the **source geometry**



Idea: select protons with high purity

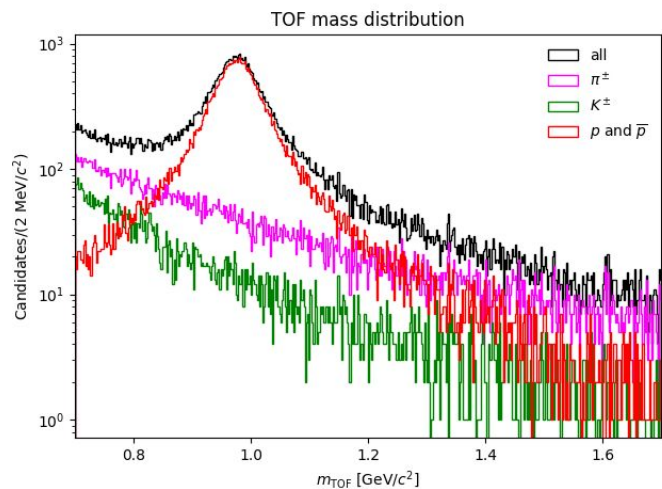
Then build $C_{\text{exp}}(k^*) = \mathcal{N} \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$

Fit to $C(k^*) = \int S(r) |\Psi(\vec{k}^*, \vec{r})|^2 d^3r$ with known Ψ

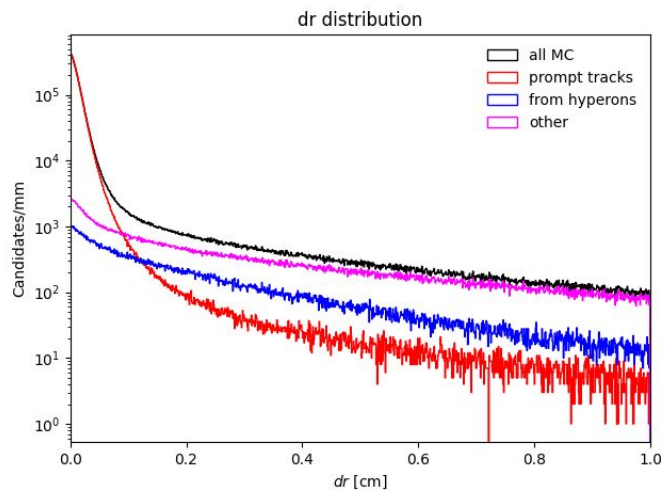
Get source size

Using this technique in $e^+e^- \rightarrow Y(nS) \rightarrow ggg$ for 1st time!

Identifying prompt protons



Fit \Rightarrow **proton** fraction



Fit \Rightarrow **prompt** tracks fraction

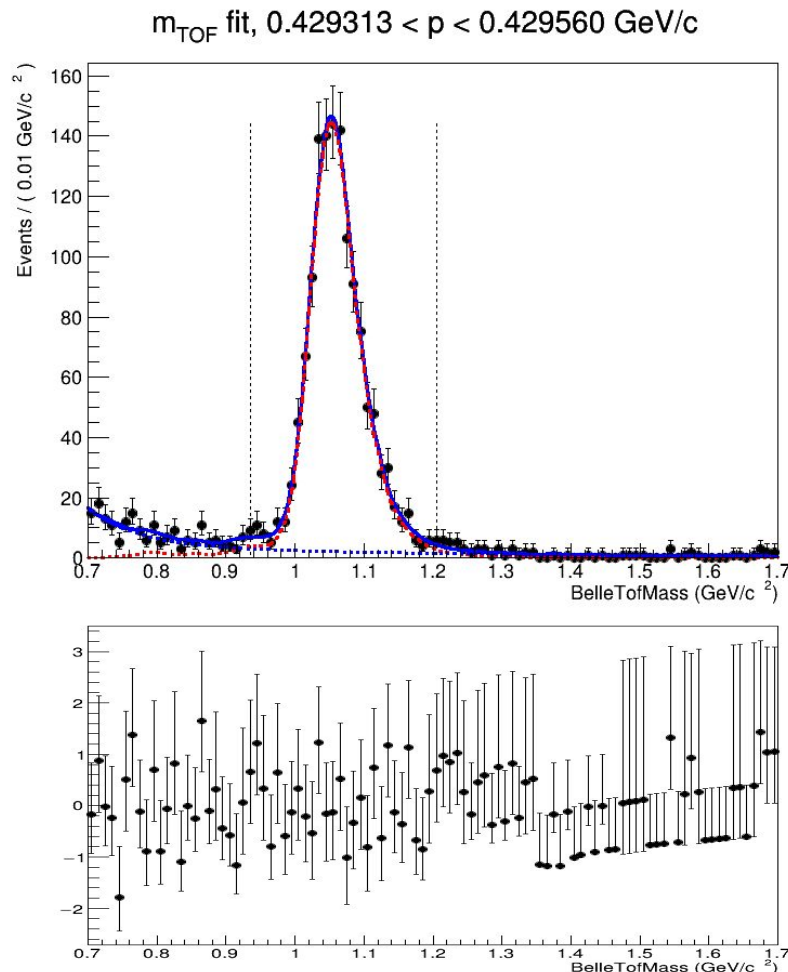
m_{TOF} fits

Extended binned ML

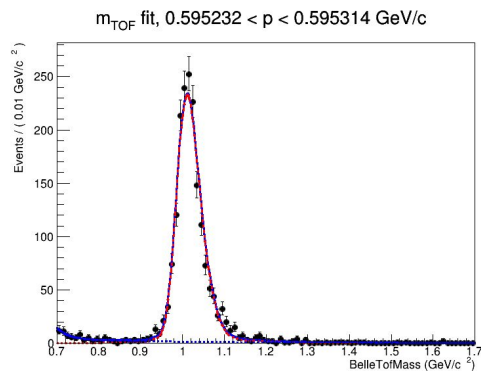
$$f(m) = n_S T_{\text{MC}} * \mathcal{SN}(\mu, \sigma_L, \sigma_R) + \\ + n_B (f_\pi \text{Exp}(\lambda_\pi m) + f_K \text{Exp}(\lambda_K m))$$

After convergence:

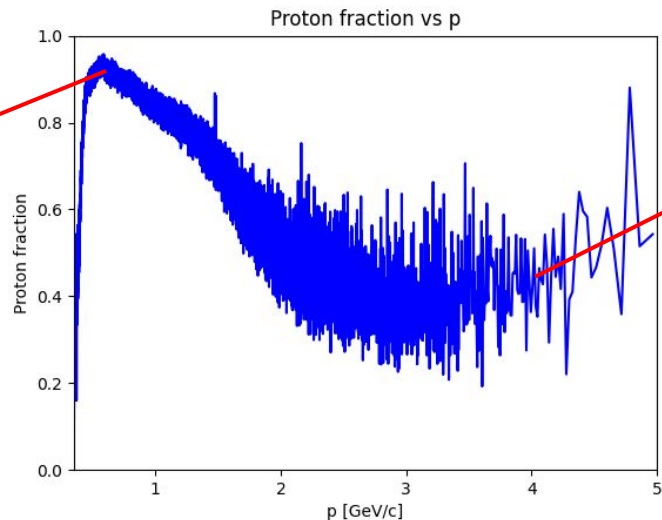
- get signal mode and FWHM
- take **(-2*FWHM, +2.5*FWHM)** range
- get **sig** and **bg** p.d.f.'s integrals inside range
- multiply integrals by n_S and n_B



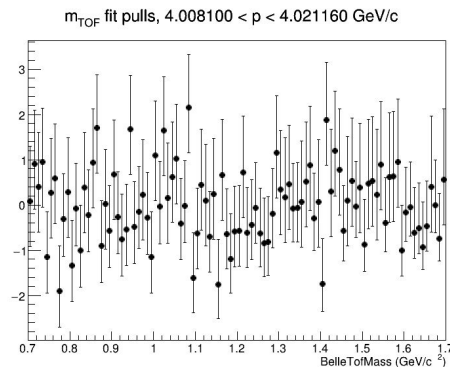
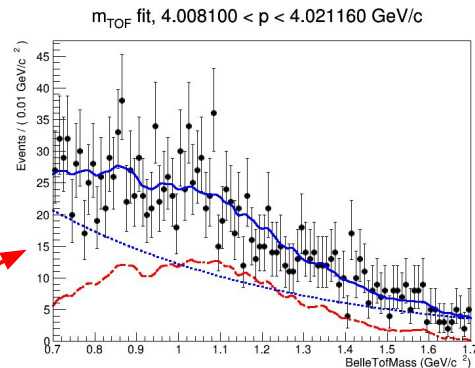
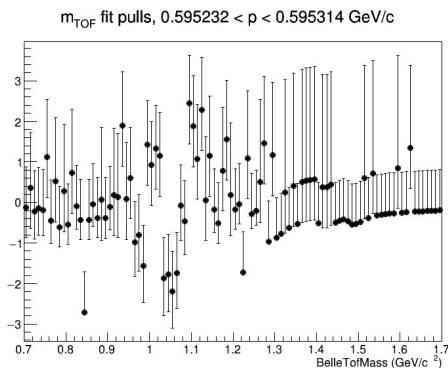
Measured (anti-)proton fraction vs p



Y(2S) data (good)



These values are put into a lookup table for proton identification



Mixed event technique

We build k^* distributions for pairs reconstructed in both **same** and **mixed** events

Mixed events: have to be similar

- N_{tracks} bins: [2, 4, 6, 10, 15, 20, 25, 30, 50]
- R_2 bins: [0.0, 0.1, 0.2, 0.3, ..., 1.0]

$$C_{\text{exp}}(k^*) = \mathcal{N} \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

