

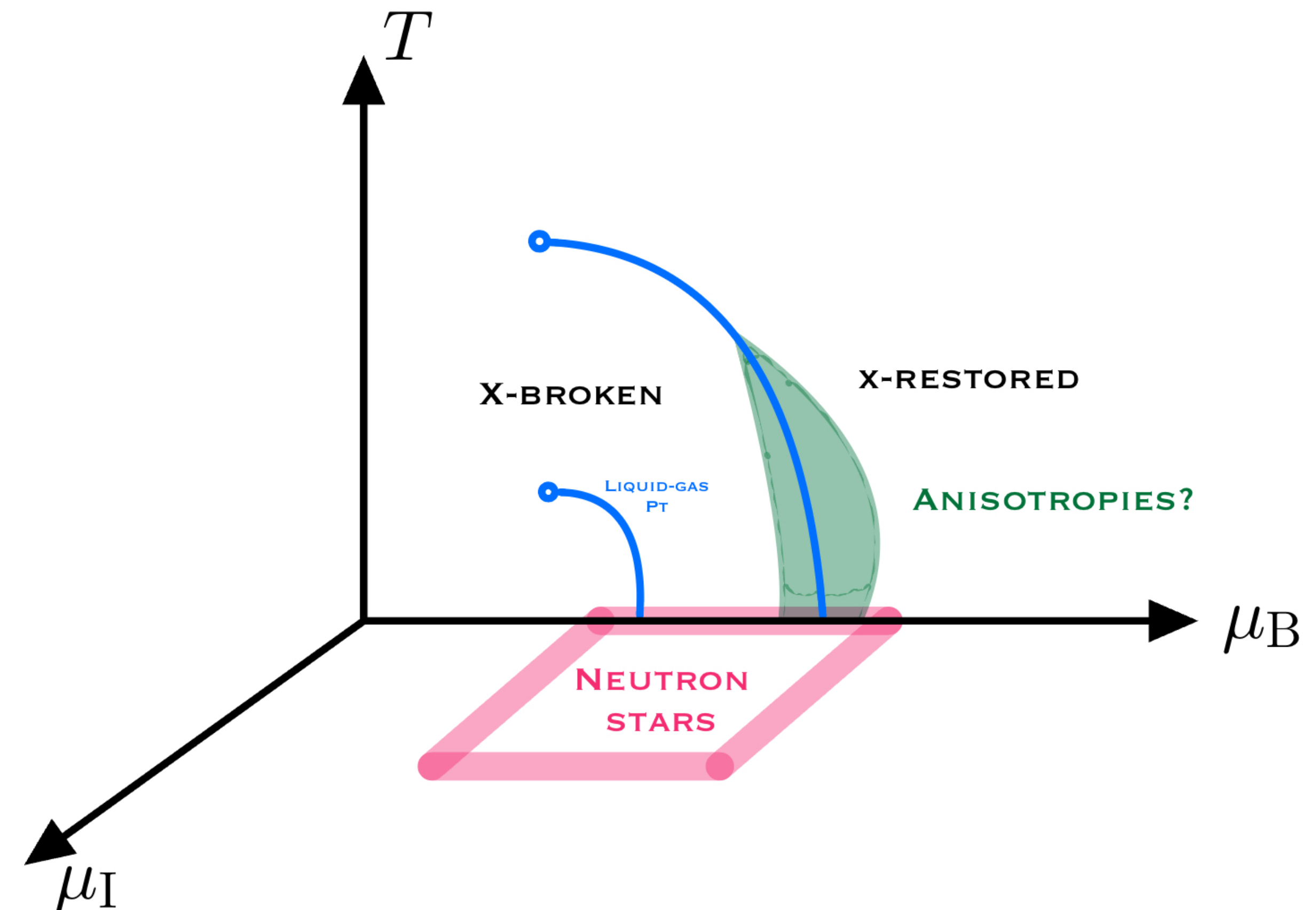
Chiral density wave in neutron stars?

PRD 111, 034010 (2025) with Andreas Schmitt

What we are interested in

- Vicinity of chiral phase transition $\rightarrow$ possible **anisotropies** [Buballa, Carignano '14 / Demircik, Jokela, Jarvinen, Piispa '24]
- Introduce μ_I , electric charge neutrality, β -equilibrium $\rightarrow$ **neutron star matter**

Question: can we have an **anisotropic phase** present inside a **neutron star**?



Chiral Density Wave

- Strongly coupled regime → use **phenomenological model** [Drews, Weise '15 / Fraga, Mata, Pitsinigkos, Schmitt '22]

$$\mathcal{L} = \bar{\psi} \left(i\gamma^\mu \partial_\mu + \gamma^0 \hat{\mu} \right) \psi + \underbrace{\frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma + \frac{1}{2} \partial_\mu \pi_a \partial^\mu \pi^a - U(\sigma, \pi^a)}_{\text{Nucleons}} + \underbrace{\frac{1}{2} \left(m_\omega^2 \omega_\mu \omega^\mu + m_\rho^2 \rho_\mu^3 \rho_3^\mu \right) + \frac{d_\omega}{4} \left(\omega_\mu \omega^\mu \right)^2 + \frac{d_\rho}{4} \left(\rho_\mu^3 \rho_3^\mu \right)^2 + \frac{d_{\omega\rho}}{2} \omega_\mu \omega^\mu \rho_\nu^3 \rho_3^\nu + \dots}_{\text{Mesons}} - \bar{\psi} \left[g_\sigma (\sigma + i\gamma^5 \pi) + \gamma^\mu (g_\omega \omega_\mu + g_\rho \rho_\mu) \right] \psi \underbrace{\hspace{1cm}}_{\text{Interactions}} + \text{Free electrons, muons}$$

- Mean-field approximation: neglect meson fluctuations (we work at $T = 0$)
- Chiral density wave (CDW)**: anisotropic chiral condensate, here

$$\langle \sigma \rangle = \phi \cos(2\vec{q} \cdot \vec{x}), \quad \langle \pi^0 \rangle = \phi \sin(2\vec{q} \cdot \vec{x}) \quad [\text{Nickel '09 / Dautry, Nyman '79 / Heinz, Giacosa, Rischke '15}]$$

- Keep nucleonic Dirac sea contribution [Pitsinigkos, Schmitt '23]

Parameter Fit

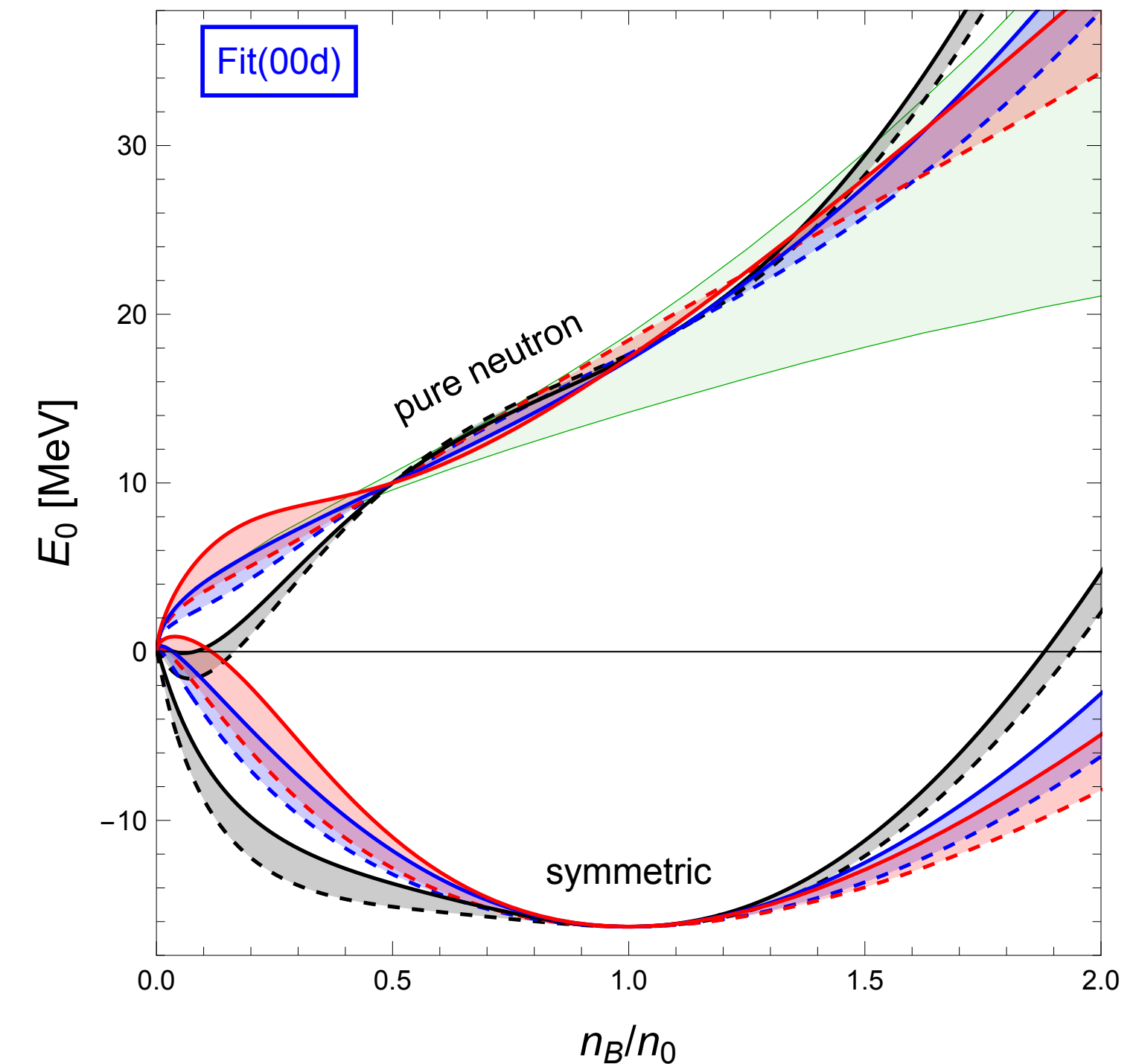
Phenomenological Model → fit model parameters to experimental data:

1. Vacuum
2. Saturation (isospin-symmetric)
3. Pure neutron matter

[Tews, Carlson, Gandolfi, Reddy '18 / Alford, Brodie, Haber, Tews '22]

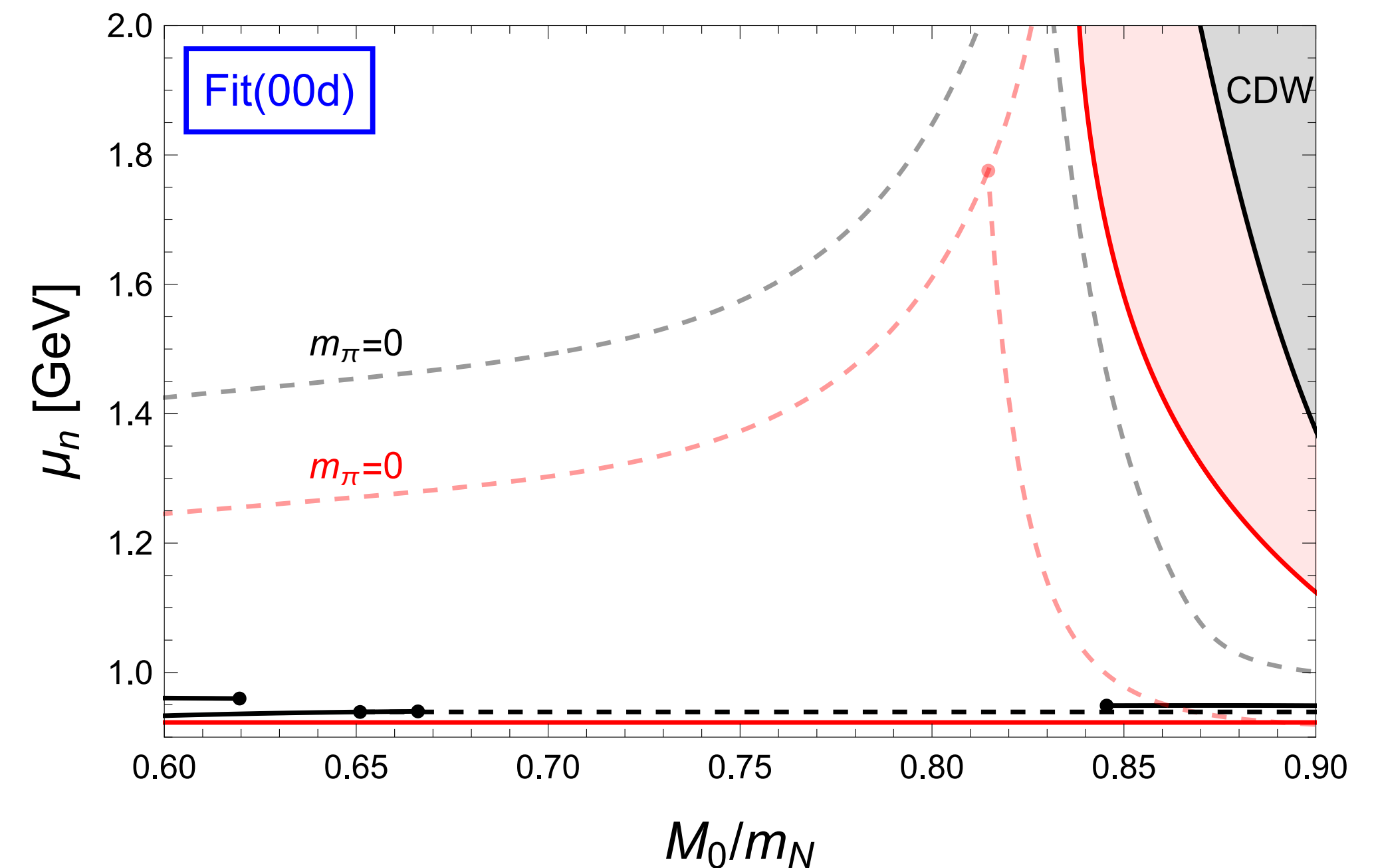
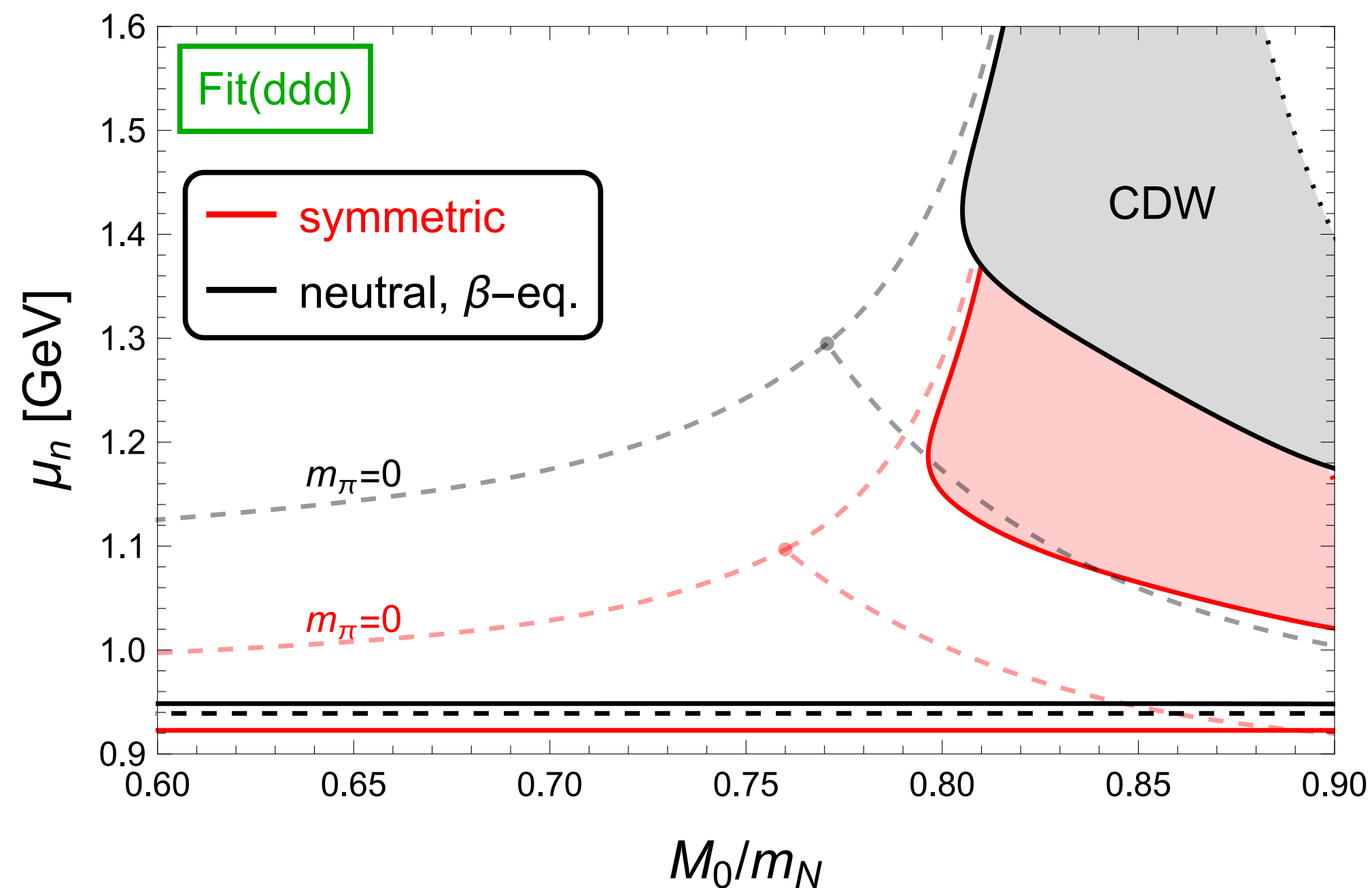
Two distinct fits: Fit(00d) and Fit(ddd)

$$\cdots \text{from } \frac{d_\omega}{4} \left(\omega_\mu \omega^\mu \right)^2 + \frac{d_\rho}{4} \left(\rho_\mu^3 \rho_3^\mu \right)^2 + \frac{d_{\omega\rho}}{2} \omega_\mu \omega^\mu \rho_\nu^3 \rho_3^\nu$$



Extremise w.r.t $\phi, q, \langle \omega_0 \rangle, \langle \rho_0^3 \rangle, \mu_n, \mu_e$: find thermodynamically stable solutions

Effect of Neutron Star Conditions

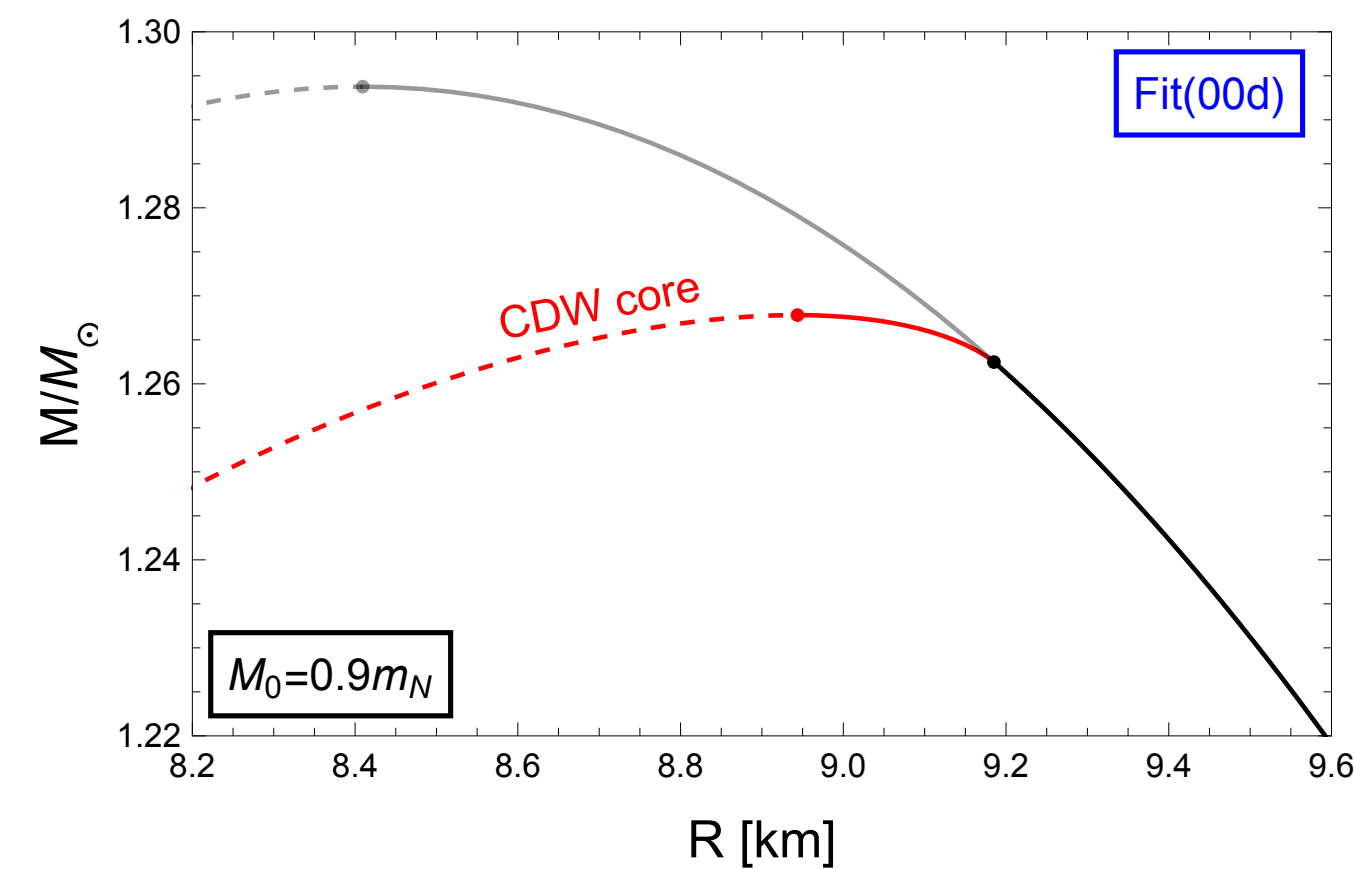


M_0 : nucleon mass at saturation $\in (0.7m_N, 0.8m_N)$

Neutron star conditions $\rightarrow$ CDW less preferred compared to isospin symmetric matter

Constructing Neutron Stars

Stable CDW core

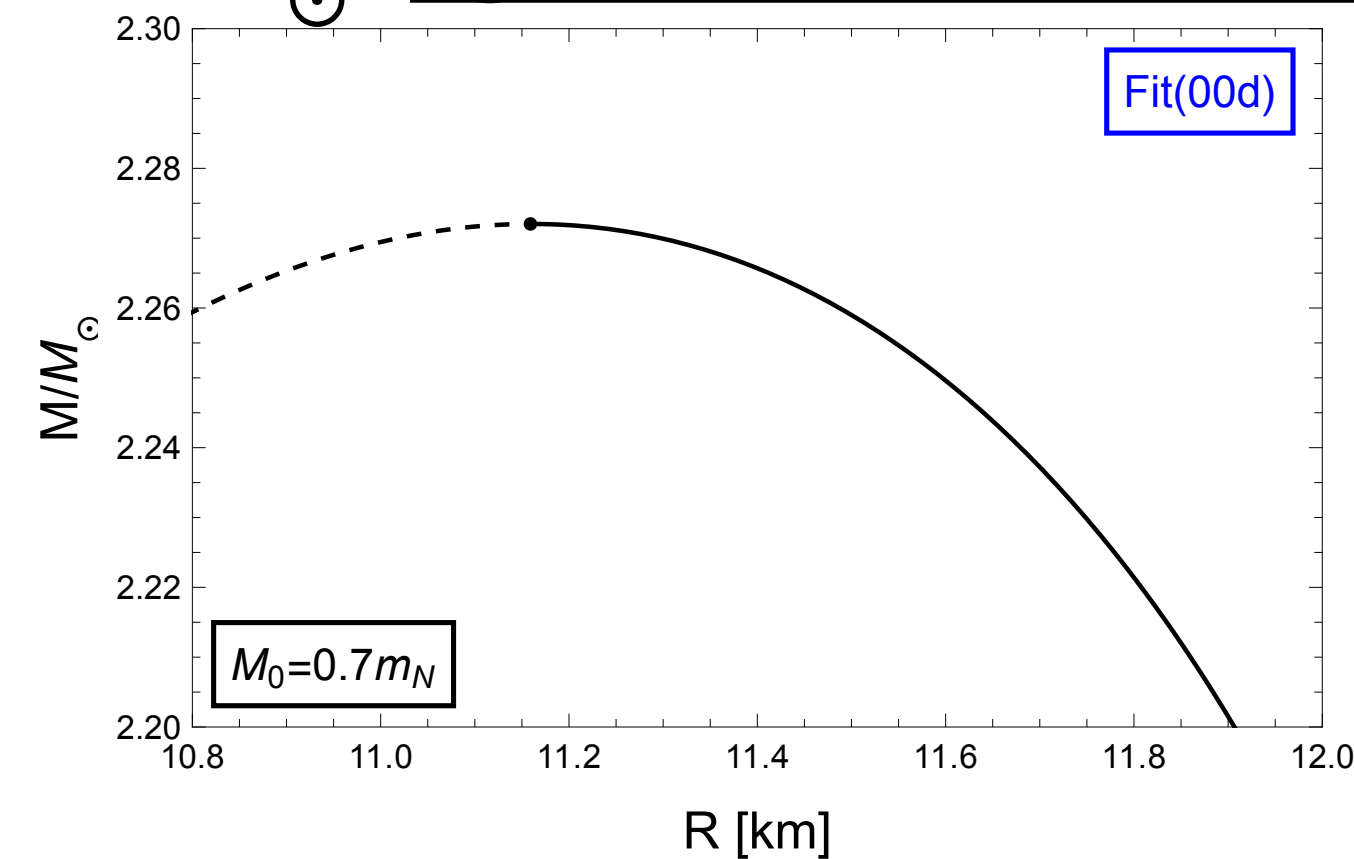


Combine with
TOV equations

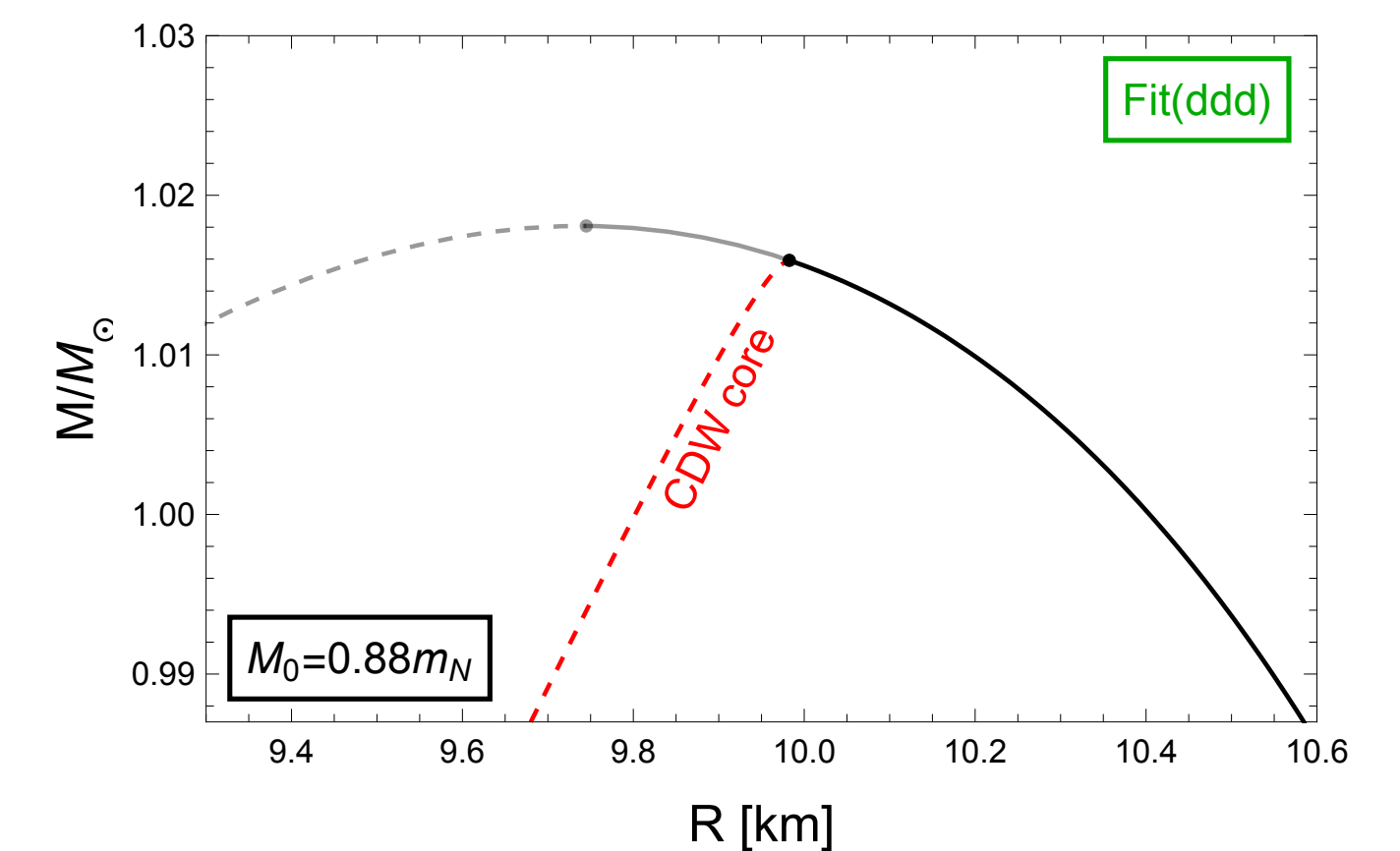


Mass-Radius
curves of stable
neutron stars

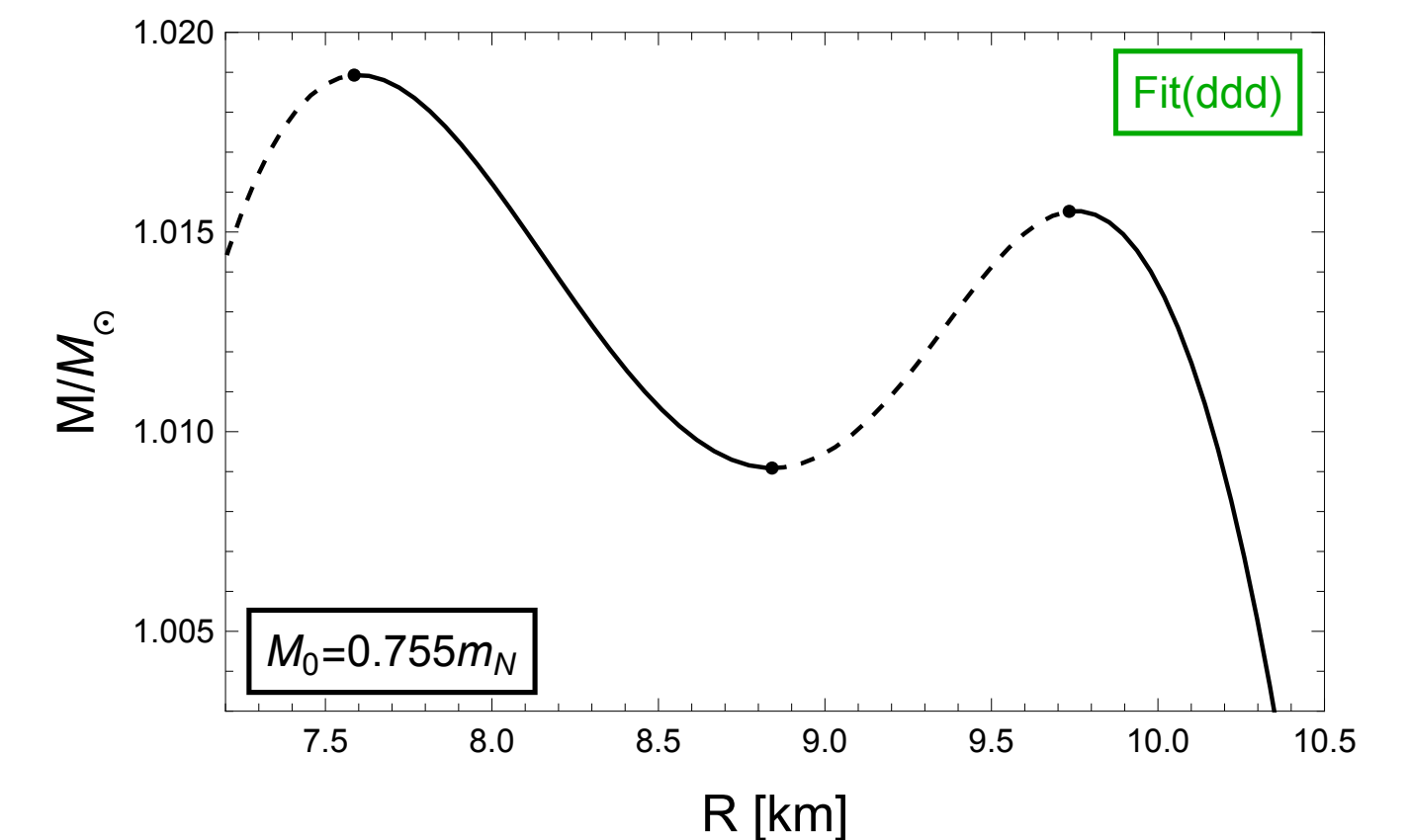
$M > 2M_\odot$ (agree with observations)



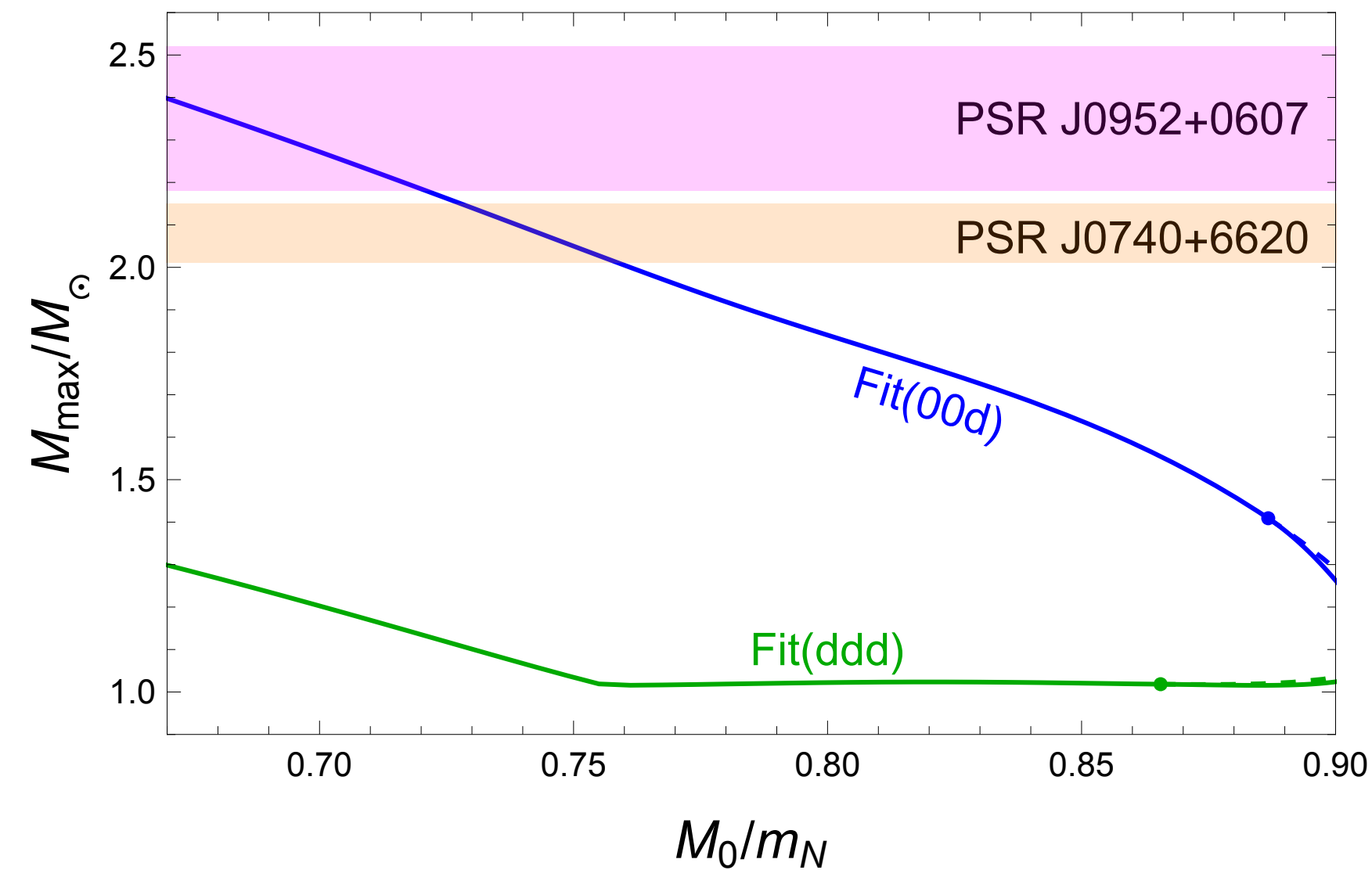
Unstable CDW core



Twin star construction



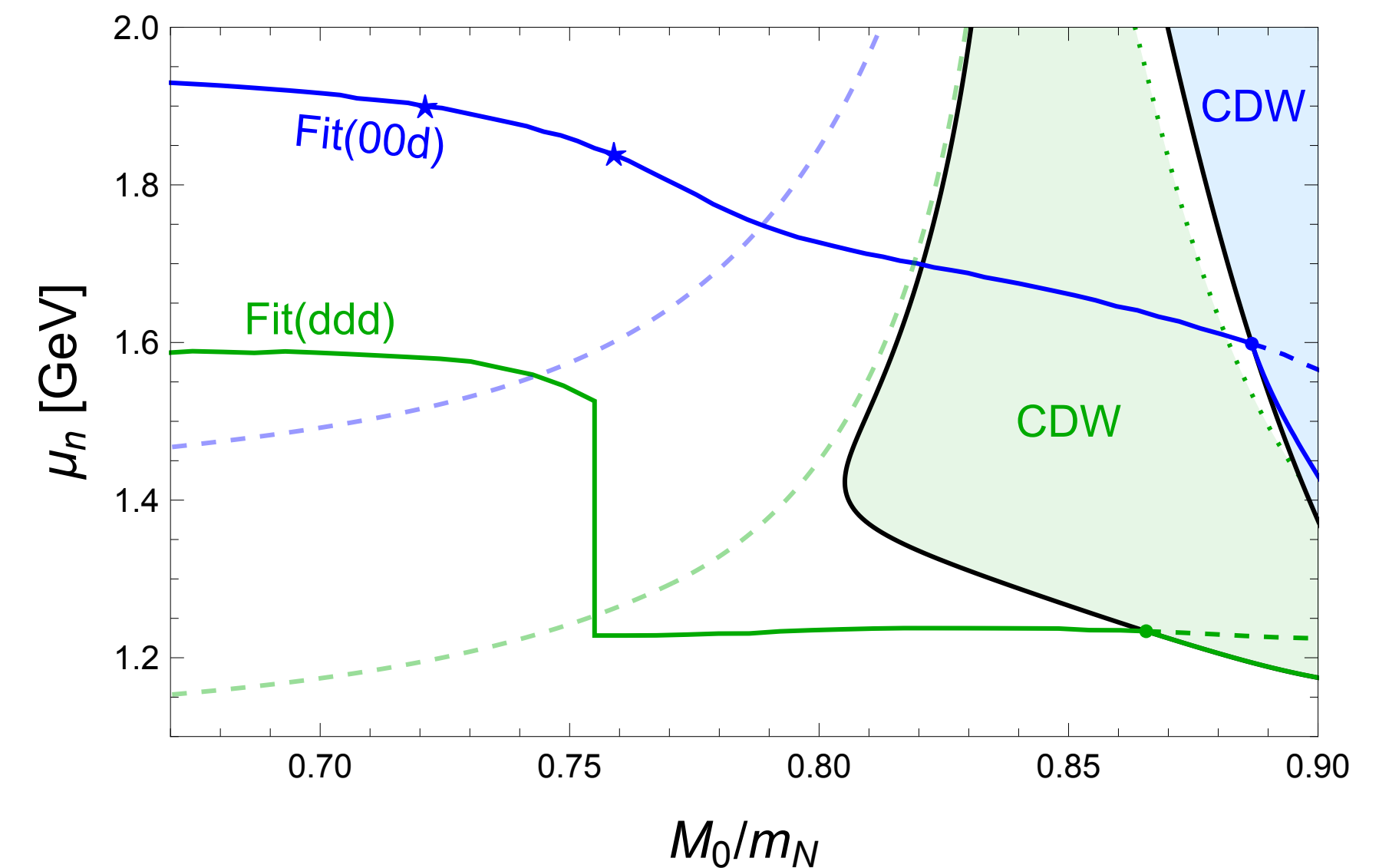
Realistic CDW Stars?



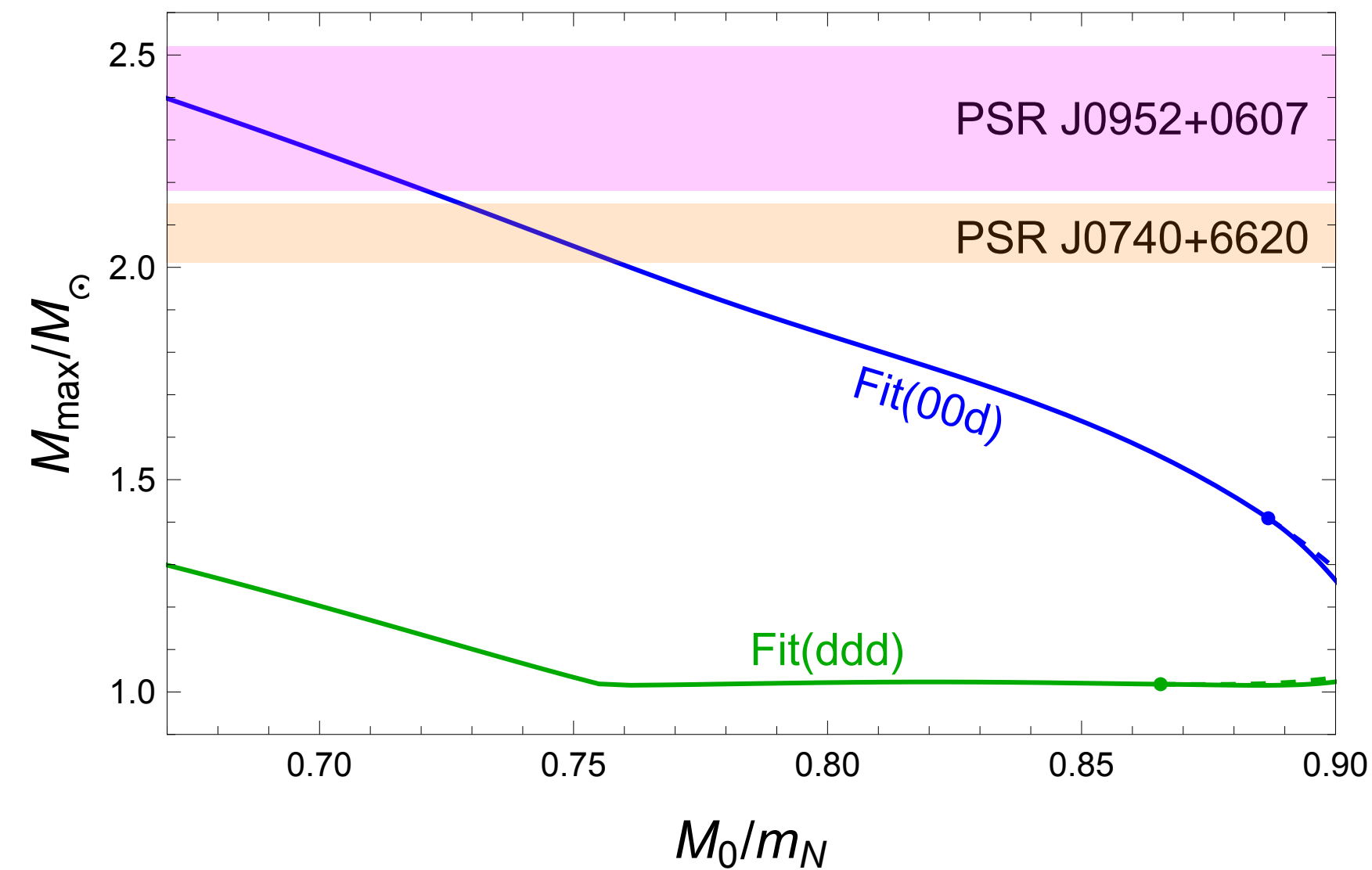
Compare with observations



Fit(00d) can create massive enough stars
(without CDW), Fit(ddd) cannot



Realistic CDW Stars?

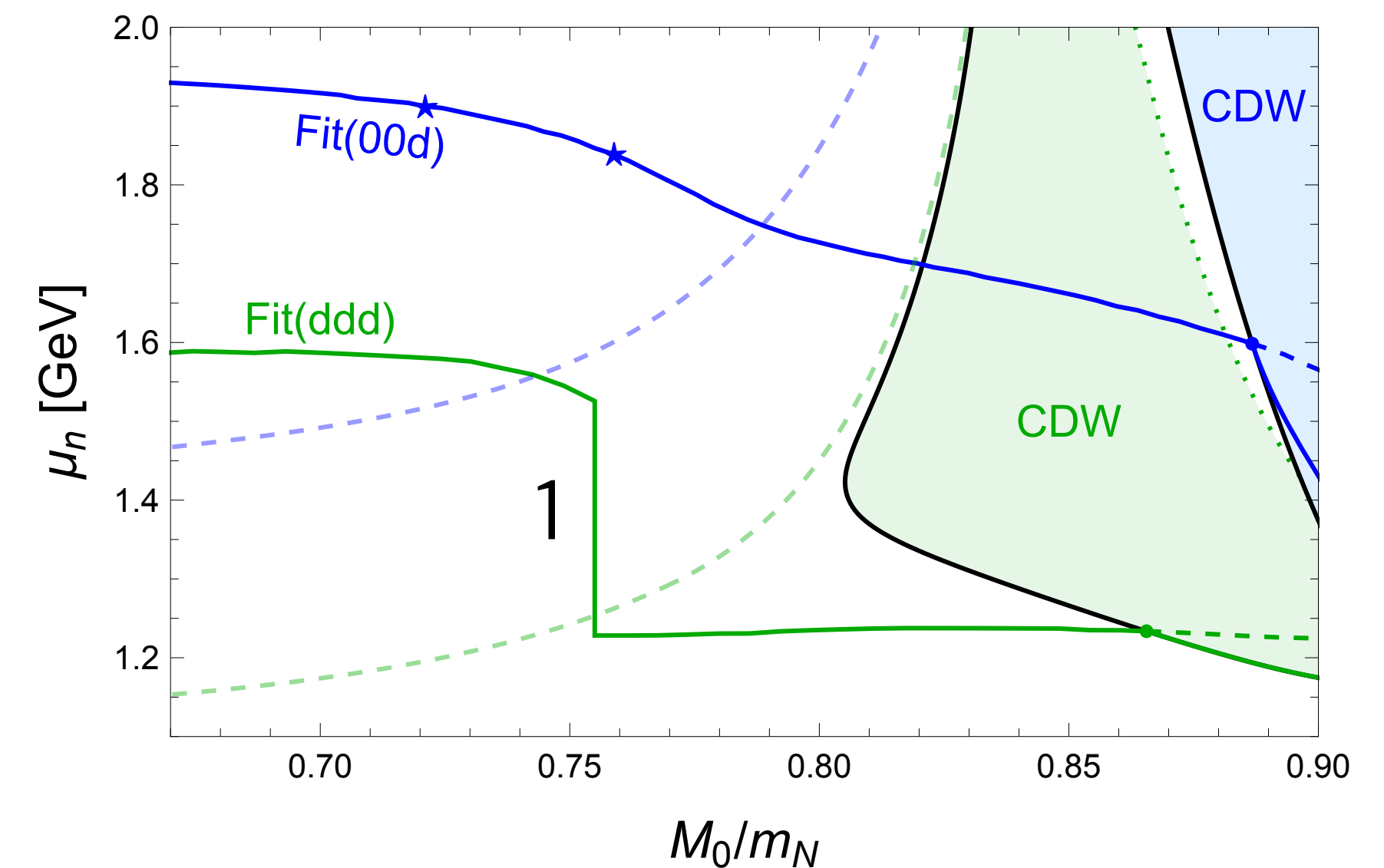


1. Twin star structure

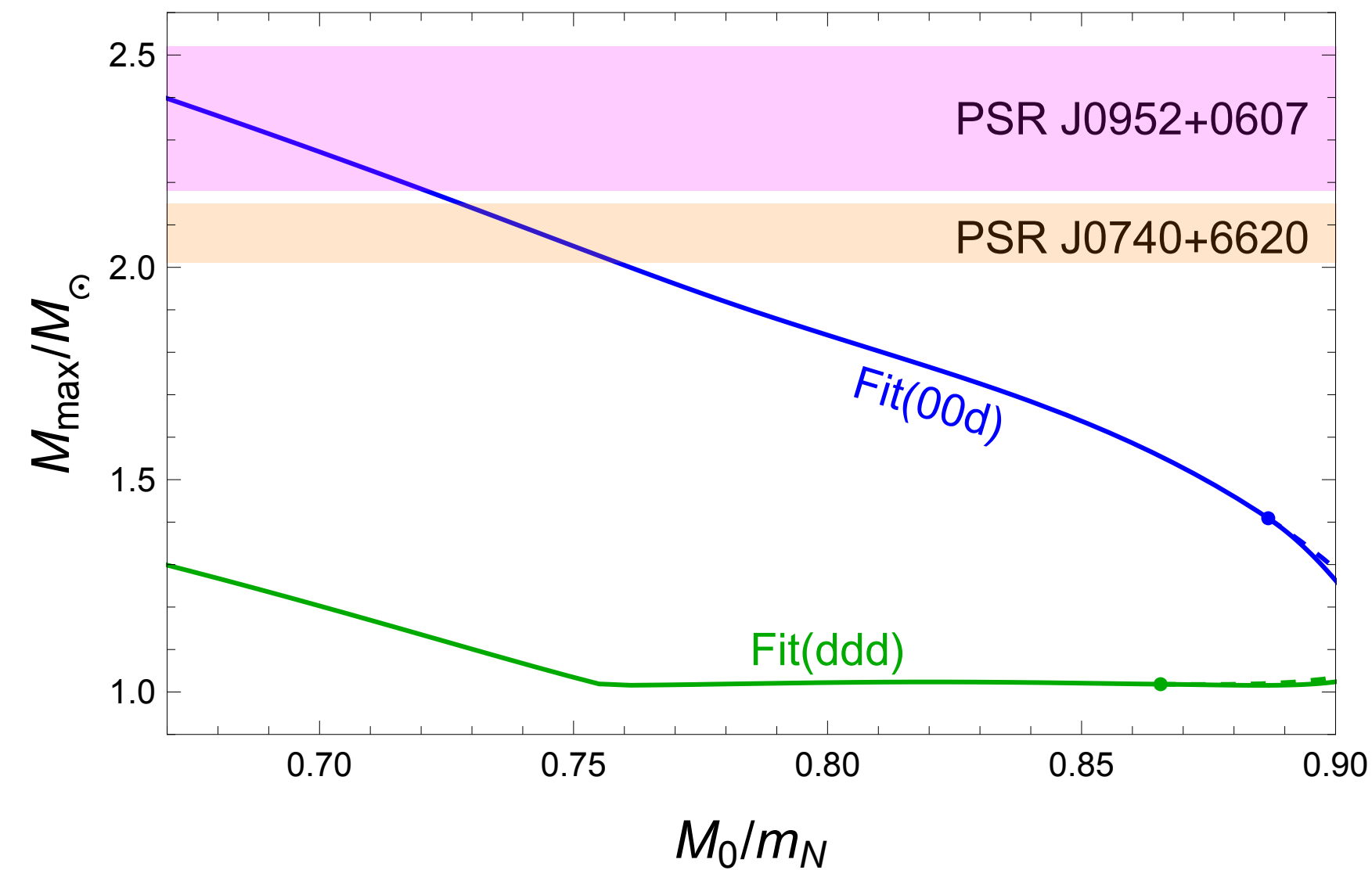
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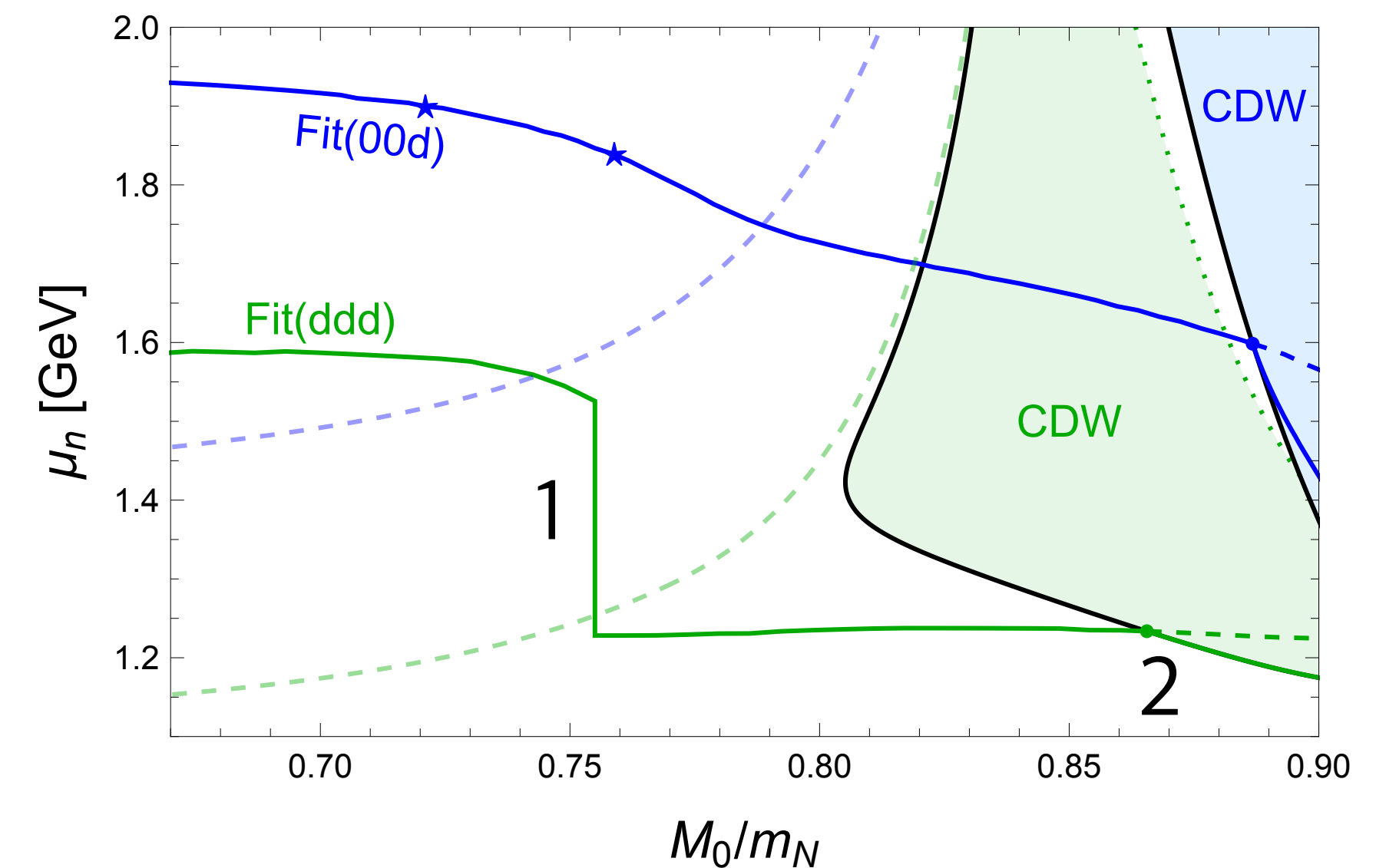


Compare with observations

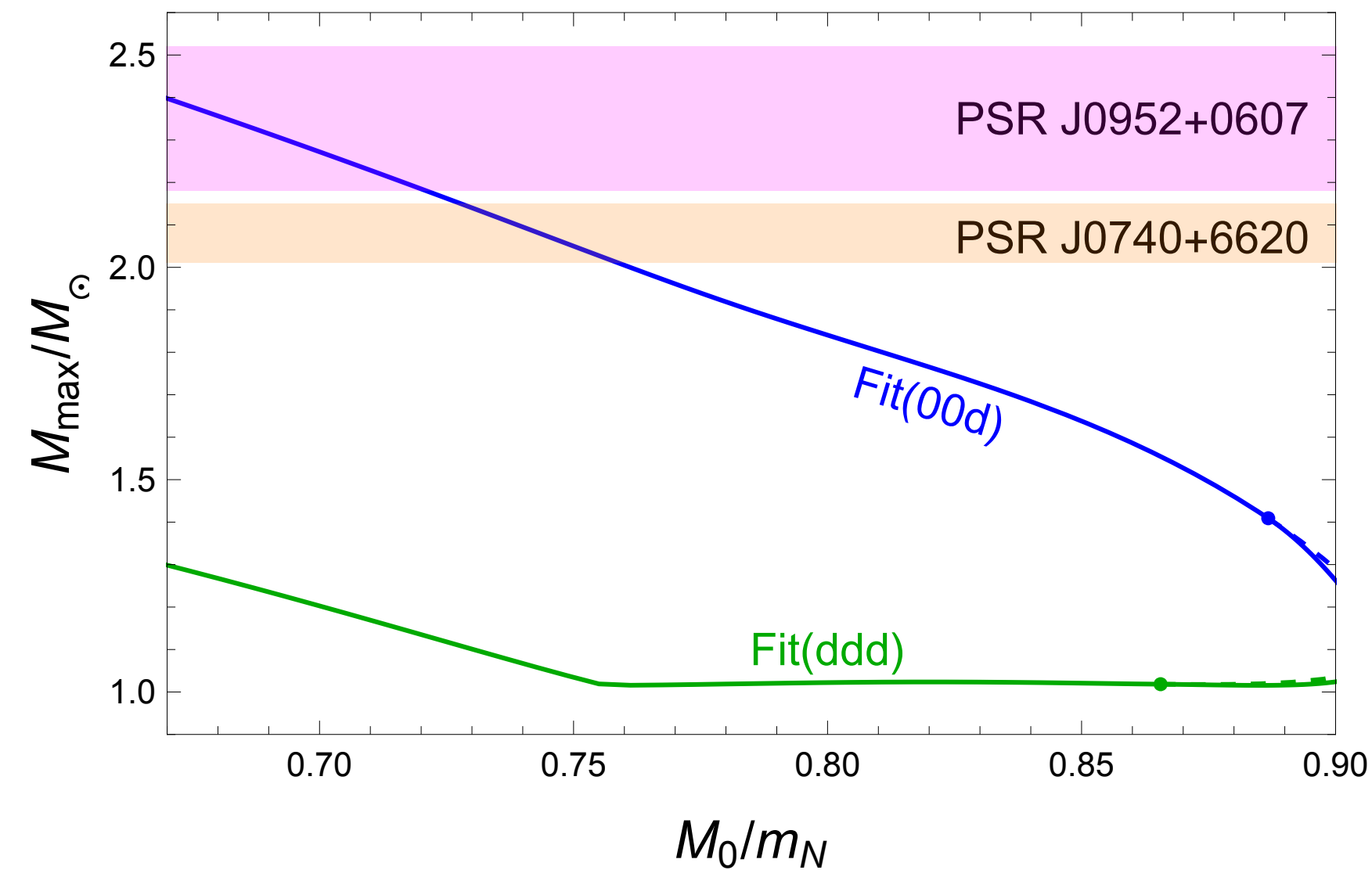


Fit(00d) can create massive enough stars
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1. Twin star structure
2. Unstable stars with CDW cores



Realistic CDW Stars?

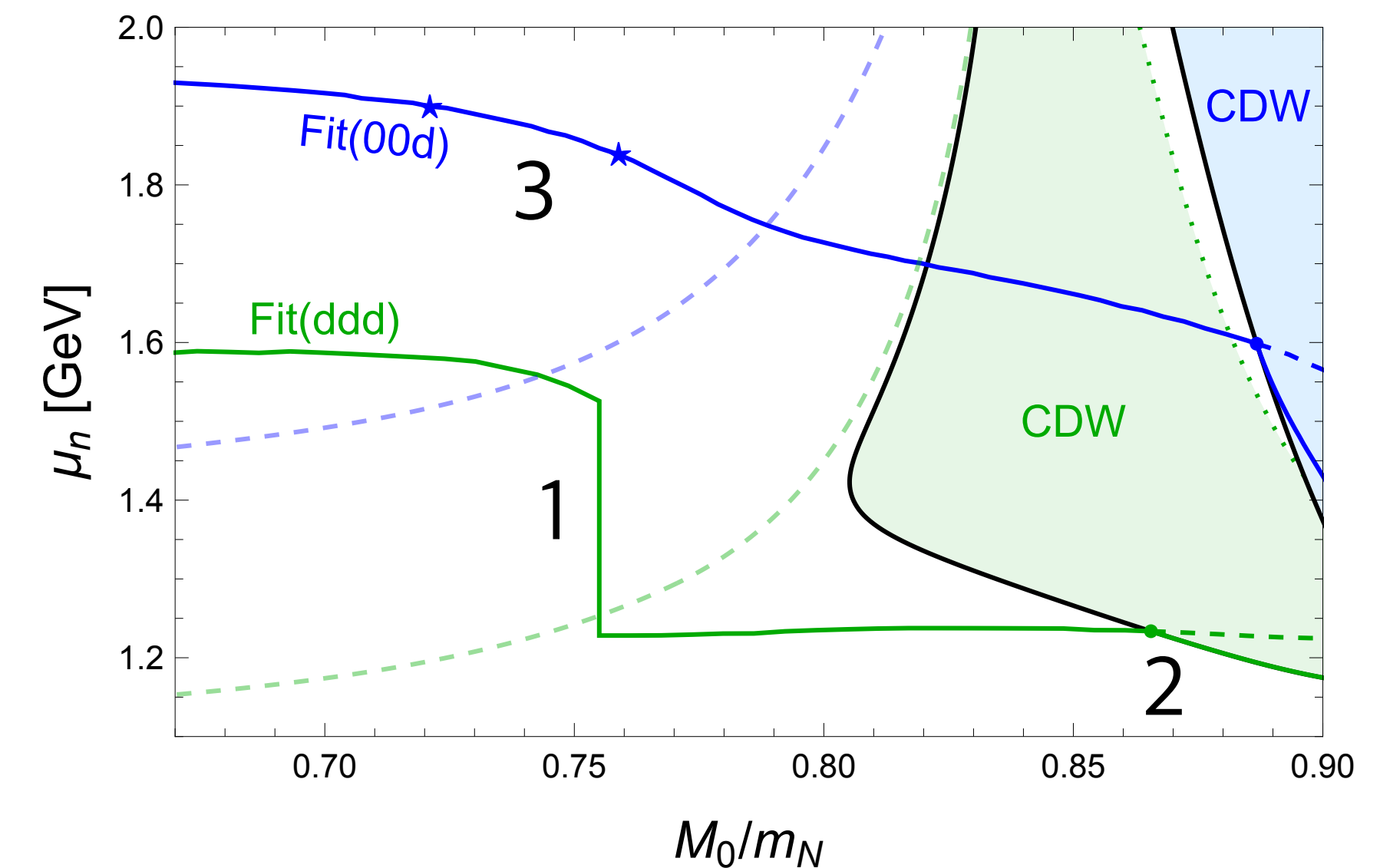


Compare with observations

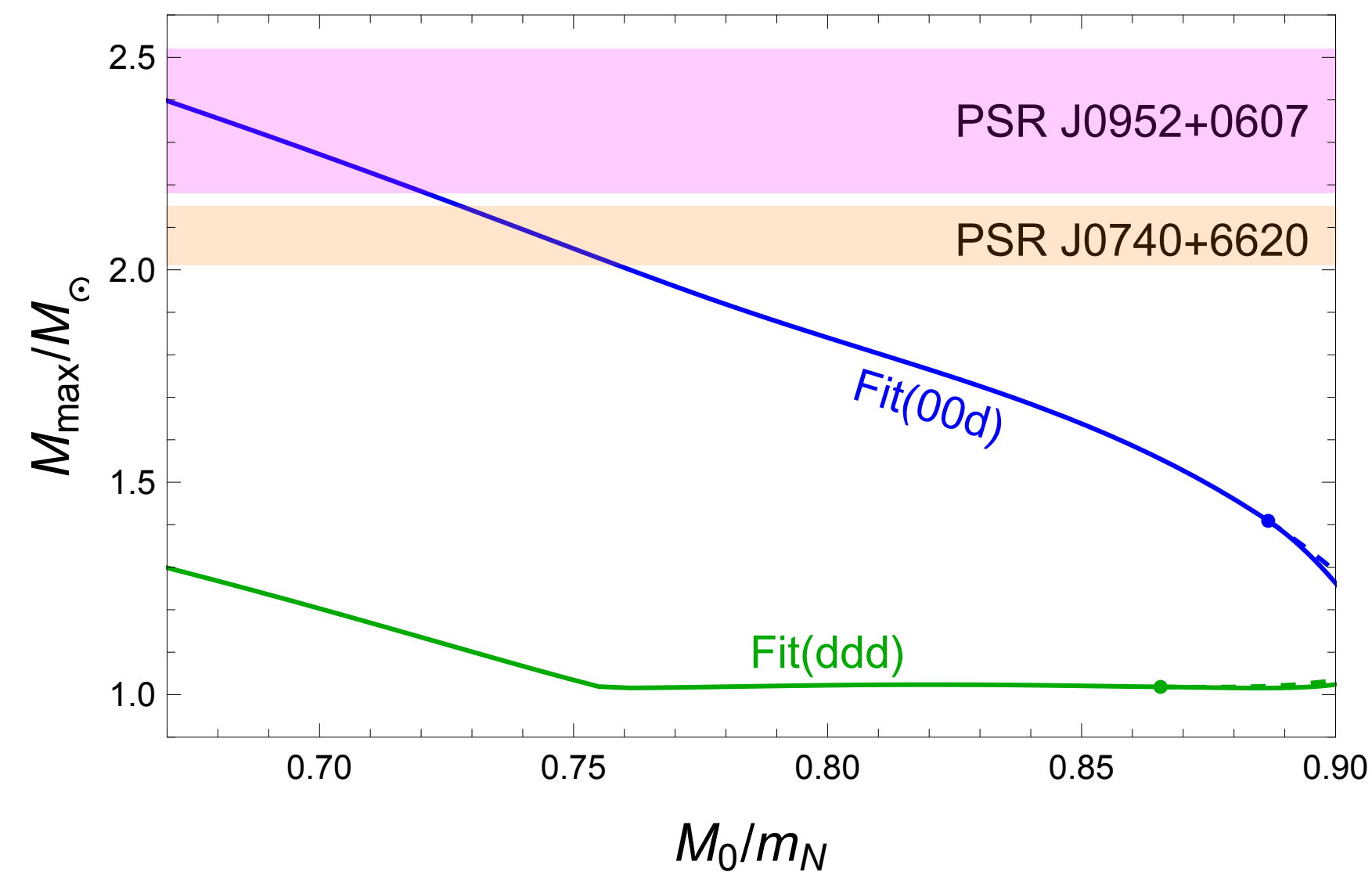


Fit(00d) can create massive enough stars
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1. Twin star structure
2. Unstable stars with CDW cores
3. Agree with observations



Realistic CDW Stars?

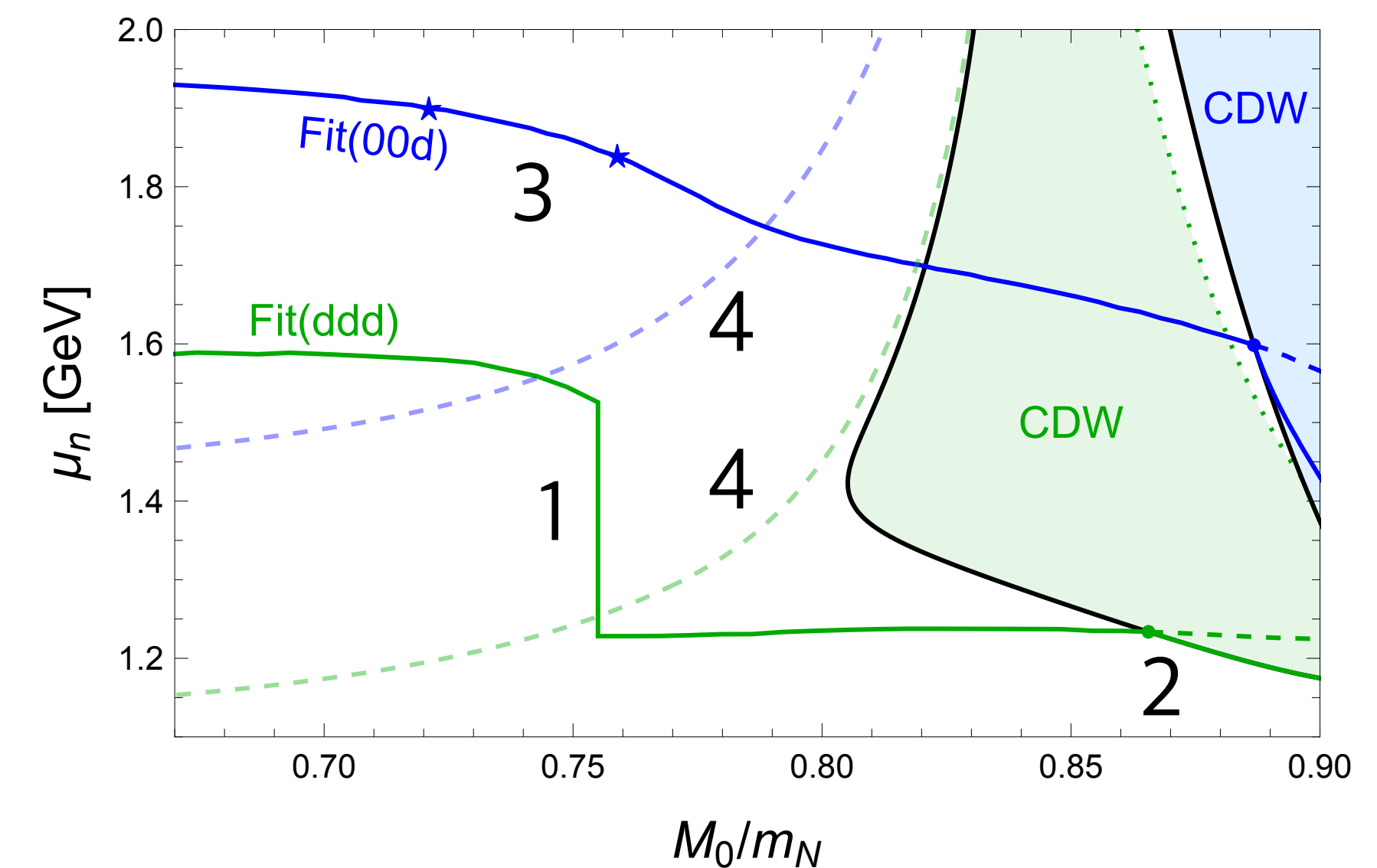


Compare with observations



Fit(00d) can create massive enough stars
(without CDW), **Fit(ddd)** cannot

1. Twin star structure
2. Unstable stars with CDW cores
3. Agree with observations
4. Hybrid star criterion



Summary

- Studied CDW ansatz within nucleon-meson model (with Dirac sea), and constructed neutron stars
- Neutron star conditions disfavour the CDW
- Can construct stars with CDW, although they are not massive enough
- Without CDW, can construct hybrid stars that agree with maximum mass observations

Outlook

- Model dependence: extend to chiral partner model [Fraga, Mata, Schaffner-Bielich '23]
- Add magnetic field: enhances the preference of anisotropic phases [Carignano, Ferrer, de la Incera, Paulucci '15]
- More complicated anisotropic structures [Pisarski, Tsvetlik, Valgushev '20]
- Strongly coupled calculation: use AdS/CFT correspondence [Kovensky, Poole, Schmitt '22 / Ecker, Kovensky, OP, Schmitt '25]

Thank you for your attention!

Grazie mille!