

HEAVY ION COLLISIONS
AND
QUANTUM FIELDS IN AND OUT EQUILIBRIUM

EMMI Workshop on

"Prospects and Challenges for Future Experiments in Heavy Ion Collisions"

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European
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Council

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OUTLINE

Issues

Thermodynamics

Hydrodynamics

Thermalization

Jets and turbulent flow

Summary

ISSUES

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- Initial motivation (*QCD asymptotic freedom, quark-gluon plasma, deconfinement transition, restoration of chiral symmetry, etc*)
- Matter in equilibrium is described by QFT (*at finite temperature and density*)
- Wave functions of nuclei at high energy are given by QF d.o.f. (*partons, color glass fields, etc*)
- Many non equilibrium phenomena in HIC (*thermalization, fluctuations, jets, etc*)
- Theoretical tools (*pert. theory, lattice, 'analytic' non perturbative methods, AdS/CFT, etc*)

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Note: QCD is important mainly in early stages of high energy collisions

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- Phase diagram, with many control parameters (T , μ 's, m_q 's, N_f , N_c , ..., B , etc)
- Temperature-density phase diagram not fully understood (*critical end point ?*)
- High temperature phase is well understood ($T > 3T_c$) in terms of weak coupling expansions (*weakly coupled massive quasiparticles*).
- Vicinity of T_c : some understanding in terms of Euclidean concepts (*Polyakov loop, etc*). Physical d.o.f. ?
- Beyond perturbation theory with non perturbative RG, DSE. Also progress in 'IR QCD' (*Landau gauge*).

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Note: activity with its own 'dynamics'. Contact with HIC ?

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Viscosity puzzle: - *small ratio of viscosity to entropy density, and early thermalization, suggest strong coupling*

- *naturally explained by AdS/CFT*
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Plasma: *soft and hard modes, particles and fields. Long wavelength modes can remain strongly coupled....*

THERMALIZATION

- How do we go from the initial nuclear wave-functions to the locally equilibrated fluid seen in experiments ?
- What are the initial d.o.f.'s : partons ? color fields (CGC)? mixture of both ?
- Initial fields are typically unstable (e.g. if anisotropic momentum distributions of particles). Instabilities provide 'fast' isotropization of momentum distributions
- Amplification of soft modes is a generic feature
- CGC picture suggests an overpopulation of soft modes

The overpopulated plasma

Initial conditions ($t_0 \sim 1/Q_s$)

$$\epsilon_0 = \epsilon(\tau = Q_s^{-1}) \sim \frac{Q_s^4}{\alpha_s} \quad n_0 = n(\tau = Q_s^{-1}) \sim \frac{Q_s^3}{\alpha_s} \quad \epsilon_0/n_0 \sim Q_s$$

overpopulation parameter

$$n_0 \epsilon_0^{-3/4} \sim 1/\alpha_s^{1/4}$$

In equilibrated quark-gluon plasma

$$\epsilon_{\text{eq}} \sim T^4 \quad n_{\text{eq}} \sim T^3 \quad n_{\text{eq}} \epsilon_{\text{eq}}^{-3/4} \sim 1$$

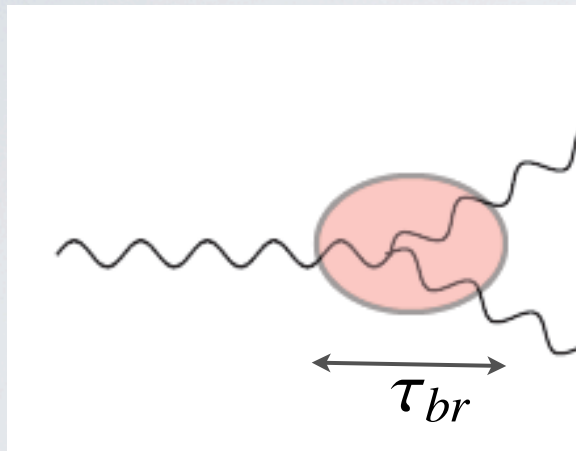
mismatch by a large factor (at weak coupling) $\alpha_s^{-1/4}$

Will the system accommodate the particle excess by forming a Bose-Einstein condensate?

(JPB, F. Gelis, J. Liao, L. McLerran, R. Venugopalan, 2012)

JETS AND TURBULENT FLOW

Medium induced gluon radiation (BDMPS-Z theory)



$$\frac{1}{\tau_{br}} \sim \frac{k_{\perp}^2}{2\omega}$$

$$k_{\perp}^2 \sim \hat{q} \tau_{br}$$

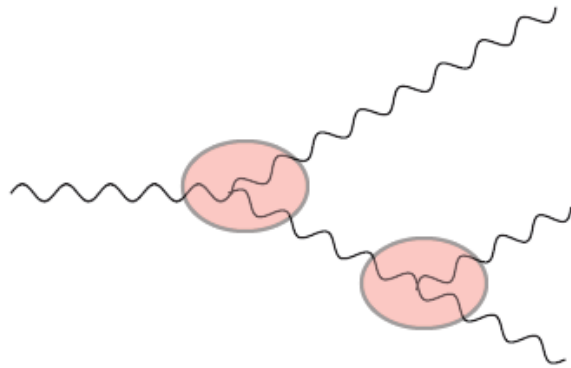
$$\tau_{br} \sim \sqrt{\frac{2\omega}{\hat{q}}}$$

$$\theta_{br} \sim \frac{k_{\perp}}{\omega} \sim \left(\frac{2\hat{q}}{\omega^3}\right)^{1/4}$$

Energy loss is dominated by a single emission with maximum energy

Multiple gluon branching can be important, and contribute to transport soft gluons towards large emission angles

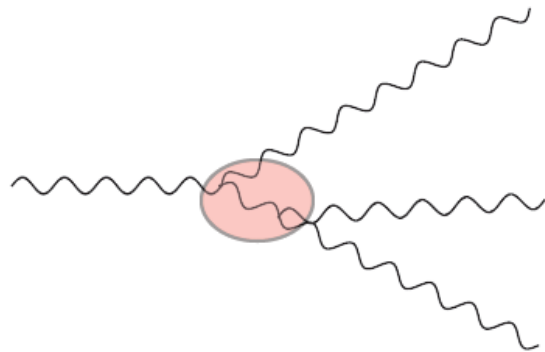
Independent emissions are enhanced by a factor L/τ_f



A Feynman diagram illustrating two independent emissions. A horizontal wavy line (representing a quark) enters from the left. It splits into two paths, each passing through a red circular vertex. From each vertex, a wavy line (representing a gluon) is emitted. The two paths then recombine into a single horizontal wavy line exiting to the right.

$$\sim \left(\alpha_s \frac{L}{t_f} \right)^2$$

Interference effects are subleading

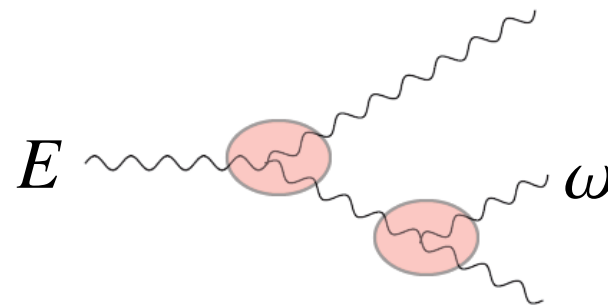


A Feynman diagram illustrating interference effects. A horizontal wavy line (representing a quark) enters from the left and passes through a red circular vertex. From this vertex, a wavy line (representing a gluon) is emitted. The quark line then splits into two paths, each passing through a red circular vertex. From each vertex, a wavy line (representing a gluon) is emitted. The two paths then recombine into a single horizontal wavy line exiting to the right.

$$\sim \alpha_s^2 \frac{L}{t_f}$$

JPB, F. Dominguez, E. Iancu, Y.
Mehtar-Tani, arXiv: 1209.4585

QCD cascade of a new kind



$$D(x, \tau) \equiv x \frac{dN}{dx}$$

$$x = \frac{\omega}{E}$$

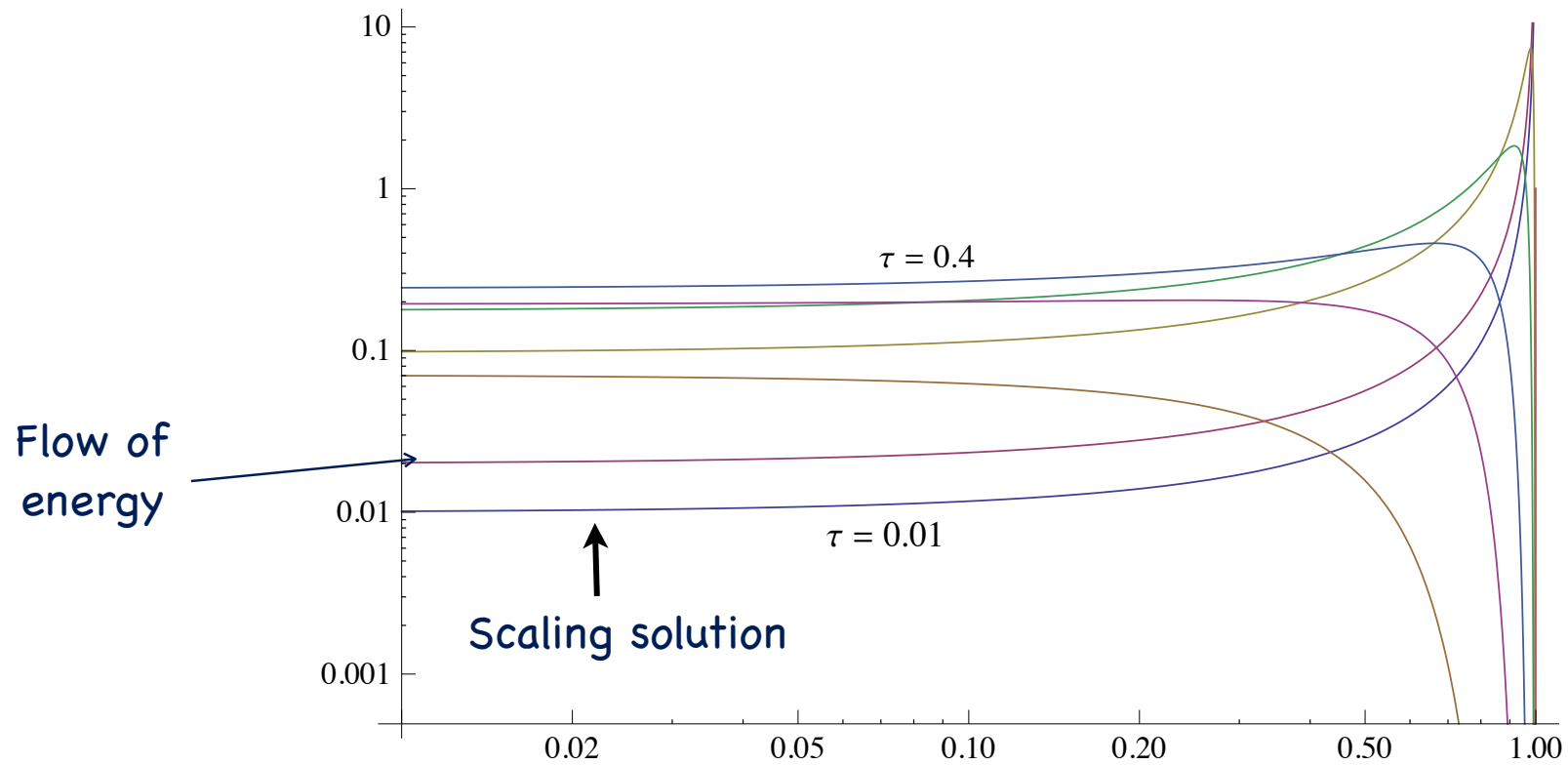
$$\frac{\partial D(x, \tau)}{\partial \tau} = \int dz \mathcal{K}(z) \left[\sqrt{\frac{z}{x}} D\left(\frac{x}{z}, \tau\right) - \frac{z}{\sqrt{x}} D(x, \tau) \right]$$

$$\mathcal{K}(z) = \frac{\bar{\alpha}}{2} \frac{f(z)}{[z(1-z)]^{3/2}}, \quad f(z) = [1 - z(1-z)]^{5/2}$$

Two features

- radiation (transport of momentum from hard to soft)
- turbulent flow (wave turbulence, nearly local interactions in momentum space = 'quasi-democratic' branching)

$$\sqrt{x}D(x, \tau)$$



$$\mathcal{E}_{\text{flow}} = E \frac{v\tau^2}{2} = \frac{v}{2} \bar{\alpha}^2 \omega_c \quad \omega_c \equiv \frac{\hat{q}L^2}{2} \quad v \simeq 5$$

Estimate

$$\hat{q} = 1 \text{ GeV}^2/\text{fm} \quad \omega_c \simeq 40 \text{ GeV} \quad \bar{\alpha}^2 \simeq 0.1 \quad \mathcal{E}_{\text{flow}} \simeq 15 \text{ GeV}$$

$$L = 4 \text{ fm}$$

from J.-P. B., E. Iancu, Y. Mehtar-Tani, arXiv: 1301.6102

SUMMARY

- nice interplay between QFT and the physics of heavy ion collisions
- new phenomena are being predicted (and perhaps even seen)