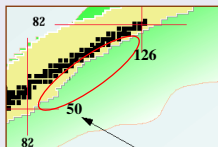


# Model predictions for deep inelastic reactions: towards high Z and A.

Giovanni POLLAROLO

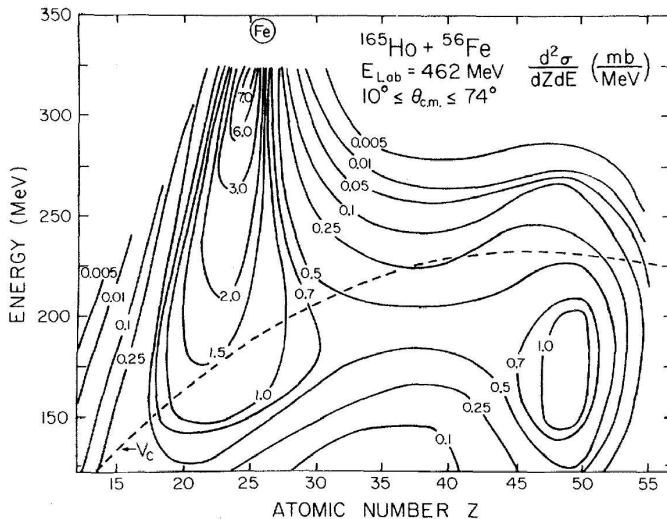
*Dipartimento di Fisica, Università di TORINO  
e INFN Sezione di Torino*



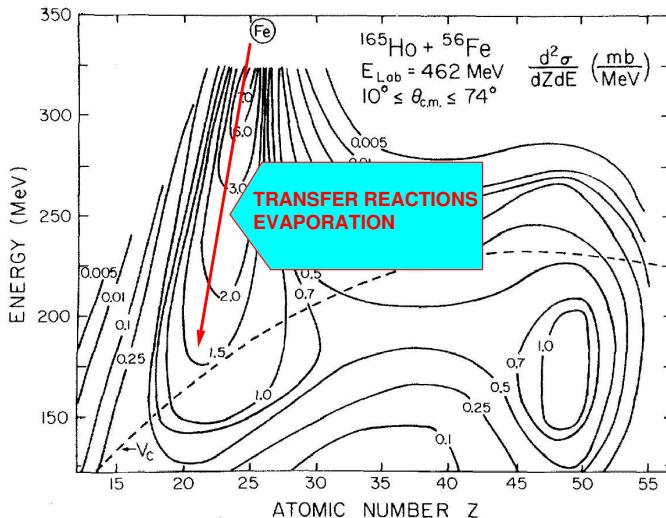
NUSTAR Annual Meeting At GSI, Darmstadt, Germany  
February 25th - March 1st 2013



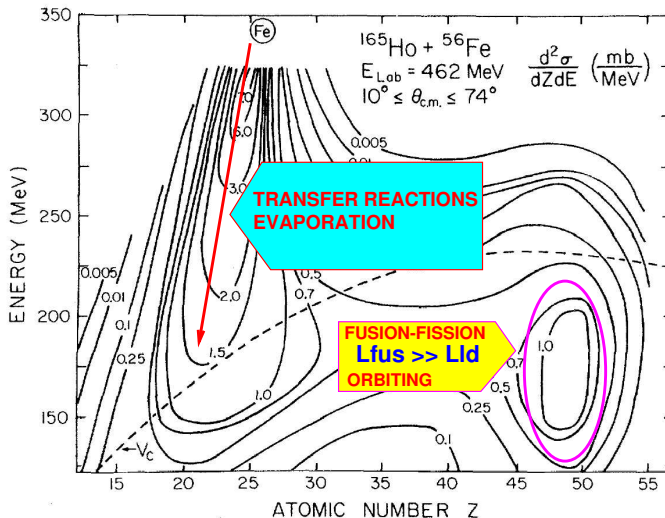
# HI reactions, a short overview



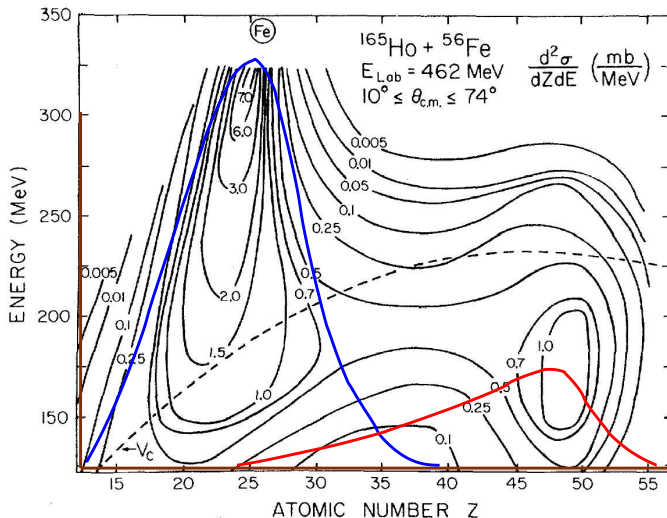
# HI reactions, a short overview



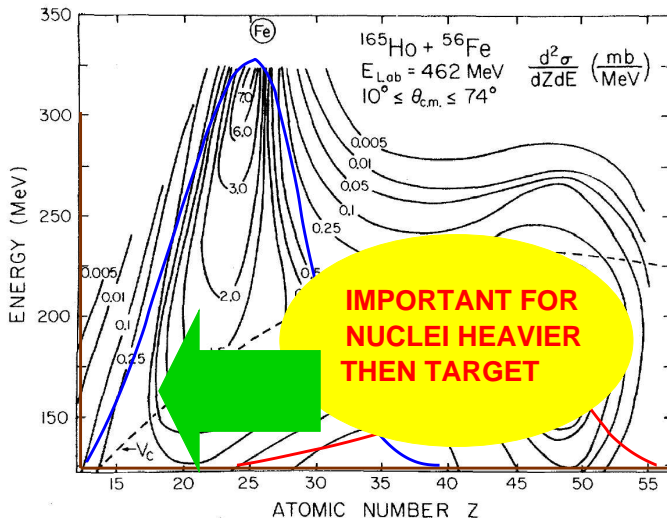
# HI reactions, a short overview



# HI reactions, a short overview



# HI reactions, a short overview



# The model - surface modes

To explain the large deformations of the fragments prior the separation one has to introduce degrees of freedoms **describing the shape of the fragments**.

This is usually done by introducing:

Surface degrees of freedom (*collision time*  $\tau = \sqrt{a/\ddot{r}_o}$ )

- INELASTIC**  $f_{in}(r) \sim e^{-r/a_{in}}$   $a_{in} = 0.65 \text{ fm}$   
 (few channels but strong)
    - low lying: mass (D) large  
force (C) small
    - high lying: mass (D) small  
force (C) large
- NON adiabatic coupled-channels**  
adiabatic

Of course also the exchange of nucleons is important-TRANSFER



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Of course also the exchange of nucleons is important-**TRANSFER**



# The model - transfer

The exchange of nucleons is characterized by the presence of channels that are **weak but very numerous**. The transfer process is governed by:

- a matrix element of the form:

$$M_{\beta\alpha'} \sim \int d^3r' \psi_{i'}^\dagger(\vec{r}') V_a(|\vec{r}'|) \psi_j(\vec{R} - \vec{r}') \propto e^{-\kappa_{tr}R}$$

Where  $V_a$  is the shell model potential binding the nucleon to the projectile or target (post/prior symmetry). The range parameter  $\kappa_{tr}$  is related to the binding-energy  $\mathcal{E}$  of the nucleon

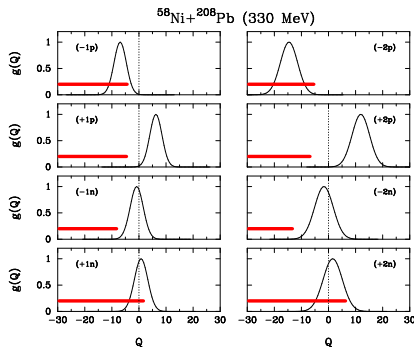
$$\kappa_{a'_1} = \frac{1}{\hbar} \sqrt{2m_o(-\mathcal{E}_{a'_1})} \sim 0.6\text{fm}$$



# The model - transfer

- Optimun Q-value conditions:

$$P_{\beta\alpha'} \sim |M_{\beta\alpha'}(r_o)|^2 \exp\left(-\frac{(Q - Q_{opt})^2}{\hbar^2 \ddot{r}_o \kappa_{a'_1}}\right)$$



# GRAZING

The time evolution of a heavy-ion reaction is described by the following system of coupled equations :

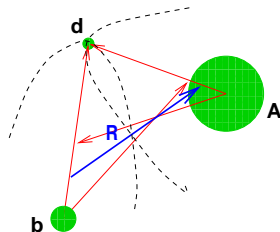
$$i\hbar\dot{c}_\beta(t) = \sum_{\alpha} \langle \beta | H_{int} | \alpha \rangle c_{\alpha}(t) e^{\frac{i}{\hbar}(E_{\beta}-E_{\alpha})t + i(\delta_{\beta}-\delta_{\alpha})}$$

$$i\hbar\dot{\Psi}(t) = (H_0 + H_{int})\Psi(t)$$

$$\Psi(t) = \sum_{\beta} c_{\beta}(t) \psi_{\beta} e^{\frac{i}{\hbar}E_{\beta}t}$$

where  $\psi_{\alpha}$  are the channels wave function (asymptotic states)

$$\psi_{\alpha}(t) = \psi^a(t) \psi^A(t) e^{i\delta(\vec{R})}$$

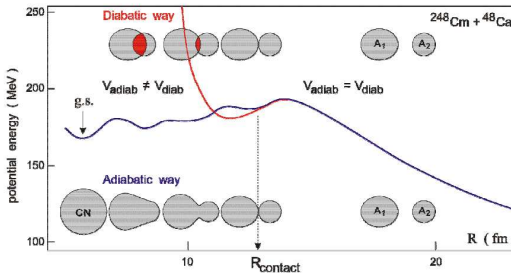


A. Winther Nucl.Phys. **A572** (1994)191, Nucl.Phys. **A594** (1995)203



# The potential (frozen-density, diabatic)

$$V_{\text{diabat}}(R, \beta_1, \beta_2, \alpha, \dots) = V_{12}^{\text{folding}}(Z_1, N_1, Z_2, N_2; R, \beta_1, \beta_2, \dots) + M(A_1) + M(A_2) - M(\text{Proj}) - M(\text{Targ})$$



$$V_{\text{adiabat}}(R, \beta_1, \beta_2, \eta, \dots) = M_{\text{TCSM}}(R, \beta_1, \beta_2, \eta, \dots) - M(\text{Proj}) - M(\text{Targ})$$

Time-dependent driving potential has to be used

$$V(t) = V_{\text{diab}}(\xi) \cdot \exp\left(-\frac{t_{\text{int}}}{\tau_{\text{relax}}}\right) + V_{\text{adiab}}(\xi) \cdot \left[1 - \exp\left(-\frac{t_{\text{int}}}{\tau_{\text{relax}}}\right)\right]$$

$$\tau_{\text{relax}} \sim 10^{-21} \text{ s}$$

*the same degrees of freedom ( $\xi = R, \theta, \varphi_1, \varphi_2, \beta_1, \beta_2, \eta_Z, \eta_N$ )!  
All forces,  $F_i(t) = -\partial V / \partial \xi_i$ , are quite smooth*

Borrowed from Valery Zagrebaev (IRIS10 Workshop, March 2010)



# The actinides (Cm target)

PHYSICAL REVIEW C

VOLUME 33, NUMBER 6

JUNE 1986

## Production of cold target-like fragments in the reaction of $^{48}\text{Ca} + ^{248}\text{Cm}$

H. Gäggeler,\* W. Brüche, M. Brügger, M. Schädel, K. Sümmerer, and G. Wirth  
*Gesellschaft für Schwerionenforschung, D-6100 Darmstadt, Federal Republic of Germany*

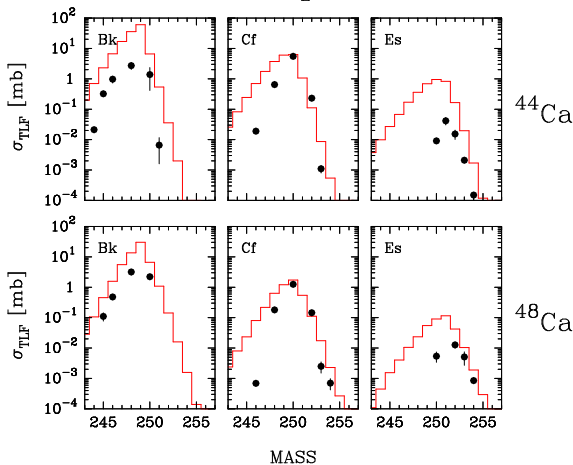
J. V. Kratz, M. Leeb, Th. Bleich, G. Harmann,† N. Hildebrand, and N. Trautmann

99	Es247 4.55 m (7/2+)	Es248 27 m (2-,0+)	Es249 102.2 m 7/2(+)	Es250 8.6 h (6+)	Es251 33 h (3/2-)	Es252 471.7 d (5-)	Es253 20.47 d 7/2+	Es254 275.7 d (7+)	Es255 39.8 d (7/2+)	Es256 25.4 m (1+)	Es257
	EC,α	EC,α	EC,α	EC,α	EC,α	EC,β,α,...	α,sf	EC,β,α,...	β,α,sf,...	β	
98	Cf246 35.7 h 0:	Cf247 3.11 h (7/2-)	Cf248 333.5 d 0:	Cf249 351 y 9/2-	Cf250 13.08 y 0:	Cf251 898 y 1/2:	Cf252 2.645 y 0:	Cf253 17.81 d (7/2-)	Cf254 60.5 d 0:	Cf255 85 m (9/2-)	Cf256 12.3 m 0:
	EC,α,sf,...	EC,α	α,sf	α,sf	α,sf	α	α,sf	β,α	α,sf	β	β,α,sf,...
97	Bk245 4.94 d 3/2-	Bk246 1.80 d 2(-)	Bk247 1380 y (3/2-)	Bk248 9 y (6+)	Bk249 320 d 7/2+	Bk250 3.217 h 2-	Bk251 55.6 m (3/2-)	Bk252	Bk253	Bk254	
	EC,α	EC,α	α	α	β,α,sf,...	β	β,α				
96	Cm244 18.10 y 0+ *	Cm245 8500 y 7/2+	Cm246 4730 y 0+ *	Cm247 1.56E+5 y 9/2-	Cm248 3.40E+5 y 0+ *	Cm249 4.15 m 1/2(+)	Cm250 9000 y 0+ *	Cm251 16.8 m (1/2+)	Cm252 2 d 0+ *		
	α,sf	α,sf	α,sf	α	α,sf	β	β,α,sf,...	β	β		
	Am243 7370 y 5/2-	Am244 10.1 h (6-)	Am245 2.05 h (5/2+)	Am246 39 m (7-)	Am247 23.6 m (5/2)	Am248	Am249				
	α,sf	β	β	β	β						



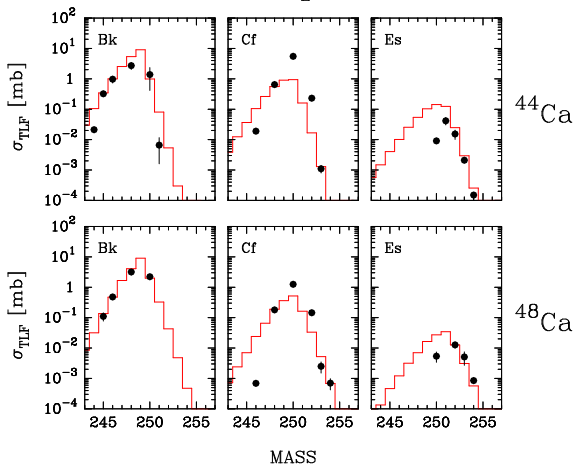
# The actinides (Cm target)

$^{44,48}\text{Ca} + ^{248}\text{Cm}$  ( $E_L = 5-7$  MeV/A)



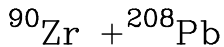
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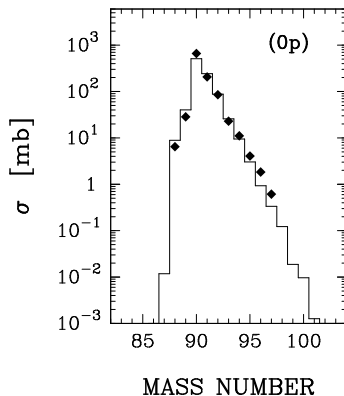




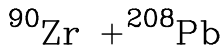
# The $^{90}\text{Zr} + ^{208}\text{Pb}$ system



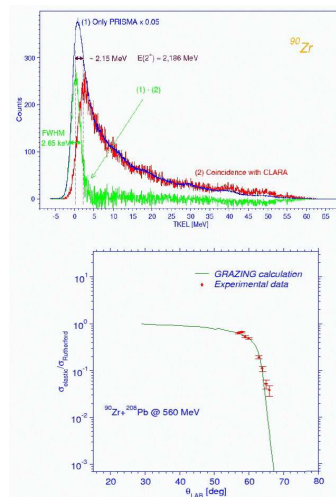
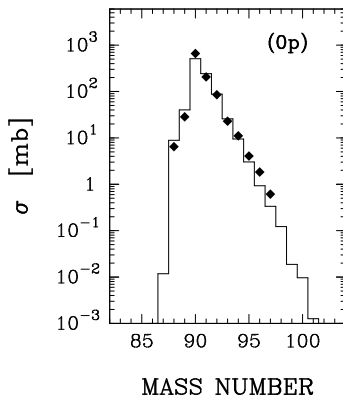
$$E_{\text{lab}} = 560 \text{ MeV}$$



# The $^{90}\text{Zr} + ^{208}\text{Pb}$ system



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# Toward heavier than target nuclei

What we have seen up to now concern stable projectile. To populate **heavier than target nuclei** besides:

- proton stripping (-1p)
- neutron pick-up (+1n)

(these reactions populate nuclei with larger **Z** but smaller **MASS**)  
we have to **OPEN** also the:

- proton pick-up (+1p)
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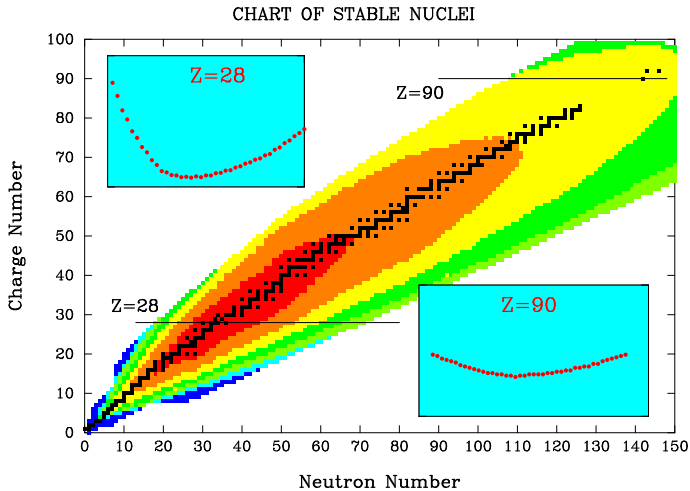
(these reactions populate nuclei with larger **Z** but smaller **MASS**)  
we have to **OPEN** also the:

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## N-rich projectiles



# Bindind energy

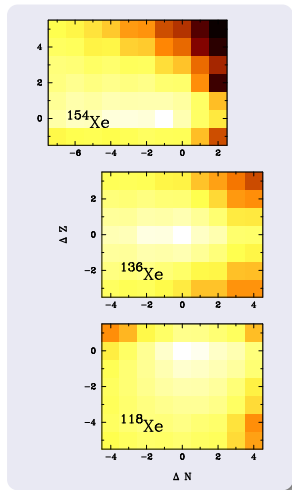


# The Xe + $^{208}\text{Pb}$ reaction at $E_{c.m.}=700$ MeV

The population of projectile-like fragments (corrected by evaporation of the light)

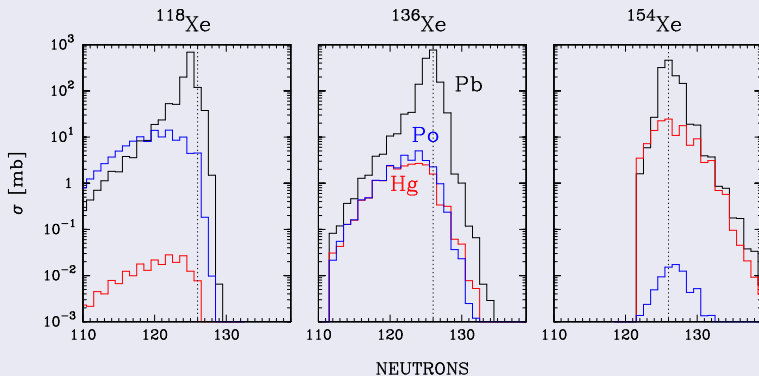
For **stable nuclei** the  $Q_{opt}(N, Z)$  is such that only:

- proton stripping (-1p)
  - neutron pick-up (+1n)
- are possible.



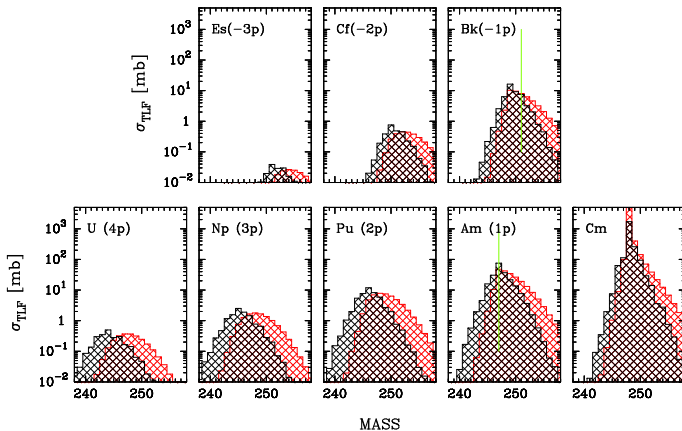
# The Xe + $^{208}\text{Pb}$ reaction at $E_{c.m.}=700$ MeV

The population of the target-like fragments:



# The $^{144}\text{Xe} + ^{248}\text{Cm}$

$^{144}\text{Xe} + ^{248}\text{Cm}$  ( $E_{\text{lab}}=950$  MeV)

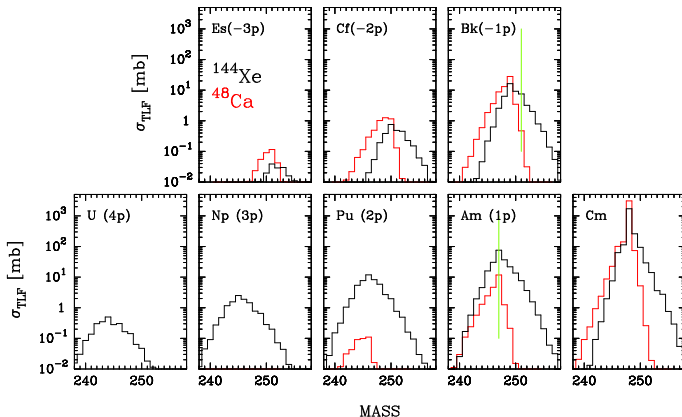




# $^{144}\text{Xe}$ versus $^{48}\text{Ca}$

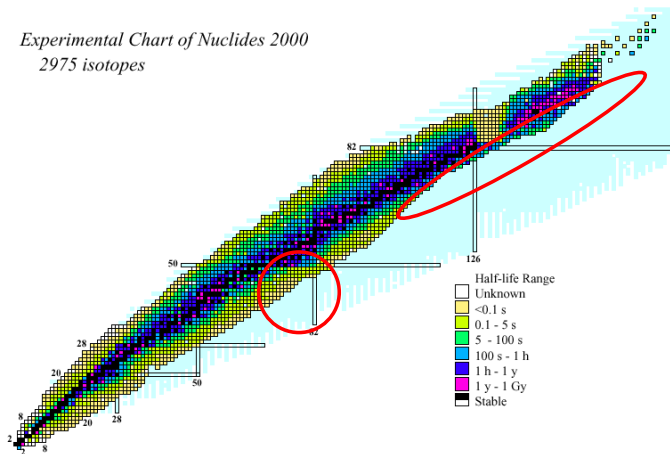
$^{48}\text{Ca} + ^{248}\text{Cm}$  ( $E_{\text{lab}}=310$  MeV)

$^{144}\text{Xe} + ^{248}\text{Cm}$  ( $E_{\text{lab}}=950$  MeV)



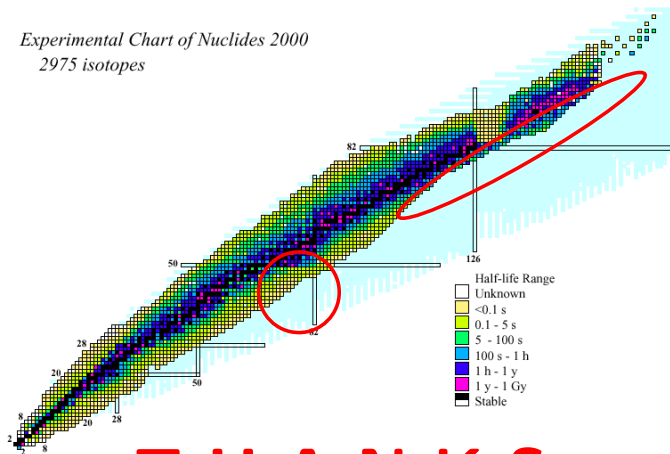
# Where multinucleon-transfer

*Experimental Chart of Nuclides 2000*  
2975 isotopes



# Where multinucleon-transfer

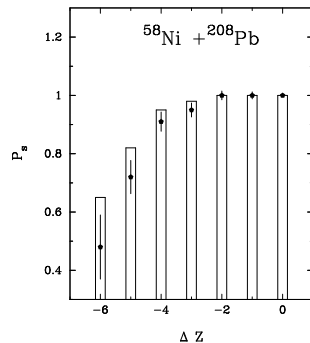
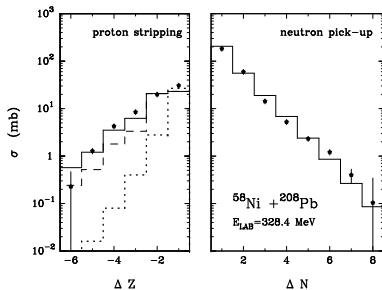
*Experimental Chart of Nuclides 2000*  
2975 isotopes



# THANKS



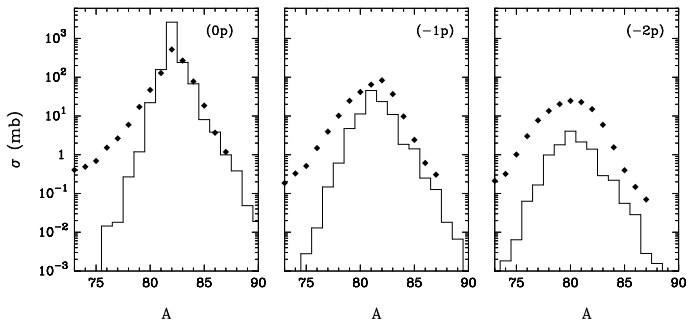
# $^{58}\text{Ni} + ^{208}\text{Pb}$



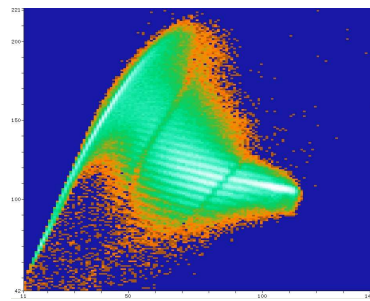
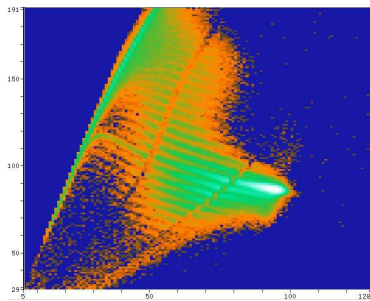
Data from  
 Legnaro National Lab. (INFN)  
 L. Corradi, et al.



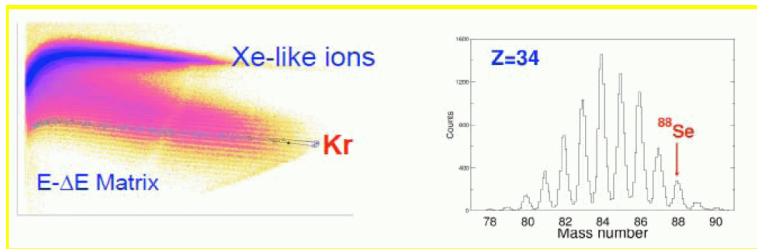
# $^{82}\text{Se} + ^{248}\text{U}$

 $^{82}\text{Se} + ^{238}\text{U}$ 
 $E_{\text{LAB}} = 500 \text{ MeV}$ 


# The $^{64}\text{Ni} + ^{248}\text{U}$ and $^{82}\text{Se} + ^{248}\text{U}$

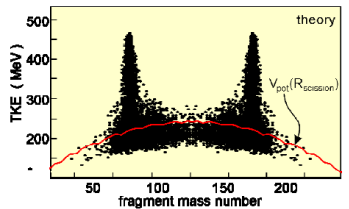
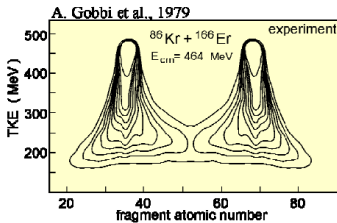


# The $^{136}\text{Xe} + ^{248}\text{U}$



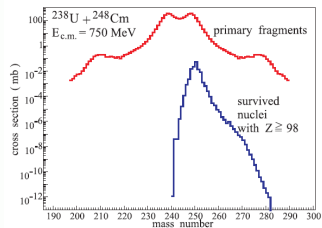
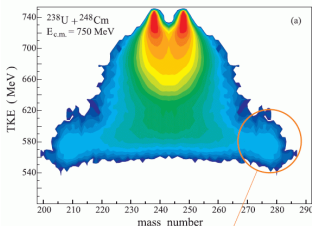
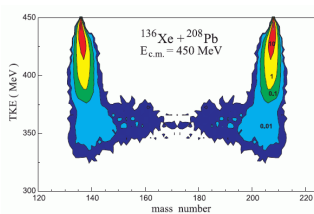
# The $^{86}\text{Kr} + ^{166}\text{Er}$

$^{86}\text{Kr} + ^{166}\text{Er}$  collision at  $E_{\text{c.m.}} = 464 \text{ MeV}$  (Coulomb barrier = 260 MeV)





# $^{136}\text{Xe} + ^{208}\text{Pb}$ and $^{238}\text{U} + ^{248}\text{Cm}$



V.I. Zagrebaev and W. Greiner Phys. Rev. C (2011) 044618

