

**Structure and Production of Superheavy Nuclei and the Island of
Stability:**

Exploring the Island of Stability

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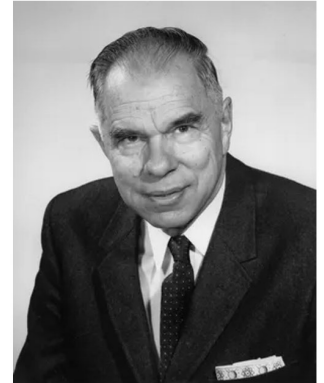
with

G. Adamian, N. Antonenko, L. Malov, V. Sargsyan

JINR Dubna

Searching for Double Magicity...

The Pioneer



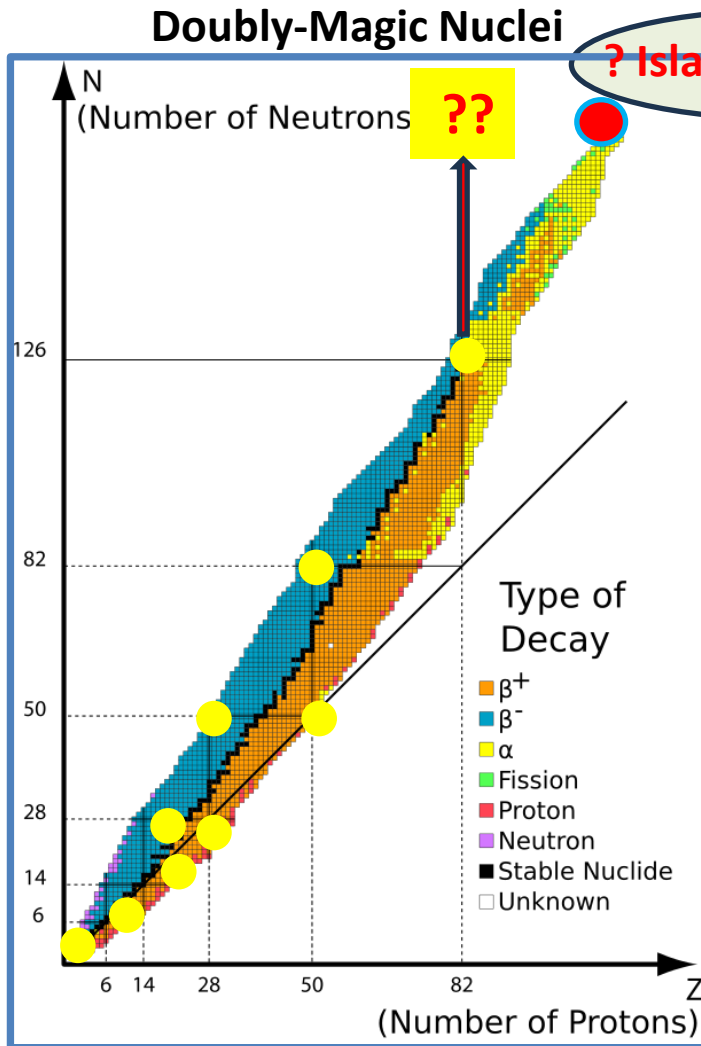
Nobel Prize in Chemistry,
1951

^{269}Sg 2.13 min $\alpha=100\%$

104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
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$Z \geq 104$: Superheavy Nuclei (SHN) / Superheavy Elements (SHE)

The Prime Numbers of Nuclear Physics: 2, 8, 20, 28, 50, 82, 126...?



...the search for SHN motivated to build
GSI, UNILAC and SHIP – the discoverers:



1940-2024

1931-2024

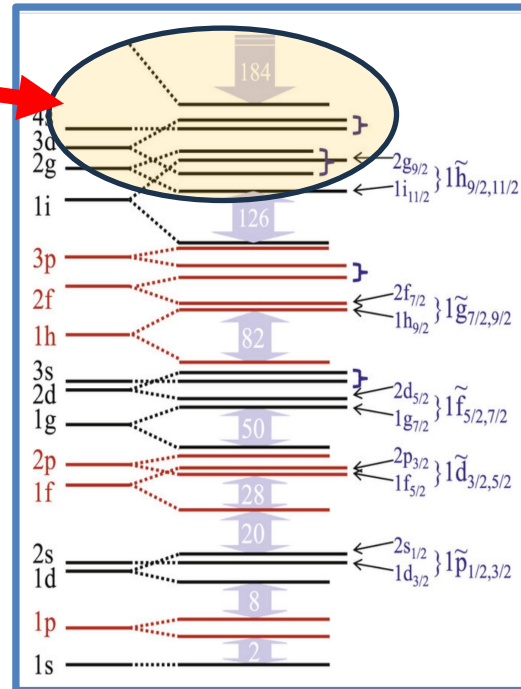
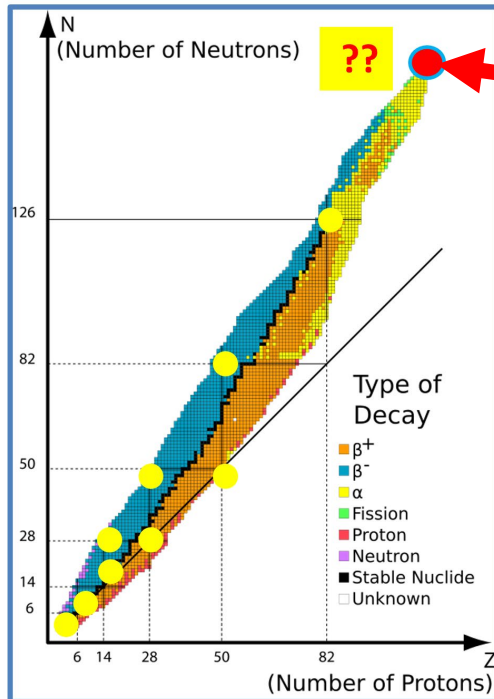


1944-2022

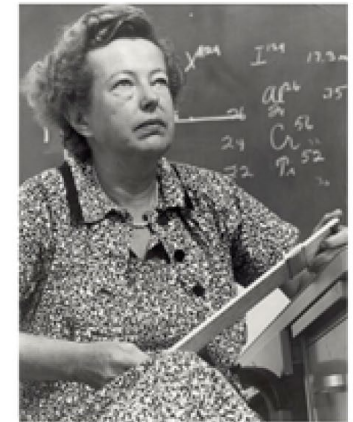
107	108	109	110	111	112
Bh	Hs	Mt	Ds	Rg	Cn

J. Khuyagbaatar *et al.*, “Stepping into the sea of instability:
The new sub- μ s superheavy nucleus ^{252}Rf ,” [Phys. Rev. Lett.](#)
[134, 022501 \(2025\)](#).

Magic Numbers: A Consequence of the Single Particle Nuclear Shell Model

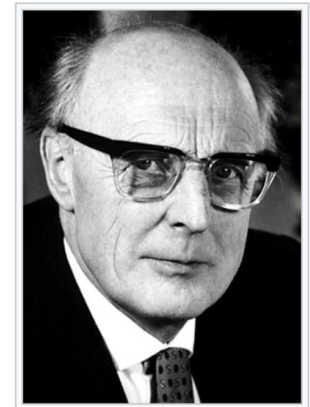


Nobel Prize 1963



Marie Goeppert-Mayer

• [28. Juni 1906](#),
† [20. Februar 1972](#)



Hans Jensen

• [25. Juni 1907](#)
• † [11. Februar 1973](#)

$$\left(-\frac{\hbar^2}{2m_q} \nabla^2 + U_q(r) + U_q^{(ls)}(r) \mathbf{L} \cdot \mathbf{s} - \varepsilon_q \right) \psi_q(r) = 0$$

Droplet Model and Shell Corrections

The Standard Approach to SHN Modeling: Liquid Drop, and Droplet Model

$$E(Z,N)/A = -16\text{MeV} + E_{\text{surf}}/A^{1/3} + E_{\text{pair}} + E_{\text{shell}} + E_{\text{coul}} + [(N-Z)/A]^2(a_4 + C_{\text{sym}}/A^{1/3})$$

Bethe-Weizsäcker Mass Formula (1935) → Liquid Drop Model (Gamow, Bohr...)

First Theoretical Prediction of Superheavy Nuclei

A. Sobiczewski, F. A. Gareev, and B. N. Kalinkin, Phys. Lett. B22, 500 (1966).

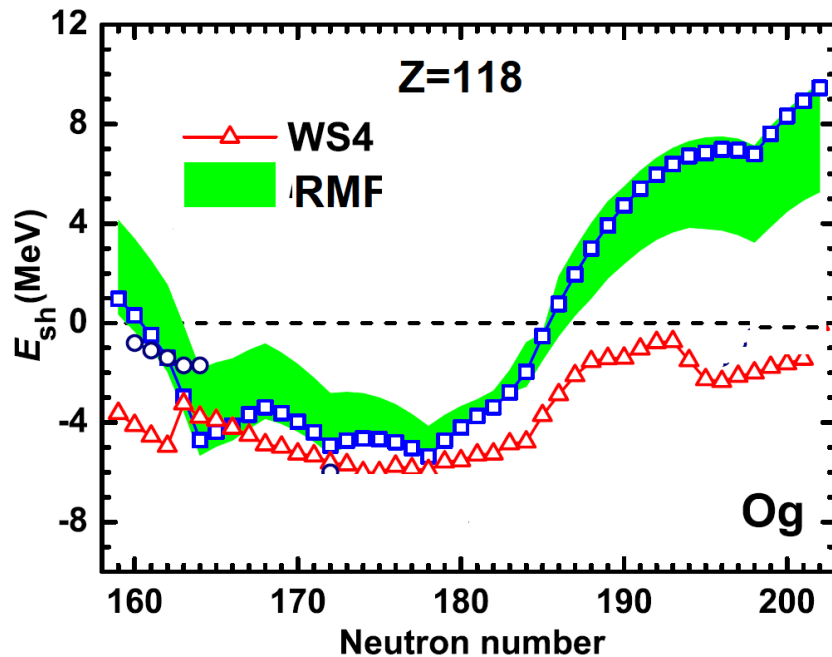
Droplet Model and Macroscopic-Microscopic Model

W. D. Myers and W. J. Swiatecki, Ark. Fys. 36, 343 (1967).

P. Moeller, J.R. Nix, *Atom.Data Nucl.Data Tabl.* 26 (1981) 165

Today: various generalized Droplet Models

Caveat:
Nuclei at $Z > 104$ exist only by shell effects!



after Jiang, PRC 98, 064323 (2018)

Strutinski Shell Corrections

Rev.Mod.Phys. 44 (1972) 320

$$E_{sh} = \sum_{i=1}^{Z(N)} \varepsilon_i - \int_{-\infty}^{\tilde{\lambda}} \varepsilon \tilde{g}(\varepsilon) d(\varepsilon).$$

$$\sim \lambda_q A_q (q=Z, N)$$

$$\tilde{g}(\varepsilon) = \frac{1}{\gamma} \int_{-\infty}^{\infty} \left[\sum_{i=1}^{\infty} \delta(\varepsilon' - \varepsilon_i) \right] f\left(\frac{\varepsilon' - \varepsilon}{\gamma}\right) d\varepsilon'.$$

Smoothed Level Density

Paradigm of SHN Theory:
Shell Corrections = Stability Criterion

Microscopic EDF Approach to SHN Structure

The Giessen EDF Approach:

EDF by BHF/DBHF Theory, HFB and Multi-Phonon QRPA Theory

$$E(\rho, \kappa) \approx E(\rho_0, \kappa_0) + \sum_{q=p,n} \left((T_q + U_q(\rho_0)) \delta\rho_q + \Delta_q \delta\kappa_q \right) + \sum_{q,q'=p,n} f_{qq'}(\rho_0) \delta\rho_q \delta\rho_{q'} + \dots$$

$$\delta\rho_q \sim \langle \varphi_k^\dagger \varphi_n \rangle - \varphi_k^\dagger \varphi_n \quad ; \quad \delta\kappa_q \sim \langle \varphi_k \varphi_n \rangle - \varphi_k \varphi_n \quad \& \text{ h.c.}$$

Single Particle Self-Energy (Potential):

$$U_q = \frac{\delta}{\delta\rho_q} \frac{1}{2} \langle V \rangle = \sum_{q'} V_{qq'}(\rho) \rho_{q'} + \frac{1}{2} \sum_{q'q''} \rho_{q'} \rho_{q''} \frac{\delta}{\delta\rho_q} V_{q'q''}(\rho)$$

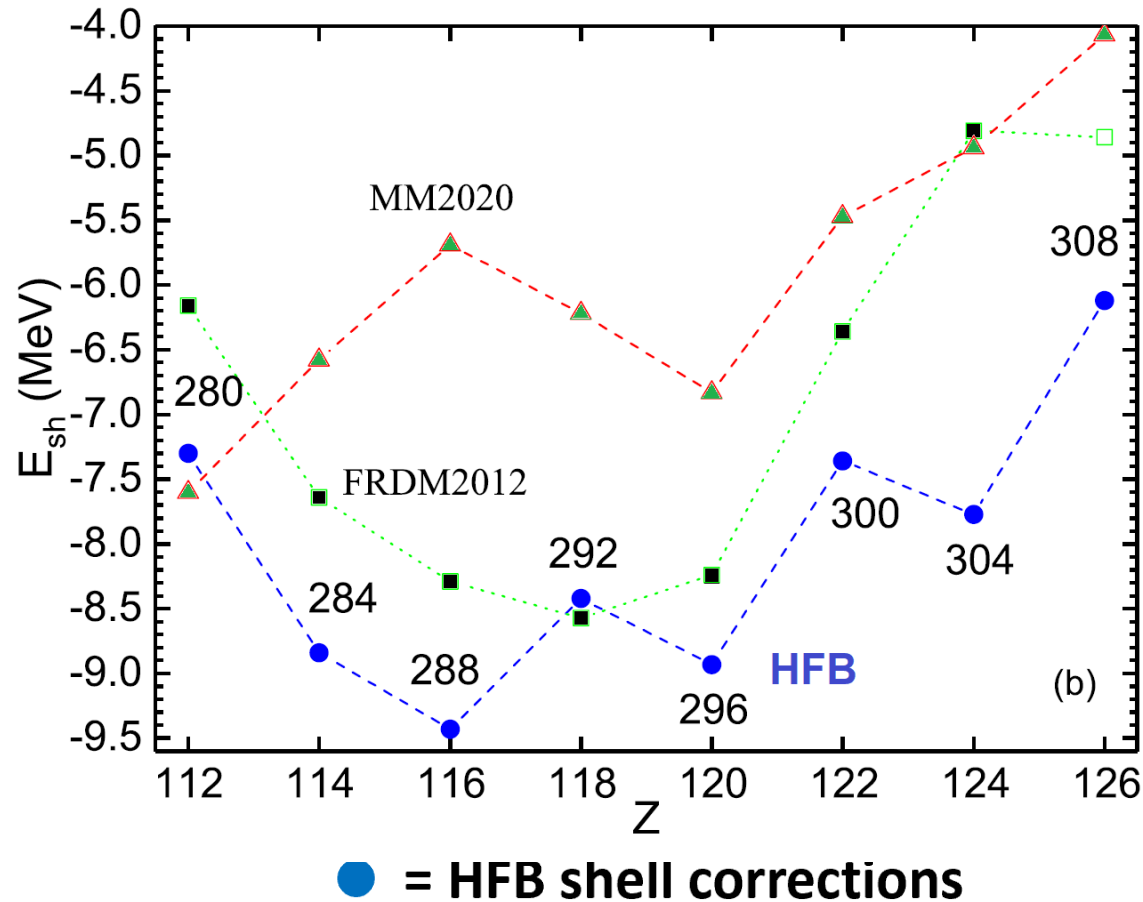
Self-consistent Mean-Field Dynamics:

$$\left(-\nabla \cdot \frac{\hbar^2}{2m_q^*(\mathbf{r})} \nabla + V_q(\mathbf{r}, \mathbf{k}) + V_q^{(ls)}(\mathbf{r}) \mathbf{L} \cdot \mathbf{s} - \varepsilon_q \right) \psi_q(\mathbf{r}) = 0$$

plus Pairing: Quasiparticle Spectrum and Wave Functions

N. Tsoneva, H.L., *Phys.Rev.C* 77 (2008) 024321, *Nature Commun.* 11 (2020), *Phys.Atom.Nucl.* 79 (2016) 6, 885, *Phys.Rev.Lett.* 110 (2013) 022503, *Eur.Phys.J.A* 55 (2019) 238, *Phys.Rev.C* 108 (2023) 5, L051301...and many more

EDF-HFB Theory, Deformation, and Shell Corrections along α -Decay Chains



PRC 104, 064303 (2021)

Our most Recent Publications on the Topics of this Contribution:

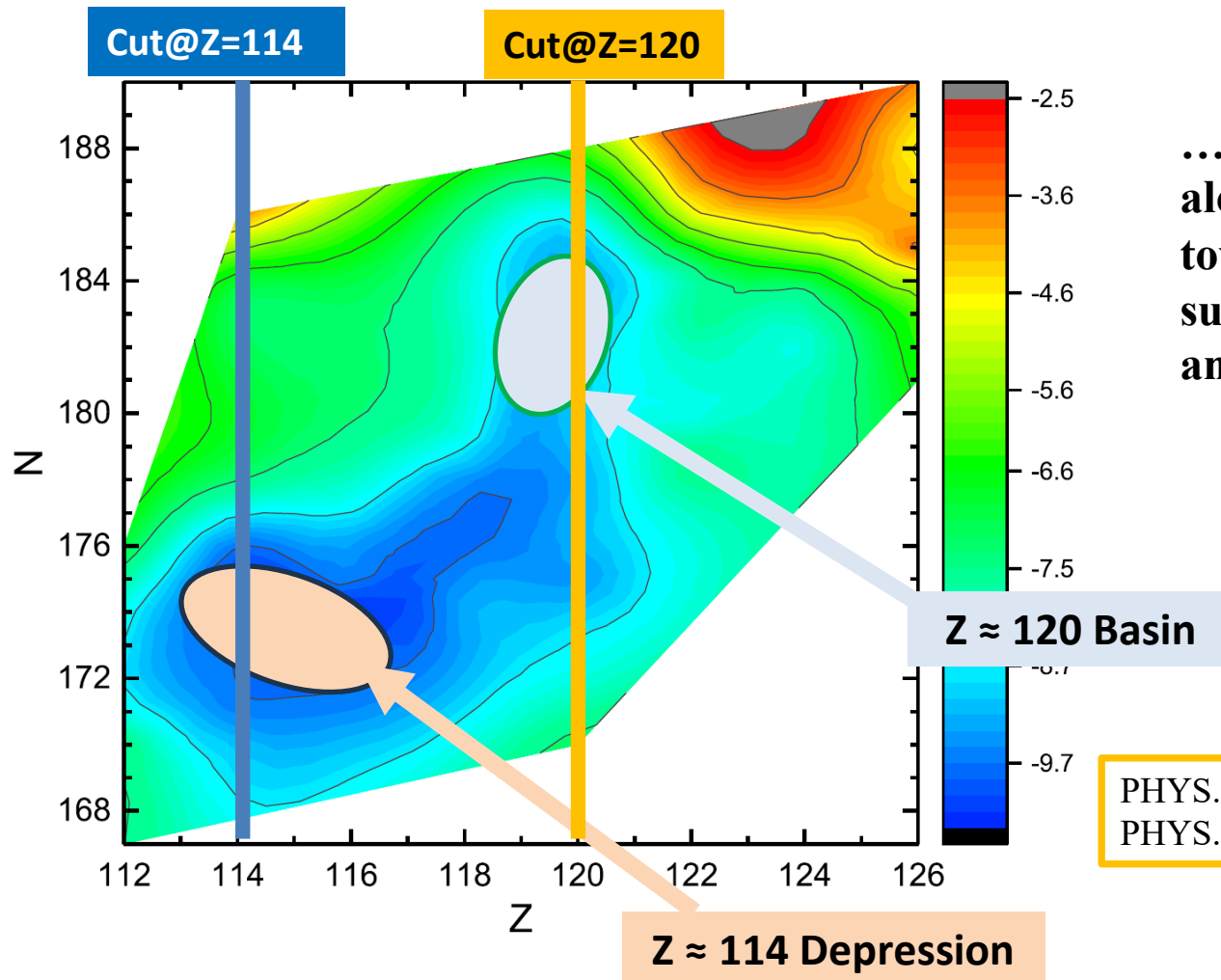
1. **Application of a universal reaction function to the description of heavy-ion reaction cross sections.** ·G.G.·Adamian,·N.V.·Antonenko,·H.·Lenske,·V.V.·Sargsyan,·DOI:·10.1103/PhysRevC.109.014602,·Published in:·Phys. Rev. C·109·(2024)·1,·014602·¶
2. **Double-folding nucleus-nucleus interaction potential based on the self-consistent calculations.** ·N.V.·Antonenko,·G.G.·Adamian,·V.V.·Sargsyan,·H.·Lenske,·DOI:·,·Published in:·Eur. Phys. J. A·58·(2022)·11,·211·¶
3. **On the possibility of formation of binary cosmic systems from the single cosmic objects.**·G.G.·Adamian,·N.V.·Antonenko,·H.·Lenske,·V.V.·Sargsyan,·DOI:·10.1142/S0218301322500719·Published in:·Int. J. Mod. Phys. E·31·(2022)·07,·2250071·¶
4. **Constraints on the appearance of a maximum in astrophysical S-factor.**·V.V.·Sargsyan,·G.G.·Adamian,·N.V.·Antonenko,·H.·Lenske,·DOI:·10.1016/j.physletb.2021.136792,·Published in:·Phys. Lett. B·824·(2022),·136792·¶
5. **Landscape of the island of stability with self-consistent mean-field potentials.** ·L.A.·Malov,·G.G.·Adamian,·N.V.·Antonenko,·H.·Lenske,·DOI:·10.1103/PhysRevC.104.064303,·Published in:·Phys. Rev. C·104·(2021)·6,·064303·¶
6. **Shaping the archipelago of stability by the competition of proton and neutron shell closures.**·L.A.·Malov,·G.G.·Adamian,·N.V.·Antonenko,·H.·Lenske,·DOI:·10.1103/PhysRevC.104.L011304,·Published in:·Phys. Rev. C·104·(2021)·1,·L011304·¶
7. **Self-consistent methods for structure and production of heavy and superheavy nuclei.**·G.G.·Adamian·(Dubna,·JINR),·N.V.·Antonenko·(Dubna,·JINR·and·Tomsk·Polytechnic·U.),·H.·Lenske·(Giessen·U.),·L.A.·Malov·(Dubna,·JINR),·Shan-Gui·Zhou·(Beijing,·KITPC·and·Beijing,·GUCAS·and·Natl.·Lab.·Heavy·Ion·Accel.,·Lanzhou·and·Hunan·Normal·U.),·DOI:·10.1140/epja/s10050-021-00375-1,·Published in:·Eur. Phys. J. A·57·(2021)·3,·89·¶
8. **Application of Regge Theory to Astronomical Objects.**·Gurgen·G.·Adamian·(Dubna,·JINR),·Nikolai·V.·Antonenko·(Dubna,·JINR),·Horst·Lenske·(Giessen·U.),·Vazgen·V.·Sargsyan·(Dubna,·JINR),·e-Print:·2012.14276·[physics.class-ph],·DOI:·10.3390/physics3030040,·Published in:·MDPI·Physics·3·(2021)·3,·669-677·¶

The *Archipelago* of Stability



Towards Magicity in the Superheavy Region

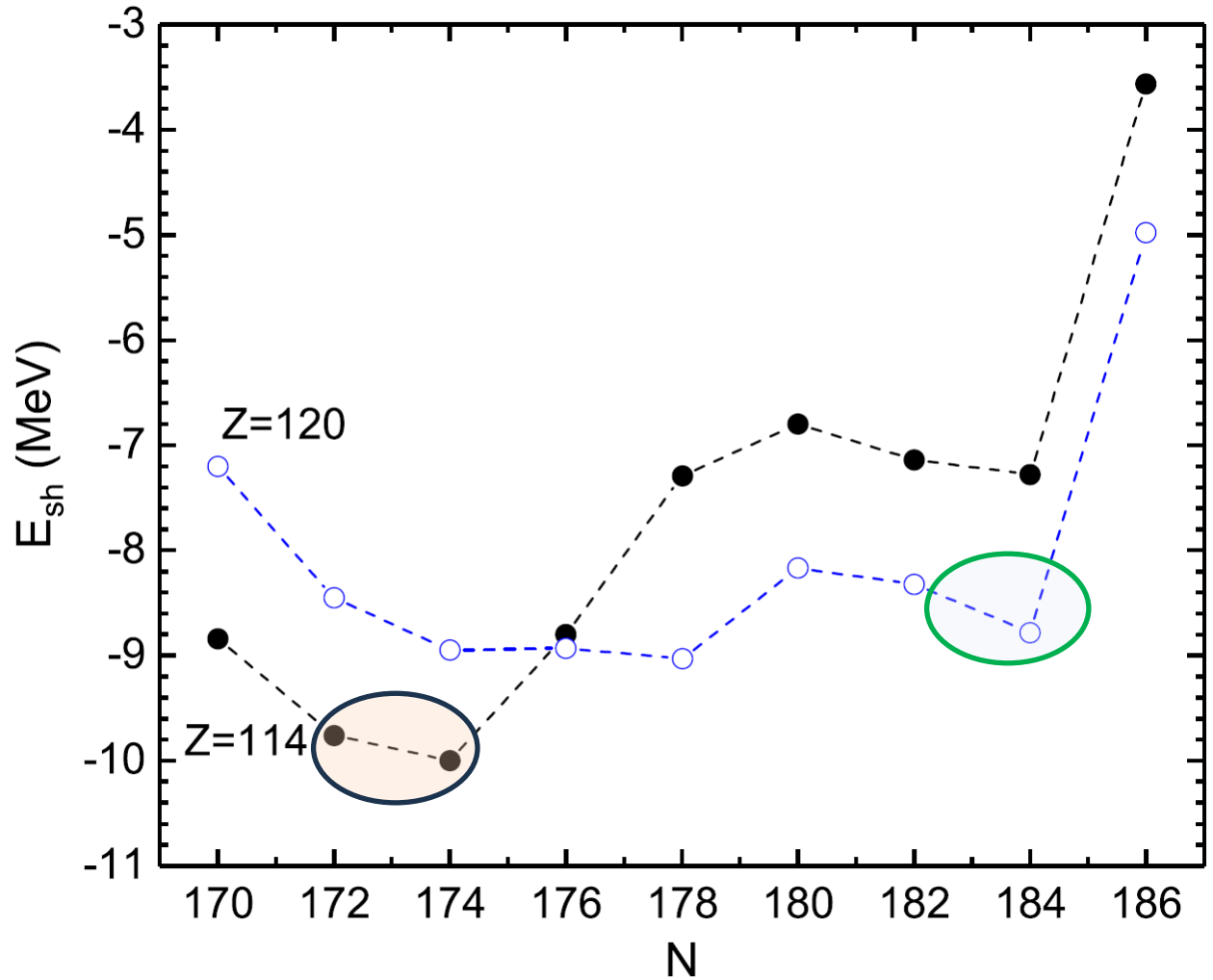
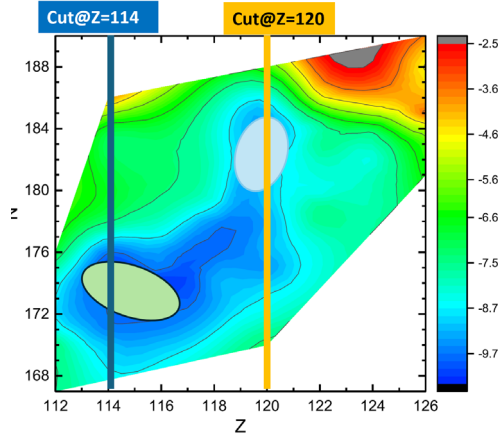
Shell Corrections in the (Z,N)-Plane



...(blue-ish) ditch extending along $N \approx 1.5Z$, then bending towards the N axis, surrounded by a rather flat and structureless ridge.

PHYS. REV. C **104**, L011304 (2021)
PHYS. REV. C **104**, 064303 (2021)

Nucleodatics of the Archipelago



Conclusion:

Hence, within our approach we conclude that the Fl nuclei at $N \approx 174$ and $Z = 120$ nuclei at $N \approx 184$ will be of double magic structure, implying strong binding and increased stability.

PHYSICAL REVIEW C **104**, L011304 (2021)

Take-Home Message:

- **$^{288}\text{Fl}_{174}$ ($Z=114$) is the next-to-Pb doubly-magic nucleus**
shell closures: $n\{1/2^+[611]$ and $p\{3/2^-[512]\}$
chemical homologs of Pb and Sn (group IV of the Periodic Table)
- **$^{304}\text{X}_{184}$ ($Z=120$) is the next-to-next-to-Pb doubly-magic nucleus**
shell closures: $n\{3/2^+[602]\}$ and $p\{5/2^-[503]\}$
chemical homologs of Ra and Ba (group II of the Periodic Table)

Supported by DFG, grant Le439/16 and
BMBF „Heisenberg-Landau-Program“

Superheavies and Astrophysics:

Eur. Phys. J. A (2023) 59:28

Nucleosynthesis and observation of the heaviest elements

E. M. Holmbeck^{1,a}, T. M. Sprouse^{2,3,b}, M. R. Mumpower^{2,3,c}

“...In the course of creating the actinides and potentially superheavies, the r process must necessarily synthesize superheavy nuclei (those with extreme proton numbers, neutron numbers or both) far from isotopes accessible in the laboratory. Many questions about this process remain unanswered, such as where in nature may this process occur?...”