

# Collective phenomena in small and large hadronic collisions

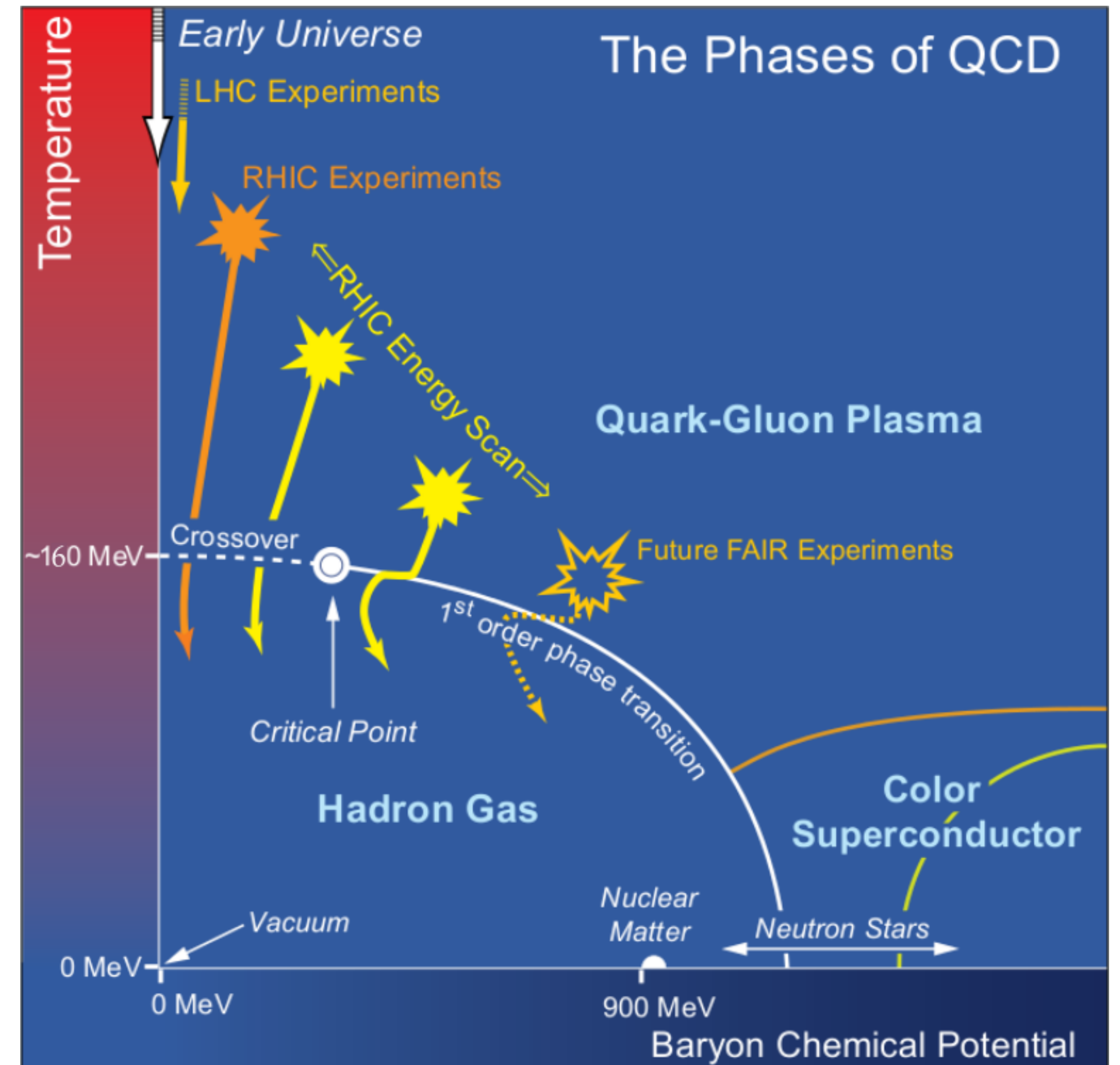
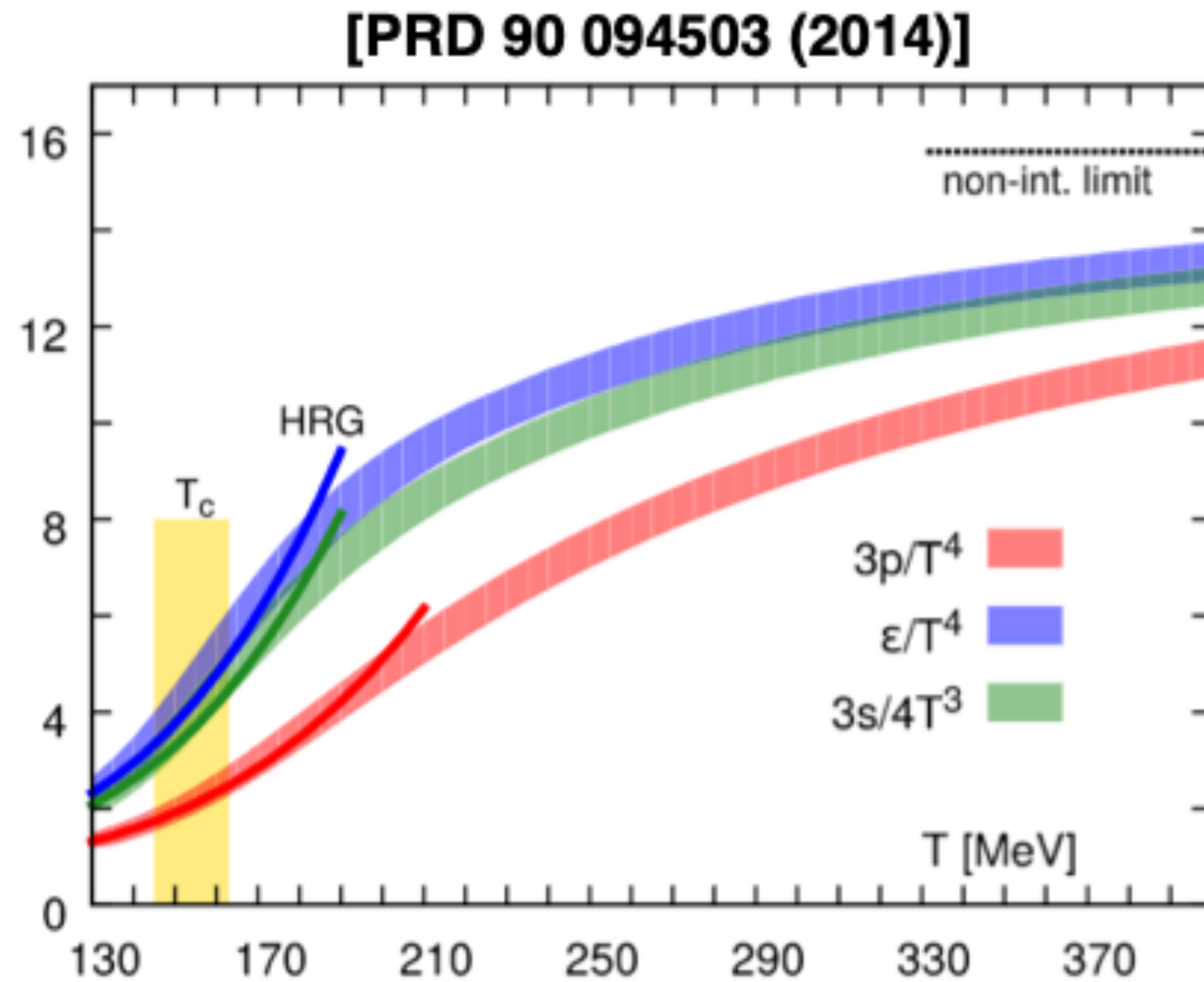
Alice Ohlson  
Lund University

EMMI RRTF Open Symposium, 18 March 2024



# High-temperature regime of QCD

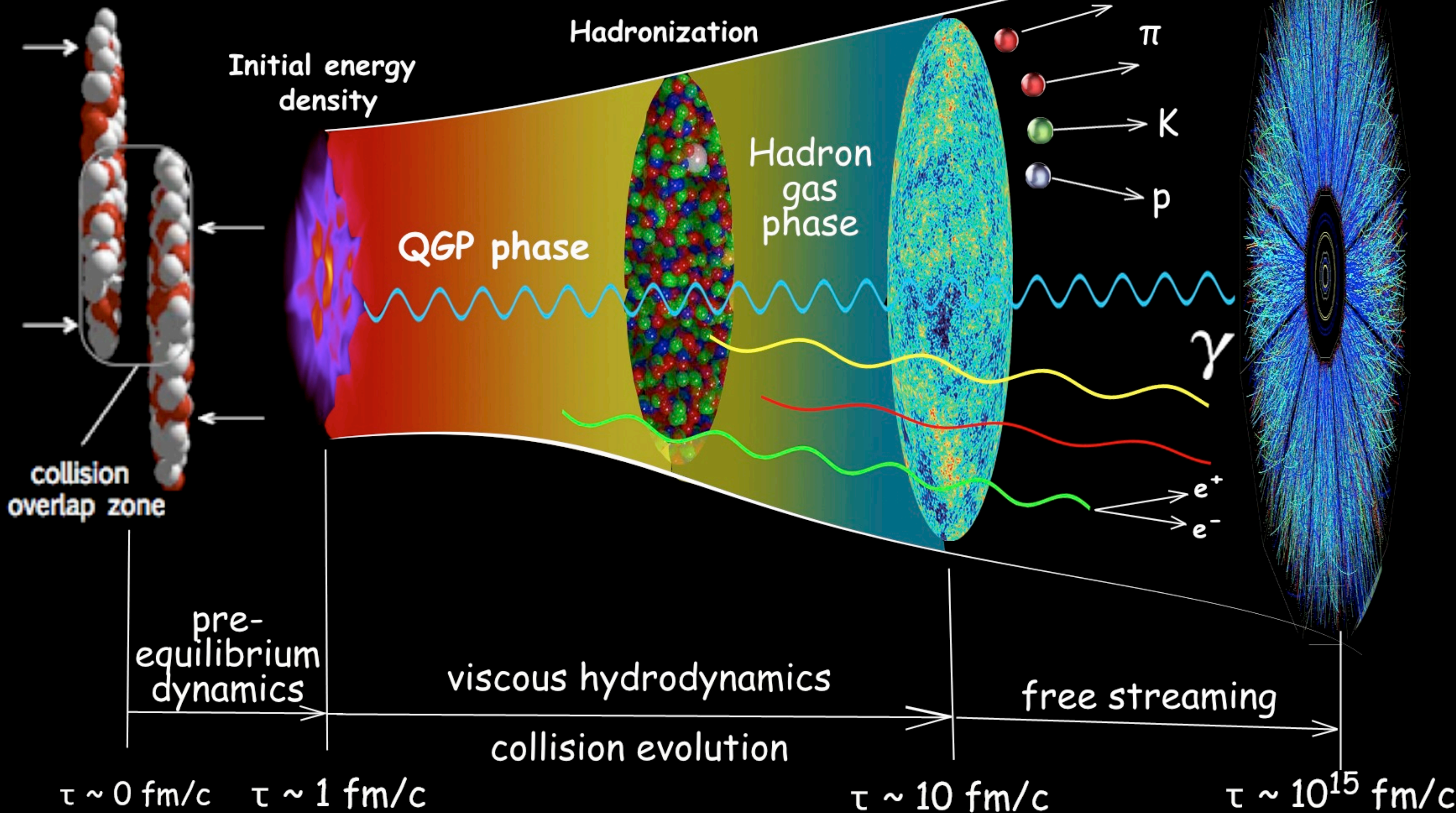
- At high temperatures and densities, quarks and gluons are no longer confined into hadrons but behave quasi-freely
  - Quark-Gluon Plasma (QGP)



# Relativistic Heavy-Ion Collisions

made by Chun Shen

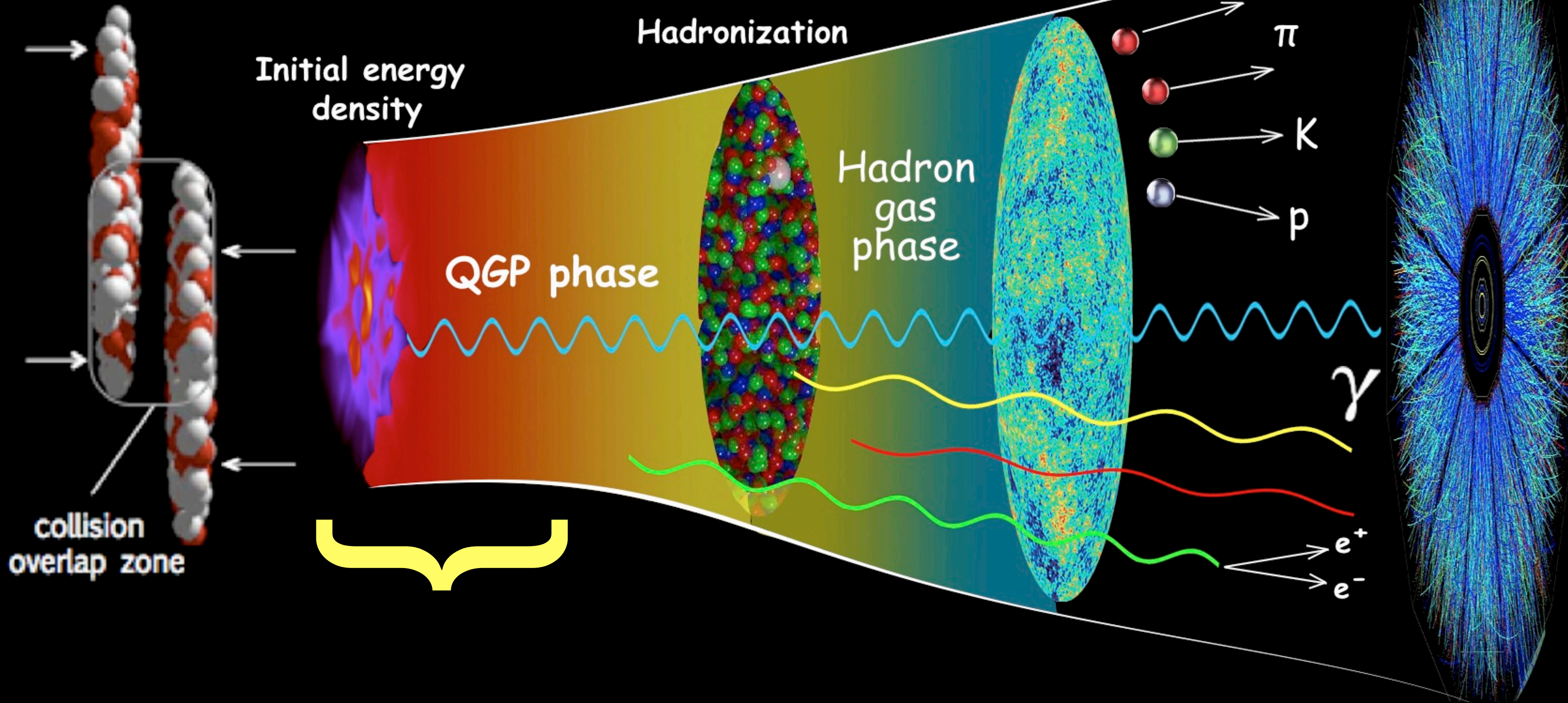
final detected particle distributions



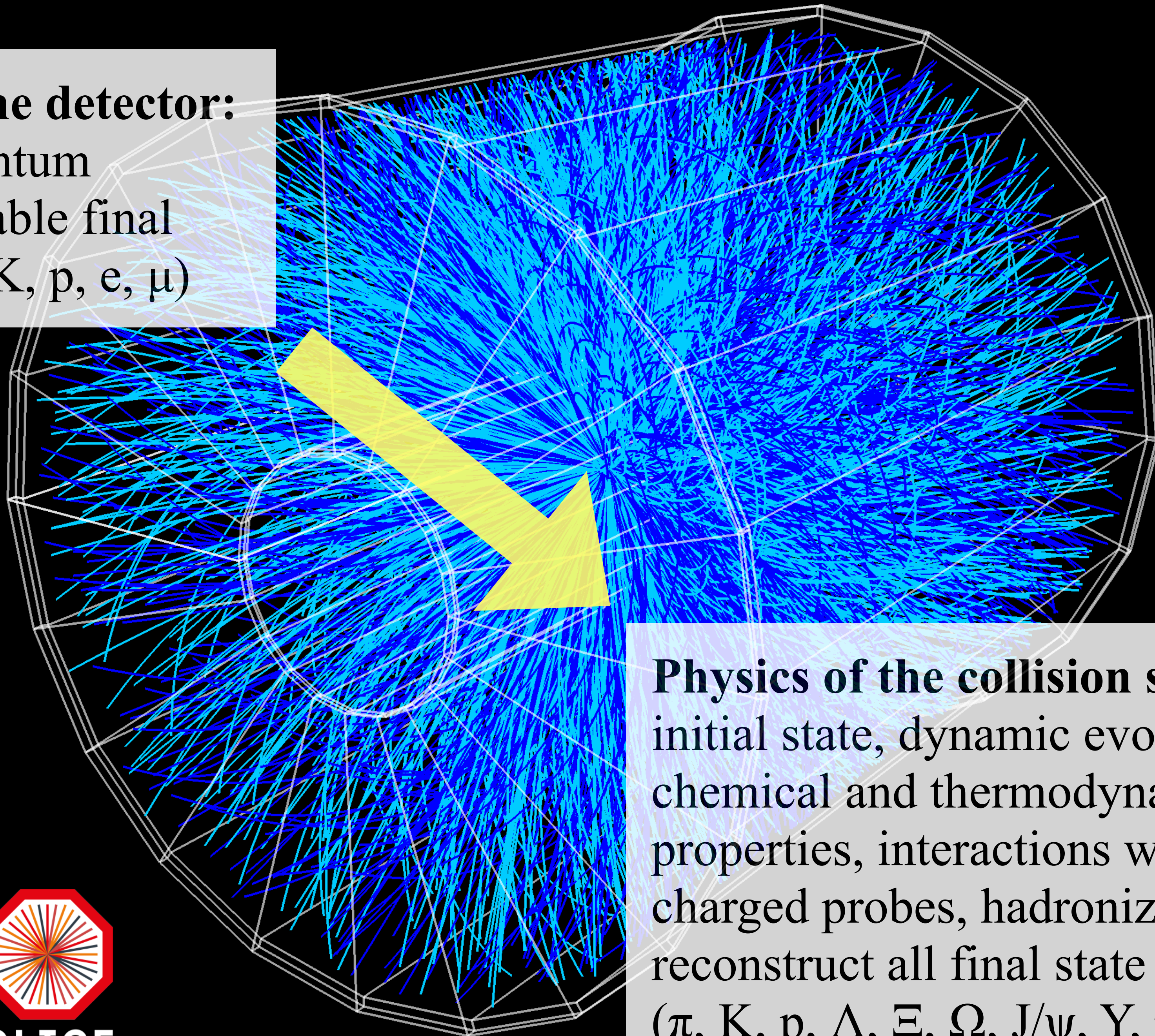
# Relativistic Heavy-Ion Collisions

made by Chun Shen

final detected  
particle distributions



**Observables in the detector:**  
spatial and momentum  
distributions of stable final  
state particles ( $\pi$ ,  $K$ ,  $p$ ,  $e$ ,  $\mu$ )

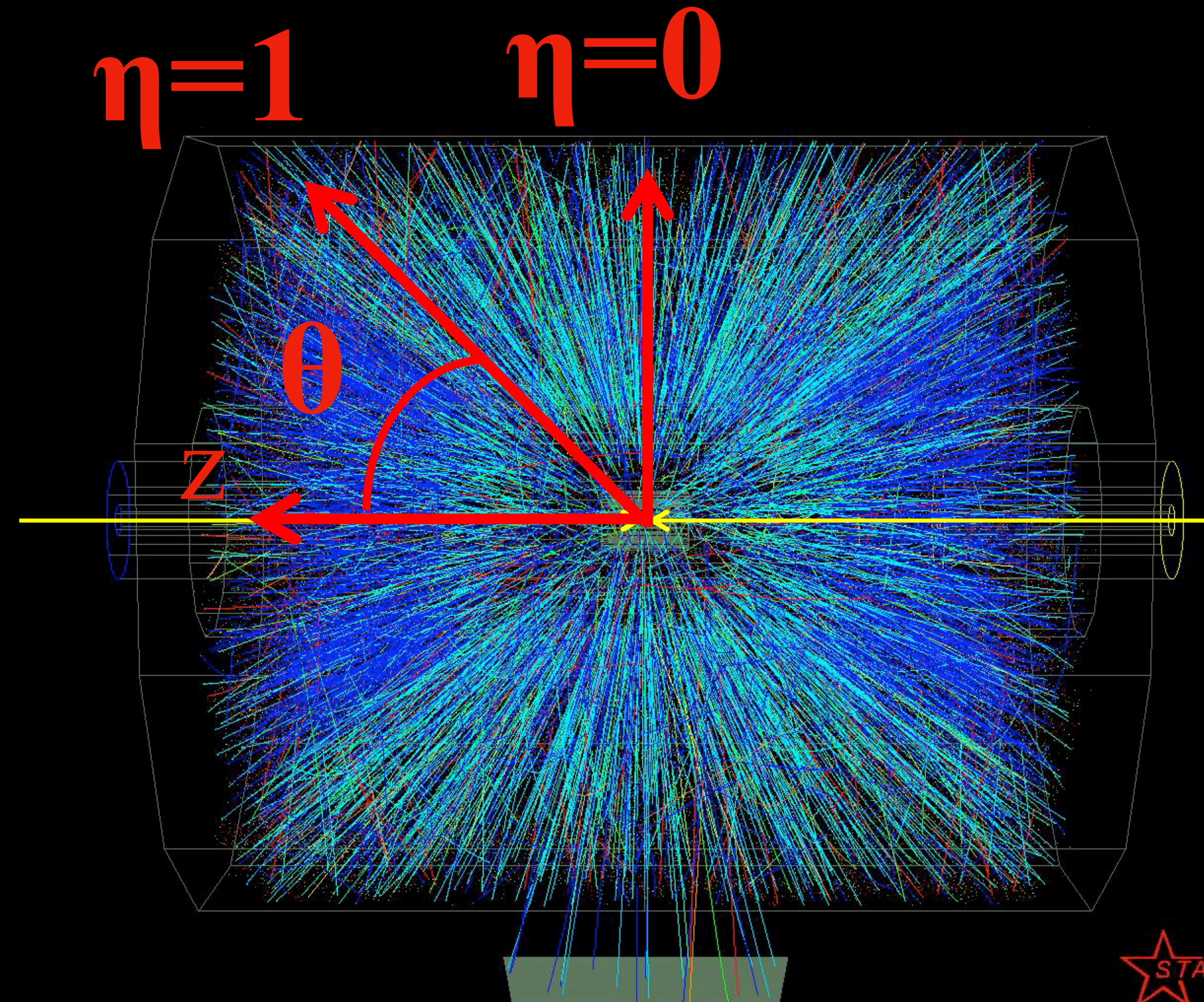
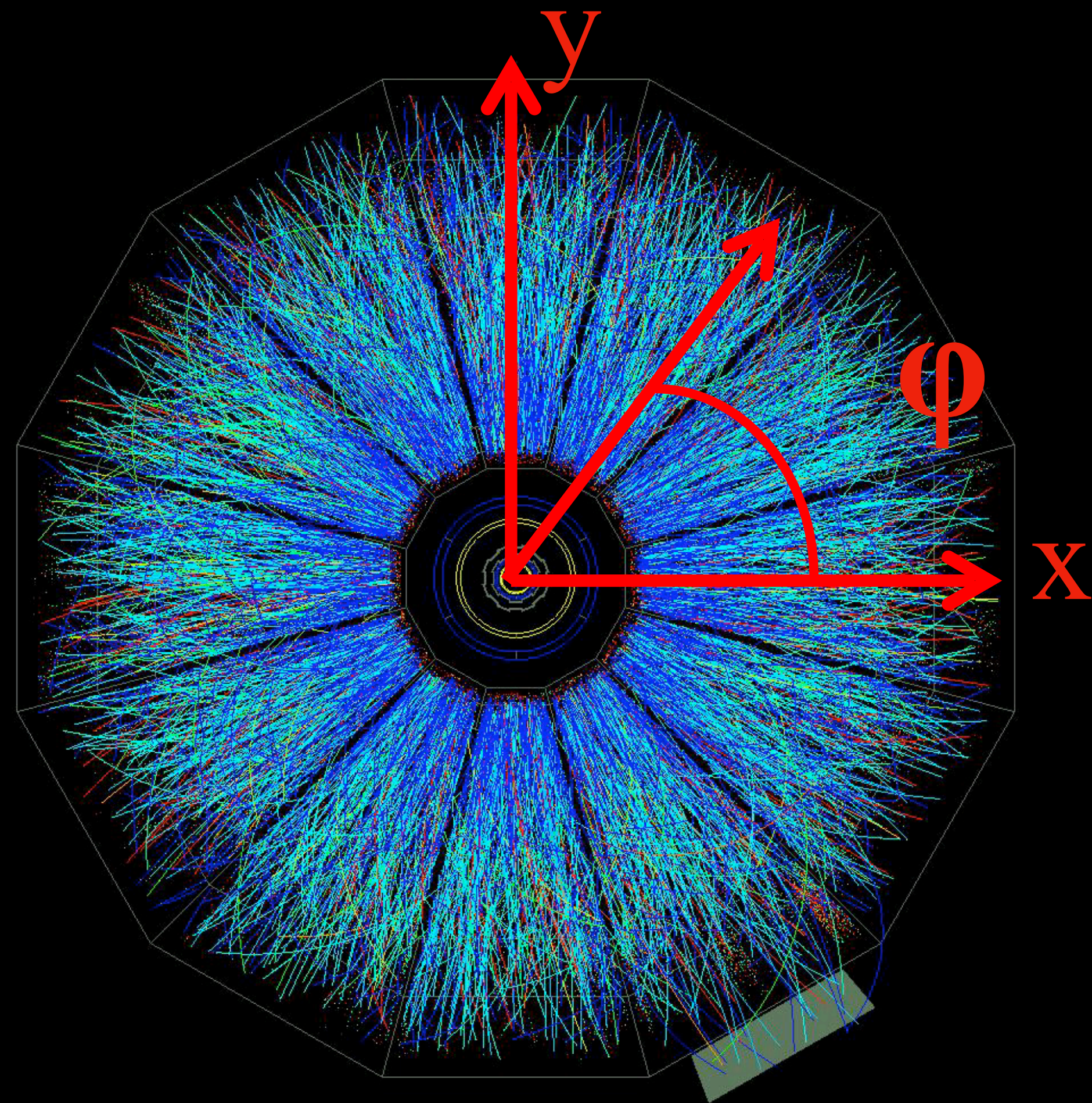


**Physics of the collision system:**  
initial state, dynamic evolution,  
chemical and thermodynamic  
properties, interactions with  
charged probes, hadronization,  
reconstruct all final state particles  
( $\pi$ ,  $K$ ,  $p$ ,  $\Lambda$ ,  $\Xi$ ,  $\Omega$ ,  $J/\psi$ ,  $Y$ ,  $\eta$ ,  $\rho$ ,  $\gamma$ ,  $e$ ,  $\mu$ ,...)



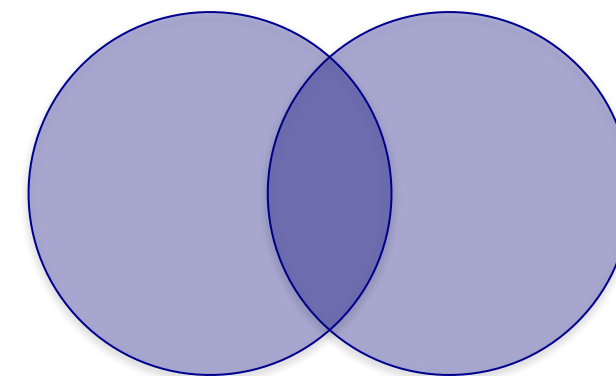
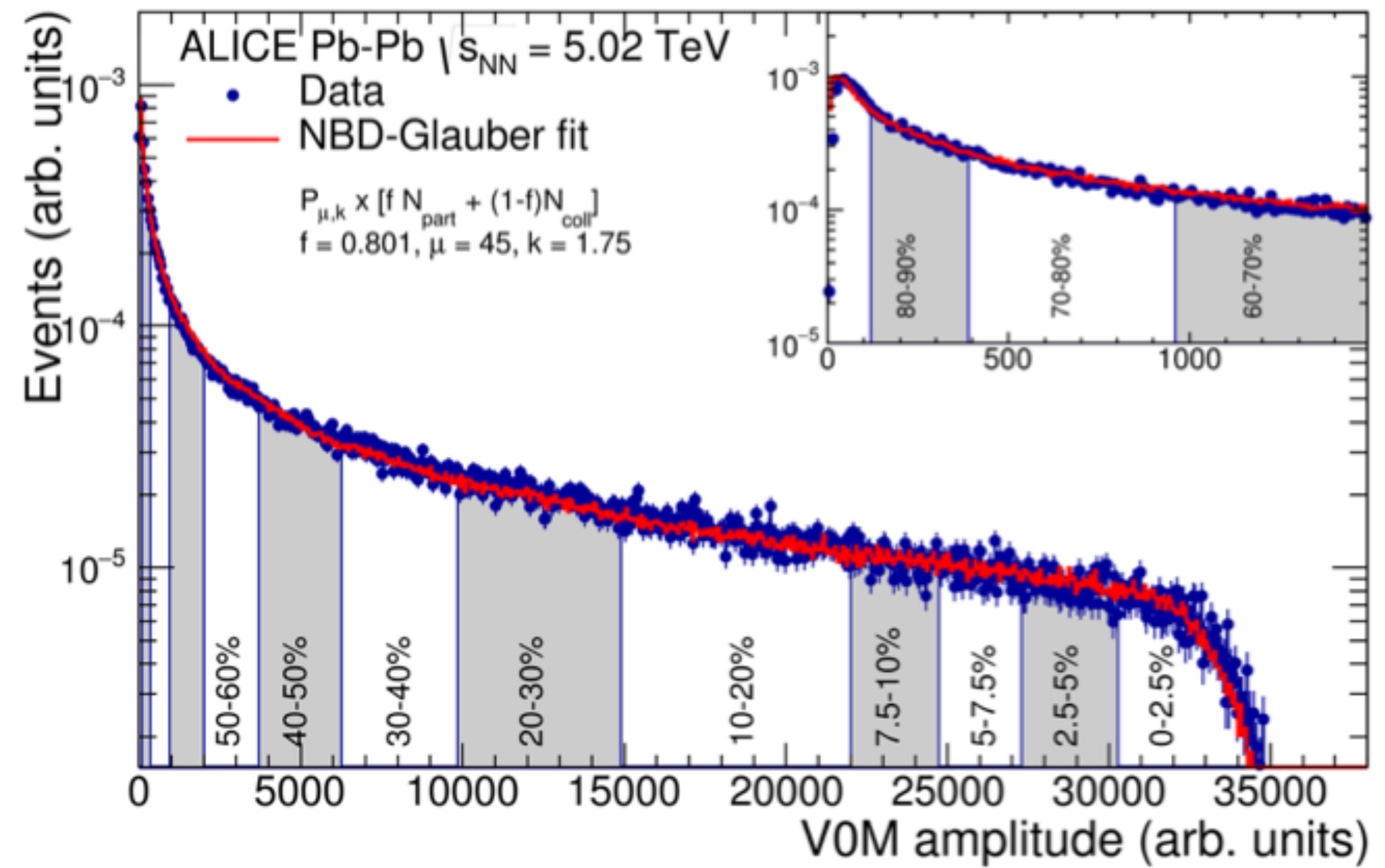
**ALICE**

# Coordinate systems ( $\varphi, \eta$ )

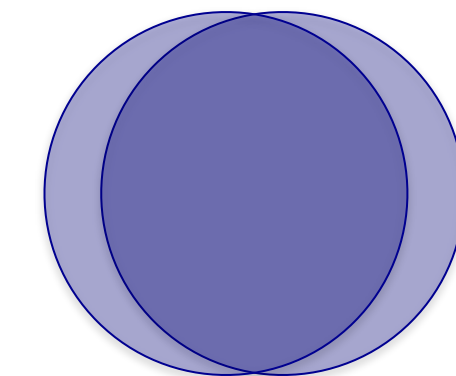


# Geometry of a heavy-ion collision

- **Central (head-on) collision**
  - smaller impact parameter
  - larger overlap region
  - more particles produced
- **Peripheral (glancing) collision**
  - larger impact parameter
  - smaller overlap region
  - fewer particles produced
- Centrality is usually quoted as a percentage of the cross-section
- Centrality determination by counting number of final-state particles (“**multiplicity**”) or energy deposition in a region of phase space *independent* from the measurement, to avoid biases/autocorrelations in the results



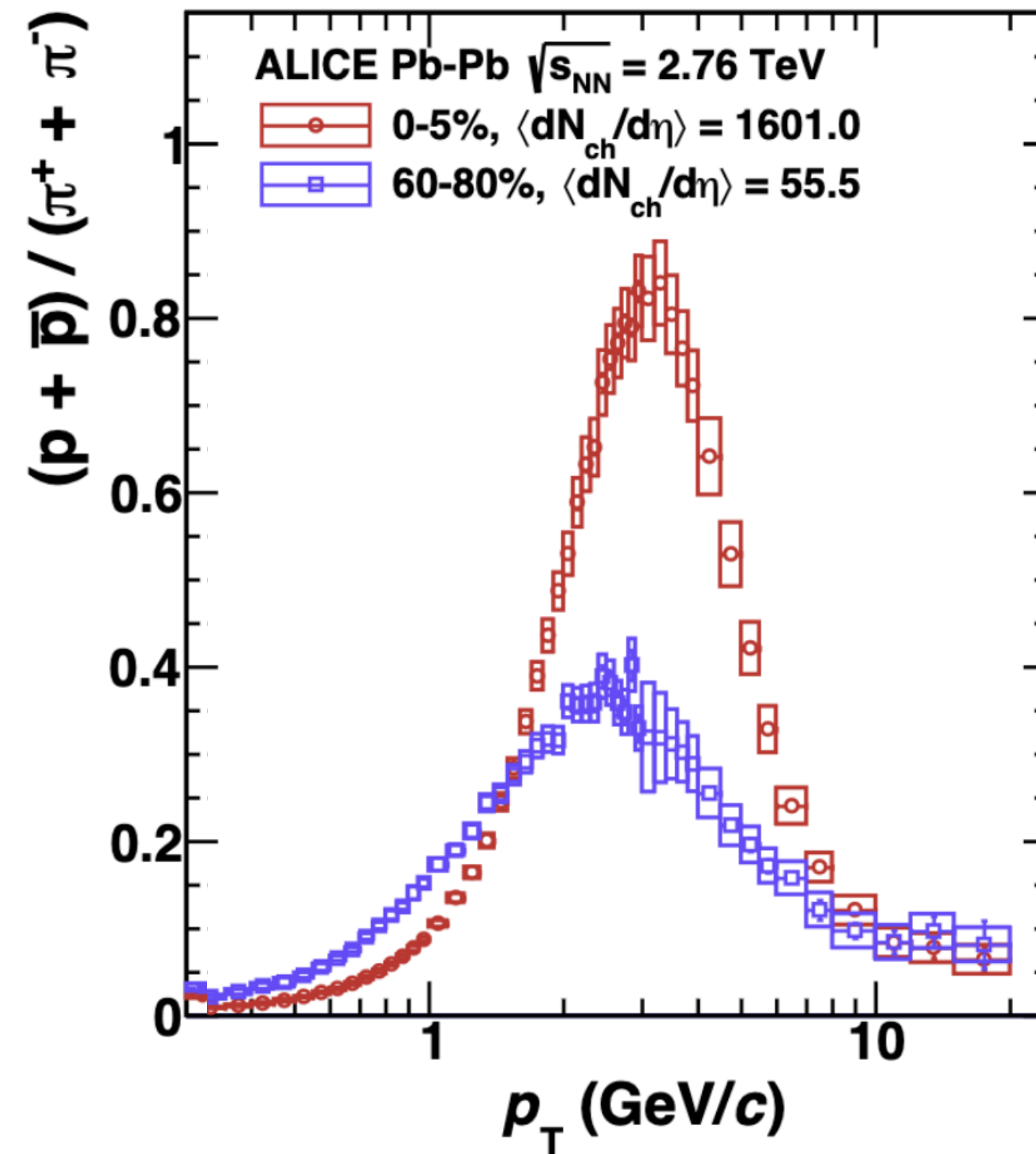
70-90%, “peripheral”



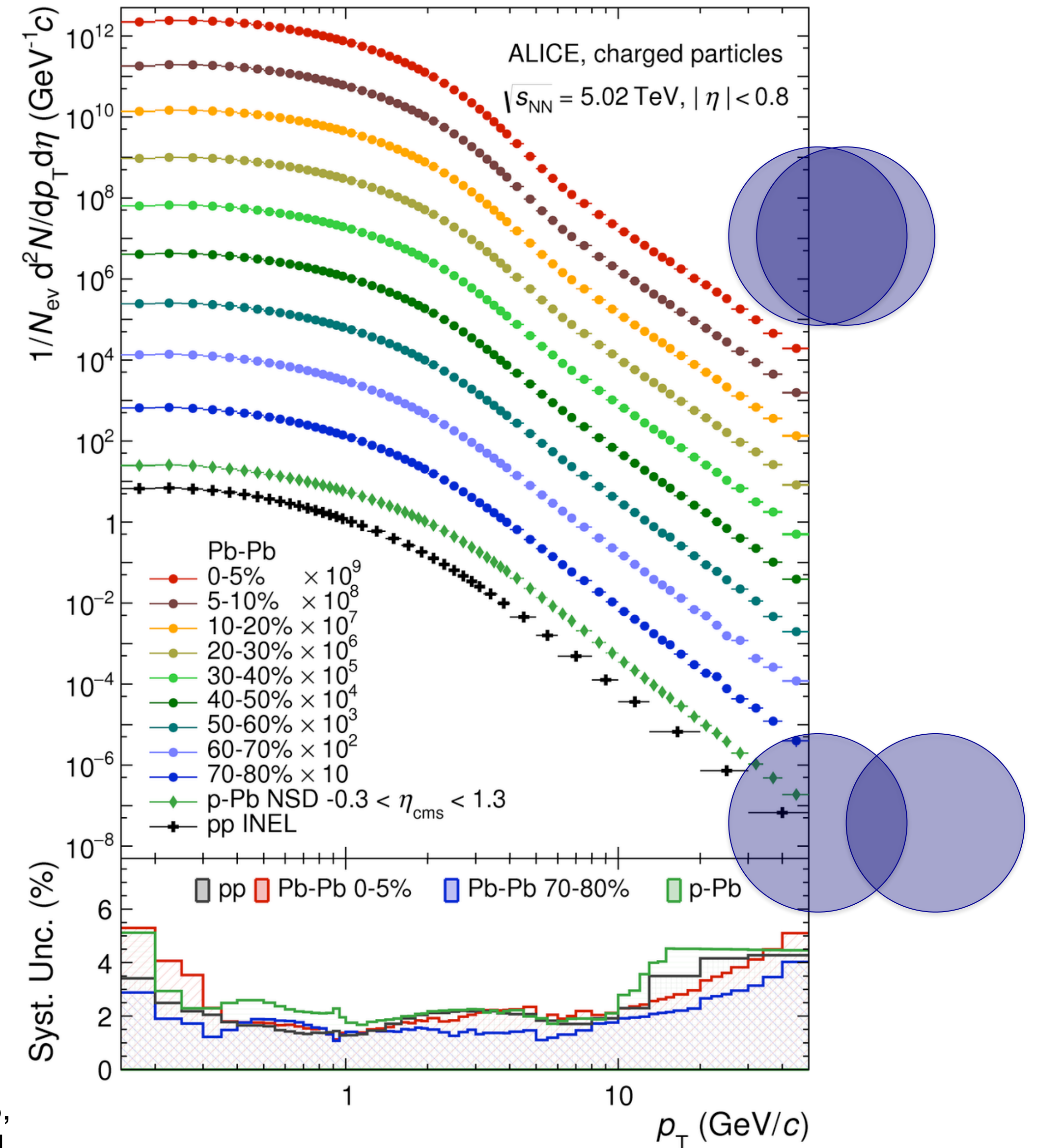
0-5%, “central”

# Isotropic expansion of the fireball

- Pressure gradients build up in the fireball
- Particles boosted in the radial direction  
→ “radial flow”  
→ higher mean  $p_T$
- Velocity boost leads to enhancement in ratio of protons (heavy) to pions (light)

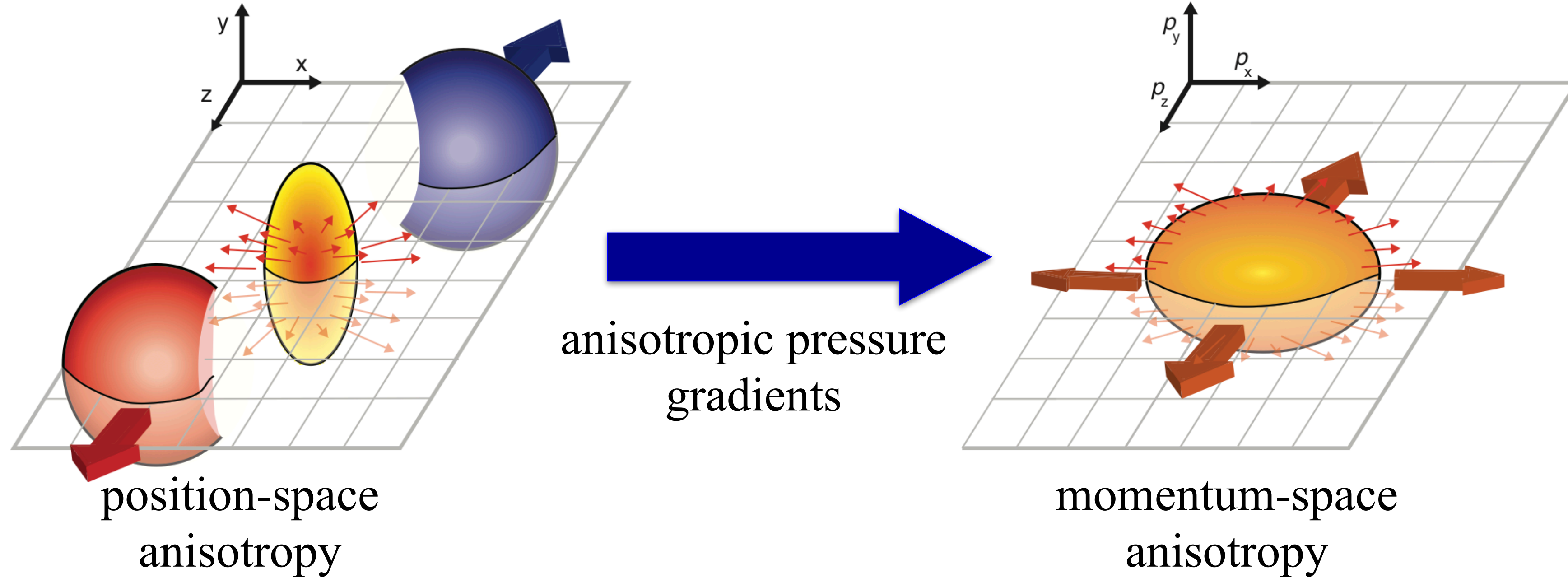


ALICE, JHEP 11 (2018) 013,  
arxiv: 1802.09145 [nucl-ex]

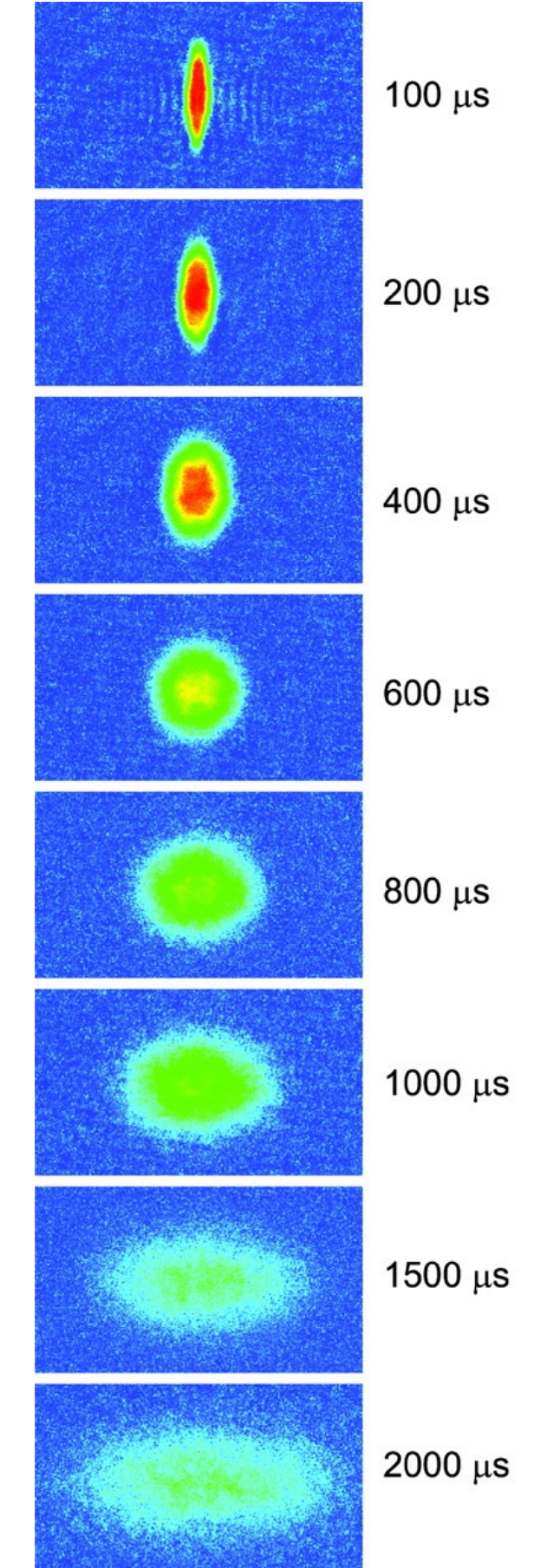
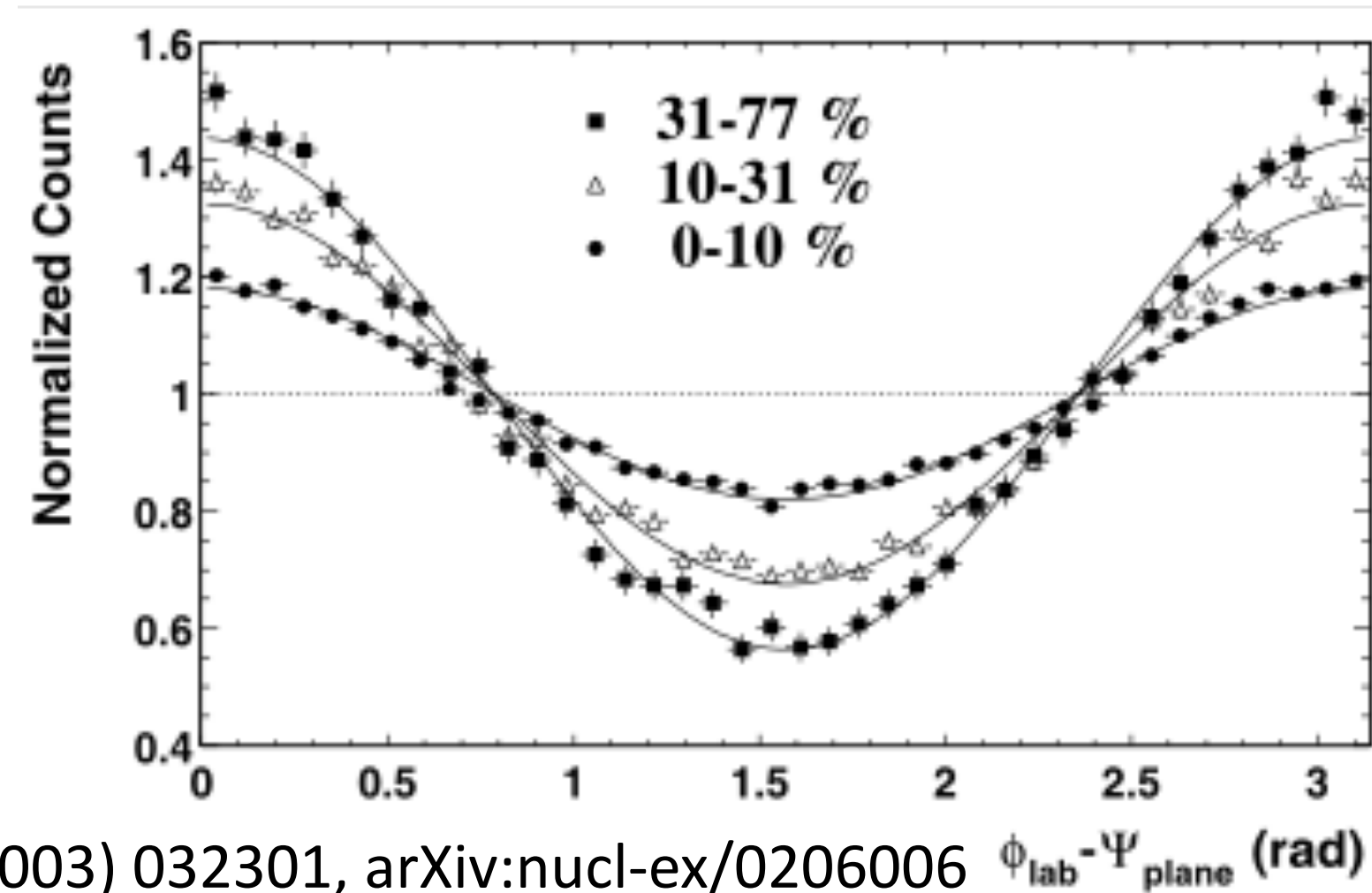




# Anisotropic expansion



- Stronger in-plane pressure gradients, velocity field  $\rightarrow$  particles boosted in-plane more than out-of-plane
- Particles correlated with a “global” symmetry plane



## Elliptic Flow in Ultracold Lithium

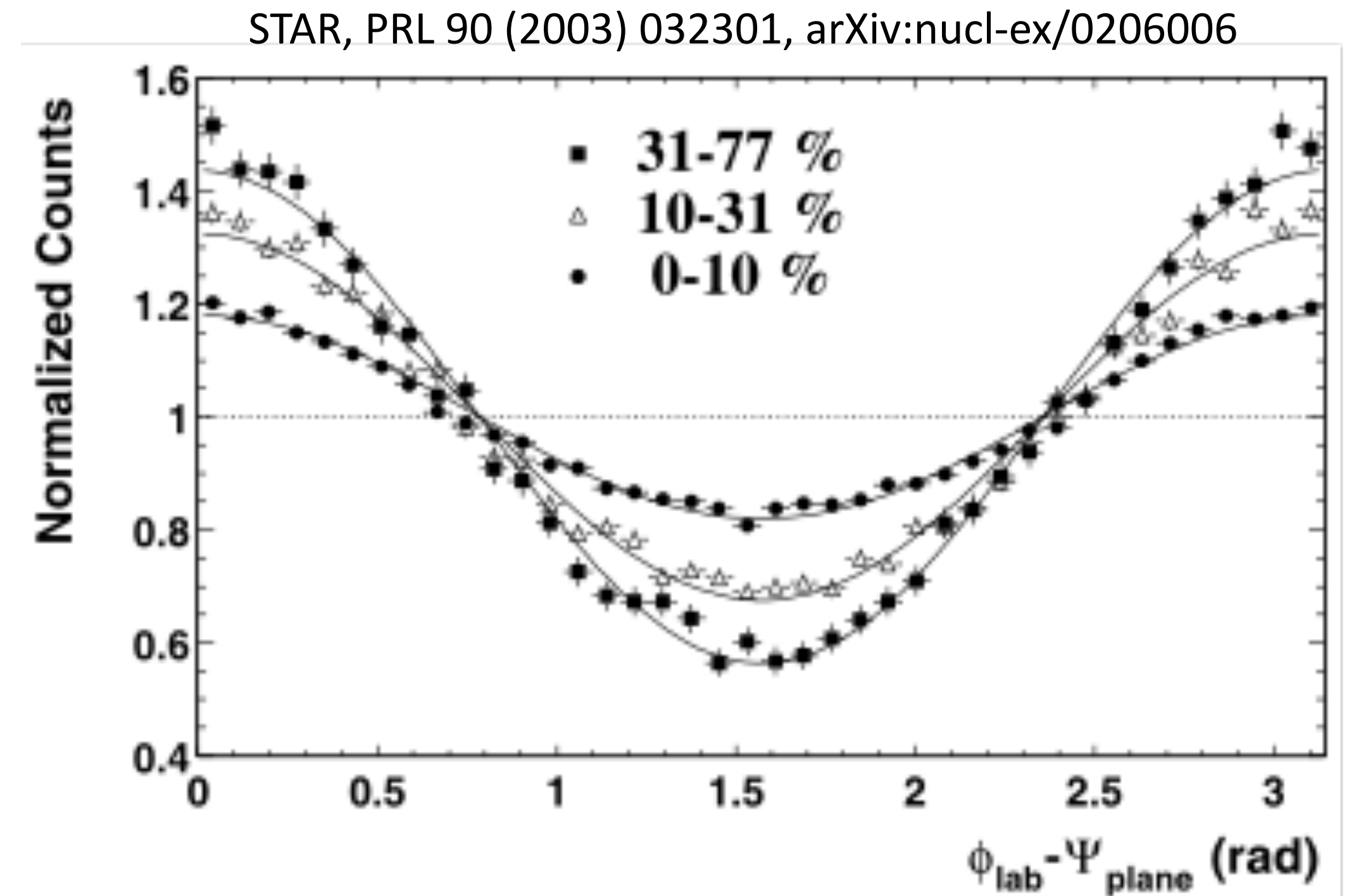
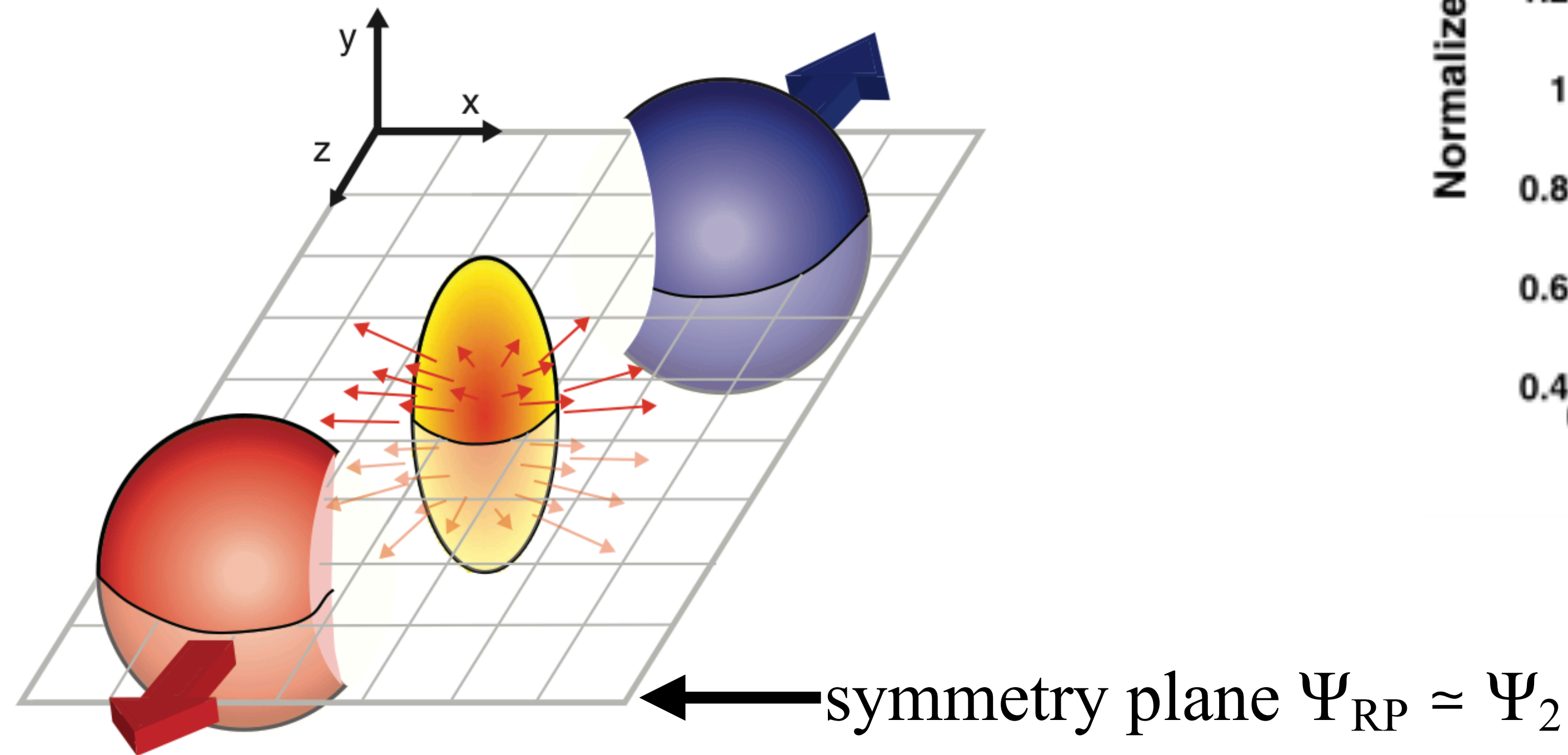
K.M. O’Hara et al., Science, 13 Dec 2002: 2179-2182

# Anisotropic flow coefficients

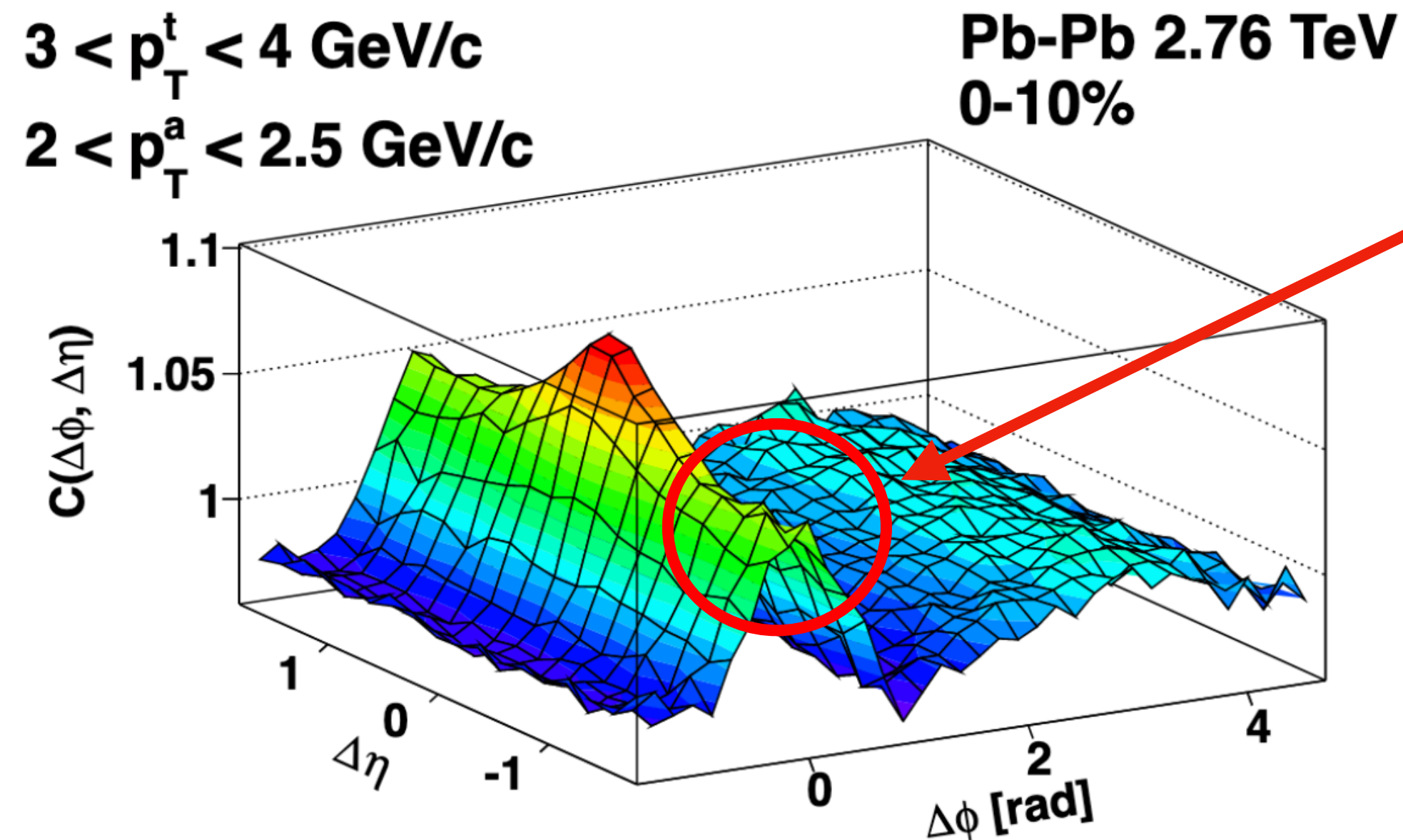
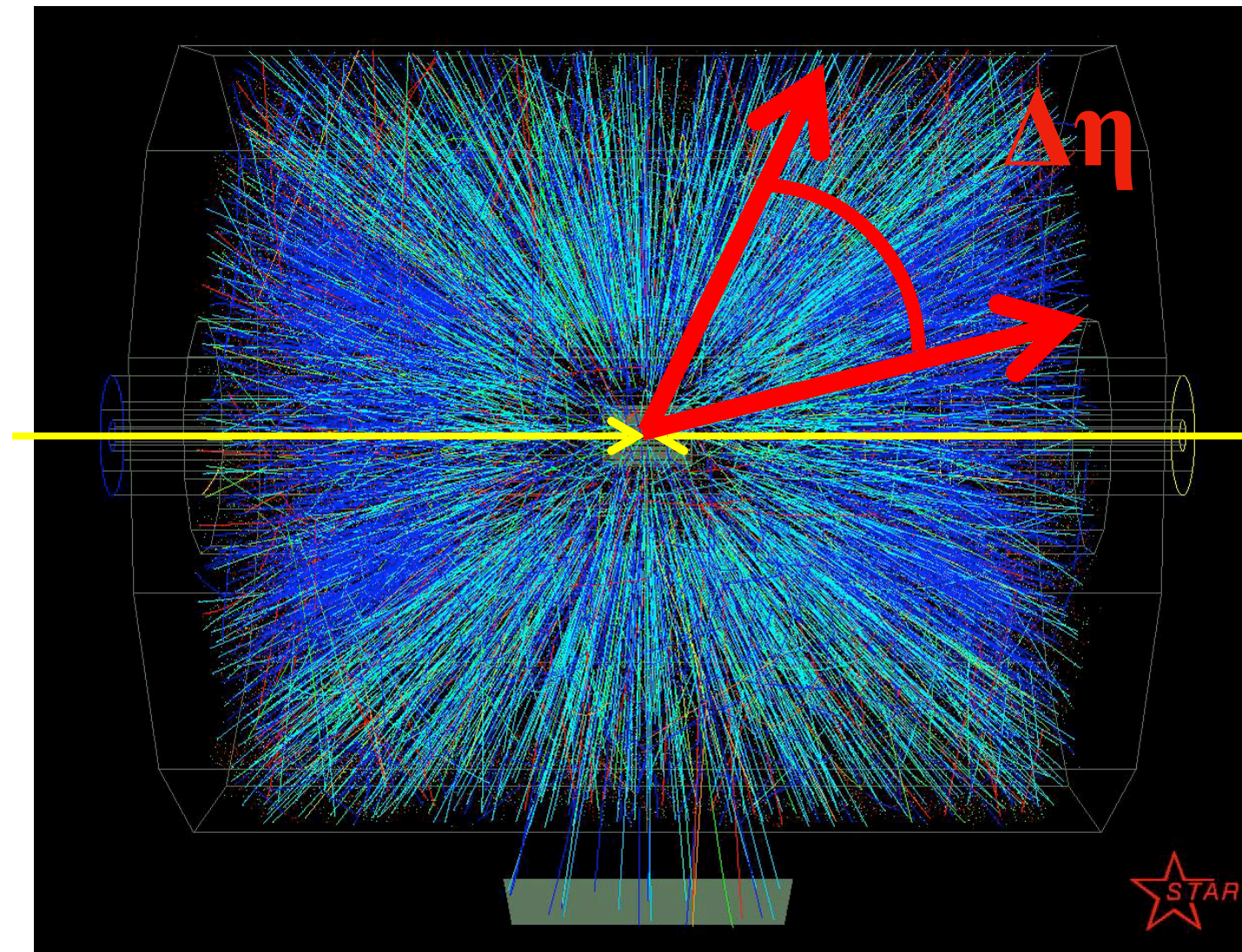
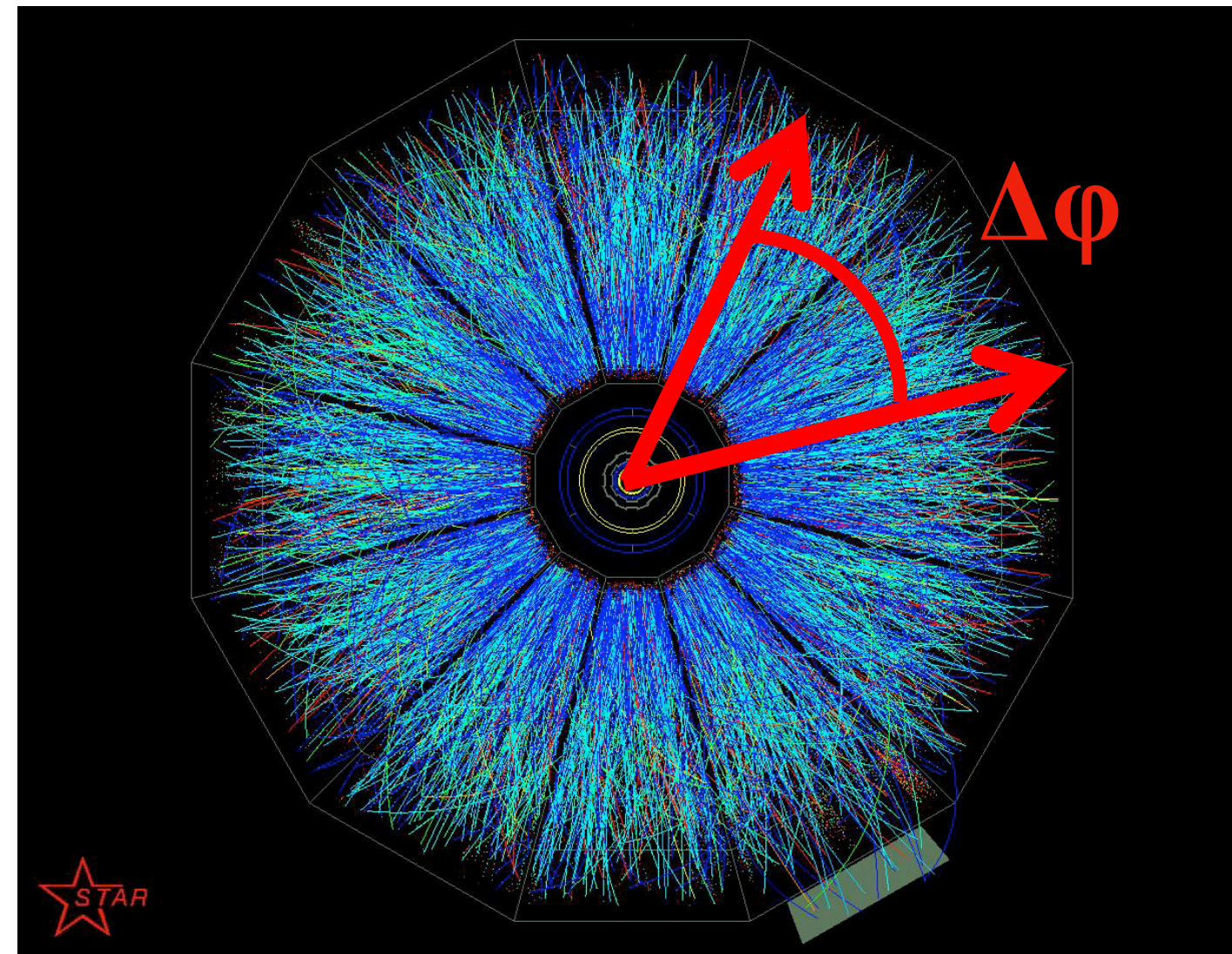
- Particle distribution described by a Fourier cosine series

$$dN/d\phi \sim 1 + 2v_2 \cos(2(\phi - \Psi_2))$$

- $v_2 \rightarrow$  “elliptic flow”



# Two-particle correlations



- Long-range correlations (localized in  $\Delta\phi$ , extended in  $\Delta\eta$ )  
→ collectivity
- Two-particle ( $\Delta\phi$ ) distribution described by Fourier series with coefficients  $v_n^2$   

$$dN/d\phi \sim 1 + 2v_2^2 \cos(2\Delta\phi)$$

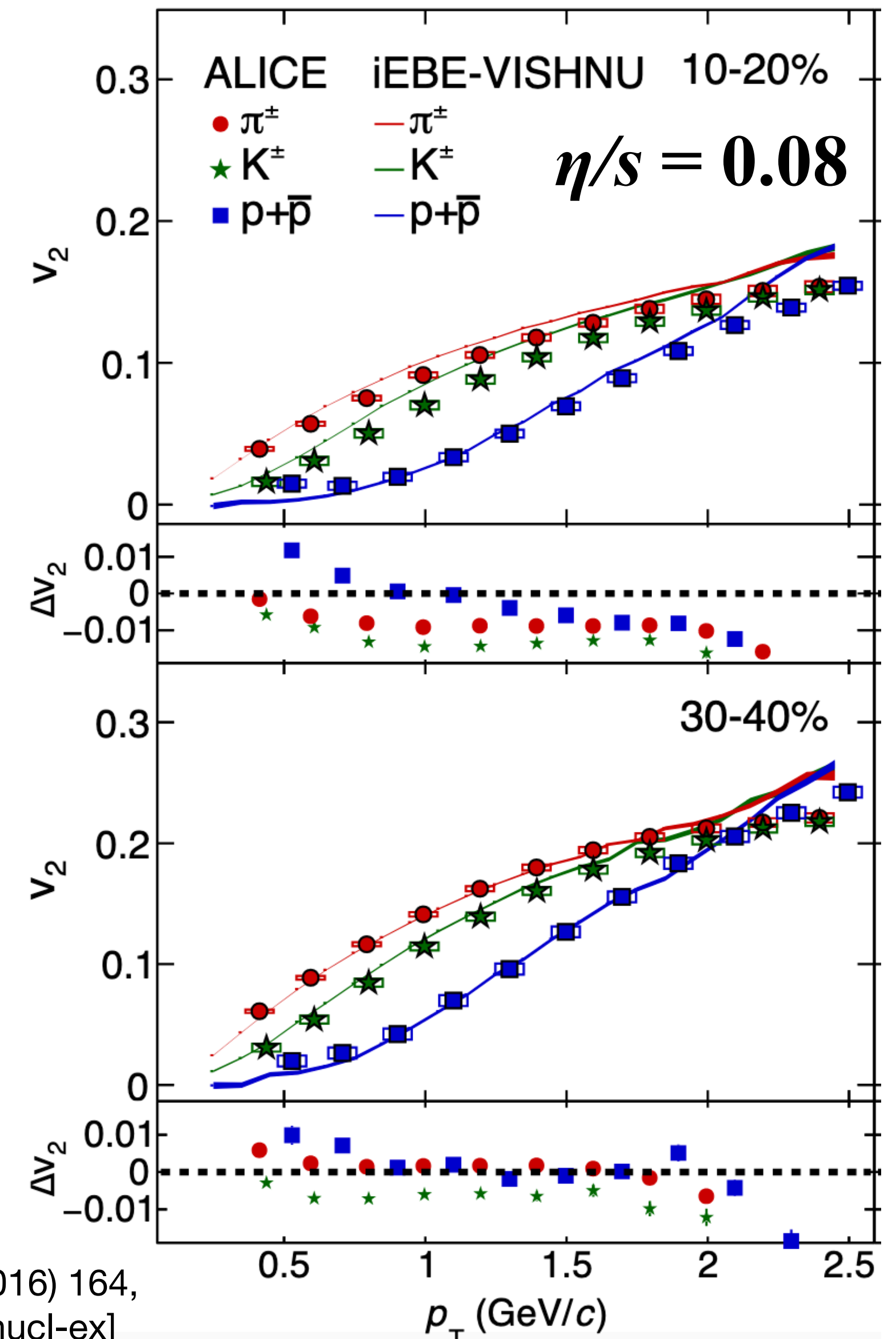
ALICE, PLB 708 (2012) 249, arXiv:1109.2501 [nucl-ex]

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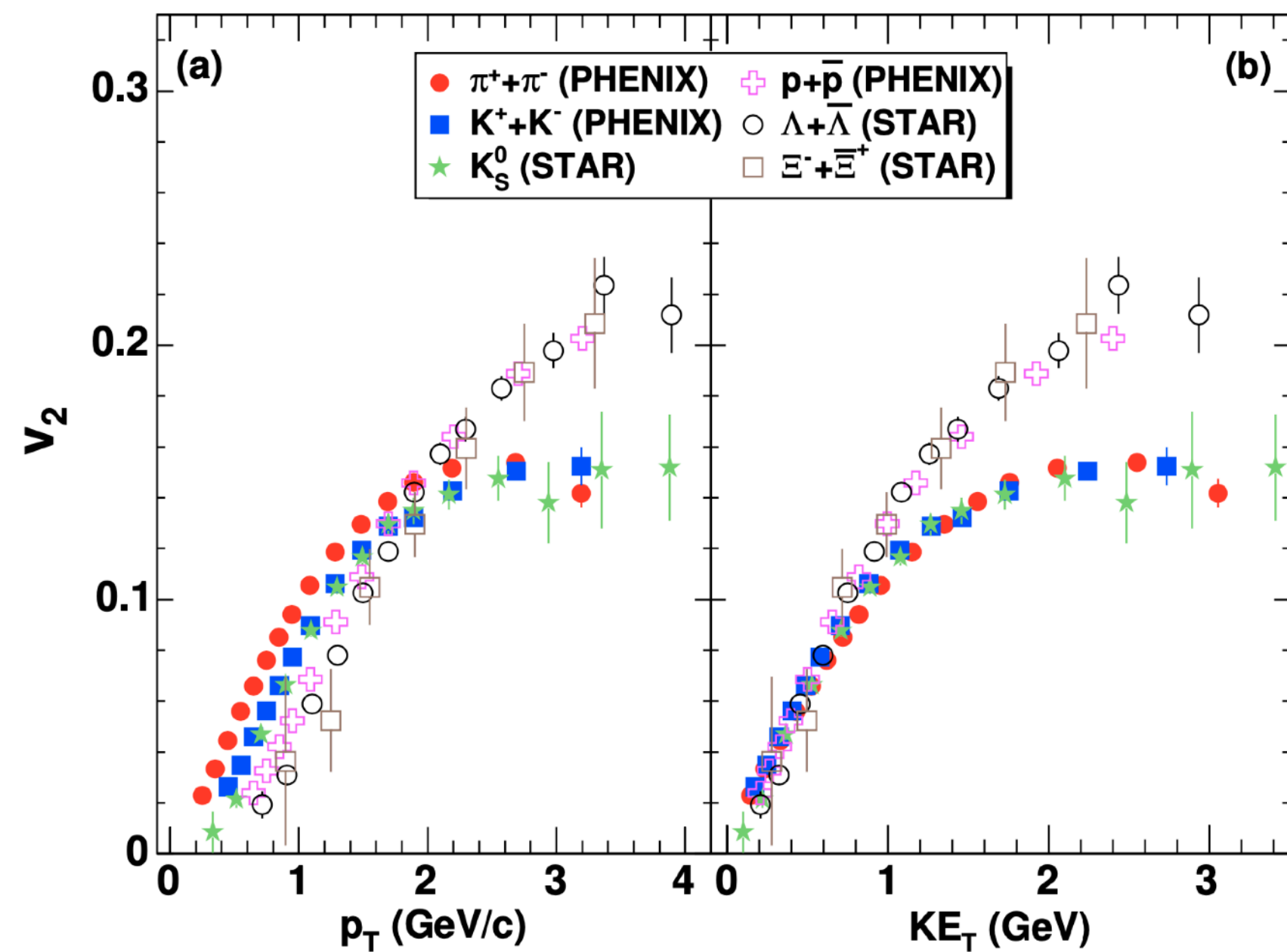
- $v_2 \rightarrow$  “elliptic flow”
- Measurements of  $v_2$  are described very well by hydrodynamic models  $\rightarrow$  QGP behaves as a liquid!
- Viscosity ( $\eta/s$ ) is near quantum lower bound  $\rightarrow$  QGP is the “perfect liquid”



ALICE, JHEP 09 (2016) 164,  
arXiv:1606.06057 [nucl-ex]

# What is flowing?

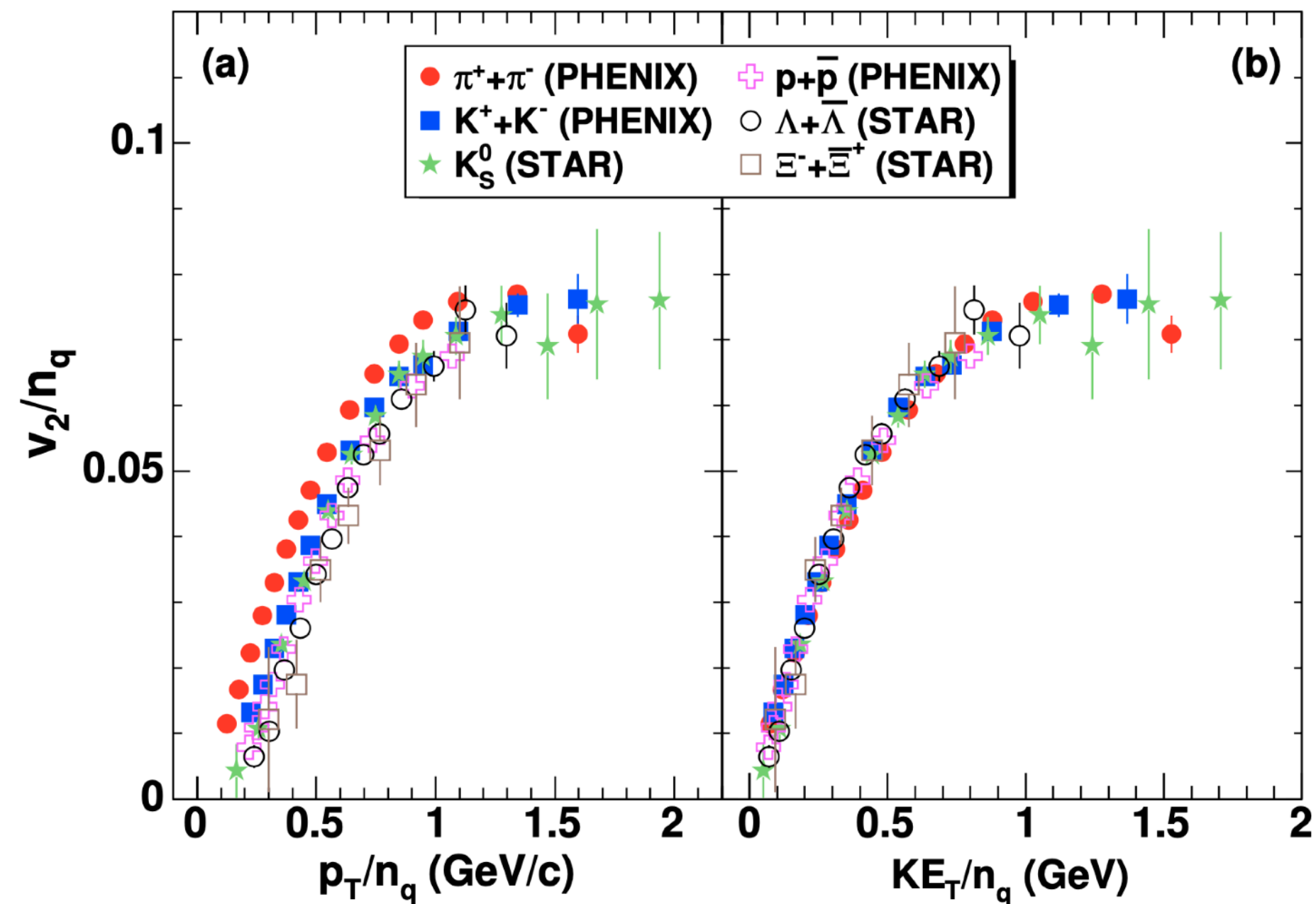
- The RHIC story: when scaled by the number of quarks (NCQ), the flow of different particle species converges on a common curve  $\rightarrow$  flow at the *parton* level
- The LHC story: NCQ scaling broken on the level of 10-20%, it's mostly a mass effect  $\rightarrow$  interesting case is the  $\phi$  meson (2 quarks, but mass similar to the proton), follows the proton at low  $p_T$  and follows the mesons at higher  $p_T$



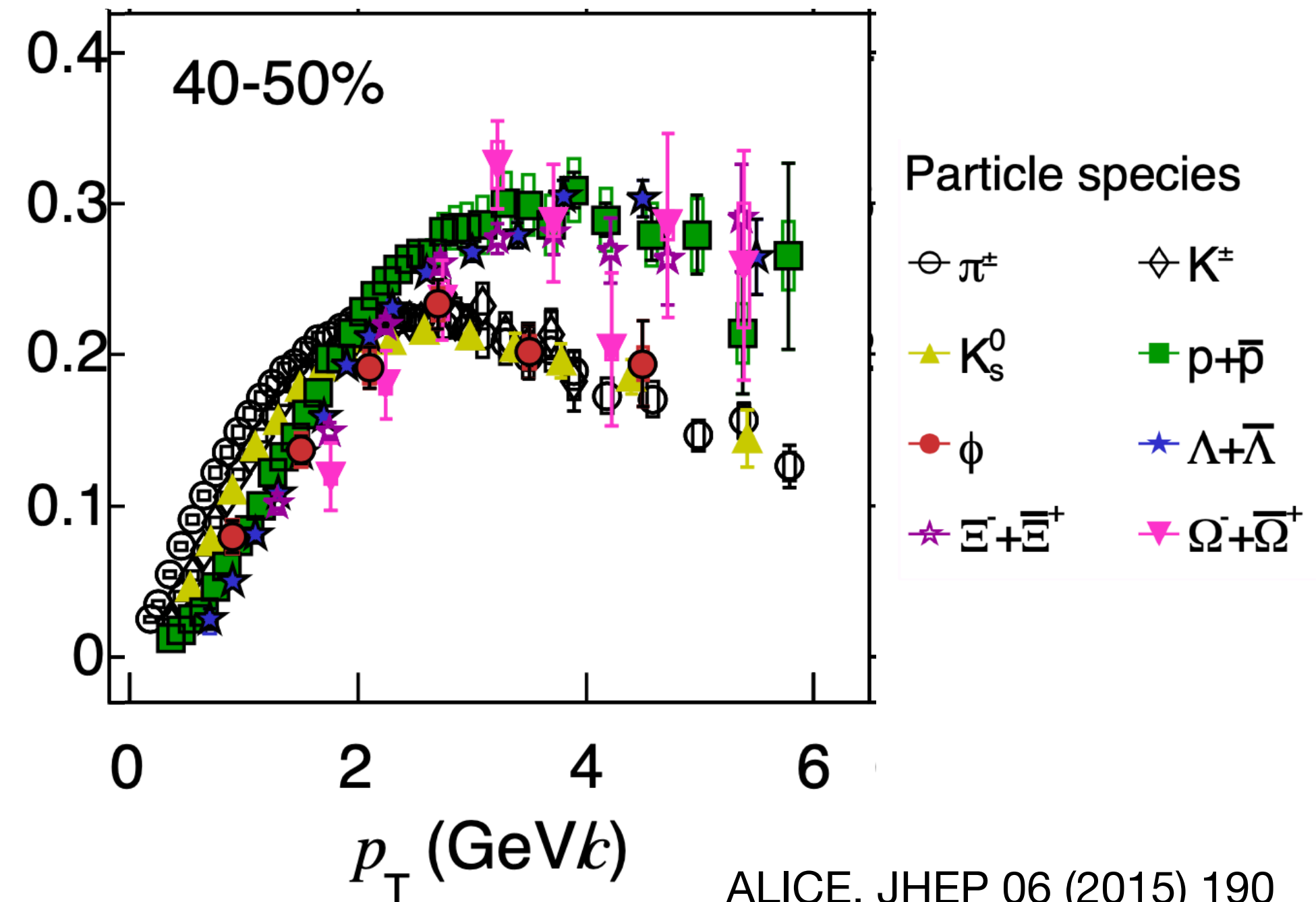
PHENIX, Phys. Rev. Lett 98 (2007)  
162301, arXiv: nucl-ex/0608033

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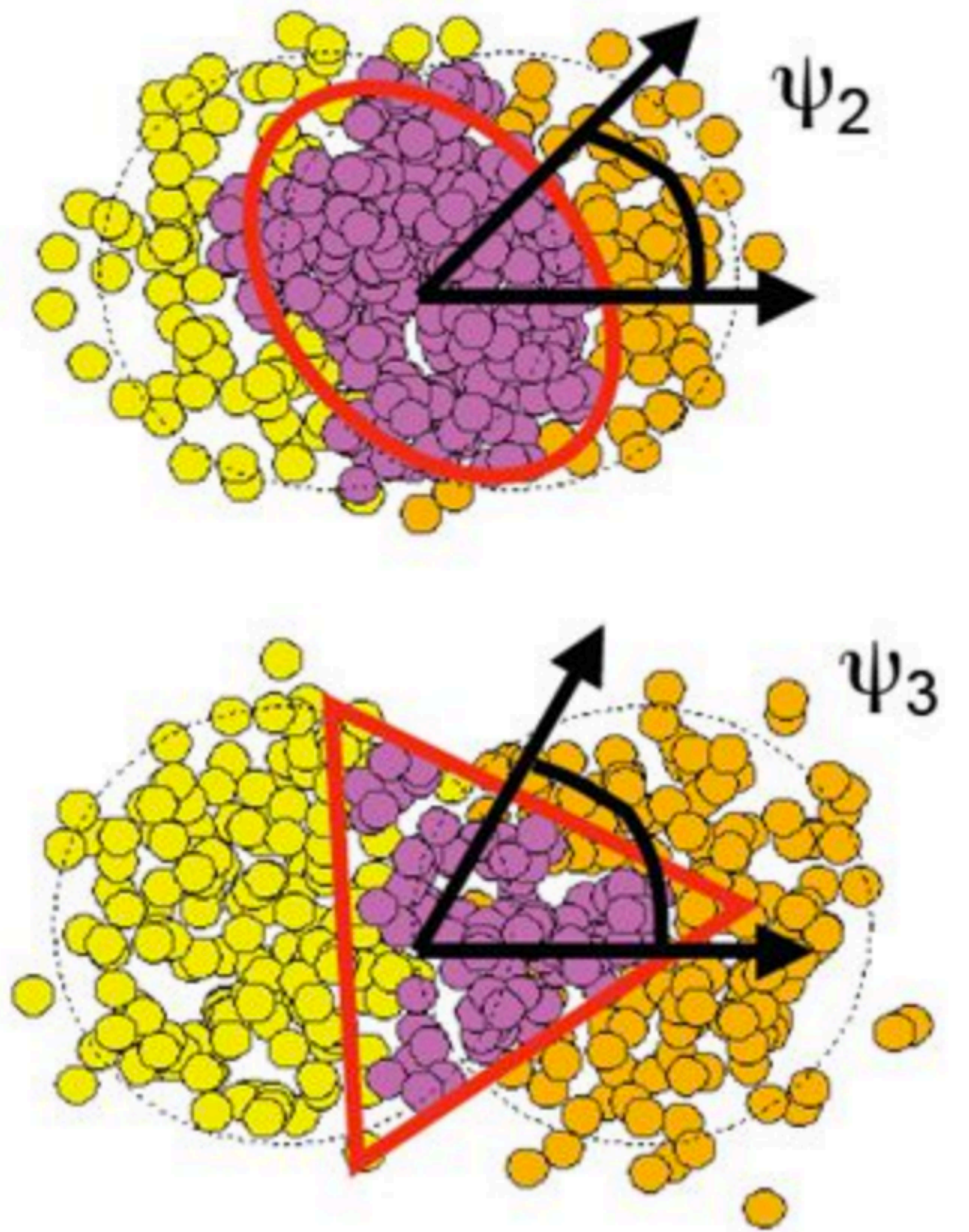


ALICE, JHEP 06 (2015) 190  
arXiv: 1405.4632 [nucl-ex]

# Higher-order flow coefficients

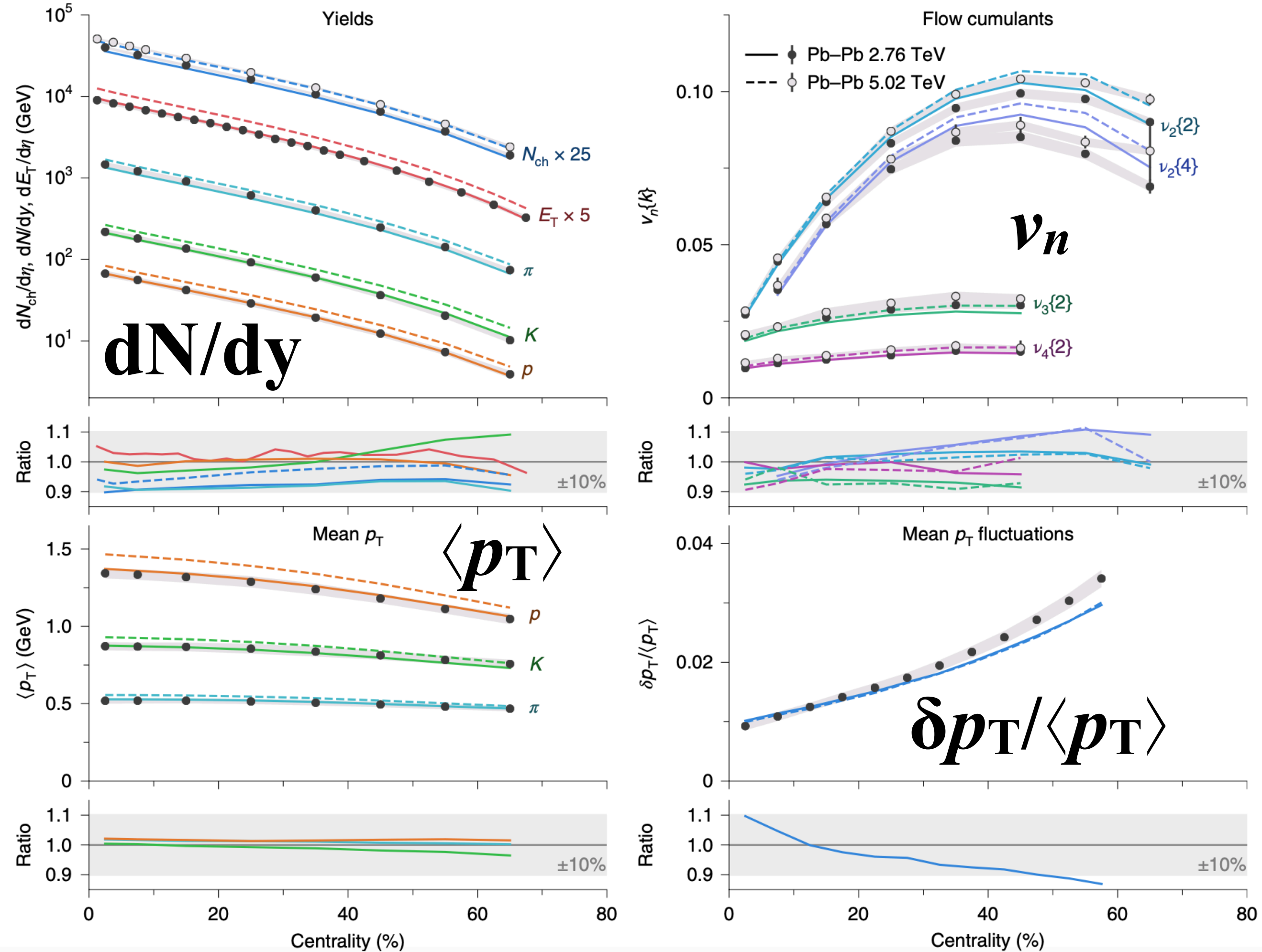
- Due to event-by-event fluctuations of the positions of nucleons, overlap region is not perfectly symmetric  
→ development of triangular flow  $v_3$ , quadrangular flow  $v_4, \dots$  with respect to higher-order symmetry planes  $\Psi_3, \Psi_4, \dots$
- $v_n$  coefficients sensitive to **geometry** and **fluctuations**
- Hydrodynamic response suggests that

$$v_n \propto \epsilon_n$$



# Extracting QGP properties with flow

- Bayesian analysis of particle yields, mean  $p_T$ ,  $v_2$ ,  $v_3$ ,  $v_4$  measured by ALICE



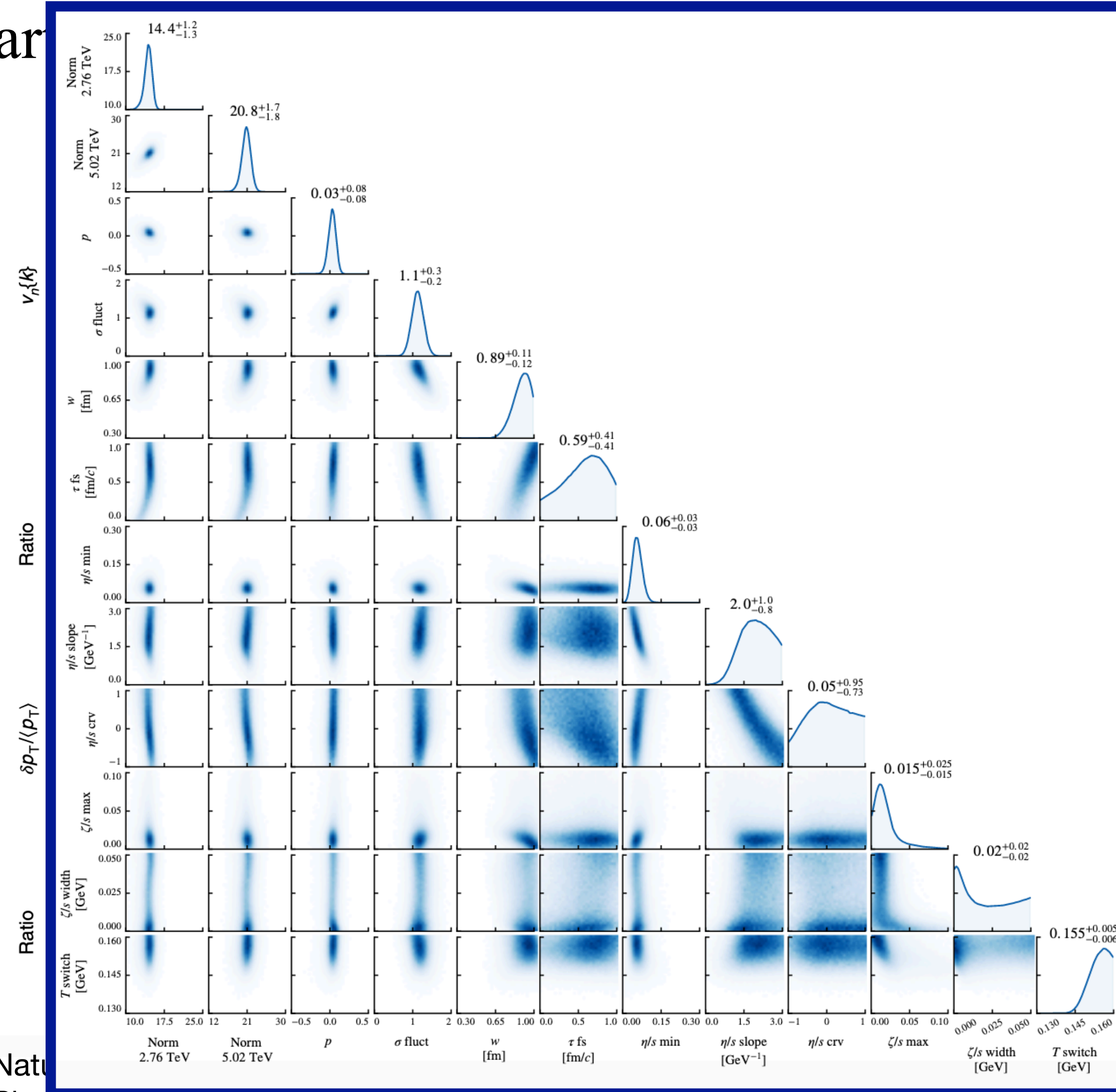
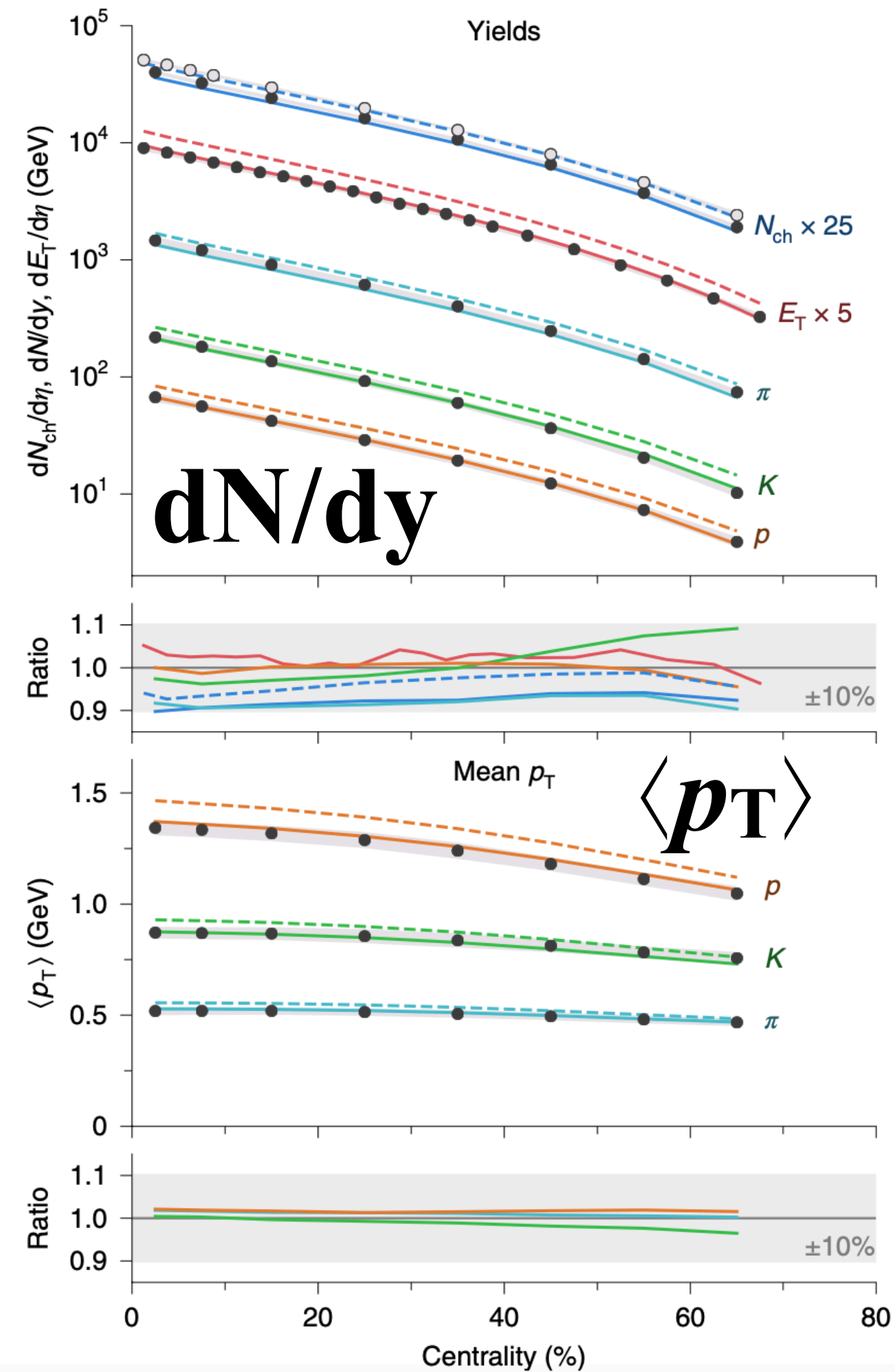
J. E. Bernhard, J. S. Moreland, S. A. Bass, Nature Physics 15 (2019) 1113

J. S. Moreland, J. E. Bernhard, S. A. Bass, Phys. Rev. C 101 (2020) 024911, arXiv:1808.02106 [nucl-th]



# Extracting QGP properties with flow

- Bayesian analysis of par



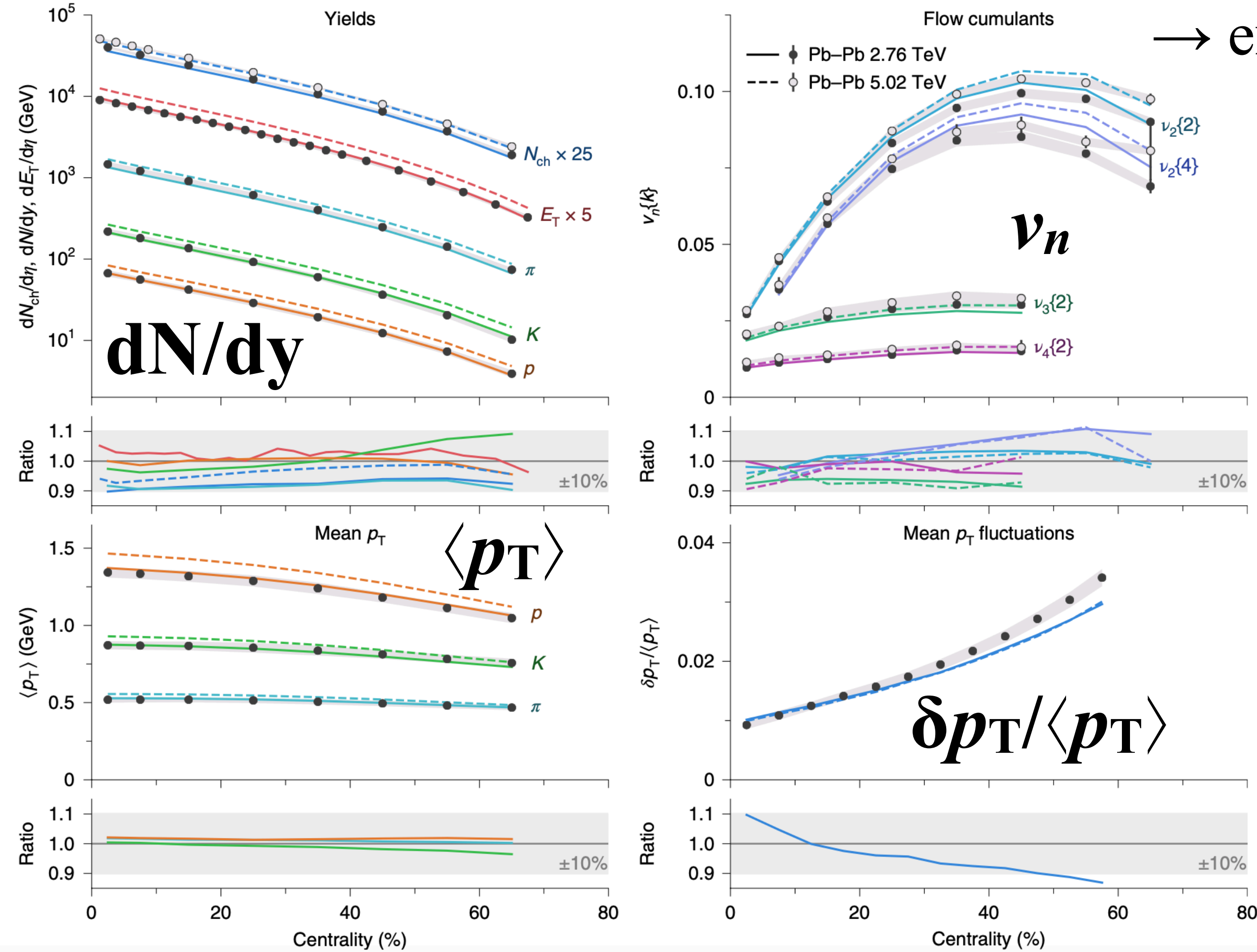
ALICE

J. E. Bernhard, J. S. Moreland, S. A. Bass, Nat

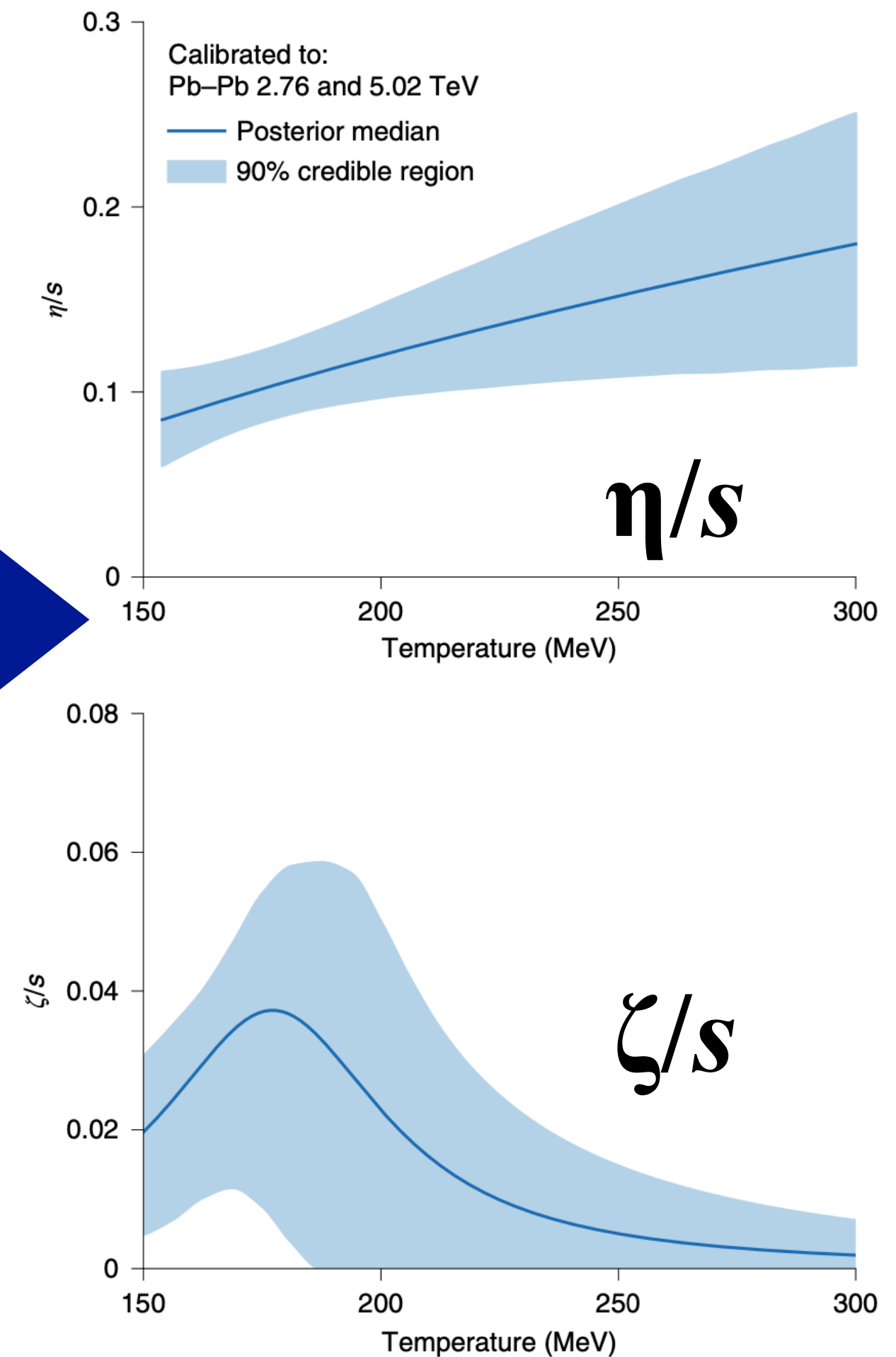
J. S. Moreland, J. E. Bernhard, S. A. Bass, Phys. Rev. C 101 (2020) 024911, arXIV:1808.02106 [nucl-th]

# Extracting QGP properties with flow

- Bayesian analysis of particle yields, mean  $p_T$ ,  $v_2$ ,  $v_3$ ,  $v_4$  measured by ALICE



→ extract shear and bulk viscosity  $\eta/s(T)$ ,  $\zeta/s(T)$

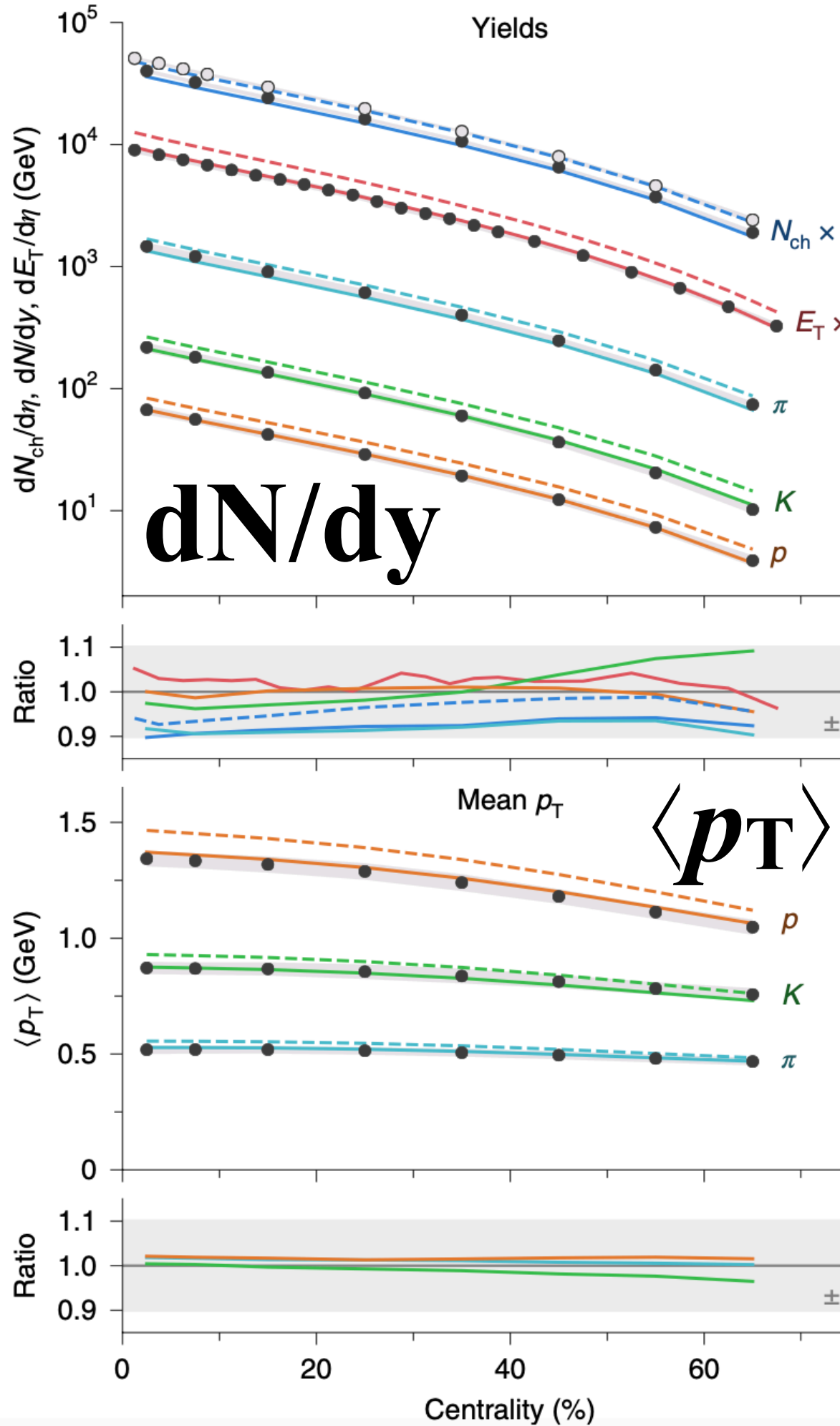


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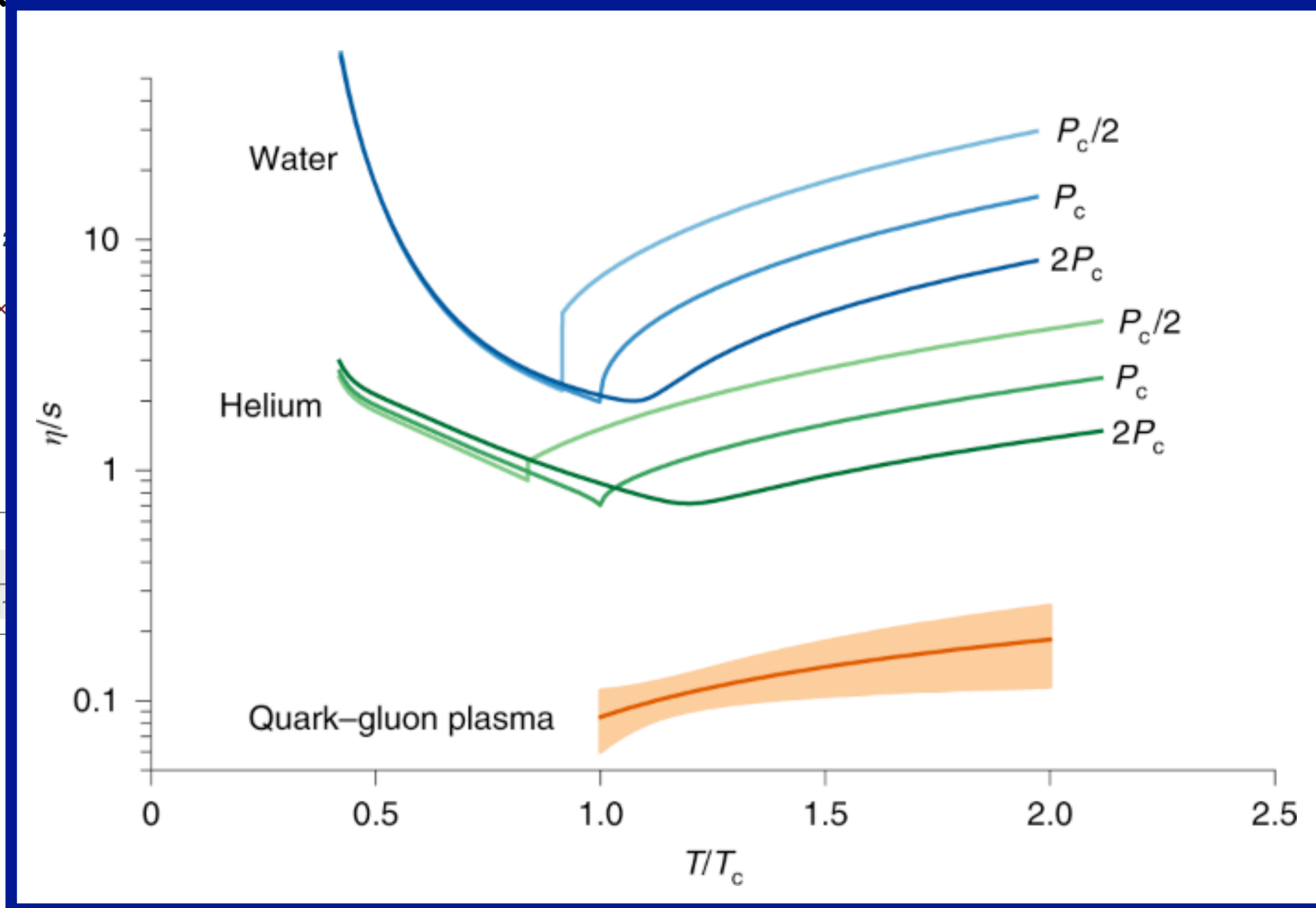
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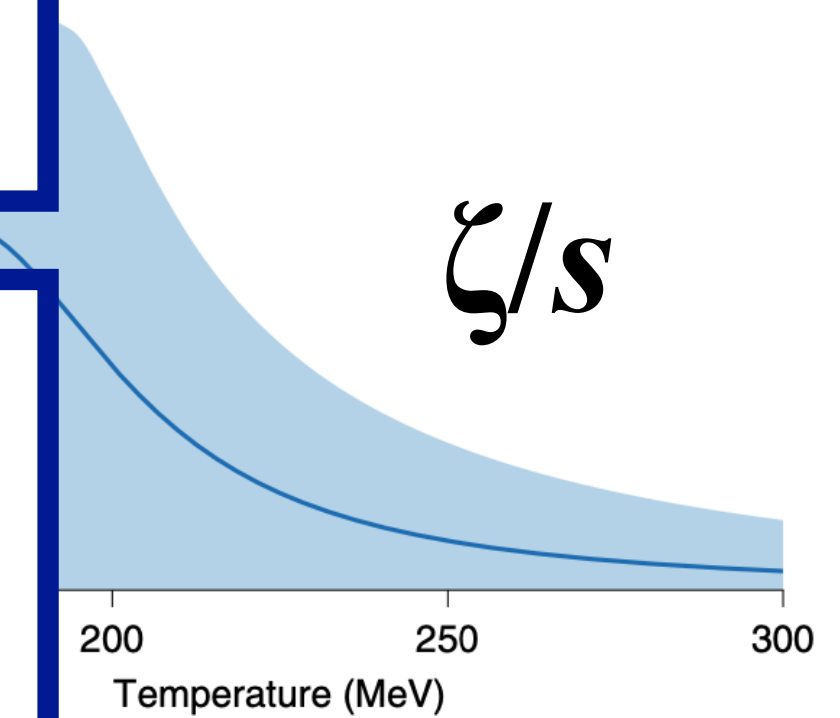
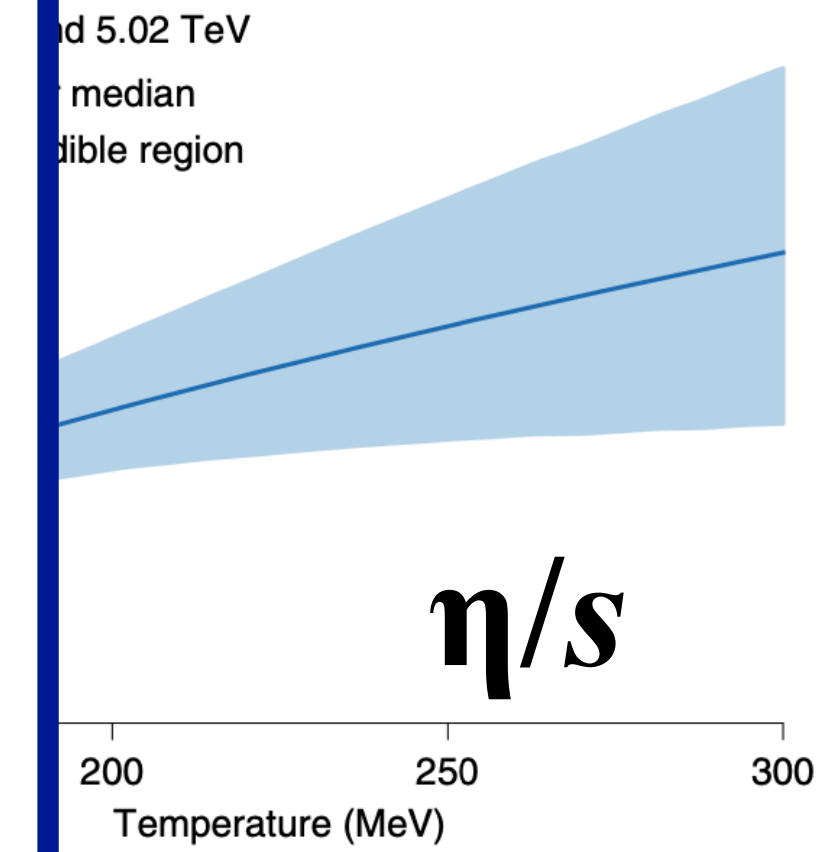


J. E. Bernhard, J. S. Moreland, S. A. Bass, J. S. Moreland, J. E. Bernhard, S. A. Bass



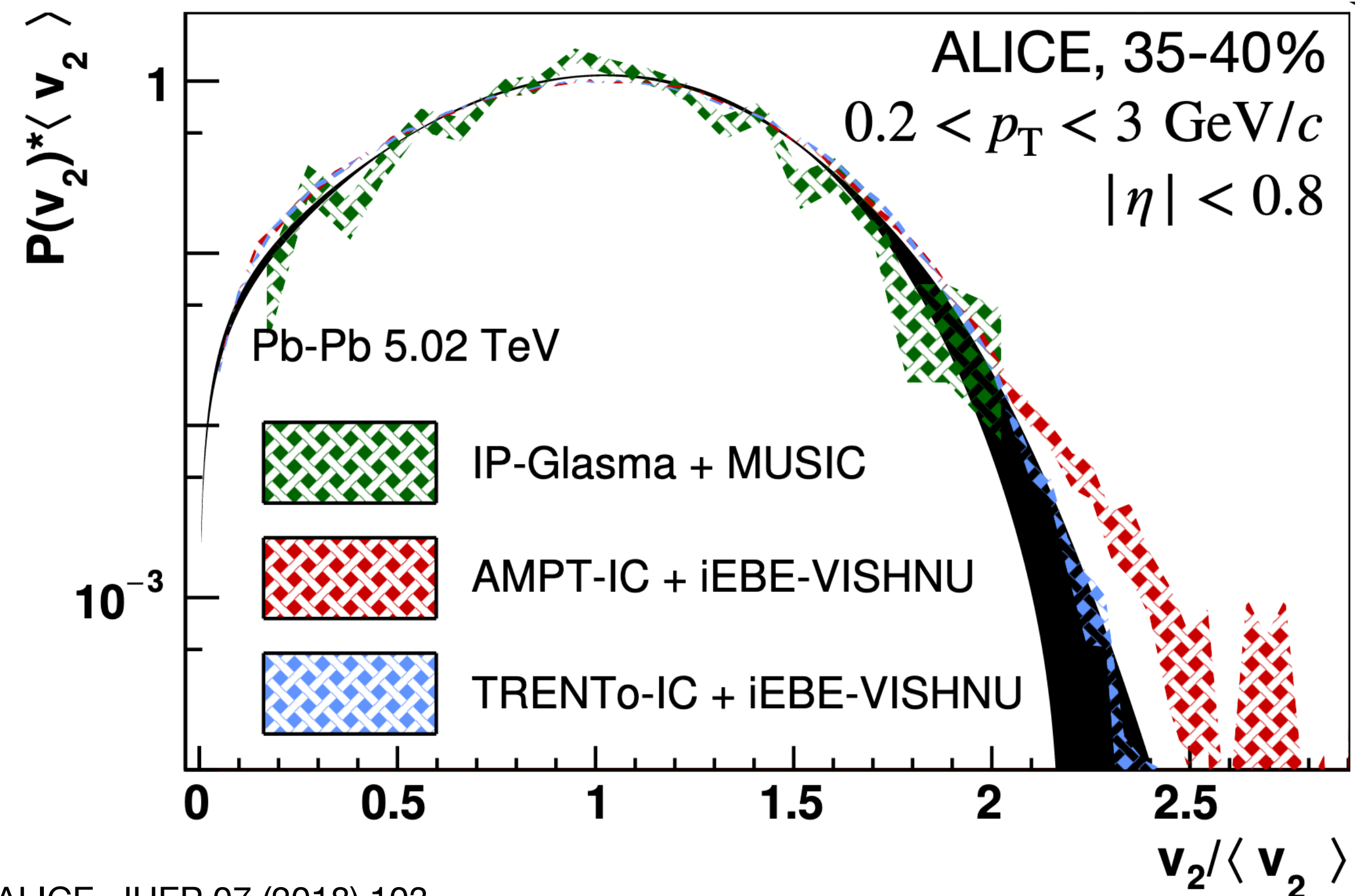
- Similar analyses performed using Trajectum [PRL 126 (2021) 202301, arXiv:2010.15130] and JETSCAPE [PRL 126 (2021) 242301, arXiv:2010.03928]

LICE  
viscosity  $\eta/s(T), \zeta/s(T)$



# Higher-order flow observables and measurements

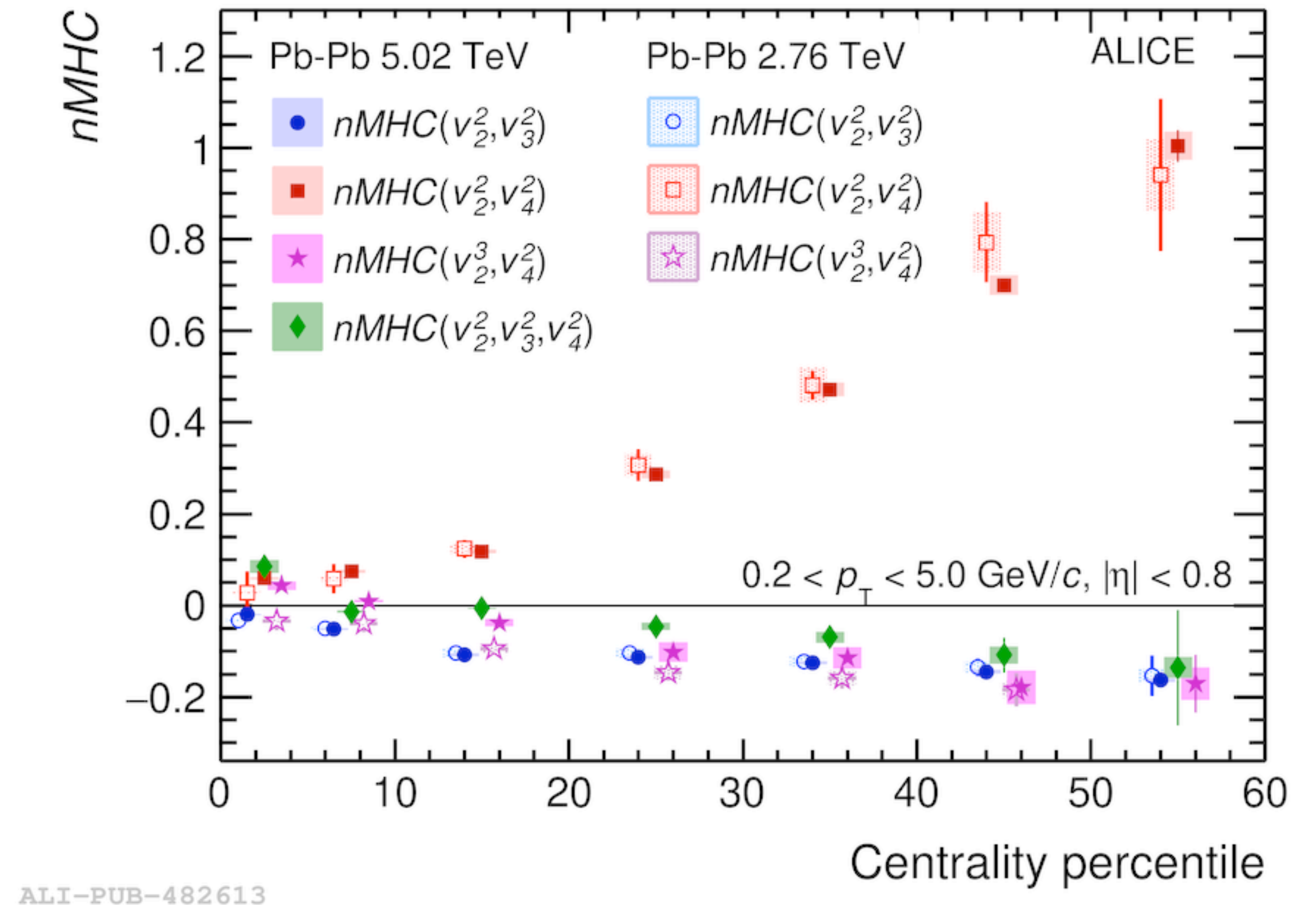
- Differential flow with respect to momentum, particle species, collision energy, pseudorapidity (decorrelation)
- Event-by-event fluctuations of flow



ALICE, JHEP 07 (2018) 103,  
arXiv:1804.02944 [nucl-ex]

# Higher-order flow observables and measurements

- Differential flow with respect to momentum, particle species, collision energy, pseudorapidity (decorrelation)
- Event-by-event fluctuations of flow
- Linear and non-linear flow components beyond  $v_n \propto \epsilon_n$
- Correlations between flow harmonics

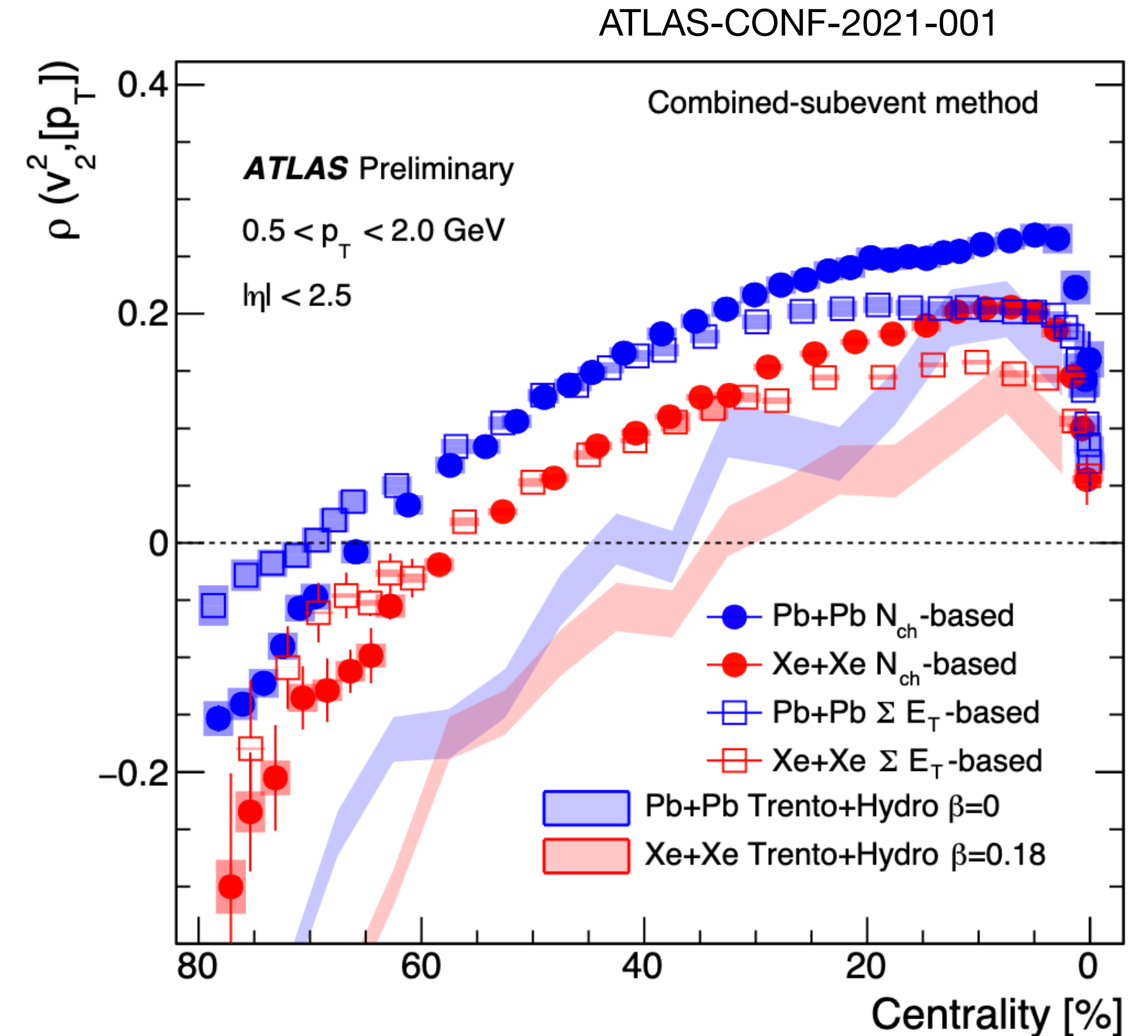


ALICE, PLB 818 (2021) 136354,  
arXiv:2102.12180 [nucl-ex]

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- Differential flow with respect to momentum, particle species, collision energy, pseudorapidity (decorrelation)
- Event-by-event fluctuations of flow
- Linear and non-linear flow components beyond  $v_n \propto \varepsilon_n$
- Correlations between flow harmonics including radial flow

$$\rho(v_n^2, \langle p_T \rangle) = \frac{\text{cov}(v_n^2, \langle p_T \rangle)}{\sqrt{\text{var}(v_n^2)} \sqrt{\text{var}(\langle p_T \rangle)}}$$



# Higher-order flow observables and measurements

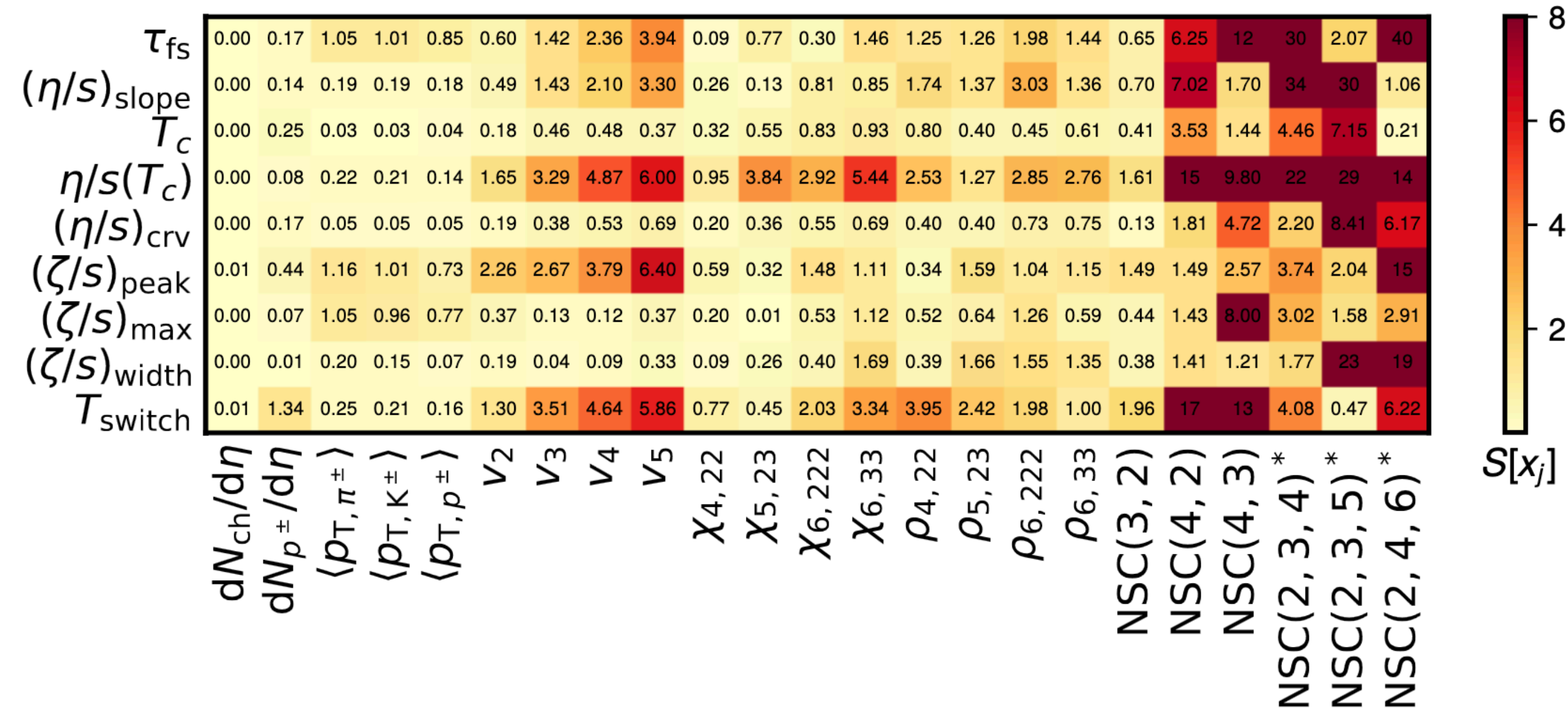
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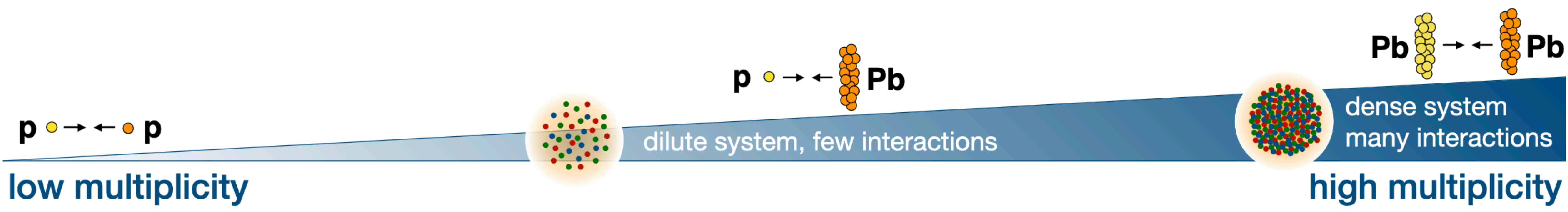
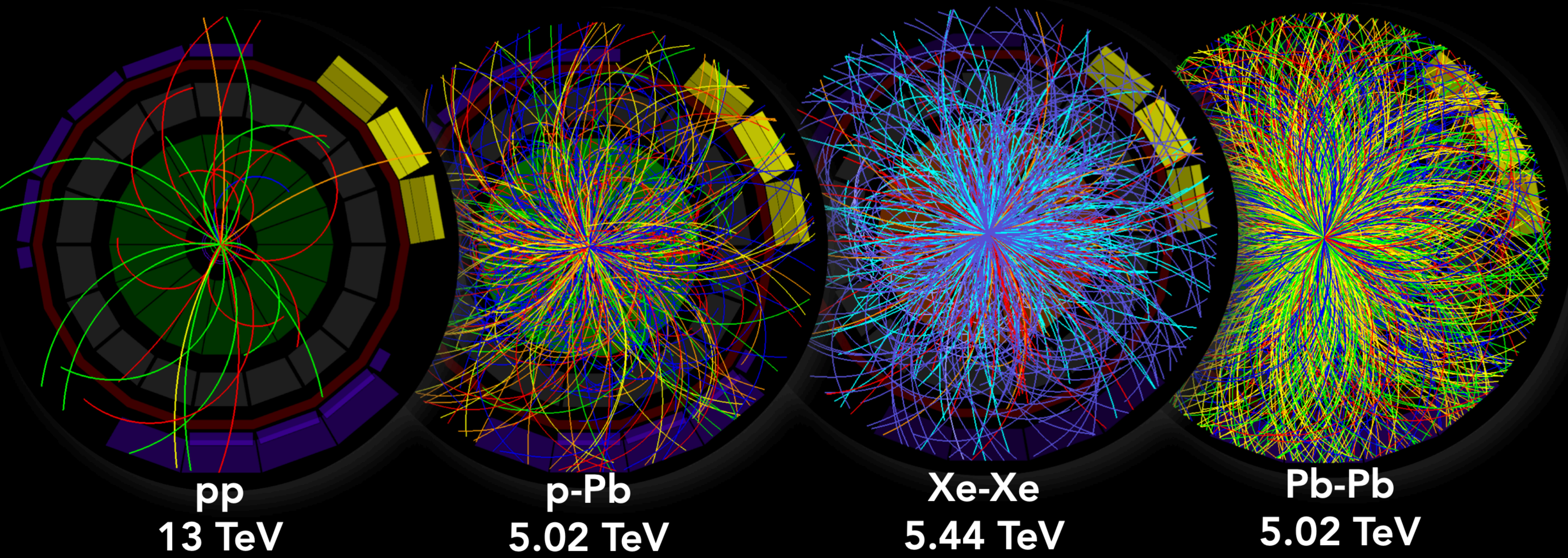
- Linear and non-linear flow components beyond  $v_n \propto \epsilon_n$

- Correlations between flow harmonics including radial flow

- These higher-order observables are very sensitive to properties of the QGP!



J.E. Parkkila, A. Onnerstad, S. F. Taghavi, C. Mordasini, A. Bilandzic, D.J. Kim, arXiv: 2111.08145 [hep-ph]

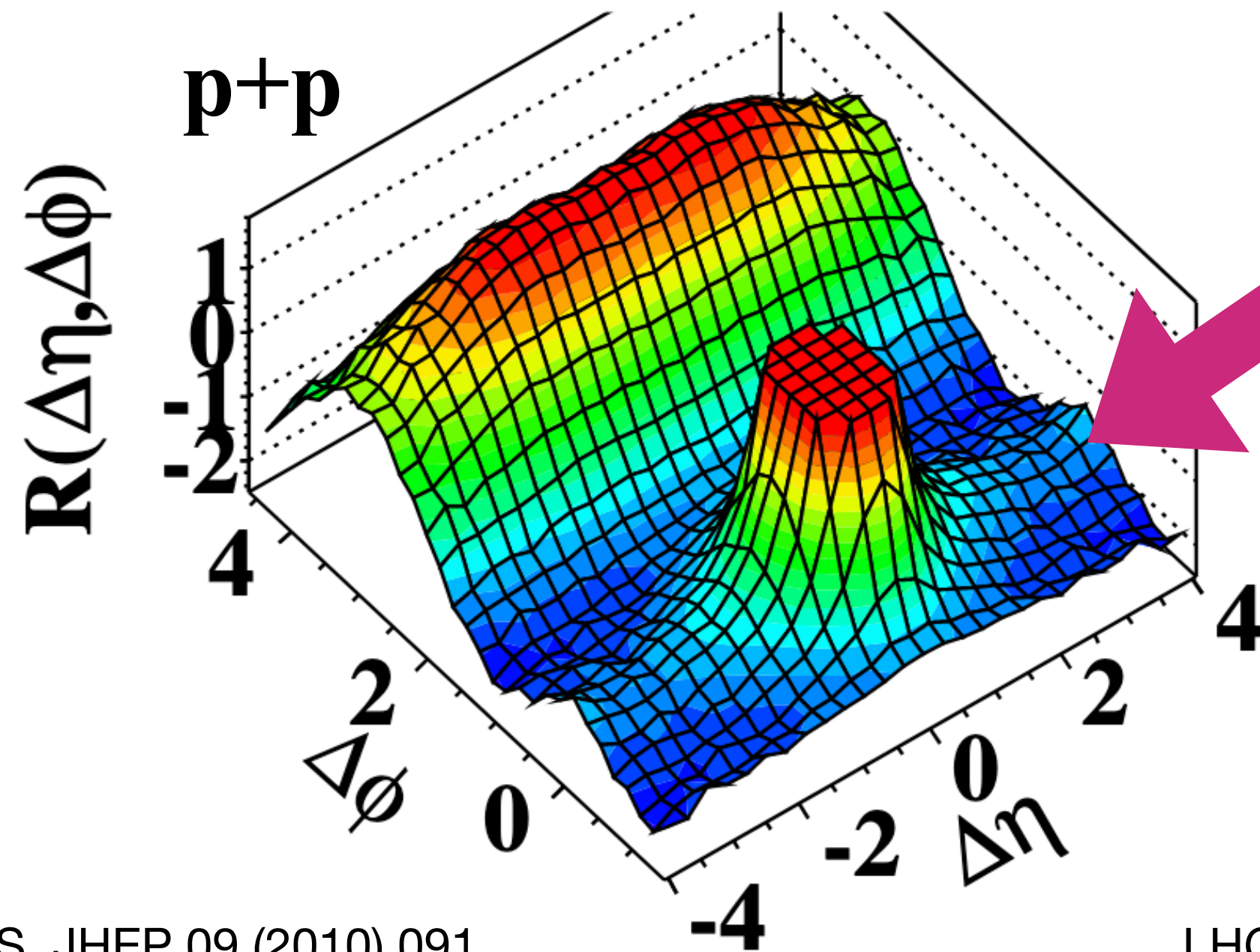




# Collective behavior in small systems

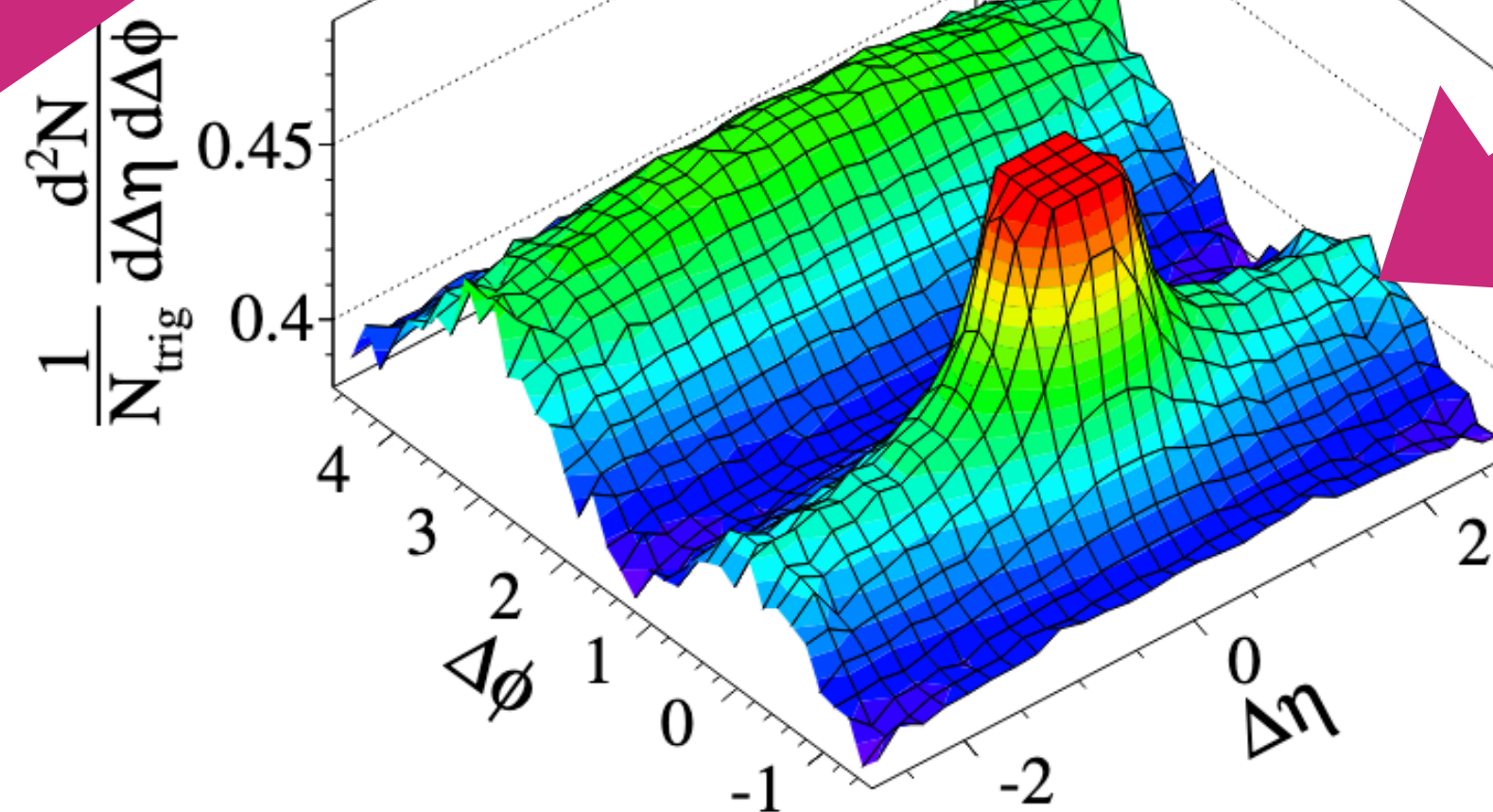
- Flow-like ( $v_n$ ) signals observed in high-multiplicity p+p and p+Pb collisions as well!

(d) CMS  $N \geq 110$ ,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$

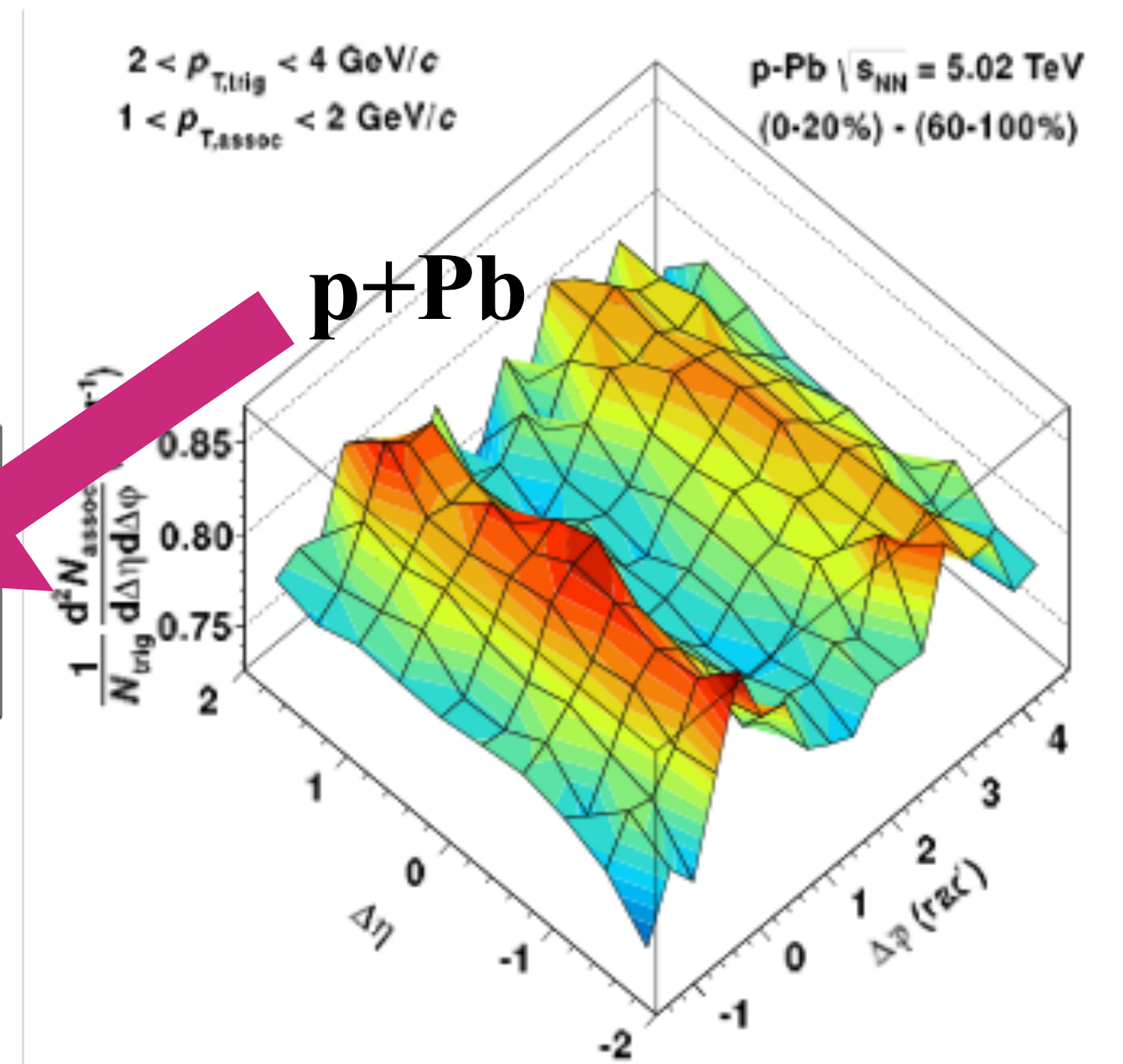


CMS, JHEP 09 (2010) 091,  
arXiv: 1009.4122 [hep-ex]

LHCb **Pb+p**  $\sqrt{s_{NN}} = 5 \text{ TeV}$   
 $2.0 < p_T < 3.0 \text{ GeV}/c$   
Event class 0-3%



LHCb, PLB 762 (2016) 473,  
arXiv:1512.00439 [nucl-ex]

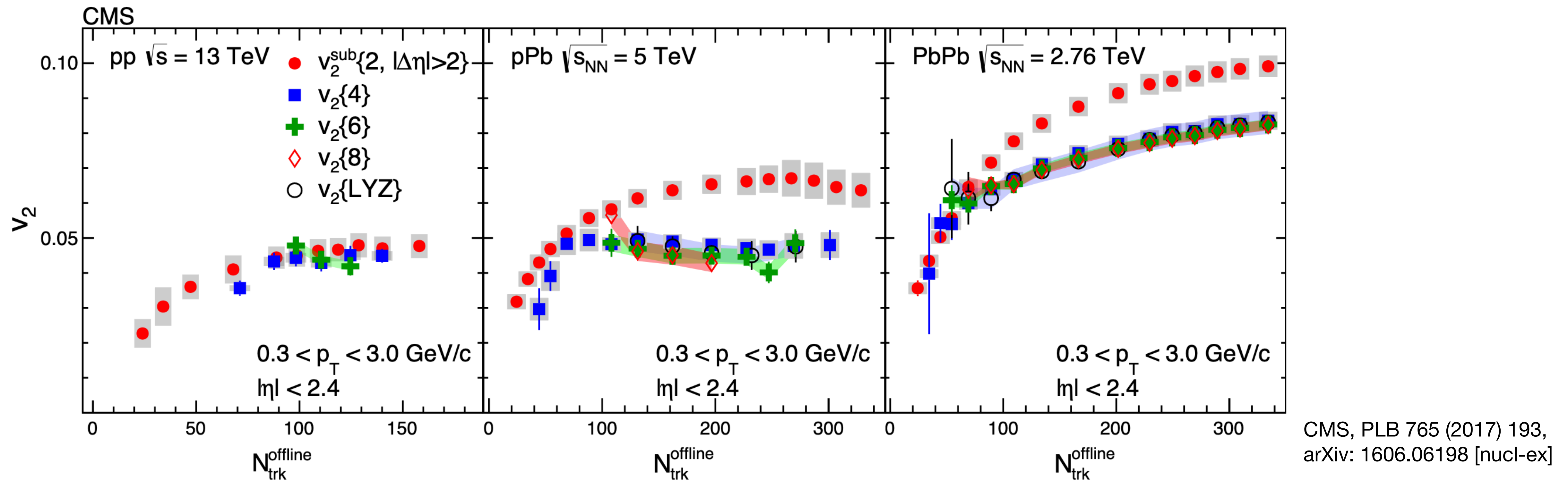


ALICE, PLB 719 (2013) 29,  
arXiv: 1212.2001 [nucl-ex]

*Surprise!*

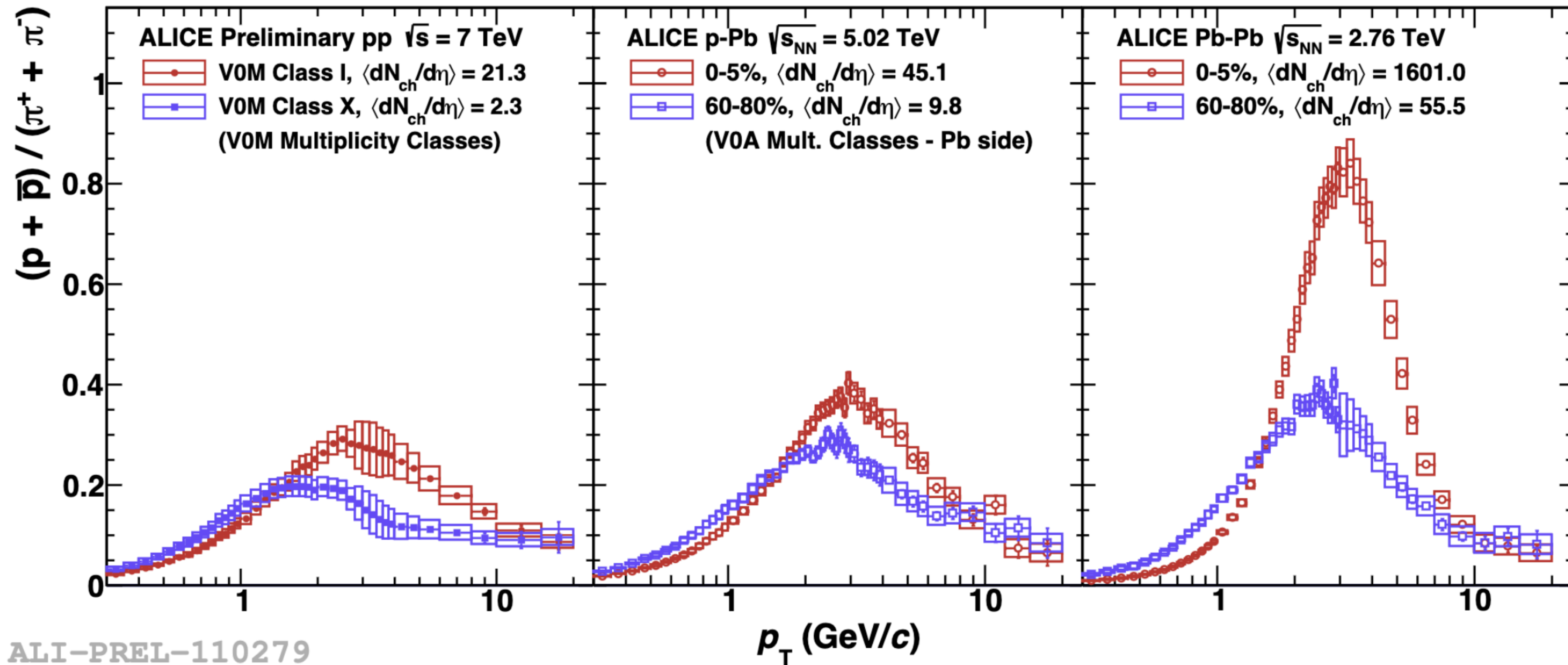
# But is it collective...?

- Collectivity: momentum **correlations** among **many particles** which are **widely separated** (e.g. in pseudorapidity)
- Multi-particle cumulants used to measure non-zero  $v_2$



- Remember! Collectivity (an observation) does not imply hydrodynamics (an interpretation)

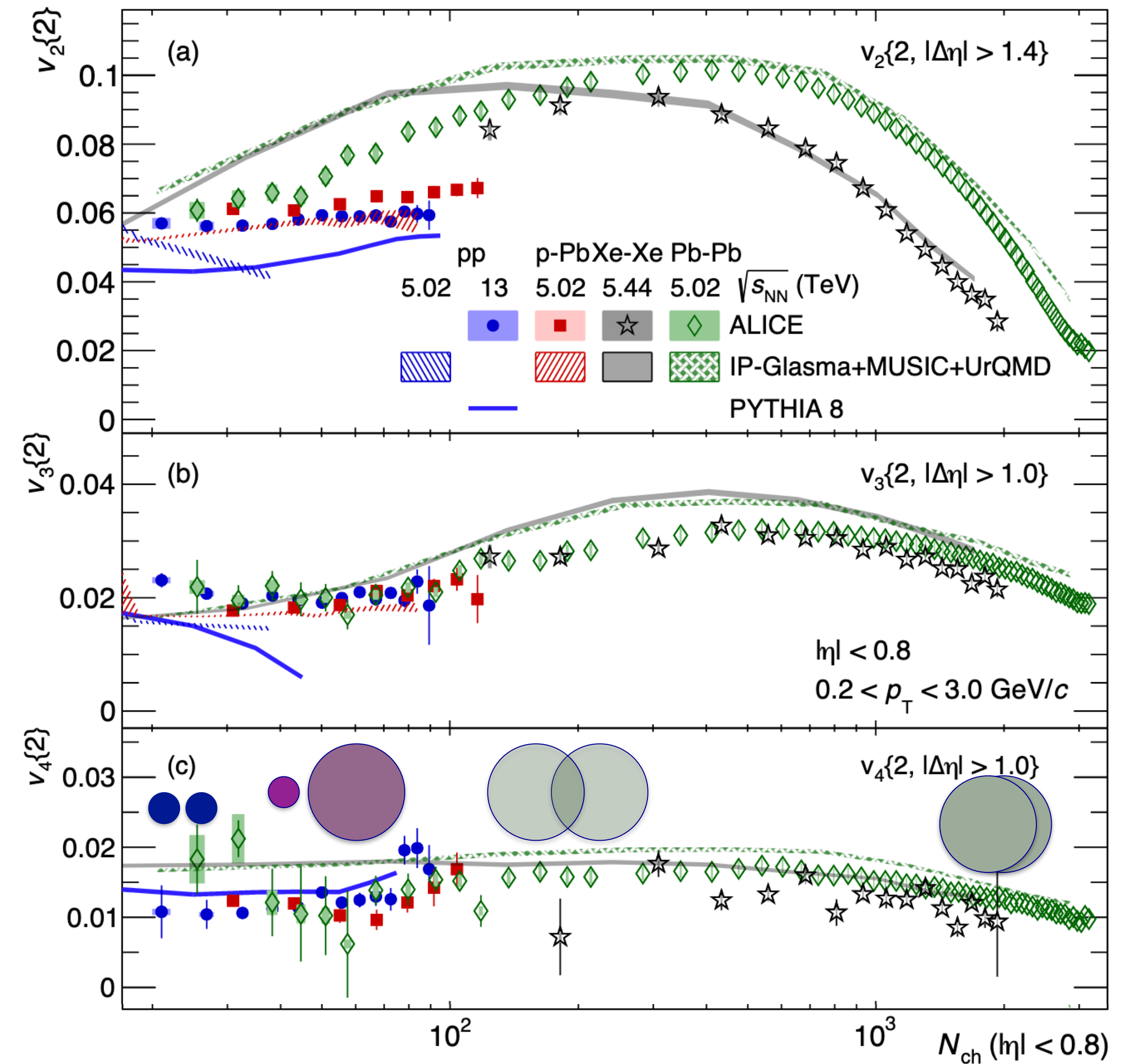
# Isotropic flow



- Increase in baryon-to-meson ratio indicates presence of radial boost in p+p, p+Pb, Pb+Pb

# Anisotropic flow $v_n$

- Non-zero  $v_n$  coefficients measured across all multiplicities in p+p, p+Pb, Xe+Xe, and Pb+Pb systems
- No clear “turn-off” or “turn-on” of collectivity
- Is this hydrodynamic flow?  
Is there a geometry in small systems? Or is it just fluctuations?  
Are there enough parton-parton interactions to produce this collective effect (e.g. translate the initial anisotropy to the final state)?



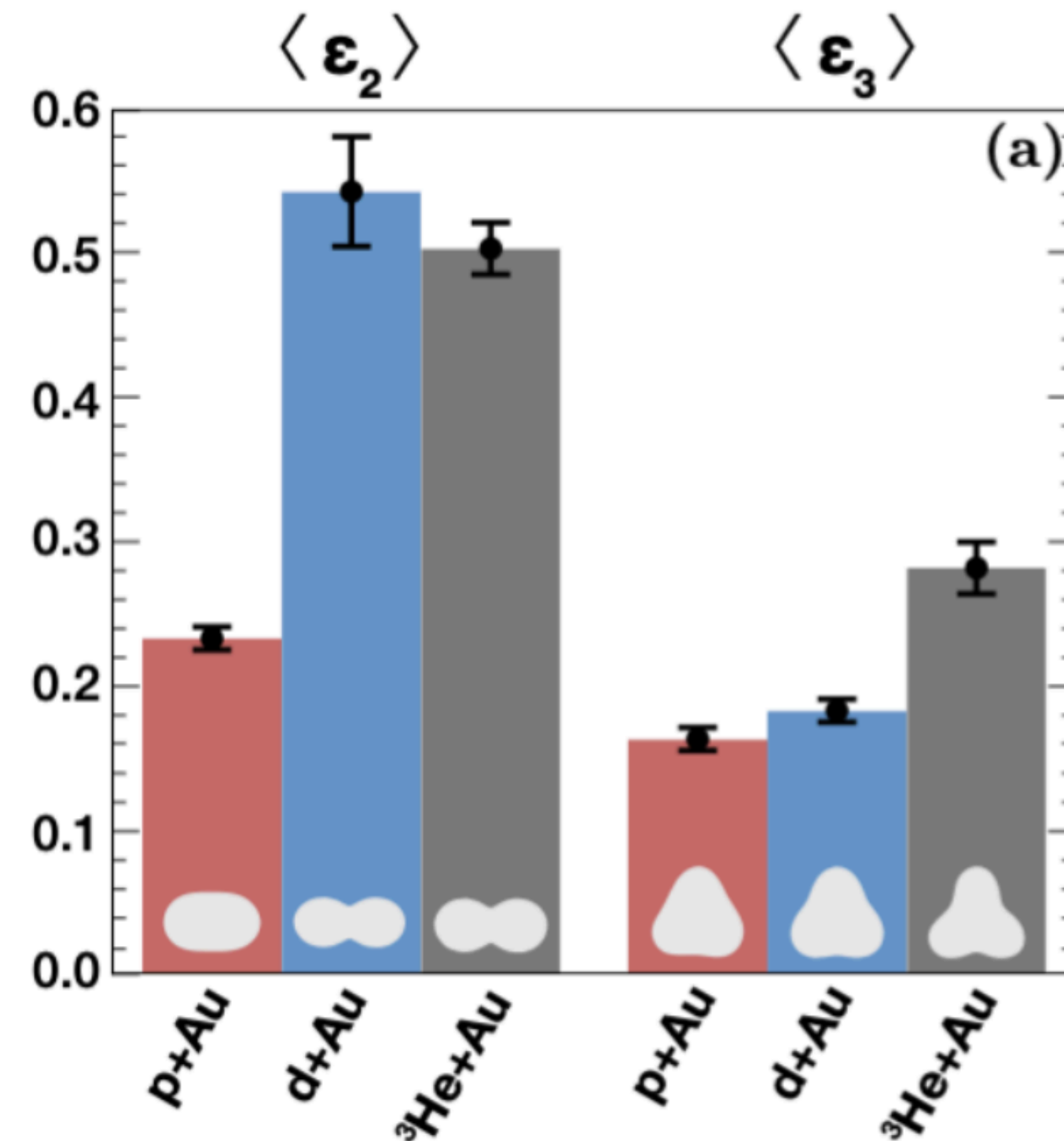
ALICE, PRL 123 (2019) 142301, arXiv: 1903.01790 [nucl-ex]

# The role of initial geometry

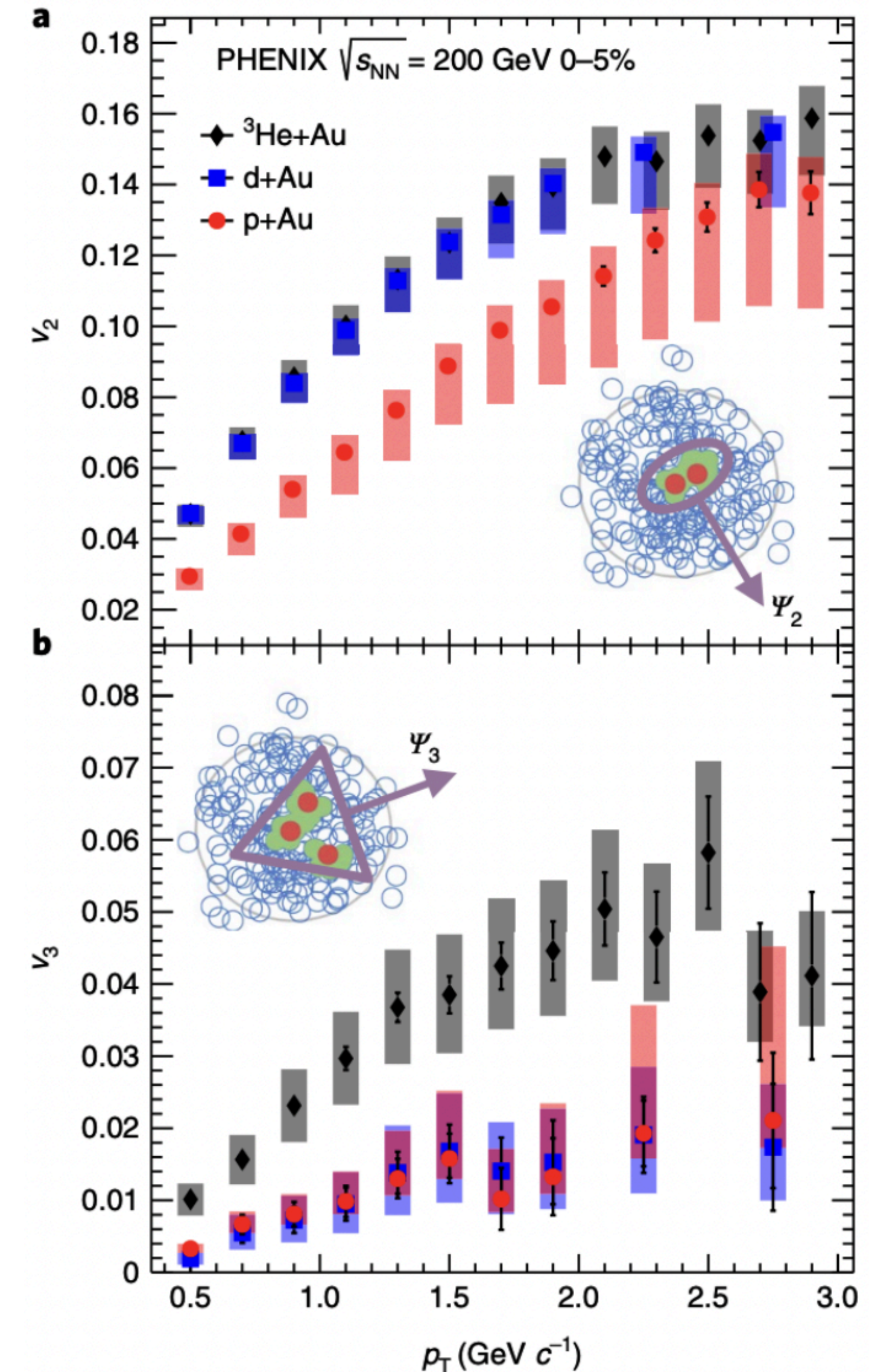
- $v_2$  measured in spherical (p+Au), ellipsoidal (d+Au), and triangular ( $^3\text{He}+\text{Au}$ ) systems
- Hydrodynamics predicts translation from initial state eccentricity to final state anisotropy  $v_n \propto \epsilon_n$
- Measurements consistent with hydro expectation

$$v_2^{\text{p+Au}} < v_2^{\text{d+Au}} \approx v_2^{\text{He+Au}}$$

$$v_3^{\text{p+Au}} \approx v_3^{\text{d+Au}} < v_3^{\text{He+Au}}$$

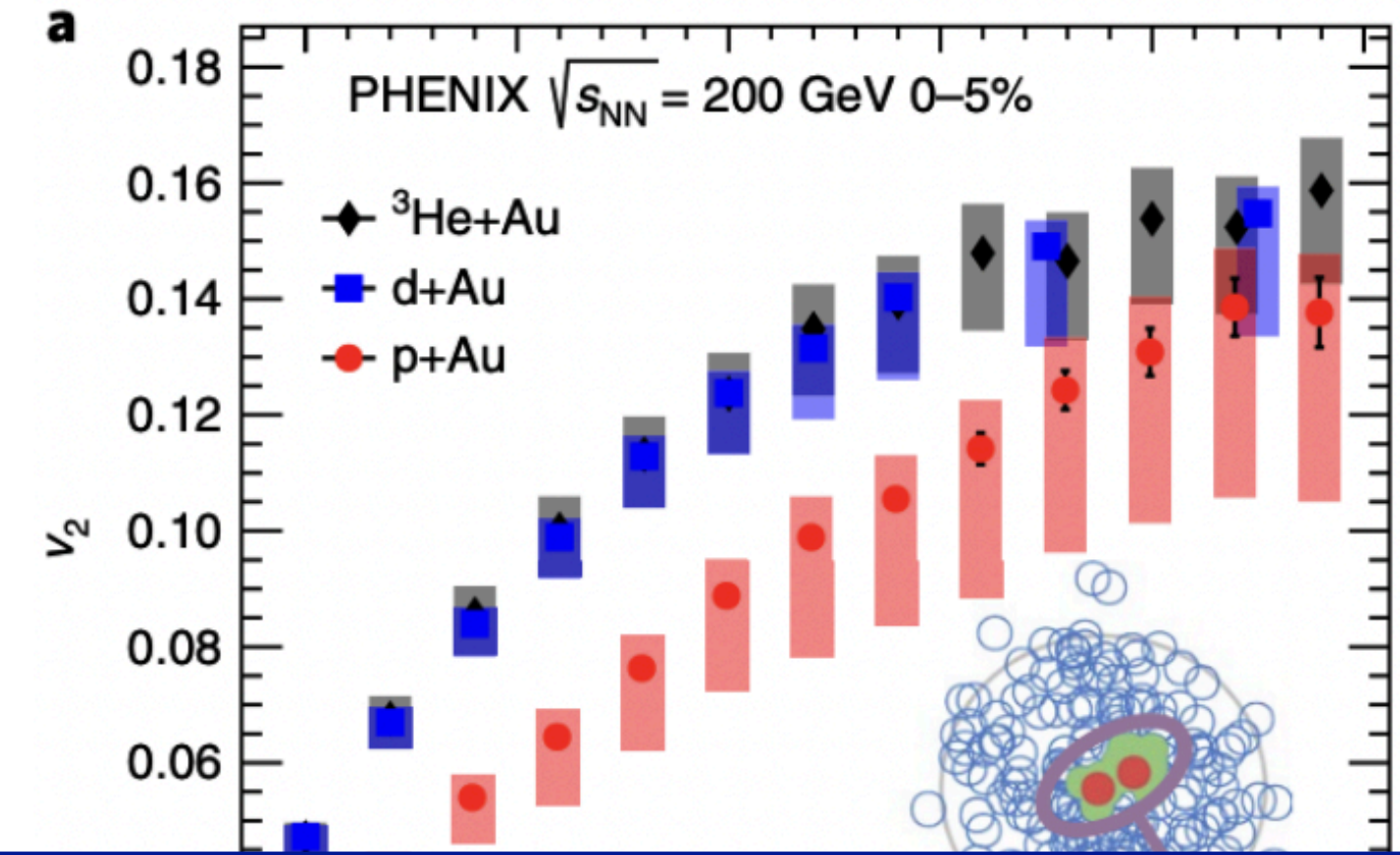


PHENIX, Nature Physics 15 (2019) 214



# The role of initial geometry

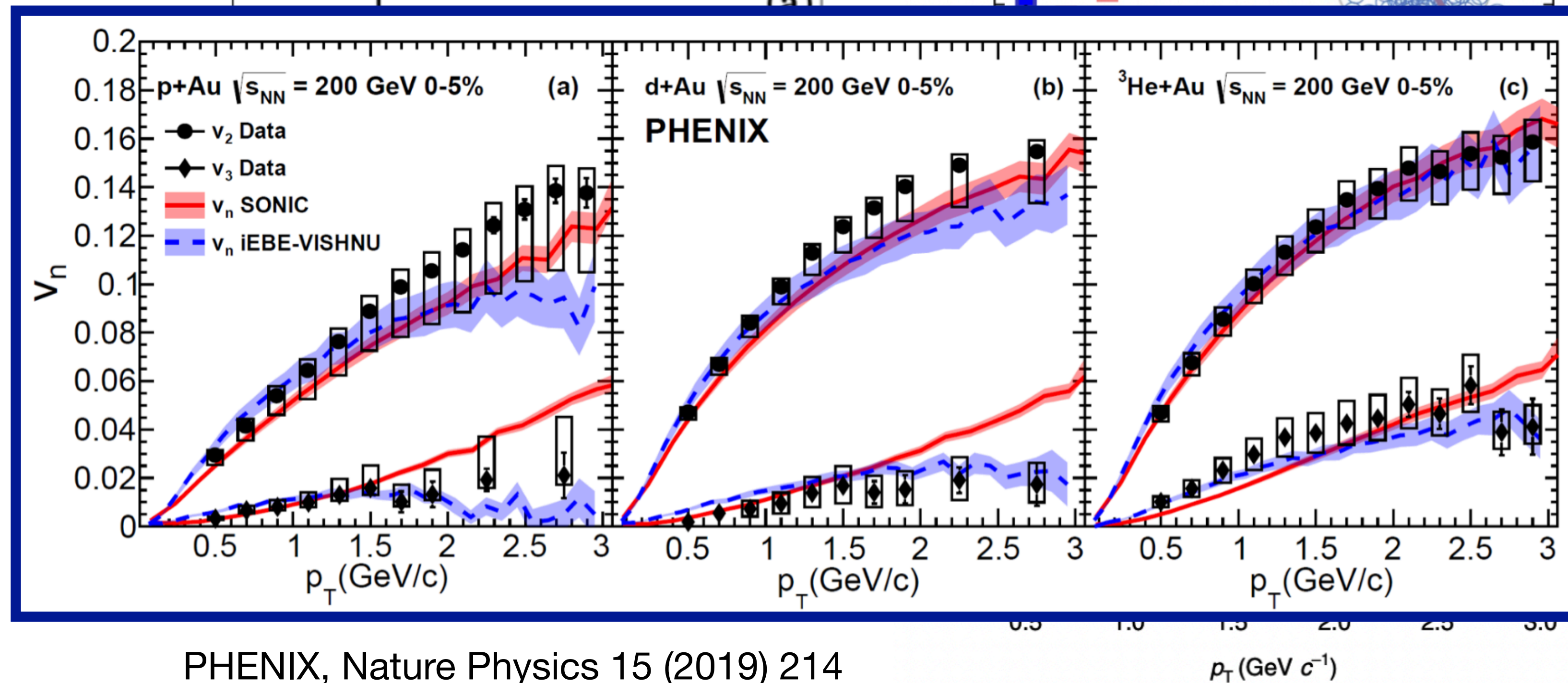
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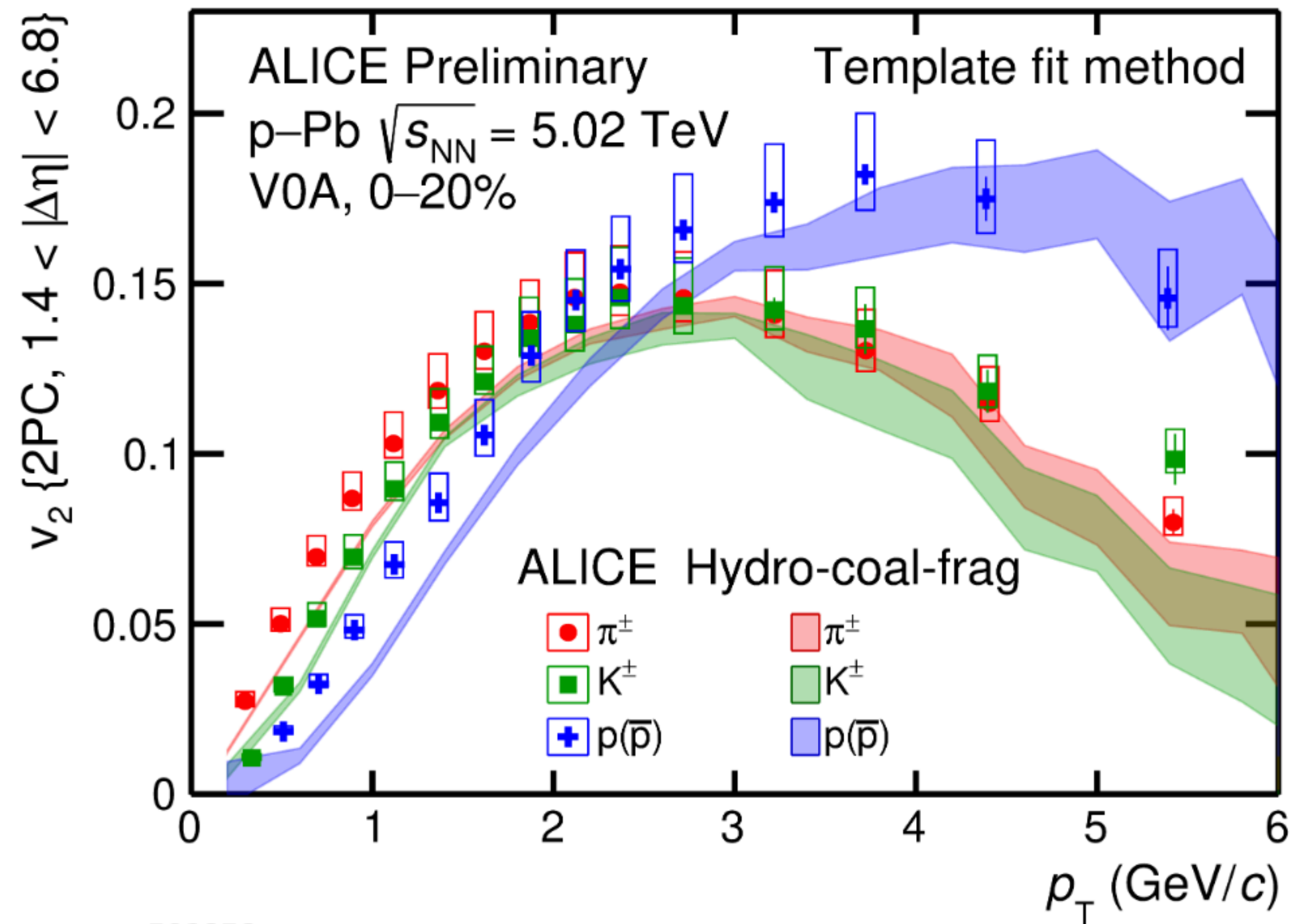
$$v_3^{\text{p+Au}} \approx v_3^{\text{d+Au}} < v_3^{\text{He+Au}}$$



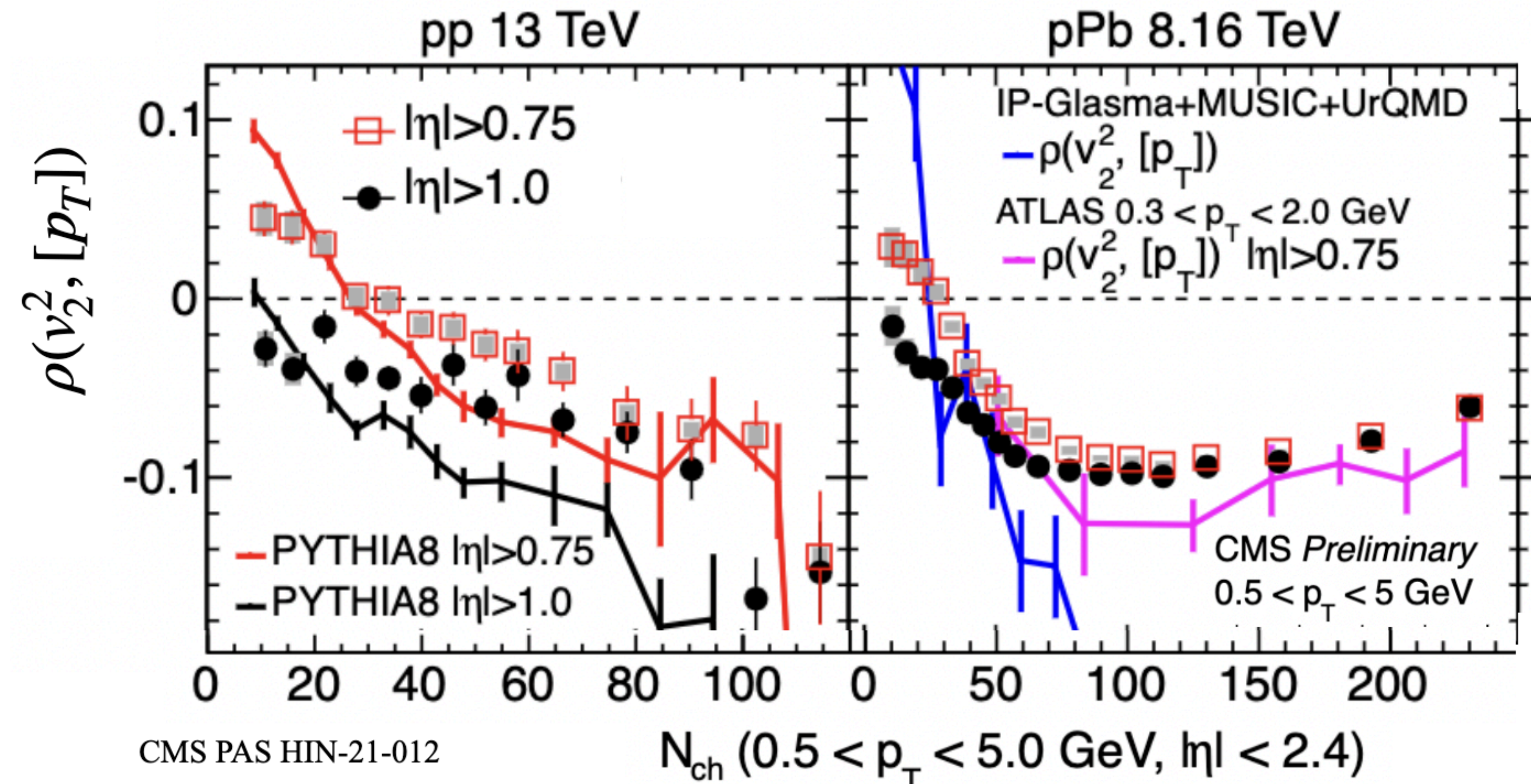
PHENIX, Nature Physics 15 (2019) 214

# Digging deeper into small-system $v_n$

- Identified-particle  $v_2$  shows similar mass ordering and baryon-meson splitting in p+Pb as in Pb+Pb
- Measurements of higher-order correlations and fluctuations are ongoing
- Can be extremely sensitive to kinematic selections and non-flow removal!



ALI-PREL-503272



# πάντα ρεῖ: Everything flows, or does it?

Increase the MPI  
Number of  
parton-parton  
interactions

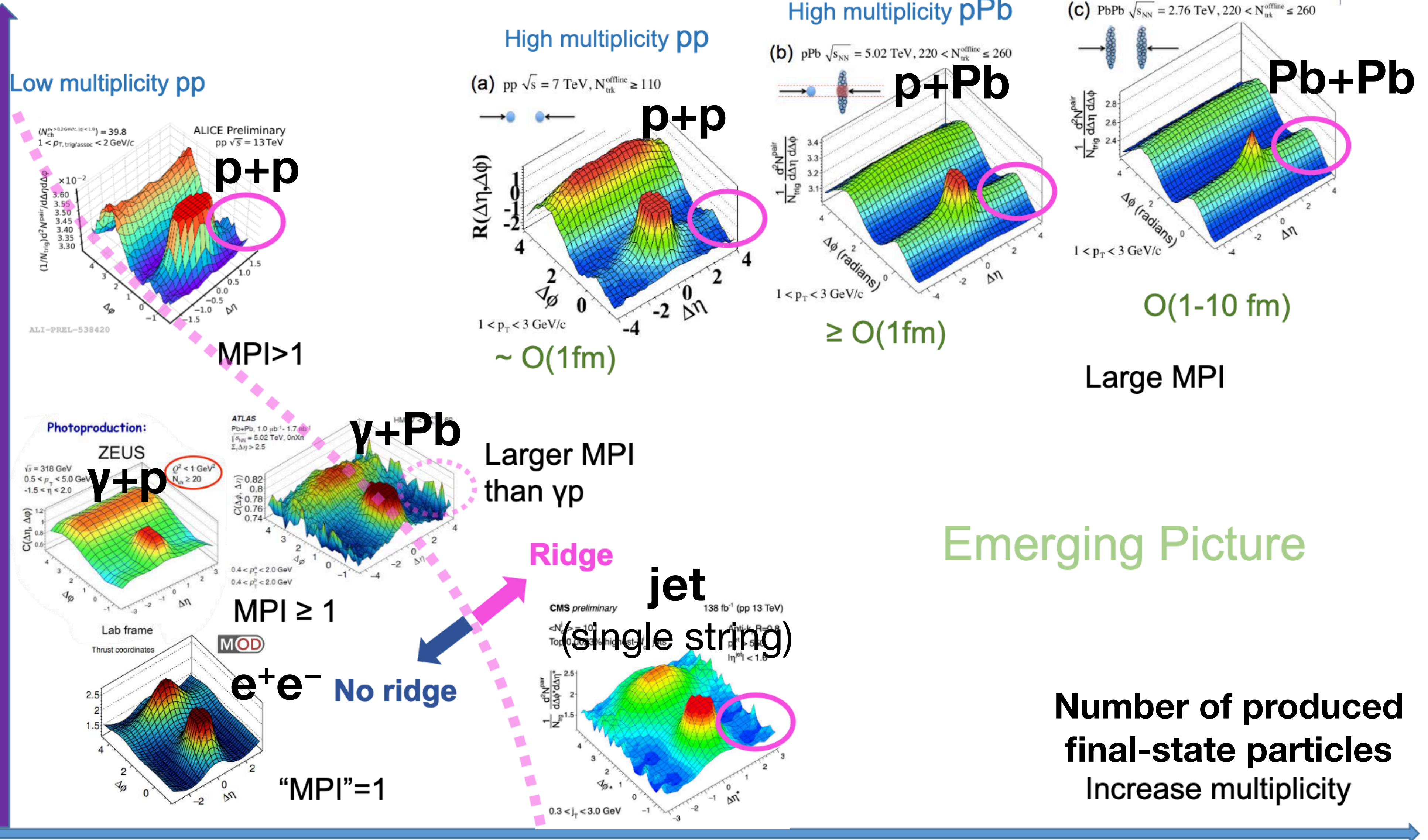


Image from  
Yen-Jie Lee's  
talk at Initial  
Stages 2023



# Open questions

- How does initial state energy deposition (geometry) transfer into final-state anisotropic particle distribution? Is hydrodynamics the explanation in large systems? Can we develop a microscopic description?
- What is the origin of anisotropic flow in small systems? Is hydrodynamics the answer?
- How many scatterings or interactions does it take to generate flow, equilibrate, thermalize?
- Is there a medium produced in small systems? What are its properties?
- What is the interplay between momentum scales (hard and soft probes)? Is there jet quenching in small systems?

# Transverse size vs multiplicity

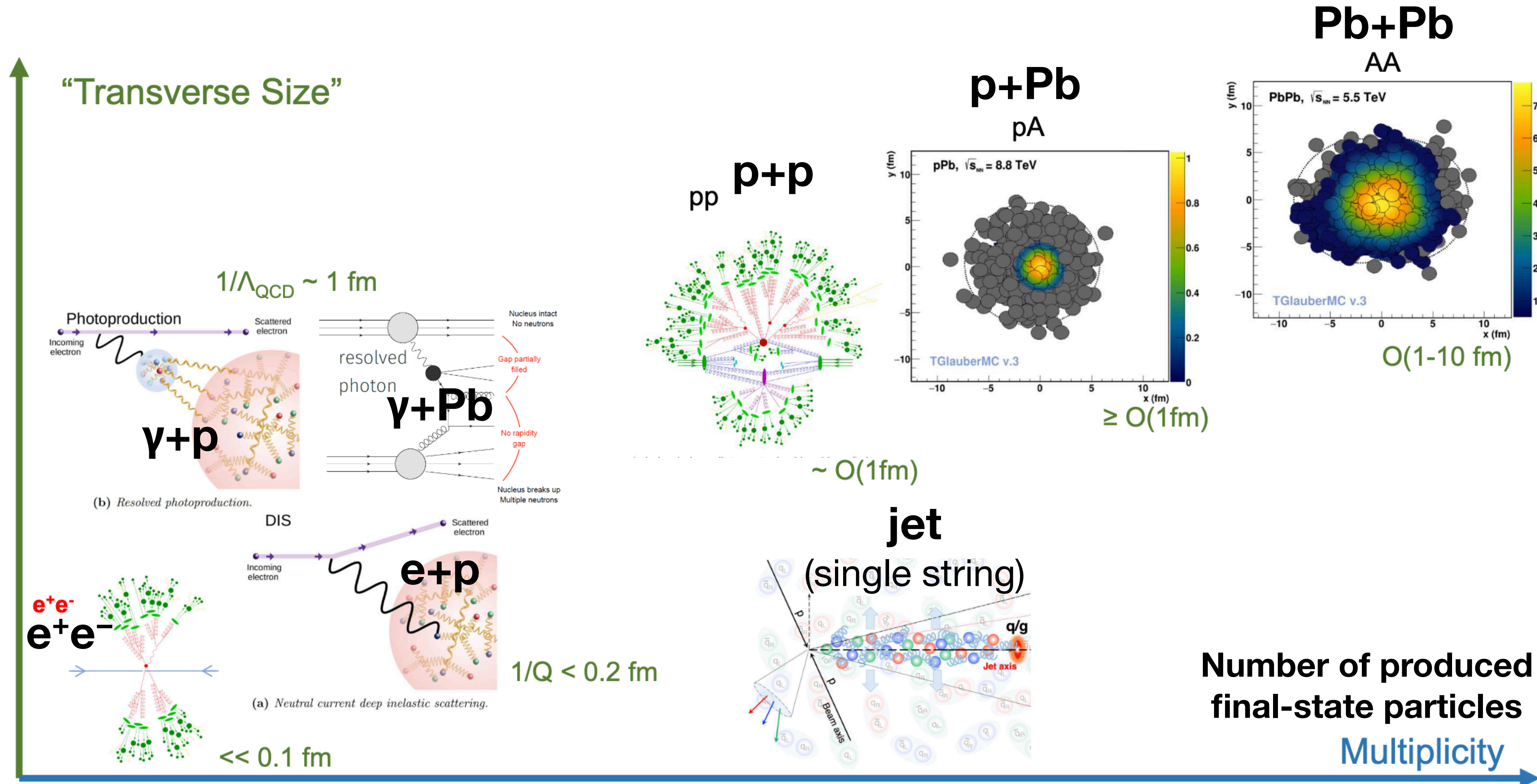


Image from Yen-Jie Lee's talk at Initial Stages 2023

# Multi-particle correlations in small systems

- Are these correlations a true “collective” (many-particle) effect, or just between few ( $\sim 2$ ) particles?

- Measure multi-particle cumulants  
Example: four-particle cumulants

$$c_2\{4\} = \langle\langle \cos 2(\varphi_1 + \varphi_2 - \varphi_3 - \varphi_4) \rangle\rangle \leftarrow \text{four-particle correlation}$$
$$- \langle\langle \cos 2(\varphi_1 - \varphi_3) \rangle\rangle \langle\langle \cos 2(\varphi_2 - \varphi_4) \rangle\rangle \leftarrow \text{subtract two-particle correlations}$$
$$- \langle\langle \cos 2(\varphi_1 - \varphi_4) \rangle\rangle \langle\langle \cos 2(\varphi_2 - \varphi_3) \rangle\rangle \leftarrow \text{subtract two-particle correlations}$$

$$v_n\{4\} = \sqrt[4]{-c_n\{4\}}$$

- Similarly for six-particle, eight-particle cumulants