

New Muon Campus Simulations for the Muon $g-2$ Experiment at Fermilab

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On behalf of the Muon $g-2$ Collaboration

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Muon Anomalous Magnetic Dipole Moment (a_μ)

$$\mu = g \frac{e}{2m} S \quad \text{Gyromagnetic ratio equation}$$

Classical: $g = 1$

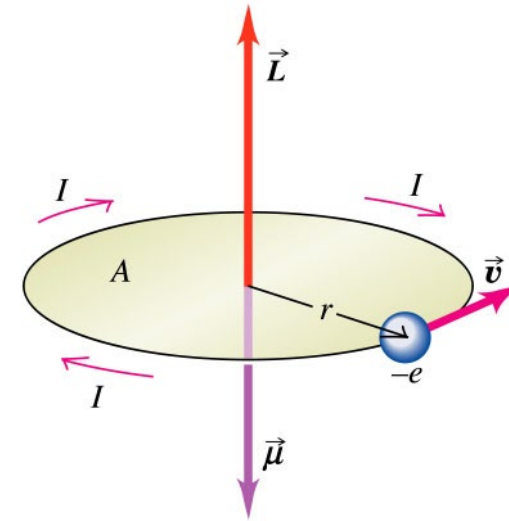
Dirac Equation: $g = 2$

$$i \left(\partial_\mu - ieA_\mu(x) \right) \gamma^\mu \psi(x) = m\psi(x)$$

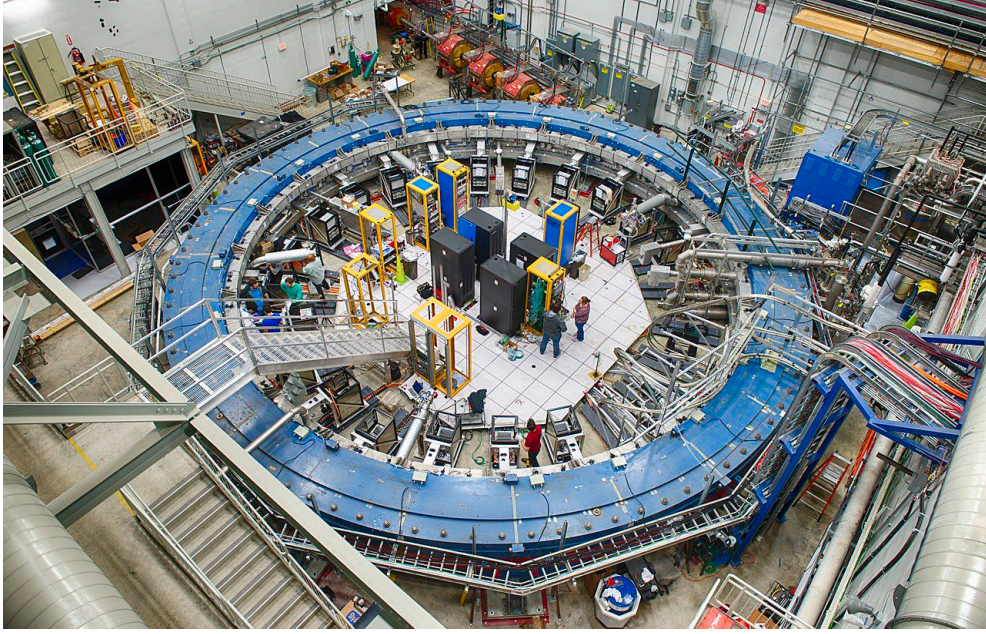
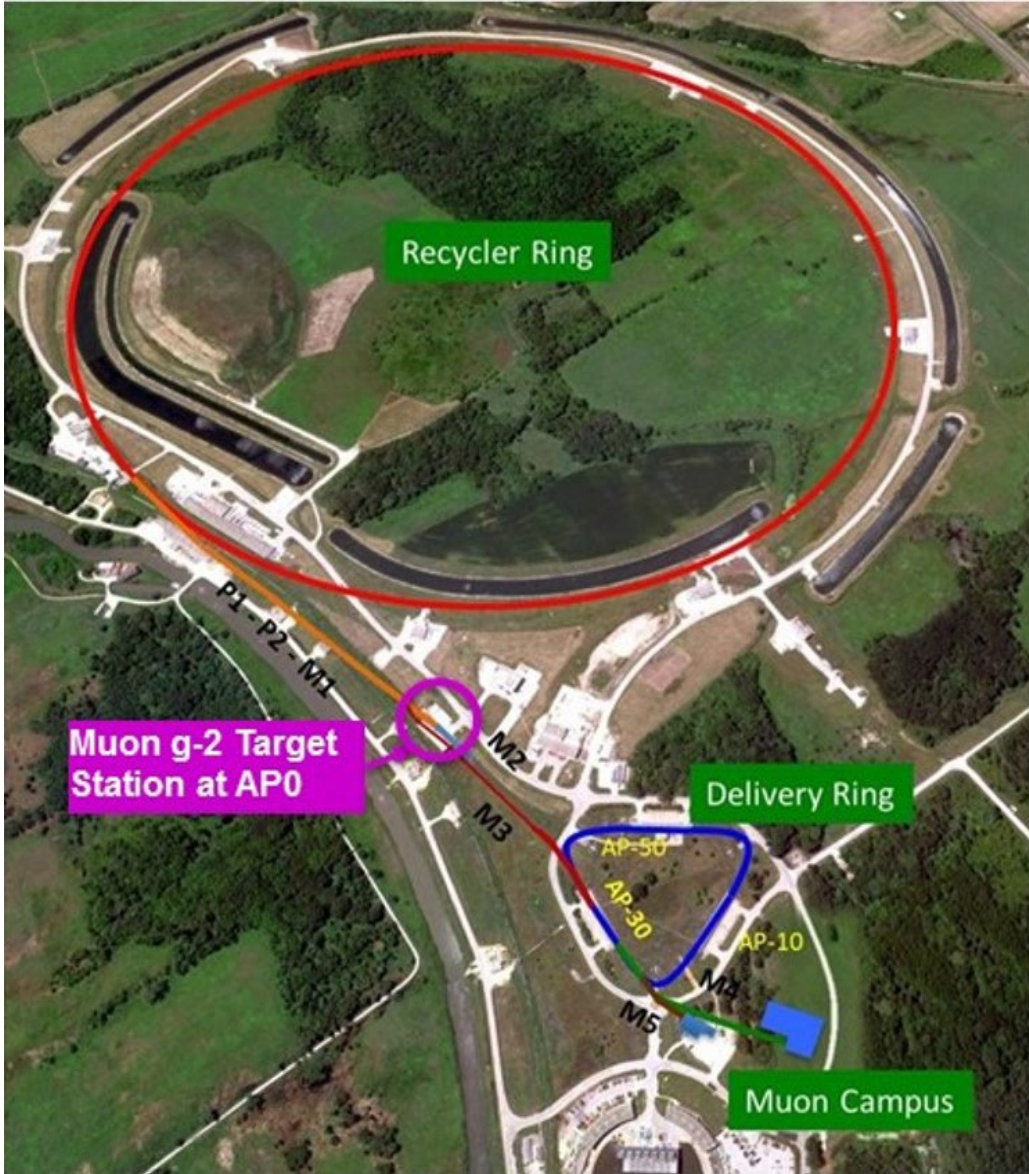
Interactions w/ quantum foam: $g > 2$

$$a_\mu = \frac{g-2}{2}$$

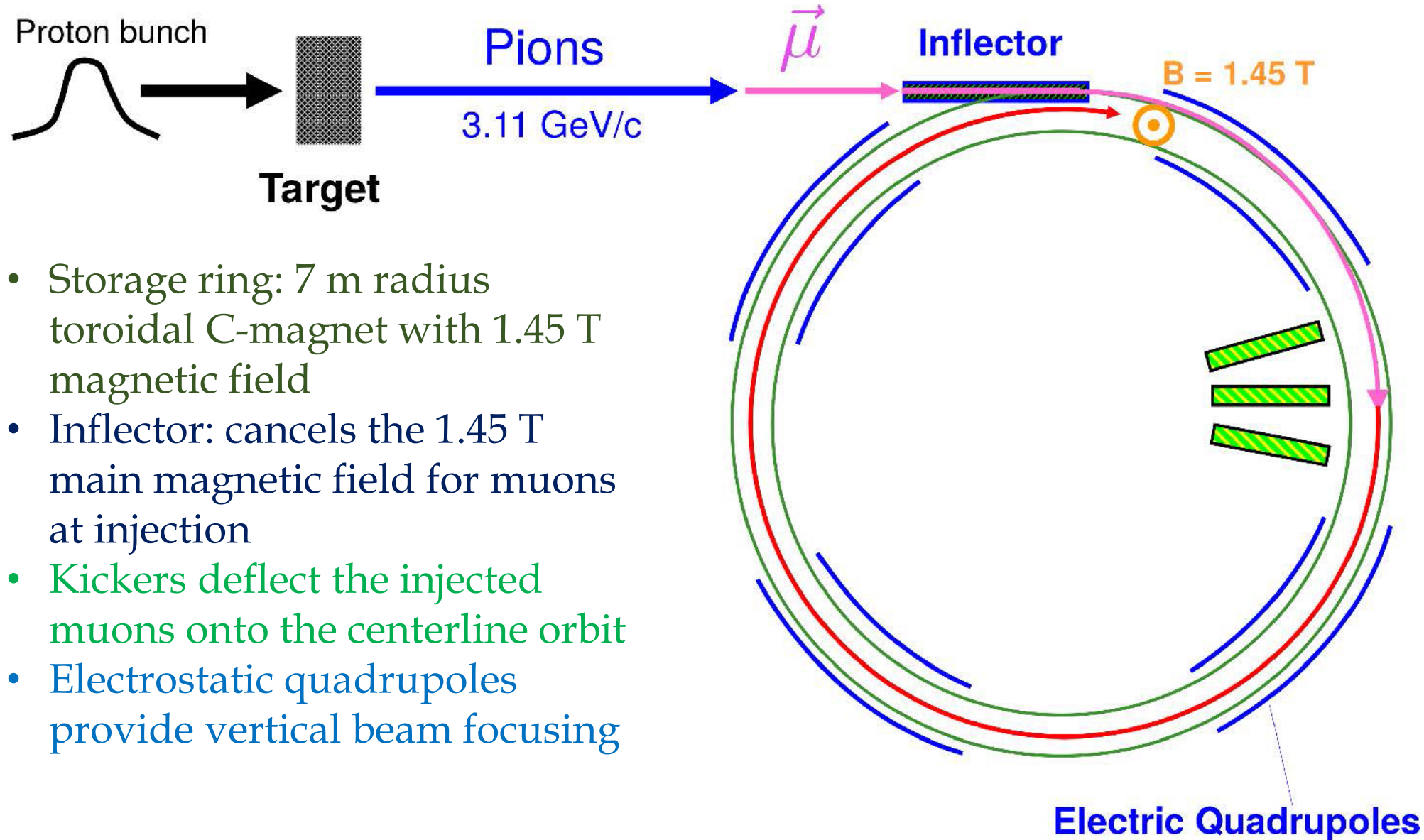
Muon anomaly

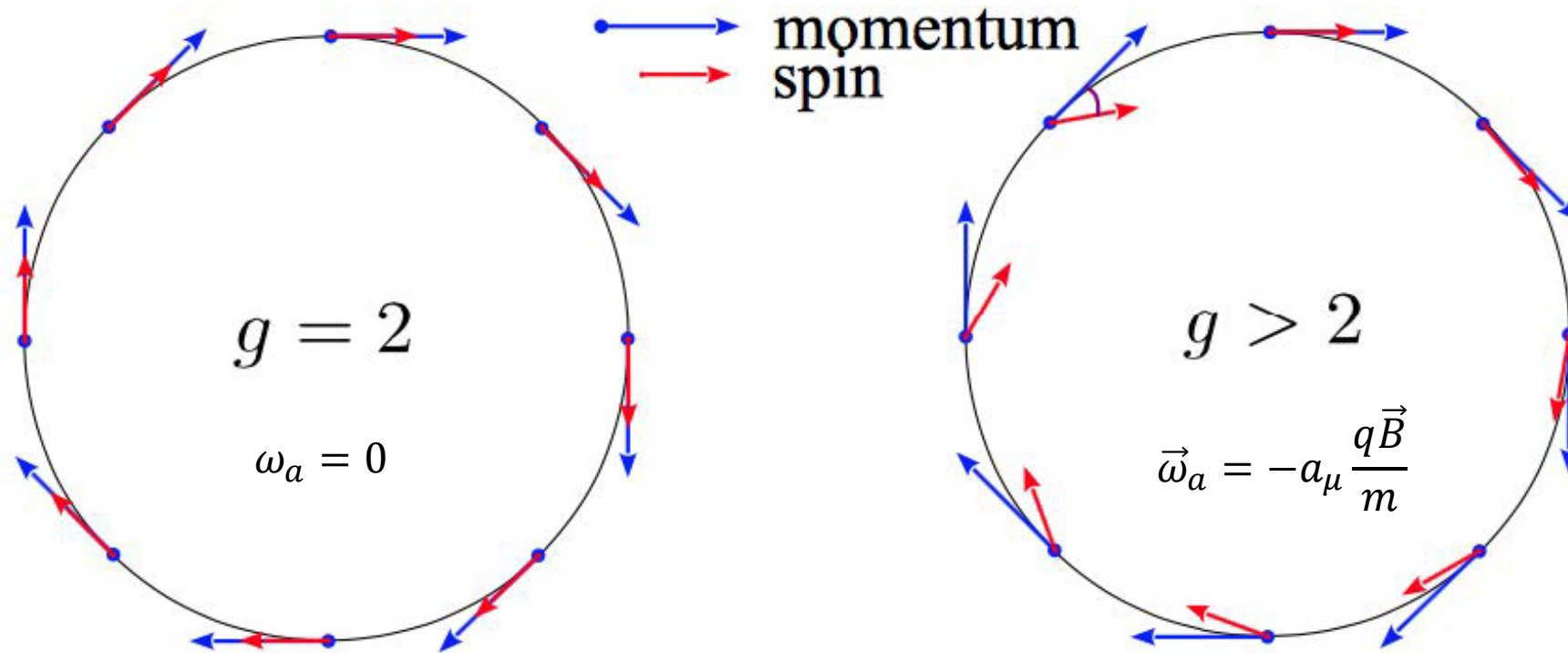


Introduction



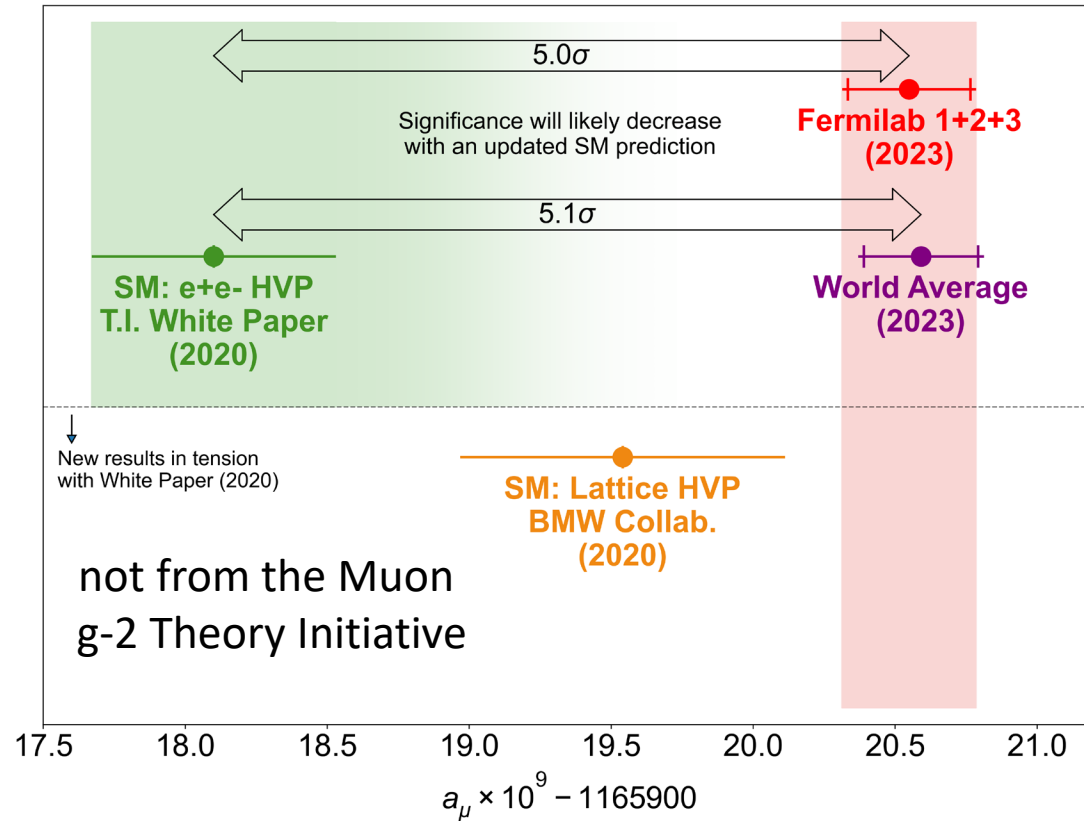
The Muon g-2 Storage Ring





If $g=2$, the angle between the magnetic moment and the momentum does not change.
If $g>2$, the angle between the magnetic moment and the momentum changes linearly.

Result from Runs 1-3



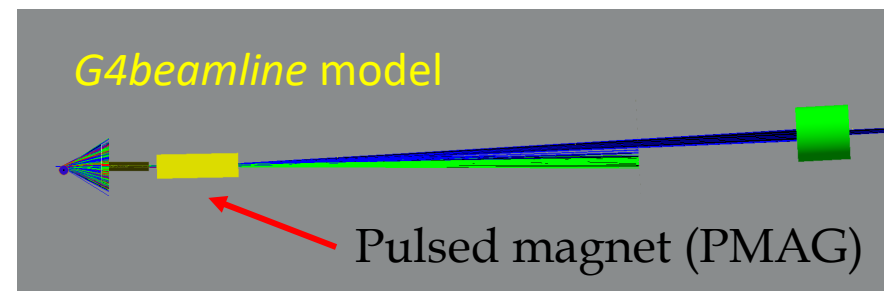
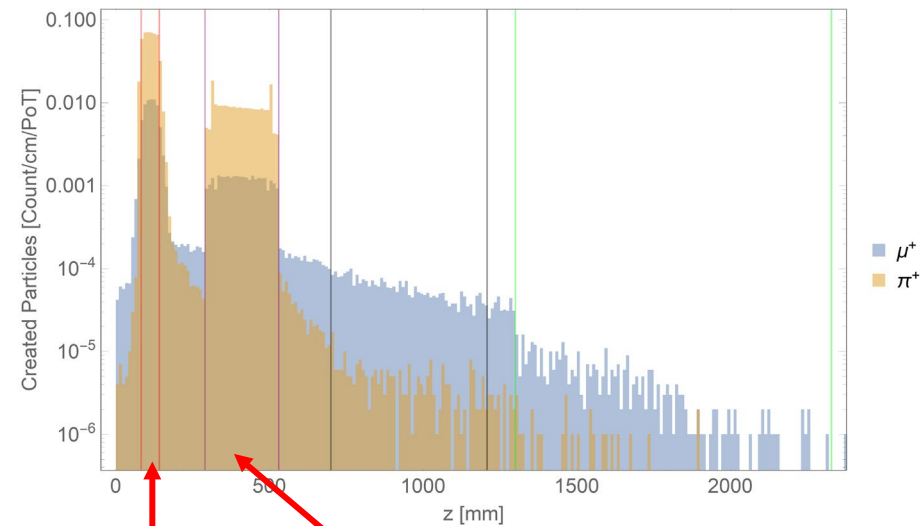
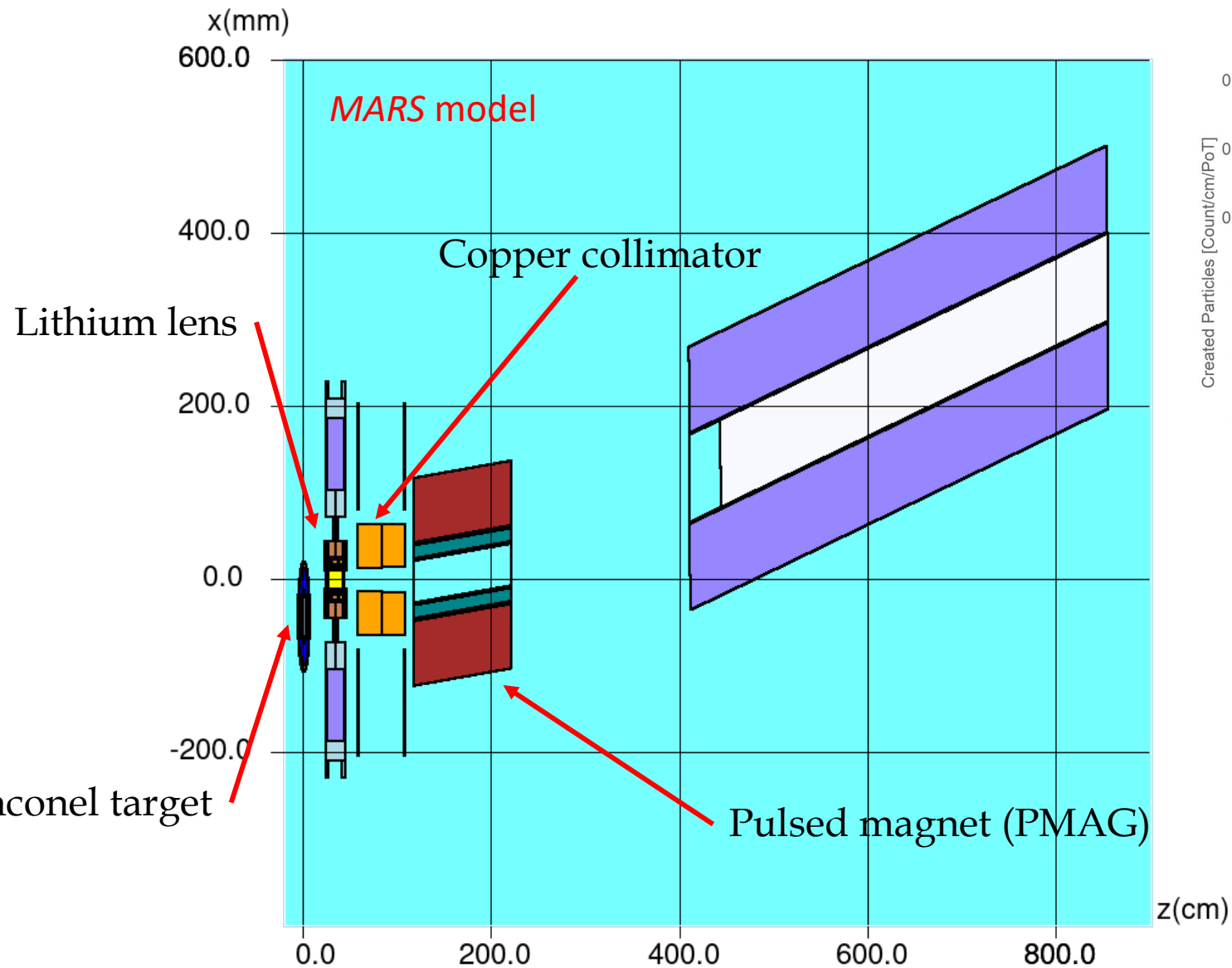
Quantity	Correction [ppb]	Uncertainty [ppb]
ω_a^m (statistical)	–	201
ω_a^m (systematic)	–	25
C_e	451	32
C_p	170	10
C_{pa}	-27	13
C_{dd}	-15	17
C_{ml}	0	3
$f_{\text{calib}} \langle \omega'_p(\vec{r}) \times M(\vec{r}) \rangle$	–	46
B_k	-21	13
B_q	-21	20
$\mu'_p(34.7^\circ)/\mu_e$	–	11
m_μ/m_e	–	22
$g_e/2$	–	0
Total systematic	–	70
Total external parameters	–	25
Totals	622	215

$$a_\mu \text{ (FNAL)} = 0.00\ 116\ 592\ 055(24) [203\ \text{ppb}]$$

$$a_\mu \text{ (Exp)} = 0.00\ 116\ 592\ 059(22) [190\ \text{ppb}]$$

$$a_\mu \text{ (Th)} = 0.00\ 116\ 591\ 810(43) [370\ \text{ppb}] \text{ (Review by Keshavarzi, 2022)}$$

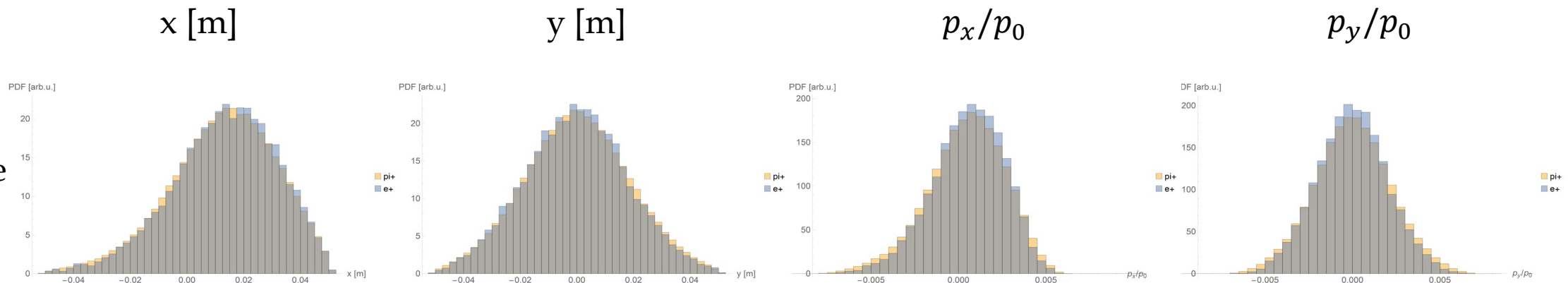
Muon g-2 Target Station



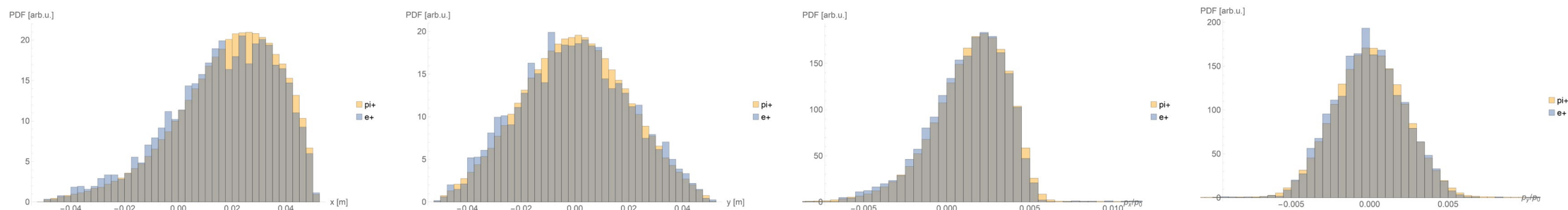
Muon g-2 Target Station

Phase space at the US end of Q801 (the first quadrupole of M2)

G4beamline



MARS15

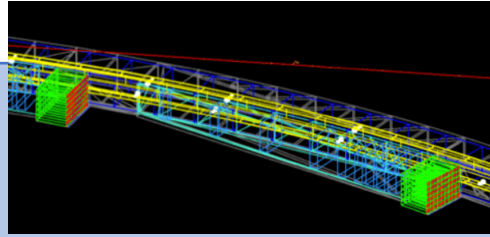


- G4beamline and MARS models of the Muon g-2 target station were carefully revised and updated
- The agreement between simulation results was improved substantially
- Notable remaining discrepancy: G4beamline-to-MARS e^+ production ratio of 4.2 (accounted for)

Muon Campus and Storage Ring Simulation Codes

gm2ringsim

- Custom simulation tool
- Based on **geant4**
- **FHiCL** configuration language
- **art** event processing
- Extensive custom source code including geometry, storage ring modules, etc.



BMAD

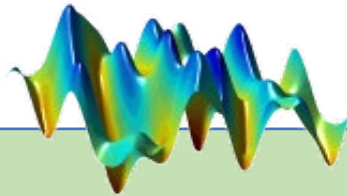
- Similar to **MAD**, with substantial expansions
- The storage ring and the Muon Campus
- Custom pion decay code

G4beamline

- Model of the Muon Campus beamlines and target station
- Based on **geant4**
- Comprehensive physics and geometry modeling, compared to **BMAD**
- Overlapping coordinate system limitation in ring lattice modeling

COSY INFINITY

- The most accurate storage ring model
- High-order DA transfer maps
- Accurate, Maxwellian fringe fields
- Symplectic tracking
- Electrostatic quadrupole multipole expansion up to order 24

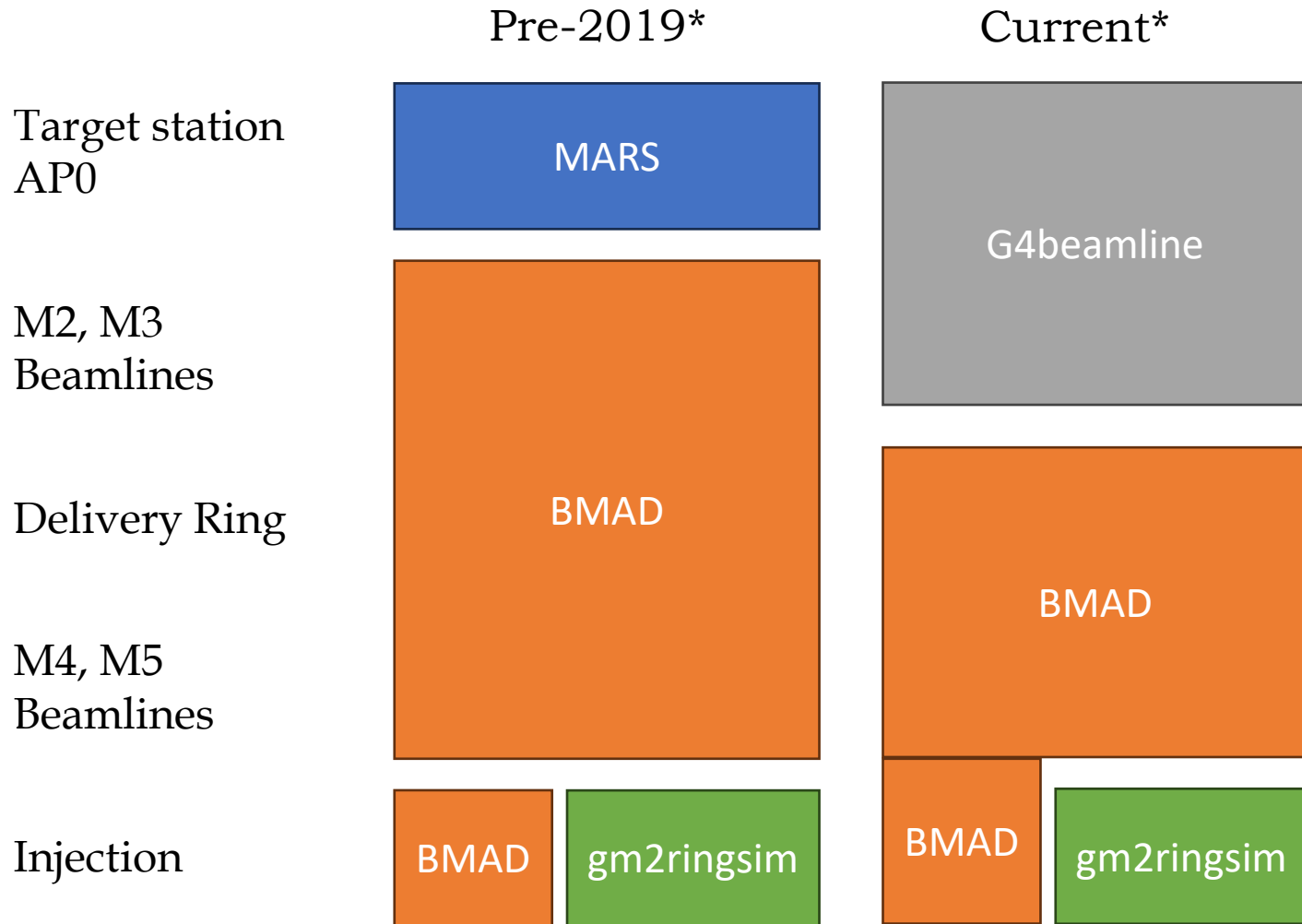


MARS

- A highly accurate Monte Carlo code for modeling of radiation transport and interaction with matter
- Used for the Muon $g-2$ target station

Muon Campus Simulation Code Pipeline

Simulation pipelines



Clusters

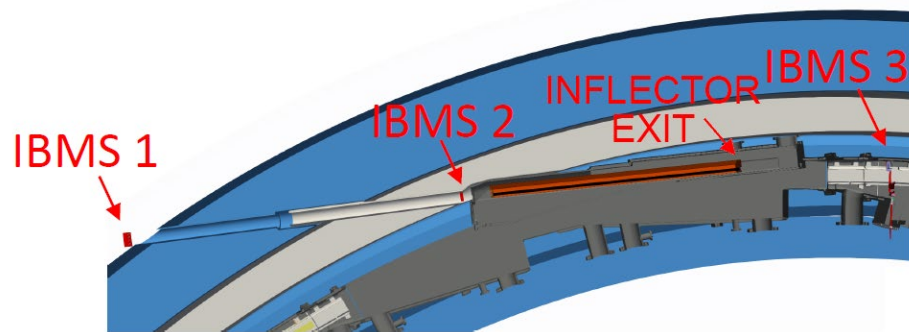
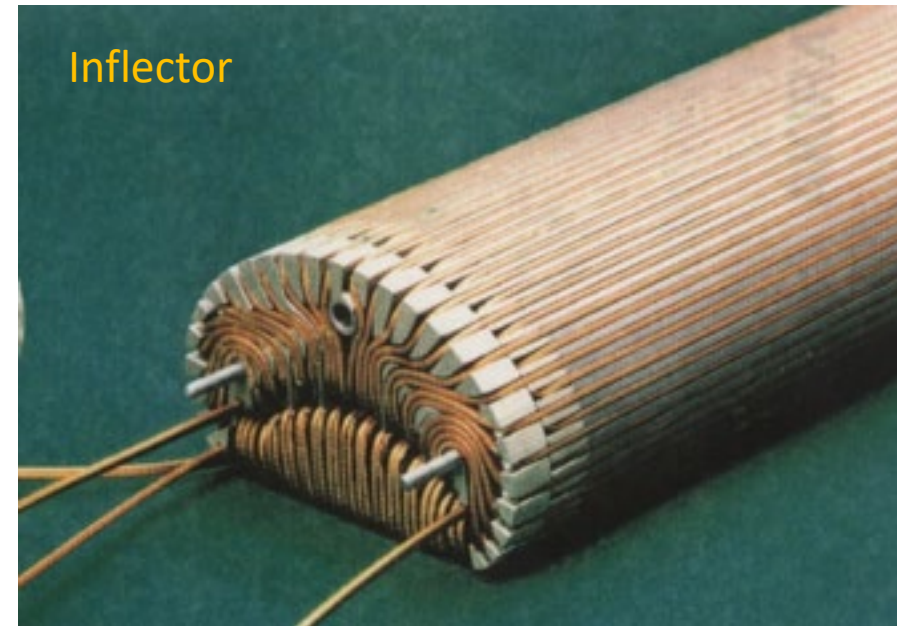
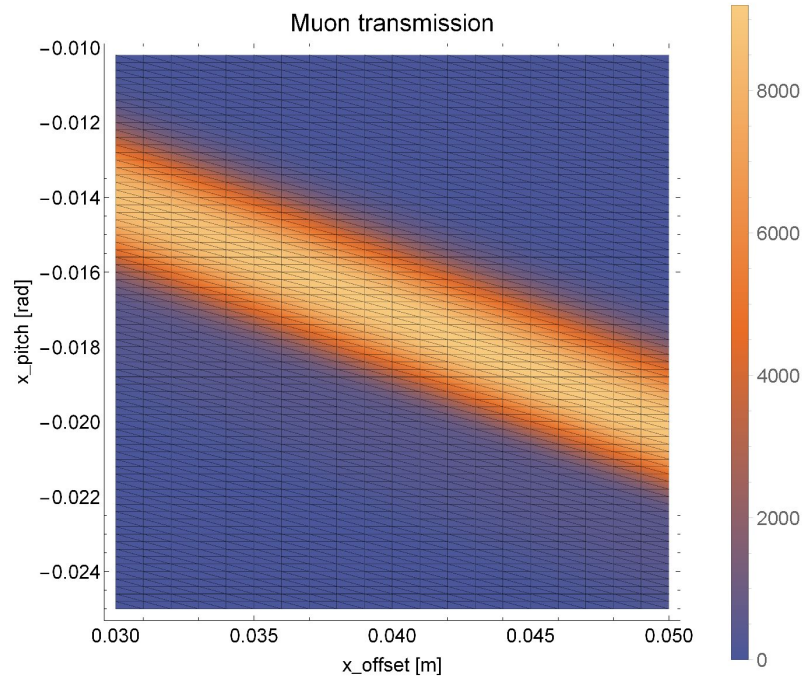


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MARS: accurate particle production
G4beamline: particle physics and beamline module geometry
BMAD: beam dynamics

* This categorisation is based on high-statistics simulations. Other codes, pipelines exist.

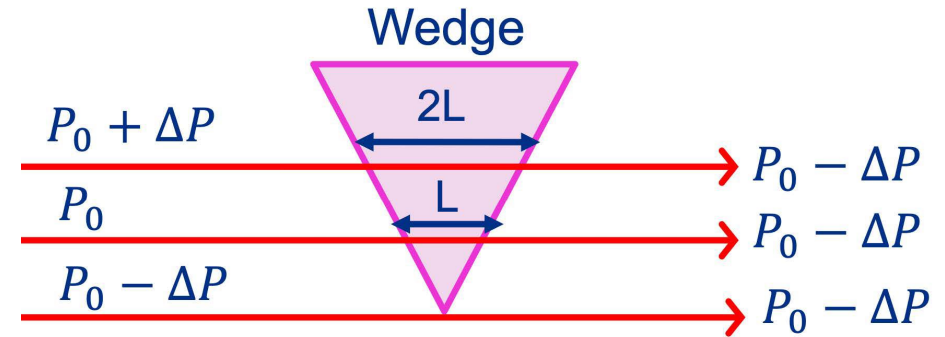
Injection Channel



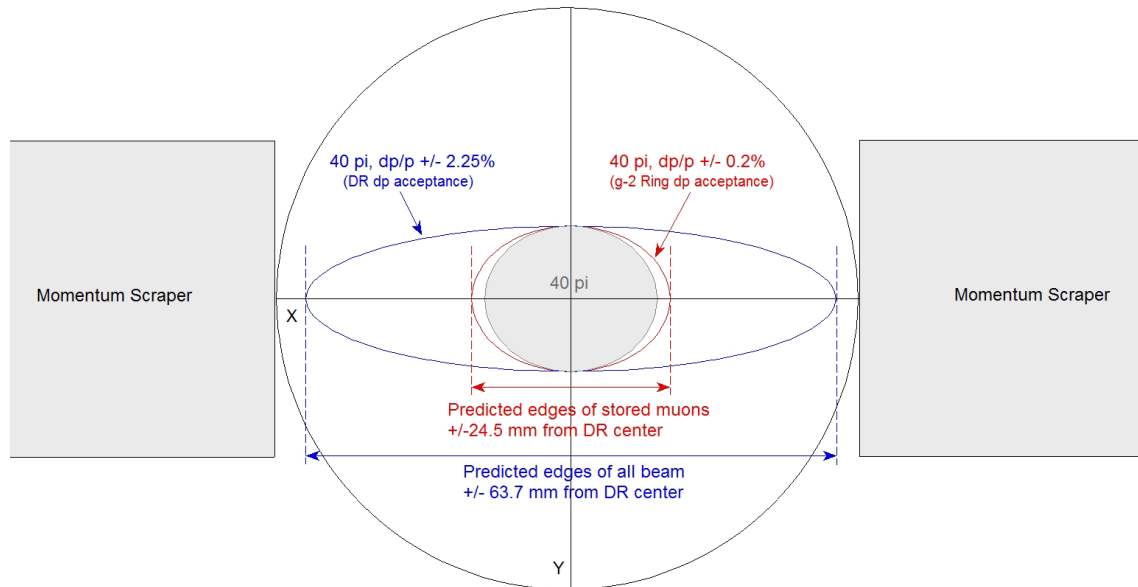
- 1.45 T bucking field to cancel main field
- Can't perturb main field by more than ~ 1 ppm
- Transition from large-scale (Muon Campus) to small-scale (inflector, Muon $g-2$ storage ring precision)
- Needs a careful and thoughtful approach to modelling

New Muon Campus Simulations

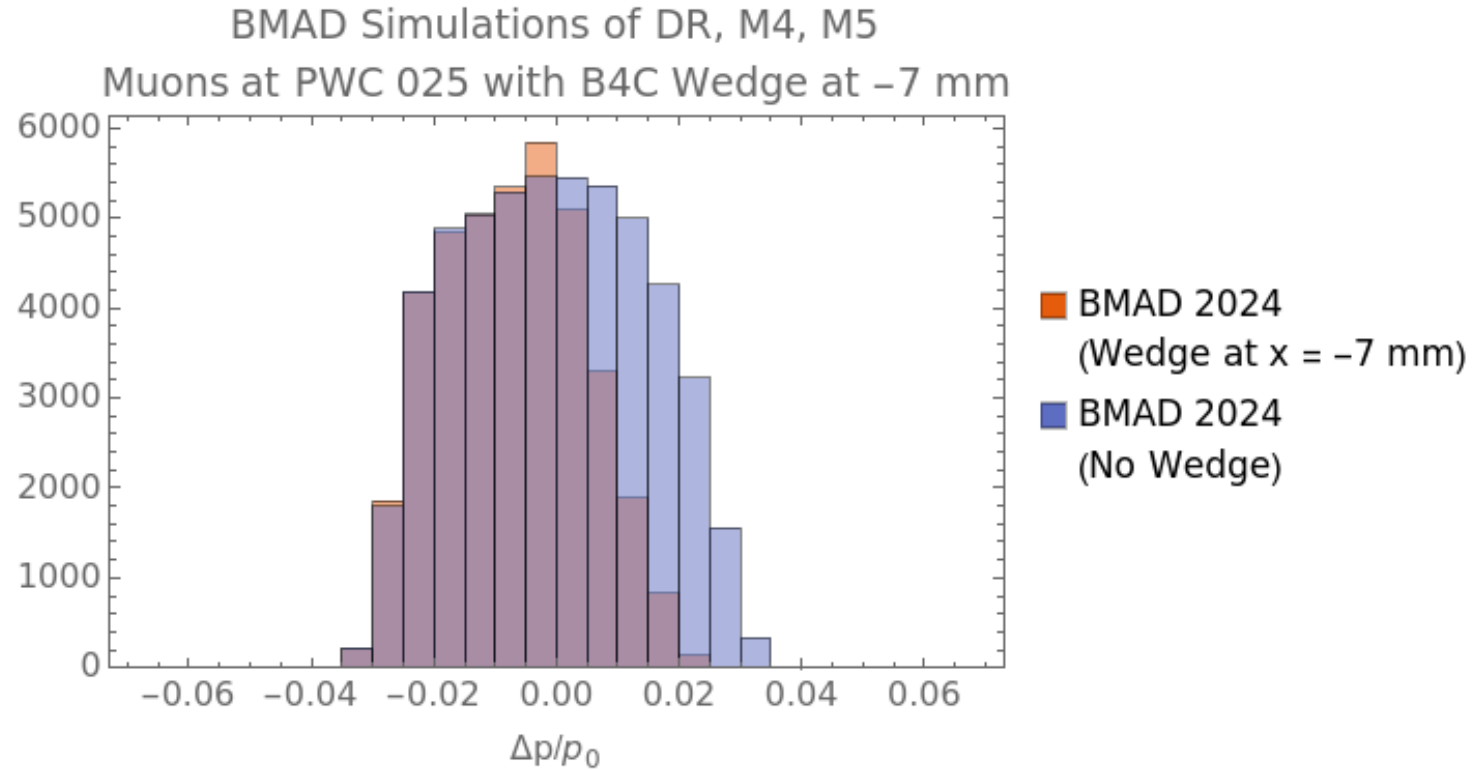
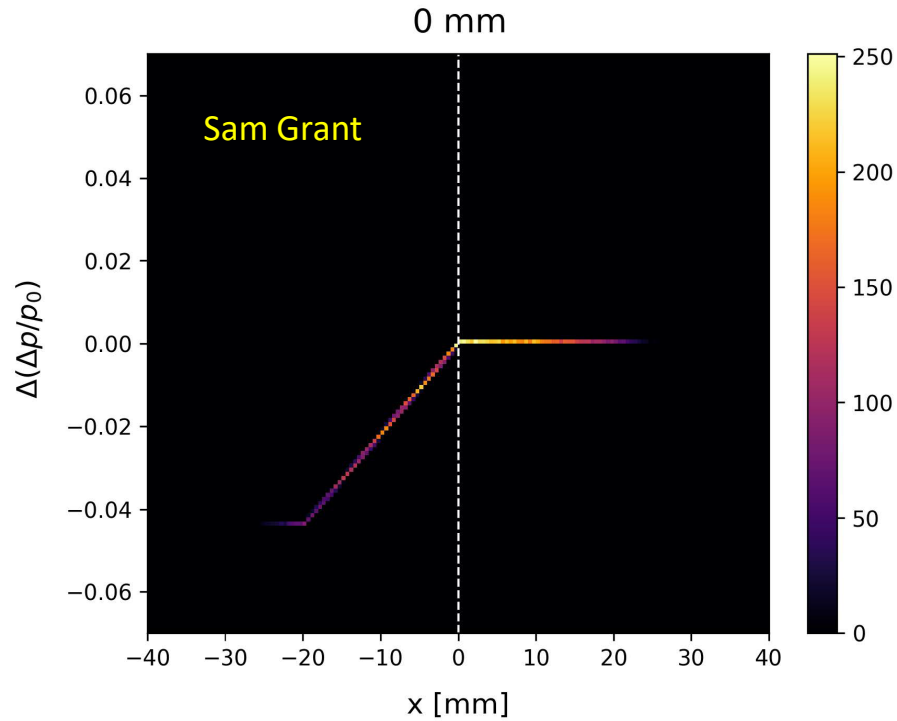
- Will be used in analyses for Runs 4-6
- Wedge in M4 for ionisation cooling
- Collimator in the Delivery Ring
- Updated quadrupole currents



Delivery Ring momentum scraper
Horizontal beta 10.7 m. Horizontal dispersion 1.91 m
Vertical beta 7.5 m, Vertical dispersion 0 m



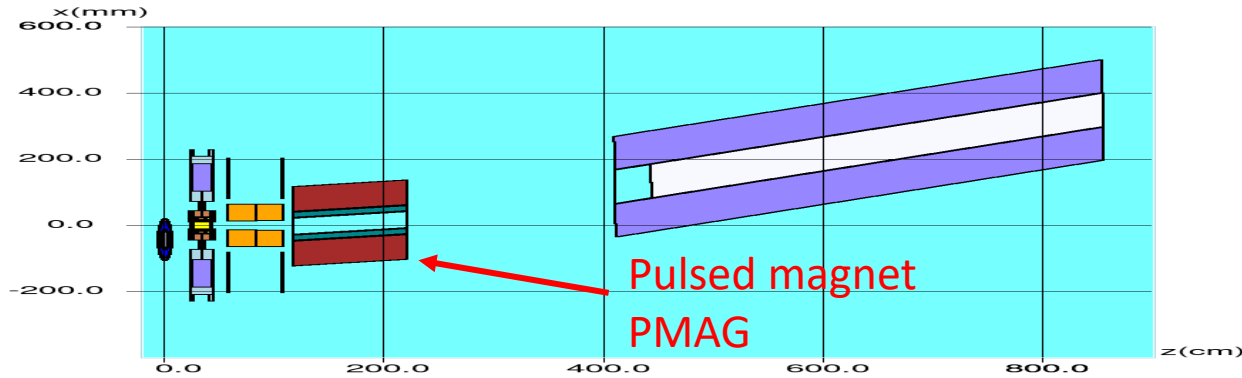
Ionisation Cooling Wedge



- Wedge implemented in BMAD using an extended implementation of the foil element
- *In collaboration with David Sagan (Cornell U., BMAD author) and Sam Grant (ANL)*

- Experimental increase in the muon flux: 4% [GM2-doc-24444]

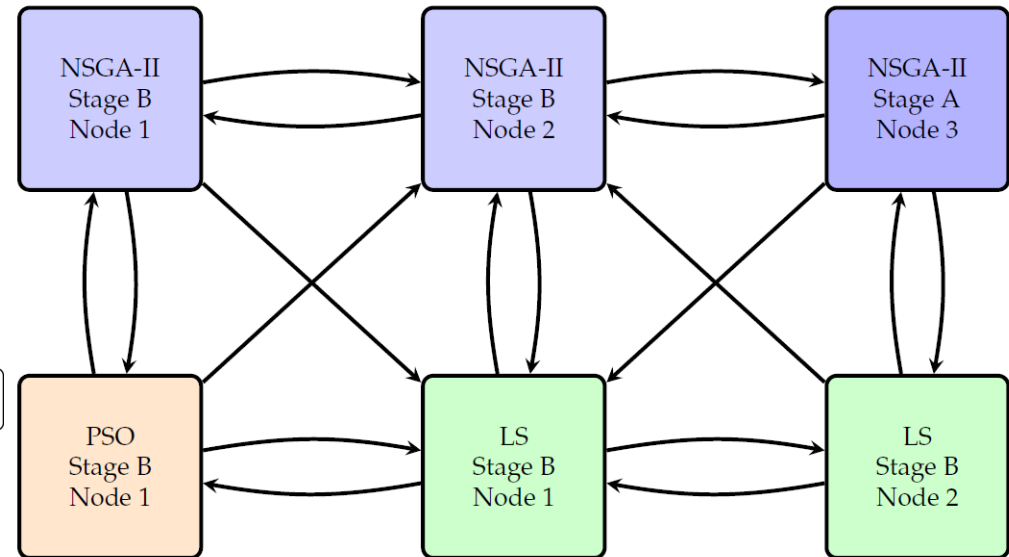
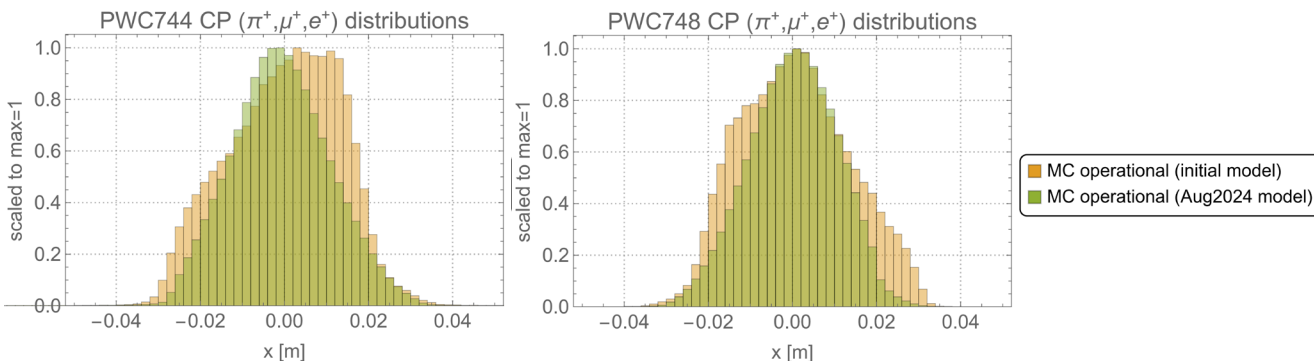
Optimisation Using Glyfada



- Exact PMAG current not known from measurements
- Optimised PMAG current and some other inexact parameters using **glyfada**
- To match wire chamber data
- Same principle as in the control room

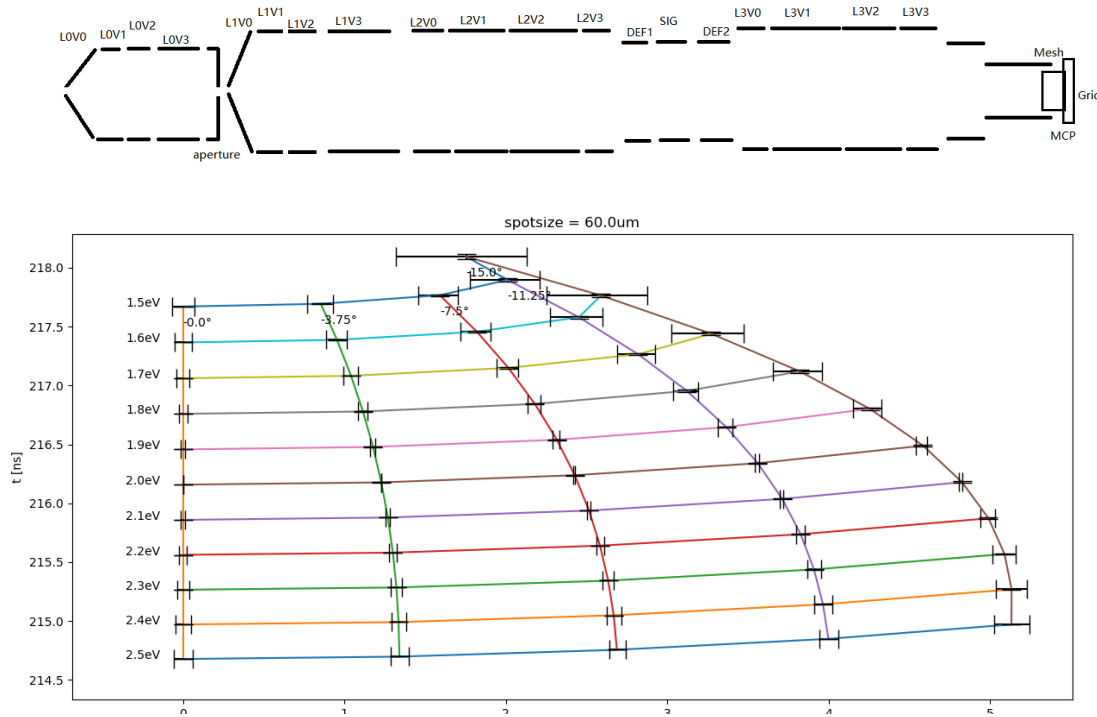
Optimiser **glyfada** (by E. Valetov)

- Based on Paradise framework
- Evolutionary optimisation and local search methods
- Heterogeneous island model
- Highly effective
- Under development (α-version stage)
- Also used by author in research for PSI, LBNL, LANL, and RadiaBeam



Examples of Glyfada Applications

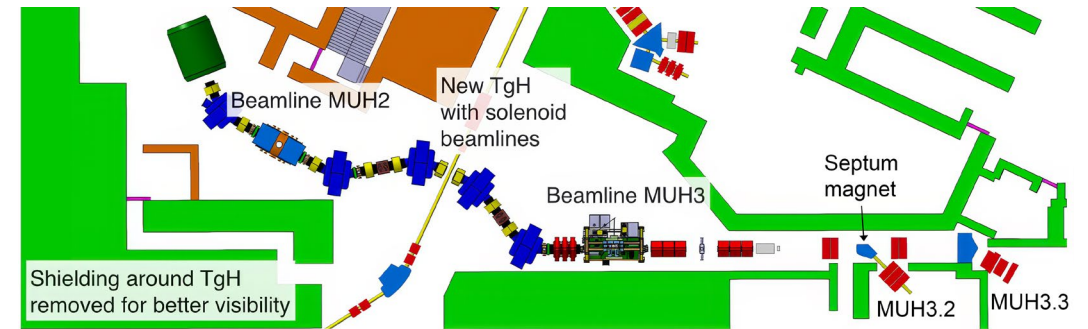
TOF Multimodal Electron Analyser (LBNL)



Conversion map showing aberrations at a set of energies and radii.

- Aberrations up to order 5 optimised
- Significantly better results using an early version of **glyfada** than using BO

High Intensity Muon Beams (PSI)



Complex final focus optimisation

- Large beam
- Two branches
- Complex septum magnet geometry
- Geometries of two collimators optimised
- **glyfada** optimiser: **2x** higher rate than BO (probably not typical)

New Muon Campus Simulations Status

Timeline

Steps

Facilities, methods

September 2024

G4beamline simulations of target station AP0, beamlines M2 and M3.
Phase 1: 3×10^{12} protons on target



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October 2024

BMAD simulations of the Delivery Ring and beamlines M4, M5:
quality checks, final focus adjustments

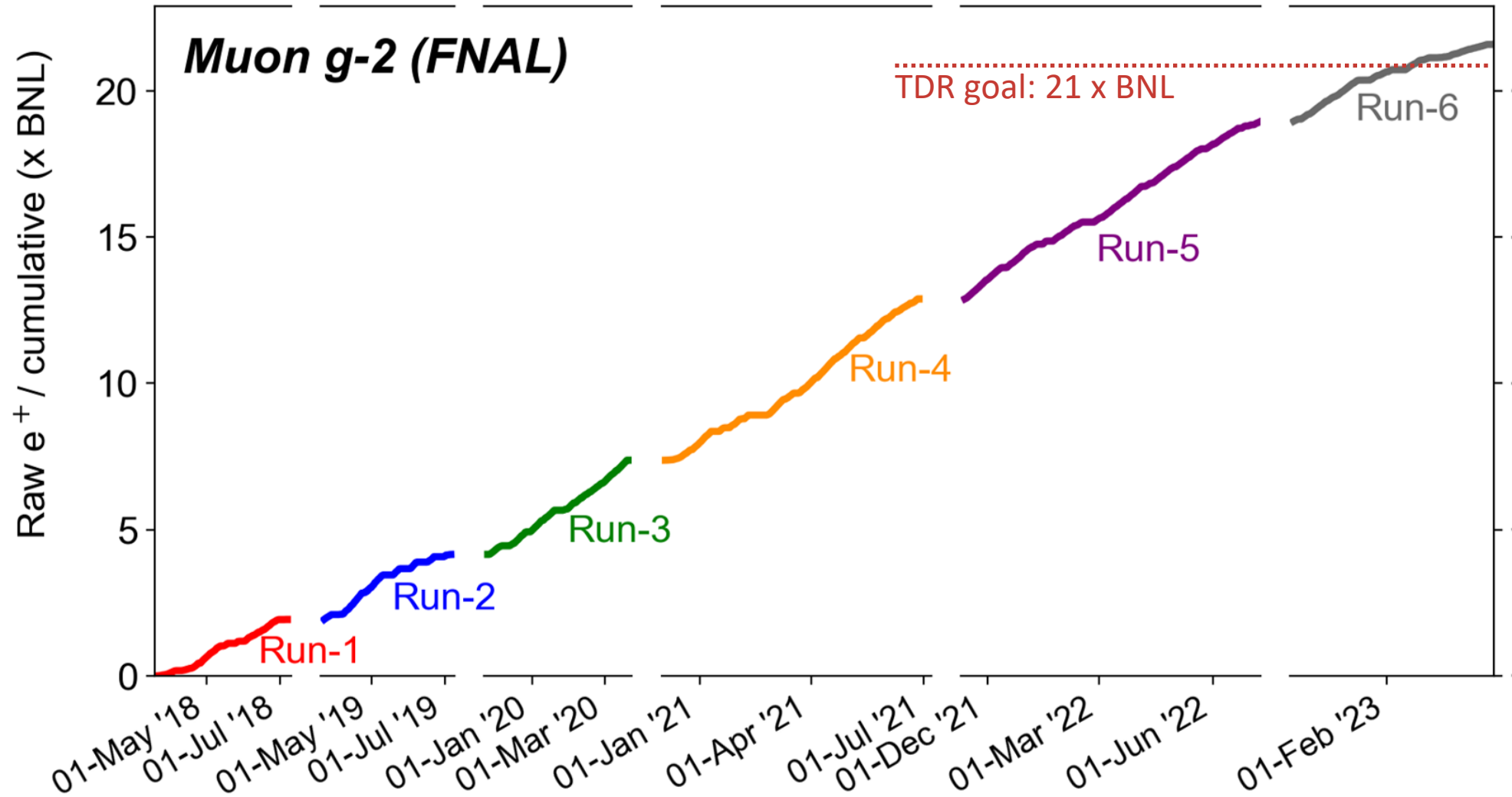
Optimiser
glyfada
(Heterogeneous island method)

October 2024

BMAD simulations of the Delivery Ring and beamlines M4, M5:
Phase1: 3×10^{12} protons on target

Local 32-core workstation

Data Acquisition as a Multiple of BNL Data



Conclusion

- Results based on Runs 2-3 were published in August 2023
- The experiment has completed its final Run 6 in July 2023
 - 21x more raw data than the Muon g-2 Experiment at BNL
 - Improving systematics:
 - Magnet temperature control
 - Magnetic field noise control
 - Analysis improvements (pileup reconstruction)
 - Achieved the TDR goal of 70 ppb systematic error
- Results from runs 4-6 planned to be released in 2025
 - **New Muon Campus simulations for the analyses in progress**
- New theory results expected in 2025

Conclusion



USA

- Boston
- Cornell
- Illinois
- James Madison
- Kentucky
- Massachusetts
- Michigan
- Michigan State
- Mississippi
- North Central
- Northern Illinois
- Regis
- Virginia
- Washington

USA National Labs

- Argonne
- Brookhaven
- Fermilab

182 collaborators
33 Institutions
7 countries



China

- Shanghai Jiao Tong



Germany

- Dresden
- Mainz



Italy

- Frascati
- Molise
- Naples
- Pisa
- Roma Tor Vergata
- Trieste
- Udine



Korea

- CAPP/IBS
- KAIST



Russia

- Budker/Novosibirsk
- JINR Dubna



United Kingdom

- Lancaster/Cockcroft
- Liverpool
- Manchester
- University College London



Collaboration meeting at University of Liverpool, July 2023
Photo credit: McCoy Wynne



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