



Introduction to Cyclotrons

**WE-Heraeus-Seminar on
accelerator physics for intense ion beams
Bad Honnef, 17.10. 2012**

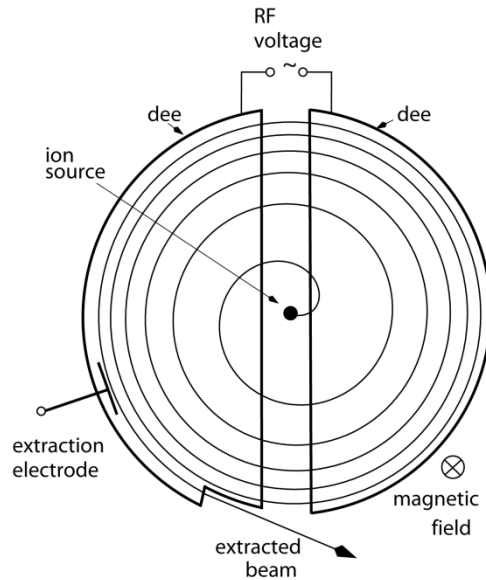
Mike Seidel
Paul Scherrer Institut

Cyclotrons - Outline

- the classical cyclotron
history of the cyclotron, basic concepts and scalings,
classification of circular accelerators and cyclotron-like acceler.
- separated sector cyclotrons
focusing in Thomas-cyclotrons, spiral angle, classical extraction:
pattern/stepwidth, transv./long. space charge
- cyclotron subsystems
extraction schemes, RF systems/resonators, magnets, vacuum
issues, instrumentation
- applications and examples of existing cyclotrons
TRIUMF, RIKEN SRC, PSI Ring, PSI medical cyclotron
- discussion
Pro's and Con's of cyclotrons for different applications



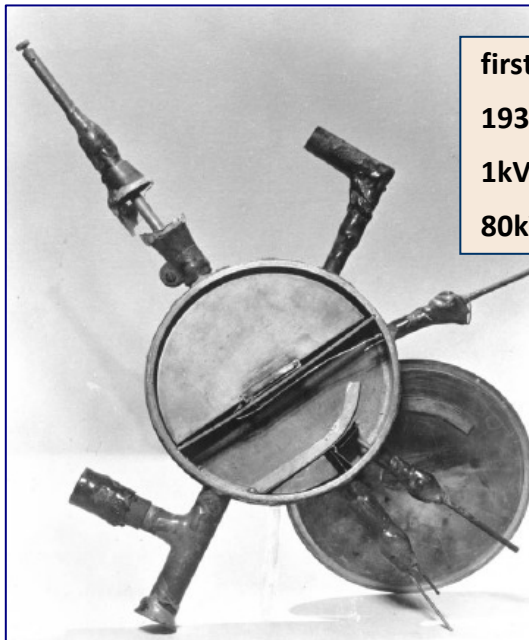
The Classical Cyclotron



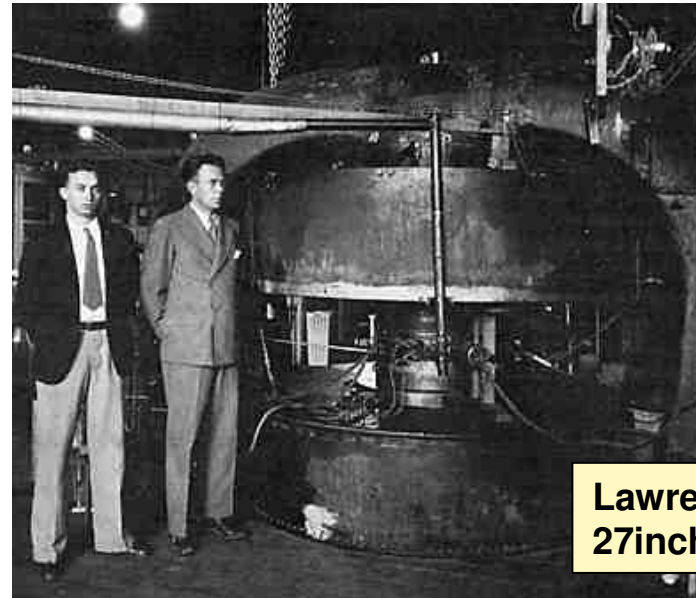
two capacitive electrodes „Dees“, two gaps per turn
internal ion source
homogenous B field
constant revolution time
(for low energy, $\gamma \sim 1$)

powerful concept:

- simplicity, compactness
- continuous injection/extraction
- multiple usage of accelerating voltage



first cyclotron:
1931, Berkeley
1kV gap-voltage
80kV Protons



**Lawrence & Livingston,
27inch Zyklotron**



cyclotron frequency and K value

- **cyclotron frequency** (homogeneous) B-field:

$$\omega_c = \frac{eB}{\gamma m_0}$$

- **cyclotron K -value:**

→ K is the **kinetic energy reach** for protons **from bending strength** in non-relativistic approximation:

$$K = \frac{e^2}{2m_0} (B\rho)^2$$

→ K can be used to rescale the energy reach of protons to other charge-to-mass ratios:

$$\frac{E_k}{A} = K \left(\frac{Q}{A} \right)^2$$

→ K in [MeV] is often used for naming cyclotrons

examples: **K-130 cyclotron / Jyväskylä**

cyclone C230 / IBA



classical cyclotron - isochronicity and scalings

continuous acceleration \rightarrow revolution time must stay constant, though E_k , R vary

magnetic rigidity:

$$BR = \frac{p}{e} = \beta\gamma \frac{m_0 c^2}{e}$$

orbit radius from isochronicity:

$$\begin{aligned} R &= \frac{c}{\omega_c} \beta = R_\infty \beta \\ &= \frac{c}{\omega_c} \sqrt{1 - \gamma^{-2}} \end{aligned}$$

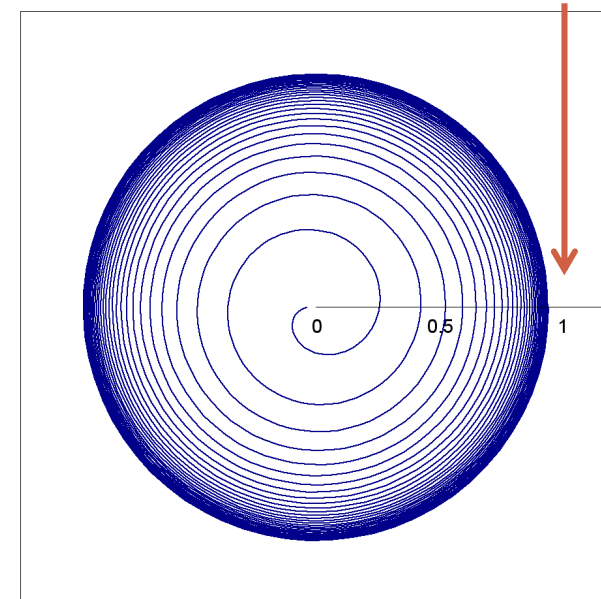
deduced scaling of B :

$$R \propto \beta; BR \propto \beta\gamma \rightarrow B(R) \propto \gamma(R)$$

thus, to keep the isochronous condition, B must be raised in proportion to $\gamma(R)$; this contradicts the focusing requirements (discussed later)

radius increment per turn
decreases with increasing energy
 \rightarrow **extraction becomes more and more difficult at higher energies**

$$R_\infty = R/\beta$$

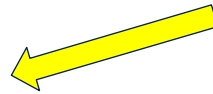


field index

the field index describes the (normalized)
radial slope of the bending field:

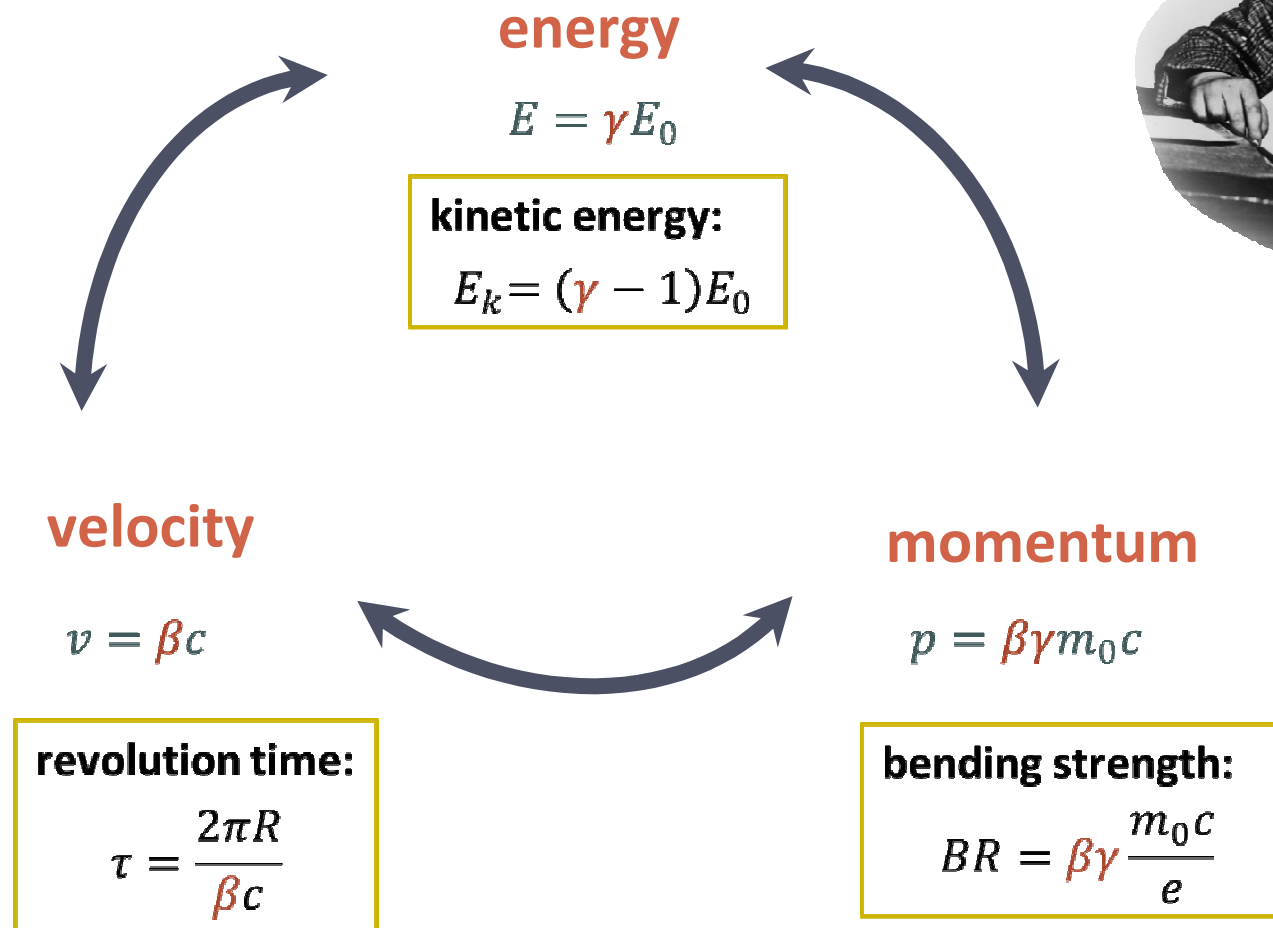
$$\begin{aligned}k &= \frac{R}{B} \frac{dB}{dR} \\&= \frac{\beta}{\gamma} \frac{d\gamma}{d\beta} \\&= \gamma^2 - 1\end{aligned}$$

from isochronous condition:
 $B \propto \gamma, R \propto \beta$

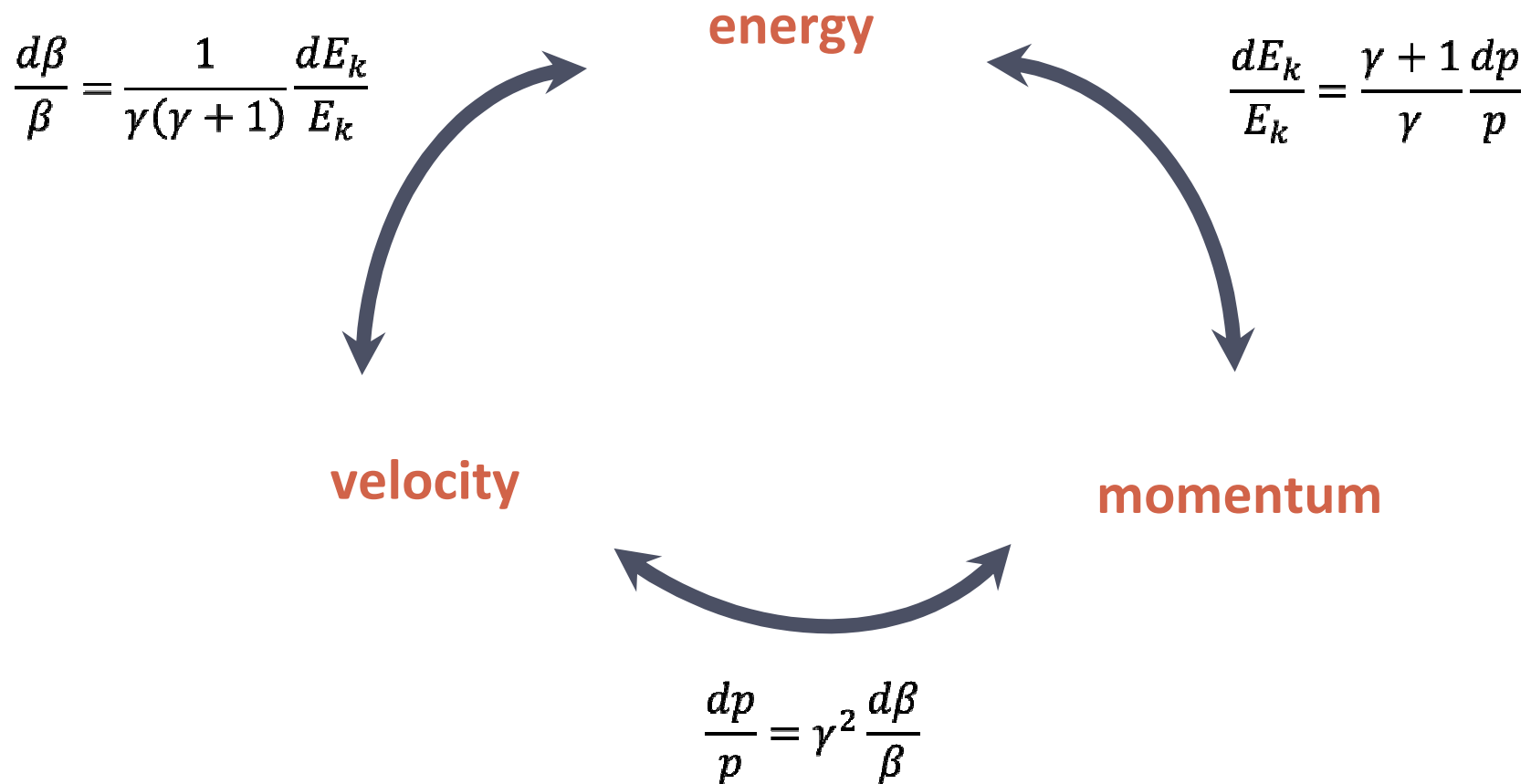


relativistic quantities in the context of cyclotrons

A. Einstein
1879-1955



useful for calculations – differential relations



equation of motion in a classical cyclotron

centrifugal force mv^2/r



Lorentz force $qv \times B$



$$m\ddot{r} = mr\dot{\phi}^2 - qr\dot{\phi}B_z$$

focusing: consider small deviations x from beam orbit R ($r = R+x$):

$$\begin{aligned}\ddot{x} + \frac{q}{m}vB_z(R+x) - \frac{v^2}{R+x} &= 0, \\ \ddot{x} + \frac{q}{m}v \left(B_z(R) + \frac{dB_z}{dR}x \right) - \frac{v^2}{R} \left(1 - \frac{x}{R} \right) &= 0, \\ \ddot{x} + \omega_c^2(1+k)x &= 0.\end{aligned}$$

$$\text{using: } \omega_c = qB_z/m \approx v/R, \quad r\dot{\phi} \approx v, \quad k = \frac{R}{B} \frac{dB}{dR}$$

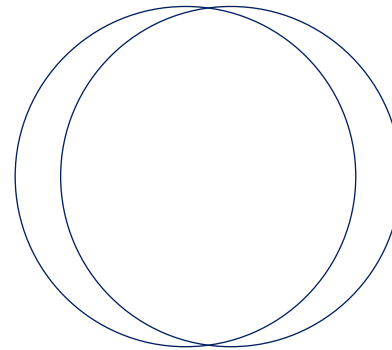


betatron tunes in cyclotrons

thus in radial plane:

$$\begin{aligned}\omega_r &= \omega_c \sqrt{1+k} = \omega_c \nu_r \\ \nu_r &= \sqrt{1+k} \\ &\approx \gamma\end{aligned}$$

note: simple case for $k = 0$: $\nu_r = 1$
(one circular orbit oscillates w.r.t the other)

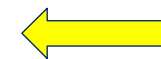


using Maxwell to relate B_z and B_R :

$$\text{rot } \vec{B} = \frac{dB_R}{dz} - \frac{dB_z}{dR} = 0$$

in vertical plane:

$$\nu_z = \sqrt{-k}$$

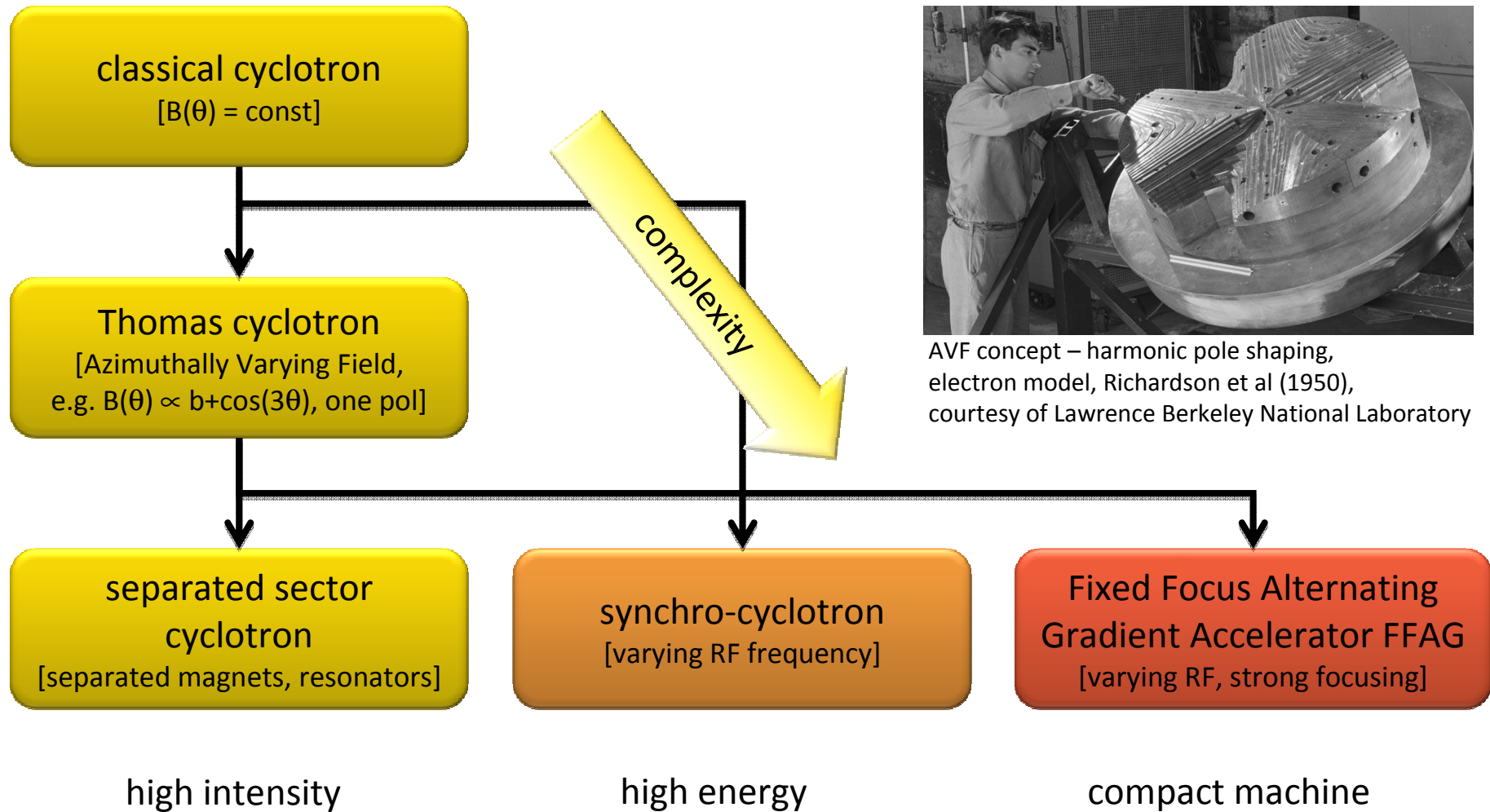


$k < 0$ to obtain
vertical focus.

**thus: in classical cyclotron $k < 0$ required;
however this violates isochronous condition $k = \gamma^2 - 1 > 0$**

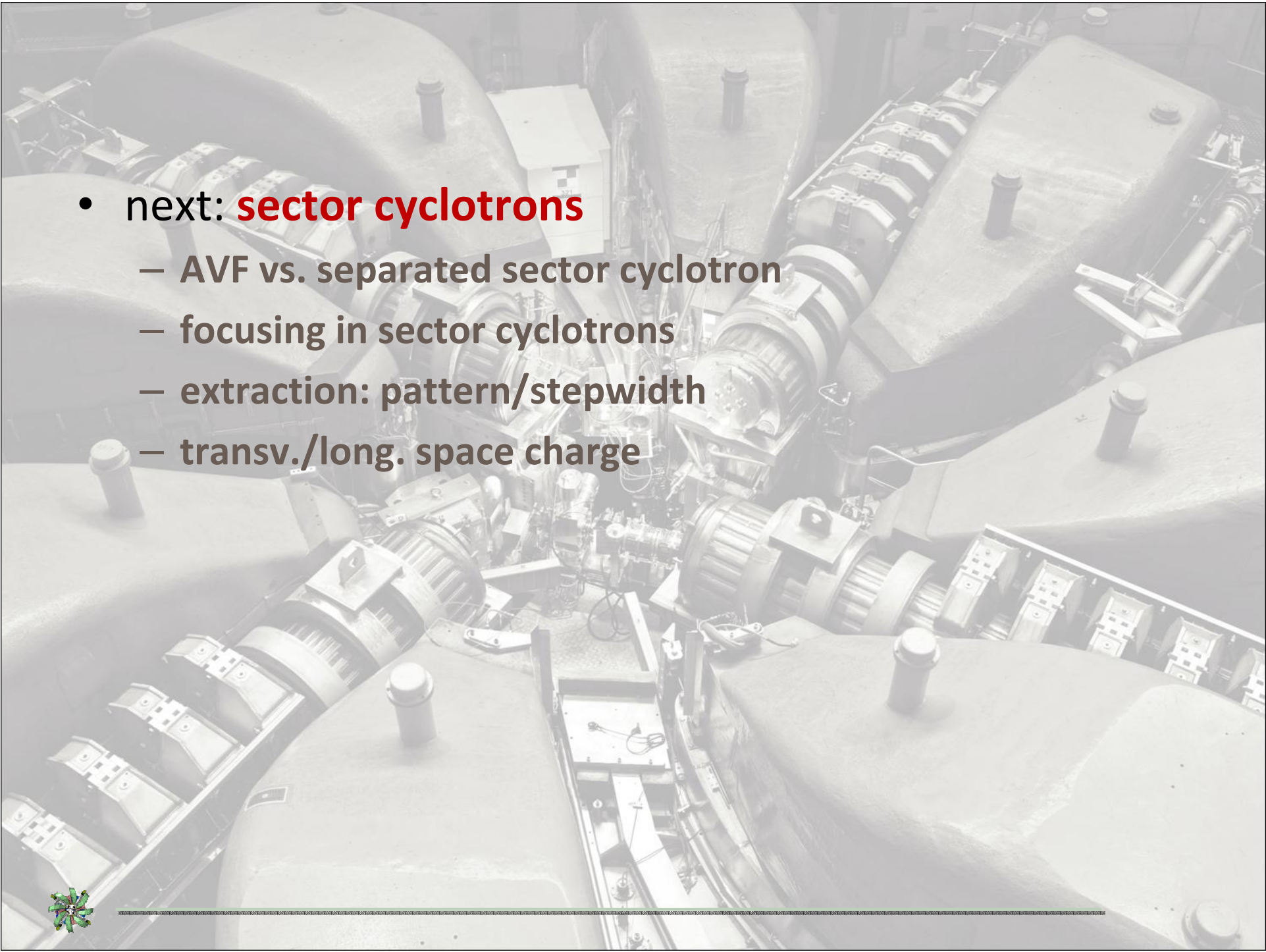


classification of cyclotron like accelerators



AVF concept – harmonic pole shaping, electron model, Richardson et al (1950), courtesy of Lawrence Berkeley National Laboratory



- 
- next: **sector cyclotrons**
 - AVF vs. separated sector cyclotron
 - focusing in sector cyclotrons
 - extraction: pattern/stepwidth
 - transv./long. space charge



focusing in sector cyclotrons

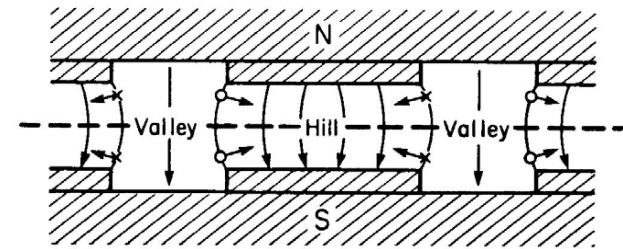
hill / valley variation of magnetic field (Thomas focusing) makes it possible to design cyclotrons for higher energies

Flutter factor:

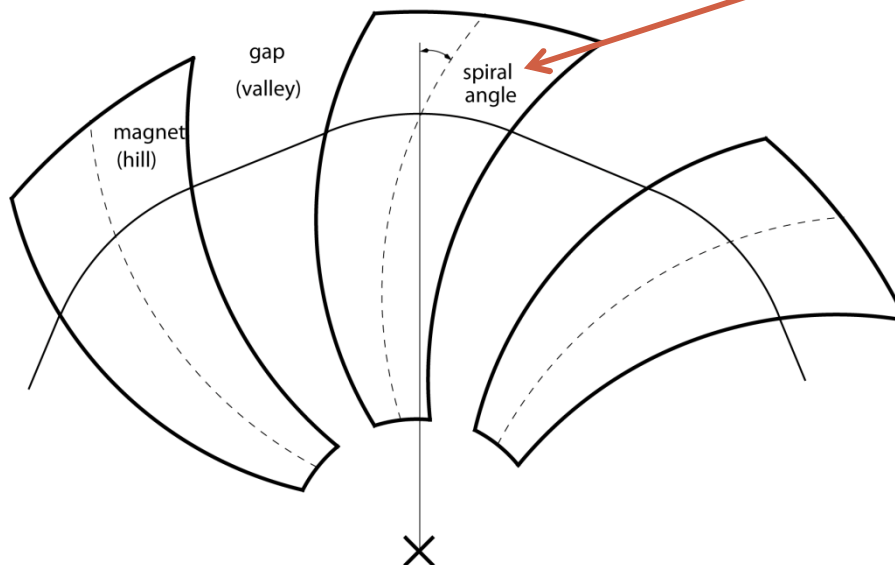
$$F^2 = \frac{\overline{B_z^2} - \overline{B_z}^2}{\overline{B_z}^2}$$

with flutter and additional spiral angle
of bending field:

$$\nu_z^2 = -\frac{R}{B_z} \frac{dB_z}{dR} + F^2(1 + 2 \tan^2 \delta)$$



[illustration of focusing at edges]

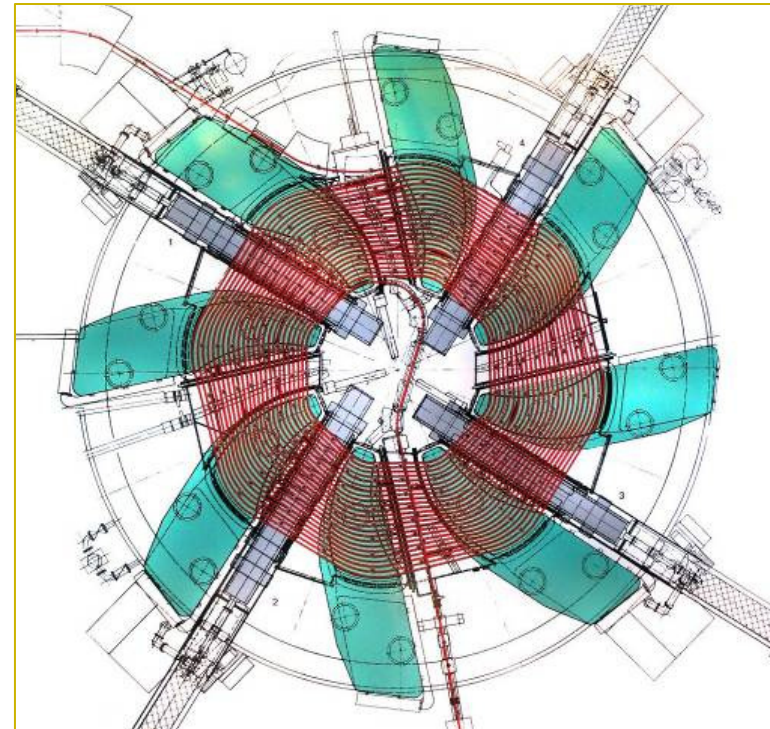


Azimuthally Varying Field vs. Separated Sector Cyclotrons



PSI/Varian comet: 250MeV sc. medical cyclotron

- **AVF = single pole with shaping**
- often **spiral poles** used
- **compact**, cost effective
- **internal source** possible
- **D-type RF electrodes**, relatively low energy gain
- depicted Varian cyclotron: 80% extraction efficiency; **not suited for high power**



PSI Ring cyclotron

- **modular layout**, larger cyclotrons possible, sector magnets, box resonators, stronger focusing, injection/extraction in straight sections
- **external injection** required, i.e. pre-accelerator
- **box-resonators** (high voltage gain)
- high **extraction efficiency** possible: e.g. PSI: 99.98% = $(1 - 2 \cdot 10^{-4})$



derivation of stepwidth / turn separation

$$BR = \sqrt{\gamma^2 - 1} \frac{m_0 c}{e} \longrightarrow \frac{dB}{B} + \frac{dR}{R} = \frac{\gamma d\gamma}{\gamma^2 - 1}$$

starting point: bending strength
 → compute total log.differential
 → use field index $k = R/B \cdot dB/dR$

$$\frac{dR}{d\gamma} = \frac{\gamma R}{\gamma^2 - 1} \frac{1}{1 + k}$$

radius change
per turn

$$\frac{dR}{dn_t} = \frac{dR}{d\gamma} \frac{d\gamma}{dn_t} = \frac{U_t}{m_0 c^2}$$

$$= \frac{U_t}{m_0 c^2} \frac{\gamma R}{(\gamma^2 - 1)(1 + k)}$$

$$= \frac{U_t}{m_0 c^2} \frac{\gamma R}{(\gamma^2 - 1) \nu_r^2}$$

$$= \frac{U_t}{m_0 c^2} \frac{R}{(\gamma^2 - 1) \gamma}$$

isochronicity not conserved
(just few outer turns)

isochronicity conserved
(general scaling)



stepwidth - discussion

for clean extraction a large stepwidth (turn separation) is of utmost importance; in the PSI Ring most efforts were directed towards maximizing the turn separation

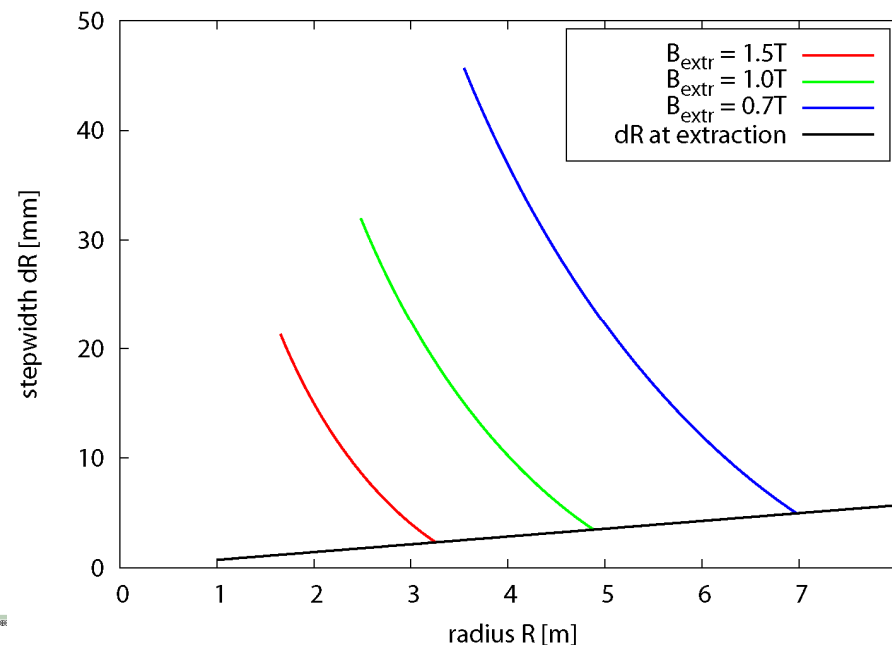
general scaling for
isochronous cyclotron:
$$\Delta R(R_{\text{extr}}) = \frac{U_t}{m_0 c^2} \frac{R_{\text{extr}}}{(\gamma^2 - 1)\gamma}$$

desirable:

- limited energy (< 1GeV)
- large radius R_{extr}
- high energy gain U_t

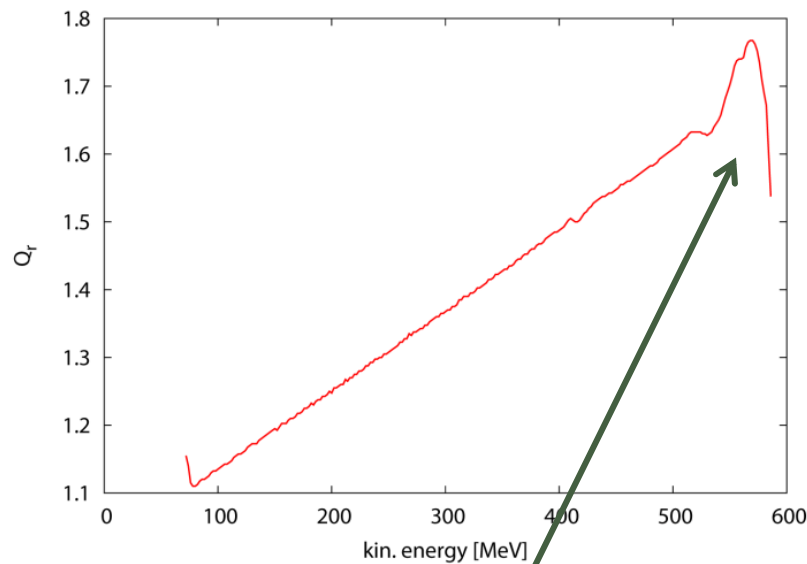
non-relativistic approx.,
scaling during acceleration:
$$\frac{dR}{dn_t} \approx \frac{U_t}{m_0 c^2} \frac{R}{\beta^2} \rightarrow \Delta R(R) \propto \frac{1}{R}$$

illustration:
stepwidth vs. radius in
cyclotrons of different sizes;
100MeV inj → 800MeV extr



extraction with off-center orbits

betatron oscillations around the “closed orbit” can be used to increase the radial stepwidth by a factor 3 !

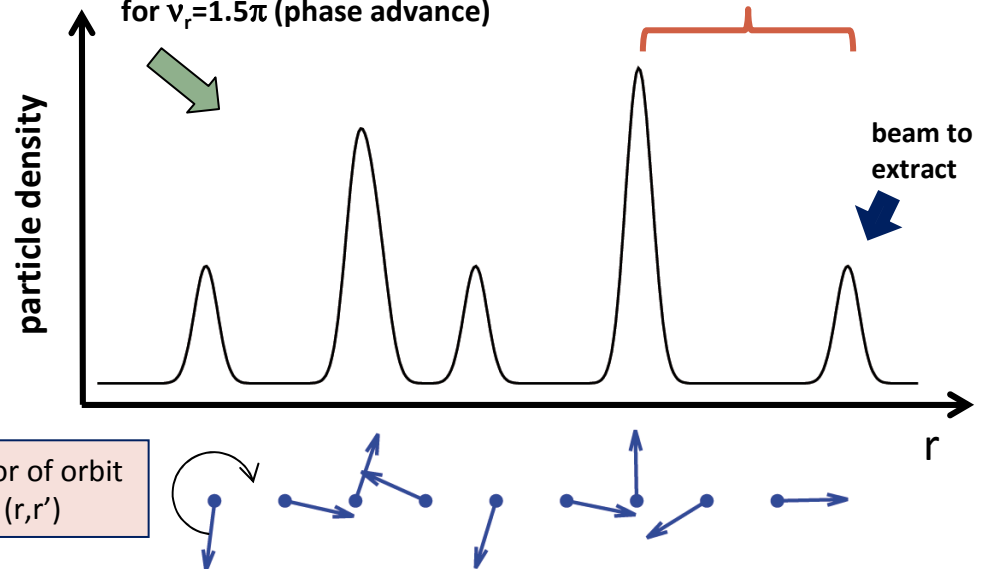


radial tune vs. energy (PSI Ring)
typically $\nu_r \approx \gamma$ during acceleration;
but decrease in outer fringe field

without orbit oscillations: stepwidth from E_k -gain (PSI: 6mm)



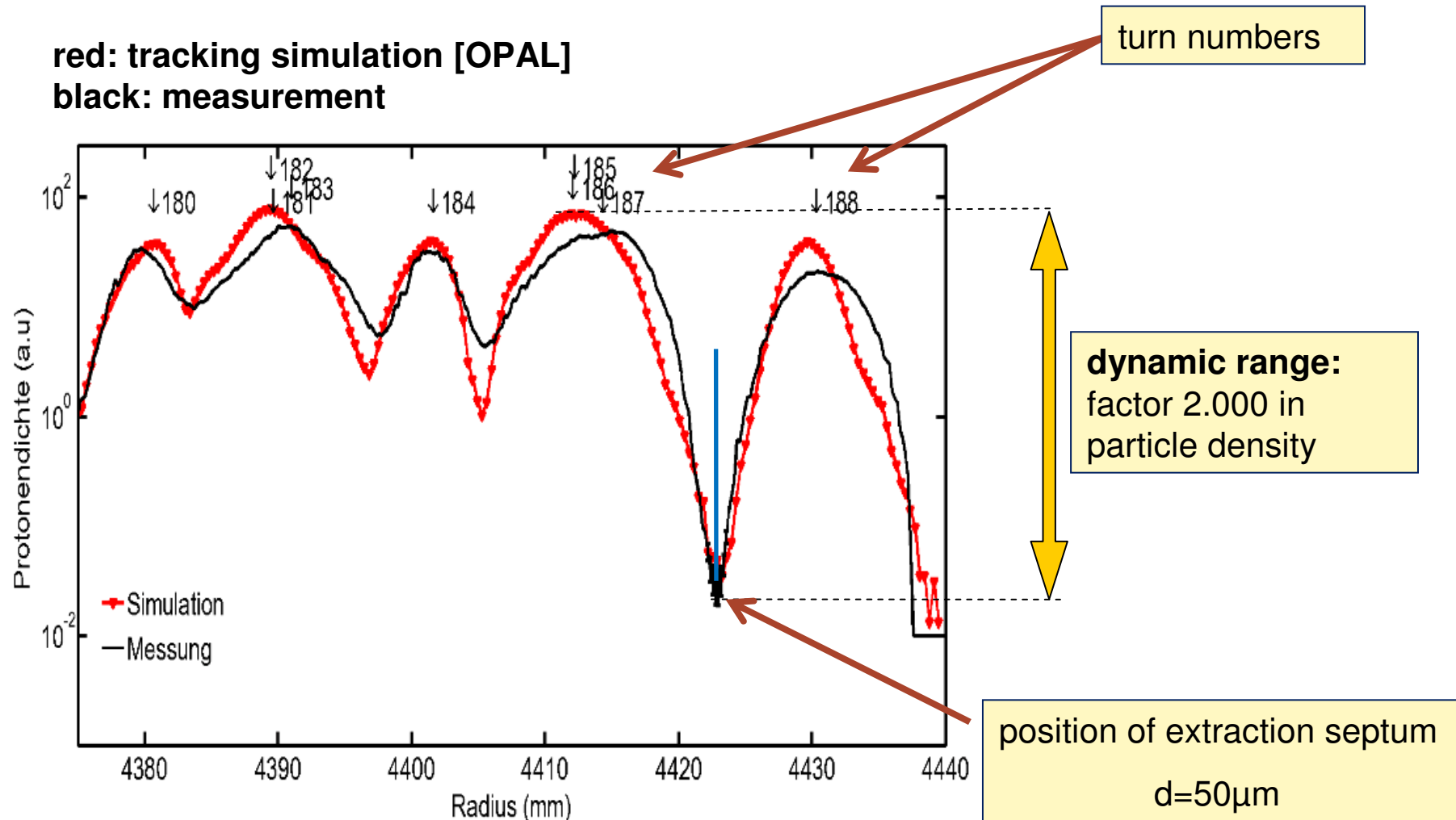
with orbit oscillations: extraction gap; up to 3 x stepwidth possible for $\nu_r = 1.5\pi$ (phase advance)



phase vector of orbit
oscillations (r, r')



extraction profile measured at PSI Ring Cyclotron



[Y.Bi et al]



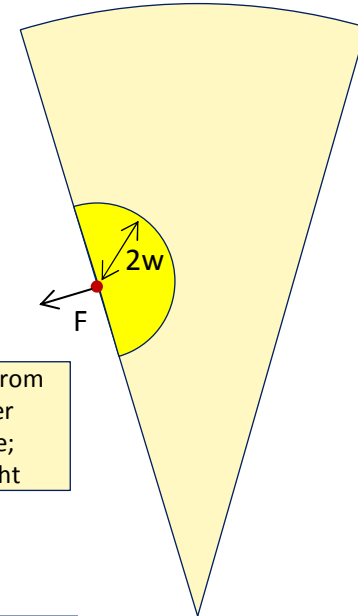
longitudinal space charge

sector model (W.Joho, 1981):

aim: compute **total energy spread** after acceleration process

generated by longitudinal electric field

- consider rotating sectors of charge
- uniform charge distribution (overlapping turns)
- test particle “sees” only fraction of sector due to shielding of vacuum chamber with gap height $2w$



$$E_{\theta} \approx \frac{\rho}{\epsilon_0} \cdot \frac{a \ln \left(4 \frac{w}{a} \right)}{\pi}$$

geometry factor from
integration over
“visible” charge;
 $2a$ = beam height

$$\begin{aligned} \rho &= \frac{Q}{\Delta R \cdot 2\pi R \cdot D_f \cdot 2a} \\ &= \frac{I_p}{\beta c \cdot \Delta R \cdot 2a} \end{aligned}$$

peak current =
constant

$$\frac{dU_{sc}}{dn} = 2\pi e R E_{\theta}$$

accumulated energy
spread per turn

$$= \frac{e R_{\infty} I_p Z_0 \ln \left(4 \frac{w}{a} \right)}{\Delta R}$$

turn separation →
varies through
acceleration



longitudinal space charge (cont.)

relation turn number / radius:

$$E_k \propto n_t \propto v^2 \propto R^2$$

non-relativistic !

$$R(n_t) = \sqrt{\frac{n_t}{n_{\max}}} R_{\max}$$

$$\frac{\Delta R}{\Delta n_t} = \frac{R_{\max}}{2\sqrt{n_t n_{\max}}}$$

next: integration over turns

front vs. trailing particle

$$\begin{aligned} \Delta U_{sc} &= 2 \cdot \int_{n_t=0}^{n_{\max}} \frac{dU_{sc}}{dn} dn_t \\ &= \frac{4eR_{\infty} I_p Z_0 \ln\left(4\frac{w}{a}\right) \sqrt{n_{\max}}}{R_{\max}} \int_{n_t=0}^{n_{\max}} \sqrt{n_t} dn_t \end{aligned}$$

for $w/a = 4$

$$= \frac{8}{3} e I_p Z_0 \ln\left(4\frac{w}{a}\right) \cdot \frac{n_{\max}^2}{\beta_{\max}}$$

$$\approx 2.800 \Omega \cdot e I_p \cdot \frac{n_{\max}^2}{\beta_{\max}}$$

note: scaling with squared number of turns

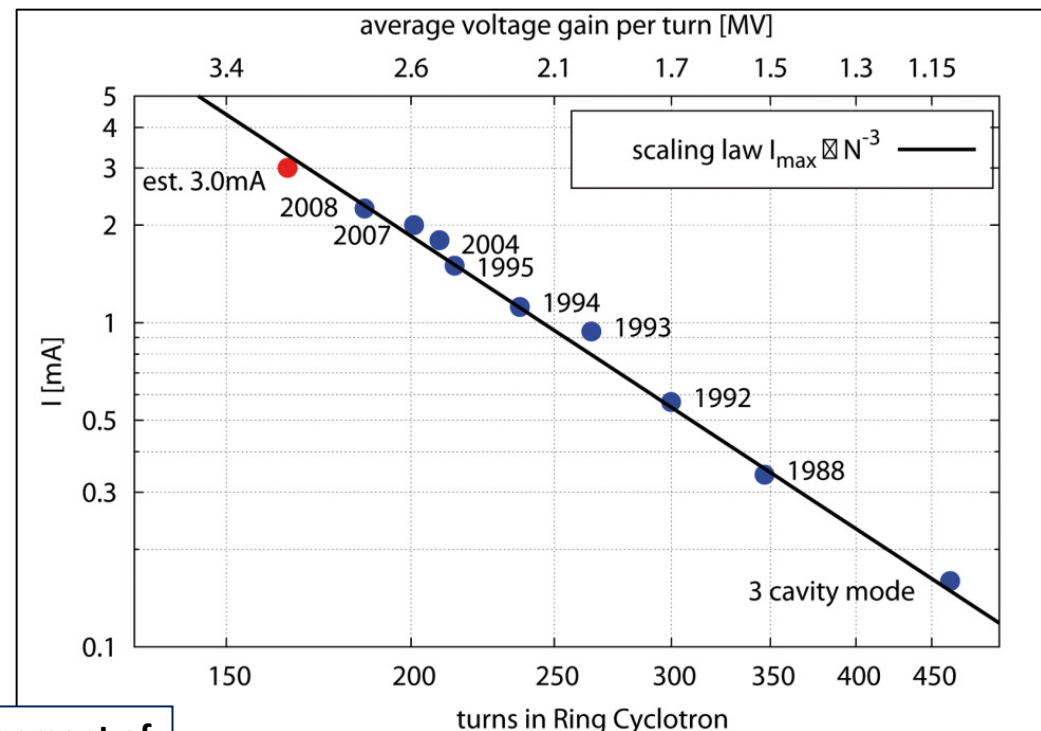


- energy spread is converted to transverse tails → losses at extraction
- in addition: turn separation at extraction element scales with n_{\max}^{-1} ; thus attainable current at constant losses scales as n_{\max}^{-3}

longitudinal space charge; evidence for third power law

- at PSI the maximum attainable current indeed scales with the third power of the turn number
- maximum energy gain per turn is of utmost importance in this type of high intensity cyclotron

→ thus with constant losses
at the extraction electrode the
maximum attainable current
scales as: $I_{\max} \propto n_t^{-3}$



historical development of
current and turn
numbers in PSI Ring
Cyclotron



different regime for very short bunches: formation of circular bunch

in theory

strong space charge within a bending field leads to rapid
cycloidal motion around bunch center

[Chasman & Baltz (1984)]

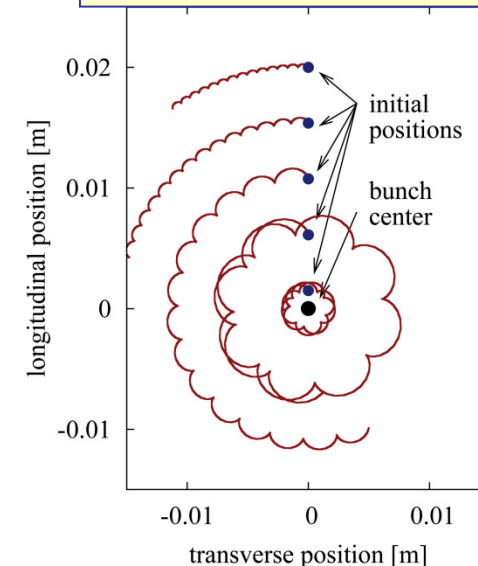
→ bound motion; circular equilibrium beam distribution

→ **see Ch. Baumgarten, ECPM 2012**

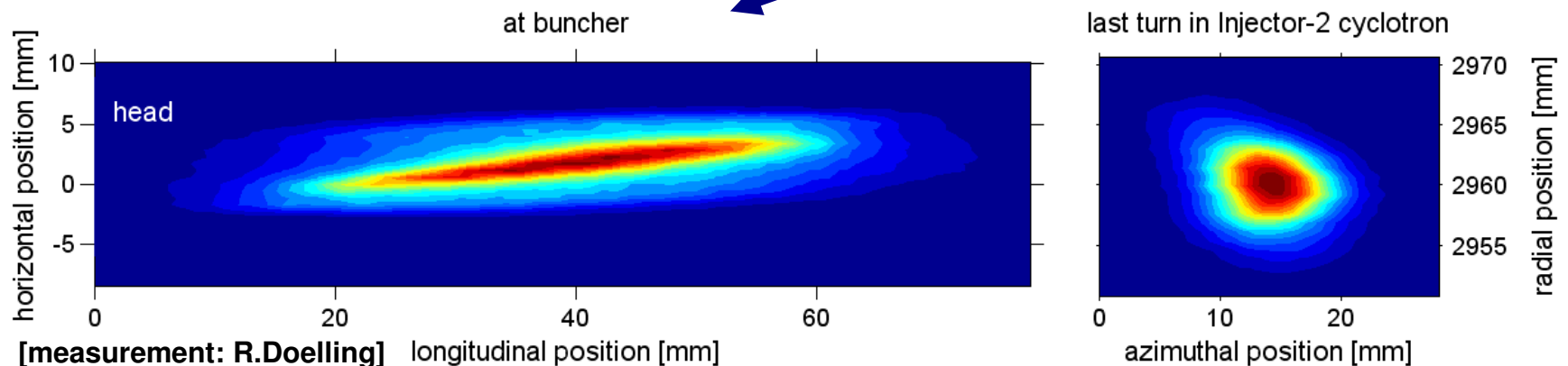
in practice

time structure measurement in injector II cyclotron → circular
bunch shape observed

**simplified model:
test charge in bunch field with
vertically oriented bending field**



blowup in ~20m drift



[measurement: R. Doelling]

transverse space charge

with overlapping turns use current sheet model!

vertical force from space charge: $F_y = \frac{n_v e^2}{\epsilon_0 \gamma^2} \cdot y$, $n_v = \frac{N}{(2\pi)^{\frac{3}{2}} \sigma_y D_f R \Delta R}$
[constant charge density, $D_f = I_{\text{avg}}/I_{\text{peak}}$]

focusing force: $F_y = -\gamma m_0 \omega_c^2 \nu_{y0}^2 \cdot y$

thus, eqn. of motion: $\ddot{y} + \left(\omega_c^2 \nu_{y0}^2 - \frac{n_v e^2}{\epsilon_0 m_0 \gamma^3} \right) y = 0$

→ equating space charge and focusing force delivers an **intensity limit for loss of focusing!**

tune shift from forces: $\Delta \nu_y \approx -n_v \frac{2\pi r_p R^2}{\beta^2 \gamma^3 \nu_{y0}}$
 $\approx -\sqrt{2\pi} \frac{r_p R}{e \beta c \nu_{y0} \sigma_z} \frac{m_0 c^2}{U_t} I_{\text{avg}}$





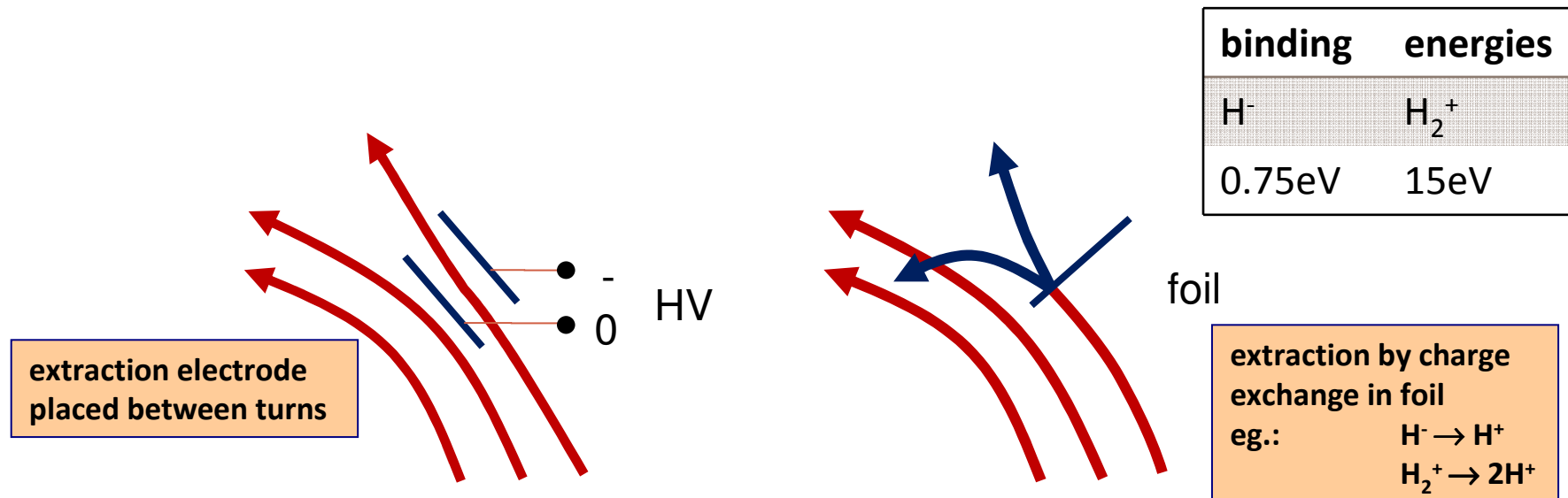
next: **cyclotron subsystems**

- extraction schemes
- RF systems/power efficiency
- cyclotron magnets
- comments on vacuum
- specific instrumentation

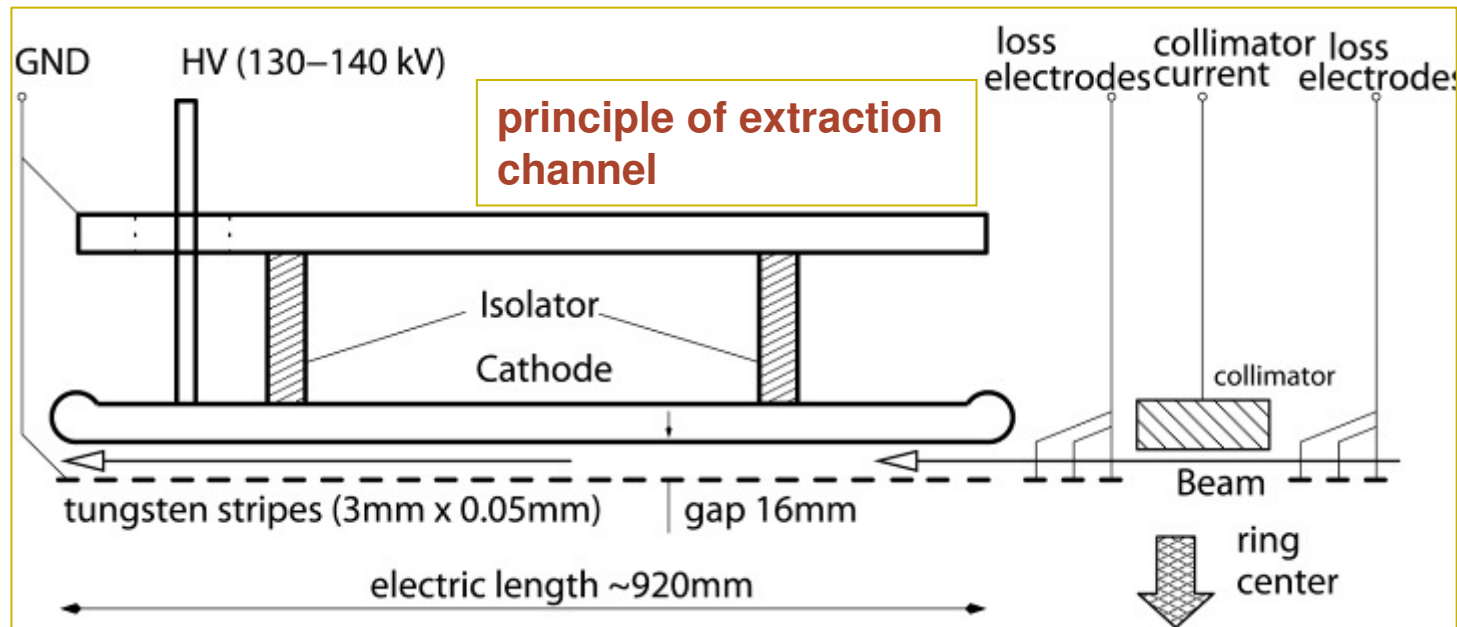


injection/extraction schemes

- deflecting element should affect just one turn, not neighboured turn → critical, cause of losses
- often used: electrostatic deflectors with thin electrodes
- alternative: charge exchange, stripping foil; accelerate H^- or H_2^+ to extract protons (problem: significant probability for unwanted loss of electron; Lorentz dissociation: B-field low, scattering: vacuum 10^{-8} mbar)



injection/extraction with electrostatic elements



**parameters
extraction chan.:**

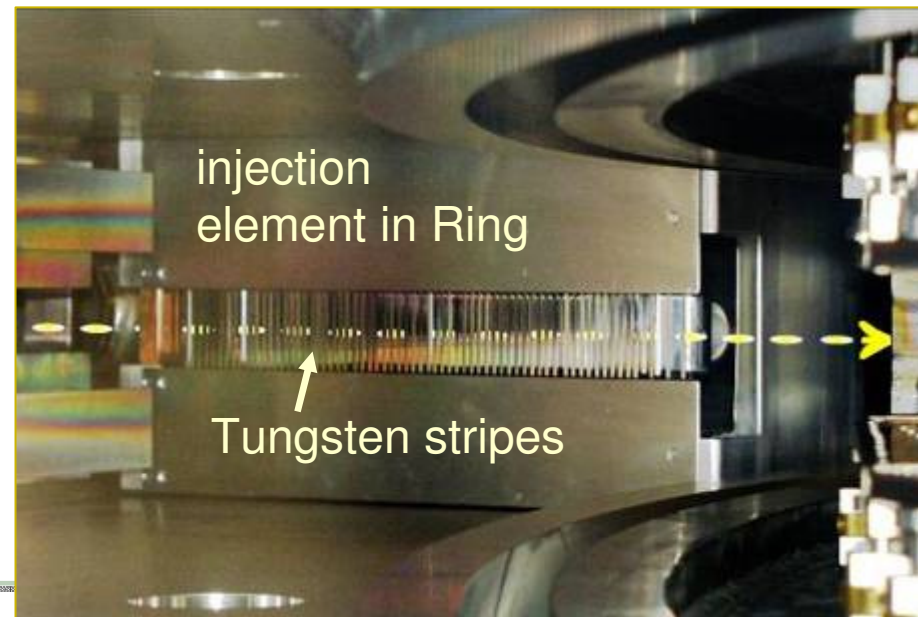
$E_k = 590 \text{ MeV}$
 $E = 8.8 \text{ MV/m}$
 $\theta = 8.2 \text{ mrad}$
 $\rho = 115 \text{ m}$
 $U = 144 \text{ kV}$

**major loss
mechanism is
scattering in $50 \mu\text{m}$
electrode!**

electrostatic rigidity:

$$E\rho = \frac{\gamma + 1}{\gamma} \frac{E_k}{q}$$

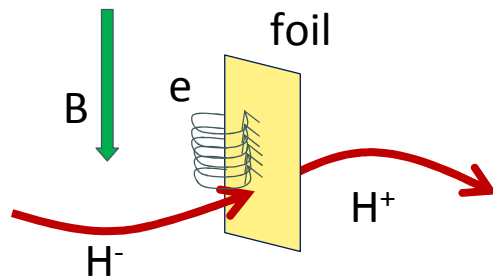
$$\theta = \frac{qlE}{E_k} \frac{\gamma}{\gamma + 1}$$



extraction foil

- thin foil, for example carbon, removes the electron(s) with high probability
- new charge state of ion brings it on a new trajectory → separation from circulating beam
- lifetime of foil is critical due to heating, fatigue effects, radiation damage
- conversion efficiencies, e.g. generation of neutrals, must be considered carefully

electrons removed from the ions spiral in the magnetic field and may deposit energy in the foil



How much power is carried by the electrons?

→ velocity and thus γ are equal for p and e

$$E_k = (\gamma - 1)E_0$$

$$\rightarrow E_k^e = \frac{E_0^e}{E_0^p} E_k^p = 5.4 \cdot 10^{-4} E_k^p$$

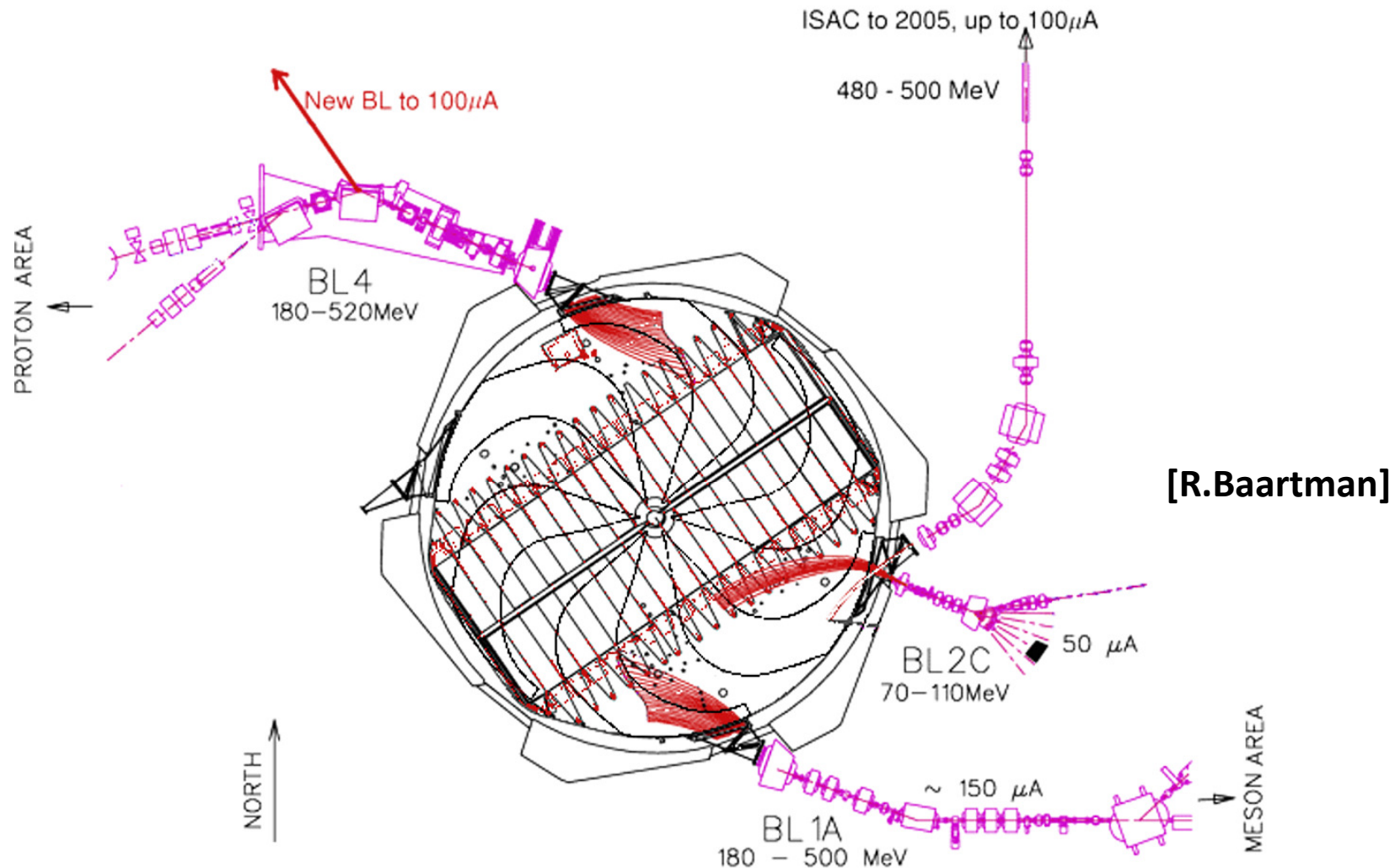
Bending radius of electrons?

$$\rho^e = \frac{E_0^e}{E_0^p} \rho^p$$

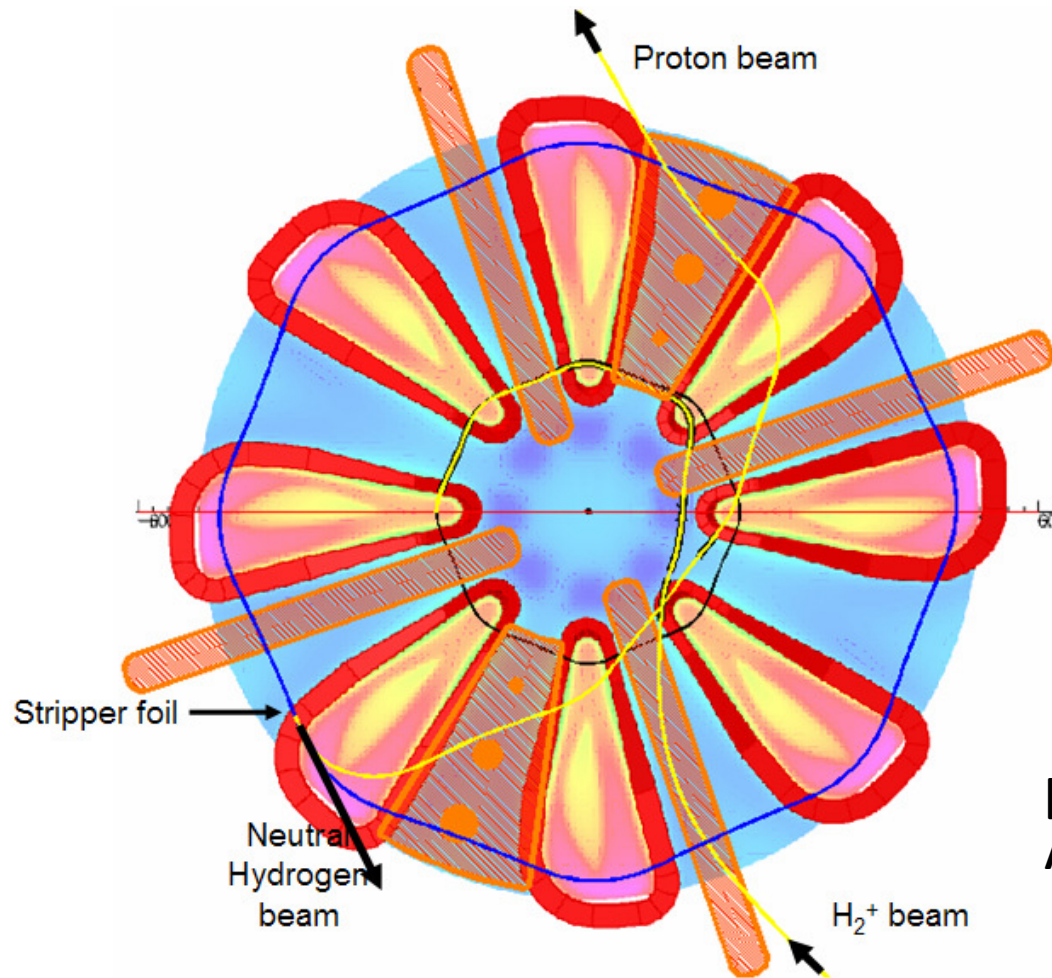
→ typically mm



example: multiple H^- stripping extraction at TRIUMF



example: H_2^+ stripping extraction in planned Daedalus cyclotron [neutrino source]



purpose: pulsed high
power beam for neutrino
production

- 800MeV
- 5MW

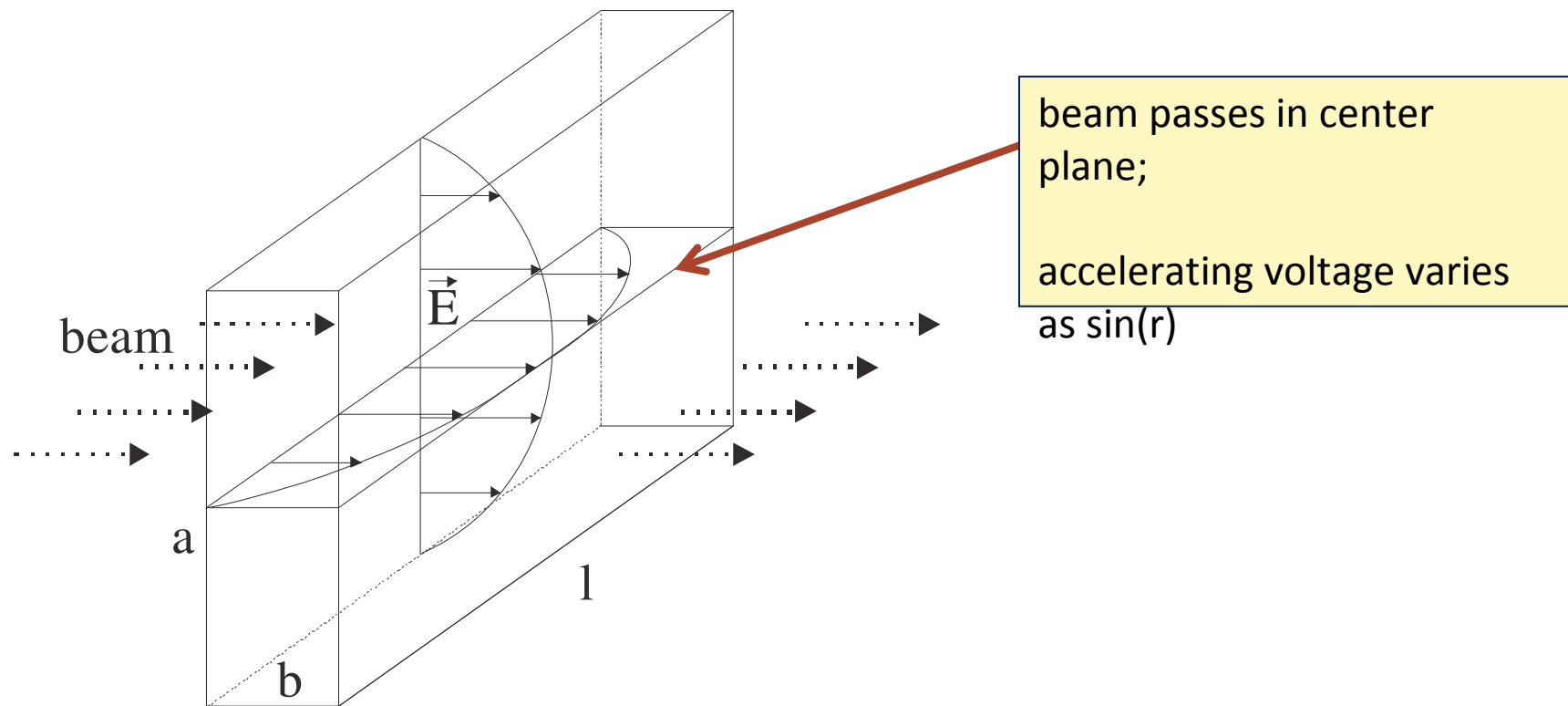
[L.Calabretta,
A.Calanna et al]



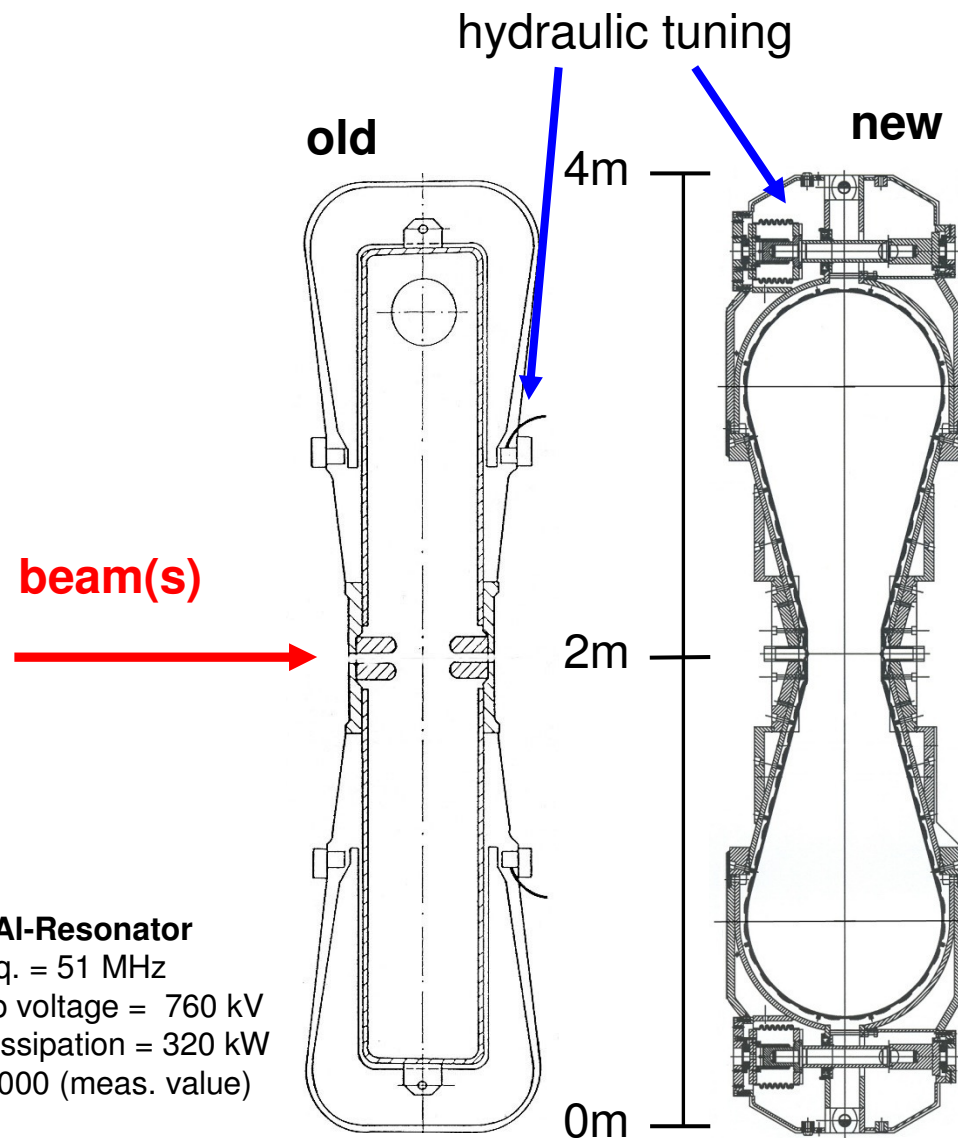
components: cyclotron resonators

cyclotron resonators are basically box resonators

resonant frequency:

$$f_r = \frac{c}{2} \sqrt{\frac{1}{a^2} + \frac{1}{l^2}}$$


cross sections of PSI resonators



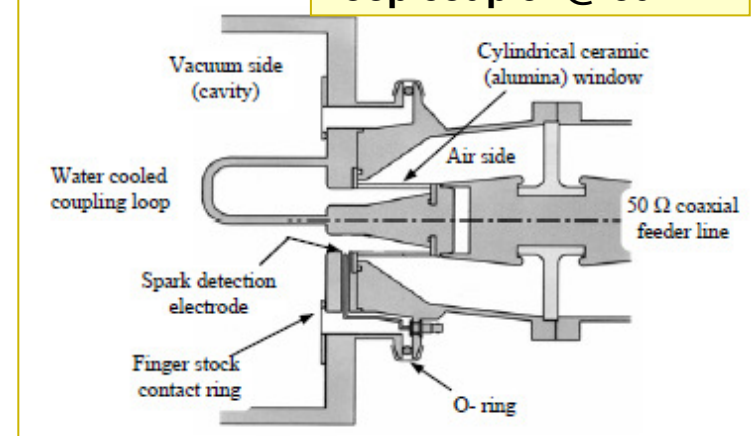
original Al-Resonator

Oper. freq. = 51 MHz
 Max. gap voltage = 760 kV
 Power dissipation = 320 kW
 $Q_0 = 32'000$ (meas. value)

new Cu-Resonator

Oper. freq. = 51 MHz
 Max. gap voltage > 1MV
 Power dissipation = 500 kW
 $Q_0 \approx 48'000$

loop coupler @ 50MHz



copper resonator in operation at PSI's Ring cyclotron

- $f = 50.6\text{MHz}$; $Q_0 = 4,8 \cdot 10^4$; $U_{\text{max}} = 1.2\text{MV}$ (presently 0.85MV)
- transfer of up to **400kW power to the beam** per cavity
- Wall Plug to Beam Efficiency (RF Systems): **32%**



resonator
inside

hydraulic tuning
devices (5x)



components: sector magnets

- cyclotron magnets typically cover a wide radial range → magnets are heavy and bulky, thus costly

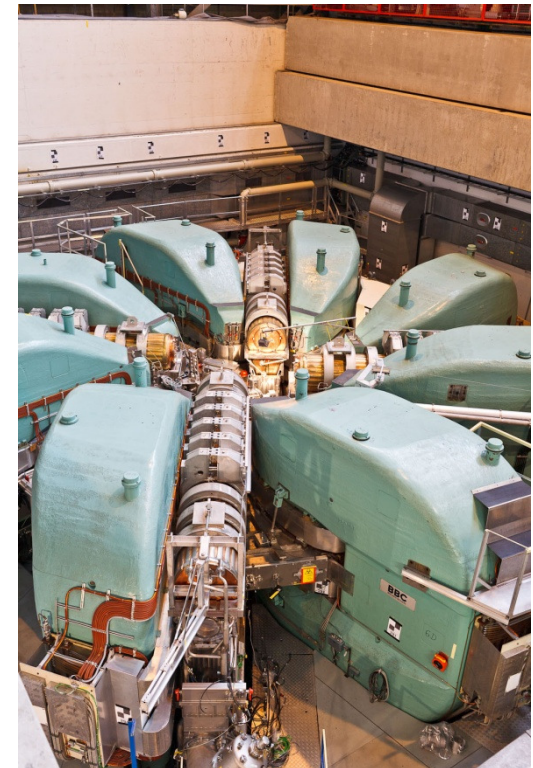
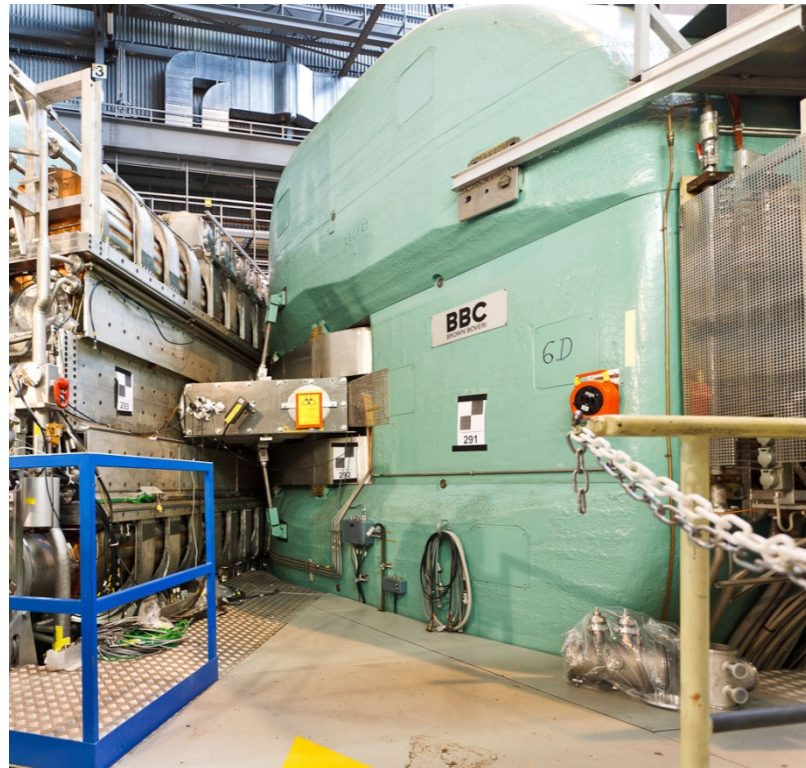
PSI sector magnet

iron weight: 250 tons

coil weight: 28 tons

orbit radius: 2.1...4.5 m

spiral angle: 35 deg



components: sector magnets

- focusing and isochronicity need to be precisely controlled → sophisticated pole shaping including spiral bounds, many trim coil circuits
- modern cyclotrons use superconducting magnets; but for high intensity compactness is generally disadvantageous

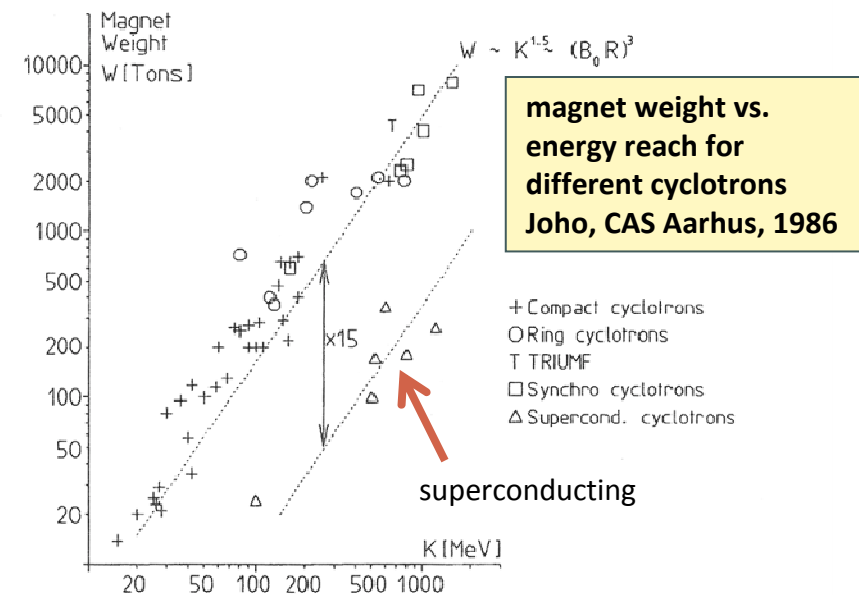
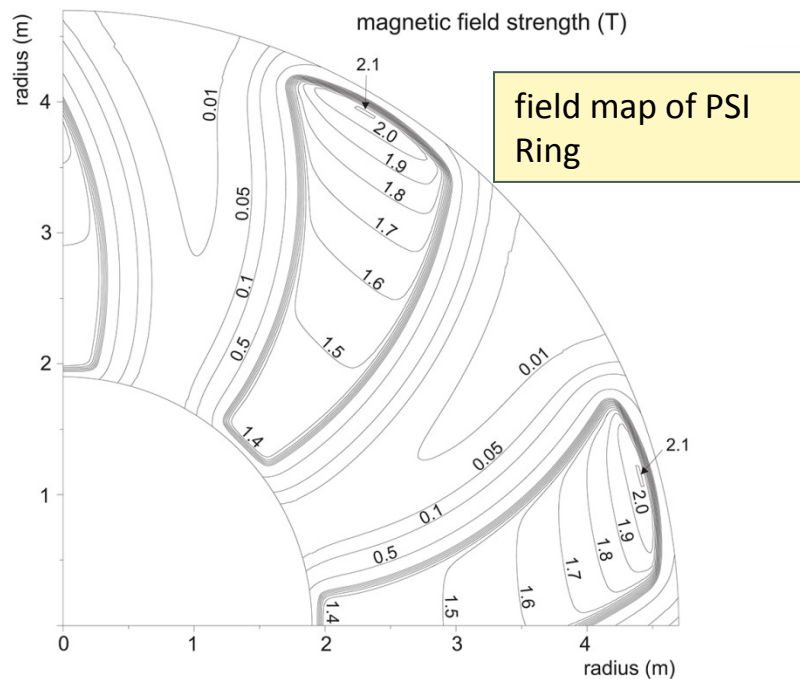
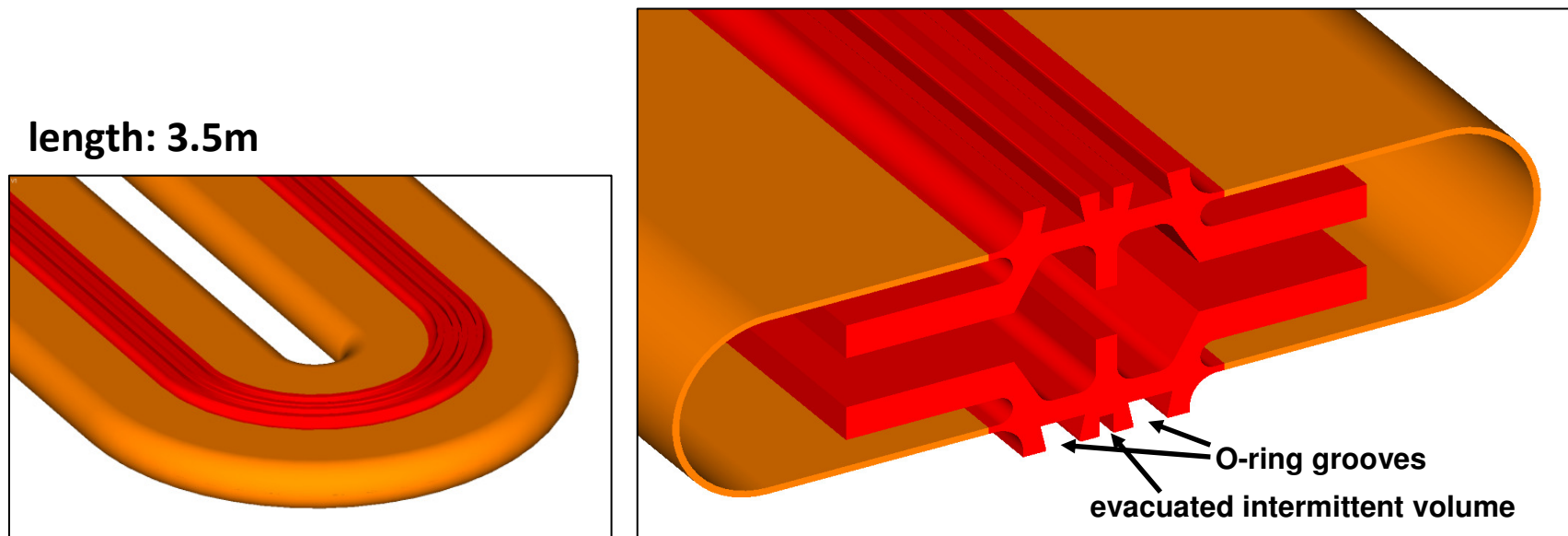


Fig. 6 Magnet weight W versus K-value for different cyclotrons and synchrocyclotrons.



cyclotron vacuum system

- vacuum chamber with large radial width → difficult to achieve precisely matching sealing surfaces → noticeable leak rates must be accepted
- use cryo pumps with high pumping speed and capacity
- $\approx 10^{-6}$ mbar for p, $\approx 10^{-8}$ mbar for ions (instability! e.g. AGOR at KVI)
- design criterion is easy access and fast mountability (activation)
example: inflatable seals installed between resonators; length: 3.5m



example: PSI 72MeV injector cyclotron

example: PSI 72MeV injector cyclotron



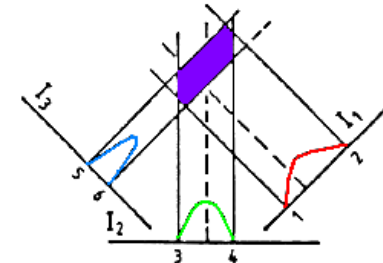
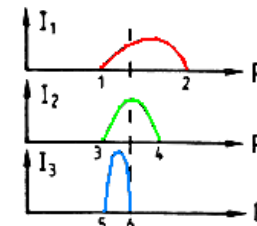
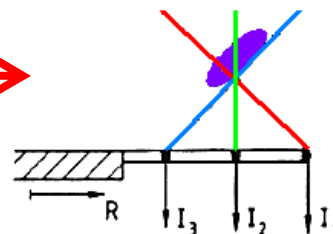
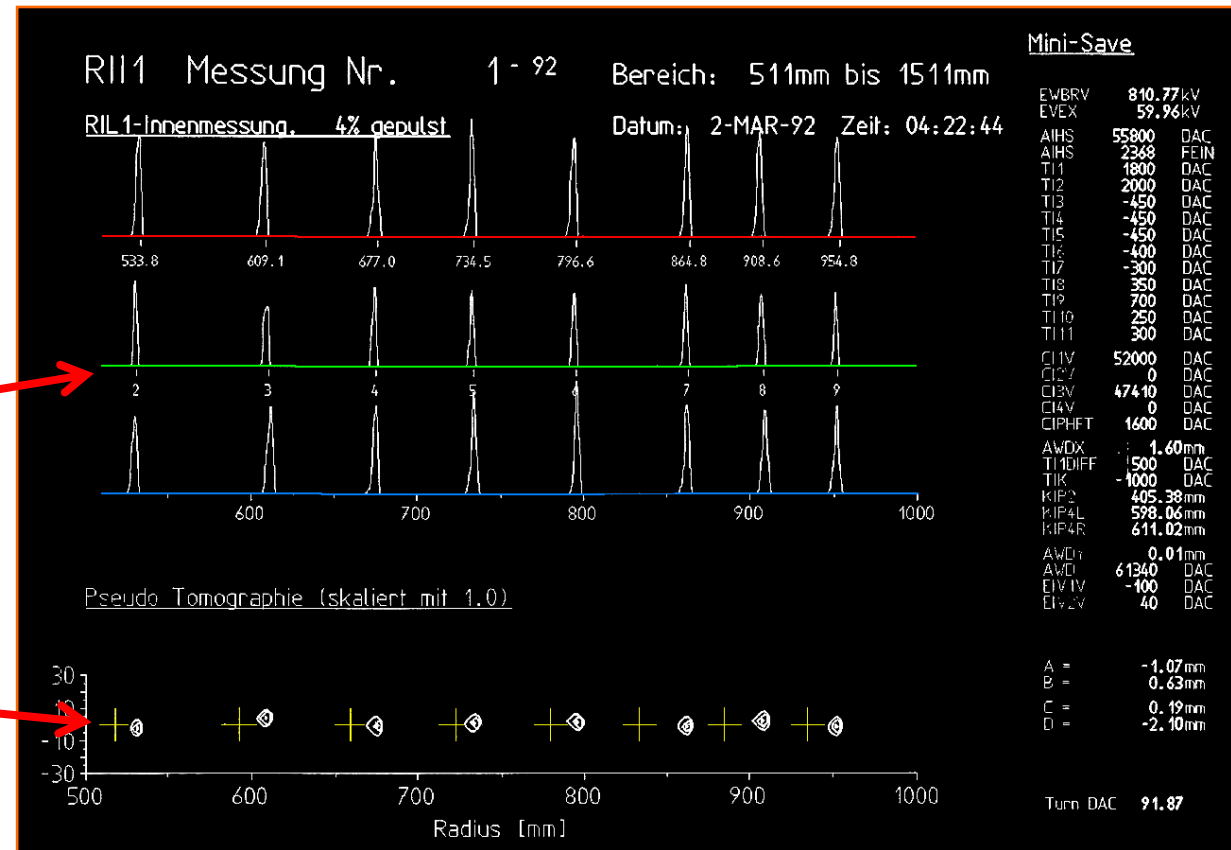
instrumentation: radial probe for turn counting / orbit analysis

wire scanner with three tilted wires delivers radial beam profile and some vertical information

radial: positions of individual turns

vertical/radial orbit positions and stored reference orbit (crosses)

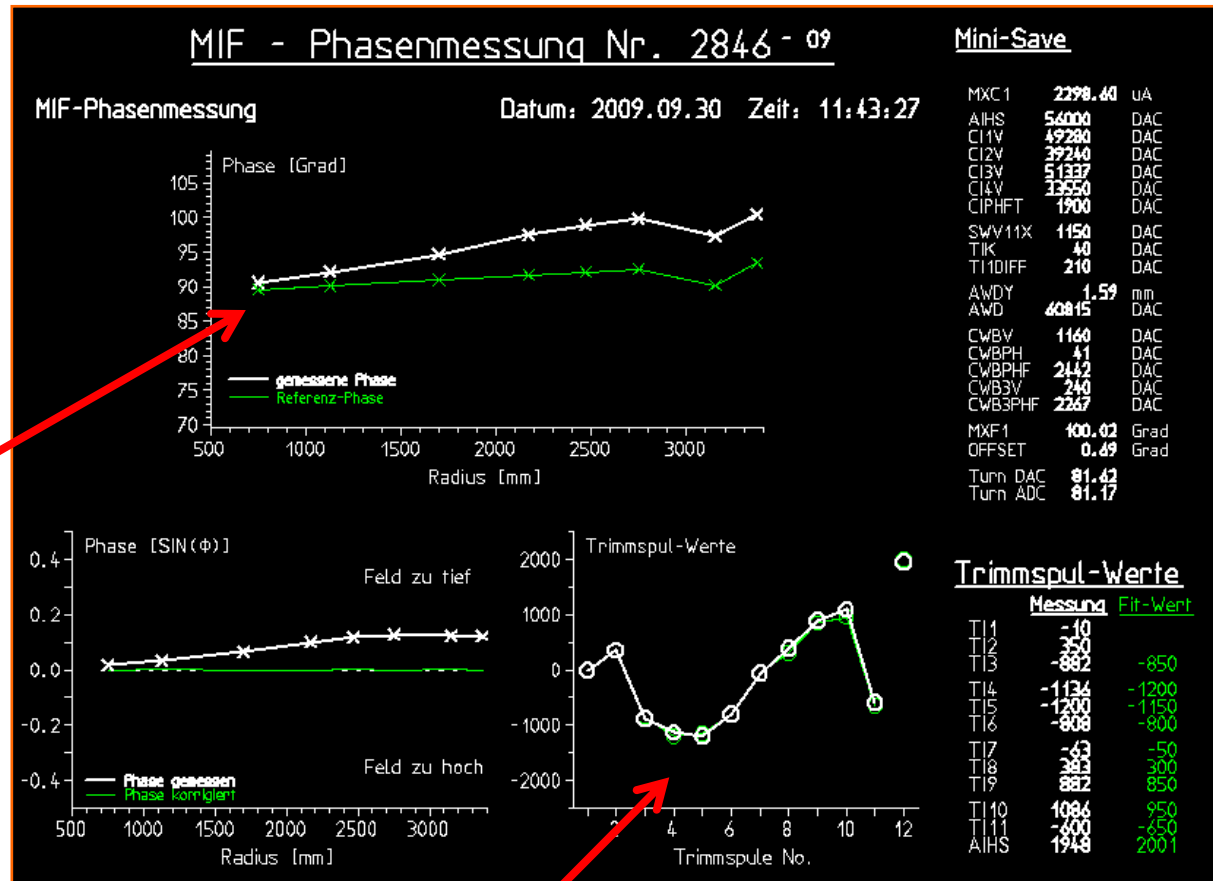
«pseudo tomography» with tilted wires



instrumentation: phase probes

phase probes are radially distributed RF pickups that detect the arrival time (phase) of bunches vs radius
→ adjustment of isochronicity

measured phase vs. radius;
green: reference phase for
«good conditions»



trim coil settings (12 circuits across radius)
green: predicted from phase measurement





next: **cyclotron examples**

- TRIUMF, RIKEN SRC, PSI-HIPA, PSI-Comet

comparison of cyclotrons

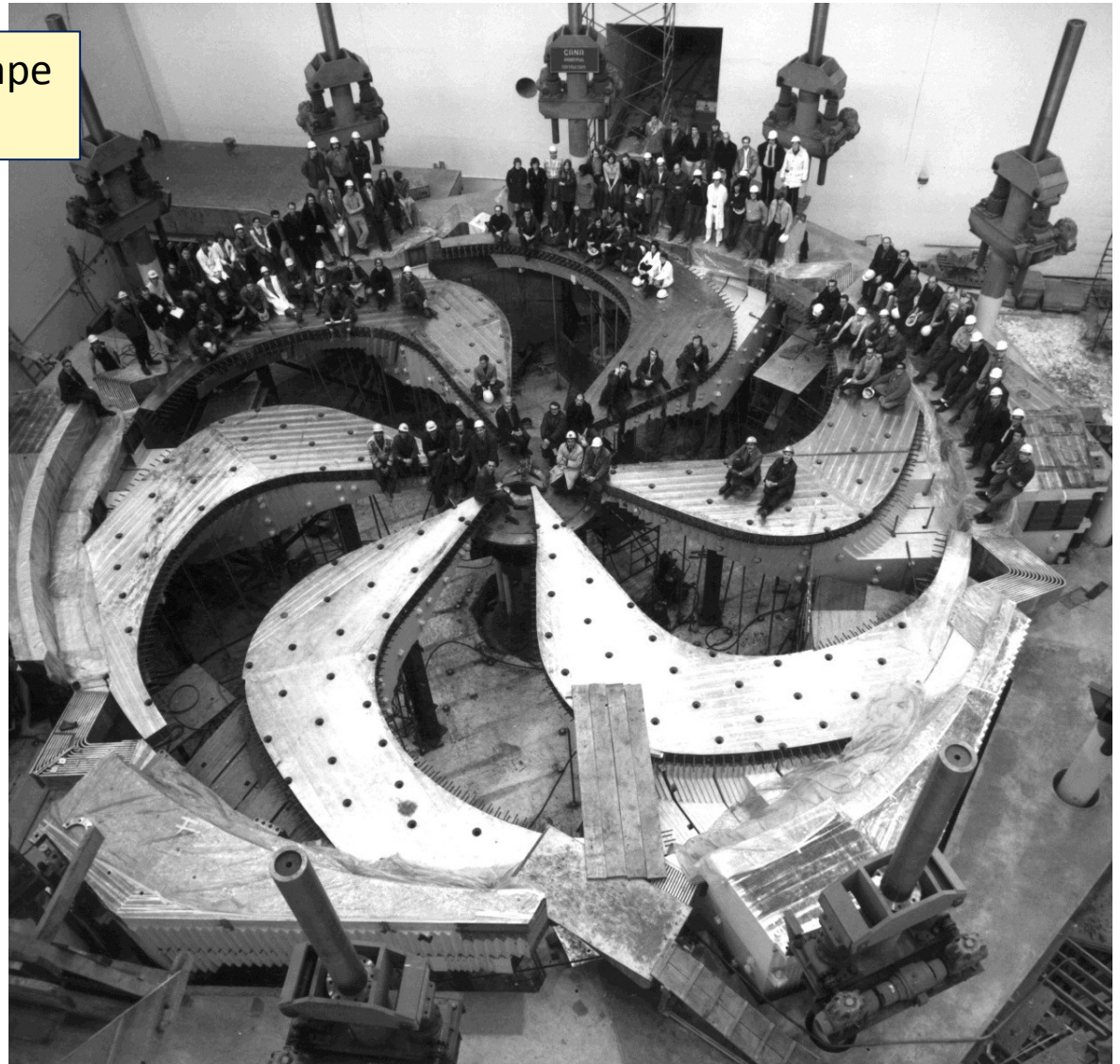
	TRIUMF	RIKEN SRC (supercond.)	PSI Ring	PSI medical (supercond.)
particles	H- \rightarrow p	ions	p	p
K [MeV]	520	2600	592	250
magnets (poles)	(6)	6	8	(4)
peak field strength [T]	0.6	3.8	2.1	3.8
R_{inj}/R_{extr} [m]	0.25/3.8...7.9	3.6/5.4	2.4/4.5	-/0.8
P_{max} [kW]	110	1 (86Kr)	1300	0.25
extraction efficiency (tot. transmission)	0.9995 (0.70)	(0.63)	0.9998	0.80
extraction method	stripping foil	electrostatic deflector	electrostatic deflector	electrostatic deflector
comment	variable energy	ions, flexible	high intensity	compact



cyclotron examples: TRIUMF

photo: iron poles with spiral shape
($\delta_{\max}=70\text{deg}$)

- p, 520MeV, up to 110kW beam power
- diameter: 18m (largest n.c. cyclotron worldwide)
- extraction by stripping H^- → variable energy; multiple extraction points possible



example: RIKEN (Jp) superconducting cyclotron

K = 2,600 MeV

Max. Field: 3.8T (235 MJ)

RF frequency: 18-38 MHz

Weight: 8,300 tons

Diameter: 19m

Height: 8m

superconducting

Sector Magnets :6

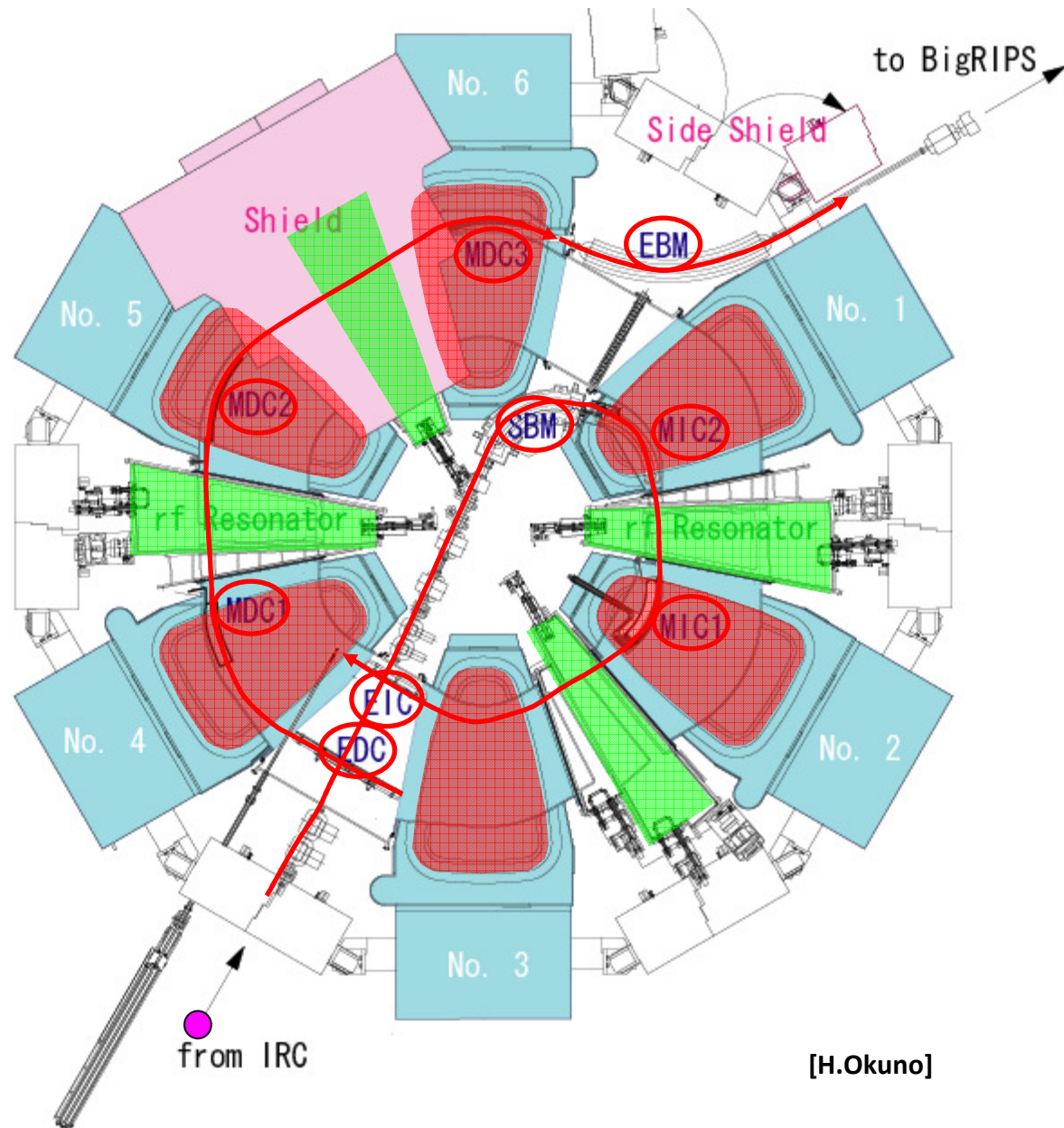
RF Resonator :4

Injection elements.

Extraction elements.

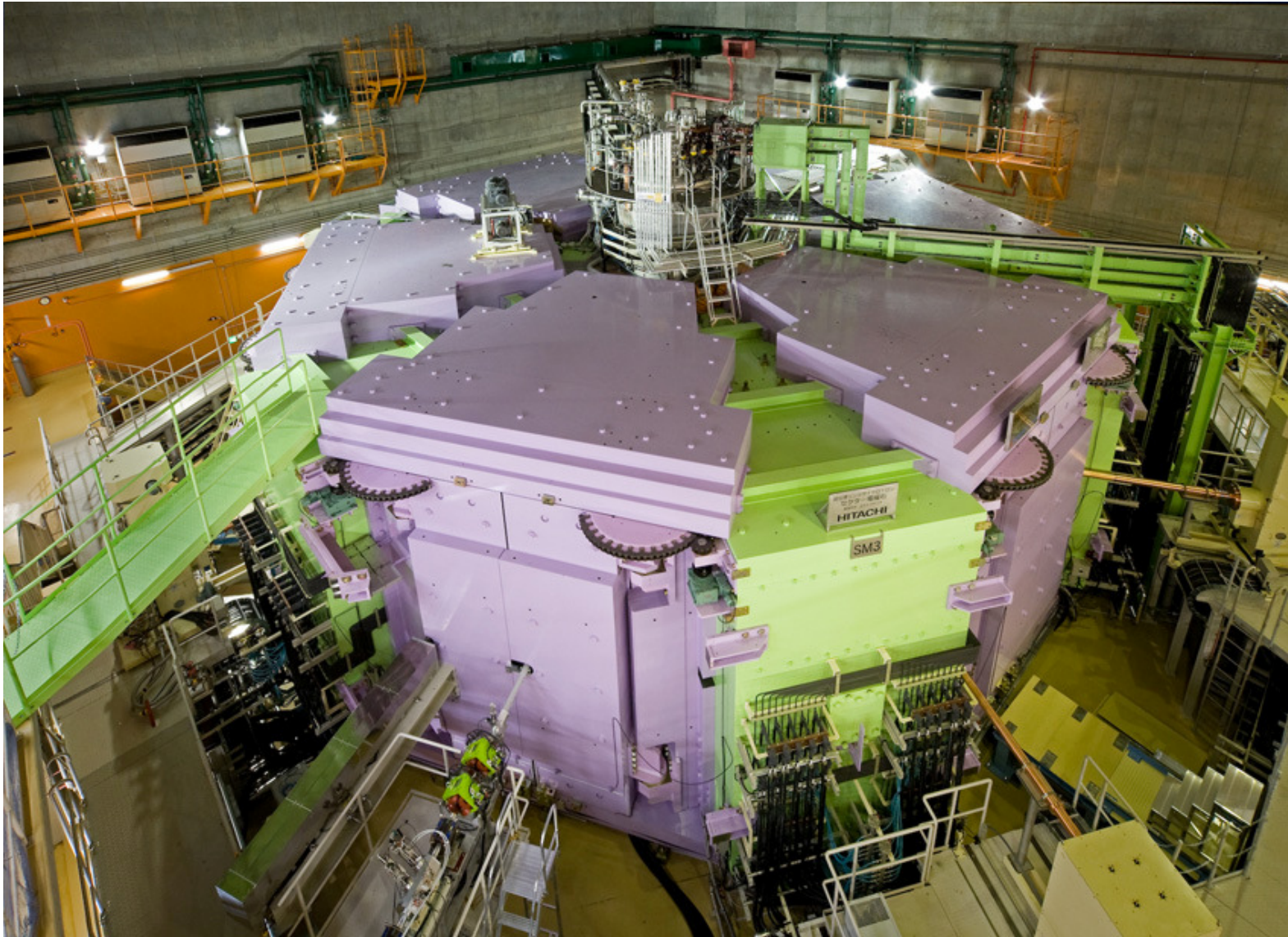
utilization:

***broad spectrum of
ions up to Uranium***

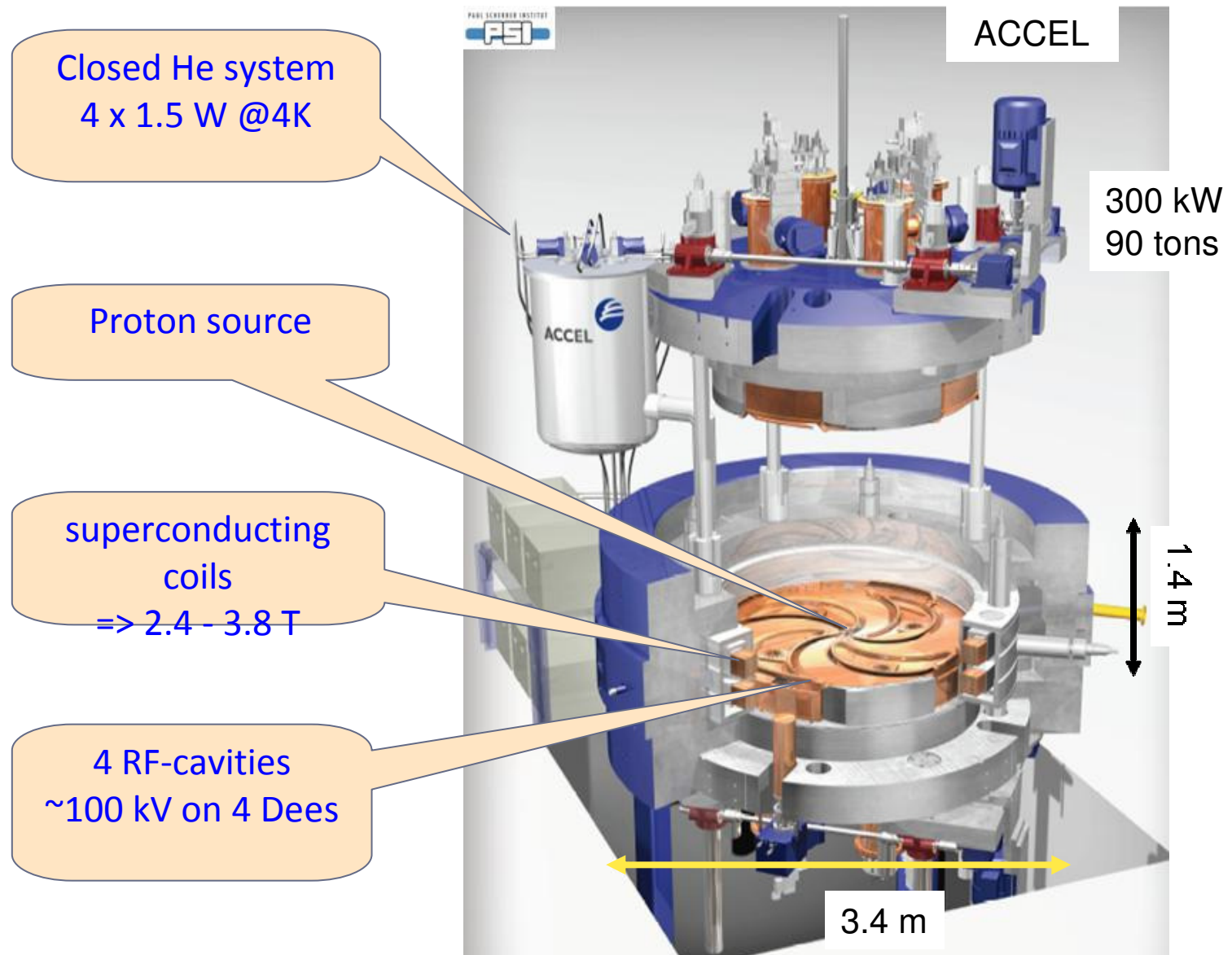


[H.Okuno]

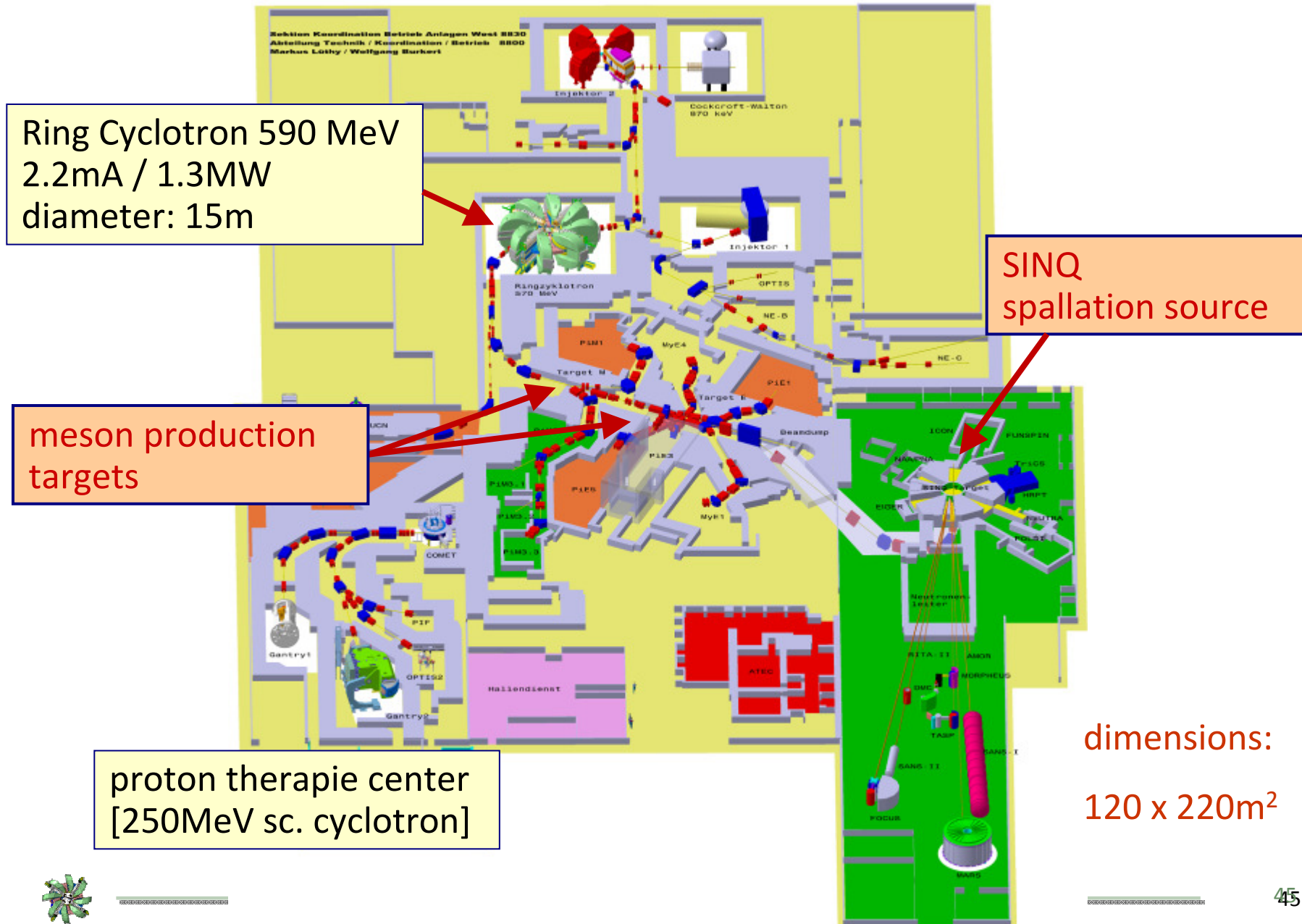
RIKEN SRC in the vault



250 MeV proton cyclotron (ACCEL/Varian)



examples: PSI High Intensity Proton Accelerator





















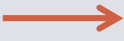




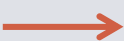









finally: **discussion**

- comparison of circular accelerators
- suitability of cyclotrons
- some literature



classification of circular accelerators

	bending radius	bending field vs. time	bending field vs. radius	RF frequency vs. time	operation mode (pulsed/CW)	
betatron						induction
microtron						varying h
classical cyclotron						simple, but limited E_k
isochronous cyclotron						suited for high power!
synchro- cyclotron						higher E_k , but low P
FFAG						strong focusing!
a.g. synchrotron						high E_k , strong focus



pro and contra cyclotron

limitations of cyclotrons	typical utilization of cyclotrons
<ul style="list-style-type: none">• energy limitation $\sim 1\text{GeV}$ due to relativistic effects• relatively weak focusing is critical for space charge effects (10mA ?)• tuning is difficult; field shape; many turns; limited diagnostics• wide vacuum vessel (radius variation)	<ul style="list-style-type: none">• medical applications $\leq 250\text{MeV}$; intensity range well covered• isotope production \rightarrow several 10MeV• acceleration of heavy ions (RIKEN)• very high intensity proton beams (PSI:1.4MW)



some literature w.r.t. cyclotrons

comprehensive overview on cyclotrons	L.M.Onishchenko, Cyclotrons: A Survey, Physics of Particles and Nuclei 39, 950 (2008) http://www.springerlink.com/content/k61mg262vng17411/fulltext.pdf
scaling of PSI concept to 10MW	Th.Stammbach et al, The feasibility of high power cyclotrons, Nuclear Instruments and Methods in Physics Research B 113 (1996) 1-7
space charge effects and scalings	W.Joho, High Intensity Problems in Cyclotrons, Proc. 5th intl. Conf. on Cyclotrons and their Applications, Caen, 337-347 (1981)
long. space charge; comparison to analytical result	E.Pozdeyev, A fast code for simulation of the longitudinal space charge effect in isochronous cyclotrons, cyclotrons (2001) http://accelconf.web.cern.ch/AccelConf/c01/cyc2001/paper/P4-11.pdf
H_2^+ concept for high power	L.Calabretta et al, A multi megawatt cyclotron complex to search for cp violation in the neutrino sector, cyclotrons (2010); upcoming NIM paper! http://accelconf.web.cern.ch/AccelConf/Cyclotrons2010/papers/tua1cio01.pdf
Ion induced desorption	E.Mahner et al, Review of heavy-ion induced desorption studies for particle accelerators, PRST-AB 11 (104801) http://accelconf.web.cern.ch/AccelConf/p01/PAPERS/WPAH036.PDF
OPAL simulations; documentation	J.Yang, A. Adelmann, et al. Phys. Rev. STAB Vol. 13 Issue 6 (2010) http://amas.web.psi.ch



thank your for your
attention !



cyclotrons – spare transparencies

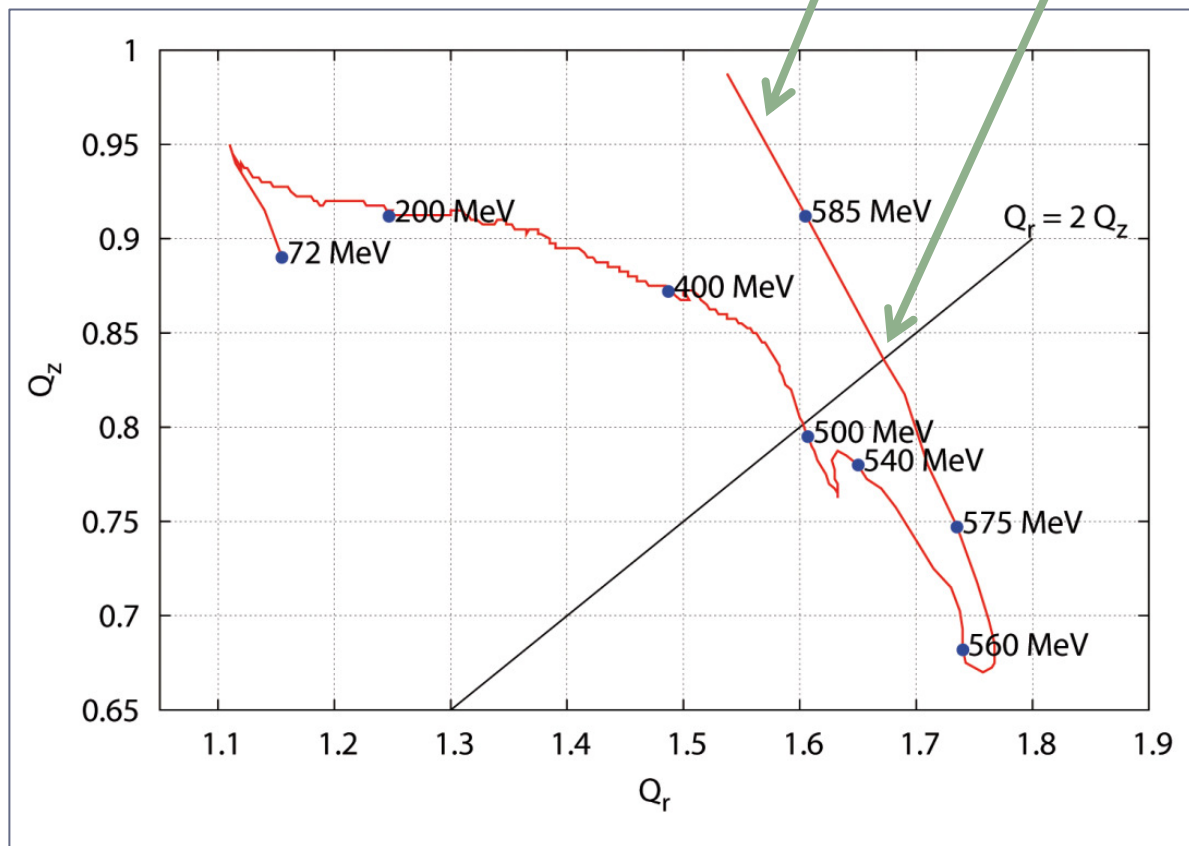
- tune diagram of PSI Ring cyclotron
- vacuum – estimate of required pressure
- measured activation levels
- 50MHz amplifier chain



PSI Ring Cyclotron – tune diagram

coupling resonance – pass quickly!

Q_r decreases towards extraction
– enhance turn separation



comments:

- special care has to be taken with fine-tuning the bending field in the extraction region
- running on the coupling resonance would transfer the large radial betatron amplitude into vertical oscillations, which must be avoided



Losses – required vacuum quality for protons

- losses are caused by inelastic scattering at residual gas molecules, use inelastic reaction cross section to estimate losses, convert to mean free path
- compute pressure for 10^{-5} relative loss

common gases :	$\lambda_{\text{inel}}(\text{air})$	=	747m
(norm.cond.)	$\lambda_{\text{inel}}(\text{CO})$	=	753m
	$\lambda_{\text{inel}}(\text{H}_2)$	=	6110m
	$\lambda_{\text{inel}}(\text{Ar})$	=	704m

mean free path:

$$\lambda_{\text{inel}} = \frac{A}{\rho N_A} \frac{1}{\sigma_{\text{inel}}}$$
$$\lambda_{\text{eff}} = \left(\frac{1}{P_0} \sum \frac{P_i}{\lambda_{\text{inel}}^i} \right)^{-1}$$

beam loss:

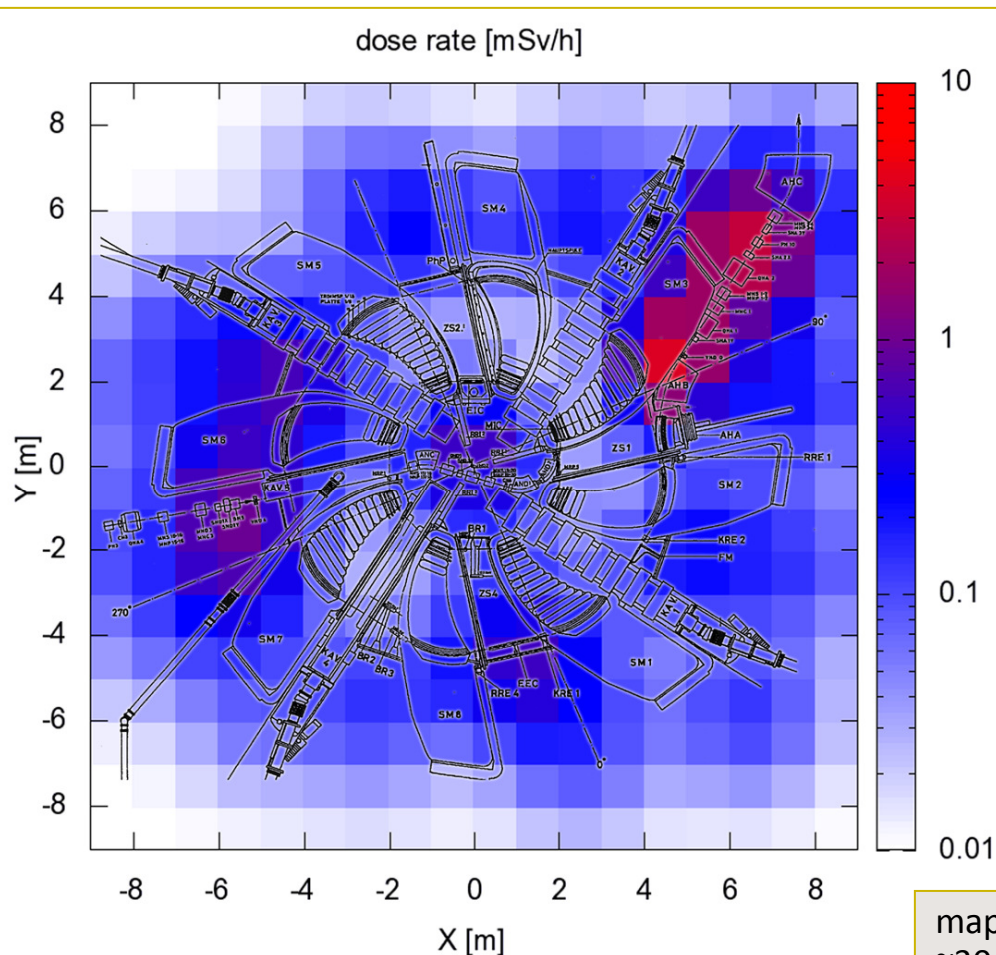
$$\frac{N_0 - N(l)}{N_0} = 1 - \exp(-l/\lambda_{\text{eff}}) \approx l/\lambda_{\text{eff}}$$

pressure for loss $< 10^{-5}$: $P_i(\text{air}) > 0.01 \text{ mbar} \rightarrow$ **easily achievable, vacuum no problem!**



losses and resulting activation in PSI Ring

- maximum intensity is limited by losses (typ. 200-400nA) and **activation**
- losses at extraction dominate the activation
- thus efforts at optimizing performance are concentrated on the extraction
→ **largest possible turn separation; design of electrostatic septum**



activation level allows for necessary service/repair work

- personnel dose for typical repair mission 50-300 μ Sv
- optimization by adapted local shielding measures; shielded service boxes for exchange of activated components
- detailed planning of shutdown work

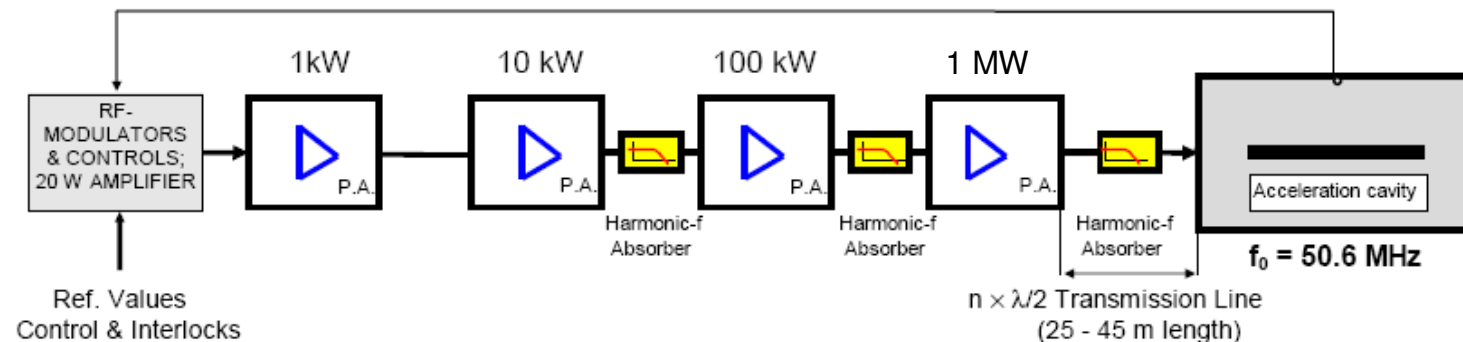
example (2010):
personnel dose for 3 month shutdown:

47mSv, 186 persons
max per person: 2.9mSv

map interpolated from
~30 measured locations

50 MHz 1 MW amplifier chain for Ring cyclotron

4- STAGE POWER AMPLIFIER CHAIN, EMPLOYING POWER TETRODE TUBES



Tube Types:	YL 1056	RS 2022 CL	RS 2074 HF	RS 2074 HF
Cooling Method:	forced air	forced air	water	water

Wall Plug to Beam Efficiency (RF Systems): **32%**
[AC/DC: 90%, DC/RF: 64%, RF/Beam: 55%]

[L.Stingelin et al]

