

# **680 Times Improved Measurement of the Antiproton Magnetic Moment**

Gerald Gabrielse

Leverett Professor of Physics, Harvard University  
Spokesperson of the CERN ATRAP Collaboration

Supported by NSF and AFOSR

- Antihydrogen
- Electron and Antiproton Magnetic Moments
- Does the Electron have an Electric Dipole Moment?

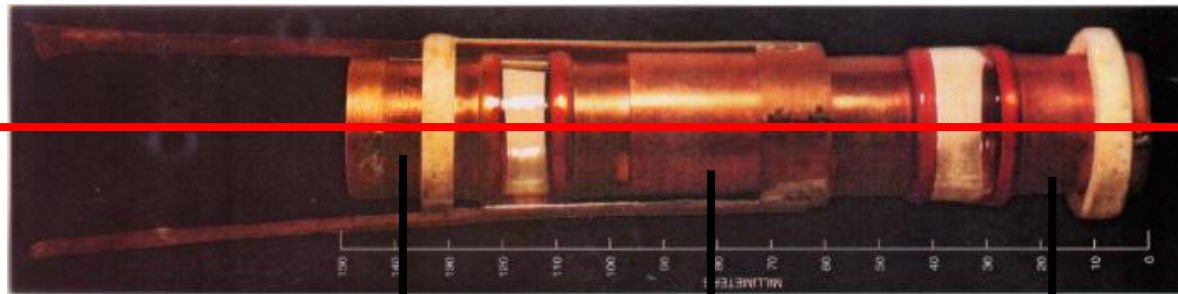
# Antihydrogen Update

# 27 Years Since We First Trapped and Then Cooled Antiprotons

TRAP Collaboration  
at CERN's LEAR

1 cm  
↔

21 MeV  
antiprotons



magnetic  
field

$10^{-10}$   
energy  
reduction

- Slow antiprotons in matter
- Capture antiprotons in flight
- Electron cooling  $\rightarrow$  4.2 K
- $5 \times 10^{-17}$  Torr

Now used by 5 collaborations  
at the CERN AD  
ATRAP, ALPHA, ASACUSA,  
AEGIS, BLAZE

# Proposal to Trap Cold Antihydrogen – 1986

- **Produce cold antihydrogen from cold antiprotons**

“When antihydrogen is formed in an ion trap, the neutral atoms will no longer be confined and will thus quickly strike the trap electrodes. Resulting annihilations of the positron and antiproton could be monitored. ...”

- **Trap cold antihydrogen**

- **Use accurate laser spectroscopy to compare antihydrogen and hydrogen**

“For me, the most attractive way ... would be to capture the antihydrogen in a neutral particle trap ... The objective would be to then study the properties of a small number of [antihydrogen] atoms confined in the neutral trap for a long time.”

Gerald Gabrielse, 1986 Erice Lecture (shortly after first pbar trapping)

In **Fundamental Symmetries**, (P.Bloch, P. Paulopoulos, and

R. Klapisch, Eds.) p. 59, Plenum, New York (1987).

Use trapped antihydrogen  
to measure antimatter gravity

G. Gabrielse, *Hyperfine Interact.* 44, 349 (1988)

# ATRAP Apparatus Built to do Two Types of Experiments Simultaneously

Antihydrogen  
Experiments

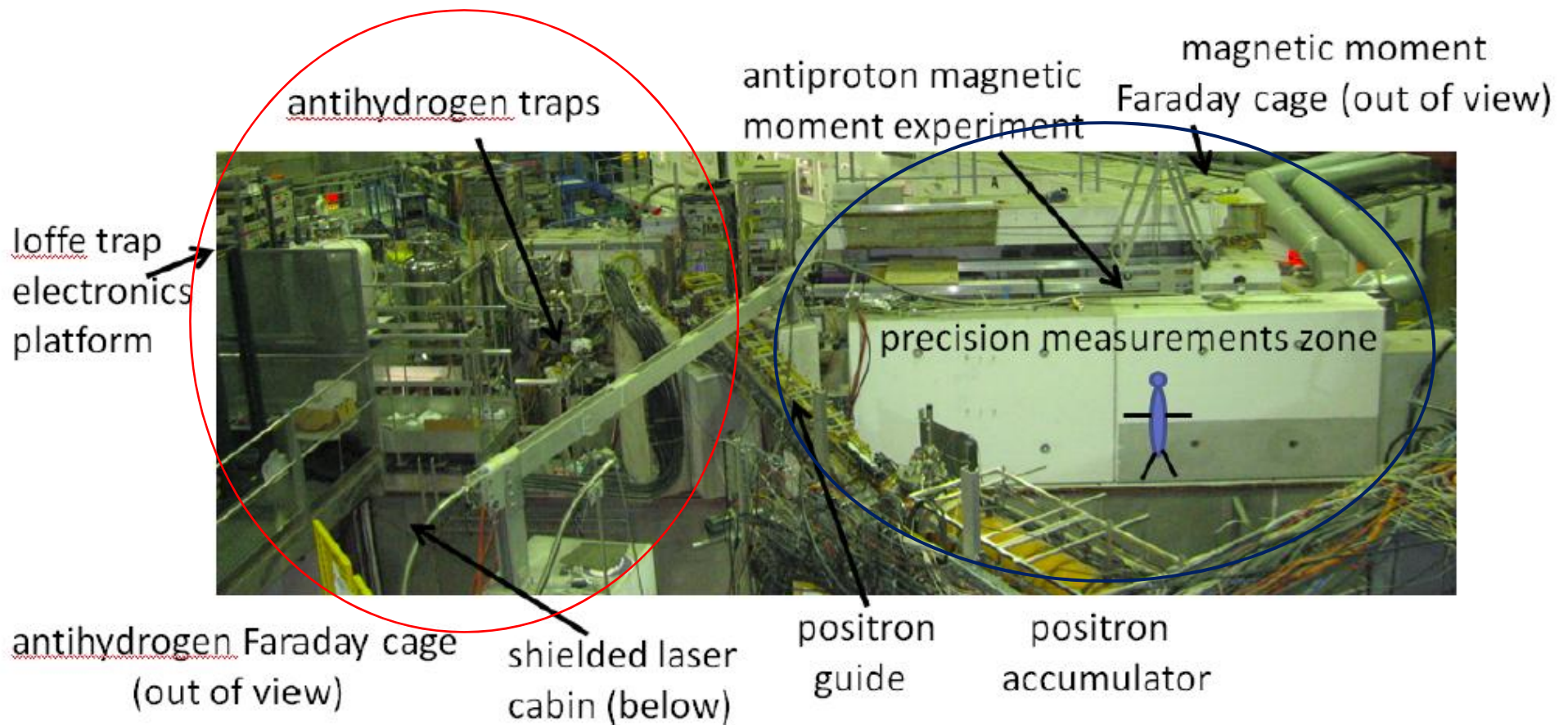
Precision Measurements  
with Antiprotons

Antiprotons  
from AD

trapped antihydrogen in  
its ground state

680-fold improved  
measurement of the  
antiproton magnetic  
motion

# Simultaneous Antihydrogen Experiments and Precision Measurements



ATRAP Experimental Area

# ATRAP Collaboration

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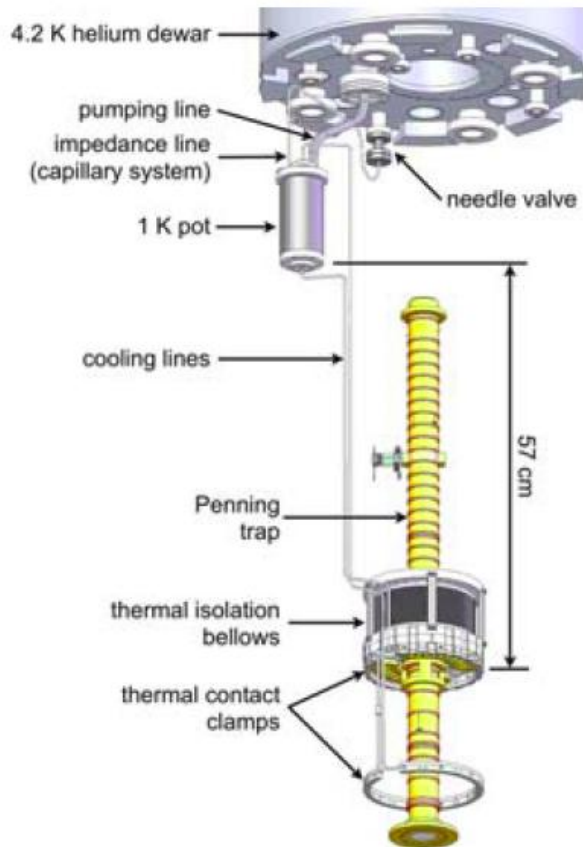
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<sup>2</sup>antihydrogen studies only



# 1.2 K Electrodes and Millions of Antiprotons



1.2 K Using  
Pumped Helium

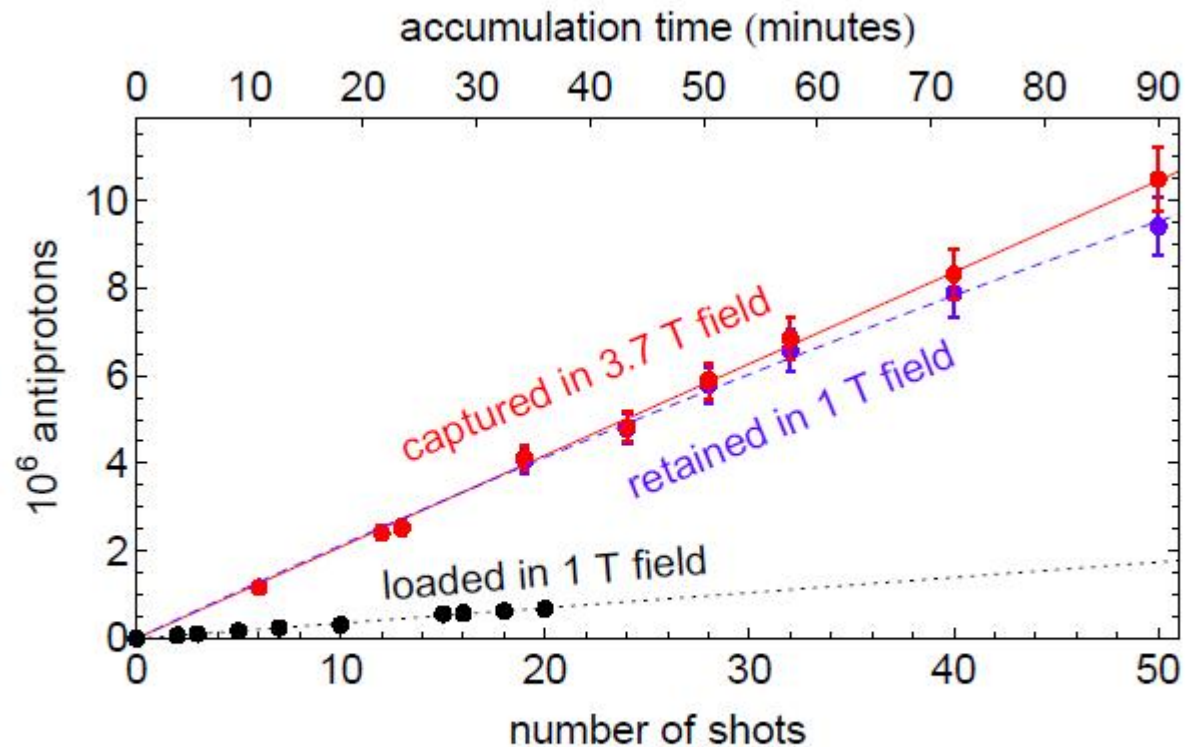


Figure 4: Accumulation of ten million  $\bar{p}$ .

ELENA will make this much faster!

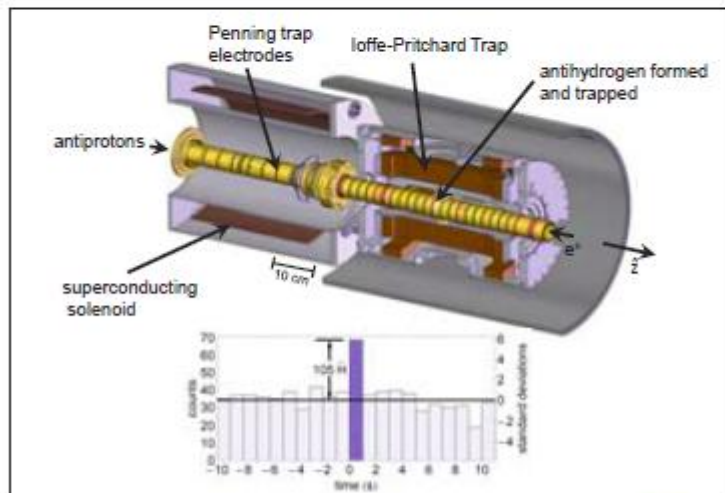


# Trapped Antihydrogen in Its Ground State

## BULLETIN OF THE AMERICAN PHYSICAL SOCIETY

43rd Annual Meeting of the APS  
Division of Atomic, Molecular and Optical Physics

June 4–8, 2012  
Anaheim, California



Used larger antiproton and positron plasmas

- Much more trapped antihydrogen per trial
- still not nearly enough

5 +/- 1 ground state atoms  
simultaneously trapped

ATRAP, “Trapped Antihydrogen in Its Ground State”, Phys. Rev. Lett. **108**, 113002 (2012)

Gabrielse

# Direct Comparison of Antimatter and Matter Gravity

Does antimatter and matter accelerate at the same rate  
in a gravitational field?

$$g_{\text{antimatter}} = | g_{\text{matter}} |$$

acceleration due to gravity  
for antimatter

acceleration due to gravity  
for matter

# The Most Precise Experimental Answer is “Yes” → to at least a precision of 1 part per million

Gravitational red shift for a clock:  $\Delta\check{S} / \check{S} = g h / c^2$

→ Antimatter and matter clocks run at different rates  
if  $g$  is different for antimatter and matter

$$\frac{\Delta\check{S}_c}{\check{S}_c} = 3(| - 1) \frac{U}{c^2}$$

Hughes and Holzschneider,  
Phys. Rev. Lett. 66, 854 (1991).

grav. pot. rnergy difference  
between empty flat space time  
and inside of hypercluster of galaxies

for tensor gravity  
(would be 1 for scalar gravity)

Experiment: TRAP Collaboration, Phys. Rev. Lett. 82, 3198 (1999).

$$\frac{\Delta\check{S}_c}{\check{S}_{\partial c}} < 10^{-10} \quad \text{---} \quad | = 1 \pm (< 10^{-6})$$

Why is this stringent direct comparison never quoted?

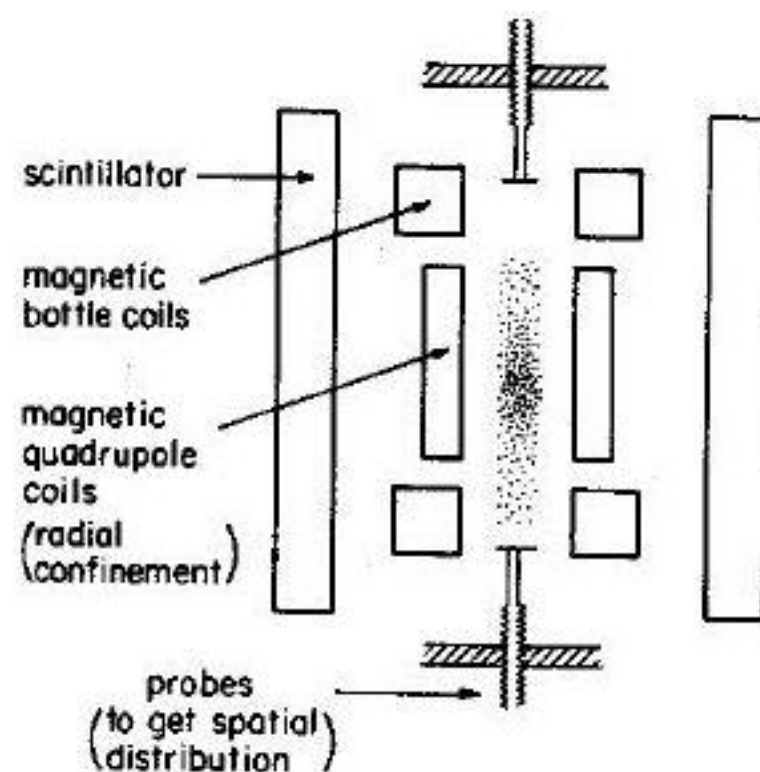
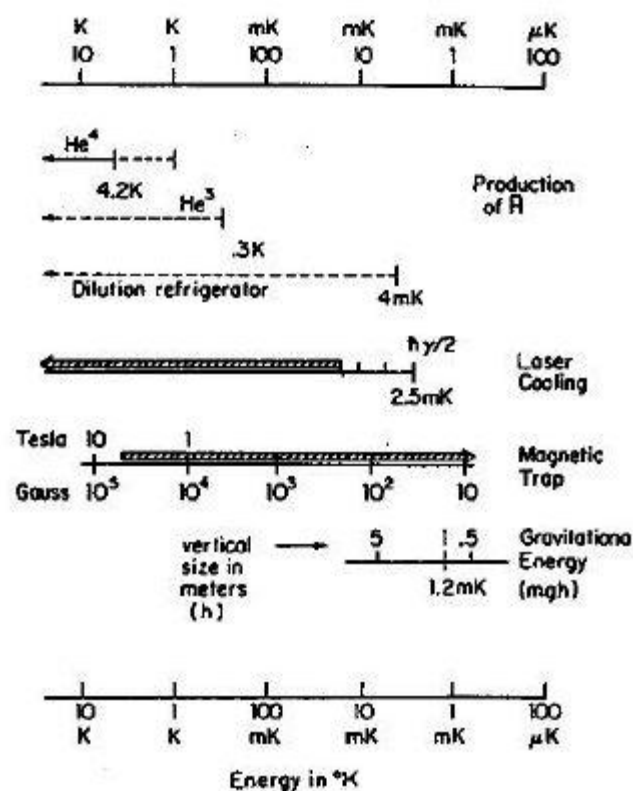
# Gravity and Antihydrogen

Hyperfine Interactions 44 (1988) 349–356

## TRAPPED ANTIHYDROGEN FOR SPECTROSCOPY AND GRAVITATION STUDIES: IS IT POSSIBLE?

G. GABRIELSE

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# Hard to Get the Part per Million Precision of the Redshift Limit with Antihydrogen and Hydrogen

$$g_{\text{antimatter}} = | g_{\text{matter}}$$

Gravitational redshift:  $\frac{\Delta\check{S}_c}{\check{S}_{\partial c}} < 10^{-10} \quad \text{---} > \quad | = 1 \pm (< 10^{-6})$

ATRAP trapped antihydrogen released (2012):

(intended to illustrate that a stringent  
limit was not at all possible so far)

$$| < 200$$

*too optimistic,  
should have released axially*

~~(Assumed radial and axial energy would exchange in  $10^6$  oscillations.)~~

ALPHA trapped antihydrogen released (2013):

$$| < 110$$

Can AEGIS and GBAR get a part per million?

# **Why Compare Matter and Antimatter**





# **Embarrassing, Unsolved Mystery: How did our Matter Universe Survive Cooling After the Big Bang?**



**Big bang → equal amounts of matter and antimatter  
created during hot time**

**As universe cools → antimatter and matter annihilate**

## **Big Questions:**

- How did any matter survive?**
- How is it that we exist?**

**Our experiments are looking for evidence of any way that  
antiparticles and particles may differ**



# Our “Explanations” are Not so Satisfactory



## Baryon-Antibaryon Asymmetry in Universe is Not Understood

### Standard “Explanation”

- CP violation
- Violation of baryon number
- Thermodynamic non-equilibrium

### Alternate

- CPT violation
- Violation of baryon number
- Thermo. equilib.

Bertolami, Colladay, Kostelecky, Potting  
Phys. Lett. B 395, 178 (1997)

**Why did a universe made of matter survive the big bang?**

Makes sense look for answers to such fundamental questions in the few places that we can hope to do so very precisely.



Bigger problem: don't understand dark energy within 120 orders of magnitude



# Why Compare H and $\bar{H}$ (or P and $\bar{P}$ )?

Reality is Invariant – symmetry transformations

~~P~~

parity

~~CP~~

charge conjugation, parity

CPT

charge conjugation, parity, and time reversal

## CPT Symmetry

→ Particles and antiparticles have

- same mass
- same magnetic moment
- opposite charge
- same mean life

→ Atom and anti-atom have

→ same structure

## Looking for Surprises

- simple systems
- extremely high accuracy
- comparisons will be convincing
- reasonable effort
- FUN

# Comparing the CPT Tests

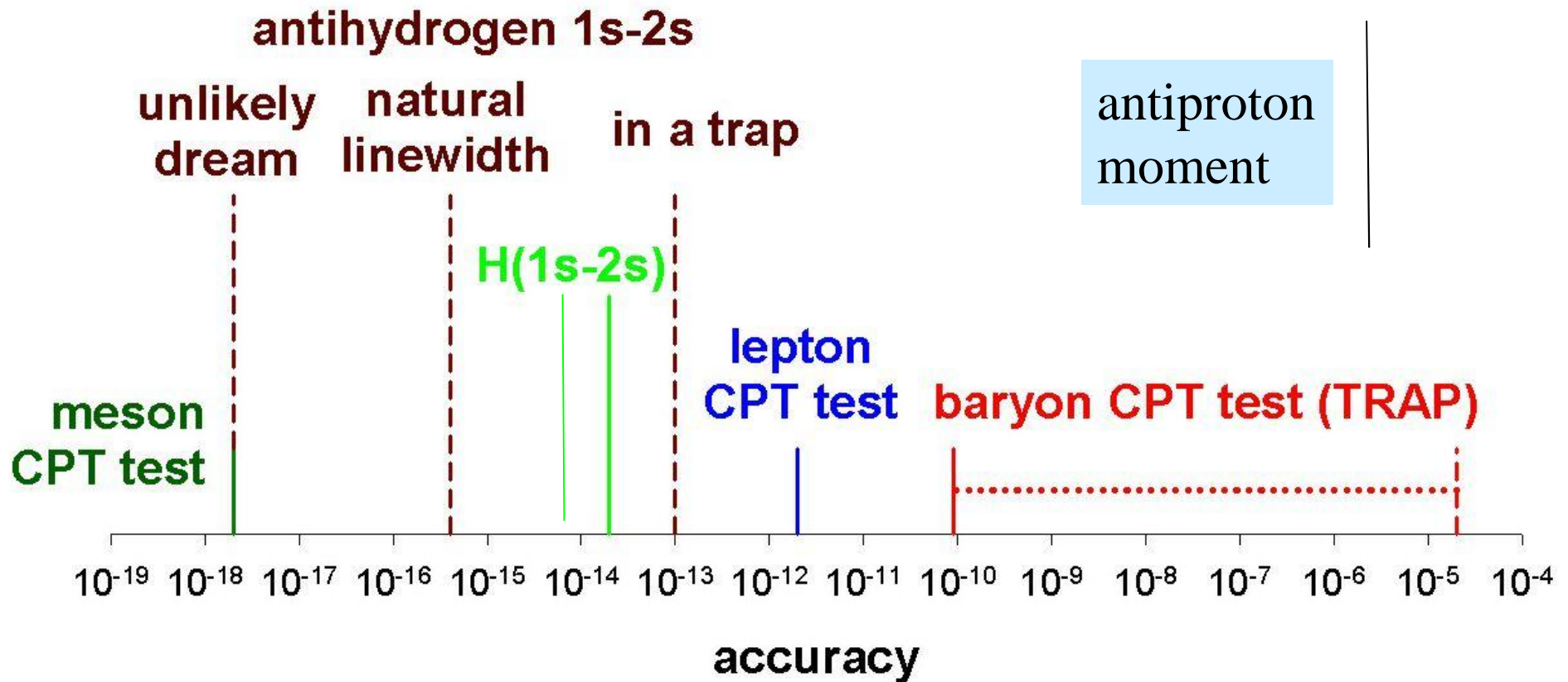
Warning – without CPT violation models it is hard to compare

3 fundamentally different types of particles

	CPT Test	Measurement	Free
	Accuracy	Accuracy	Gift
$K_0 \bar{K}_0$	$2 \times 10^{-18}$	$2 \times 10^{-3}$	$10^{15}$
Mesons			
$e^+ e^-$	$2 \times 10^{-12}$	$2 \times 10^{-9}$	$10^3$
Leptons			
$P \bar{P}$	$9 \times 10^{-11}$	$9 \times 10^{-11}$	1
baryons			

improve with antihydrogen

# Seek to Improve **Lepton** and **Baryon** CPT Tests



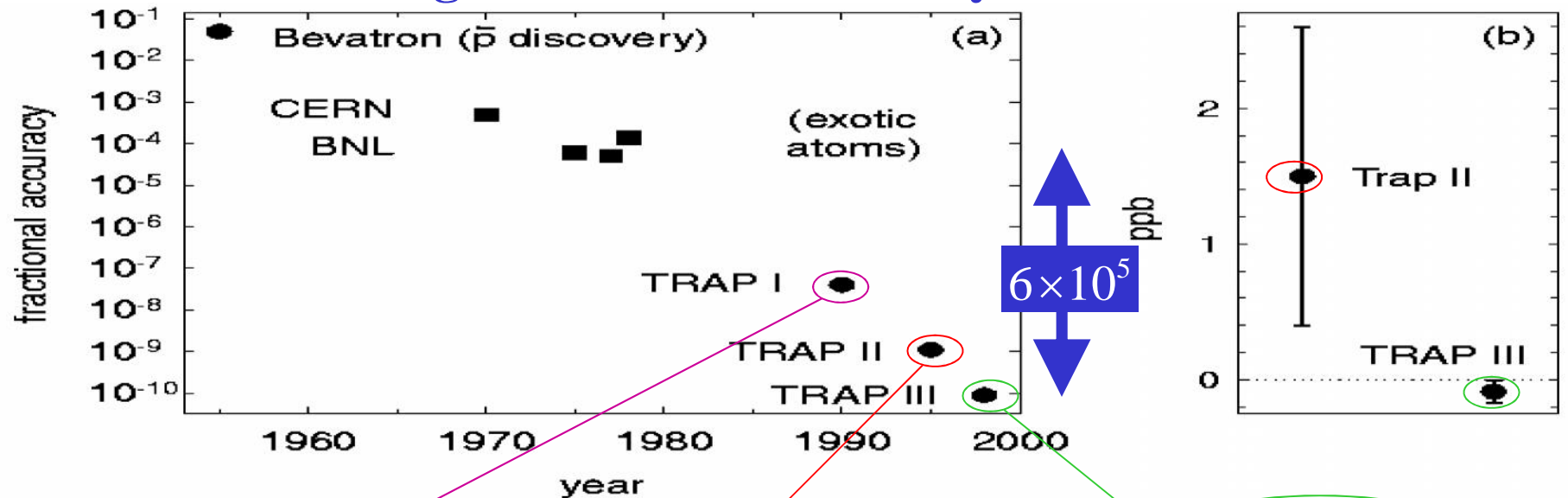
$$\frac{R_{\infty}[\bar{\text{H}}]}{R_{\infty}[\text{H}]} = \frac{m[e^+]}{m[e^-]} \left( \frac{q[e^+]}{q[e^-]} \right)^2 \left( \frac{q[\bar{p}]}{q[p]} \right)^2 \frac{1 + m[e^-]/M[p]}{1 + m[e^+]/M[\bar{p}]}$$

# We Improved the Comparison of Antiproton and Proton by $\sim 10^6$

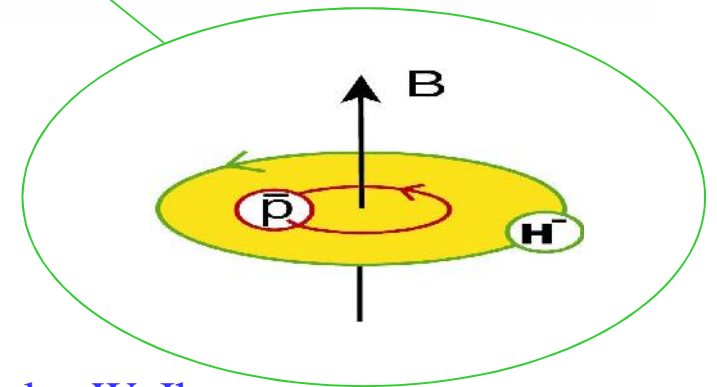
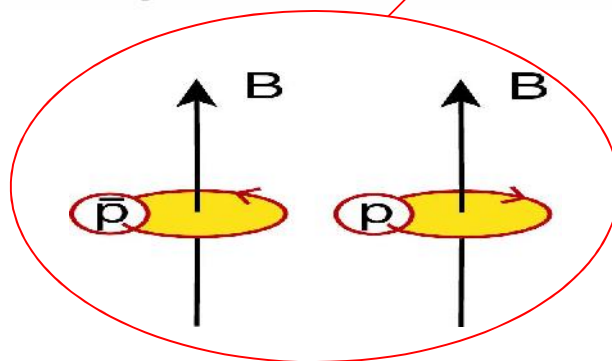
$$\frac{q/m \text{ (antiproton)}}{q/m \text{ (proton)}} = -0.99999999991(9)$$

$$9 \times 10^{-11} = 90 \text{ ppt}$$

most stringent CPT test with baryons

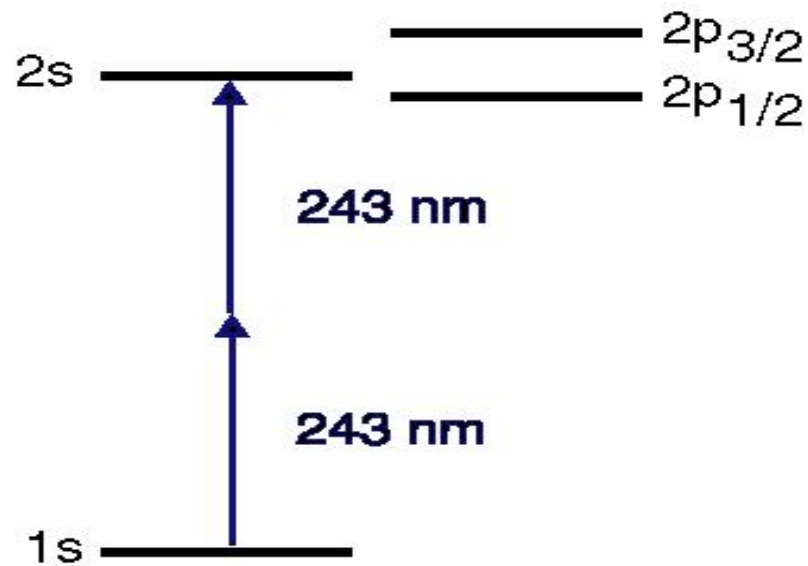


100  
antiprotons  
and protons

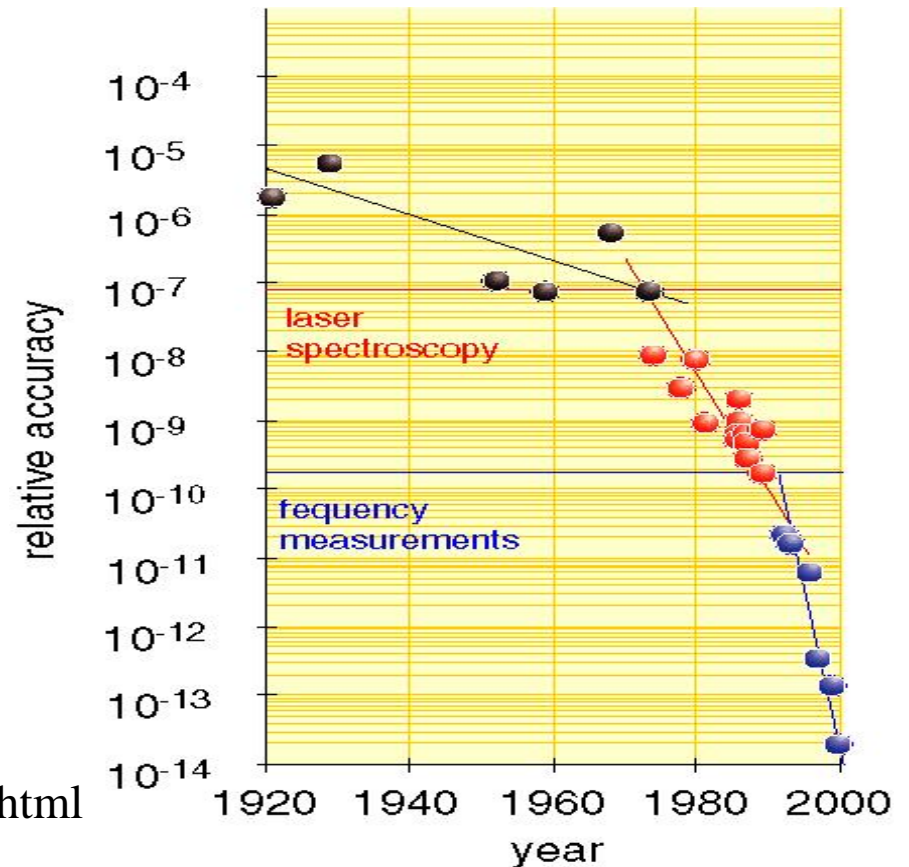


G. Gabrielse, A. Khabbaz, D.S. Hall, C. Heimann, H. Kalinowsky, W. Jhe;  
Phys. Rev. Lett. **82**, 3198 (1999).

# Ultimate Goal: Hydrogen 1s – 2s Spectroscopy



(Haensch, et al., Max Planck Soc., Garching)  
<http://www.mpg.de/~haensch/hydrogen/h.html>



Many fewer antihydrogen atoms will be available



Gabrielse

# CPT for Antiprotons and Antihydrogen

## Compare Antiproton and Proton

$q/m$

TRAP (direct)

$q$  and  $m$  separately

TRAP + ASACUSA  
(indirect, not nearly as precise)

$\mu$

ATRAP

## Compare antihydrogen and hydrogen structure

Despite all the publicity → no interesting comparisons of antihydrogen and hydrogen have yet been possible

# Highest Precision Test of Baryon CPT Invariance

→ by TRAP at CERN



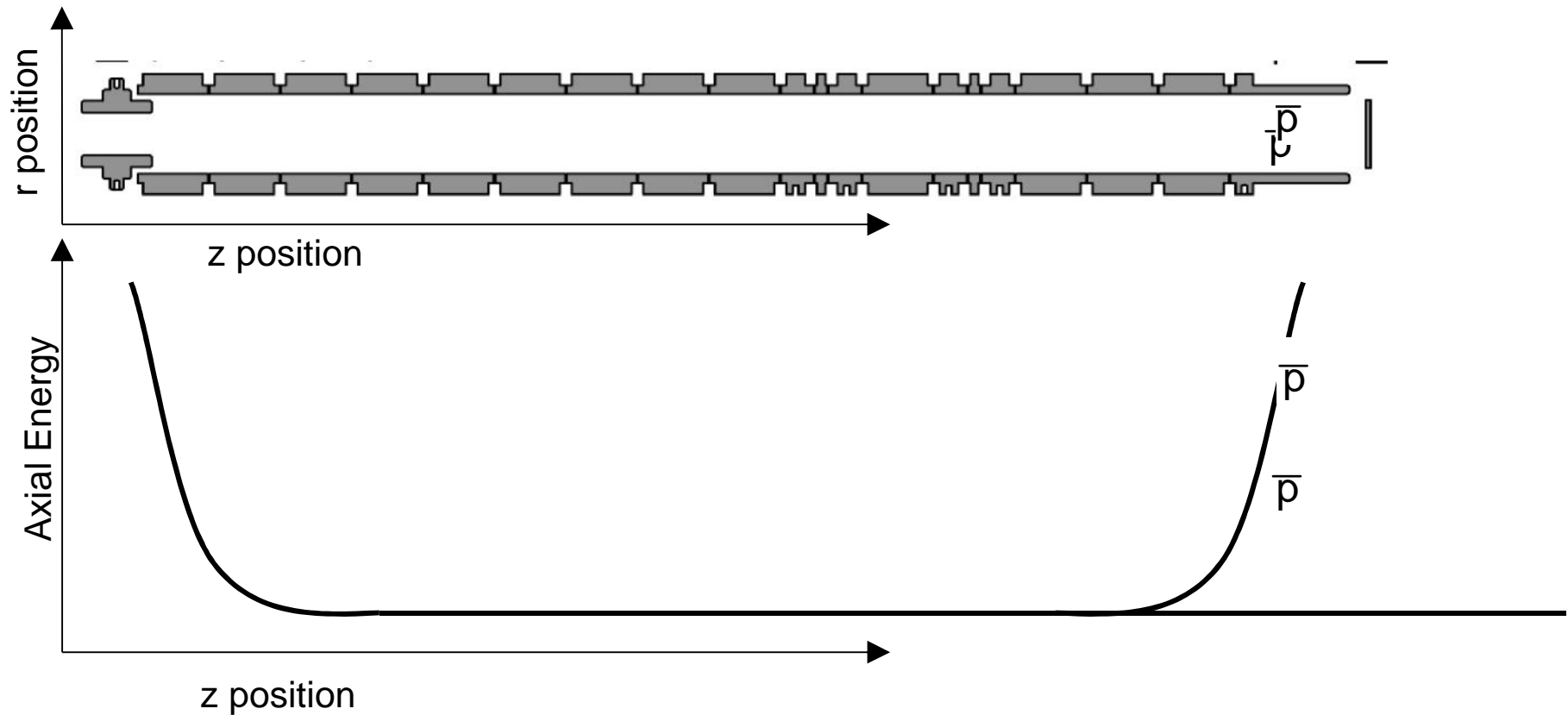
G. Gabrielse, A. Khabbaz, D. S. Hall, C. Heimann, H. Kalinowsky, and W. Jhe, Phys. Rev. Lett. **82**, 3198 (1999).

$$\frac{q/m \text{ (antiproton)}}{q/m \text{ (proton)}} = -0.999\,999\,999\,91(9) \quad 9 \times 10^{-11} = 90 \text{ ppt}$$

(most precise result of CERN's antiproton program)

Goal at the AD: Make CPT test that approach  
exceed this precision

# Antiproton Capture – the Movie



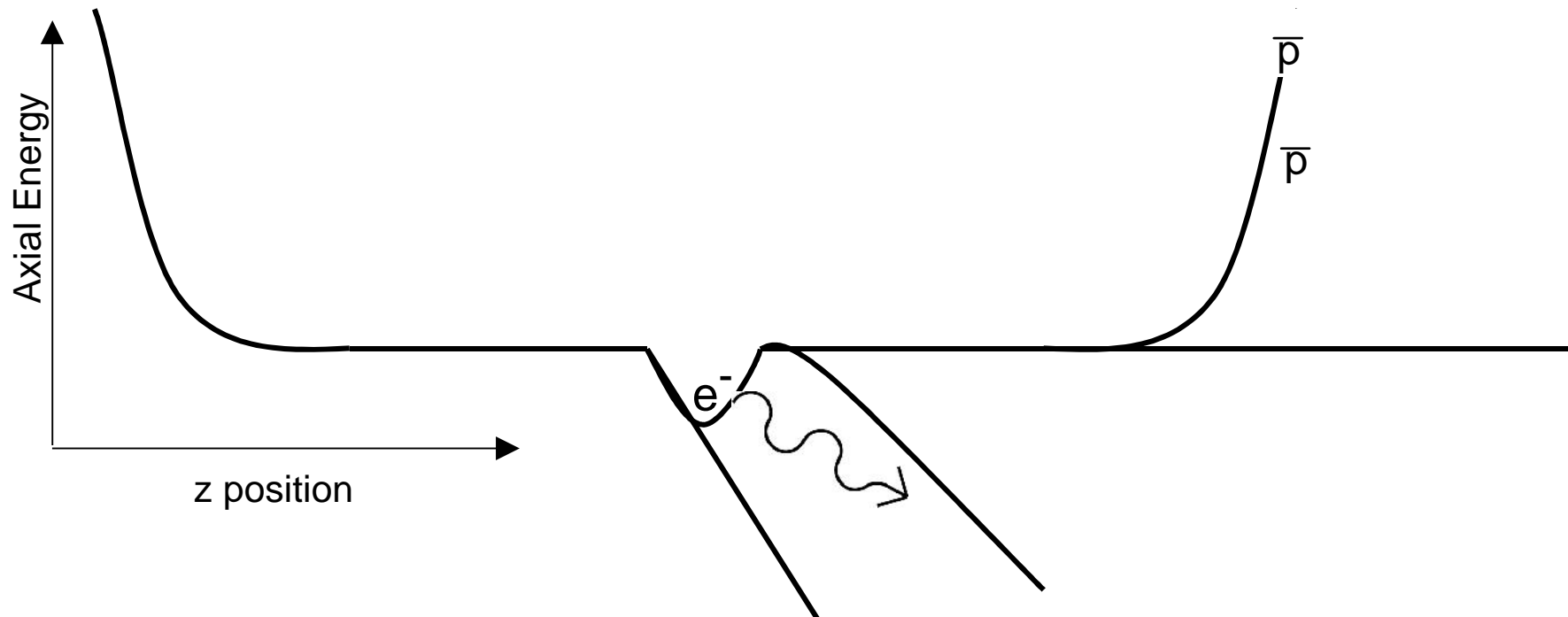
**"First Capture of Antiprotons in a Penning Trap: A KeV Source",**

G. Gabrielse, X. Fei, K. Helmerson, S.L. Rolston, R. Tjoelker, T.A. Trainor, H. Kalinowsky,  
J. Haas, and W. Kells;

Phys. Rev. Lett. 57, 2504 (1986).

# Electron-Cooling of Antiprotons – in a Trap

- Antiprotons cool via collisions with electrons
- Electrons radiate away excess energy



**"Cooling and Slowing of Trapped Antiprotons Below 100 meV",**  
G. Gabrielse, X. Fei, L.A. Orozco, R. Tjoelker, J. Haas, H. Kalinowsky, T.A. Trainor, W. Kells;  
*Phys. Rev. Lett.* 63, 1360 (1989).

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**ATRAP's Principle Focus in 2012**  
**→ First Direct Comparison of the**  
**Antiproton and Proton Magnetic Moments**



# **Magnetic Moments**

## **Can be Measured Very Precisely**

e.g. Electron magnetic moment is the most precisely measured property of an elementary particle

# Electron Magnetic Moment

electron  
magnetic  
moment

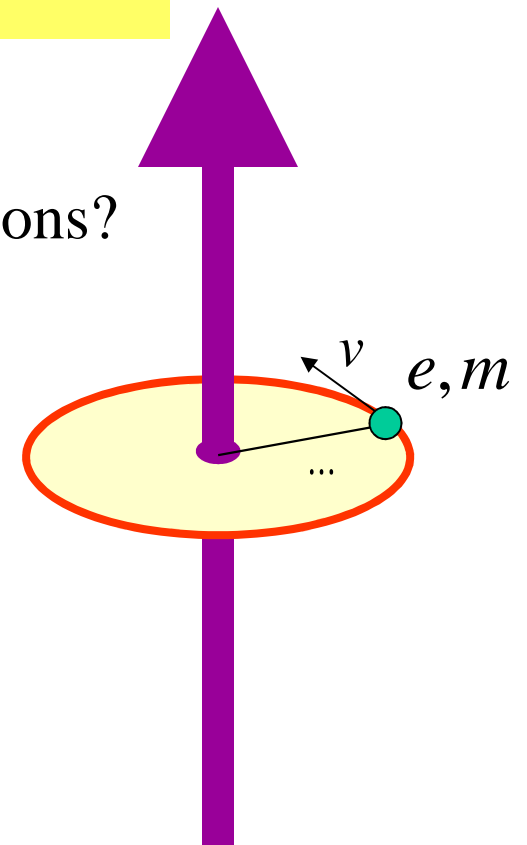
$$\vec{\mu} = -g \underbrace{\mu_B}_{\text{Bohr magneton } \frac{e\hbar}{2m}} \frac{\vec{L}}{\hbar} \quad \leftarrow \text{angular momentum}$$

e.g. What is  $g$  for identical charge and mass distributions?

$$\mu = IA = \frac{-e}{\left(\frac{2f \dots}{v}\right)} (f \dots)^2 = -\frac{ev \dots}{2} \frac{L}{mv \dots} = -\frac{e}{2m} L = -\frac{e\hbar}{2m} \frac{L}{\hbar}$$

$$\Rightarrow g = 1$$

$\uparrow$   
 $\mu_B$



# Electron Magnetic Moment

$$\text{magnetic moment } \vec{\mu} = -\frac{g}{2} \mu_B \frac{\vec{S}}{\hbar/2}$$

← angular momentum

↑ Bohr magneton  $\frac{e\hbar}{2m}$

$g/2$  = magnetic moment in Bohr magnetons for spin 1/2

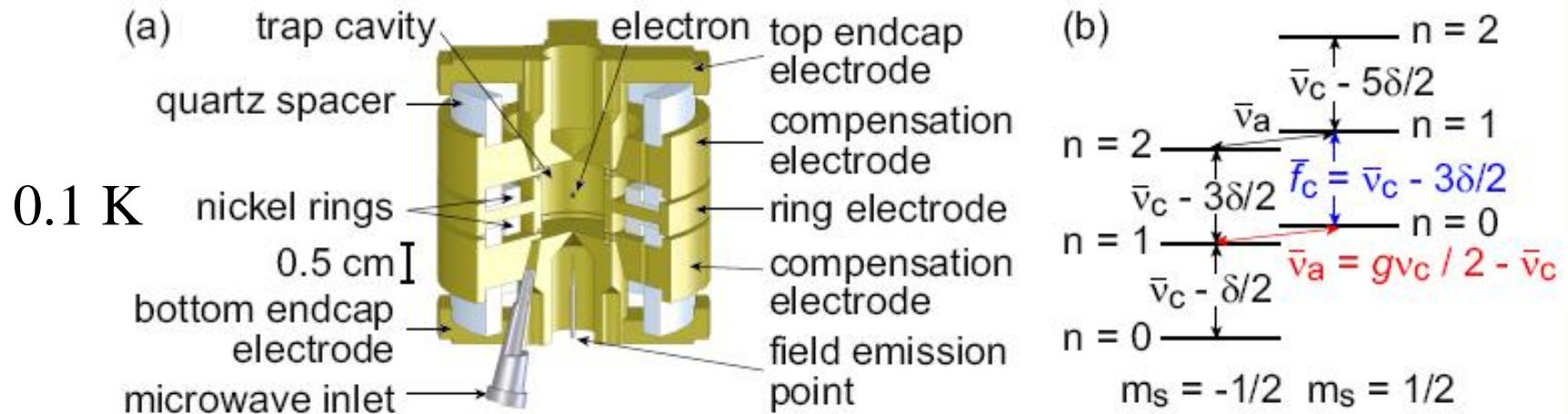
$g = 1$     mechanical model with identical charge  
and mass distribution

$g = 2$     spin for simple Dirac point particle

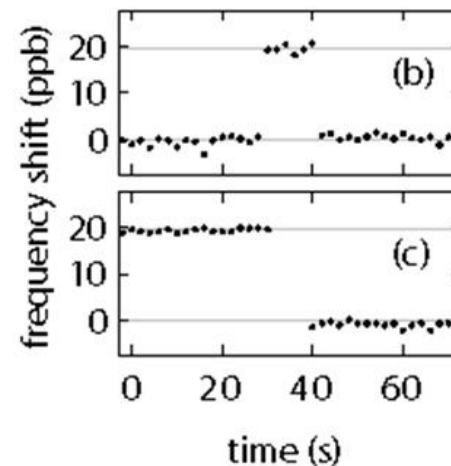
$g = 2.002\,319\,304 \dots$     simplest Dirac spin, plus QED

(if electron  $g$  is different  $\rightarrow$  electron has substructure)

## One Electron: Resolve One-Quantum Excitation



# QND observations of one-quantum transitions



one quantum  
cyclotron  
excitation

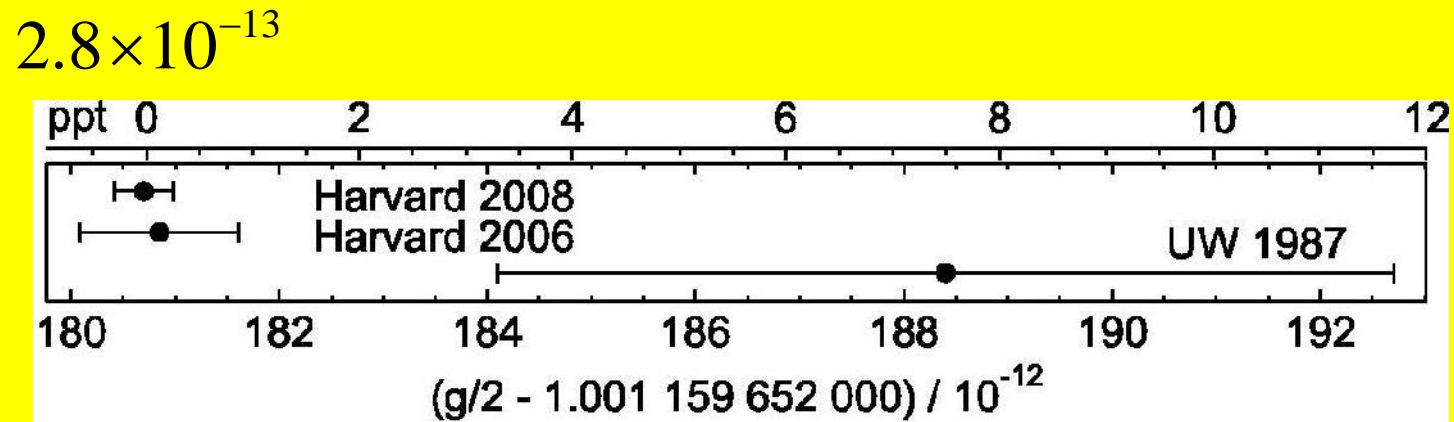
spin flip

"Single-Particle Self-excited Oscillator",  
B. D'Urso, R. Van Handel, B. Odom and G. Gabrielse  
Phys. Rev. Lett. **94**, 113002 (2005).

Most precisely measured property of an elementary particle

Gabrielse

## Electron Magnetic Moment Measured to $3 \times 10^{-13}$



(improved measurement is currently underway)

electron magnetic moment in Bohr magnetons

trying to do as well with a as with an electron

["New Measurement of the Electron Magnetic Moment and the Fine Structure Constant"](#)

D. Hanneke, S. Fogwell and G. Gabrielse,

Phys. Rev. Lett. **100**, 120801 (2008) and arXiv:0801.1134v1 [physics.atom-ph].

["Cavity Control of a Single-Electron Quantum Cyclotron: Measuring the Electron Magnetic Moment"](#)

D. Hanneke, S. Fogwell Hoogerheide and G. Gabrielse,

Phys. Rev. A **83**, 052122 (2011).

# Standard Model → Relates $g/2$ and $\alpha$

$$\frac{g}{2} = 1 + C_2 \left( \frac{\alpha}{\pi} \right) + C_4 \left( \frac{\alpha}{\pi} \right)^2 + C_6 \left( \frac{\alpha}{\pi} \right)^3 + C_8 \left( \frac{\alpha}{\pi} \right)^4 \\ + C_{10} \left( \frac{\alpha}{\pi} \right)^5 + \dots + a_{\text{hadronic}} + a_{\text{weak}}$$

$$C_2 = 0.500\,000\,000\,000\,00 \text{ (exact)}$$

$$C_4 = -0.328\,478\,444\,002\,55 \text{ (33)}$$

$$C_6 = 1.181\,234\,016\,815 \text{ (11)}$$

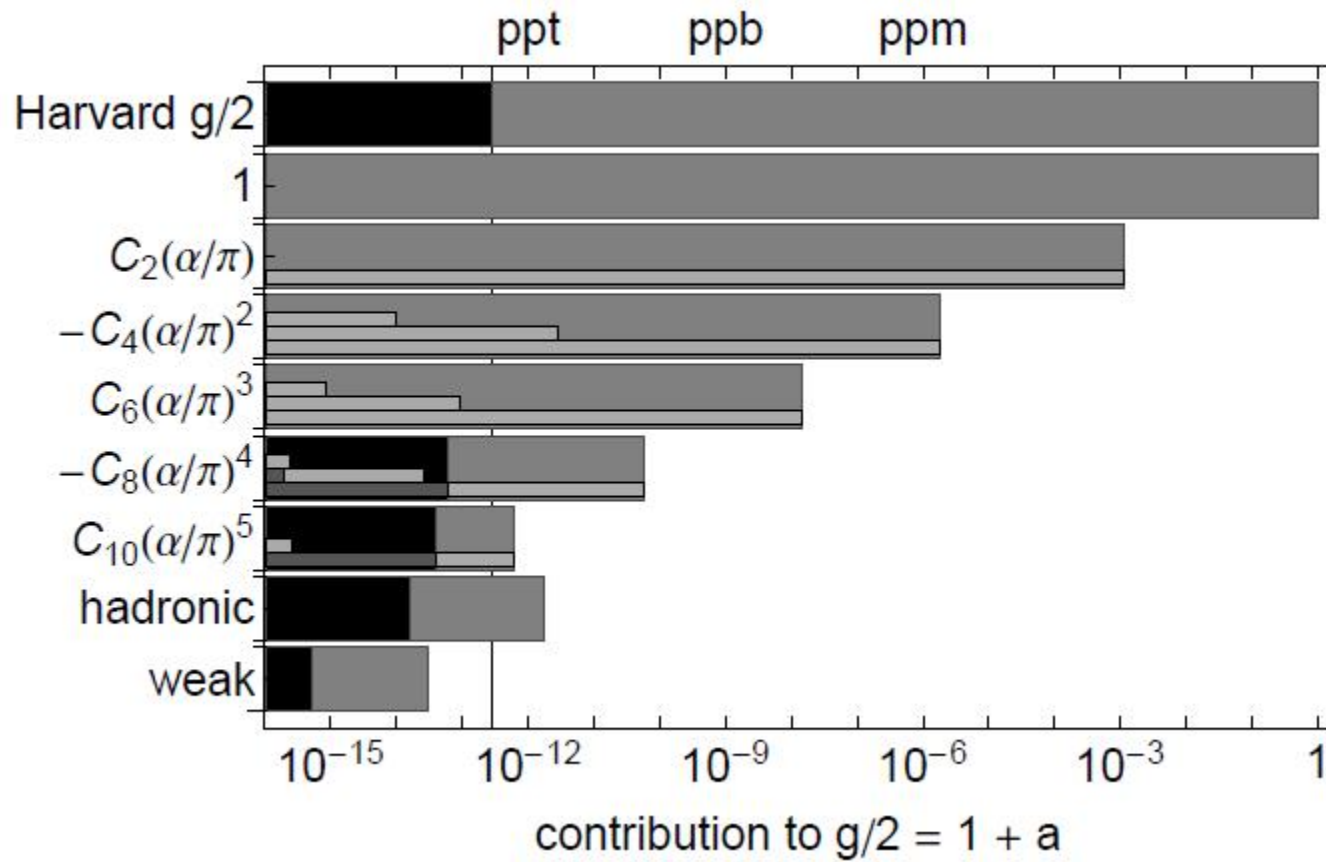
$$C_8 = -1.909\,7 \text{ (20)}$$

$$C_{10} = 9.16 \text{ (0.57)}.$$

Essentially exact  
-- depend weakly on  
mass ratios

$$a_e^{\text{hadronic}} = 1.677(16) \times 10^{-12}$$

# Standard Model Contributions



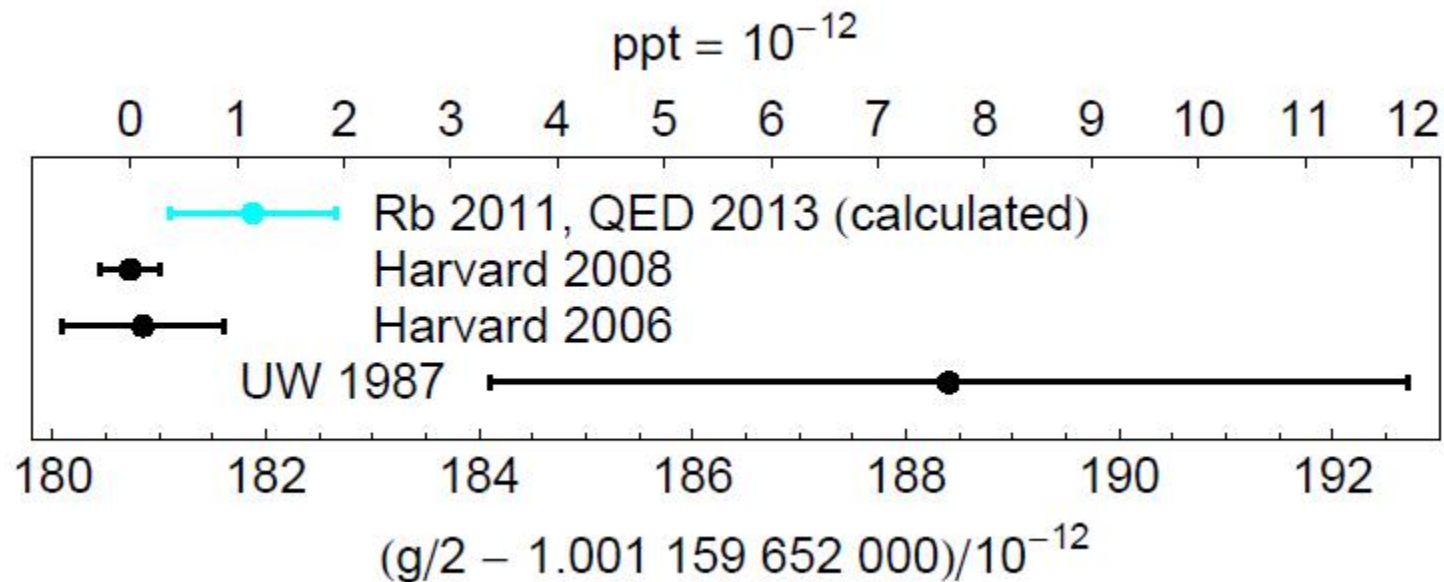


# (Greatest?) Triumph of the Standard Model

Measured:  $\mu/\mu_B = -g/2 = -1.001\,159\,652\,180\,73(28)$  [0.28 ppt].

“Calculated”:  $\mu/\mu_B = -g/2 = -1.001\,159\,652\,181\,88(78)$  [0.77 ppt]

(Uncertainty from measured fine structure constant)



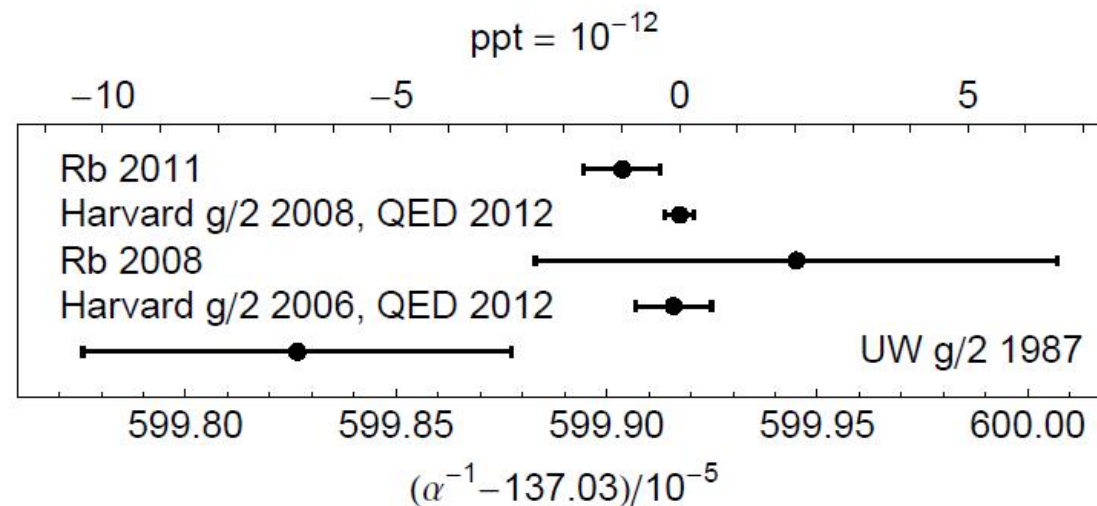
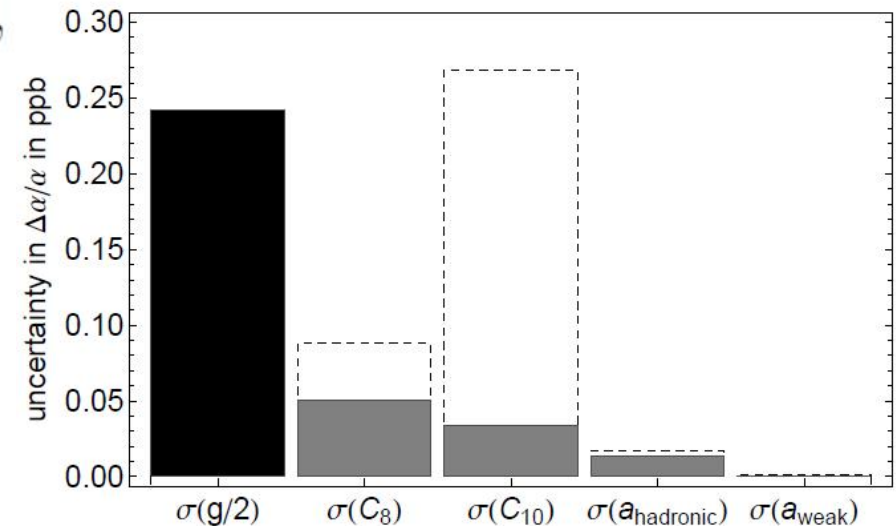
$$\frac{\mu - \mu(SM)}{\mu} = 0.000\,000\,000\,000\,15(82) [0.82 \text{ ppt}],$$

$$= 1.5(0.8) \times 10^{-12} [0.8 \text{ ppt}].$$

# Determine Fine Structure Constant

$$\alpha^{-1} = 137.035999173(33)(8) [0.24 \text{ ppb}] [0.06 \text{ ppb}]$$

$$= 137.035999173(34) [0.25 \text{ ppb}],$$



# Proton and Antiproton Magnetic Moments are Much Smaller

Harder: nuclear magneton rather than Bohr magneton

$$\mu_N/\mu_B = m_e/m_p \sim 1/2000$$

# Precise Proton Magnetic Moment Measurement

- Most precise so far (0.01 ppm)
- Cannot be Used with Antiprotons

$$\frac{\mu_p}{\mu_N} \equiv \frac{g_p}{2} = \frac{\mu_e}{\mu_B} \frac{m_p}{m_e} \frac{\mu_p(H)}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{\mu_p}{\mu_p(H)}$$

free electron  
magnetic  
moment

Harvard

0.0003 ppb

theory corrections  
1 ppb

10 ppb

hydrogen  
maser

MIT

2 ppb or 0.7 ppb

UW

direct

bound electron  
magnetic  
moment

Mainz

ppb =  $10^{-9}$

## **Exotic Atom Measurements**

- Very low precision (3000 ppm)**
- Works only with an antiproton**

# **Single Particle Measurements Have Three Big Advantages**

Can be done with antiparticles

Can reach a much higher precision

Direct measurement → same measurement and apparatus  
is used with a particle and antiparticle

# Antiproton Magnetic Moment

$$\boldsymbol{\mu}_{\bar{p}} = \mu_{\bar{p}} \mathbf{S} / (\hbar/2)$$

Single particle method: Measure two frequencies

current  
challenge

$$\frac{\mu_{\bar{p}}}{\mu_N} \equiv \frac{g_{\bar{p}}}{2} \frac{q_{\bar{p}}/m_{\bar{p}}}{q_p/m_p} \approx -\frac{g_{\bar{p}}}{2} = -\frac{f_s}{f_c}$$

nuclear magneton

-1

we measured to be  
to 9 parts in  $10^{11}$

we measured  
to  $< 9 \times 10^{-11}$

# Phys. Rev. Lett. 180, 153001 (2012)

## Direct Measurement of the Proton Magnetic Moment

J. DiSciacca<sup>1</sup> and G. Gabrielse<sup>1, \*</sup>

<sup>1</sup>*Dept. of Physics, Harvard University, Cambridge, MA 02138*

(Dated: January 14, 2012)

The proton magnetic moment in nuclear magnetons is measured to be  $\mu_p/\mu_N \equiv g/2 = 2.792\,846 \pm 0.000\,007$ , a 2.5 ppm (parts per million) uncertainty. The direct determination, using a single proton in a Penning trap, demonstrates the first method that should work as well with an antiproton ( $\bar{p}$ ) as with a proton (p). This opens the way to measuring the  $\bar{p}$  magnetic moment (whose uncertainty has essentially not been reduced for 20 years) at least  $10^3$  times more precisely.

## Earlier contributions

[12] N. Guise, J. DiSciacca, and G. Gabrielse, Phys. Rev. Lett. **104**, 143001 (2010).

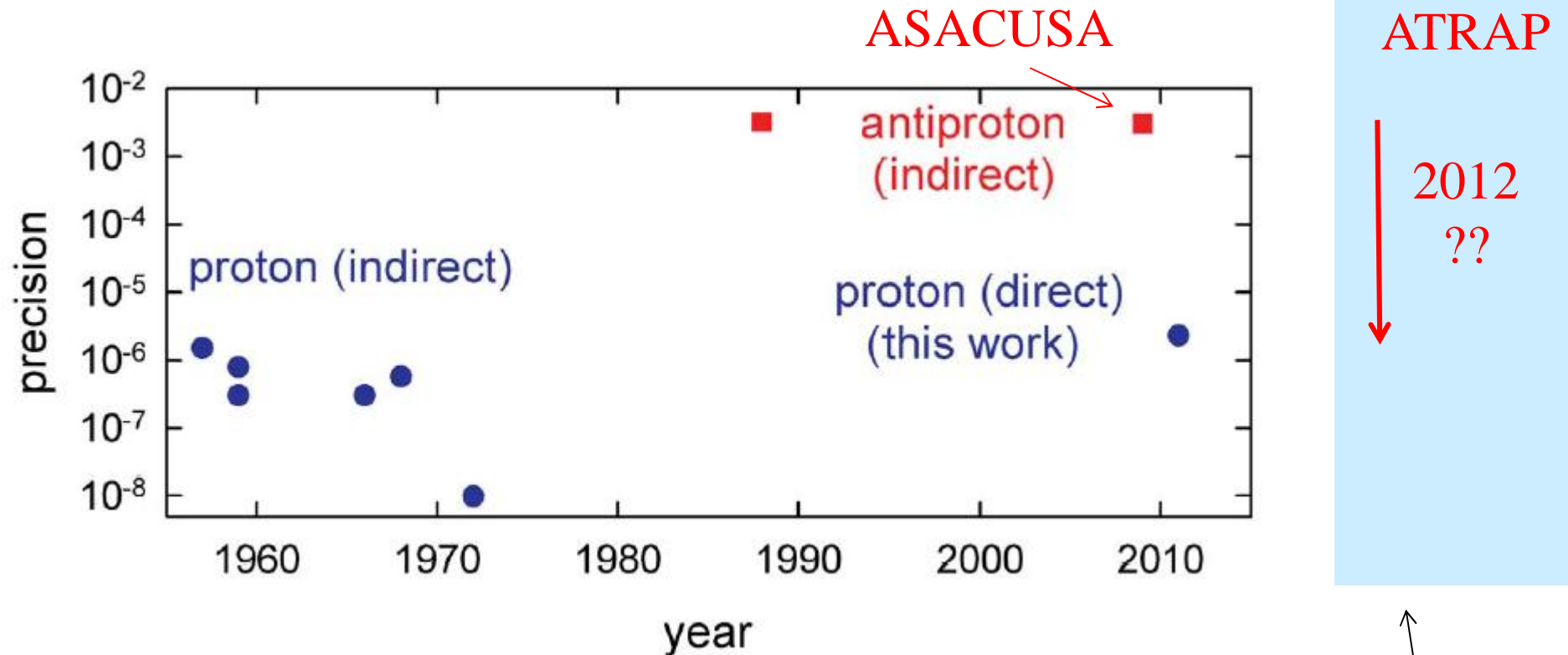
[14] S. Ulmer, C. C. Rodegheri, K. Blaum, H. Kracke, A. Mooser, W. Quint, and J. Walz, Phys. Rev. Lett. **106**, 253001 (2011).

## Later measurement with similar methods

C. C. Rodegheri, K. Blaum, H. Kracke, S. Kreim, A. Mooser, W. Quint, S. Ulmer, and J. Walz, New J. Physics **14**, 063011 (2012).



# Suggested Possibility of a Thousand-fold Improved Measurement of the Antiproton Moment



If everything went exactly right it would be possible to do this with antiprotons in 2012

Expect to eventually be more precise than all proton measurements

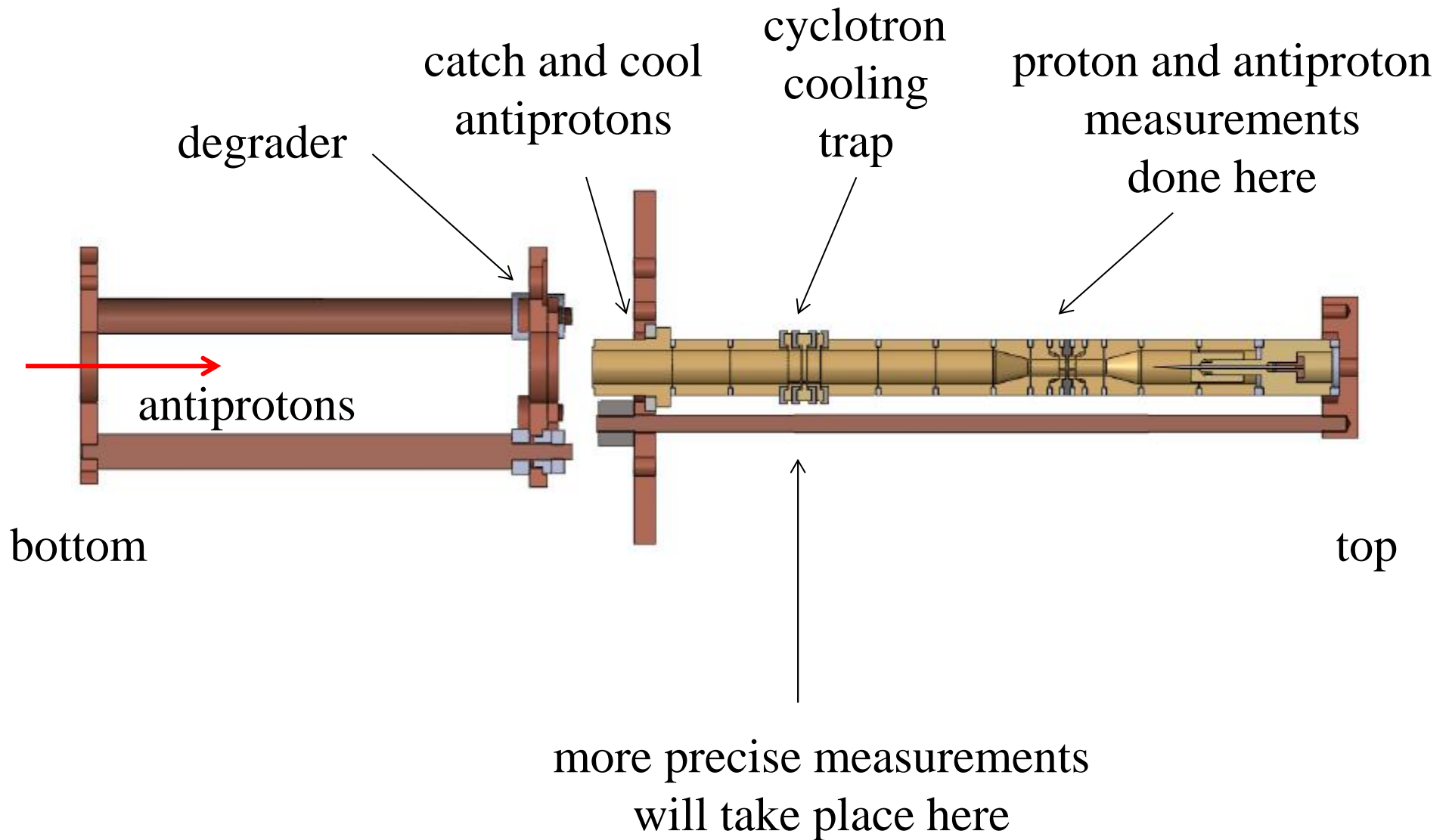
## **Could We Adapt the Apparatus, Move to CERN, and Make the -- all in 2012?**

Decided to take the risk:

- even if we failed, we would learn what to work on over the long shutdown
- we were not anticipating any major scientific accomplishments at the ATRAP or the AD in 2012
- perhaps we could succeed

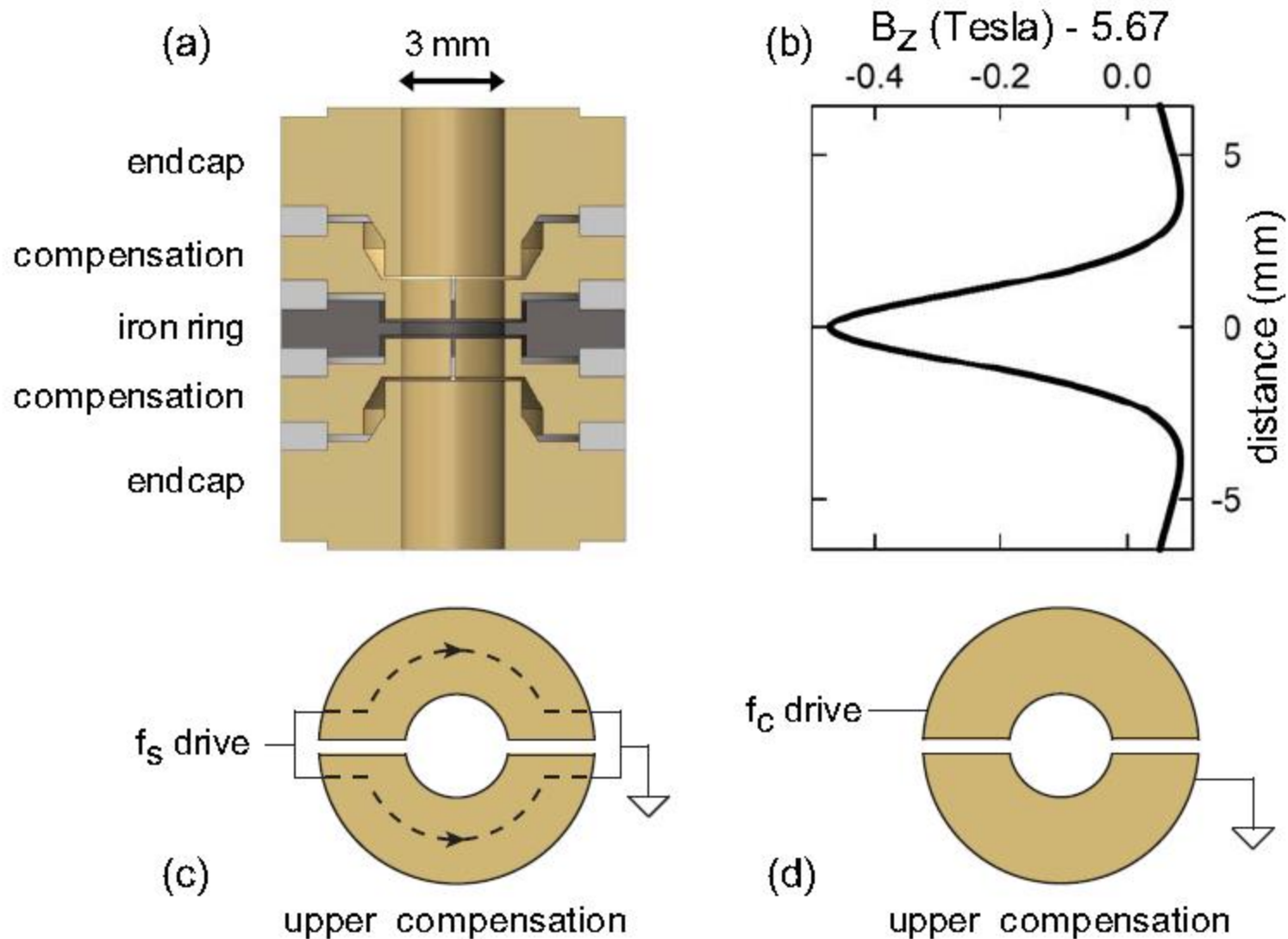
# Antiproton Magnetic Moment Apparatus

# For Magnetic Moments: Three Antiproton Traps



# Huge Magnetic Bottle Gradient

190 times larger than used for electron



# One-Particle Method

With one proton or antiproton suspended in a trap,  
measure spin and cyclotron frequencies

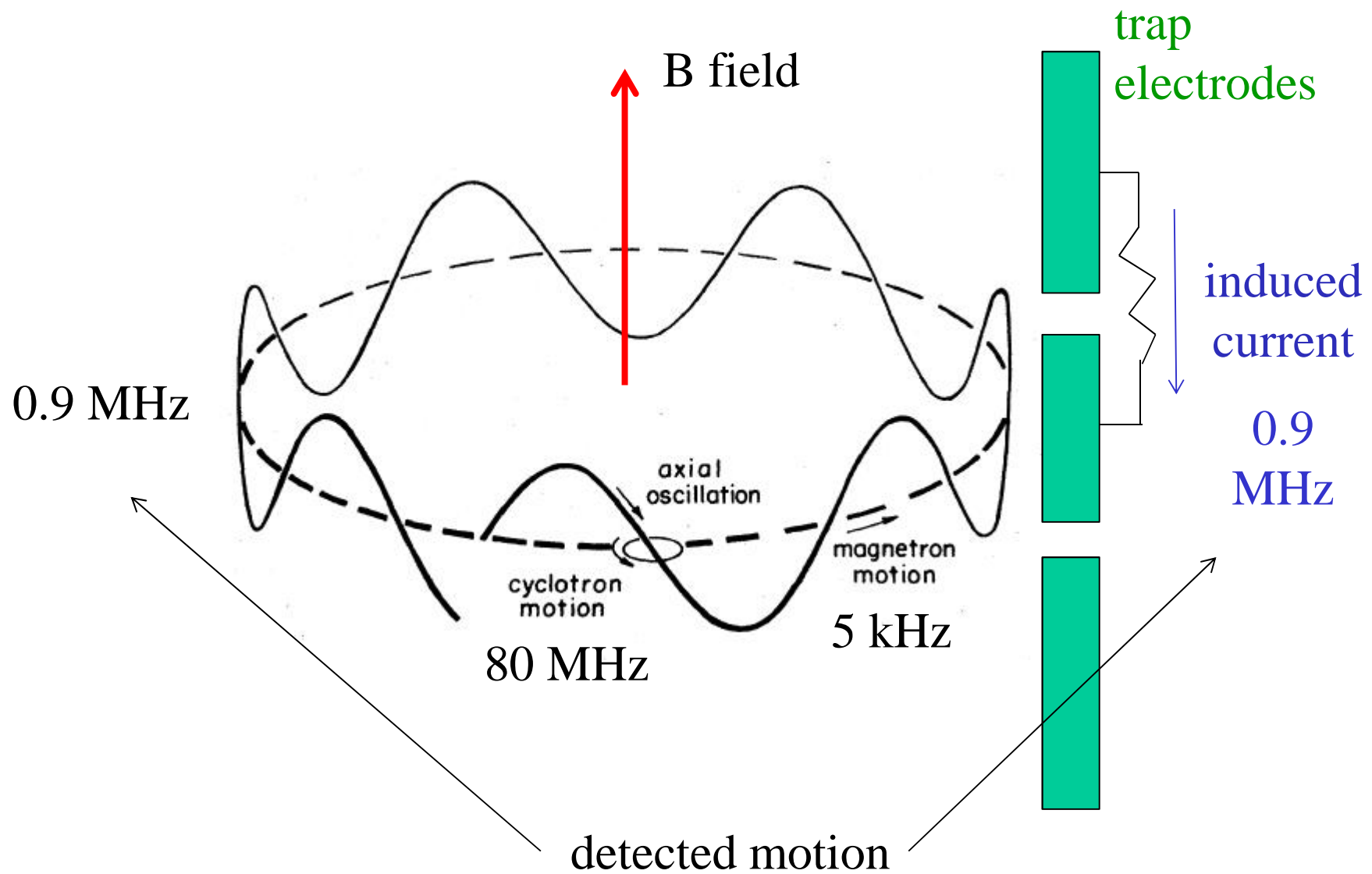
$$\frac{\mu_p}{\mu_N} \equiv \frac{g_p}{2} = \frac{f_s}{f_c}$$

current challenge

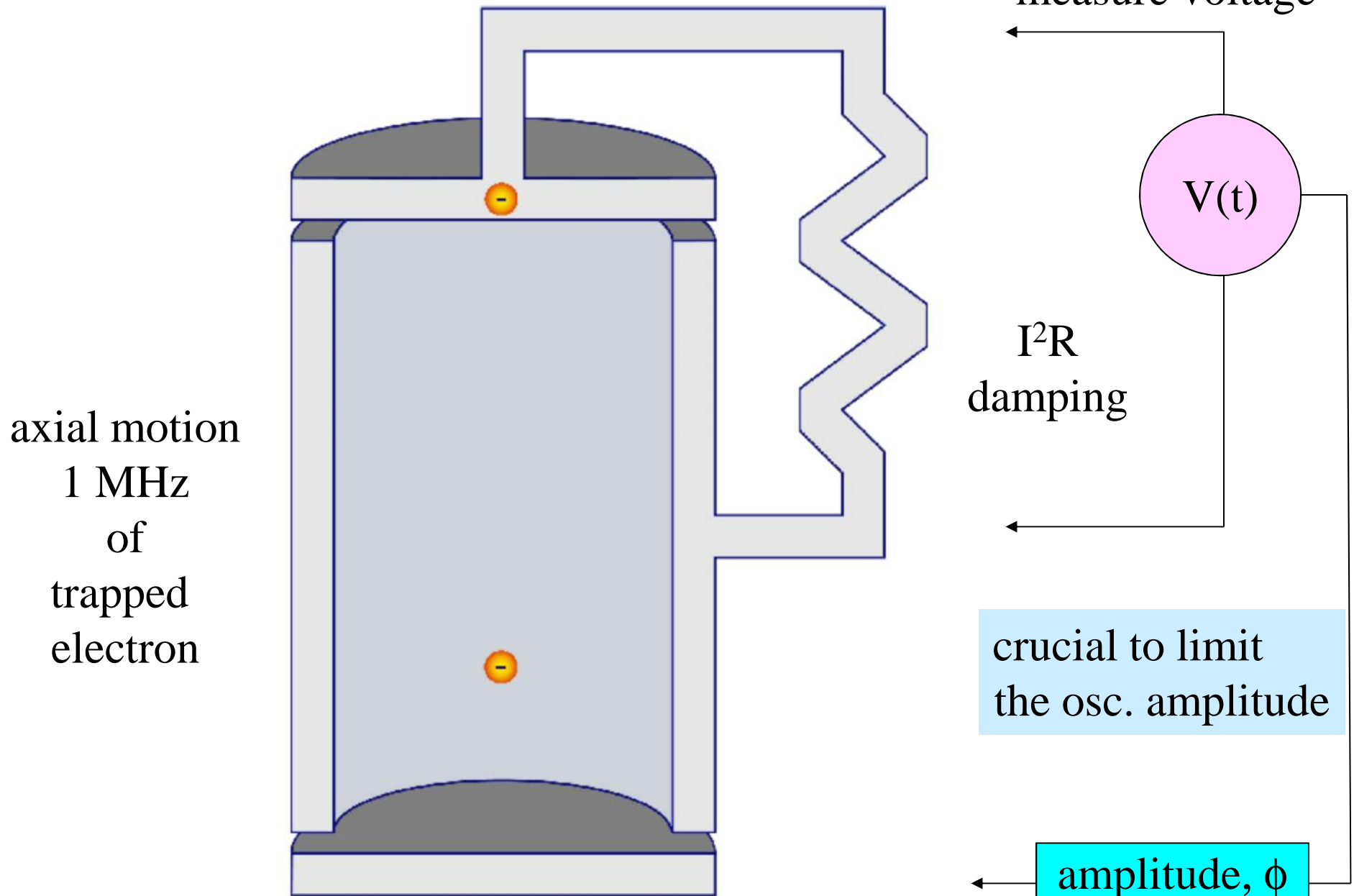
we measured to  
< 9 x 10<sup>-11</sup>  
back at LEAR

no previous method has been devised to measure  
antiproton and proton moments in the same way

# Antiproton Orbits in a Penning Trap

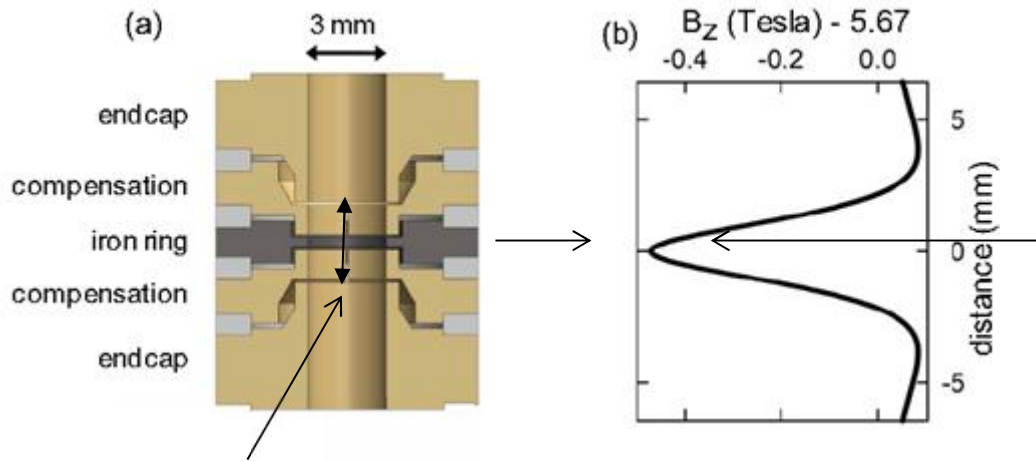


## What We Directly Detect (SEO)





# Detecting the Antiproton Magnetic Moment



$$\Delta \mathbf{B} = \beta_2 [(z^2 - \rho^2/2)\hat{\mathbf{z}} - z\rho\hat{\boldsymbol{\rho}}]$$

magnetic moment

$$\Delta H \sim -\mu \Delta B \sim \mu z^2$$

$$\Delta f \sim \mu$$

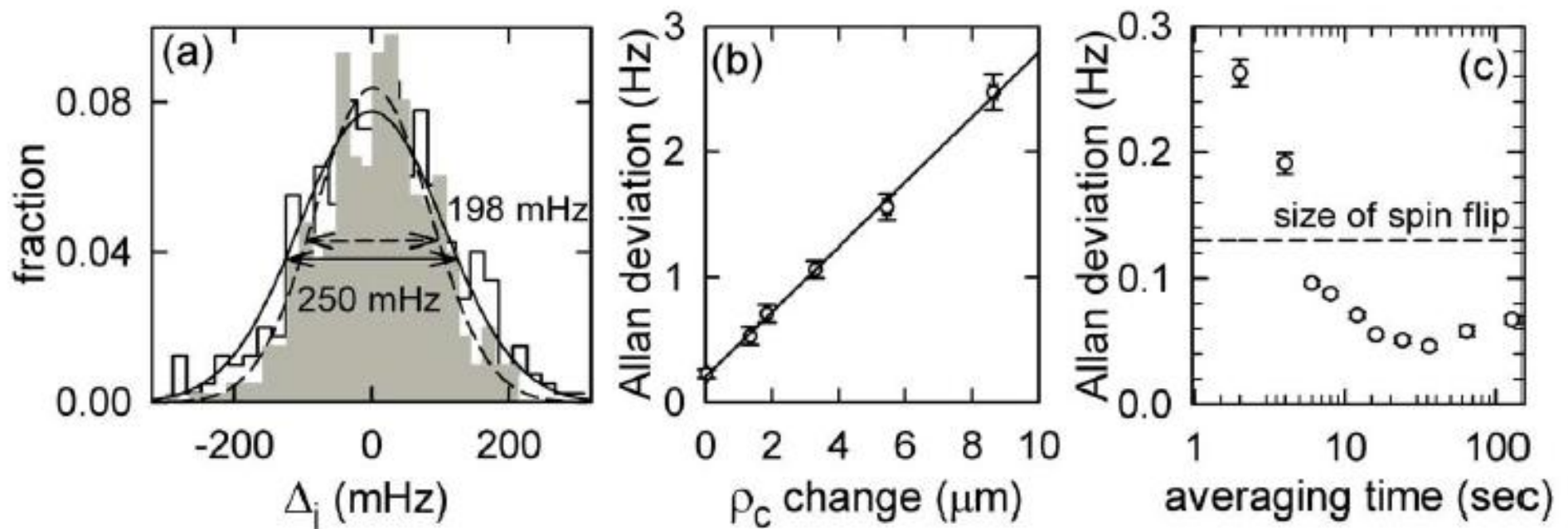
Harmonic oscillator

$$H \sim f^2 z^2$$

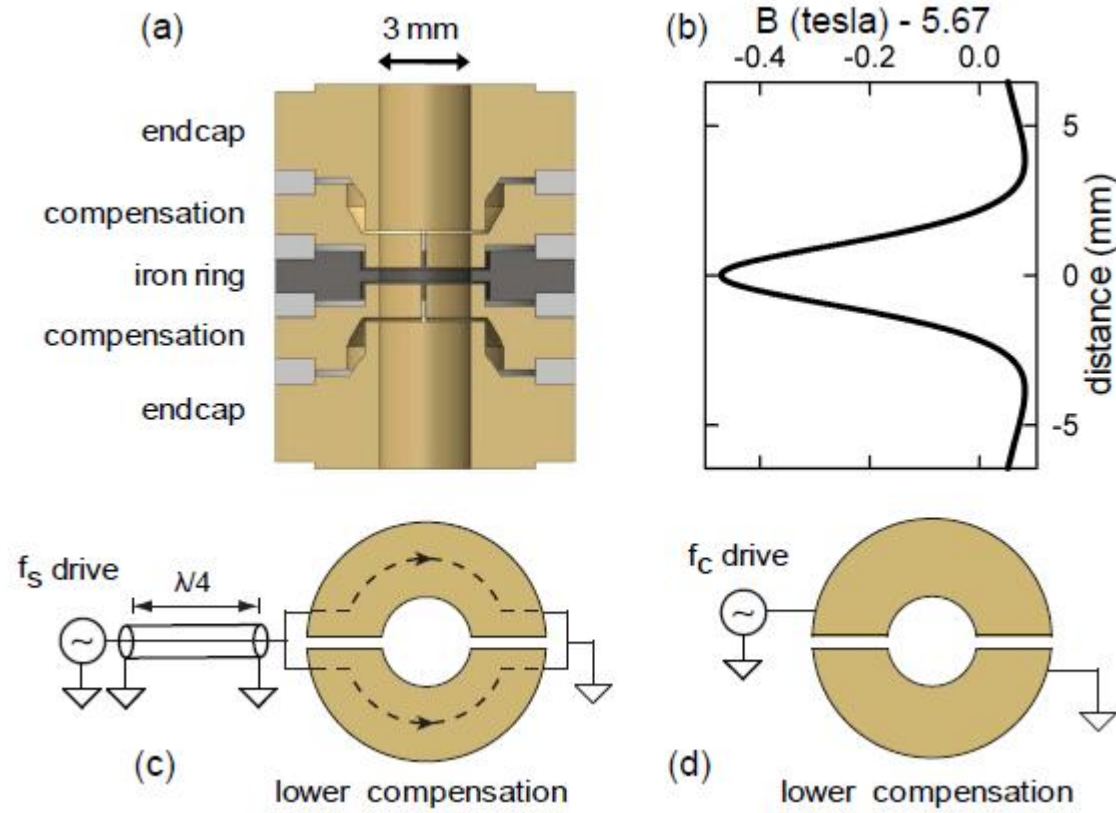
oscillation frequency

shift in oscillation frequency

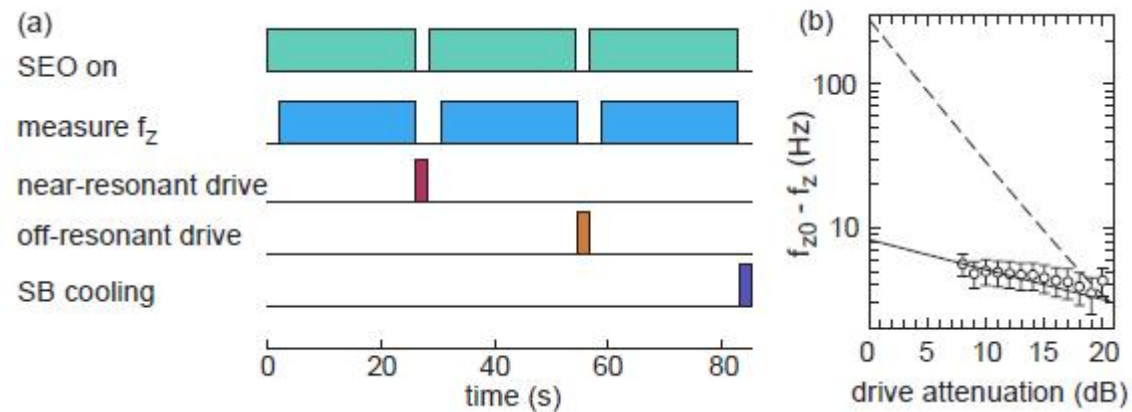
# Spin-Flips Increase Allan Deviation



# Slightly Improved Apparatus



# Measurement Sequence – for Spin Measurement

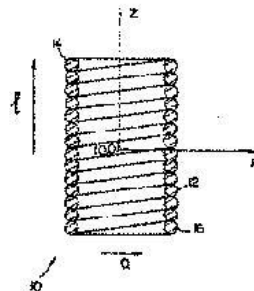


# Self-Shielding Solenoid

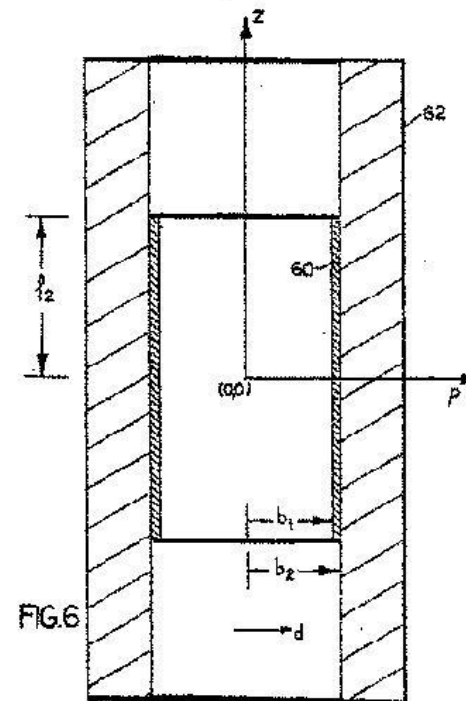
Flux conservation  $\rightarrow$  Field conservation  
 Reduces field fluctuations by about a factor  $> 150$

<b>United States Patent</b> [3]		[11] Patent Number: <b>4,974,113</b>
Gabrielse et al.		[45] Date of Patent: <b>Nov. 27, 1990</b>
[24] <b>SHIELDING SUPERCONDUCTING SOLENOIDS</b>		
[75] Inventors: <b>Gerald S. Gabrielse, Lexington, Mass.; Joseph H. Tan, Cebu City, Philippines</b>		
[73] Assignee: <b>President and Fellows of Harvard College, Cambridge, Mass.</b>		
[31] App. No.: <b>106928</b>		
[22] Filed: <b>Mar. 16, 1988</b>		
[51] Int. Cl.: <b>H01H 47/00</b>		
[52] U.S. Cl.: <b>305/348; 333/315; 324/320</b>		
[58] Field of Search: <b>361/70, 141, 324, 720, 324/322, 335/216</b>		
[26] <b>References Cited</b>		
U.S. PATENT DOCUMENTS		
3,571,396 6/1974 Kaplan <b>361/741</b>		
4,133,899 7/1984 Pivovarov et al. <b>334/320</b>		
FOREIGN PATENT DOCUMENTS		
239,216 2/1982 Fed. Rep. of Germany		
25,192 1/1985 United Kingdom <b>324/321</b>		
OTHER PUBLICATIONS		
Datta et al., "High Field Nuclear Magnetometer", Rev. Sci. Instrum. 51 (4), Apr. 1987, 1987 American Institute of Physics, pp. 638-651.		
Van Dyke et al., "Variable Magnetic Bottle For Precision Oscillation Experiments", Rev. Sci. Instrum. 37 (4), Apr. 1966, 1966 American Institute of Physics, pp. 595-597.		
Primary Examiner—L. T. Hix Assistant Examiner—David M. Gray Attorney, Agent or Firm—Fish & Richardson		
[57] <b>ABSTRACT</b>		
A self-shielding system of closed superconducting circuits shields a specific volume from changes in an external magnetic field in which the circuits are located; the configuration of the circuits is chosen so that induced currents in the circuits, arising from magnetic flux conservation for each closed circuit, tend to cancel any change in the external magnetic field. In another aspect, a single closed self-shielding superconducting circuit comprises of more than two circular loops connected in series encloses a specific volume from changes in an external magnetic field in which the circuit is located; the configuration of the circuit is chosen so that induced currents in the circuit, arising from magnetic flux conservation for the circuit, tends to cancel any change in the external magnetic field.		

26 Claims, 3 Drawing Sheets



U.S. Patent Nov. 27, 1990 Sheet 6 of 8 4,974,113



"Self-shielding Superconducting Solenoid Systems",  
 G. Gabrielse and J. Tan, J. Appl. Phys. **63**, 5143 (1988)

# Resonance Lines to Determine the “Two” Frequencies

square  
of extra  
width

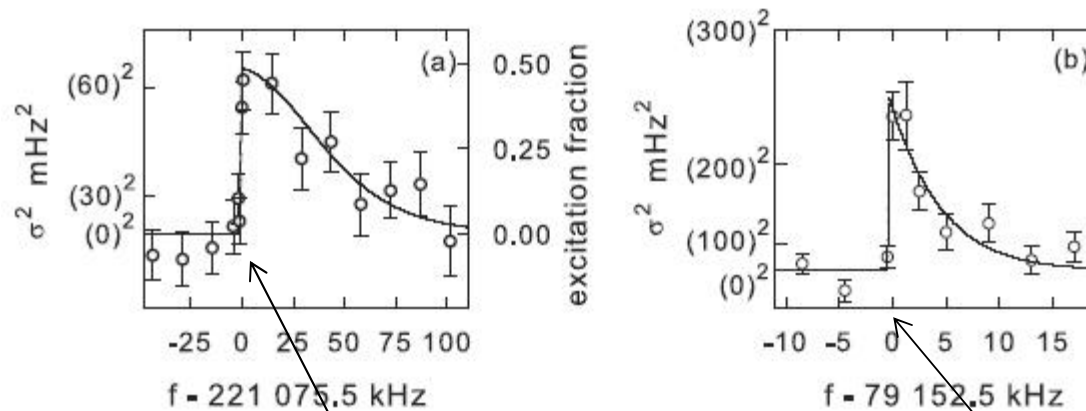


FIG. 4. (a) The spin line. (b) The cyclotron line.

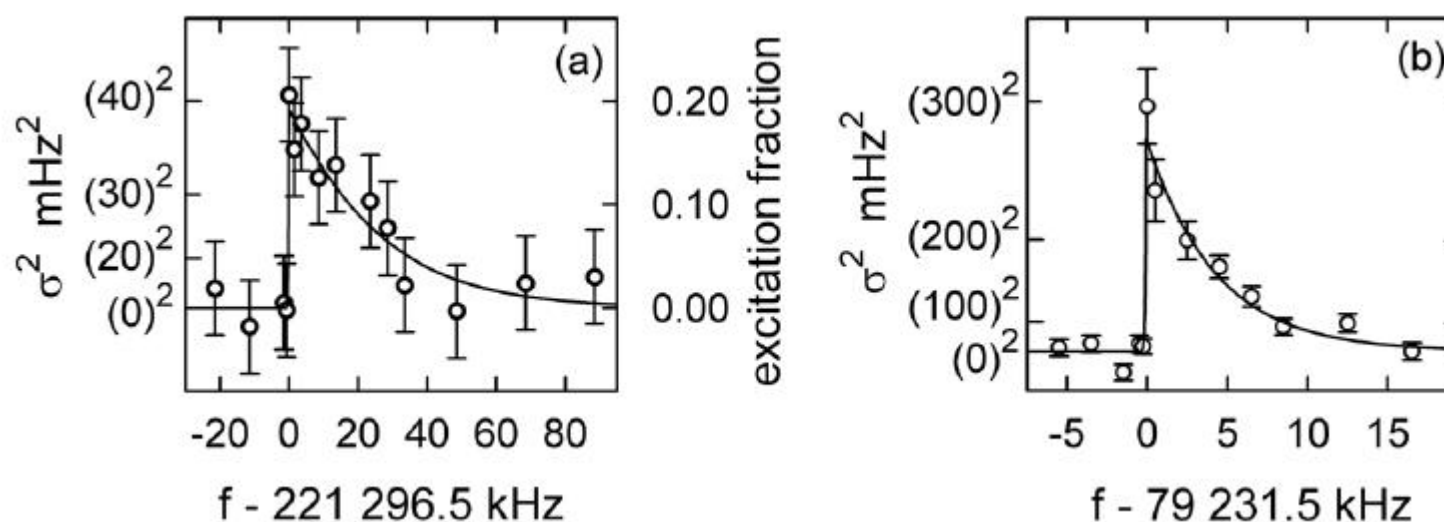
$$\frac{\mu_p}{\mu_N} \equiv \frac{g_p}{2} = \frac{f_s}{f_c}$$

$$f_c^2 = f_+^2 + f_z^2 + f_-^2$$

Brown-Gabrielse  
Invariance Theorem

# Direct Measurement of the Proton Mag. Moment

$$\frac{\mu_p}{\mu_N} \equiv \frac{g_p}{2} = \frac{f_s}{f_c}$$



$$\frac{\mu_p}{\mu_N} = \frac{g}{2} = 2.792\,846 \pm 0.000\,007 \quad [2.5 \text{ ppm}]$$

Harvard:	$g/2 =$	5.585 692	$\pm$	0.000 007	2 506.4 ppb
CODATA:	$g/2 =$	5.585 694 713	$\pm$	0.000 000 023	8.24 ppb





## One-Particle Measurement of the Antiproton Magnetic Moment

J. DiSciacca,<sup>1</sup> M. Marshall,<sup>1</sup> K. Marable,<sup>1</sup> G. Gabrielse,<sup>1,\*</sup> S. Ettenauer,<sup>1</sup> E. Tardiff,<sup>1</sup> R. Kalra,<sup>1</sup> D. W. Fitzakerley,<sup>2</sup>  
 M. C. George,<sup>2</sup> E. A. Hessels,<sup>2</sup> C. H. Storry,<sup>2</sup> M. Weel,<sup>2</sup> D. Grzonka,<sup>3</sup> W. Oelert,<sup>3,4</sup> and T. Sefzick<sup>3</sup>

(ATRAP Collaboration)

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<sup>2</sup>*Department of Physics and Astronomy, York University, Toronto, Ontario M3J 1P3, Canada*

<sup>3</sup>*IKP, Forschungszentrum Jülich GmbH, 52425 Jülich, Germany*

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(Received 21 January 2013; published 25 March 2013)

For the first time a single trapped antiproton ( $\bar{p}$ ) is used to measure the  $\bar{p}$  magnetic moment  $\mu_{\bar{p}}$ . The moment  $\mu_{\bar{p}} = \mu_{\bar{p}} S / (\hbar/2)$  is given in terms of its spin  $S$  and the nuclear magneton ( $\mu_N$ ) by  $\mu_{\bar{p}}/\mu_N = -2.792\,845 \pm 0.000\,012$ . The 4.4 parts per million (ppm) uncertainty is 680 times smaller than previously realized. Comparing to the proton moment measured using the same method and trap electrodes gives  $\mu_{\bar{p}}/\mu_p = -1.000\,000 \pm 0.000\,005$  to 5 ppm, for a proton moment  $\mu_p = \mu_p S / (\hbar/2)$ , consistent with the prediction of the *CPT* theorem.



# First One-Particle Measurement of the Antiproton Magnetic moment

$$\mu_{\bar{p}}/\mu_N = -2.792\,845 \pm 0.000\,012 \quad [4.4 \text{ ppm}].$$

$$\mu_{\bar{p}}/\mu_p = -1.000\,000 \pm 0.000\,005 \quad [5.0 \text{ ppm}]$$

$$\mu_{\bar{p}}/\mu_p = -0.999\,999\,2 \pm 0.000\,004\,4 \quad [4.4 \text{ ppm}].$$

680  
times  
lower  
than  
previous

Resonance	Source	ppm
spin	resonance frequency	2.7
spin	magnetron broadening	1.3
cyclotron	resonance frequency	3.2
cyclotron	magnetron broadening	0.7
total		4.4

TABLE I. Significant uncertainties in ppm.

# 680 – Fold Improved Precision

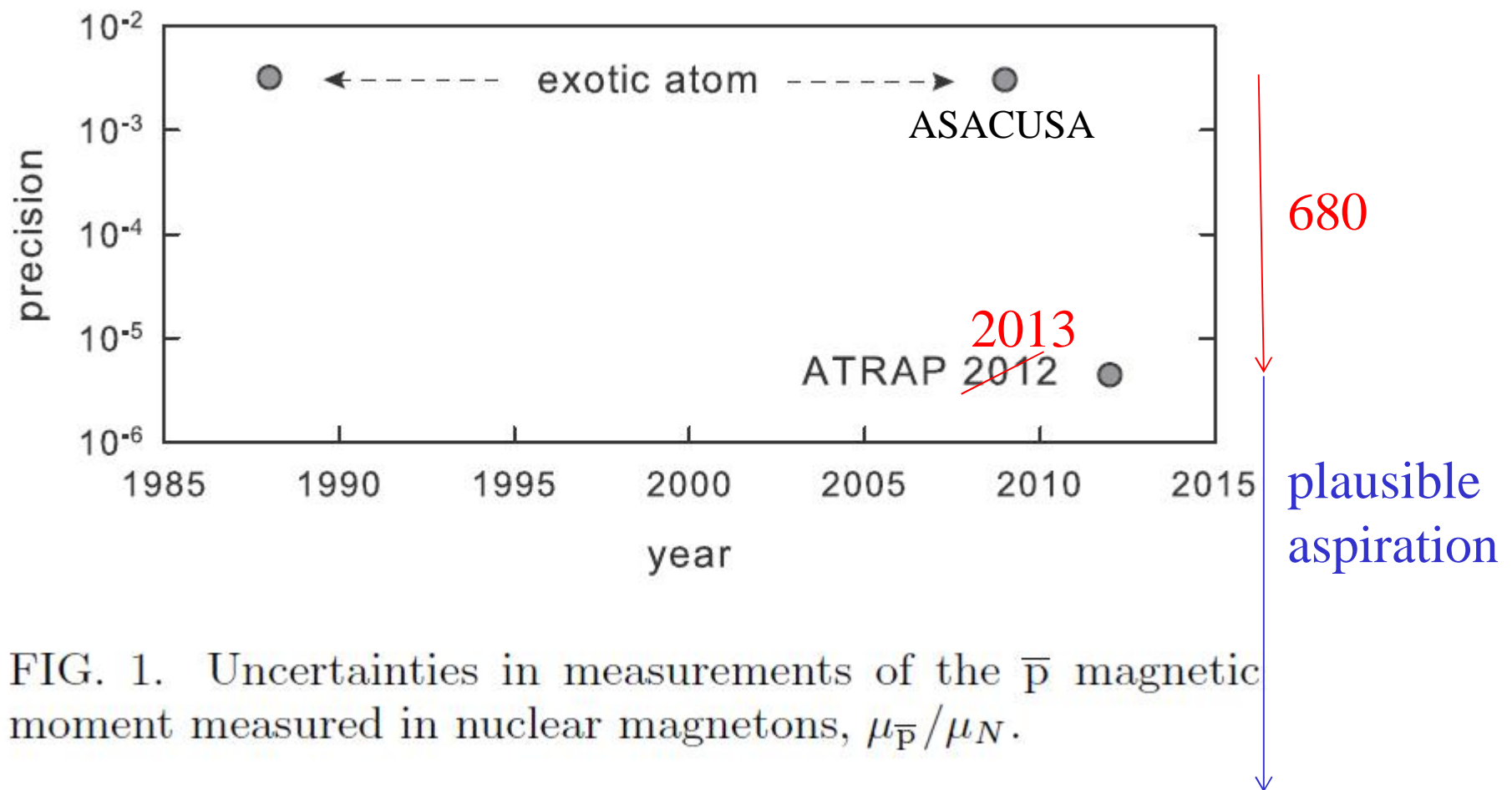
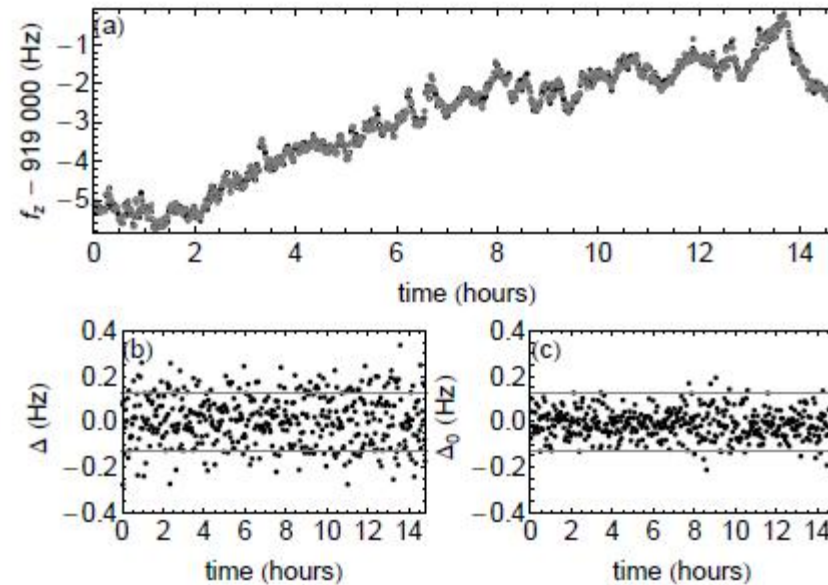


FIG. 1. Uncertainties in measurements of the  $\bar{p}$  magnetic moment measured in nuclear magnetons,  $\mu_{\bar{p}}/\mu_N$ .

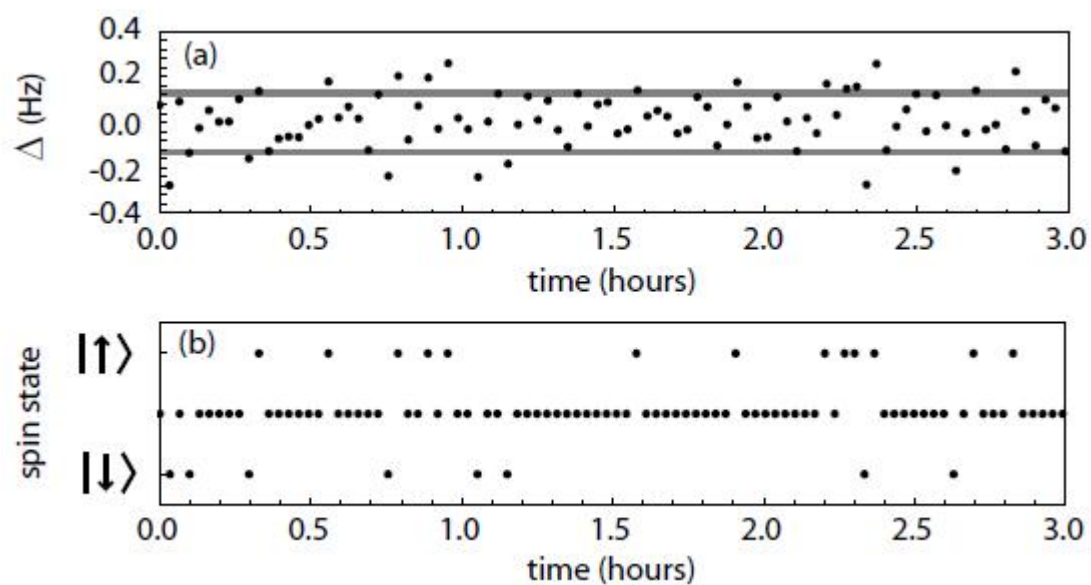
ATRAP, Phys. Rev. Lett. (2013).

Gabrielse

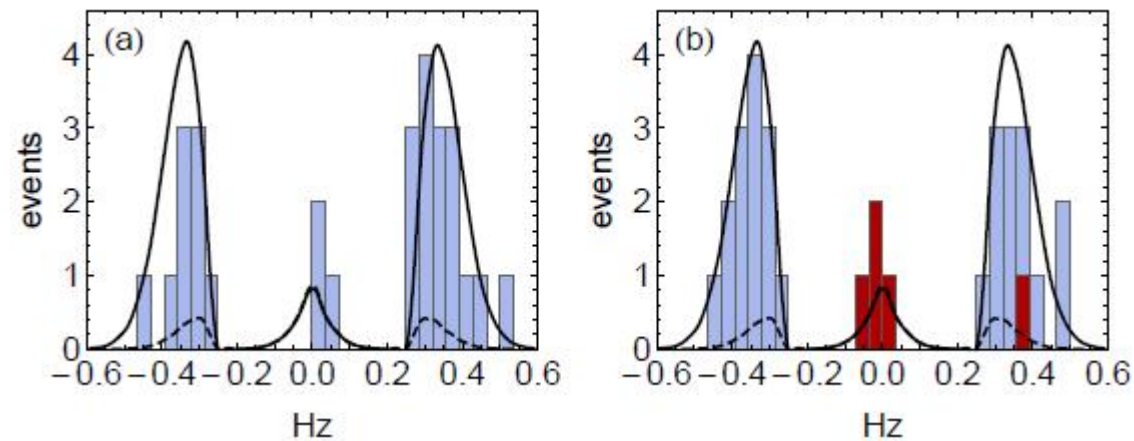
# For the Future A 1000 to 10000-fold Improved Precision May be Possible



# Single Proton Spin Flips Resolved



# Spin Down to Up must follow Spin Up to Down: Correlation Function



# Proton Spin Flip Report

PRL **110**, 140406 (2013)

PHYSICAL REVIEW LETTERS

week ending  
5 APRIL 2013

## Resolving an Individual One-Proton Spin Flip to Determine a Proton Spin State

J. DiSciaccia, M. Marshall, K. Marable, and G. Gabrielse\*

*Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA*

(Received 21 February 2013; published 4 April 2013)

Previous measurements with a single trapped proton ( $p$ ) or antiproton ( $\bar{p}$ ) detected spin resonance from the increased scatter of frequency measurements caused by many spin flips. Here a measured correlation confirms that individual spin transitions and states are rapidly detected instead. The 96% fidelity and an efficiency expected to approach unity suggests that it may be possible to use quantum jump spectroscopy to measure the  $p$  and  $\bar{p}$  magnetic moments much more precisely.

DOI: [10.1103/PhysRevLett.110.140406](https://doi.org/10.1103/PhysRevLett.110.140406)

PACS numbers: 13.40.Em, 14.20.Dh, 37.10.Ty

Similar proton result from Mainz group in same issue

Gabrielse



# **Does the Electron Also Have an Electric Dipole Moments**

# Particle EDM Requires Both P and T Violation

Magnetic moment:

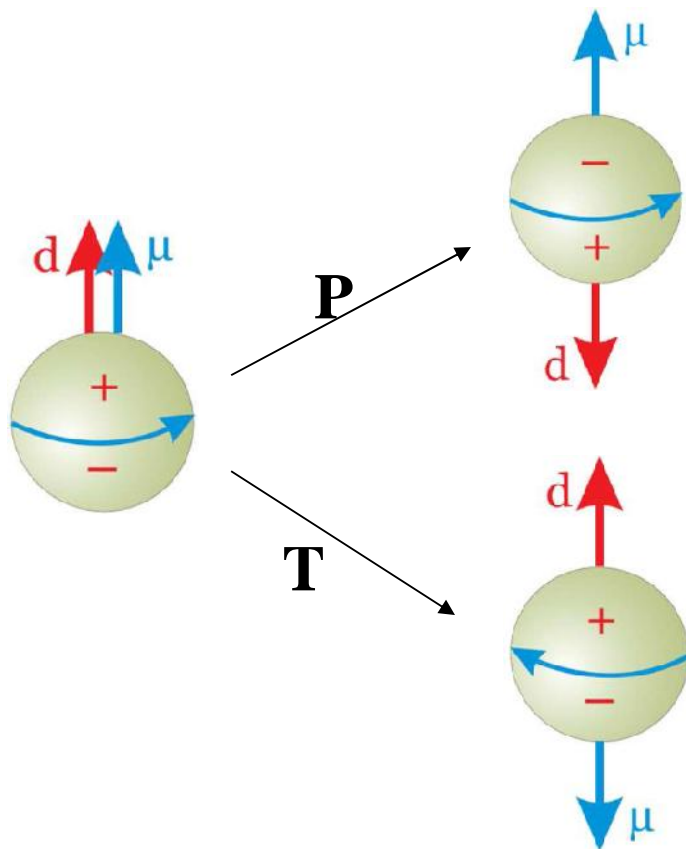
$$\vec{\mu} = -g \frac{e}{2m} \frac{\hbar}{2} \frac{\vec{S}}{\hbar/2}$$

(exists and well-measured)

Electric dipole Moment:

$$\vec{d} = -d \frac{\vec{S}}{\hbar/2}$$

(d is extremely small)



If reality is invariant under parity transformations **P**

$$\rightarrow \mathbf{d} = \mathbf{0}$$

If reality is invariant under time reversal transformations **T**

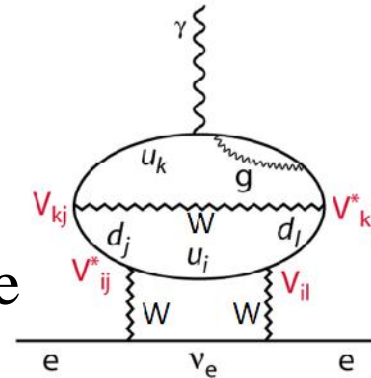
$$\rightarrow \mathbf{d} = \mathbf{0}$$

# Standard Model of Particle Physics

## → Currently Predicts a Non-zero Electron EDM

Standard model:  $d \sim 10^{-38}$  e-cm

Too small to measure by orders of magnitude  
best measurement:  $d \sim 2 \times 10^{-27}$  e-cm



four-loop  
level in  
perturbation  
theory

M. Pospelov and I. B. Khriplovich, "Electric dipole moment of the W boson and the electron in the Kobayashi-Maskawa model," Sov. J. Nucl. Phys. **53**, 638–640 (1991).

Weak interaction couples quark pairs (generations)

$$\begin{pmatrix} u \\ d' \end{pmatrix}, \begin{pmatrix} c \\ s' \end{pmatrix}, \begin{pmatrix} t \\ b' \end{pmatrix}$$

CKM matrix relates to d, s, b quarks  
(Cabibbo-Kabayashi-Maskawa matrix)

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

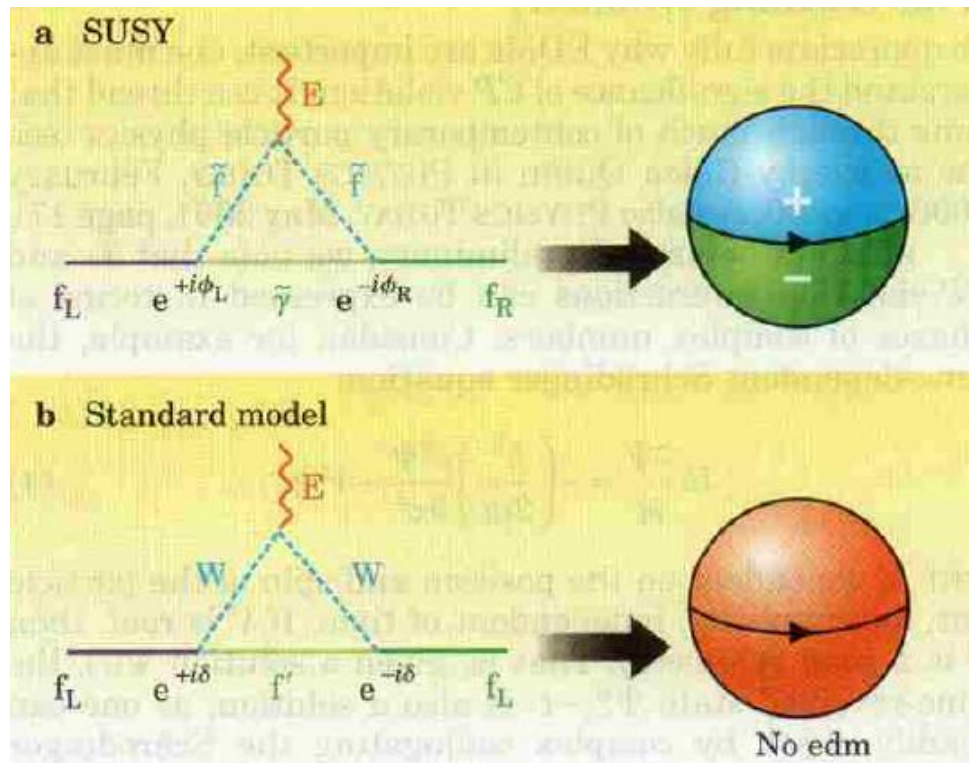
almost the unit matrix

$$\begin{pmatrix} 0.974 & 0.227 & 0.004 \\ 0.227 & 0.973 & 0.042 \\ 0.008 & 0.042 & 0.999 \end{pmatrix}$$

# Extensions to the Standard Model

## → Measureable Electron EDM

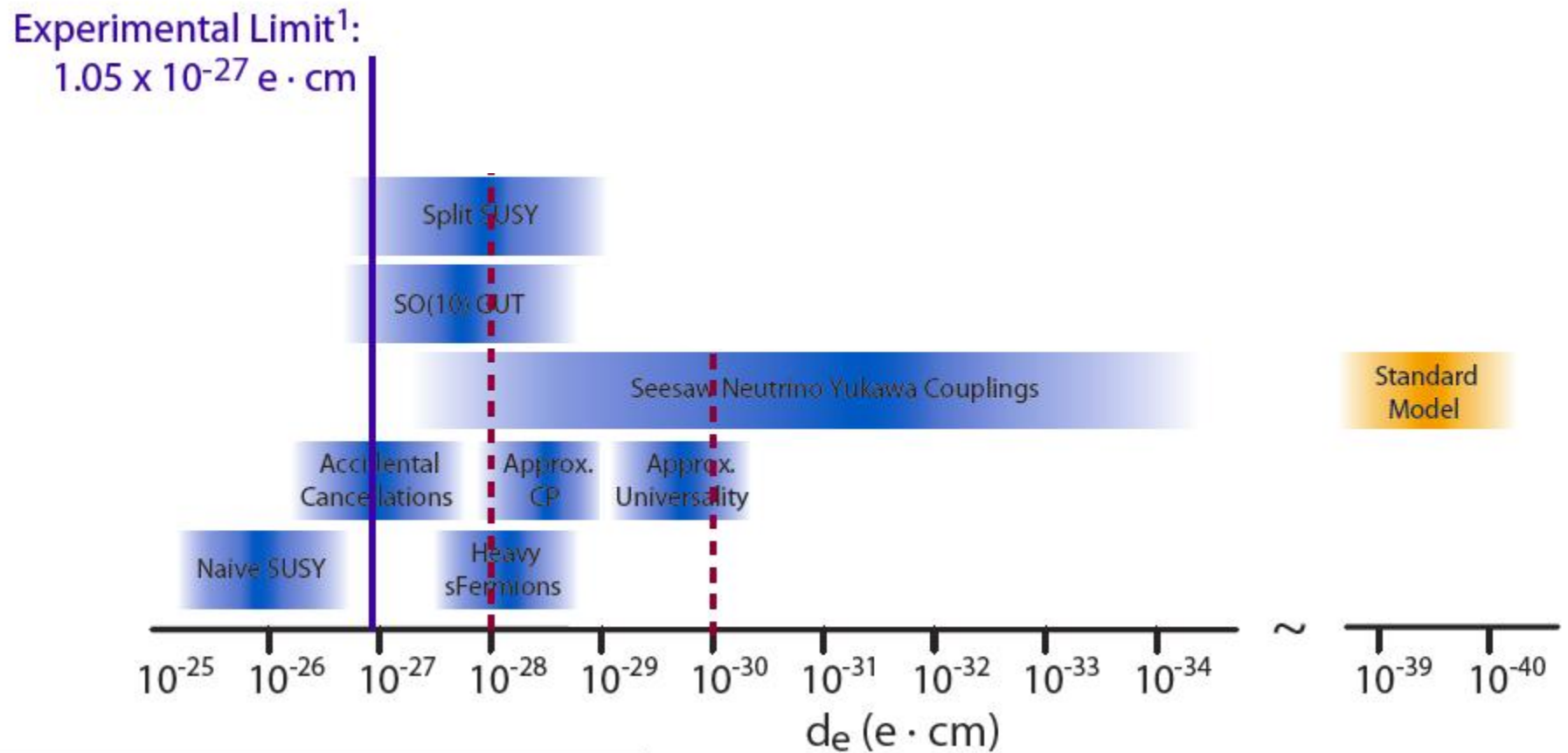
An example



Low order contribution  
→ larger moment

Low order contribution  
→ vanishes

# EDM Predictions



<sup>1</sup>J.J. Hudson et al, Nature 473, 493-496 (2011)

# No Particle EDM Has Yet Been Detected

Electron EDM limit  $|d_e| \leq 1.6 \times 10^{-27} e \text{ cm}$

Commins, ...

PRL **88**, 071805 (2002)

1.0

Hinds, 2011

Neutron EDM limit  $|d_n| < 2.9 \times 10^{-26} e \text{ cm}$

ILL Grenoble,

PRL **97**, 131801 (2006)

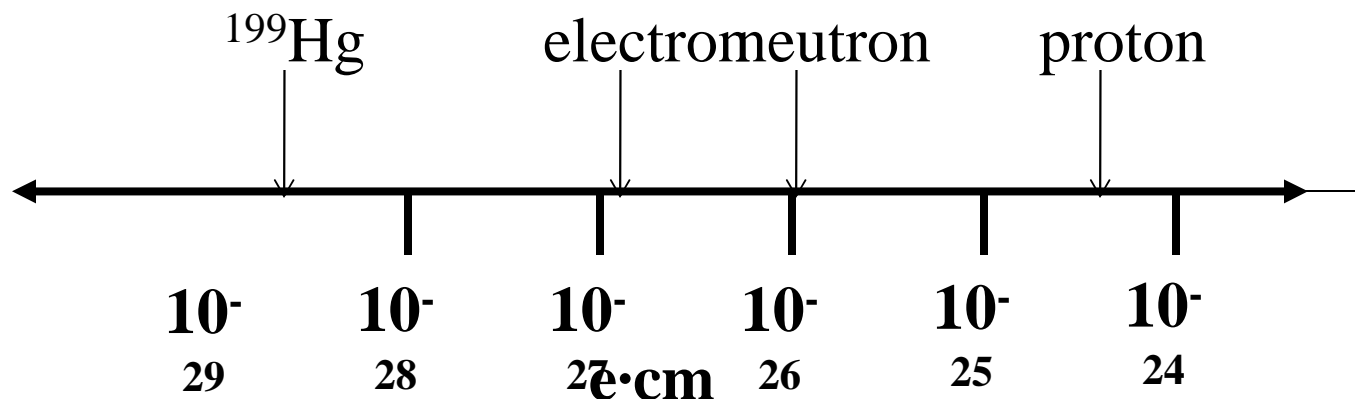
Proton EDM limit  $|d_p| < 7.9 \times 10^{-25} e \text{ cm}$

Heckel, Fortson, ...

PRL **102**, 101601 (2009)

from  $|d(^{199}\text{Hg})| < 3.1 \times 10^{-29} e \text{ cm}$

also sets  $|d_n| < 5.8 \times 10^{-26} e \text{ cm}$



# Does the Electron Also Have an Electric Dipole Moment?

Magnetic moment:  $\vec{\mu} = -g \frac{e}{2m} \vec{S}$

(exists and well-measured)

Electric dipole moment:  $\vec{d} = -d \frac{\vec{S}}{\hbar/2}$

(d is extremely small)

## No Electron EDM Detected so Far

Commins limit (2002)

$$|d_e| \leq 1.6 \times 10^{-27} e \text{ cm}$$

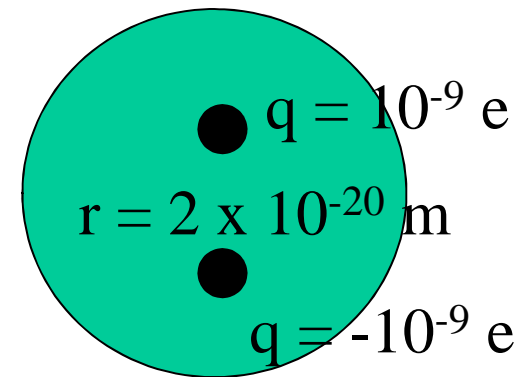
Regan, Commins, Schmidt, DeMille,  
Phys. Rev. Lett. **88**, 071805 (2002)

Imperial College (2011)

$$|d_e| < 10.5 \times 10^{-28} e \text{ cm}$$

Hudson, Kara, Smallman, Sauer, Tarbutt, Hinds,  
Nature **473**, 493 (2011)

Tl



YbF

# Advanced Cold-Molecule Electron EDM



**Harvard University**  
John Doyle Group  
Gerald Gabrielse Group

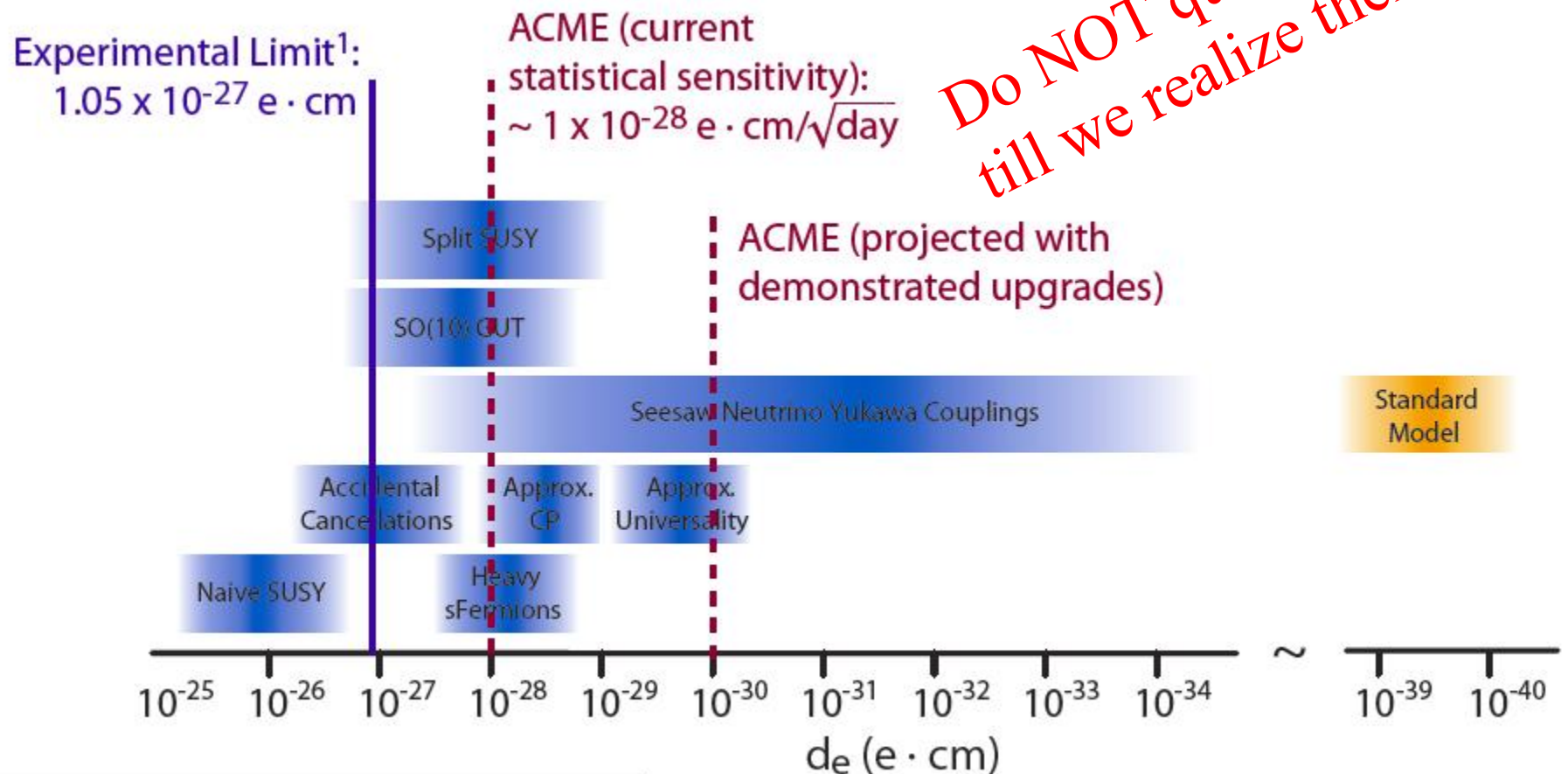
**Yale University**  
David DeMille Group

Nearing publication of a new result  
for the electron EDM

Funding from NSF



# New Electron EDM Measurement Close



<sup>1</sup>J.J. Hudson et al, Nature 473, 493-496 (2011)

## **Relationship to LHC Physics**

The LHC is exciting and important but EDMs also play a role

- should get an improved electron EDM on the LHC time scale
- If the LHC sees new particles, is CP violation involved?
- If the LHC sees nothing, EDM game is the only one in town

## **Main point for this conference**

- It is easy to speak about making new EDM measurements
- It is much harder to get measurements within orders of magnitude of the precision in current measurements (especially with charged particles)

# Summary

## Antiproton magnetic moment

4.4 ppm (factor of 680 improvement)

Not so often that one gets to make such a step

Aspire to get 1000 to 10000 times better

Then will have a second extremely precise test of CPT with baryon/antibaryon system

Gabrielse