

# Partial Wave Analysis for $\bar{p}p$ and $e^+e^-$ Annihilation Processes

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# Outline

- PWA software for PANDA and other hadron spectroscopy experiments
- PWA @ PANDA
  - detector and physics program
  - PWA challenges for PANDA
- Analyses of Crystal Barrel @ LEAR data with relevance for PANDA
  - investigation of the  $\bar{p}p$  annihilation process and the production mechanisms of vector mesons
  - $\bar{p}p \rightarrow \omega \pi^0$
  - $\bar{p}p \rightarrow K^+ K^- \pi^0$  with the focus on  $\phi \pi^0$  and  $K^{*\pm} K^\mp$
- PWA of BESIII data

# PWA Software Package

PWA activities for PANDA started in Bochum in spring 2010 with the aims:

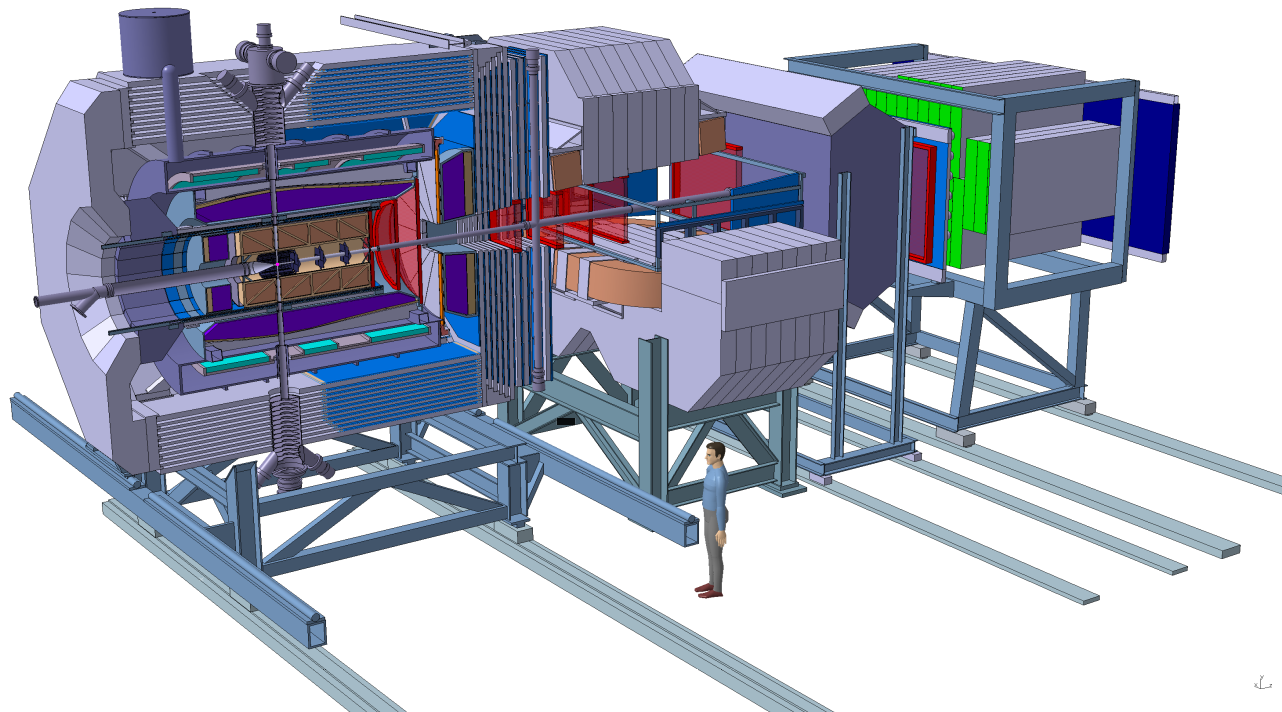
- to develop a generic PWA software package
- to support all physics cases to be studied with PANDA and partly other hadron spectroscopy experiments

Software package PAWIAN (**P**Artial **W**ave Interactive **A**Nalysis) already in a good shape and first analyses have been started

- Full hypothesis and other input settings defined via configuration files
- Event based maximum likelihood fit
- Minimization with MINUIT2 in multithreaded and networked mode
- qft++: decay amplitudes in various formalisms ([M. Williams \(CLAS, GlueX\) Computer Physics Communications, Vol. 180, Issue 10, 2009](#))

# PANDA @ FAIR

- Fixed target experiment integrated into the HESR @ FAIR, Darmstadt
- $\bar{p}p$ - and  $\bar{p}A$ -annihilation with  $\bar{p}$ -momentum between 1.5-15 GeV/c
- Rich physics program with the focus on charmonium and open charm spectroscopy and the search of exotic states



# PWA Challenges @ PANDA

## $\bar{p}p$ production mechanism

- Contributing initial  $\bar{p}p$  states rise with increasing beam momentum
  - number of fit parameters rises dramatically
- $p_{\bar{p},\max} = 1.94 \text{ GeV}/c$  @ CB-LEAR  $\rightarrow L_{\max} \approx 5$
- $p_{\bar{p},\max} = 15 \text{ GeV}/c$  @ PANDA  $\rightarrow L_{\max} = ?$ 
  - threshold effects relevant for production of heavy resonances (e.g. charmonia)

$J$	Singulett $\lambda = 0$	$J^{PC}$	Triplet $\lambda = \pm 1$	$J^{PC}$	Triplet $\lambda = \pm 1, 0$	$J^{PC}$
0	$^1S_0$	$0^{-+}$			$^3P_0$	$0^{++}$
1	$^1P_1$	$1^{+-}$	$^3P_1$	$1^{++}$	$^3S_1, ^3D_1$	$1^{--}$
2	$^1D_2$	$2^{-+}$	$^3D_2$	$2^{--}$	$^3P_2, ^3F_2$	$2^{++}$
3	$^1F_3$	$3^{+-}$	$^3F_3$	$3^{++}$	$^3D_3, ^3G_3$	$3^{--}$
4	$^1G_4$	$4^{-+}$	$^3G_4$	$4^{--}$	$^3F_4, ^3H_4$	$4^{++}$
5	$^1H_5$	$5^{+-}$	$^3H_5$	$5^{++}$	$^3G_5, ^3I_5$	$5^{--}$
6	$^1I_6$	$6^{-+}$	$^3I_6$	$6^{--}$	$^3H_6, ^3J_6$	$6^{++}$

## Statistics

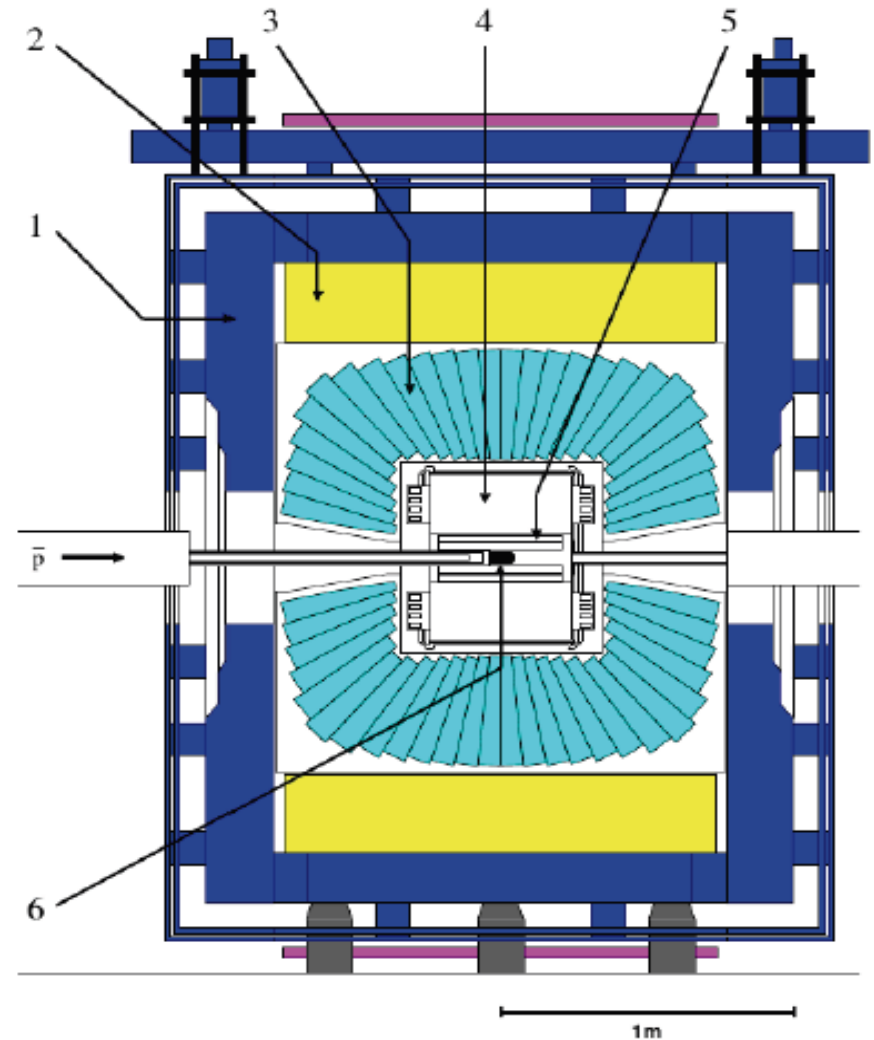
- Low cross sections for some channels of interest (pb-nb)
- How many events are needed for reliable fits?

# PWA with Crystal Barrel Data

## Crystal Barrel experiment @ LEAR (CERN)

- Fixed target experiment
- $\bar{p}p$  annihilation at rest and in flight
  - highest beam momentum 1.94 GeV/c
- Physics program
  - study of the annihilation process
  - spectroscopy of light mesons
  - search for exotics: glueballs, hybrids and multiquark states
- In operation between 1989 and 1996

Excellent opportunity for the investigation of specific physics aspects for PANDA



- (1) Iron Joke, (2) Magnet Coil  
(3) CsI(Tl)-Calorimeter, (4) Jet-Drift-Chamber  
(5) Vertex-Detector, (6)  $\text{LH}_2$ -Target

# PWA: $\bar{p}p \rightarrow \omega\pi^0$

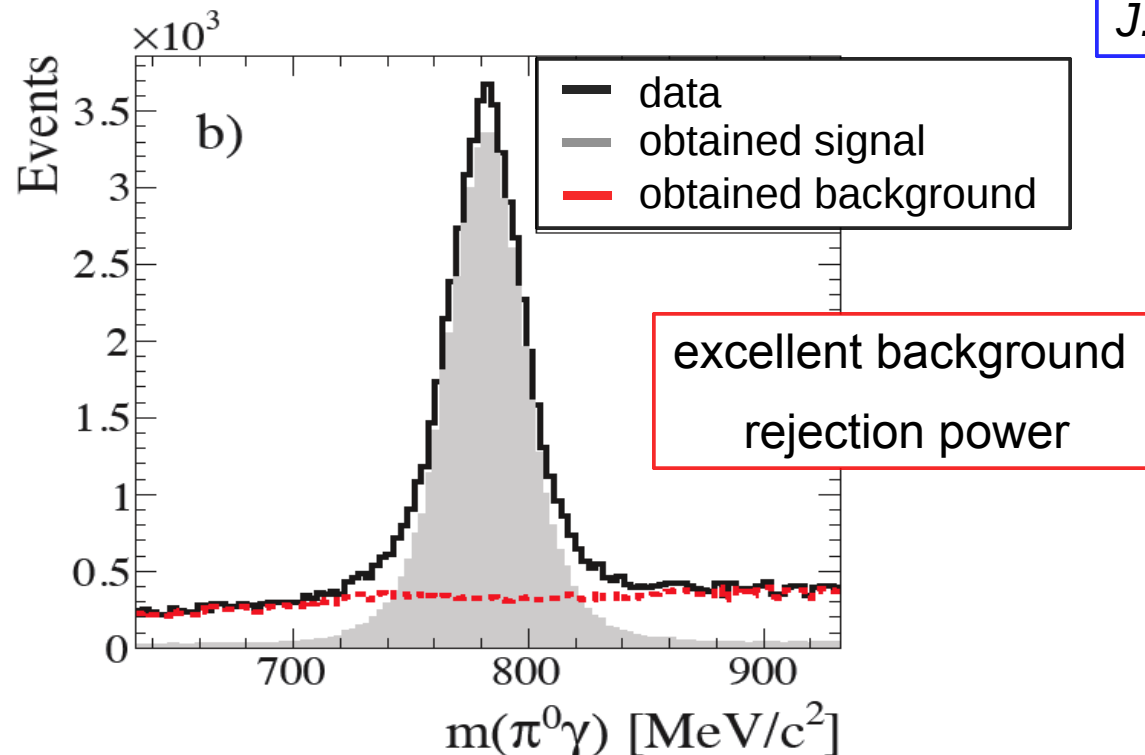
- Relatively simple reaction with easy access to the initial  $\bar{p}p$ -system
- Determination of the  $\omega$  spin density matrix (SDM) which contains the full information of the production mechanism
- Two decay modes  $\omega \rightarrow \pi^0\gamma$  and  $\omega \rightarrow \pi^+\pi^-\pi^0$  separately analyzed at various beam momenta between 0.6-1.94 GeV/c

## PWA Strategy

- Preparation of accurate and clean data samples by applying a kinematic fit and an event based background rejection
  - old offline software re-installed
- Fits to determine the largest contributing  $L_{\max}$  of the  $\bar{p}p$  system
  - description of the full decay chain including the  $\omega$  decay by making use of the helicity and canonical formalism
- Extraction of the  $\omega$ -SDM with two independent methods from
  - the obtained PWA fit result
  - angular distribution of the decay products (Schilling method)

# $\bar{p}p \rightarrow \omega\pi^0$ : Background Rejection

- New background rejection method by assigning a probability for each event to be a signal event (*M. Williams, M. Bellis, C.A. Meyer: arXiv:0809.2548 [nucl-ex]*)
- Event weight for each event
  - determination of the signal to background ratio for the n nearest neighbors in the phase space
- Origin of the background sources not necessarily needed to be known



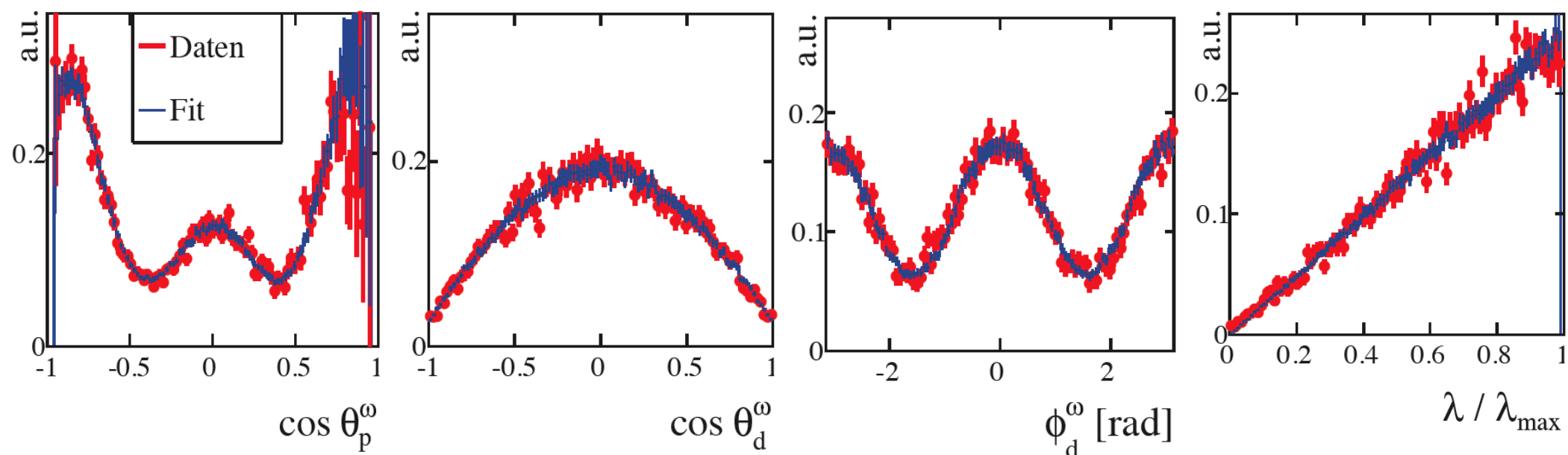


# PWA results for $\bar{p}p \rightarrow \omega \pi^0$

- $L_{\max}$  determined unambiguously
- $L_{\max}$  increases from 3 @ 600 MeV/c to 5 @ 1940 MeV/c

$$\bar{p}p \rightarrow \omega \pi^0 \rightarrow (\pi^+ \pi^- \pi^0) \pi^0 \quad p_{\bar{p}} = 900 \text{ MeV/c}$$

*J. Pychy, Bochum*



# $\bar{p}p \rightarrow \omega\pi^0$ : $\omega$ Spin Density Matrix

- SDM provides all information of the production mechanism
- Spin 1 particle: 3x3 complex elements
- Normalization, parity and hermicity conservation yields to only 4 independent real parameters

$$\rho = \begin{pmatrix} 1/2(1 - \rho_{00}) & \Re\rho_{10} + i\Im\rho_{10} & \rho_{1-1} \\ \Re\rho_{10} - i\Im\rho_{10} & \rho_{00} & -\Re\rho_{10} + i\Im\rho_{10} \\ \rho_{1-1} & -\Re\rho_{10} - i\Im\rho_{10} & 1/2(1 - \rho_{00}) \end{pmatrix}$$

- Alignment if  $\rho_{11} \neq \rho_{00}$

- Extraction of the elements via PWA:

$$\rho_{\lambda_\omega \lambda'_\omega}^0 = \frac{1}{N} \sum_{M_{\bar{p}p}} A_{M_{\bar{p}p}, \lambda_\omega} A_{M_{\bar{p}p}, \lambda'_\omega}^* \quad \text{with} \quad N = \sum_{M_{\bar{p}p}, \lambda_\omega} |A_{M_{\bar{p}p}, \lambda_\omega}|^2$$

*H. Koch,  
Helicity amplitude for  $\bar{p}p \rightarrow \omega\pi^0$ ,  
Internal PANDA Note*

- Extraction of the parameters via fit to decay angular distribution ( $\omega \rightarrow \pi^+ \pi^- \pi^0$ )

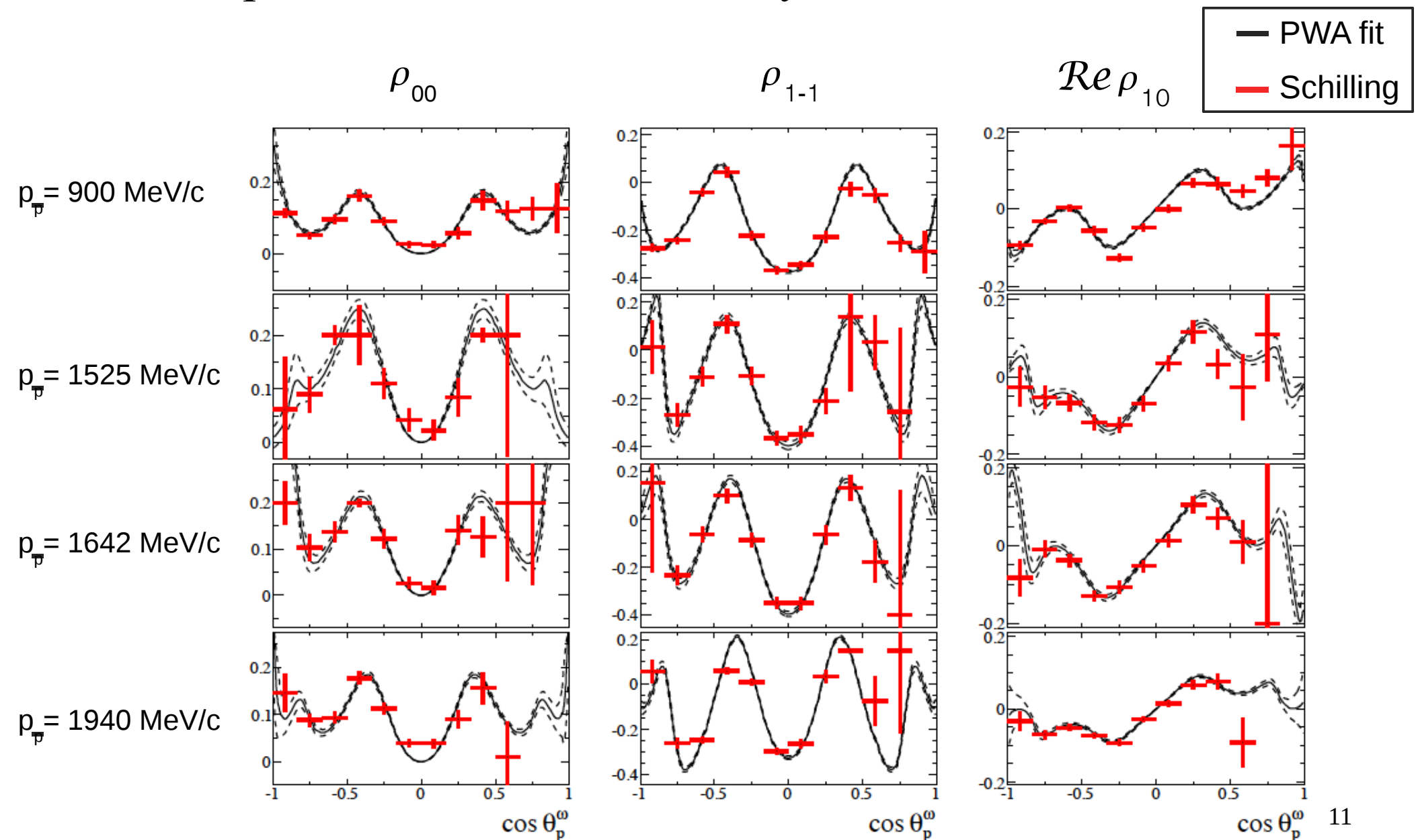
$$W(\cos(\theta), \phi) \propto \frac{1}{2}(1 - \rho_{00}) + \frac{1}{2}(3\rho_{00} - 1) \cos\theta$$

$$- \sqrt{2} \Re\rho_{10} \sin 2\theta \cos\phi - \rho_{1-1} \sin^2\theta \cos 2\phi$$

*Schilling, Seyboth and Wolf,  
Nucl.Phys. B15 (1970) 397-412,  
Erratum-ibid. B18 (1970) 332*

# $\bar{p}p \rightarrow \omega\pi^0$ : $\omega$ Spin Density Matrix

SDM parameters in the  $\omega$  helicity frame for  $\omega \rightarrow \pi^+\pi^-\pi^0$

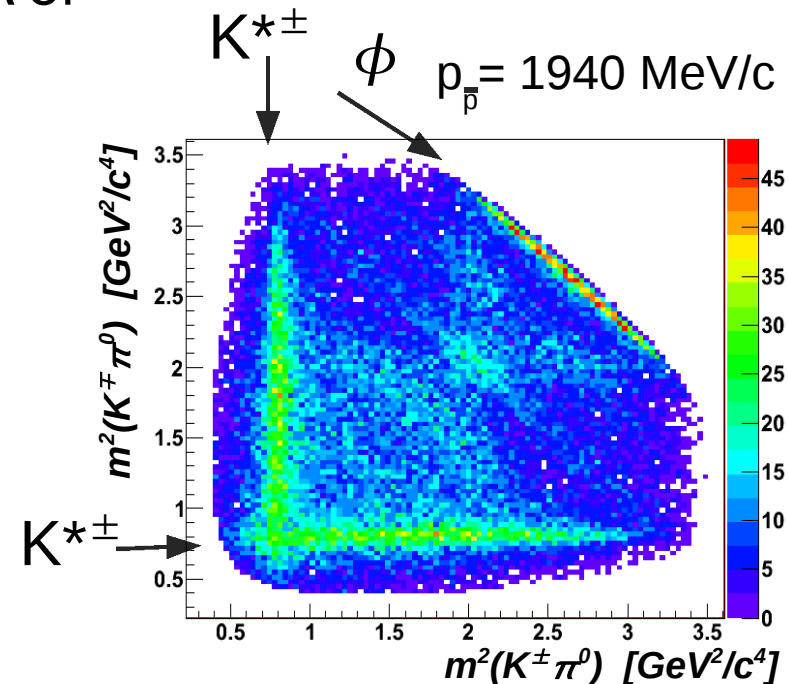
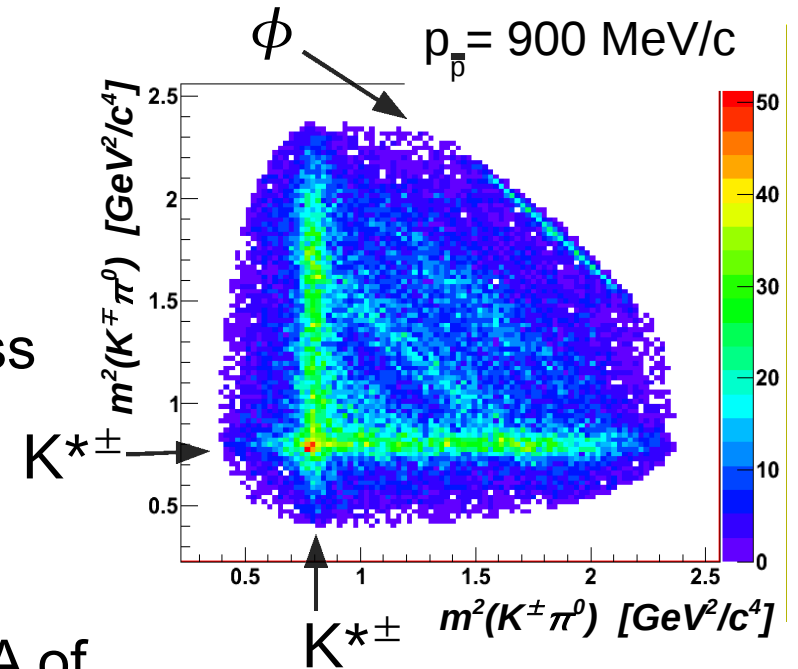


# $\bar{p}p \rightarrow \omega\pi^0$ : $\omega$ Spin Density Matrix

- Good agreement between the two independent methods
- $\rho_{00} < 0.33$  over the whole production angle for all beam momenta
  - **strong alignment visible**
- Strong oscillatory dependence along the production angle for all beam momenta
  - origin not yet clear
  - **formation of intermediate resonances?**
- Comparison of SDMs obtained for different decay modes is a good check for the understanding of the detector
  - accurate access to the systematics
  - suitable for first measurements @ PANDA

$$\bar{p}p \rightarrow K^+K^-\pi^0$$

- Contains  $\phi\pi^0$  and  $K^{*\pm}K^\mp$  events
- Production of vector mesons with strangeness
  - different process in comparison to  $\omega$  production
  - rearrangement vs. annihilation
- Interference of resonances require a full PWA of the complete channel
- SDM via extraction of the fitted  $\phi$  and  $K^{*\pm}$  amplitudes



# PWA: $\bar{p}p \rightarrow K^+K^-\pi^0$

- Full PWA from the initial to the final state
- $L_{\text{max}}=4$  @ 900 MeV/c and 1940 MeV/c
- Hypotheses based on previous results (*Crystal Barrel: Phys. Lett. B639 (2006) 165*)
  - $\phi\pi^0$ ,  $\phi(1680)\pi^0$ ,
  - $f_2(1270)\pi^0$ ,  $f'_2(1525)\pi^0$
  - $a_2(1320)\pi^0$
  - $K^*K$ ,  $K^*(1680)K$
  - all  $f_0\pi^0$  channels via  $(KK)_S$ -wave
  - all  $K^{*\pm}_0 K$  channels via  $(K\pi)_S$  ( $l=1/2$ ) wave
  - $K (K\pi)_S$  ( $l=3/2$ ) wave
- Many resonances yield in a large number fit parameters
  - 420 @ 900 MeV/c
  - 464 @ 1940 MeV/c

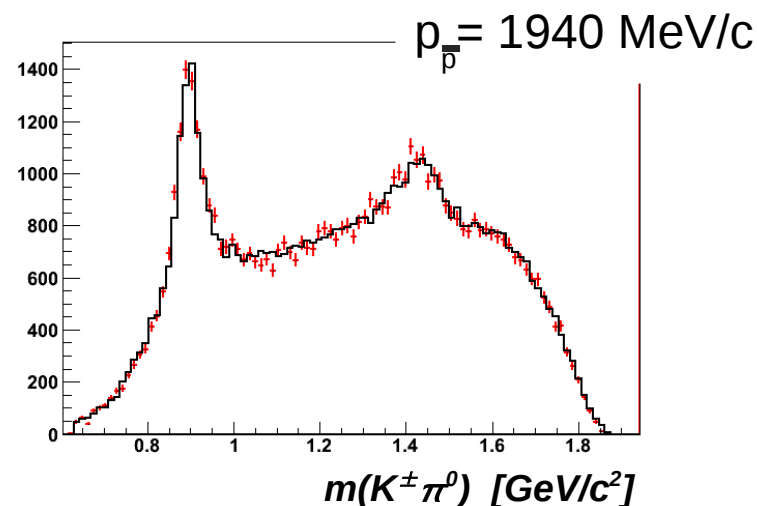
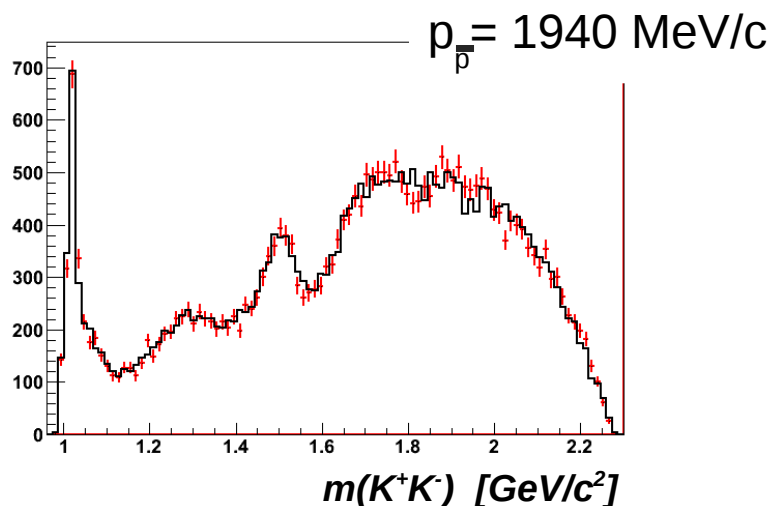
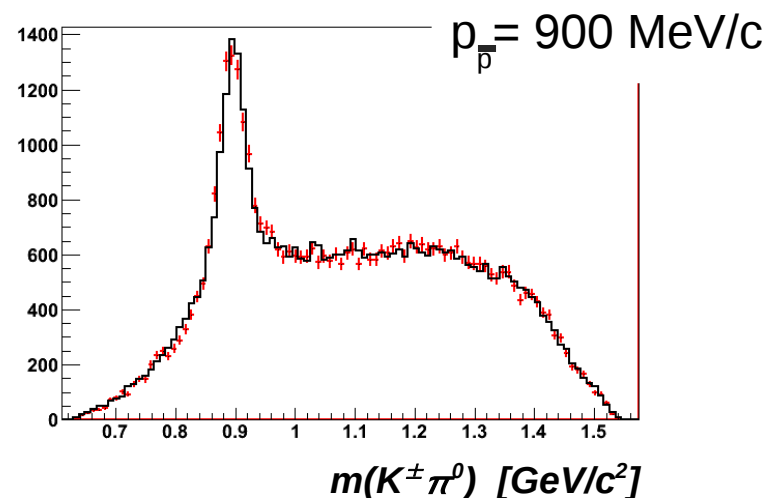
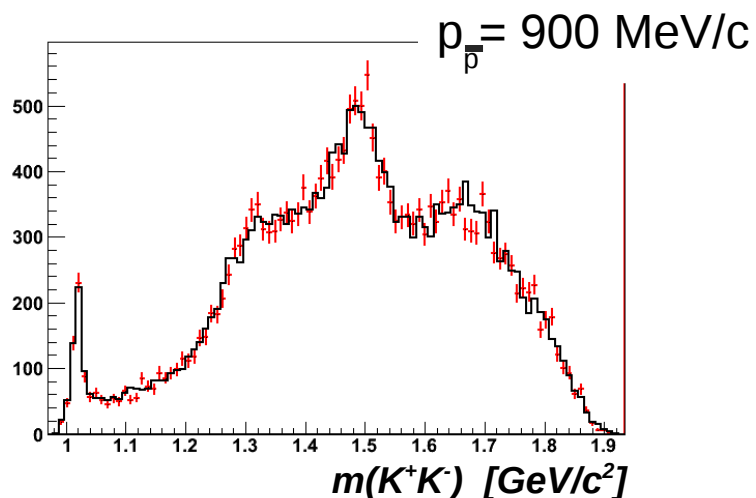
K-matrix parametrization by  
*Anisovich and Sarantsev,*  
*Eur. Phys. J. A16, 229(2003)*

K-matrix parametrization used  
by FOCUS:  
*Phys. Lett. B653 (2007) 1-11*

# PWA: $\bar{p}p \rightarrow K^+K^-\pi^0$

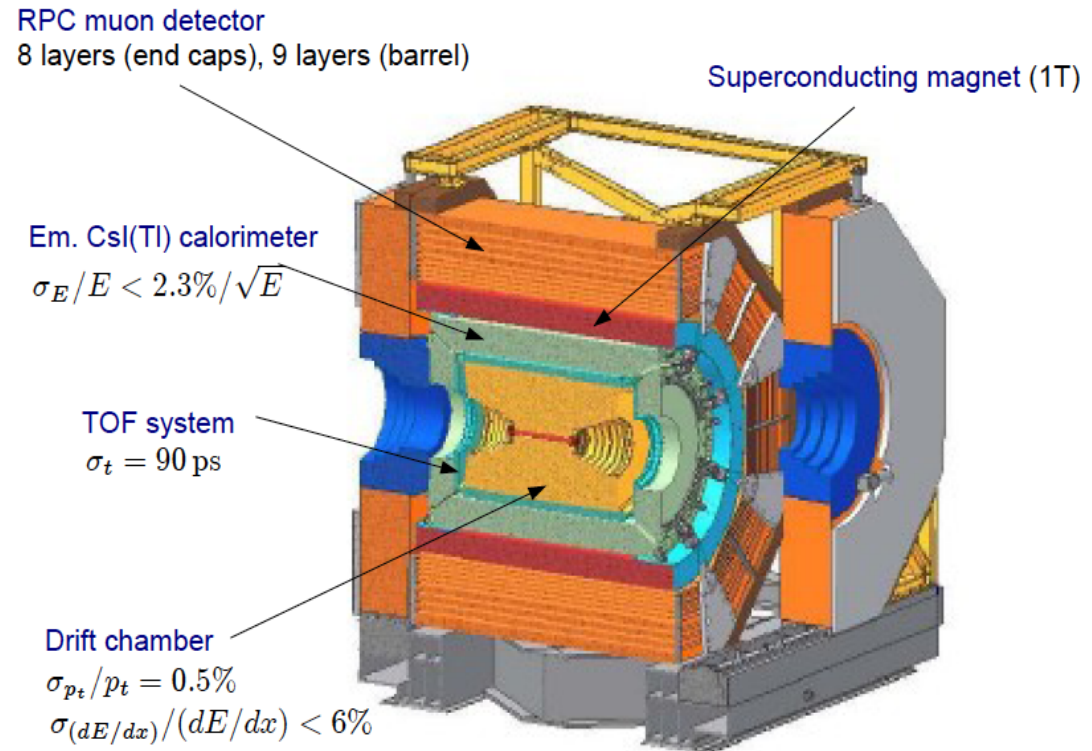
- Excellent description of the data
- Extraction of the SDMs for  $\phi$  and  $K^*$  possible

*J. Pychy, Bochum*



# PWA of BESIII Data

- Symmetric  $e^+e^-$  collider
  - beam energy 1.0-2.3 GeV
  - max. luminosity  $10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- Physics program
  - light meson spectroscopy
  - charmonium spectroscopy
  - open charm physics
  - . . .



- PWA activities focused on search for exotic particles
  - initial states limited to  $J^{PC}=1^-$  with helicities  $\lambda=\pm 1$
- Radiative decays from charmonia, especially from  $J/\psi$ 
  - gluon rich process



# $J/\psi \rightarrow \phi\phi\gamma$

- Glueballs decay flavor blind
  - strong coupling to  $\phi\phi$
  - one of the most promising channel:  $J/\psi \rightarrow \phi\phi\gamma \rightarrow (K^+K^-) (K^+K^-) \gamma$
- Lightest tensor glueball predicted between 2.0-2.4 GeV/c<sup>2</sup>
- Unexpected large cross sections of three  $f_2$  resonances in  $\pi^-p \rightarrow n\phi\phi$   
(*Atkin et. al.: Phys.Lett. B201 (1988) 568-572*)

## PWA Strategy

- Mass independent fits by scanning the invariant  $\phi\phi$  mass
  - identification of the strongest waves
- Mass dependent fits in the complete phase space using Breit-Wigner and Flatté parametrizations
- Helicity formalism
- First results very promising and good description of the data

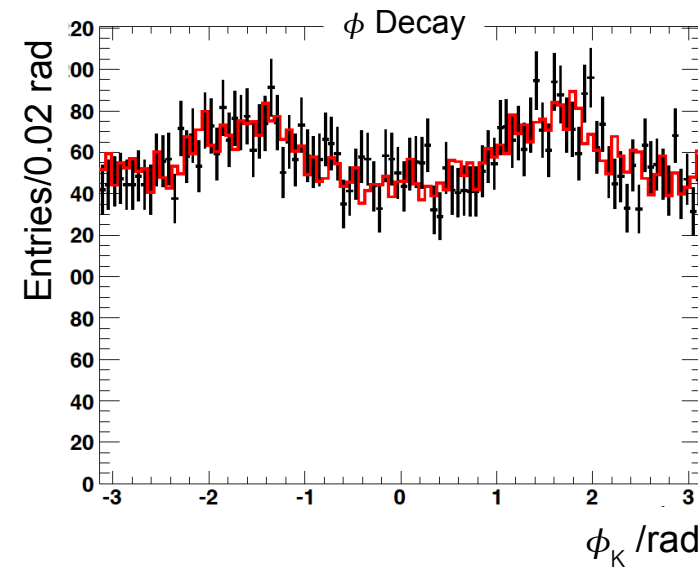
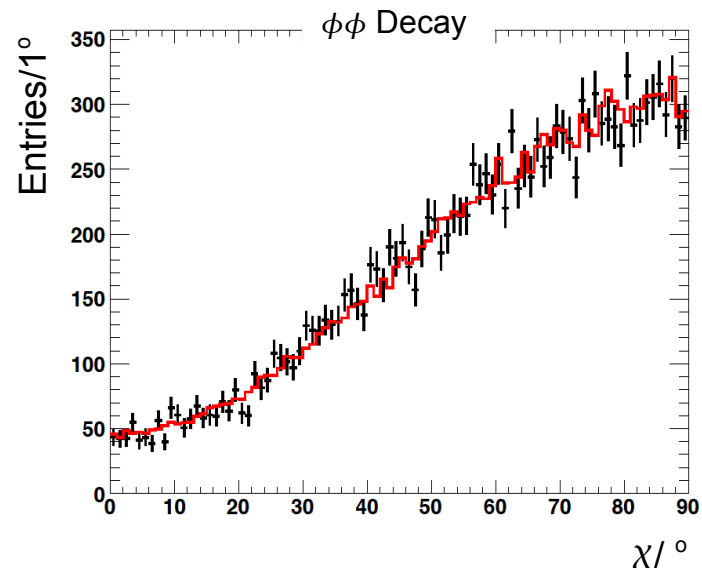
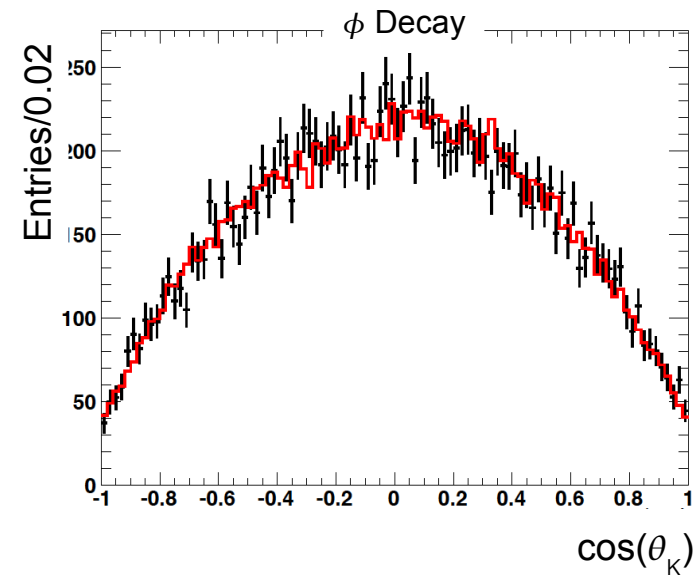
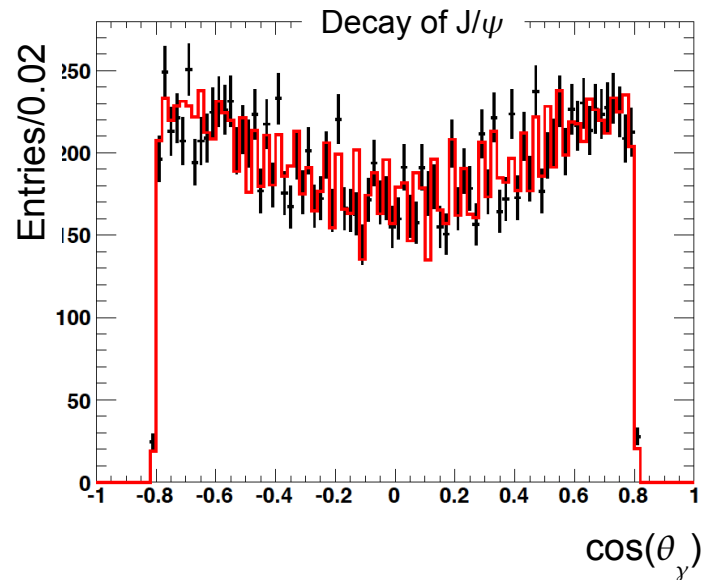
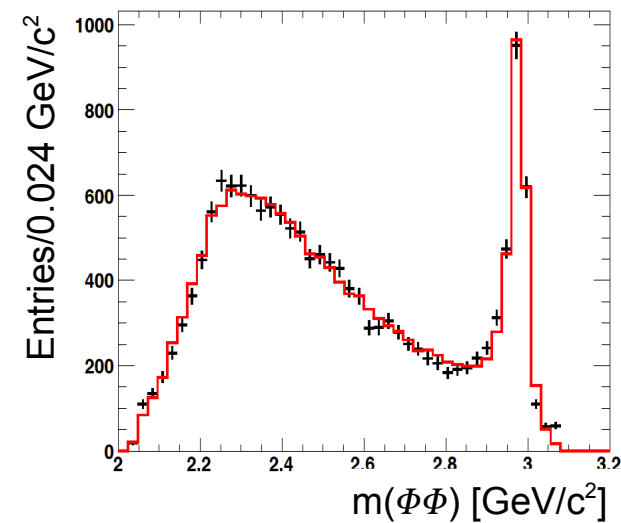
# $J/\psi \rightarrow \phi\phi\gamma$

P. Friedel, PhD thesis, Bochum

## Mass dependent fit

Data

weighted MC



# Summary

- New developed PWA software package is in a good shape and first analyses have been shown
- Analyses of Crystal Barrel @ LEAR data with relevance for PANDA
  - $\bar{p}p$  initial states and production of vector mesons
  - $\bar{p}p \rightarrow \omega\pi^0$ 
    - ➔ new background rejection method
    - ➔  $L_{\text{max}}$  rises from 3 @ 600 MeV/c to 5 @ 1940 MeV/c
    - ➔ extraction of the  $\omega$ -SDM via full PWA
    - ➔ strong alignment and oscillation of  $\rho_{00}$  along the production angle
  - $\bar{p}p \rightarrow K^+K^-\pi^0$ 
    - ➔ excellent description of the data
    - ➔ extraction of the SDM for  $\phi$  and  $K^*$  possible
- PWA of BESIII data with the same PWA package
  - focus on radiative decays of charmonia
  - first promising results achieved