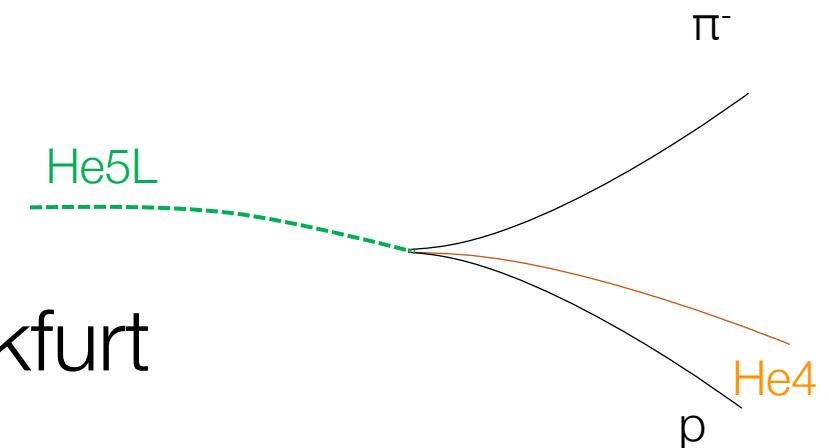


Hypernuclei reconstruction with CBM

Susanne Gläßel, IKF Frankfurt

Sept 26th 2024, FAIRNess, Croatia



Agenda

Hypernuclei 3-body-decay

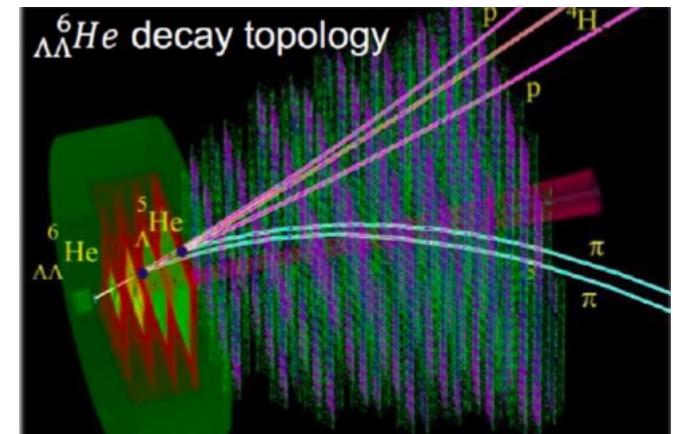
with ${}^3_{\Lambda}\text{H}$ 3-body decay as test bed for the ${}^6_{\Lambda\Lambda}\text{He}$ decay.



1) ${}^3_{\Lambda}\text{H}$ reconstruction: Systematic error estimation for

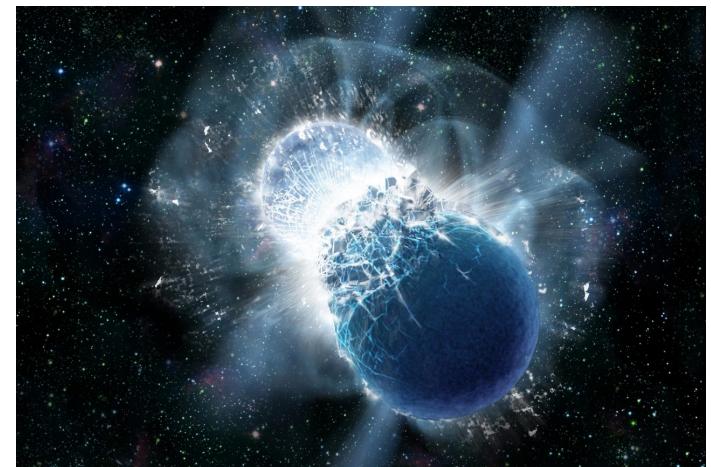
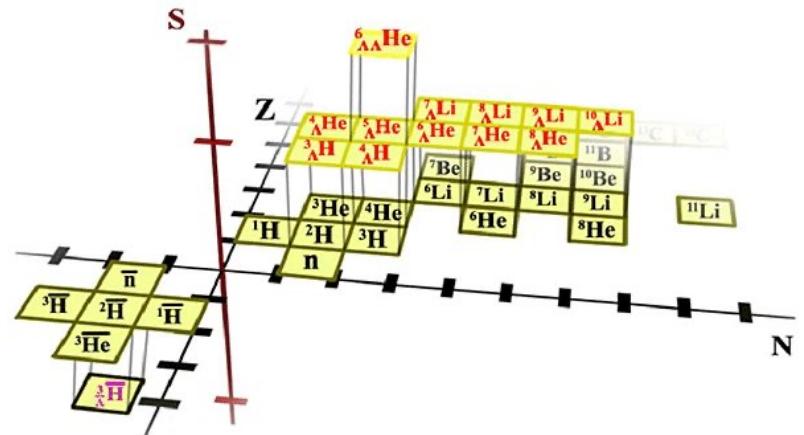
- y-spectra
- lifetime measurement

2) ${}^5_{\Lambda}\text{He}$ reconstruction: Improvement with Trd-dE/dx



Hypernuclei physics

- ★ Properties of hypernuclei: lifetime, binding energy
“Hypertriton lifetetime puzzle”
- ★ Hyperon-Nucleon(YN)- /Hyperon-Hyperon(YY) interactions “hyperon puzzle”
- ★ Equation of state of hadronic matter at high density and low temperature
→ inner structure of neutron stars
- ★ Production mechanism of hypernuclei
 - Thermal model: multiplicities \leftrightarrow masses, T , μ_B at chemical freezeout
 - Cohesion model: multiplicities \leftrightarrow phase-space-distribution of baryons at kinetic freezeout (coalescence radius)
 - Dynamical model: PHQMD



Hyperon puzzle

Mass-radius relation for neutron stars: Depends on EOS of dense nuclear matter

Constraints from observation of $M_{NS} \approx 2 M_\odot$

Hyperons should appear when density increases

\Rightarrow EOS softens with hyperon matter

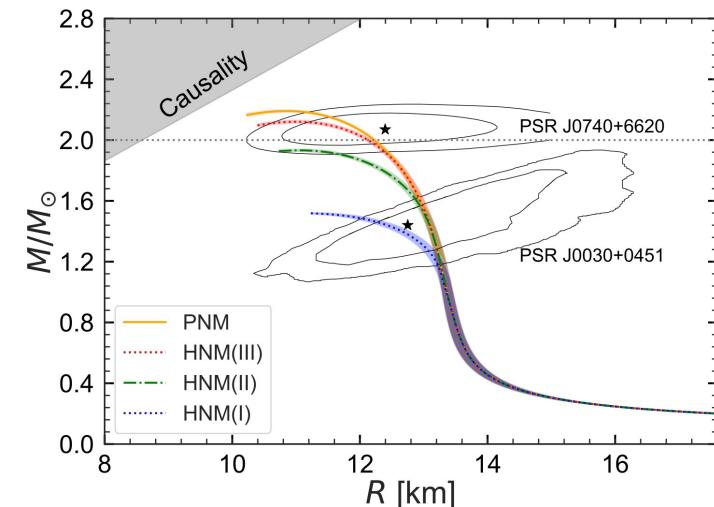
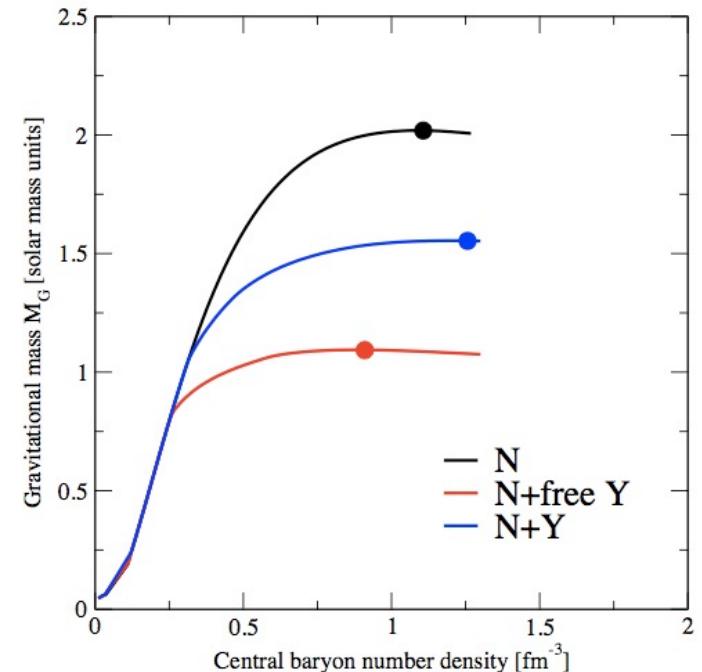
$\Rightarrow 2 M_\odot$ cannot be reached

YN and YY interaction

- Repulsive YN and YY interactions \Rightarrow stiffer EOS

- 3-body forces between Ys to be studied

\Rightarrow Important input from hypernuclei measurements



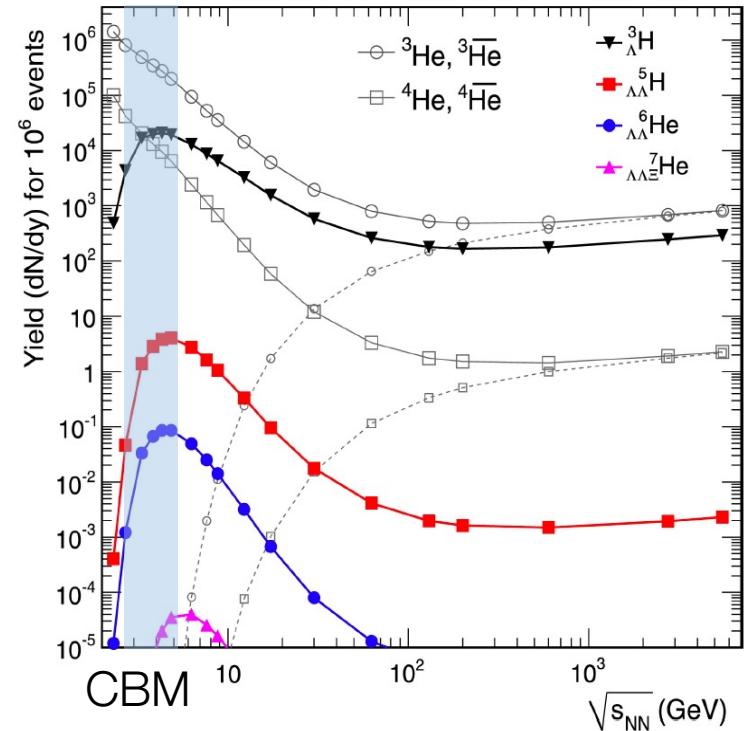
Hypernuclei physics with CBM

CBM

Maximum in the production of hypernuclei

- ★ Relatively low beam energies at FAIR & high interaction rates
- ★ CBM detector design: clean identification

- precise measurement of hypernuclei lifetime, branching ratios of decays, binding energy B_Λ , spectra and flow
- sufficient statistics for double hypernuclei, e.g. $\Lambda^6\text{He}$
expected rates: $\sim 10^{-6}/\text{evt.} - \sim 10^{-11}/\text{evt.}$ in CBM range
- Search for the new hyper-nucleus or charmed nucleus ${}^4_D\text{He}$



Parton-Hadron-Quantum-Molecular Dynamics

= n-body microscopic transport approach for the description of heavy-ion dynamics with dynamical cluster formation

PHSD



+ QMD

+ MST

Relativistic considerations

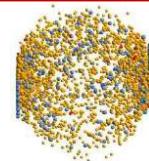
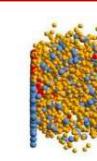
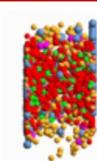
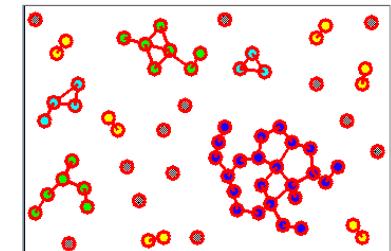
but: mean-field potentials
=> correlations are smeared out

Correlations between baryons

n-body transport approach
=> formation of clusters due to potential interactions

Cluster recognition

search for accumulations of particles in coordinate space



QMD Initialization nuclei

propagation of baryons



local $\epsilon > \epsilon_c$: dissolution of pre-hadrons

propagation of partons

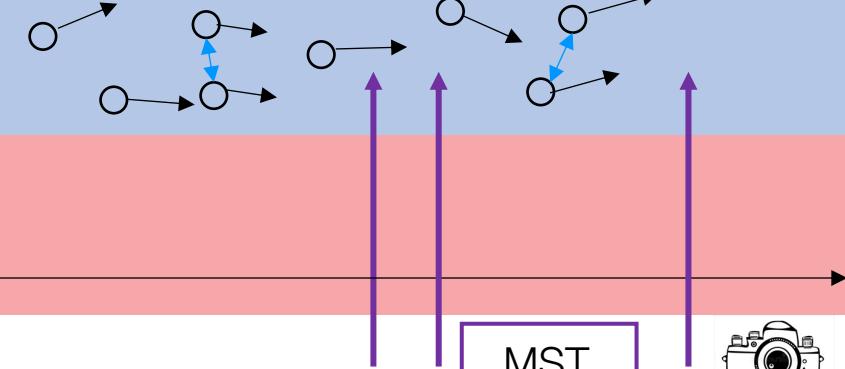
interactions of partons

interactions of hadrons

propagation of mesons



→



MST



Hypertriton

Loosely bound object

Λ binding energy: $B_\Lambda \approx 400$ keV
(compare $B_d = 2.2$ MeV)

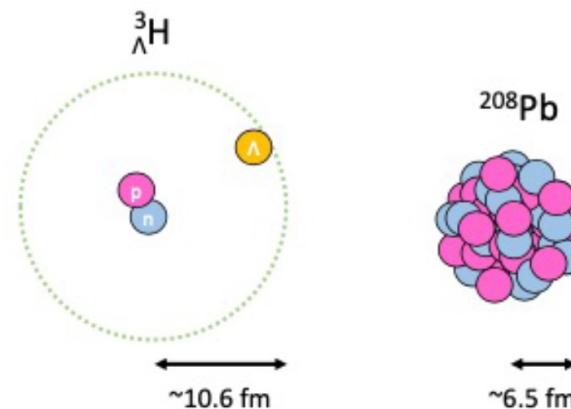
Wavefunction is larger than Pb-nucleus

Hypertriton lifetime “puzzle”

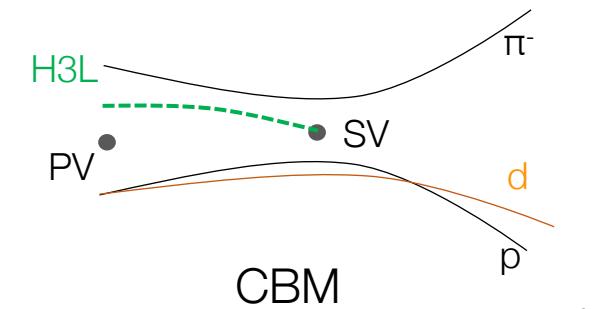
- Lifetime smaller than the one of free Λ ?
- Life-time particularly sensitive to YN interaction.

Decay modes:

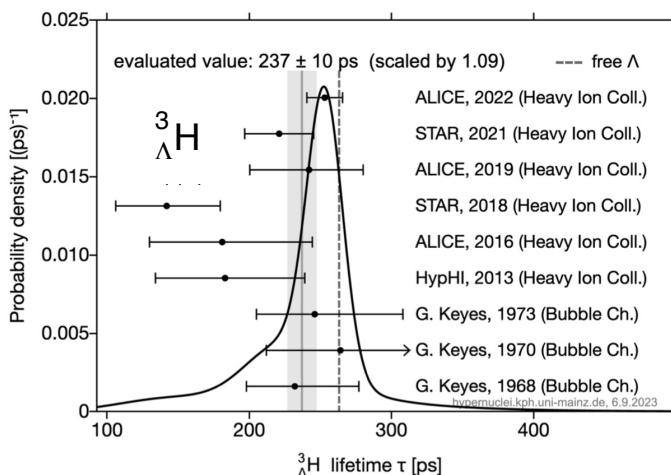
$$\begin{aligned} {}^3_{\Lambda}\text{H} &\rightarrow {}^3\text{He} + \pi^-, {}^3_{\Lambda}\text{H} \rightarrow {}^3\text{H} + \pi^0 \\ {}^3_{\Lambda}\text{H} &\rightarrow d + p + \pi^-, {}^3_{\Lambda}\text{H} \rightarrow d + n + \pi^0 \end{aligned}$$



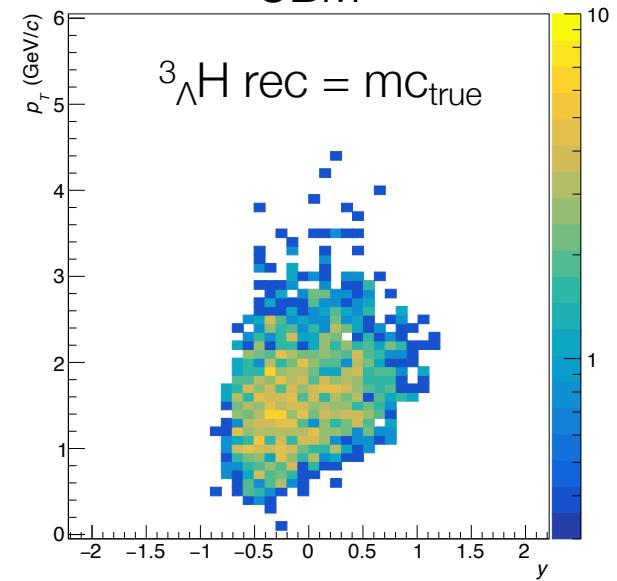
Reconstruction of 3-body-decay
1) reconstruct mother from π^- & p
2) Add d at SV of π^- & p



Worldwide lifetime measurements



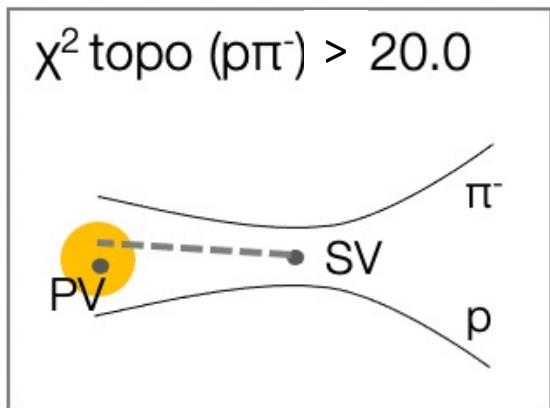
<https://hypernuclei.kph.uni-mainz.de>



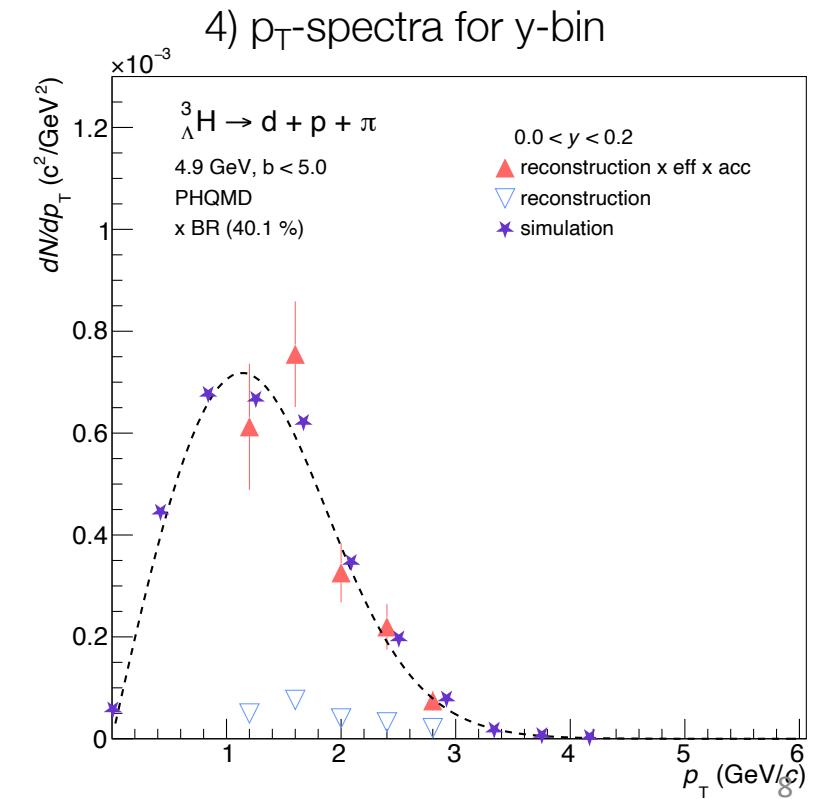
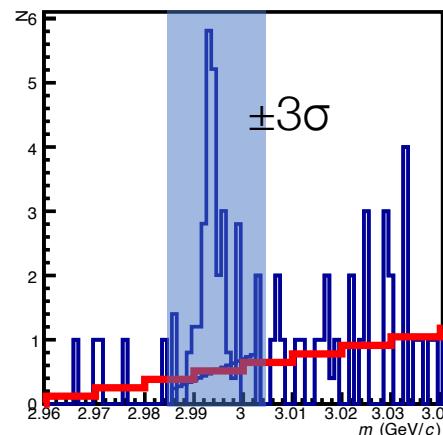
Systematic error estimation for different simulation & reconstruction steps

- 1) different simulation input with different y - & p_T -distributions 
- 2) different cut sets for reconstruction
- 3) different invariant mass-cuts (2, 3 & 4 σ) 
- 4) different input for efficiency correction 
- 5) different fits for p_T -spectra to extrapolate to unmeasured regions

2) Cut variation (e.g.)

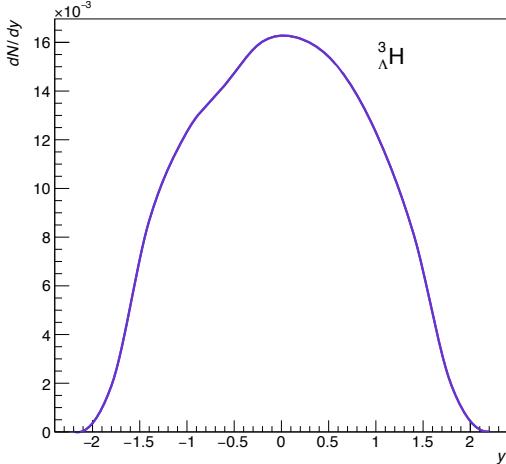


3) Mass spectrum for p_T -y-bin



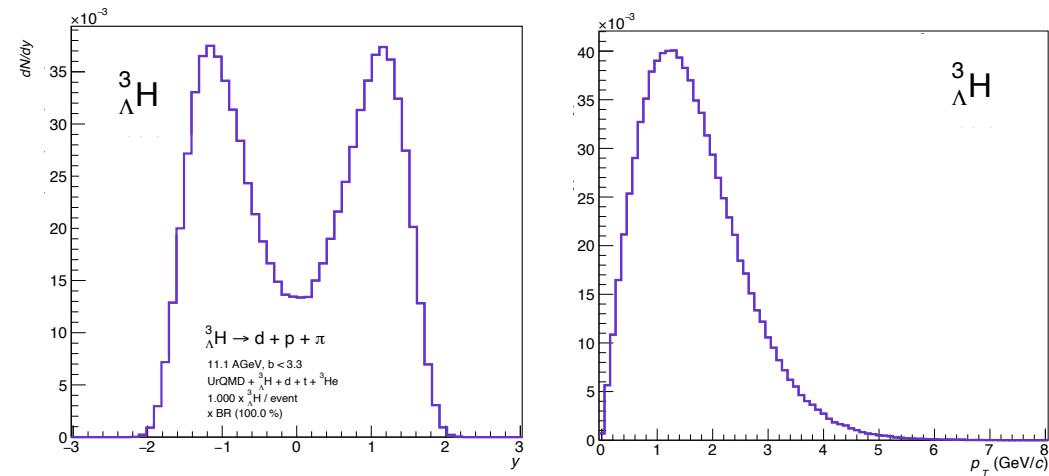
Simulated datasets: different y - & p_T -distributions

PHQMD (0.0427 $^3\Lambda$ H/event)

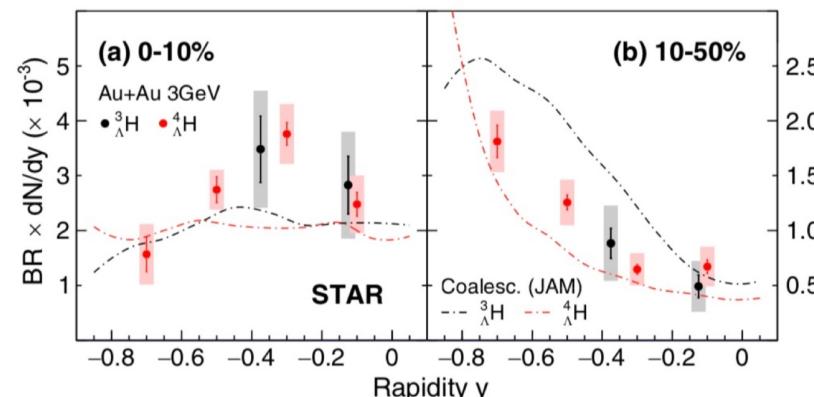


thermal signal (0.087 $^3\Lambda$ H/event) + UrQMD + d, t, 3 He

p_T - & y -distribution**: Experimental nuclei-shape from E864-data***



Shape of $^3\Lambda$ H rapidity distribution is not 100% known yet.



=> Different distributions relevant for detector efficiencies.

=> Used for systematic error estimation of lifetime measurement.

Extrapolation of p_T -spectra to unmeasured regions

Fit p_T -spectra with:

1) Blast-Wave model fits*

$$\frac{1}{2\pi p_T} \frac{d^2N}{dp_T dy} \propto \int_0^R r dr m_T I_0\left(\frac{p_T \sinh \rho}{T}\right) \times K_1\left(\frac{m_T \cosh \rho}{T}\right)$$

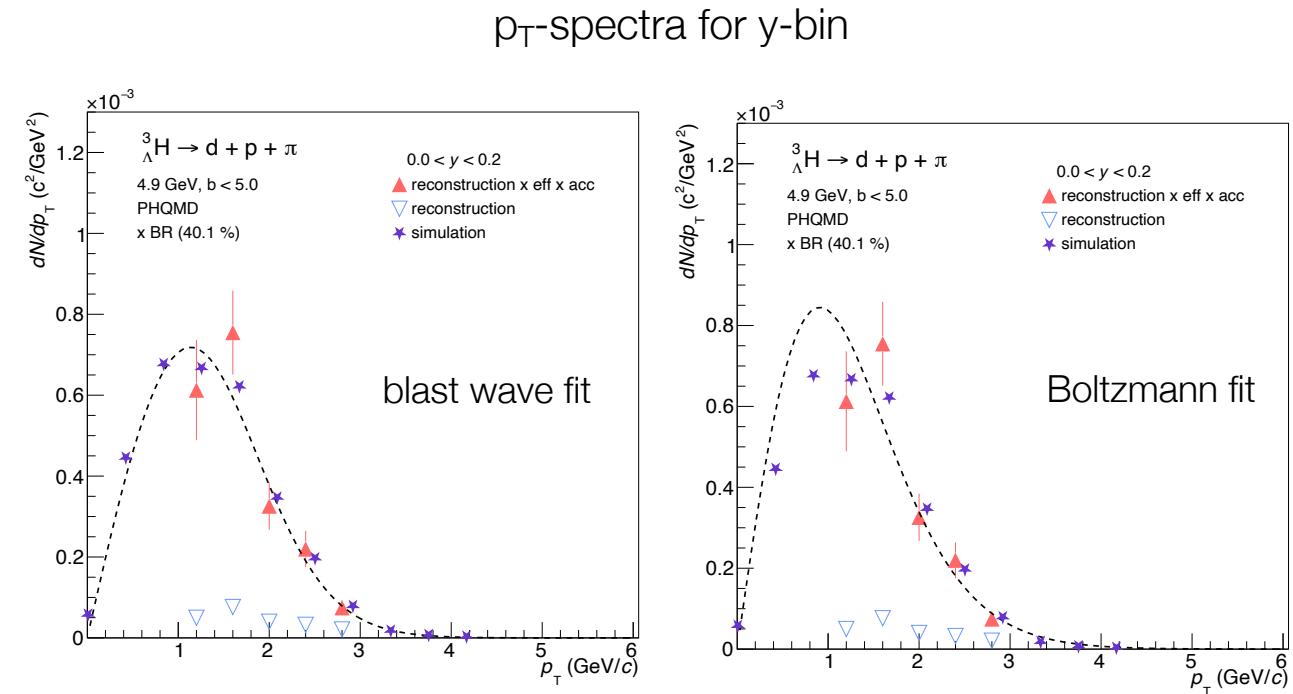
Parameters:

$\langle \beta \rangle$: transverse expansion velocity (linear velocity profile)

T: kinetic freeze-out temperature

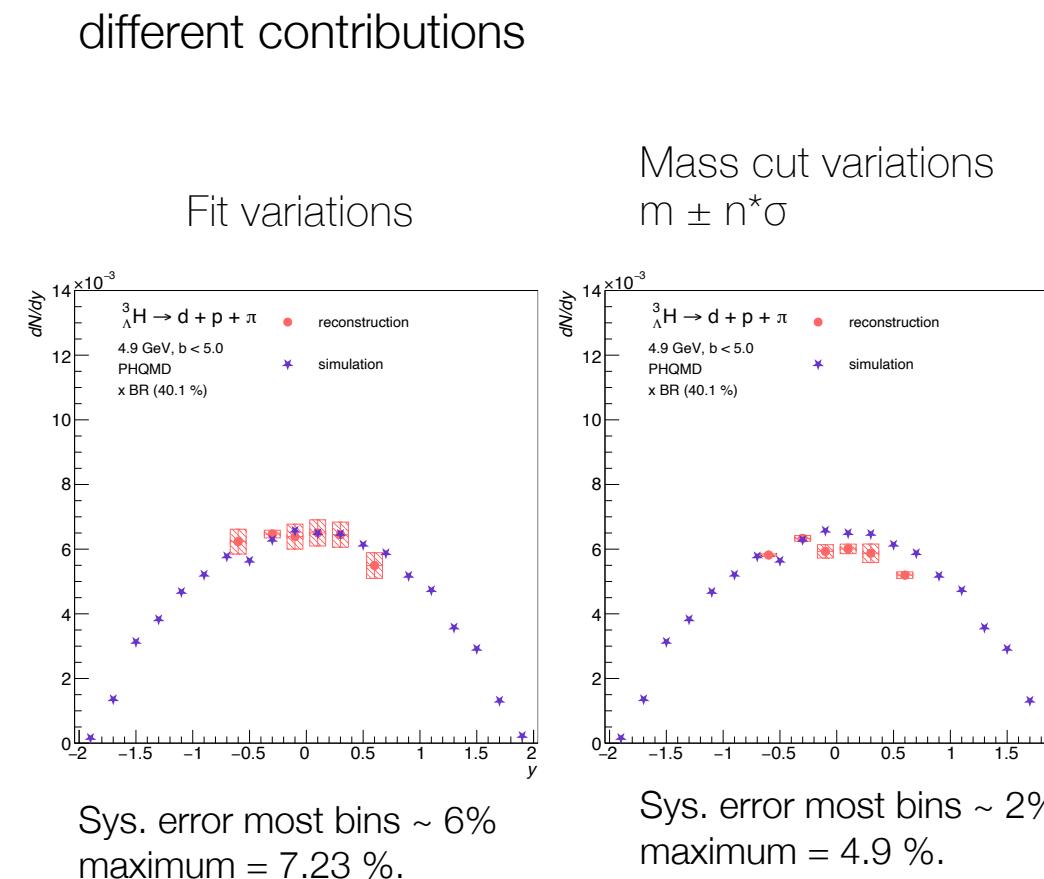
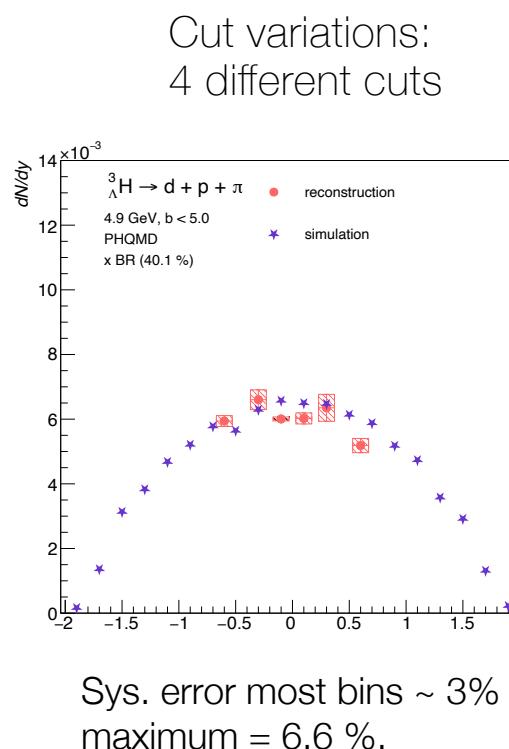
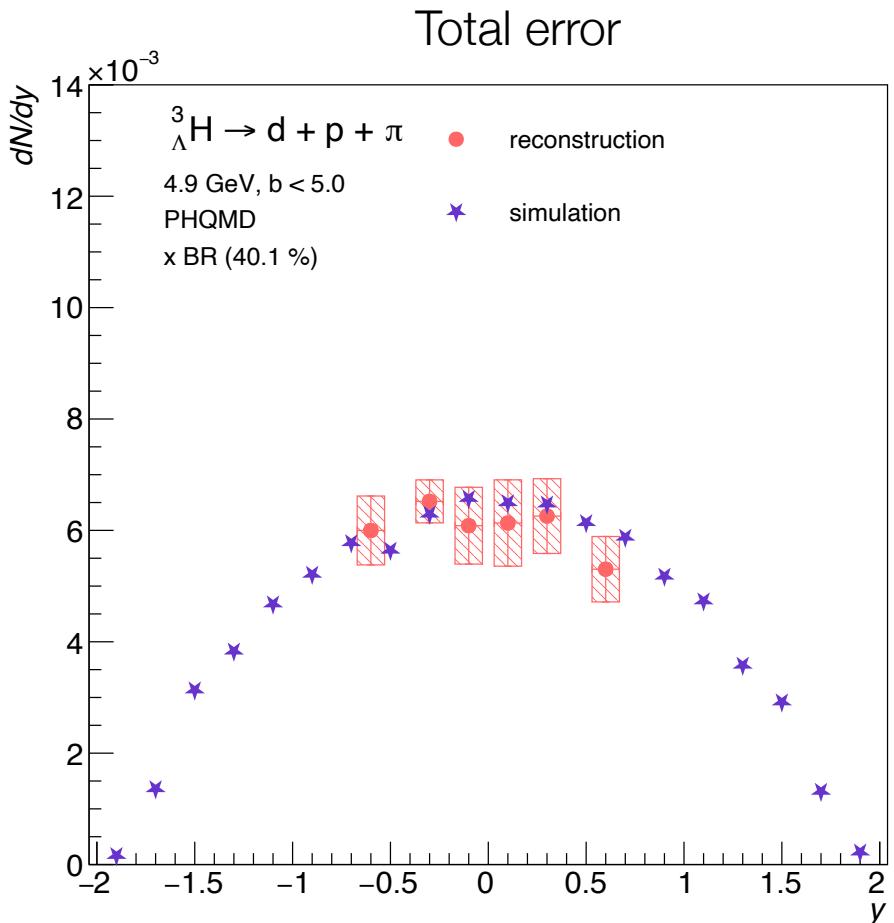
2) Boltzmann fits

$$\frac{dN}{dp_T} \sim m_T \cdot e^{-\frac{m_T}{T}}$$



*E. Schnedermann, J. Sollfrank, and U. Heinz, Phys. Rev. C 48, 2462 (1993).

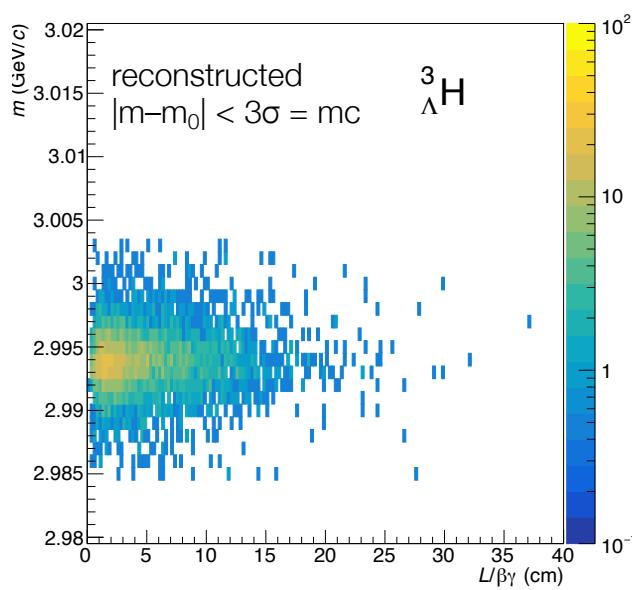
Systematic error for ${}^3_{\Lambda}\text{H}$ γ -spectra



Main contribution to systematic error comes from fit variations.

Lifetime measurement of ${}^3\Lambda$ H with CBM

decay length L
after Lorentz-boost

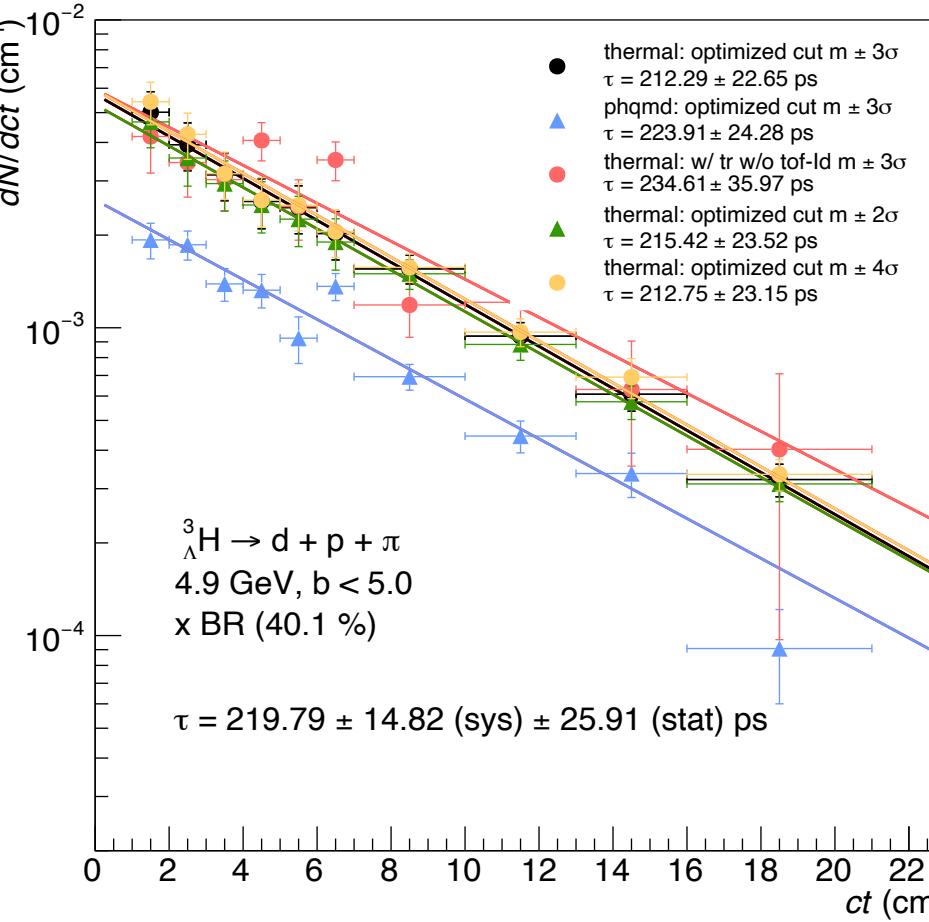


Fit dN/dct vs. ct with
exponential decay law:

$$\frac{dN}{dct} = C \cdot e^{-ct \cdot \frac{1}{\tau}}$$

$$\text{where } \frac{L}{\beta\gamma} = ct$$

Efficiency corrected decay-length distributions
after background subtraction for different variations



- Statistical error is 11.7 % for 1 million events only.
- Estimated uncertainty the first year of data taking is $\sigma_{\text{stat}} = \pm 0.17 \text{ ps}$.
- Total systematic error is 6.7 %.
- Lifetime is slightly underestimated.
 - > Reason might be: low efficiencies for particles with longer lifetime & decaylength -> stronger bending in magnetic field.
 - > Explore improvement by removing bins for longer lifetime from fit.

Reconstruction of ${}^5_{\Lambda}\text{He}$

- important also for the reconstruction the of ${}^6_{\Lambda\Lambda}\text{He}$ decay



- low multiplicities 0.003 ${}^5_{\Lambda}\text{He}$ / event

using PHQMD events is not possible (very high statistics needed)

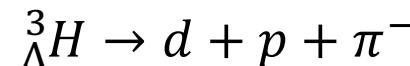
→ embed thermal signal into UrQMD event + d + t + ${}^3\text{He}$

& mix signal-events with bg-events

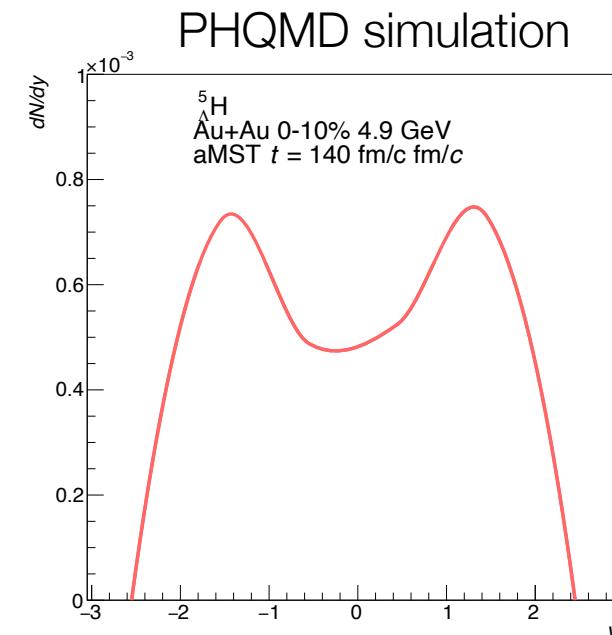
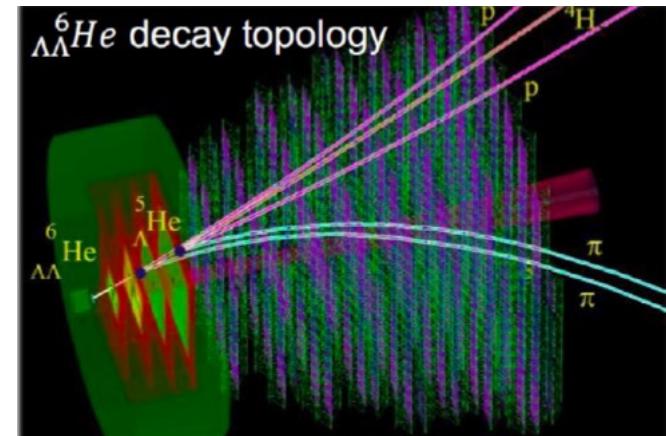
- separation of d & ${}^4\text{He}$ is very important to separate



&



→ use of Trd-dE/dx (PidTrd-software)

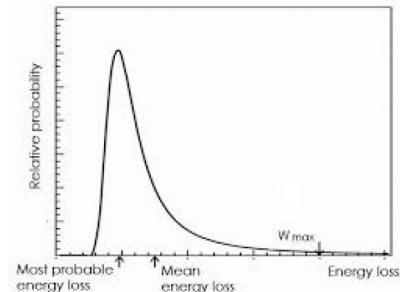


PID with TRD-dE/dx

TRD: Specific energy loss for every particle specie depending on momentum (Bethe-Bloch)

Calculation of $\langle dE/dx \rangle$ over 4 TRD-detector layers:

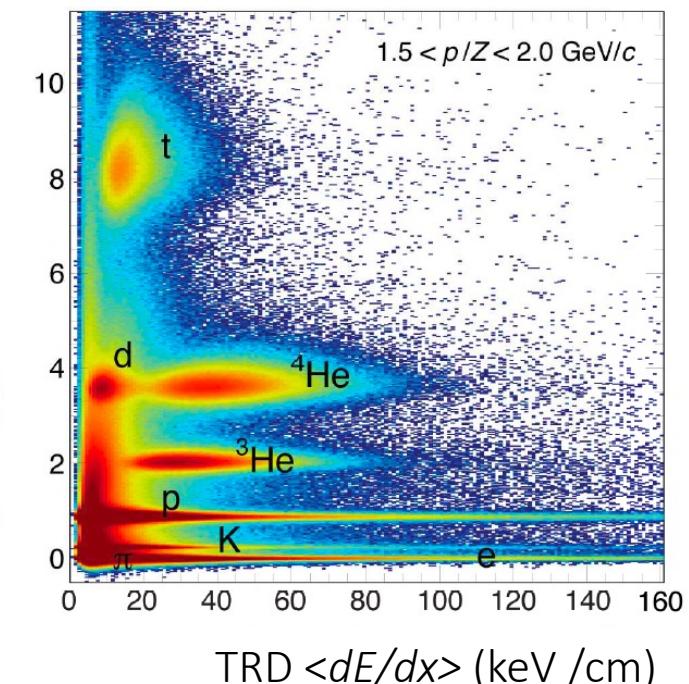
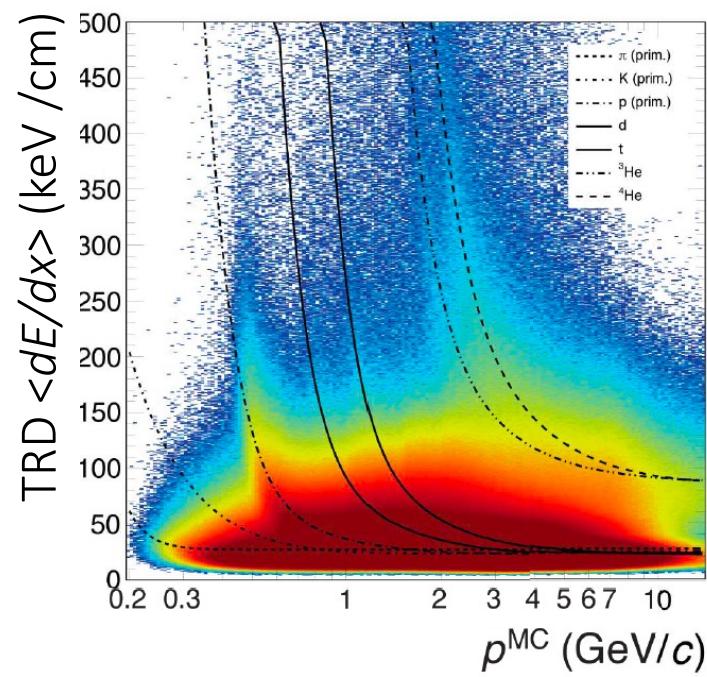
Truncation: reduce Landau-fluctuations => select 2 hits with smallest dE/dx



1) Separation of d & ${}^4\text{He}$

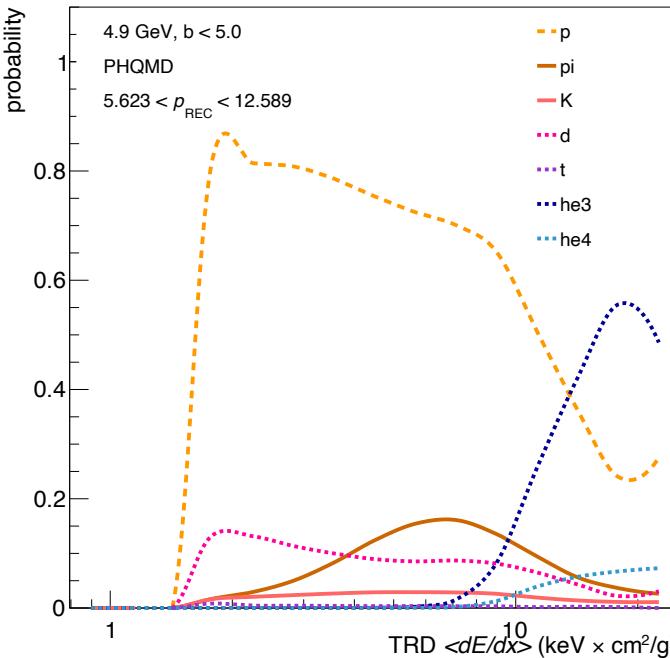
- o can not be separated with TOF alone (similar m/q)
- o important for reconstruction of $\Lambda^6\text{He}$ decay chain => very rare signal

2) Pid for hadrons: Increase efficiency or s/b

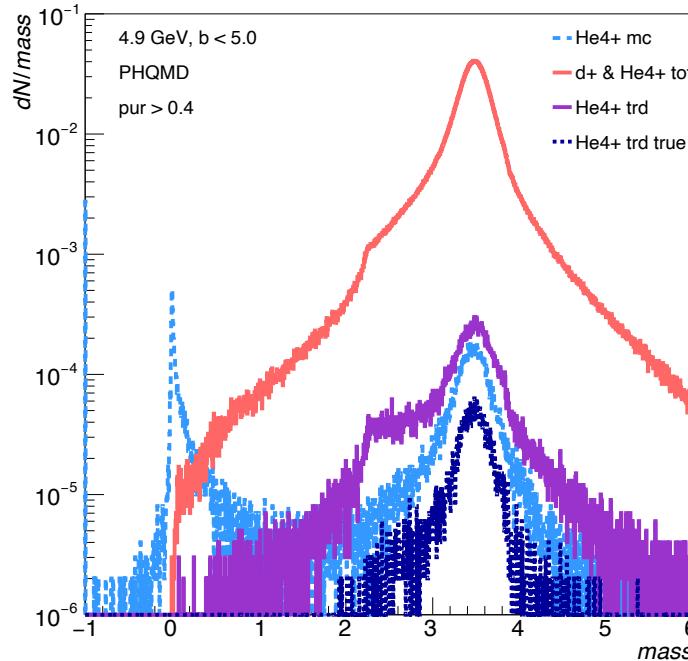


Separation of d & ^4He with TRD-dE/dx

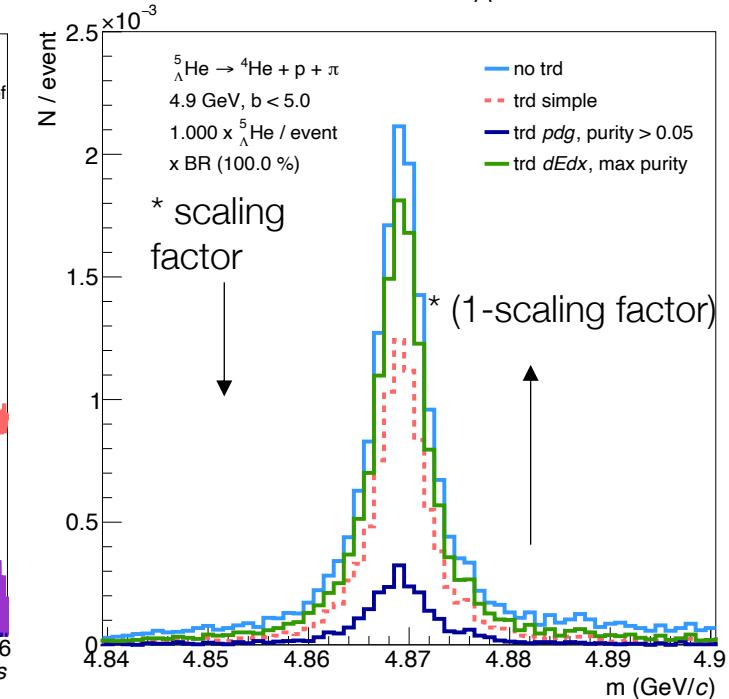
Track probability for particle species



^4He Mass spectrum w/ and w/o Trd



Reconstructed ^5He



⇒ Background can be suppressed with TRD (different settings for TRD cut possible).

! Results are for 1 ${}^5\text{He}$ / event. ! For scaling with bg-events more statistic is needed.

Scaling factor: ${}^5\text{He} / \text{event} \times \text{br} = 0.03 \times 0.323 = 10^{-4}$

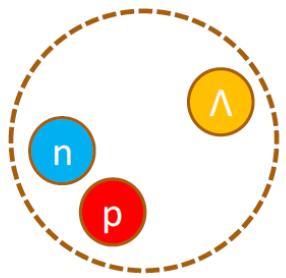
⇒ Strong background suppression is needed.

Summary & Conclusion

- Systematic error of ${}^3_{\Lambda}\text{H}$ γ -spectra could be estimated to ~10% for PHQMD dataset.
- Systematic error of ${}^3_{\Lambda}\text{H}$ lifetime measurement could be estimated to 6.7 %, lifetime is slightly underestimated.
- Reconstruction of ${}^5_{\Lambda}\text{He}$ can be improved with Trd-dE/dx.

Next steps:

- Improve procedure to estimate systematic uncertainties by using different datasets for efficiency estimation.
- Improve estimation of lifetime value (e.g. remove particles with long lifetimes that might not reach detector).
- Realistic ${}^5_{\Lambda}\text{He}$ reconstruction with scaled background – high statistics needed.



THANK YOU.

BACKUP

Minimum Spanning Tree (MST)

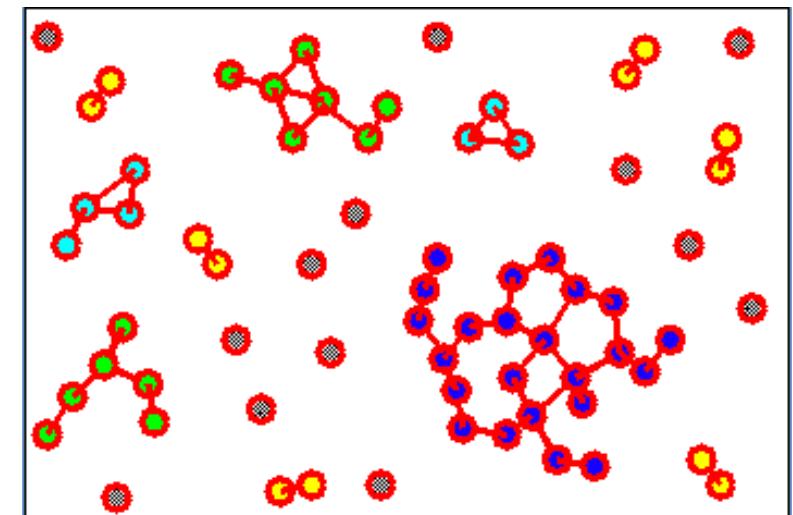
Cluster criterion: distance of nuclei

Algorithm: search for accumulations of particles in coordinate space

1. Two particles i & j are bound if:

$$|r_i - r_j| < 4.0 \text{ fm}$$

2. Particle is bound to cluster if bound with at least one particle of cluster



Remark: additional momentum cuts lead to a small changes: particles with large relative momentum are mostly not at the same position (V. Kireyeu, Phys.Rev.C 103 (2021) 5)

Reconstruction of rapidity spectrum

1. Mass spectra in y - p_T -bins: Calculation of dN/dp_T

- N_{rec} : Integration for $|m - m_0| < 3\sigma$
- Subtraction of background with linear fit
- Corrected for efficiency \times acceptance in y - p_T -bin

$$\frac{dN}{dp_T} = \frac{N_{\text{rec}} - \text{bg}}{\text{eff} \cdot \text{acc} \cdot dp_T \cdot \text{nevents}}$$

2. p_T -spectra in y -bins: Calculation of dN/dy

- Sum over dN/p_T for reconstructed points
- Extrapolation to unmeasured regions with Blast-Wave model fits*

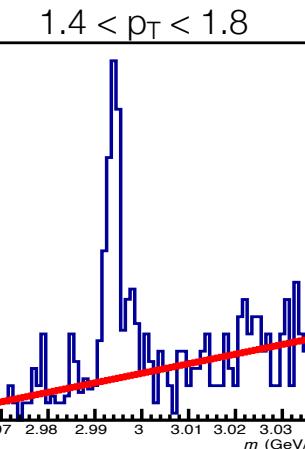
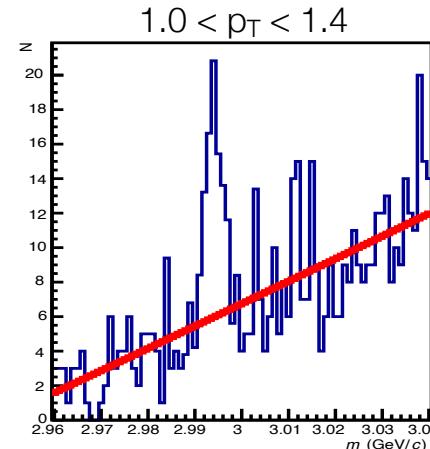
$$\frac{1}{2\pi p_T} \frac{d^2N}{dp_T dy} \propto \int_0^R r dr m_T I_0\left(\frac{p_T \sinh \rho}{T}\right) \times K_1\left(\frac{m_T \cosh \rho}{T}\right)$$

Parameters:

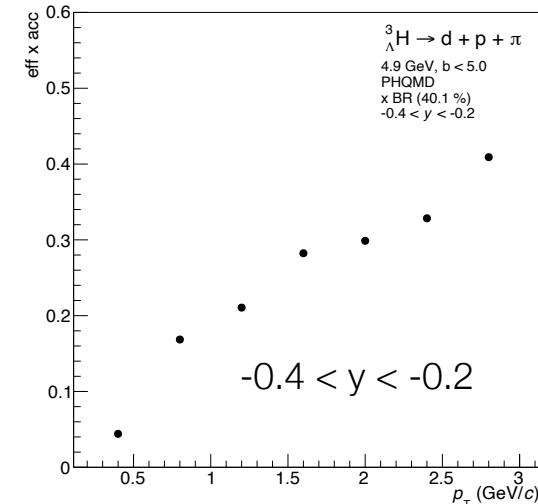
$\langle \beta \rangle$: transverse expansion velocity (linear velocity profile)

T: kinetic freeze-out temperature

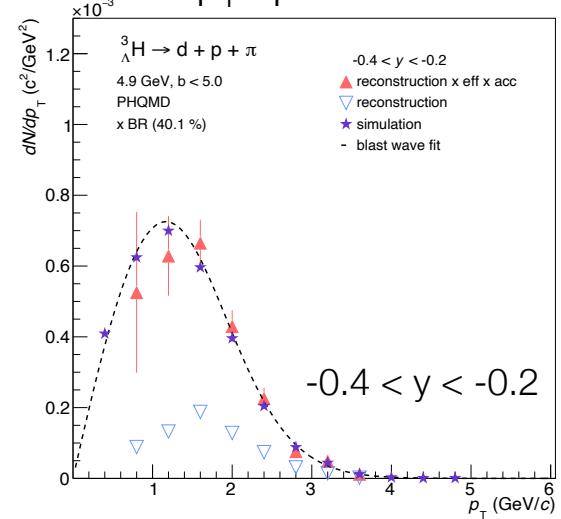
Mass spectra $-0.4 < y < -0.2$



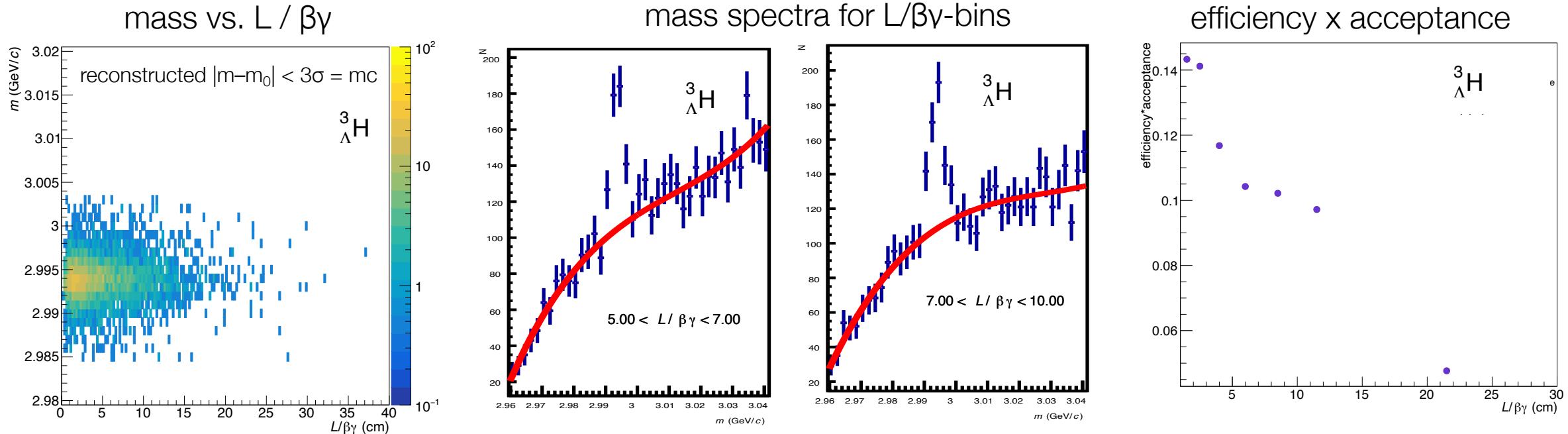
efficiency \times acceptance



p_T -spectrum



Lifetime measurement of ${}^3\Lambda$ H with CBM



1. decay length $L \rightarrow$ after Lorentz-boost $\frac{L}{\beta\gamma}$
2. mass projections in $\frac{L}{\beta\gamma}$ -bins: calculation of $dN/d\left(\frac{L}{\beta\gamma}\right)$
 - Sum up signal in 3σ -mass-window
 - Fit background with polynomial function
 - Scale with efficiency

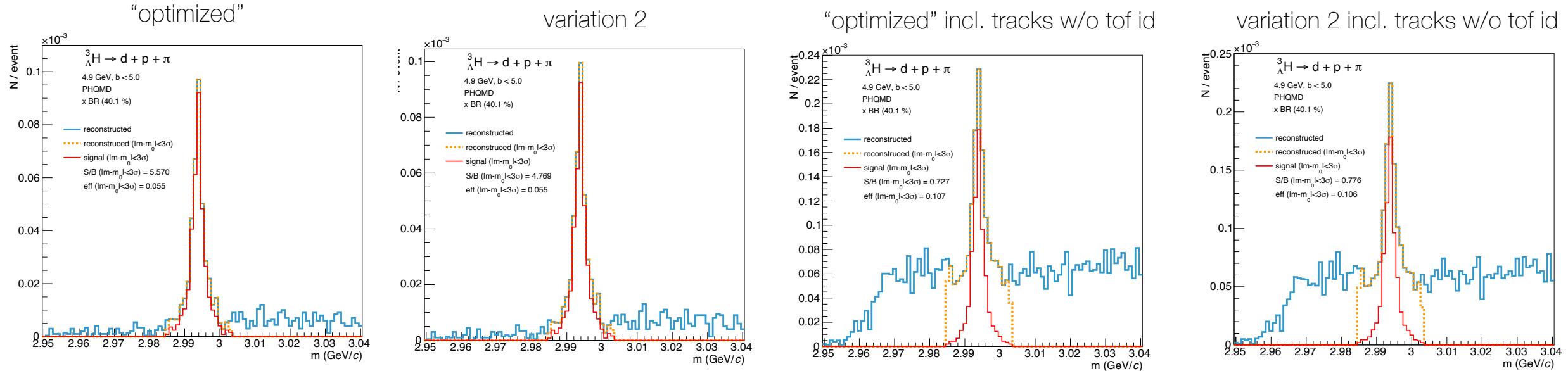
Reconstructed hypertritons in $\frac{L}{\beta\gamma}$ -bin:

$$\frac{dN}{d\left(\frac{L}{\beta\gamma}\right)} = \frac{N_{\text{rec}} - \text{bg}}{d\left(\frac{L}{\beta\gamma}\right) \cdot \text{eff} \cdot \text{nevents}}$$

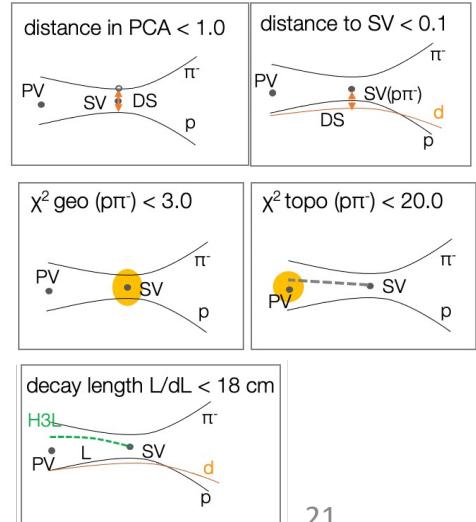
with efficiency:

$$\text{eff}\left(\frac{L}{\beta\gamma}\right) = \frac{N_{\text{mc}}\left(\frac{L}{\beta\gamma}\right)}{N_{\text{sim}}^{\text{tot}} \cdot e^{-\Delta \frac{L}{\beta\gamma} \cdot \frac{1}{c\tau}}}$$

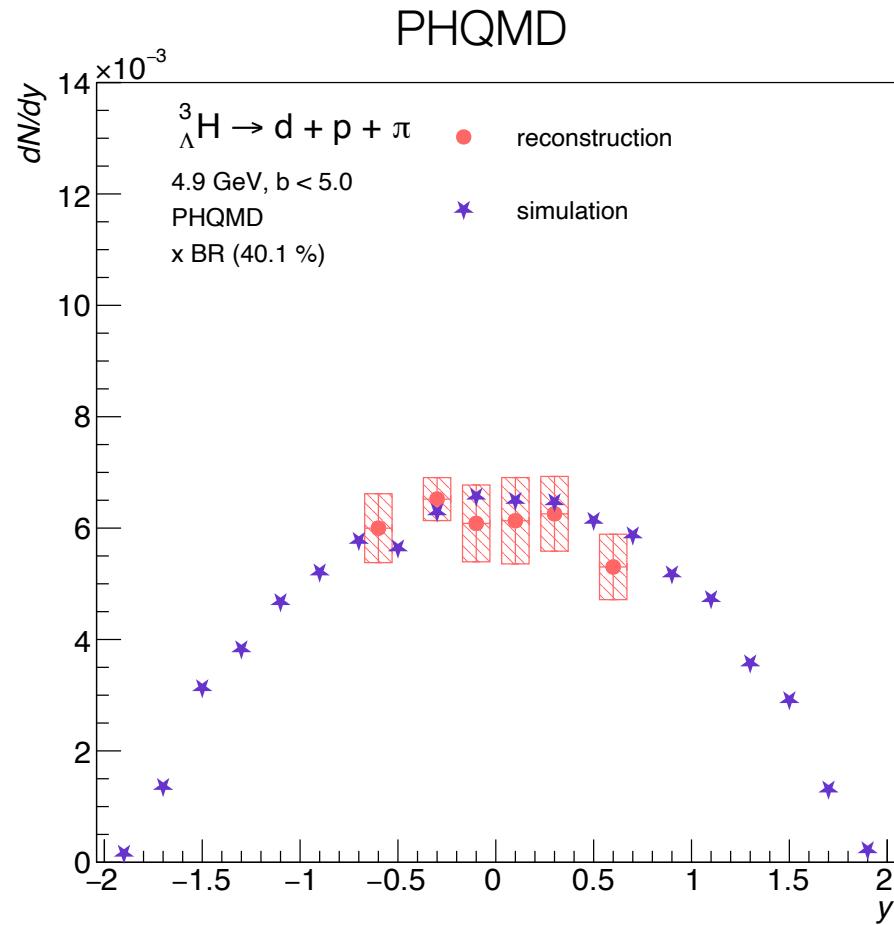
Cut selection for systematic error estimation



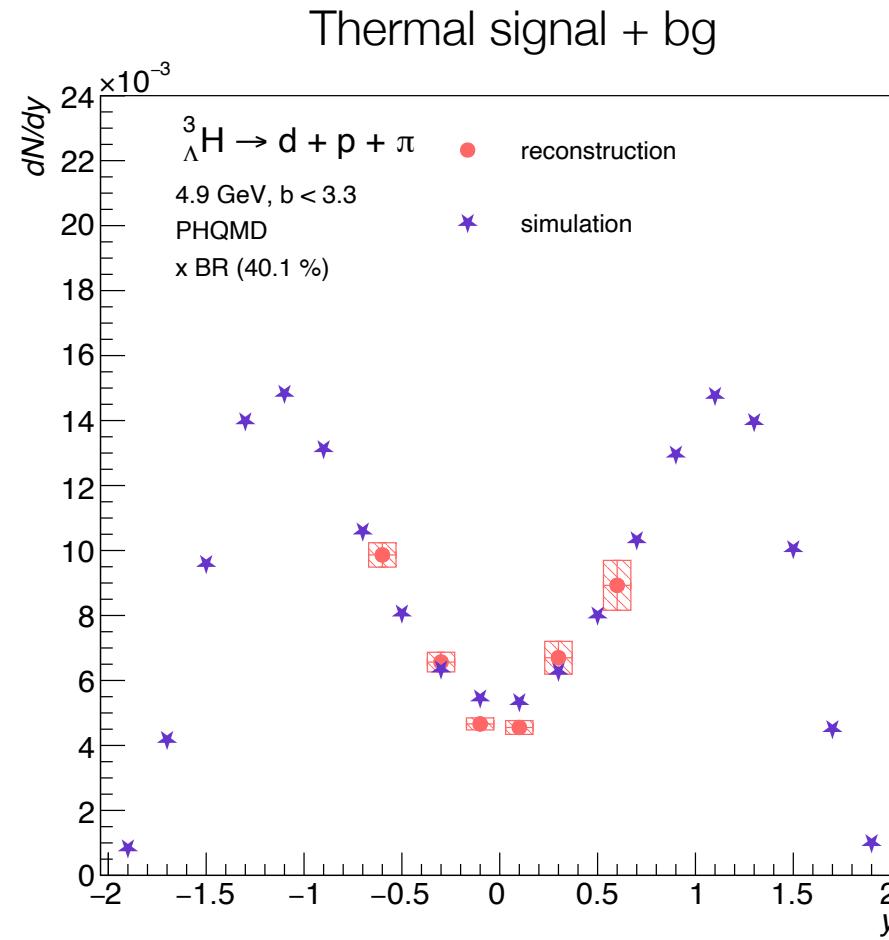
	"optimized"	variation 2	"optimized" w/ tr w/o tof id	variation 2 w/ tr w/o tof id
χ^2 to PV p/ π /d	40/90/10	40/90/10	40/90/10	40/90/10
distance p & π	1.0	1.0	1.0	1.0
distance d to SV	0.1	0.1	0.1	0.1
χ^2 geo p- π -mother	3.0	3.0	3.0	3.0
χ^2 topo p- π -mother	20.0	5.0	20.0	5.0
decaylength L/dL	18.0	18.0	18.0	18.0
efficiency	0.055	0.055	0.107	0.106
s/b ratio	5.570	4.769	0.727	0.776



Total systematic error for ${}^3_{\Lambda}\text{H}$ γ -spectra



Systematic error most bins $\sim 10\%$
maximum = 12.6 %.

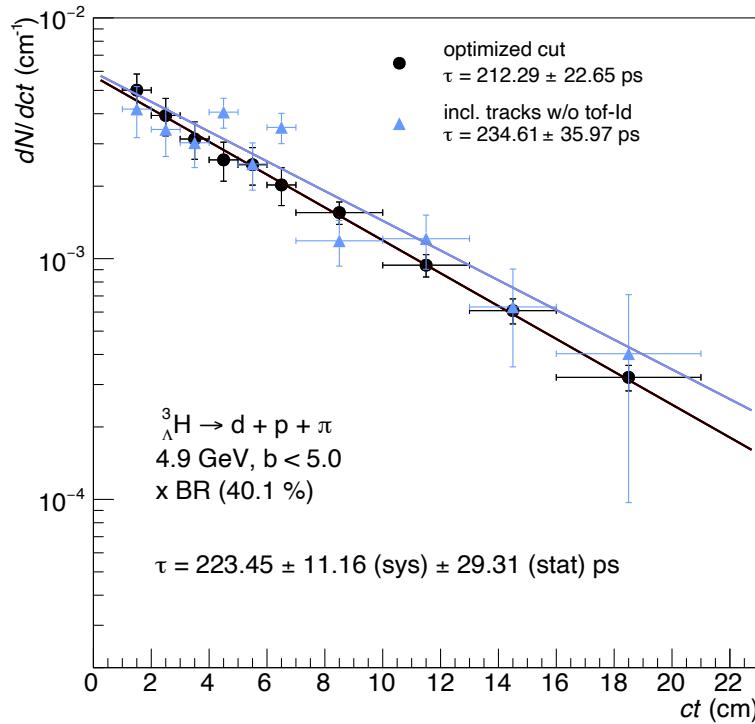


Systematic error most bins $\sim 4\%$
maximum = 8.6 %.

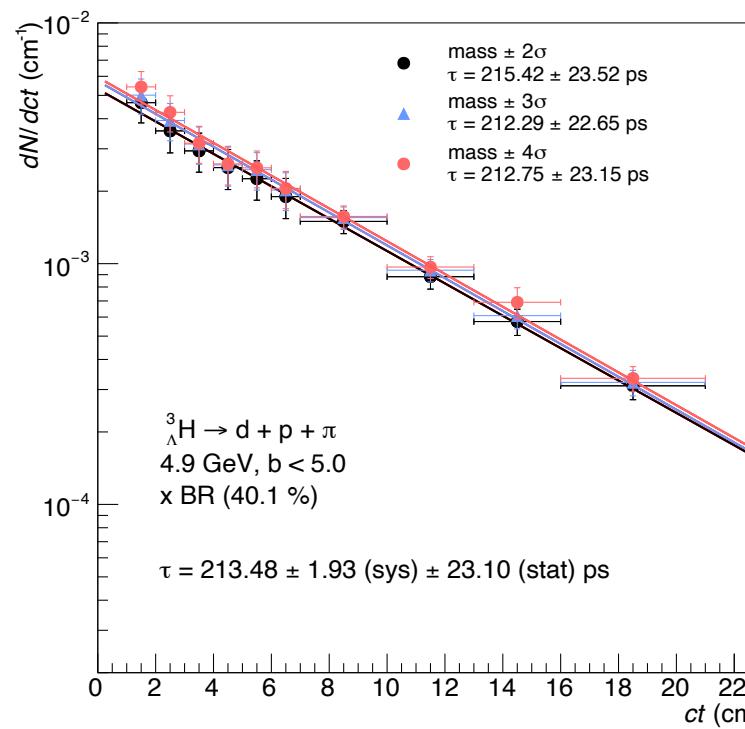
Lifetime measurement systematic error: different contributions

Examps:

Cut variations
for thermal signal + bg



Mass cut variations ($m \pm n^*\sigma$)
for thermal signal + bg



Thermal + phqmd
for optimized cut

