



# Luminosity detector software

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on behalf of the luminosity detector group

September 11, 2012



- 1 Introduction
- 2 Reconstruction chain
- 3 Background studies
- 4 Software alignment

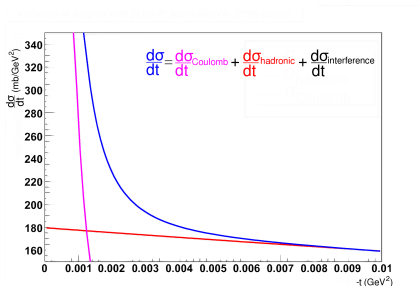


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## $p\bar{p}$ elastic scattering

- coulomb part: can be calculated from QED
- hadronic part: measurement + models



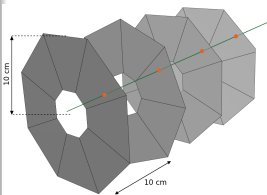
measurement at small momentum transfer

$$t = 2p_{CM}^2(1 - \cos\theta_{cm}) \rightarrow \text{small } \theta$$

- measurement at small  $\theta$  (3-8 mrad)
- position downstream from IP ( $\sim 11$  m)
- placed inside vacuum to minimize  $\bar{p}$  scattering

## Original design

- 4 silicon planes
- distance between planes 10 cm
- each plane contains 8 double sided strip sensors (thickness 150-300  $\mu\text{m}$ )
- strips with 50  $\mu\text{m}$  pitch and 45° stereo angle



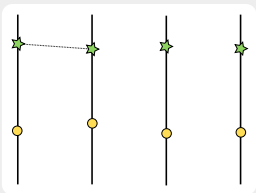


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# Track search



## Track-Following



- build combinations between 1st and 2nd planes
- look for hits on 3rd plane inside corridor

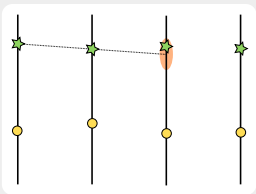
## Cellular Automata

- build combinations between hits on pairs of planes (**cells**)
- search for neighboring **cells**
- *missing plane* track search automatically included

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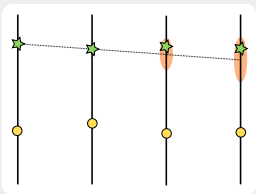
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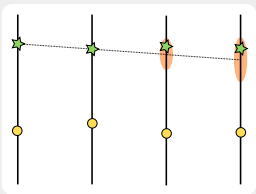
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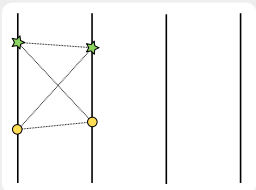


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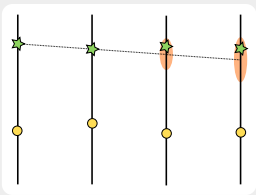


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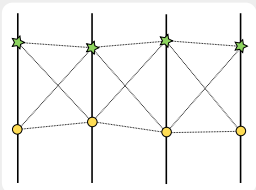


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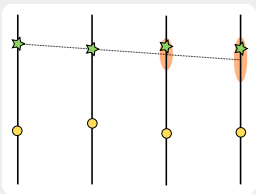


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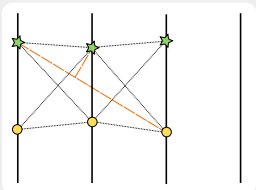


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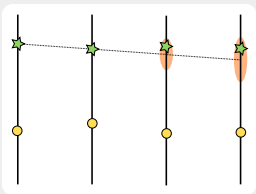


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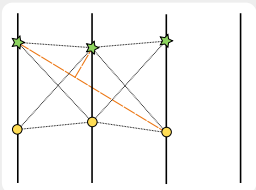


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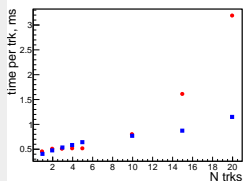
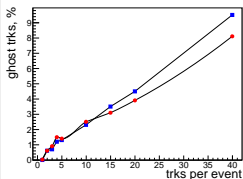
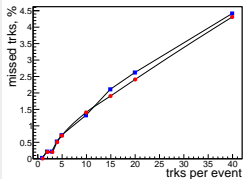
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# Track search

## algorithms performance



### Cellular Automata vs. Track-Following

- Track-Following faster for high multiplicity of tracks, but Cellular Automata gives less missing and less ghost tracks
- For low multiplicity of tracks both algorithms show the same performance

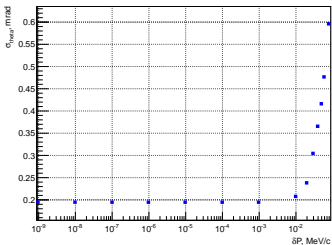
Main reason for ghost tracks is fake hits due to double strip structure of sensors

# Back-propagation to IP

Calculation of track parameters near interaction point with GEANE



- GEANE helps to calculate track parameters and their errors inside magnetic field
- for all reconstructed tracks  $\bar{p}$  assumption with momentum equal  $P_{beam}$  is used



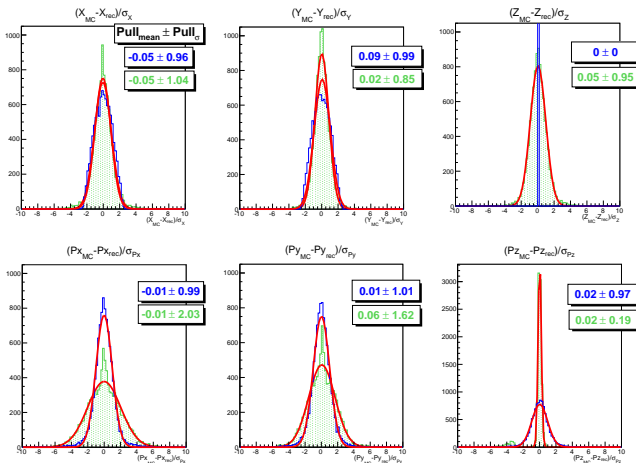
no influence on  $\theta$  resolution for expected beam uncertainty ( $10^{-3}$  GeV/c)

# Back-propagation to IP

## Problem with pull distributions



near luminosity detector & near interaction point ( $P_{beam}=1.5 \text{ GeV}/c$ )



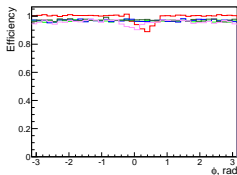
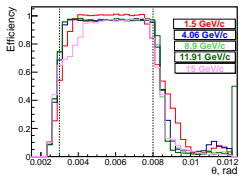


# Track reconstruction performance

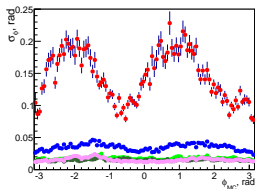
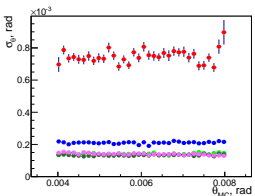
## simulation with beam pipe (v.201112)



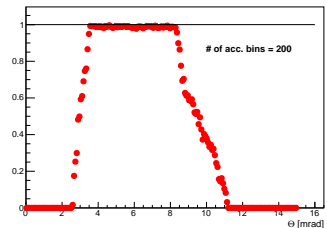
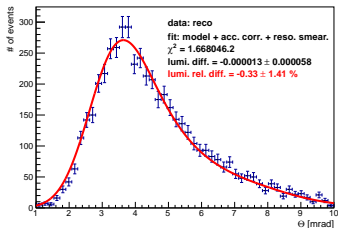
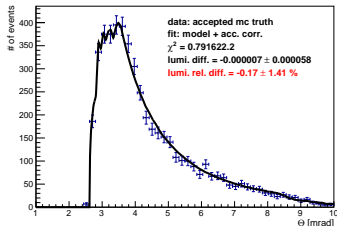
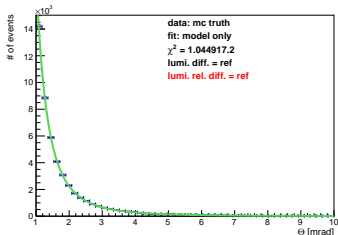
### Efficiency



### Resolution



# Luminosity fit





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- tracking system without PID and momentum measurement  
→ knowledge of signal and background contribution is important

## Strategy

- Generation of background with DPM:  
 $0.0018 < \theta < 2\pi$  rad,  $2 \cdot 10^7$  events  
 $P_{beam} = 1.5, 4.06, 8.9, 11.91, 15$  GeV/c
- Track reconstruction in the luminosity detector:  
 $\bar{p}$  assumption
- Comparison of reconstructed and MC information  
(for scattered  $\bar{p}$  and bkg signal )

## Background channels and particles



15 GeV/c

channel	ratio to $\bar{p}^{el}$ , %
$p\bar{p}$	100
$p\bar{p}\pi^0$	0.8
$p\bar{p}\pi^-\pi^+$	0.63
$p\bar{p}\pi^-\pi^+\pi^0$	0.55
$n\bar{p}\pi^+\pi^0$	0.46
$n\bar{p}2\pi^+\pi^-\pi^0$	0.19
$n\bar{p}\pi^+2\pi^0$	0.12
$p\bar{p}\pi^-\pi^+\gamma$	0.06
$p\bar{p}\pi^-\pi^02\gamma$	0.05
$p\bar{p}\pi^-\pi^+3\pi^0$	0.04
...	
<b>Total</b>	<b>3.72</b>

particle	% of tracks
$\bar{p}$	103.4
$\pi^-$	0.17
$e^+$	0.11
$e^-$	0.1
$\pi^+$	0.01
$K^-$	0.008
$p$	0.007
$K^+$	0.0002

90.4% of bkg =  $\bar{p}$  tracks

1.5 GeV/c

channel	ratio to $\bar{p}^{el}$ , %
$p\bar{p}$	100
$\pi^+\pi^-\pi^0$	0.005
$\pi^+\pi^-\pi^0$	0.003
$2\pi^+2\pi^-\pi^0$	0.003
$2\pi^+2\pi^-$	0.002
$\pi^+\pi^-$	0.001
$p\bar{p}\pi^0$	0.001
$p\bar{p}\pi^+\pi^-$	0.001
$2p\bar{p}\pi^-$	0.001
...	
<b>Total</b>	<b>0.025</b>

particle	% of tracks
$\bar{p}$	100.01
$\pi^-$	0.02
$e^+$	0.0002
$e^-$	0.0003
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58.6% of bkg =  $\bar{p}$  tracks

# Background channels and particles



## 15 GeV/c

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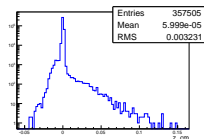
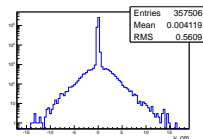
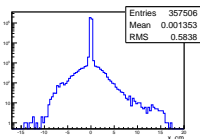
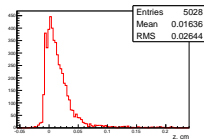
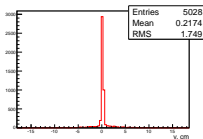
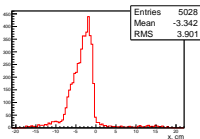
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# Background suppression



How to distinguish **background** from **signal**?



Any dedicated cut to reduce background has significant signal inefficiency

Possible solution: fit signal and bkg together  
(with Kernel Density Estimation as p.d.f for bkg)



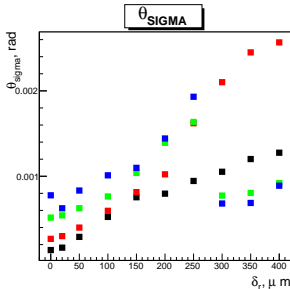
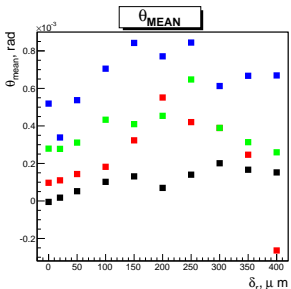
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# Impact of sensors misalignment on $\theta$ resolution



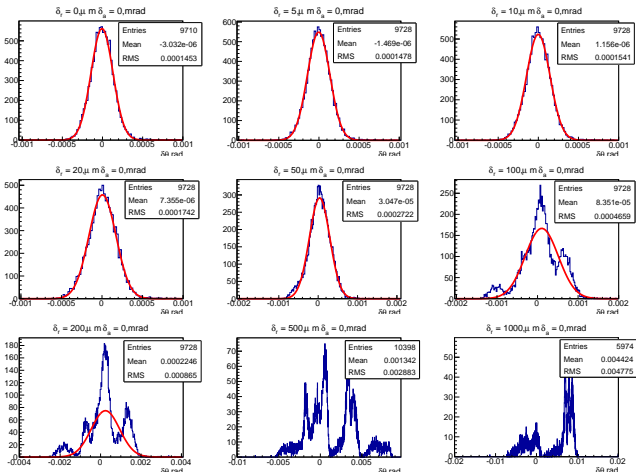
Each sensors has 6 d.o.f: 3 translation ( $\delta_r$ ) and 3 rotation ( $\delta_\alpha$ )  
 $\delta_r = 0, 20, 50, 100, 150, 200, 250, 300, 350, 400 \mu\text{m}$   
 $\delta_\alpha = 0, 3, 6, 9 \text{ mrad}$



$P_{beam} = 11.91 \text{ GeV}/c$ :

for  $\delta_r \sim 100 \mu\text{m}$  ( $\delta_\alpha = 0 \text{ mrad}$ )  $\theta$  resolution become 5 times worse!

# Impact of sensors misalignment on $\theta$ resolution ( $P_{beam}=11.91$ GeV/c)



# Software alignment

Fitting the residuals (Alignment in one step)



two different types of fitted parameters:

- Related to the track properties determined by the fit.  
different for each tracks → LOCAL parameters
- Parameters which are depending on the detector position.  
Alignment parameters → GLOBAL parameters

To get a good accuracy significant number of tracks is needed

Matrix size of the system equation:  $n_{tot} = n_{loc} \cdot n_{tracks} + n_{gl}$

Millepede algorithm can resolve such problems

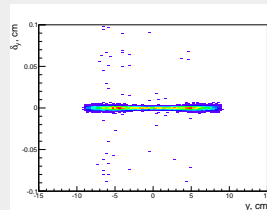
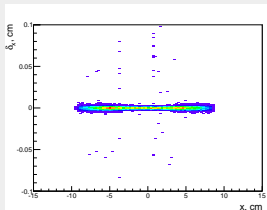
And it was used for VELO at LHCb (arXiv:0807.3532)

# Alignment Results

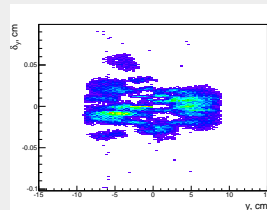
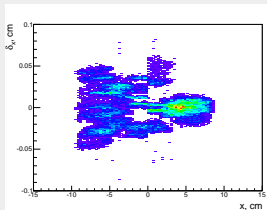
Residuals between reconstructed hit and track ( $P_{beam}=11.91$  GeV/c)



## Ideal case



## Misaligned sensors

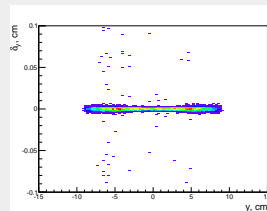
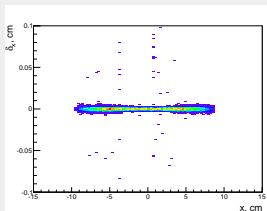


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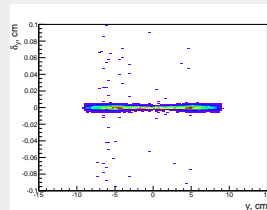
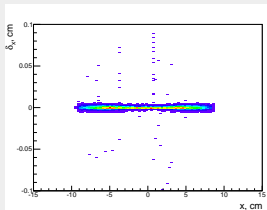
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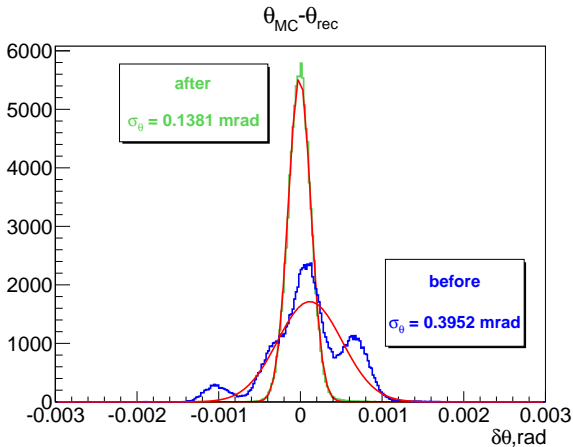


## Misaligned sensors



# Sensors alignment for translation

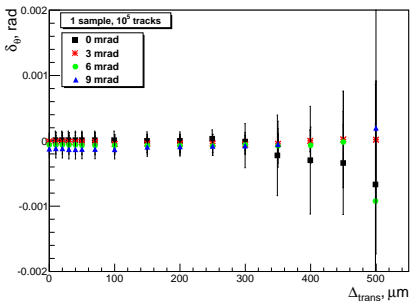
misalignment  $\sim 100\mu\text{m}$  ( $P_{beam}=11.91\text{ GeV}/c$ )



Without sensor misalignment resolution 0.1361 mrad

# Sensors alignment

sensitivity to misalignment scale (11.91 GeV/c)



## Limits

For translation 300  $\mu\text{m}$ , for rotation 6 mrad

## Expectation from mechanical point

translation 200  $\mu\text{m}$ , rotation 3 mrad



## Reconstruction

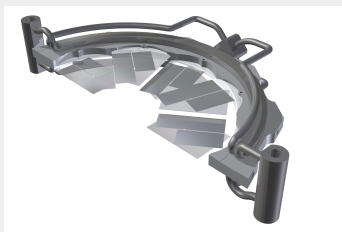
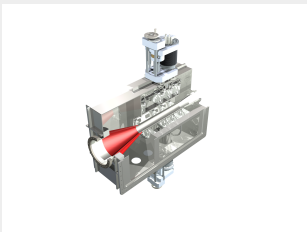
- Track reconstruction chain is tested on original design
- We have another design with HV-MAPS as sensors
  - 50  $\mu\text{m}$  sensors  $2 \times 4 \text{ cm}^2$  and  $2 \times 6 \text{ cm}^2$  on both sides
  - 200  $\mu\text{m}$  CVD diamond for heat conduction
  - Length 1m. Halfs diameter 30 cm.





## Reconstruction

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## Background study

- Background studies are done with DPM generator
- Amount of bkg varies from 0.03% up to 4%
- We are keeping in mind Kernel Density Estimator as a tool for bkg p.d.f description

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- Software alignment is under development
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Thank you for your attention!



Estimating a Signal In the Presence of an Unknown Background,  
W. Rolke and A. Lopez (arXiv:1112.2299)

## "Non-parametric" density estimation

- $X_1, \dots, X_n$  – observations from some unknown density  $f$ .
- $K$  – continuous, non-negative and symmetric function with  $K(x) \rightarrow 0$  as  $x \rightarrow \pm\infty$   
(Often  $K$  is chosen to be p.d. itself: Gaussian density)

$$\hat{f}_h(x) = \frac{1}{nh} \sum_{i=1}^n K\left(\frac{x-X_i}{h}\right)$$

- $h$  – tuning parameter called bandwidth.  
→ constant or adaptive bandwidth  $h_x$

# Semi-parametric fitting



## Function for maximum likelihood

$$f(x; \alpha, \theta) = (1 - \alpha)f_B(x) + \alpha f_S(x; \theta)$$

for  $f_B(x)$  (estimation of bandwidth and density) one need pure sample of background events

:(

## RooFit contains RooKeysPdf class:

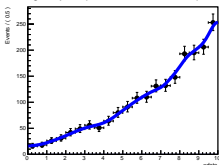
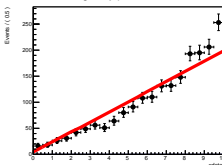
A one-dimensional kernel estimation p.d.f which model the distribution of an arbitrary input dataset as a superposition of Gaussian kernels

:)

# Example



Bkg fit by adaptive kernel estimation pdf

Bkg fit by polinom  $a^*x$ 

$$\text{Sig}(x) = \text{Landay}(3.5, 1) \otimes \text{Gaus}(0, 0.1)$$

$$\text{Bkg}(x) = x + 0.001x^2 + 0.01x^3$$

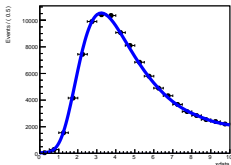
$$\text{Data}(x) = \text{Sig}(x) + \text{Bkg}(x)$$

$$\text{sig}(\text{sig}+\text{bkg})=0.95$$

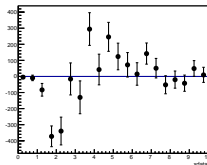
$$\text{Kernel: } 9.4966\text{e-}01 \pm 2.35\text{e-}03 (\ll\sigma)$$

$$\text{Lin: } 9.3780\text{e-}01 \pm 2.84\text{e-}03 (4\sigma)$$

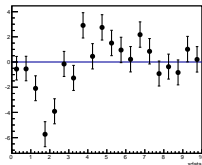
Sig+Bkg data (Kernel estim)



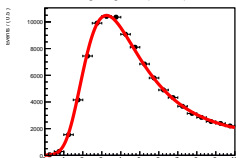
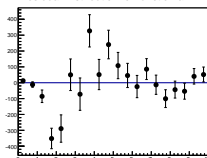
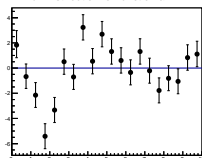
Residual Distribution for Kernel estim



Pull Distribution for Kernel estim



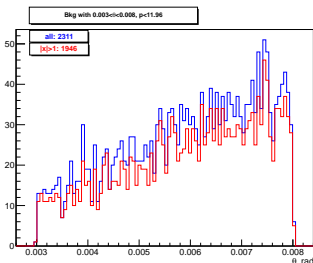
Sig+Bkg data (lin func)

Residual Distribution for function  $a^*x$ Pull Distribution for function  $a^*x$ 

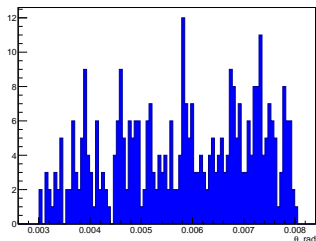
# Sample of "pure" background



- Shape of background is not fixed (important for us, because it could differ for different  $P_{beam}$ )
- But to fit it background sample is needed.



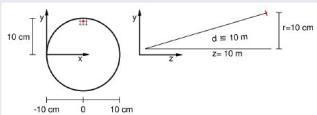
■



Small signal fraction to bkg sample doesn't change shape too much



# $\Delta\phi$ vs. $\Delta\theta$



$$\Delta y = \Delta x$$

$$r = \sqrt{x^2 + y^2}, \quad \Delta r = \Delta x$$

$$\Delta z \simeq \Delta x$$

$$\cos\phi = \frac{x}{r}, \quad \Delta\cos\phi = \frac{\Delta x}{r} \sqrt{1 + \frac{x}{r}}$$

$$\cos\theta = \frac{z}{d}, \quad \Delta\cos\theta = \frac{\Delta x}{d} \sqrt{1 + \frac{z}{d}}$$

$$\Delta\cos\theta / \Delta\cos\phi \simeq \frac{r}{d} = 10^{-2}$$

# Elastic Cross Section



$$\frac{d\sigma}{dt} = \frac{d\sigma_C}{dt} + \frac{d\sigma_{int}}{dt} + \frac{d\sigma_H}{dt}$$

with

$$\frac{d\sigma_C}{dt} = \frac{4\pi\alpha_{EM}^2 G^4(t)}{\beta^2 t^2}$$

$$\frac{d\sigma_{int}}{dt} = \frac{\alpha_{EM}\sigma_{Total}}{\beta|t|} G^2(t) e^{\frac{1}{2}Bt} (\rho \cos(\delta) + \sin(\delta))$$

$$\frac{d\sigma_H}{dt} = A_1 \cdot [e^{t/2t_1} - A_2 \cdot e^{t/2t_2}]^2 + A_3 \cdot e^{t/t_2}$$

# A few words about generated statistic

$2 \cdot 10^7$  events with DPM were generated

$$\frac{dN}{dt} = \sigma \cdot L \rightarrow \tilde{N} = \sigma \cdot \tilde{L} \cdot t$$

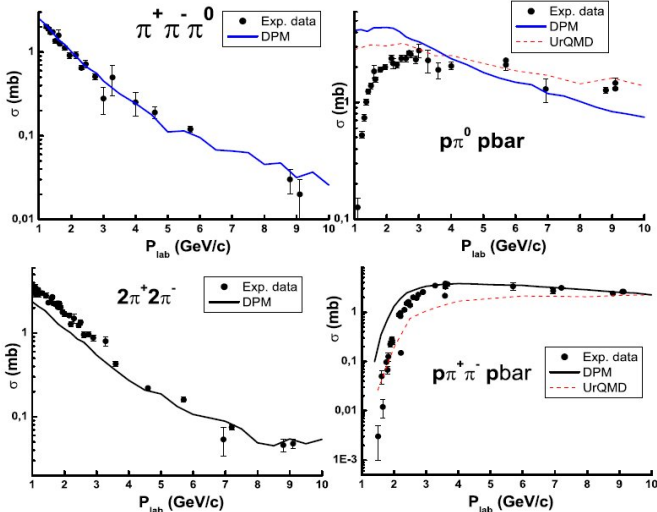
$$\tilde{L} = 2 \cdot 10^{32} \frac{1}{\text{cm}^2 \text{s}} \text{ (High lumi mode)}$$

$$\sigma = (100 - 51) \text{ mb}$$

$$t = \frac{2 \cdot 10^7}{2 \cdot 10^{32} (100 - 51) \cdot 10^{-27}} = (1 - 2) \text{ s}$$

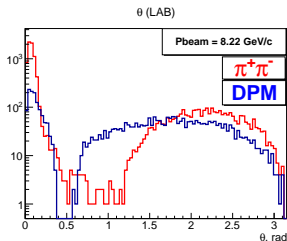
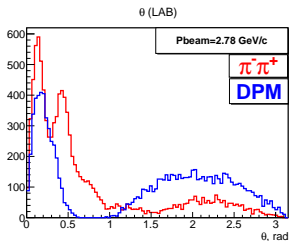
# DPM generator

Total cross-sections for different channels



# DPM generator

## Differential cross-sections



comparison with dedicated  $p\bar{p} \rightarrow \pi^+\pi^-$  generator (M.Zambara & D. Khanef)

# Hit reconstruction



Hit position  $(x,y,z)$  reconstruction from digital information



- sensor & strip number
- $(x,y,z)$  local sensor
- Global PANDA frame
- Global Lumi frame

result of sensor alignment will be applied at this stage



## 3D straight line fit by the least-squares method

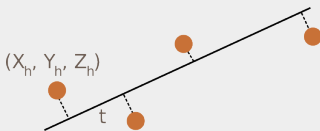
$$x = p_0 + p_1 t$$

$$y = p_2 + p_3 t$$

$$z = p_4 + p_5 t$$

$$p_4 = Z_0$$

$$p_5 = \sqrt{1 - p_1^2 - p_3^2} \quad t_{min} = p_1(x_h - p_0) + p_3(y_h - p_2) + p_5(z_h - p_4)$$



$$\chi^2 = \frac{(x_h - (p_0 + p_1 t_{min}))^2}{\sigma_x^2} + \frac{(y_h - (p_2 + p_3 t_{min}))^2}{\sigma_y^2} + \frac{(z_h - (p_4 + p_5 t_{min}))^2}{\sigma_z^2}$$

# Software alignment

## Minimizing the residuals (Iterative)



- Fit a large number of tracks and plot the residuals for each sub-detector
- The mean value of each residual distribution should then be centered on the misalignment value
- Correct the sub-detector coordinates from this value
- Fit the track again, plot the residuals,...  
And so on until the residuals central values are stabilized at 0.

Iterations are based on biased track fit results (fit with misaligned detector). Then, even if the method converges, it could lead to biased misalignment values (offsets to real values).



# Software alignment

How to deal with large matrix equation?



## Millepede algorithm

- Matrix is divided on sub-matrices of dimensions  $n_{loc} * n_{loc}$
- C++ implementation is done for LHCb VELO (Knossos)

## Track parametrization

$$\begin{cases} x = a \cdot z + b \\ y = c \cdot z + d \end{cases}$$

## Residuals parametrization

$$\begin{cases} \epsilon_x = -\Delta_x + y_{hit} \cdot \Delta_\gamma + a \cdot (\Delta_z + x_{hit} \cdot \Delta_\beta + y_{hit} \cdot \Delta_\alpha) \\ \epsilon_y = -\Delta_y - x_{hit} \cdot \Delta_\gamma + c \cdot (\Delta_z + x_{hit} \cdot \Delta_\beta + y_{hit} \cdot \Delta_\alpha) \end{cases}$$

3 translations ( $\Delta_x, \Delta_y, \Delta_z$ ) and 3 rotation ( $\Delta_\alpha, \Delta_\beta, \Delta_\gamma$ ) around x, y, z