

Search for $\bar{p}-^{16}\text{O}$ Bound States in $\bar{\text{P}}\text{ANDA}$

Simulation with GiBUU

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10.09.2012

3 The Conclusions of Simulation

$\bar{p}$ -nucleus interaction

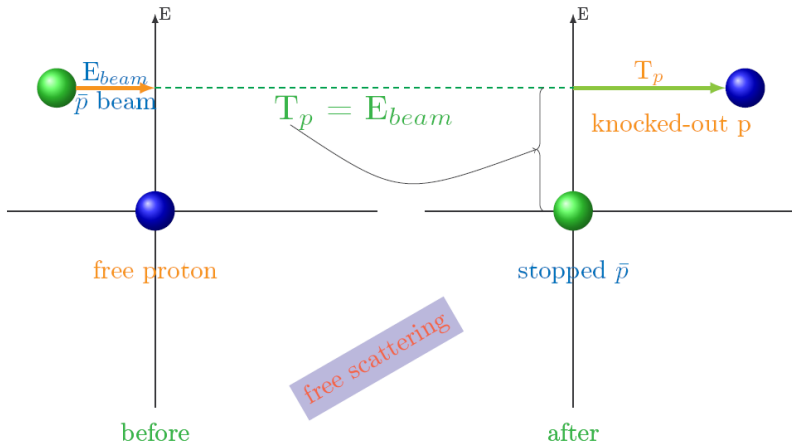
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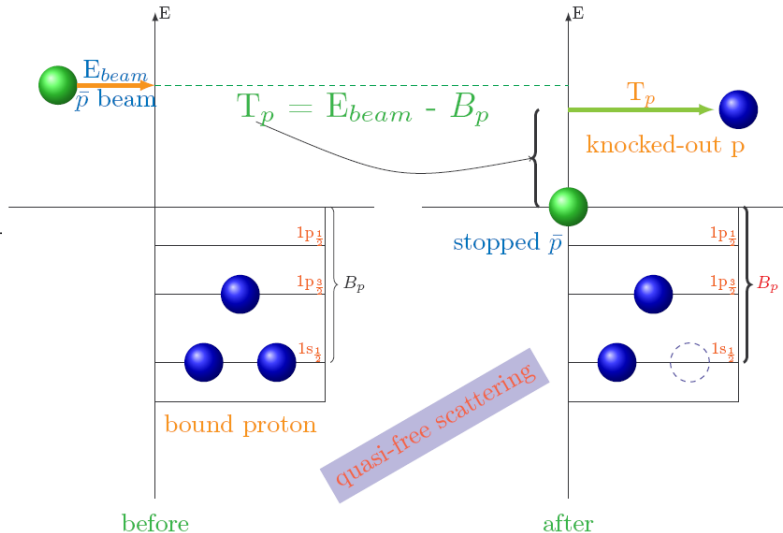
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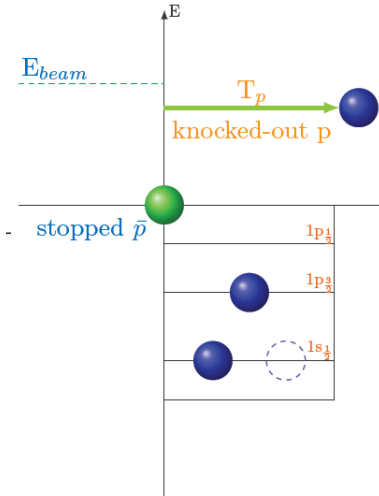
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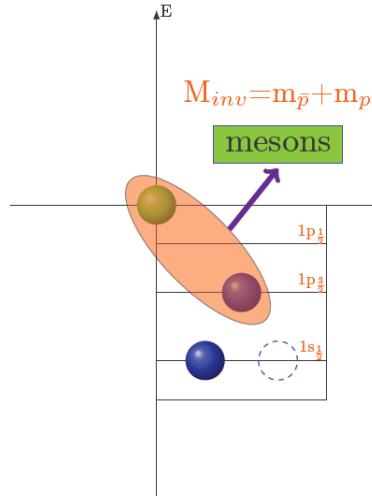
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annihilation at rest

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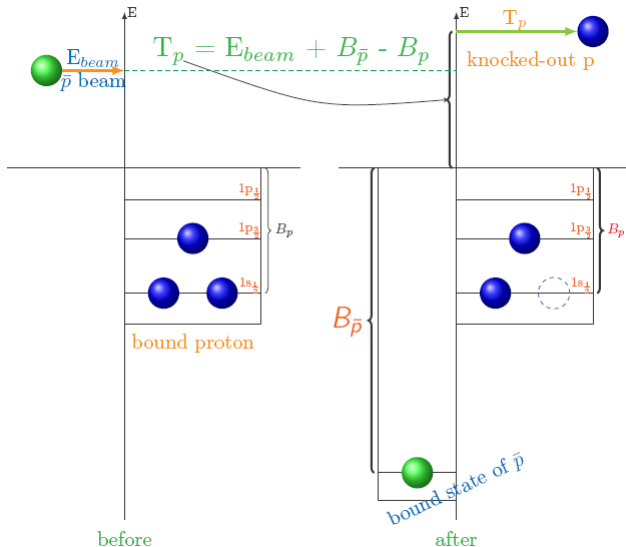
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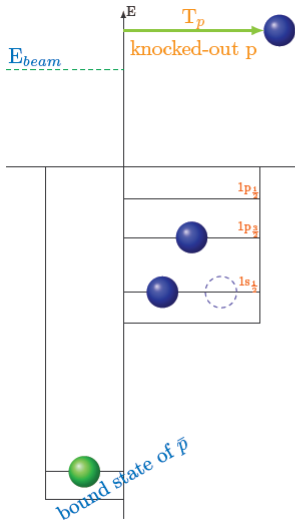
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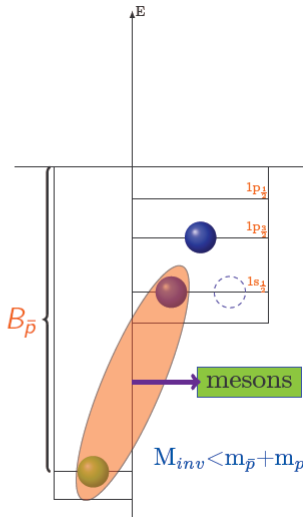
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annihilation with potential

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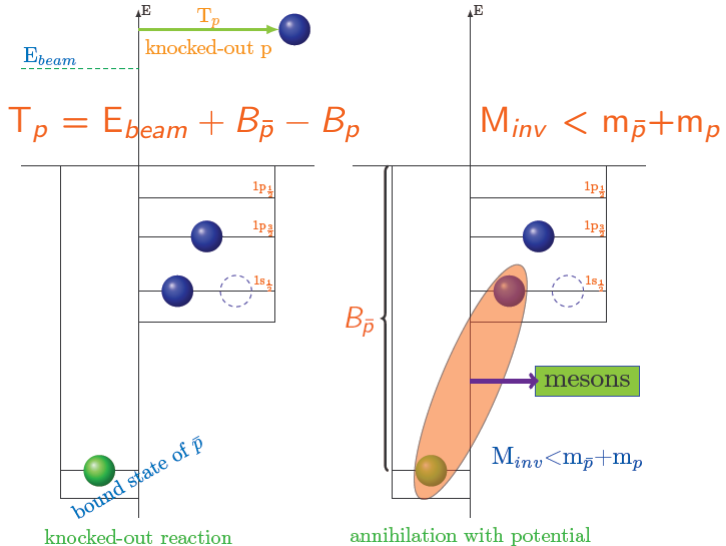
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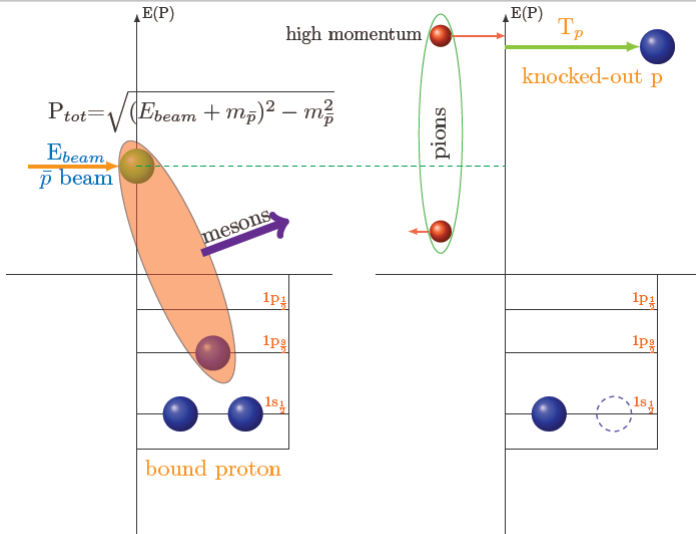
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annihilation in flight

knocked-out by pion

$(\bar{p}, p)$ knock-out experiment

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LEAR experiment in 1980s @CERN

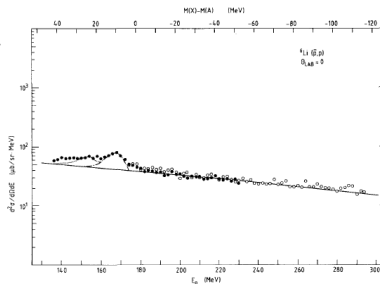
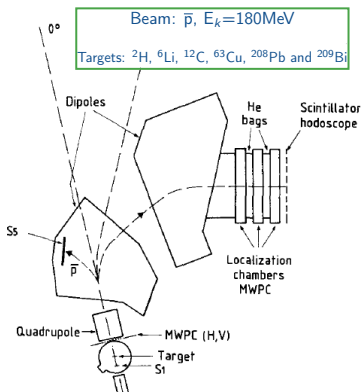


Fig. 2. Double differential cross sections for the $^6\text{Li}(\bar{p}, p)X$ reaction at $E_p = 177.9$ MeV. The full line corresponds to an average temperature $T = 101$ MeV. The dash-dotted line is the result of a quasi-free scattering calculation corresponding to an effective proton number $N_{\text{eff}} = 0.15$. The dotted line represents the contribution of the quasi-free scattering on 1s-shell protons with an effective proton number 0.09.

$(\bar{p}, p)$ knock-out experiment

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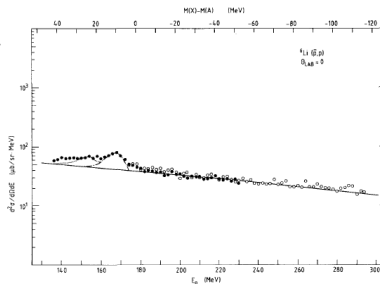
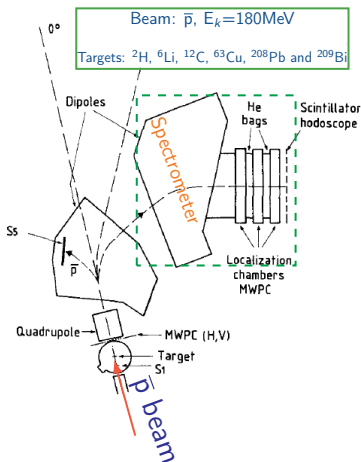


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$(\bar{p}, p)$ knock-out experiment

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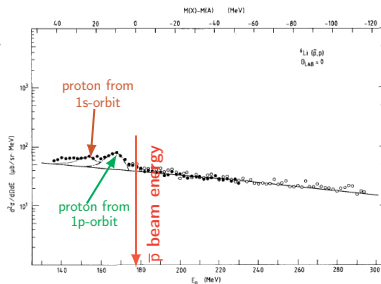
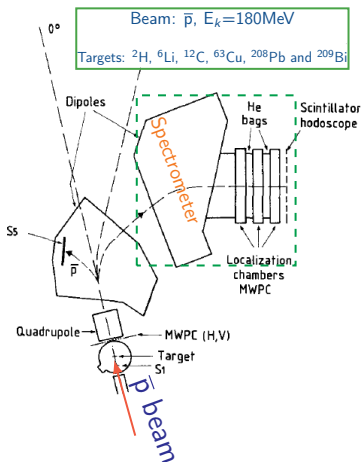


Fig. 2. Double differential cross sections for the $^6\text{Li}(\bar{p}, p)X$ reaction at $E_k=127.9$ MeV. The full line corresponds to an average temperature $T=101$ MeV. The dash-dotted line is the result of a quasi-free scattering calculation corresponding to an effective proton number $N_{eff}=0.15$. The dotted line represents the contribution of the quasi-free scattering on 1s-shell protons with an effective proton number 0.09.

$(\bar{p}, p)$ knock-out experiment

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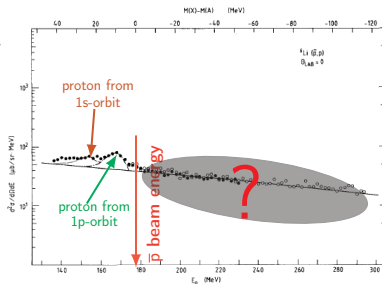
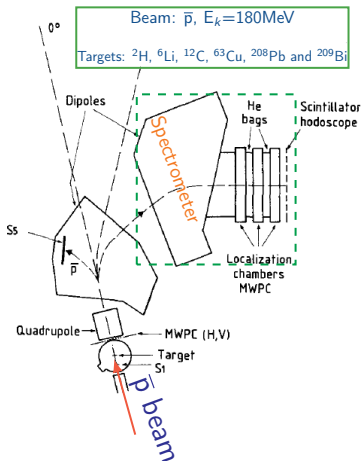


Fig. 2. Double differential cross sections for the $^6\text{Li}(\bar{p}, p)X$ reaction at $E_k=127.9\text{ MeV}$. The full line corresponds to an average temperature $T=101\text{ MeV}$. The dash-dotted line is the result of a quasi-free scattering calculation corresponding to an effective proton number $N_{\text{eff}}=0.15$. The dotted line represents the contribution of the quasi-free scattering on 1s-shell protons with an effective proton number 0.09.

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- Institut für Theoretische Physik, JLU Gießen
 Prof. U. Mosel, Dr. A. B. Larionov, *et al.*
- Framework for elementary reactions on nuclei

The GiBUU project

The **GiBUU project** is aiming to provide an unified transport framework in the MeV and GeV energy regimes for

- elementary reactions on nuclei, as e.g.
 - electron + A,
 - photon + A,
 - neutrino + A,
 - **hadron + A (especially pion + A and proton + A)**
- and for heavy-ion collisions.



For those reactions, the flow of particles is modelled within a **Boltzmann-Uehling-Uhlenbeck (BUU) framework**. The relevant degrees of freedom are **mesons** and **baryons**, which propagate in mean fields and scatter according to cross sections which are tuned to the energy range of 10 MeV to more than 10 GeV. In the higher energy regimes the concept of **pre-hadronic** interactions is implemented in order to realize **color transparency** and **formation time** effects. For a general overview of the model, please refer to our recent review paper:

Transport-theoretical Description of Nuclear Reactions

O. Buss, T. Gaitanos, K. Gallmeister, H. van Hees, M. Kaskulov, O. Lalakulich, A. B. Larionov, T. Leitner, J. Weil, U. Mosel
 Phys. Rept. 512 (2012) 1-124 [Inspire](#) [arXiv:1106.1344](#)

Parameters of $\bar{p}$ -nucleus interaction in GiBUU

Parameters for $\bar{p}$ -nucleus interaction:

E_{beam} (GeV)	$\sigma_{ann}^{\bar{p}p}$ (mb)	$\sigma_{el}^{\bar{p}p}$ (mb)	Target	Note
0.18	84.7	80.9	${}^6\text{Li}$	.. comparing the background with LEAR experiment
1.5	40.0	32.2	${}^{16}\text{O}$	.. searching for ${}^{15}_{\bar{p}}\text{N}$ & ${}^{15}_{\bar{p}}\text{O}$ bound states

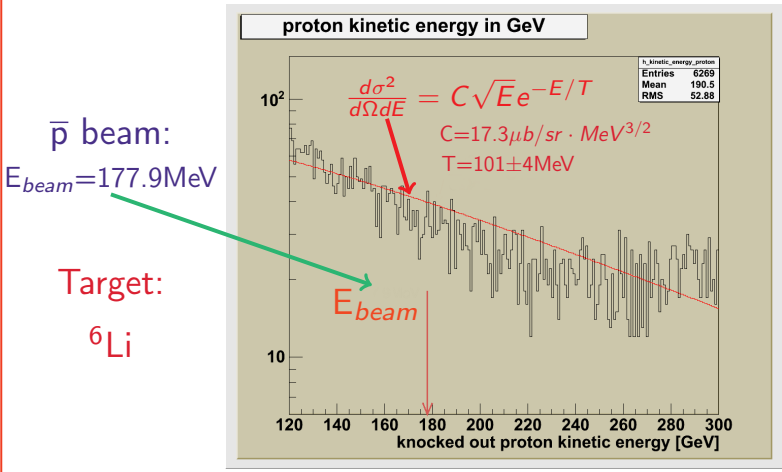
$\bar{p}$ potential in GiBUU:

$$\xi = 0.2 - 0.3 \rightarrow \text{Re}(V_{opt}) = -220 - -150 \text{ MeV}$$

$\bar{p}$ - ${}^6\text{Li}$ collision simulation

— Same conditions as LEAR experiment

The continuous background of knocked-out protons



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$\bar{p}$ - ^{16}O collision simulation

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$\bar{p}$ beam: $E_{beam}=1.5\text{GeV}$;

Target: ^{16}O

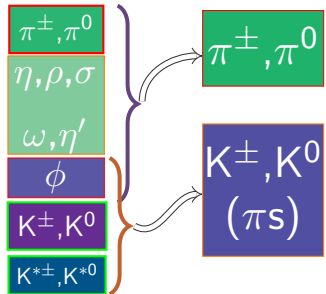
Signature:

First, knocked-out reaction

Only one knocked-out
proton or neutron

$\bar{p}$ stopping

Second, annihilation at rest



Background: knocked-out nucleons by high-momentum pions

The events with only pions in final state

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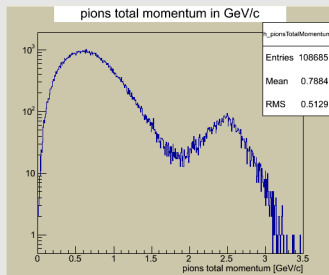
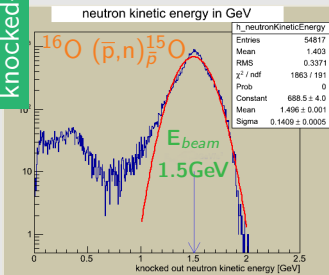
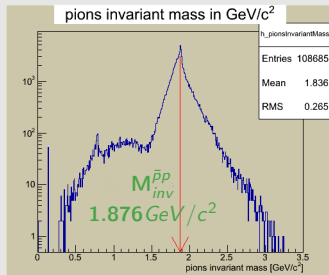
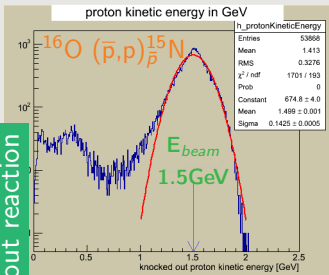
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$\bar{p}p$ or $\bar{p}n$ annihilation

$\pi^\pm \pi^0$

$\eta \rho \sigma \omega \eta' \phi$

$\pi^\pm \pi^0$

The events with Kaons(and pions) in final state

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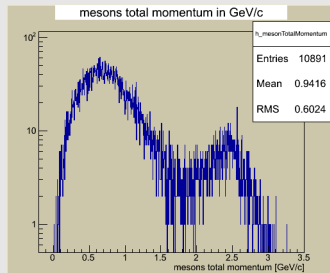
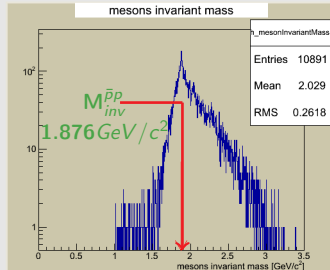
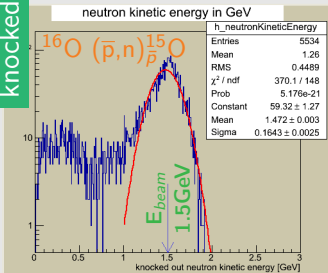
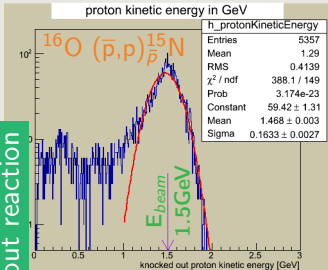
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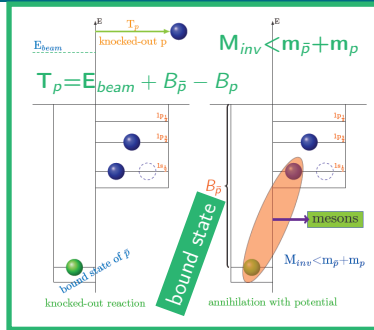
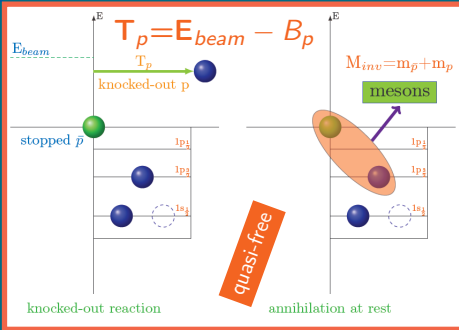


$\bar{p}p$ or $\bar{p}n$ annihilation

$K^{\pm} K^0$
 $K^{*0} \phi$

$K^{\pm} K^0$
 (πS)

The cutting conditions setting



If $B_p = 30 \text{ MeV}$ and $B_{\bar{p}} = 150 \text{ MeV}$ ($\epsilon \sim 37 \text{ MeV}$):

	$T_p (\text{GeV})$	$M_{inv} (\text{GeV}/c^2)$
quasi-free	1.47	~ 1.86
bound state	1.62	$1.85 \sim 1.70$

The correlation of knocked-out nucleon and decayed mesons

The events with pions in final state

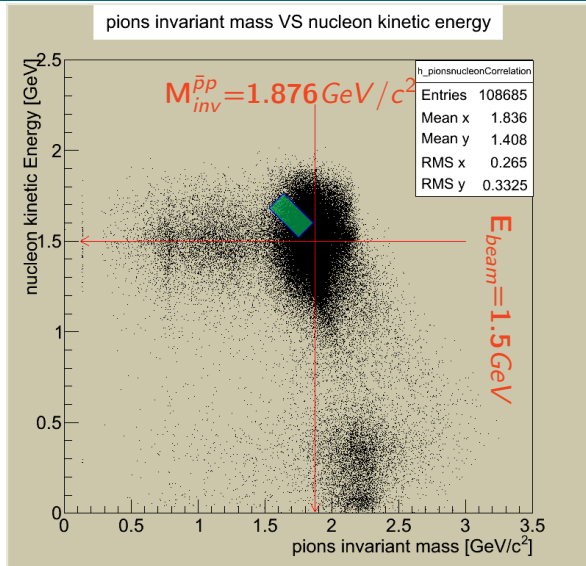
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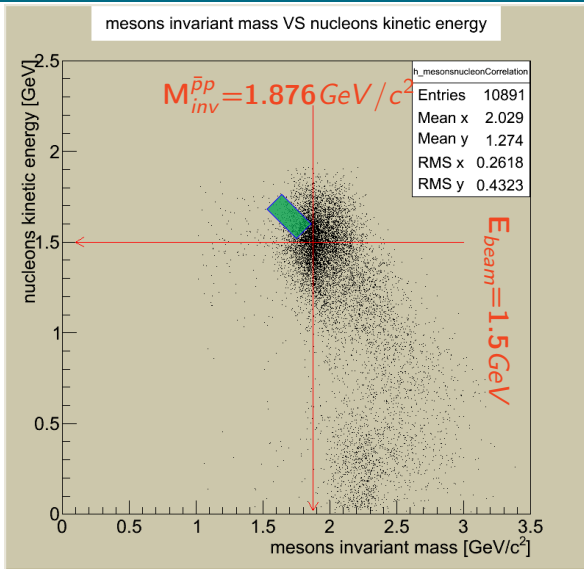
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The correlation of knocked-out nucleon and decayed mesons

The events with kaons in final state



Search for bound state events

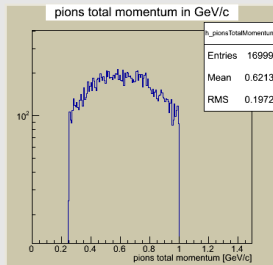
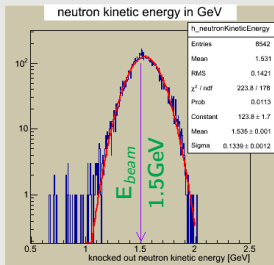
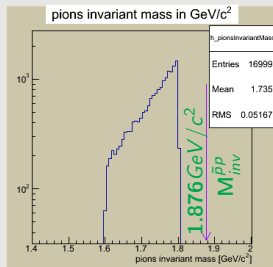
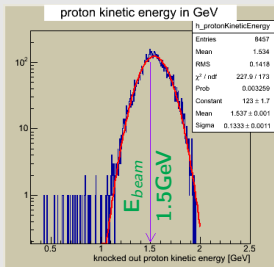
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cutting conditions

$$1.6 \leq M_{inv}^{mesons} \leq 1.8$$

$$0.25 \leq p_{tot}^{mesons} \leq 1.0$$

Search for bound state events

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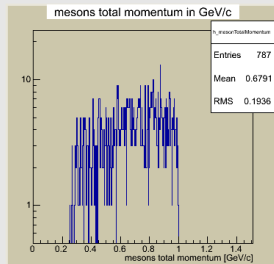
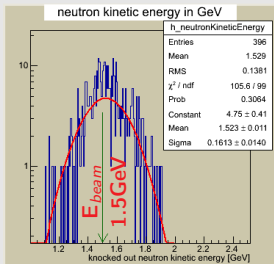
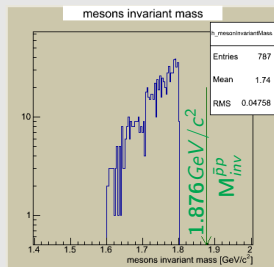
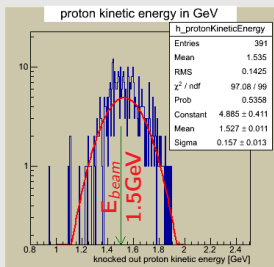
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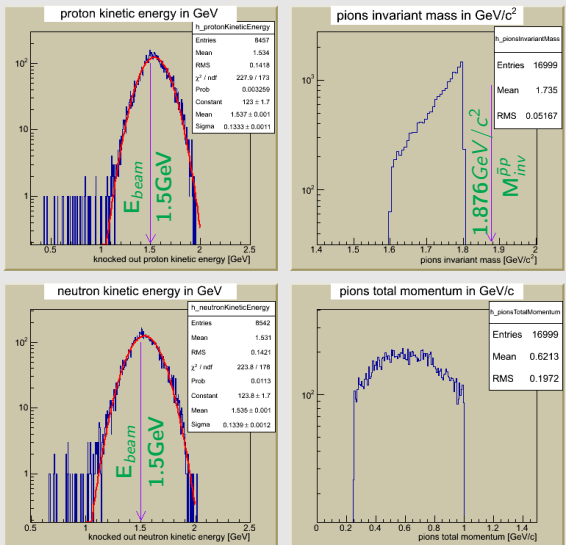
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$$0.25 \leq P_{tot}^{mesons} \leq 1.0$$

Mean value of
the kinetic energy of
knocked-out nucleon
spectrum

$$\sim 1.53 \text{ GeV}$$

The correlation of knocked-out nucleon and decayed mesons

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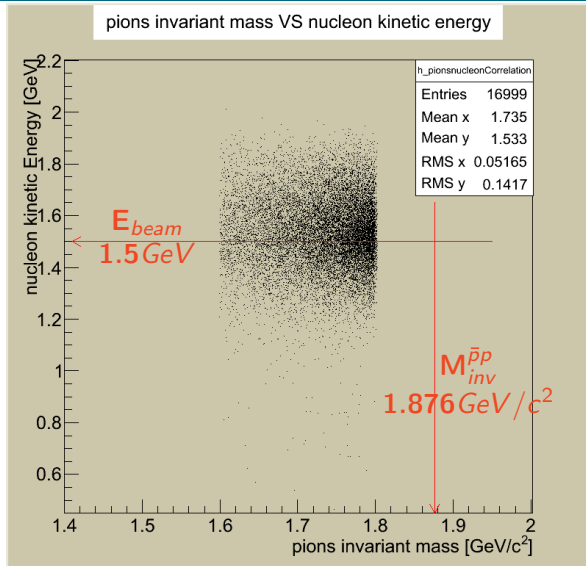
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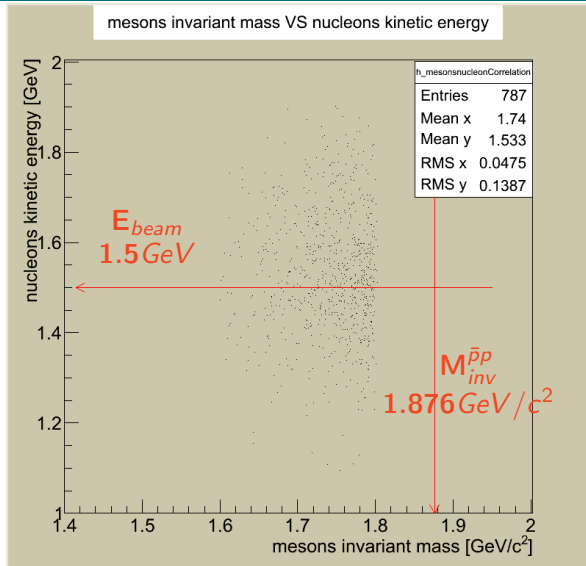
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- 9×10^8 $\bar{p}^{-16}\text{O}$ collision events had been simulated
- Suppression of the continuous knocked-out nucleon background by event selection of data analysis
- Up to now, **no bound state event has been found**
- The quasi-free scattering reaction cannot be rejected

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Thank You for Your Attention!

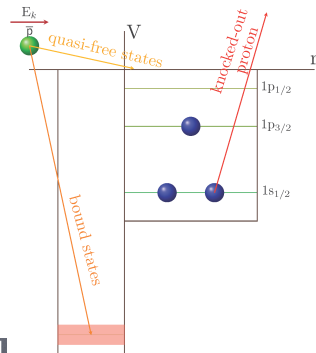
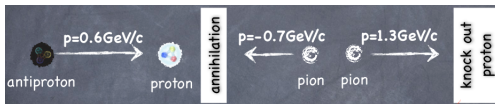
Why no bound states structure observed?

- Kinetic energy of knocked-out proton:

$$T_p = E_{beam} + B_{\bar{p}} - B_p$$

- Low beam energy
- Strong background

$$\frac{d^2\sigma}{d\Omega dE} = C\sqrt{E}e^{-E/T}$$



${}^6\text{Li}$ protons

Search for
 $\bar{p}-{}^{16}\text{O}$
Bound
States in
PANDA

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$\bar{p}$ -nuclear collision simulation with GiBUU

Output data structure from GiBUU

particle ID&charge		parents ID		position (x,y,z)			momentum (p _x ,p _y ,p _z)							
1	0	37	0	0	0.938	1	22.700	-19.206	5.979	0.205	-0.189	0.056	951	19
-1	0	1159159	1	-1	0.938	1	0.849	-6.822	84.775	0.021	-0.233	2.257	951	19
1	1	37	0	0	0.938	1	17.485	24.554	-6.891	0.167	0.206	-0.048	952	19
1	0	37	0	0	0.938	1	-1.495	6.852	-6.576	0.054	0.108	0.090	952	19
1	1	37	0	0	0.938	1	13.230	-24.473	6.864	0.117	-0.247	0.072	952	19
1	0	37	0	0	0.938	1	6.957	-15.335	22.646	0.039	-0.380	0.280	952	19
1	1	37	0	0	0.938	1	-46.391	17.748	-13.506	-0.511	0.188	-0.165	952	19
1	1	37	0	0	0.938	1	18.707	-32.110	-12.055	0.174	-0.356	-0.085	952	19
101	0	1161528	103	0	0.138	1	12.105	-71.356	-15.531	0.111	-0.436	-0.073	952	19
1	1	37	0	0	0.938	1	12.645	17.096	10.720	0.115	0.096	0.087	952	19
1	0	37	0	0	0.938	1	26.447	-32.964	-15.097	0.264	-0.371	-0.154	952	19
1	0	37	0	0	0.938	1	-45.723	-16.568	3.307	-0.592	-0.212	0.022	952	19
1	0	37	0	0	0.938	1	41.655	-33.162	21.746	0.550	-0.439	0.294	952	19
1	0	37	0	0	0.938	1	8.039	6.803	5.444	-0.032	0.044	-0.024	952	19
1	1	37	0	0	0.938	1	19.627	-9.880	-22.527	0.174	-0.109	-0.211	952	19
1	0	37	0	0	0.938	1	23.193	4.969	12.149	-0.244	0.042	0.034	952	19
1	1	1156293	1	-1	0.938	1	4.817	-1.671	85.798	0.133	-0.060	2.288	952	19
1	0	37	0	0	0.938	1	22.181	13.839	-14.753	0.217	0.124	-0.133	952	19
101	-1	1161528	1	-1	0.138	1	-54.952	24.827	44.689	-0.203	0.099	0.199	952	19
101	1	1161528	1	-1	0.138	1	-18.099	47.498	20.542	-0.028	0.109	0.056	952	19
101	-1	1161528	1	-1	0.138	1	5.740	65.098	10.616	0.038	0.203	0.044	952	19
101	1	1161528	103	0	0.138	1	-60.224	17.232	-55.460	-0.408	0.125	-0.393	952	19
1	1	37	0	0	0.938	1	17.197	11.546	-3.880	0.100	0.110	-0.091	953	19
1	0	37	0	0	0.938	1	13.775	-30.747	-9.313	0.067	-0.341	-0.020	953	19
1	1	1158628	2	0	0.938	1	-35.348	-18.626	41.149	-0.474	-0.253	0.551	953	19

knocked-out proton

BUU Equation

Search for
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Boltzmann-Uehling-Uhlenbeck equation:

$$(\partial_t + \nabla_p H \cdot \nabla_r - \nabla_r H \cdot \nabla_p) f_i(r, p, t) = I_{coll}[f_i, f_N, f_\pi, f_\Delta, \dots]$$

$$H = \sqrt{[M + U(r, p)]^2 + p^2}$$

This model is based on the BUU equation which describes the space-time evolution of a many-particle system in a mean-field potential.

where $f_i(r, p, t)$ is the phase space density, H is the relativistic Hamiltonian of a particle of mass M in a scalar potential U , and I_{coll} is the collision term which accounts for changes in the phase space density due to elastic and inelastic collisions between the particles, and also due to particle decays into other hadrons.

- The cross section of $\bar{p}$ -nucleus interaction:

$\bar{p}p$ annihilation cross section

$$\sigma_{\text{ann}}^{\bar{p}p} = \begin{cases} 51.52 p_{\text{lab}}^{-0.85} + 0.034 p_{\text{lab}}^{-2.94} & \text{for } p_{\text{lab}} < 0.51 \\ 88.8 p_{\text{lab}}^{-0.4} - 24.2 & \text{for } 0.51 < p_{\text{lab}} < 6.34 \\ 38 p_{\text{lab}}^{-0.5} + 24 p_{\text{lab}}^{-1.1} & \text{for } 6.34 < p_{\text{lab}} \end{cases}$$

$\bar{p}p$ elastic scattering cross section

$$\sigma_{\text{el}}^{\bar{p}p} = 40 p_{\text{lab}}^{-0.56} + 5.8 \exp[-(p_{\text{lab}} - 1.85)^2]$$

σ in mb and p_{lab} in GeV/c

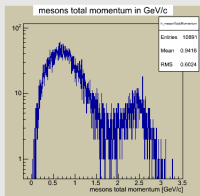
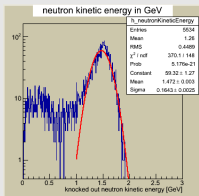
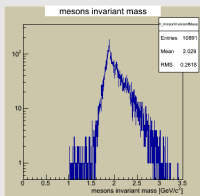
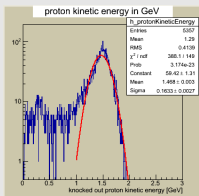
if $p_{\text{lab}} = 2.25 \text{ GeV/c}$, then:

$$\sigma_{\text{ann}}^{\bar{p}p} = 40.0 \text{ mb and } \sigma_{\text{el}}^{\bar{p}p} = 32.2 \text{ mb}$$

The events with Kaons (and pions) in final state

Search for
 $\bar{p}^{16}\text{O}$
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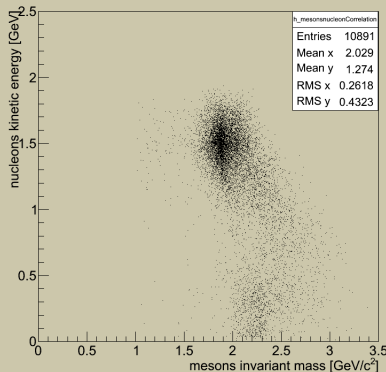
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knocked-out reaction



mesons invariant mass VS nucleons kinetic energy



$\bar{p}p$ or $\bar{p}n$ annihilation at rest



The $\bar{p}$ potential calculation

- Kinetic energy of knocked-out nucleon

$$T_p = T_{\bar{p}} + B_{\bar{p}} - B_p \text{ (Fermi Energy: } \epsilon \sim 37 \text{ MeV)}$$

- $\bar{p}p$ or $\bar{p}n$ annihilation at rest

- Without potential

$$\begin{aligned}
 M_{inv} &= \sqrt{E_{total}^2 - P_{total}^2} = \sqrt{(M_0 + M_0)^2 - P_{\bar{p}}^2} \\
 &= \sqrt{(0.938 + 0.938)^2 - (0)^2} = 1.876 [\text{GeV}/c^2]
 \end{aligned}$$

- With potential ($V = -150 \text{ MeV}$)

$$\begin{aligned}
 E_{total} &= E'_{total} = \delta E_k + M_0 + M_0 + V \\
 (\delta E_k &= -V = 150 \text{ MeV})
 \end{aligned}$$

$$\begin{aligned}
 M'_{inv} &= \sqrt{E'^2_{total} - P'^2_{total}} \\
 &= \sqrt{(2M_0)^2 - (0.551)^2} = 1.793 [\text{GeV}/c^2]
 \end{aligned}$$

Search for bound state events

Search for
 $\bar{p}^{-16}\text{O}$
 Bound
 States in
 $\bar{\text{PANDA}}$

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- The continuous background of knocked-out nucleons
- Quasi-free(QF) scattering VS bound-state(BS) formation

$$\left(\frac{\sigma^2}{d\Omega dE}\right)_{QF} / \left(\frac{\sigma^2}{d\Omega dE}\right)_{BS} \sim 10^3$$

