

# The Tracking Code RF-Track and its Applications

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# Contents

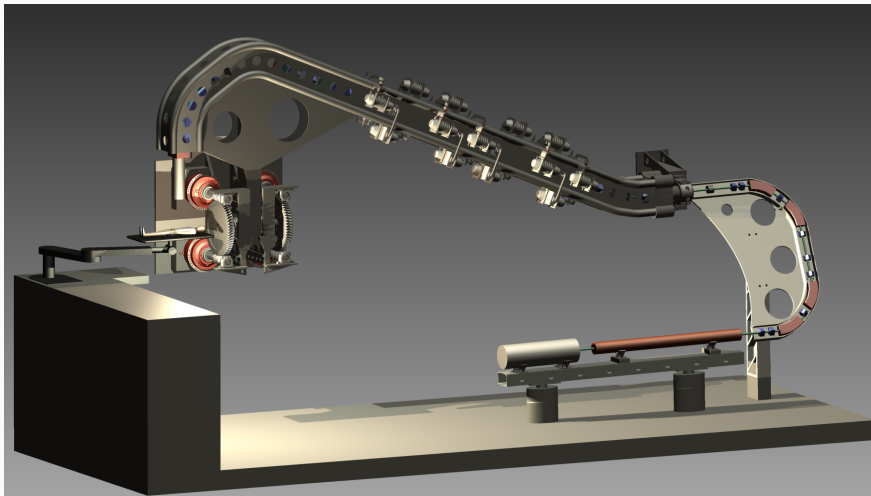
1. Introduction and RF-Track highlights
2. Beamline elements
3. Collective effects
4. Examples of applications
5. Conclusions and future developments

# Introduction and highlights

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# Motivation for developing RF-Track: the TULIP project

A linac for hadron therapy featuring high-gradient S-band backward travelling-wave structures



S. Benedetti, A. Grudiev, and A. Latina, "High gradient linac for proton therapy", Phys. Rev. Accel. Beams 20, 040101 [2017]

# RF-Track highlights

- It handles **Complex 3D field maps** of oscillating RF electromagnetic fields:
  - *Standing-wave*; *Backward*  $\ll$  and *Forward*  $\gg$  travelling-wave fields
  - *Static* electric and magnetic fields
  - Robust interpolation algorithms
- It can simulate particles with **any mass** and **charge**
  - No approximations, like  $\beta \simeq 1$  or  $\gamma \gg 1$ , are made
  - It is used to simulate: *protons*, *ions*, *electrons*, *positrons*, *photons*, *muons*, ... from creation to ultra-relativistic
  - It implements **photocathodes**
  - It can simulate **mixed-species beams**
- Implements **high-order adaptive integration algorithms**
  - Can do **back-tracking**
- Implements several **collective effects**
- It's **modular**, **flexible**, and **fast**

# RF-Track, minimalistic and physics-oriented

RF-Track is written in parallel and fast C++, focusing *only* on accelerator simulation:

- Flexible accelerator description and beam models
- Accurate integration of the equations of motion
- Robust interpolation of the field maps
- Collective effects
- Easy realisation of imperfections and correction algorithms

For *all the rest* (ODE solvers, random number generation, special functions, ...), it relies on two robust and well-known open-source libraries:

- GSL, "Gnu Scientific Library", provides a wide range of mathematical routines such as high-quality random number generators, ODE integrators, linear algebra, and much more
- FFTW, "Fastest Fourier Transform in the West", arguably the fastest open-source library to compute discrete Fourier transforms

RF-Track provides **two user interfaces**: one in Octave and one in Python.

# Tracking, in space and in time

RF-Track implements two beam models:

## 1. Beam moving in space: `Bunch6d()`

- All particles have the same  $S$  position
- The equations of motion are integrated in  $dS$ :  $S \rightarrow S + dS$  (moves the bunch element by element)

## 2. Beam moving in time: `Bunch6dT()`

- All particles are considered at same time  $t$
- The equations of motion are integrated in  $dt$ :  $t \rightarrow t + dt$
- Particles can have  $P_z < 0$  or even  $P_z = 0$  : particles can move backward

For each particle also considers

$m$  : mass [MeV/c<sup>2</sup>],  $Q$  : charge [ $e^+$ ]

$N$  : nb of particles / macroparticle,  $t_0$  : creation time<sup>(\*)</sup>       $\tau$  : lifetime [NEW!]

(\*) only for beams moving in time.

RF-Track can simulate **mixed-species beams**, and the **creation** and **decay** of particles.

# Two tracking environments

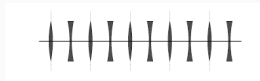
**Lattice:** for integration *in space*

- A list of elements
- Tracks the particles element by element, along the longitudinal direction
- Elements can be misaligned

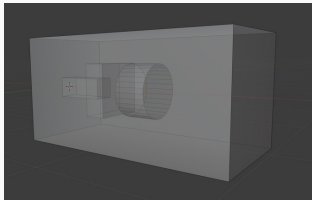
**Volume:** for integration *in time*

- A **portion of 3D space**
- Elements can be placed **anywhere**
- **Element misalignment** via Euler angles (pitch, yaw, roll)
- Allows **element overlap**
- Allows **creation of particles**
- **Can simulate cathodes and field emission**
- Includes **cathode mirror charges**

Lattice



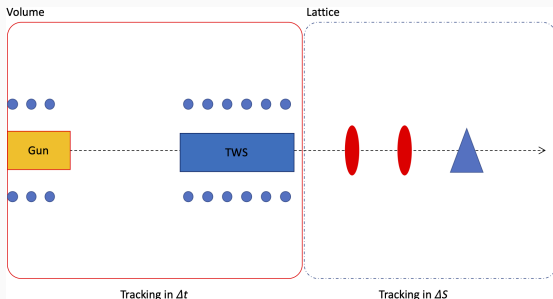
Volume





# Lattice and Volume

Lattice and Volume can be used together or separately



Typically, *Volume* (time integration) is suitable for space-charge dominated regimes, whereas *Lattice* (space integration) is suitable for ultra-relativistic regions of the machine.

*Volumes* can be inserted in a *Lattice*. And *Lattices* can be placed in a *Volume*.

# Example of Volume (Octave)

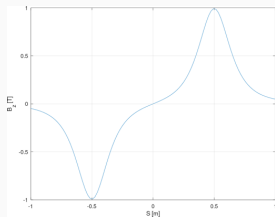
```
%% Load RF-Track
RF_Track;

%% Declare two coils
Cm = Coil(0.01, -1.0, 0.2); % L length [m],
                             % B field at the center of the coil [T],
                             % R radius [m]
Cp = Coil(0.01, +1.0, 0.2);

%% Create a Volume
V = Volume();

%% Add the two coils
V.add(Cm, 0, 0, -0.5);
V.add(Cp, 0, 0, 0.5);

%% Set the boundaries
V.set_s0(-1.0); % -1 m
V.set_s1(+1.0); % +1 m
```



# Example of Lattice (Octave)

```
% load RF-Track
RF_Track;

% create a bunch from phase-space matrix
B0 = Bunch6d(electronmass, 200 * pC, -1, phase_space_matrix);

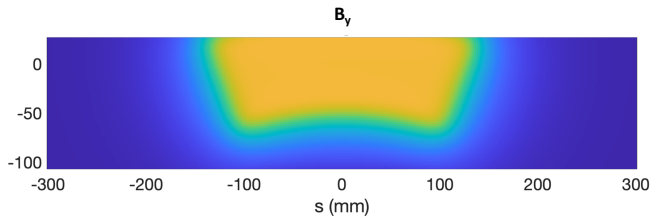
% create a lattice (1 FODO cell)
Lq = 0.4; % m
Ld = 0.6; % m
G = 1.2; % T/m

FODO = Lattice();
FODO.append (Quadrupole (Lq, G));
FODO.append (Drift (Ld));
FODO.append (Quadrupole (Lq, -G));
FODO.append (Drift (Ld));

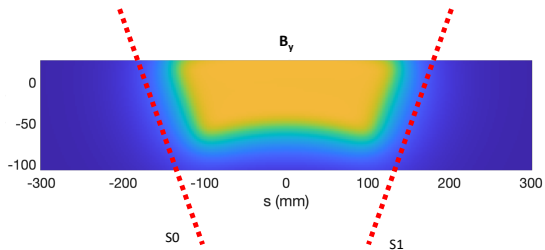
% track the beam
B1 = FODO.track(B0);

% plot the phase space
T1 = B1.get_phase_space("%x %xp %y %yp");
scatter (T1(:,1), T1(:,2), "*");
xlabel ("x [mm]");
ylabel ("x' [mrad]");
```

# Complex simulation scenarios (new feature!)

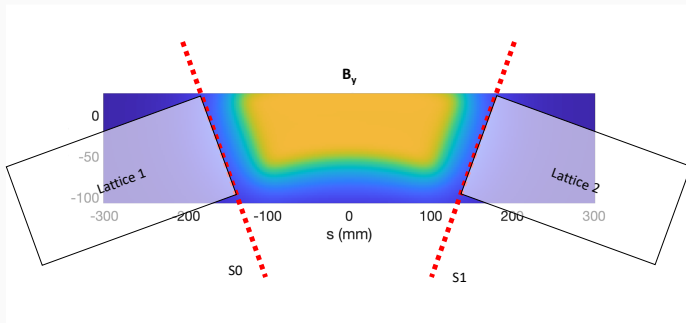


# Complex simulation scenarios (new feature!)



The boundaries of a Volume can have any orientation in space.

# Complex simulation scenarios (new feature!)



One can sandwich a Volume between two Lattices.

# Beamline elements

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# Overview of the beamline elements

## 1. **Standard set of matrix-based symplectic** elements:

- **Sector bend, Quadrupole**
- **Multipoles**
- **Drift** (with an optional constant electric and magnetic fields, can be used to simulate e.g., rbends, or solenoids)



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2. **Field maps** (see next slide)

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## 2. **Field maps** (see next slide)

## 3. **Special elements:**

- **Absorber** (predefined materials: air, water, beryllium, lithium, tungsten, ... )
- 3D analytic fields: **Coil** and **Solenoid, Standing-wave** and **Traveling-wave** structures, **Adiabatic matching devices, Toroidal Harmonics**
- **LaserBeam** for Inverse Compton Scattering simulations
- **Electron Cooler**
- **Twiss table:** tracks through an arbitrary lattice given as Twiss table (phase advances, momentum compaction, 1<sup>st</sup> and 2<sup>nd</sup> order chromaticity are considered)

# Field maps

RF-Track can import several types of oscillating RF field maps, which are interpolated *linearly* or *cubically*

- **1D field maps** (on-axis field)
  - It uses Maxwell's equations to reconstruct the 3D fields off-axis, assuming cylindrical symmetry
- **2D field maps**: given a field on a plane, applies cylindrical symmetry
- **3D field maps** of oscillating electro-magnetic fields
  - It accepts 3D meshes of complex numbers
  - It accepts quarter field maps and performs mirroring automatically

It also provides elements dedicated to **StaticElectric** and **StaticMagnetic** field maps

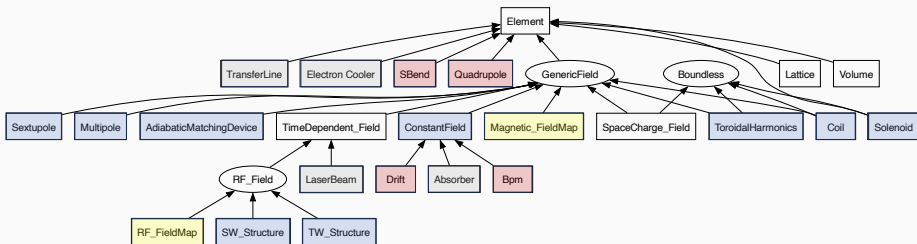
- They ensure curl-free (electric) and divergence-free (magnetic) interpolation of the field





# Integration algorithms

In field maps and analytic fields,

- The default is: **"leapfrog"**:
    - ★ super fast, second-order accurate, symplectic
  
  - **"analytic"** algorithm:
    - ★ integration assuming a locally-constant EM field, symplectic
  
  - **Higher-order, adaptive algorithms** provided by GSL:
    - ★ **"rk2"** Runge-Kutta (2, 3)
    - ★ **"rk4"** 4th order Runge-Kutta
    - ★ **"rkf45"** Runge-Kutta-Fehlberg (4, 5)
    - ★ **"rkck"** Runge-Kutta Cash-Karp (4, 5)
    - ★ **"rk8pd"** Runge-Kutta Prince-Dormand (8, 9)
    - ★ **"msadams"** multistep Adams in Nordsieck form  
(order varies dynamically between 1 and 12)
- (backtracking is possible)

# Element hierarchy



-  Field maps 1D, 2D, 3D
-  Analytic fields 3D
-  Matrix based
-  Special elements

# **Collective and Single-particle effects**

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# Overview of the collective and single-particle effects

## Collective effects:

- **Space-charge**, full 3D, Particle-in-Cell (FFT) or P2P
  - Full computation of electric and magnetic effects
  - Beam-beam effects are automatically included
  - Optionally considers mirror charges at cathode
- **Short-range wakefields:**
  - Karl Bane's approximation
  - 1D user-defined spline, longitudinal monopole or transverse dipole
- Two models of **Long-range wakefields:**
  1. Damped oscillator. Takes modes: frequency, amplitude, and  $Q$  factor
  2. 1D user-defined spline, longitudinal monopole or transverse dipole
- Self-consistent **Beam-loading** effect in TW and SW structures
  - Given: a field map, group velocity and  $Q$  factors along the structure, computes the beam loaded fields

## Single-particle effects:

- **Incoherent Synchrotron Radiation** (from *any* fields)
- **Magnetic multipole kicks** for imperfection studies
- **Multiple Coulomb Scattering** (recently updated!)

## **Example applications**

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# Example applications

RF-Track is currently used for the design, optimisation, and simulation of:

- the **DEFT facility** (CERN, PMB), the **CLIC** and **FCC-ee positron sources** (CERN, IJClab, PSI) and **FCC-ee pre-injector linacs** (CERN, PSI)
- **Linac4** (CERN), **Inverse-Compton Scattering sources** (CERN, IJClab, INFN Ferrara, Korea University), and the **Cooling channel** of a future **Muon Collider** (CERN), etc.

I'll show six examples:

1. ADAM's RFQ
2. ThomX and Inverse Compton Scattering
3. Electron Cooling at LEIR
4. Multiple Coulomb Scattering
5. Muon Cooling Channel
6. CERN's RFQ and Linac4

# 1. ADAM's RFQ

Credits: Veliko Dimov (CERN, ADAM)

«LIGHT is a normal conducting 230 MeV medical proton linear accelerator being constructed by ADAM.

For the commissioning, RFQ beam dynamics simulations were performed with RF-Track by simulating the particles through the 3D field map.»

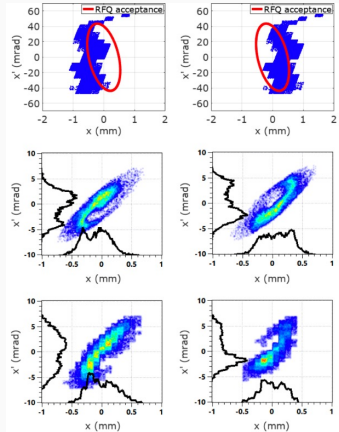
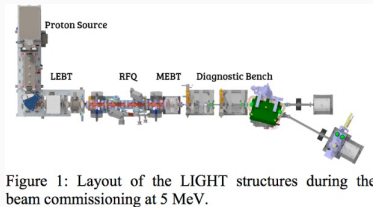
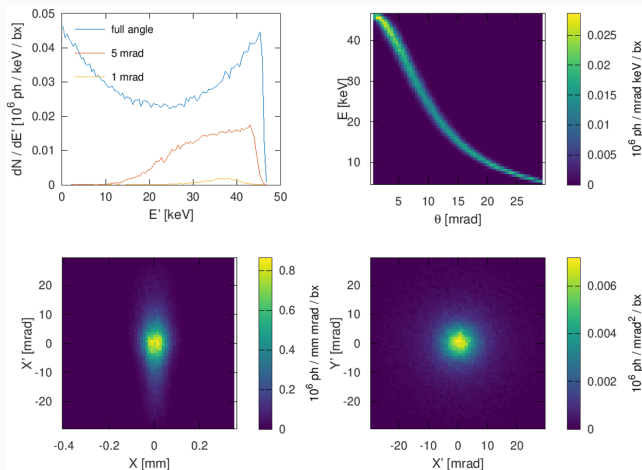


Figure 7: Horizontal phase space plots of the RFQ input beam when steered in the negative and positive  $x$  directions (first row), expected (second row) and the measured (third row) phase space plots after the RFQ for each case.

## 2. LaserBeam element and Inverse Compton Scattering

Generation of hard X-rays via Inverse Compton Scattering at ThomX



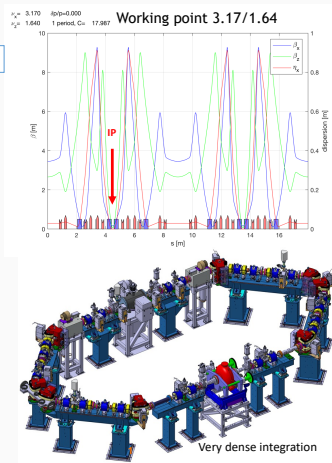
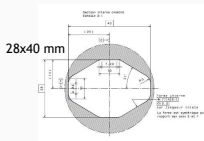
## 2. ThomX simulation (1/4)

RF-Track helped to solve a serious design issue:

- ▶ 8 Dipoles
- ▶ 24 Quadrupoles
- ▶ 12 Sextupoles
- ▶ 2 Kickers
- ▶ 1 Septum
- ▶ 1 RF cavity
- ▶ 12 BPM
- ▶ 12 Correctors

ThomX SR: L = 18 m, T = 60 ns,  $f_{\text{rep}} = 16.7$  MHz

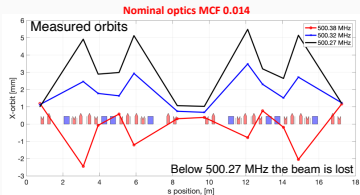
Parameter	Value/Units
Beam energy	50-70 MeV
Bunch Charge	1 nC
Bunch length (rms)	~30 ps
Circumference	18 m
<b>Revolution frequency</b>	<b>16.7 MHz</b>
Current	16.7 mA
<b>RF frequency/Harmonics</b>	<b>500/30 MHz</b>
Momentum compaction	0.0125 - 0.025
Betatron tunes	3.17/1.64
Natural chromaticity	-9/-13
Damping time trans./long.	1.2/0.6 s
Repetition frequency	50 Hz (20 ms)
Beam size at the IP	70 $\mu\text{m}$
Nominal RF Voltage/cavity	300 kV (500 kV max)
Energy loss per turn	1.57 eV



Courtesy of Viacheslav Kubyskiy (IJCLab)

## 2. ThomX simulation (2/4)

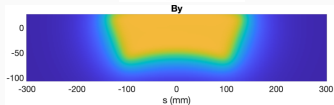
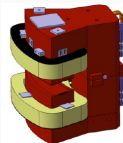
### An unexpected find: shorter circumference



- ▶ The RF frequency is found experimentally to be 0.3 - 0.4 MHz higher than the nominal. What is the reason?
- ▶ Need explicit simulation!

#### Short and small-radius dipoles, long fringe fields

Features of dipoles	
Quantity	14 + 1 (pre-serie)
Radius of curvature	352 mm
Main field $B_0$	0.7 Tesla
Gap	42 mm
Good field region	+/- 20mm
Integral of field	184.59 mT.m
Current max.	275 Amp
Beam energy	from 50 to 70 MeV



Courtesy of Viacheslav Kubytskyi (IJCLab)

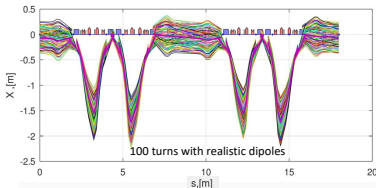
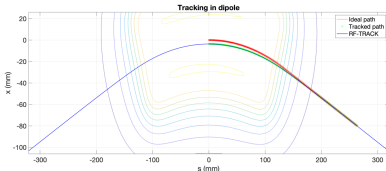
## 2. ThomX simulation (3/4)

### “Experiment on the table” with RF-track

First study to measure ring frequency :

- Lattice with dipoles represented by **SBEND** (usual way) :  $F = 500.02$  MHz
- Lattice with dipoles represented by **VOLUME** with realistic magnetic field :  $F = 500.38$  MHz, dispersive orbit. The same effect as in the experiment!

It was found that the beam trajectory in the dipoles is shorter wrt. to the ideal path => shorter pathlength and so smaller total circumference



Big step in understanding of the problem

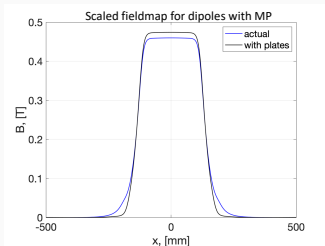
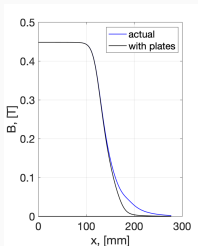
Courtesy of Viacheslav Kubyskiy (IJCLab)

## 2. ThomX simulation (4/4)

### “Experiment on the table” with RF-track

Studies to compensate dipole fringing fields and retrieve nominal frequency by:

- Displacement of dipole
- Adding metallic plates to reduce fringing field
- Mechanical extension of the ring by +12mm

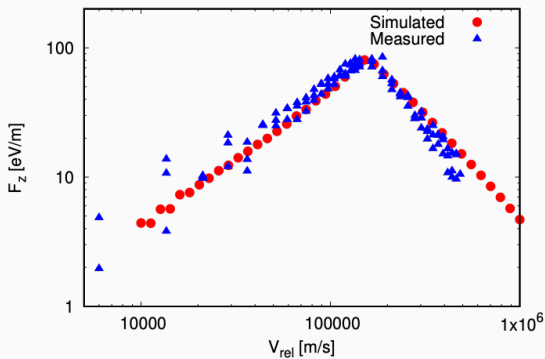


Correct scaling of magnetic field for the magnet with plates allows to recover the nominal frequency

Courtesy of Viacheslav Kubyskyi (IJCLab)

### 3. Electron Cooling at LEIR

In 2019 we measured and benchmarked the cooling force as a function of ion-electron relative velocity measured at LEIR (blue) and simulated with RF-Track (red).

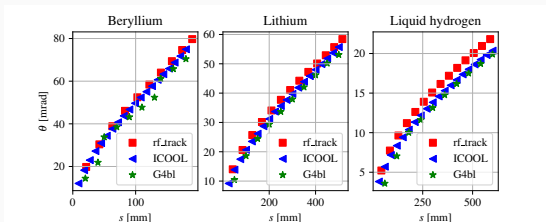


Very good agreement between measurements and simulations.

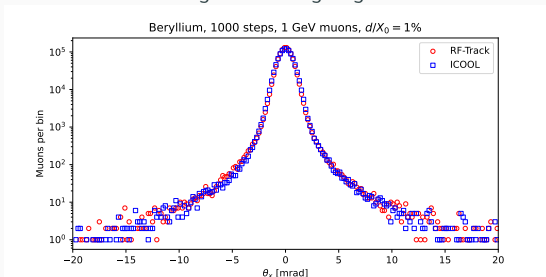


# 4. Absorber element and Multiple Coulomb Scattering

Credits: Bernd Stechauner (CERN)

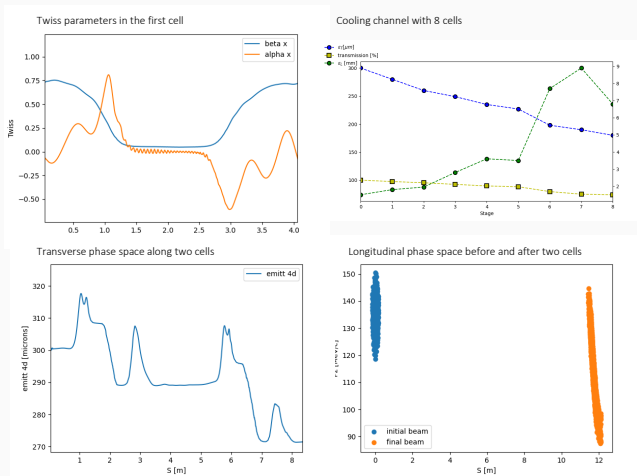


## Large scattering angles



# 5. Muon cooling channel optimisation

Credits: Elena Fol (CERN)



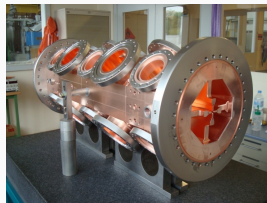
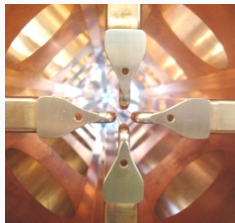
This simulation includes: a constant solenoid field, realistic 3D solenoid, several standing-wave structures, and the absorber, simultaneously together and overlapping.

## 6. CERN's Linac4 RFQ (1/2)

352.2 MHz RFQ (45 keV  $\rightarrow$  3 MeV) injecting into Linac4

4 vanes, 3m length (3x1m modules)  
Entire in-house fabrication (2009-2012)

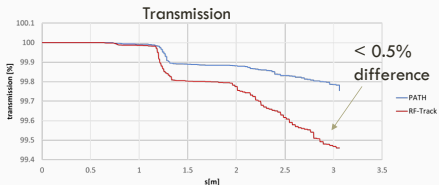
Parameter	Value	Unit
Operating frequency	352.2	MHz
Inter-vane Voltage	78	kV
Kilpatrick factor	1.84	-
Unloaded Quality factor	6700	-
Cavity Coupling factor <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> without beam)	1.59	-
Total dissipated RF Power (without beam)	390	kW



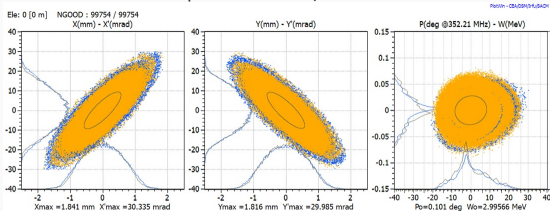
Credits: Giulia Bellodi (CERN)

# 6. CERN's Linac4 RFQ (2/2)

352.2 MHz RFQ injecting into Linac4. Benchmark against PATH



Output 3 MeV beam, PATH vs RF-Track



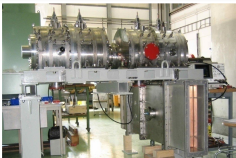
Credits: Giulia Bellodi (CERN)

## 6. CERN's Linac4 (1/3)

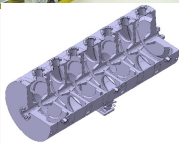
DTL: 3 → 50 MeV  
3 tanks in Cu-plated St5t  
120 drift tubes with PMQs  
FFDD system  
ESS-Bilbao collaboration



CCDTL: 50 → 100 MeV  
7 modules of 3 tanks each  
DTL-like tanks w/ coupling cells  
PMQs+ EMQs (external cells)  
VNIITF/BINP collaboration



PIMS: 100-160 MeV  
12 tanks of 7 pi-mode cells each  
External EMQs  
Soltan Institute/FZ Juelich coll.



Credits: Giulia Bellodi (CERN)

## 6. CERN's Linac4 (2/3)

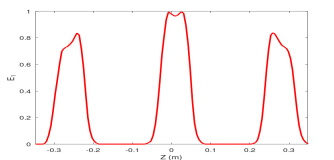
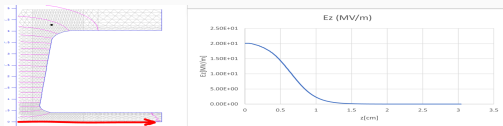
**PATH:** sequence of drifts and zero-length RF gaps giving acceleration kicks (thin gap model).

**RF-Track:** choice to use 1D field maps of on-axis longitudinal electric field obtained with Poisson-Superfish.

The longitudinal electric field is modelled with a generalized Gaussian function whose main parameters are fitted case by case to reproduce the different geometry and match the specified TTF (*ad-hoc* fitting procedure).

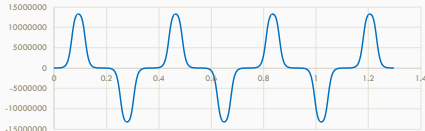
The same procedure is applied to all types of Linac4 cavities (DTL, CCDTL, PIMS): 77% of the Linac is simulated using field maps.

DTL-type gap



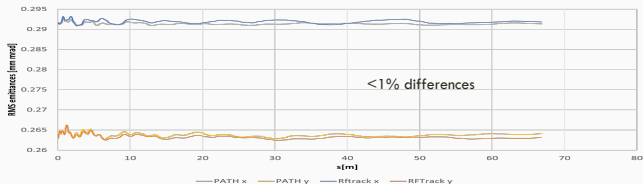
CCDTL tank

PIMS cavity

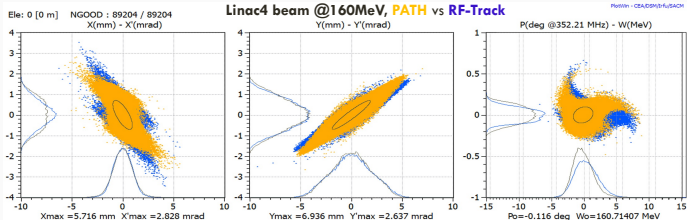


Credits: Giulia Bellodi (CERN)

# 6. CERN's Linac4 (3/3)



Linac4  
with zero  
space  
charge



Credits: Giulia Bellodi (CERN)

# Summary, future developments, and how to get it

## RF-Track:

- Minimalistic, parallel, fast
- Friendly and flexible, it uses Octave and Python as user interfaces
- Ideal for nontrivial optimisation and numerical experimentations
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## “Official” documentation:

- <https://zenodo.org/record/4580369>

**Pre-compiled binaries** and **more up-to-date documentation** are available here:

- <https://gitlab.cern.ch/rf-track>

The end.

Thank you for your attention!

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