

# Quarkonium as a probe of deconfinement

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A. Andronic - University of Münster



- Quarkonium as probe of deconfinement
- A brief overview of data
- Models in brief
- **Quarkonium (and open HQ) in the statistical hadronization model**



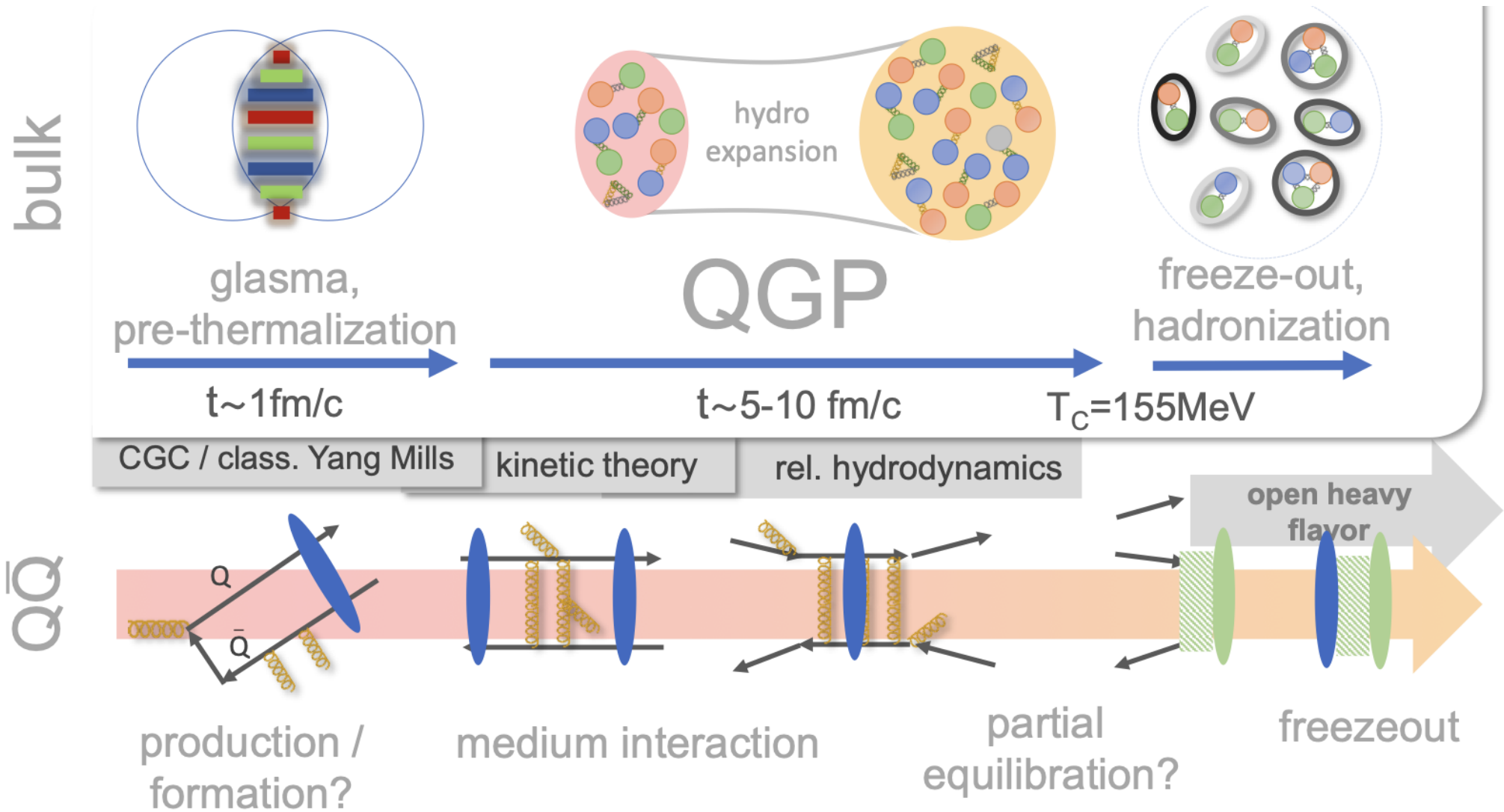
Andronic, Braun-Munzinger, Redlich, Stachel, [Nature 561 \(2018\) 321](#)

...+ Brunßen, Crkovská, Mazeliauskas, Vislavicius, Völkl, [JHEP 07 \(2021\) 035](#); [2308.14821](#)

# The Quark-Gluon Plasma

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A. Rothkopf, [Phys. Rep. 858 \(2020\) 1](#)

# Charmonium and deconfined matter

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the original idea: Matsui & Satz, [Phys.Lett. B 178 \(1986\) 178](#)

*"If high energy heavy-ion collisions lead to the formation of a hot quark-gluon-plasma, then color screening prevents  $c\bar{c}$  binding in the deconfined interior of the interaction region."*

Refinements: "sequential suppression":

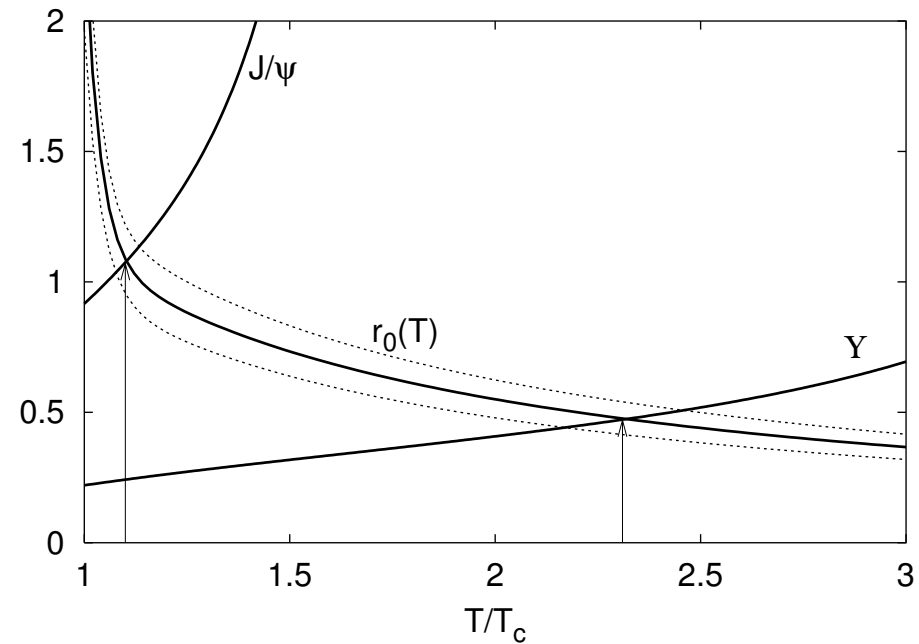
Digal et al., [PRD 64 \(2001\) 75](#)

no  $q\bar{q}$  bound state if

$$r_{q\bar{q}}(T) > r_0(T) \simeq \frac{1}{g(T)T}$$

$r_0$  Debye length in QGP

$\Rightarrow q\bar{q}$  "thermometer" of QGP

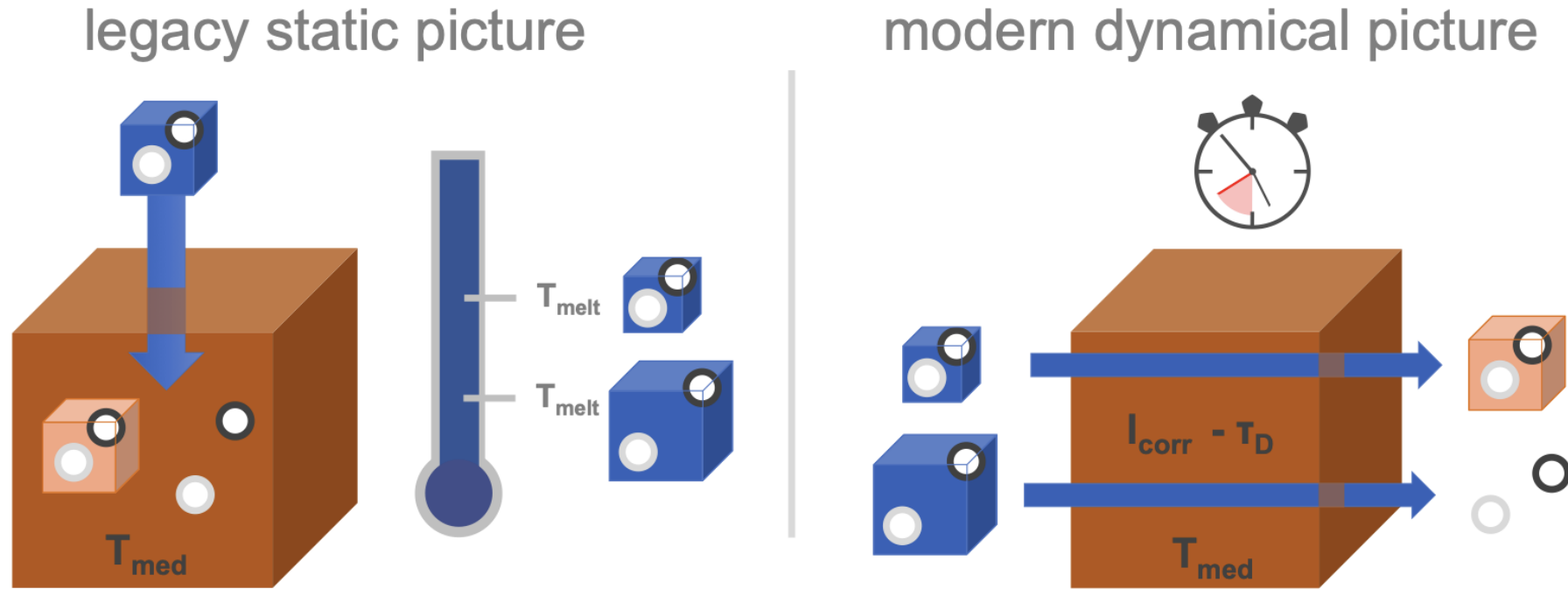


Thermal picture ( $n_{partons} = 5.2T^3$  for 3 flavors)

for  $T=500$  MeV:  $n_p \simeq 84/\text{fm}^3$ , mean separation  $\bar{r}=0.2$  fm  $< r_{J/\psi}$



# Quarkonium pictures

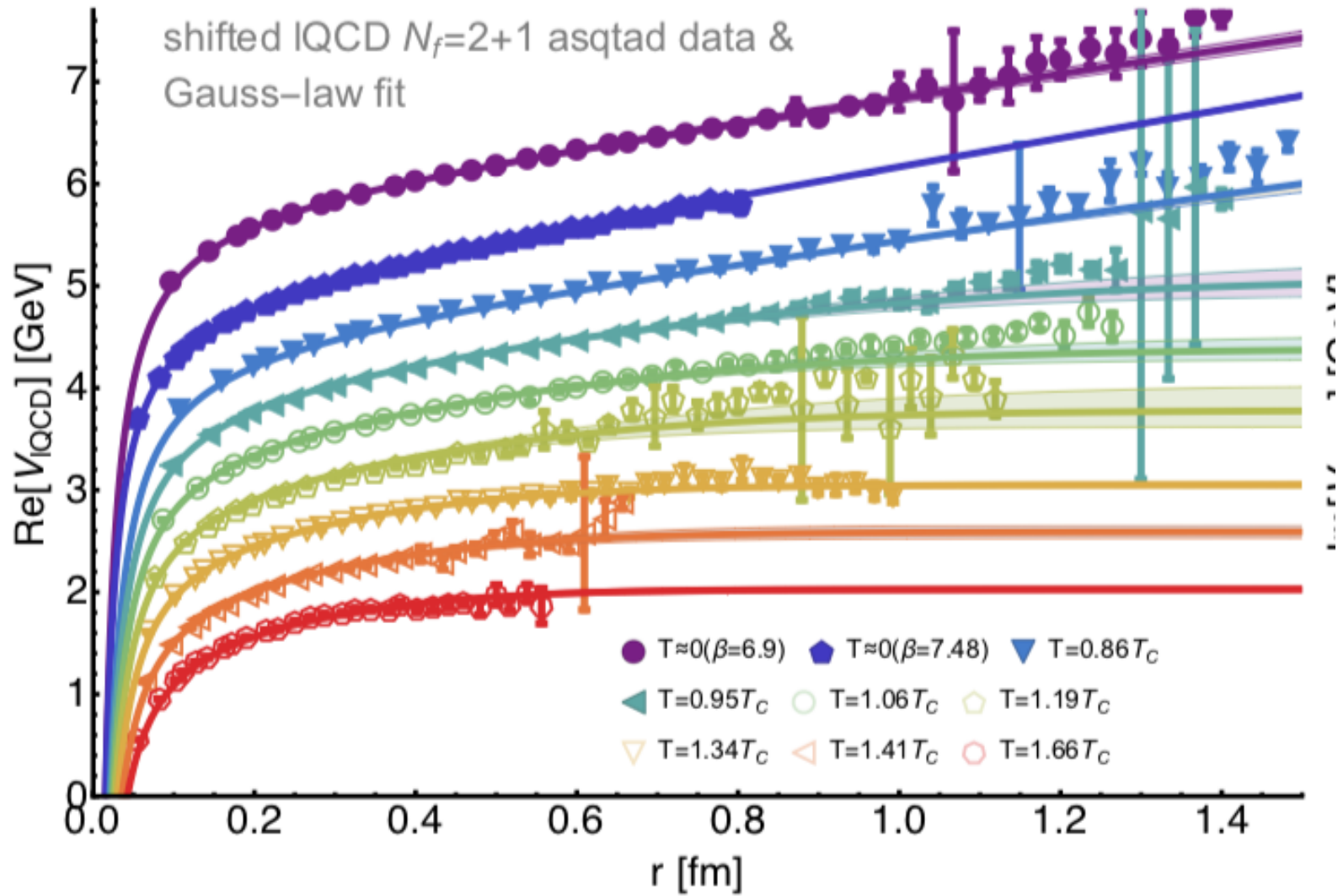


A. Rothkopf, [Phys. Rep. 858 \(2020\) 1](#)

for  $T(\tau)$  we anyway have more basic (bulk) observables (collective flow)

$$T \sim \Lambda_{QCD} \sim E_{b, Q\bar{Q}}^{vac} \quad (m_Q \gg \Lambda_{QCD})$$

# Heavy-quark potential - Lattice QCD



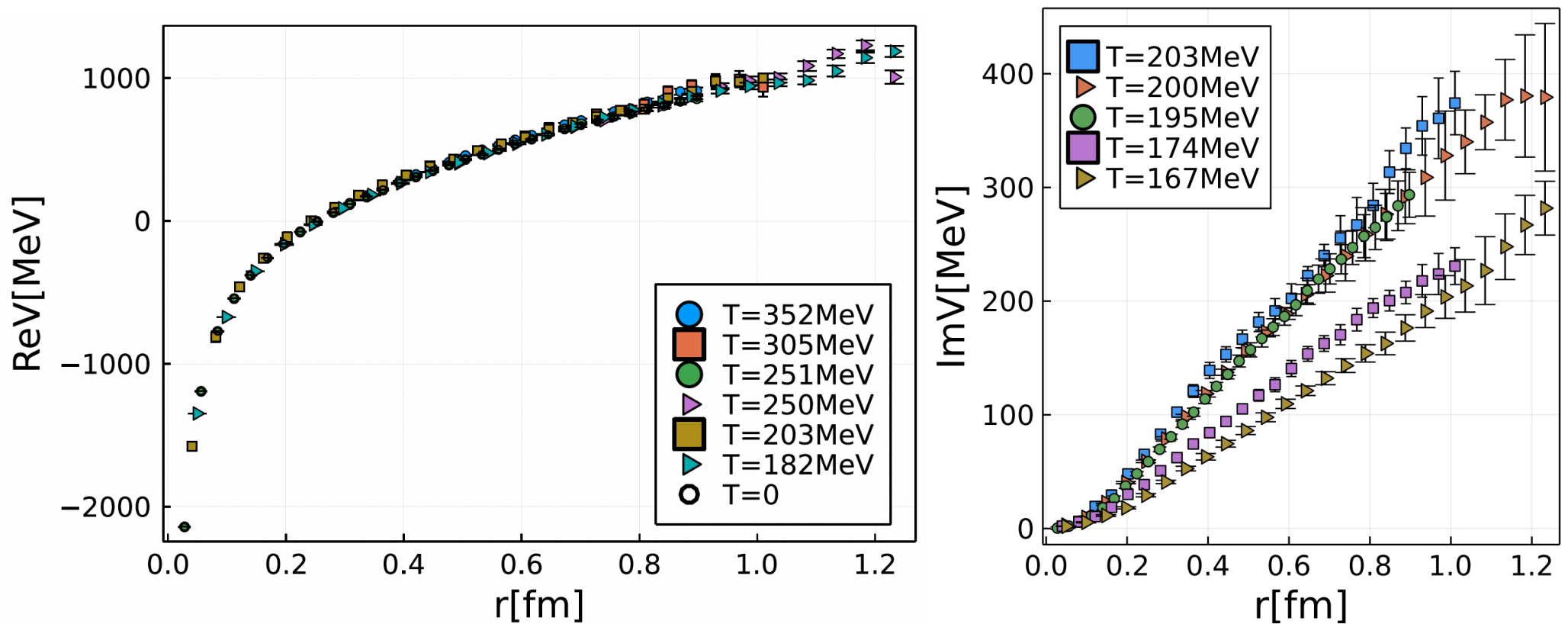
A. Rothkopf, *Phys. Rep.* 858 (2020) 1

$$(T_C \simeq 174 \text{ MeV})$$

# Heavy-quark potential - Lattice QCD

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HotQCD coll., [arXiv:2308.16587](https://arxiv.org/abs/2308.16587)

$\text{Re}V$ : not screened!

$\text{Im}V$ : large, increases with distance

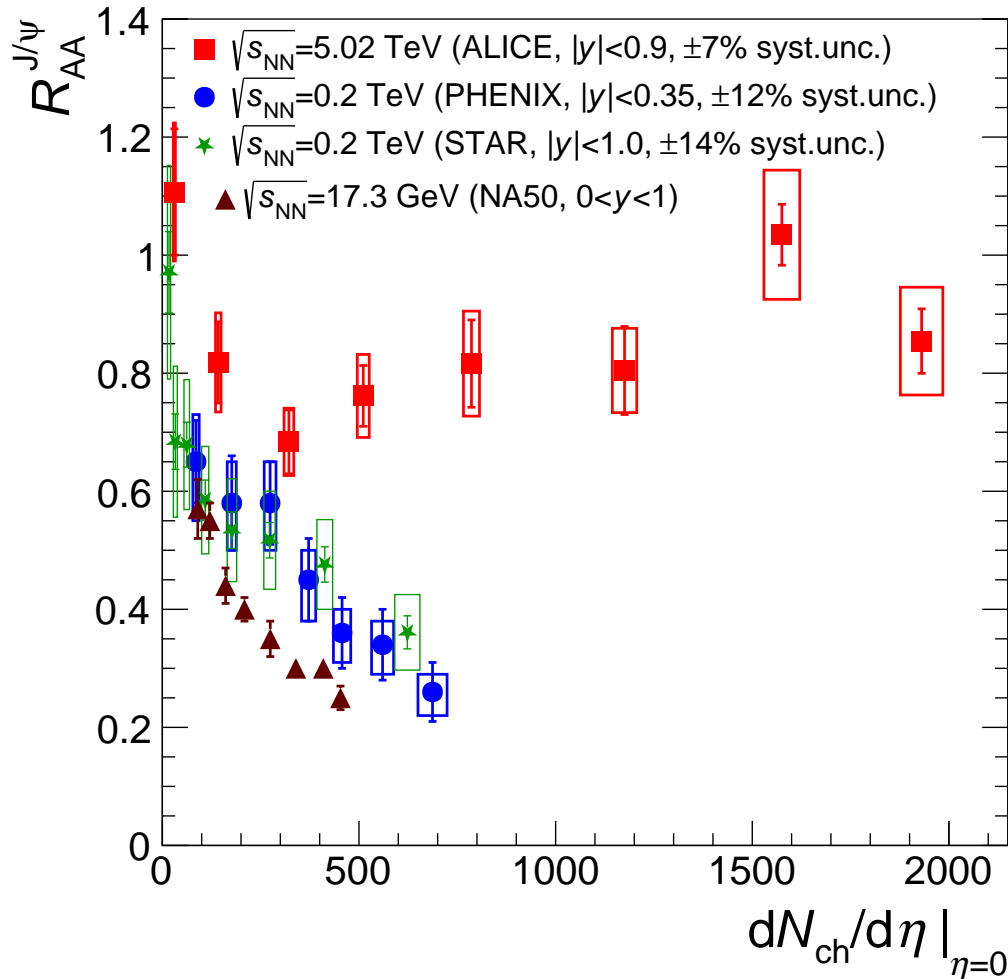
→ “melting of quarkonium is not related to color screening” (P.Petreczky)

# Charmonium data: SPS, RHIC, LHC

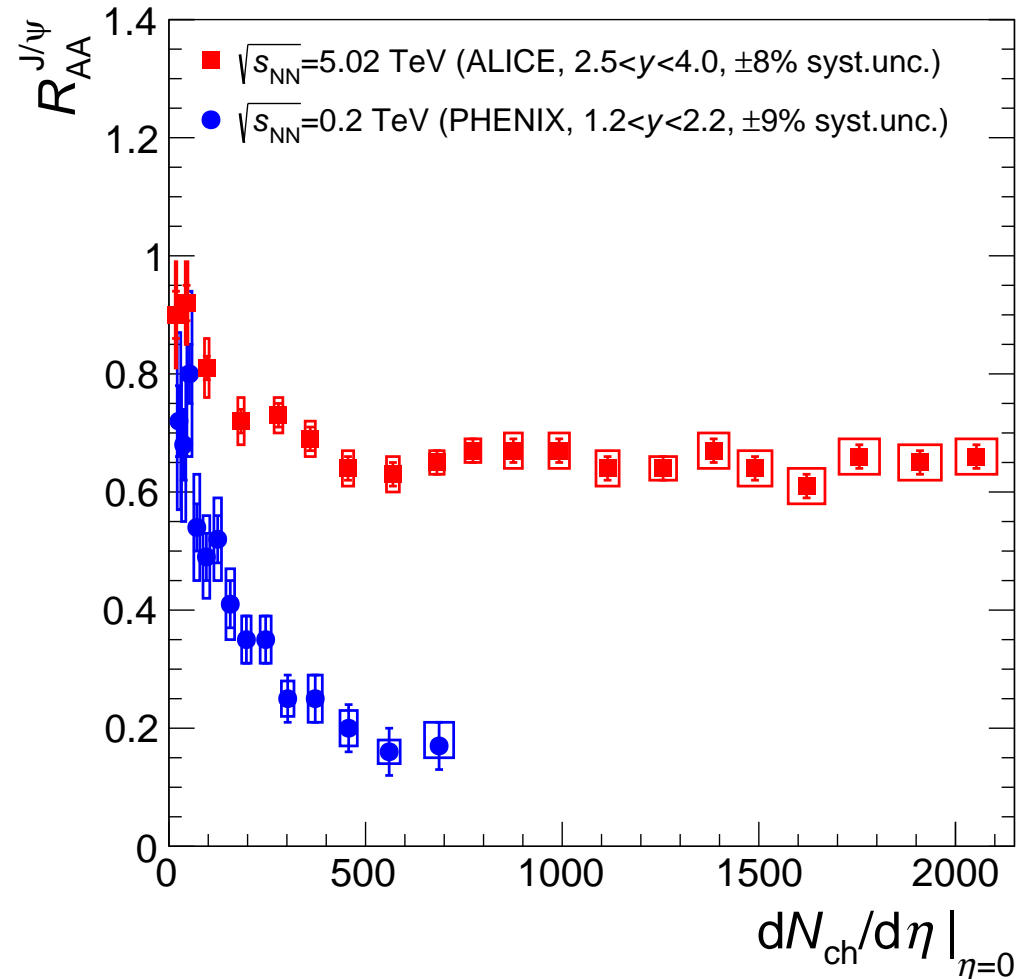
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midrapidity



forward rapidity



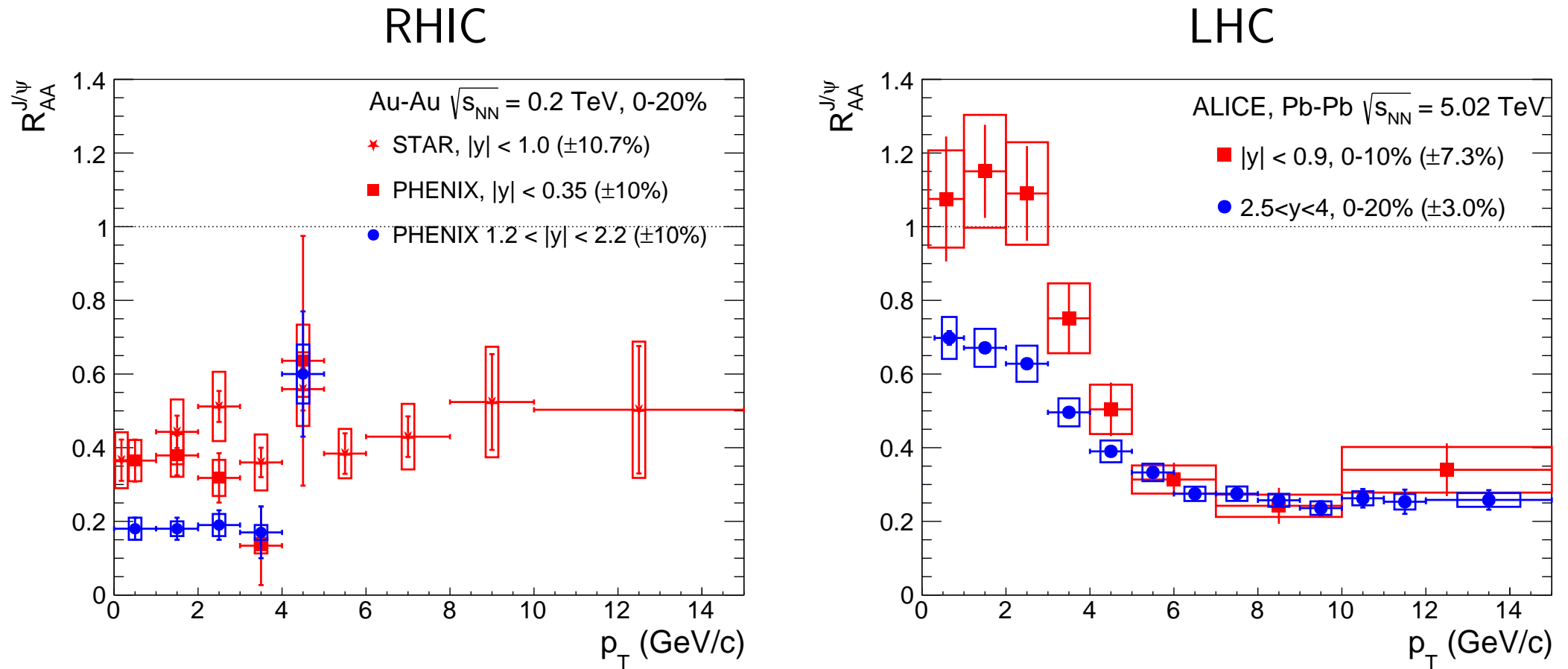
suppression at lower energies, but not obviously a sequential one  
at the LHC another effect offsets the dissociation



# Charmonium data: RHIC and LHC

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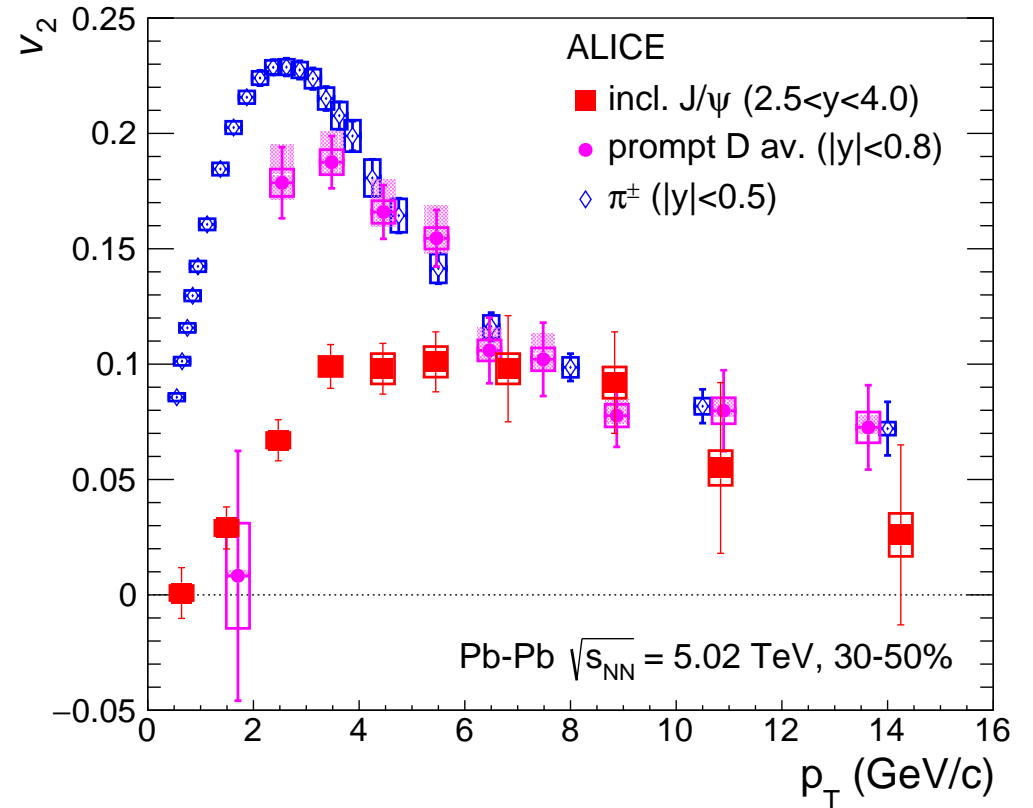
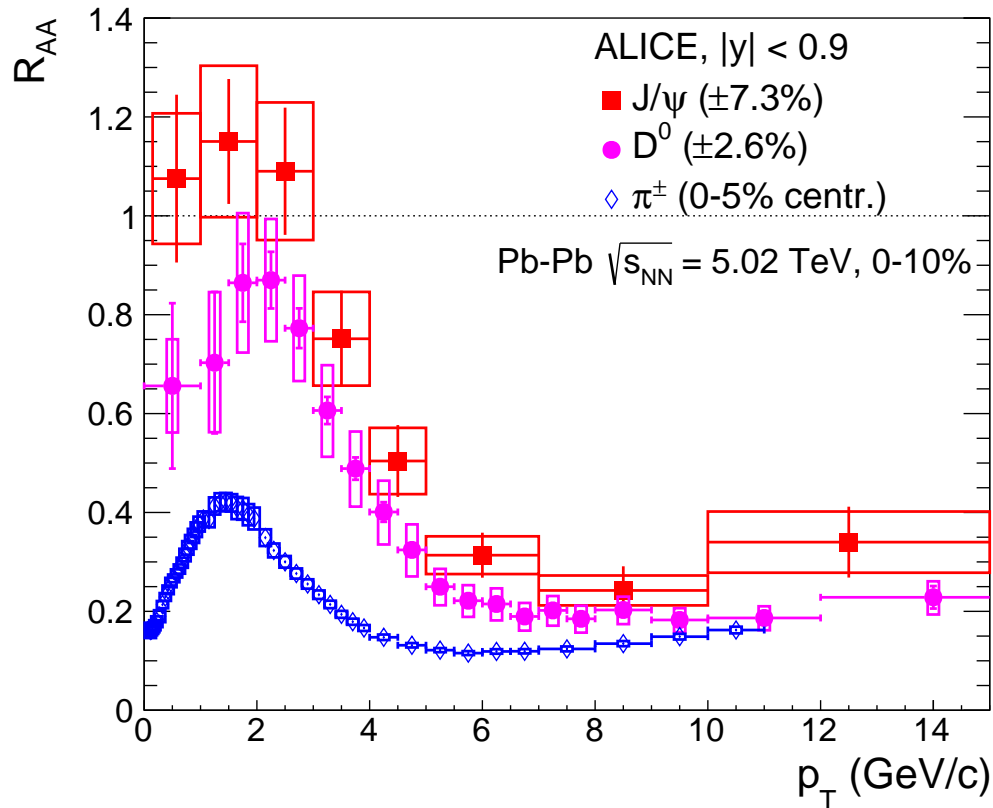


production at low  $p_T$  is enhanced at the LHC compared to RHIC  
...stronger at midrapidity

# Charmonium data at the LHC: in perspective

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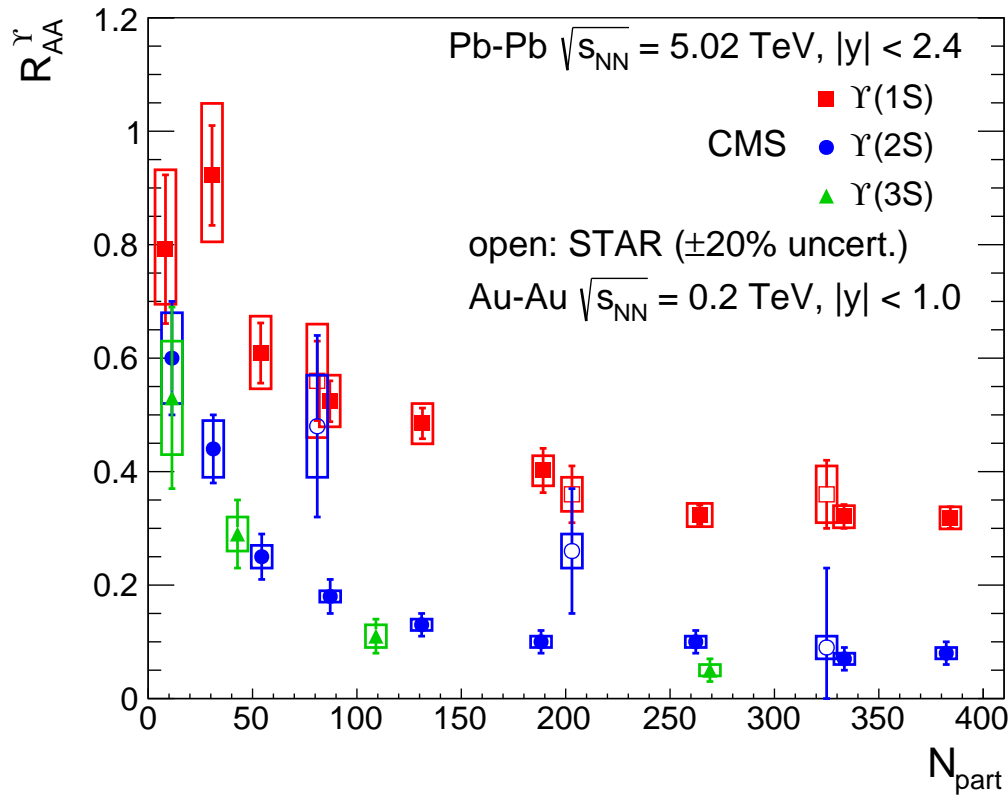
ALICE, [arXiv:2303.13361](https://arxiv.org/abs/2303.13361), [arXiv:2110.09420](https://arxiv.org/abs/2110.09420), [arXiv:1802.09145](https://arxiv.org/abs/1802.09145)

a very clear hierarchy at low/intermediate  $p_T$

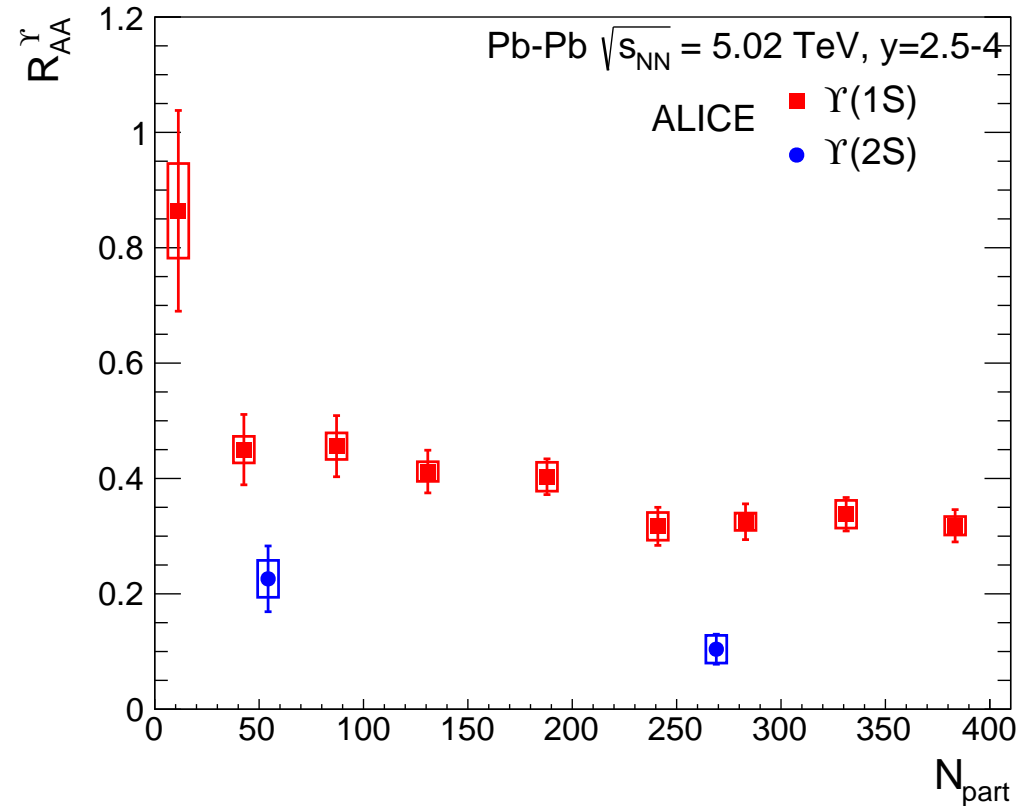
charm production is a pQCD process, pion production largely a thermal process

# Bottomonium data: RHIC and LHC

midrapidity



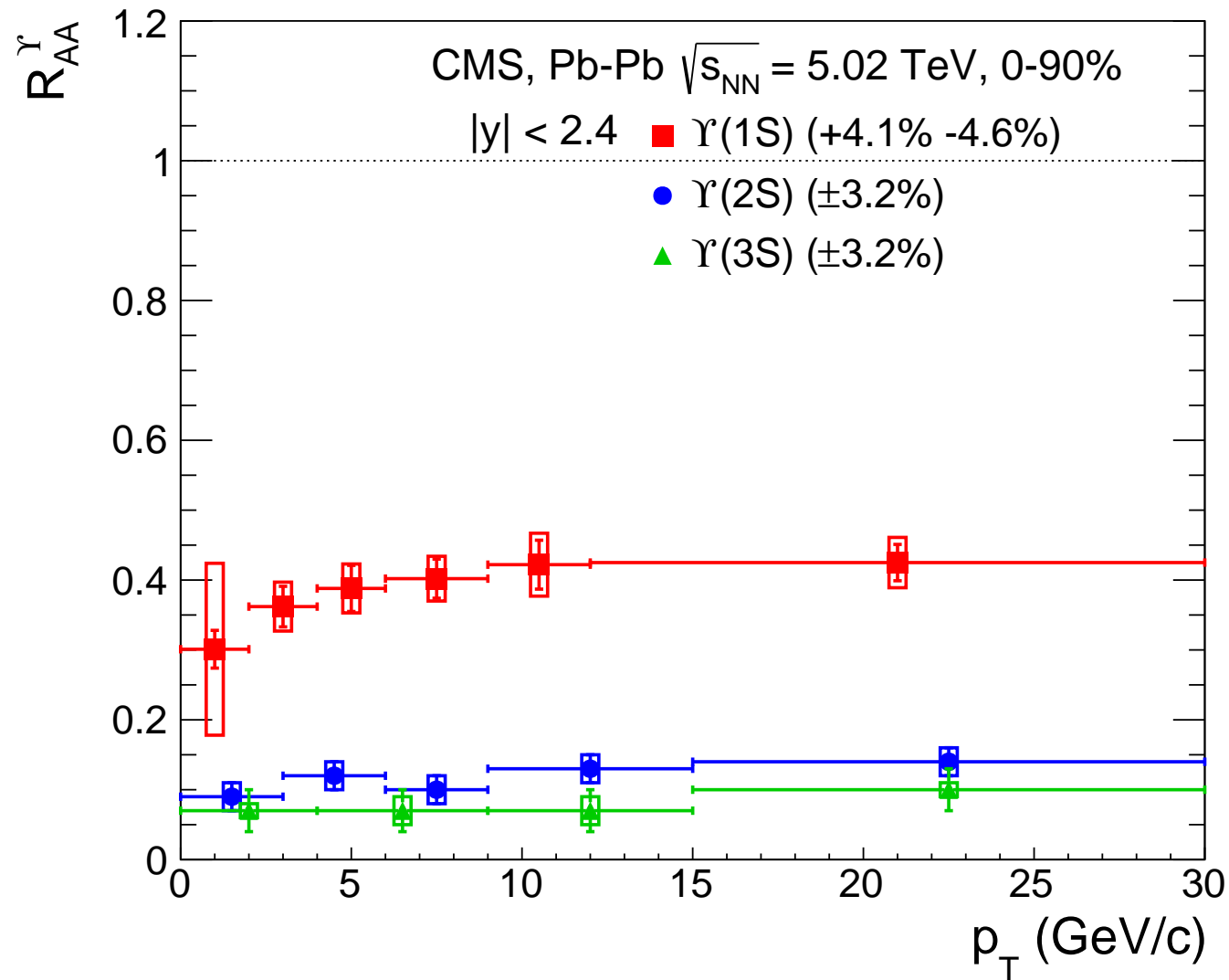
forward rapidity



significant suppression, hierarchy between states (sequential?)

not significantly different at LHC and RHIC (except perhaps  $\Upsilon(2S)$ )

# Bottomonium data at the LHC

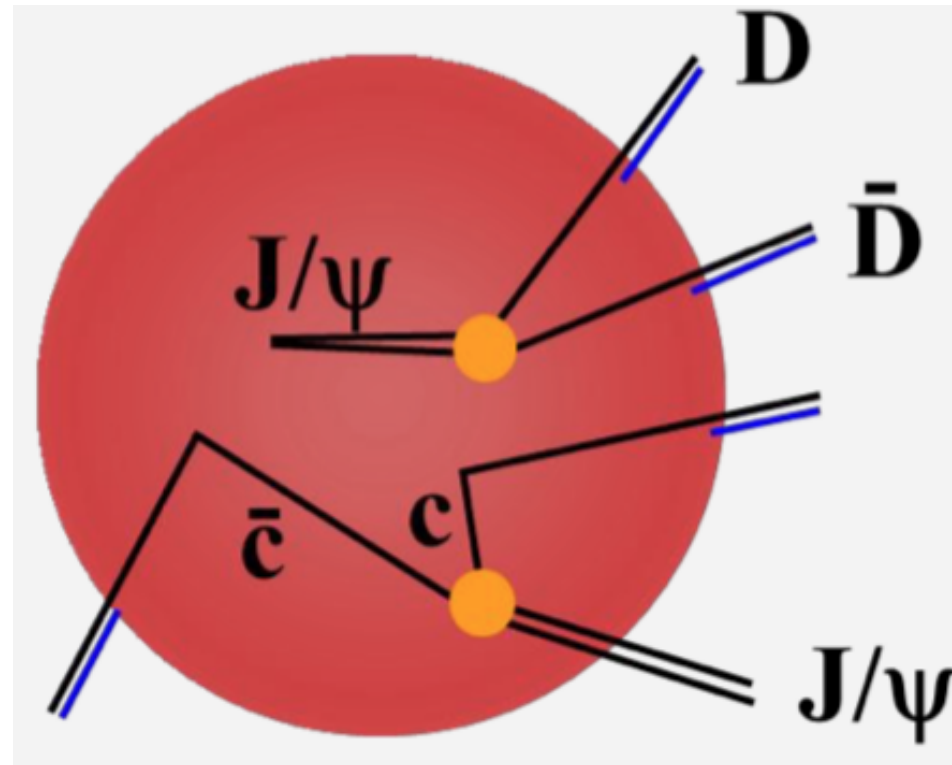


weak  $p_T$  dependence (dissociation expected to be stronger at low  $p_T$ )

# There is dissociation and there is (re)generation

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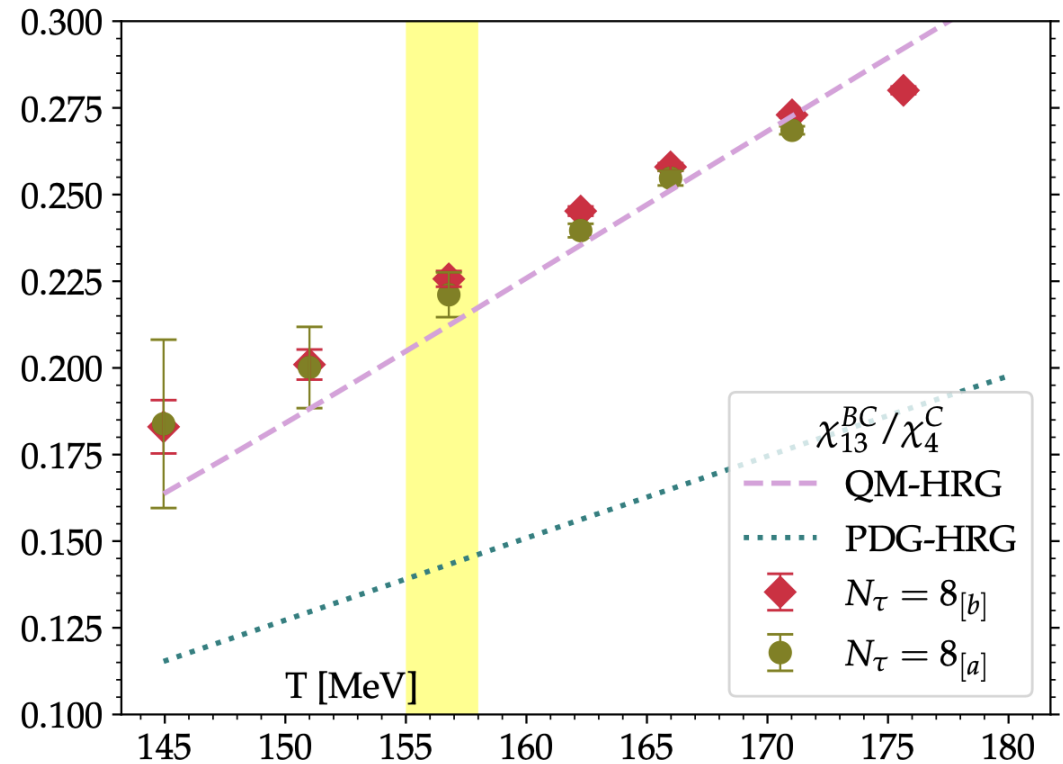
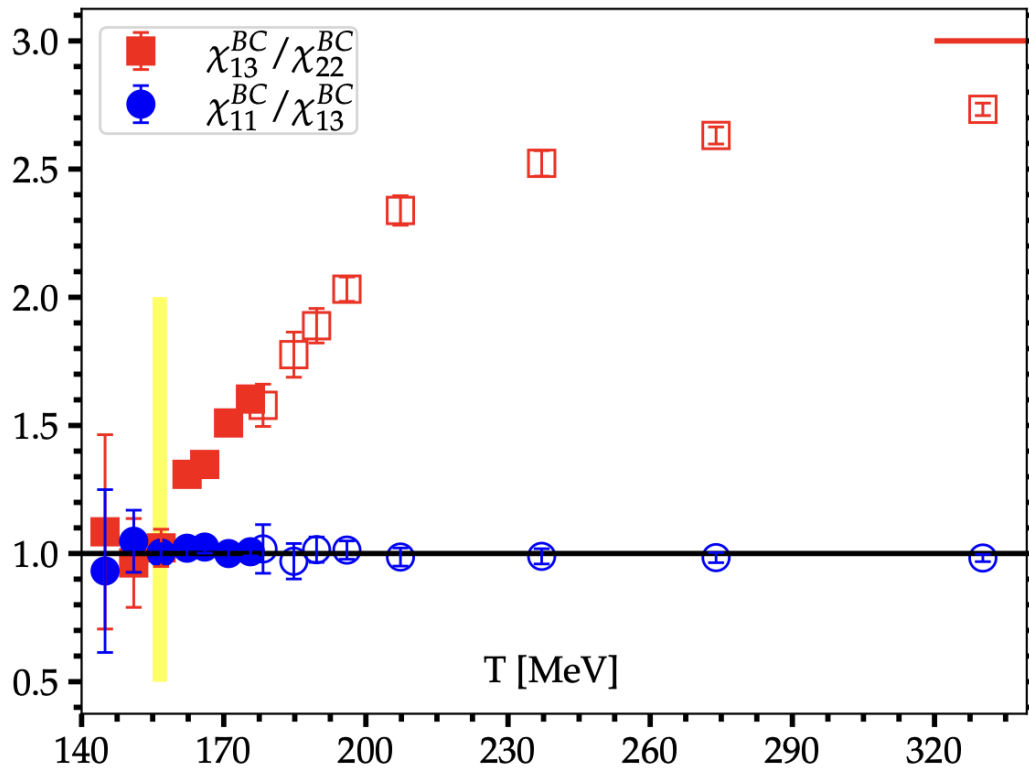
This picture is implemented in models in 2 basic ways:

- 1) statistical hadronization: full screening, generation at hadronization ( $c, \bar{c}$  produced in initial scattering and fully thermalized in QGP)
- 2) transport: continuous destruction and (re)generation, also from different  $c, \bar{c}$  (time evolution of  $T$  constrained by other measurements)

# Charm in QGP - the lattice view

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Bazavov et al., [arXiv:2312.12857](https://arxiv.org/abs/2312.12857)

$$\chi_{11}^{BC} = \chi_{1m}^{BC} = P_B^C, \quad m \text{ odd};$$

$$\chi_{13}^{BC} / \chi_4^C \sim P_B^C / P^C$$

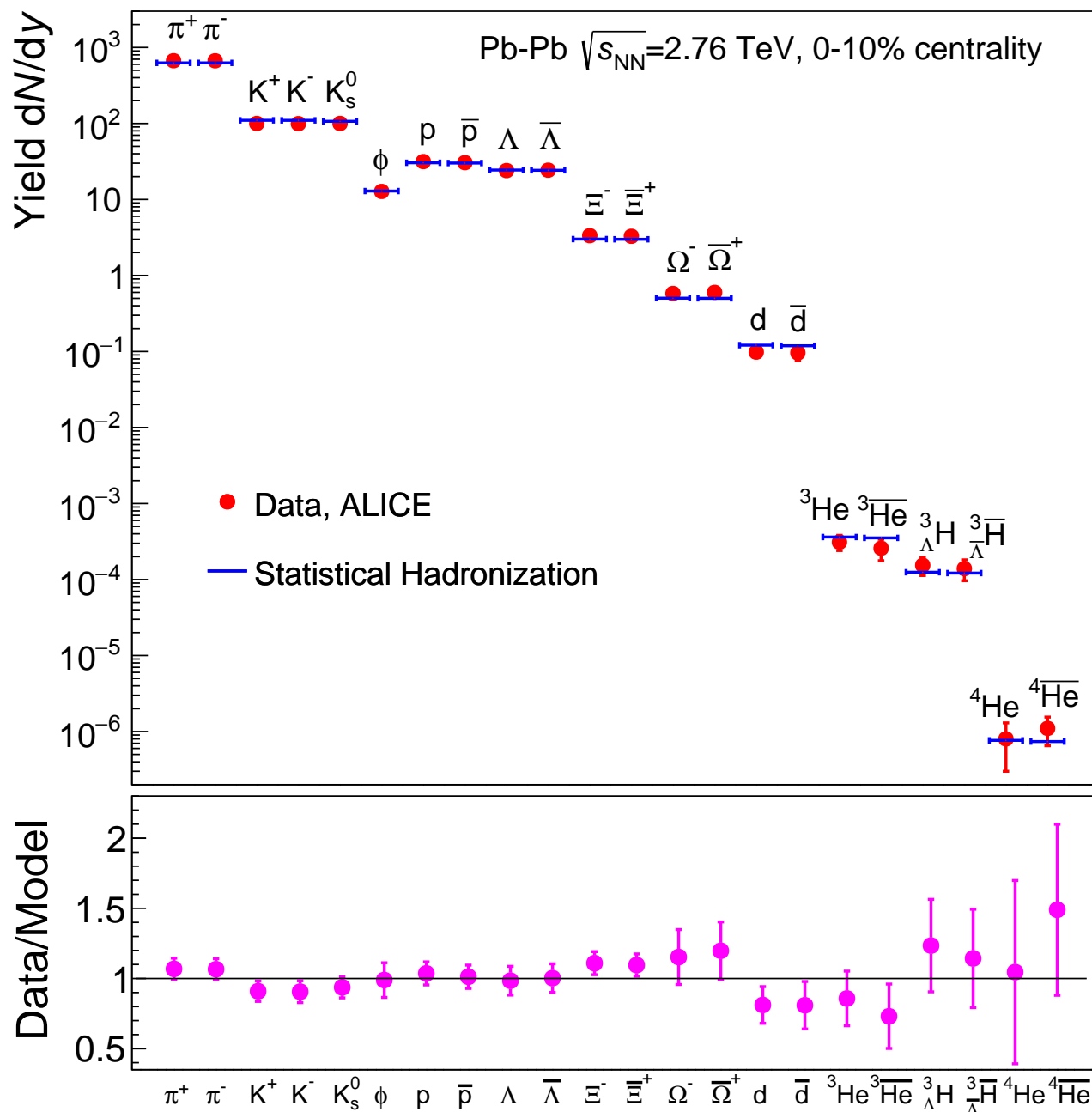
Indication of charm-quark dofs at  $T_c$ , but “pure-quark” state at  $\simeq 200$  MeV

Clear need of an enhanced charm-baryon spectrum wrt PDG

# Thermal fit – LHC, Pb–Pb, 0-10%

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matter and antimatter produced in equal amounts

$$T_{CF} = 156.6 \pm 1.7 \text{ MeV}$$

$$\mu_B = 0.7 \pm 3.8 \text{ MeV}$$

$$V_{\Delta y=1} = 4175 \pm 380 \text{ fm}^3$$

$$\chi^2/N_{df} = 16.7/19$$

*S*-matrix treatment ( $p, \bar{p}$ )

remarkably, loosely-bound objects are also well described ( ${}^3\Lambda\text{H}$ : 25% B.R.)

hadronization as bags of quarks and gluons?

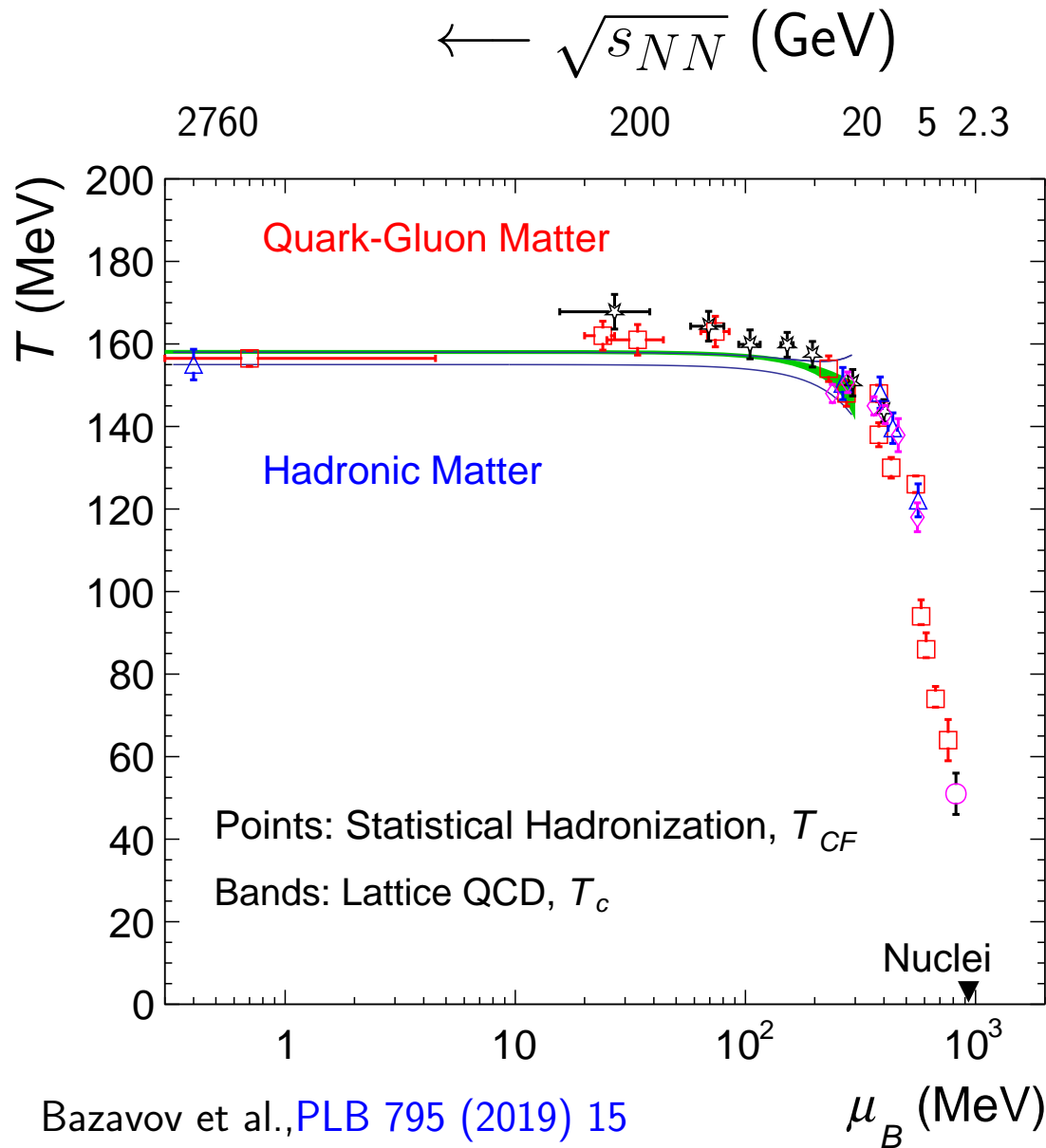
hadron spectrum beyond PDG  $\rightarrow$

same  $T_{CF}$  [NPA 1010 \(2021\) 122176](#)

# The phase diagram of QCD

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at LHC, remarkable “coincidence” with Lattice QCD results

at LHC ( $\mu_B \simeq 0$ ): purely-produced (anti)matter ( $m = E/c^2$ ), as in the Early Universe

$\mu_B > 0$ : more matter, from “remnants” of the colliding nuclei

$\mu_B \gtrsim 400 \text{ MeV}$ : the critical point awaiting discovery  
(RHIC BES / FAIR)

Bazavov et al., [PLB 795 \(2019\) 15](#)

Borsanyi et al., [PRL 125 \(2020\) 052001](#)

see refs. in [Nature 561 \(2018\) 321](#)

points: independent analyses of same data  $\rightarrow$  “model/code uncert.” are small



# The statistical hadronization model

Braun-Munzinger, Stachel, PLB 490 (2000) 196; NPA 789 (2006) 334, PLB 652 (2007) 259

All charm quarks are produced in primary hard collisions ( $t_{c\bar{c}} \sim 1/2m_c \simeq 0.1 \text{ fm}/c$ )

...survive and thermalize in QGP (thermal, but not chemical equilibrium)

charmed hadrons are formed at chemical freeze-out together with all hadrons  
“generation” ...no  $J/\psi$  survival in QGP (full screening)

(if supported by data)  $J/\psi$  loses status as “thermometer” of QGP

...and gains status as a powerful observable for the QCD phase boundary

Predicts  $p_T$  spectra too: hydrodynamics (MUSIC) (input for  $\beta_T$  in blast-wave formula)

[JHEP 07 \(2021\) 035](#), [arXiv:2308.14821](#)

# SHM for charm (SHMc)

pQCD production, "throw in":  $N_{c\bar{c}} = 9.6 \rightarrow g_c = 30.1$  ( $I_1/I_0 = 0.974$ )

LHC, central collisions

assume:

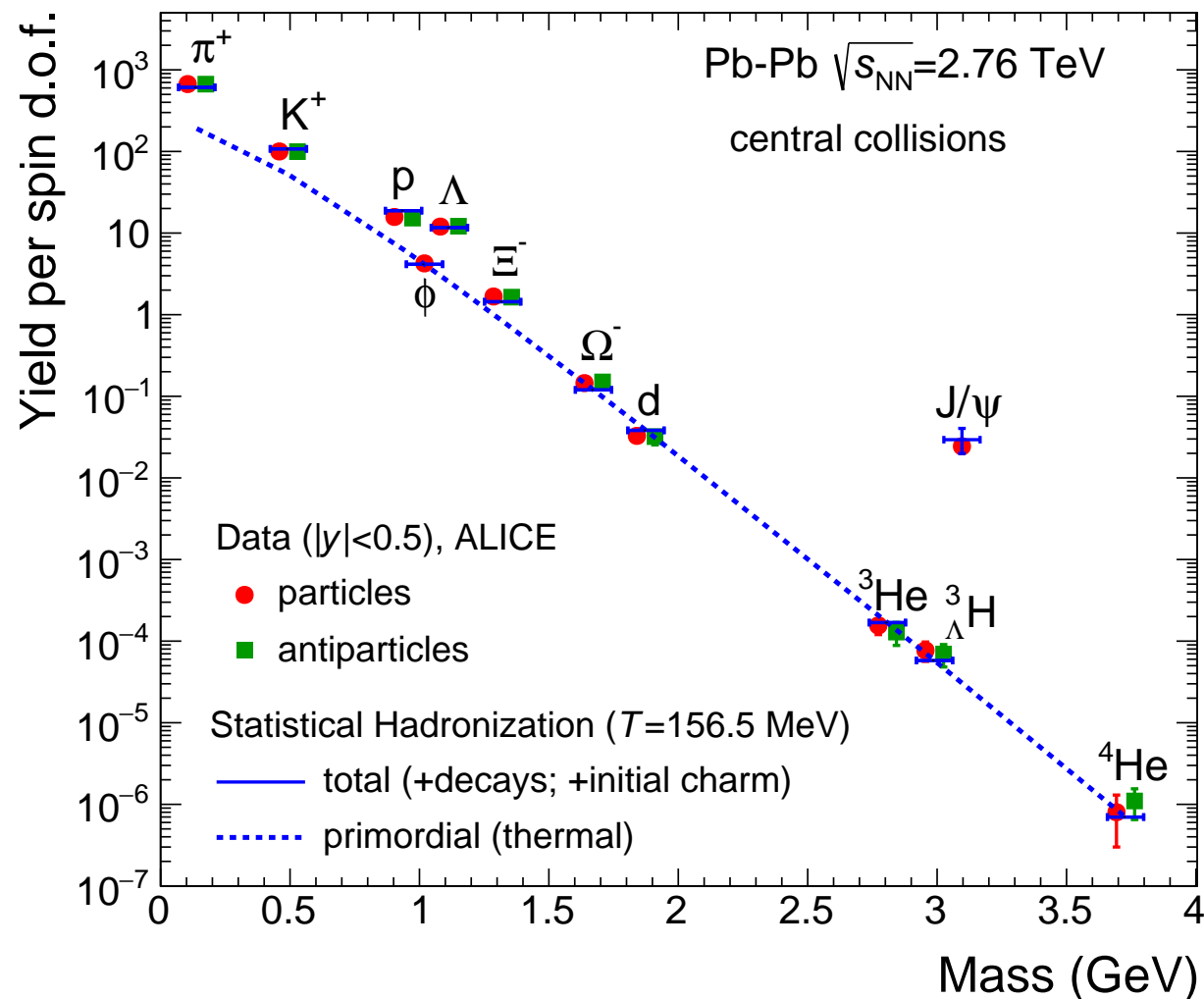
- full thermalization of  $c, \bar{c}$   
("mobility" in  $V \simeq 4000 \text{ fm}^3$ )

- full color screening  
(Matsui-Satz)

Braun-Munzinger, Stachel, [PLB 490 \(2000\) 196](#)

Model predicts all charm  
chemistry ( $\psi(2S), X(3872)$ )

$\pi, K^\pm, K^0$  from charm included in the thermal fit  
(0.7%, 2.9%, 3.1% for  $T=156.5 \text{ MeV}$ )



# SHMc: method and inputs

Braun-Munzinger, Stachel, [PLB 490 \(2000\) 196](#), [NPA 690 \(2001\) 119](#)

- Thermal model calculation (grand canonical)  $T, \mu_B$ :  $\rightarrow n_X^{th}$
- $N_{c\bar{c}}^{dir} = \frac{1}{2}g_c V (\sum_i n_{D_i}^{th} + n_{\Lambda_i}^{th}) + g_c^2 V (\sum_i n_{\psi_i}^{th} + n_{\chi_i}^{th})$
- $N_{c\bar{c}} \ll 1 \rightarrow$  Canonical (Cleymans, Redlich, Suhonen, Z. Phys. C51 (1991) 137):

Gorenstein, Kostyuk, Stöcker, Greiner, [PLB 509 \(2001\) 277](#)

$$N_{c\bar{c}}^{dir} = \frac{1}{2}g_c N_{oc}^{th} \frac{I_1(g_c N_{oc}^{th})}{I_0(g_c N_{oc}^{th})} + g_c^2 N_{c\bar{c}}^{th} \rightarrow g_c(N_{part}) \text{ (charm fugacity)}$$

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Outcome:  $N_D = g_c V n_D^{th} I_1/I_0 + N_D^{corona}$ ,  $N_{J/\psi} = g_c^2 V n_{J/\psi}^{th} + N_{J/\psi}^{corona}$

Inputs:  $T, \mu_B, V_{\Delta y=1} (= (dN_{ch}^{exp}/dy)/n_{ch}^{th}), N_{c\bar{c}}^{dir}$  (exp. or pQCD)

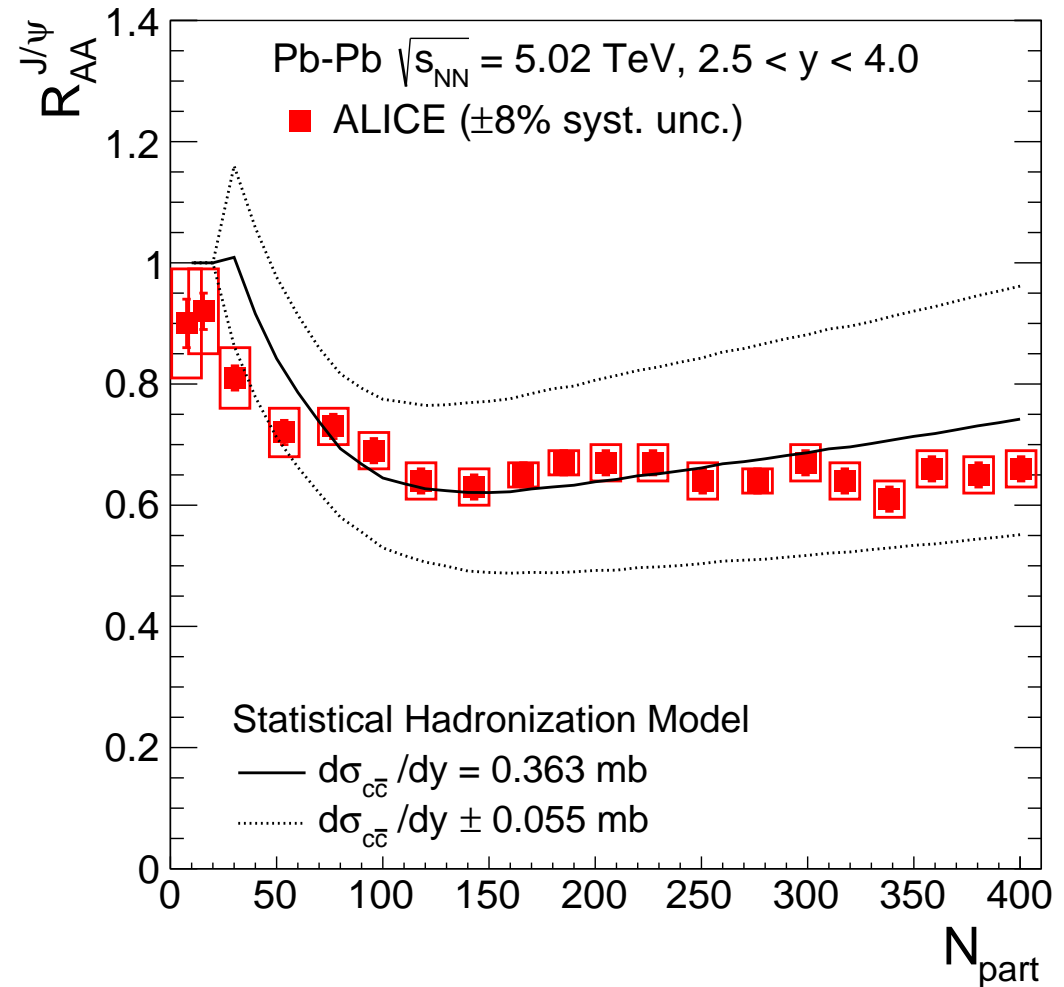
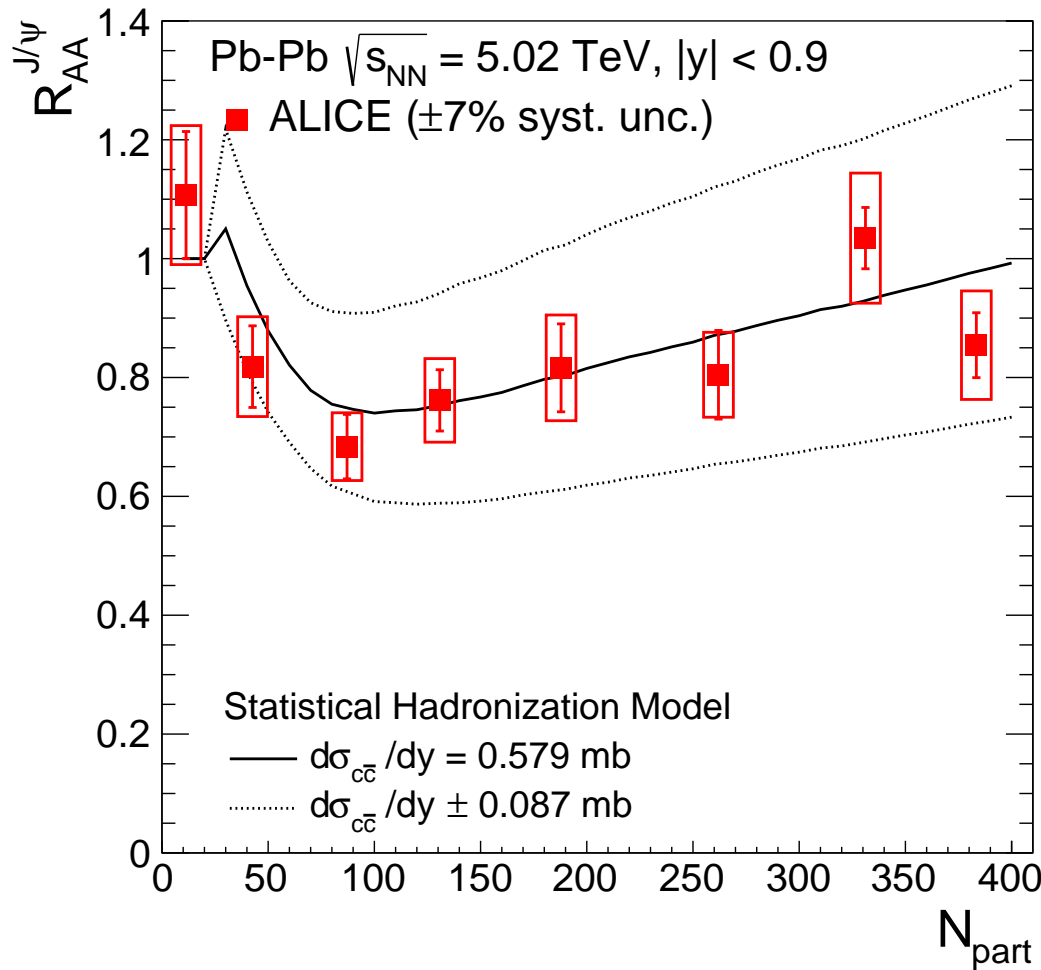
Assumed minimal volume for QGP:  $V_{QGP}^{min} = 200 \text{ fm}^3$

# SHMc and charmonium data at the LHC

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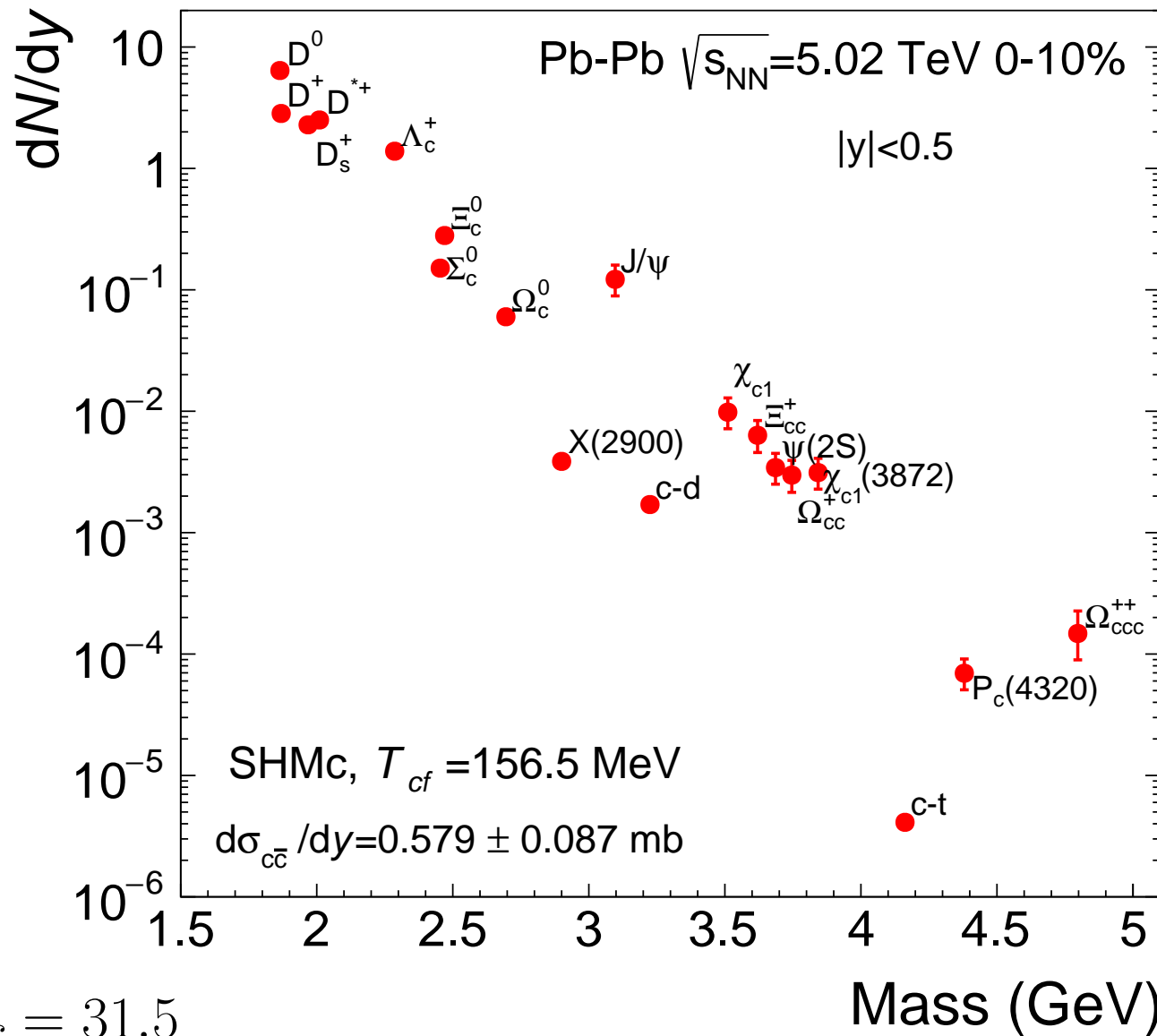
*full thermalization of c quarks in QGP, hadronization at chemical freeze-out*



$d\sigma_{c\bar{c}}/dy$  via normalization to  $D^0$  in Pb-Pb 0-10%, ALICE, [arXiv:2110.09420](https://arxiv.org/abs/2110.09420)

$dN/dy = 6.82 \pm 1.03$  ( $|y| < 0.5$ ; FONLL for  $y=2.5-4$ ; assuming hadronization fractions in data as in SHMc)

# SHMc: the full charm zoo



$$\frac{dN_{c\bar{c}}}{dy} = 13.8$$

$$\rightarrow g_c = 31.5$$

$$T_{cc}^+ \simeq 0.9 \cdot \chi_{c1}(3872)$$

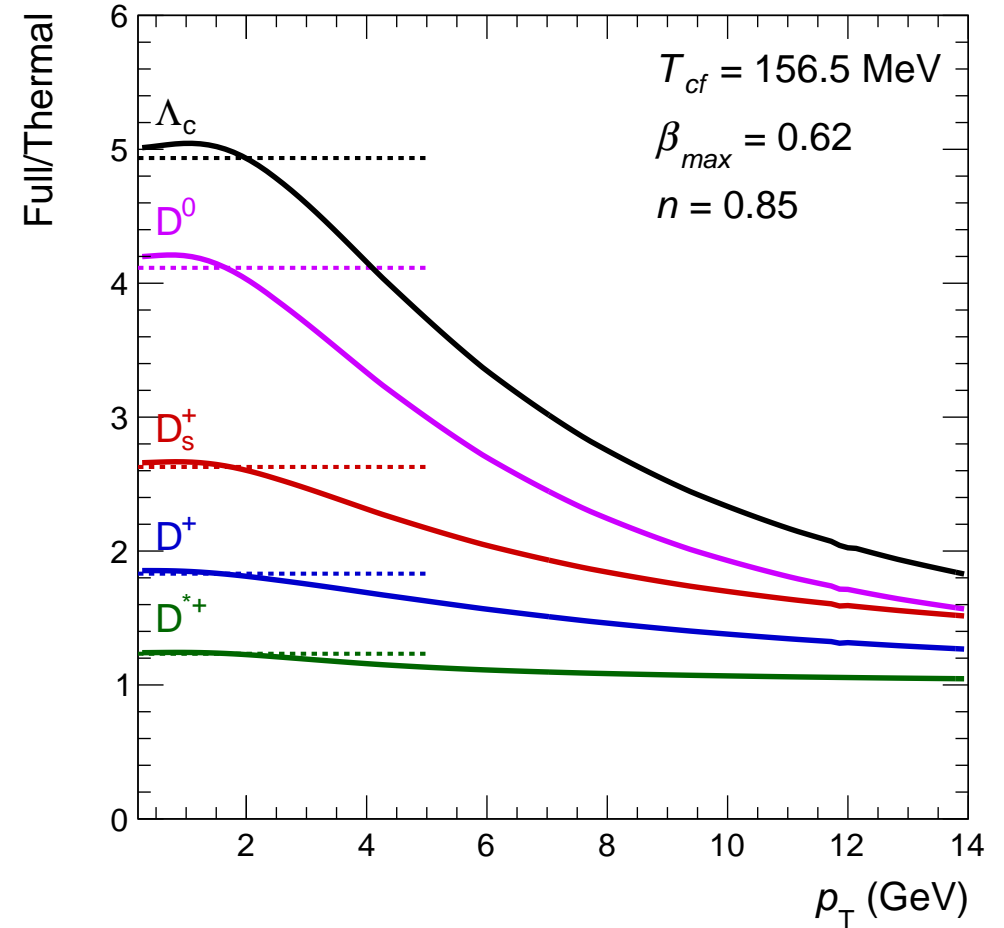
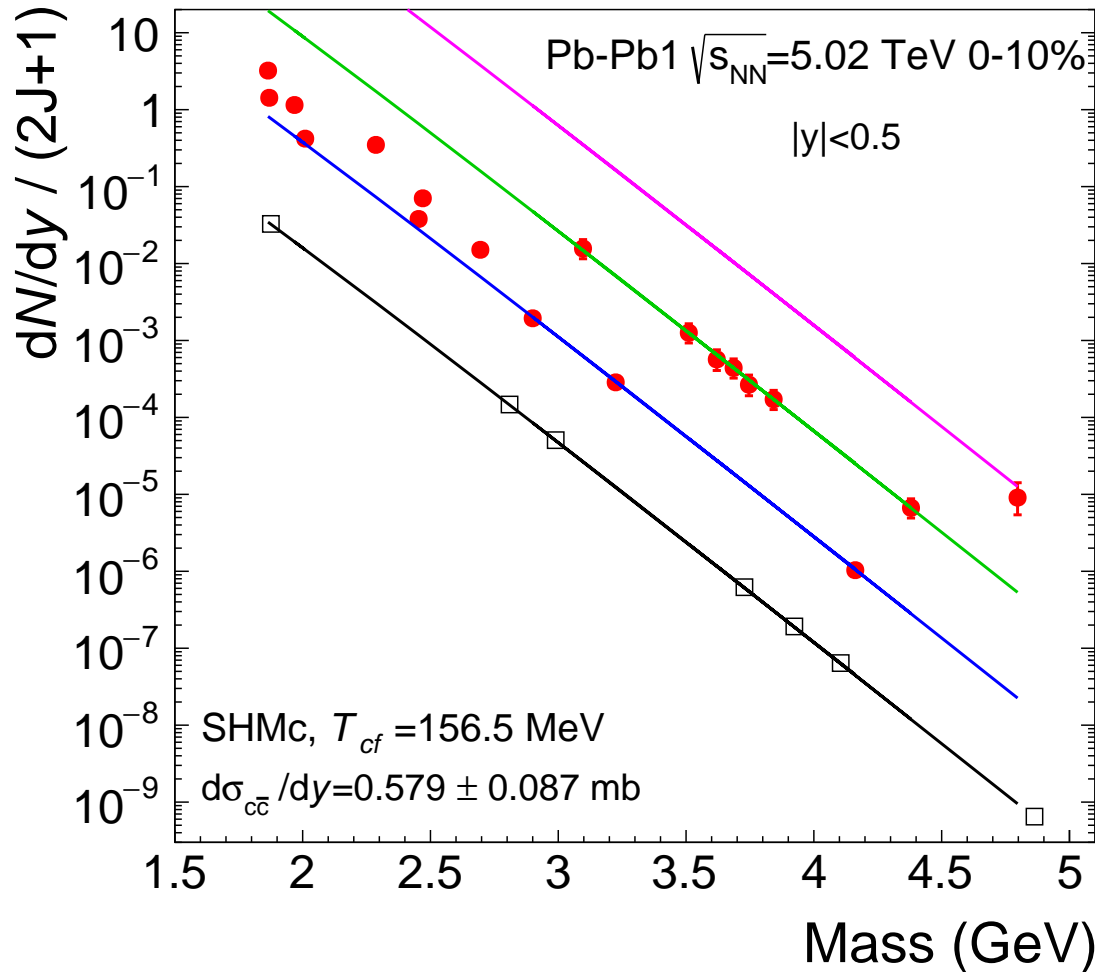
$$X(6900) \sim 10^{-8}$$

The power of the model: predicting the full suite of charmed hadrons

# Full charm predictions for the LHC

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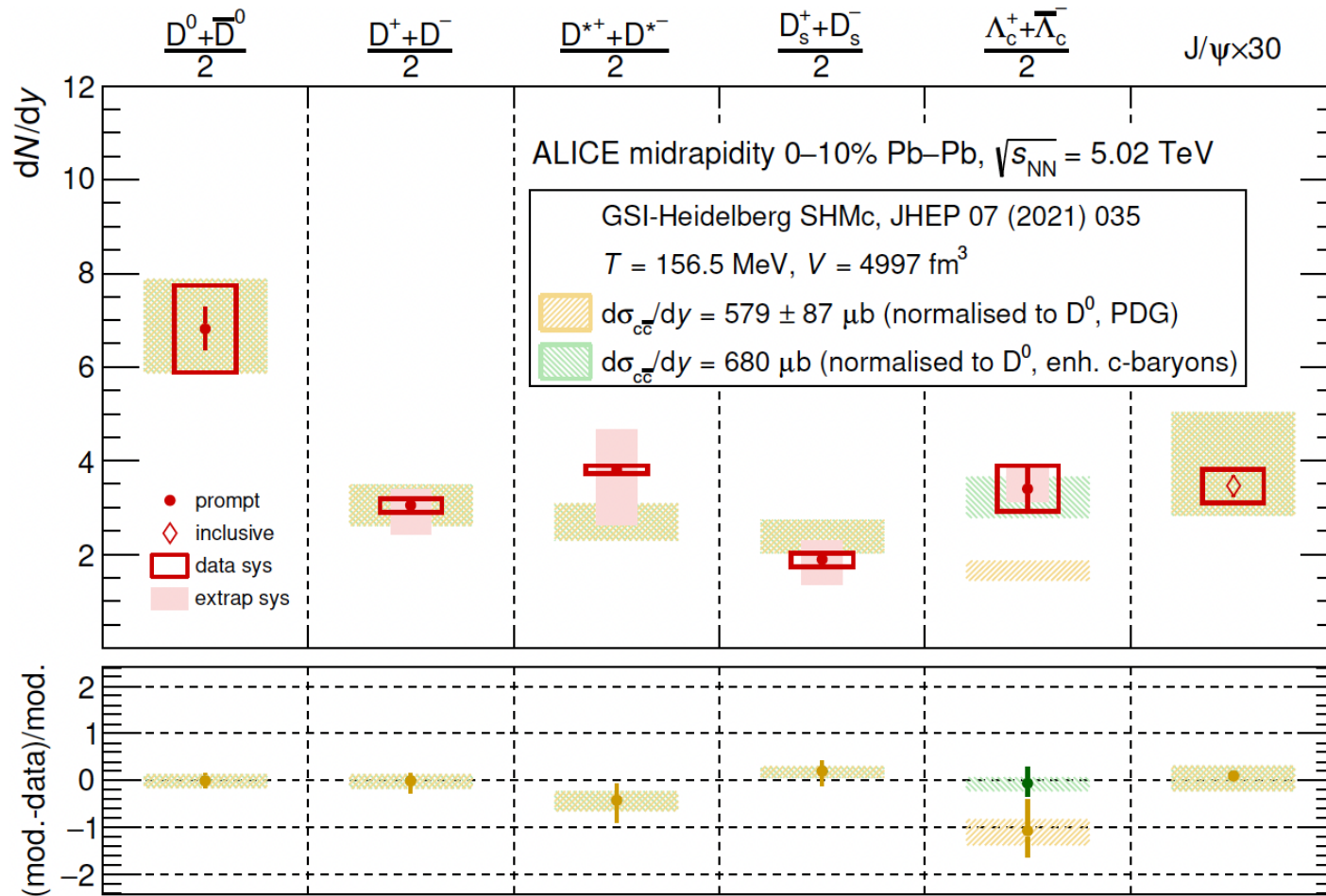
Charm-hadron spectrum as in PDG: 55 c-mesons, 74 c-baryons (part.+antipart.)

...large, but may not be complete

# Charm data and SHMc model

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ALICE, [arXiv:2212.04348](https://arxiv.org/abs/2212.04348)

Enh. c-baryons: *tripled* the excited charm-baryon states, *and*  $d\sigma_{c\bar{c}}/dy$ : +19%

RQM: He,Rapp, [PLB 795 \(2019\) 117](https://arxiv.org/abs/1905.07574); LQCD, Bazavov et al., [PLB 737 \(2014\) 210](https://arxiv.org/abs/1403.7093)

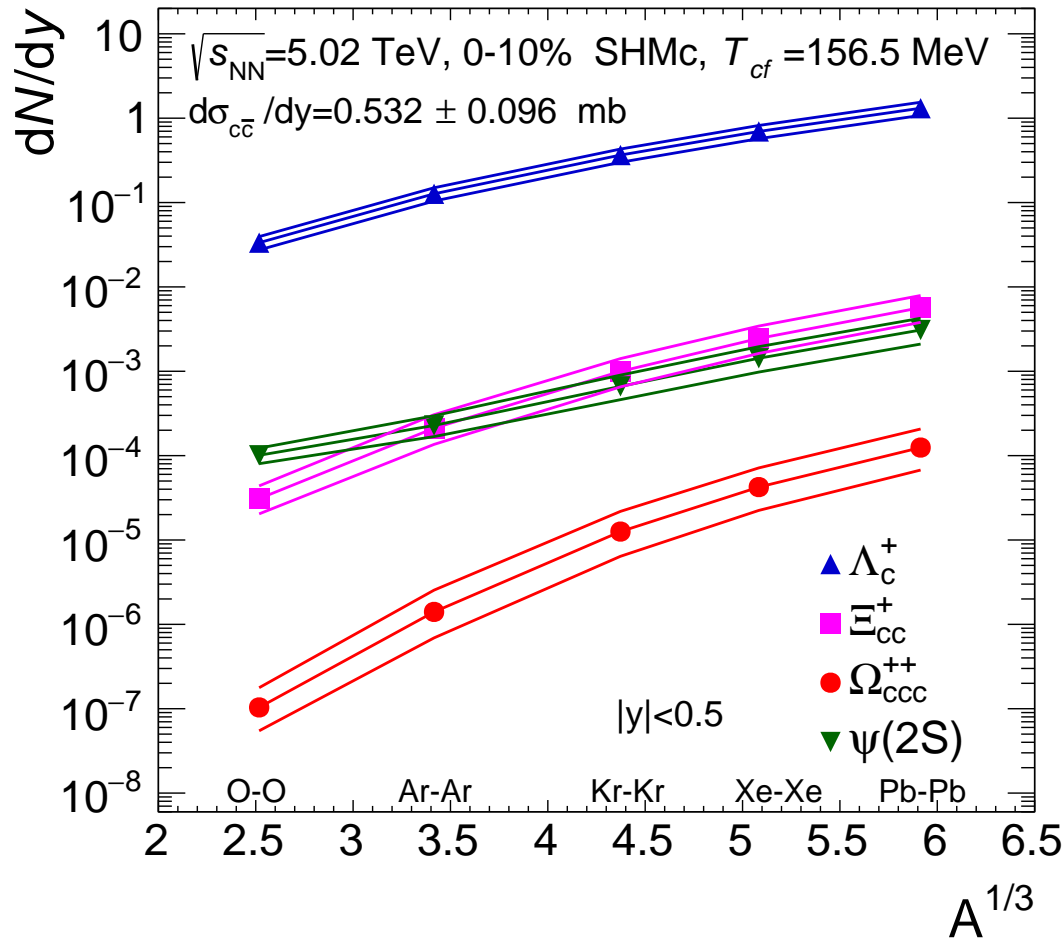
leaves the mesonic sector unaffected, for the commensurately larger  $\sigma_{c\bar{c}}$

# SHMc: system-size dependence (central, 0-10%)

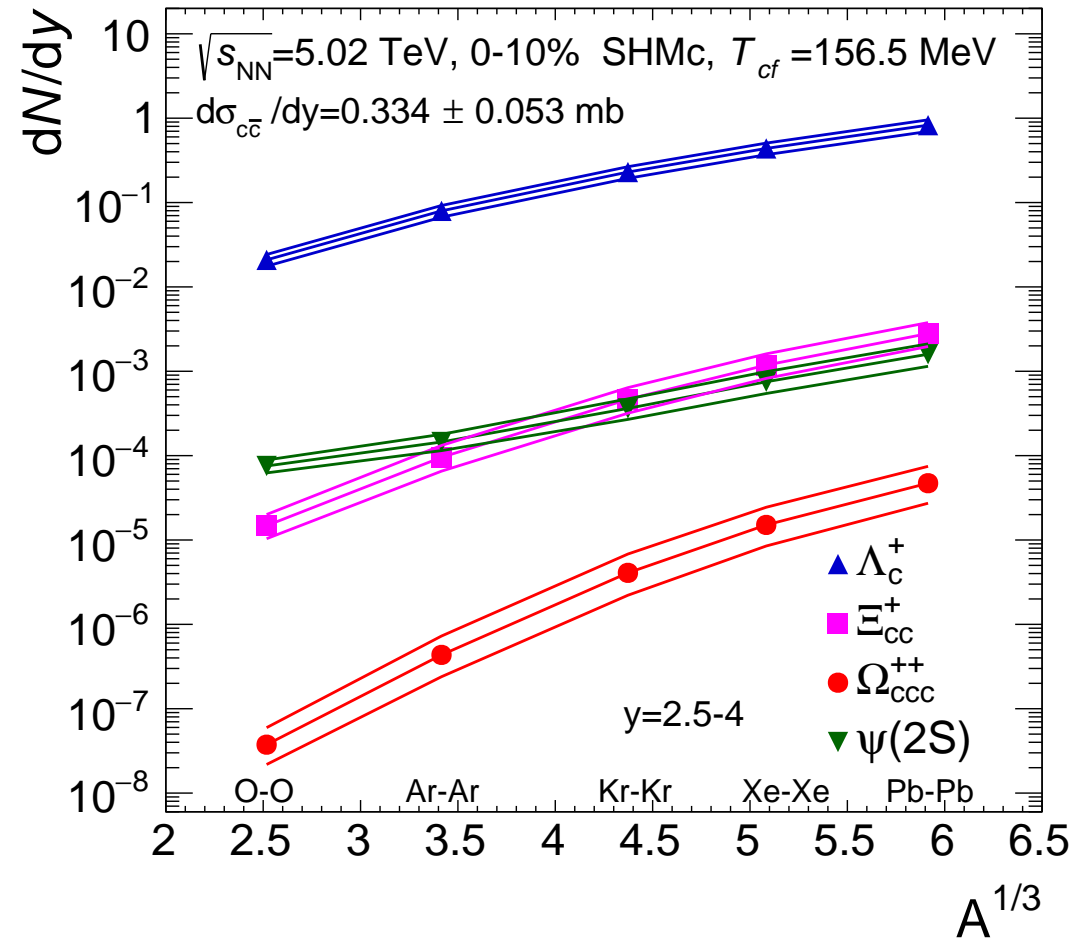
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midrapidity



forward rapidity

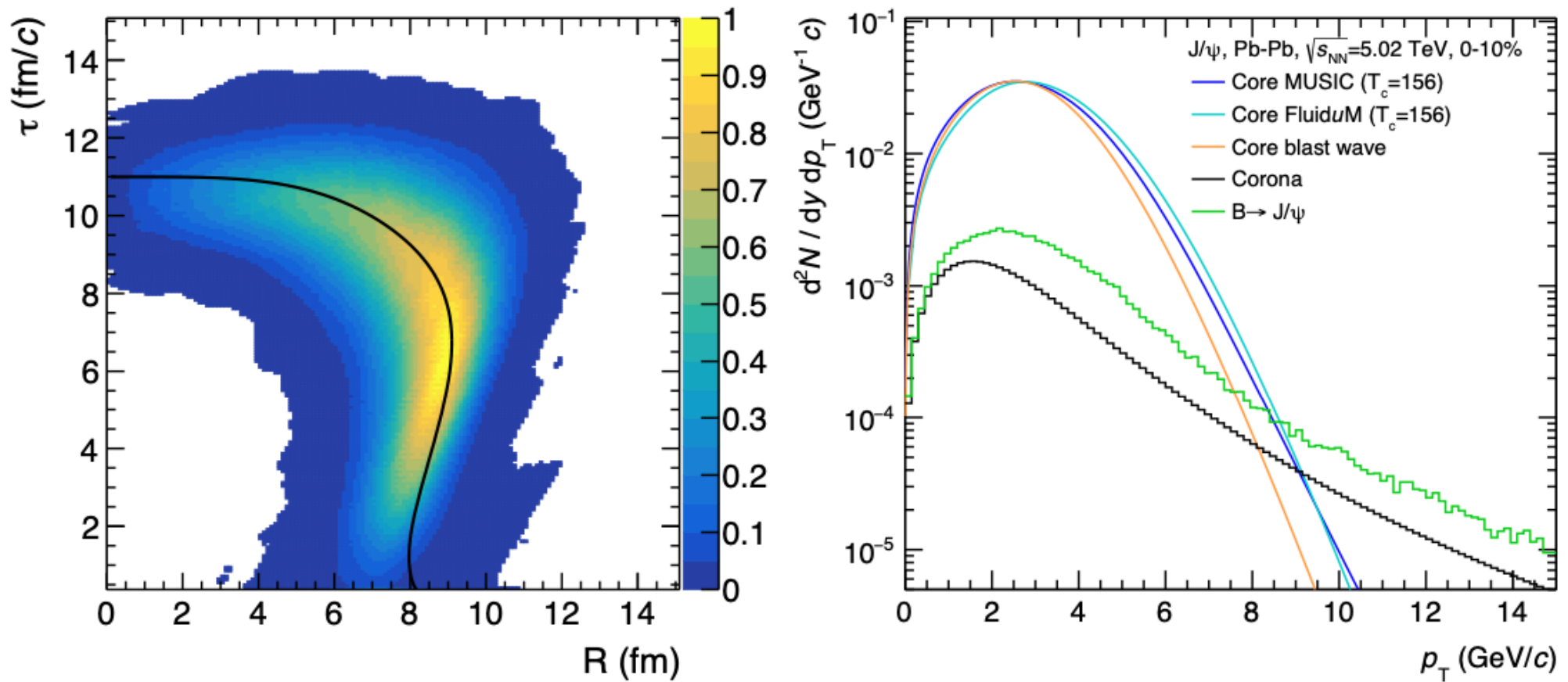




# SHMc - coupling to hydrodynamics

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AA, ..., M. Vökl, [arXiv:2308.14821](https://arxiv.org/abs/2308.14821)

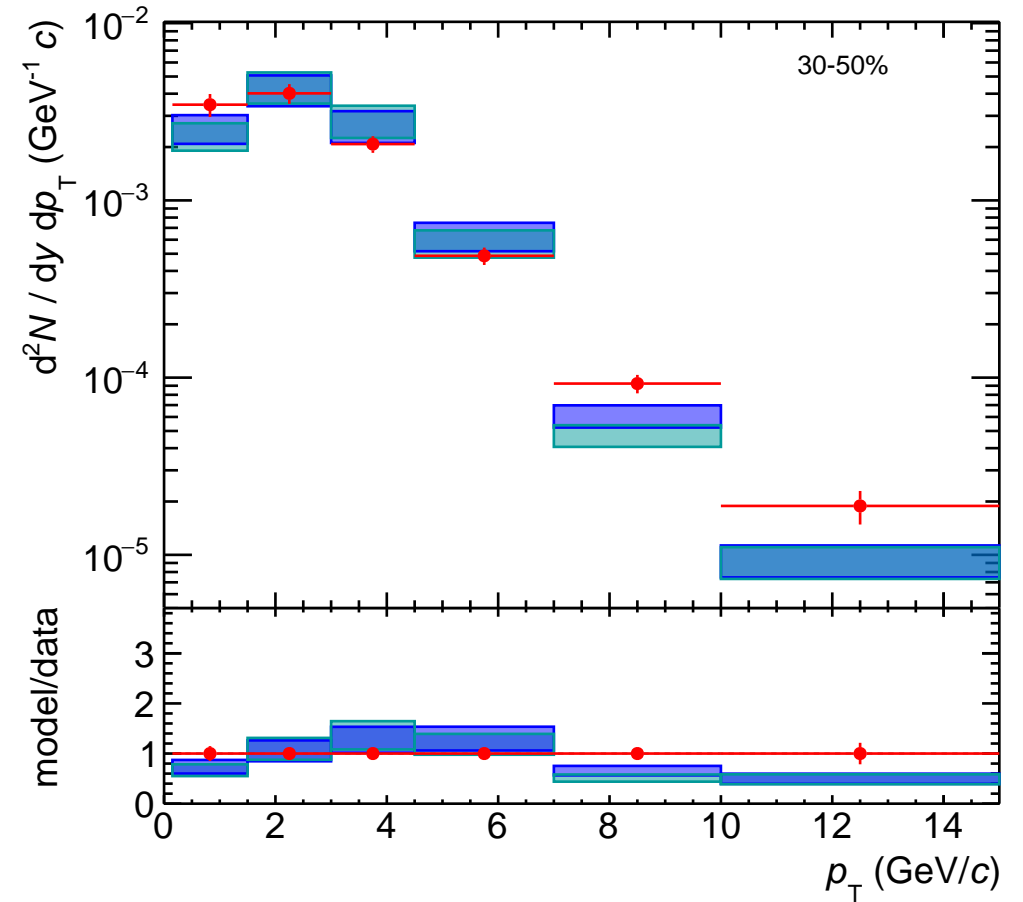
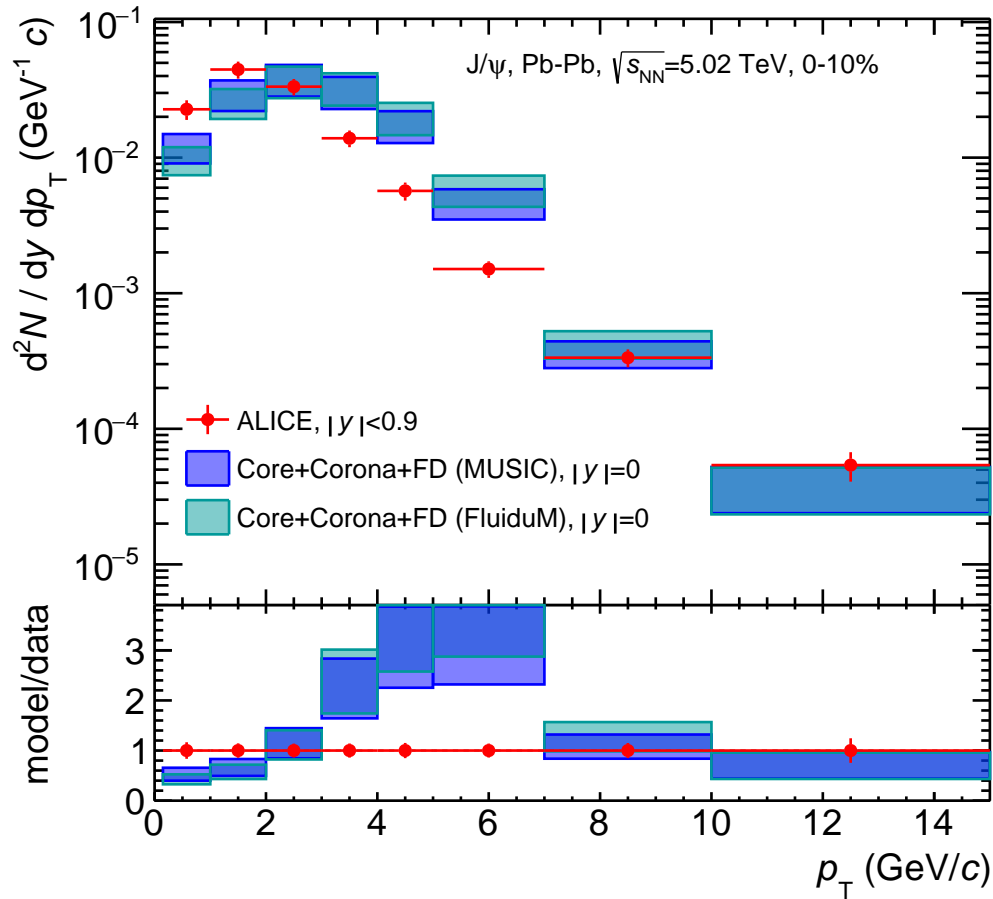
Distribution: MUSIC (IP-Glasma;  $\tau_0 = 0.4$  fm/c)

Line: FluiduM ( $T_{R}$ ENTO;  $\tau_0 = 0.18$  fm/c)

# SHMc: $p_T$ spectra

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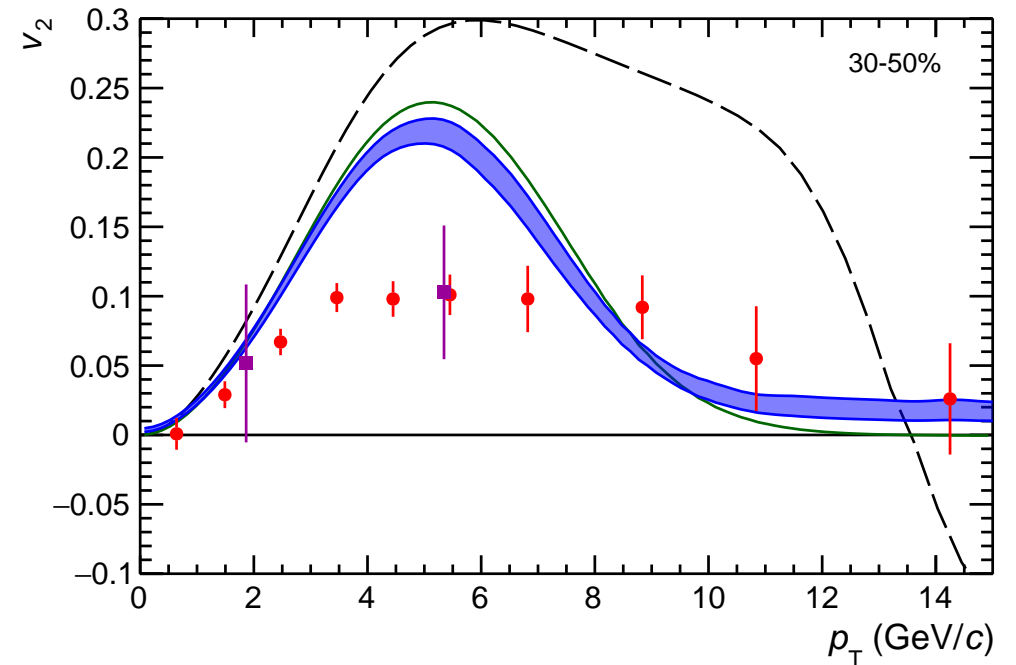
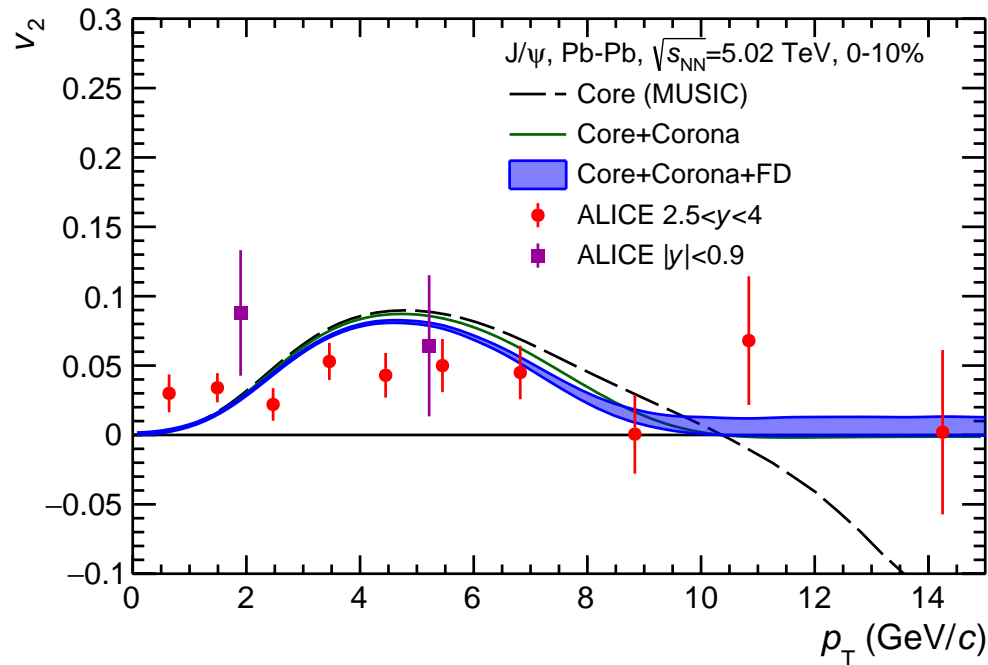
AA, ..., M. Vökl, [arXiv:2308.14821](https://arxiv.org/abs/2308.14821)

Too strong flow in 0-10% centrality

# SHMc: $v_2$ distributions

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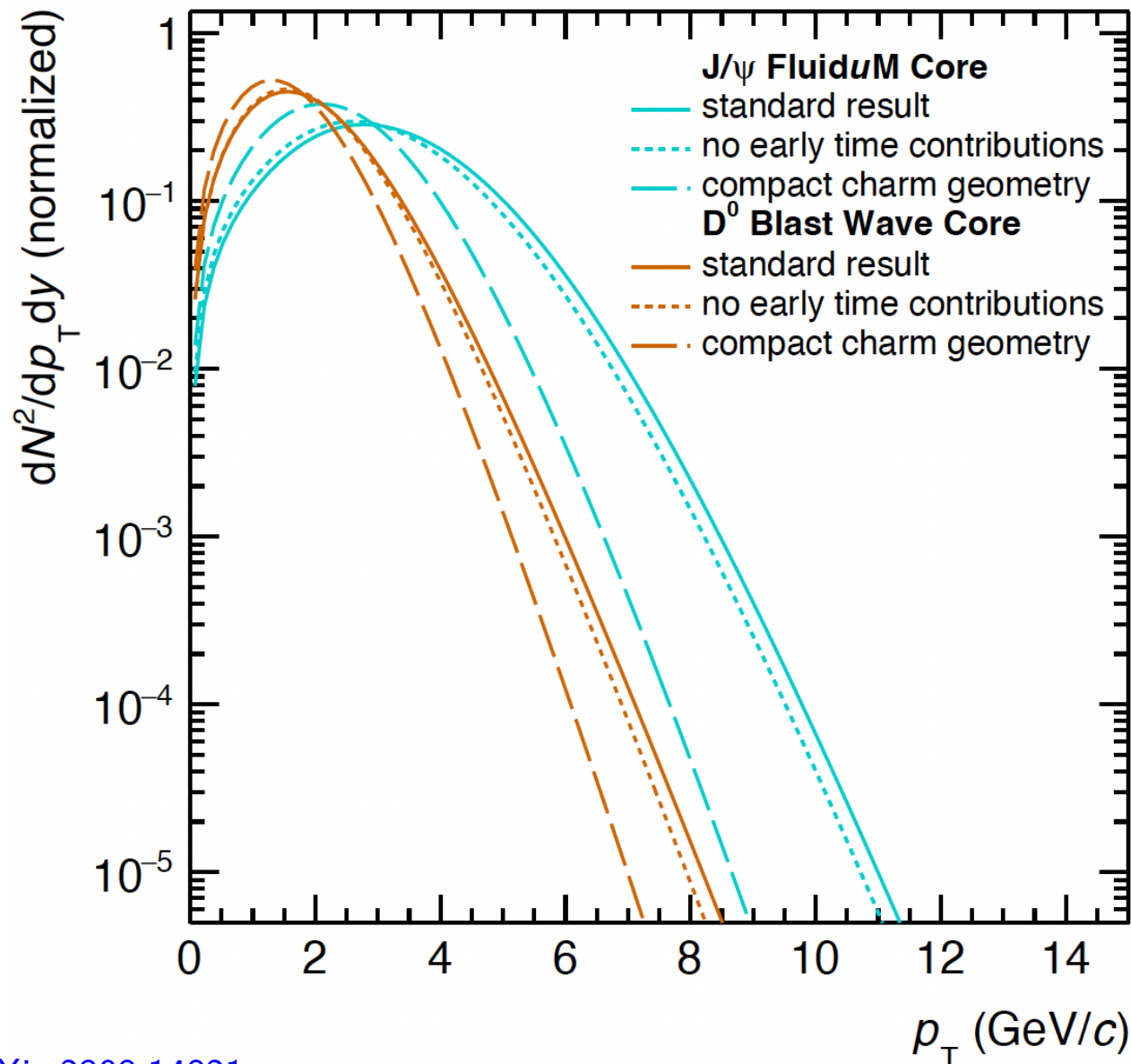
AA, ..., M. Vökl, [arXiv:2308.14821](https://arxiv.org/abs/2308.14821)

again, we predict too much flow ( $v_3$  is also overpredicted)

# SHMc - coupling to hydrodynamics, refinements

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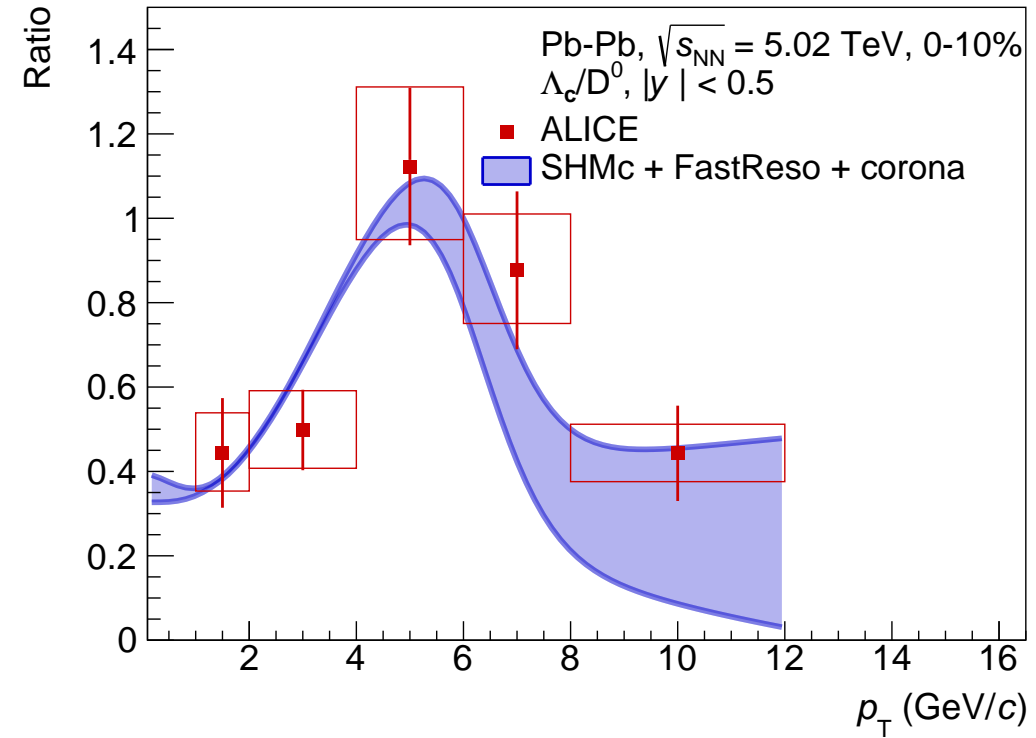
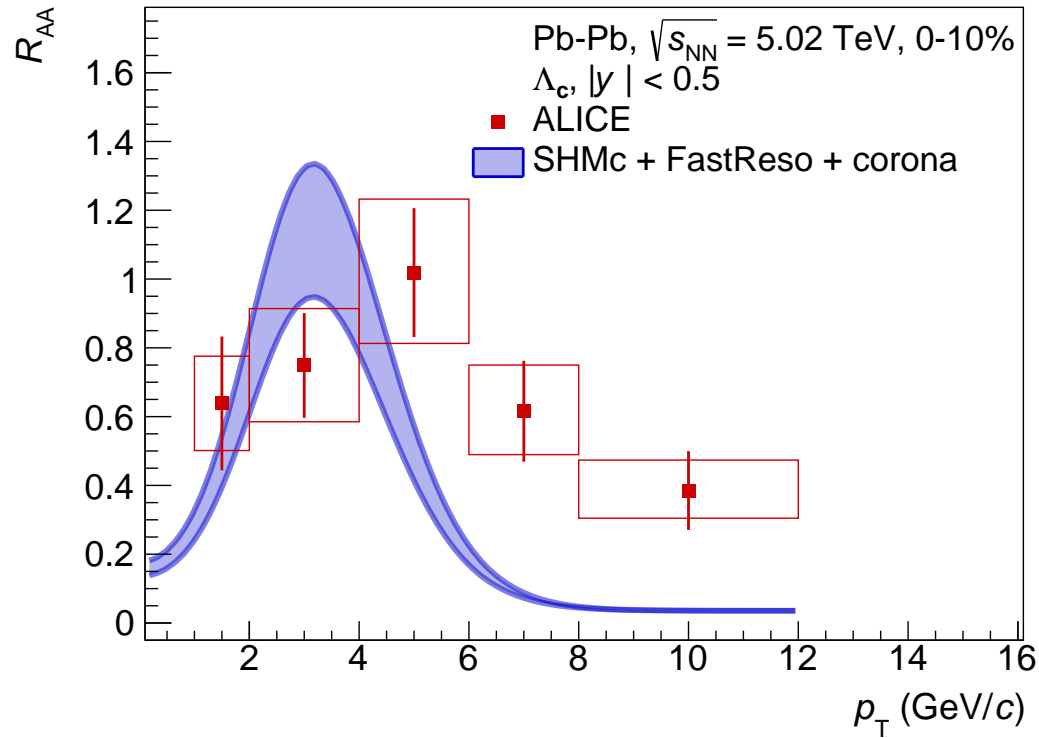
AA, ..., M. Völkl, [arXiv:2308.14821](https://arxiv.org/abs/2308.14821)

A spatially-mapped  $N_{coll}$  distribution needs to be implemented in addition.

# SHMc: $p_T$ , open charm

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AA, ..., M. Vökl, [arXiv:2308.14821](https://arxiv.org/abs/2308.14821)

implement screening picture with space-time evolution of the fireball (hydro-like)  
continuous destruction and “(re)generation” (“recombination”)  
Boltzmann equation (loss and gain terms)

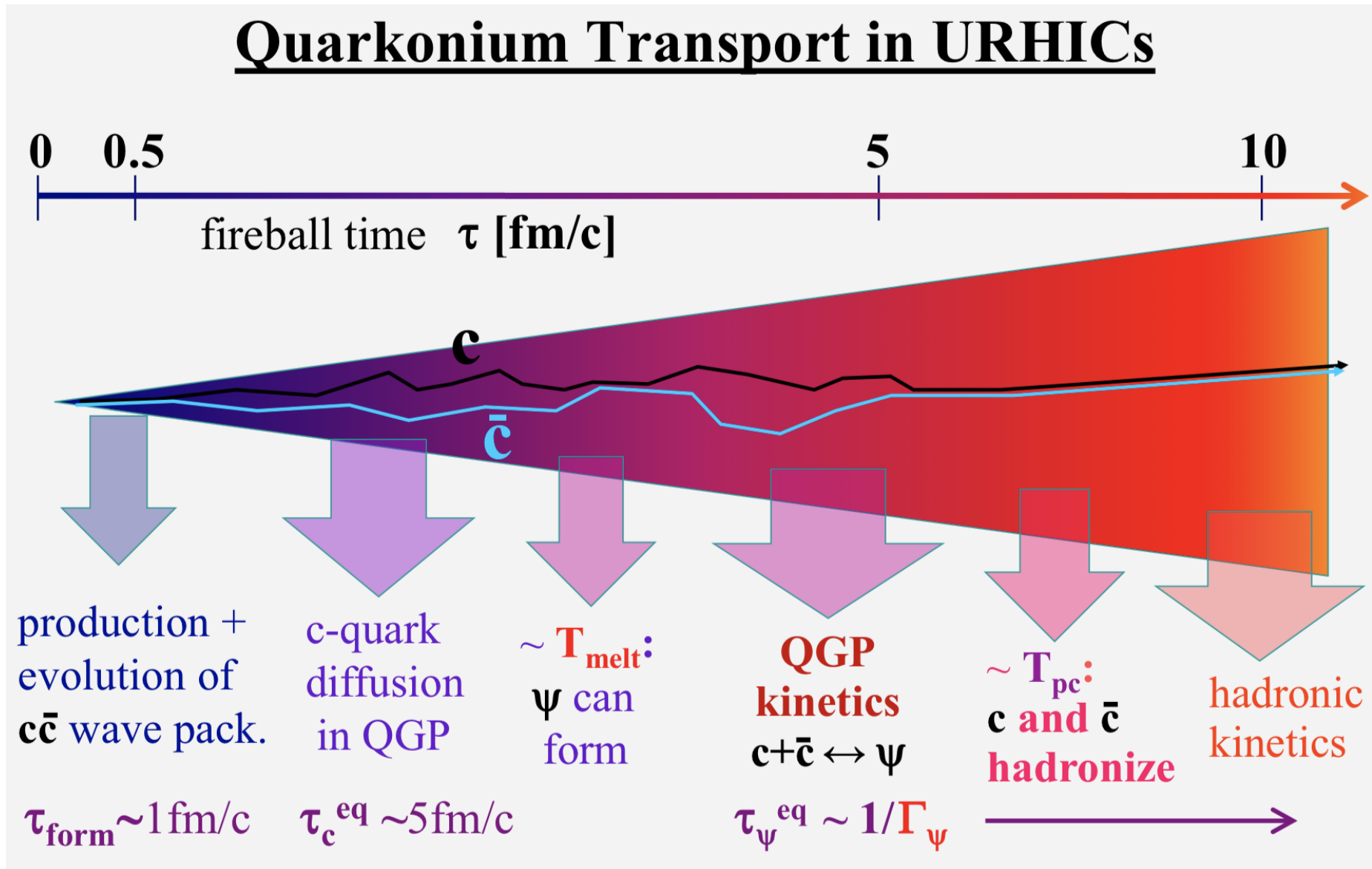
Thews et al., PRC 63 (2001) 054905 ...

“TAMU”, PLB 664 (2008) 253, NPA 859 (2011) 114, EPJA 48 (2012) 72

“Tsinghua”, PLB 607 (2005) 107, PLB 678 (2009) 72, arXiv:1401.5845

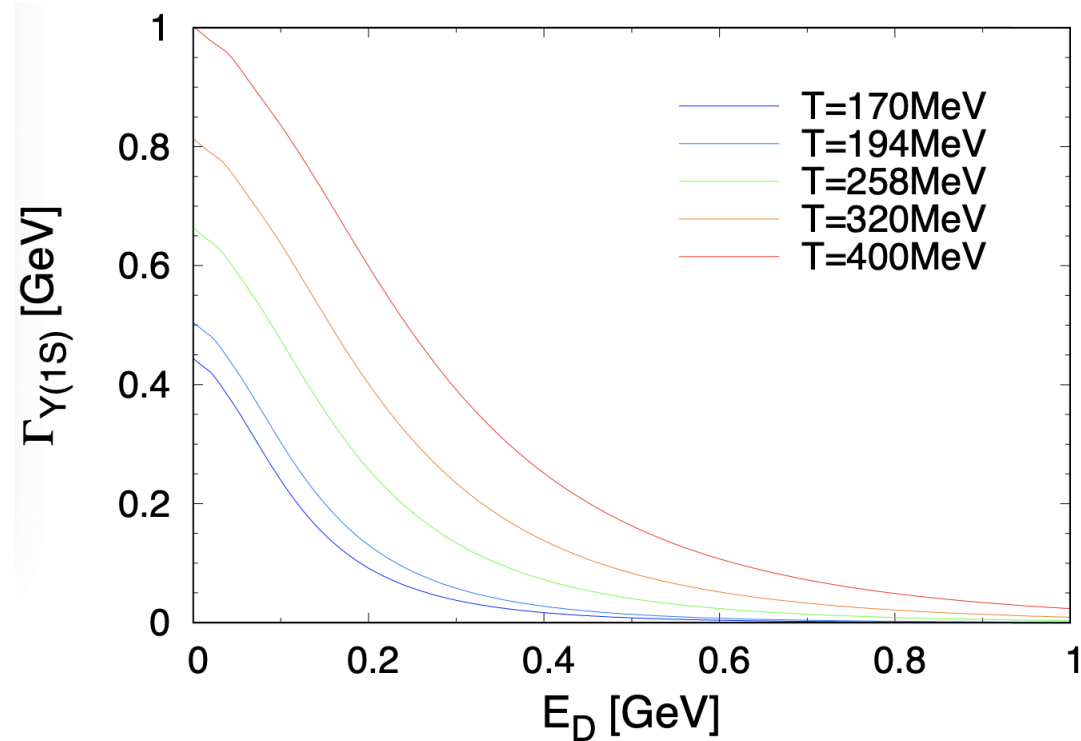
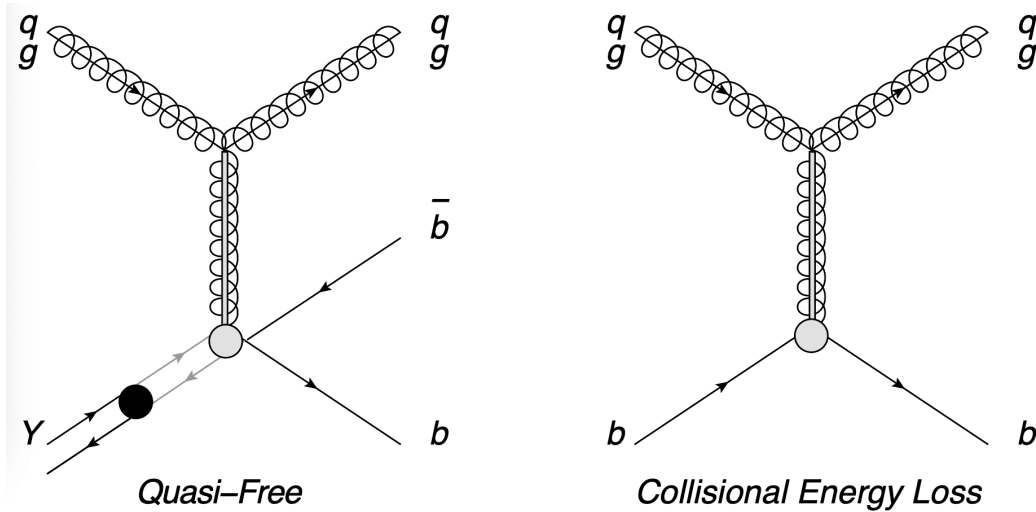
Predicts  $R_{AA}, v_2(p_T)$  (TAMU describes D mesons too)

# Transport models - schematics



# Transport models - the essentials

$$\frac{dN_\Upsilon}{d\tau} = -\Gamma(T(\tau)) [N_\Upsilon(\tau) - N_\Upsilon^{eq}(T(\tau))]$$



Du, Liu, Rapp, *Phys. Lett. B* 796 (2019) 20

Quasi-free = inelastic (dissociation) [imaginary part of HQ potential?]

$K$  factor: enhancement over perturbative results ( $K = 5$  in  $\Gamma_{\Upsilon(1S)}$  above)

$N^{eq}$ : SHM generation



## 2 other models

- “Comovers” model (Santiago):  
( invented to describe suppression in the (final-state) hadronic medium at SPS  
 $J/\psi + \pi \rightarrow D + \bar{D}$  )

at LHC: gluo-dissociation and a (re)generation component (dominant for  $J/\psi$ )  
(the Boltzmann equation of the transport model is also in the comoving system)

E. Ferreiro et al., PLB 731 (2014) 57

- Hydrodynamic model (Kent State Univ.)  
hydro gives energy density vs. space-time  
suppression probability vs.  $\varepsilon$  gives  $R_{AA}$  (of  $Y$ )

Strickland, Bazow, NPA 879 (2012) 25

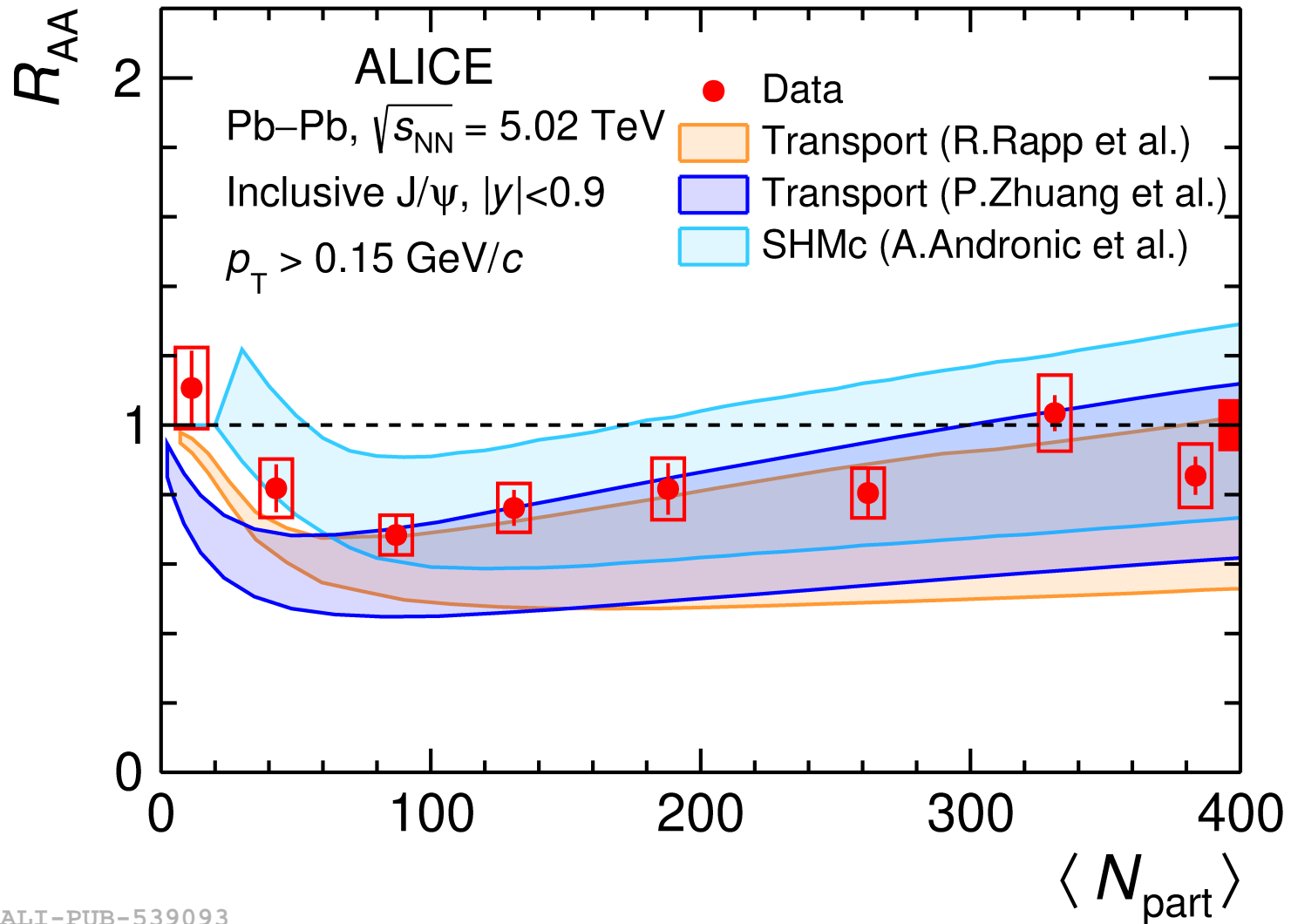
## ...and one more: the quantum approach

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Open quantum systems description + Effective NRQCD theory  
quantum evolution of the  $b\bar{b}$  pair in QGP (heat bath; hydrodynamics)  
Lindblad equation (accuracy: at NLO in the binding energy over temperature)

Strickland, Thapa, [PRD 108 \(2023\) 014031](#) and refs therein

# SHMc vs. transport models



ALI-PUB-539093

ALICE, [arXiv:2303.13361](https://arxiv.org/abs/2303.13361)

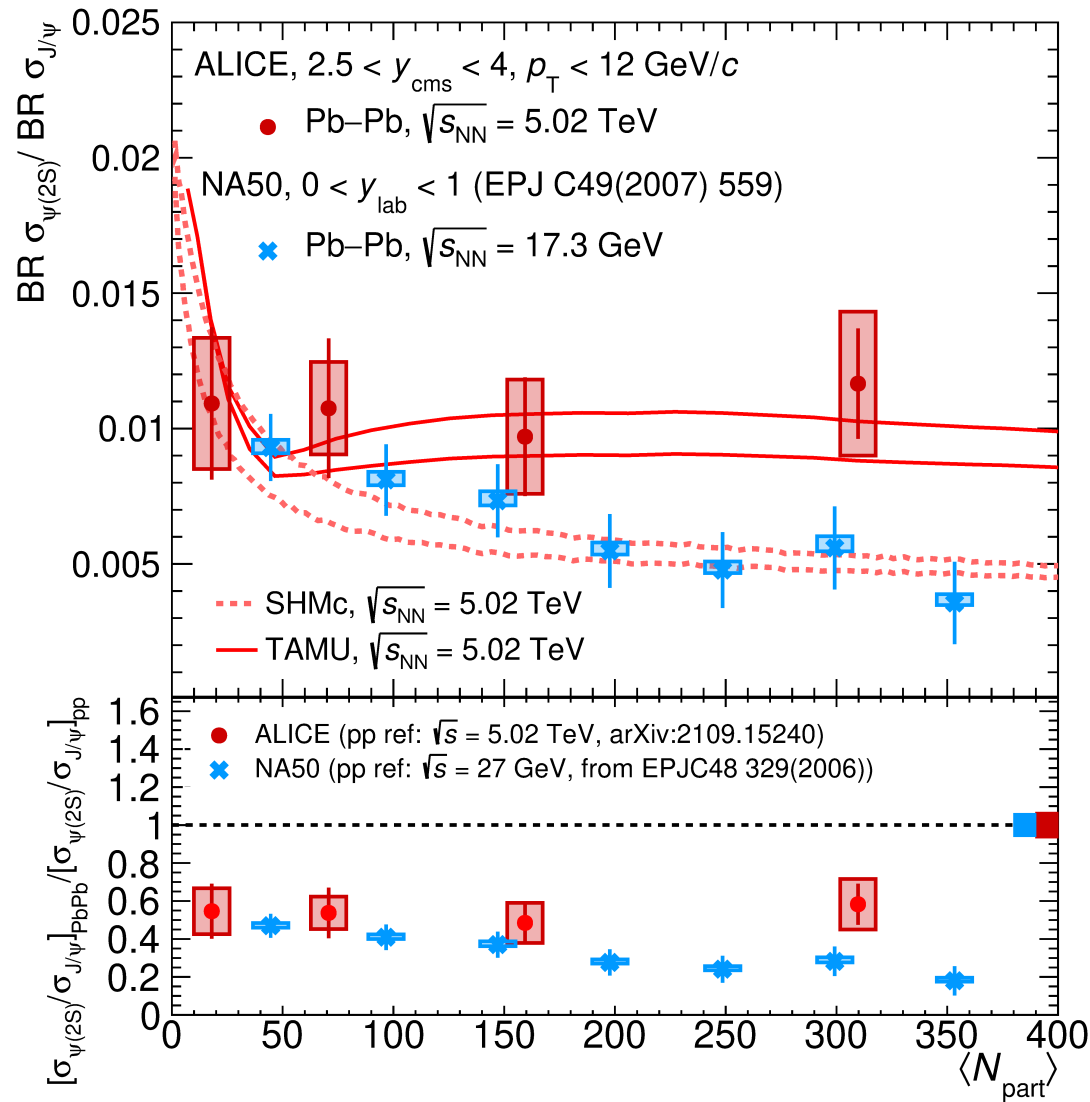
SHMc:  $d\sigma_{c\bar{c}}/dy$  via normalization to  $D^0$  in Pb–Pb 0-10%, ALICE, [arXiv:2110.09420](https://arxiv.org/abs/2110.09420)

$dN/dy = 6.82 \pm 1.03$  ( $|y| < 0.5$ ; FONLL for  $y=2.5-4$ ; assuming hadronization fractions in data as in SHMc)

# $\psi(2S)/J/\psi$ at the LHC (and SPS)

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ALI-PUB-528400

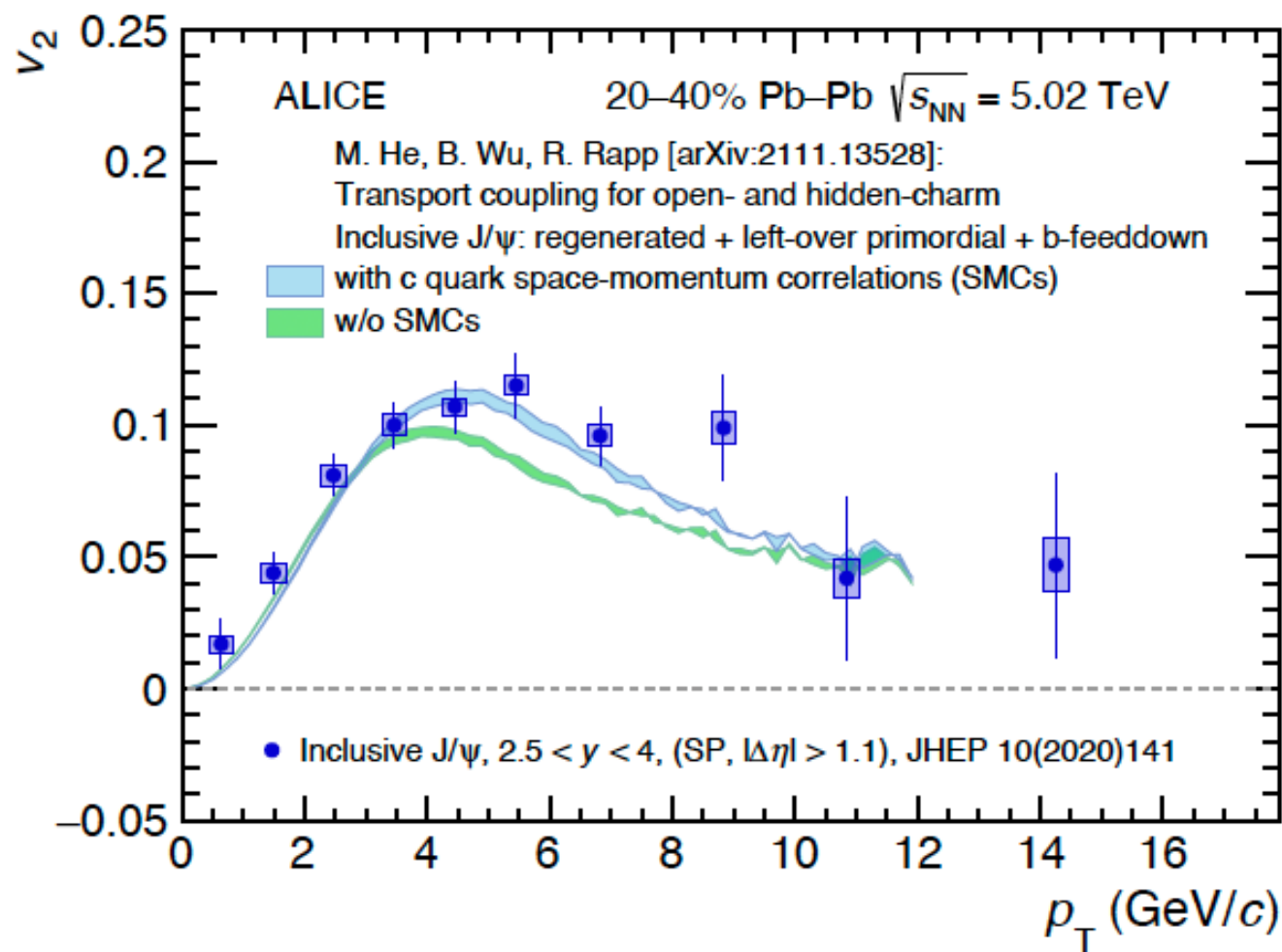
In SHMc uncertainty only due to nuclear-corona  
 ( $\sigma_{c\bar{c}}$  cancels out completely)

ALICE, [arXiv:2210.08893](https://arxiv.org/abs/2210.08893)

# J/ψ elliptic flow: data and transport model

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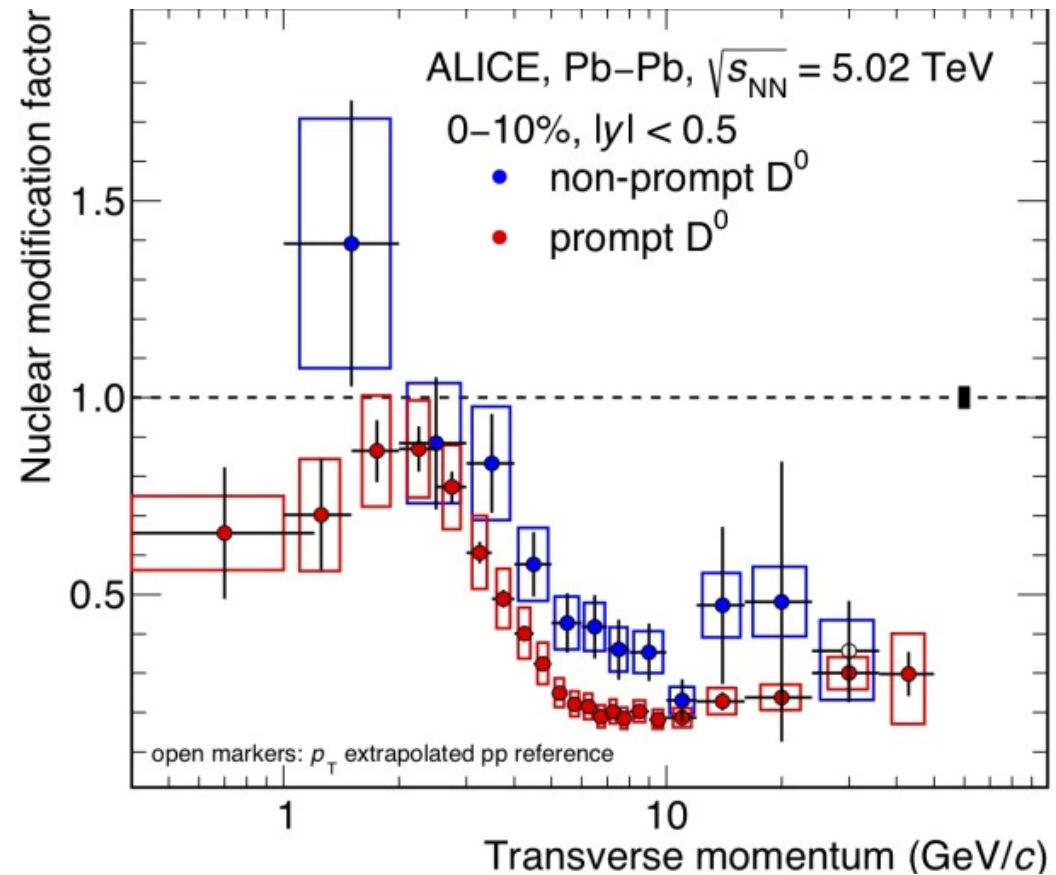
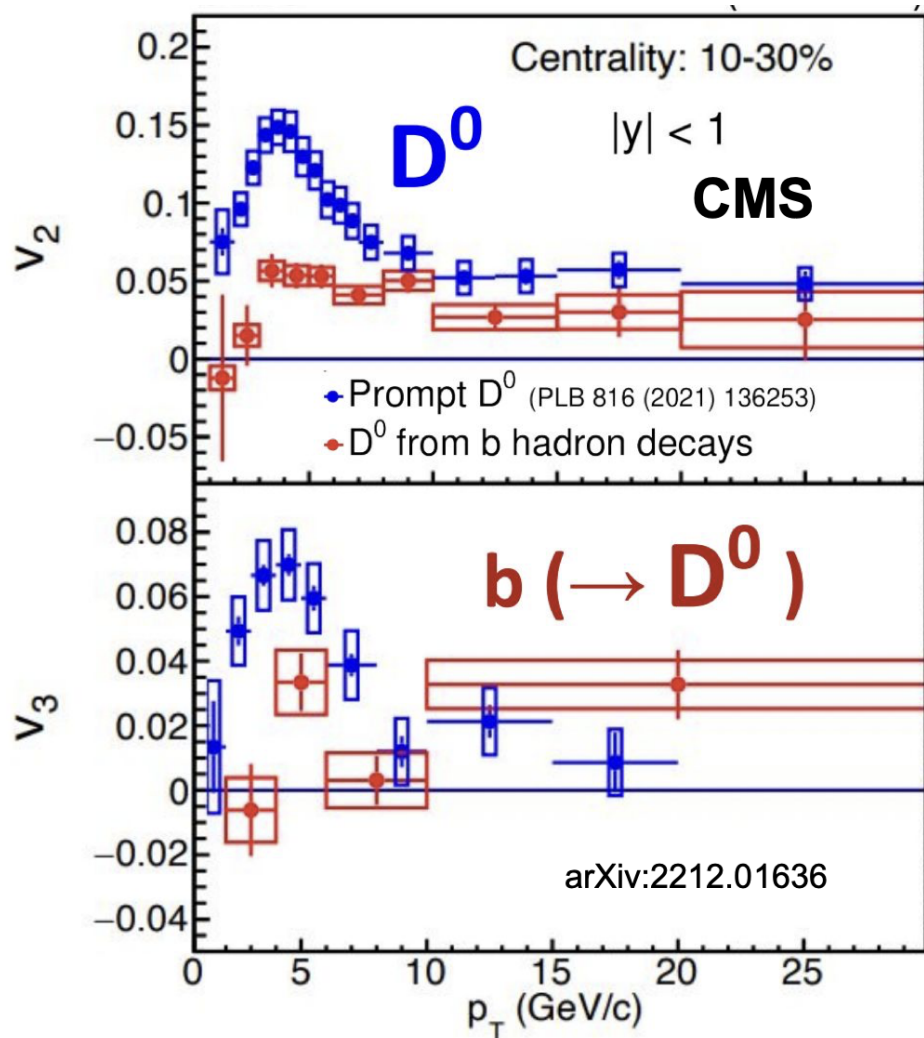
ALICE, [arXiv:2212.04348](https://arxiv.org/abs/2212.04348)

a very good description of data by the TAMU model [PRL 128 \(2022\) 162301](https://arxiv.org/abs/2111.13528)

# Beauty quark thermalization?

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ALICE, [arXiv:2202.00815](https://arxiv.org/abs/2202.00815), ATLAS

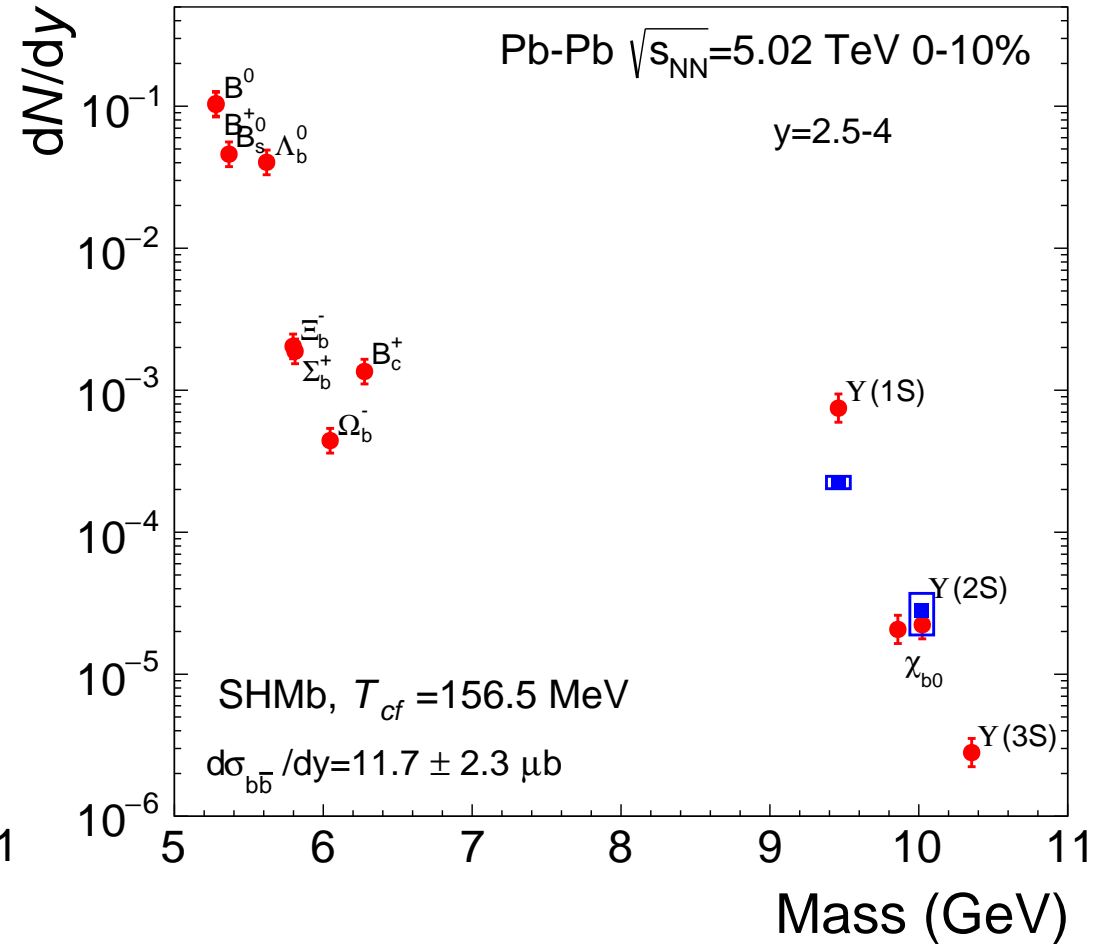
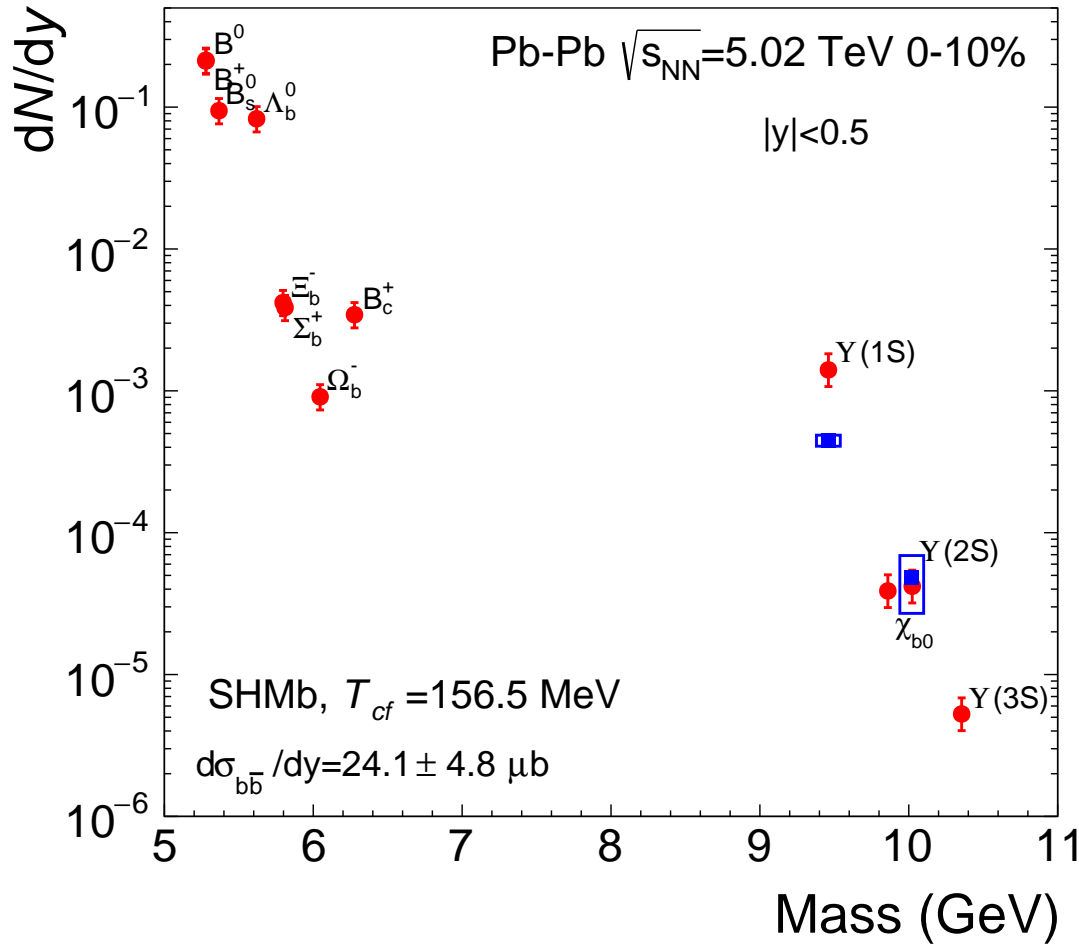
definitely strong flow but clearly less strong than for charm (CMS, QM'22, HIN-21-003)

...and a strong coupling with the medium (less energy loss than charm,  $p_T \simeq 10$  GeV/c)

# The limiting case: full beauty thermalization

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$$g_b = 1.05 \cdot 10^9 \quad \left( \frac{dN_{b\bar{b}}}{dy} = 0.57 \right)$$

$$B_c : 3.44 \cdot 10^{-3}$$

$$g_b = 0.86 \cdot 10^9 \quad \left( \frac{dN_{b\bar{b}}}{dy} = 0.28 \right)$$

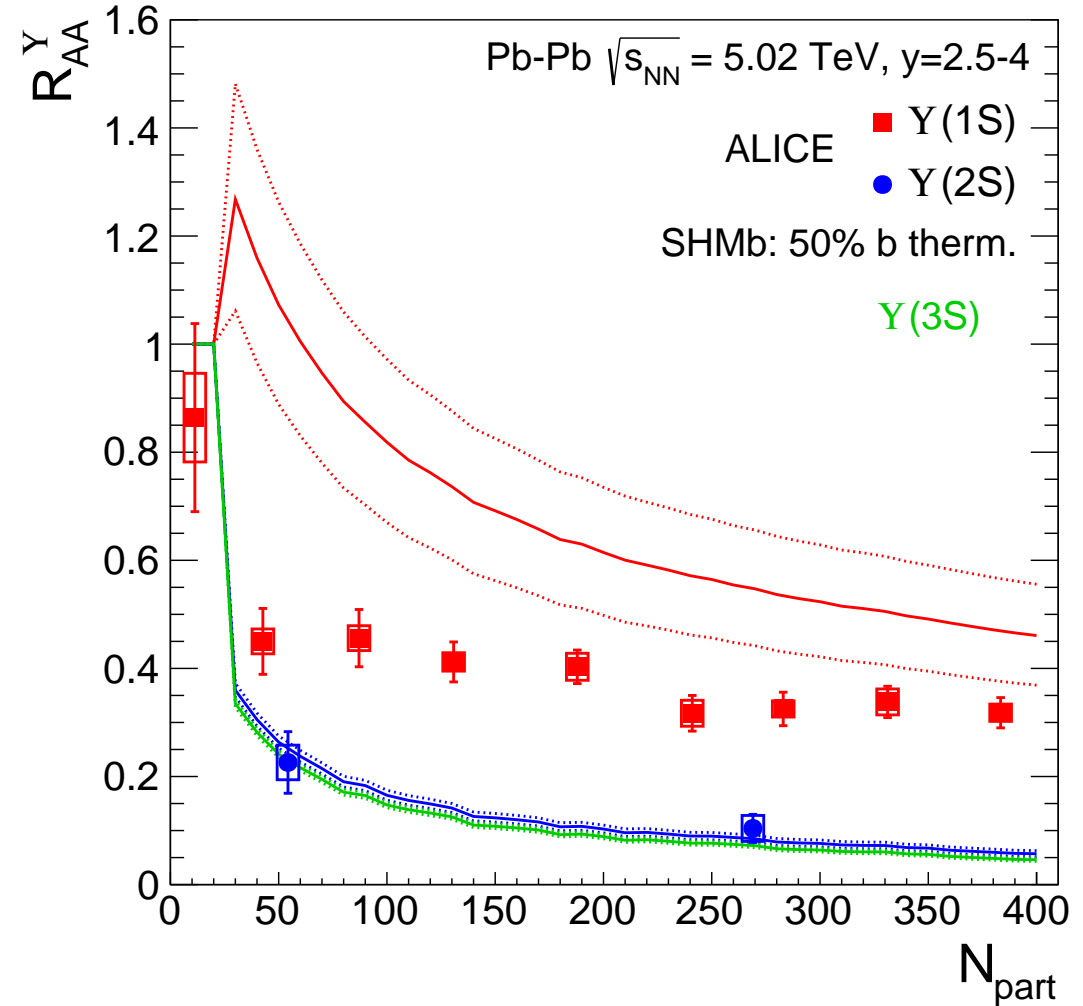
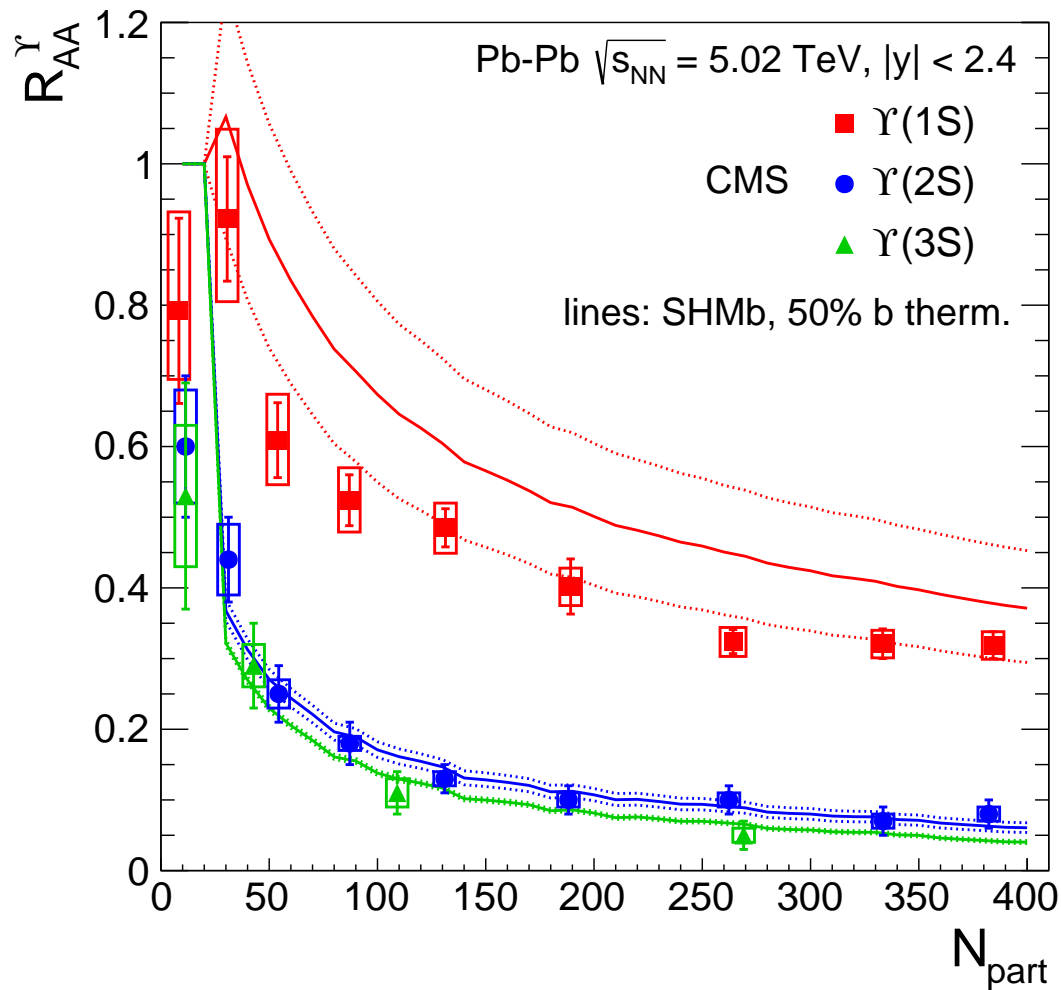
$$B_c : 1.36 \cdot 10^{-3}$$

Blue:  $\Upsilon$  data (CMS, ALICE): calc. based on  $R_{AA}$  and pp (would be nice to include in publications  $dN/dy$ )

# $R_{AA}$ , 50% $b\bar{b}$ thermalized

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CMS, PRL 120 (2018) 142301

ALICE, PLB 822 (2021) 136579

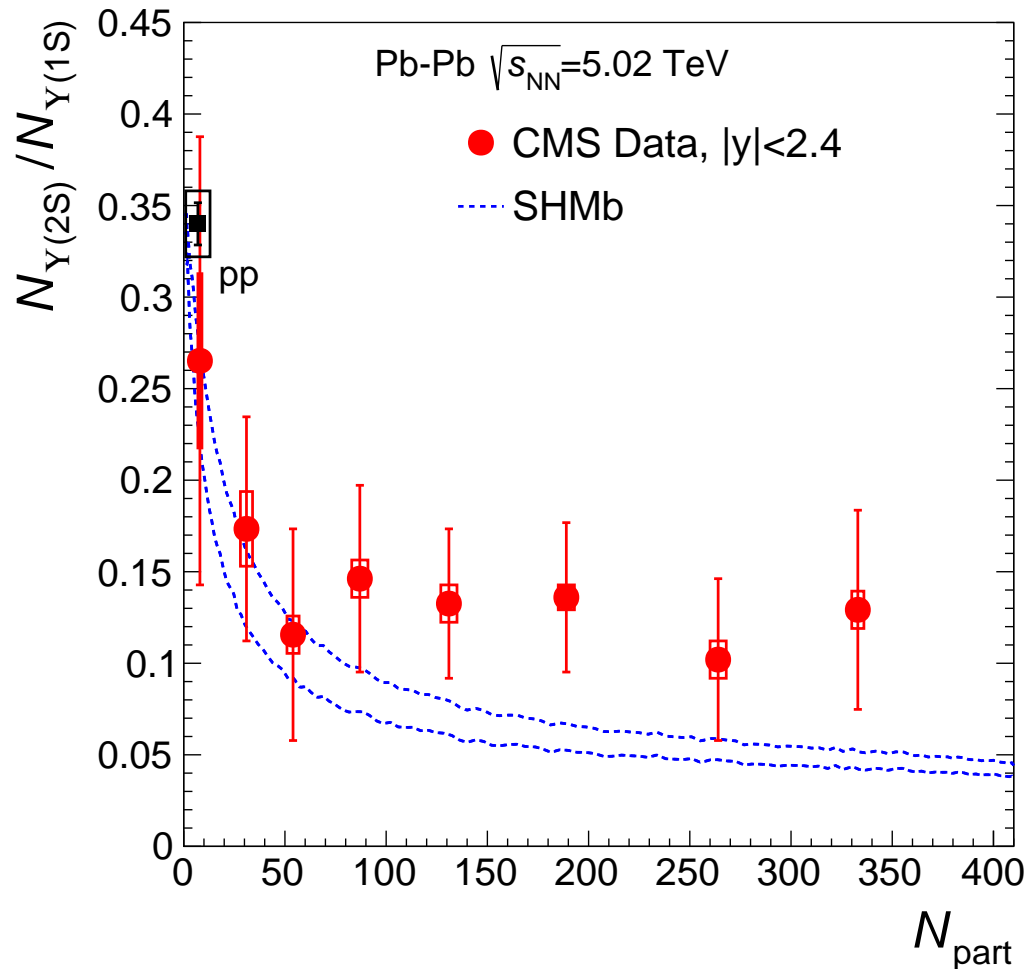
*What does non-thermalized beauty produce? (no room for it in SHMb)*



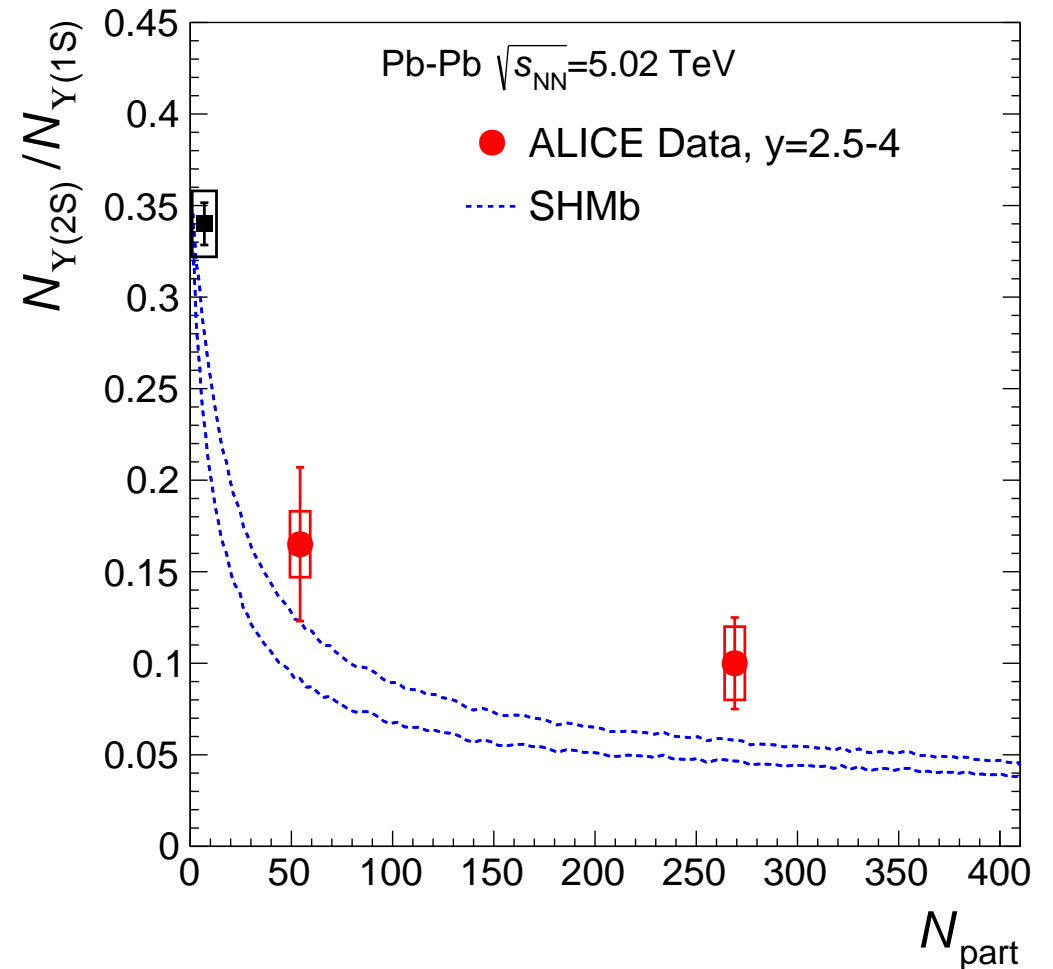
# $\Upsilon(2S)/\Upsilon(1S)$ ratio (100% b thermalization)

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CMS, [PRL 120 \(2018\) 142301](#)



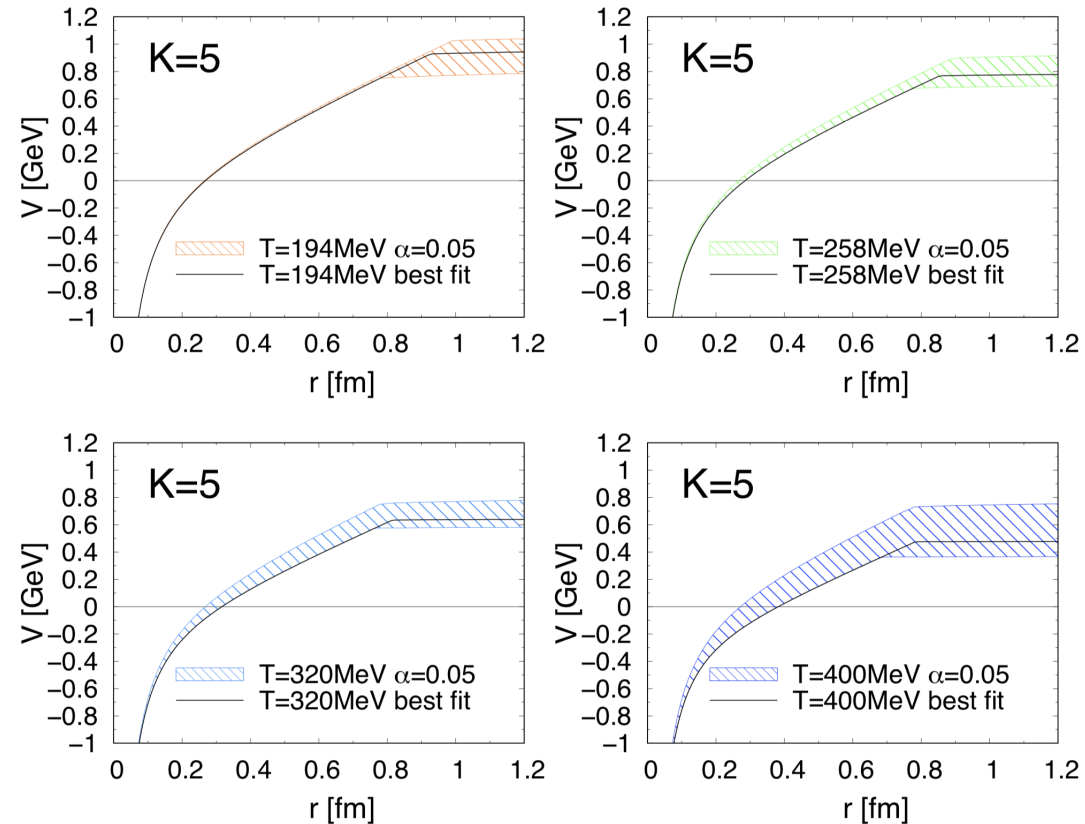
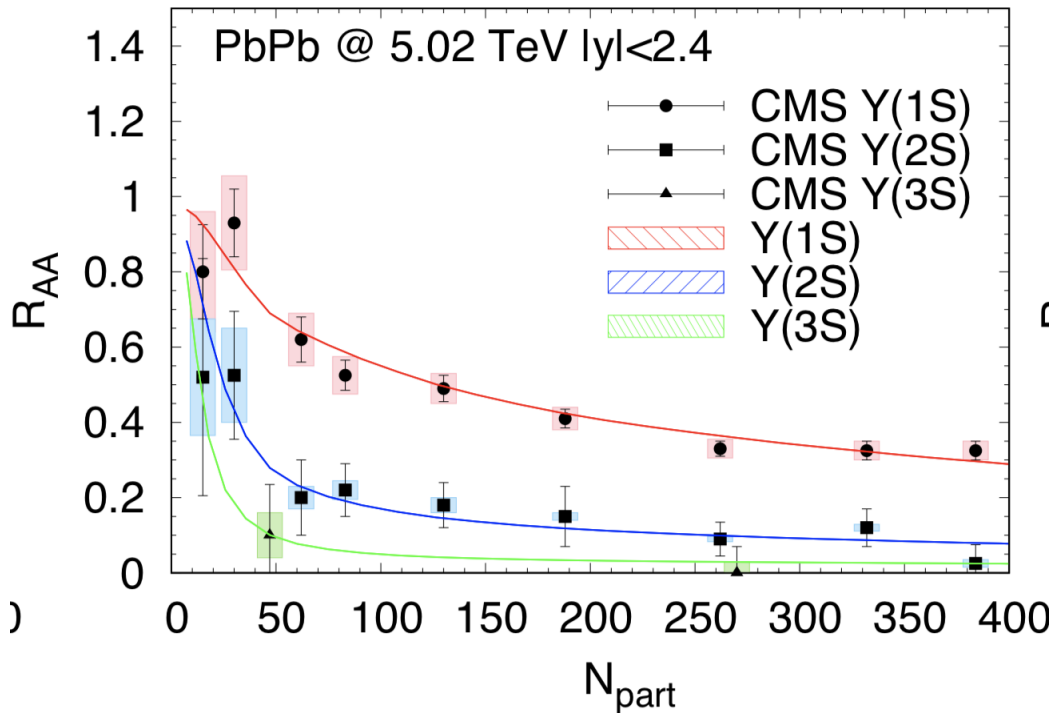
ALICE, [PLB 822 \(2021\) 136579](#)

ALICE pp:  $\Upsilon(2S)/\Upsilon(1S) = 0.5 \pm 0.1$ , [arXiv:2109.15240](#)

SHMb uncert.: nuclear-corona (fraction)

# $\Upsilon$ description in the transport model

...is very good; allows extraction of in-medium (Cornell) potential



(re)generation important for  $\Upsilon(2S)$

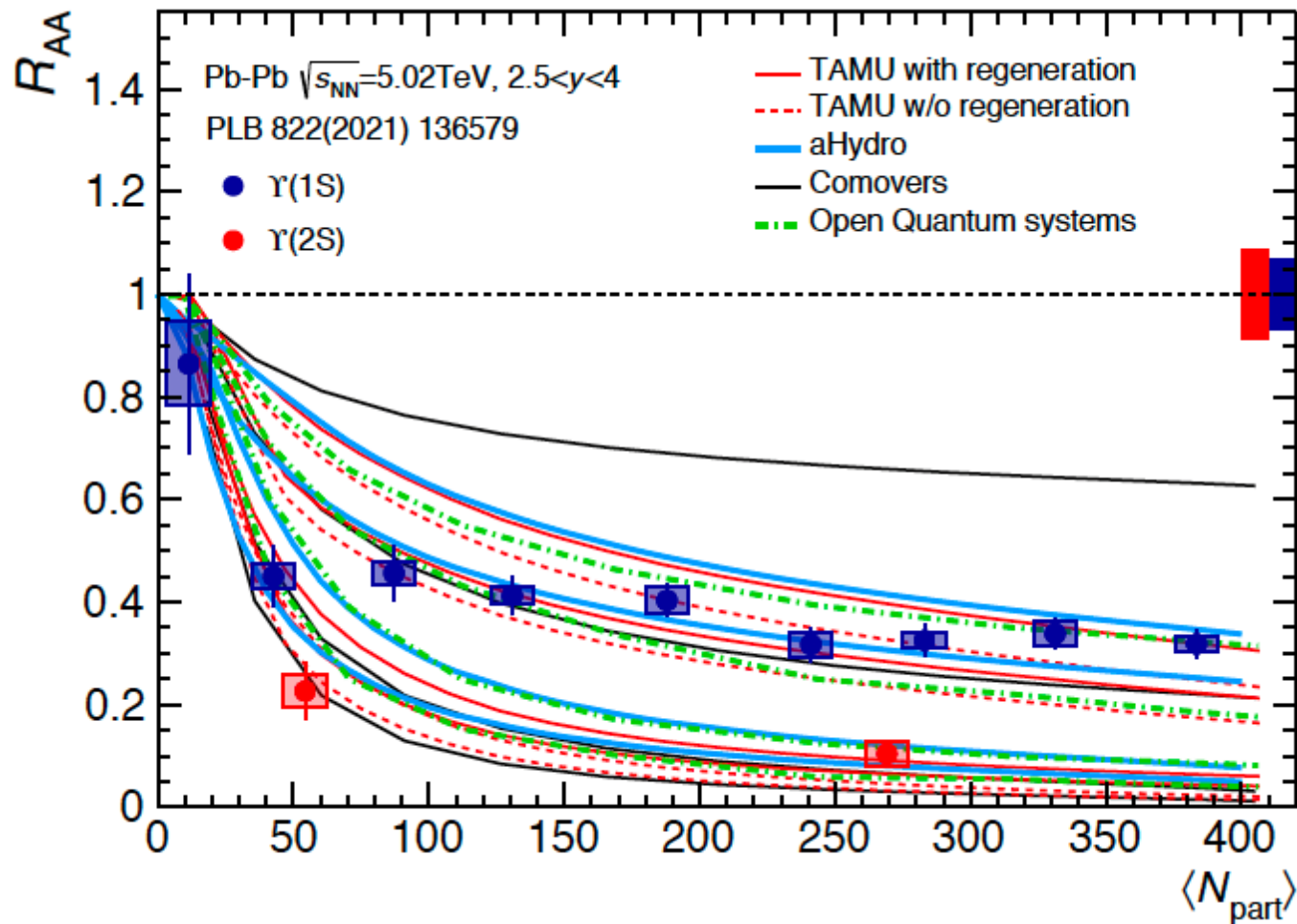
Transport Model (TAMU), Du, Liu, Rapp, [PLB 796 \(2019\) 20](#)

*Substantial remnants of the long-range color confining force in QGP*

# $\Upsilon$ suppression data and models

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ALICE, [arXiv:2212.04348](https://arxiv.org/abs/2212.04348)

All models (except perhaps Comovers ...large uncert.) reproduce the data well  
TAMU: Regeneration important for  $\Upsilon(2S)$

# Summary / Conclusions: charm

- Charm quarks seem to thermalize very effectively (close to 100%) in QGP
- SHM: all charmonium *and open charm states* are generated exclusively at hadronization (chemical freeze-out) ...full color screening

The model is very successful in reproducing the  $J/\psi$  and open charm data  
*A handle for hadronization  $T$  with a mass scale well above  $T$*

- Transport models: continuous  $J/\psi$  destruction and (re)generation in QGP  
(only up to 2/3 of the  $J/\psi$  yield (LHC, central collisions) originates from deconfined  $c$  and  $\bar{c}$  quarks)

*Discriminating the two pictures implies providing an answer to fundamental questions related to the fate of hadrons in a hot deconfined medium.*

A precision ( $\pm 10\%$ ) measurement of  $d\sigma_{c\bar{c}}/dy$  in Pb-Pb (Au-Au) collisions needed for a stringent test  
(within reach with the upgraded detectors at the LHC and RHIC)

# Summary / Conclusions: beauty

- Full beauty thermalization seems not realized in nature  
...with 30-50% of beauty quarks fully thermalized SHM can explain the  $\Upsilon$  data  
...but this fraction is (significantly) dependent on the b-hadron spectrum

What does non/partially-thermalized beauty produce?

no  $\Upsilon$  because strong coupling with the medium destroys the  $b\bar{b}$  correlation?

- Transport and Hydro models are successfully reproducing  $\Upsilon$  suppression  
Transport: regeneration important for  $\Upsilon(2S)$  (at the LHC)
- Quantum approaches on strong rise

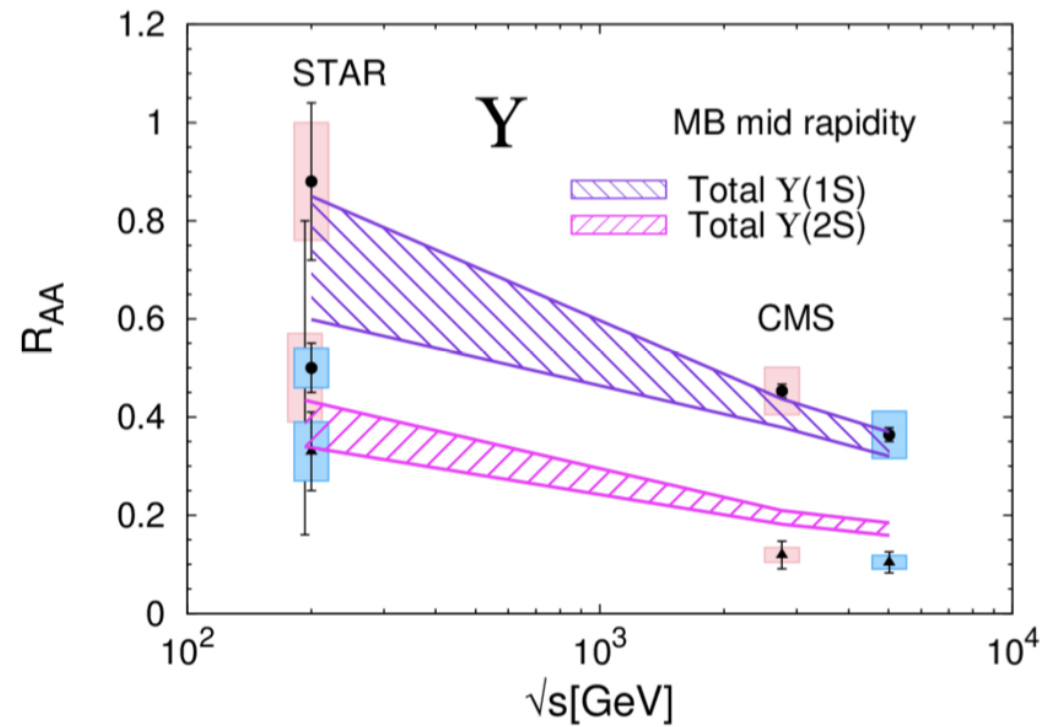
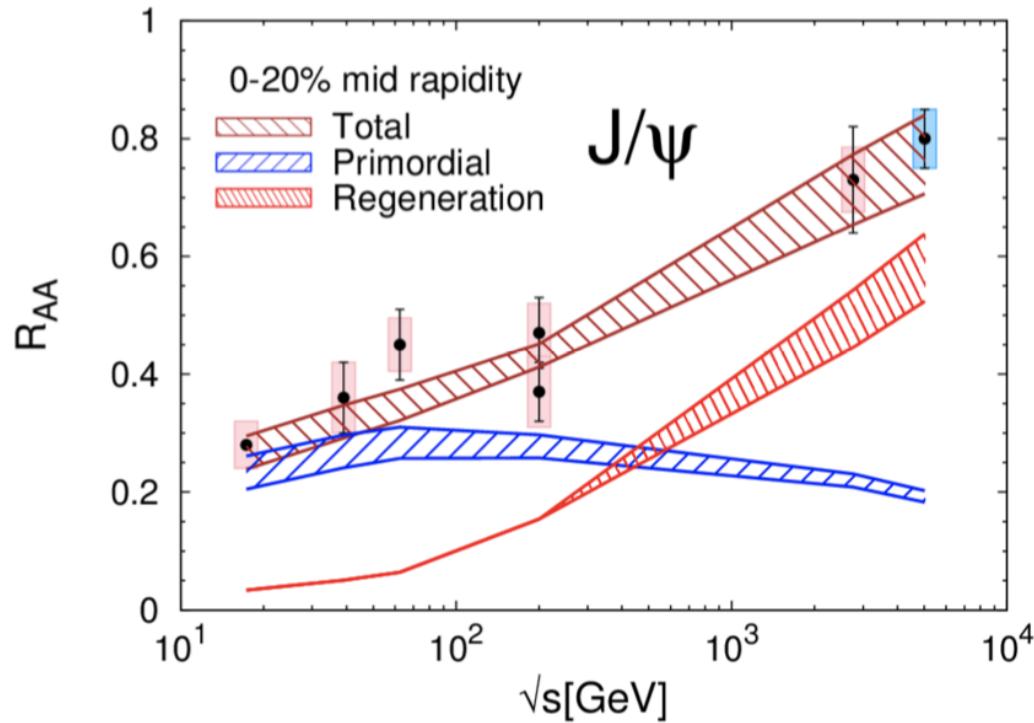
# Additional material

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# Fractions primordial, (re)generated - energy dependence

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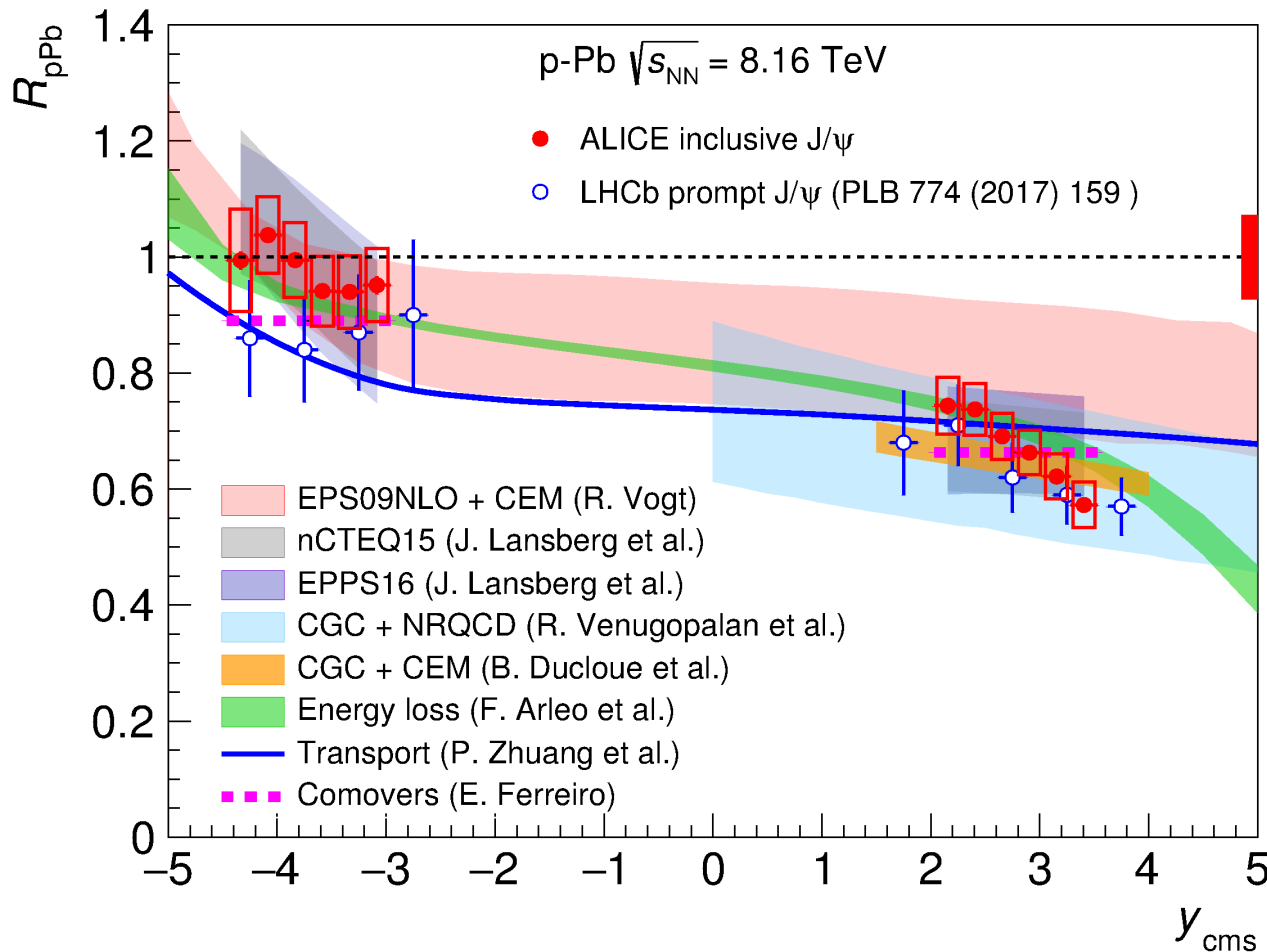


Rapp, Du, [arXiv:1704.07923](https://arxiv.org/abs/1704.07923)

# J/ψ production in p–Pb collisions

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$$7 \cdot 10^{-3} \lesssim x \lesssim 3 \cdot 10^{-2}$$

$$10^{-5} \lesssim x \lesssim 5 \cdot 10^{-5}$$

$$R_{pPb} = \frac{dN_{pPb}/dp_T dy}{\langle N_{coll}^{pPb} \rangle \cdot dN_{pp}/dp_T dy}$$

$$\langle N_{coll}^{pPb} \rangle \simeq 7$$

Shadowing describes data  
(shadowing uncert. are large)

Color Glass Condensate also  
successful

ALICE, [JHEP 07 \(2018\) 160](#)

LHCb, [PLB 774 \(2017\) 159](#)

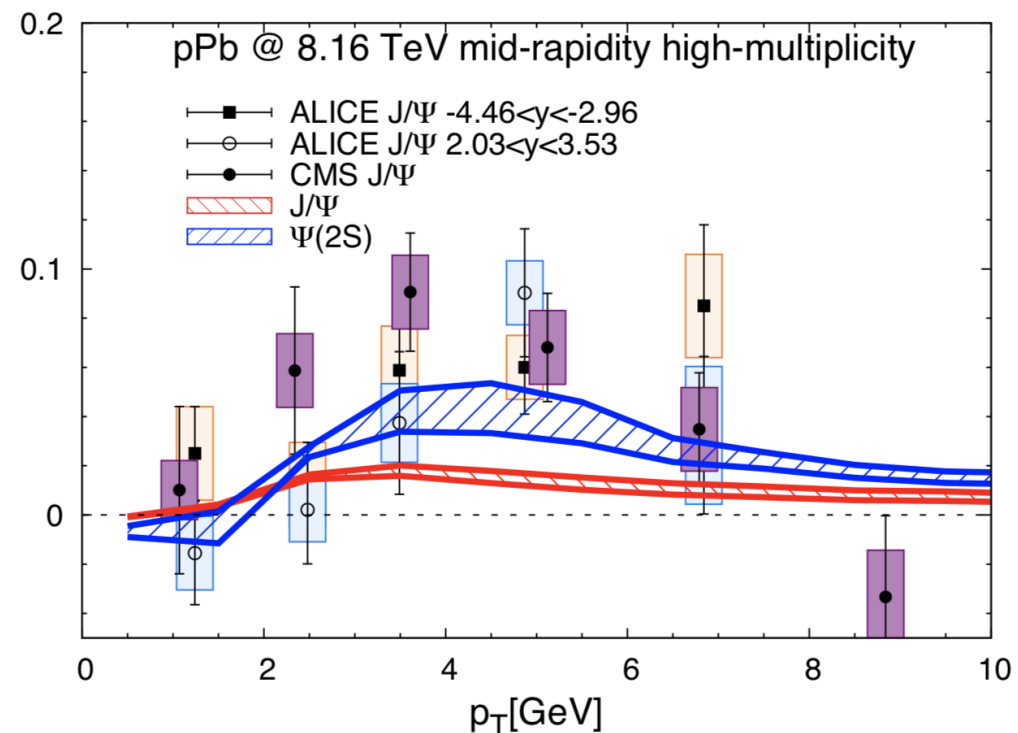
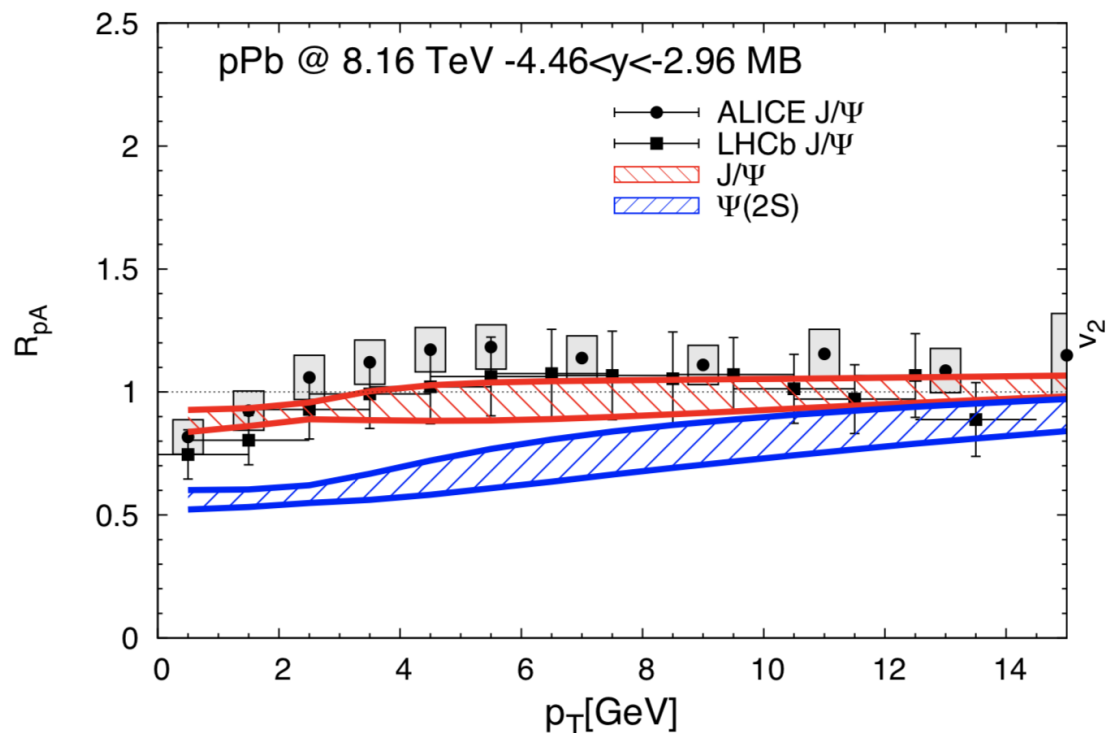
Seen also with Run 1 data (5.02 TeV): ALICE, [JHEP 02 \(2014\) 073](#), [06 \(2015\) 55](#)



# J/ $\psi$ production in p-Pb collisions

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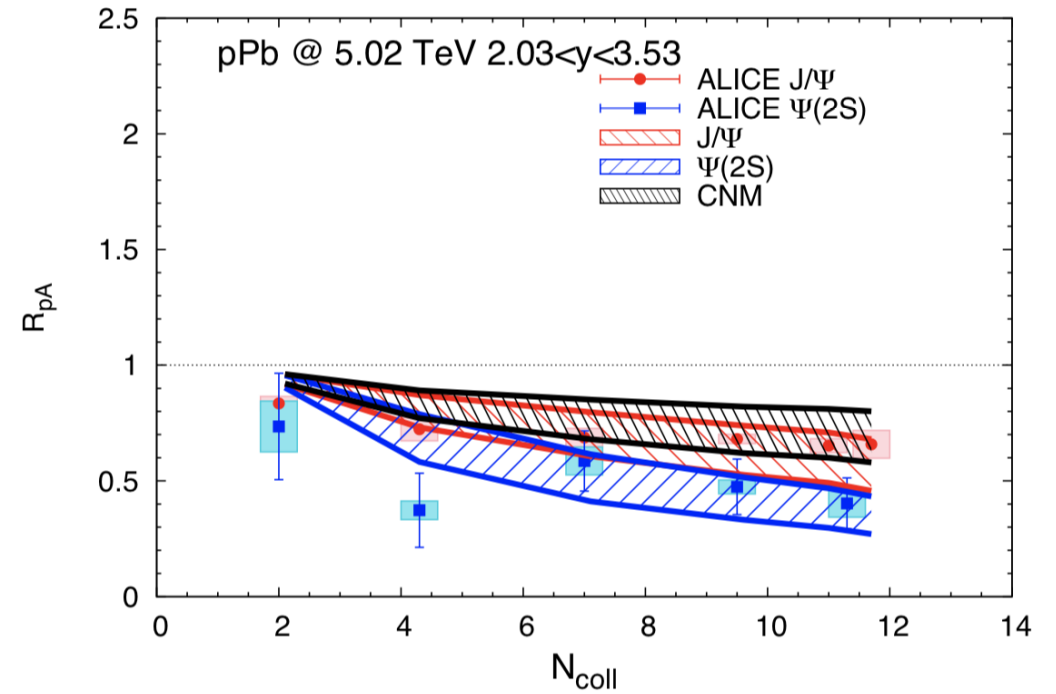
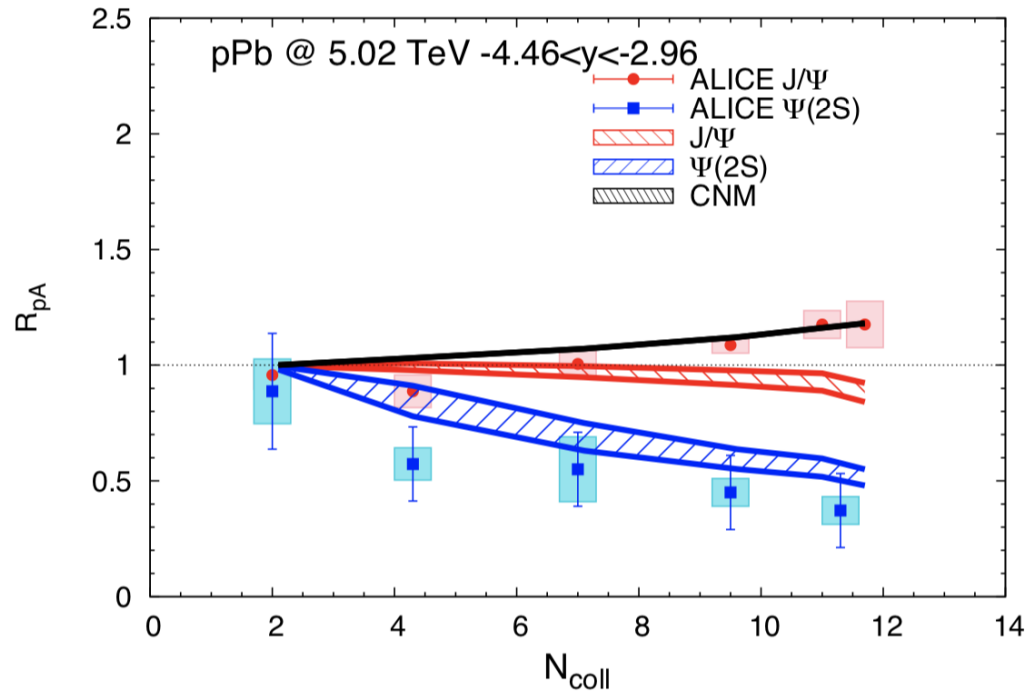
Bands: Transport Model, TAMU  $D_u$ , Rapp, [JHEP 1903 \(2019\) 015](#)

*Need experimentally* (in reach for Run 3,4): better precision; also  $v_3$ ;  
separate  $B$  component;  $v_2$  of  $\psi(2S)$  ?

# $J/\psi$ and $\psi(2S)$ production in p-Pb collisions

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Du, Rapp, [JHEP 1903 \(2019\) 015](#)