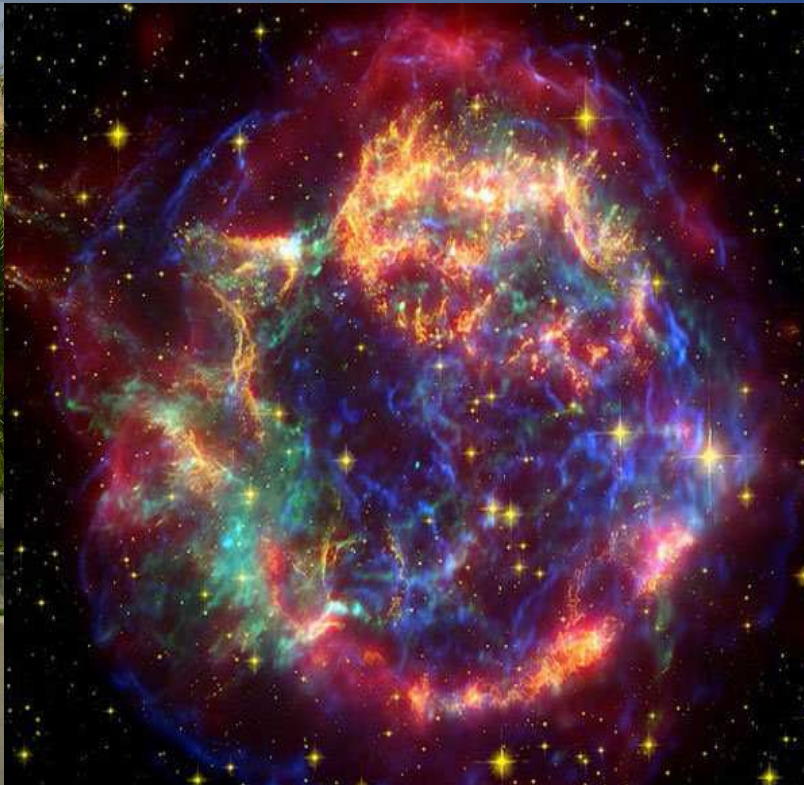


# Structure and Cooling of Compact Stars - an update after J1614-2230 and Cas A

David Blaschke (Wroclaw University, JINR Dubna)



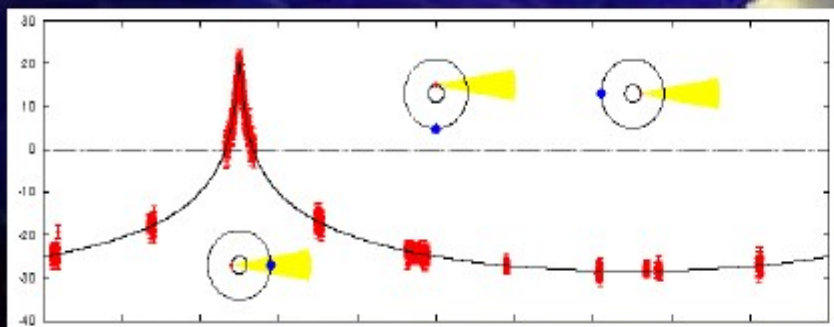
Thanks to 'cool' coauthors:  
Hovik Grigorian, Fridolin Weber, Dima Voskresensky

EMMI Workshop "Dense Baryonic Matter ...", Tübingen, 12.10.12



# PSR J1614-2230 - A new constraint for the Compact Star EoS

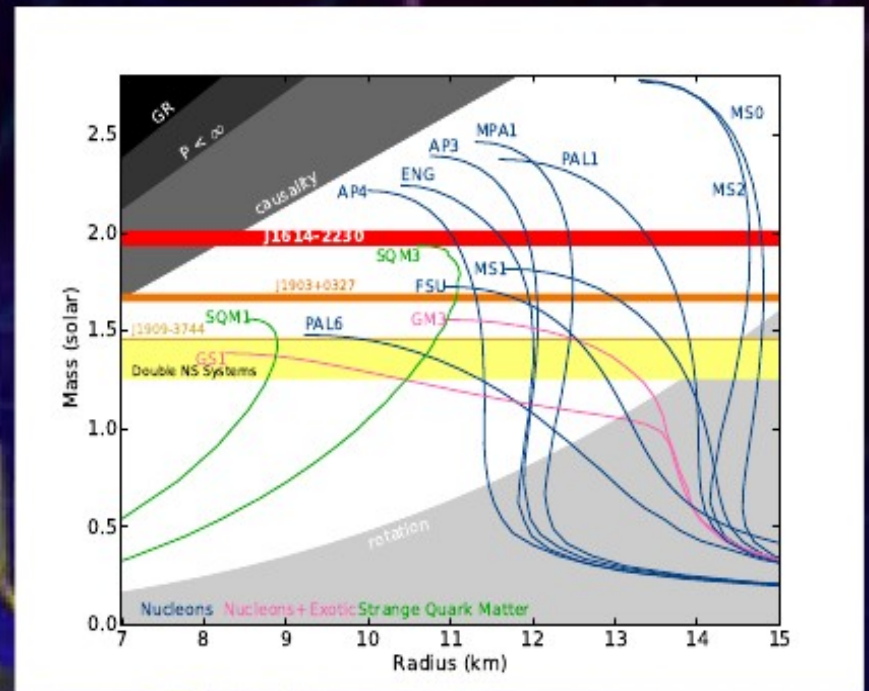
- NS-WD binary in Scorpius
- NS is recycled MSP with  $P = 3.15$  ms
- almost edge-on, inclination  $89.17^\circ$
- Shapiro delay measured!
- $M_{WD} \sim 0.5 M_\odot$
- $M_{NS} = (1.97 \pm 0.04) M_\odot$



Demorest et al., Nature 467, 1081 (2010)

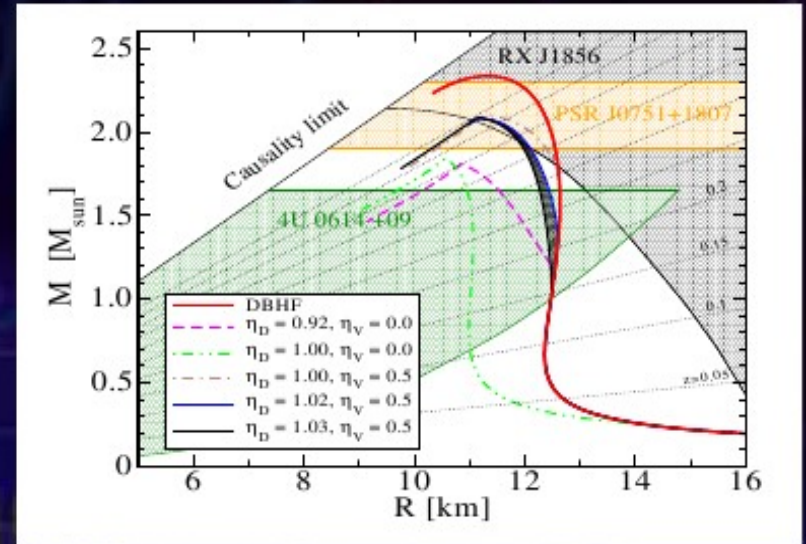


# PSR J1614-2230 - A new constraint for the Compact Star EoS

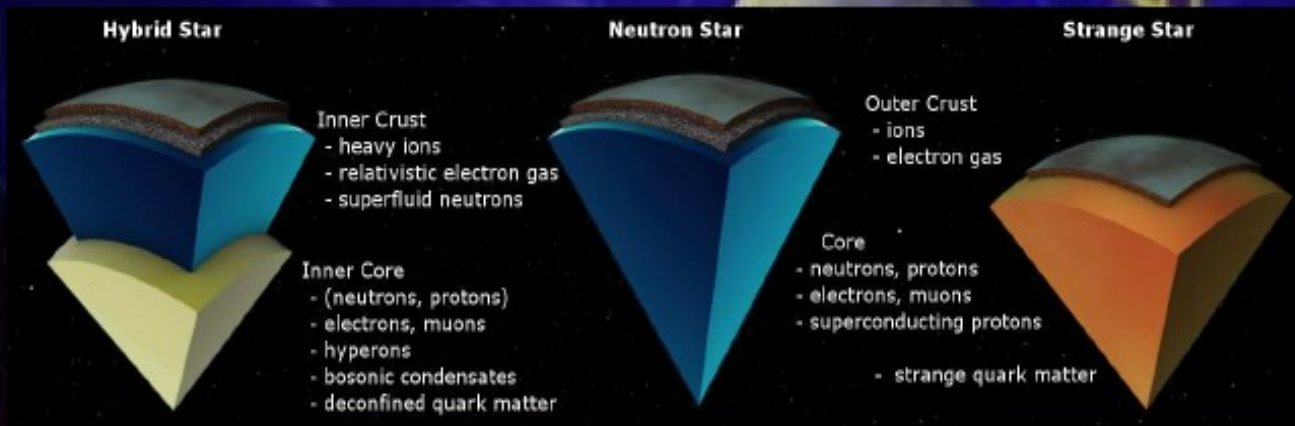


Demorest et al., Nature 467, 1081 (2010)

# PSR J1614-2230 - A new constraint for the Compact Star EoS

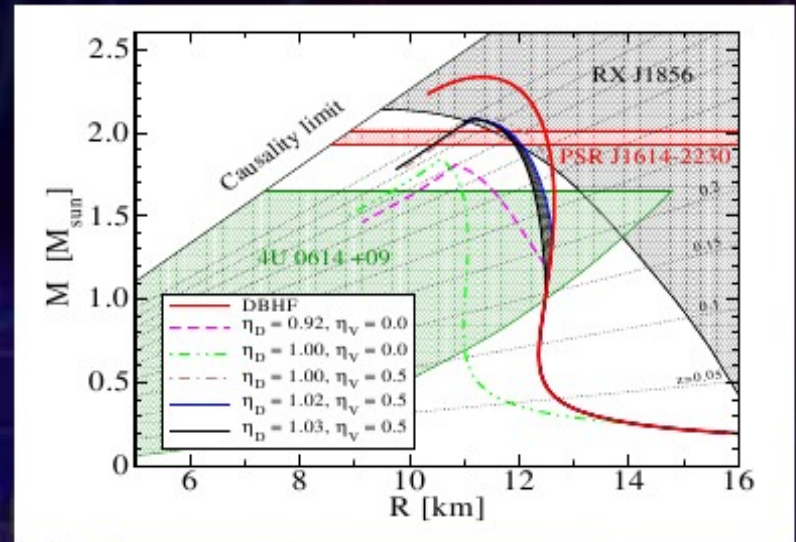


Klähn et al., PLB 654, 170 (2007)





# PSR J1614-2230 - A new constraint for the Compact Star EoS



CompStar, in preparation (2010)

State-of-the-art hybrid EoS model:

- Chiral symmetry restoration
- Color superconductivity
- Vector meanfield “stiffening”

# PSR J1614-2230 - A new constraint for the Compact Star EoS

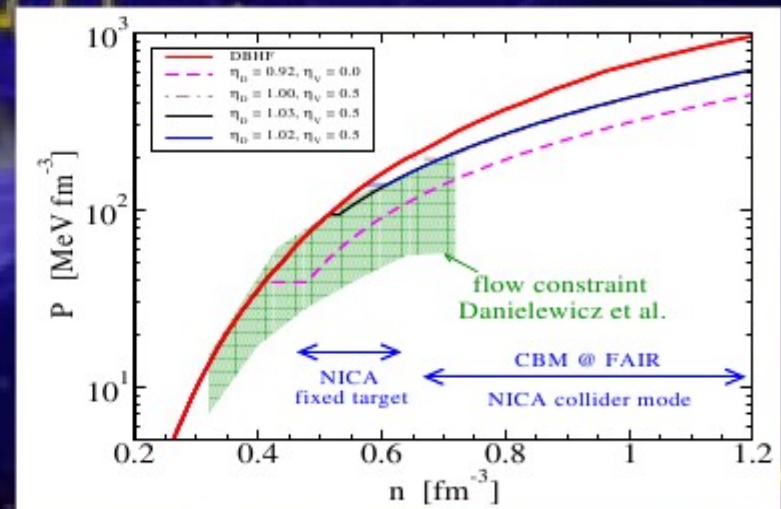
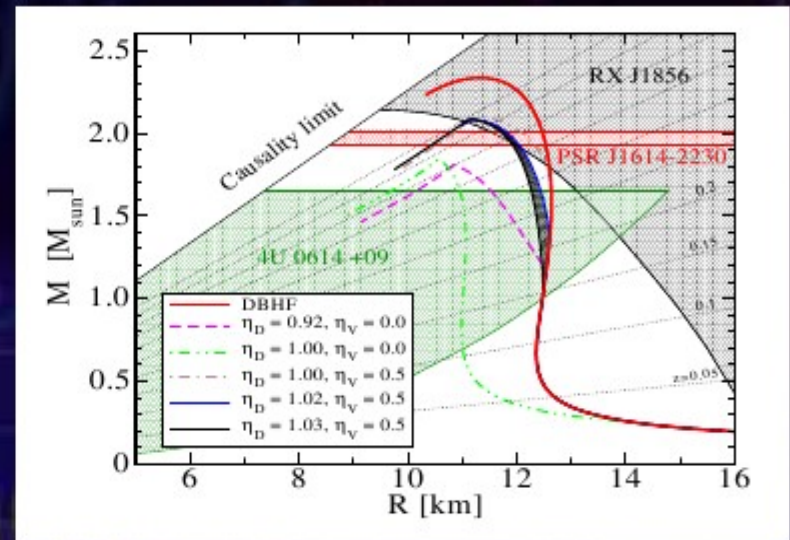
State-of-the-art hybrid EoS model:

- Chiral symmetry restoration
- Color superconductivity
- Vector meanfield “stiffening”

Constraints from heavy-ion collisions:

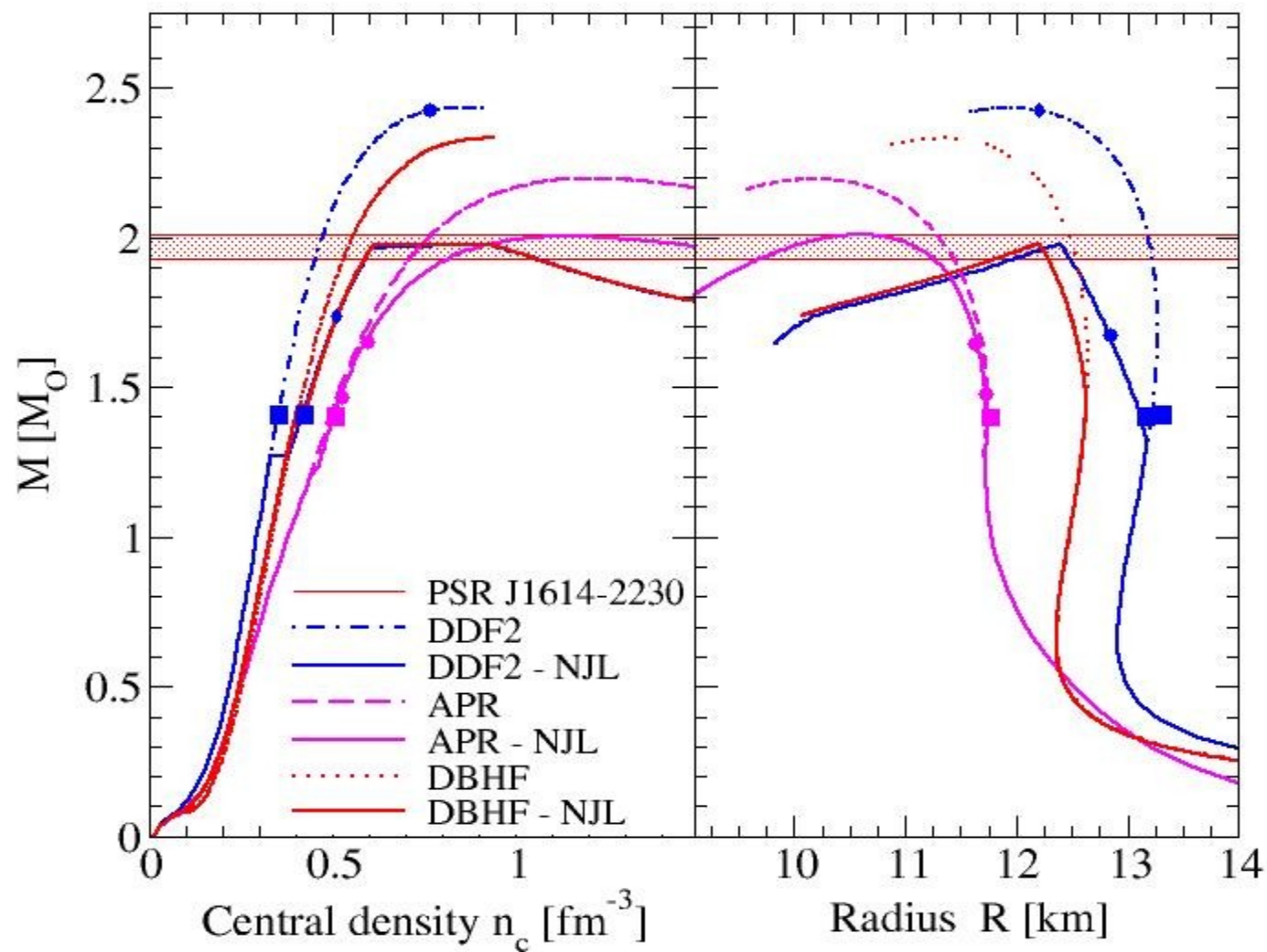
- Flow constraint at high densities
- Not too early onset of quark matter

⇒ **QCD phase diagram**

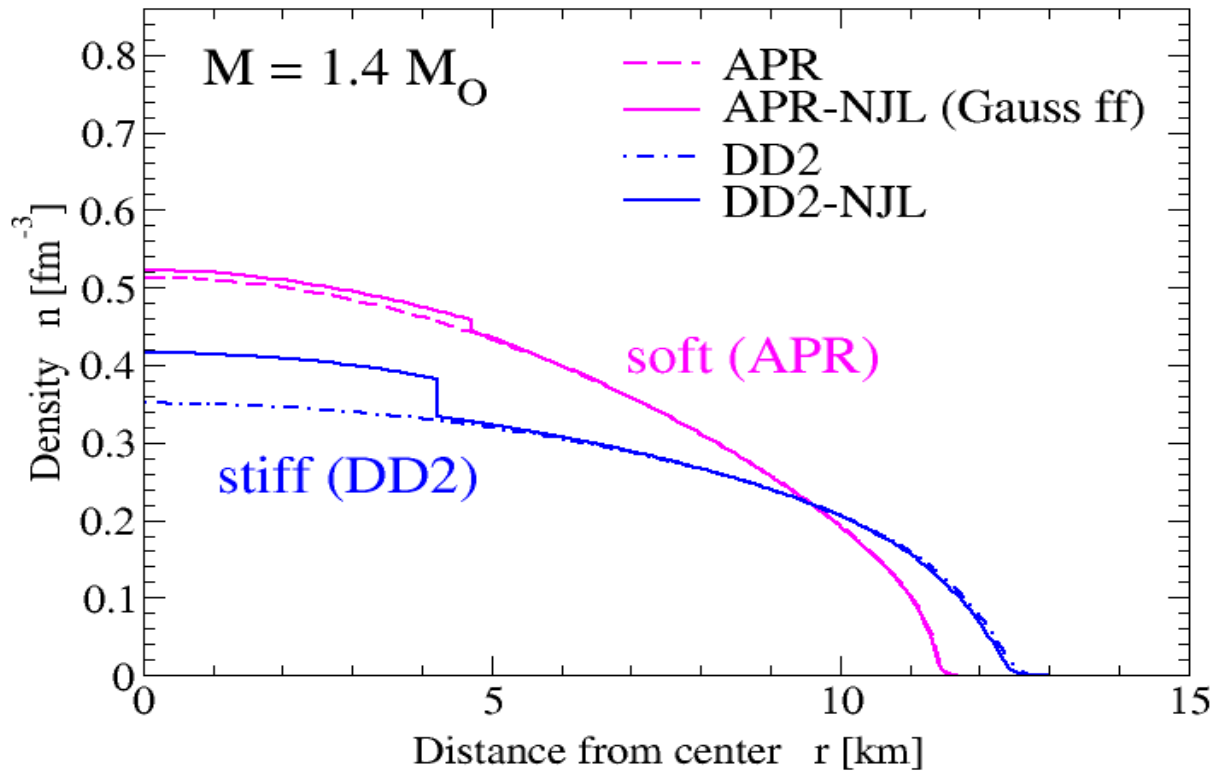




# Hybrid star configuration sequences



# Hybrid star structure



Larger  $M_{\text{max}} \rightarrow$  stiffer EoS  $\rightarrow$  lower central densities, flatter profiles  $\rightarrow$  slower cooling



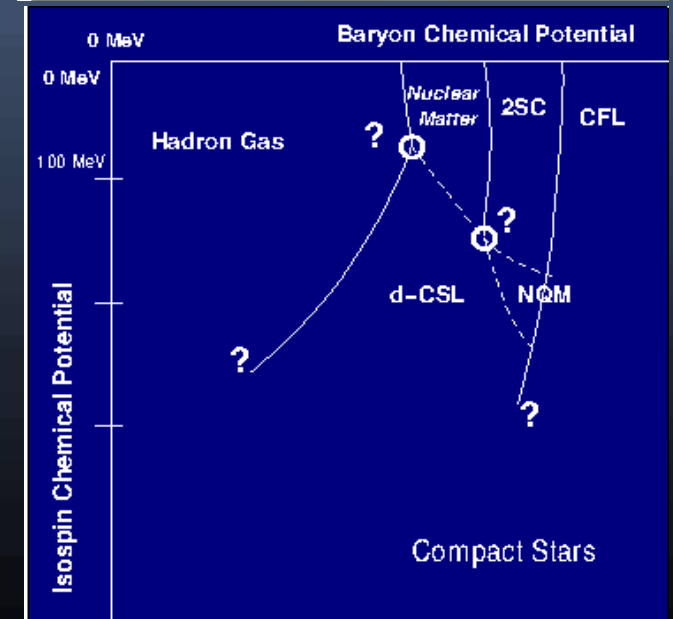
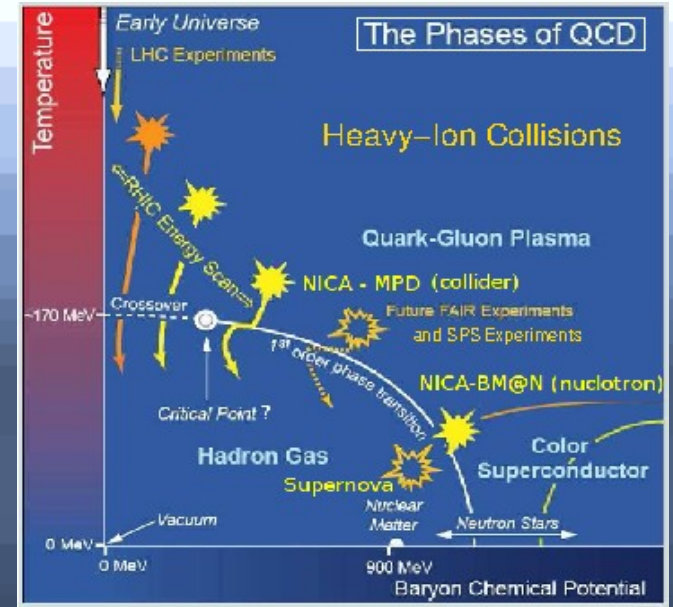
# QCD Phase Diagram

## Heavy-Ion Collisions

Chemical freeze-out  
(Hadron Resonances)

Flow data (EoS)

## Compact Stars

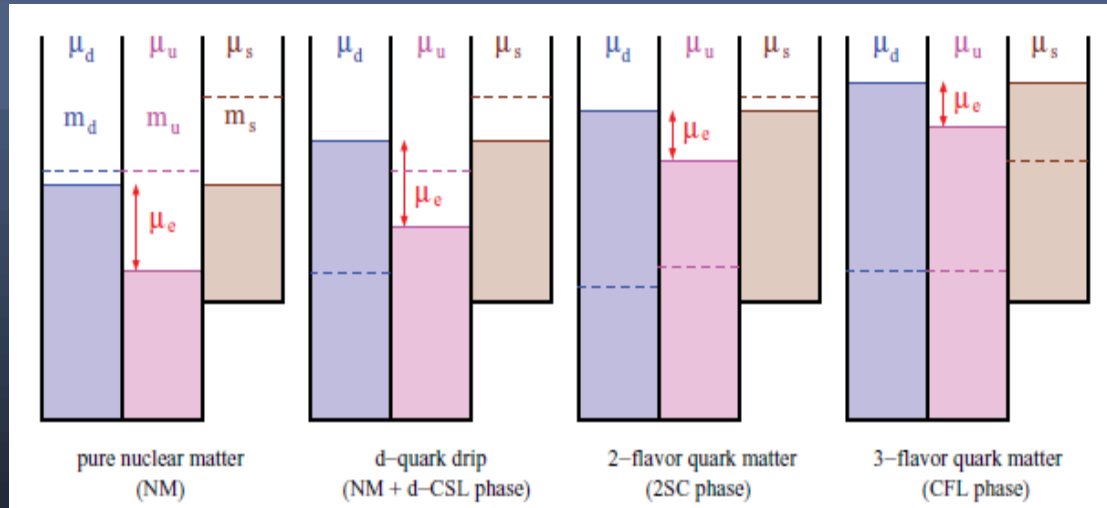


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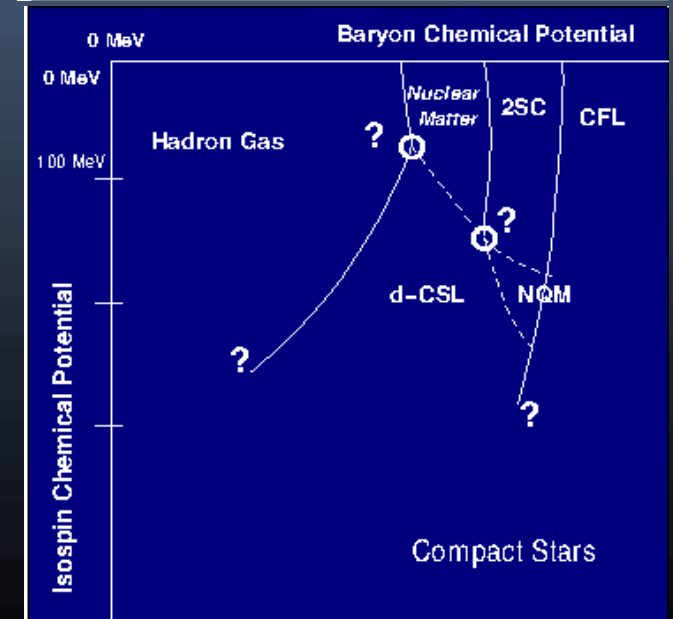
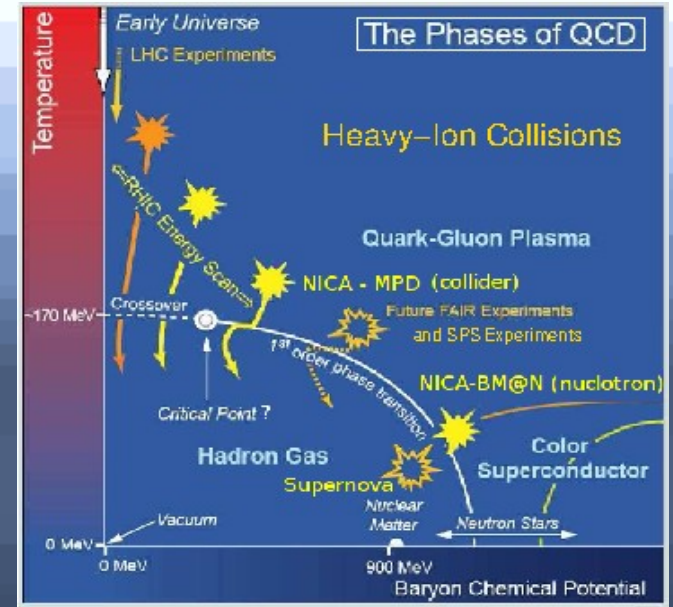
## Compact Stars



→ increasing baryon density

**d-Quark dripline effect (asymmetric matter only!**

D.B., Klahn, Sandin, Berdermann, PRC 80 (2009)



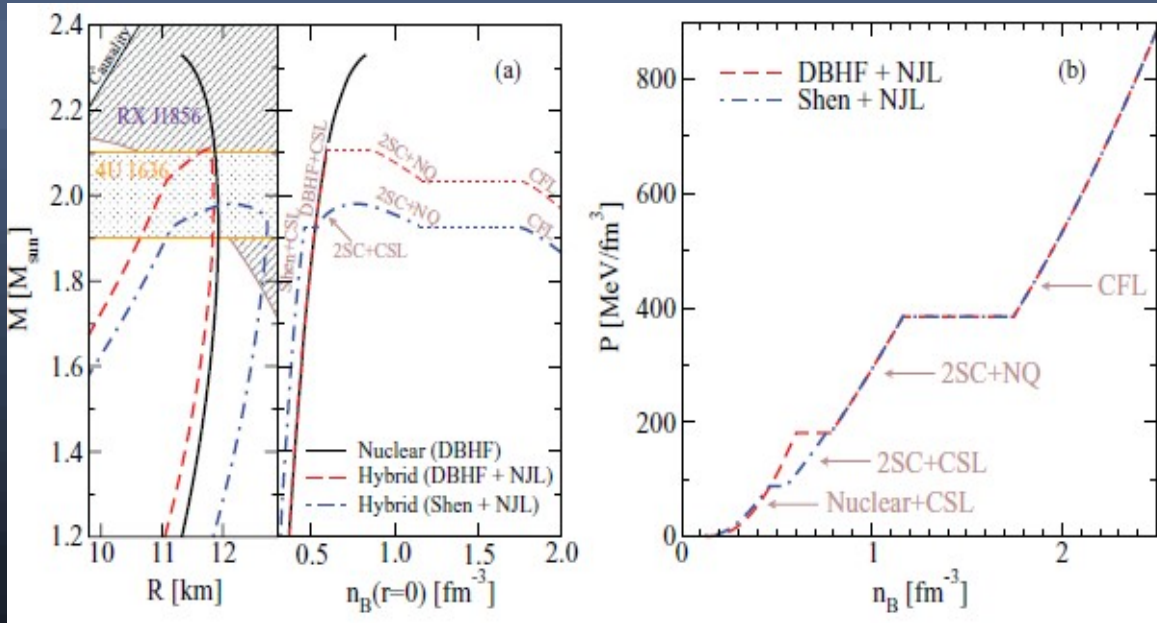


# QCD Phase Diagram

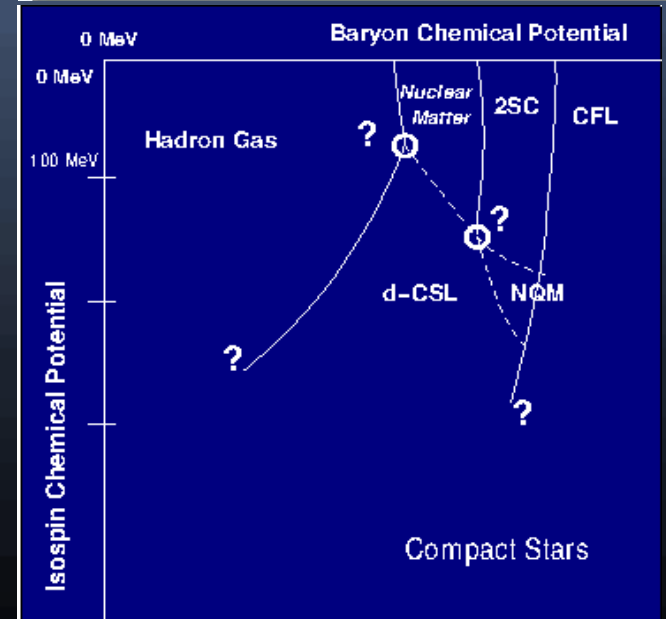
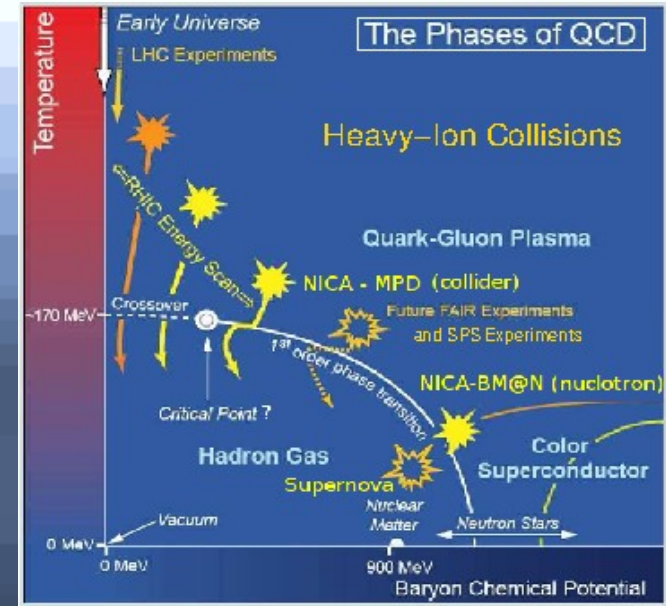
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Chemical freeze-out  
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D.B., Klahn, Sandin, Berdermann, PRC 80 (2009)



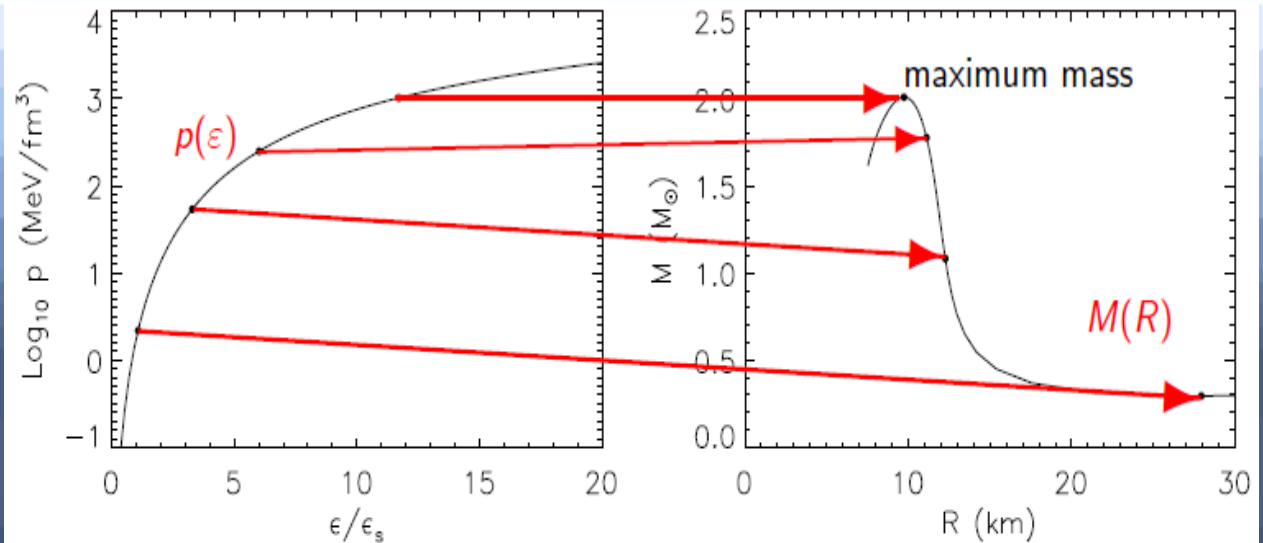
# QCD Phase Diagram

## Heavy-Ion Collisions

Chemical freeze-out  
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Flow data (EoS)

## Compact Stars



Bayesian TOV inversion [Steiner, Lattimer, Brown (2010)]

Tolman-Oppenheimer-Volkov equations

$$\frac{dp}{dr} = -\frac{G}{c^2} \frac{(m + 4\pi pr^3)(\epsilon + p)}{r(r - 2Gm/c^2)}$$
$$\frac{dm}{dr} = 4\pi \frac{\epsilon}{c^2} r^2$$



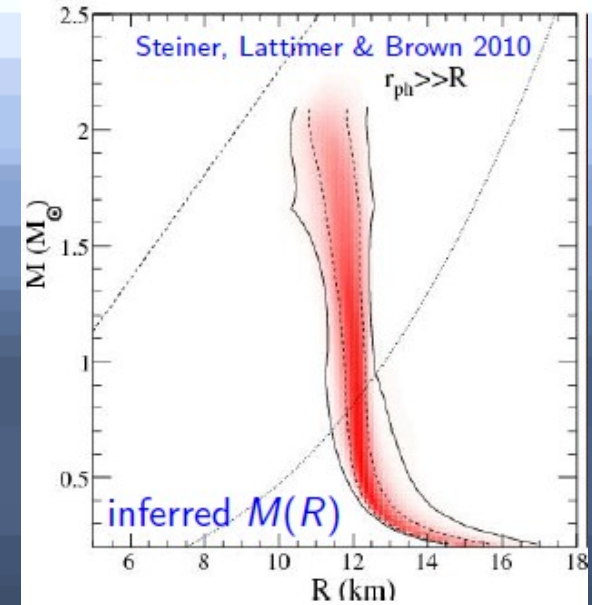
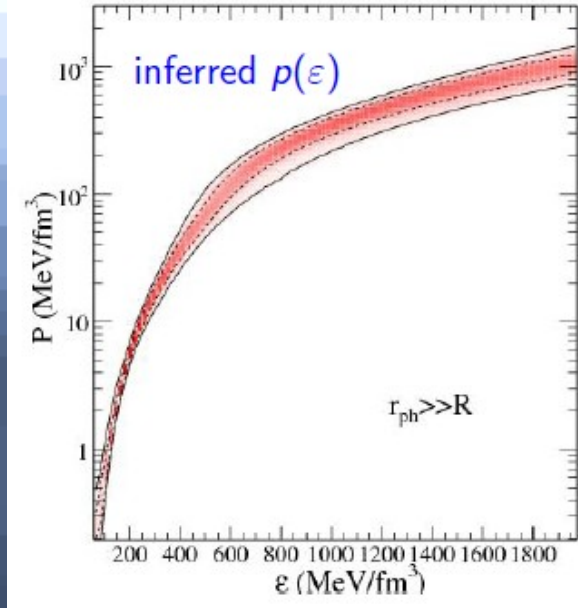
# QCD Phase Diagram

## Heavy-Ion Collisions

Chemical freeze-out  
(Hadron Resonances)  
Flow data (EoS)

## Compact Stars

$M(R) \leftrightarrow P(\epsilon)$



Bayesian TOV inversion [Steiner, Lattimer, Brown (2010)]

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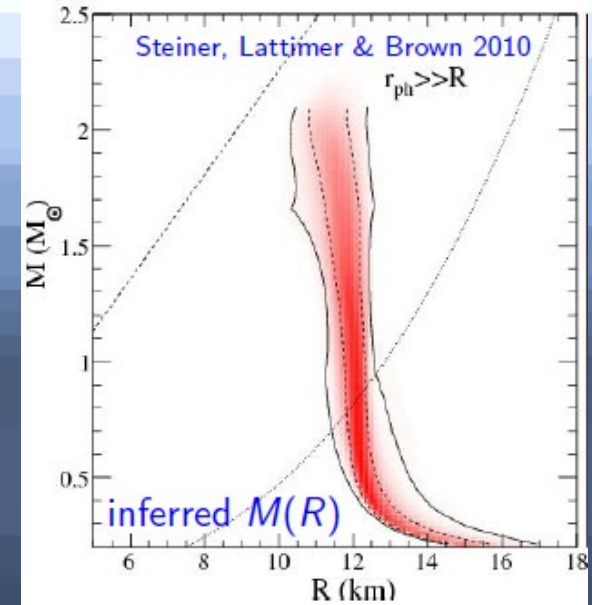
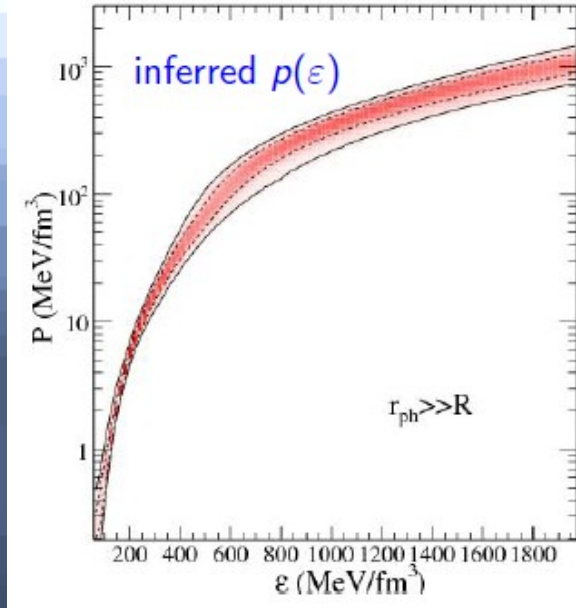
# QCD Phase Diagram

## Heavy-Ion Collisions

Chemical freeze-out  
(Hadron Resonances)  
Flow data (EoS)

## Compact Stars

$M(R) \leftrightarrow P(\epsilon)$



Bayesian TOV inversion [Steiner, Lattimer, Brown (2010)]

- ▶  $\epsilon < 0.5\epsilon_0$ : Known crustal EOS
- ▶  $0.5\epsilon_0 < \epsilon < \epsilon_1$ : EOS parametrized by  $K, K', S_v, \gamma$
- ▶  $\epsilon_1 < \epsilon < \epsilon_2$ :  $n_1$ ;  $\epsilon > \epsilon_2$ : Polytropic EOS with  $n_2$
- ▶ EOS parameters ( $K, K', S_v, \gamma, \epsilon_1, n_1, \epsilon_2, n_2$ ) uniformly distributed
- ▶  $M$  and  $R$  probability distributions for 8 neutron stars treated equally.

$$\epsilon = n_B \left\{ m_B + B + \frac{K}{18}(u-1)^2 + \frac{K'}{162}(u-1)^3 + (1-2x)^2 [S_k u^{2/3} + S_p u^\gamma] + \frac{3}{4} \hbar c x (3\pi^2 n_b x)^{1/3} \right\}$$



# QCD Phase Diagram

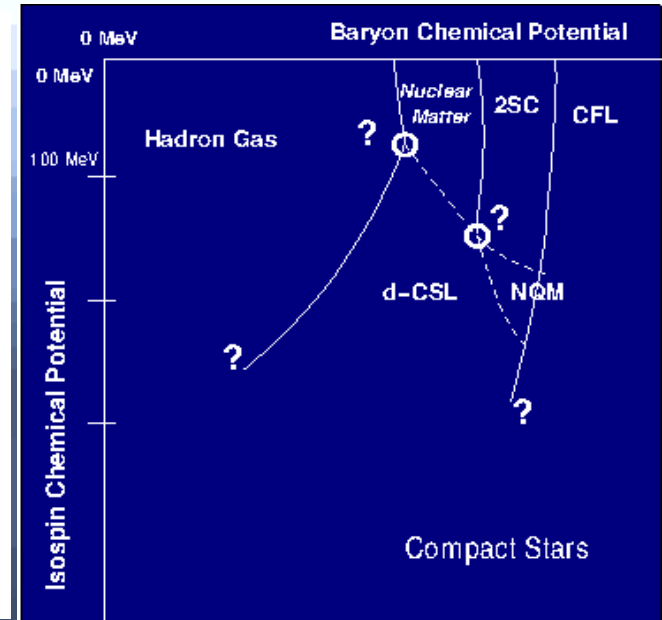
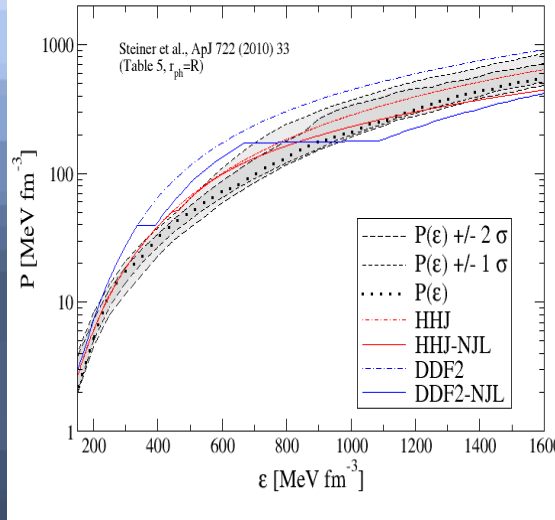
## Heavy-Ion Collisions

Chemical freeze-out  
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Flow data (EoS)

## Compact Stars

$M(R) \leftrightarrow P(\epsilon)$



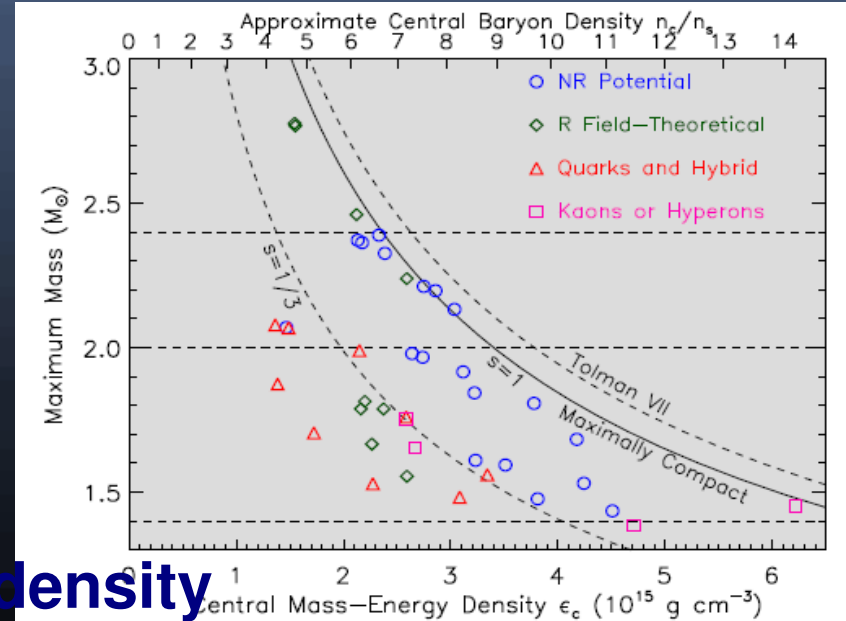
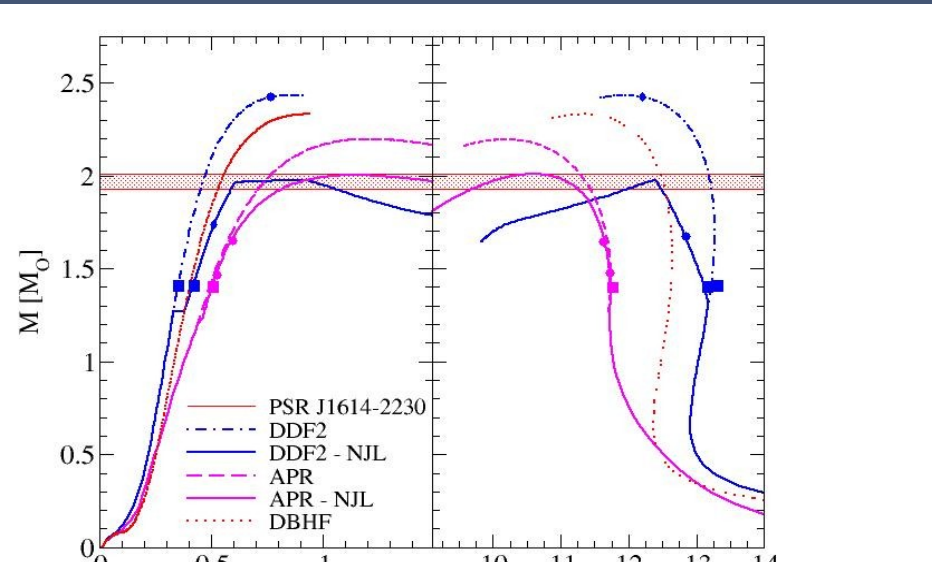
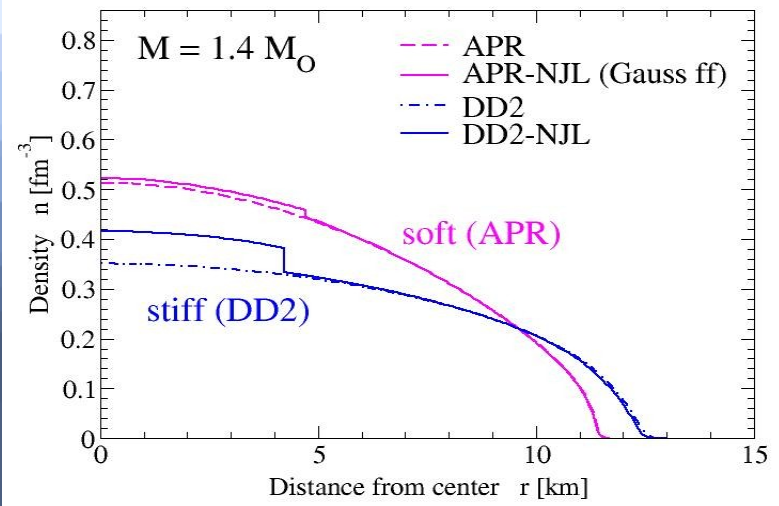
## Comparison with recent hadronic and hybrid EoS:

- Analysis depends on the template for  $P(\epsilon)$
- Systematic investigations of EoS classes possible
- Much more and sufficiently precise data needed!

# QCD Phase Diagram

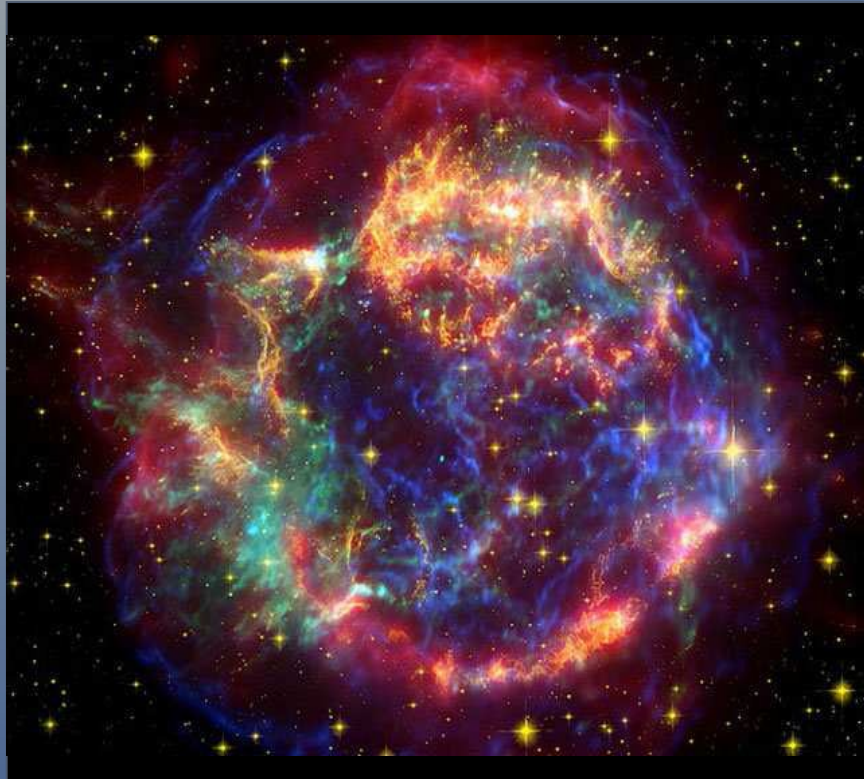
Heavy-Ion Collisions  
 Chemical freeze-out  
 (Hadron Resonances)  
 Flow data (EoS)

Compact Stars  
 $M(R) \leftrightarrow P(\epsilon)$   
 PSR J1614-2230



High max. mass  $\rightarrow$  low central density

# Neutron Star in Cassiopeia A (Cas A)



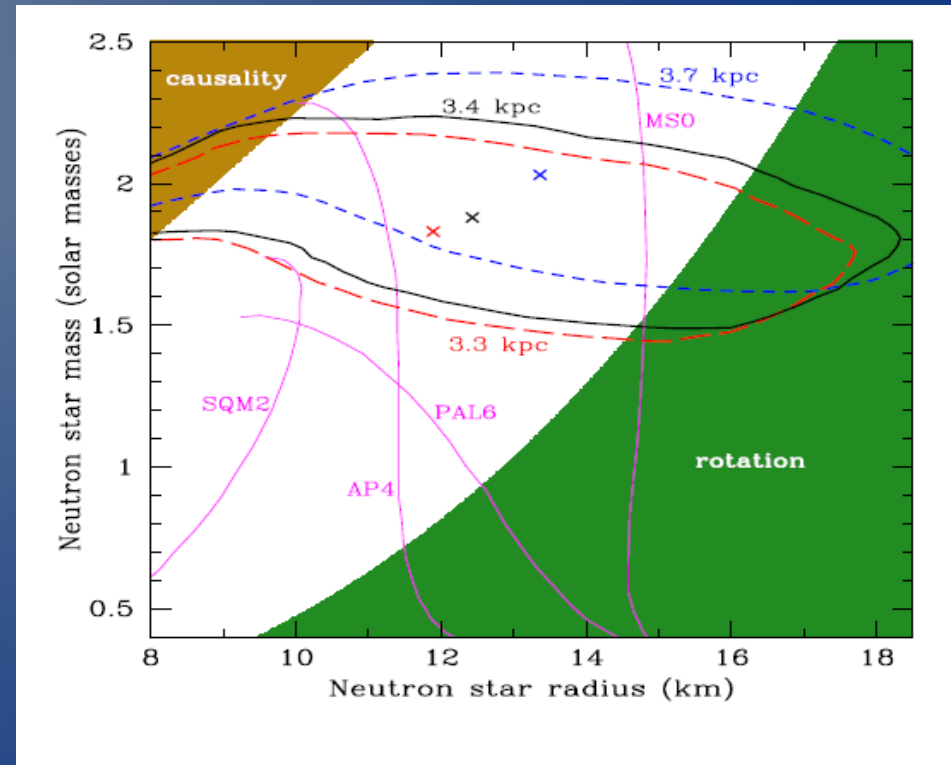
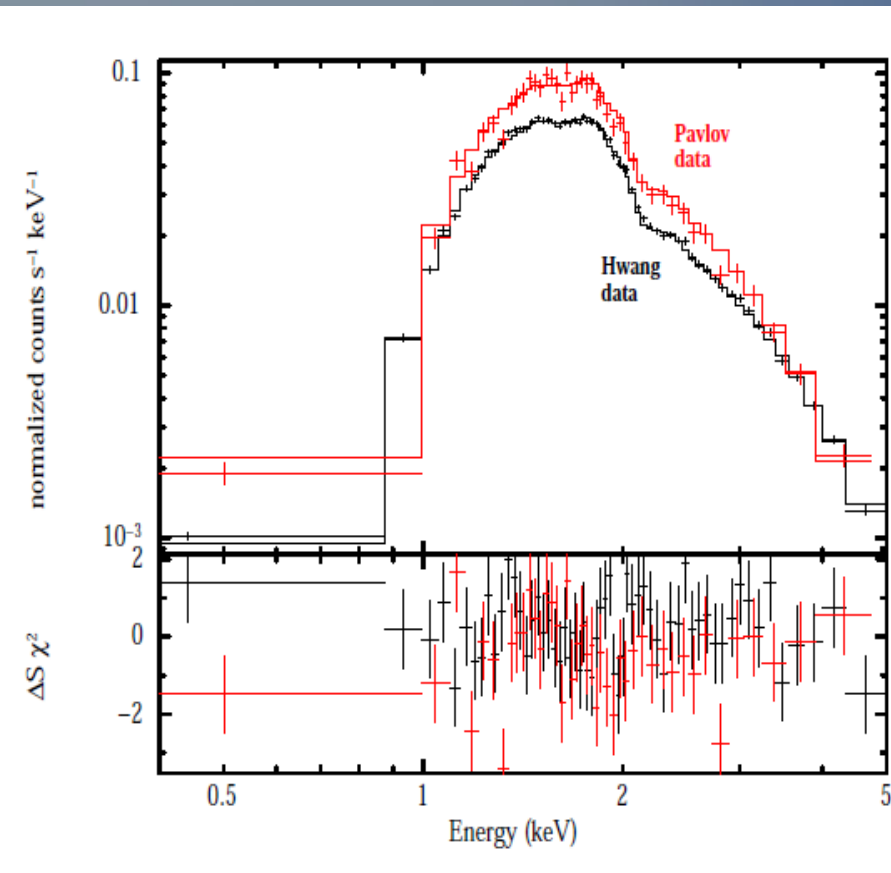
- 16.08.1680 John Flamsteed
  - 6m star 3 Cas
- 1947 re-discovery in radio
  - 1950 optical counterpart
    - $T \sim 30 \text{ MK}$
- $V_{\text{exp}} \sim 4000 - 6000 \text{ km/s}$
- distance  $11.000 \text{ ly} = 3.4 \text{ kpc}$

□ *picture: spitzer space telescope*



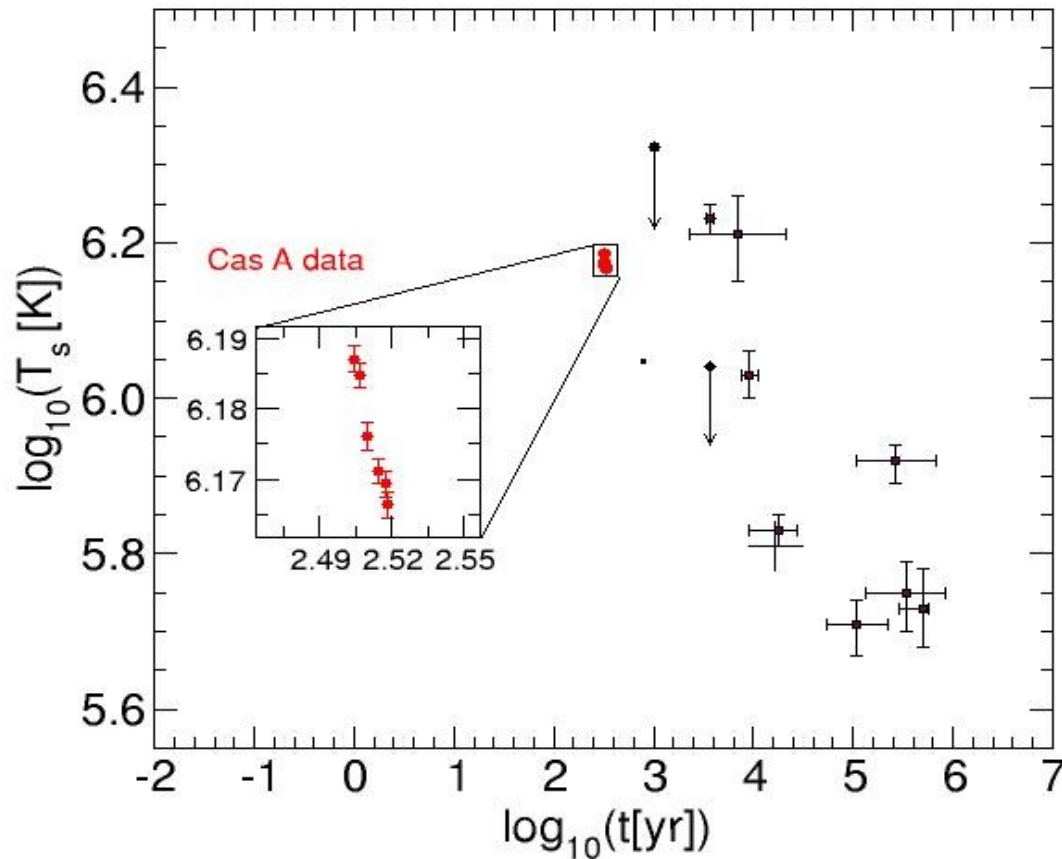
# Cas A Cooling Observations

Cas A is a rapidly cooling star –  
Temperature drop  $\sim 4\%$  in 10 years



- W.C.G. Ho, C.O. Heinke, Nature 462, 71 (2009)

# Cas A Cooling Observations



# Cooling Evolution

The energy flux per unit time  $l(r)$  through a spherical slice at distance  $r$  from the center is:

$$l(r) = -4\pi r^2 k(r) \frac{\partial(Te^\Phi)}{\partial r} e^{-\Phi} \sqrt{1 - \frac{2M}{r}}.$$

The equations for energy balance and thermal energy transport are:

$$\frac{\partial}{\partial N_B}(le^{2\Phi}) = -\frac{1}{n}(\epsilon_\nu e^{2\Phi} + c_V \frac{\partial}{\partial t}(Te^\Phi))$$
$$\frac{\partial}{\partial N_B}(Te^\Phi) = -\frac{1}{k} \frac{le^\Phi}{16\pi^2 r^4 n}$$

where  $n = n(r)$  is the baryon number density,  $N_B = N_B(r)$  is the total baryon number in the sphere with radius  $r$

$$\frac{\partial N_B}{\partial r} = 4\pi r^2 n \left(1 - \frac{2M}{r}\right)^{-1/2}$$

**F.Weber: Pulsars as Astro. Labs ... (1999);**  
**D. Blaschke Grigorian, Voskresensky, A& A 368 (2001)561.**



# Crust Model

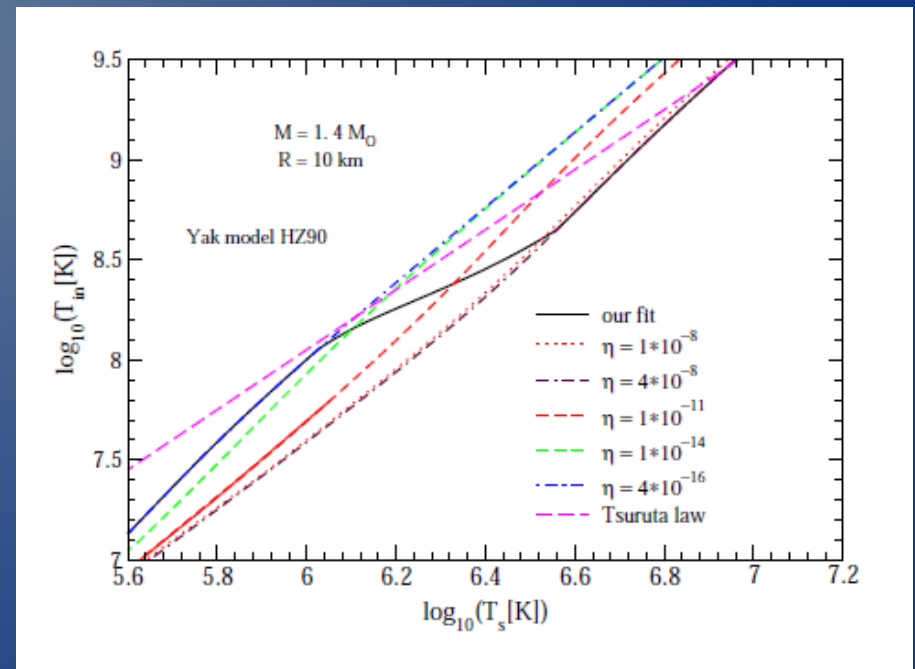
Time dependence of the light element contents in the crust

$$\Delta M_L(t) = e^{-t/\tau} \Delta M_L(0)$$

Page, Lattimer, Prakash & Steiner, *Astrophys. J.* 155, 623 (2004)

Yakovlev, Levenfish, Potekhin, Gnedin & Chabrier, *Astron. Astrophys.*, 417, 169 (2004)

Blaschke, Grigorian, Voskresensky, *A&A* 424 (2004) 979



# Neutrino Emissivities in Quark Matter

Quark direct Urca (QDU) the most efficient process

$$d \rightarrow u + e + \bar{\nu} \text{ and } u + e \rightarrow d + \nu$$

$$\epsilon_{\nu}^{\text{QDU}} \simeq 9.4 \times 10^{26} \alpha_s u Y_e^{1/3} \zeta_{\text{QDU}} T_9^6 \text{ erg cm}^{-3} \text{ s}^{-1},$$

Compression  $n/n_0 \simeq 2$ , strong coupling

Quark Modified Urca (QMU) and Quark Bremsstrahlung

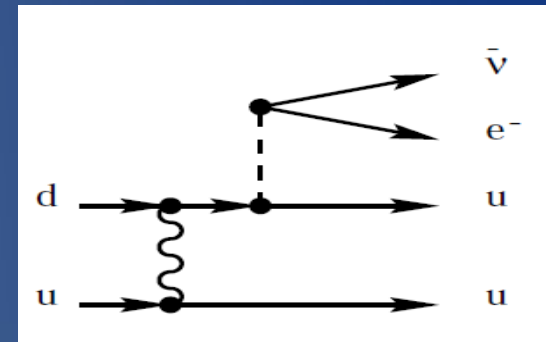
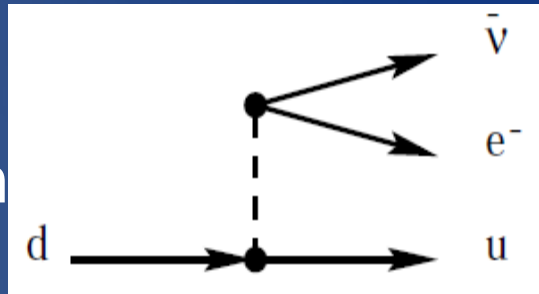
$$d + q \rightarrow u + q + e + \bar{\nu} \text{ and } q_1 + q_2 \rightarrow q_1 + q_2 + \nu + \bar{\nu}$$

$$\epsilon_{\nu}^{\text{QMU}} \sim \epsilon_{\nu}^{\text{QB}} \simeq 9.0 \times 10^{19} \zeta_{\text{QMU}} T_9^8 \text{ erg cm}^{-3} \text{ s}^{-1}.$$

Suppression due to the pairing

**QDU** :  $\zeta_{\text{QDU}} \sim \exp(-\Delta_q/T)$   
**QMU and QB** :  $\zeta_{\text{QMU}} \sim \exp(-2\Delta_q/T)$  for  $T < T_{\text{crit},q} \simeq 0.57 \Delta_q$

Enhanced cooling due to the pairing: Quark PBF



- $e + e \rightarrow e + e + \nu + \bar{\nu}$  (becomes important for  $\Delta_q/T \gg 1$ )

$$\epsilon_{\nu}^{ee} = 2.8 \times 10^{12} Y_e^{1/3} u^{1/3} T_9^8 \text{ erg cm}^{-3} \text{ s}^{-1},$$

Quark PBF

# SC pairing gaps – hybrid stars

2SC phase: 1 color (blue) is unpaired (mixed superconductivity)

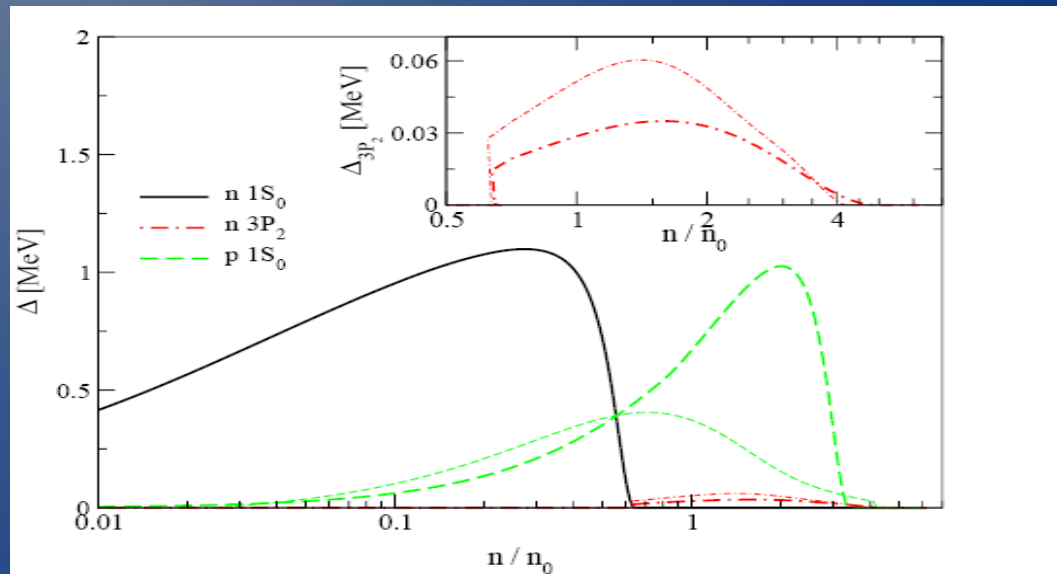
Ansatz 2SC + X phase:

$$\Delta_0^X = \Delta_0 \exp -\alpha \left( \frac{\mu - \mu_c}{\mu_c} \right)$$

Model	$\Delta_0$ [MeV]	$\alpha$	BC	T - t	Log N - Log S	$M_{\text{typ}} \leq 1.5 M_\odot$	All tests
I	1	10	+	+	o	-	-
II	0.1	0	+	-	+	-	-
III	0.1	2	+	o	+	-	-
IV	5	25	+	+	+	+	+

Grigorian, DB, Voskresensky , PRC 71 (2005) 045801

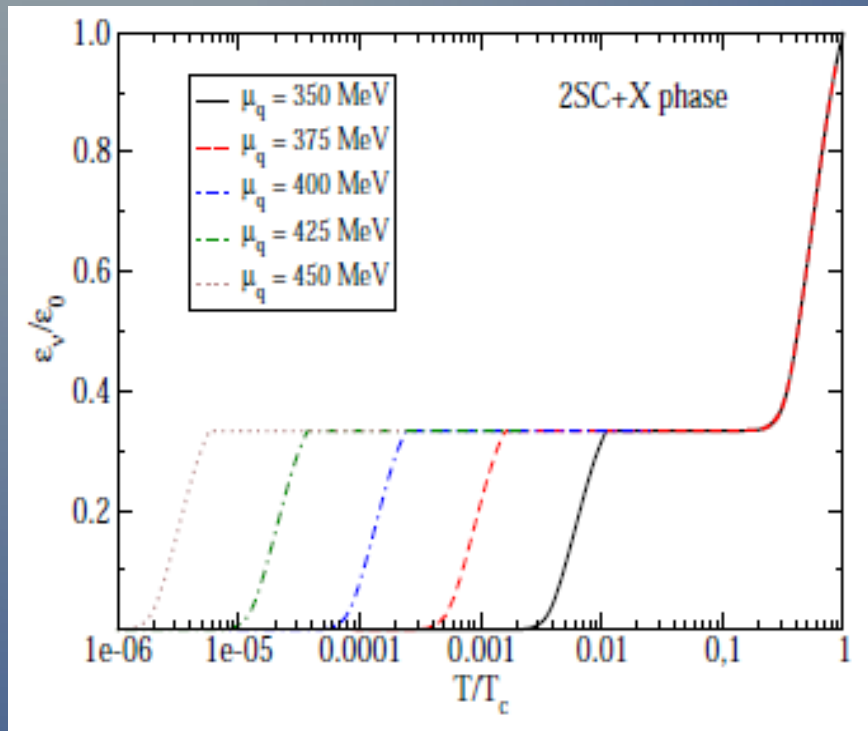
Pairing gaps for hadronic phase  
**(AV18 - Takatsuka et al. (2004)**  
**Yakovlev et al. (1999))**



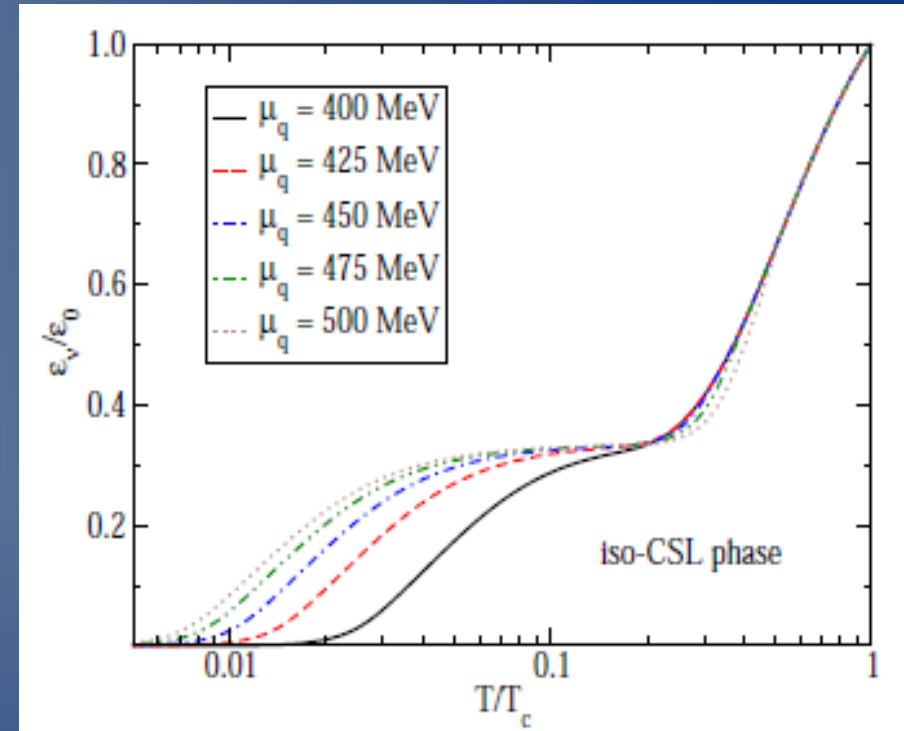
Blaschke, Grigorian, Voskresensky , A&A 424 (2004) 979



# SC pairing gaps – consistent picture?

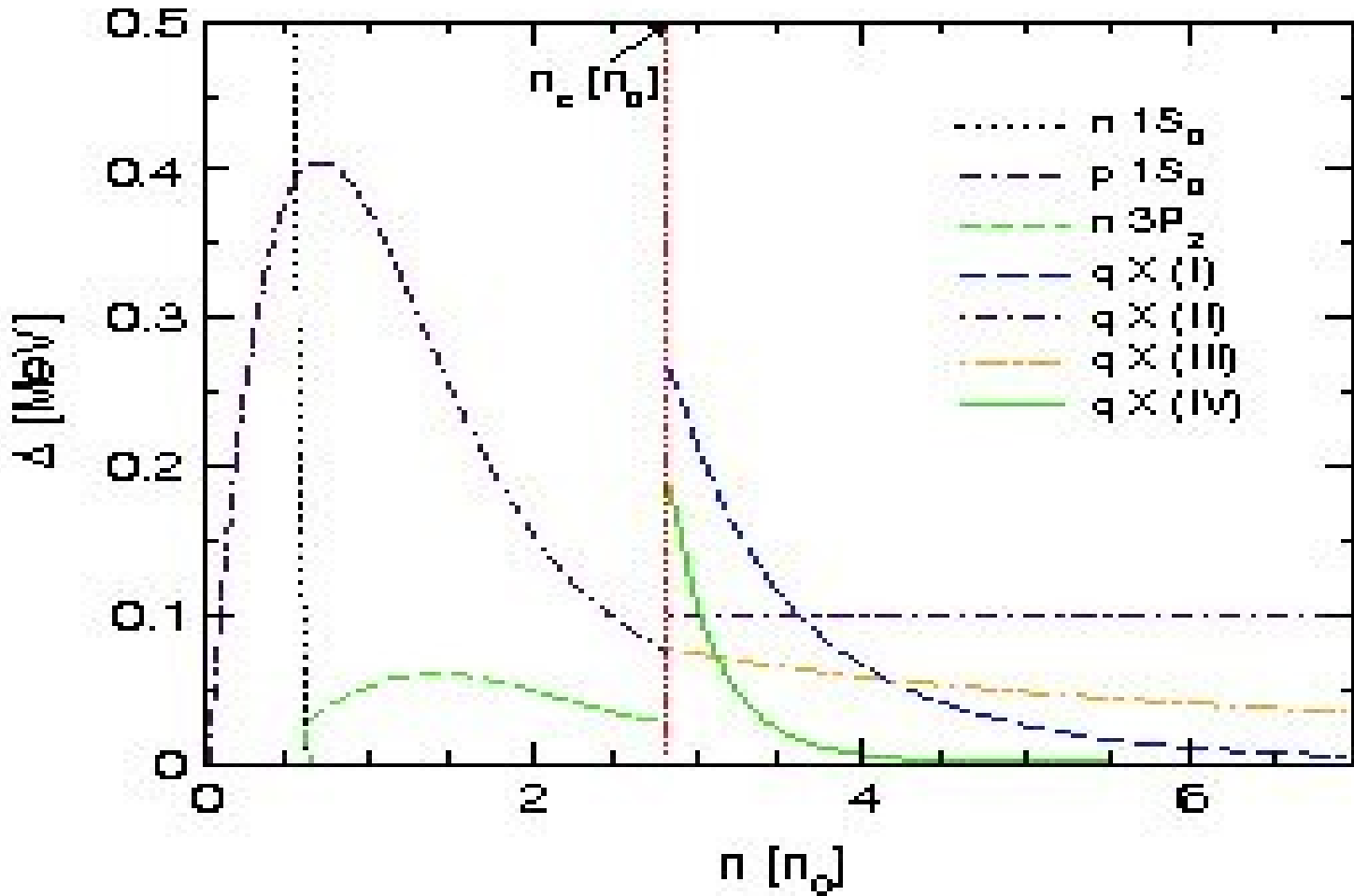


2SC + X phase (blue quarks)



Isotropic CSL phase for d-quarks

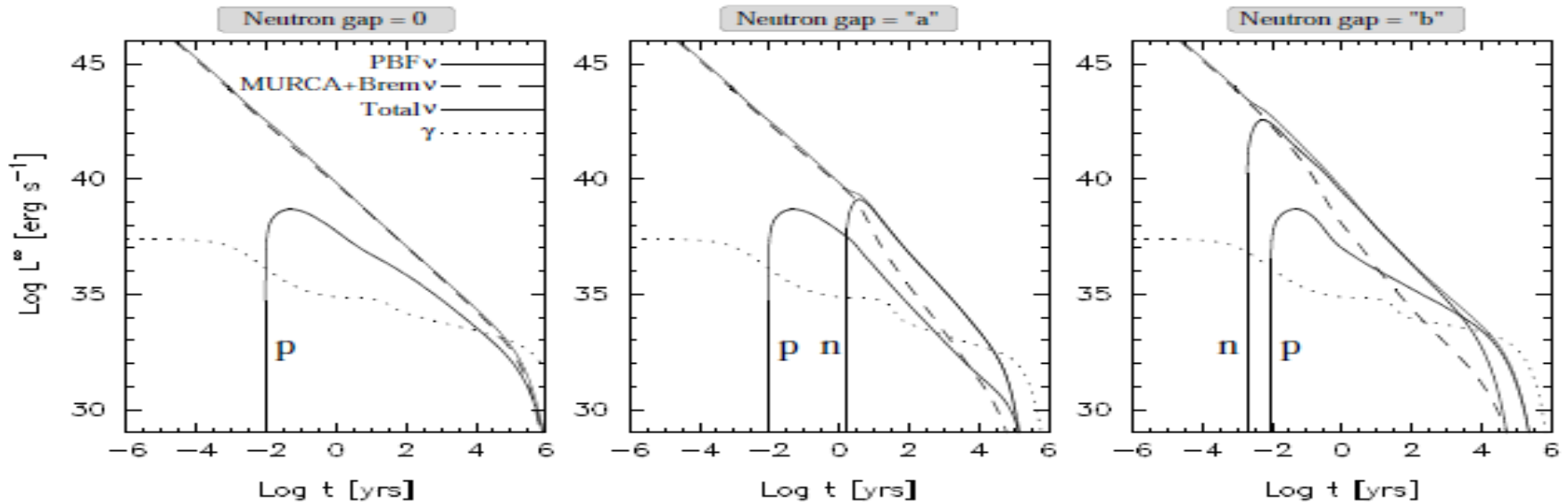
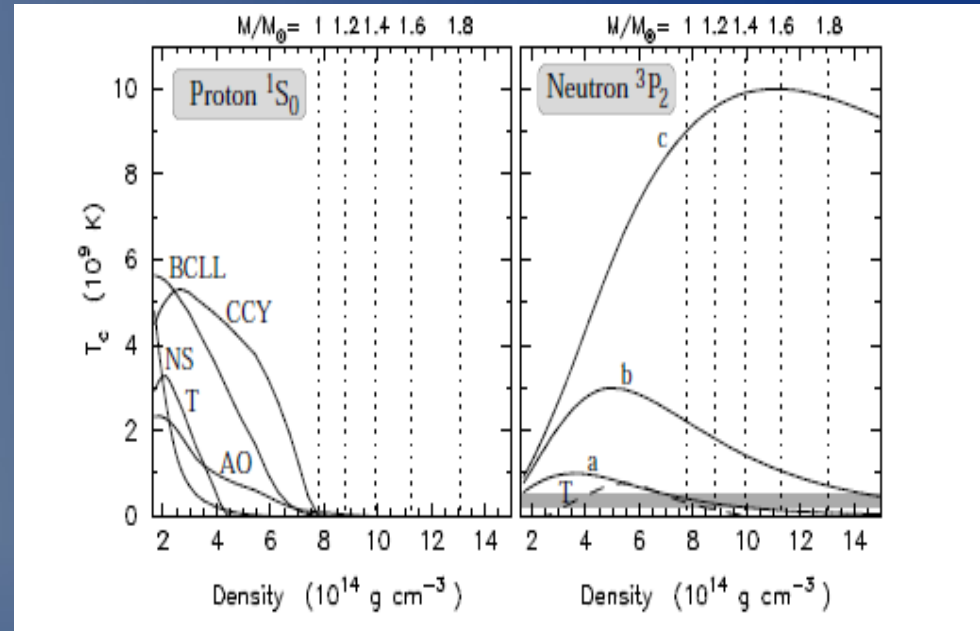
# SC pairing gaps – hybrid stars



# Influence of SC on luminosity

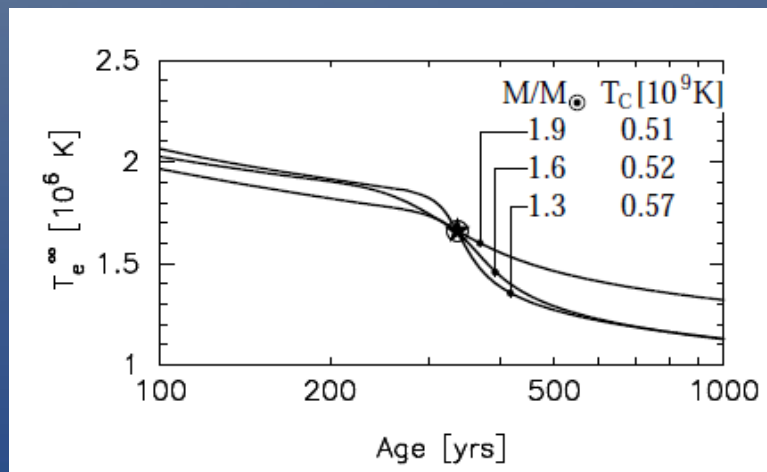
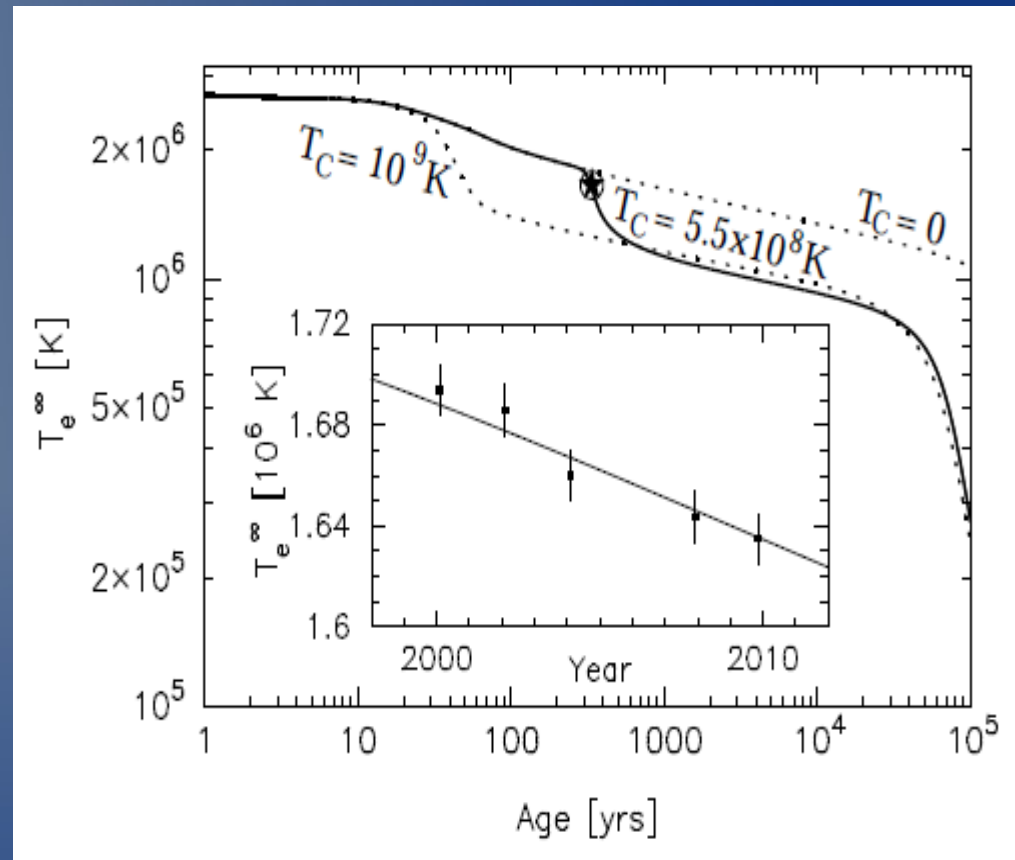
Critical temperature  $T_c$ ,  
for the proton  $^1S_0$  and  
neutron  $^3P_2$  gaps, used in

Page, Lattimer, Prakash & Steiner,  
Astrophys. J. 707 (2009) 1131



# $T_c$ 'measurement' from Cas A

- $1.4 M_{\odot}$  star built from the APR EoS
- Rapid cooling at ages  $\sim 30$ - $100$  yrs due to the thermal relaxation of the crust
- Mass dependence



Page, Lattimer, Prakash & Steiner,  
Phys. Rev. Lett. 106 (2011) 081101



# Medium effects in cooling of neutron stars

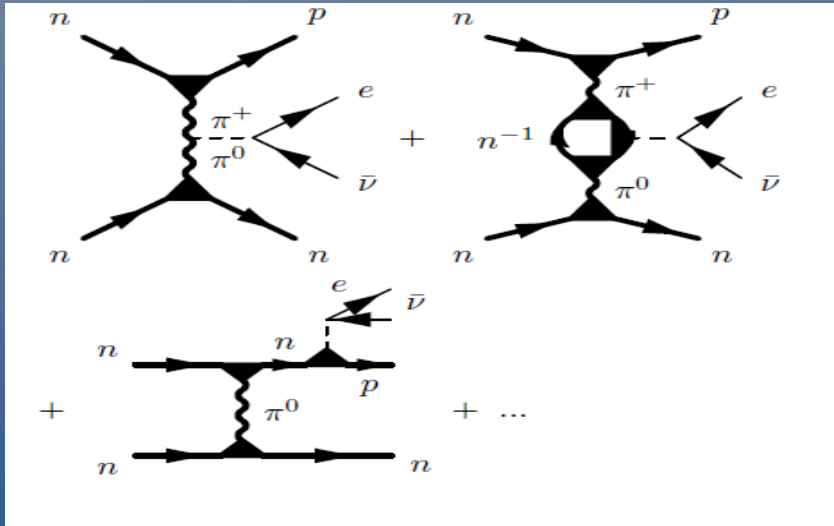
Based on Fermi liquid theory: Landau (1956), Migdal (1967), Migdal et al. (1990):

MMU – medium-modified modified Urca process

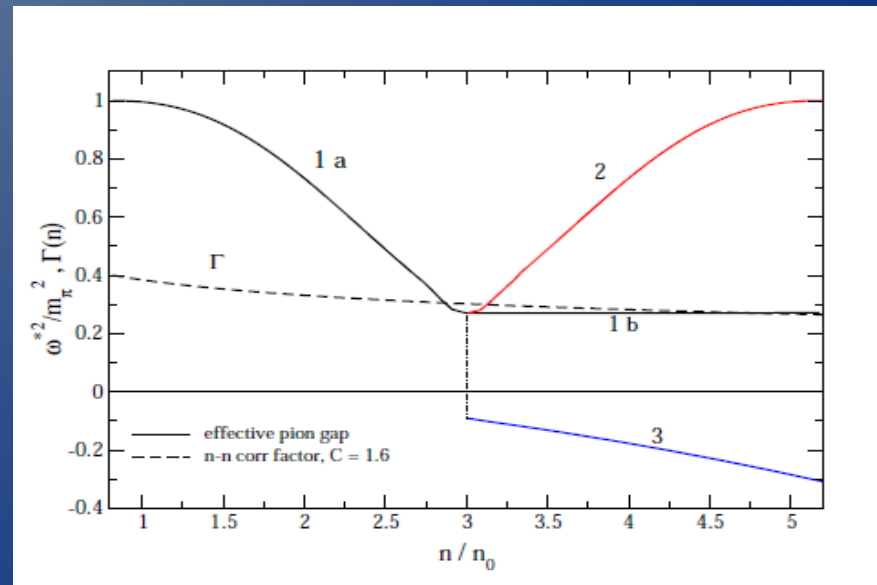
Main regulator in Minimal Cooling:

PBF – pair breaking/formation

$$\epsilon_\nu [\text{MpPBF}] \sim 10^{29} \frac{m_N^*}{m_N} \left[ \frac{p_{Fp}}{p_{Fn}(n_0)} \right] \left[ \frac{\Delta_{pp}}{\text{MeV}} \right]^7 \times \left[ \frac{T}{\Delta_{pp}} \right]^{1/2} \xi_{pp}^2 \frac{\text{erg}}{\text{cm}^3 \text{ sec}}, \quad T < T_{cp}.$$



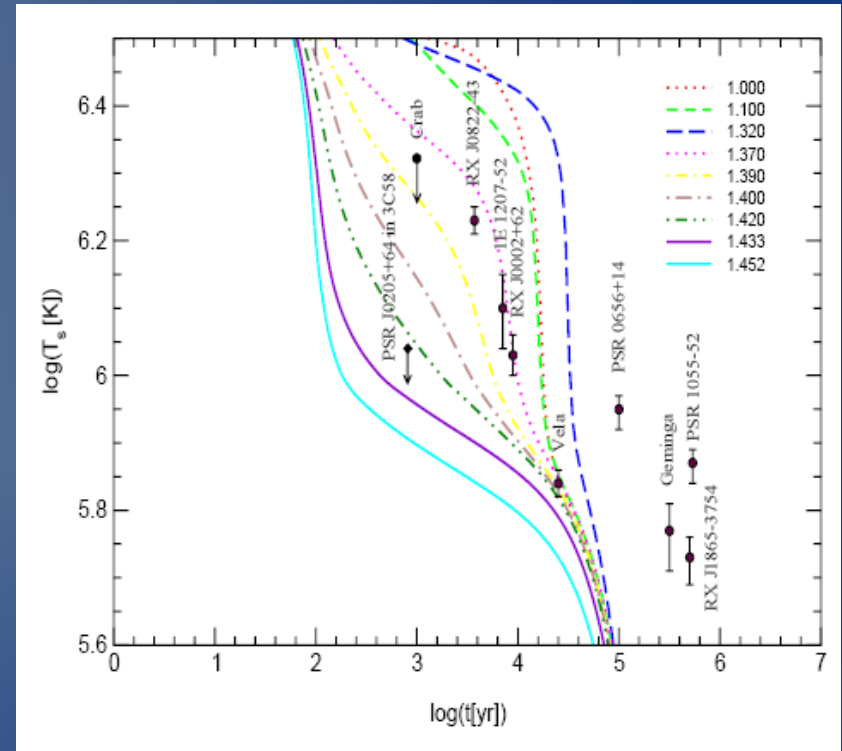
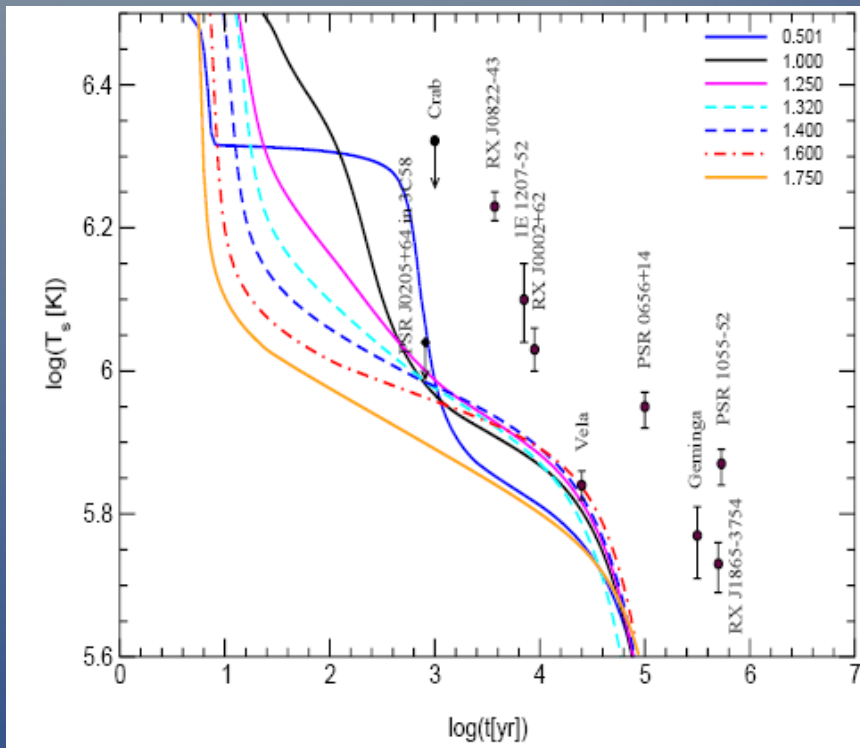
$$\frac{\epsilon_\nu [\text{MMU}]}{\epsilon_\nu [\text{MU}]} \sim 3 \left( \frac{n}{n_0} \right)^{10/3} \frac{[\Gamma(n)/\Gamma(n_0)]^6}{[\omega^*(n)/m_\pi]^8}$$



# Anomalies because of PBF process

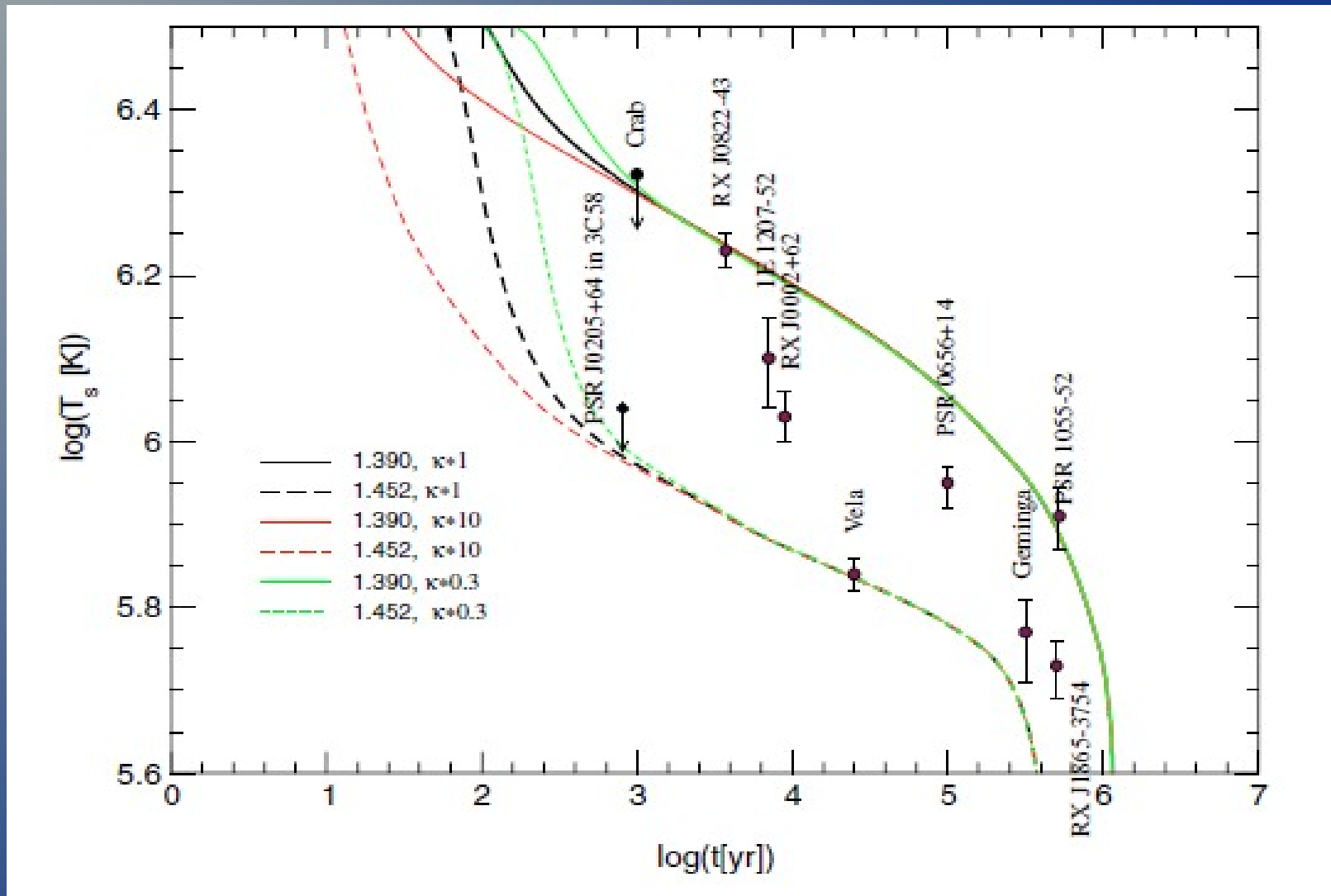
AV18 gaps, pion condensate, without suppression of 3P2 neutron pairing - Enhanced PBF process

Gaps taken from Yakovlev et al. (2003)

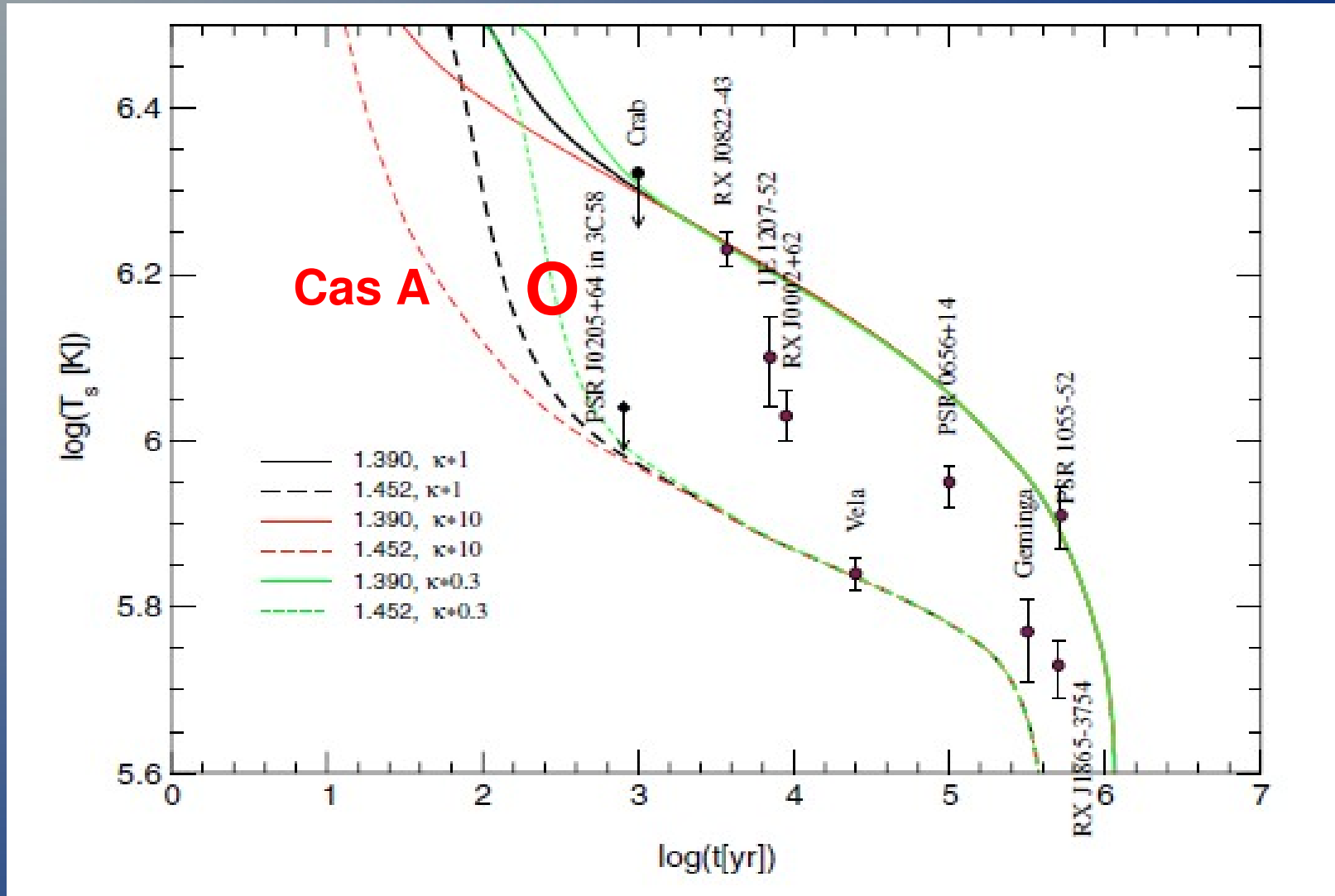


n 3P2 gap **strongly suppressed:** Friman&Schwenk, PRL (2004)

# The influence of the (core) heat conductivity

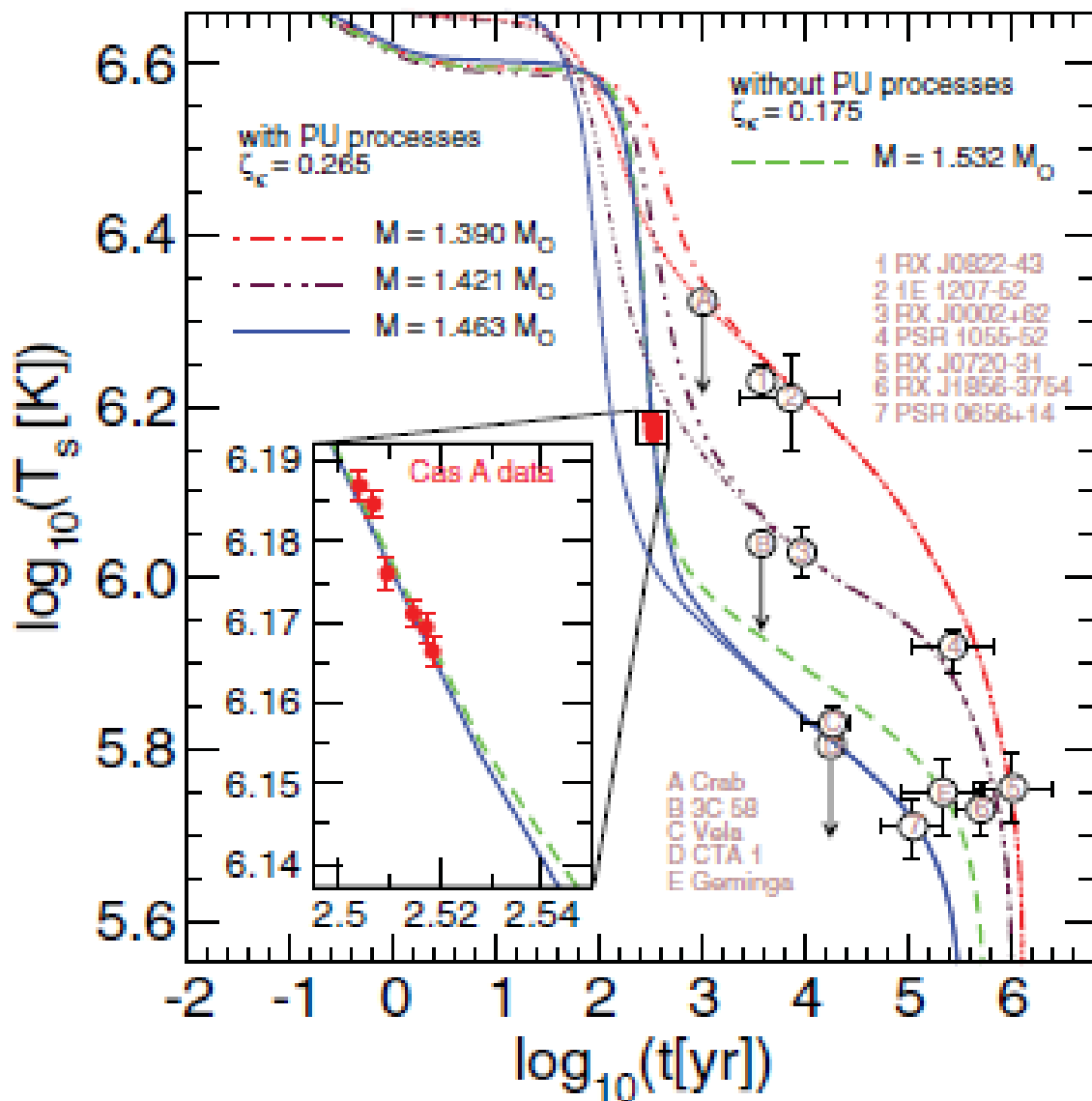


# The influence of the (core) heat conductivity





# Cas A as a Hadronic Star



## Soft hadronic EoS (APR)

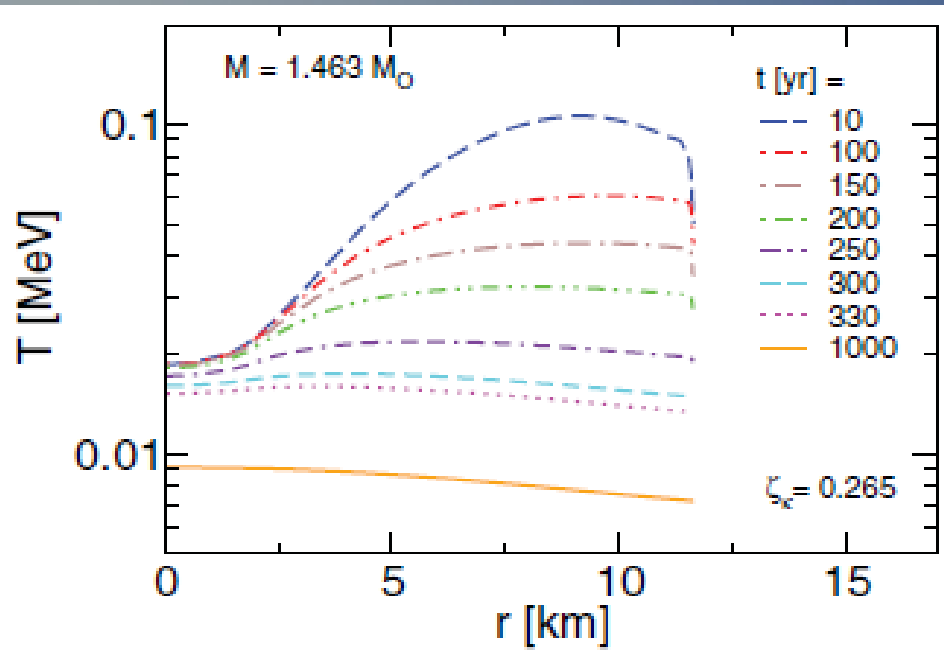
D.B., H. Grigorian,  
D.N. Voskresensky, F. Weber,  
PRC 85, 022802 (2012)

D.B., H. Grigorian,  
D.N. Voskresensky,  
A&A 424, 979 (2004)

# Cas A as Hadronic Star

## T-profile evolution:

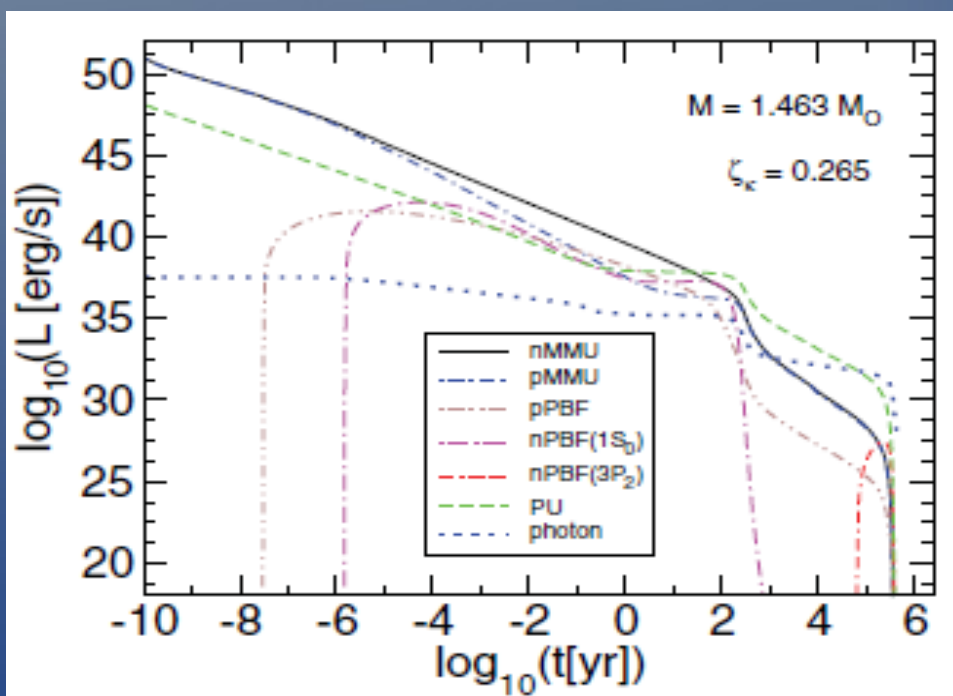
Thermal equilibration after  
~ 300 yrs



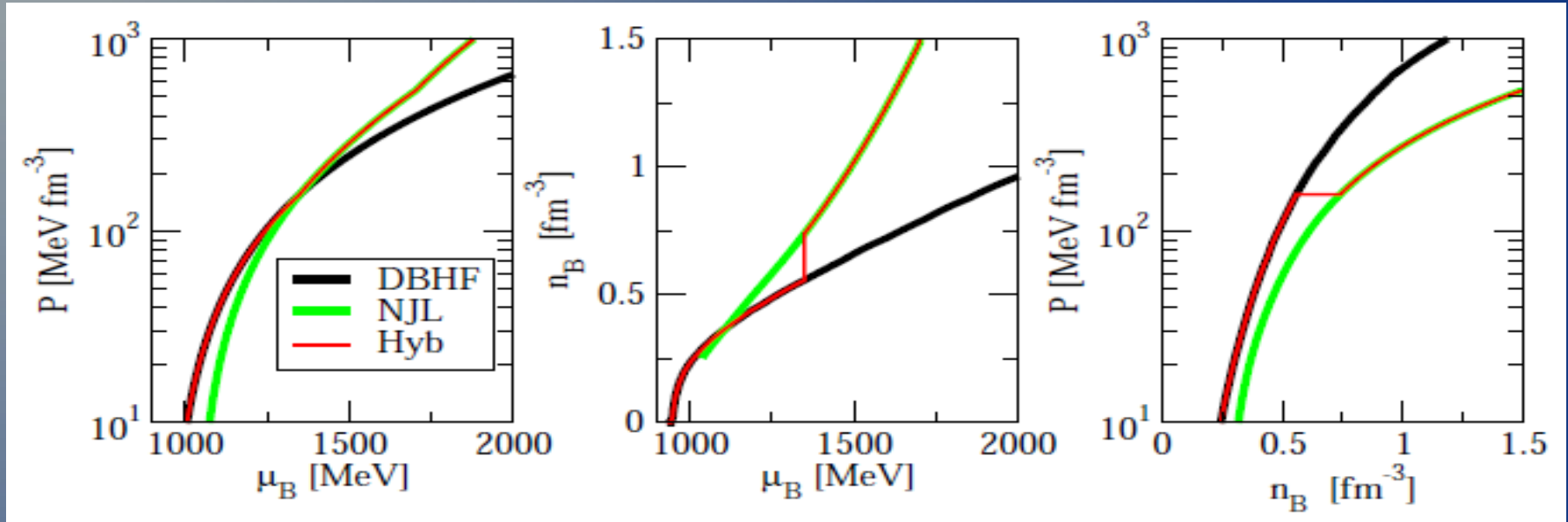
## Individual contributions to total luminosity:

MMU: medium modified mod. Urca  
PBF: pair breaking and formation  
PU: pion condensate Urca

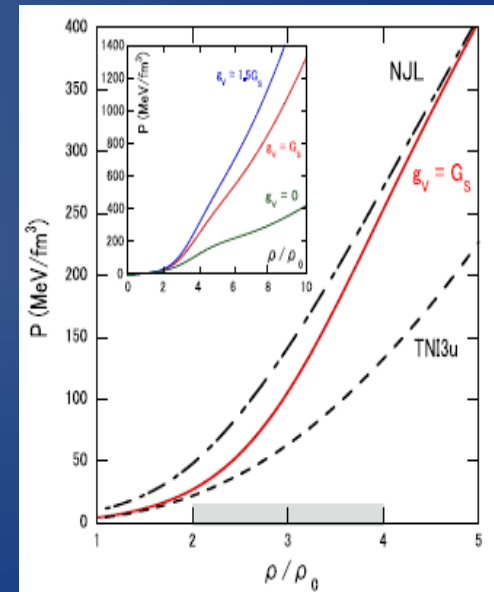
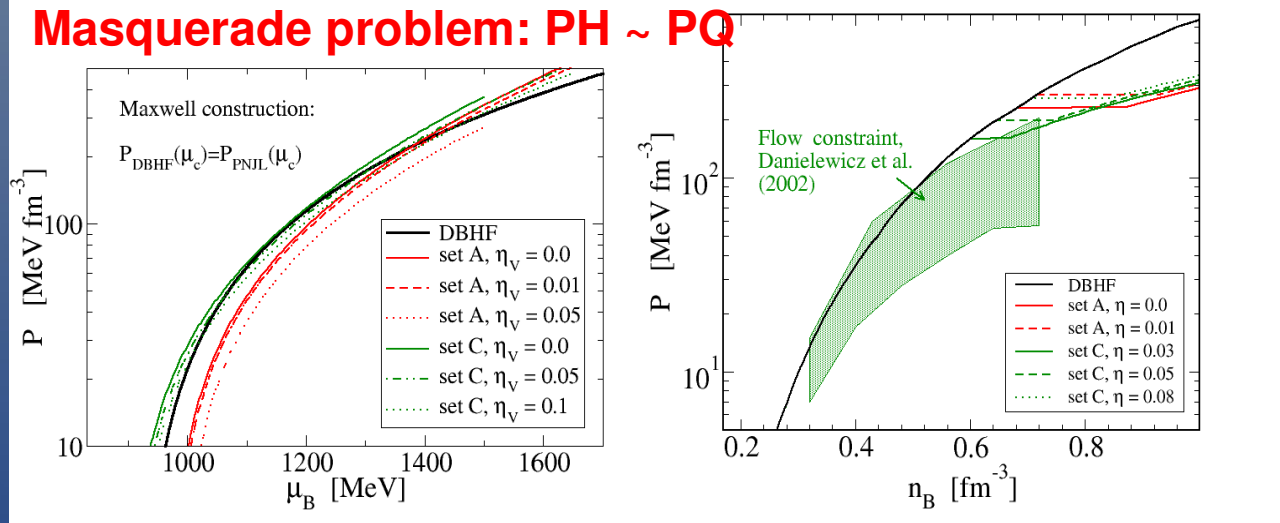
$\zeta_{\kappa}$  :  
suppresses thermal conductivity



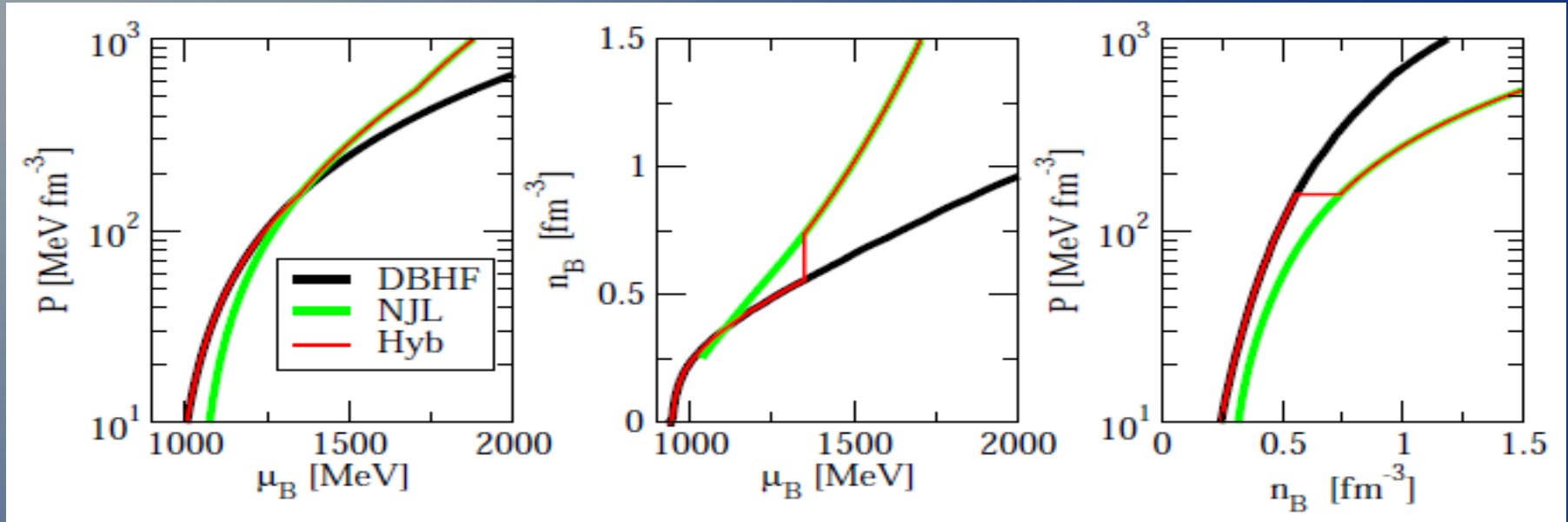
# Phase transition: Maxwell construction



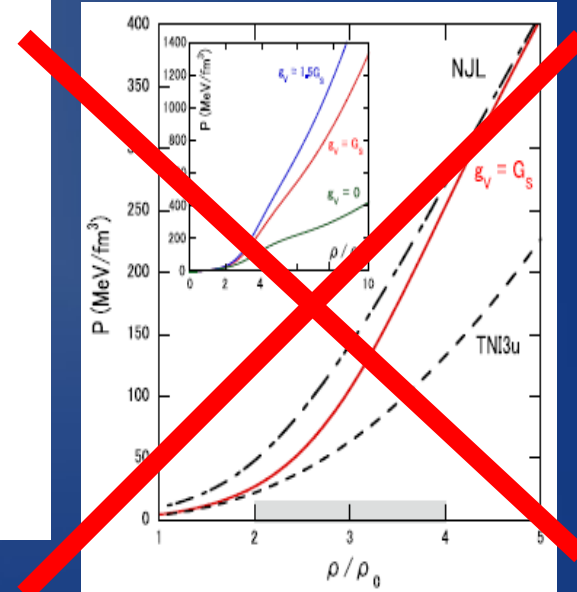
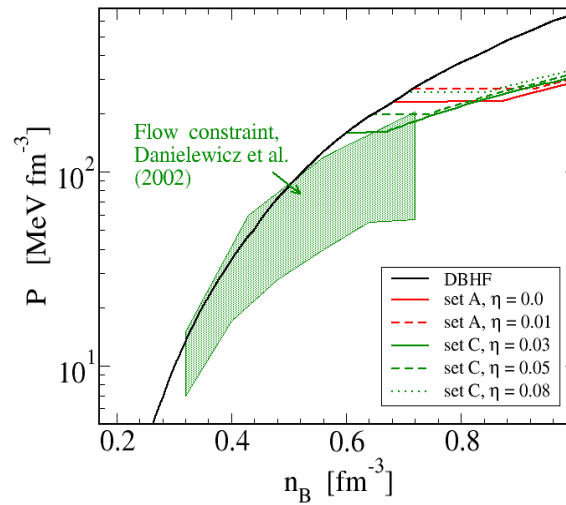
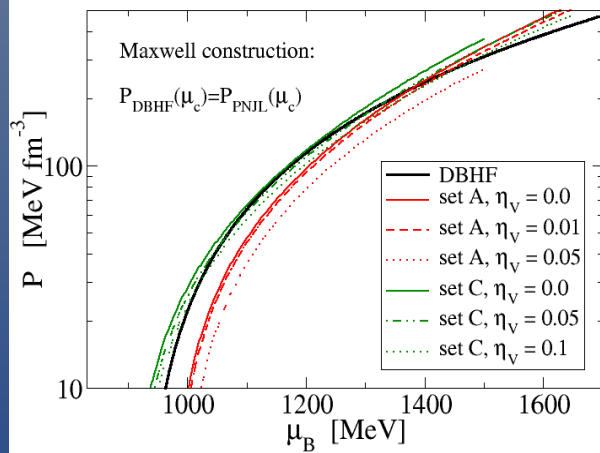
## Masquerade problem: PH $\sim$ PQ



# Phase transition: Maxwell construction

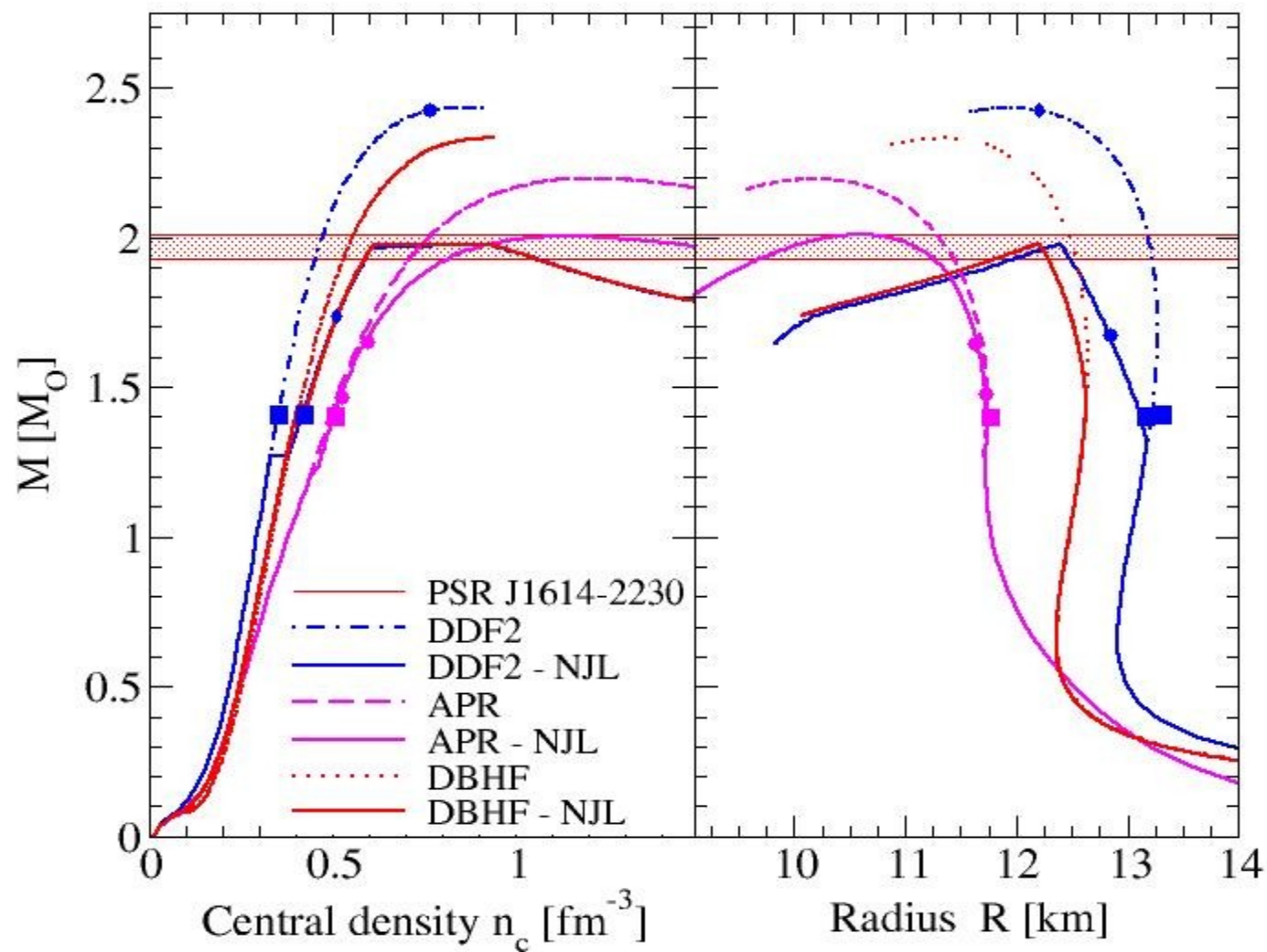


**Always softens the EoS !**

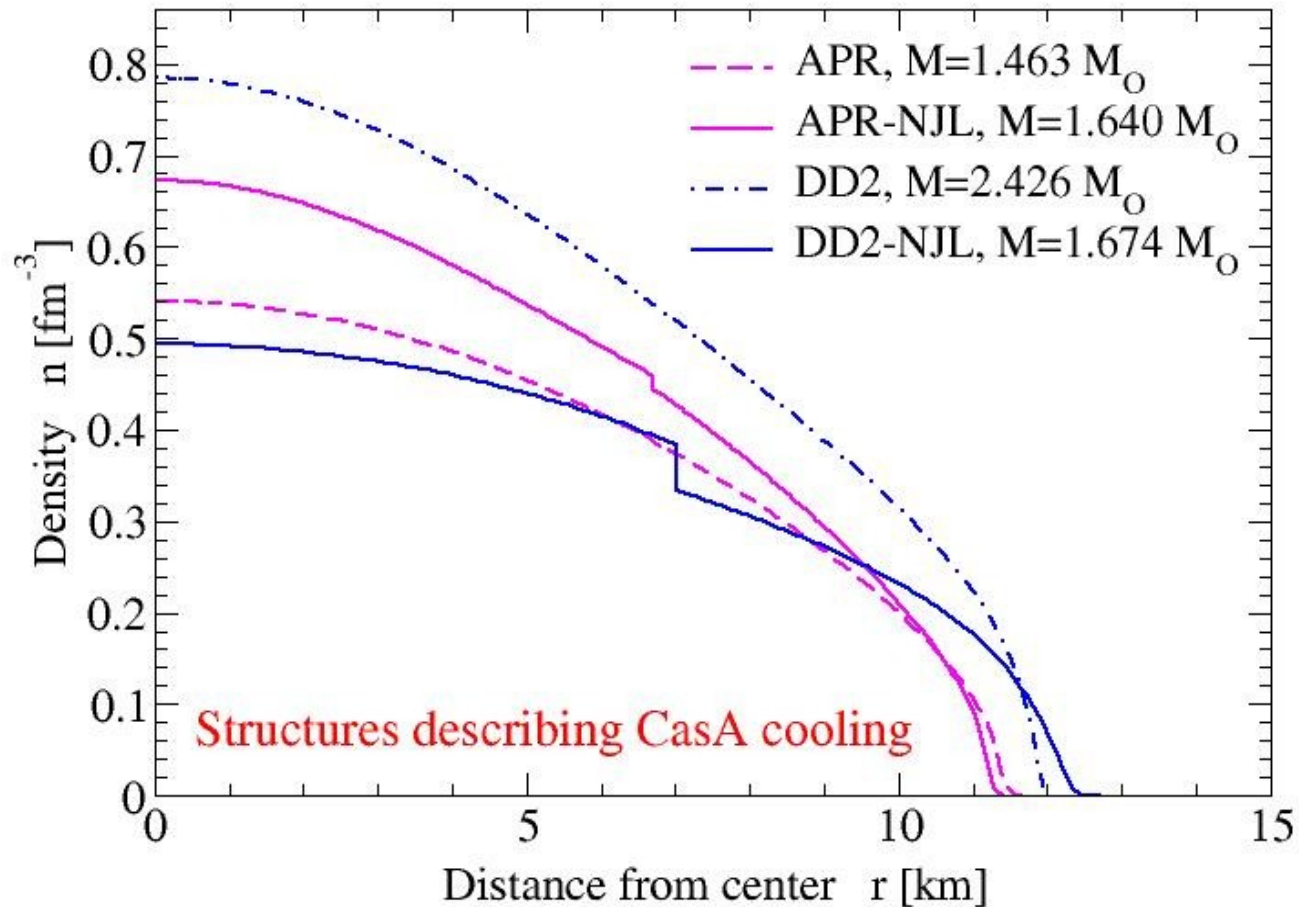




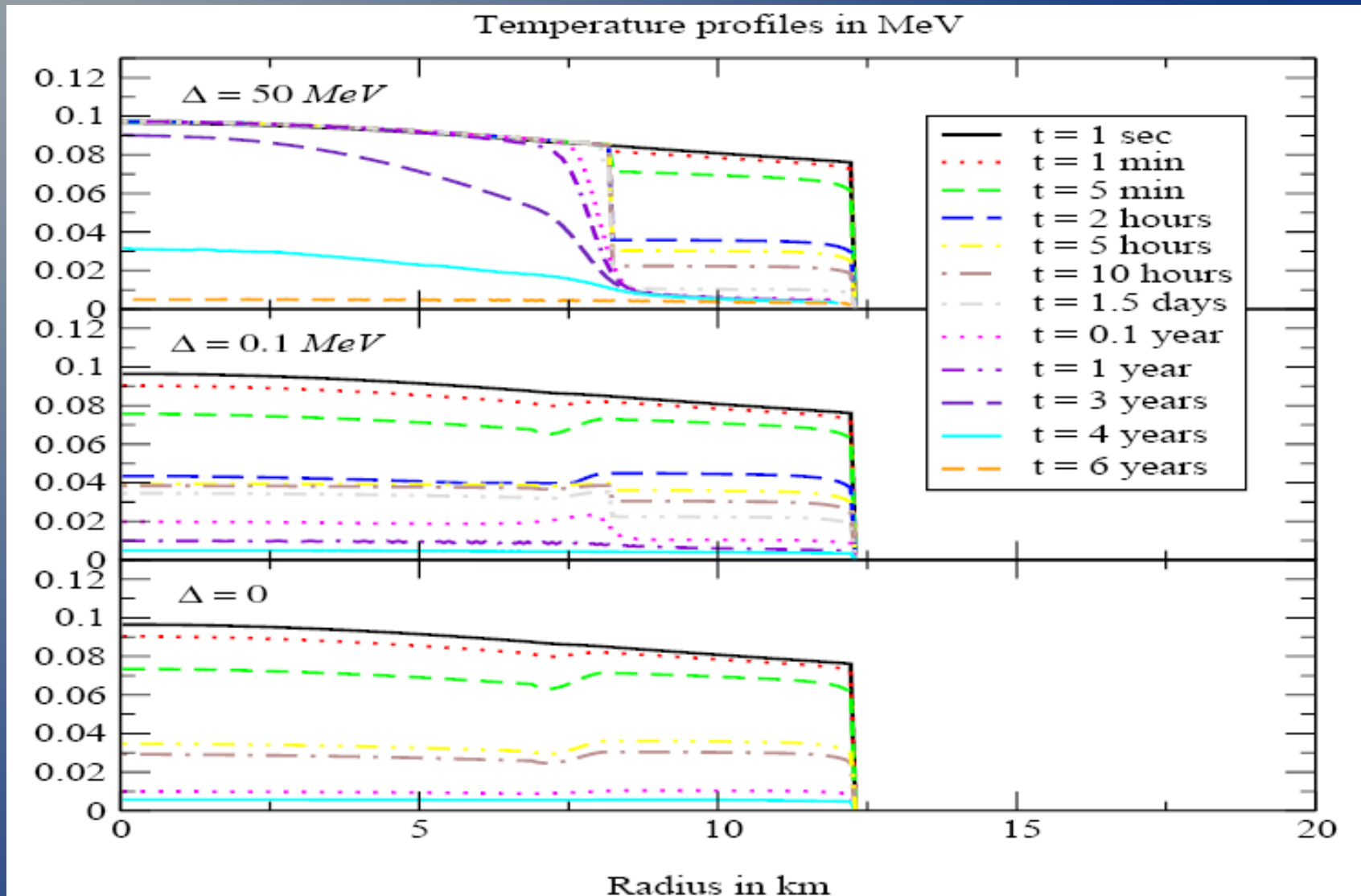
# Hybrid star configuration sequences



# Hybrid Star Structure & Cas A



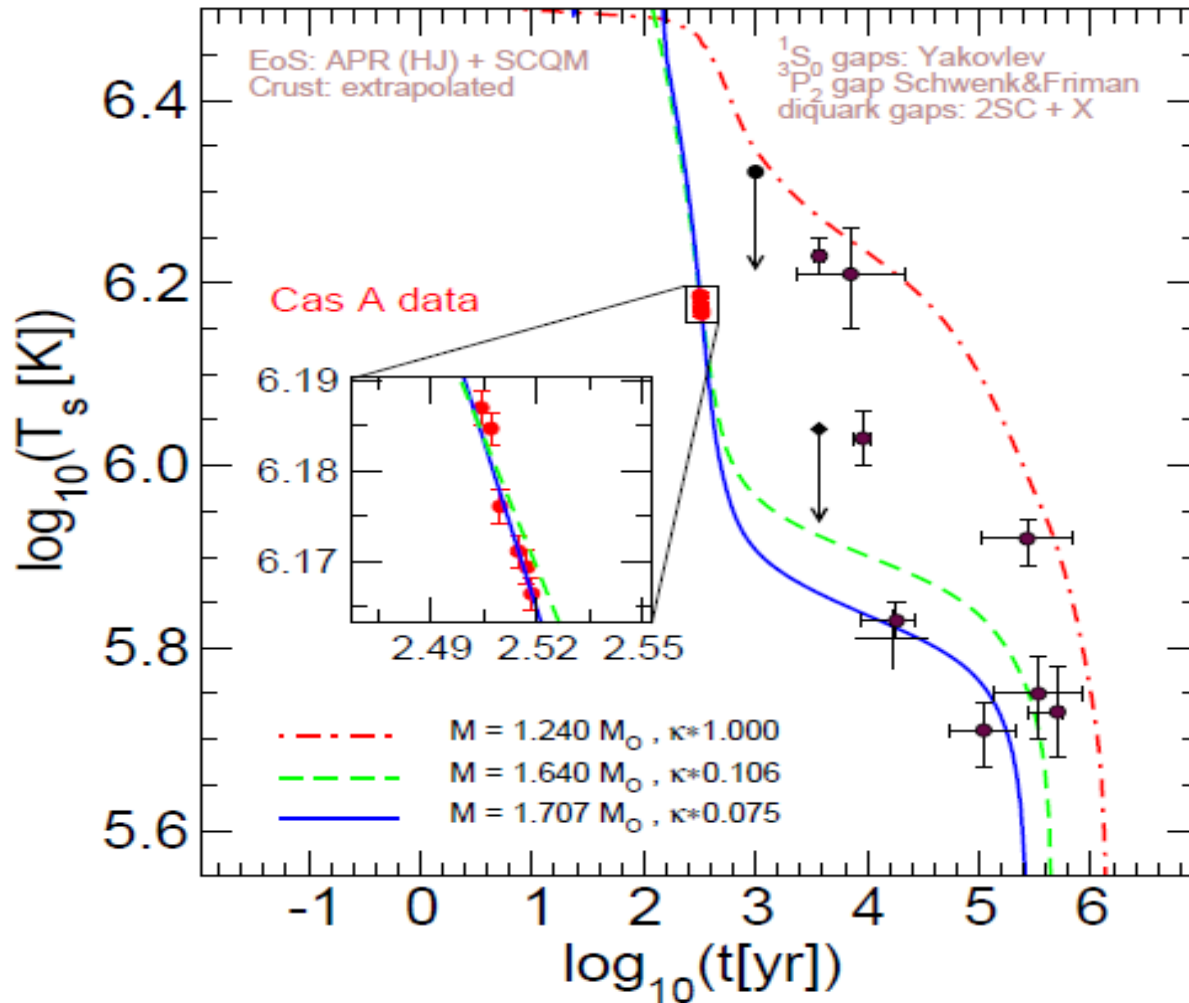
# Temperature in the Hybrid Star Interior



- Blaschke, Grigorian, Voskresensky, A& A 368 (2001) 561

# Cas A as a Hybrid Star

H. Grigorian, D. Blaschke, D.N. Voskresensky, Phys. Rev. C 71, 045801 (2005)



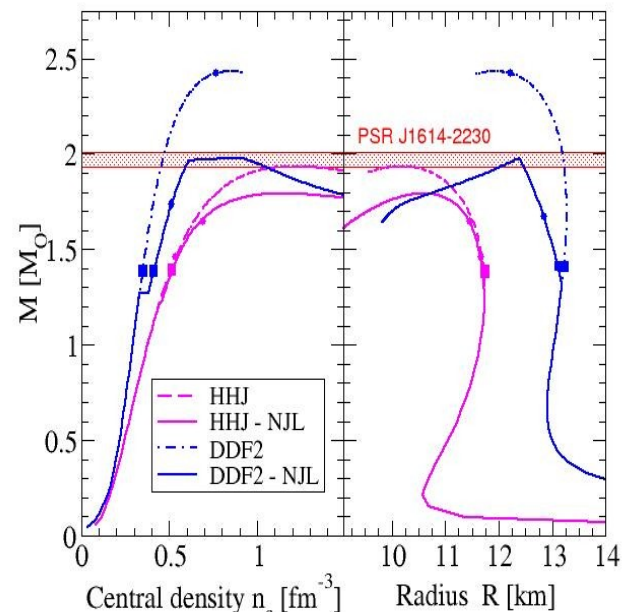
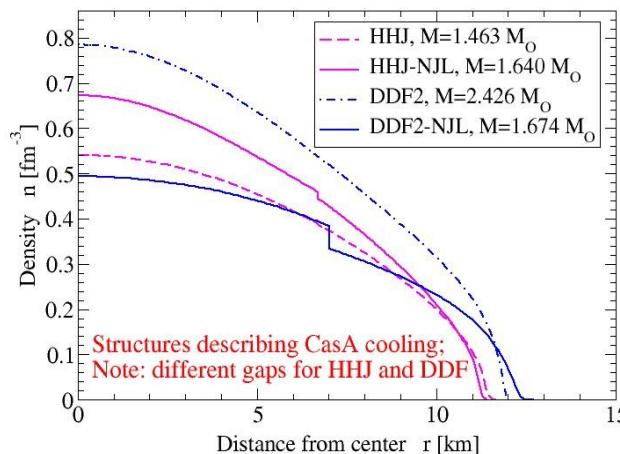
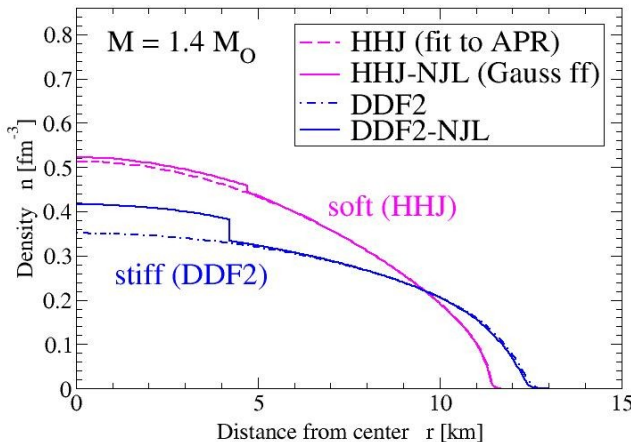
Soft hadronic  
EoS (APR)



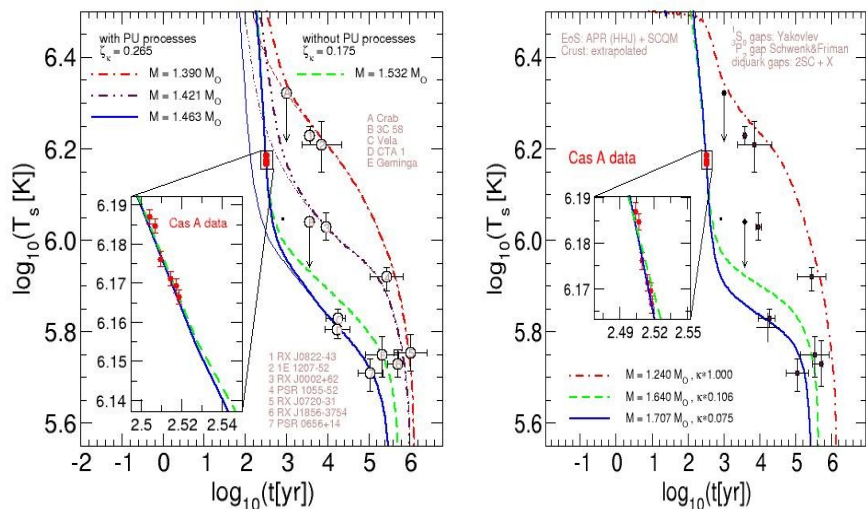
# What PSR J1614-2230 (Demorest) & Cas A imply for compact star structure & cooling

D. Blaschke @ Confinement X

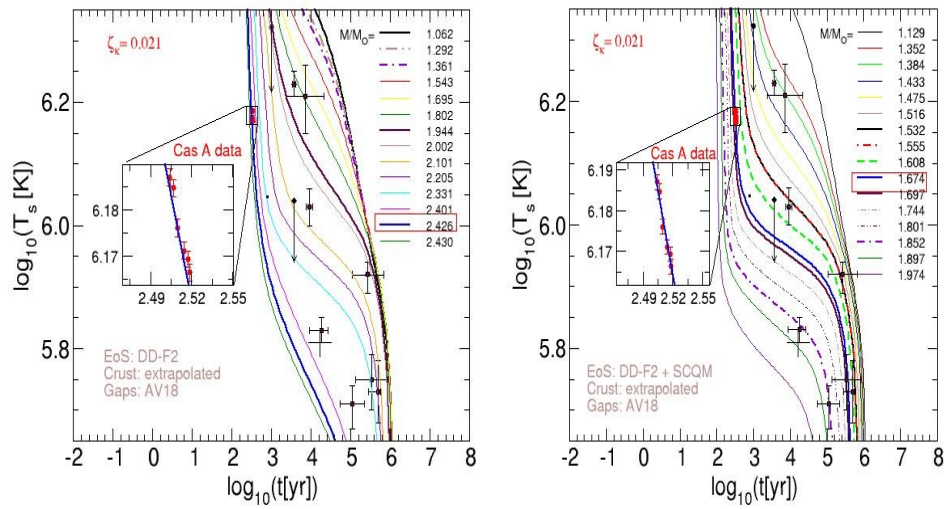
Stiff nuclear EoS (DDF2) → low central density → slow cooling



HHJ and HHJ-NJL EoS too soft for Demorest, but CasA cooling OK [DB et al., PRC (2012)]  
 $M_{\text{CasA}} = 1.463 M_{\odot}$     $M_{\text{CasA}} = 1.640 M_{\odot}$



DDF2 and DDF2-NJL support 2 MO  
 Hadronic cooling too slow, but hybrid OK  
 $M_{\text{CasA}} = 2.426 M_{\odot}$     $M_{\text{CasA}} = 1.674 M_{\odot}$



# Conclusions

- Cas A rapid cooling is consistently described by the nuclear medium cooling (NMC) model as a “first drop” delayed by low thermal conductivity
- Both alternatives for the inner structure, hadronic and hybrid star, are viable for Cas A if hadronic matter is just stiff enough (e.g., APR); for a too stiff hadronic EoS (e.g., DD2) the hadronic scenario requires a modification of pairing gaps while the hybrid model is OK
- In contrast to the minimal cooling scenario, the NMC model is sensitive to the star mass and the thermal conductivity of the superfluid star core
- Discriminating test?  $\log N - \log S$  !! (?)

- **Research ...**



- **... is gong on!**

- **Thanks for Your attention!**





Zadar, Croatia, September 2012

**It's cool to be a CompStar member!**