

Atomic Clocks and Frequency Metrology



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Outline

- Atomic clocks
 - μW clocks (fountains)
 - Optical clocks
- Applications of clocks
 - Atomic physics, fundamental physics,...
 - SI second, international atomic time (TAI)
 - Frequency and time transfer methods
- Metrology in curved space-time
 - General relativity, gravitational redshift
 - Impact on clock comparisons: present and future
- Other examples
 - Ion clocks
 - Lattice clocks
 - Ultra-stable lasers

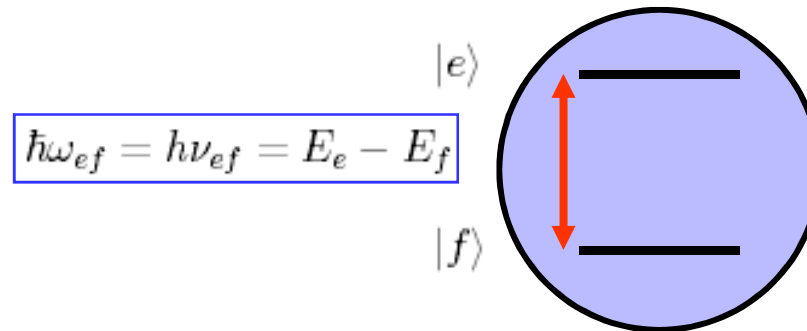


Atomic clocks

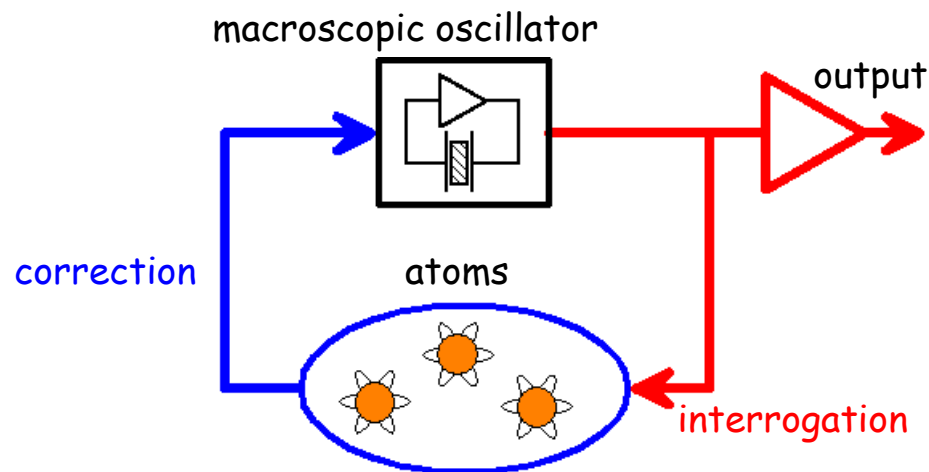
Principle of atomic clocks

Goal: deliver a signal with stable and universal frequency

Bohr frequencies of unperturbed atoms are expected to be stable and universal



Building blocks of an atomic clock



$$\omega(t) = \omega_{ef} \times (1 + \varepsilon + y(t))$$

ε : fractional frequency offset

Accuracy: overall uncertainty on ε

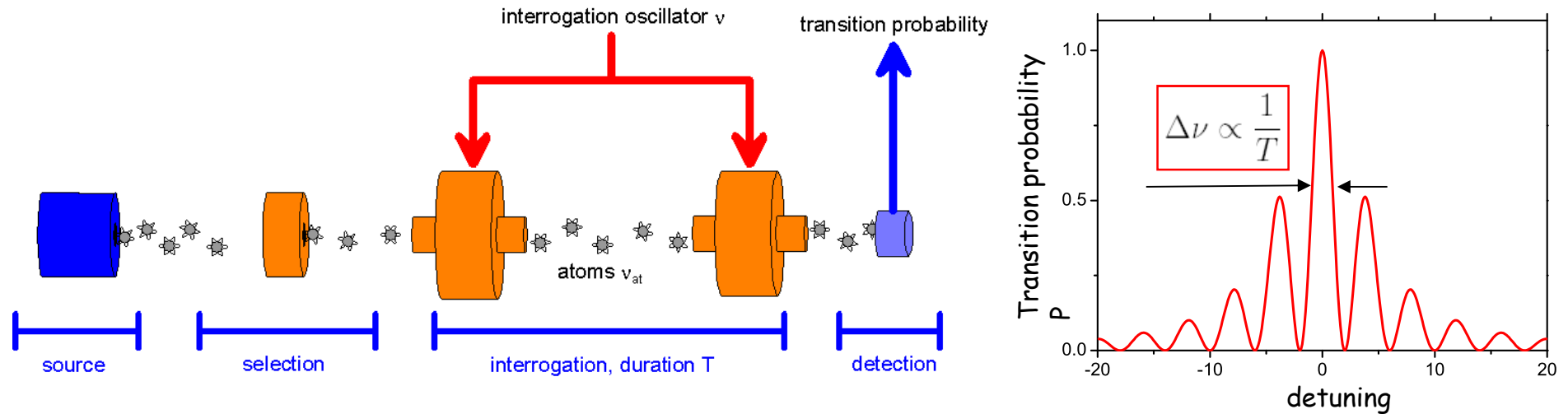
$y(t)$: fractional frequency fluctuations

Stability: statistical properties of $y(t)$, characterized by the Allan variance $\sigma_y^2(\tau)$

Can be done with microwave or optical frequencies, with neutral atoms, ions or molecules

Principle of atomic clocks (2)

How to probe the atomic transition:



The two main parameters:

the atomic quality factor

$$Q_{at} = \frac{\nu_{ef}}{\Delta\nu} \propto \nu_{ef} T$$

fluctuations of the measured transition probability for integration time T_c :

$$\sigma_{\delta P}$$

Scaling of the fractional frequency instability:

$$\sigma_y(\tau) \propto \frac{\sigma_{\delta P}}{Q_{at}} \sqrt{\frac{T_c}{\tau}}$$

Example: optimized Ramsey interrogation
$$\sigma_y(\tau) = \frac{2}{\pi} \frac{\sigma_{\delta P}}{Q_{at}} \times \sqrt{\frac{T_c}{\tau}}$$

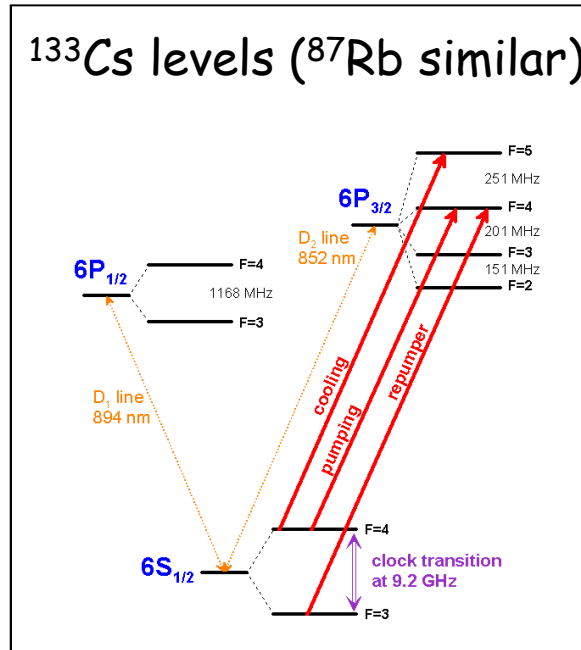
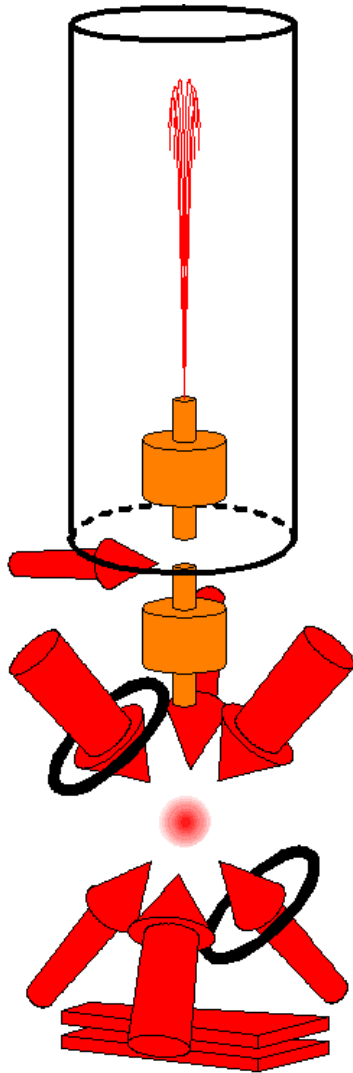
Atomic fountain clocks

J. Guéna et al., IEEE TUFFC 59, 391 (2012)

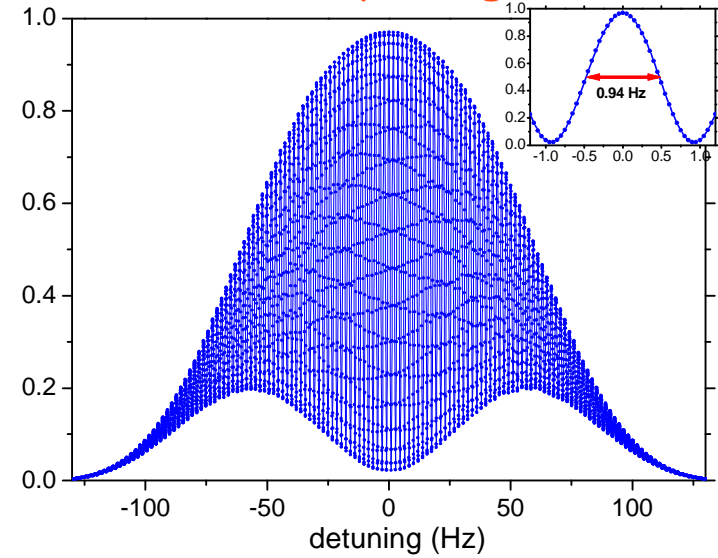
interrogation

capture selection

detection



Ramsey fringes

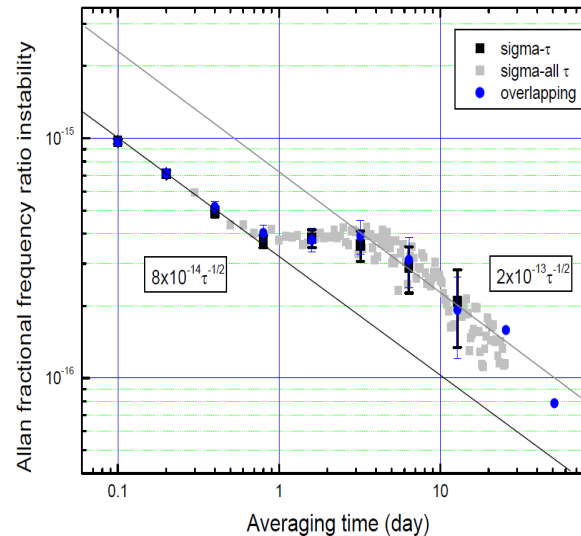


Atomic quality factor:

$$Q_{at} = \nu_{ef} / \Delta\nu \simeq 9.8 \times 10^9$$

Best frequency stability
(Quantum Projection Noise limited): 1.6×10^{-14} @1s

Best accuracy: $(2-3) \times 10^{-16}$



Motivations for developing optical clocks

Quantum limited stability :

$$\sigma_y(\tau) = \frac{1}{\pi Q_{at}} \times \frac{1}{\sqrt{N_{det}}} \times \sqrt{\frac{T_c}{\tau}}$$

$$Q_{at} = \frac{\nu_{ef}}{\Delta\nu} \propto \nu_{ef} T$$

Microwave transition : $\nu_{ef} \sim 10$ GHz, optical transition : $\nu_{ef} = c/\lambda \sim 10^{14}$ Hz

Example #1: cycle $T_c \sim 1$ s, linewidth ~ 1 Hz et $\sigma_{\delta p} \sim 10^{-4}$:

Microwave : $\sigma_y = 10^{-14}$ @1s

Optical : $\sigma_y = 10^{-18}$ @1s

In practice, best reported stabilities

$\sigma_y = 5 \times 10^{-16}$ @1s

Example #2: cycle $T_c \sim 1$ s, linewidth ~ 1 Hz et $N_{det} \sim 1$ (1 atom !):

Optical : $\sigma_y = 3 \times 10^{-15}$ @1s

- Better stability implies better resolution to evaluate systematic shifts
- Many systematic shifts are much smaller as compared to microwave clocks

→ 10^{-17} or better is within reach provided a solution is found for the effects of external motion

$$\delta\omega_{Doppler} = \vec{k} \cdot \vec{v} \sim \omega \times \frac{v}{c}$$

$$\frac{\delta\omega_{Doppler}}{\omega} \sim \frac{v}{c}$$

1 mm/s (~ 1 recoil) corresponds to a 3×10^{-12} fractional shift !

Motional effects on confined atoms: Lamb-Dicke regime

- Consider an atom spatially confined to much less than the wavelength of the incoming photon

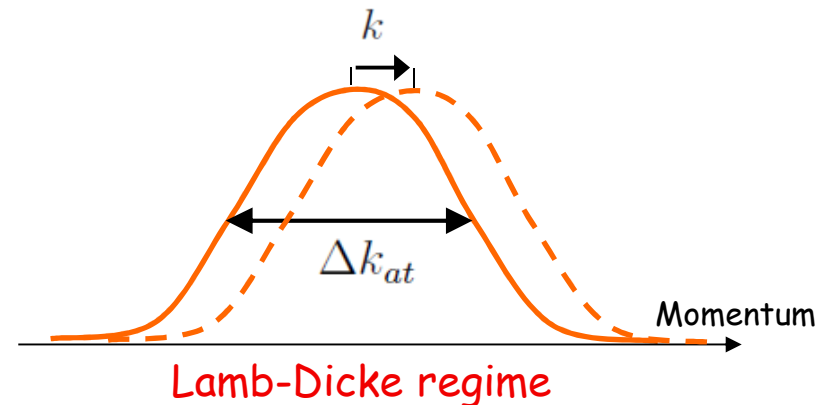
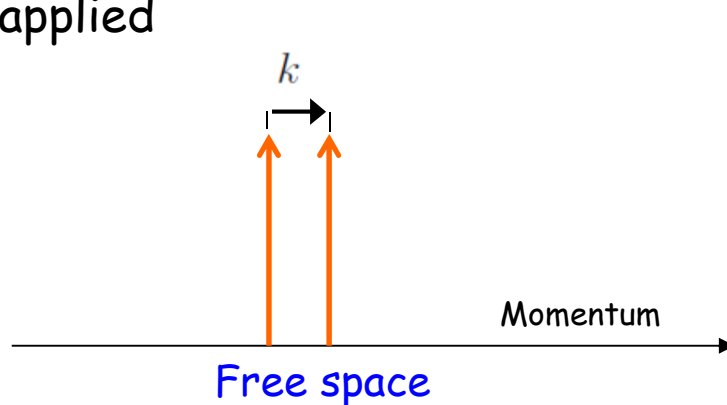
$$\Delta x_{at} \ll \frac{\lambda}{4\pi}$$

- In momentum space, the atomic wave-function is such that:

$$\Delta p_{at} \cdot \Delta x_{at} > \hbar/2 \quad \text{or} \quad \Delta k_{at} \cdot \Delta x_{at} > 1/2$$

- This implies that: $\Delta k_{at} > \frac{1}{2\Delta x_{at}} \gg \frac{2\pi}{\lambda} = k$ or $\Delta k_{at} \gg k$

- the size of the wave-function in momentum space is large compared to the photon momentum
- The shift in momentum space implied by momentum conservation induces a minor modification of the wave-packet
- Small shift of the resonant frequency when the energy conservation is applied

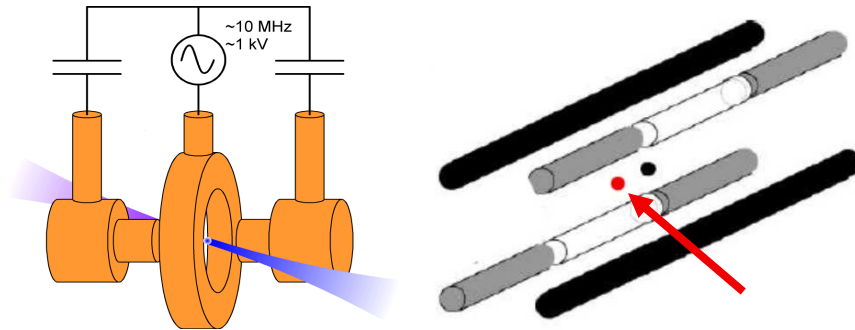


Optical clocks

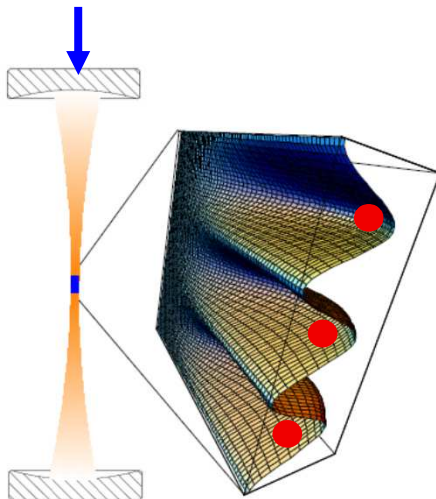
- The clock transition is in the optical domain allowing improved accuracy
- Confinement into the Lamb-Dicke regime is used to dramatically reduce the effects of external motion
 - Mandatory to gain over μ Wave clocks:

$$\delta\omega_{Doppler} = \vec{k} \cdot \vec{v} \sim \omega \times \frac{v}{c} \Rightarrow \frac{\delta\omega_{Doppler}}{\omega} \sim \frac{v}{c}$$

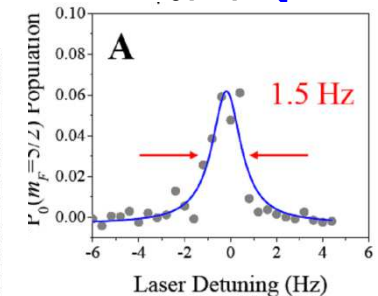
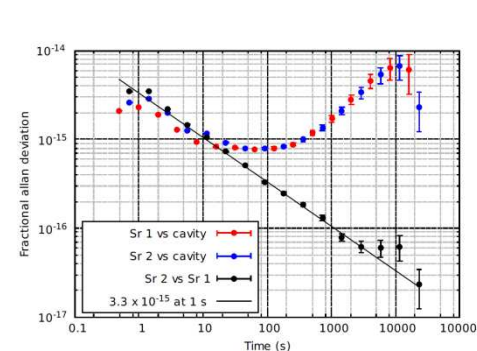
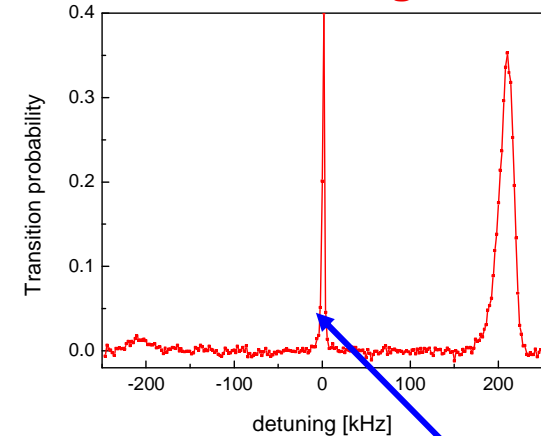
Trapped ion clocks



Lattice clocks



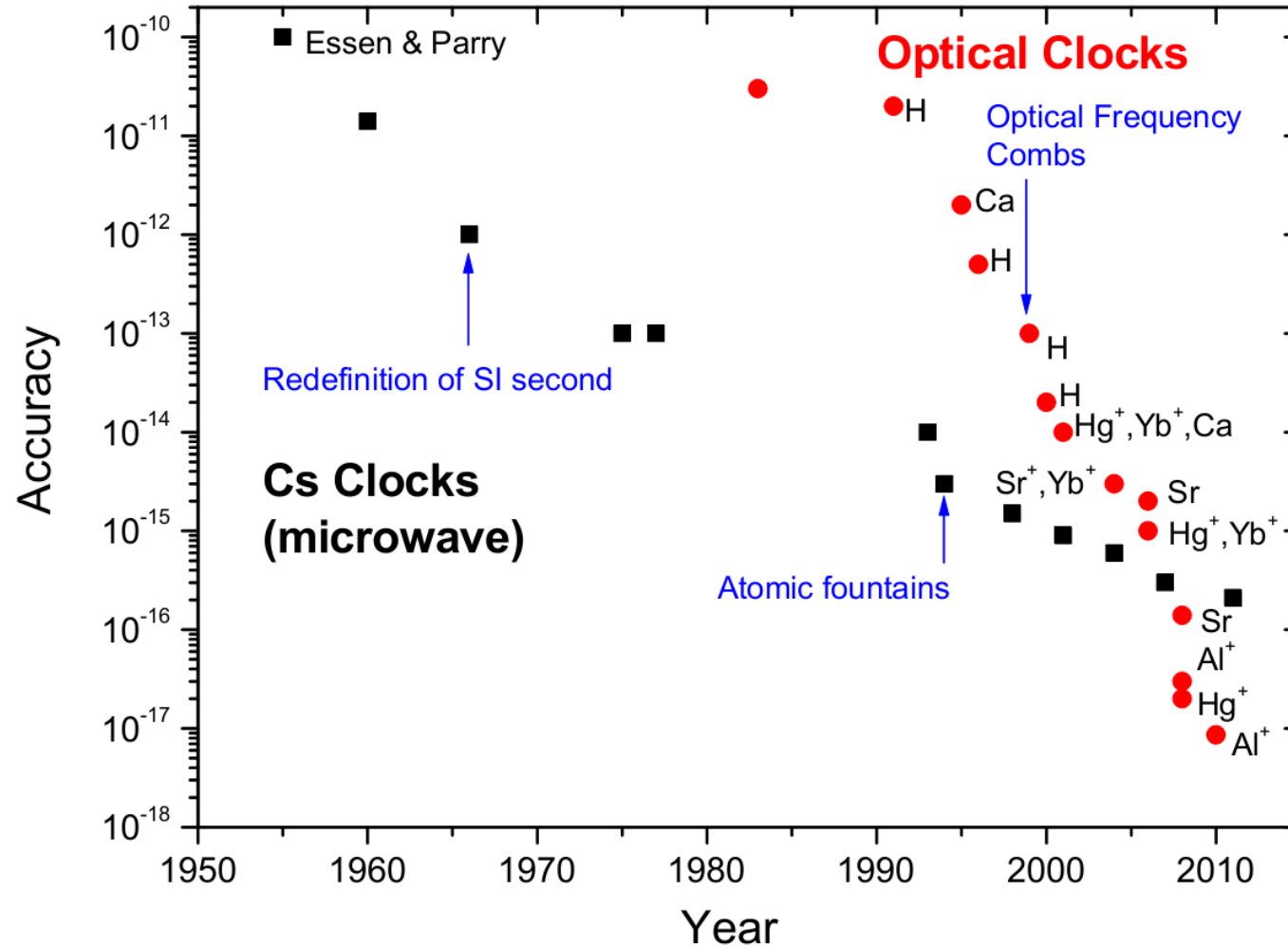
Spectroscopy in the Lamb-Dicke regime



Research in optical clocks

- Best performance to date:
 - Accuracy: Al^+ , 8.6×10^{-18} (NIST)
 - Stability: Yb & Sr, $(4-5) \times 10^{-16}$ @1s (PTB, NIST, JILA)
- Many aspects to this active research field
 - Physics of the clock
 - Use of quantum gates, quantum non-demolition measurements, spin-squeezing
 - Ultra-stable lasers
 - Optical frequency combs
 - Toward transportability and optical space clocks
- Many systems investigated
 - Hg^+ , Al^+ , Sr^+ , Ca^+ , Yb^+ (quad., octup.), In^+
 - Sr, Yb, Mg, Hg. Bosons and fermions
 - Nuclear transition in ^{229}Th

Improvement of clock accuracy with time



- Optical clocks are clearly surpassing microwave clocks in terms of accuracy and stability
- Optical clock development is an active, innovative and competitive field

LNE-SYRTE ATOMIC CLOCK ENSEMBLE



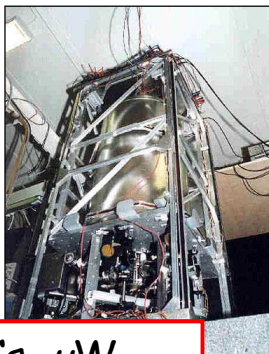
Systèmes de Référence Temps-Espace

H-maser

H, μW



FO1 fountain



Cs, μW

Cryogenic sapphire Osc.

Macroscopic oscillator



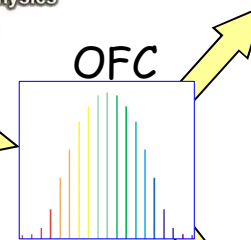
department of physics

Phaselock loop
 $\tau \sim 1000$ s

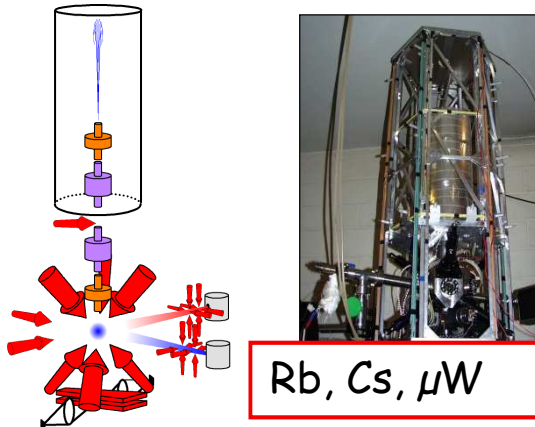
Optical lattice clock



Hg, opt



FO2 fountain



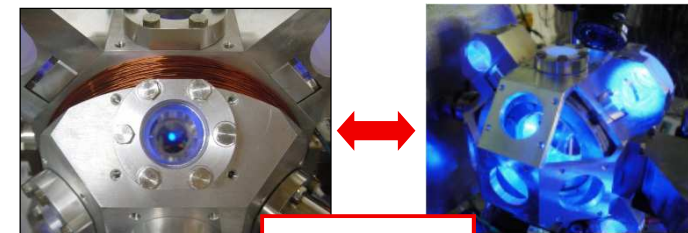
Rb, Cs, μW

FOM transportable fountain



Cs, μW

Optical lattice clock



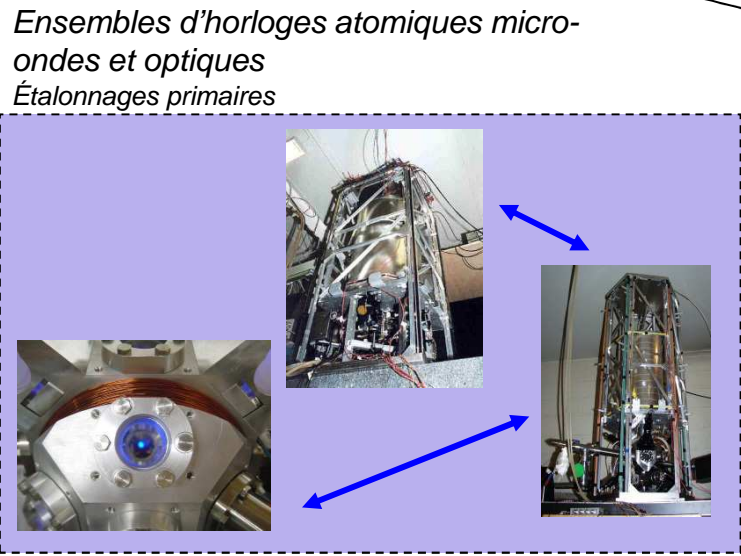
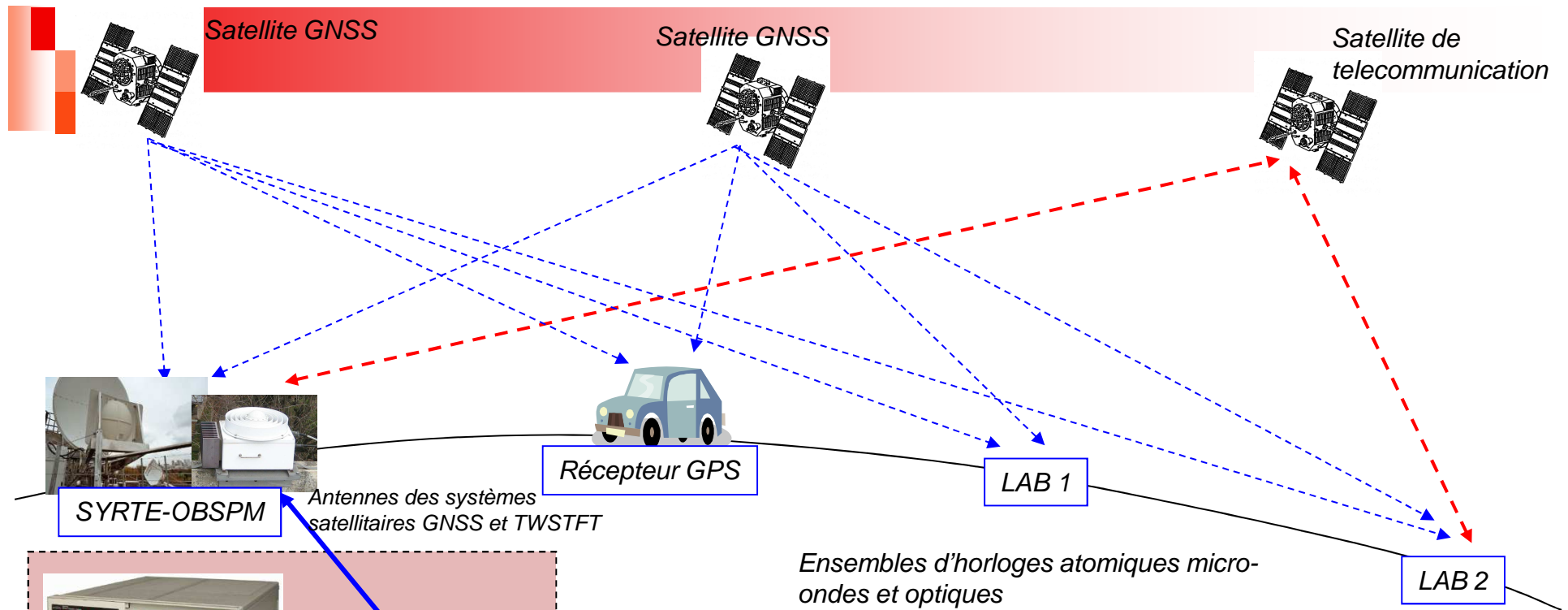
Sr, opt



Applications of clocks

Applications of clock ensembles

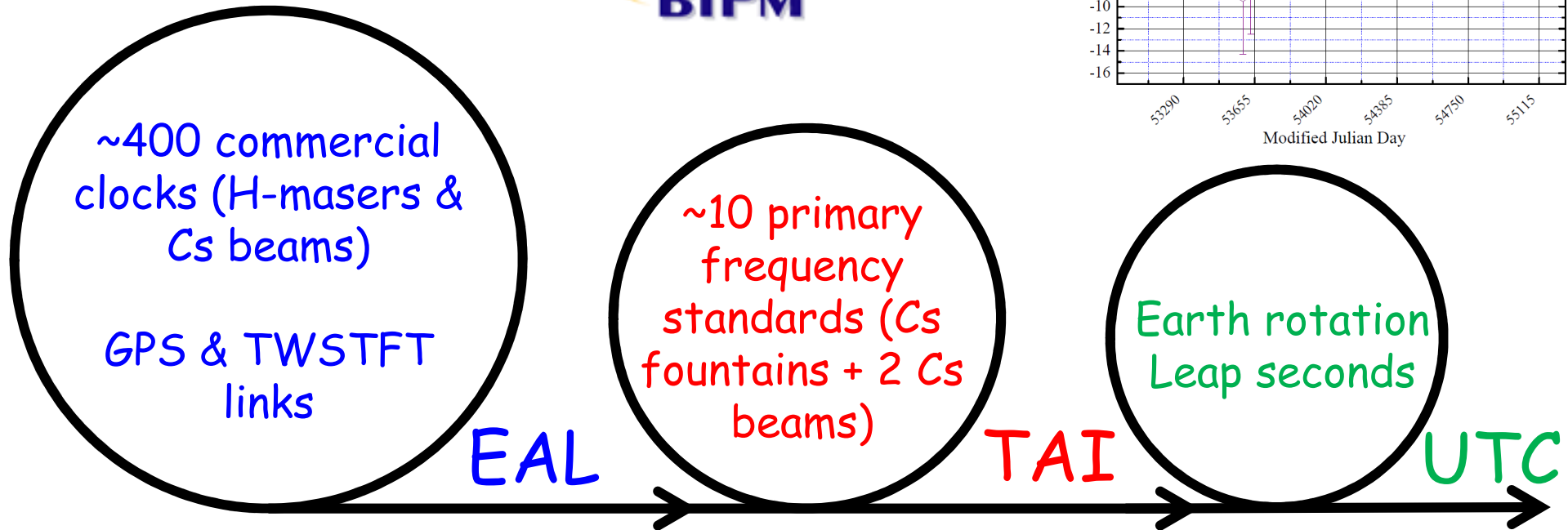
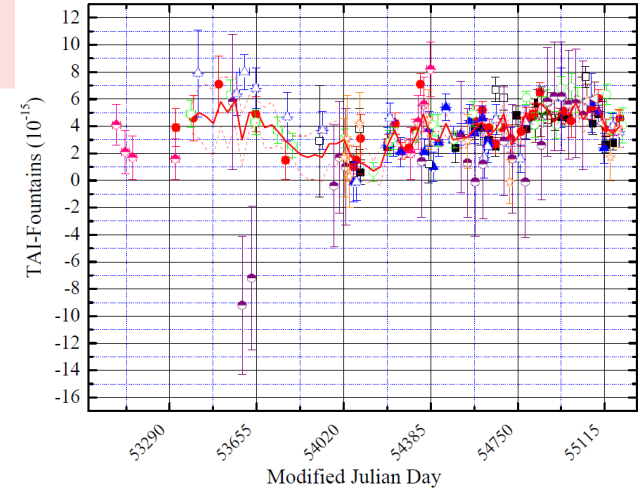
- Atomic and quantum physics
 - Collisions, Feshbach resonances, collisions in relation with fermion/boson statistics in confined atoms
 - Distributed cavity phase shift, microwave lensing
 - High precision atomic properties: polarizabilities, hyperpolarizabilities, vector and tensor light shifts
- Time and frequency metrology
 - Realization of the SI second, of international atomic time (TAI)
 - High accuracy absolute frequency measurements (Rb, Sr, Hg, H, Ca⁺,...), secondary representations, toward a new SI second
 - Determination of natural constants (R_y , α , m_e/m_p), radius charge of the proton
- Fundamental physics tests
 - Local Lorentz Invariance (photon sector, matter sector, MM, KT)
 - Local Position Invariance, Stability of natural constants, Isotropy of space
- Space clock missions (ACES) and projects (STE-QUEST,...)
 - Support to the development of PHARAO with ACES
 - Ground segment of ACES



Ensemble d'horloges commerciales
Comparaisons et algorithmes d'échelle de temps
Horloge parlante
Diffusion Temps Légal Français

International Atomic Time (TAI)

Timescale elaborated by BIPM



- Stability of TAI (τ in days)
 $\sigma_y(\tau) = 20 \times 10^{-16} \tau^{-1/2}$
 $\sigma_y(\tau) = 4 \times 10^{-16}$
 $\sigma_y(\tau) = 1 \times 10^{-16} \tau^{-1/2},$
- Several PFS reports/month. Accuracy of TAI-SI: mid- 10^{-16}
- UTC-UTC(k): few 10 ns typical. Best, experimental: 1 ns ¹⁶

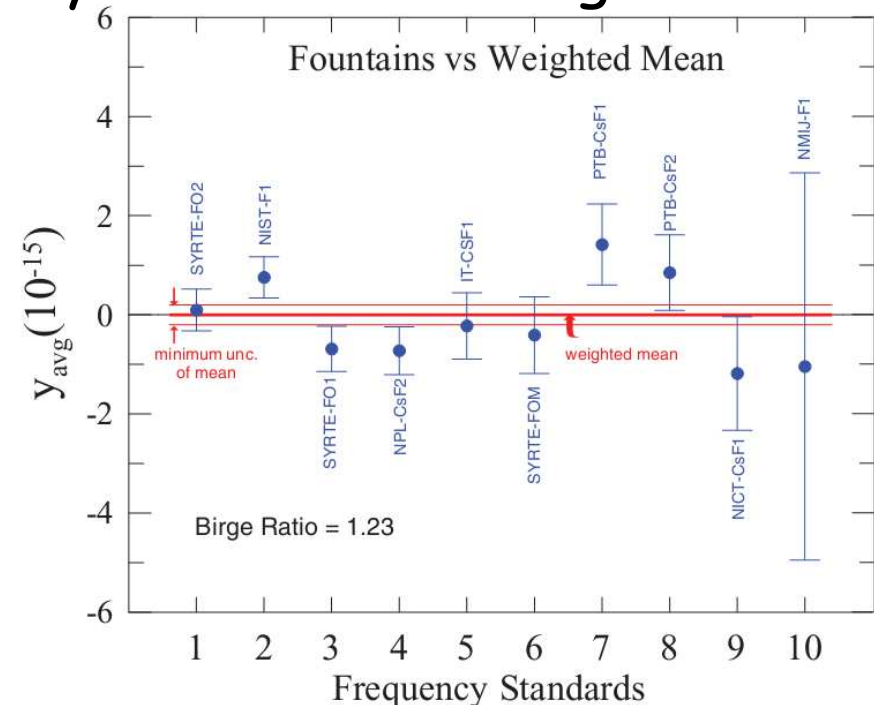
Example of applications

- Metrology: consistency of time and frequency references between NMIs
- Dissemination of accurate frequency and time to laboratories
- Synchronization of VLBI stations
- Study of Earth rotation
- Pulsar timing → astrophysics, tests of GR, evidence of gravitational waves,...
- ...

Frequency comparisons through TAI

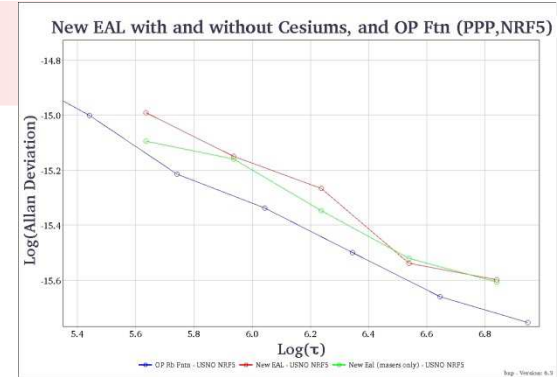
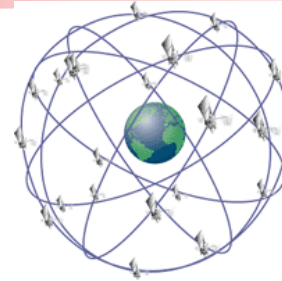
Comparisons of Primary Frequency Standard through TAI

T. Parker, *Rev. Sci. Instrum.* 83 , 021102 (2012)
G. Petit et al., *BIPM*



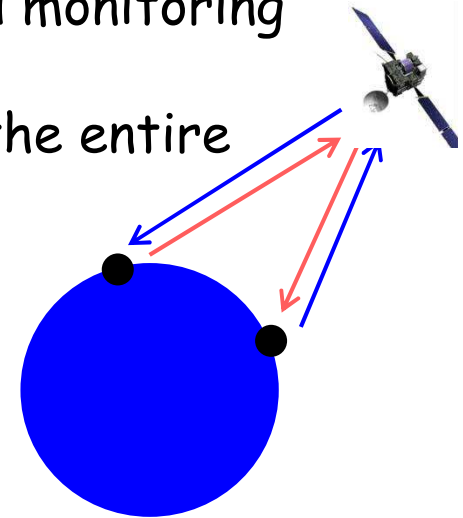
- A high accuracy measurement through TAI
 - >80 formal calibrations of TAI by LNE-SYRTE PFS since Jan. 2009
 - Calibrations by FO2-Rb used as a SFS submitted to BIPM in Jan. 2012 and evaluated by the WG PFS
 - FO2-Rb data now included in *Circular T*, but with no weight in TAI
 - 17 formal reports already, allowing FO2-Rb SFS to be directly linked to TAI to $<3 \times 10^{-16}$ [G. Petit, BIPM]

Long distance T&F transfer via satellite



■ GPS

- Satellites broadcast several carriers modulated with PRN codes
- Satellites orbits and clocks are known from ground monitoring stations and master clocks
- "PPP" method: a global post-processed analysis of the entire constellation is made to make T&F transfer



■ TWSTFT

- Exchange of PRN coded signal through the same geostationary telecommunication satellite

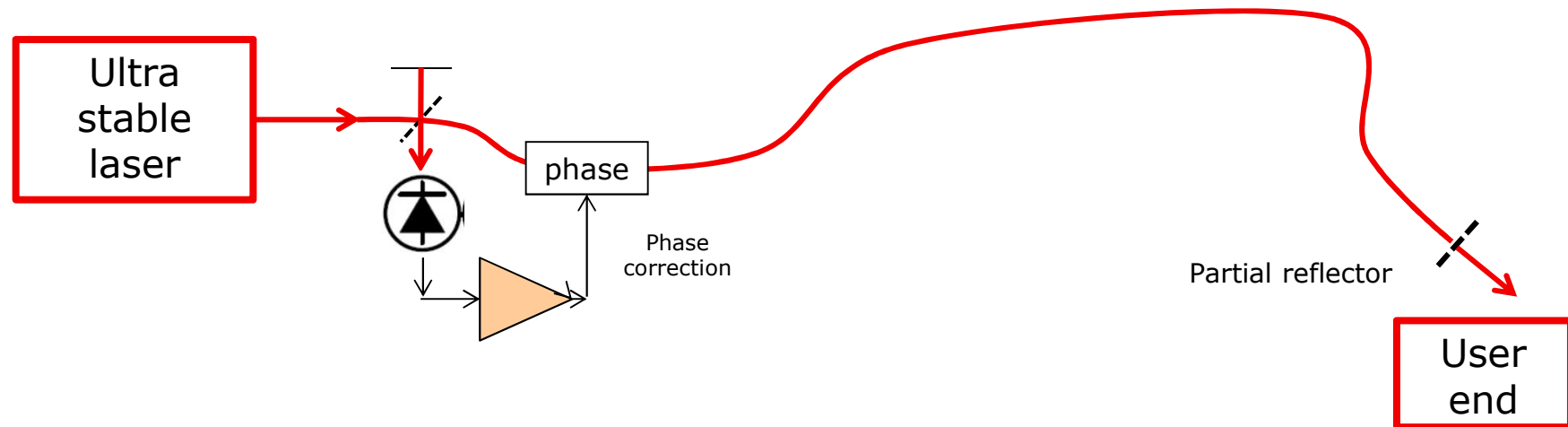
■ Typical performance

- Stability: 10^{-15} @1d. Timing accuracy: 1 ns
- NOT sufficient for present and future optical clocks₁₉

Long distance T&F transfer: advanced methods

■ Coherent optical fiber link

- Enabled by the “easy” manipulation/measurement of optical carrier signals (ultra-stable lasers, optical frequency combs)
- Largely passes GPS PPP and TWSTFT
- Adapted to the generation of optical clocks
- Principle: heterodyne Michelson-like interferometer

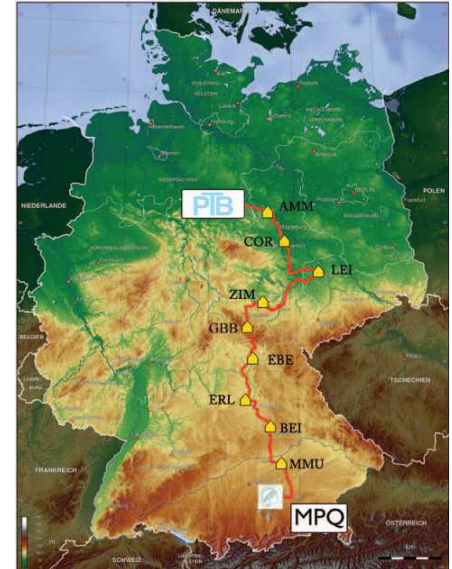
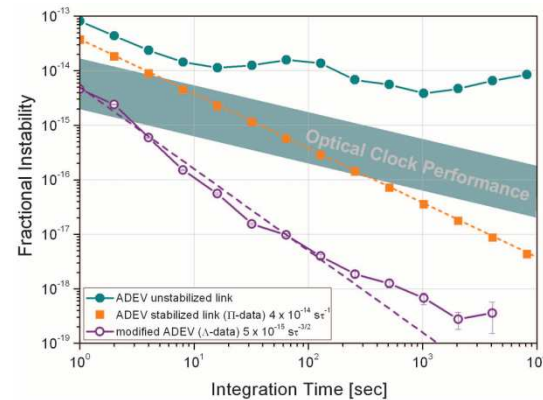


- Investigation of similar ground to space optical link
- ACES μW link: $\sim 10^{-16}$ @1d

Coherent optical fiber links

- Feasibility well-established (years ago)
 - Demonstration of ultra stable optical carrier transfer in telecom fiber over ~100-200 km in several groups (PTB, JILA/NIST, SYRTE/LPL, NMIJ/Tokyo Univ.,...)
 - Over a single such segment stability is $<10^{-19}$ @1d
- Long link demonstrated
 - PTB: 920 km in a dark fiber

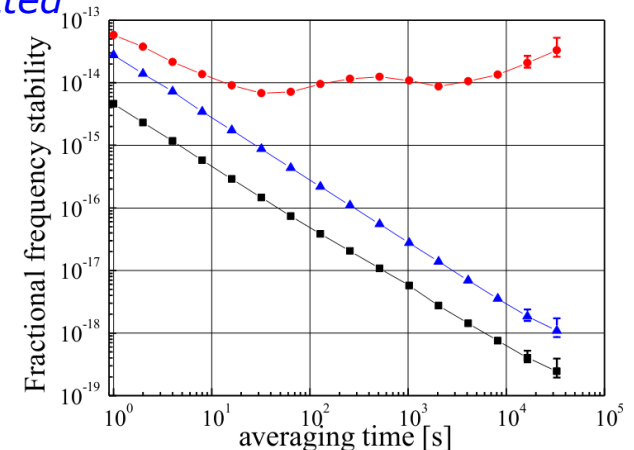
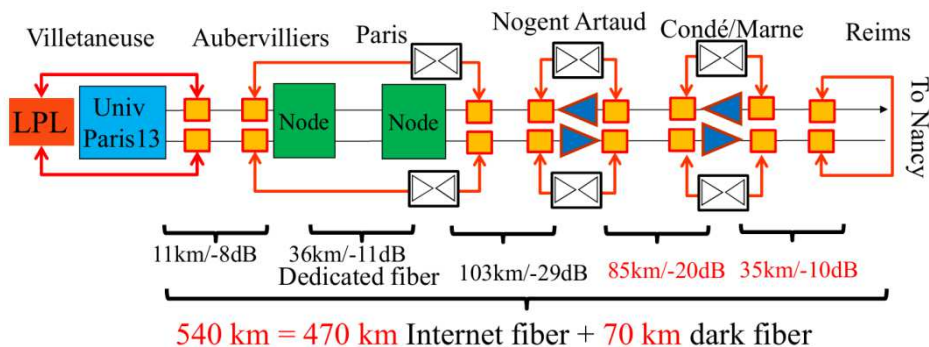
Science 336, 441 (2012)



- SYRTE/LPL: 540 km in a dark channel (fiber shared with internet)

Opt. Express 18, 16849 (2010)

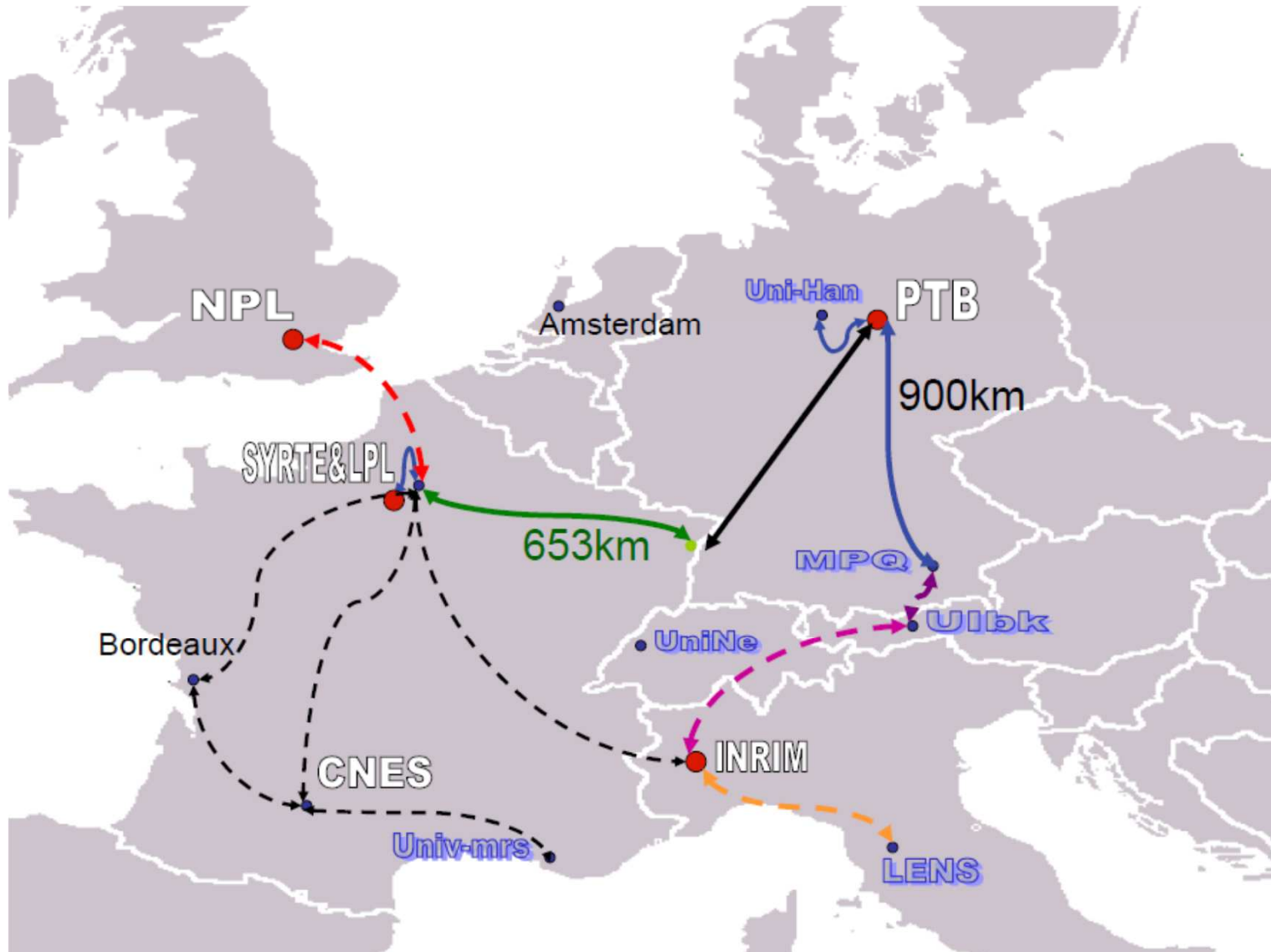
Opt. Express submitted arXiv:1206.5591



In the future: a European network

On-going now

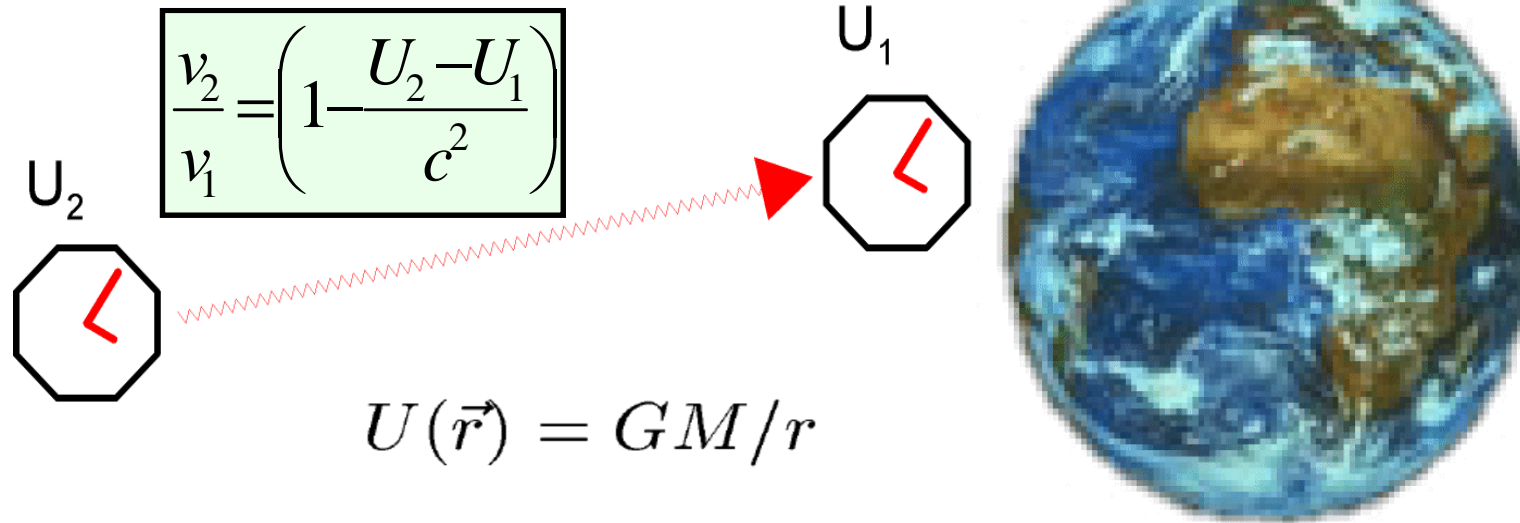
- Deployment at national and international scales





Metrology in curved space-time

Einstein's Gravitational Redshift



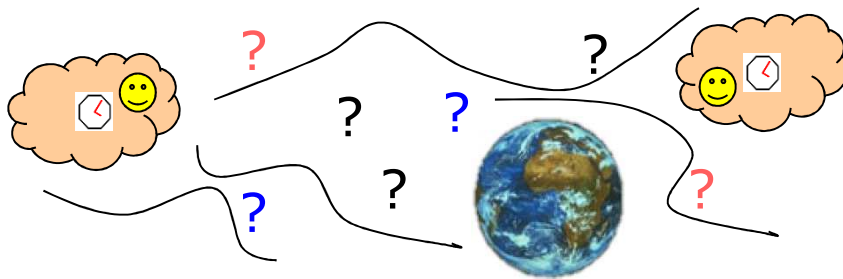
- Potential of the Earth at its surface: 7×10^{-10}
- Gradient at Earth surface: $\sim 10^{-16} \text{ m}^{-1}$
- Surface to GNSS satellite ($R=29600 \text{ km}$) difference: $\sim 5.5 \times 10^{-10}$

Redshift measurement with a 7×10^{-5} uncertainty: GPA, R. Vessot *et al.* (1976)
To be improved by ~ 30 by ACES

Frequency metrology and General Relativity

- A clock realizes its proper time
 - valid in a small volume where the metric is ~flat

$$d\tau^2 = \left(1 - 2\frac{U(T, \vec{R})}{c^2}\right) dT^2 - \frac{1}{c^2} d\vec{R}^2 \qquad d\tau \simeq \left(1 - \frac{U(T, \vec{R})}{c^2} - \frac{1}{2} \frac{\vec{V}^2}{c^2}\right) dT,$$



- Given present accuracies, remote clock comparisons in the vicinity of the Earth unavoidably amount to big General Relativity experiments
 - Need to define coordinate system
 - Need to taken into account for gravitation precisely
 - In this context, TAI is a realization the T coordinate of the chosen geocentric coordinate system

Impact of gravitation on TAI & clock comparisons

- A gravitational redshift correction must be included
- For TAI, the gravitational potential difference wrt the geoid is what matters
 - Ex: NIST Boulder: -1.7987×10^{-13} with a 3×10^{-17} unc. ($\Leftrightarrow 30$ cm)
 - Significant impact of Rocky Mountains *Metrologia 40, 66 (2003)*
 - In some places, 10^{-17} or slightly less
- Currently, temporal variations due to tides are not taken into account
- Clocks with accuracy of 10^{-17} - 10^{-18} (will) exist shortly as well as the means of comparing them remotely at this level
- → the current approach must be refined or modified
- → possibility to use clock to learn about the gravitational potential: "relativistic geodesy"



Ion clocks examples

Doppler cooling and fluorescence detection

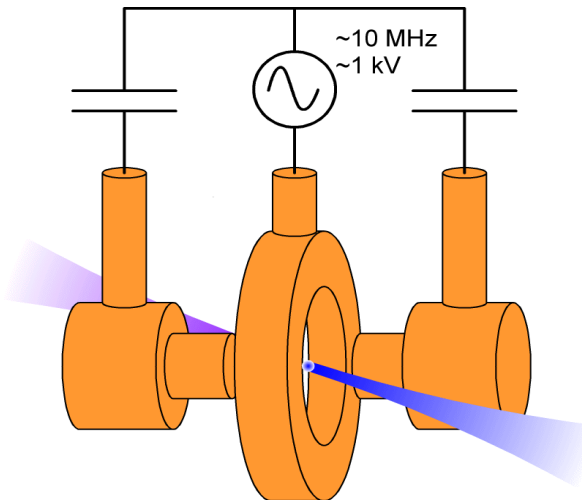
Trap configuration

Ring inner diameter: 0.8 mm

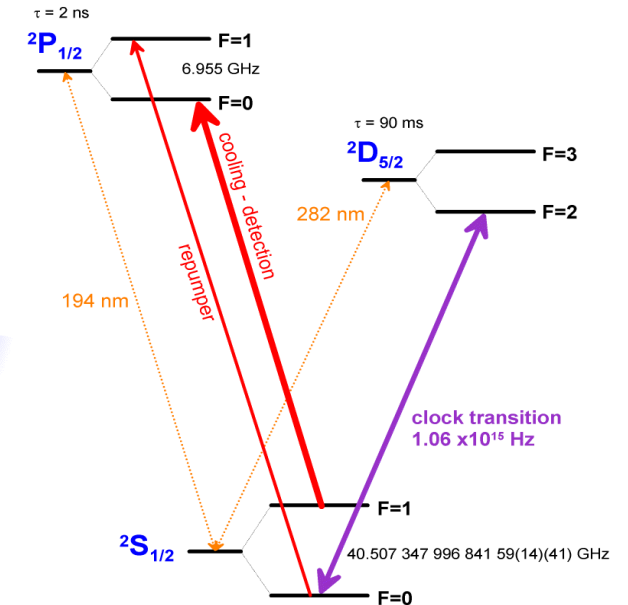
Drive frequency: 10 MHz

Drive amplitude: 1 kV

$$\begin{aligned} \nu_x, \nu_y &\sim 1 \text{ MHz} \\ \nu_z &\sim 2 \text{ MHz} \end{aligned}$$



Hg⁺: cooling wavelength: 194 nm
 $\Gamma=1/\tau$; $\tau \sim 2 \text{ ns} \rightarrow T_{\min} \sim 1.7 \text{ mK}$

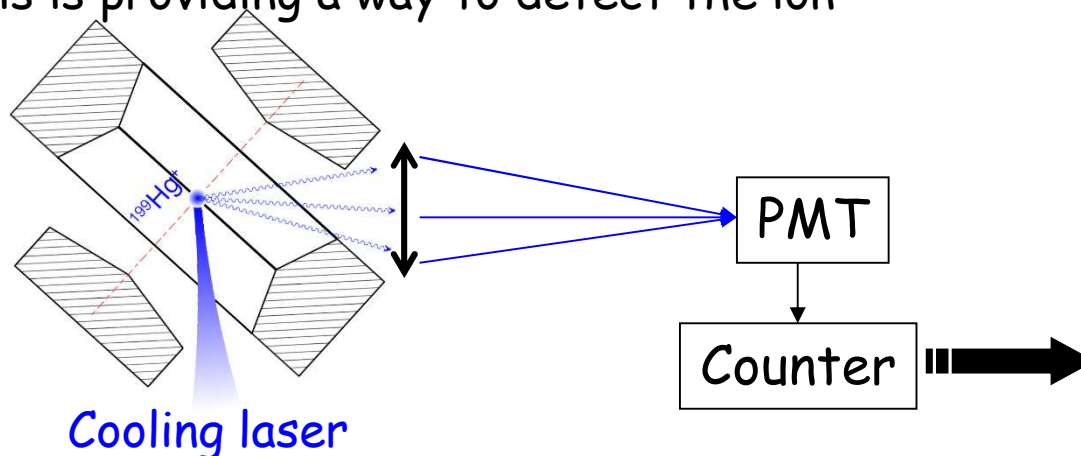


Doppler cooling

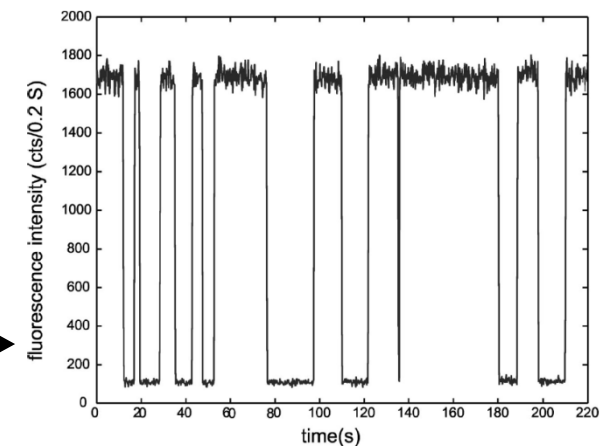
- Temperature: \sim few mK
- Average vibrational quantum number: $\langle ni \rangle \sim 35$
- RMS size of motion: $\Delta z \sim 42 \text{ nm}$

Fluorescence detection

- When cooling light is on, the ion is scattering photons
- This is providing a way to detect the ion



Quantum jumps in Ba⁺



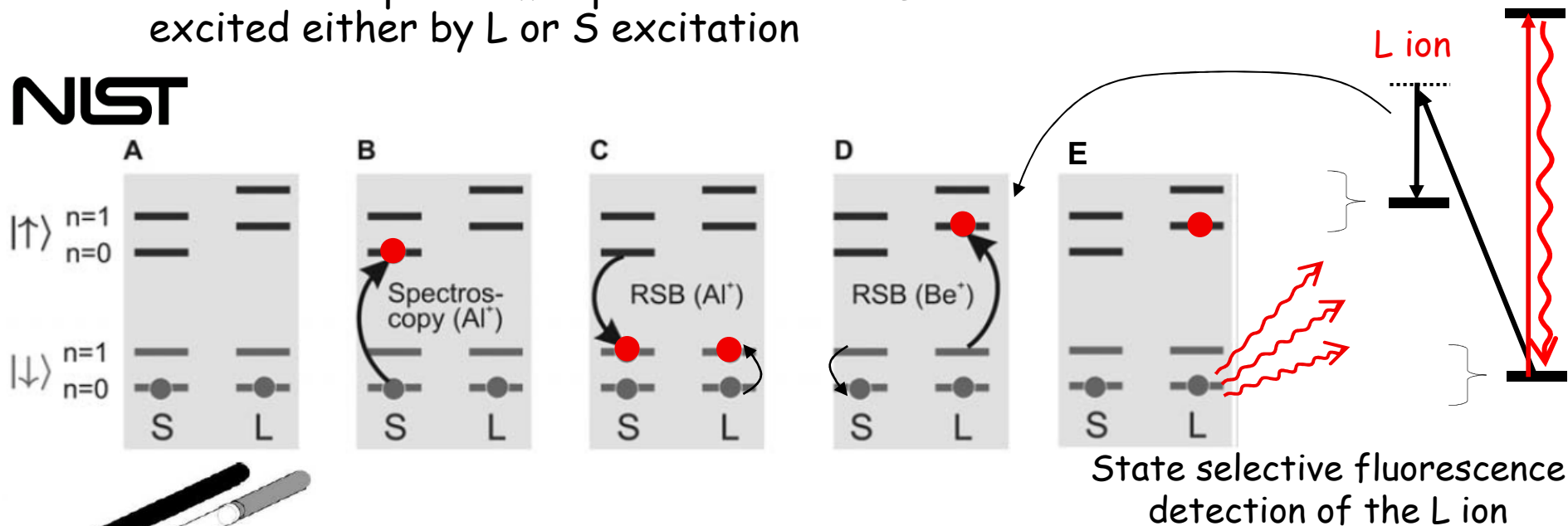
Detection and spectroscopy using quantum logic

Assume the following situation

P. O. Schmidt et al., Science 309, 749 (2005)

- 2 ions in a linear trap: Spectroscopy (clock) ion (S: Al⁺) + Logic ion (L: Be⁺)
- System cooled to the vibration ground state (sympathetic Raman sideband cooling with the logic ion)
- Usual probe pulse on the clock transition of the S ion
- The scheme is a way to detect the out-coming state of the S ion using a quantum logic gate to transfer the information to the L ion
 - Vibrational spectrum is present on both L and S transitions and can be excited either by L or S excitation

NIST

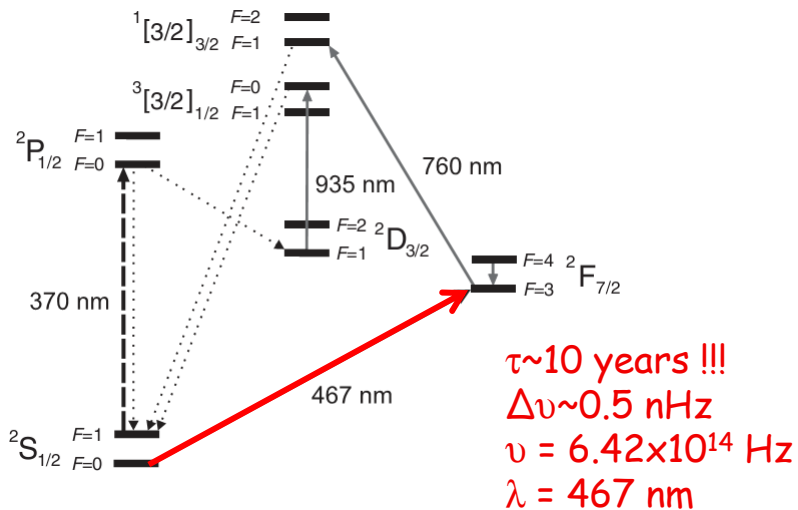


Fluorescence means "detection in the ground state of the S ion"

No Fluorescence means "detection in the excited state of the S ion"

Ion clock performance

$^{171}\text{Yb}^+$ octupole clock (NPL, PTB)



Huntemann et al., Phys. Rev. Lett. 108, 090801 (2012)

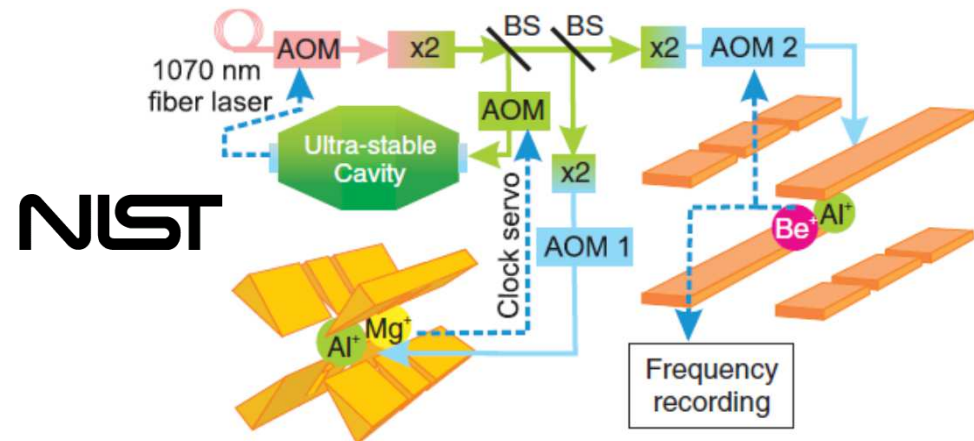
| Effect | $\delta\nu/\nu_0(10^{-18})$ | $u/\nu_0(10^{-18})$ |
|----------------------------|-----------------------------|---------------------|
| Blackbody radiation shift | -105 | 50 |
| Light shift extrapolation | 0 | 42 |
| Quadrupole shift | 0 | 22 |
| Second-order Doppler shift | 0 | 16 |
| Quadratic dc Stark shift | 0 | 4 |
| Servo error | 0 | 3 |
| Second-order Zeeman shift | -36 | 1 |
| Total | -141 | 71 |

PTB

Al^+ quantum logic clocks (NIST,...)

| Effect | Shift (10^{-18}) | Uncertainty (10^{-18}) |
|---------------------------|----------------------|----------------------------|
| Excess micromotion | -9 | 6 |
| Secular motion | -16.3 | 5 |
| Blackbody radiation shift | -9 | 3 |
| Cooling laser Stark shift | -3.6 | 1.5 |
| Quad. Zeeman shift | -1079.9 | 0.7 |
| Linear Doppler shift | 0 | 0.3 |
| Clock laser Stark shift | 0 | 0.2 |
| Background-gas collisions | 0 | 0.5 |
| AOM freq. error | 0 | 0.2 |
| Total | -1117.8 | 8.6 |

Stability: $\sim 2.8 \times 10^{-15}$ @1s



Fractional frequency difference:

$$(\nu_{\text{AlMg}} - \nu_{\text{AlBe}})/\nu = (-1.8 \pm 0.7) \times 10^{-17}$$

Chou et al., PRL 104, 070802 (2010)

Total uncertainty:

$$2.5 \times 10^{-17}$$

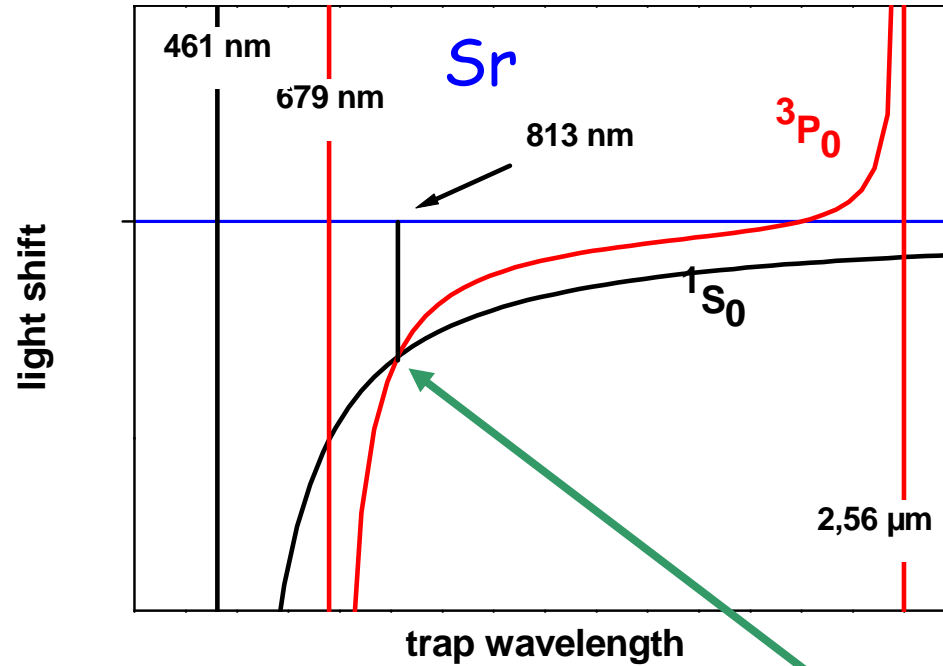


Lattice clocks examples

"Non-perturbing" dipole lattice trap

H. Katori et al., *Phys. Rev. Lett.* 91, 173005 (2003)

Light shift as a function of trap wavelength

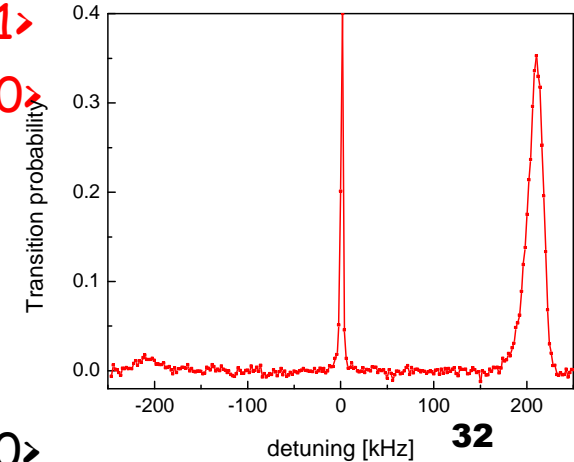
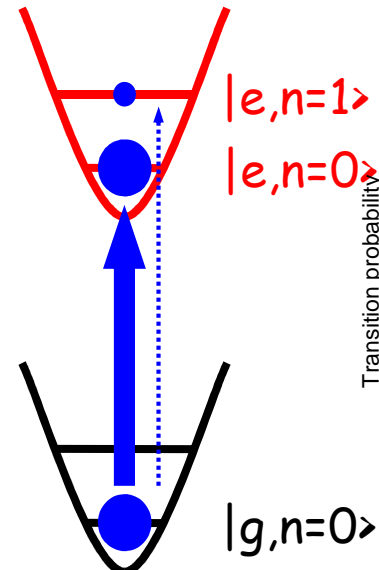
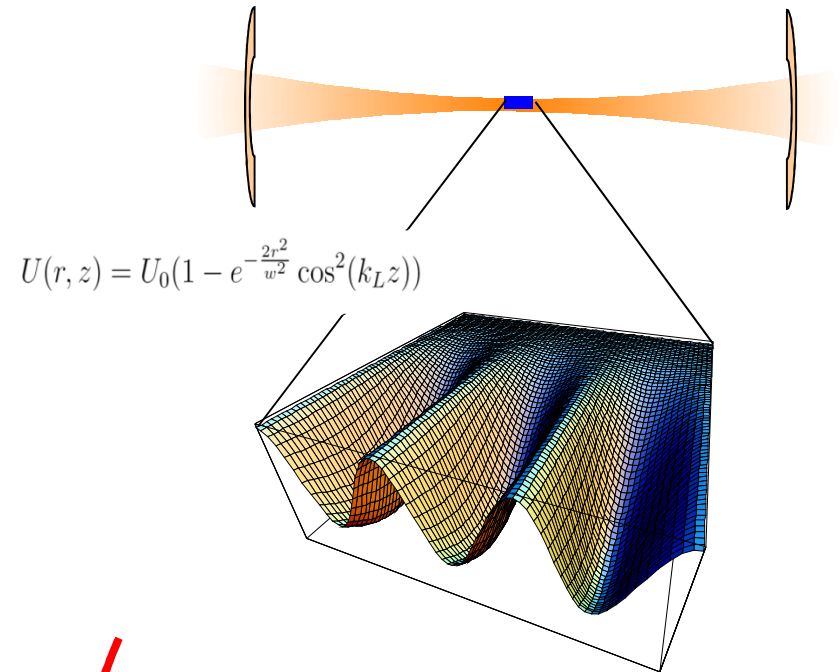


Magic wavelength : polarizabilities are equal for both clock states

Sensitivity under typical conditions : 10^{-15} /GHz

Combines the advantages of trapped ion and neutral atom: large atom number in the Lamb-Dicke regime

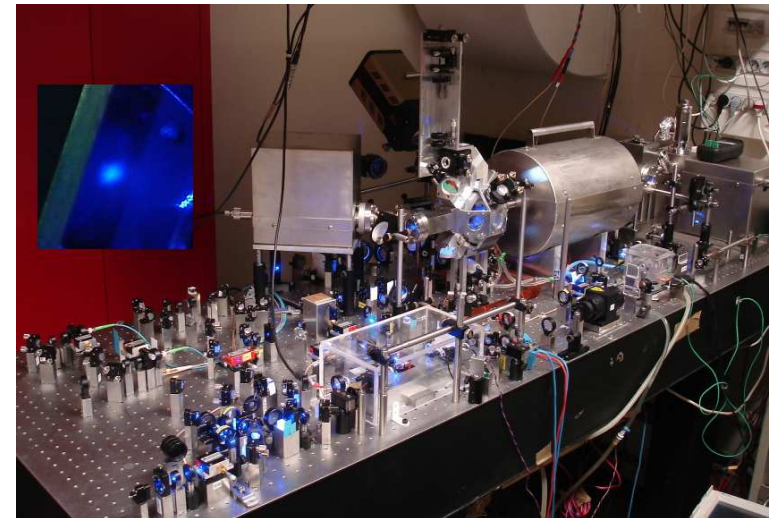
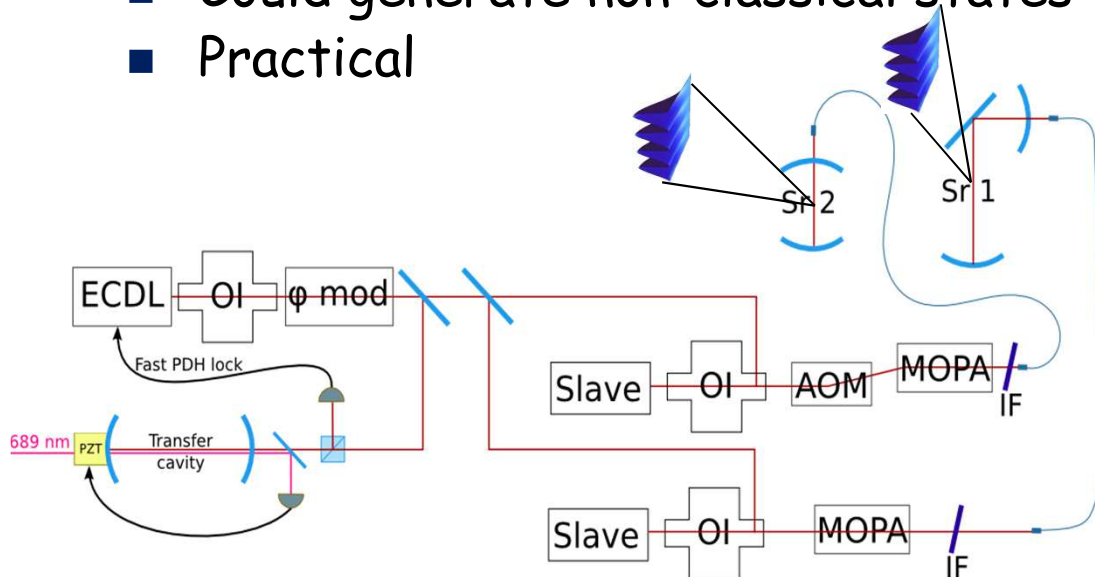
Typical max depth
 ~ 4 MHz
 ~ 200 μ K



Sr lattice clocks at LNE-SYRTE

- 2 operating Sr optical lattice clocks
 - Ultra-stable laser (698 nm) with 10 cm FS mirror cavity
 - Lattice traps with build-up cavity: depth up to several 1000 E_R
 - Only semi-conductor lasers
- Recent studies of systematic shifts
 - Hyperpolarizability
 - Tensor lattice light shift

P. Westergaard et al., PRL 106, 210801 (2011)
- Non-destructive detection
 - High stability by reducing the Dick effect
 - Could generate non-classical states → sub-QPN regime
 - Practical



Accuracy of Sr clocks

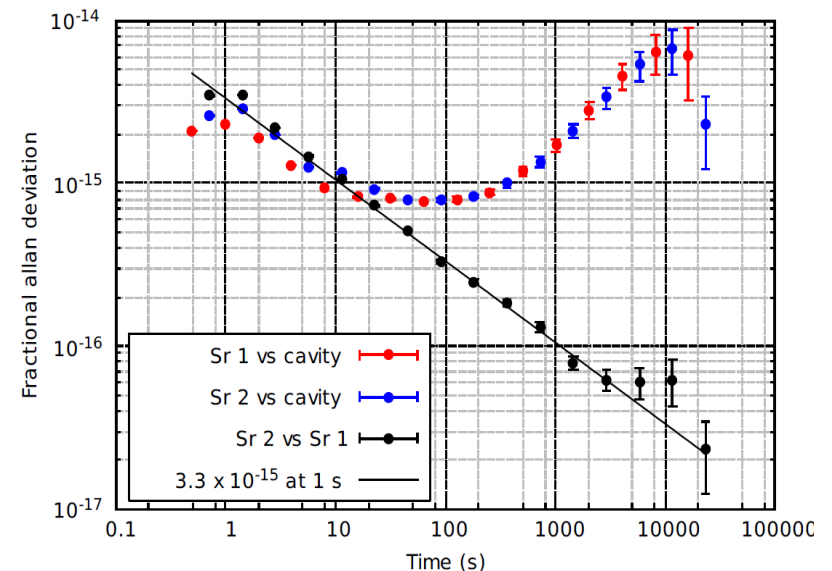
Typical accuracy budget at 500 E_R trap depth

| Effect | Correction | Uncertainty | |
|------------------------|------------|-------------|------------------------|
| Quadratic zeeman | 835 mHz | 2 mHz | 0.05×10^{-16} |
| Lattice (first order) | -84 mHz | 20 mHz | 0.5×10^{-16} |
| Lattice (second order) | -35 mHz | 14 mHz | 0.3×10^{-16} |
| Black body | 2.376 Hz | 45 mHz | 1×10^{-16} |
| Density shift | -8 mHz | 19 mHz | 4.5×10^{-17} |
| Line pulling | 0 | 20 mHz | 0.5×10^{-16} |
| Lightshift probe | 0 | 8 mHz | 2×10^{-17} |
| Total | 3.084 Hz | 58 mHz | 1.4×10^{-16} |

- Note: see also JILA (Science 319, 1805 (2008)) and PTB (Metrologia 48, 399 (2011))

Comparisons

- Agreement to $<10^{-16}$...
- ... After fighting several unexpected "technical" shifts



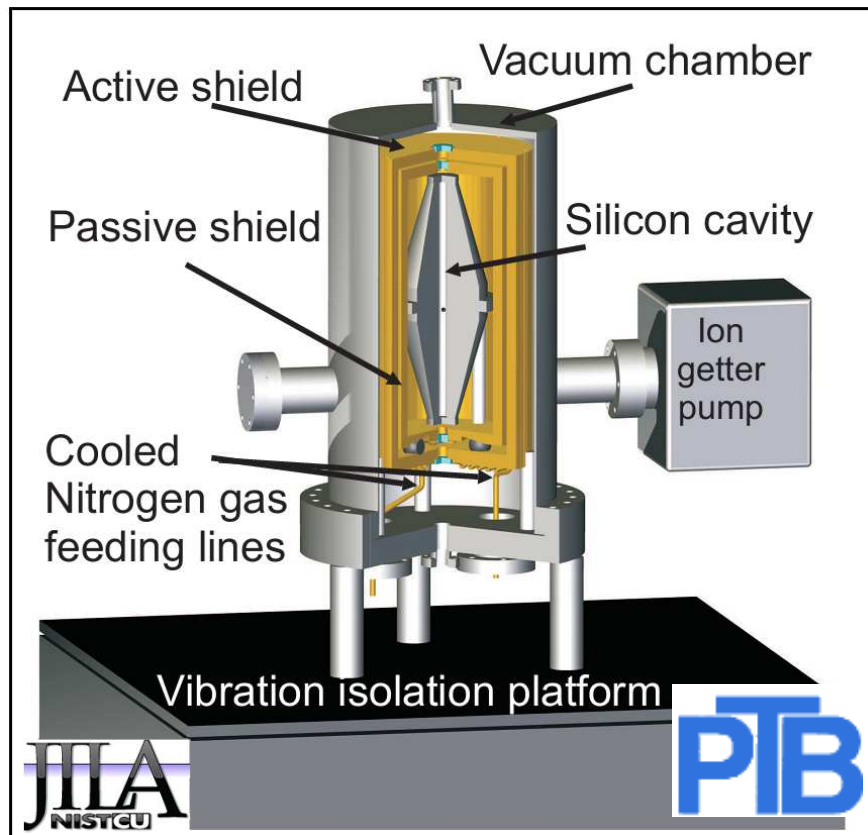
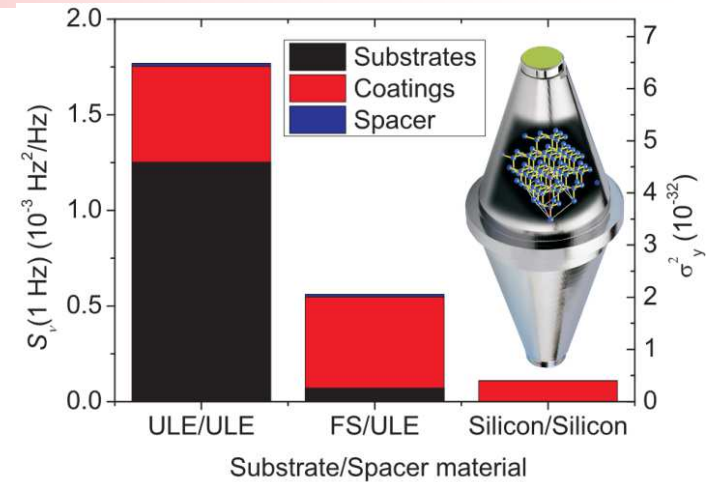


Ultra-stable lasers examples

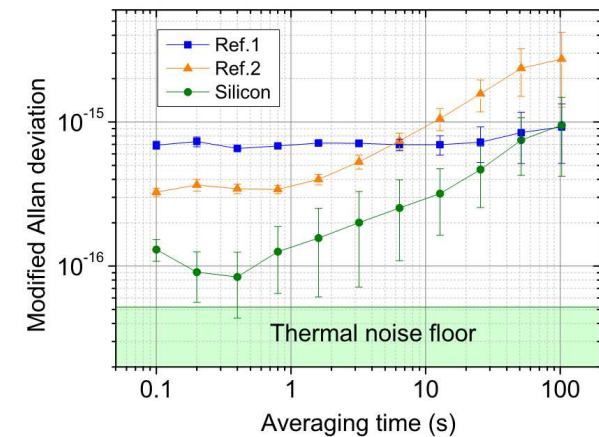
Cryogenic silicon cavity

T. Kessler et al., Nat Photon (2012)

- Features of crystalline Si
 - Turning point in thermal expansion at 124 K
 - Higher mechanical Q than ULE or FS : $Q > 10^7$
 - Transparent at $1.5 \mu\text{m}$
 - High Young modulus: $E = 187.5 \text{ GPa}$ ($\langle 111 \rangle$ axis)
 - High thermal conductivity: $500 \text{ W m}^{-1} \text{ K}^{-1}$



→ 1×10^{-16} at short times



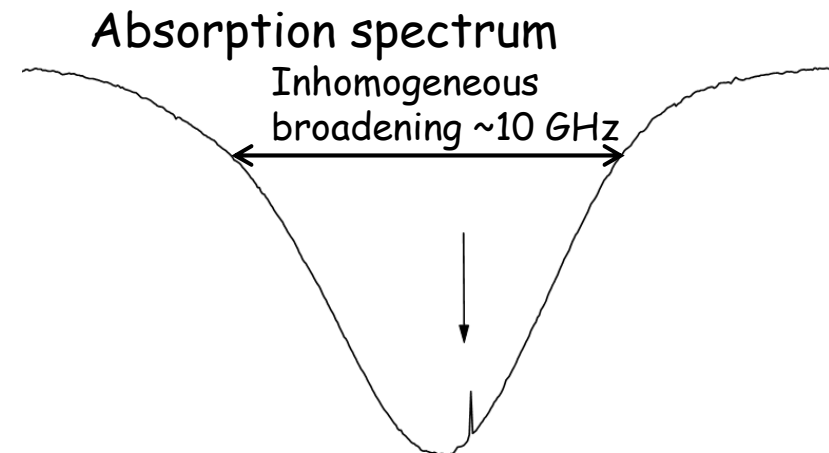
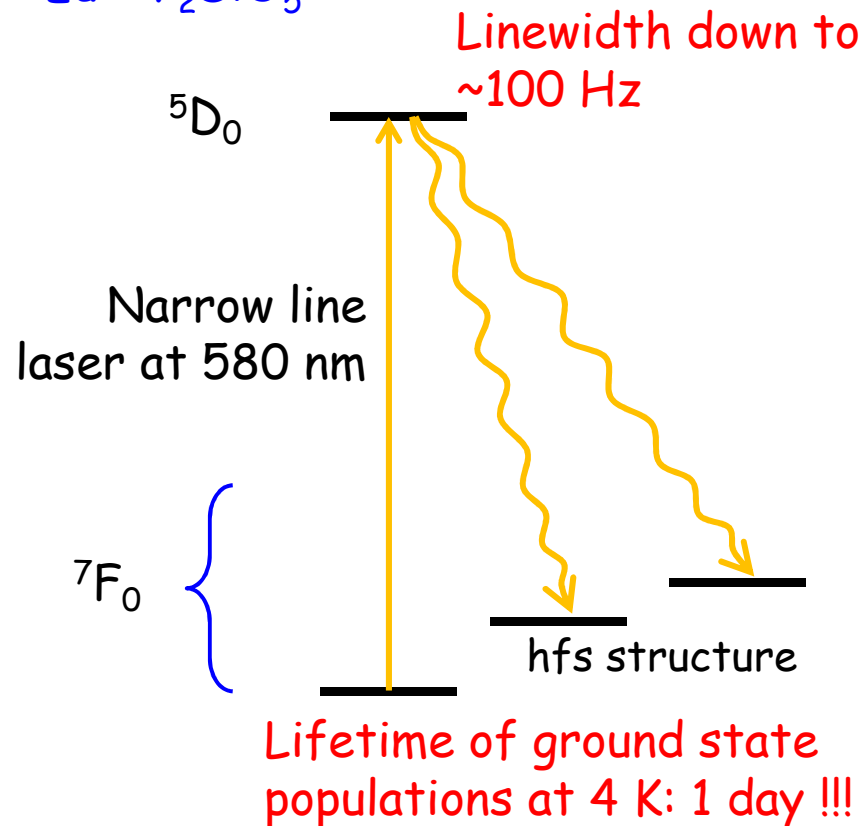
Measured with three-cornered hat method

→ 4.5×10^{-16} @1s with Sr lattice clock at PTB

Stabilization using spectral hole burning (1)

Rare-earth ions in crystal at 4 K

$\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$

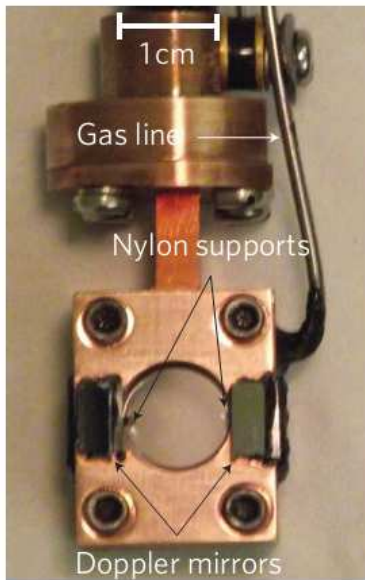


- A narrow line (0.1-1 kHz) hole can be burned in the absorption spectrum
- The same hole can be probed later to stabilize the laser frequency
- → increases the autocorrelation of the laser in time
- ⇔ improving the laser stability
- Many absorbers → low quantum limit
- Atomic system (+ well-chosen matrix) → low thermal noise limit, low sensitivity to vibration,...
- $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$ chosen for narrow line, long lifetime, low sensitivity to B,...

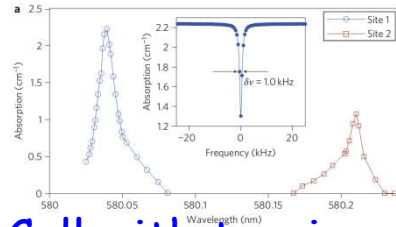
Stabilization using spectral hole burning (2)

Thorpe et al., Nat. Photon. 5, 688 (2011)

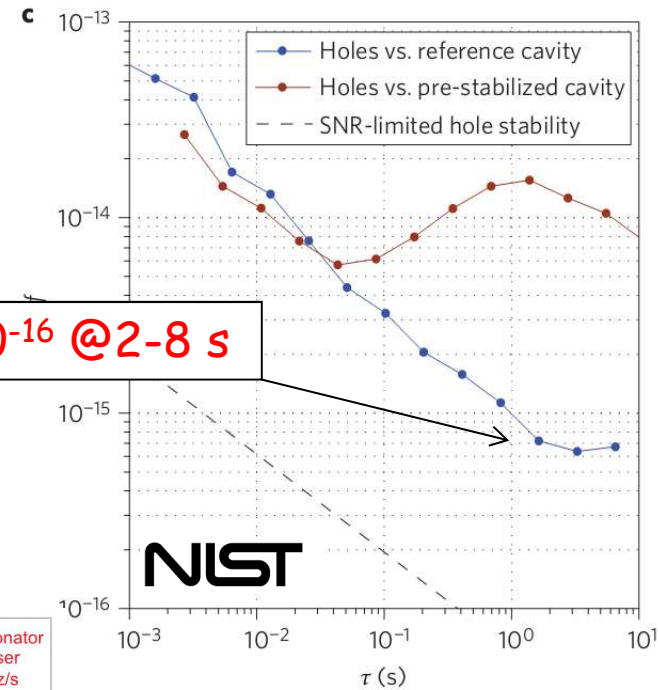
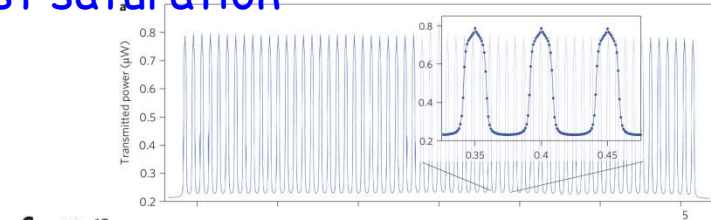
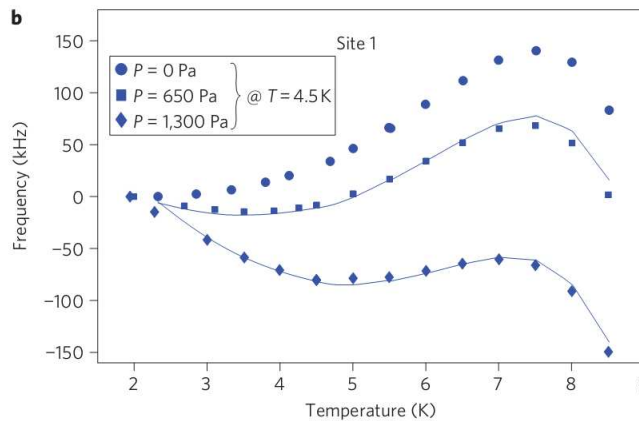
Uses multiple holes to "save" them from fast saturation



NIST



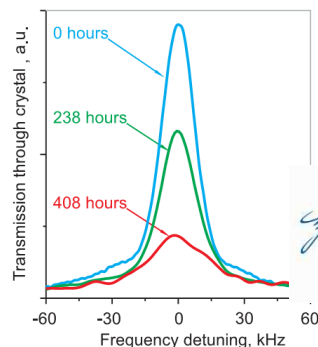
Cell with turning point in T°



NIST

Chen et al., Phys. Rev. Lett. 107, 223202 (2011)

- Long term stability with a single hole
- 5 mHz/s drift rate
- $10^{-17}/s$



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