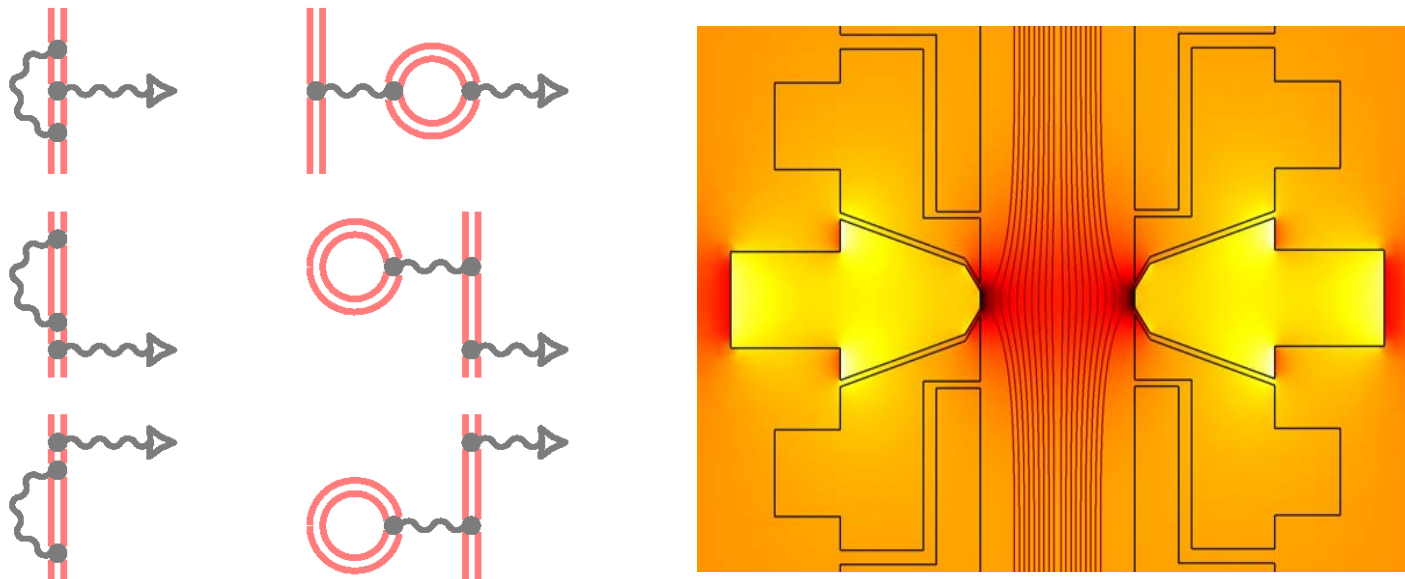
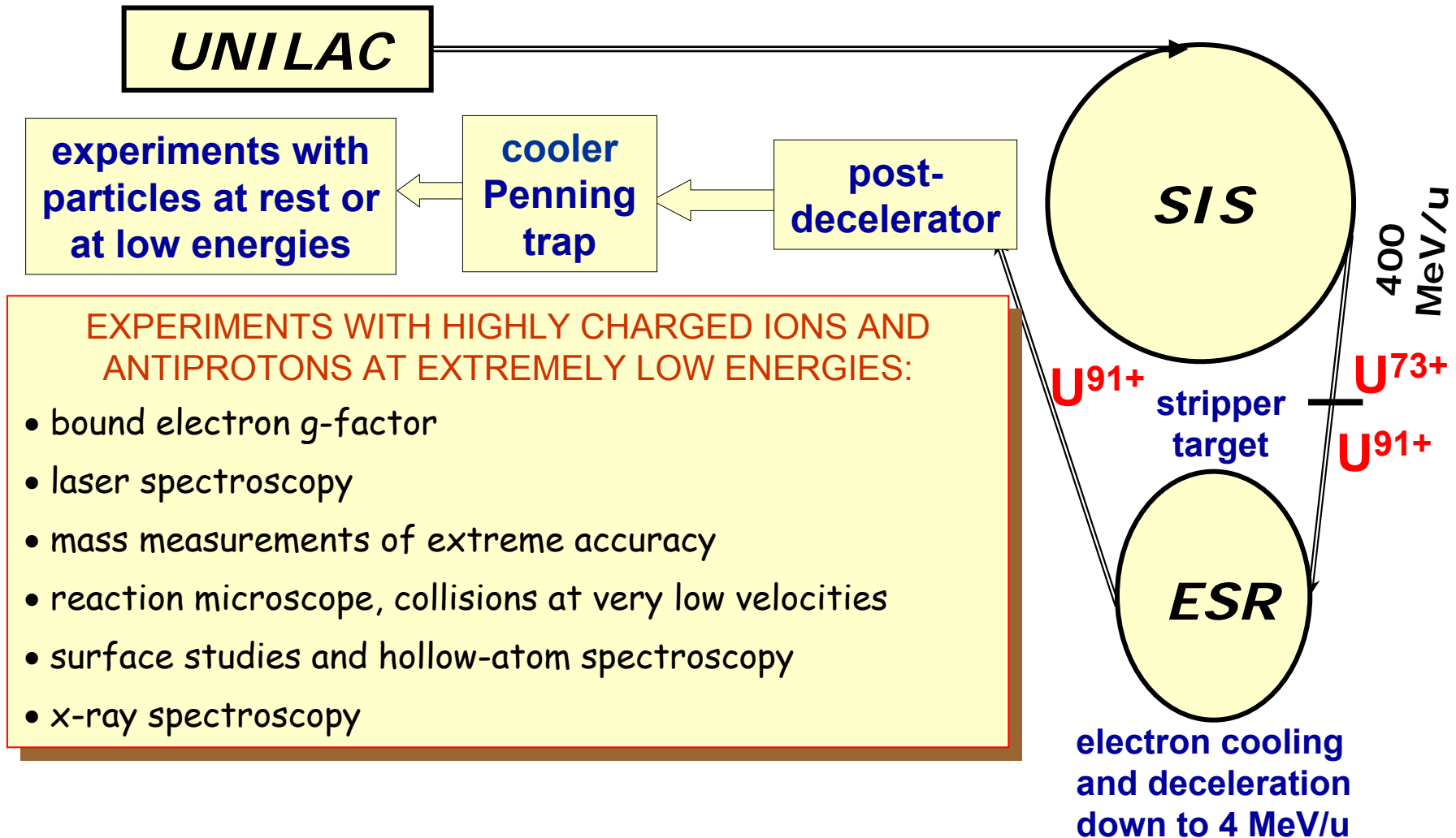


Precision Experiments with Cooled Highly Charged Ions in Penning Traps at HITRAP



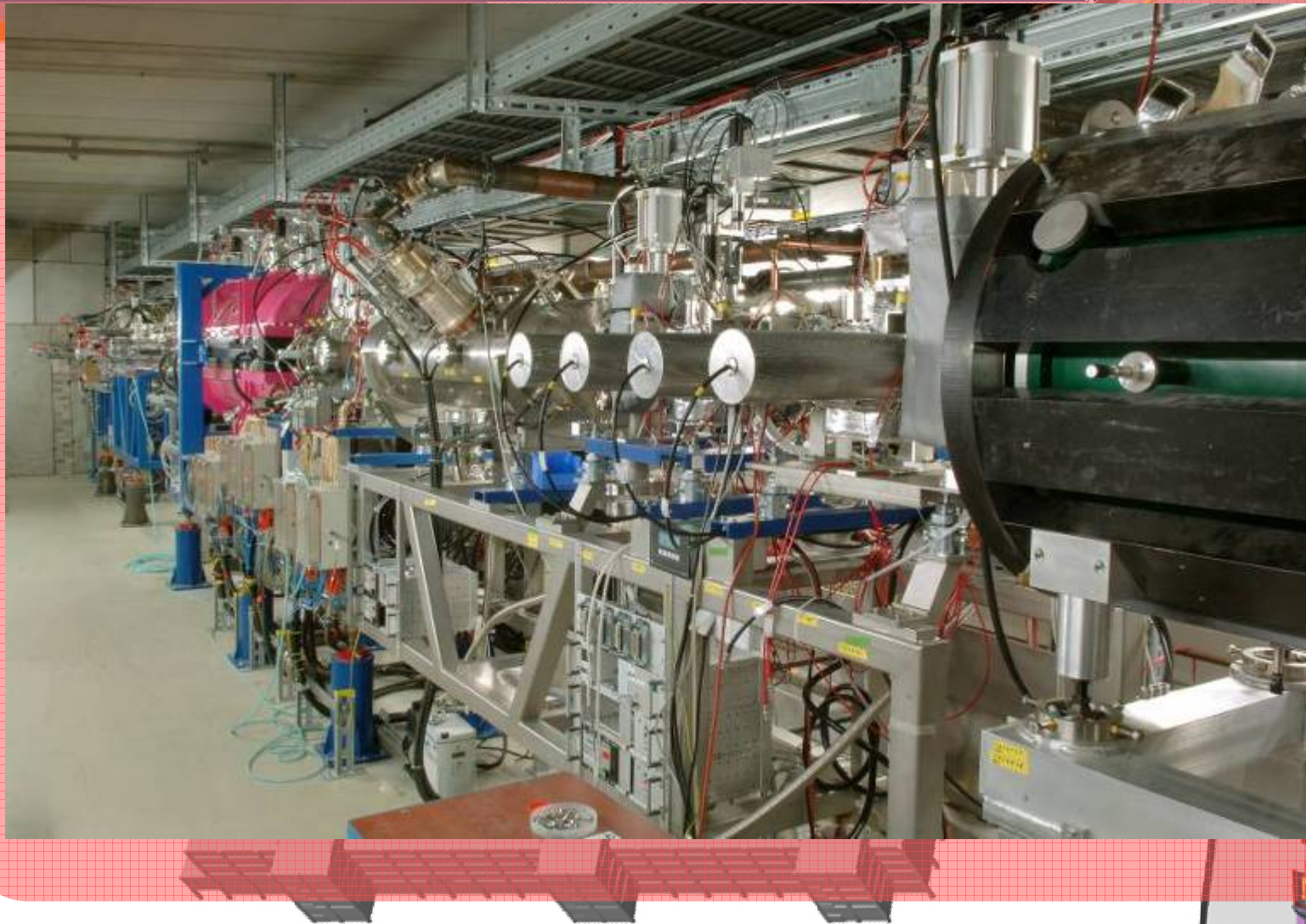
*Wolfgang Quint
GSI Darmstadt and Univ. Heidelberg*

HITRAP at the ESR storage ring / GSI



HITRAP

GSI accelerator facility

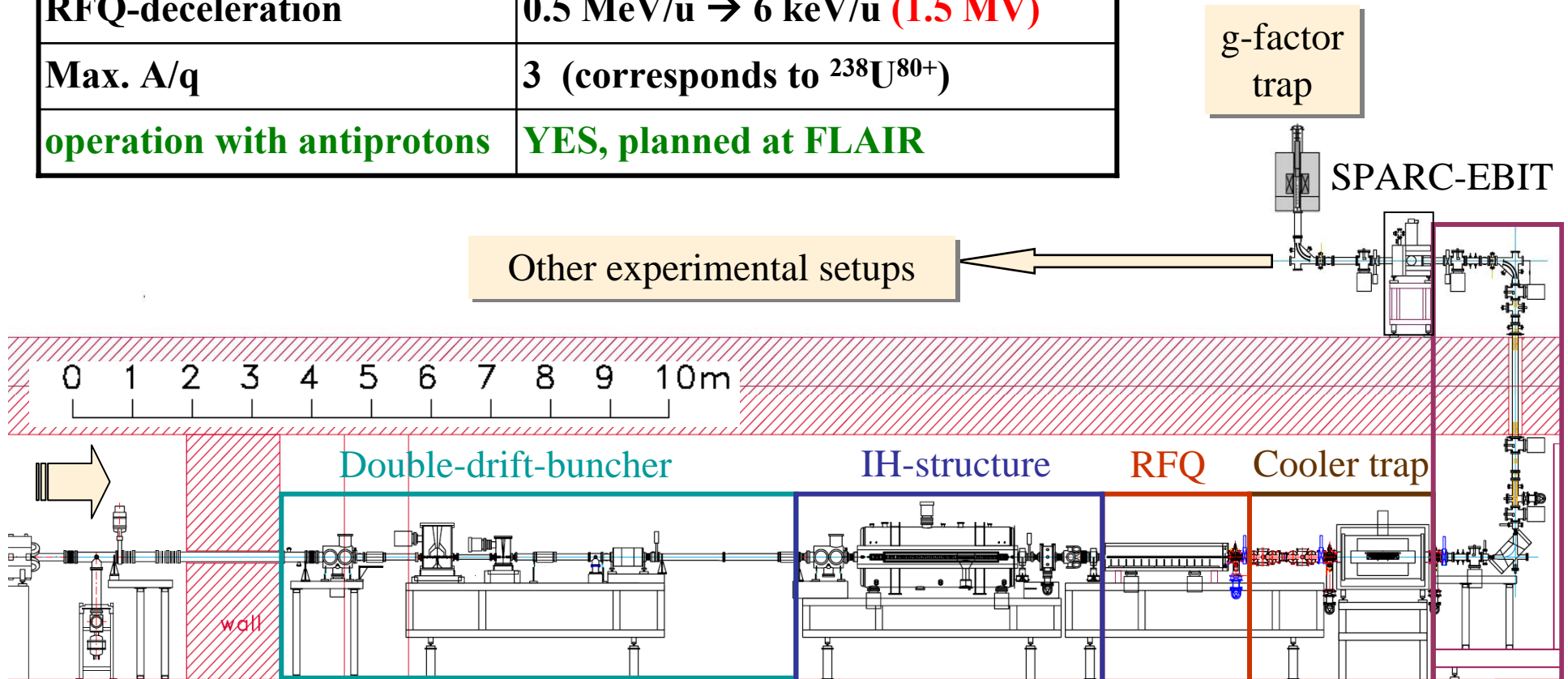


GeV/u

Ref.:
Frank Herfurth

HITRAP facility at ESR storage ring

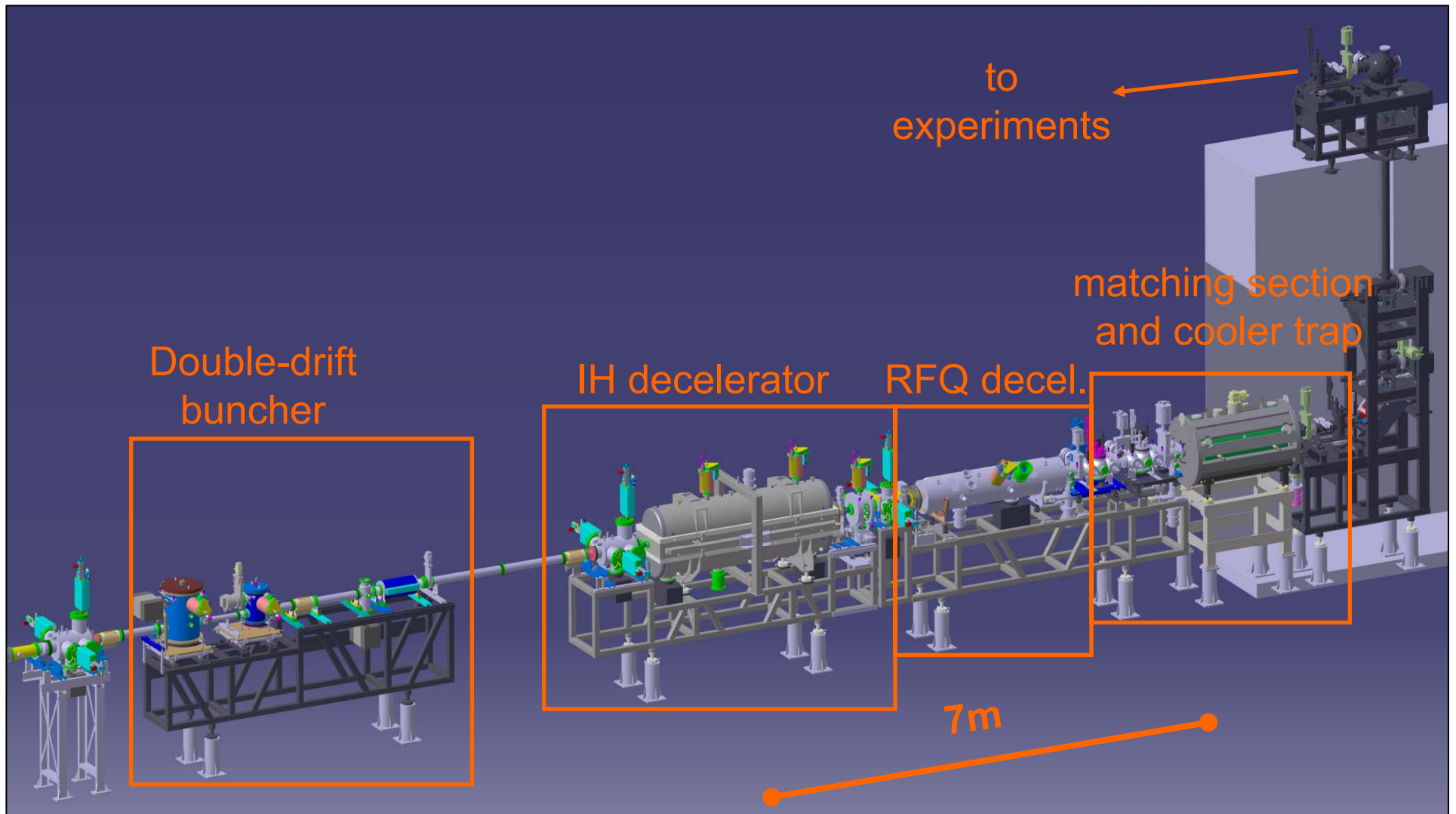
Linac operation frequency	108.408 MHz
IH-deceleration	4 MeV/u \rightarrow 0.5 MeV/u (10.5 MV)
RFQ-deceleration	0.5 MeV/u \rightarrow 6 keV/u (1.5 MV)
Max. A/q	3 (corresponds to $^{238}\text{U}^{80+}$)
operation with antiprotons	YES, planned at FLAIR



HCI from ESR 4 MeV/u

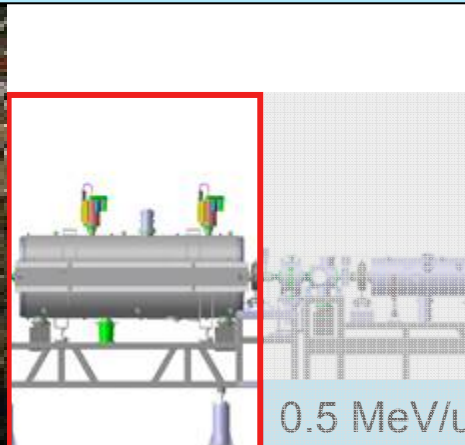
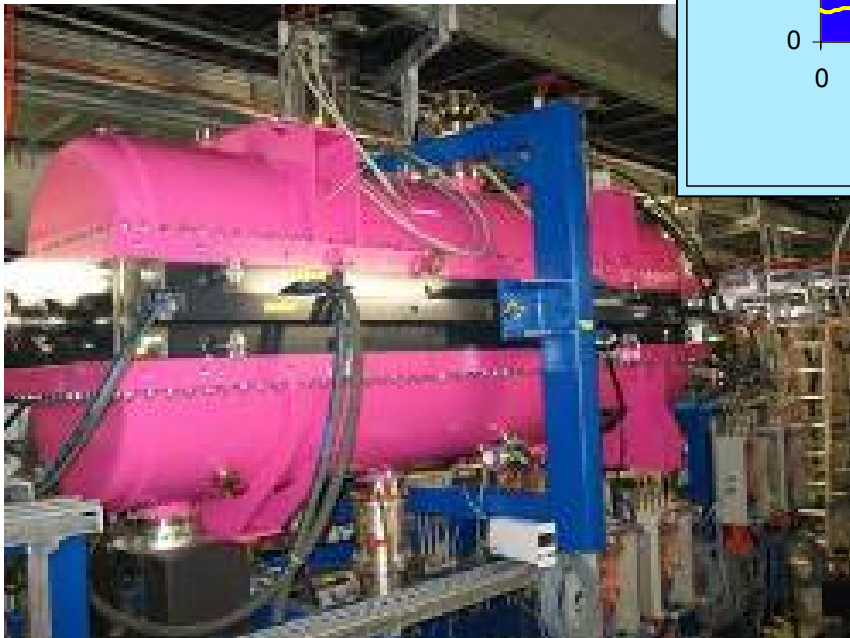
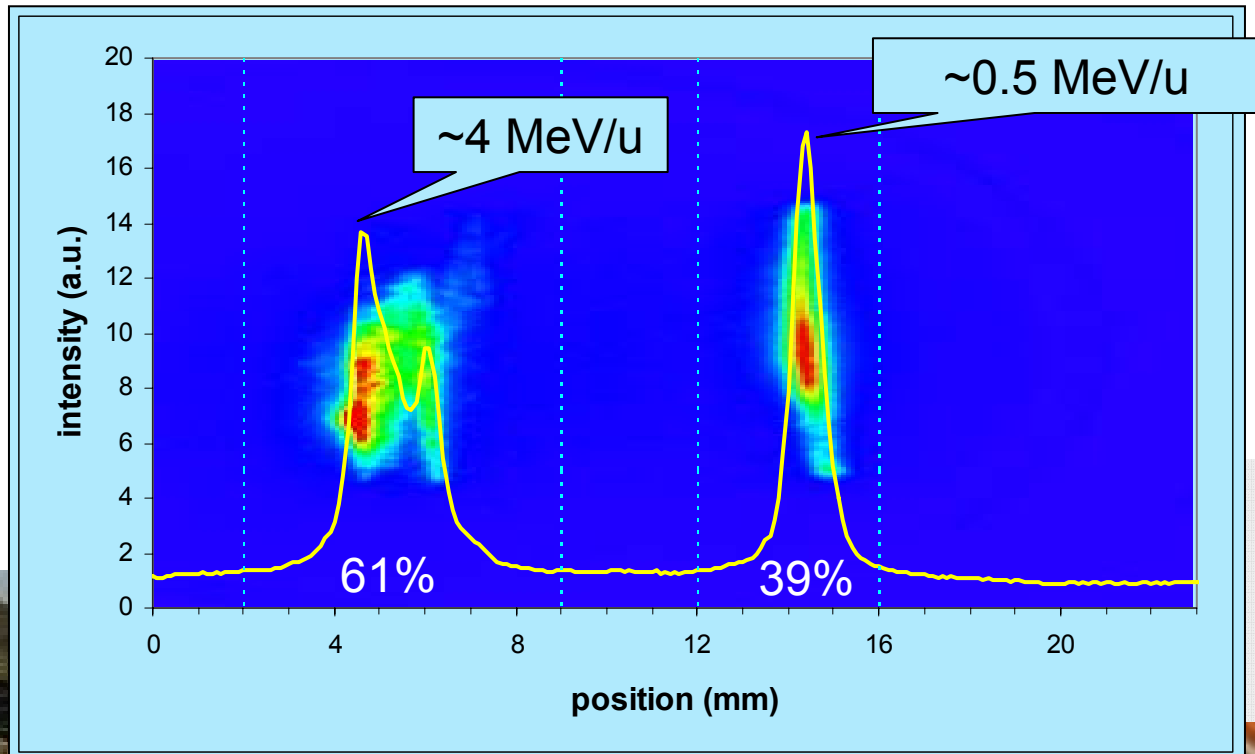
\rightarrow 0.5 MeV/u \rightarrow 6 keV/u

HITRAP: Technical design



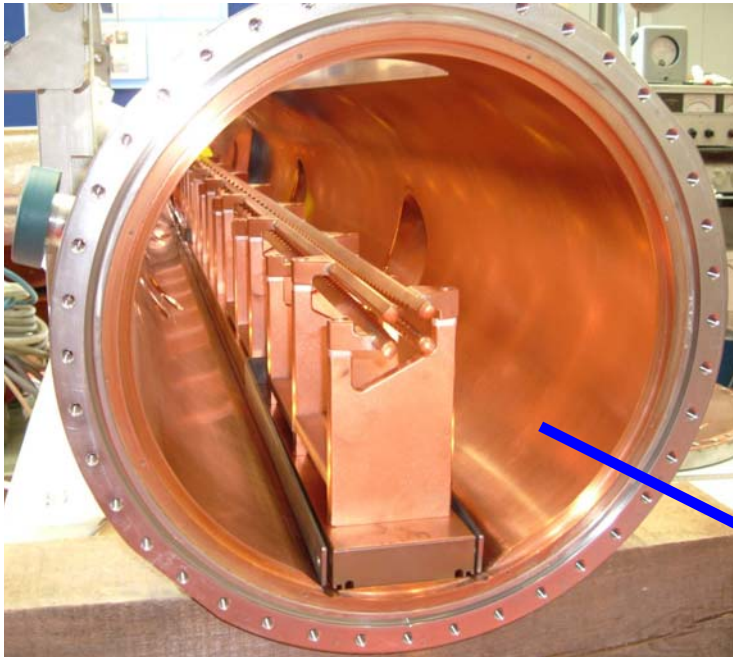
HITRAP – Linear decelerator

- Fraction of decelerated particles close to theory

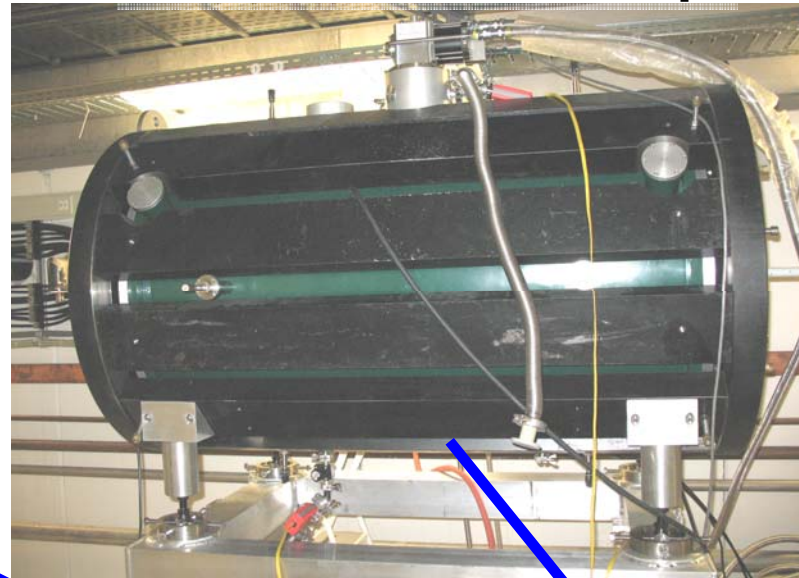


Commissioning of RFQ decelerator and of cooler trap in progress

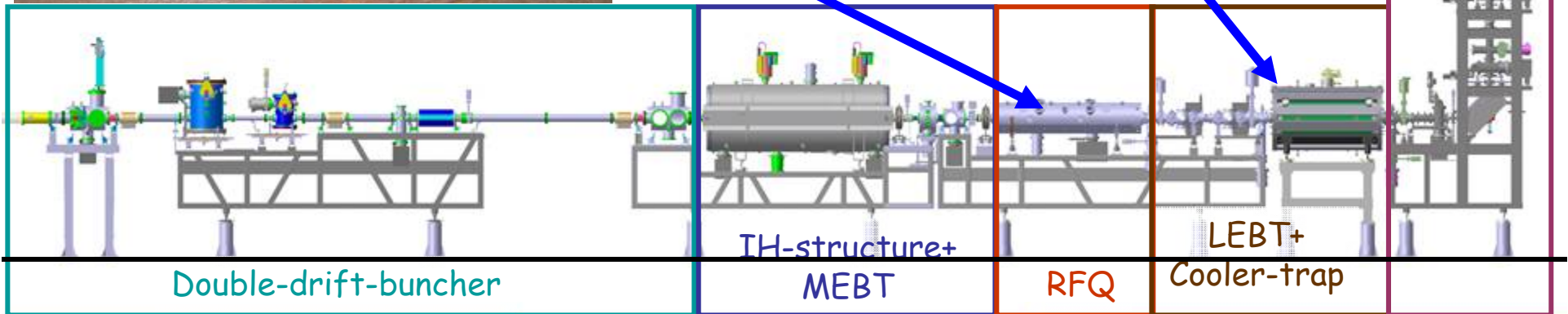
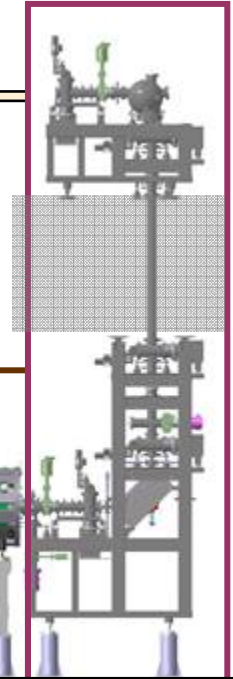
RFQ decelerator



HITRAP cooler trap



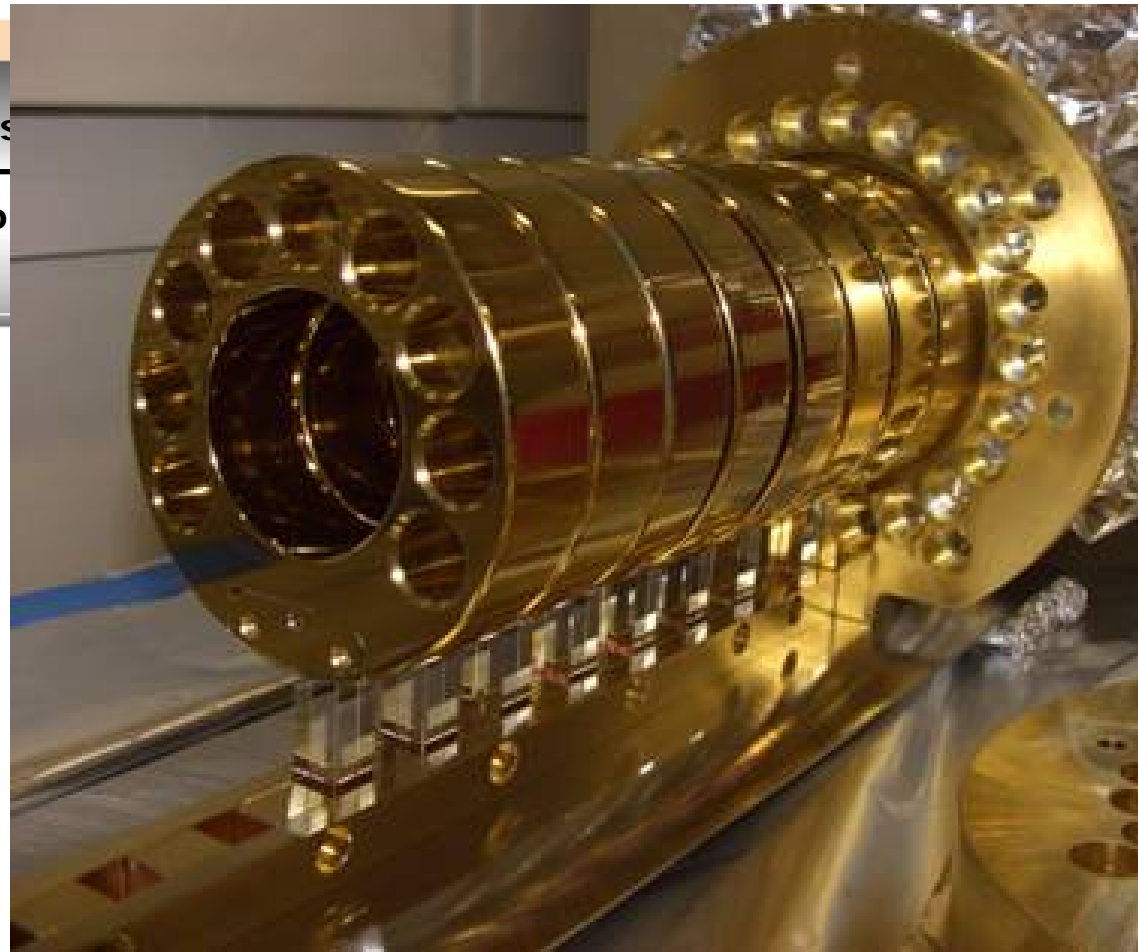
vertical
beam line



HITRAP Cooler Penning trap

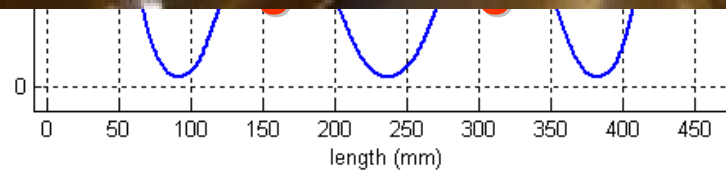
- electron cooling
- resistive cooling to $T = 4\text{ K}$

highly charged ions
from _____
HITRAP decelerator

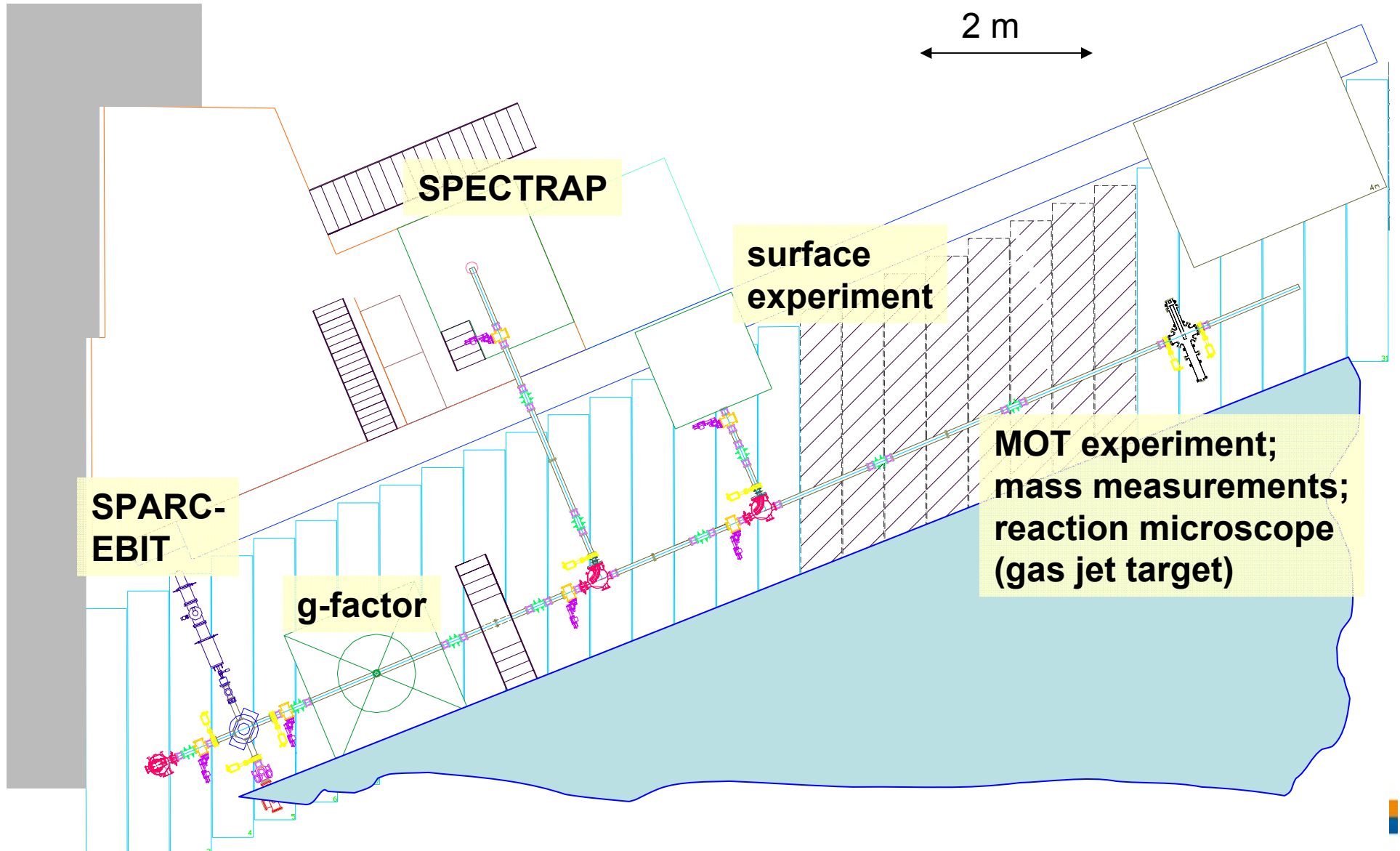


cooled HCl
to HITRAP
experiments

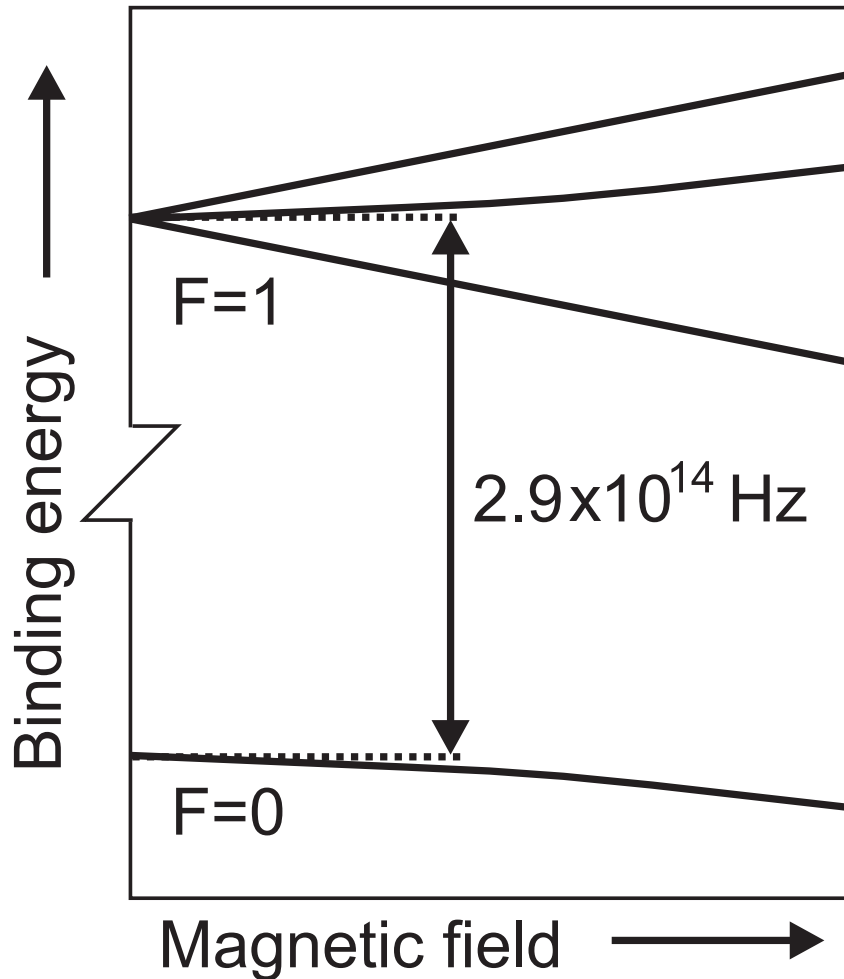
cooler trap:
(ms...sec)



HITRAP experimental area



SPECTRAP: Laser spectroscopy of hyperfine splitting in highly charged ions

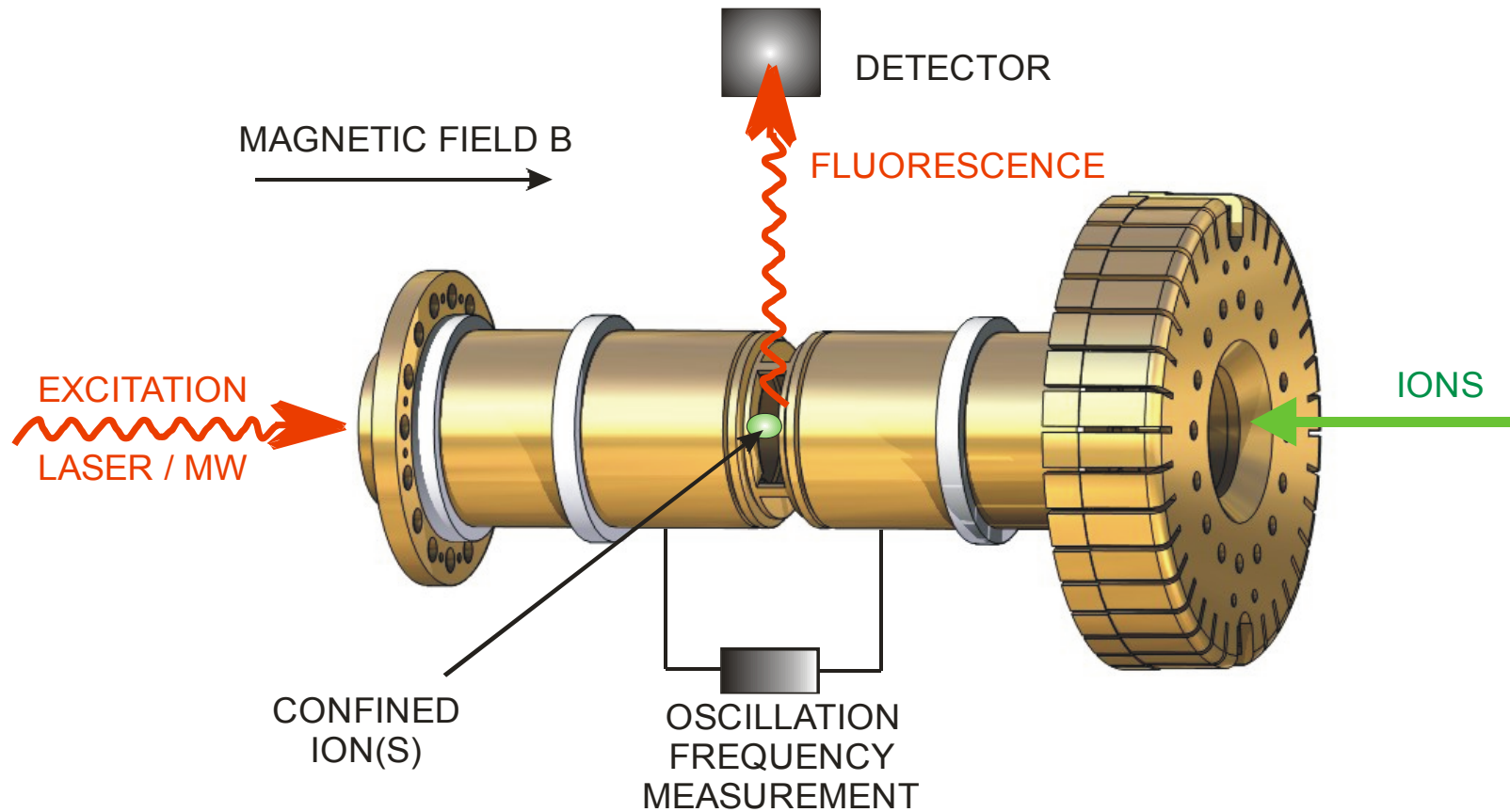


- example: H-like lead $^{207}\text{Pb}^{81+}$
- HFS wavelengths move into visible for $Z > 70$
- very small Doppler width at $T = 4$ K
- relative wavelength accuracy $\leq 10^{-7}$

Physics goals:

- test of QED in strong fields
- nuclear structure studies

SPECTRAP: Laser spectroscopy of HFS transitions in highly charged ions

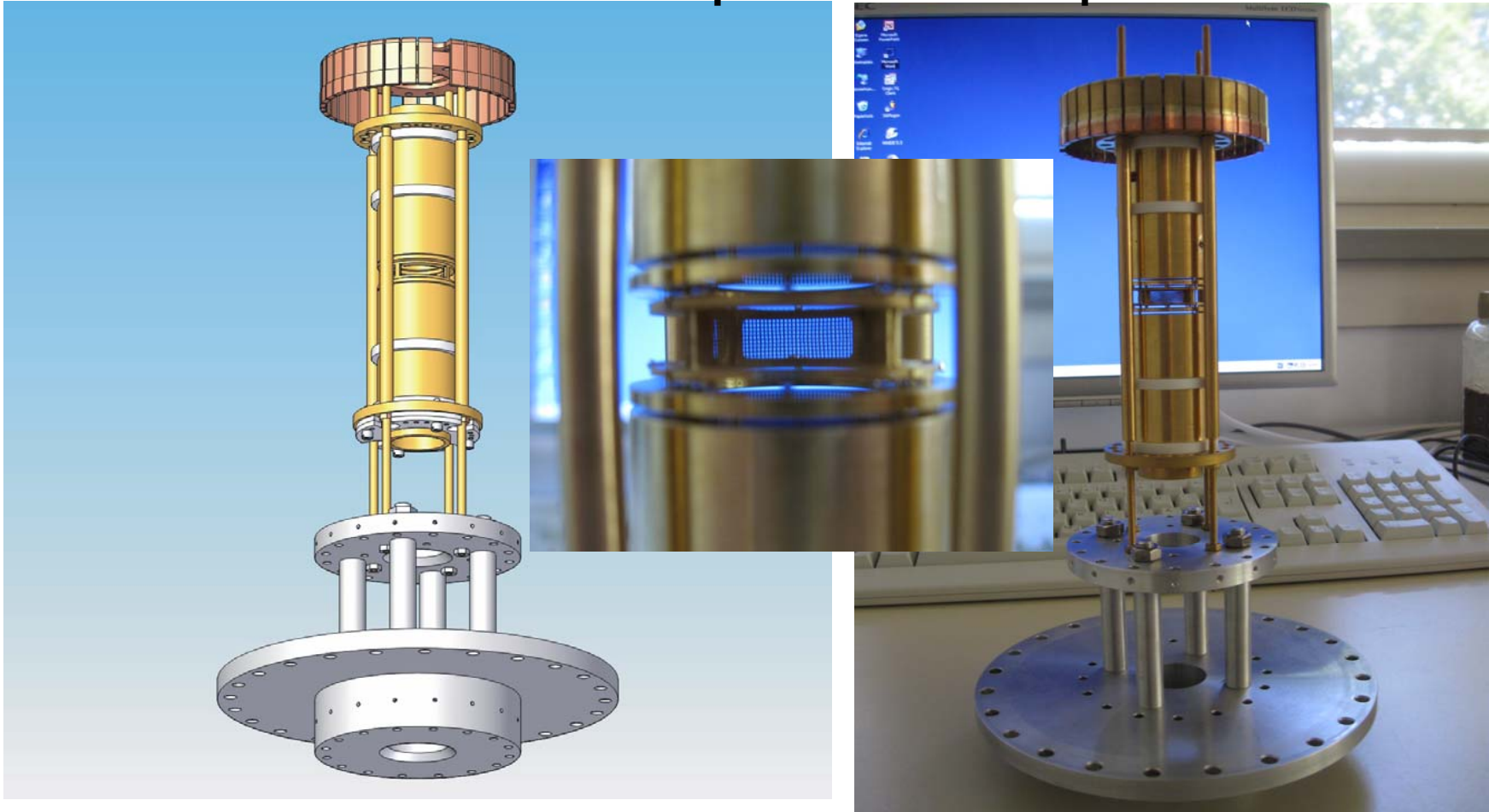


$$4 \text{ K} \longrightarrow \Delta E/E \sim 10^{-7}$$

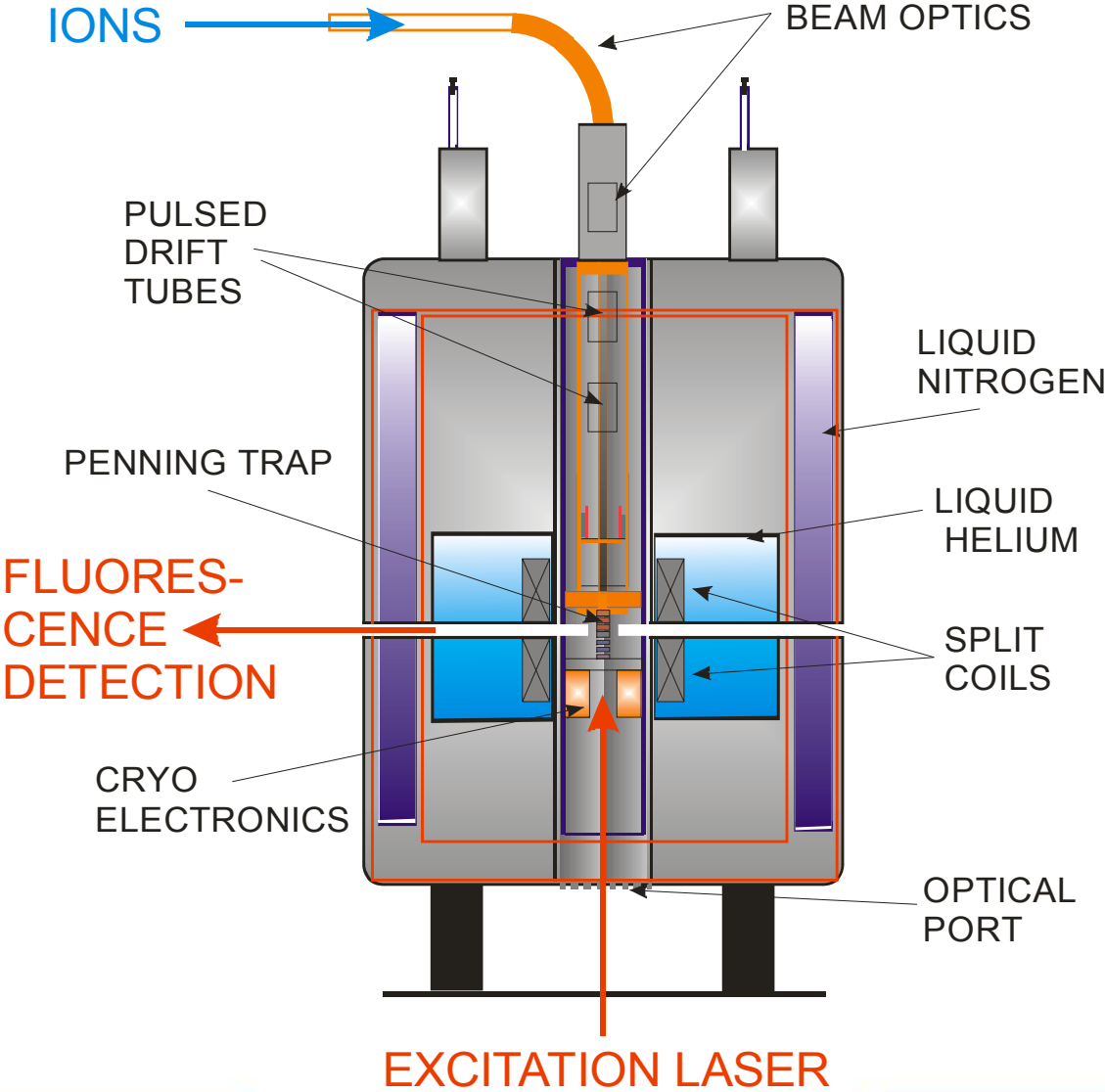
Ref.:
Wilfried Nörtershäuser et al.

SPECTRAP: Laser spectroscopy of HFS transitions in highly charged ions

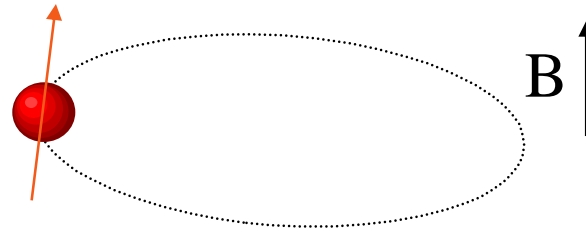
virtual trap meets real trap



SPECTRAP setup at the HITRAP facility



g-Factor of the electron



$$\mu = g \cdot \frac{e}{2m} J$$

m: magnetic moment

g: g-factor

e: charge

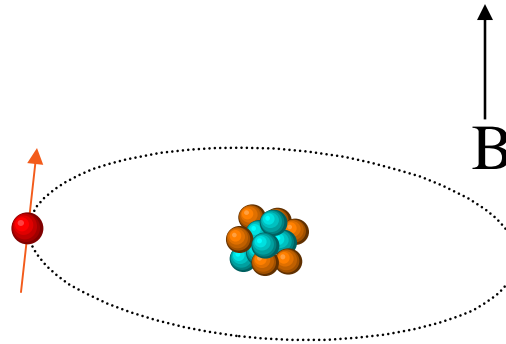
m: mass

J: angular momentum

g-Factor of the electron bound in a hydrogen-like ion

Larmor precession
frequency of the
bound electron:

$$\omega_L^e = \frac{g_J}{2} \frac{e}{m_e} B$$



Ion cyclotron frequency:

$$\omega_c^{ion} = \frac{Q}{M_{ion}} B$$

$$g_J = 2 \cdot \frac{\omega_L^e}{\omega_c^{ion}} \cdot \frac{m_e}{M_{ion}} \cdot \frac{Q^{ion}}{e}$$

→ 'experimental
g-factor'
→ comparison
with theory

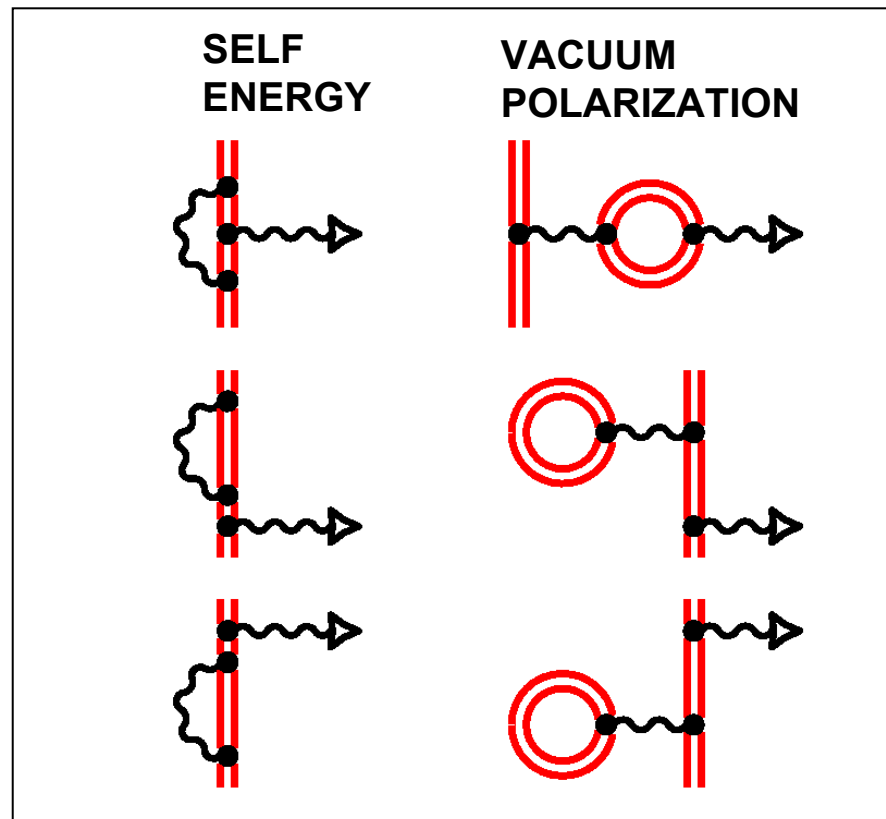
our external input
measurement parameter

Bound-electron g-factor: Feynman graphs 1st order in α/π

$$g_{\text{bound}}/g_{\text{free}} \approx 1 - (Z\alpha)^2/3 + \alpha(Z\alpha)^2/4\pi + \dots$$

Dirac theory

bound-state QED

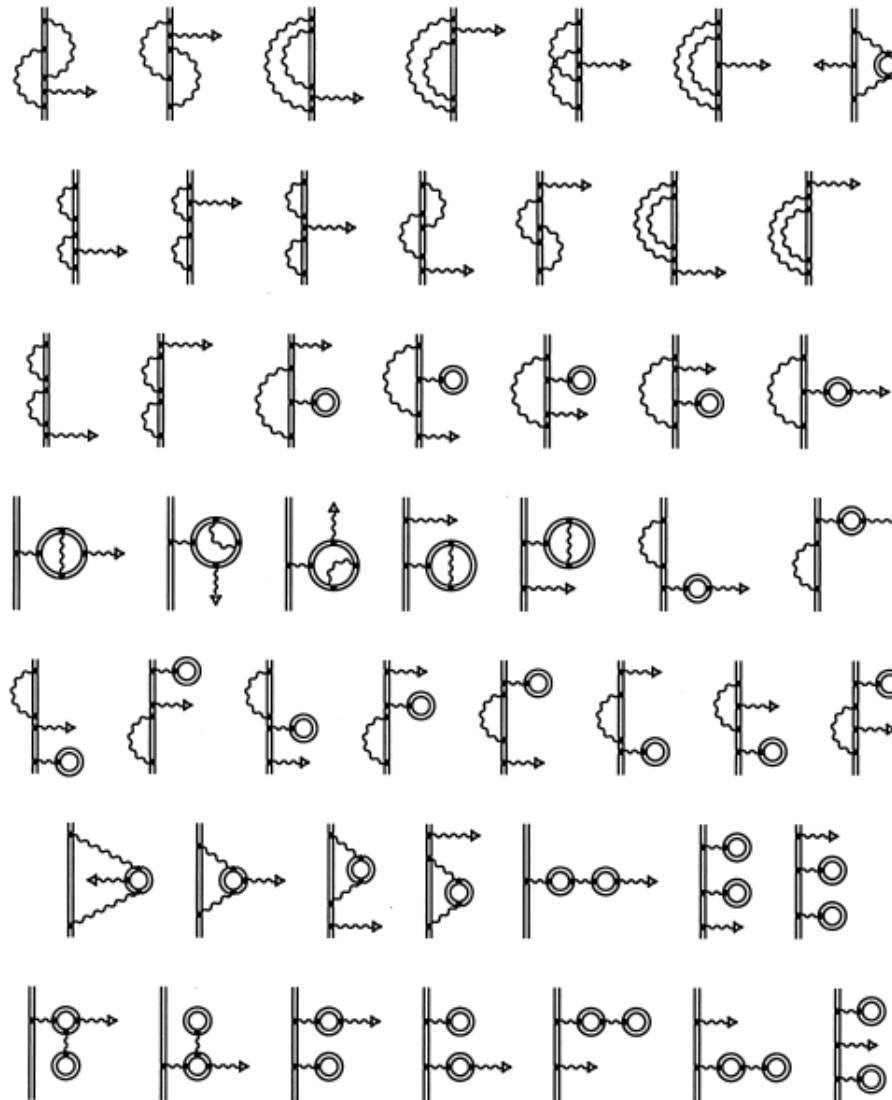


Ref.:

T. Beier, Physics Reports 339, 79 (2000)

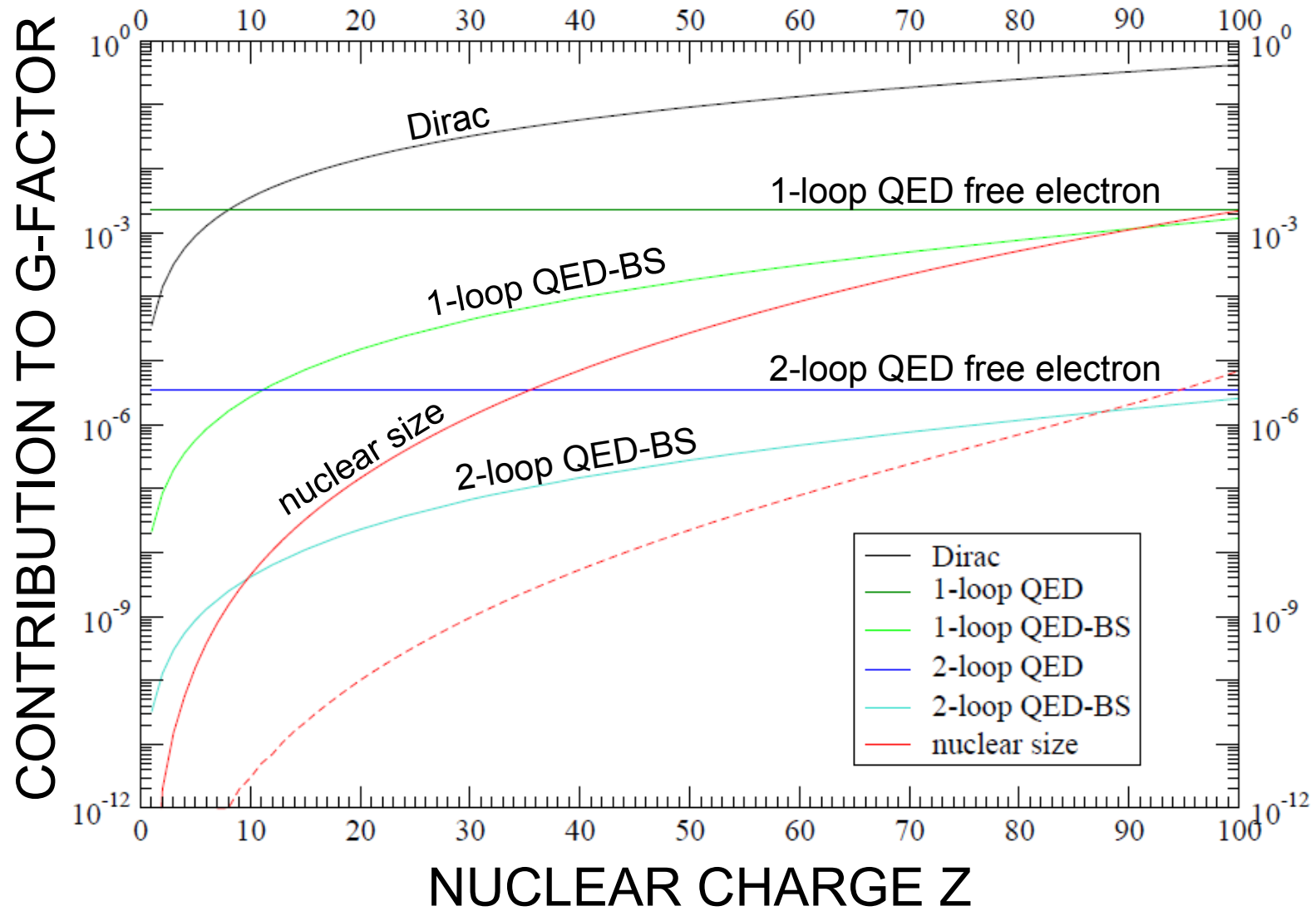
Bound-electron g-factor: Feynman graphs 2nd order in α/π

50 graphs



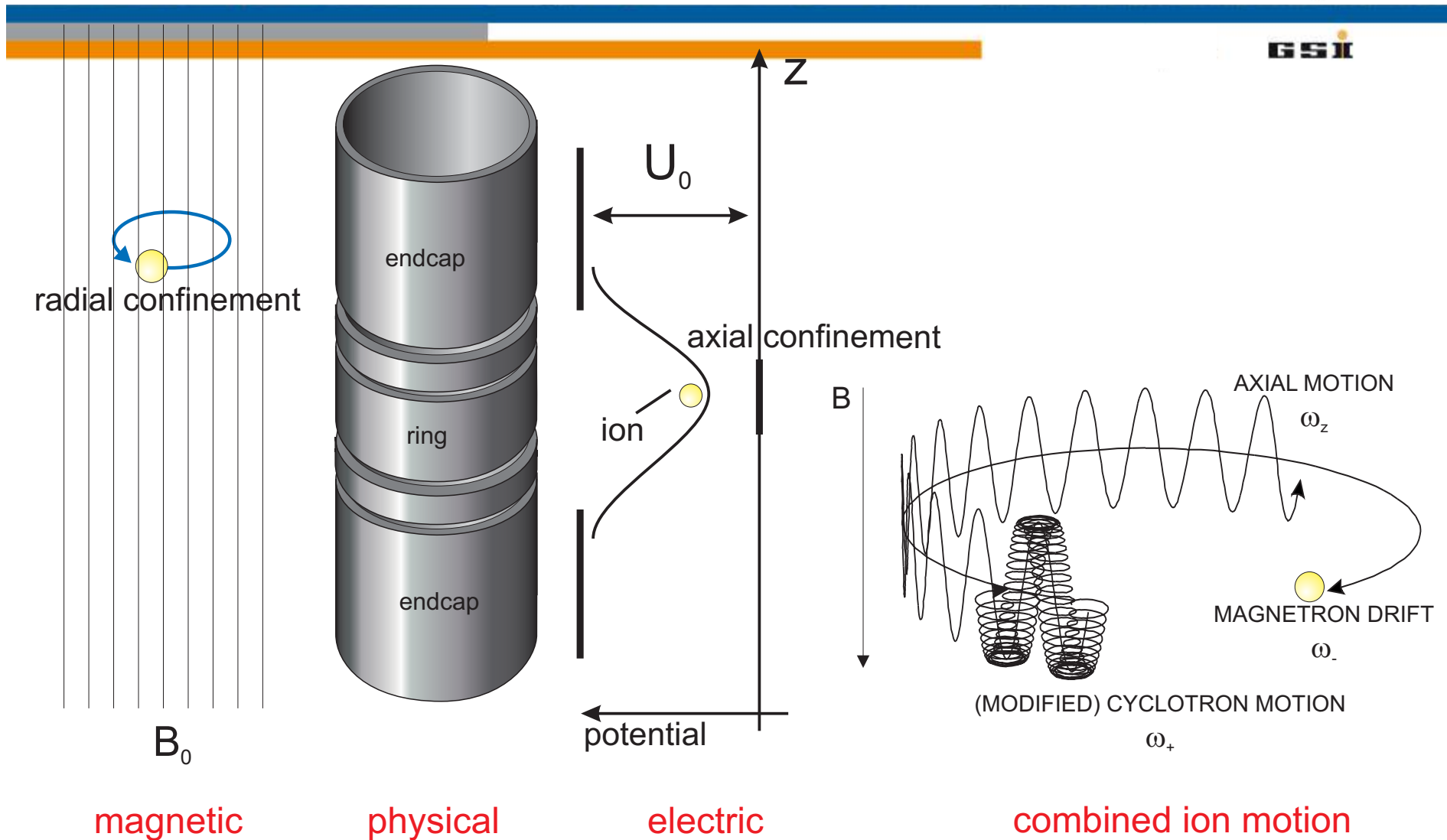
Ref.:
T. Beier, Physics Reports 339, 79 (2000)

Bound-electron g-factor

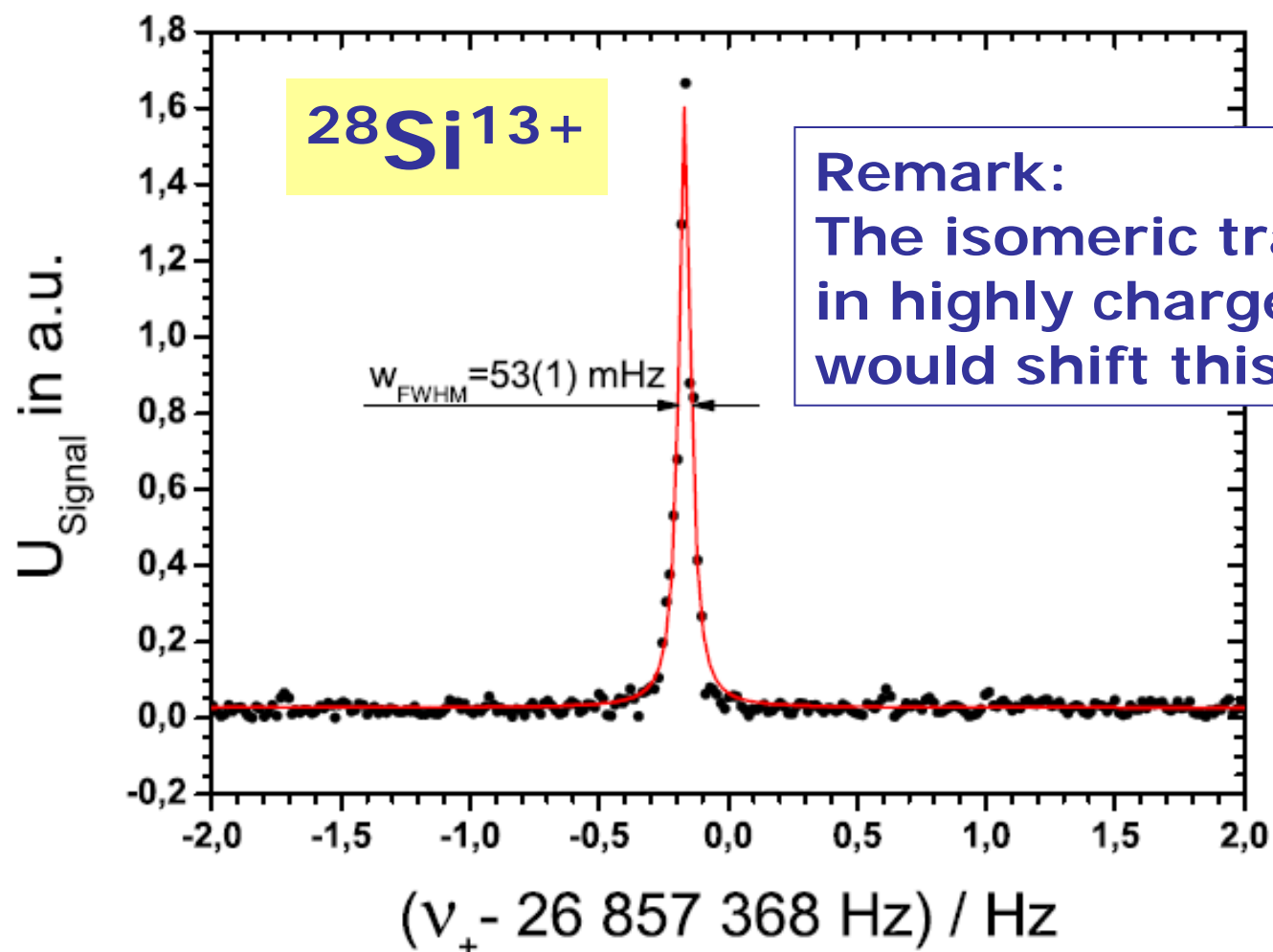


Ref.:
D. Glazov

A single HCl stored in a Penning trap



High-resolution cyclotron frequency measurement of a single highly charged silicon ion by Schottky detection

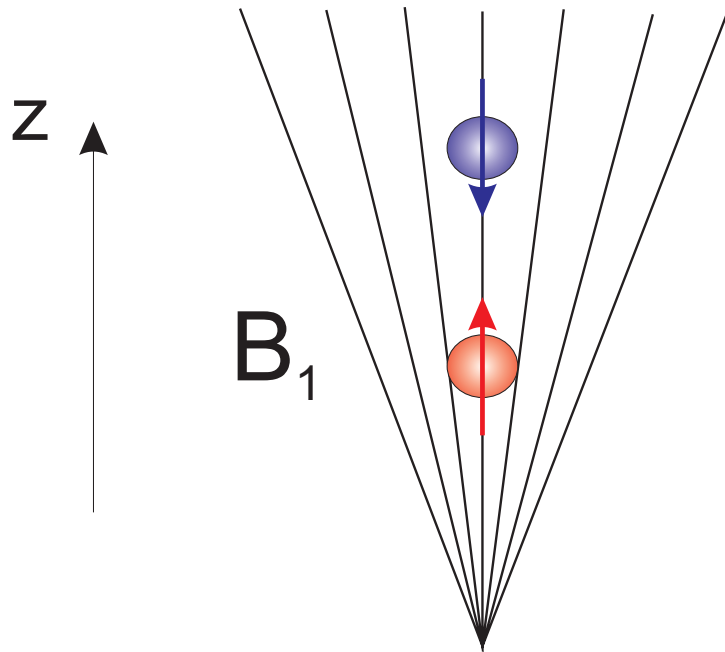


Ref.:
Birgit Schabinger, Sven Sturm, Anke Wagner

Continuous Stern-Gerlach effect: Determination of spin direction

CLASSICAL STERN-GERLACH

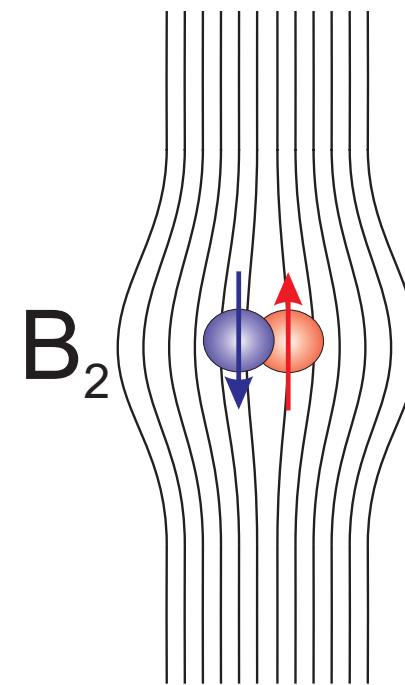
SEPARATION IN POSITION SPACE



$$\Delta z = \frac{\mu L^2}{2KE} B_1$$

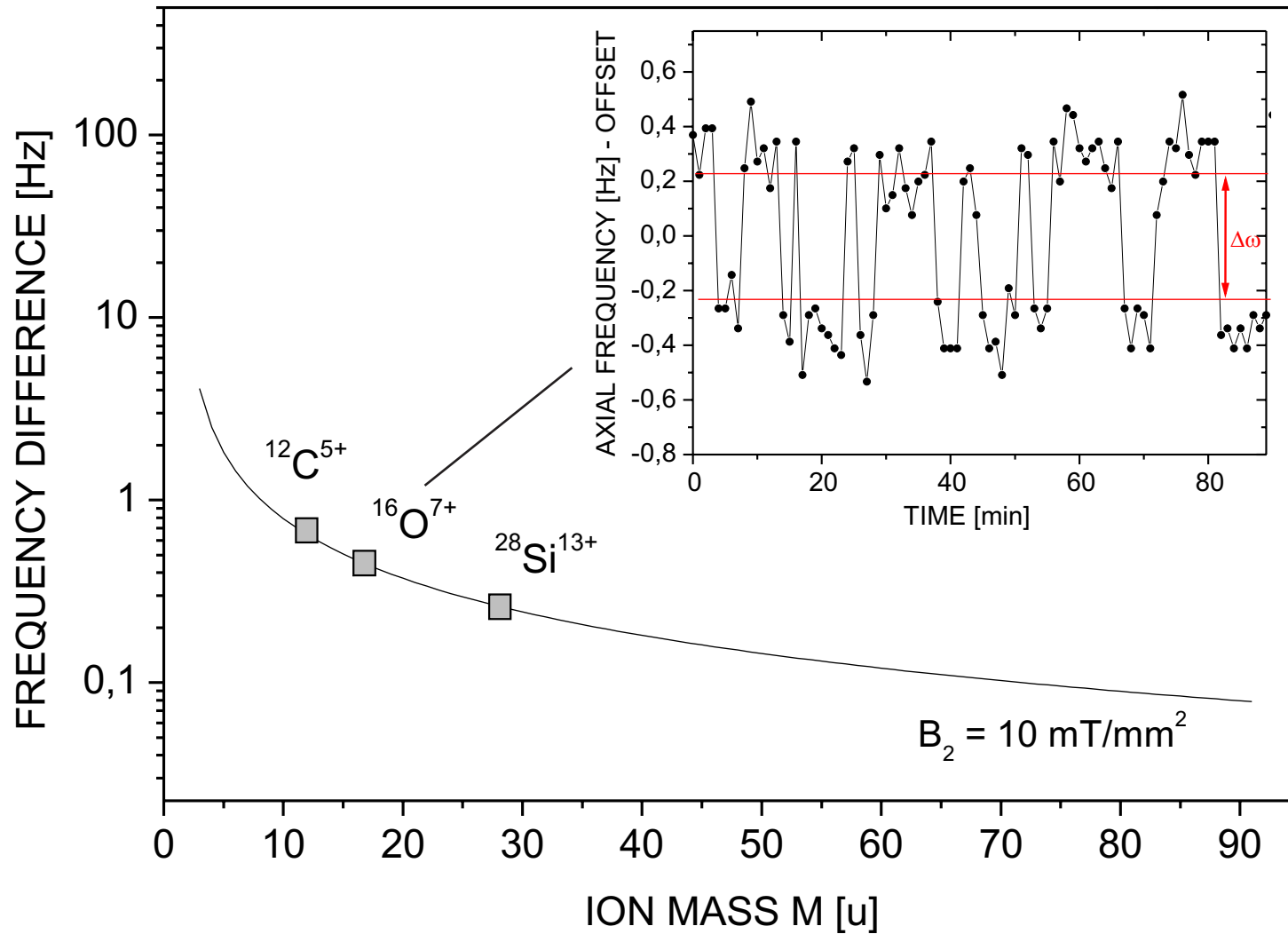
CONTINUOUS STERN-GERLACH

SEPARATION IN FREQUENCY SPACE



$$\Delta \omega_z = \frac{\mu}{m \omega_z} B_2$$

Quantum jumps of a single HCl in a Penning trap



Bound electron magnetic moment measurement on hydrogen-like silicon $^{28}\text{Si}^{13+}$

g Factor of Hydrogenlike $^{28}\text{Si}^{13+}$

S. Sturm,^{1,2} A. Wagner,¹ B. Schabinger,^{1,2} J. Zatorski,¹ Z. Harman,^{1,3} W. Quint,⁴ G. Werth,² C. H. Keitel,¹ and K. Blaum¹

¹Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany

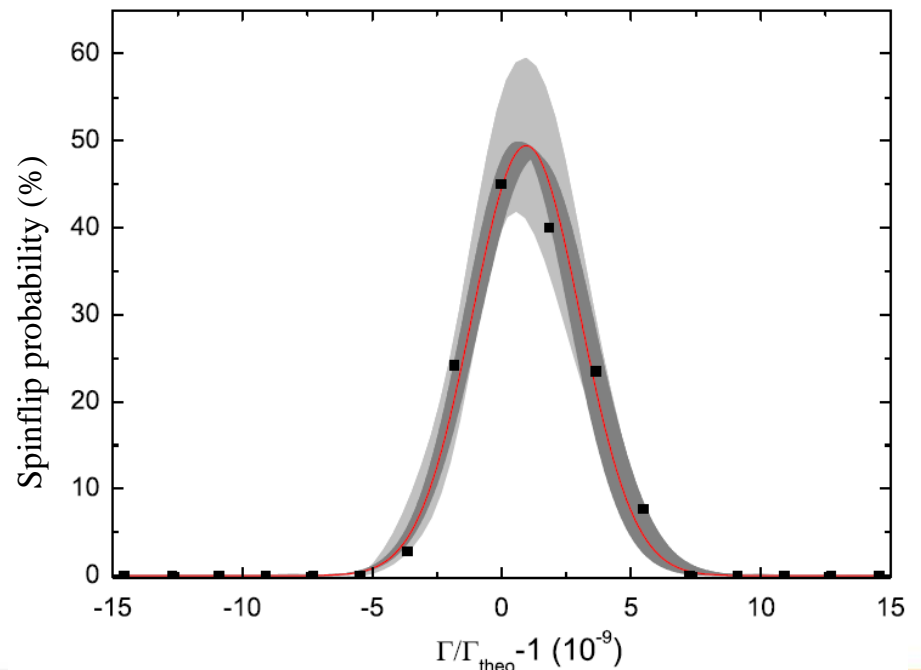
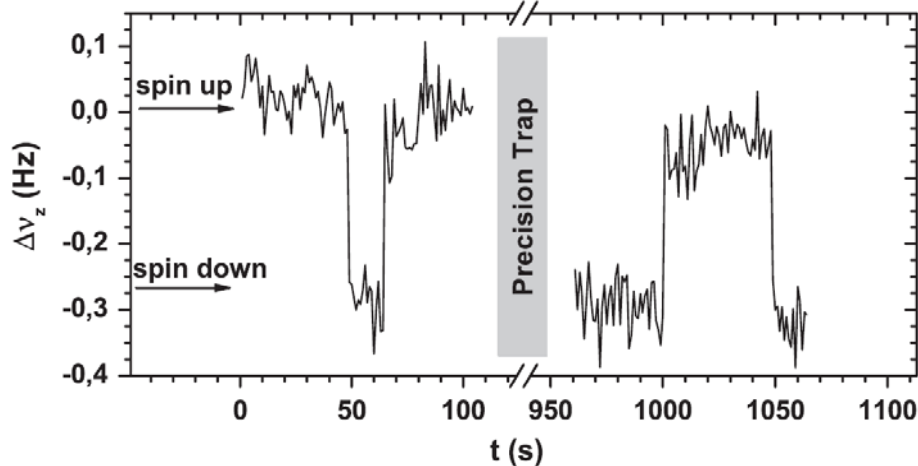
²Institut für Physik, Johannes Gutenberg-Universität, 55099 Mainz, Germany

³ExtreMe Matter Institute EMMI, Planckstraße 1, 64291 Darmstadt, Germany

⁴GSI Helmholtzzentrum für Schwerionenforschung GmbH, Planckstraße 1, 64291 Darmstadt, Germany

(Received 6 May 2011; published 7 July 2011)

We determined the experimental value of the g factor of the electron bound in hydrogenlike $^{28}\text{Si}^{13+}$ by using a single ion confined in a cylindrical Penning trap. From the ratio of the ion's cyclotron frequency and the induced spin flip frequency, we obtain $g = 1.995\,348\,958\,7(5)(3)(8)$. It is in excellent agreement with the state-of-the-art theoretical value of $1.995\,348\,958\,0(17)$, which includes QED contributions up to the two-loop level of the order of $(Z\alpha)^2$ and $(Z\alpha)^4$ and represents a stringent test of bound-state quantum electrodynamics calculations.



Comparison of theory and experiment: g-Factor of the bound electron in H-like carbon $^{12}\text{C}^{5+}$, oxygen $^{16}\text{O}^{7+}$ and silicon $^{28}\text{Si}^{13+}$

$$g_J(^{12}\text{C}^{5+}) = 2.001\,041\,590\,18\,(3) \text{ theoretical value}$$
$$g_J(^{12}\text{C}^{5+}) = 2.001\,041\,596\,4\,(10)(44) \text{ our measurement}$$

$$g_J(^{16}\text{O}^{7+}) = 2.000\,047\,020\,32\,(11) \text{ theoretical value}$$
$$g_J(^{16}\text{O}^{7+}) = 2.000\,047\,025\,4\,(15)(44) \text{ our measurement}$$

$$g_J(^{28}\text{Si}^{13+}) = 1.995\,348\,958\,0\,(17) \text{ theoretical value}$$
$$g_J(^{28}\text{Si}^{13+}) = 1.995\,348\,958\,7\,(5)(3)(8) \text{ our measurement}$$

Lit.:

T. Beier et al., PRL 88, 011603 (2002)

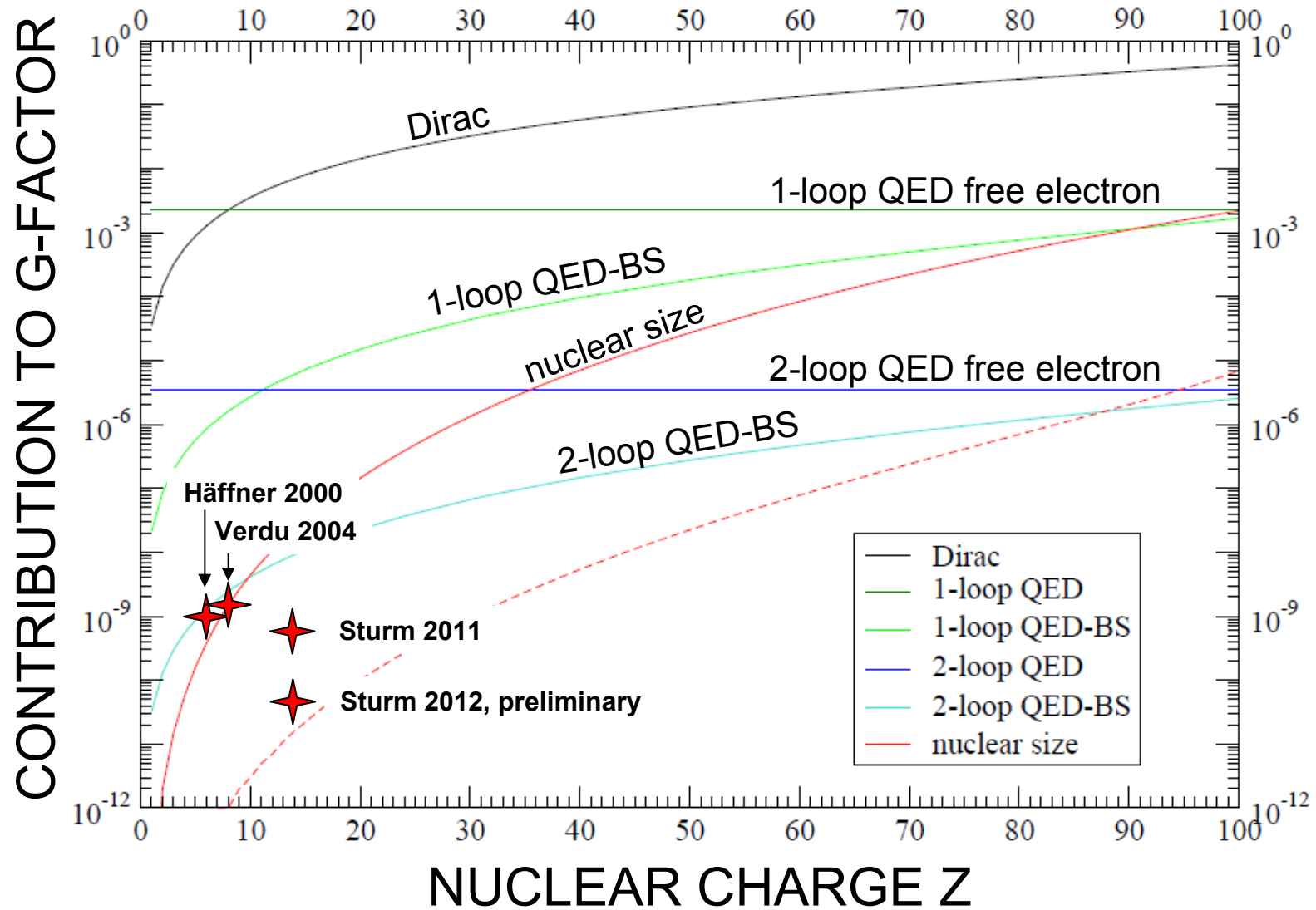
V. Shabaev et al., PRL 88, 091801 (2002)

V. Yerokhin et al., PRL 89, 143001 (2002)

K. Pachucki, V. Yerokhin et al., PRA 72, 022108 (2005)

S. Sturm et al., PRL 107, 023002 (2011)

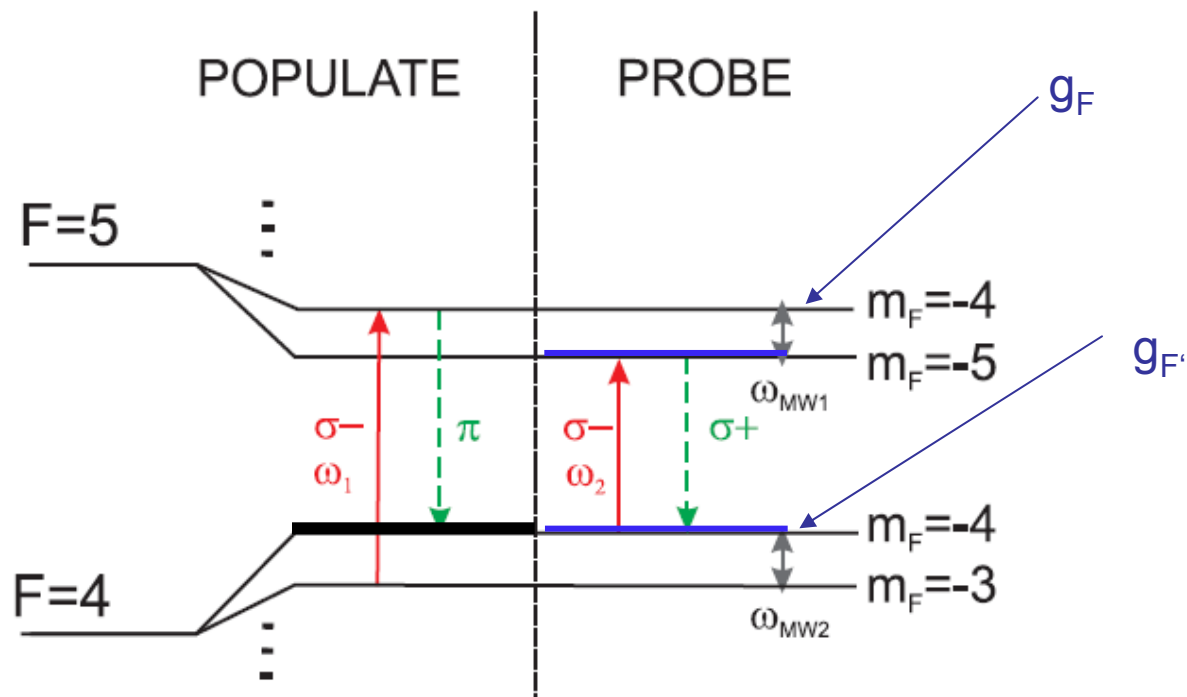
Bound-electron g-factor



Ref.:
D. Glazov

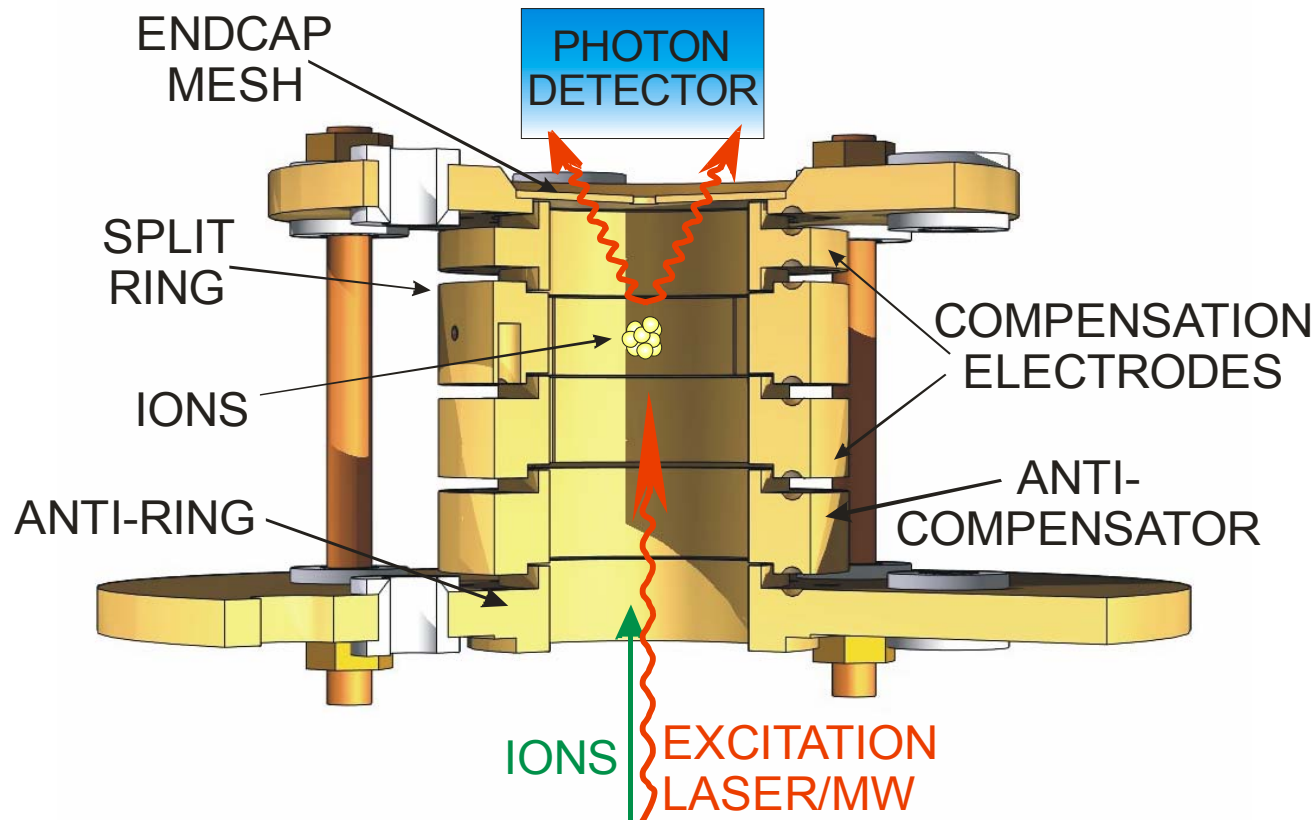
Laser-microwave double resonance spectroscopy for bound electron g-factor measurements in $^{209}\text{Bi}^{82+}$

idea:
use the light from the optical transition
as a probe for the Zeeman transitions



Alternative to quantum jump spectroscopy
by continuous Stern-Gerlach effect

Half-open Penning trap for laser-microwave double resonance spectroscopy: ARTEMIS



Ref.:
David von Lindenfels, Marco Wiesel, Manuel Vogel

Determination of electron g-factor g_J and nuclear g-factor g_I from two g_F -factors (thanks to Moskovkin, Shabaev)

if g_F is measured for two different F levels,
then we can **simultaneously and independently** get

$$g_J = (I + 1)g_{F'} - Ig_F - \delta_Q Q \left(\frac{m_e c}{\hbar} \right)^2 \frac{2(I + 1)}{2I - 1}$$

theoretical uncertainty: 1.5×10^{-10}

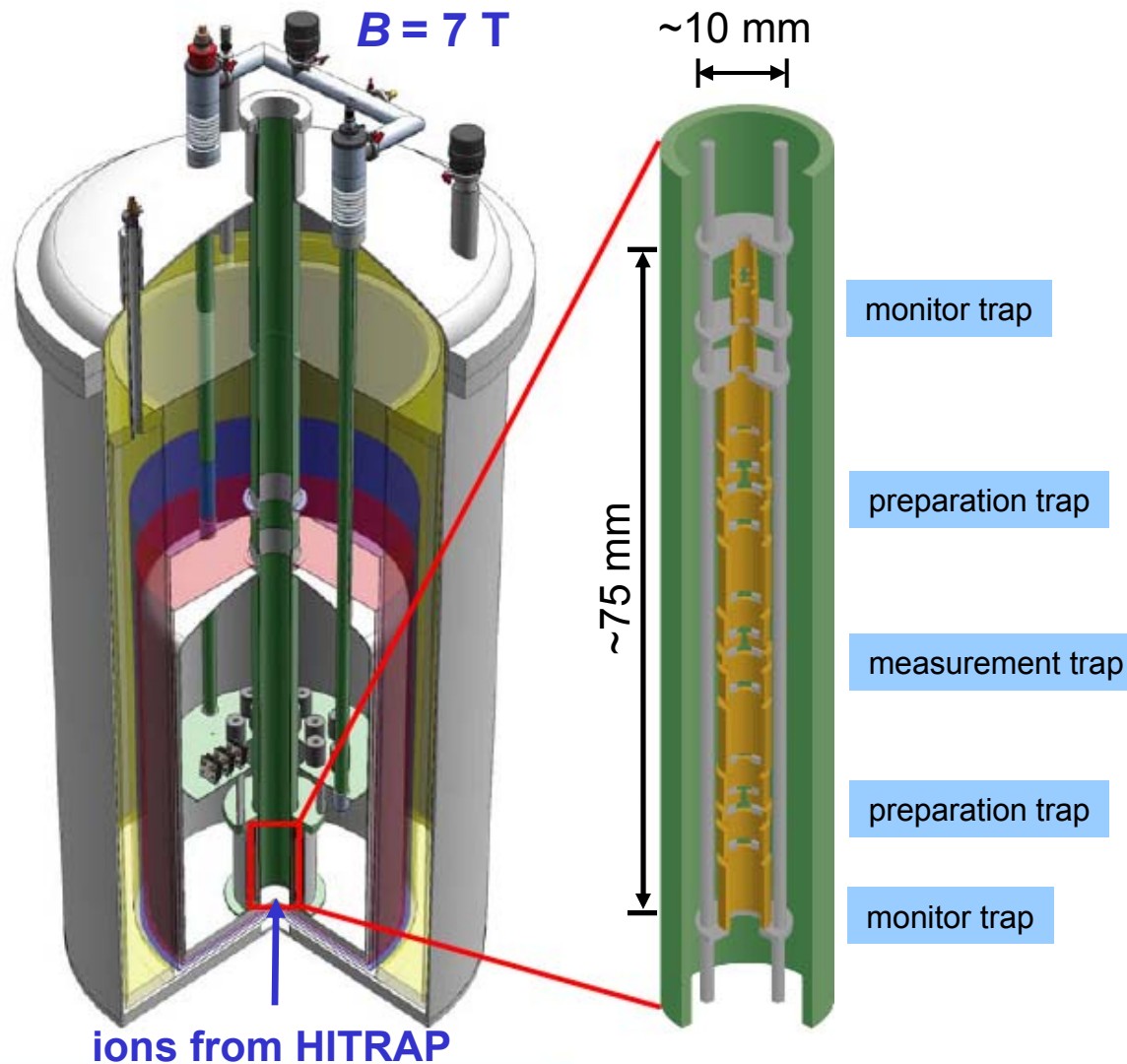
$$g_I = -\frac{m_p}{m_e} \frac{g_{F'} + g_F + \delta_Q Q \left(\frac{m_e c}{\hbar} \right)^2 \frac{3}{I(2I-1)}}{2(1 - \delta_\mu)}$$

Remark:

We are **independent of diamagnetic shielding**,
i.e. shielding effects can for the first time be measured
and theory can be tested.

High-accuracy mass measurements with heavy HCl

PENTATRAP: novel five-fold Penning trap mass spectrometer



- measurement of cyclotron frequency in different charge states
- determination of atomic and nuclear binding energies

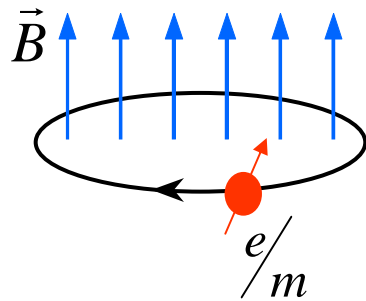
$\delta m/m < 1 \cdot 10^{-11} \rightarrow$
 $\delta mc^2 \approx 2\text{ eV} \rightarrow$
'weighing' of Lamb shift
or isomeric excitation
energy

Ref.:
MPIK Heidelberg, Klaus Blaum

Determination of the proton g-factor

$$\omega_c = \frac{e}{m_p} B$$

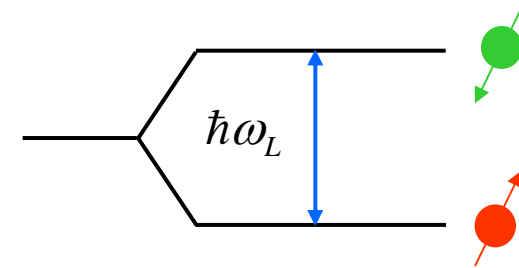
Cyclotron frequency



$$g = 2 \frac{\omega_L}{\omega_c}$$

$$\omega_L = g \frac{e}{2m_p} B$$

Larmor frequency

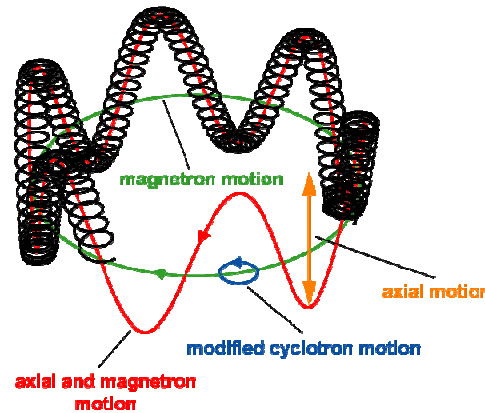


$$\omega_c = \sqrt{\omega_+^2 + \omega_-^2 + \omega_z^2}$$

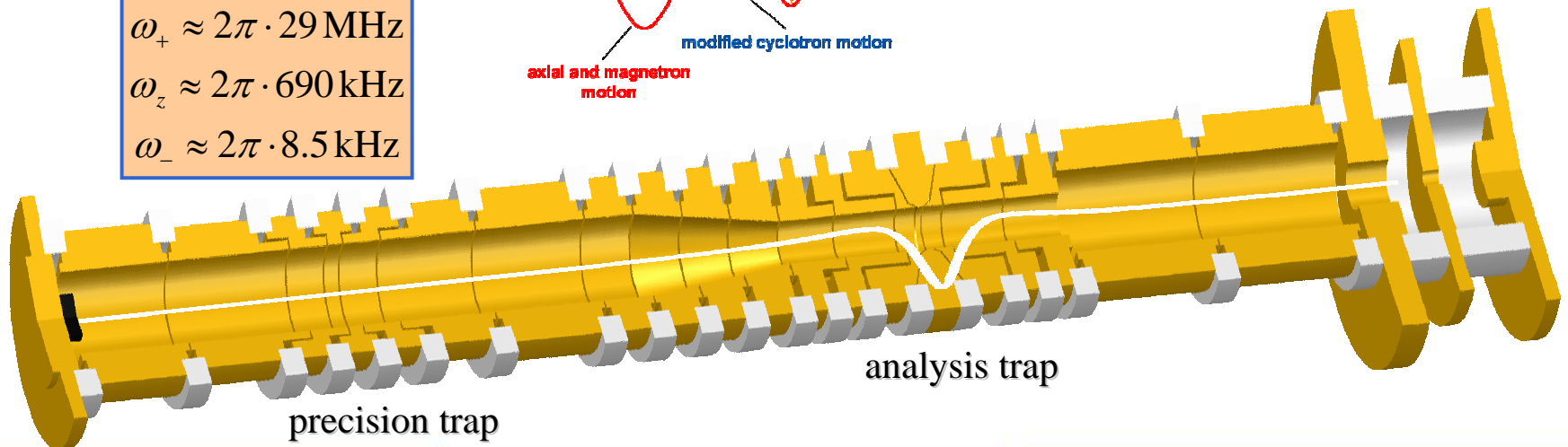
$$\omega_+ \approx 2\pi \cdot 29 \text{ MHz}$$

$$\omega_z \approx 2\pi \cdot 690 \text{ kHz}$$

$$\omega_- \approx 2\pi \cdot 8.5 \text{ kHz}$$



$$\omega'_z(\uparrow) - \omega'_z(\downarrow) = \Delta\omega_z$$



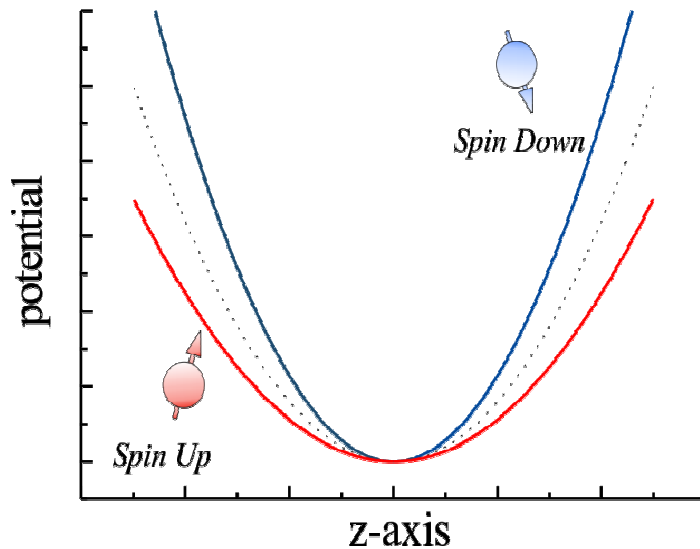
A single trapped proton and the continuous Stern-Gerlach effect

axial frequency shift
due to spinflip:

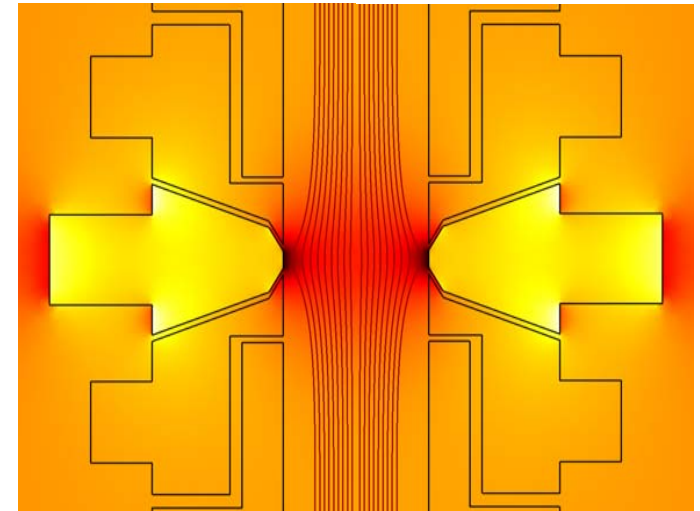
$$\Delta\nu_z \approx \frac{1}{2\pi^2} \frac{\mu_z B_2}{m\nu_z}$$



Proton measurement is 10 000 times harder compared to electron g-2 measurement.



$$B_2 = 0.3 \text{ T/mm}^2$$
$$\Delta\nu_z = 190 \text{ mHz}$$



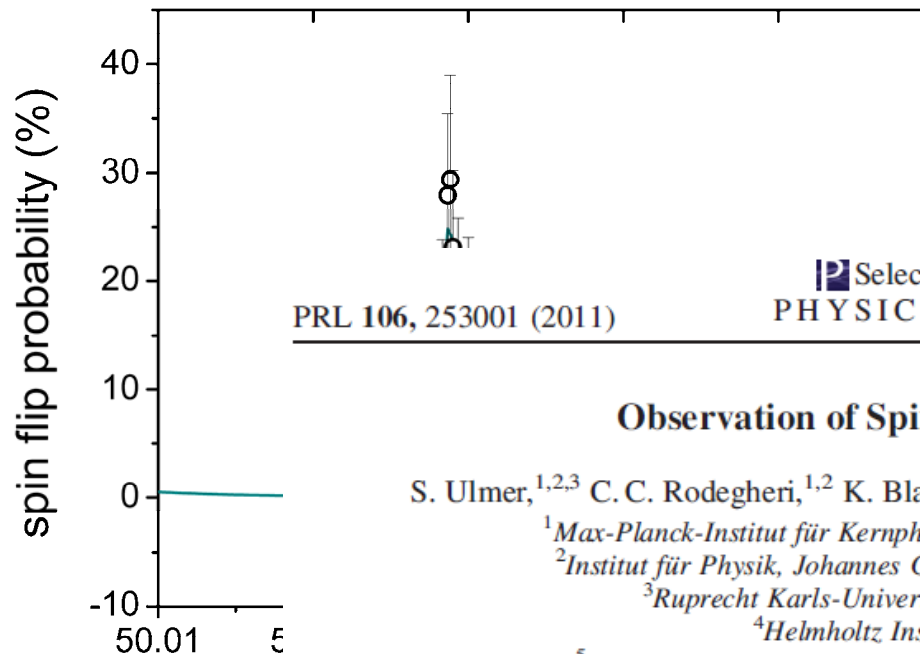
First Larmor resonance curve of a single proton in the Penning trap

- ✓ Axial temperature reduced
- ✓ Larmor resonance narrower

$$\frac{\Delta \nu_L}{\nu_L} = 1.2 \cdot 10^{-6}$$

$$g = 2 \frac{\nu_L}{\nu_c}$$

GSI



Next steps:

- Reduce axial frequency fluctuations further

PRL 106, 253001 (2011)

Selected for a Viewpoint in *Physics*
PHYSICAL REVIEW LETTERS

week ending
24 JUNE 2011

Observation of Spin Flips with a Single Trapped Proton

S. Ulmer,^{1,2,3} C. C. Rodegheri,^{1,2} K. Blaum,^{1,3} H. Kracke,^{2,4} A. Mooser,^{2,4} W. Quint,^{3,5} and J. Walz^{2,4}

¹Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, D-69117 Heidelberg, Germany

²Institut für Physik, Johannes Gutenberg-Universität Mainz, D-55099 Mainz, Germany

³Ruprecht Karls-Universität Heidelberg, D-69047 Heidelberg, Germany

⁴Helmholtz Institut Mainz, D-55099 Mainz, Germany

⁵GSI—Helmholtzzentrum für Schwerionenforschung, D-64291 Darmstadt, Germany

(Received 28 February 2011; published 20 June 2011)

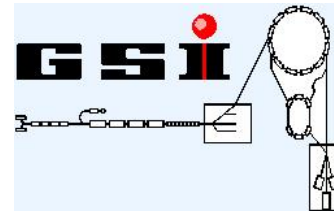
Radio-frequency induced spin transitions of one individual proton are observed. The spin quantum jumps are detected via the continuous Stern-Gerlach effect, which is used in an experiment with a single proton stored in a cryogenic Penning trap. This is an important milestone towards a direct high-precision measurement of the magnetic moment of the proton and a new test of the matter-antimatter symmetry in the baryon sector.

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- ✓ Atomic Physics Division at GSI Darmstadt
- ✓ Group at the institute of physics - Mainz
- ✓ Group of at MPIK Heidelberg

JOHANNES
GUTENBERG
UNIVERSITÄT
MAINZ

Deutsche
Forschungsgemeinschaft
DFG



VH-NG-037



Thank you for your attention !