

“Solid-state nuclear clock”



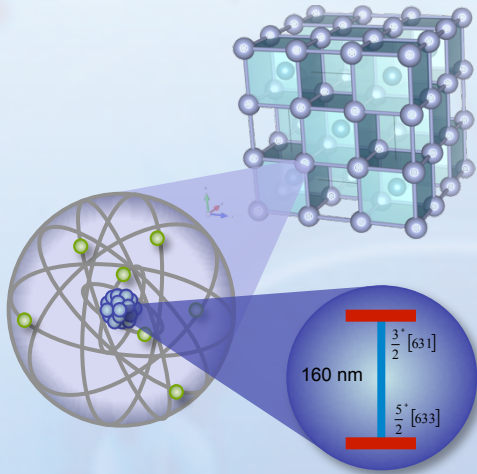
Thorsten Schumm

Institute for Atomic and Subatomic Physics

University of Technology, Vienna

www.thorium.at





Part 1 - A nuclear transition in a solid-state environment

- doping Thorium: microscopic configuration
- electronic structure calculations for Th-doped CaF_2
- quantum physics of the nucleus (in the crystal)

Part 2 - Consequences for a clock

- fluorescence interrogation scheme
- projected clock performance

Poster Kazakov

Part 3 - Experimental efforts

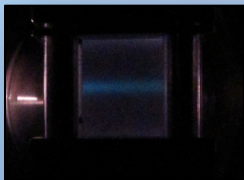
- ^{232}Th -doped CaF_2 crystals:
 - bulk characterization
 - transmission + luminescence

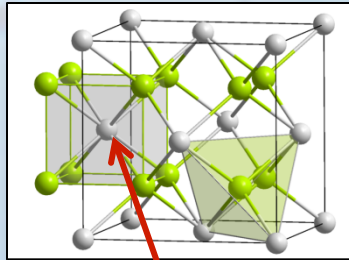


Part 4 - Conclusions and outlook

- Towards homegrown crystals
- Towards a UV frequency comb

Poster Schreitl
Poster Winkler





put ^{229}Th here!

^{229}Th replaces an Ca ion in a CaF_2 crystal

- a macroscopic (up to 10^{18}) number of nuclei for spectroscopy (clock)
- a UV transparent host matrix to hold them (line shifts/broadenings)

Pure CaF_2 properties:

- highest bandgap insulator (11.6 eV, VUV transparent)
- simple cubic lattice structure (can be calculated)
- „easy“ to grow (Czochralski, Bridgeman, MicroPulling)
- high damage threshold, well characterized...

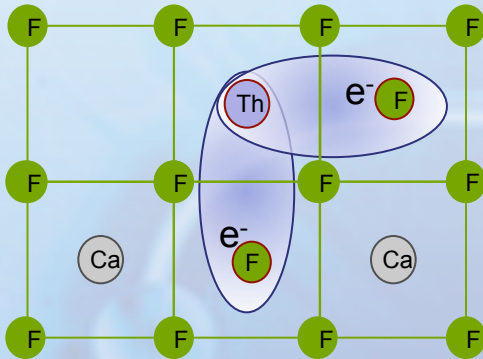
Thorium doping:

- Thorium chemically prefers 4+ state (Radon-like)
- 4+ ion instead of 2+ ion: needs **charge compensation**
- ...will break the symmetry + modify electronic structure

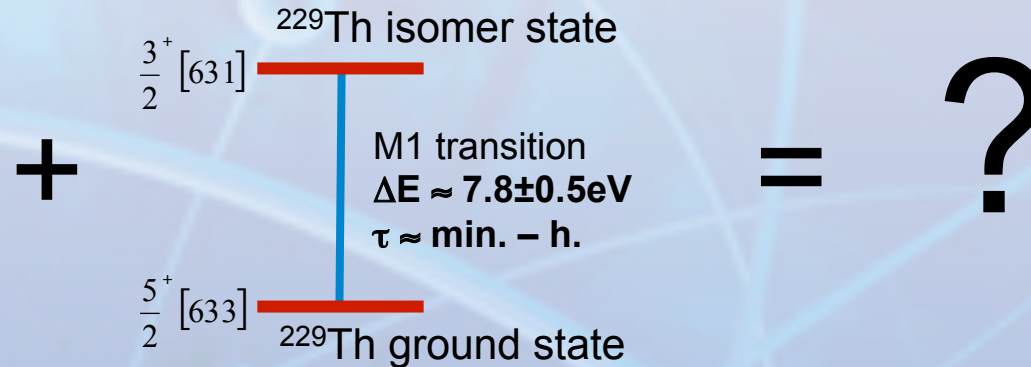
2 main questions (...in this talk):

- Will Thorium-doping change the crystal properties (e.g. transparency)?
- What will be the effects of the crystal on the nuclear transition (clock performance)?

Solid-state system



Nuclear system



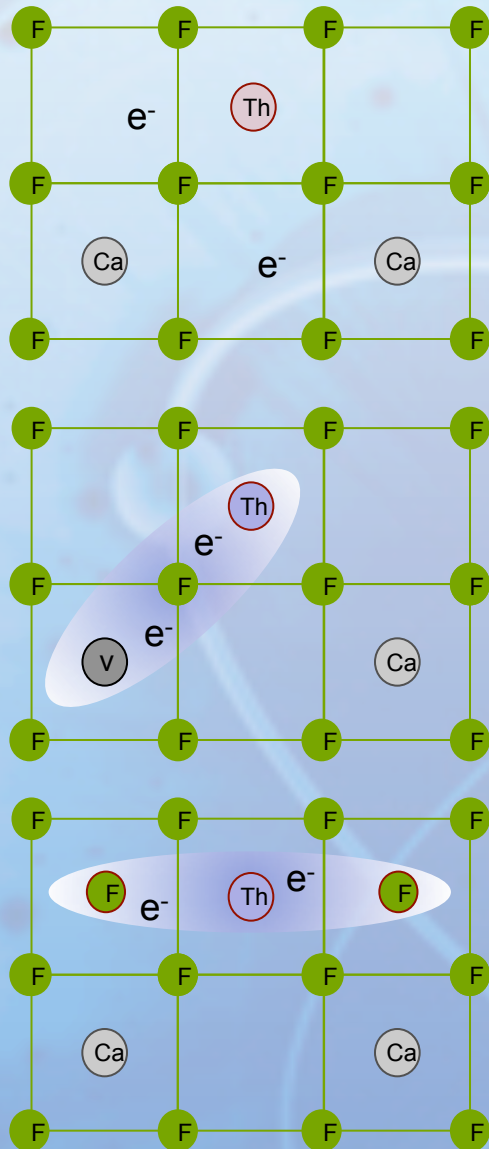
Step 1: Determine charge compensation mechanism

„Atomistic“ simulations based on GULP code (R. Jackson, Keele Univ.)

Step 2: Determine electronic structure of doping complex

DFT calculations based on VASP code (P. Mohn, CMS, Vienna)

Step 3: Quantum physics of the nuclear states → **clock performance?**



Charge compensation mechanisms

Possible candidates:

- 2 x F-interstitial (many spatial combinations)
- Ca vacancy (nearest Ca)
- (impurity compensation, e.g. O₂)

Calculate solution Energies using GULP code

Example: Ca vacancy (only one possibility):

$$E_{sol} = -E_{latt}(ThF_4) + E(Th_{Ca}^{**}) + E(V_{Ca}^{\prime\prime}) + 2E_{latt}(CaF_2)$$

energy to „melt“
ThF₄

energy to
replace Ca
with Th

energy to
remove
one Ca

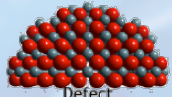
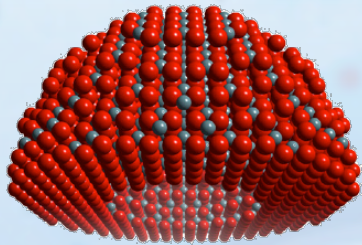
binding
energy of
CaF₂

How it is done (Rob Jackson, Keele University)

- Model ion interactions with (classical) **Buckingham potential**

$$V_{Buck}(r_{i,j}) = A_{i,j} \underbrace{\exp\left(-\frac{r_{i,j}}{\rho_{i,j}}\right)}_{\text{repulsive}} - \underbrace{\frac{C_{i,j}}{r_{i,j}^6}}_{\text{attractive}}$$

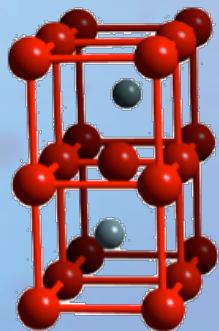
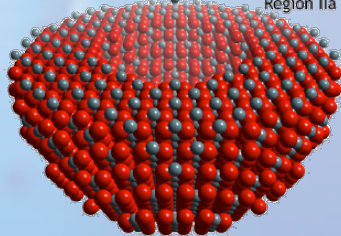
- Determine potential parameters by fitting the undoped structures (lattice spacing, dielectric properties, stress tensors...)
- Start with a given geometry
- Relax all ion positions in region 1 (scaling region 2)
- Determine solution energy for relaxed system
- search for configuration of the lowest solution energy...



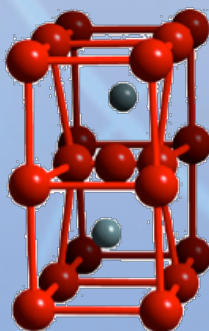
Defect

Region I

Region IIa



unrelaxed

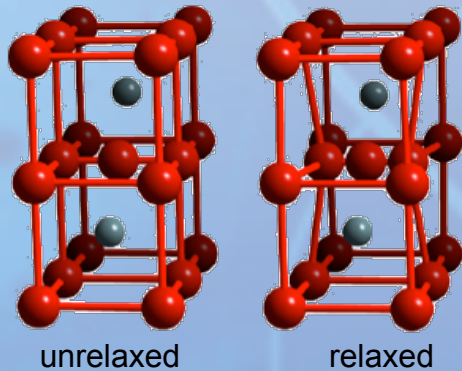
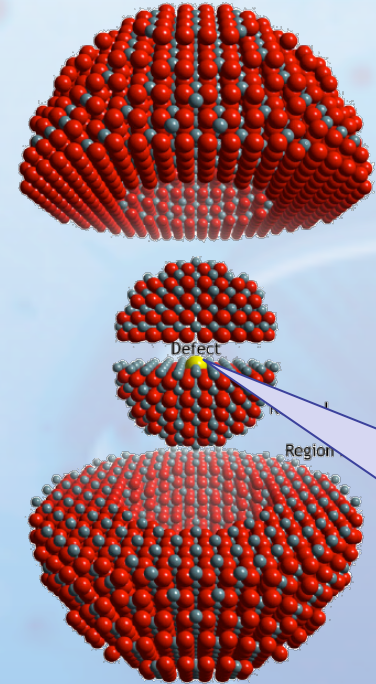


relaxed

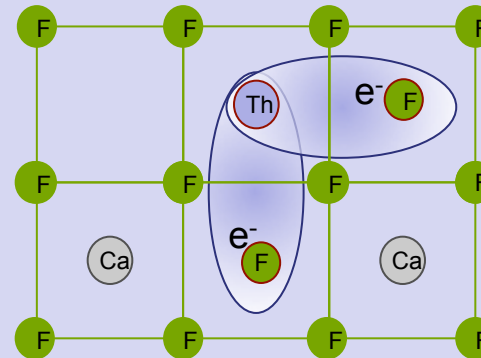
How it is done

- Model ion interactions with (classical) Buckingham potential

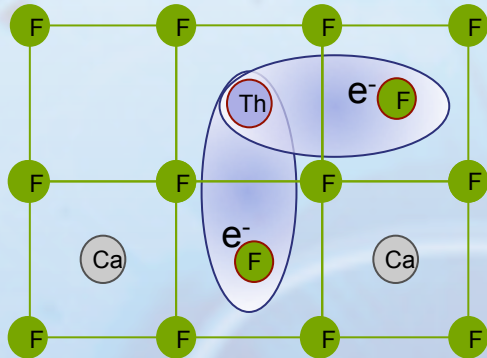
$$V_{Buck}(r_{i,j}) = A_{i,j} \underbrace{\exp\left(-\frac{r_{i,j}}{\rho_{i,j}}\right)}_{\text{repulsive}} - \underbrace{\frac{C_{i,j}}{r_{i,j}^6}}_{\text{attractive}}$$



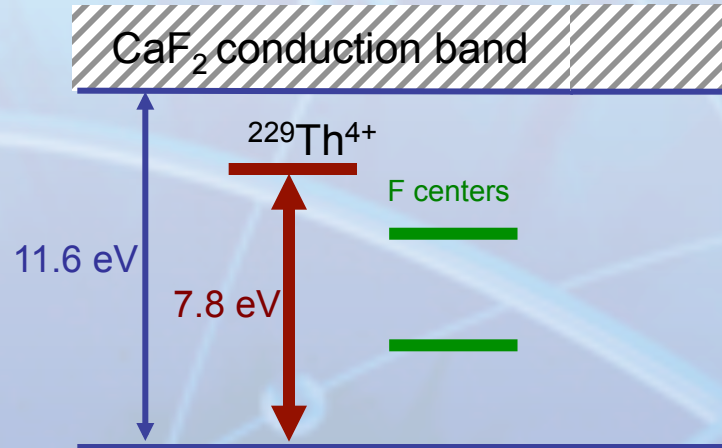
Result: System will go to a 90° F-interstitial compensation



(also confirmed by VASP calculations)



What about the electronic structure?

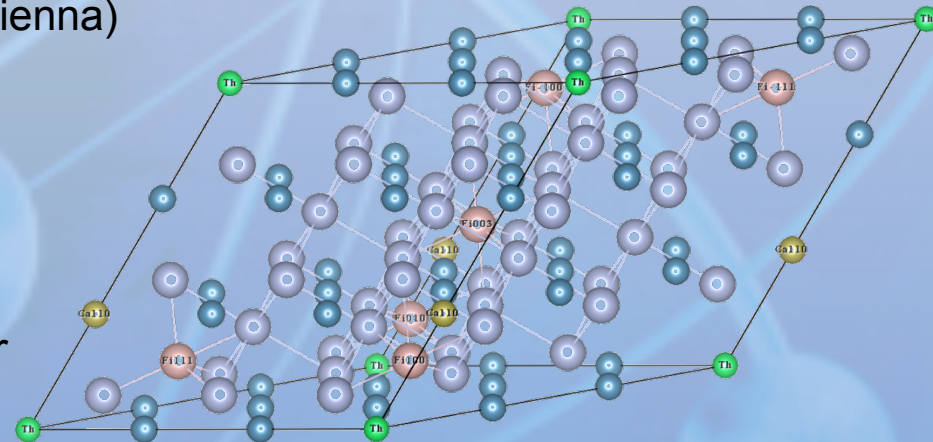


- new absorption levels?
- band gap shifts?
- effects of impurities?

Full electronic structure calculations using VASP code...

(collaboration with P. Mohn, P. Dessovic, CMS Vienna)

- 83 ions in „supercell“
- Full spatial relaxation
- 612 total electron orbitals
- 348 orbitals treated dynamically
- several weeks on large computer cluster

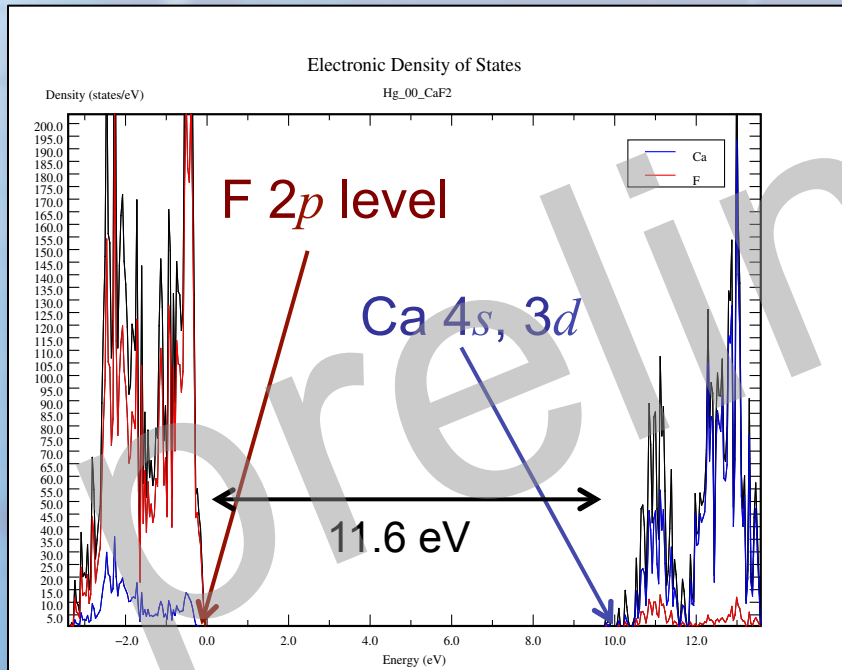


Results:

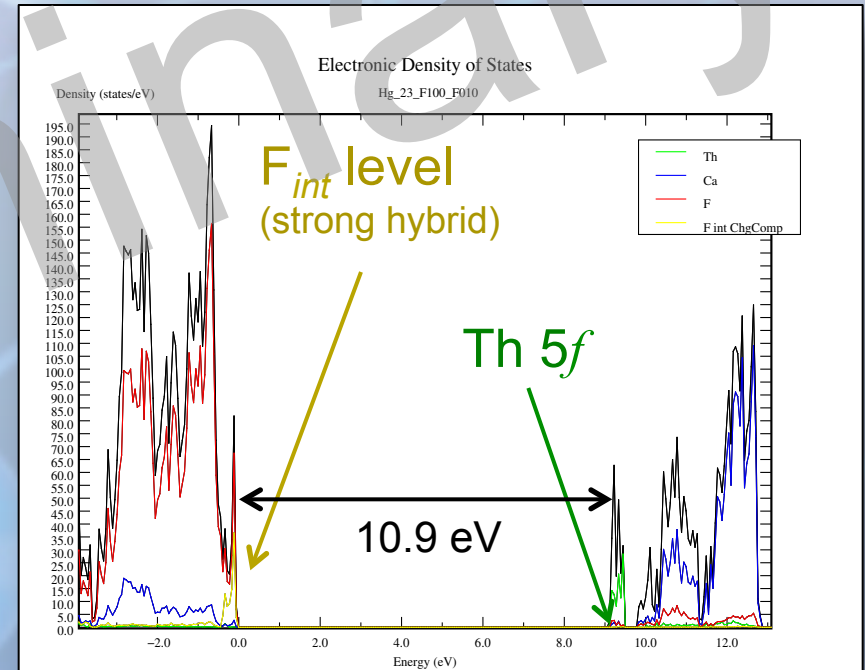
- Undoped CaF₂:
- **Th-doped CaF₂:**

large bandgap of 11.6 eV

slightly reduced bandgap 10.9 eV



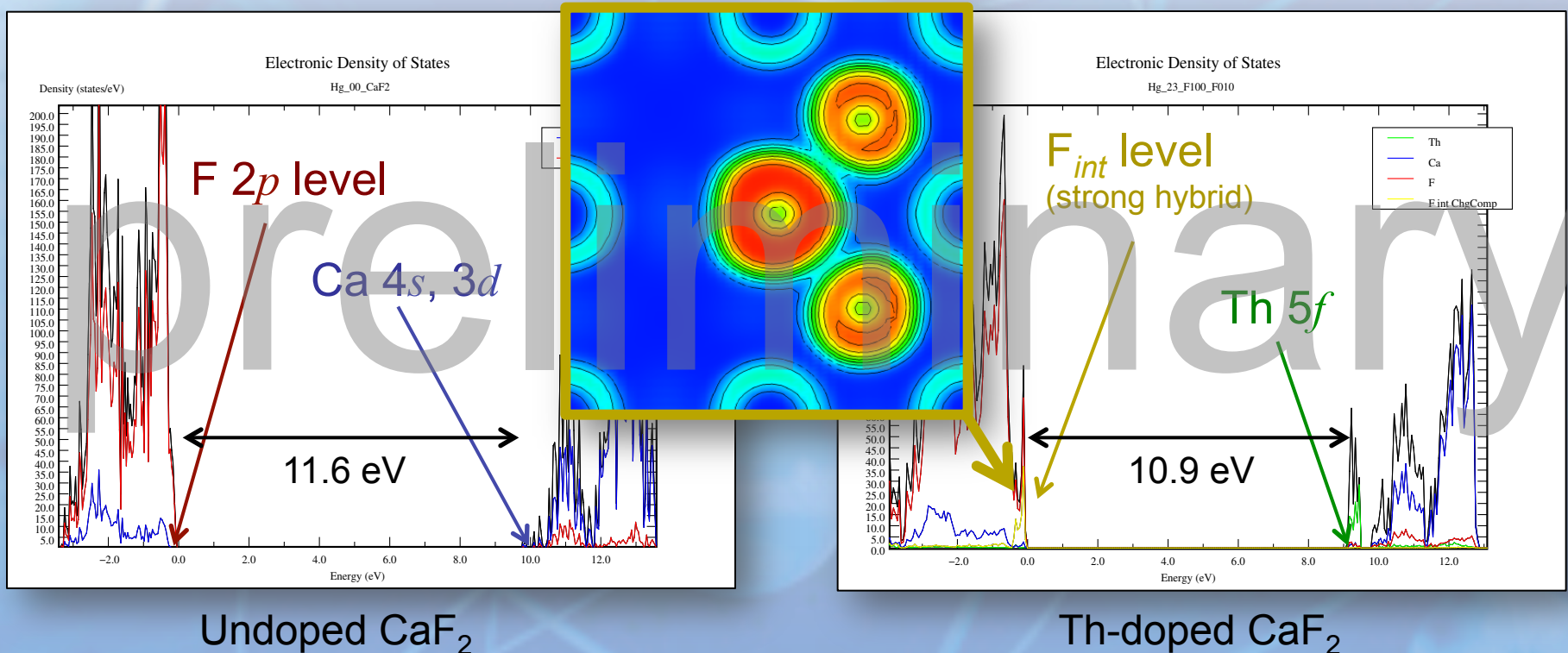
Undoped CaF₂



Th-doped CaF₂

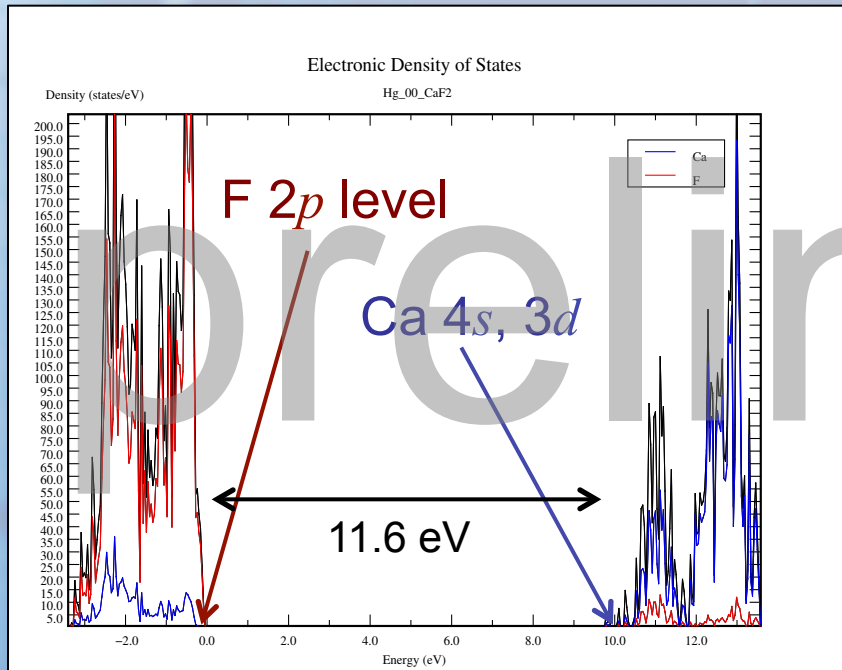
Results:

- Undoped CaF₂: large bandgap of 11.6 eV
- **Th-doped CaF₂:** **slightly reduced bandgap 10.9 eV** 😊
 - we also know the wave function at the fermi edge (field gradients)
 - input for calculations of the nuclear quantum levels...

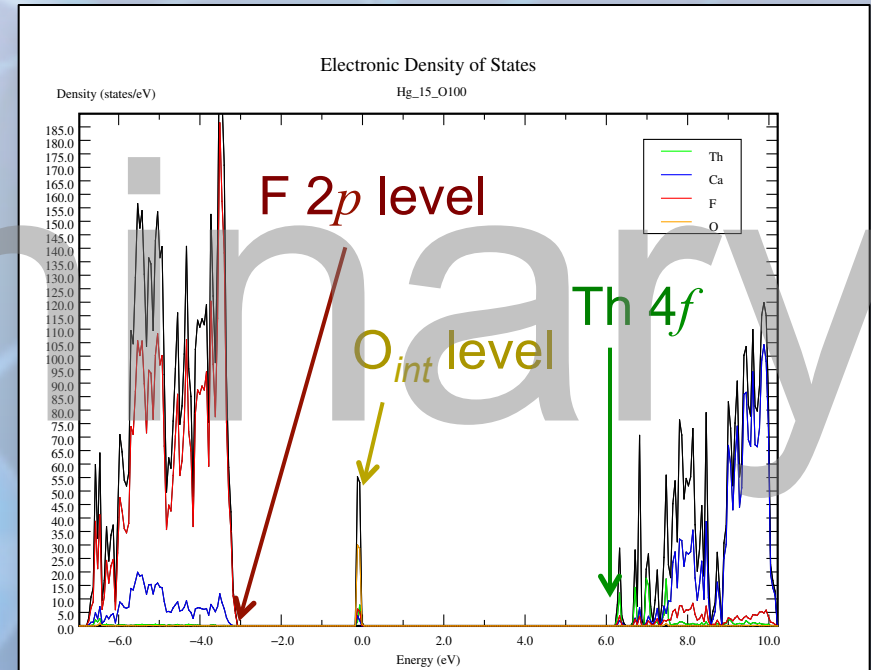


Results:

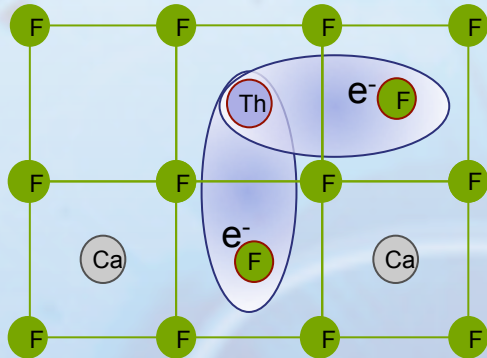
- Undoped CaF₂: large bandgap of 11.6 eV
- Th-doped CaF₂: slightly reduced bandgap 10.9 eV
- **O charge comp. in Th:CaF₂: kills transparency!** ☹️
(multi-step excitation via co-doping?)



Undoped CaF₂



Th-doped CaF₂ with O charge compensation



+

Nuclear-lattice interaction (via electronic states)

$$H = \cancel{H_{FS}} + H_{HFS}$$

no unpaired electrons
→ No fine interaction

$$H_{HFS} = H_{E0} + H_{M1} + H_{E2} + \dots$$

multipole expansion of the hyperfine interaction

H_{E0} : electric monopole shift (DC field at nucleus pos.)

- order GHz (exact calculation under way)
- identical for all Th ions up to temperature (≈ 10 kHz/K)

H_{E2} : electric quadrupole shift (gradient at nucleus pos.)

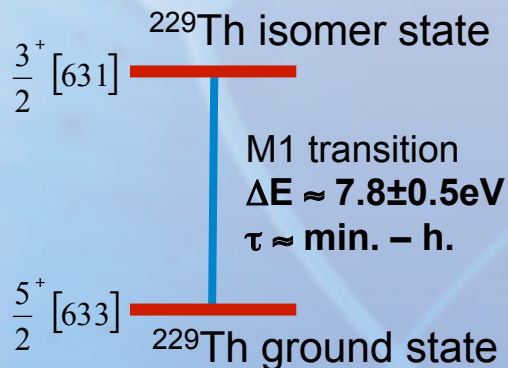
- 1.52×10^{18} V/cm² for calculated electronic structure
- gives splittings on order **100 MHz**
- inhom. broadening ≈ 100 Hz

H_{M1} : magnetic dipole interaction

- randomly oriented neighboring nuclei (F-ions, $2.63 \mu_N$)
- inhom. broadening $\approx 1 - 2$ kHz (dominant broadening)

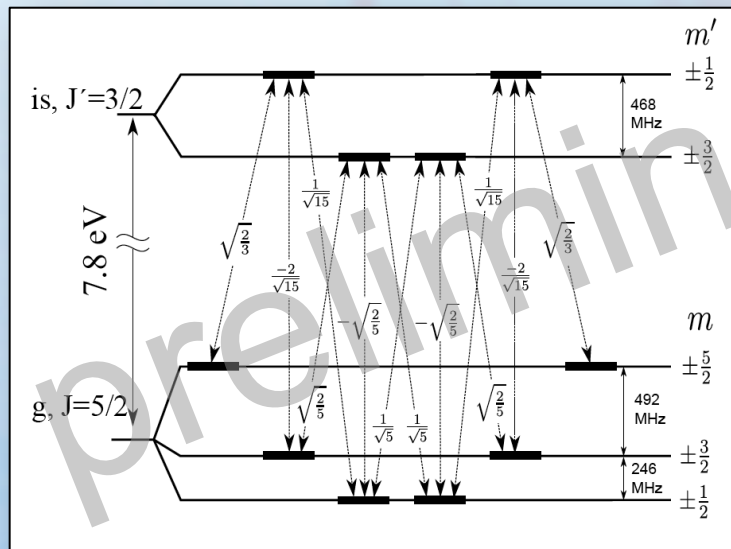
+ 2nd order Doppler effect

- global shift: 10 Hz/K (**700 Hz** at liquid Nitrogen)
- broadening: 7 Hz/K (**500 Hz** at liquid Nitrogen)



W.G. Rellergert, et al., Phys. Rev. Lett. 104, 200802 (2010)
Kazakov et al, New. J. Phys. 14, 083019 (2012)

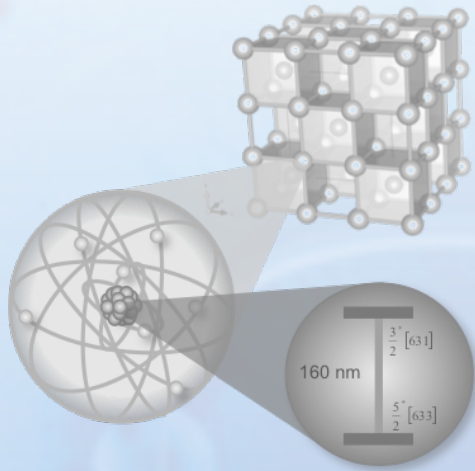
Quantum states of the nuclear transition inside the CaF₂ crystal



- **Global shift** due to electric monopole interaction (≈ 1 GHz, calculation under way)
 - **Hyperfine splitting** due to interaction with electron orbital of the charge compensation
 - **Broadening + dephasing** (≈ 1.5 kHz) due to magnetic interaction to nearby nuclei
- ➔ **expected ensemble linewidth: 1.5 kHz**

Consequences:

- Direct **nuclear spectroscopy seems feasible** in the solid-state approach (bandgap only slightly reduced by doping)
- Solid-state environment **reduces Q-factor to 1×10^{13}**
- Rapid dephasing (order ms) makes **„coherent“ interrogation schemes impossible!**



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Part 2 - Consequences for a clock

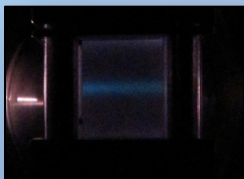
- fluorescence interrogation scheme
- projected clock performance

Poster Kazakov



Part 3 - Experimental efforts

- ^{232}Th -doped CaF_2 crystals:
 - bulk characterization
 - transmission + luminescence

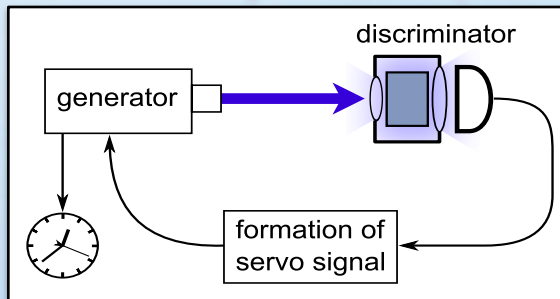


Part 4 - Conclusions and outlook

- Towards homegrown crystals
- Towards a UV frequency comb

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„Nuclear fluorescence spectroscopy“

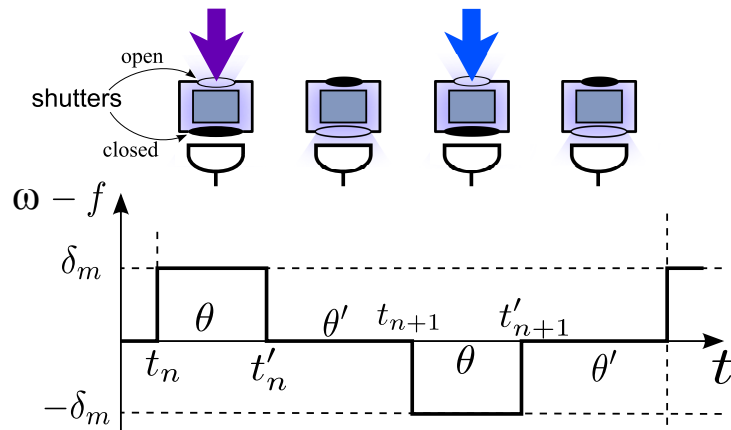


Problem: Coherence time ≈ 1 ms

→ We have to rely on spontaneous decay

Next problem: lifetime of nuclear state: $1/\gamma \approx 1000$ s

Clock interrogation scheme



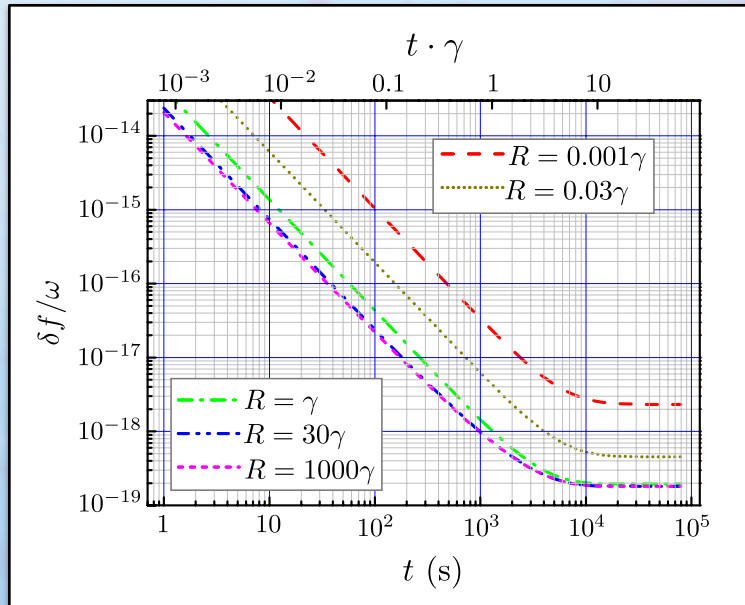
- detune red by δ from nominal frequency
- illuminate for time θ with a pumping rate R
- count photons for time θ'
- repeat for blue detuning
- correct frequency offset f
- start again (**continuous operation!**)

cycle determined by **4 parameters** $\delta, \theta, \theta', R$

- can be optimized to minimize the error δf on f (numerical optimization, photon shot noise limit)
- optimal parameters maintain a constant number of excited nuclei

Fractional frequency error per interrogation cycle

Kazakov et al, New. J. Phys. 14, 083019 (2012)



fractional clock instability
for a series of N measurements:

$$\sigma_{opt}(N) = \frac{\delta f}{\omega \sqrt{N}} = \frac{1.6 \times 10^{-17} s^{-1/2}}{\sqrt{\tau}}$$

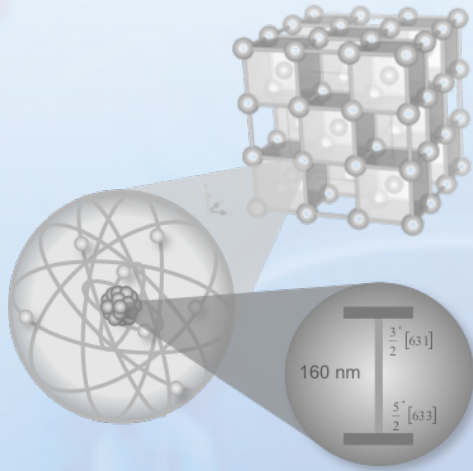
(for $R \approx 1/\gamma$)

should reach **10⁻¹⁹ fractional instability**
within a few hours of averaging
(similar to trapped ion approach?)

NOT included here (...the real world):

- temperature stability of the sample (2nd order Doppler@10 Hz/K)
- properties of the laser (linewidths, frequency/amplitude stability)
- external fields
- non-nuclear luminescence effects (background)

+ this is **never an accurate clock!** → secondary standard?



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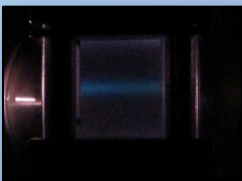
Part 2 - Consequences for a clock

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Part 3 - Experimental efforts

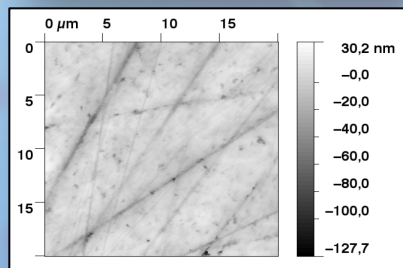
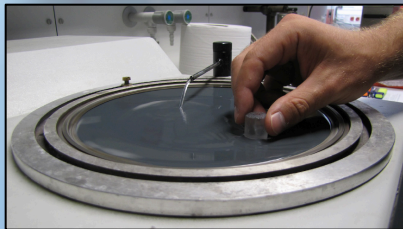
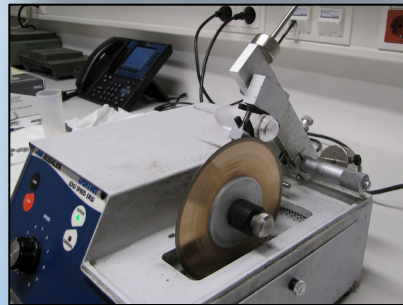
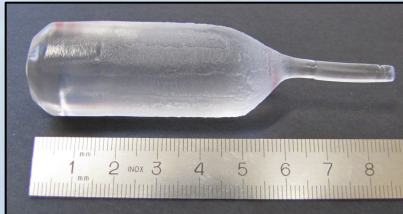
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Poster Winkler



AFM after polishing

Bulk material properties

- Grown at IKZ Berlin using Czochralski method (2 weeks total)
 - Measured Thorium concentration:
 - 200-300 ppm ($2 \times 10^{18} / \text{cm}^3$), homogeneous over the crystal, crystal-melt distribution 1:3 (30% efficiency)
 - ICP mass spectrometry, neutron activation analysis, gamma spectroscopy (identical for us;-)
- CaF chemically accepts the Thorium, doping concentration under control**

Surface properties

- Cut and polished at TU Wien (radiation safety area)
- Corrugation after polishing: 30 nm RMS, 300 nm P-P
- Parallelism an issue



Transmission measurements:

In-house UV spectrometer (deuterium lamp)

- smooth transmission down to 150 nm
- no additional absorption bands compared to CaF_2

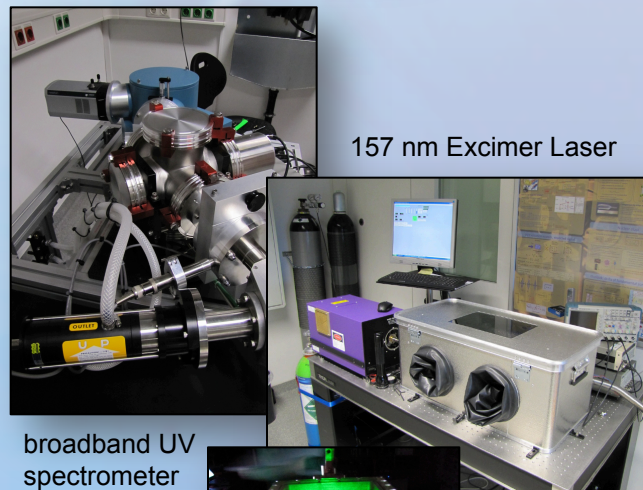
In-house F_2 -Excimer laser

- 157 nm fixed, narrow band (?)
- 8 ns pulse duration, 200 Hz replate
- peak photon flux: $4 \times 10^{21} \text{ s}^{-1}\text{mm}^{-2}$ ($7 \times 10^{14} \text{ s}^{-1}\text{mm}^{-2}$ CV eq.)
- **> 80% transmission** (9% surface loss)
- weak 2-photon processes, no visible damage

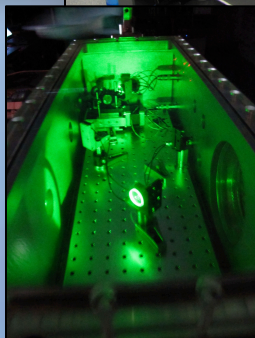
MBI Berlin femtosecond system

- 160 nm tuneable (?), 1 nm linewidth
- 50 fs pulse duration, 1 kHz replate
- peak photon flux: $4 \times 10^{24} \text{ s}^{-1}\text{mm}^{-2}$ ($2 \times 10^{14} \text{ s}^{-1}\text{mm}^{-2}$ CV eq.)
- **> 65% transmission, clear 2-photon processes**
- slight reversible damage for focused beam

We suspect: laser-induced damage for short pulses

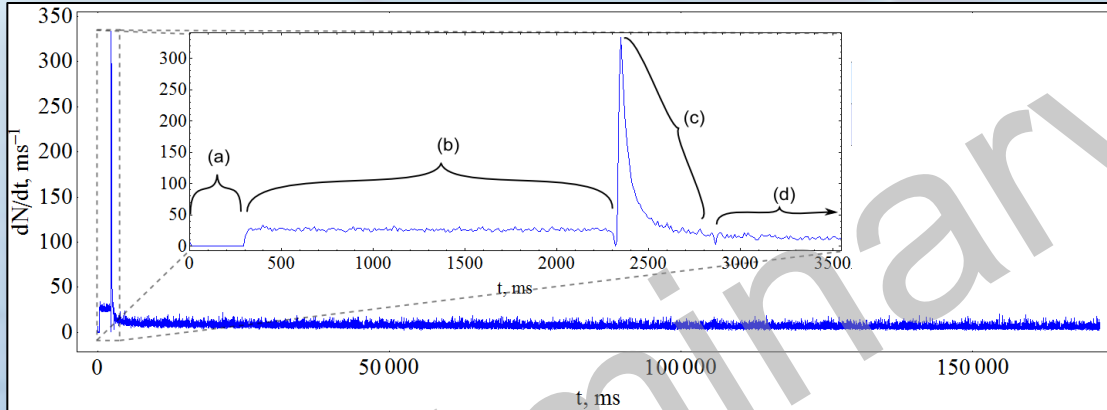


broadband UV spectrometer



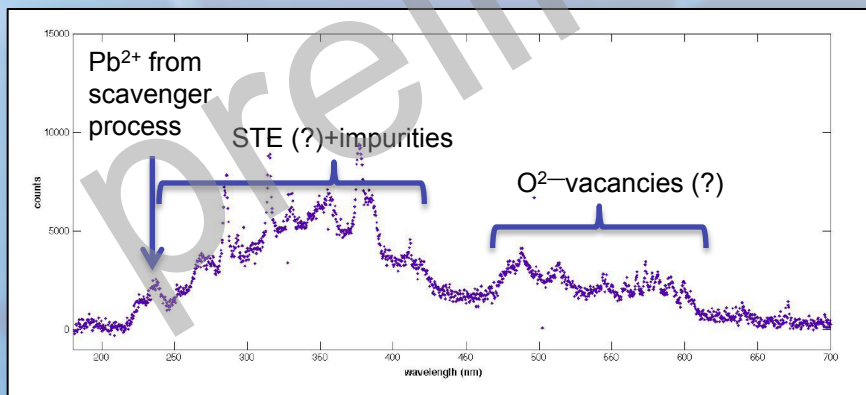
160 nm fs pulse laser
@MBI Berlin

luminescence AFTER exposure by femtosecond pulse:



- very long „afterglow“ (up to seconds!) after illumination with laser (only femtolaser so far)
- luminescence shows (at least) three exponential decay timescales (different processes?)
- build-up of luminescence over several illuminations

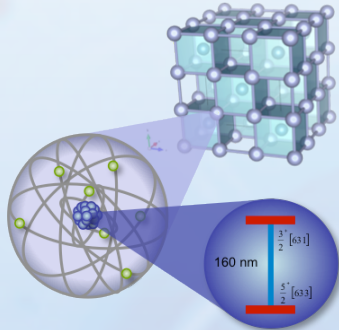
luminescence spectrum after nanosecond pulse:



Luminescence timescale collides with expected lifetime of nuclear state!

We need to:

- clearly **identify impurities** (e.g. Pb^{2+} , Yt^{3+} , Eu^{2+} , Eu^{3+})
- measure timescales of the respective processes
- filter by time, frequency, spatial direction, ...
- compare other host crystals



Part 1 – Solid-state theory

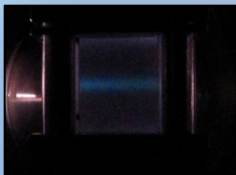
- Identified “microscopics” of Th:CaF₂ doping complex (charge compensation, geometry)
- Th-doped CaF₂ maintains large band gap (impurities problematic)
- main source of de-coherence (≈ 1 ms): neighboring F-nuclei

Part 2 - Consequences for a clock

- fluorescence interrogation scheme required
- still $<10^{-17}$ performance can be achieved
(@ liquid N temp., neglecting ALL technical constrains)

Part 3 - Experimental efforts

- ²³²Th doping performed successful
- transmission indicates good transparency (avoid high pulse intensity)
- luminescence shows long-term component (more studies needed)

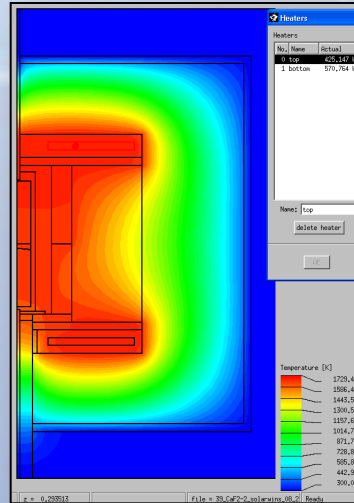


Produce $^{229}\text{Th}:\text{CaF}_2$ crystals...

will have to be done in-house...



assembled vessel



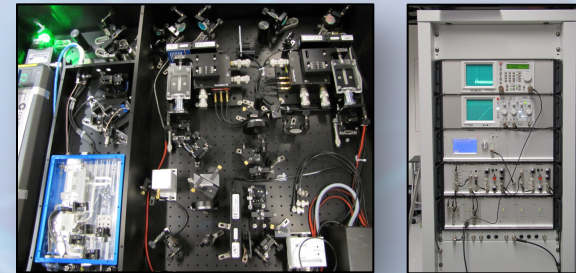
temperature simulations

Collaboration with Fraunhofer Institute IISB Erlangen

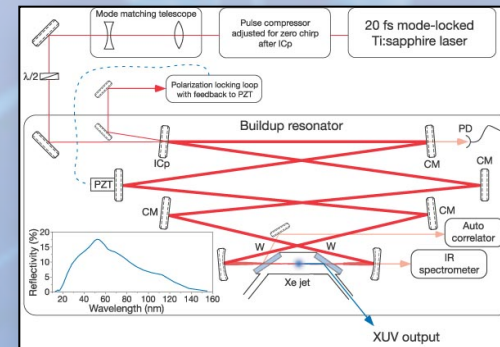
See posters of:
Matthias Schreitl
Georg Winkler

Perform VUV spectroscopy

in-house VUV frequency comb

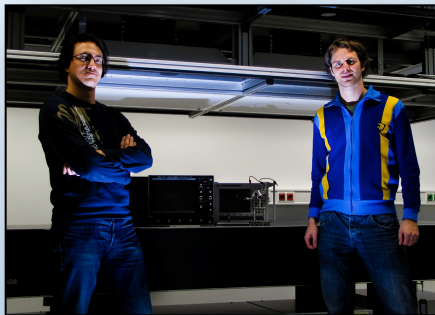


help by MENLO SYSTEMS & MPQ



High-harmonic generation in a passive build-up cavity (following Hänsch/Gohle, Ye...)

The Thorium team:



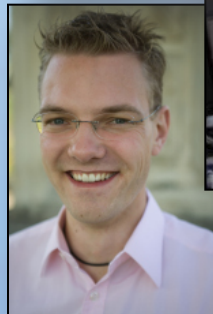
Georg Winkler

Matthias Schreitl

Wolfgang Schlichtner



Bianka Ullmann



Georg Steinhauser



Georgy Kazakov



Thorsten Schumm

Collaborators:

- Crystal growing
 - IKZ Berlin
 - IISB Erlangen
 - University of Pisa
- Crystal characterization
 - Inorganic Chemistry University of Siegen
 - Kristallographie Universität Bremen
- Crystal simulations
 - Keele University
 - CMS Vienna (P. Mohn, P. Dessoic)
- Excitation sources
 - Max Born Institute Berlin
 - MPQ Munich
- Thorium extraction/handling
 - ATI radio chemistry group

More info: www.thorium.at

The Thorium team:

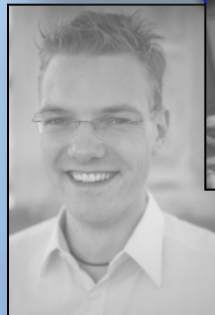


Georg Winkler

Matthias Schreitl

Wolfgang Schlichtner

Blank Uilmann



Georg Kazakov

Georg Steinhauser

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PostDoc Wanted!
Thorium Wanted!

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