

# Study the QCD Phase Structure in High-Energy Nuclear Collisions

Nu Xu

( GSI, LBNL )

# Outline

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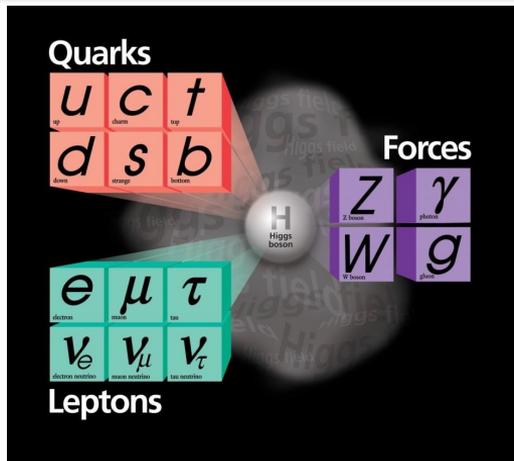
## 1) Introduction

## 2) Selected Recent Results

- Collectivity
- Criticality
- Hyper-nuclei Production

## 3) Future Physics Programs

# Strong Interaction and QCD Phase Structure



2004 asymptotic freedom (QCD)

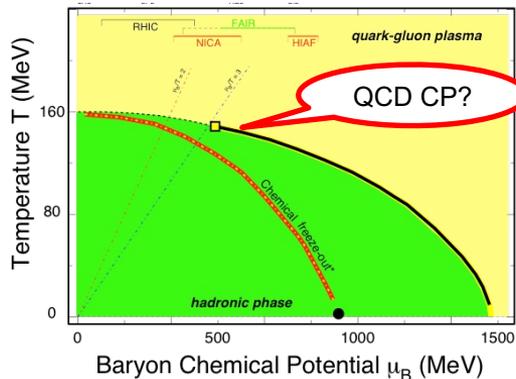
2013 Higgs

## ➤ Discovery of the Higgs boson

- ✓ Origin of mass
- ✓ Standard Model → Theory

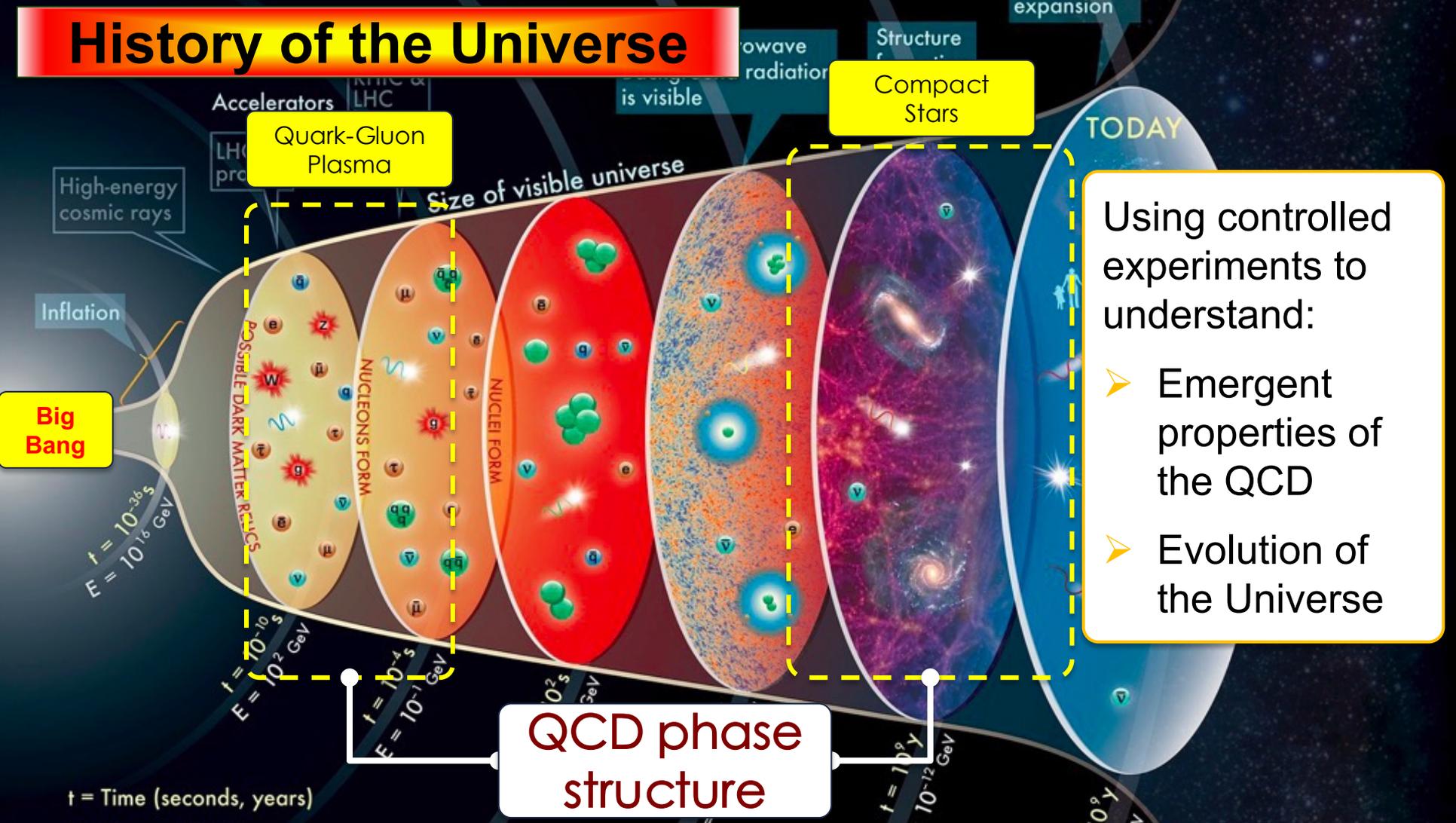
## ➤ QCD Phase Structure (?)

- Confinement
- SCB: mass of hadrons and the visible world
- QCD phase boundary and critical point ...



## Emergent Properties of QCD

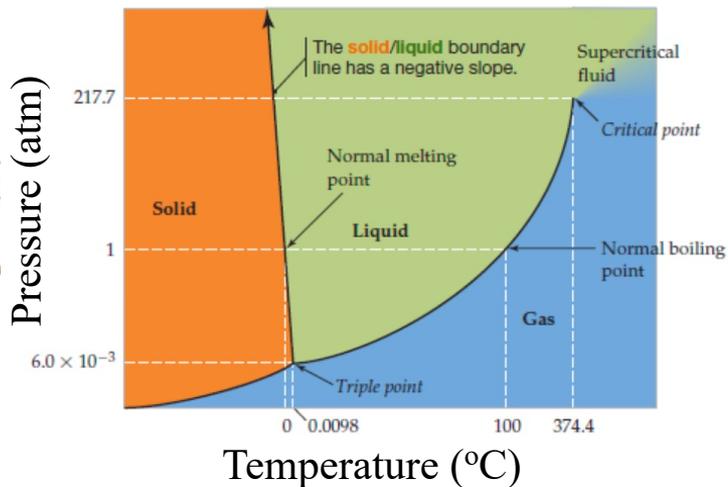
# History of the Universe



# Phase Structure of Strong Interactions

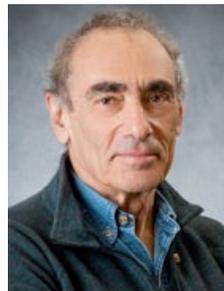
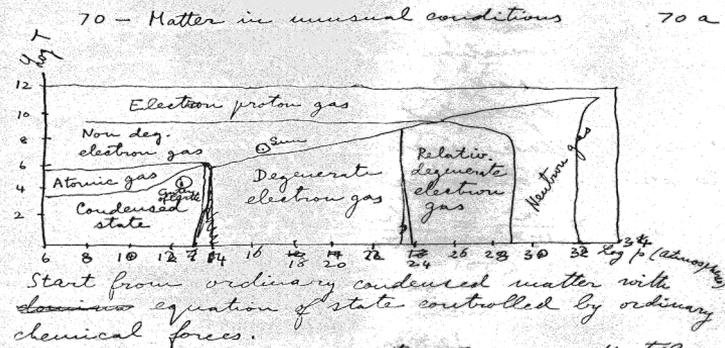
**Phase Diagram:** For given degrees of freedom, how matter (re)organizes itself under external conditions

Phase Diagram of Water: QED at Work



E. Fermi

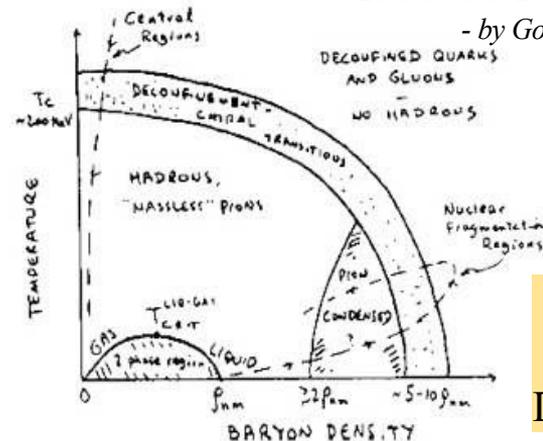
“Notes on Thermodynamics and Statistics” (1953)



Gordon Baym

1983 US NP LRP

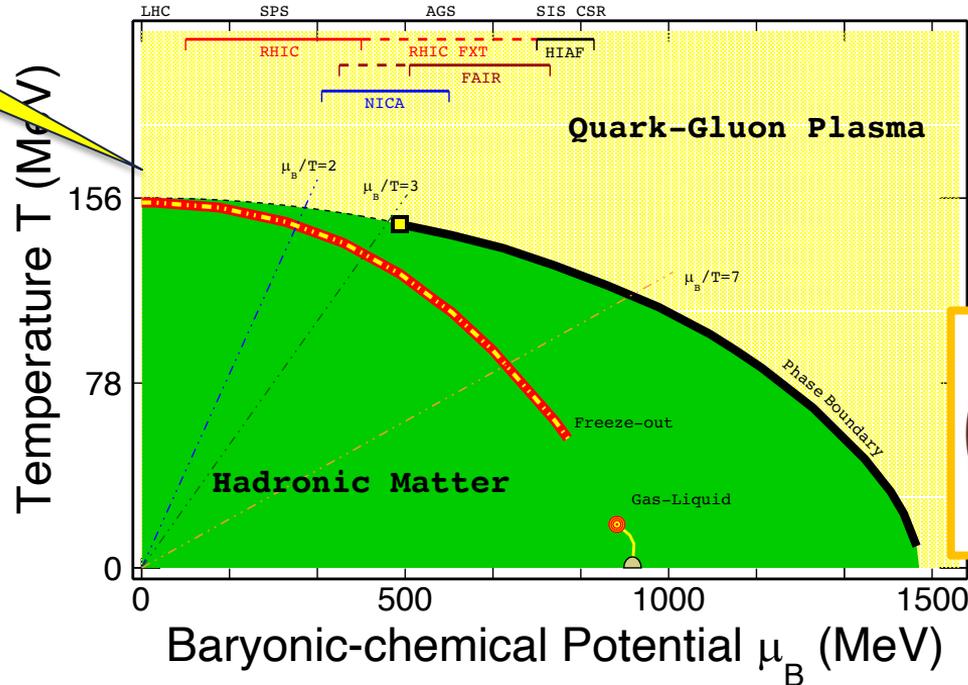
- by Gordon Baym



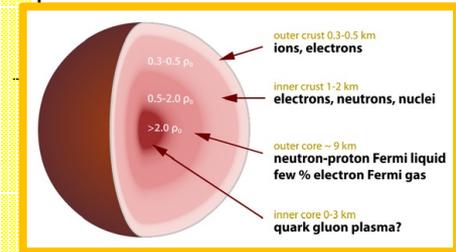
QCD  
Phase  
Diagram

# High-Energy Nuclear Collisions and QCD Phase Diagram

Early Universe



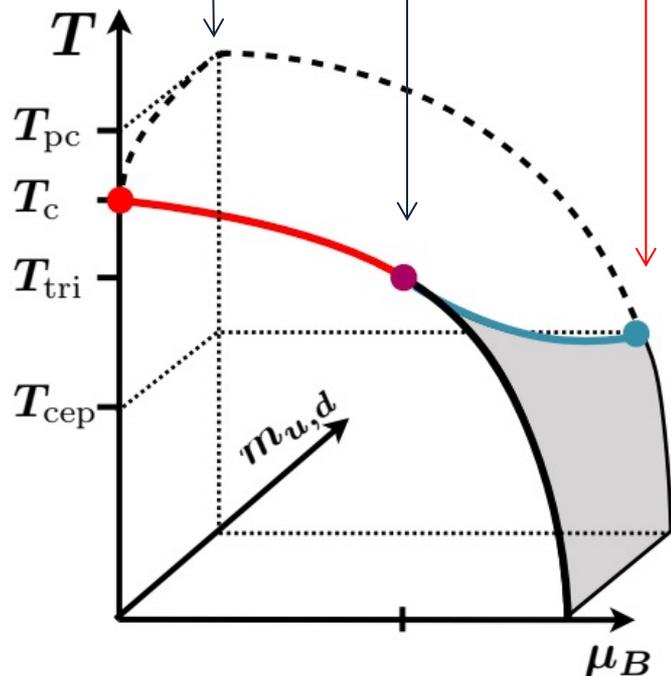
High baryon density:  
Inner structure of  
compact stars



- 1) RHIC BES: → search for 1<sup>st</sup>-order phase transition and **QCD critical point**;
- 2) Baryon interactions (e.g.  $N - N$ ,  $Y - N$ ) → inner structure of compact stars

# LGT Calculation: QCD Phase Structure

$T_C^0$     $T_{PC}$     $T^{\text{TriC}}$     $T^{\text{CEP}}$



F. Karsch *et al.*, 2020

1) QCD transition temperature:

$$T_{PC} = 156.5 \pm 1.5 \text{ MeV}$$

2) Chiral crossover line

$$T_{PC}(\mu_B) = T_{PC}^0 \left[ 1 - \kappa_2 \left( \frac{\mu_B}{T_{PC}^0} \right)^2 - \kappa_4 \left( \frac{\mu_B}{T_{PC}^0} \right)^4 \right]$$

$$\kappa_2 = 0.012(4), \quad \kappa_4 = 0.00(4)$$

3) Chiral transition temperature:

$$T_C = 132_{-6}^{+3} \text{ MeV}$$

4) QCD critical end point:

$$T^{\text{CEP}} < T_C, \quad \mu_B^{\text{CEP}} \gtrsim 3T_C$$

HotQCD: Phys.Lett.**B795**, 15(2019);  
Phys. Rev. Lett. **123**, 062002(2019)

# High-Energy Nuclear Collisions and QCD Phase Diagram

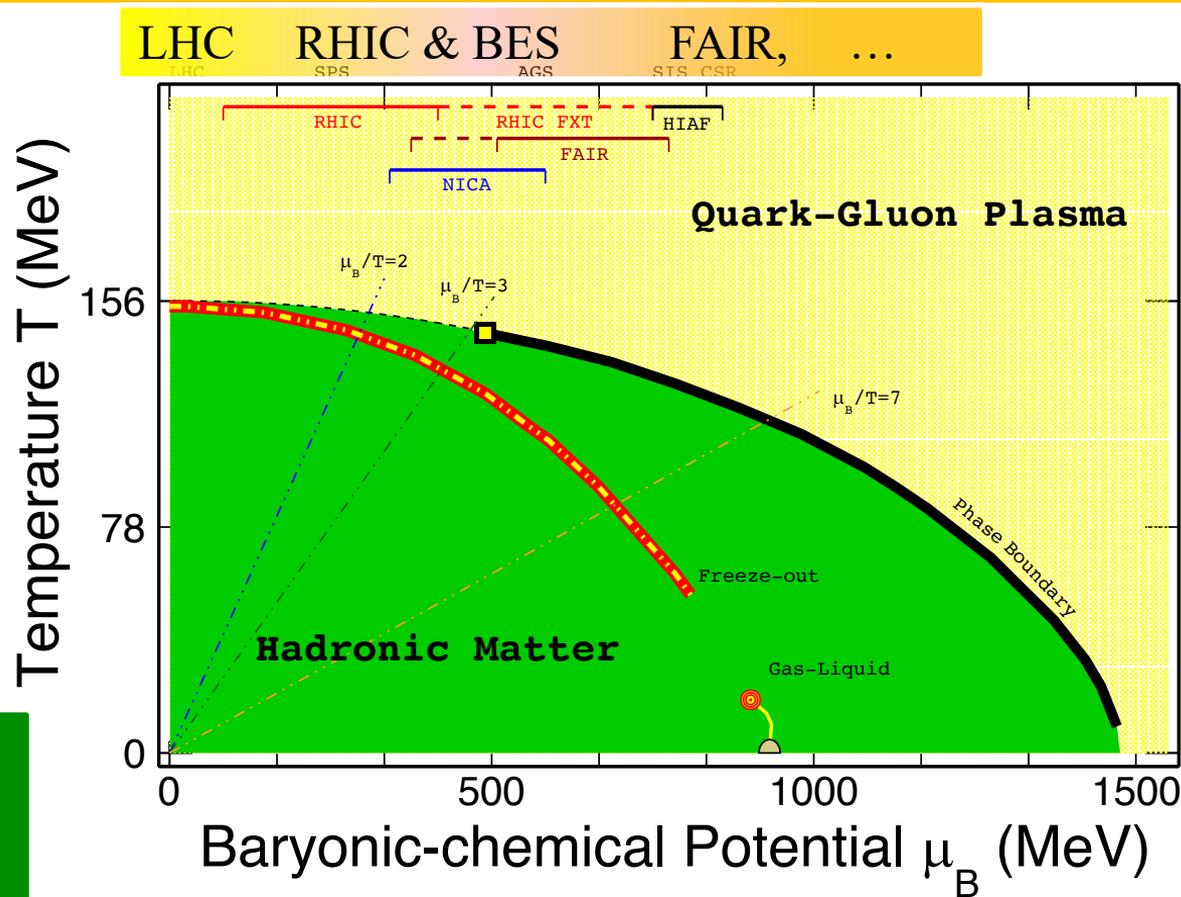
At LHC and RHIC top energy:

- Jet quenching;
- Collectivity data;
- Net-p  $C_2/C_1$



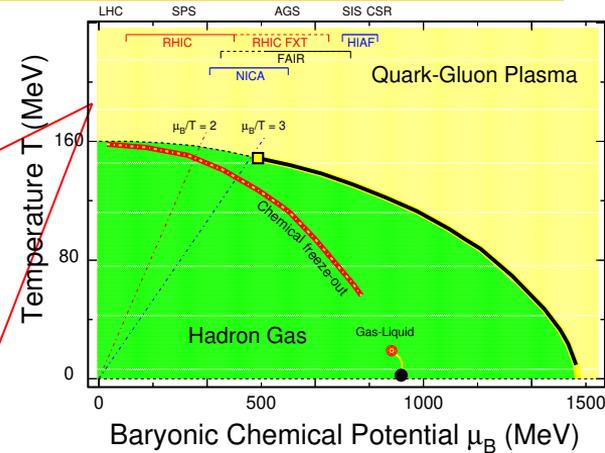
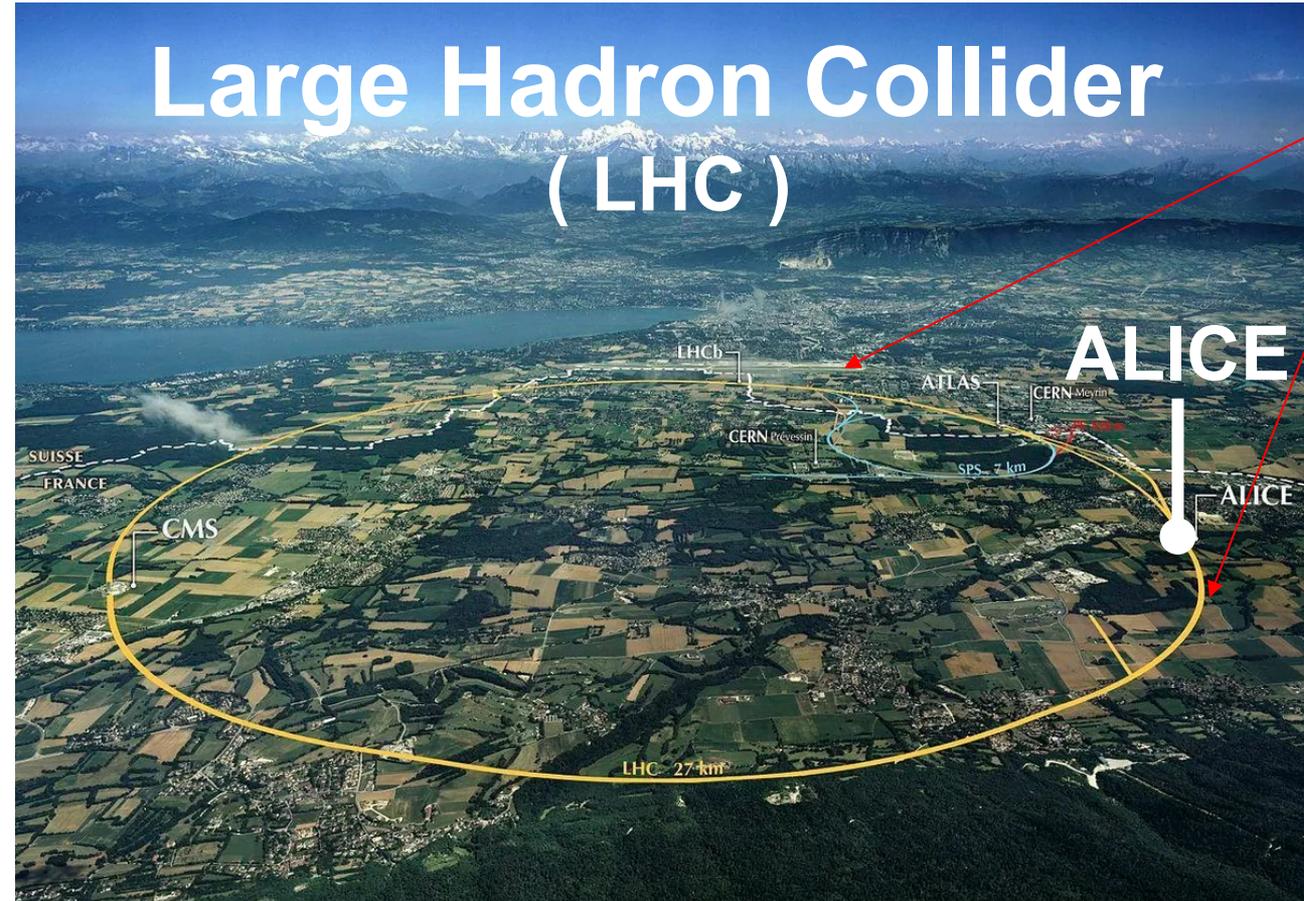
- 1) At  $\mu_B \sim 0$ , smooth crossover.  $\mu_B/T \leq 2$  (LGT);
- 2) CP at  $\mu_B/T > 3$

- 1) STAR: Phys.Rev. **C79**, 034909(2009);
- 2) P. Braun-Munzinger *et al.* Nature, **561**, 321(2018);
- 3) A. Bzdak *et al.* Phys. Rep., **853**, 1(2020);
- 4) ALICE: 2211.04384 (review)



# High-Energy Nuclear Collisions and QCD Phase Diagram

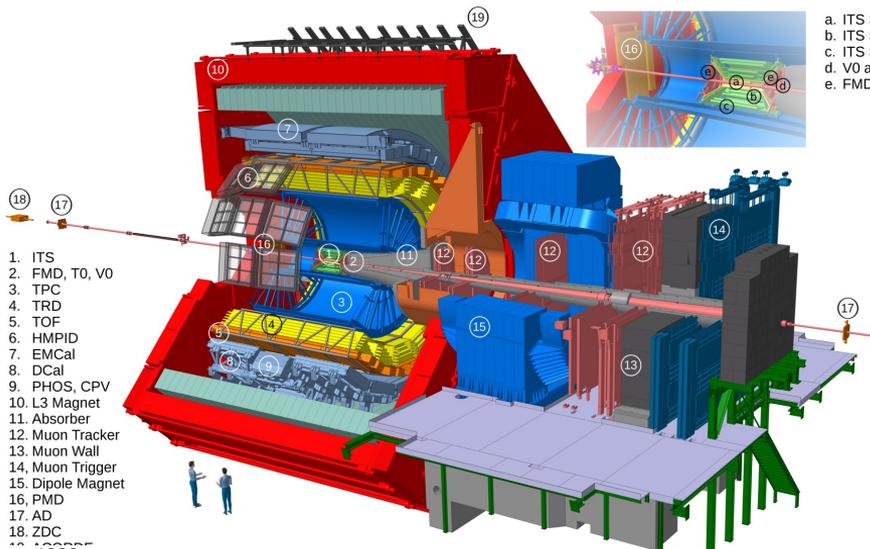
## Large Hadron Collider (LHC)



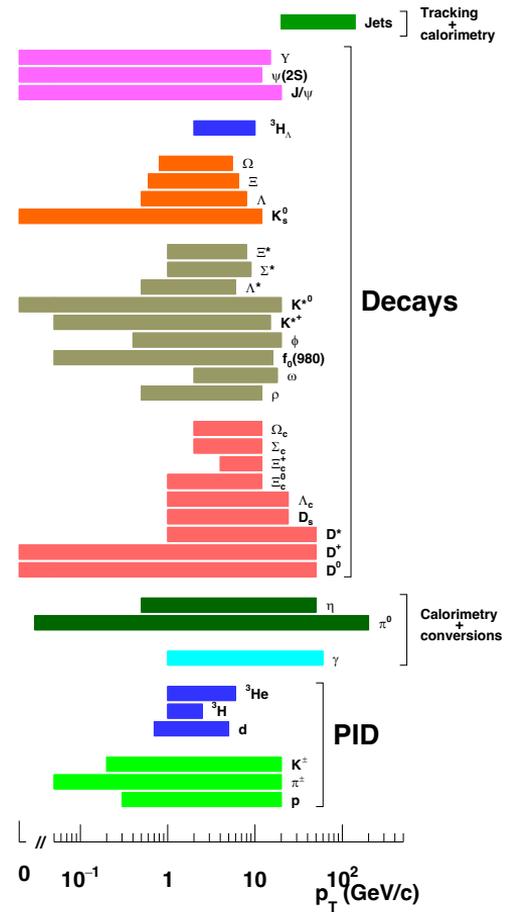
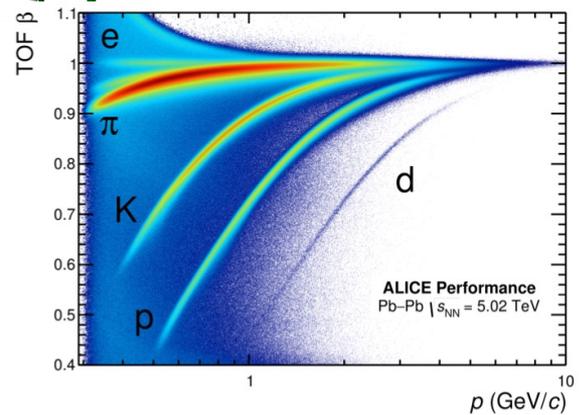
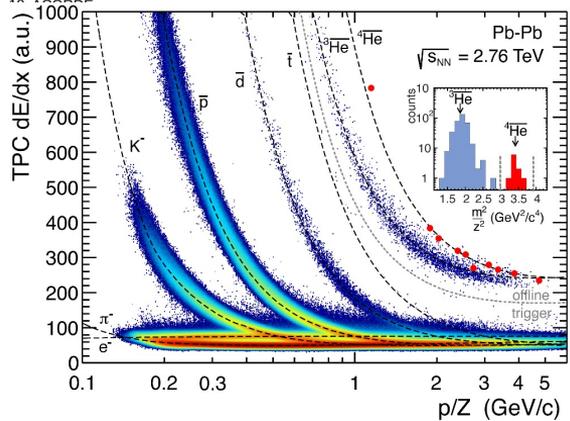
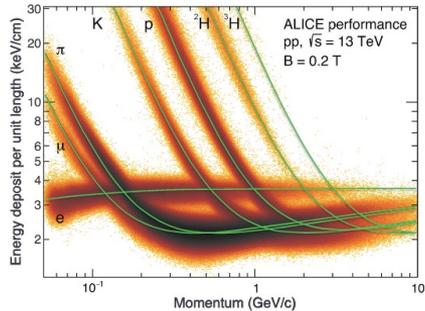
### LHC collision energies:

- $\sqrt{s_{NN}} = 0.9, 2.76, 5.02, 5.44$  TeV  
Xe+Xe, Pb+Pb
- $\sqrt{s} = 0.9 - 13$  TeV p+p
- $\mu_B \rightarrow 0$

# ALICE DETECTOR SYSTEM

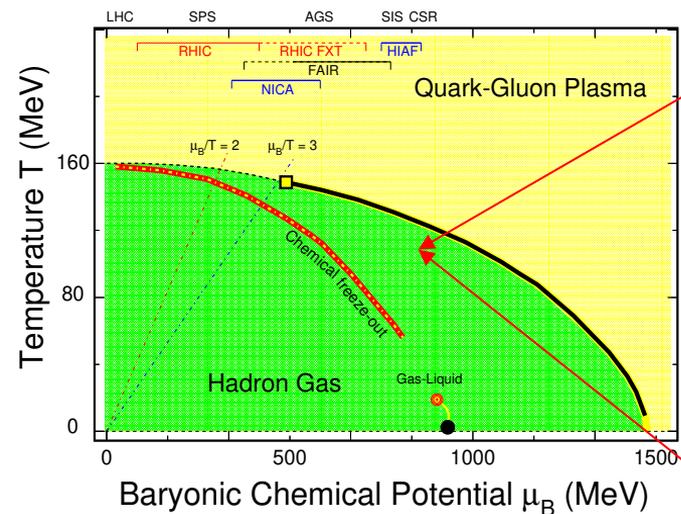


(Particle Data Group),  
Prog. Theor. Exp. Phys.,  
083C01 (2022)



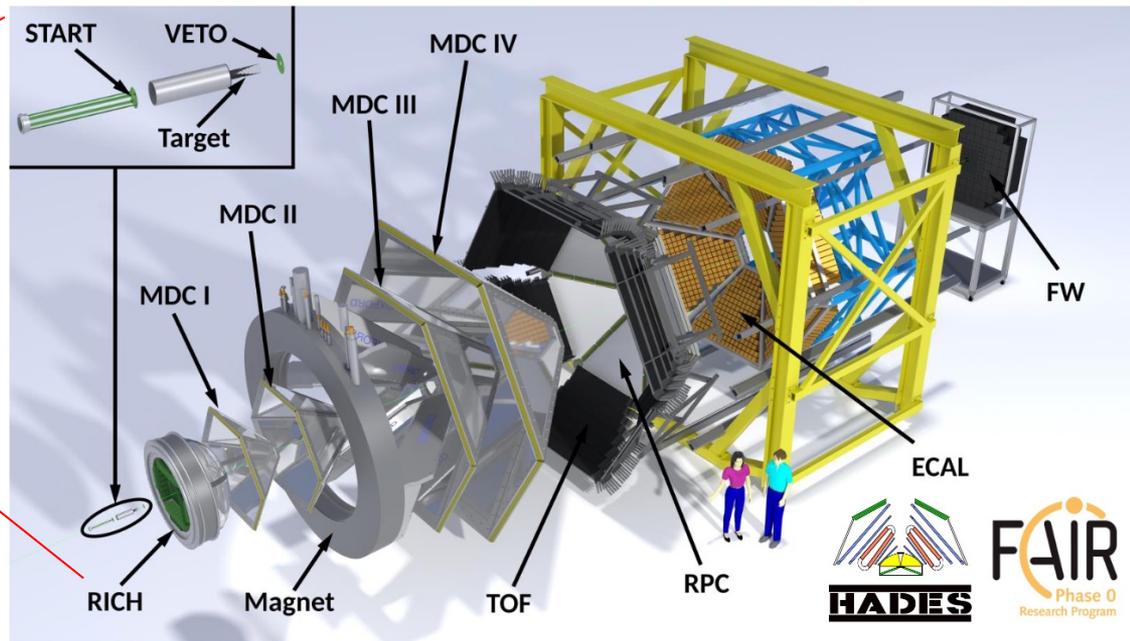
ALICE: 2211.04384

# HADES DETECTOR SYSTEM



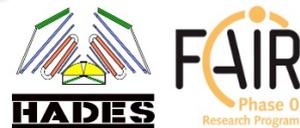
## SIS18 Collisions:

- $E_K = 1.76$  AGeV Ar+Kl
- $E_K = 1.58/1.23$  AGeV Ag+Ag
- $E_K = 1.23$  AGeV Au+Au
- $\mu_B \rightarrow 800$  MeV
- $E_K = 4.5$  GeV p+p
- $E_K = 3.5$  GeV p+Nb
- $E_K = 1.7$  GeV  $\pi$ +W / +C / +PE

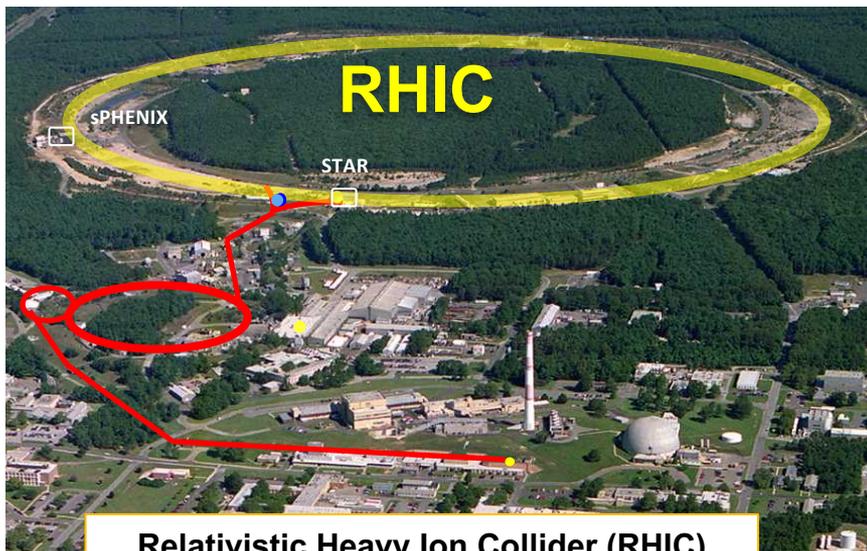


Properties of nuclear matter at high baryon potential and nuclear density:

- 1) Correlations and fluctuations;
- 2) Strangeness production;
- 3) **Di-lepton signals from various sources**



# Nuclear Collisions and QCD Phase Diagram



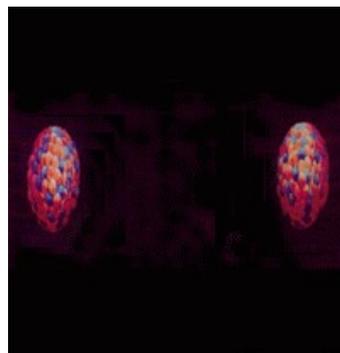
Relativistic Heavy Ion Collider (RHIC)

RHIC top collision energies:

- $\sqrt{s_{NN}} = 200$  GeV U+U / Au+Au / Zr+Zr / Ru+Ru / O+O
- $\sqrt{s} = 510$  GeV p+p

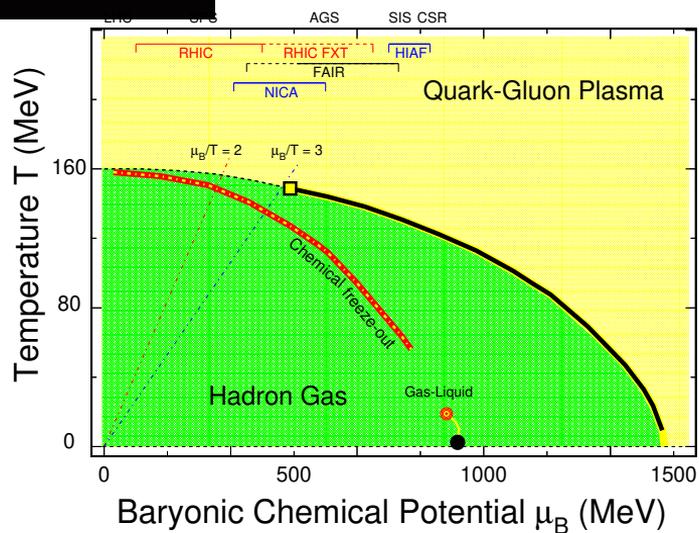
RHIC Beam Energy Scan (BES):

- $\sqrt{s_{NN}} = 200 - 7.7$  GeV (collider mode)
- $\sqrt{s_{NN}} = 17.3 - 3$  GeV (fixed-target mode)

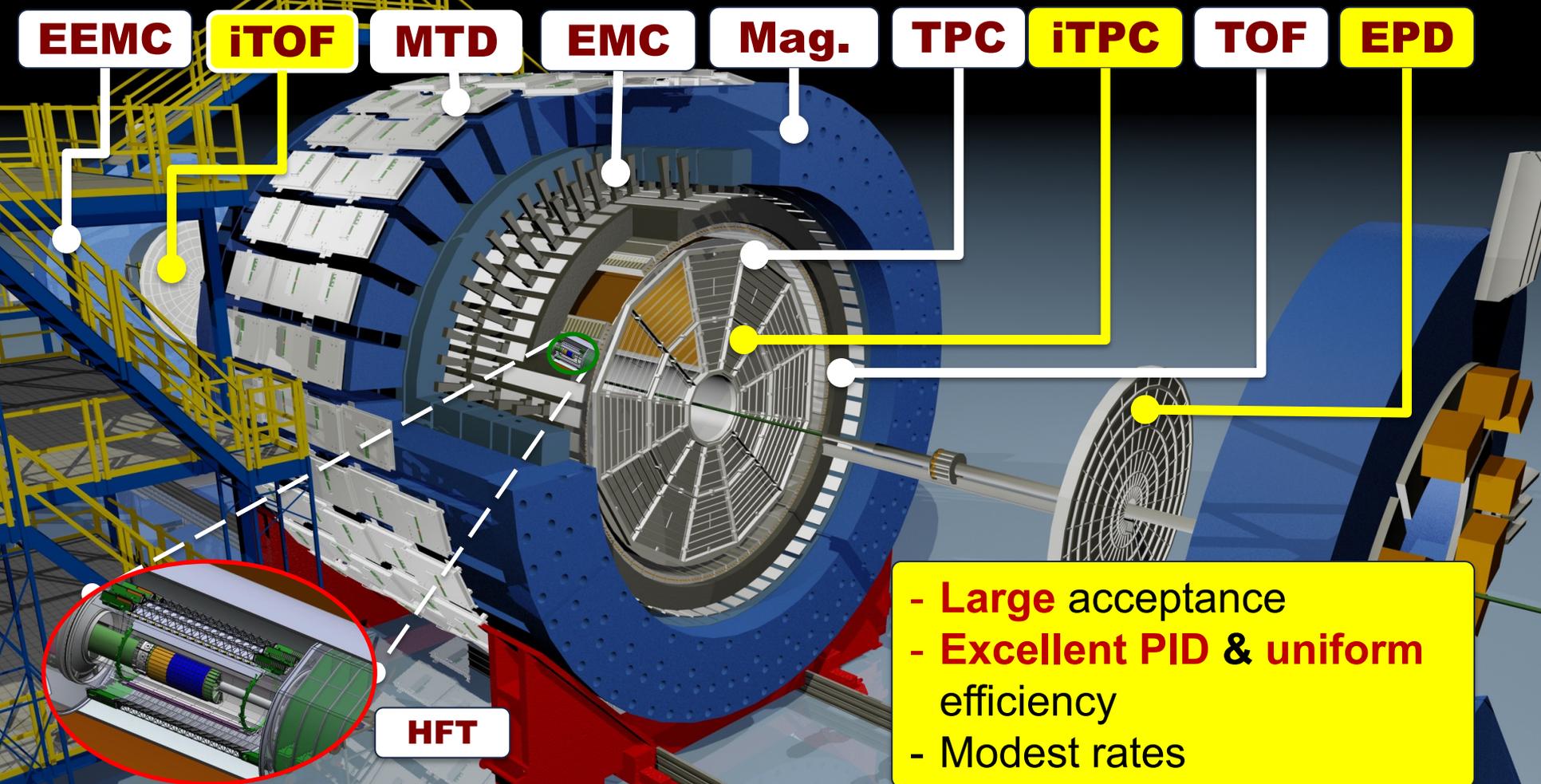


Quark-Gluon Plasma (QGP)

QCD Phase Diagram



# STAR DETECTOR SYSTEM



**EEMC**

**iTOF**

**MTD**

**EMC**

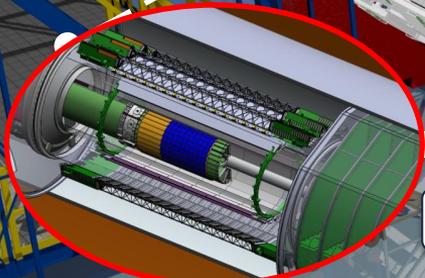
**Mag.**

**TPC**

**iTPC**

**TOF**

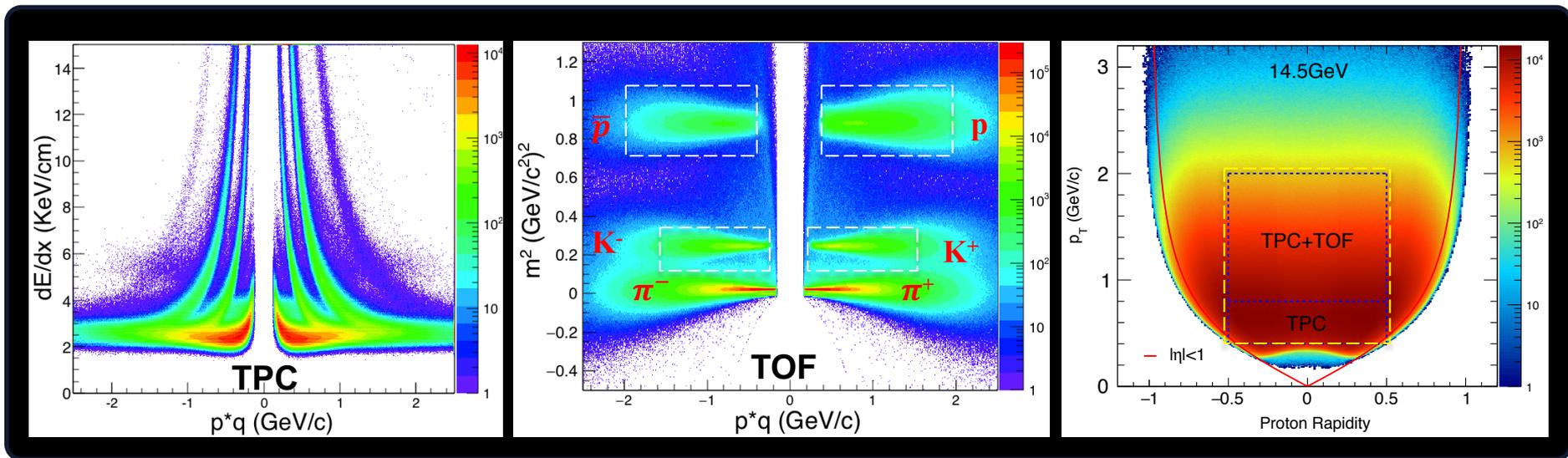
**EPD**



**HFT**

- **Large** acceptance
- **Excellent PID & uniform** efficiency
- Modest rates

# Particle Identification and Acceptance



	Net-charge	Net-Kaon	Net-proton
Kinetic cuts	$0.2 < p_T < 2.0$ GeV/c, $ \eta  < 0.5$	$0.2 < p_T < 1.6$ GeV/c, $ y_K  < 0.5$	$0.2 < p_T < 1.6$ GeV/c, $ y_p  < 0.5$
Particle identifications	Reject spallation p at $p_T < 2.0$ GeV/c	TPC: $0.2 < p_T < 0.4$ GeV/c TPC/TOF: $0.4 < p_T < 1.6$ GeV/c	TPC: $0.4 < p_T < 0.8$ GeV/c TPC/TOF: $0.8 < p_T < 2.0$ GeV/c
Efficiency corrections		TPC: $\epsilon_{\text{TPC}} \sim 0.8$ ;    TPC+TOF: $\epsilon_{\text{TPC+TOF}} \sim 0.5$	
Centrality Definitions	Un-corrected charge particles $0.5 <  \eta  < 1.0$	Un-corrected charge particles and reject Kaons, $ \eta  < 1.0$	Un-corrected charge particles and reject p and anti-p, $ \eta  < 1.0$

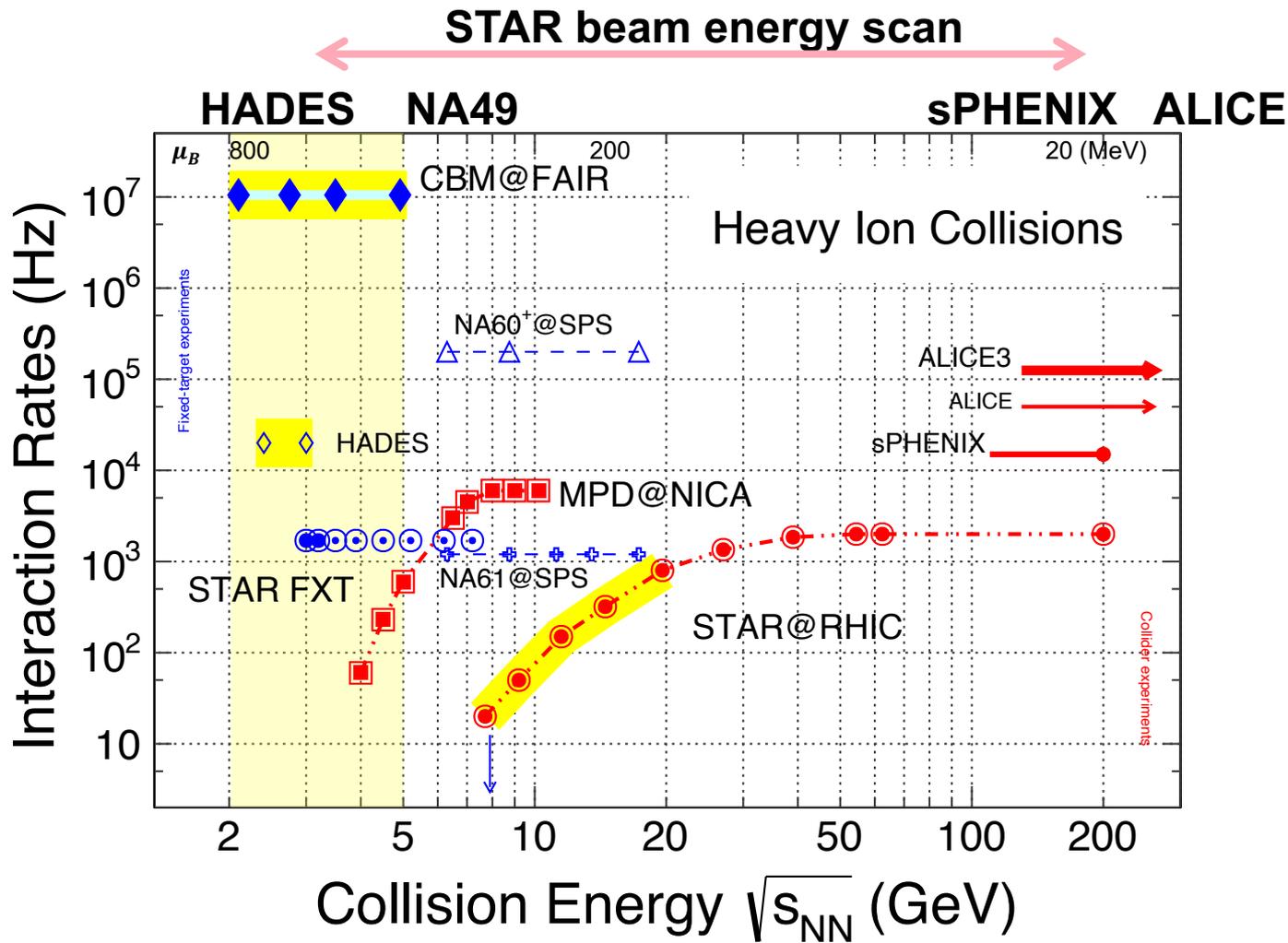


# STAR BES-I and BES-II Data Sets

Au+Au Collisions at RHIC											
Collider Runs						Fixed-Target Runs					
	$\sqrt{s_{NN}}$ (GeV)	#Events	$\mu_B$	$y_{beam}$	run		$\sqrt{s_{NN}}$ (GeV)	#Events	$\mu_B$	$y_{beam}$	run
1	<b>200</b>	<b>380 M</b>	<b>25 MeV</b>	5.3	Run-10, <b>19</b>	1	13.7 (100)	50 M	280 MeV	-2.69	Run- <b>21</b>
2	62.4	46 M	75 MeV		Run-10	2	11.5 (70)	50 M	320 MeV	-2.51	Run- <b>21</b>
3	54.4	1200 M	85 MeV		Run-17	3	9.2 (44.5)	50 M	370 MeV	-2.28	Run- <b>21</b>
4	39	86 M	112 MeV		Run-10	4	7.7 (31.2)	260 M	420 MeV	-2.1	Run- <b>18, 19, 20</b>
5	27	585 M	156 MeV	3.36	Run-11, <b>18</b>	5	7.2 (26.5)	470 M	440 MeV	-2.02	Run- <b>18, 20</b>
6	19.6	595 M	206 MeV	3.1	Run-11, <b>19</b>	6	6.2 (19.5)	120 M	490 MeV	1.87	Run- <b>20</b>
7	17.3	256 M	230 MeV		Run- <b>21</b>	7	5.2 (13.5)	100 M	540 MeV	-1.68	Run- <b>20</b>
8	14.6	340 M	262 MeV		Run-14, <b>19</b>	8	4.5 (9.8)	110 M	590 MeV	-1.52	Run- <b>20</b>
9	11.5	57 M	316 MeV		Run-10, <b>20</b>	9	3.9 (7.3)	120 M	633 MeV	-1.37	Run- <b>20</b>
10	9.2	160 M	372 MeV		Run-10, <b>20</b>	10	3.5 (5.75)	120 M	670 MeV	-1.2	Run- <b>20</b>
11	7.7	104 M	420 MeV		Run- <b>21</b>	11	3.2 (4.59)	200 M	699 MeV	-1.13	Run- <b>19</b>
						12	<b>3.0 (3.85)</b>	<b>260 + 2000 M</b>	<b>760 MeV</b>	-1.05	Run-18, <b>21</b>

Most precise data to map the QCD phase diagram

$$3 < \sqrt{s_{NN}} < 200 \text{ GeV}; \quad 760 > \mu_B > 25 \text{ MeV}$$



# Outline

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## 1) Introduction

## 2) Selected Recent Results

- Collectivity
- Criticality
- Hyper-nuclei Production

## 3) Future Physics Programs

# Collectivity

$$\begin{aligned}\partial_\mu [(\varepsilon + p)u^\mu u^\nu - pg^{\mu\nu}] &= 0 \\ \partial_\mu [s u^\mu] &= 0\end{aligned}$$

$$\frac{d^2N}{p_T dp_T d\varphi} = \frac{1}{2\pi} \frac{dN}{p_T dp_T} \left\{ 1 + \sum_{n=1}^{\infty} 2v_n(p_T) \cos[n(\varphi - \Psi_R)] \right\}$$

–  $v_1$  Directed flow;

–  $v_2$  Elliptic flow;

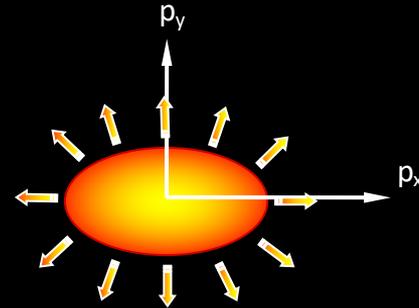
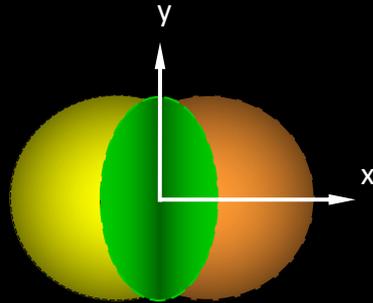
–  $v_3$  Triangle flow

# Anisotropy Parameter $v_2$

coordinate-space-anisotropy



momentum-space-anisotropy



$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

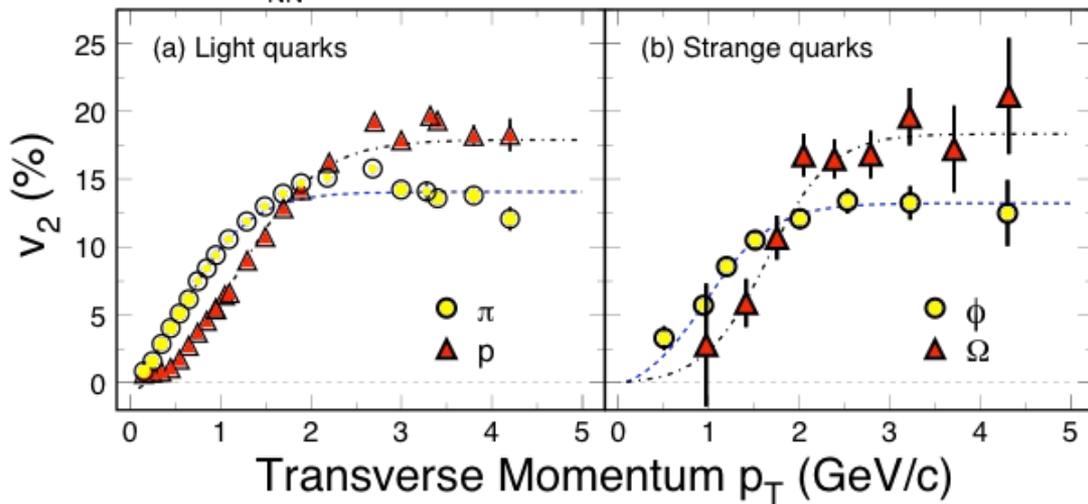
$$v_2 = \langle \cos 2\varphi \rangle,$$

$$\varphi = \tan^{-1} \left( \frac{p_y}{p_x} \right)$$

**Sensitive to initial/final conditions, EoS and degrees of freedom**

# Partonic Collectivity at RHIC

$\sqrt{s_{NN}} = 200 \text{ GeV } ^{197}\text{Au} + ^{197}\text{Au}$  Collisions at RHIC



STAR: PRL116, 62301(2016)

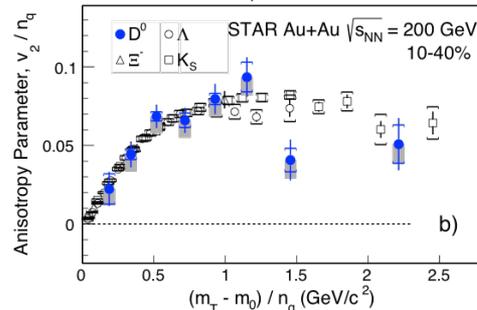
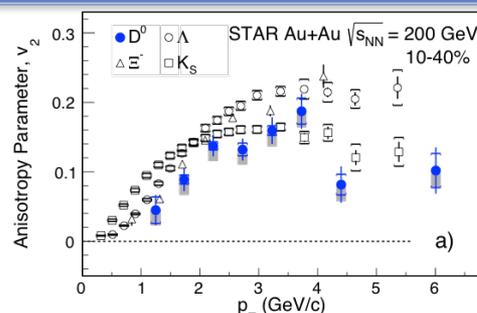
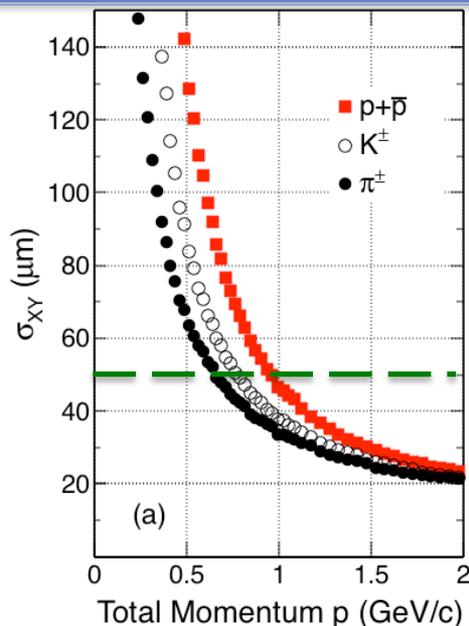
- ✓ Low  $p_T$  ( $\leq 2 \text{ GeV}/c$ ): hydrodynamic mass ordering
- ✓ High  $p_T$  ( $> 2 \text{ GeV}/c$ ): **number of quarks scaling (NCQ)**

u-, d-, and s-quarks flow!

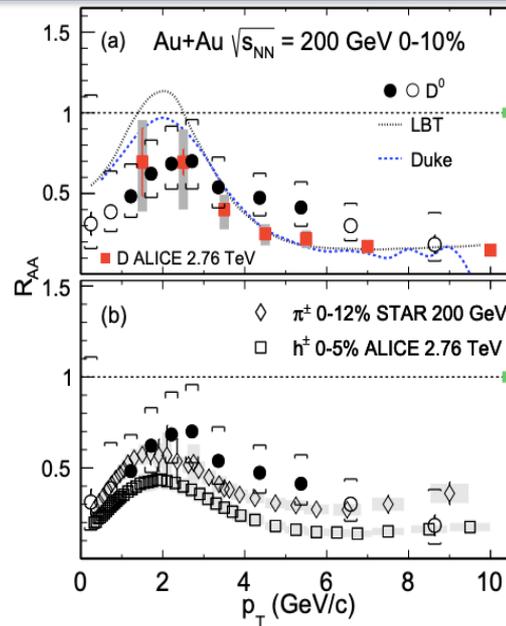
- **Partonic Collectivity!**
- **De-confinement Au+Au collisions at RHIC!**

STAR: PRL116, 62301(2016)

# Heavy Flavor Hadron $D^0$ Collectivity at HRIC



PRL118, 212301 (2017)

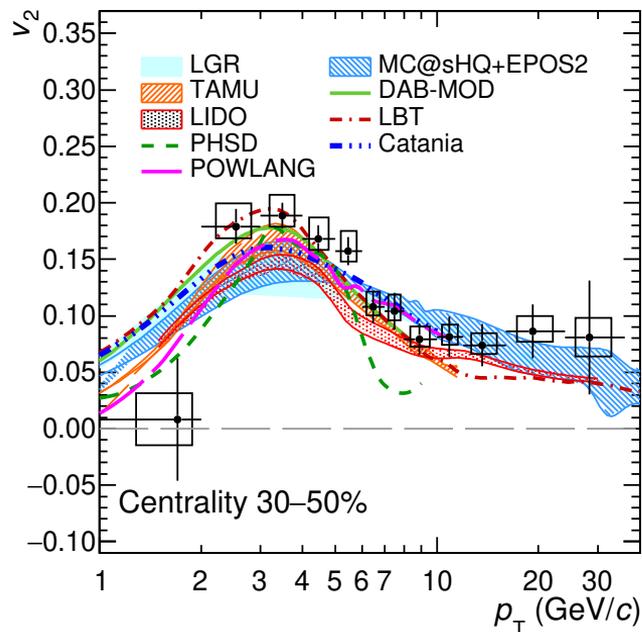
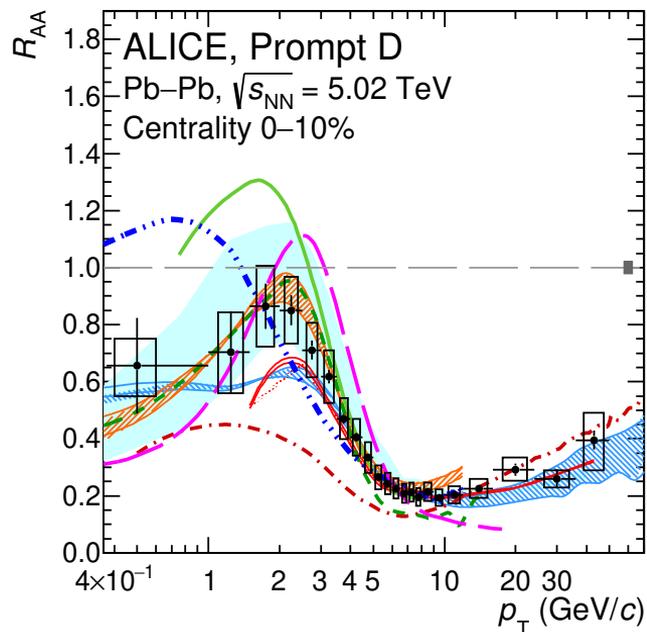


PRL113, 142301 (2014)  
 PRC99, 034908(2019)

- 1) First application of MAPS technology in high energy collisions, excellent position resolution;
  - “These results suggest that charm quarks have achieved **local thermal equilibrium** with the medium created in such (200GeV Au+Au) collisions”
  - Hadronization via **quark coalescence** process

STAR: PRL113, 142301(14); PRC99, 034908(19); PRL118, 212301(17); PRL123, 162301(19); PRL124, 172301(20)

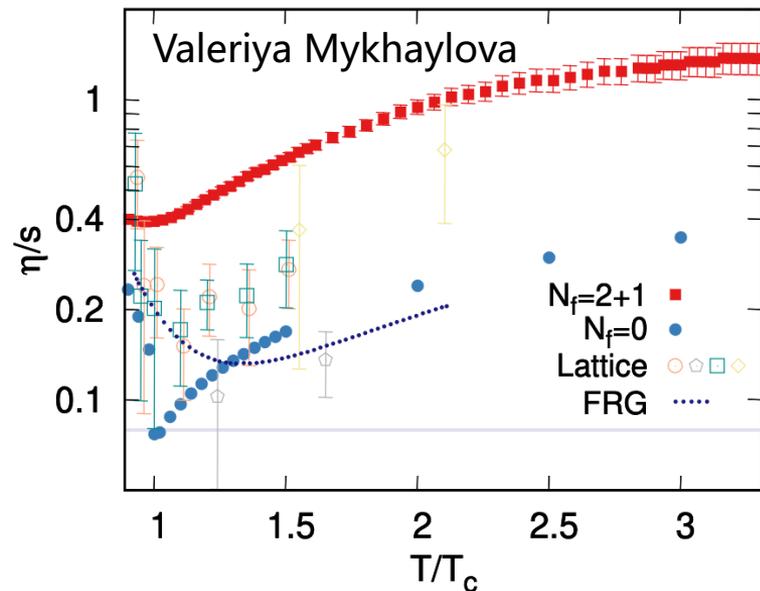
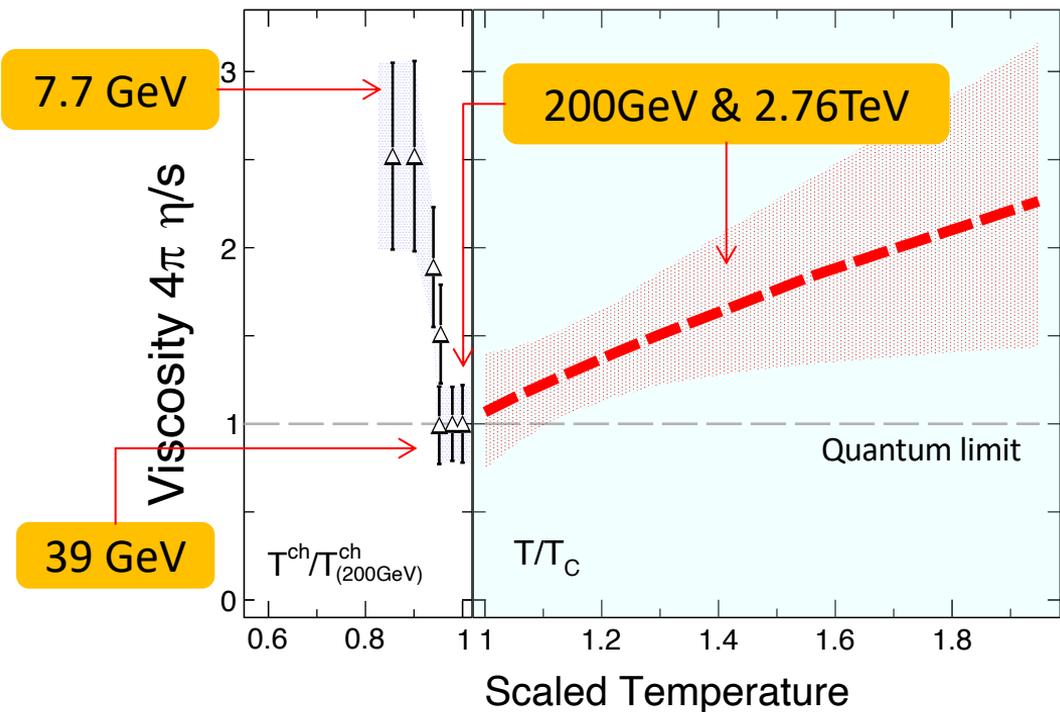
# D<sup>0</sup> Partonic Energy Loss and Collectivity at LHC



ALICE:  
1) 2211.04384;  
2) JHEP 01 (2022) 174  
3) Phys. Lett. B813 (2021) 136054

- D<sup>0</sup> strong suppress in  $R_{AA}$  and collectivity  $v_2$  are evident at LHC;
- Calculations: Charm-transport in hydrodynamically expanding QGP

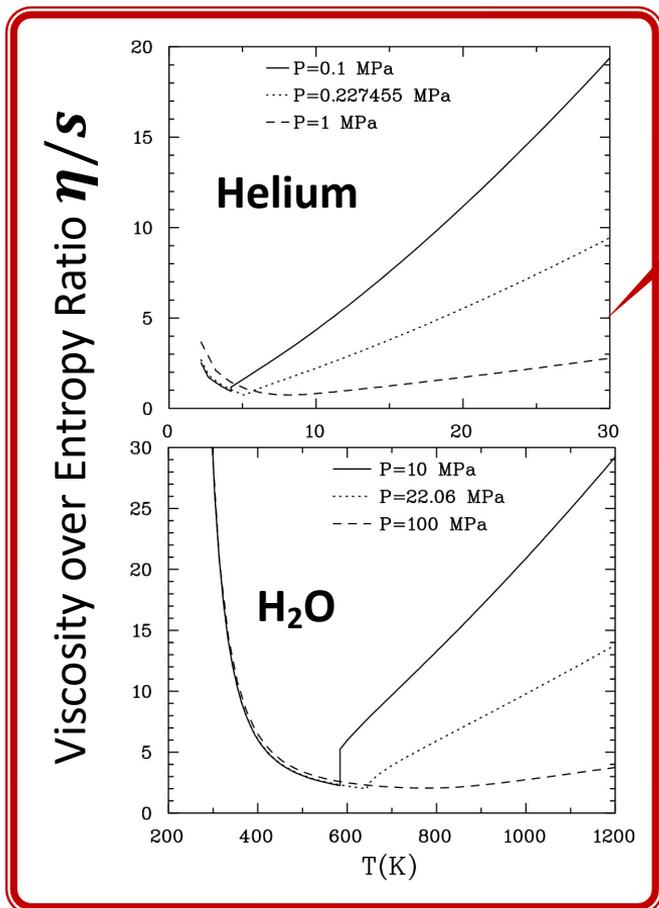
# Equation of State for Strong Interaction



## 4) Evidence of the QCD transition!

- L.P. Csernai, J.I. Kapusta, L.D. McLerran, PRL **97** (2006) 152303
- X.Dong, Y.J. Lee & R.Rapp, ARNPS, **69** (2019) 417
- J.E.Bernhard, J.S.Moreland & S. Bass, Nat. Phys. **15** (2015) 1113
- I. Karpenko, P. Huovinen, H. Petersen, and M. Bleicher, Phys.Rev. **C91**, 064901 (2015).
- G.Nijs, W.van der Schee, U. Gürsoy and R. Snellings, PRL **126**, (2021) 202301

# Strongly-Interacting Low-Viscosity Matter

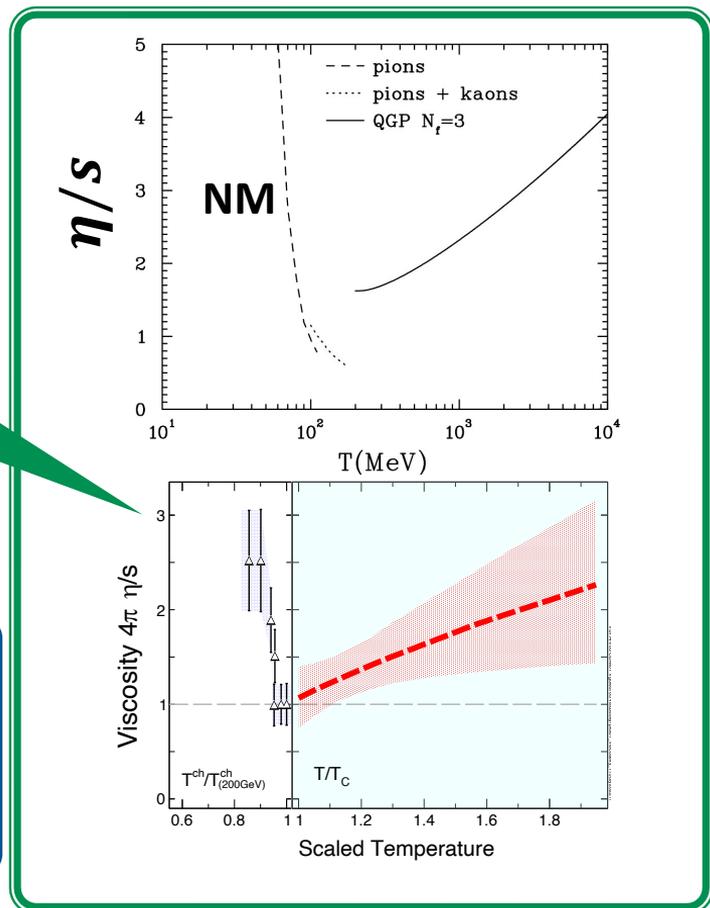


**EM interaction**  
 $\eta/s \sim 1$

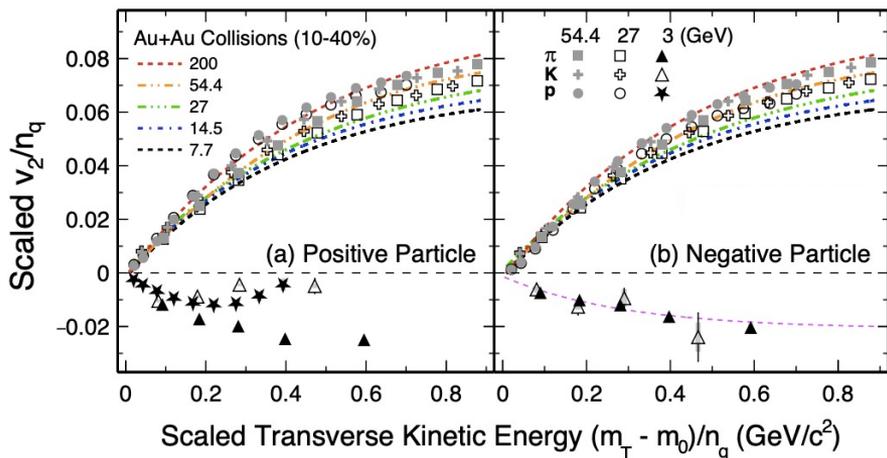
L.P. Csernai, J.I. Kapusta, L.D. McLerran, PRL97 (2006) 152303

**Strong Interaction**  
 $\eta/s \sim 0.1$

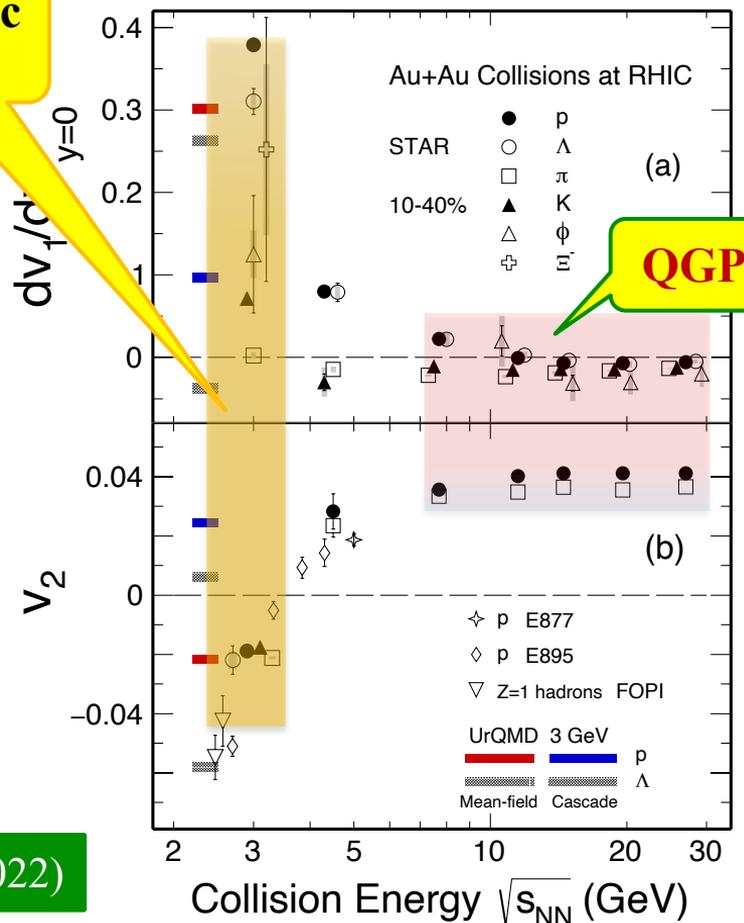
- QGP matter in  $\sqrt{s_{NN}} \geq 39$  GeV collisions!
- Universal behavior for phase transition!



# Disappearance of Partonic Collectivity



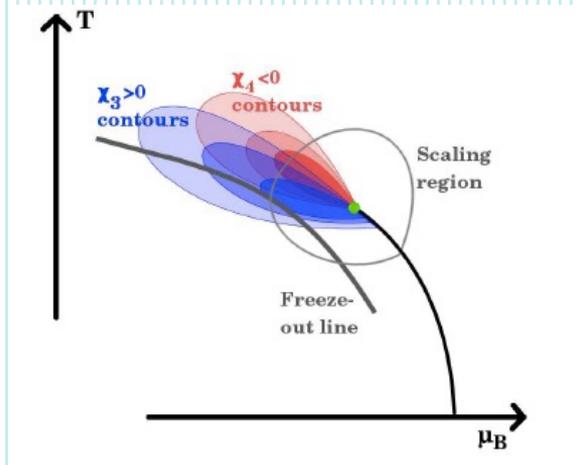
**Hadronic Matter**



- At **3 GeV**, NCQ scaling is absent ;
- Transport model calculations, with baryonic mean field, reproduce both  $v_1$  and  $v_2$  results ;
- **hadronic interactions dominant!**

STAR: PLB827, 137003(2022)

# Criticality



# Conserved Quantities (B, Q, S)

- 1) In strong interactions, baryons (B), charges (Q) and strangeness (S) are conserved;
- 2) Higher order moments/cumulants describe the shape of distributions and quantify fluctuations. They are sensitive to the correlation length  $\xi$ , phase structure;
- 3) Direct connection to theoretical calculations of susceptibilities.

Measured multiplicity  $N$ ,  $\langle \delta N \rangle = N - \langle N \rangle$

mean:  $M = \langle N \rangle = C_1$

variance:  $\sigma^2 = \langle (\delta N)^2 \rangle = C_2$

skewness:  $S = \langle (\delta N)^3 \rangle / \sigma^3 = C_3 / C_2^{3/2}$

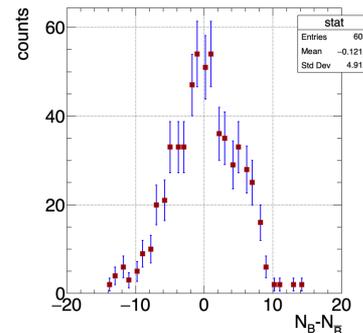
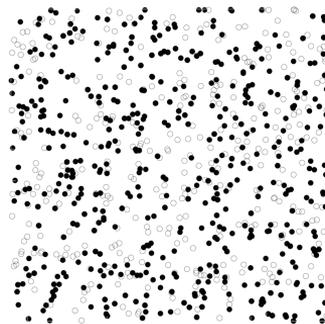
kurtosis:  $\kappa = \langle (\delta N)^4 \rangle / \sigma^3 - 3 = C_4 / C_2^2$

Moments, cumulants and susceptibilities:

2<sup>nd</sup> order:  $\sigma^2 / M \equiv C_2 / C_1 = \chi_2 / \chi_1$

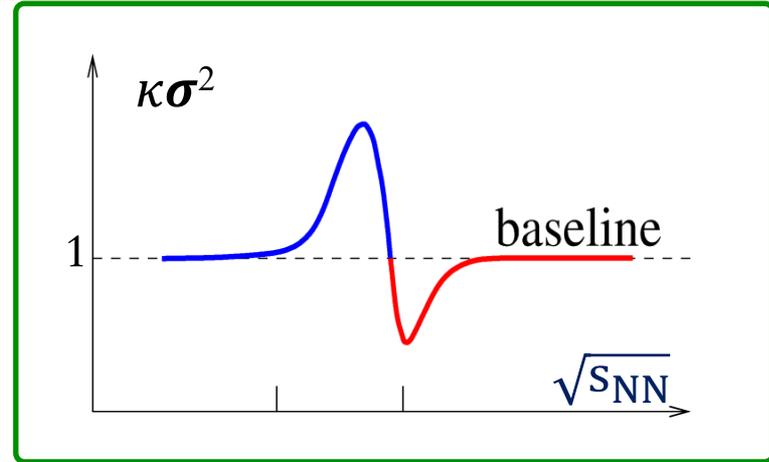
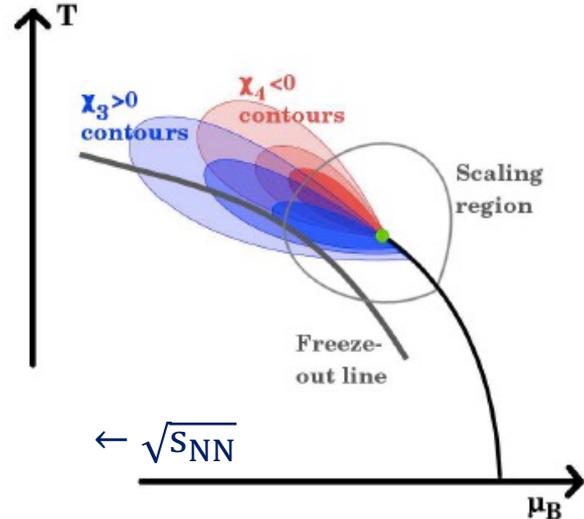
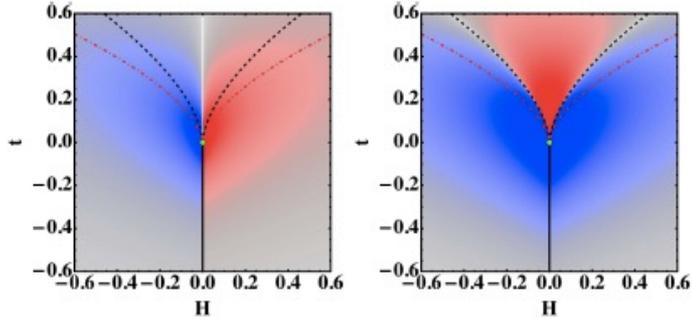
3<sup>rd</sup> order:  $S \sigma \equiv C_3 / C_2 = \chi_3 / \chi_2$

4<sup>th</sup> order:  $\kappa \sigma^2 \equiv C_4 / C_2 = \chi_4 / \chi_2$



INT 2008-2b : The QCD Critical Point

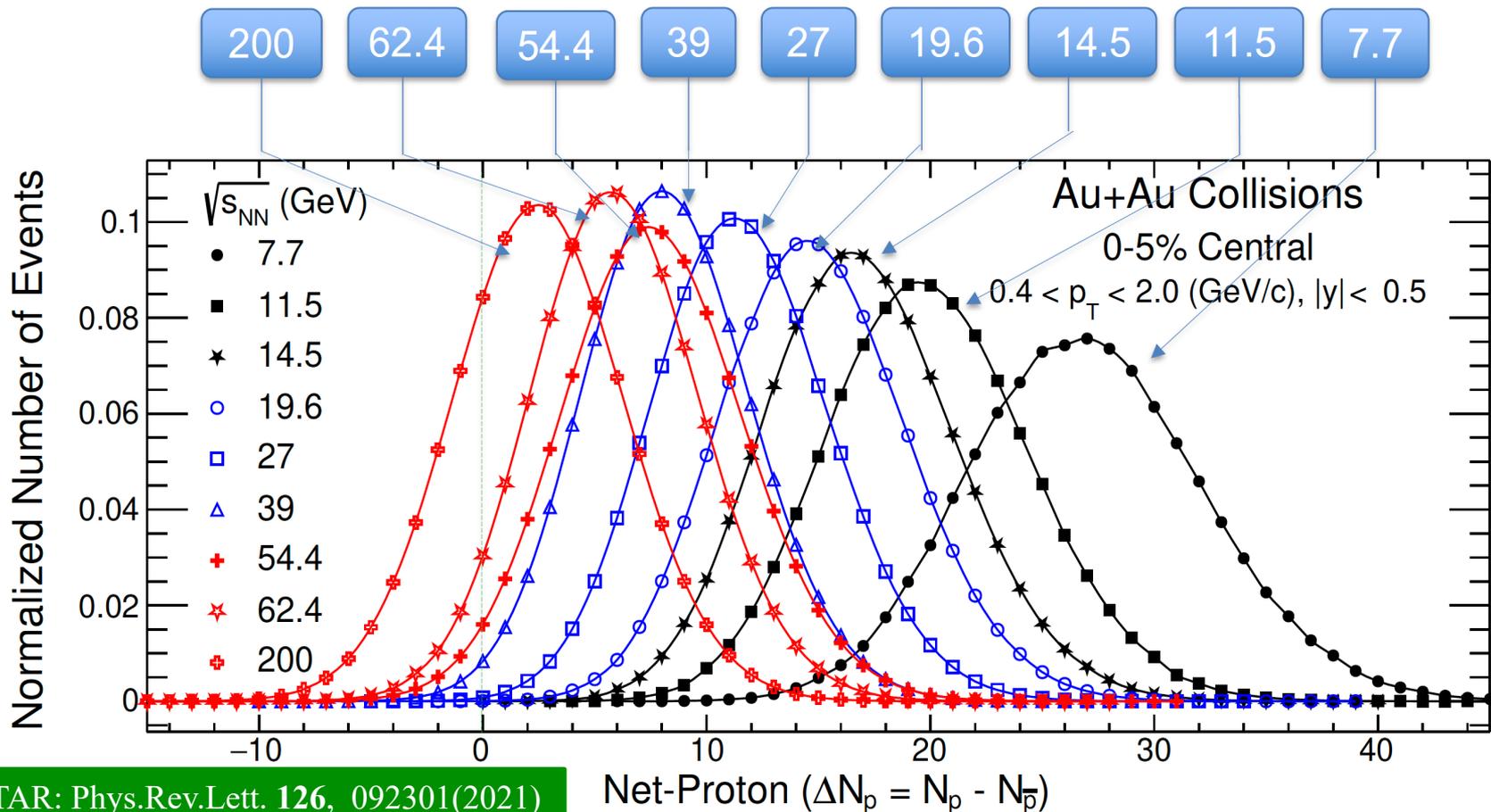
# Expectations for Models



- Characteristic “Oscillating pattern” is expected for the QCD critical point but **the exact shape depends on the location of freeze-out with respect to the location of CP**
- Critical Region (CR)

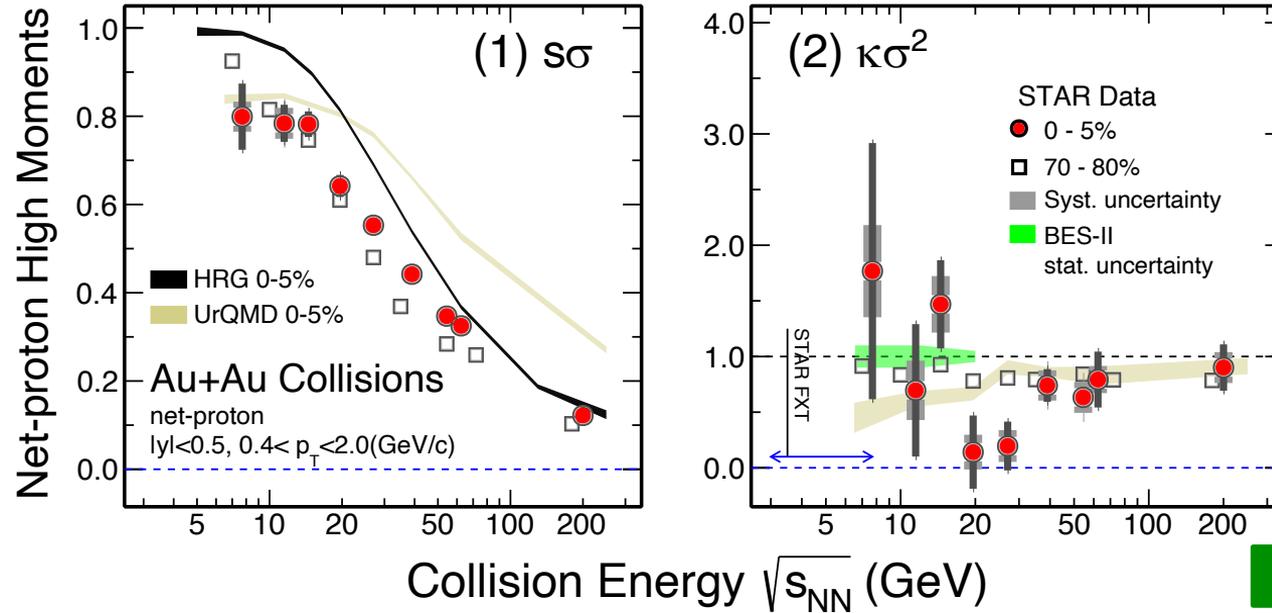
- M. Stephanov, PRL**107**, 052301(2011) - V. Skokov, Quark Matter 2012  
 - J.W. Chen, J. Deng, H. Kohyama, Phys. Rev. **D93** (2016) 034037

# Event-by-Event Net-Proton Distributions (raw)



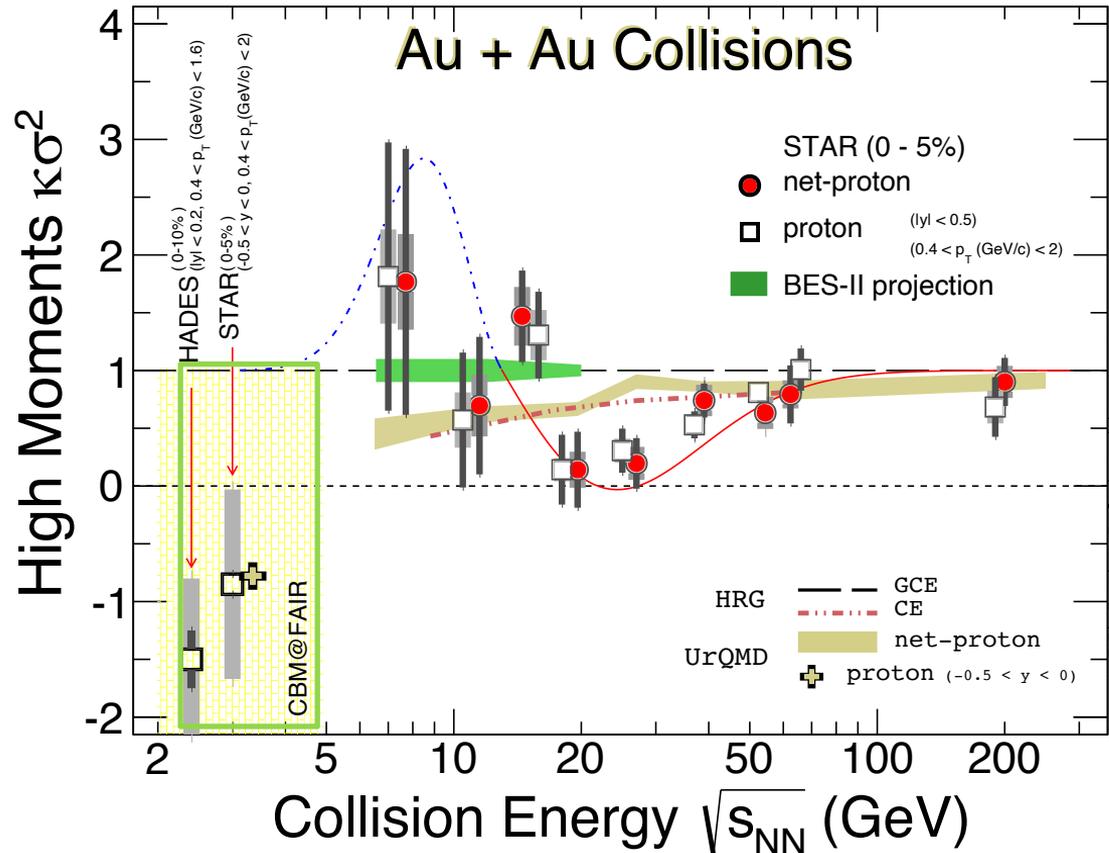
STAR: Phys.Rev.Lett. 126, 092301(2021)

# “Nonmonotonic Energy Dependence of Net-Proton Number”



- 1) HRG and transport model predicted monotonical energy dependence: AMPT, JAM, UrQMD. Suppression at low energy due to conservation;
- 2) The 3rd and 4<sup>th</sup> orders: **deviate from the Poisson limit** in the most central collisions!

# Net-p $\kappa\sigma^2$ Energy Dependence



- 1) Non-monotonic energy dependence;
- 2) 3 GeV proton high moments data → **Hadronic interaction dominant!**
- 3) Energy gap between 3 and 7.7 GeV, important for **Critical Point search**

STAR: PRL126, 92301(2021)  
 PRL128, 202303(2022)  
 HADES: PRC102, 024914(2020)

# Thermalization in Heavy-Ion Collisions

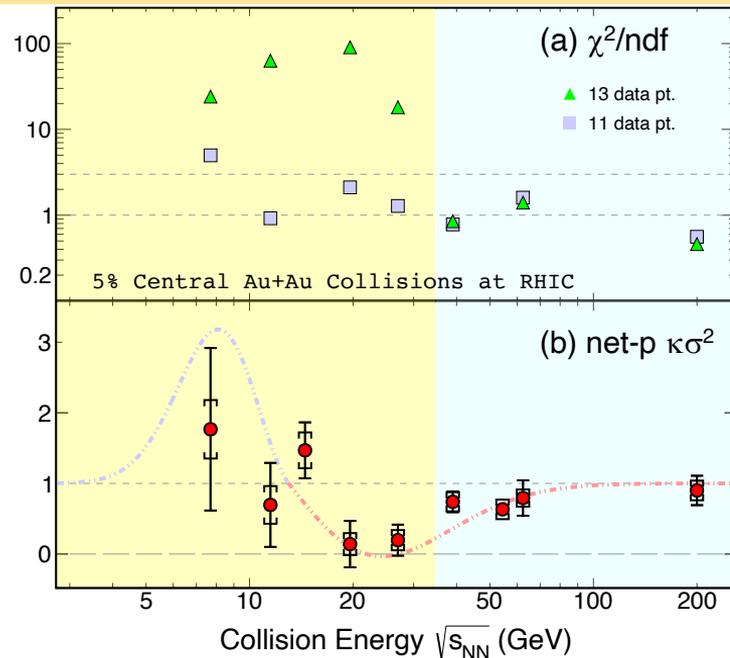
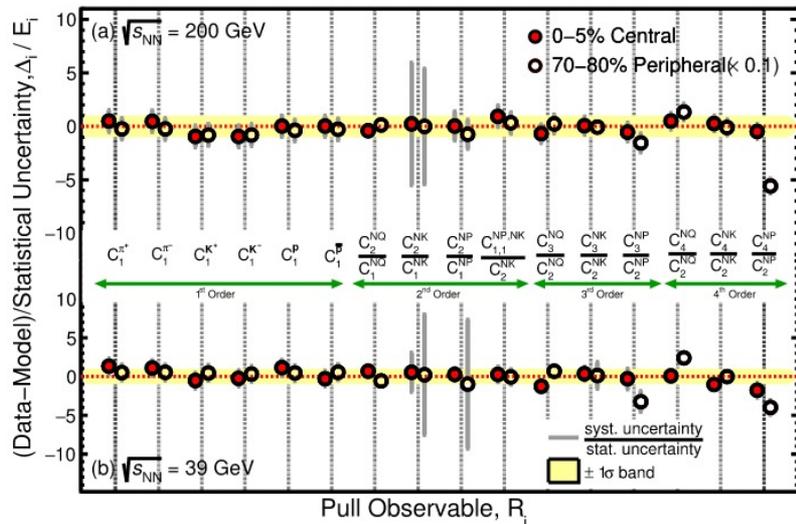
S. Gupta *et al.* Phys. Lett. **B829**, (2022) 137021



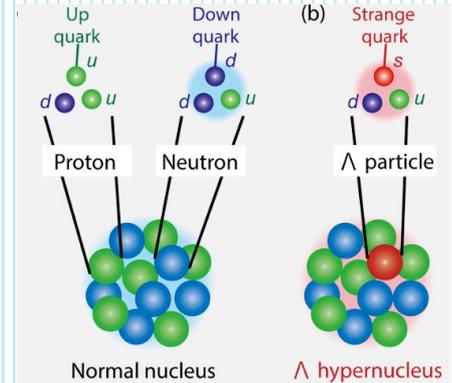
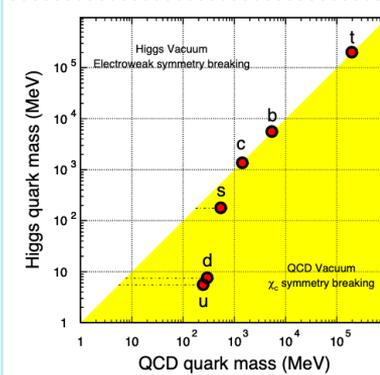
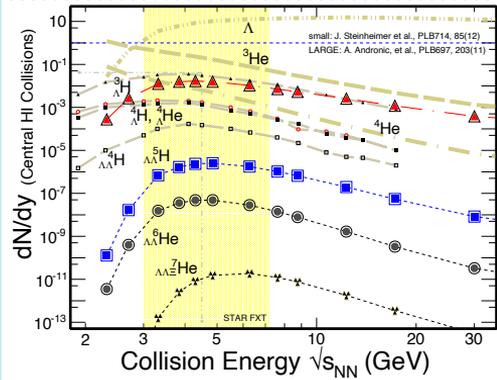
- 1) Test of the thermal model with high moments data: 4<sup>TH</sup> order;
- 2) Below 39 GeV, **data is not consistent with equilibrium.**

Limits of thermalization in relativistic heavy ion collisions

Sourendu Gupta<sup>a</sup>, Debasish Mallick<sup>b,c</sup>, Dipak Kumar Mishra<sup>d</sup>, Bedangadas Mohanty<sup>b,c,\*</sup>, Nu Xu<sup>e</sup>



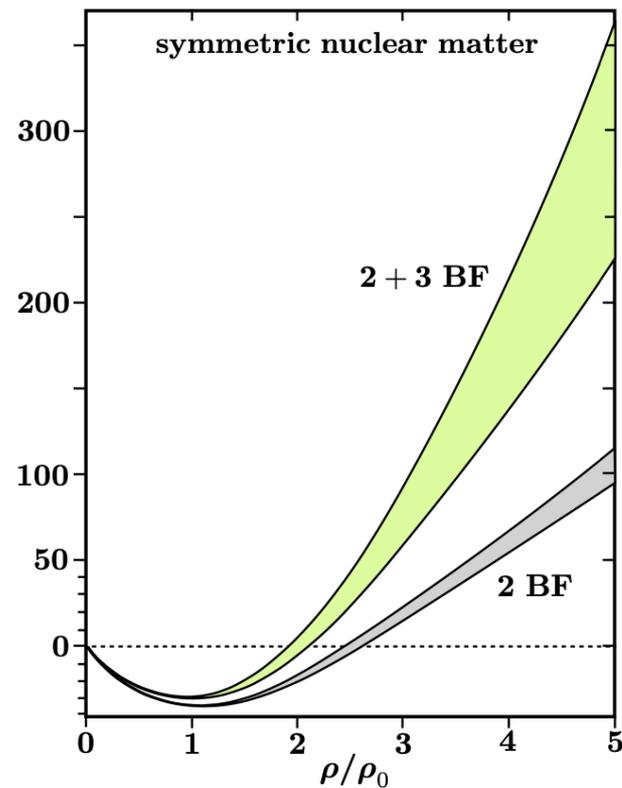
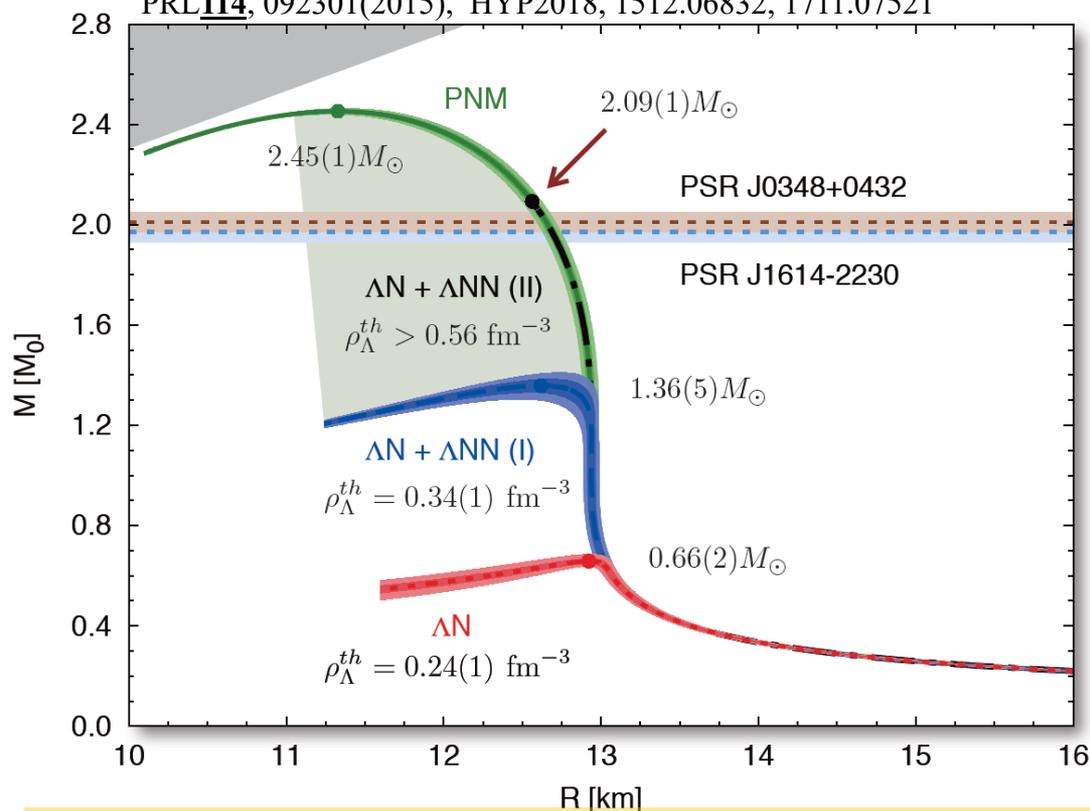
# Strangeness and Hyper-Nuclei



A. Andronic *et al.* PLB697, 203(2011)  
 J. Steinheimer *et al.* PLB714, 85(2012)

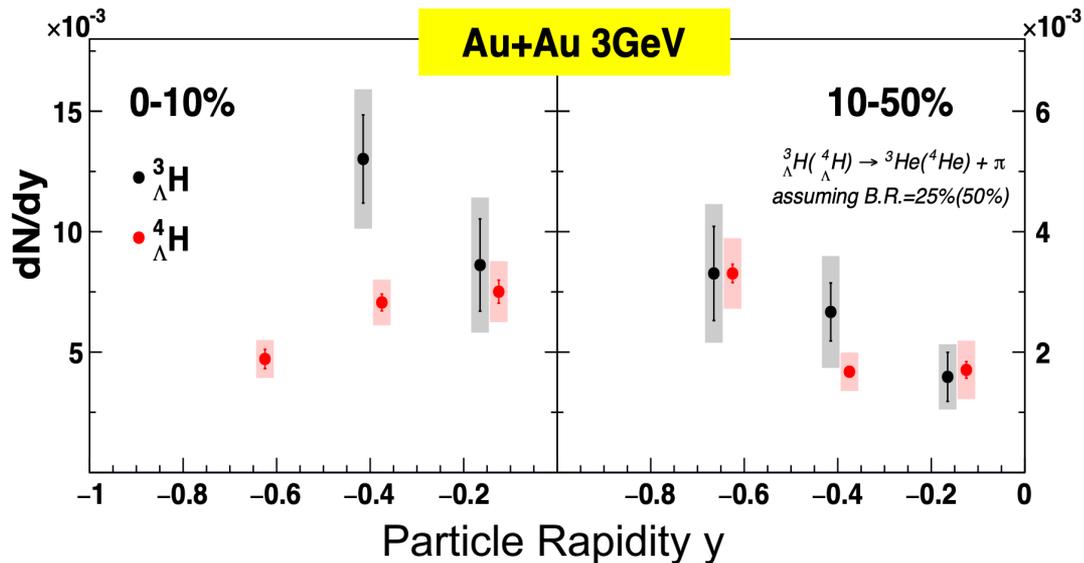
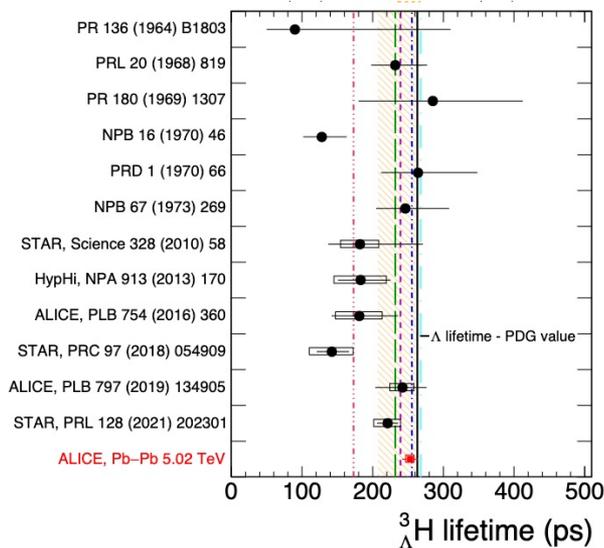
# $\Lambda$ -N Interaction inside Compact Stars

PRL **114**, 092301(2015), HYP2018, 1512.06832, 1711.07521



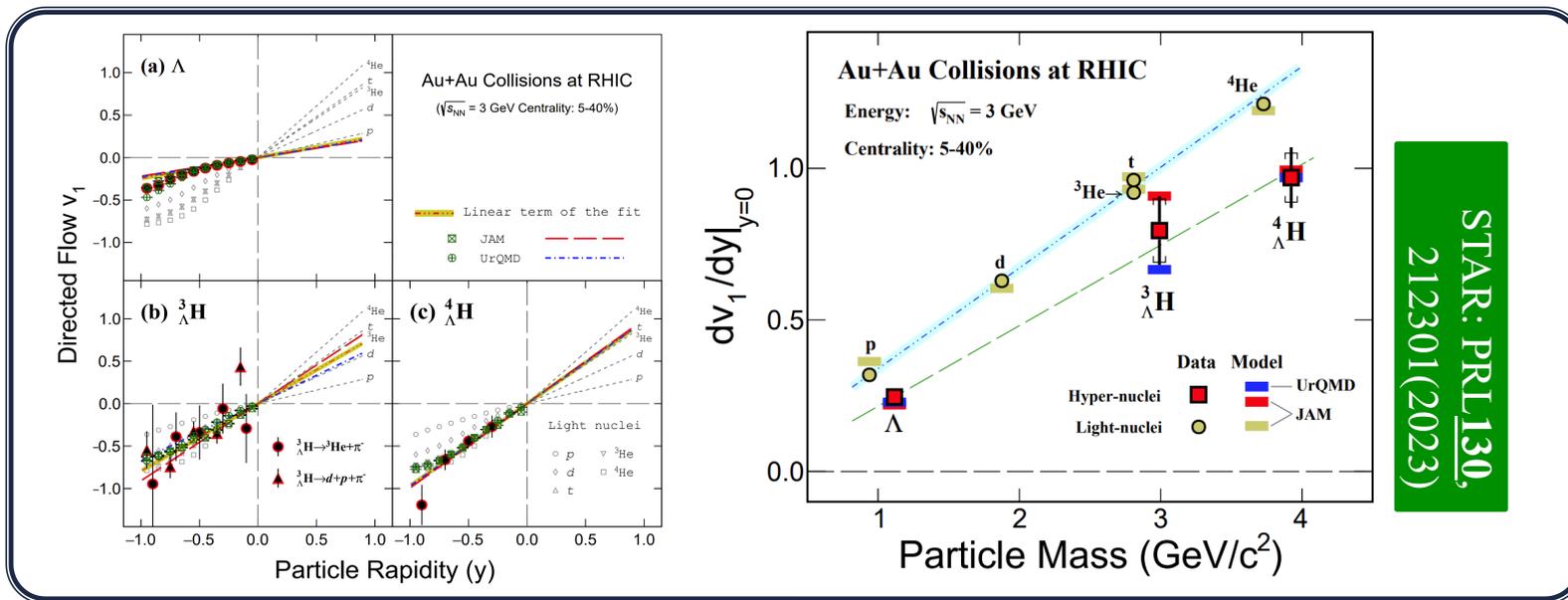
Y-N interaction: key to understand the inner structure of compact stars

# Hyper-Nuclei Lifetime and Yields



- 1) Precision results on lifetime; ALICE: 2209.07360; STAR: PRL128 202301(2022)
- 2) Abundant hyper-nuclei at the high baryon density region;
- 3) Coalescence calculations seem work for hyper-nuclei yields

# Collectivity of Hyper-Nuclei



STAR: PRL 130,  
212301(2023)

- Coalescence: the dominant procedure for hyper nuclei production;
- Hyper nuclei collectivity (e.g.  $v_1$  and  $v_2$ )  $\rightarrow$  **Y-N** and **Y-Y** interactions under finite pressure gradient;
- **Questions:** Connection to the EOS of compact stars? Effect of isospin?

# Outline

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## 1) Introduction

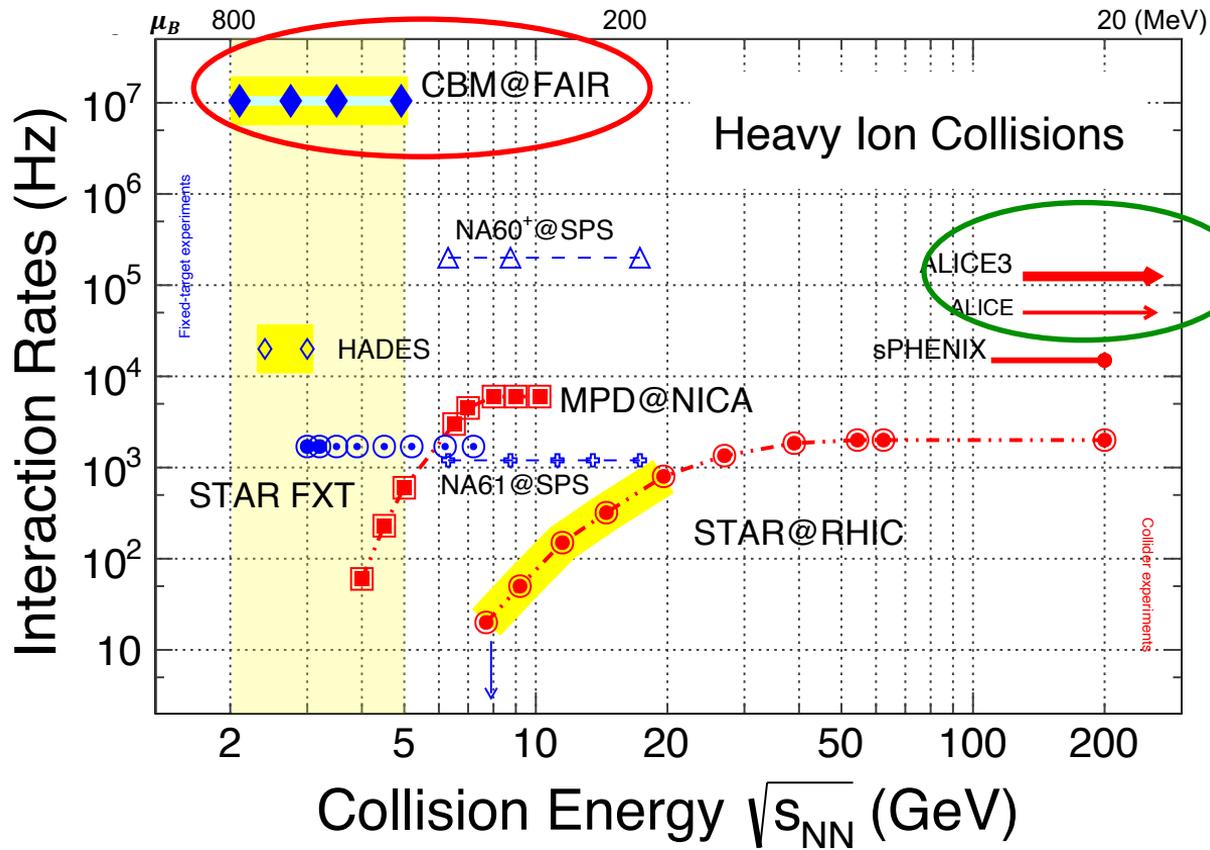
## 2) Selected Recent Results

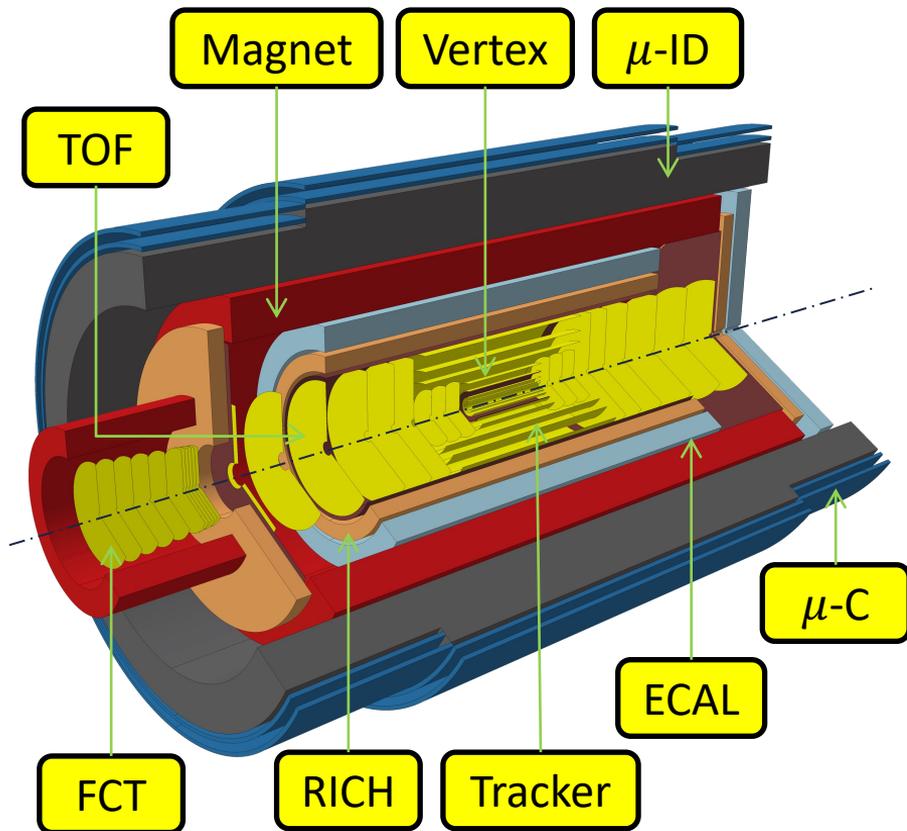
- Collectivity
- Criticality
- Hyper-nuclei Production

## 3) Future Physics Programs

# Future High Rates Experiments

- **ALICE3:**  $\mu_B \sim 0$  Properties of QGP!
- **CBM:** Unprecedented rate capability and  $\mu_B \sim 800$  MeV
  - 1) High order baryon fluctuation and correlation;
  - 2) 3D di-lepton spectra (collision centrality, pair mass and  $p_T$ );
  - 3) Hyper-nuclei production and Y-N interactions





## ALICE3: Low Mass, Large Rapidity Coverage

### Key Physics Measurements:

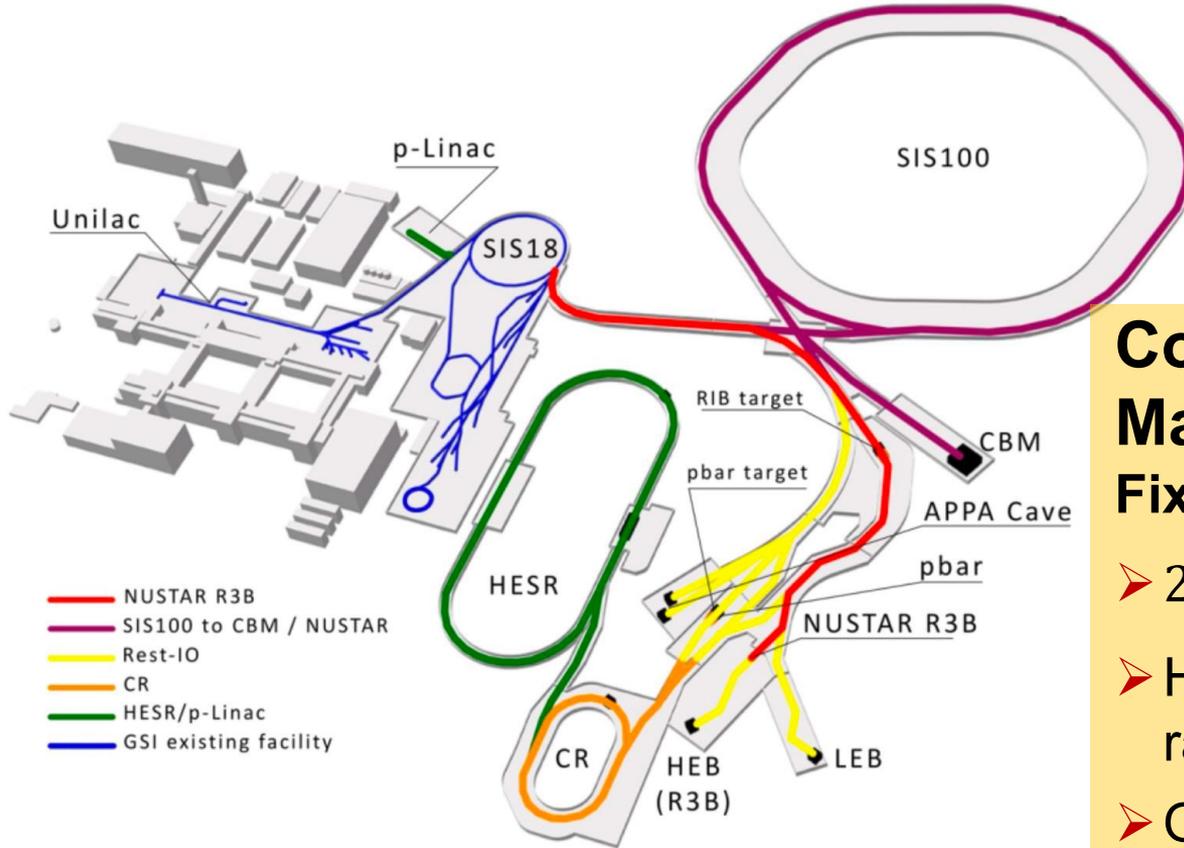
- 1) Heavy flavor: Medium effects and hadronization;

State-of-the-art detector!  
Great potentials for physics!

**A dream experiment!**

cumulants, ...

# CBM Experiment at FAIR

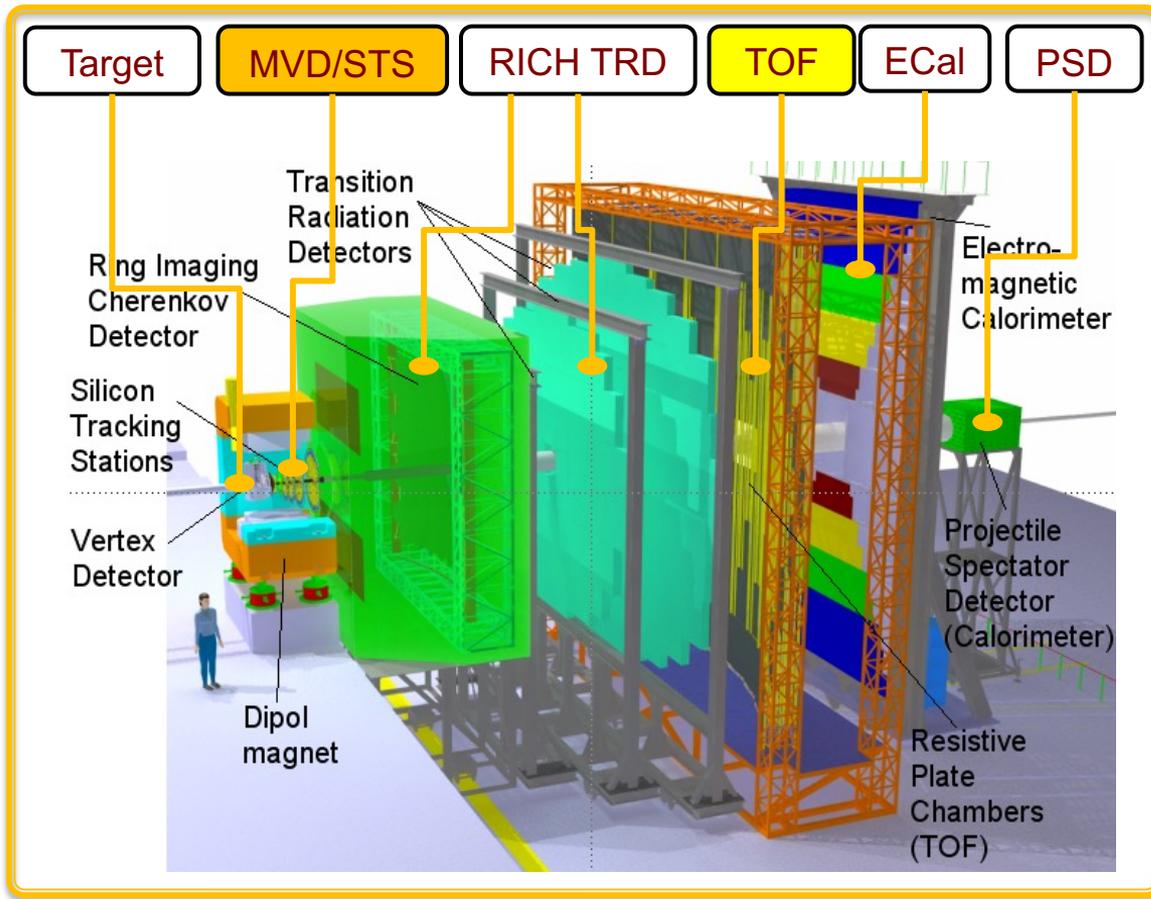


## Compressed Baryonic Matter (CBM)

Fixed-target experiment:

- $2.4 < \sqrt{s_{NN}} < 4.9$  GeV
- High intensity & collision rates up to 10MHz
- Operation starts in 2028

# CBM Experiment at FAIR



- FAIR: One of the brightest accelerator complexes
- Precision measurements at high baryon density region:
  - (i) Dileptons ( $e, \mu$ );
  - (ii) High order correlations;
  - (iii) Flavor productions ( $s, c$ ) and hyper-nuclei

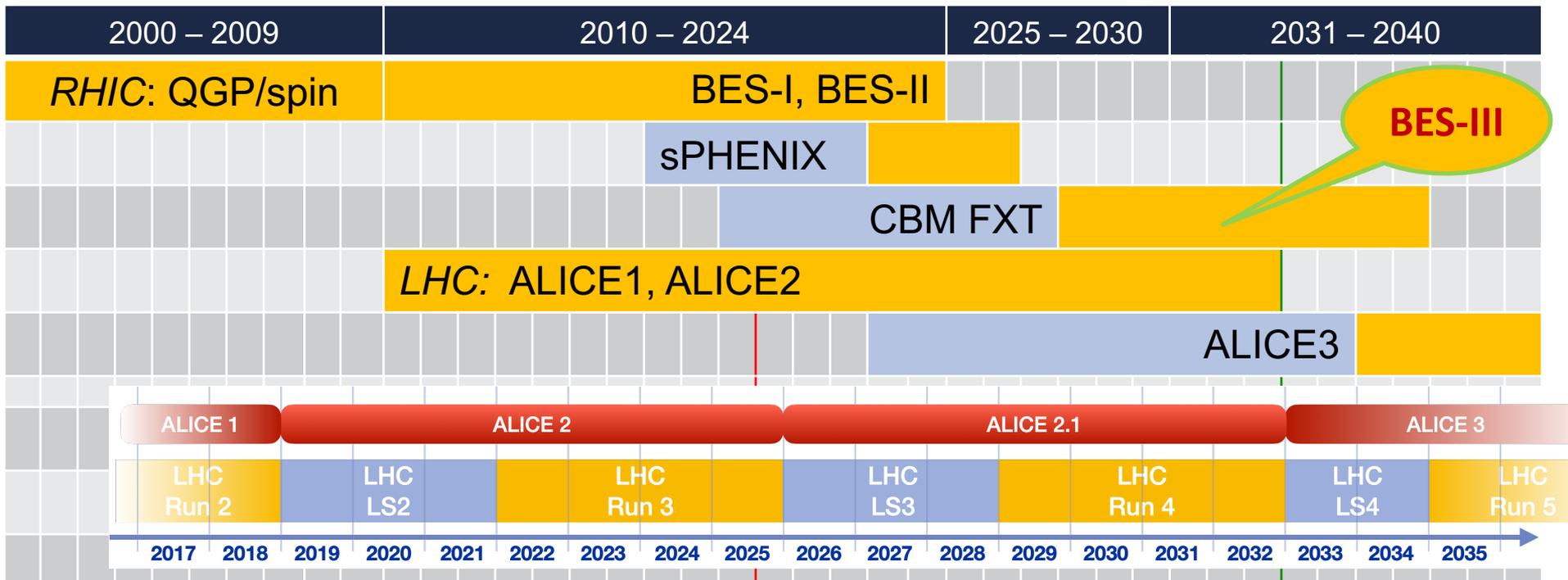
**Beam on target in 2028**

# Projects and Timelines

## Emergent Properties of QCD: Confinement & Mass of VM

### Structure of the QCD Matter

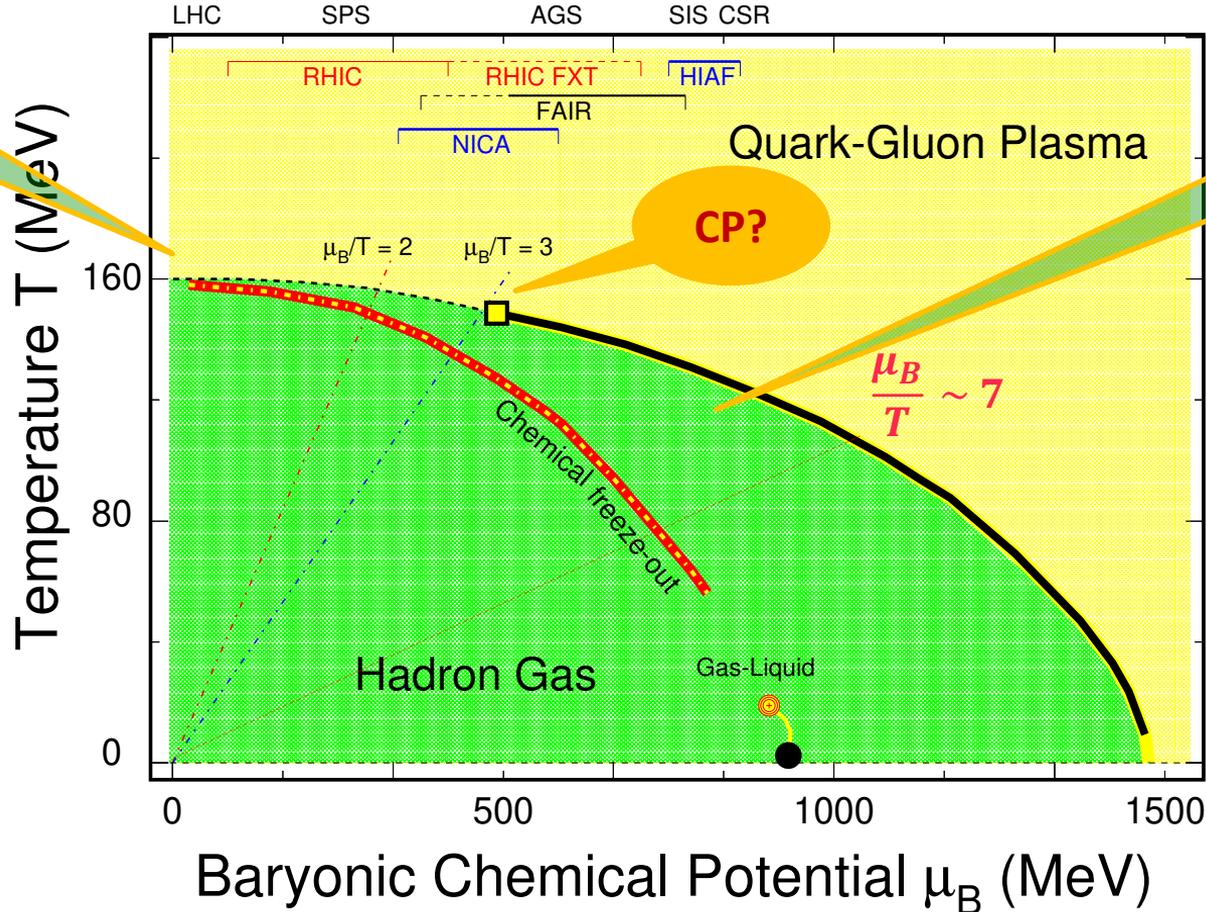
### Structure of Proton



# Future Physics Programs

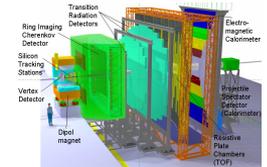
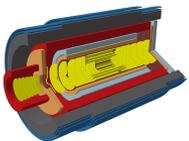
**ALICE**

**BES-II  
CBM**



- Properties of the smooth cross-over;
- p+p collisions;
- Full lepton distributions with **ALICE3**

- Critical point and phase boundary;
- Nuclear matter EOS at high baryon density;
- Y-N interactions



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**Y.P. Zhang**, **Y.J. Zhou**

// BLUE: Theory // RED: Experiment // GREEN: student

Alexander von Humboldt Foundation



EMMI



# Thank you for your attention!