SILICON TRACKING SYSTEM (STS) COOLING - CONCEPT AND EXPERIMENTAL VERIFICATION --

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- For the CBM Collaboration -

CBM-STS Cooling Engineering Design Review

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MATHEMATISCH-NATURWISSENSCHAFTLICHE FAKULTÄT Physikalisches Institut





APPROACH TOWARDS PINPOINTING STS OPERATING TEMPERATURE



ASPECT #1: IRRADIATION

How does the performance of STS sensors under irradiation dictate the sensor's operating temperature?

ASPECT #2: THERMAL MANAGEMENT & MECHANICS

Can a cooling concept be feasible enough to fulfil the input from ASPECT #1, under reasonable experimental conditions?

BIGGER PICTURE:

A collective answer to these questions will lead us to the STS operating temperature and its experimental feasibility

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ASPECT #1

IRRADIATION & INPUT TO OPERATING TEMP.

[1.1] LEAKAGE CURRENT & SIGNAL-TO-NOISE RATIO (S/N)



- The STS track reconstruction requirements mandates that the S/N \ge 10
- No deterioration in signal generation, i.e., charge collected expected till the STS EOL $\Phi_{eq} = 1 \times 10^{14} \, n_{eq(1MeV)}/cm^2$, given that up to 500 V bias voltage can be applied

I. Momot. PhD Thesis. Goethe-Universität – Frankfurt (2019)

The sensor temperature must minimize the rise of shot noise at EOL Φ_{ea}

P. Larionov, PhD Thesis, Goethe-Universität – Frankfurt (2016)

$$ENC_{IL} \propto \sqrt{I_{Leakage}} \qquad \Delta I_{Leakage} = \alpha \cdot \Phi_{eq} \cdot A \cdot d$$
$$I_{Leakage} \propto T_{sensor}^2 \cdot e^{-E_{gap}/2 \cdot k_B \cdot T_{sensor}}$$



STS sensors can be operated at $14^{+4.7}_{-6.1}$ °C throughout their operational lifetime and still maintain the ensured S/N ≥ 10

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[1.2] REVERSE ANNEALING & FULL DEPLETION VOLTAGE



- The STS sensors will operate at 500V at the EOL Φ_{eq} to recover the charge collection efficiency, i.e., deposited charge
- The operating temperatures must be low enough not to invoke reverse annealing and keep the full depletion voltage sufficiently below 500V

$$\begin{split} V &= \frac{e}{2\varepsilon} \cdot \left| N_{eff} \right| \cdot d^2 \\ N_{eff} &= N_d - \Delta N_{eff}(\Phi, T, t) \\ \Delta N_{eff}(\Phi, T, t) &= \Delta N_C(\Phi) + \Delta N_a(\Phi, T, t) + \Delta N_Y(\Phi, T, t) \end{split}$$



STS sensors can be operated at 10°C even after accumulating EOL Φ_{eq} as the full depletion voltage after 10 years of annealing (350 V) < 500V

APPROACH TOWARDS PINPOINTING STS OPERATING TEMPERATURE



ASPECT #1: IRRADIATION

How does the performance of STS sensors under irradiation dictate the sensor's operating temperature?

[1.1] Signal-to-Noise Ratio (S/N) with time and fluence Sensor Operating Temperature = $14^{+4.7}_{-6.1}$ °C

- The STS track reconstruction requirements mandates that the S/N > 10
- The operating temperatures must be low enough to minimize the rise of shot noise at EOL fluence, thereby keeping S/N safely above 10

[1.2] Reverse Annealing with time and temperature Sensor Operating Temperature = 10°C

- The STS sensors will operate at 500V at the EOL fluence to recover the charge collection efficiency, i.e., deposited charge
- The operating temperatures must be low enough not to invoke reverse annealing and keep the full depletion voltage sufficiently below 500V

Collectively, STS sensor operating temperature throughout operational lifetime must be 10°C to safely negate irradiation effects and fulfil physics requirements

ASPECT #2: THERMAL MANAGEMENT & MECHANICS

Can a cooling concept be feasible enough to fulfil the input from ASPECT #1, under reasonable experimental conditions?

ASPECT #2

THERMAL MANAGEMENT (CONCEPT & VERIFICTION)

(THERMAL) INTRODUCTION TO CBM-STS



STS-Module: Silicon Sensors + Shielded Microcables + FEE-Boards (FEBs)



- Double-sided silicon microstrip silicon sensors connected to the frontend electronics (FEEs) via ultra-light shielded microcables
- End-of-Lifetime (EOL) radiation up to $10^{14} n_{eq}/cm^2$ (1 MeV eq.)
- FEEs outside the physics aperture dissipating approx. 25W per module

STS Stations (Tracking Layers, including peripherally located electronics & services)



- 8 tracking stations, 0.3 1.0 m downstream target
- $\approx 4 \text{ m}^2$ area, 876 modules, 1.8 M channels
- Sensors mounted to carbon-fibre ladders
- Material budget per station: $\approx 0.3\% 2\% X_0$
- Total FEE power dissipation of approx. 40 kW
- Located inside an aluminium-cladded CF-Foam thermal and electromagnetic enclosure

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(THERMAL) INTRODUCTION TO CBM-STS





SILICON SENSOR COOLING

- Power dissipation \approx 40 mW/cm² at +10°C (only after STS EOL $\Phi_{eq} = 1 \times 10^{14} n_{eq(1MeV)}/cm^2$)
- Target Temp. ≤ +10°C, by adding minimal material budget



OBSERVABLE: (MARGIN FROM) THERMAL RUNAWAY



Non-Ionizing Radiation Damage \propto Defects in Si-Lattice \propto Intermediate Energy States \propto (Higher) Leakage Current

 $ENC_{IL} \propto \sqrt{I_{Leakage}} \qquad \Delta I_{Leakage} = \alpha \cdot \Phi_{eq} \cdot A \cdot d$ $I_{Leakage} \propto T_{sensor}^{2} \cdot e^{-E_{gap}/2 \cdot k_{B} \cdot T_{sensor}}$





If the Cooling Power can't neutralise the Heating Power caused due to high STS irradiation environment, then this self-feeding system goes into '<u>Thermal Runaway</u>'

[2.1] STS COOLING CONCEPT

SILICON SENSORS: COOLING CONCEPT []



- Only the innermost sensors ($\Delta x = \Delta y \le \pm 10$ cm) on a given STS station will be exposed to EOL fluence
- The power dissipation of STS sensors is highly non-uniform and follows the fluence distribution (falls exponentially in radial direction)



<u>Innermost sensors</u>: Actively air cooled by perforated tubes <u>Peripheral sensors</u>: Passively air cooled by natural convection



SILICON SENSORS: COOLING CONCEPT [I]









$$Nu = 0.5K \left(A_r \frac{H}{D}\right) G \left(A_r \frac{H}{D}\right) Re^{2/3} P r^{0.42}$$

where,

$$K = \left[1 + \left(\frac{H/D}{0.6/A_r^{1/2}}\right)^6\right]^{-0.05}$$

H. Martin, Advances in Heat Transfer, Vol. 13, Academic Press, New York, 1977

$$G = 2A_r^{1/2} \frac{1 - 2.2A_r^{1/2}}{1 + 0.2(H/D - 6)A_r^{1/2}}$$

and the valid within the following range

 $[2000 \le Re \le 400,000]$ $2 \leq H/D \leq 12$ $0.004 \leqslant A_r \leqslant 0.04$ $4 \leq S \leq 14$





Y.A. Cengel and R.H. Turner. Fundamentals of Thermal-fluid Sciences. McGraw-Hill series in mechanical engineering. McGraw-Hill Companies, 2004. ISBN: 9780072976755

$$Nu = \frac{hL}{k} = \frac{\dot{q}L}{k(T_s - T_\infty)}$$
$$Nu = \left\{ 0.825 + \frac{0.387 Ra_L^{1/6}}{\left[1 + (0.492/Pr)^{9/16}\right]^{8/27}} \right\}^2$$

hL

where,

$$Ra_L = Gr_L Pr$$
$$Gr_L = \frac{g\beta(T_s - T_\infty)L^3}{\nu^2}$$

S. W. Churchill and H. Chu, International Journal of Heat and Mass Transfer 18.11 (1975), pp. 1323–1329

SILICON SENSORS: COOLING CONCEPT



- Only the innermost sensors ($\Delta x = \Delta y \le \pm 10$ cm) on a given STS station will be exposed to EOL fluence
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<u>Innermost sensors</u>: Actively air cooled by perforated tubes <u>Peripheral sensors</u>: Passively air cooled by natural convection



• Advantage: Low material budget, respective empirical formulations for both cases allow to predict the thermal behaviour (temp., runaway, ...)

Impinging Jets: H. Martin, Advances in Heat Transfer, 13 (1977) Natural Convection: S. W. Churchill and H. Chu, International Journal of Heat and Mass Transfer, 18.11 (1975)

 Perforated tube's geometry has been optimized within STS boundary conditions to reduce the tube diameter and ensure flow balancing amongst all perforations Calculation details in backup

SILICON SENSORS: THERMAL RUNAWAY (CFD & CALCULATIONS)

Impinging air jets for centrally located ladders

- Ladder with the highest power dissipation in STS (40 mW/cm² at 10^oC)
- Calculations and CFD simulations for different flow rates per perforated tube (20 ... 40 L/min) and varying ambient air temperatures
- Reasonable agreement observed between calculations and CFD simulations for all considered cases

Natural air convection for peripherally located ladders

- Ladder with sensors with highest power dissipation to be cooled by natural air convection (2.5 mW/cm² at 10°C)
- Reasonable agreement observed between calculations and CFD simulations for all considered cases

Sensor cooling concept leads to sensors at 10°C (at EOL fluence) for ambient air temp. of 5°C with sufficient margin from thermal runaway. Can the ambient air in the STS be kept at these temperatures by neutralizing 50 kW worth of other heat sources?

FRONT END ELECTRONICS: COOLING CONCEPT []

Since the FEB boxes carrying the FEEs are only 25...50 cm away from the innermost silicon sensors, the temperature gradient between the two must be minimal, i.e., FEEs should be at 0°C

Front-End Electronics Box (FEB-Box)

- FEB box host up to 5 fins/10 front-end electronics boards (FEBs), with total power dissipation of approx. 100 W
- Provide a thermally conducting pathway to the cooling plate
- Modular design with several thermal interface materials (TIMs)

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FRONT END ELECTRONICS: COOLING CONCEPT [I]

Since the FEB boxes carrying the FEEs are only 25...50 cm away from the innermost silicon sensors, the temperature gradient between the two must be minimal, i.e., FEEs should be at 0°C

Cooling Plate

- Cooling plates are foreseen to remove power dissipation of up to 1 kW
- Coolant to be used here 3M NOVEC 649
- Plates manufactured by "Friction Stir Technology"
 - Flexibility to add threaded connections for inlet-outlet
 - Flexibility to mill fluid channels to enhance local heat transfer coefficient and cooling performance
- Maximum bulging on the cooling plate under 5 bar(g) is < 100 μm
 Measurement details in backup

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FRONT END ELECTRONICS: CFD & THERMAL SIMULATIONS

A combination of CFD simulations for the cooling plate and thermal simulations for the FEB box show that the coolant temperature of -40°C (-20°C) leads to the max. FEB temp. of < -10°C (+10°C)

What is the interplay between the coolant/FEB temp. and the silicon sensors?

-31.52

-32.18

-32.84 -33.50 -34.17 -34.83

-35.49

Temperature

0

[2.2] EXPERIMENTAL VERIFICATION - THERMAL DEMONSTRATOR -

THERMAL DEMONSTRATOR: CONCEPT

Thermal demonstrator aims to experimentally verify the sensor and FEE cooling concept under (quasi-)realistic boundary conditions

- Three STS-like half-stations with one "active" layer (power dissipation of approx. 1 kW) sandwiched between two "passive" layers
- Sensor cooling done with perforated CF-tubes
- FEE cooling done with 3M NOVEC 649

- Dummy silicon sensor heaters and FEE heaters
- STS-like peripheral services, such as electronics and coolant feedthroughs, coolant manifold, valves and transfer lines
- CF-AIREX based thermal enclosure, with actively cooled panels

THERMAL DEMONSTRATOR: COMPONENTS []

Humidity Monitoring System

HYT221 Michell ES20 FBG Hygrometer

C-Frame assembled with heat sources mounted on ladders, along with cooling elements and power distribution

THERMAL DEMONSTRATOR: COMPONENTS [II]

NOVEC Manifold and Feedthroughs

Thermal Enclosure made from CF-AIREX sandwich panels, cladded with aluminised-Kapton sheets and cold plates on the side panels

THERMAL DEMONSTRATOR: COMPONENTS [III]

NOVEC Chillers

Option #1 Julabo Presto W50 (-20 ... +20°C)

 $\frac{\text{Option #2}}{\text{Custom-made NOVEC Chiller (CO}_2 \text{ in primary cycle)}}$ (-40 ... -20°C)

I. Eliazov. STS-FEE Cooling Plant. FTDM 2023 | Link

Air Handling System

Dry Air Dewpoint = down to approx. -70°C Cold Air Temperature= -15 ... +30°C

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THERMAL DEMONSTRATOR: CONCEPT & COMPONENTS [IV]

STS Thermal Demonstrator – Assembled and Running... 😳

FIRST RESULTS: THERMAL RUNAWAY BEHAVIOUR AT EOL FLUENCE

- FEE Power Dissipation = Approx. 1 kW
- NOVEC Temperature = -20°C (Julabo Presto W50)
- Ambient Dew Point = below -70°C
- Ambient Overpressure = 12...13 mbar
- Cold plates on side panels OFF
- Inlet Air Temperature = 24...25°C
- Sensor power dissipation across the half-station varied proportional to the expected EOL radiation damage distribution

When using perforated-tube based active air cooling, the innermost STS sensors can be safely operated at 9°C at EOL fluence with sufficient margin from thermal runaway while using NOVEC at -20°C

APPROACH TOWARDS PINPOINTING STS OPERATING TEMPERATURE

ASPECT #1: IRRADIATION

How does the performance of STS sensors under irradiation dictate the sensor's operating temperature?

[1.1] Signal-to-Noise Ratio (S/N) with time and fluence Sensor Operating Temperature = $14^{+4.7}_{-6.1}$ °C

- The STS track reconstruction requirements mandates that the S/N > 10
- The operating temperatures must be low enough to minimize the rise of shot noise at EOL fluence, thereby keeping S/N safely above 10

[1.2] Reverse Annealing with time and temperature Sensor Operating Temperature = 10°C

- The STS sensors will operate at 500V at the EOL fluence to recover the charge collection efficiency, i.e., deposited charge
- The operating temperatures must be low enough not to invoke reverse annealing and keep the full depletion voltage sufficiently below 500V

Collectively, STS sensor operating temperature throughout operational lifetime must be 10°C to safely negate irradiation effects and fulfil physics requirements

ASPECT #2: THERMAL MANAGEMENT & MECHANICS

Can a cooling concept be feasible enough to fulfil the input from ASPECT #1, under reasonable experimental conditions?

[2.1] Concept: Simulations and Calculations

- Sensors can be cooled down to 10°C (at EOL fluence) for ambient air temp. of 5°C with sufficient margin from thermal runaway
- 3M NOVEC 649 temperature should be -40°C (-20°C) to neutralize the FEBs at -10°C (+10°C)

[2.2] Verification: Thermal Demonstrator and other setups

- 3M NOVEC 649 at -20°C inside 12 mm thick friction-stir welded plates can neutralize the FEB power dissipation
- Perforated tubes with air flow of 30 L/min leads to stable sensor operating temperature of 9°C, with 30°C margin from runaway
- Acceptable vibrations induced by airflow
- FEBs survive thermal cycling at FEB coolant temperature of -20°C

Thermal management concepts and mechanics can ensure the STS sensor temperature of approx. 10°C, i.e., 3M NOVEC 649 temperature of -20°C

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CBM-FAIR

FACILITY FOR ANTI-PROTON AND ION RESEARCH (FAIR)

SIS-100 Capabilities					
Beam	Z	А	E _{max} [AGeV]		
р	1	1	29		
d	1	2	14		
Са	20	40	14		
Au	79	197	11		
U	92	238	10.7		

C. Höhne et al. (2011) CBM Experiment. In: B. Friman (eds) The CBM Physics Book. Lecture Notes in Physics, vol 814. Springer

M. Durante et al., Phys. Scr. 2019, 94, 033001

- Intensity gain: x 100 1000 (~10⁹/s for Au)
- Energy gain: 10 x energy (compared to SIS-18@GSI)
- Antimatter: antiproton beams
- Precision: System of storage and cooler rings

- Current estimate: SIS100 commissioning with beams starts in 2028-29
- Recommendation from Heuer-Tribble Committee: downscale FAIR project (SIS100 & SFRS/R3B & CBM); Decision by FAIR council expected in Feb. 2023

VOTE OF CONFIDENCE FOR CBM-FAIR

GSI Press Release – <u>Link</u> Report PDF – <u>Link</u>

CBM PHYSICS GOALS

Unanswered fundamental questions for QCD at high densities

- Equation of State (EoS) of symmetric nuclear (and asymmetric neutron) matter at neutron star core densities
- Phase structure of QCD matter (1st-order phase trans.? critical point?)
- Chiral symmetry restoration at large μ_B
- Bound states with strangeness
- Charm in cold and dense matter

Bengt L. Friman Claudia Höhne Jörn E. Knoll Stefan K.K. Leupold Jorgen Randrup Ralf Rapp Peter Senger Editors

LECTURE NOTES IN PHYSICS 814

The CBM Physics Book

Compressed Baryonic Matter in Laboratory Experiments

Lect. Notes Phys. 814 (2011) pp.1-980 DOI: 10.1007/978-3-642-13293-3 Eur.Phys.J.A 53 (2017) 3, 60 DOI: 10.1140/epja/i2017-12248-y

RECENT (& BRIEF) ACHIEVEMENTS IN DETECTOR PROJECTS

Beam Monitoring (BMON) Detector

pcCVD diamond sensor (16-ch) for high-intensity tests

Superconducting Dipole Magnet

Magnet Yoke housed in BINP (Russia). Tendering for replacement started.

Micro-Vertex Detector (MVD)

MVD's TDR accepted. Improved MIMOSIS-2 being submitted.

Silicon Tracking System (STS)

Pre-series STS module production for E16 (J-PARC) exp.

Muon Chambers (MUCH)

RPCs at tested at nominal rates at GIF++ (Nov.21)

Ring Imaging Cherenkov (RICH) Detector

Photocamera and Mechanical Prototypes (Mirror Wall)

Transition Radiation Detector (TRD)

TRD-2D-addendum submitted. TRD-1D pre-production by Q1-2023.

Full-size counters (all types) built and tested

for high-rate and longer-term tests

Projectile Spectator Detector (PSD)

Efforts to replace PSD with HADES-like FWALL. Still open issue.

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STS SENSOR COOLING

SENSOR COOLING CONCEPT (JETS AND CONVECTION)

Non-ionizing energy loss, n_{eq}/cm^2 after 1 month at Z = 30.0 cm from target

0

- Only the innermost sensors of all stations (x,y ≤ ± 10 cm → 4 ladders) requires active cooling because of the higher fluence or higher power dissipation (> 1mW/cm² at -10°C)
- The peripheral sensors of all stations are aimed to be cooled by natural convection

Online Tool: <u>https://fair-center.eu/fileadmin/fair/experiments/CBM/tmp/CBM_FLUKA.htm</u>

100 X. cm

50

-50

-20

-40

-100

SENSOR COOLING CONCEPT (JETS AND CONVECTION)

Impinging jets are commonly used to achieve enhanced coefficients for convective heating, cooling, or drying

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STS FRONT-END ELECTRONICS COOLING

REQUIREMENTS ON ELECTRONICS COOLING

TRANSITION FROM BI-PHASE CO₂ TO MONO-PHASE 3M NOVEC 649

58 μ m, strip lengths between 20 and 60 mm, and a thickness of 300 μ m of silicon. According to the CBM running scenario the maximum non-ionizing dose for the sensors closest to the beam line does not exceed $1 \times 10^{14} n_{eq} \text{ cm}^{-2}$. The STS is operated in a thermal enclosure that keeps the sensors at a temperature of about -5° C. The heat dissipated in the read-out electronics is removed by a CO_2 cooling system. The mechanical structure of the detector system including

J.M. Heuser (eds.) *et al., Technical Design Report for the CBM Silicon Tracking System (STS)* – GSI Report 2013-4 (2013)

Biphase CO_2 (GWP = 1)

- **Operational in various trackers at (HL-)LHC, ISS**
- **Great performance**

•

- $H = 150 \text{ kJ/kg} (at -20^{\circ}C)$
- low pressure drop; $\nu = 0.14 \text{ cSt} (\text{at} - 23^{\circ}\text{C})$
- $h_{vol} = 10 \text{ kW/m^2.K}$ smaller tubes;
- uniform temperature •

less mass flow;

- Higher system pressures i.e., safety regulations
- Potentially difficult for commercial manufacturing (2PACL-type system)

CBM-STS FEE Cooling Conceptual Design Review, 10.12.2019 | Link

Monophase 3M NOVEC 649 (GWP = 1)

- To be used in LHCb Sci-Fi Tracker. Considered for more... \checkmark
- **Relatively lower performance** X
 - higher mass flow;
 - higher pressure drop;
 - larger tubes;

 $c_p = 1.1 \text{ kJ/kg.K}$

- $\nu = 0.70 \text{ cSt} (\text{at} 40^{\circ}\text{C})$
- h_{vol} = 2 kW/m².K
- non-uniform temperature
- Lower system pressures i.e., safe to use \checkmark
- **Easier commercial manufacturing**

Based on recommendations from CERN, CBM and industrial experts, the coolant for STS-FEE is NOVEC 649

Heat Sources	Power Dissipation [kW]
Front End Electronics (FEE)	24.2
Readout Boards (ROBs)	4.7
Power Boards (POBs)	18.1
Heat transfer through thermal enclosure	4
Low Voltage (LV) Cables	3
Total Power Dissipation [kW]	54

Table 2: Breakdown of major power dissipation contributions by their sources. These are approximate values only which represent the worst case scenario and are dependent on the specific setting at which the electronics are operated (e.g. value of charge-sensitive-amplifier, efficiency of the DC-DC converters, etc) [9].

CFD SIMULATIONS – COOLING PLATE

-33.8 °C

-28.2 °C

1.32 bar

Temperature outlet:

Pressure loss:

Max. temp. of cooling plate:

THERMAL FEA SIMULATIONS – FEB BOX

THERMAL FEA SIMULATIONS – FEB BOX

Since the temp. exposed to the environment (i.e., temp. 'seen' by the silicon sensors) is ~ -20°C which is much lower than -10°C, there is substantial headroom for increasing the coolant temp. from -40°C

BABY COOLING PLANT – SIMPLIFIED P&ID

- All coolants used in this concept are GWP = 1, which makes this cooling plant usable for coming decades
- 'Simple' to manufacture commercially by using established technology and industrial practices
- To be used by STS for the Thermal Demonstrator and detector assembly procedure & testing

BABY COOLING PLANT – COMPLETE P&ID

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compact

modeling methods are described in [17, 18]. Correlations from Martin [19] ⁵ are considered here as they are widely used to determine the Nusselt number (Nu) and consequently, the convective heat transfer coefficient for impinging gas jets for a range of geometrical features (see Fig. 11) and flow rates (in terms of Reynolds Number (Re), which are described below in Eq. 2.4, 2.5:

Figure 11: Plan view of an in-line array of round jets [21].

$$Nu = 0.5K \left(A_r \frac{H}{D}\right) G \left(A_r \frac{H}{D}\right) Re^{2/3} Pr^{0.42} \quad (2.4)$$

where,

$$K = \left[1 + \left(\frac{H/D}{0.6/A_r^{1/2}}\right)^6\right]^{-0.05}$$
(2.5a)

$$G = 2A_r^{1/2} \frac{1 - 2.2A_r^{1/2}}{1 + 0.2(H/D - 6)A_r^{1/2}}$$
(2.5b)

and the valid within the following range

$$\begin{bmatrix} 2000 \leqslant Re \leqslant 400,000 \\ 2 \leqslant H/D \leqslant 12 \\ 0.004 \leqslant A_r \leqslant 0.04 \\ 4 \leqslant S \leqslant 14 \end{bmatrix}$$

Figure 13: (a) Variation of the volumetric air flow rate $[L/\min]$ from each hole for various tube diameters (D_0) or area ratios (α) . The plot is only for half of the tube's actual length because the air flow is expected to be symmetric when air inlet is from both ends of the tube. (b) The same plot as shown in the left. This shows the deviation of flow rate per hole from the average flow rate, where the error bars show the extent of flow deviation from the left plot.

Inner Diameter (D_0)	3.50 mm
Shell Thickness	$0.25 \mathrm{~mm}$
Material Budget (local)	$0.68\% \text{ x/X}_0$
Material Budget (averaged over sensor area)	$0.02\% \text{ x/X}_0$
Pitch (S)	14 mm
Length (L) per half	$100 \mathrm{mm}$
Number of Holes (N) per half	8
Height (H) from the innermost sensor of a normal (central) ladder	12 mm (10.5 mm)

Table 3: Properties of the carbon-fibre based perforated tube. Since gas flow will enter from both sides of the tube, values for tube length and number of holes are quoted for half of the tube's actual length.