

# Insights of many body degrees of freedom in (p,pN) reactions

**Raquel Crespo**

Collaboration: E. Cravo, A. Deltuva, R.B. Wiringa, D. Jurčiukonis, M. Piarulli, A. Arriaga



# Synopsis

- Motivation

- Revisit  ${}^A X(p, pN)$  at 400 MeV/u (inverse kinematics) for light nuclei

E. Cravo, R.B. Wiringa, R. Crespo, A. Arriaga, A. Deltuva and M. Piarulli

- Revisit  ${}^{12}\text{C}(p, 2p)$  at 100 MeV/u (direct kinematics) measured at IUCF

A. Deltuva, E. Cravo, R. Crespo, D. Jurciukonis, submitted for publication

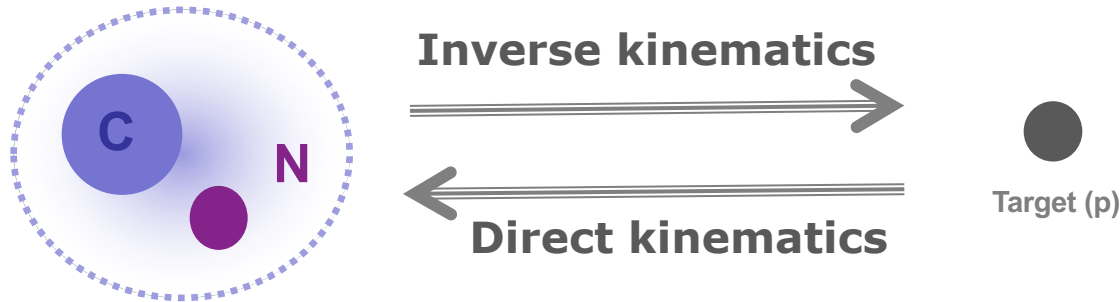
- Dynamical core excitation signatures in kinematical fully exclusive observables

E. Cravo, R. Crespo, A. Deltuva

- Perspectives

# Motivation

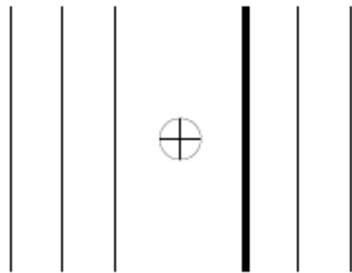
## ➤ Truncated Hilbert space



## ➤ Spectator core during the scattering process

One-nucleon **spectroscopic overlaps** (its strength being the **SF**) become the structure input to the reaction formalism.

$$\mathcal{H} = \mathcal{H}_g \oplus \mathcal{H}_x$$



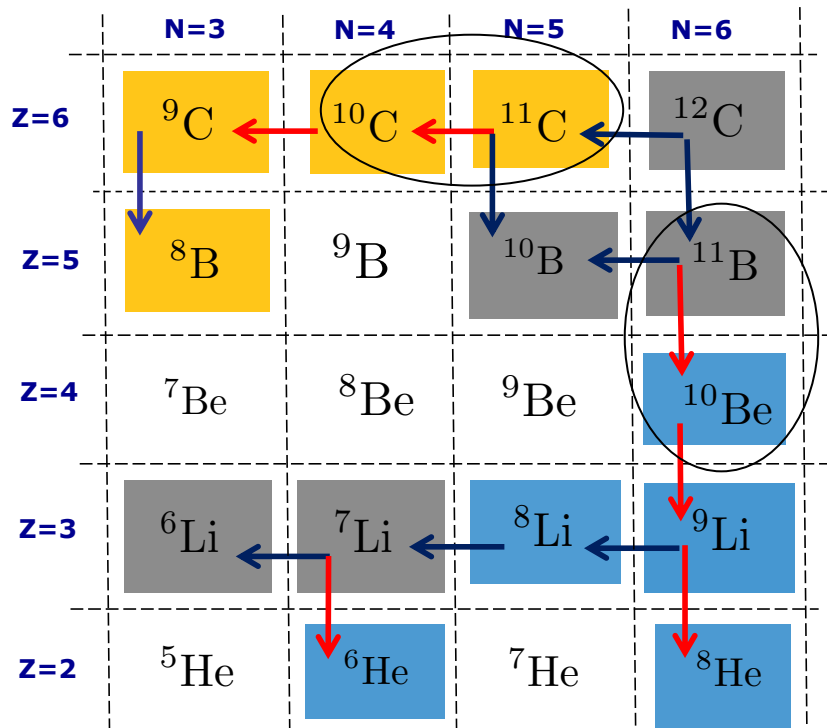
- 2-body DWIA =  $\mathcal{R} \times$  PWIA
- 3-body Faddeev-AGS (F/AGS)
- 3-Body CDCC, TC,
- ...

# Motivation

- Can the *p*-shell spectroscopic quenching obtained from structure and reactions be conciliated ?
- Can observables for (p,pN) reactions provide unequivocal information about nuclear spectroscopy, testing structure models and their underlying interactions ?
- What is the role of many-body degrees of freedom ?



# Revisit $^A X(p, pN)$ at 400 MeV/u (inverse kinematics)



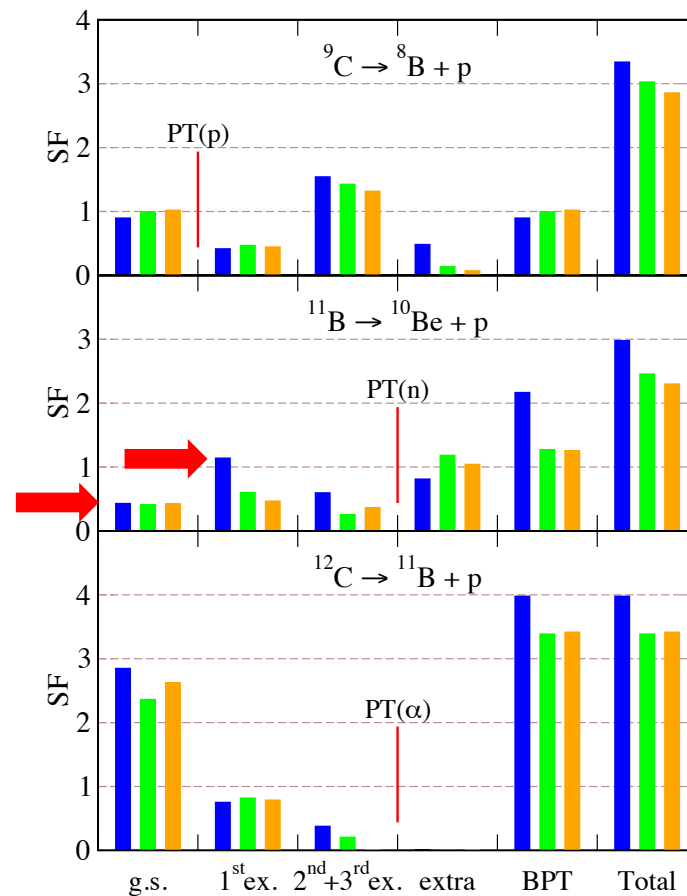
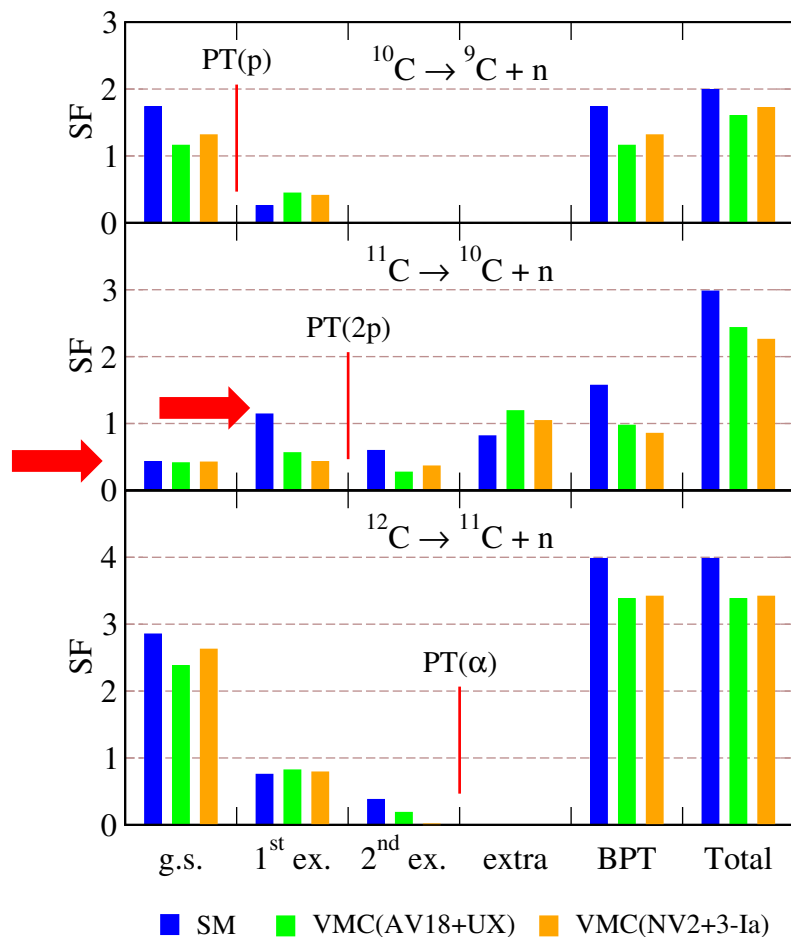
Knockout of a **deficient species nucleon N** (n/p)

**Approach:** Merging into the **Fadd/AGS** reaction mechanism the SO overlaps deduced from **Quantum Monte Carlo Techniques (QMC)** using two interactions:

- Argonne V18 two-nucleon and Urbana X three-nucleon potentials (AV18+UX)
- Norfolk NV2+3  $\Delta$ -full local chiral field theory

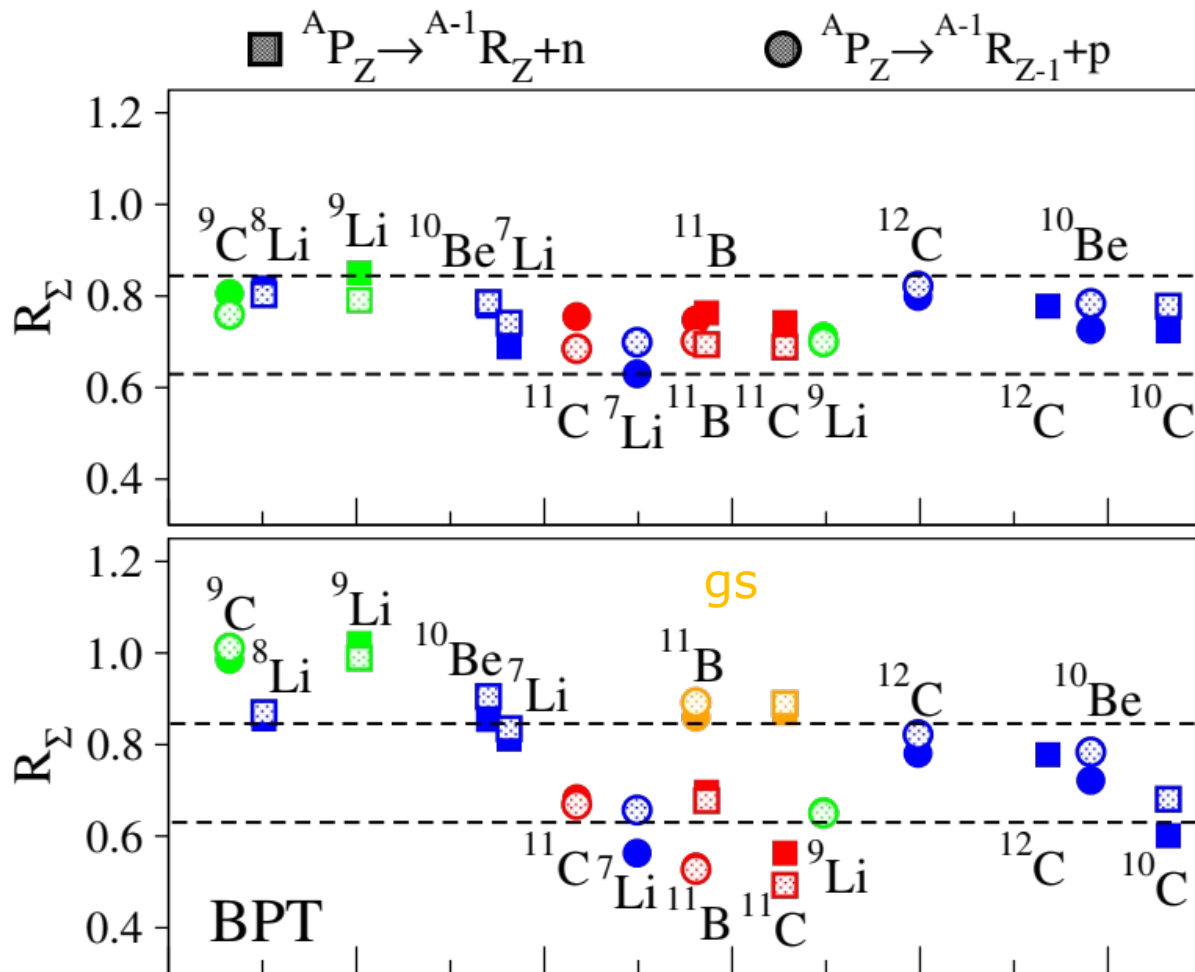
# Revisit $^AX(p,pN)$ at 400 MeV/u (inverse kinematics)

## Selected examples and **special cases in mirror transitions**



E.C., R.B.W., R.C., A.A., A.D. and M.P.

# Revisit $^A X(p, pN)$ at 400 MeV/u (inverse kinematics)



$$\Sigma(\mathcal{M}) = \sum_i Z^i(\mathcal{M})$$

$$R_\Sigma = \frac{\Sigma(\text{QMC})}{\Sigma(\text{SM})}$$

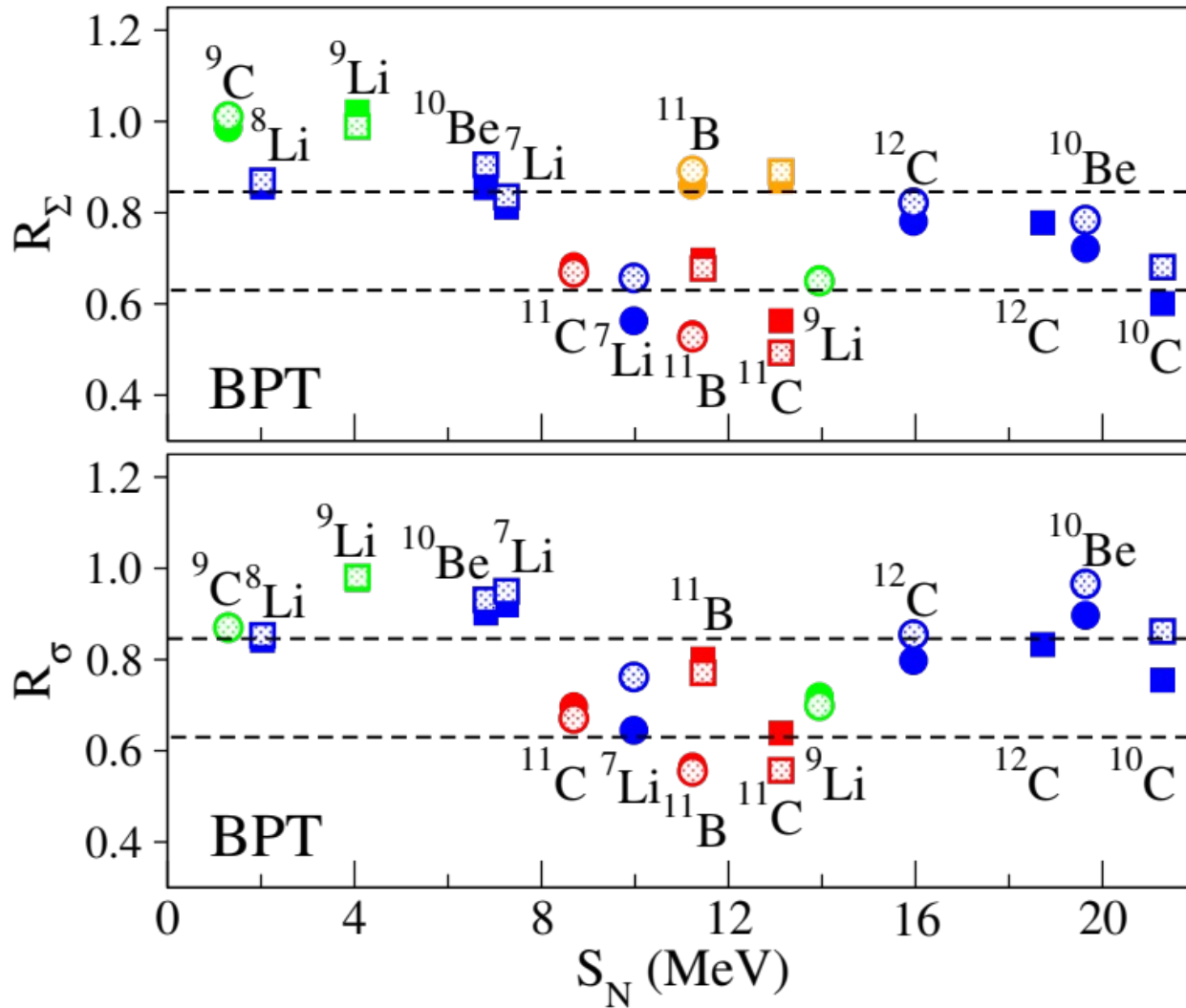
Total sums of SFs

$$R_\Sigma \sim 2/3$$

Sums of SFs that contains the states BPT

E.C., R.B.W., R.C., A.A., A.D. and M.P.

# Revisit $^AX(p,pN)$ at 400 MeV/u (inverse kinematics)



Sums of cross sections BPT, using the standard Fadeev/AGS reaction formalism

$$\sigma_{\text{th}}(\mathcal{M}) = \sum_i Z^i(\mathcal{M}) \sigma_{\text{sp}}^i(\mathcal{M})$$

$$R_\sigma = \frac{\sigma_{\text{th}}(\text{QMC})}{\sigma_{\text{th}}(\text{SM})}$$

E.C., R.B.W., R.C., A.A., A.D. and M.P.

# Revisit $^A X(p, pN)$ at 400 MeV/u (inverse kinematics)

$$R_S(\mathcal{M}) = \frac{\sigma_{\text{exp}}}{\sigma_{\text{th}}(\mathcal{M})}$$

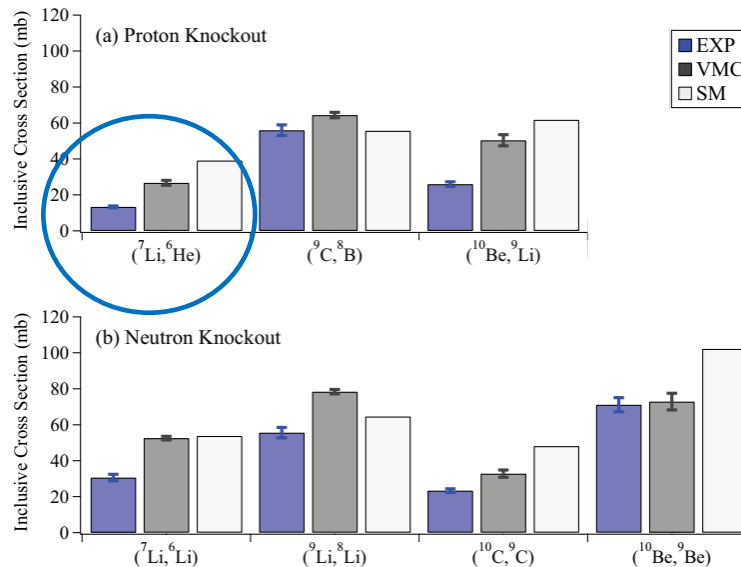
The theoretical QMC cross sections **underestimates** the data for  $\sim$  factor **2** for  $^{11}\text{C}(p, pn)$

E.C., R.B.W., R.C., A.A., A.D. and M.P.

The theoretical QMC cross sections **overestimates** the data for  $\sim$  factor **2** for **p removal from  $^7\text{Li}$**

G.F. Grinyer, D. Bazin, A. Gade, J.A. Tostevin et al, Pys Rev C 86, 024315 (2012)

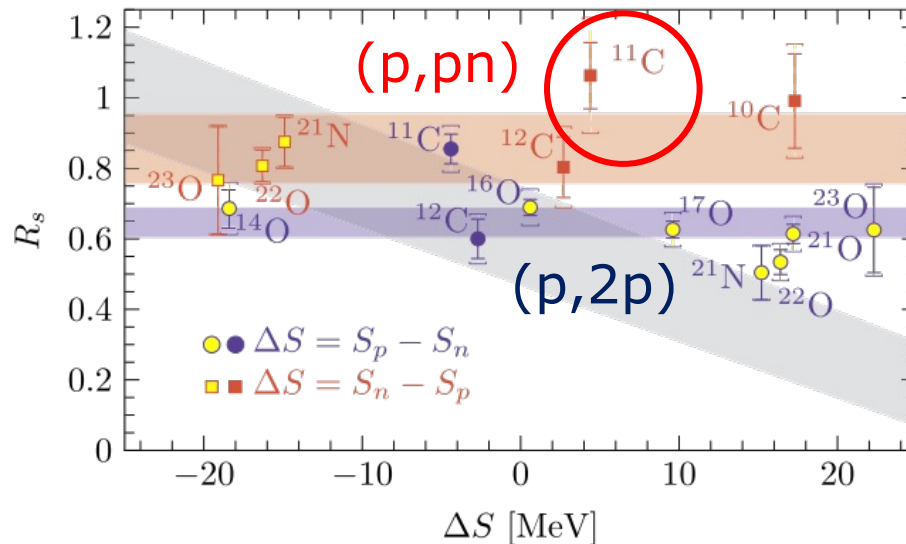
Reaction	QMC			SM	
	AV18-UX	NV2+3-Ia	NV2+3-Ia*/IIb*	CK	OXBASH 5 10
$^{12}\text{C}(p, 2p)^{11}\text{B}$	0.90	0.79	0.99/0.84	0.72	0.60(6)(4)
$^{12}\text{C}(p, pn)^{11}\text{C}$	1.08	--	--	0.90	0.80(9)(7)
$^{11}\text{C}(p, 2p)^{10}\text{B}$	1.34	1.52	--	0.92	0.86(4)(5)
$^{11}\text{C}(p, pn)^{10}\text{C}$	1.81	2.08	--	0.96	1.06(9)(12)
$^{10}\text{C}(p, pn)^9\text{C}$	1.43	1.23	--	1.08	0.99(13)(9)



# Revisit $^A X(p, pN)$ at 400 MeV/u (inverse kinematics)

$$R_S(\mathcal{M}) = \frac{\sigma_{\text{exp}}}{\sigma_{\text{th}}(\mathcal{M})}$$

Reaction	QMC			SM	
	AV18-UX	NV2+3-Ia	NV2+3-Ia*/IIb*	CK	OXBASH <span style="border: 1px solid green; padding: 2px;">5</span> <span style="border: 1px solid green; padding: 2px;">10</span>
$^{12}\text{C}(p, 2p)^{11}\text{B}$	0.90	0.79	0.99/0.84	0.72	0.60(6)(4)
$^{12}\text{C}(p, pn)^{11}\text{C}$	1.08	---	---	0.90	0.80(9)(7)
$^{11}\text{C}(p, 2p)^{10}\text{B}$	1.34	1.52	---	0.92	0.86(4)(5)
$^{11}\text{C}(p, pn)^{10}\text{C}$	1.81	2.08	---	0.96	1.06(9)(12)
$^{10}\text{C}(p, pn)^9\text{C}$	1.43	1.23	---	1.08	0.99(13)(9)

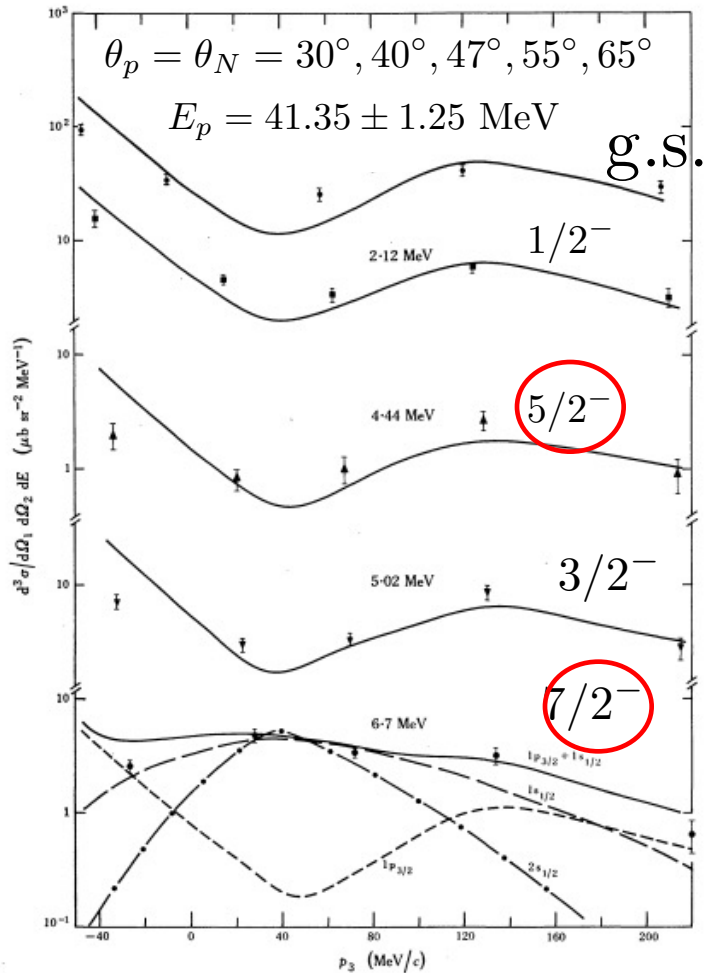


**DWIA + SM-OXBAH  $\sim 1$**

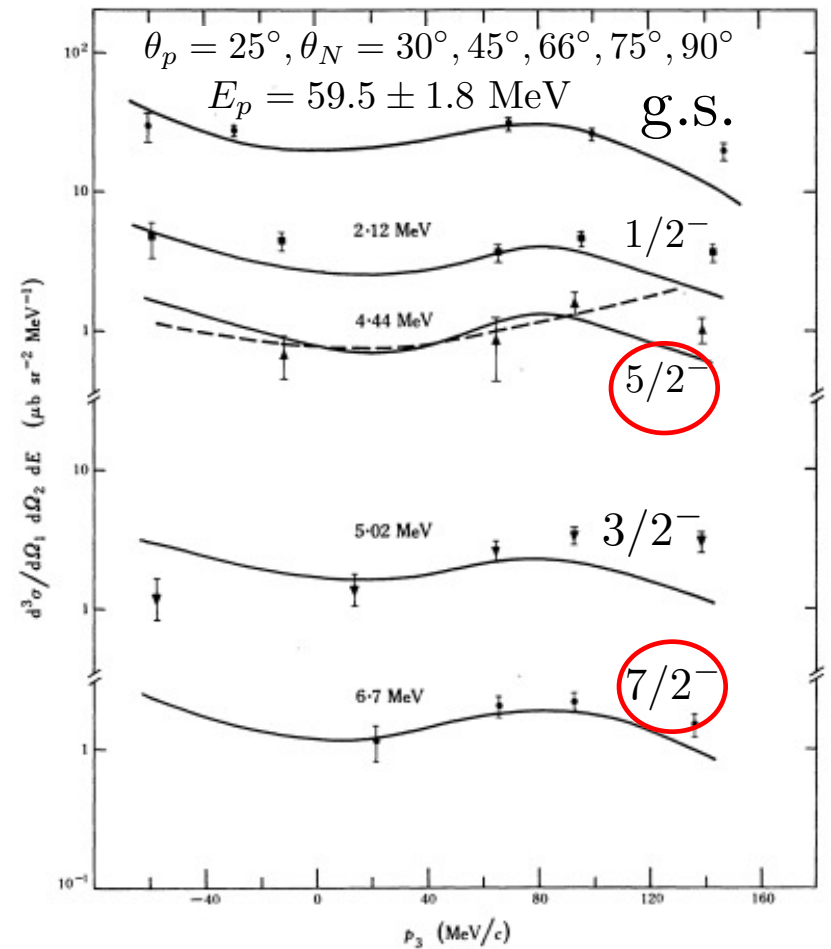
M.Holl, V. Panin, H. Alvarez-Pol,  
L. Atar, T. Aumann et al, Phys  
Lett B 795 (2019), 682

# Revisit $^{12}\text{C}(p,2p)$ at 100 MeV/u (direct kinematics)

Geometry: coplanar, Symmetric



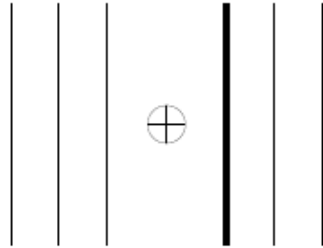
Geometry: coplanar, Asymmetric



Devins et al, Aust. J. Phys 32, 323 (1979)

# Revisit $^{12}\text{C}(p,2p)$ at 100 MeV/u (direct kinematics)

$$\mathcal{H} = \mathcal{H}_g \oplus \mathcal{H}_x$$



sector coupling by interaction

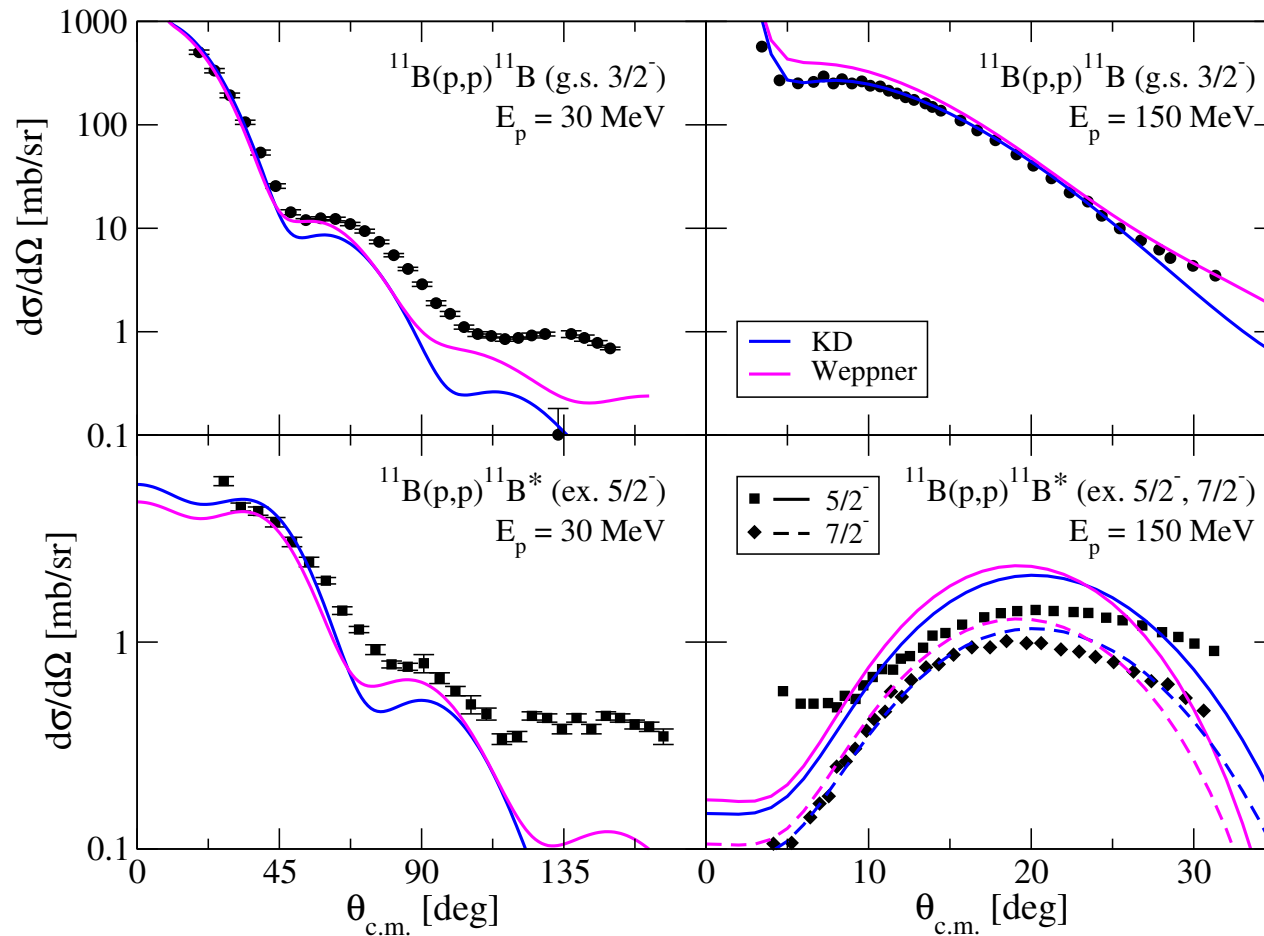


The two sectors are coupled by the core – valence nucleon interaction

A. Deltuva, PRC 88, 011601 (R) & [A. Deltuva talk](#)



# Revisit $^{12}\text{C}(p,2p)$ at 100 MeV/u (direct kinematics)



➤ Data: V.M. Hannen *et al*, Phys Rev C67, 054320 (2003)

A.D., E.C., R.C., D.J.

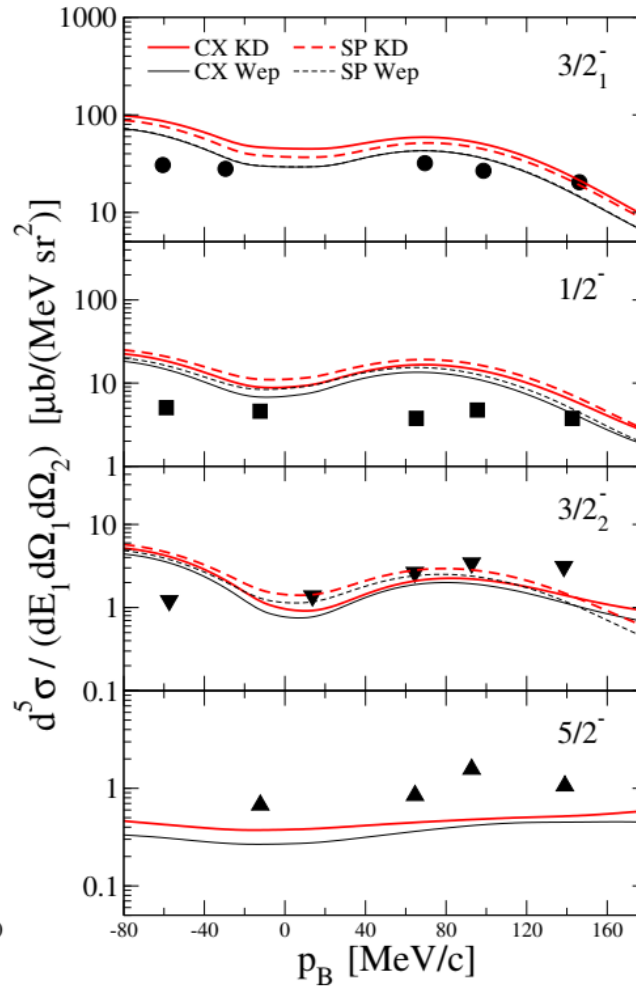
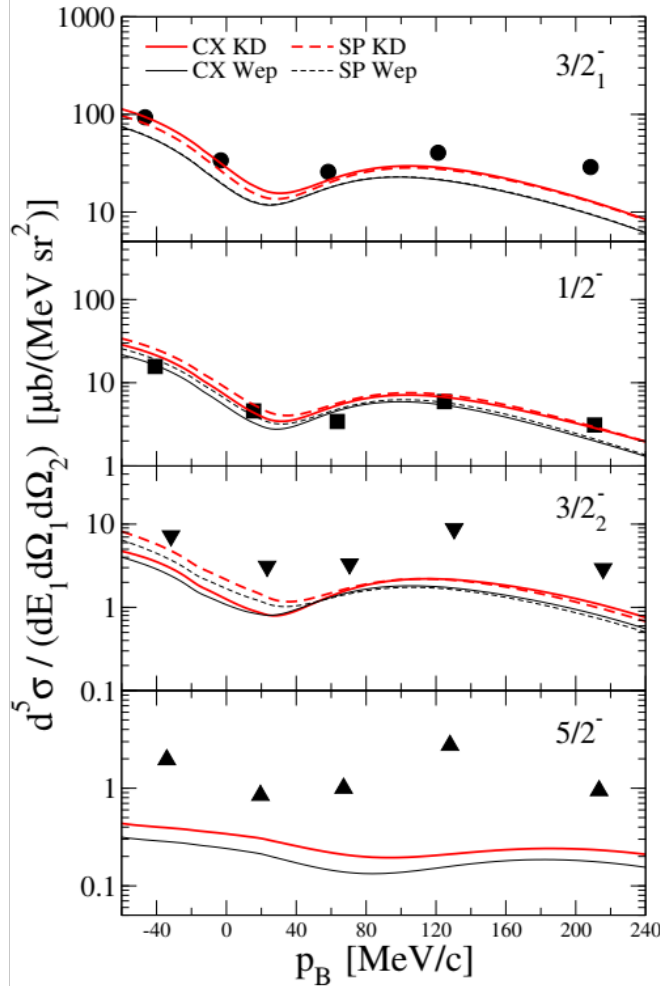
# Revisit $^{12}\text{C}(p,2p)$ at 100 MeV/u (direct kinematics)

$$\theta_p = \theta_N = 30^\circ, 40^\circ, 47^\circ, 55^\circ, 65^\circ$$

$$E_p = 41.35 \pm 1.25 \text{ MeV}$$

$$\theta_p = 25^\circ, \theta_N = 30^\circ, 45^\circ, 66^\circ, 75^\circ, 90^\circ$$

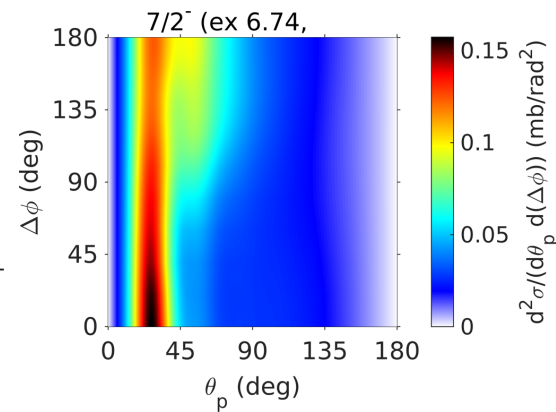
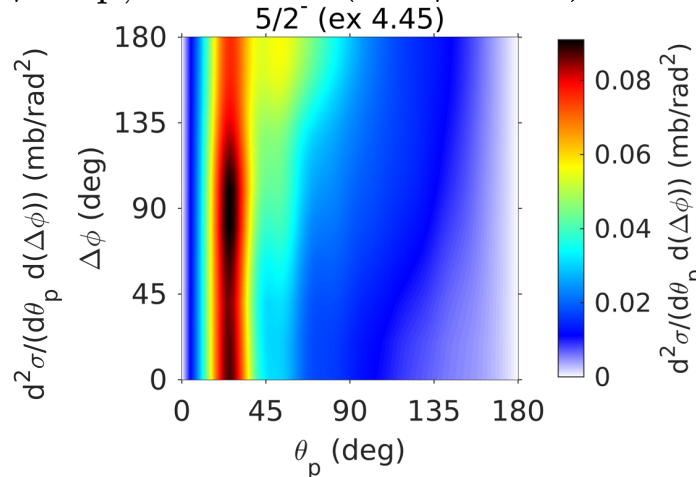
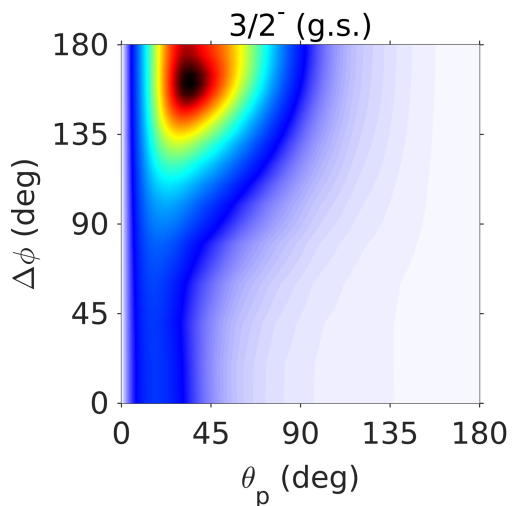
$$E_p = 59.5 \pm 1.8 \text{ MeV}$$



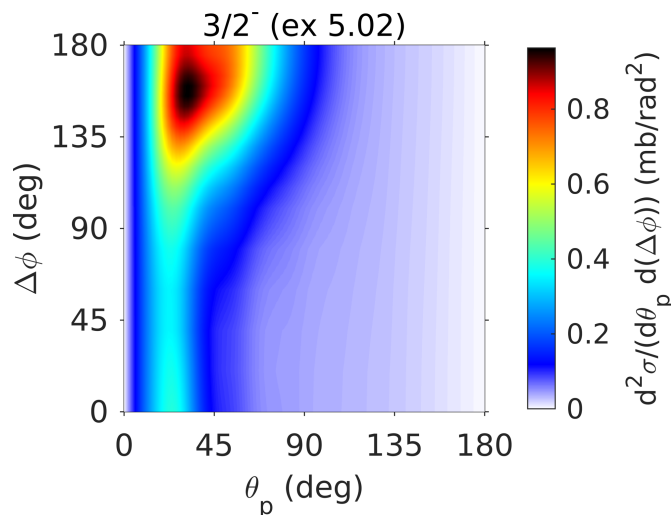
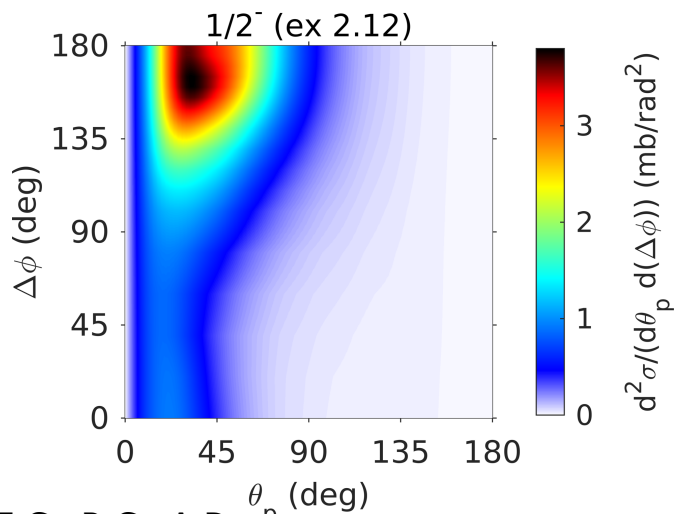
A.D., E.C., R.C., D.J.

# Dynamical core excitation signatures

$$d^2\sigma/d\theta_p, \text{lab } d\Delta\phi \text{ (mb/rad}^2\text{)}$$



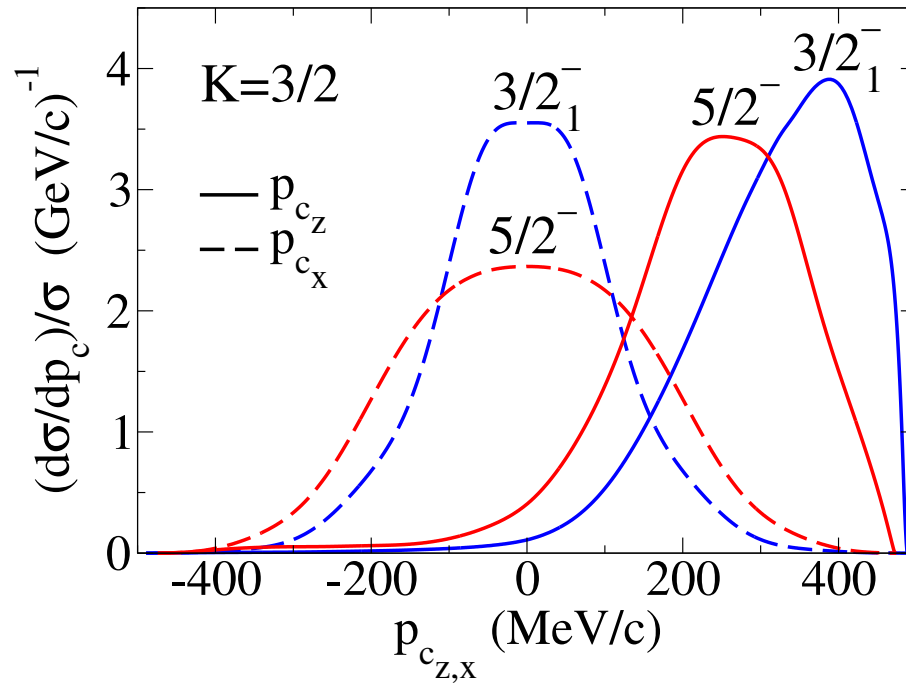
## Random distribution of the measured proton



E.C., R.C., A.D.

# Dynamical core excitation signatures

Renormalized core momentum distributions for comparison

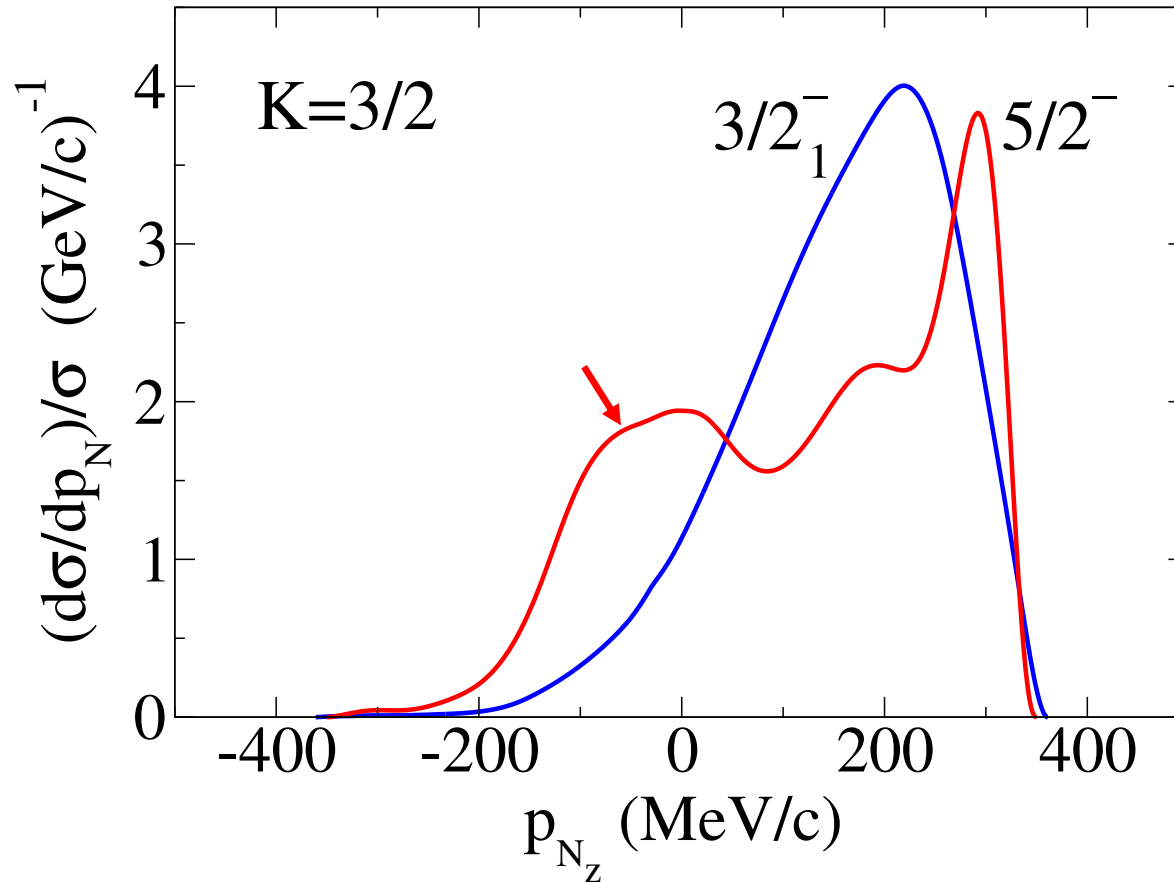


## Signature of core excitation:

- The **longitudinal core** momentum distribution peaks at lower momentum
- The **transverse core** momentum distribution is broader

E.C., R.C., A.D.

# Dynamical core excitation signatures

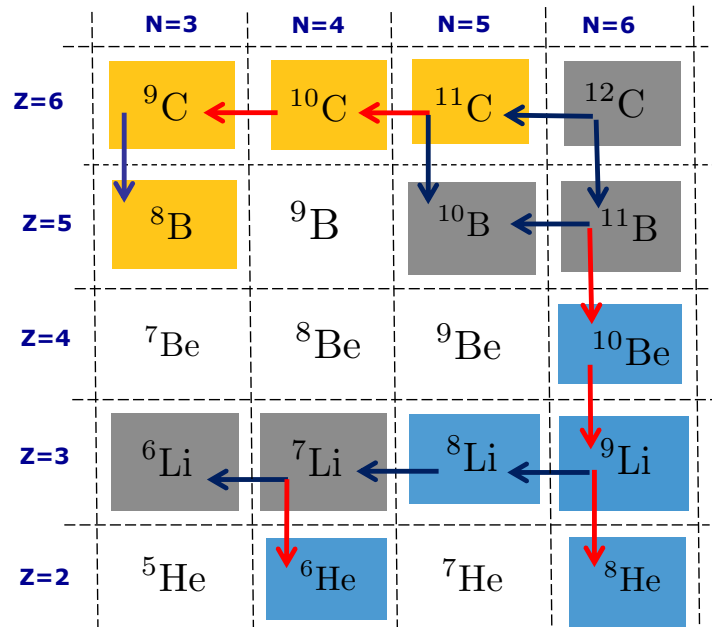


➔ **Clear signature of core excitation:**

The longitudinal nucleon momentum distribution has a **double peak structure**

E.C., R.C., A.D.

# Perspectives



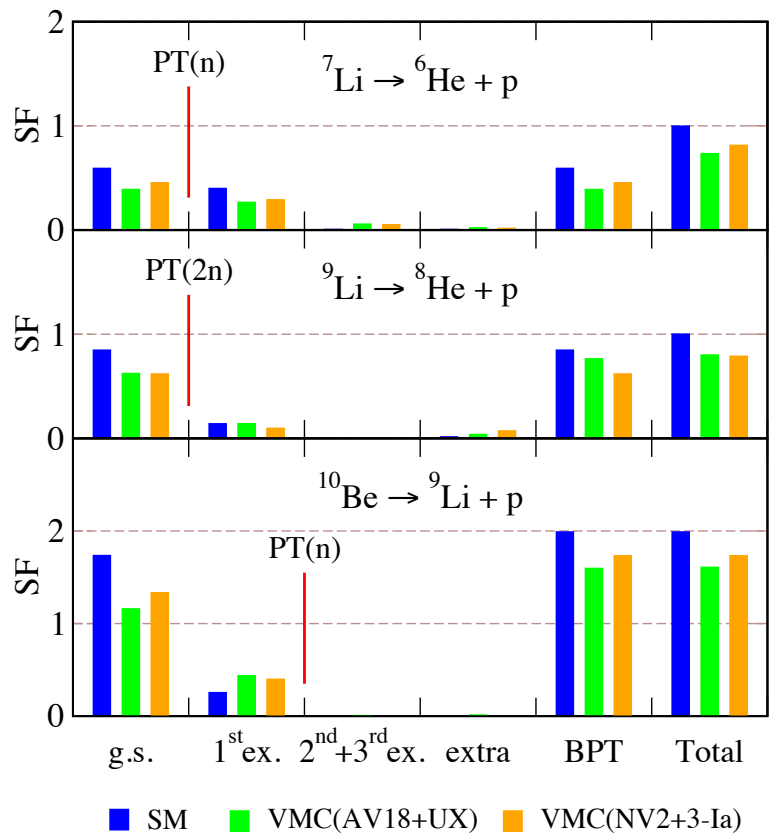
**Comprehensive theoretical & experimental program of  
N- knockout with light nuclei ( $A \leq 12$ )**

**Thank you !**

Extra slides

# Revisit $^A X(p, pN)$ at 400 MeV/u (inverse kinematics)

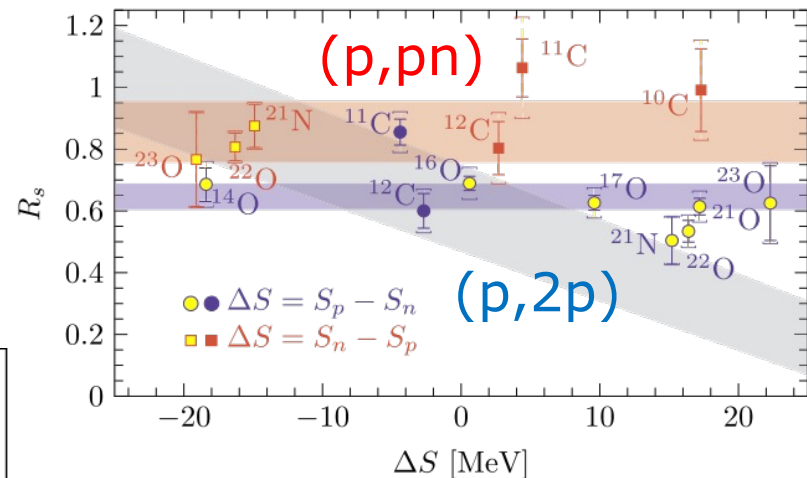
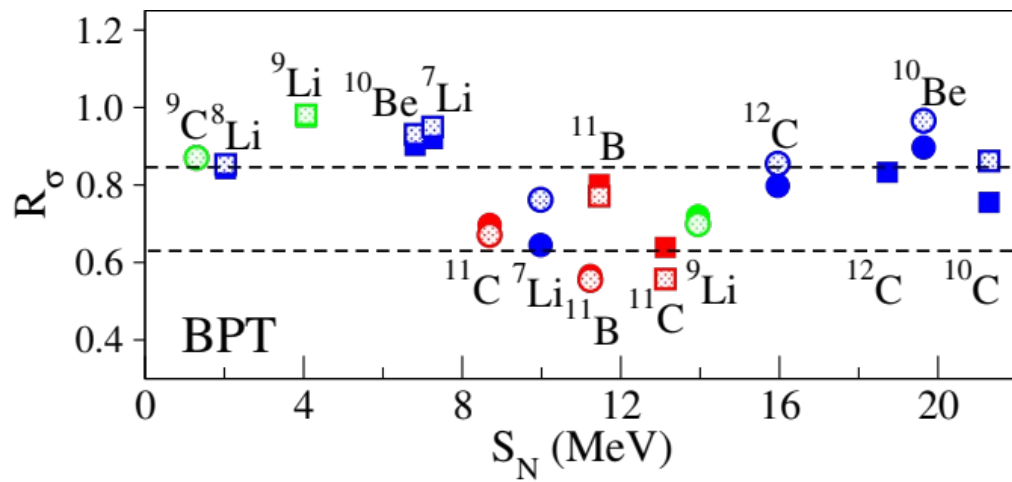
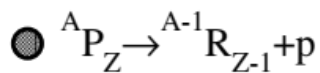
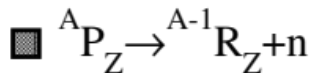
Selected examples and **special cases in mirror transitions**



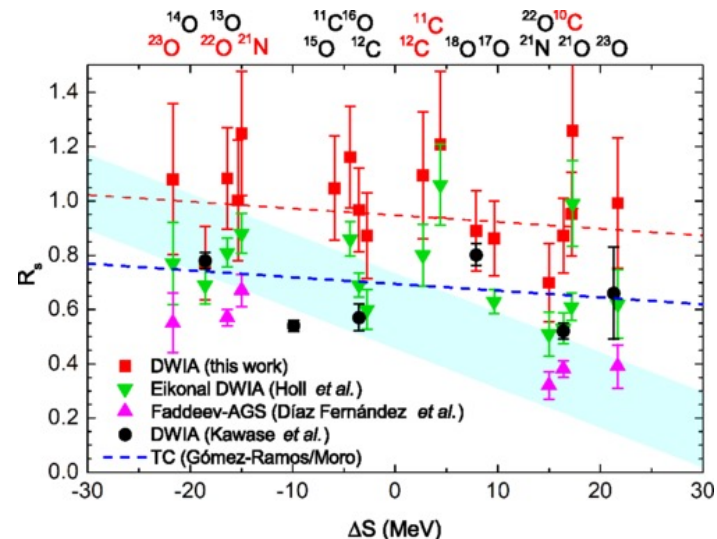
E.C., R.B.W., R.C., A.A., A.D. and M.P.



# Revisit $^A X(p, pN)$ at 400 MeV/u (inverse kinematics)



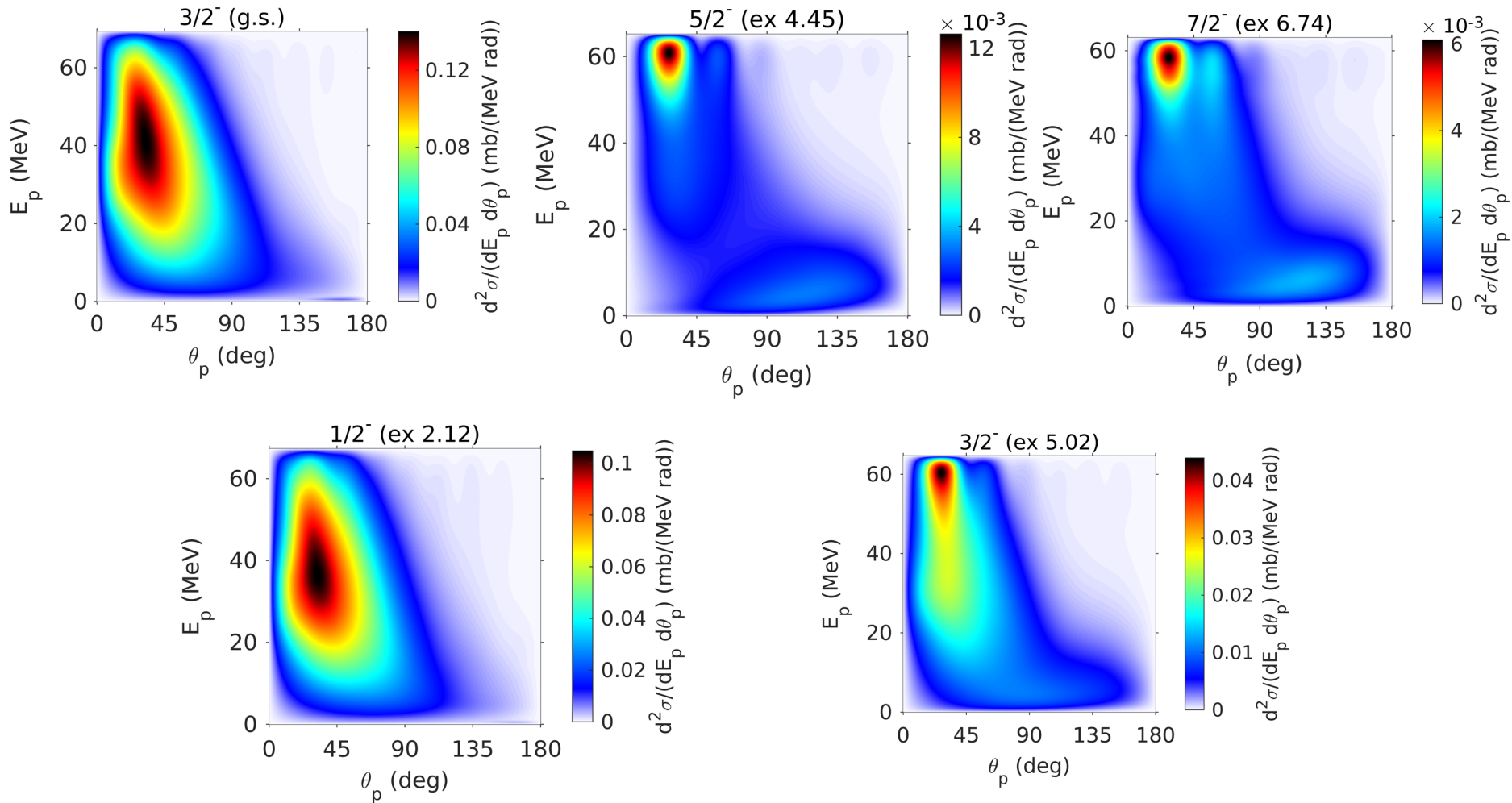
M. Holl, V. Panin, H. Alvarez-Pol, L. Atar, T. Aumann et al, Phys Lett B 795 (2019), 682



Nguyen Tr Toan Phuc, K. Yoshida, K. Ogata, Phys Rev C100, 064604

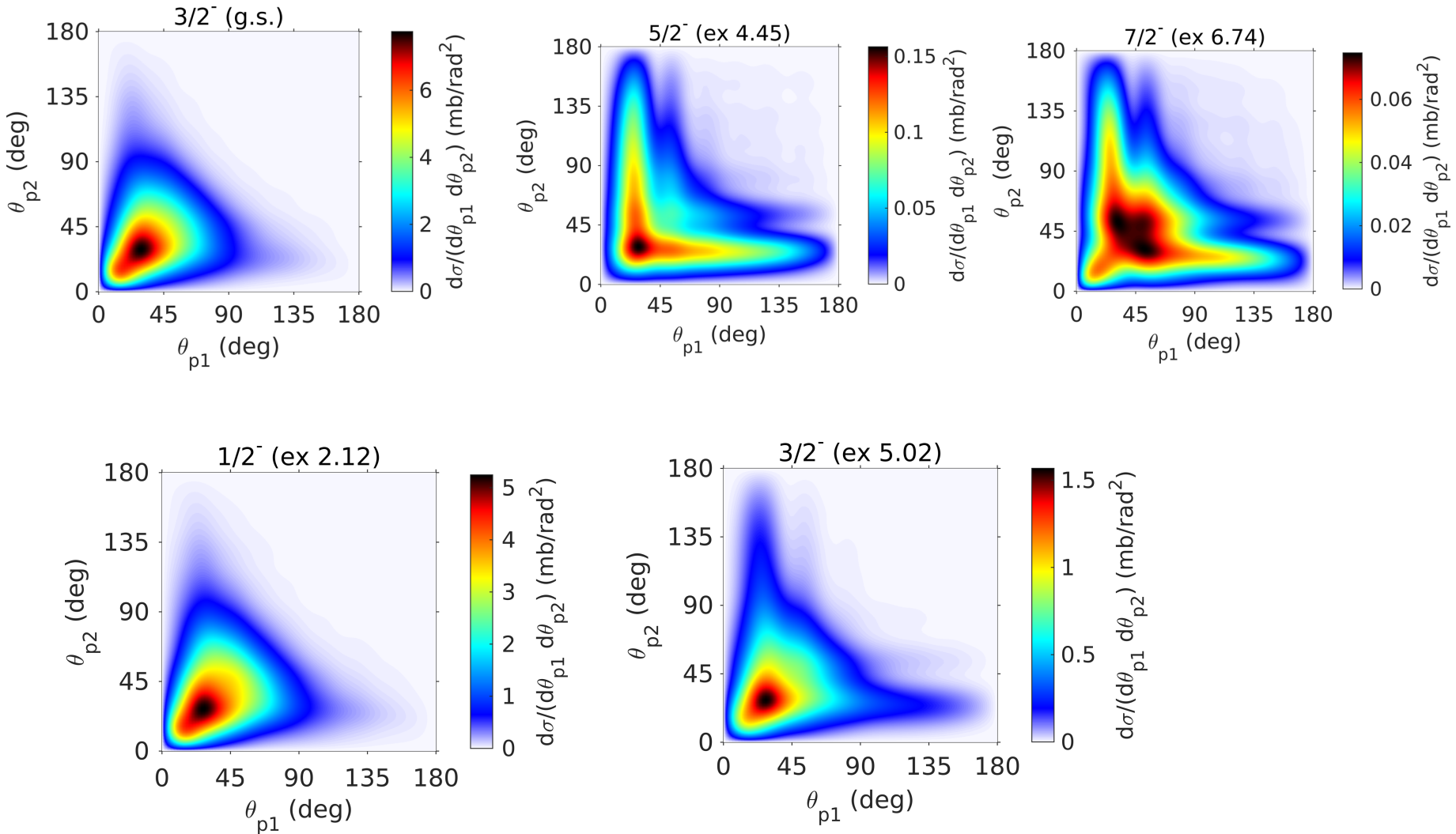
# Dynamical core excitation signatures

$$d^2\sigma/dE_{p,cm}d\theta_{p,cm} \text{ (mb/MeV rad)}$$



E.C., R.C., A.D.

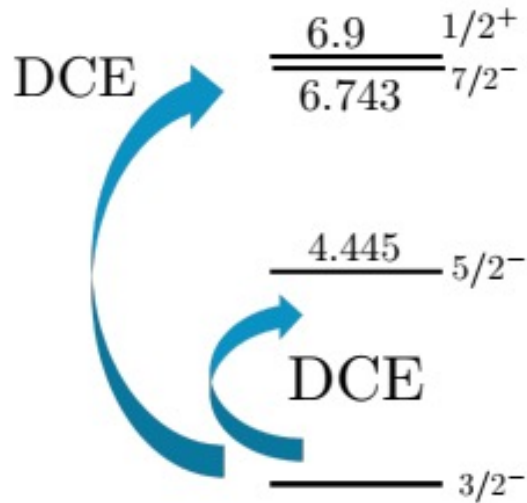
# Dynamical core excitation signatures



E.C., R.C., A.D.

# Revisit $^{12}\text{C}(p,2p)$ at 100 MeV/u (direct kinematics)

Two independent dynamical coupling problems for the scattering process



$$K = 3/2$$

(I)

$^{11}\text{B}$



$$K = 1/2$$

(II)

$$(I) \quad |\Phi^{JM}(^{12}\text{C})\rangle \simeq \alpha |3/2_1^-\rangle \otimes p_{3/2}(\pi) \rangle$$

$$(II) \quad |\Phi^{JM}(^{12}\text{C})\rangle = \beta |1/2^-\rangle \otimes p_{3/2}(\pi) \rangle + \gamma |3/2_2^-\rangle \otimes p_{3/2}(\pi) \rangle$$

# Motivation

Geometry: coplanar, Symmetric

$$\theta_p = \theta_N = 30^\circ, 40^\circ, 47^\circ, 55^\circ, 65^\circ$$

$$E_p = 41.35 \pm 1.25 \text{ MeV}$$

Geometry: coplanar, Asymmetric

$$\theta_p = 25^\circ, \theta_N = 30^\circ, 45^\circ, 66^\circ, 75^\circ, 90^\circ$$

$$E_p = 59.5 \pm 1.8 \text{ MeV}$$

**Table 2. Spectroscopic factors obtained from DWIA calculations for  $^{11}\text{B}$  states populated in  $^{12}\text{C}(p, 2p)^{11}\text{B}$**

State of $^{11}\text{B}$ $E_x$ (MeV)	$J^\pi$	Spectroscopic factors $C^2S$				
		Experimental geometry		Theoretical results <sup>A</sup>		
		Symmetric	Asymmetric	CK	S	K
g.s.	$3/2^-$	$2.0 \pm 0.2$	$1.0 \pm 0.2$	2.85	3.27	2.79
2.12	$1/2^-$	$0.33 \pm 0.06$	$0.20 \pm 0.05$	0.38	0.60	0.79
4.44	$5/2^-$	$0.10 \pm 0.05$	$0.11 \pm 0.04$	—	—	$0.0005^{\text{B}}$
5.02	$3/2^-$	$0.33 \pm 0.1$	$0.13 \pm 0.03$	0.75	0.12	0.345
6.74 <sup>c</sup>	$7/2^-$	$0.06 \pm 0.03$	$0.12 \pm 0.04$	—	—	$0.035^{\text{B}}$
6.79 <sup>c</sup>	$1/2^+$	$0.05 \pm 0.02$				

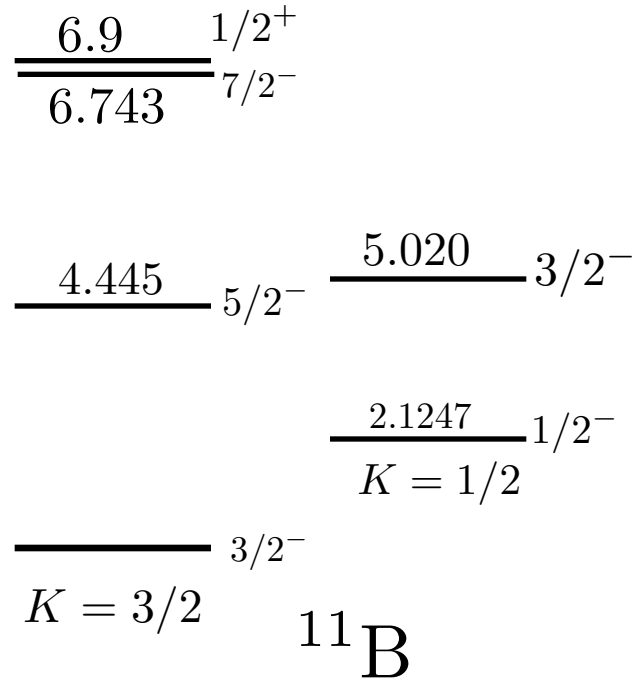
<sup>A</sup> Results from: CK, intermediate coupling calculation of Cohen and Kurath (1967); S, Singh *et al.* (1973); K, Kurath (1968).

<sup>B</sup> These calculations assumed f-wave knockout.

<sup>C</sup> These states were not resolved; see the text for the method of estimating their separate contributions.

Devins et al, Aust. J. Phys 32, 323 (1979)

# Motivation



${}^{11}\text{B}$  is strongly deformed and the low lying states are of rotational nature:

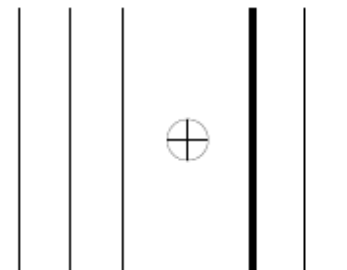
The excitation spectra exhibit an approximate  $J(J+1)$  dependence

# Revisit $^{12}\text{C}(p,2p)$ at 100 MeV/u (direct kinematics)

$$U_{\beta\alpha} = \bar{\delta}_{\beta\alpha} G_0^{-1} + \sum_{\sigma} \bar{\delta}_{\beta\sigma} T_{\sigma} G_0 U_{\sigma\alpha}$$

$$U_{0\alpha} = G_0^{-1} + \sum_{\sigma} T_{\sigma} G_0 U_{\sigma\alpha}$$

$\mathcal{H} = \mathcal{H}_g \oplus \mathcal{H}_x$



$$T_{\sigma} = v_{\sigma} + v_{\sigma} G_0 T_{\sigma} \quad \text{2-particle Transition operator}$$

$$G_0 = (E + i0 - H_0)^{-1} \quad \text{Free resolvent}$$

$$\text{channel states} \quad (E - H_0 - v_{\alpha}) |\phi_{\alpha}\rangle = 0$$

$$H_0 |\mathbf{p}_{\alpha} \mathbf{q}_{\alpha}\rangle_a = [p_{\alpha}^2 / 2\mu_{\alpha} + q_{\alpha}^2 / 2M_{\alpha} + (m_{A^*} - m_A) \delta_{ax}] |\mathbf{p}_{\alpha} \mathbf{q}_{\alpha}\rangle_a$$

Where the extended free Hamiltonian  $H_0$  is the sum of the kinetic energy operator and the intrinsic operator of the core whose contribution is the mass difference relative to the  $A+p+n$  threshold

# Revisit $^{12}\text{C}(p,2p)$ at 100 MeV/u (direct kinematics)

2-particle transition operator, requires the potentials  $v_\sigma$  for each interaction pair

$$T_\sigma = v_\sigma + v_\sigma G_0 T_\sigma$$

- Realistic CD BONN for the np interaction
- **N-Core** and **p-Core** interactions are obtained from a **rotation model for the core with a permanent quadrupole deformation**.  
In the body-fixed frame, the surface radius is parametrized as

$$R(\hat{\xi}) = R_0 [1 + \beta_2 Y_{20}(\hat{\xi})]$$

**Input parameter: deformation length**



# Revisit $^{12}\text{C}(p,2p)$ at 100 MeV/u (direct kinematics)

Deformed surface radius  $R(\hat{\xi}) = R_0[1 + \beta_2 Y_{20}(\hat{\xi})]$

The N-Core and p-Core interactions are obtained assuming that the interaction follows the deformation of the Core.

That is: starting from a central potential,  $V_{xc}^{(0)}(r)$

the X-core (x=N,p) interaction is obtained by **deforming this central interaction**

$$V_{xc}(r, \hat{\xi}) = V_{xc}^{(0)}(r) \left[ r - \delta_2 Y_{20}(\hat{\xi}) \right] ; \delta_2 = \beta_2 R_0$$

The deformed central interaction is supplemented by a central/deformed spin-orbit term

**Input parameter: deformation length**

$$\delta_2 = 1.5 \text{ fm}$$