



北京大學

GSI - FAIR Colloquium

GSI, Main Lecture Hall, Tuesday, July 11, 2023

Mass and shape of the exotic nuclei

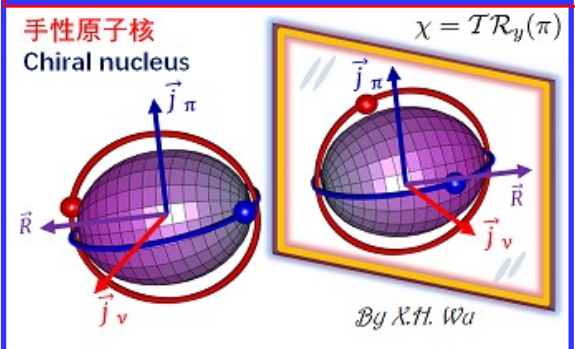
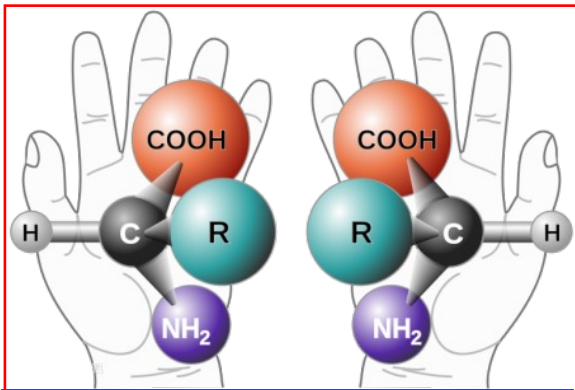
Jie MENG (孟杰)

School of Physics, Peking University (北京大学物理学院)



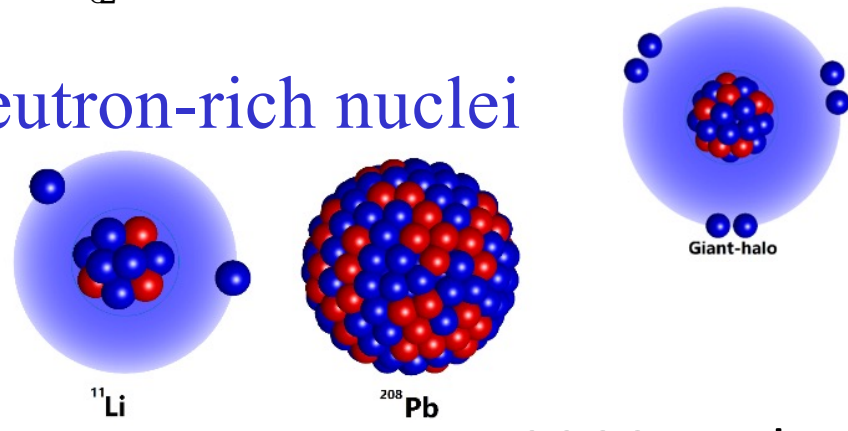
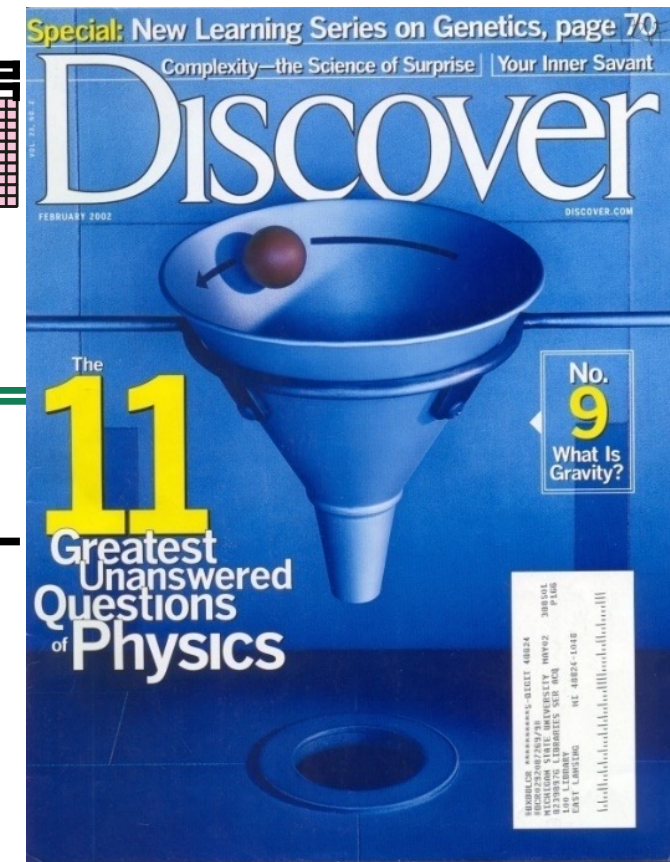
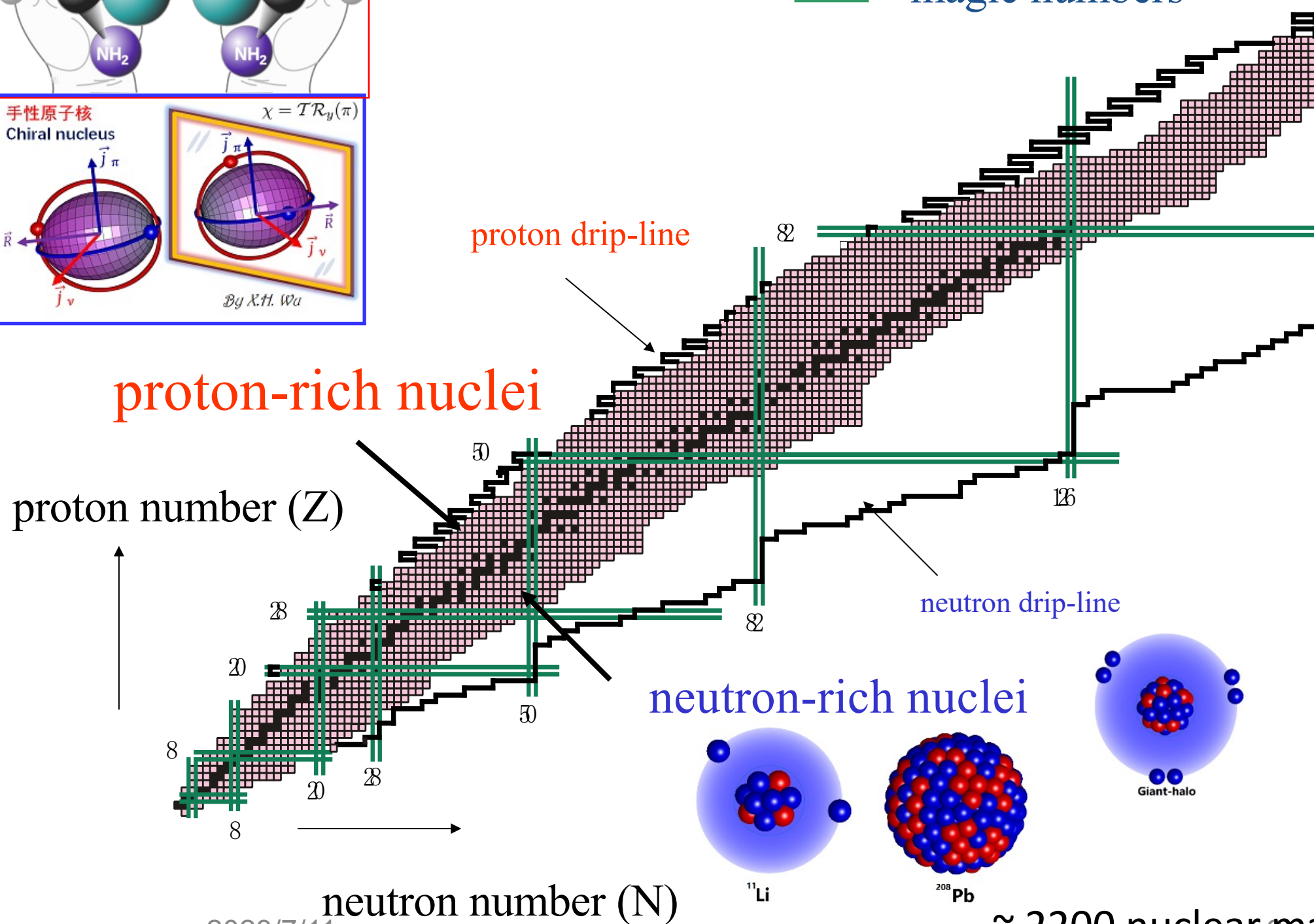
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Existence Limit of nucleus



- stable nuclei
- unstable nuclei observed
- drip-lines (predictions)
- == magic numbers

~300 nuclei
~2700 nuclei
~8000 nuclei



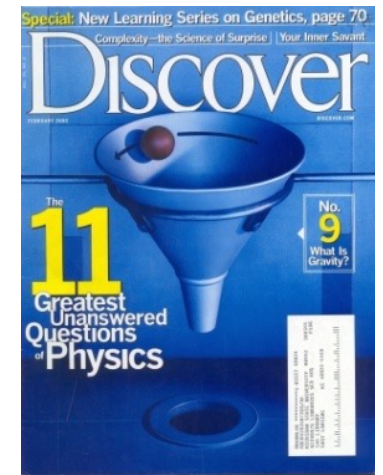
2023/7/11

~ 2200 nuclear masses were measured

How were the heavy elements from iron to Uranium made?

Discovery: "11 greatest unanswered questions of Physics"

Key mechanism: rapid neutron capture process (r-process)



r-process sites

GW170817 neutron-star-merger event shows that neutron star merger is one of the r-process sites

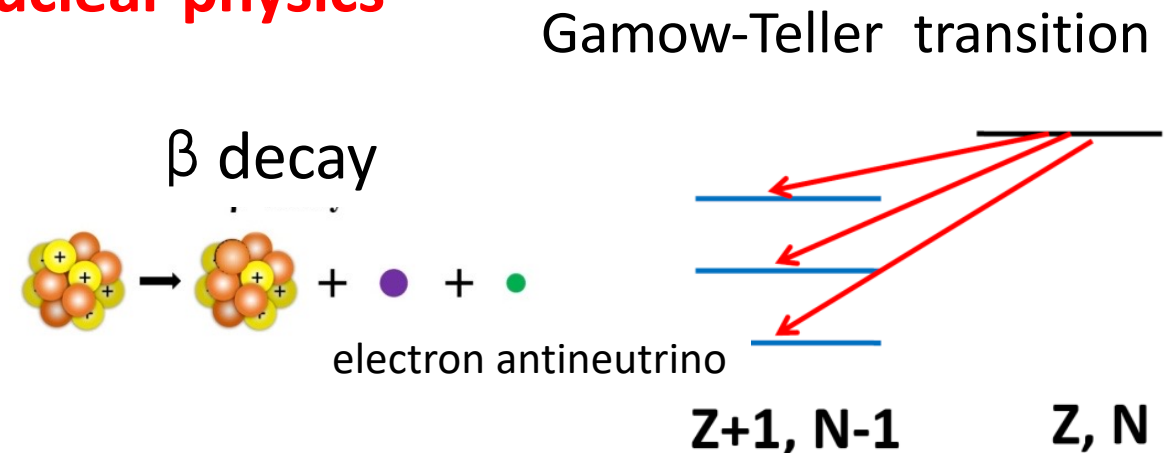
ApJL 848, L12 (2017)



big process in nucleosynthesis study

Systematic nuclear physics knowledge: mass, β -decay half-lives, reaction rates ...

Accurate description: difficult problem in nuclear physics



key: difficulties in experiments

Large-scale accurate theoretical calculations nuclear are demanded

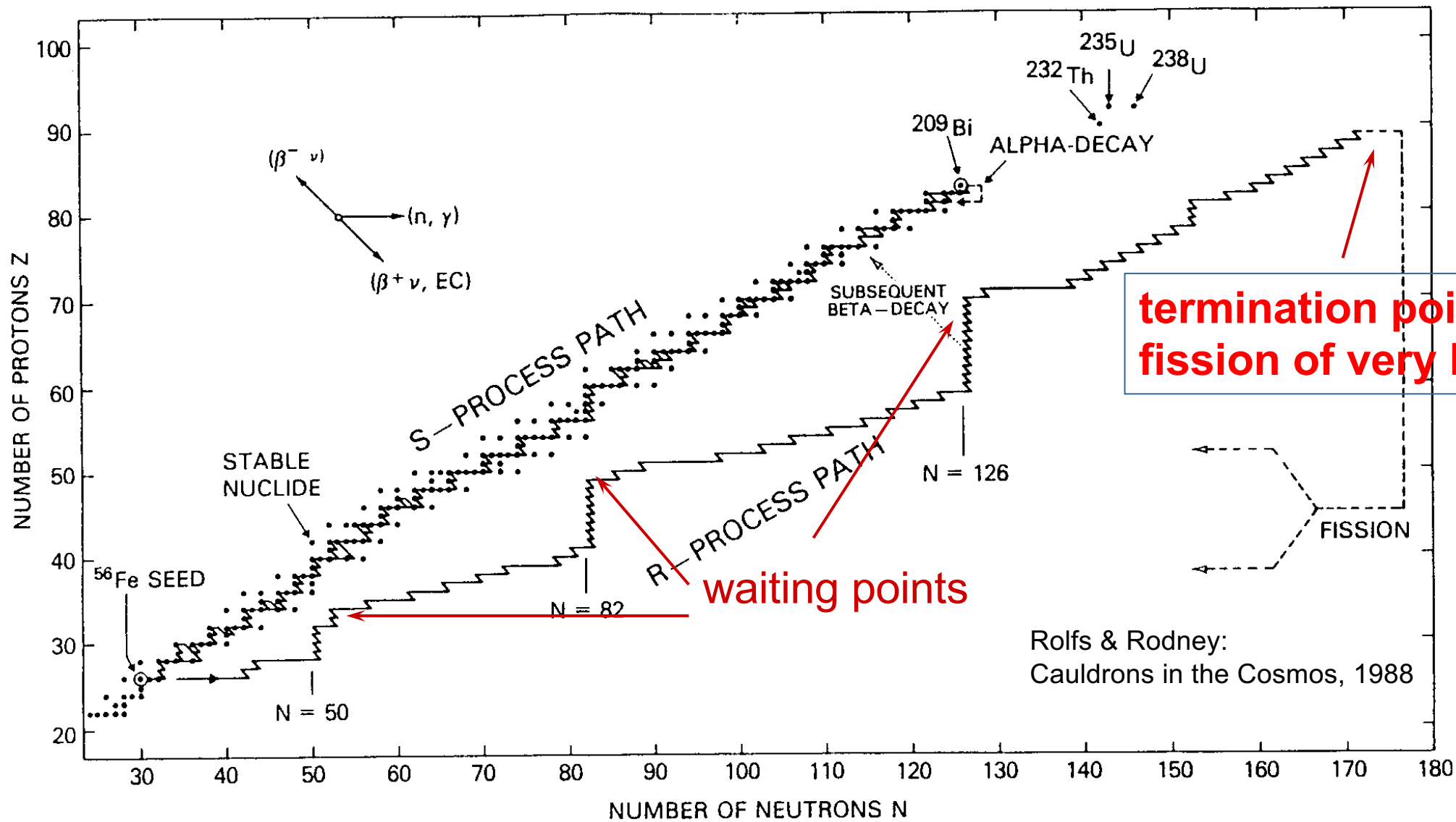


r-process (r = rapid neutron capture process)



n capture time: $\tau_n \ll \tau_\beta$

unstable nucleus reacts before capturing decay



typical lifetimes for unstable nuclei far from the valley of β stability: $10^{-4} - 10^{-2}$ s

requiring n
capture time:

$$\tau_n \sim 10^{-4} \text{ s}$$



$$n_n \sim 10^{20} \text{ n/cm}^3$$

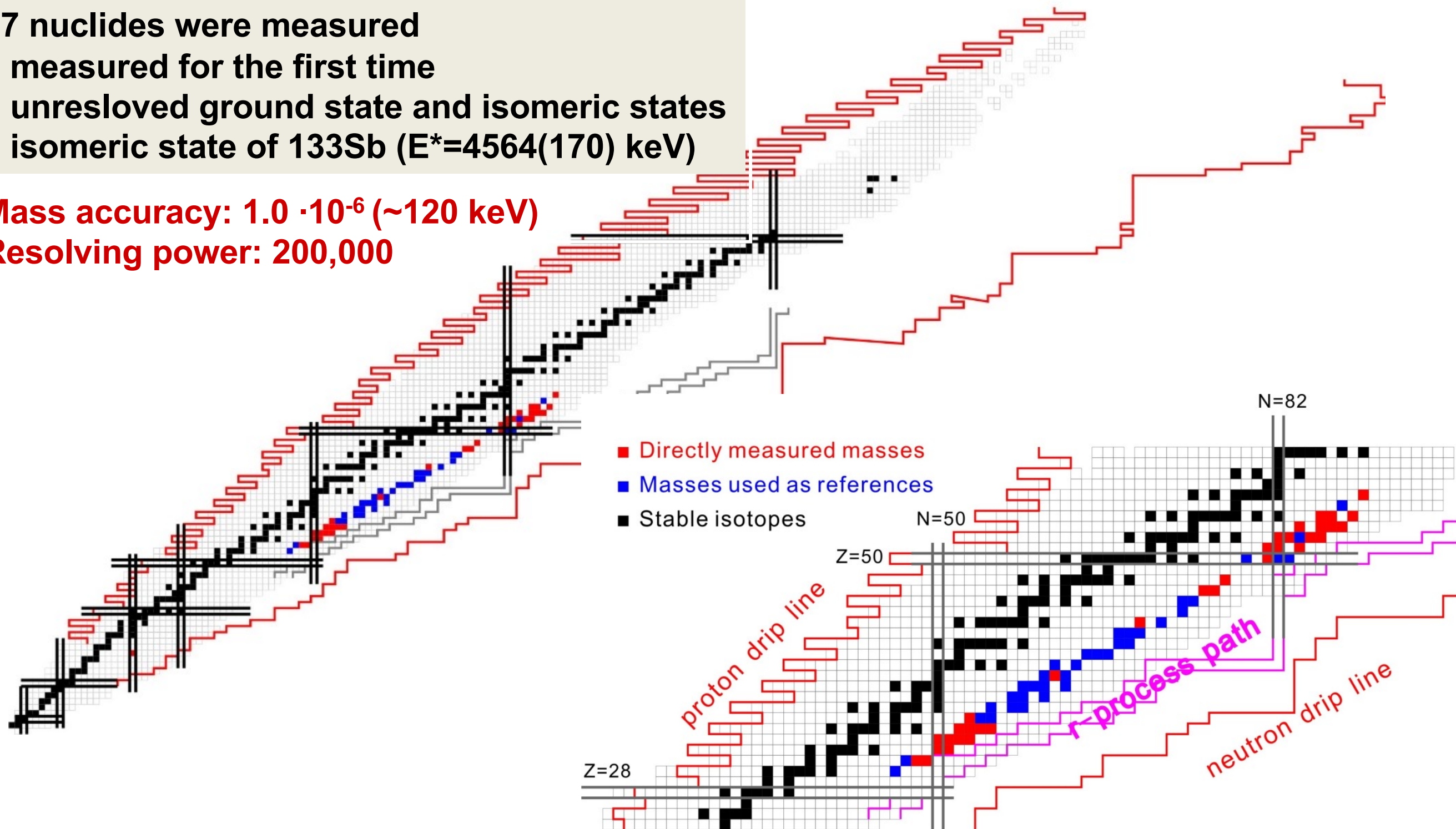
explosive scenarios needed to account for such high neutron fluxes



Short-Lived Neutron-Rich Nuclei with the Novel Large-Scale Isochronous Mass Spectrometry at the FRS-ESR Facility Sun et al. NPA 812 (2008) 1-12

71 nuclides covered
27 nuclides were measured
8 measured for the first time
8 unresolved ground state and isomeric states
1 isomeric state of ^{133}Sb ($E^*=4564(170)$ keV)

Mass accuracy: $1.0 \cdot 10^{-6}$ (~120 keV)
Resolving power: 200,000

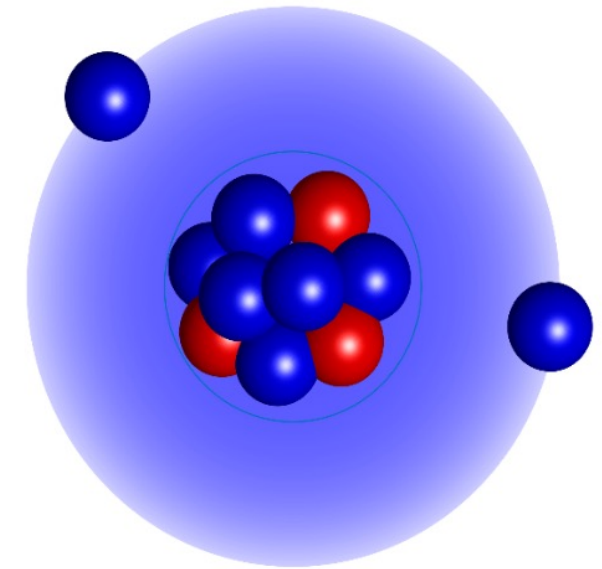
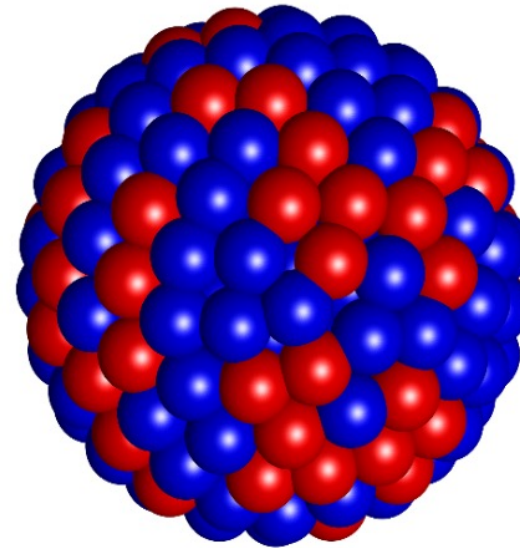
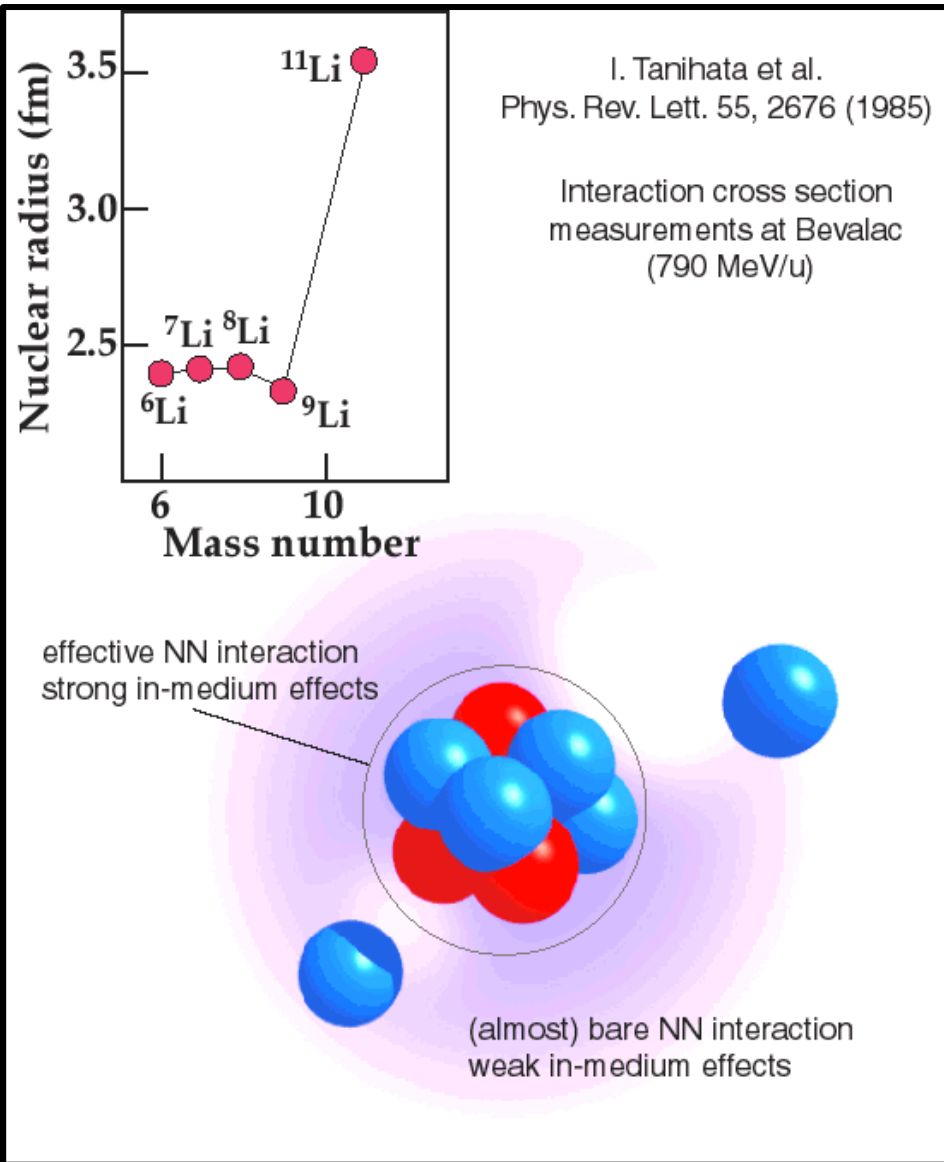


Facility for Antiproton and Heavy Ion Research (FAIR) Darmstadt





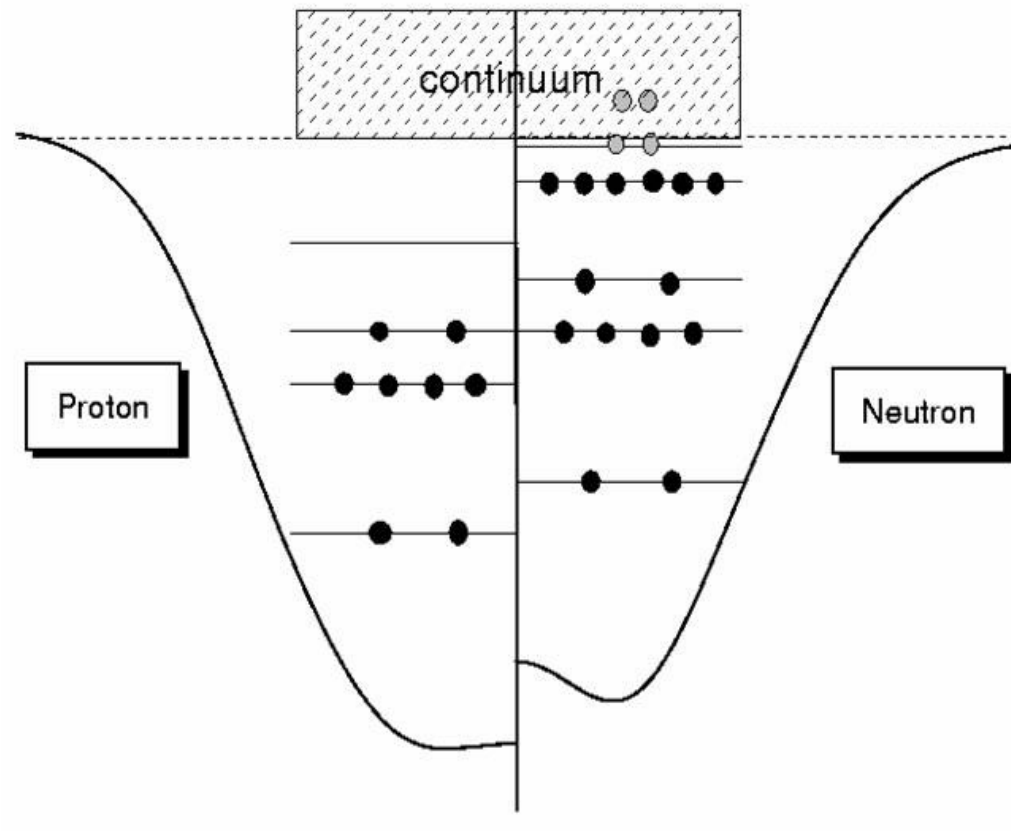
I. Tanihata, et al Phys. Rev. Lett. 55 (1985) 2676



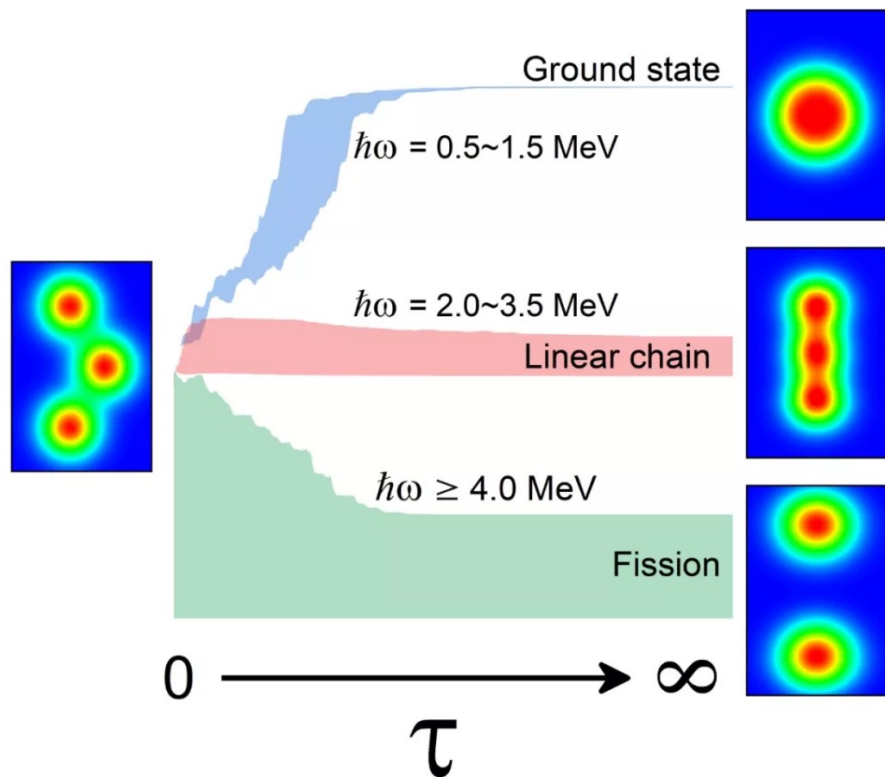
Meng and Ring, Phys. Rev. Lett. 77 (1996) 3963
 Meng and Ring, Phys. Rev. Lett. 80 (1998) 460

Shell structure, low density, continuum, bound state, spatial distribution, pairing correlation, coupling between bound state and continuum...

- Meng, Toki, Zhou, Zhang, Long & Geng, Prog. Part. Nucl. Phys. 57 (2006) 470
- Meng and Zhou, J. Phys. G: 42 (2015) 093101



$\beta_{\lambda\mu} = 0$	$\beta_{20} > 0$	$\beta_{20} < 0$	$\beta_{40} > 0$
$\beta_{22} \neq 0$	$\beta_{30} \neq 0$	$\beta_{32} \neq 0$	$\beta_{20} \gg 0$



By Bing-Nan Lu



Progress in Particle and Nuclear Physics 109 (2019) 103713



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Review

Towards an *ab initio* covariant density functional theory for nuclear structure

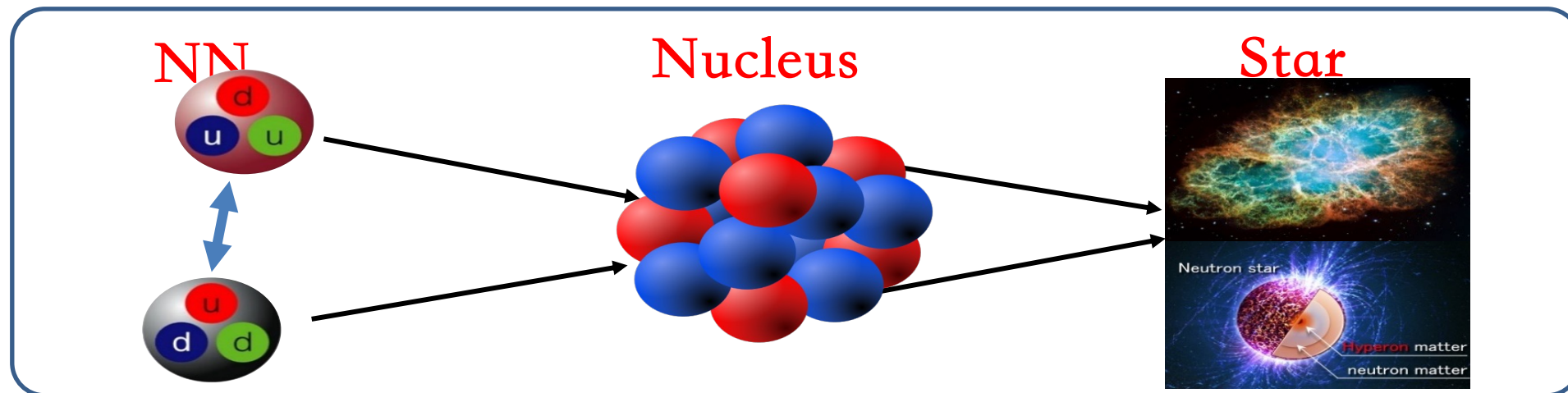
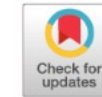
Shihang Shen^{a,b,c}, Haozhao Liang^{d,e}, Wen Hui Long^{f,g}, Jie Meng^{a,h,i,*},
Peter Ring^{a,j}

^a State Key Laboratory of Nuclear Physics and Technology, School of Physics, Peking University, Beijing 100871, China

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^c INFN, Sezione di Milano, via Celoria 16, I-20133 Milano, Italy

^d RIKEN Nishina Center, Wako 351-0198, Japan



QCD/EFT



Relativistic
ab initio



Relativistic
DFT

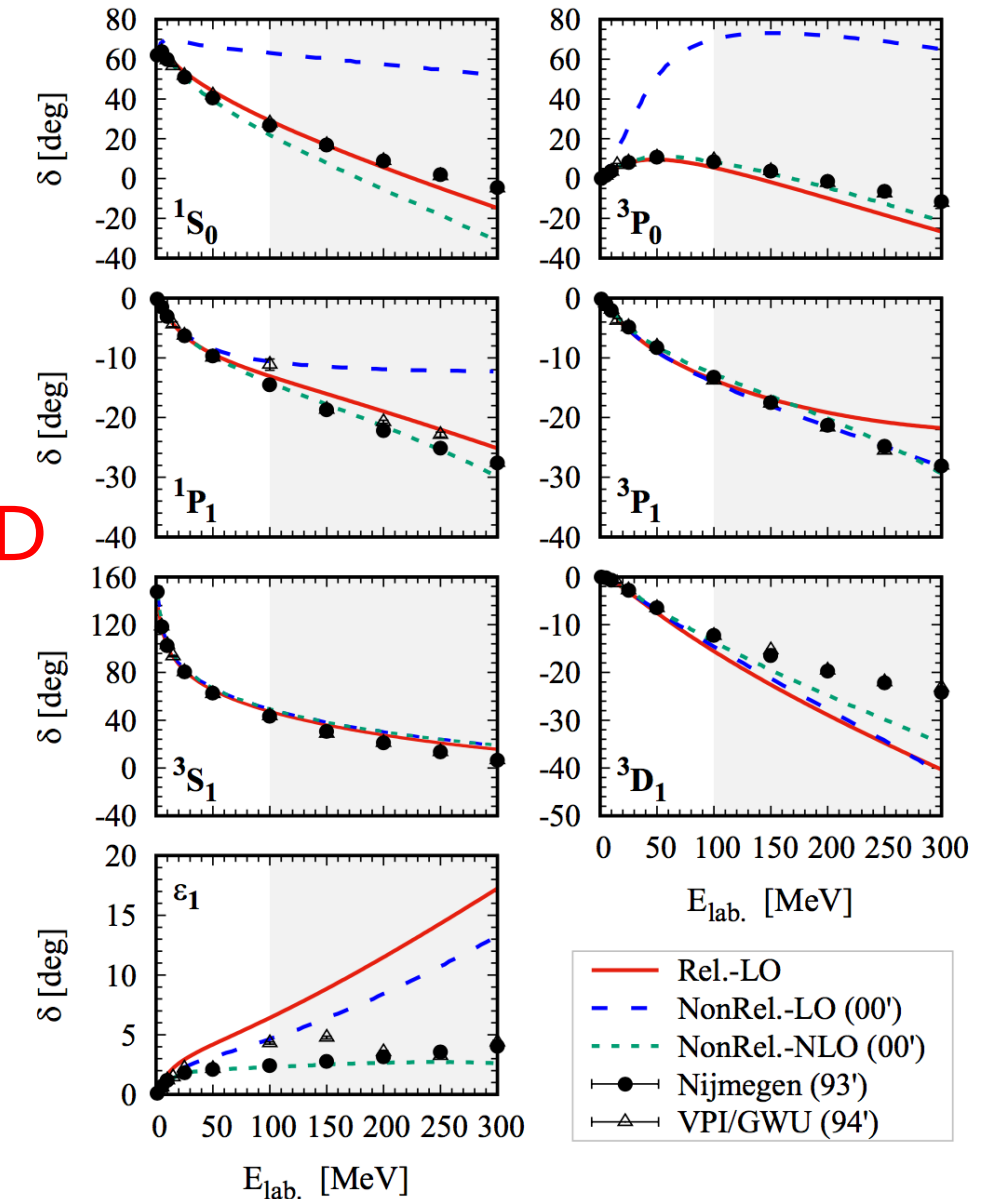


Chiral Nucleon-Nucleon Interaction

X. L. Ren, K. W. Li, L. S. Geng, B. W. Long, P. Ring, and J. Meng,

Leading order relativistic chiral nucleon-nucleon interaction,

Chin. Phys. C 42, 014103(2018)]



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Accurate Relativistic Chiral Nucleon-Nucleon Interaction up to Next-to-Next-to-Leading Order

Jun-Xu Lu, Chun-Xuan Wang, Yang Xiao, Li-Sheng Geng, Jie Meng, and Peter Ring
Phys. Rev. Lett. **128**, 142002 – Published 6 April 2022

Baryon Interaction by lattice QCD

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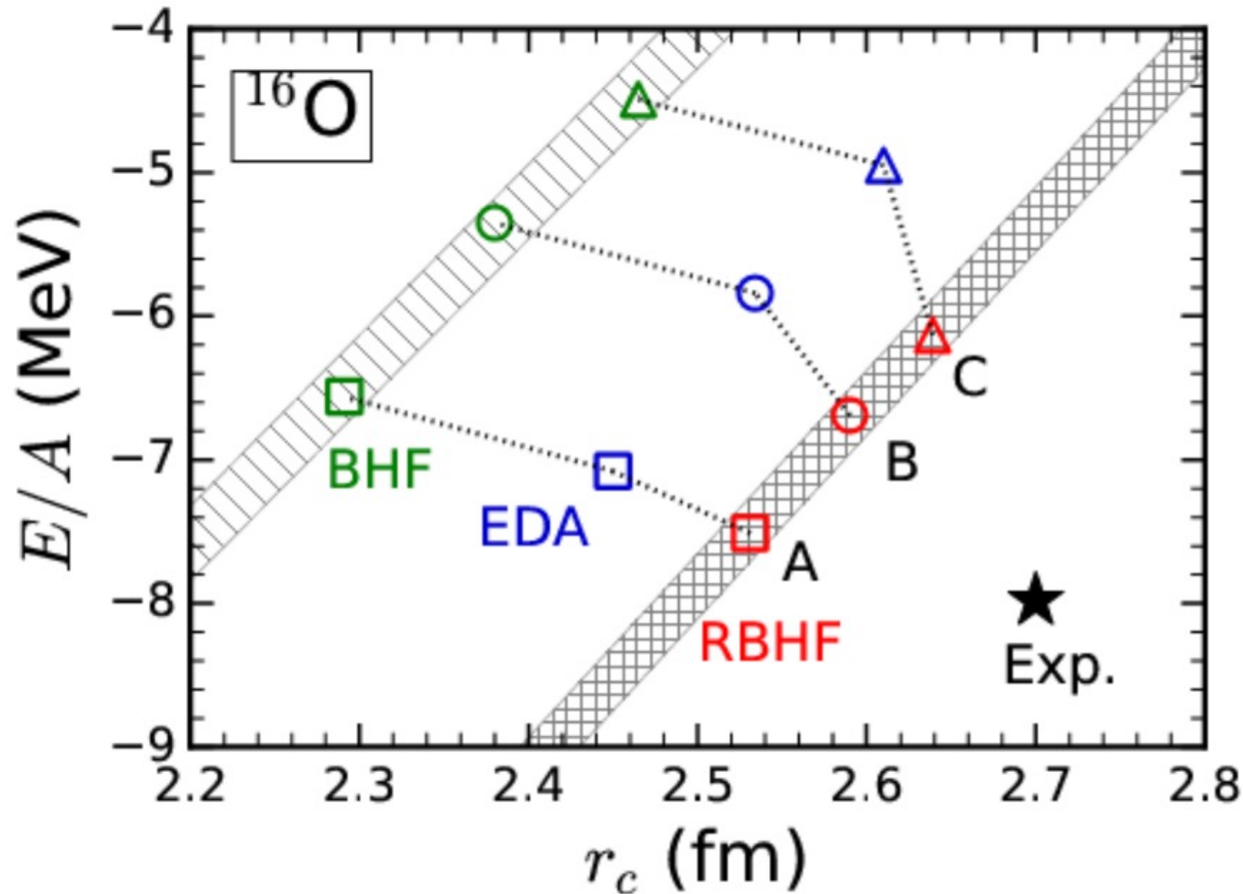
Accepted Paper

Dibaryon with highest charm number near unitarity from lattice QCD

Phys. Rev. Lett.
Yan Lyu, Hui Tong, Takuya Sugiura, Sinya Aoki, Takumi Doi, Tetsuo Hatsuda, Jie Meng, and Takaya Miyamoto
Accepted 2 July 2021

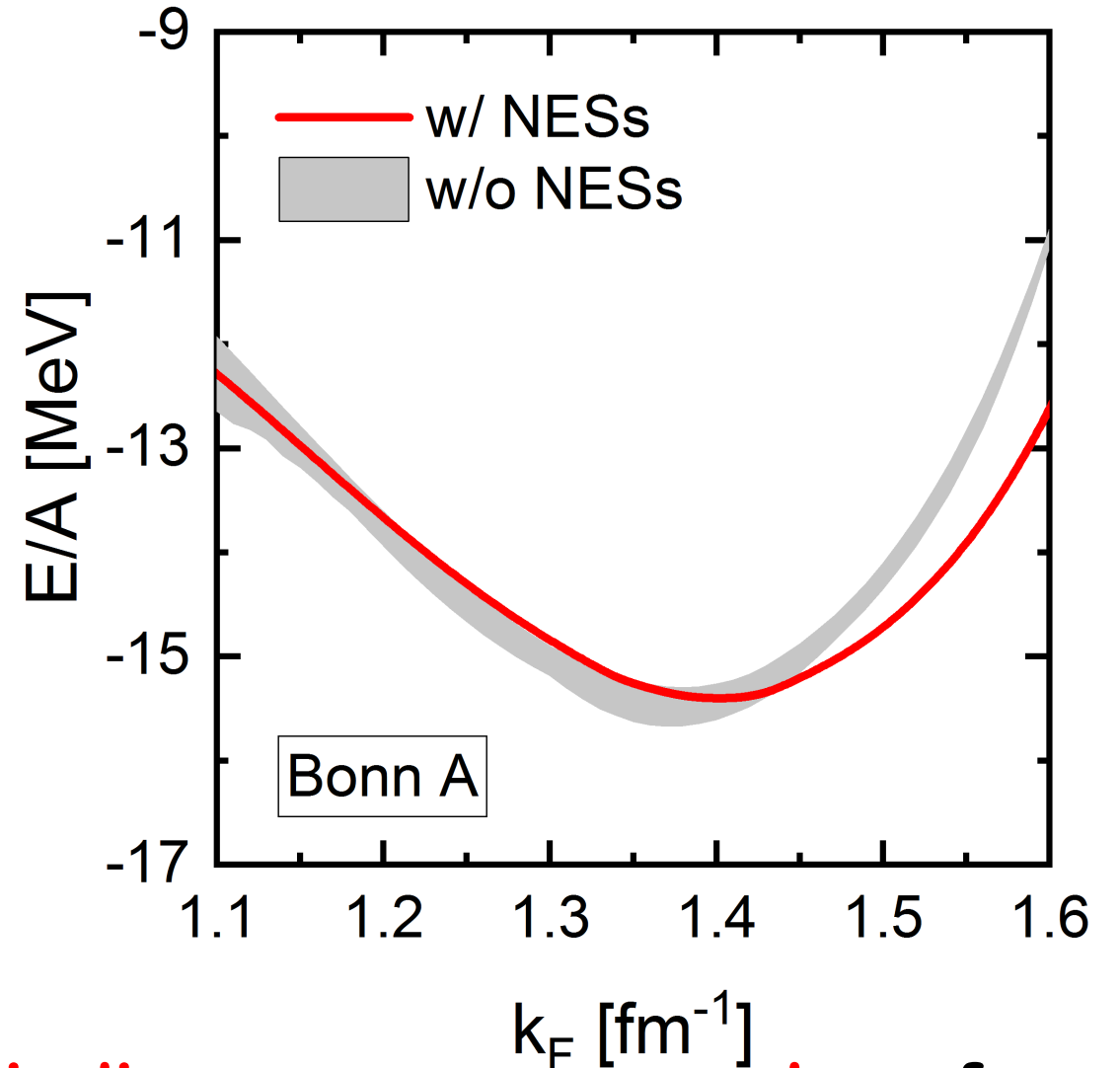


Relativistic Brueckner Hartree-Fock Theory



Energies and charge radii of ^{16}O in RBHF in comparison with EDA and BHF

Shen, Hu, Liang, Meng, Ring, Zhang,
Relativistic Brueckner-Hartree-Fock
Theory for Finite Nuclei .
Chin. Phys. Lett. 33 (2016) 102103

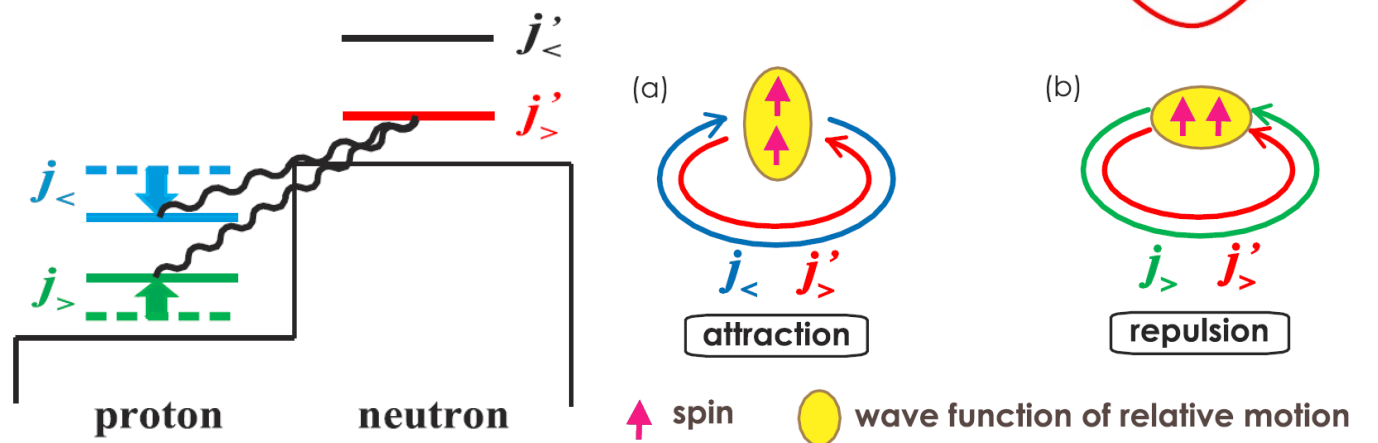
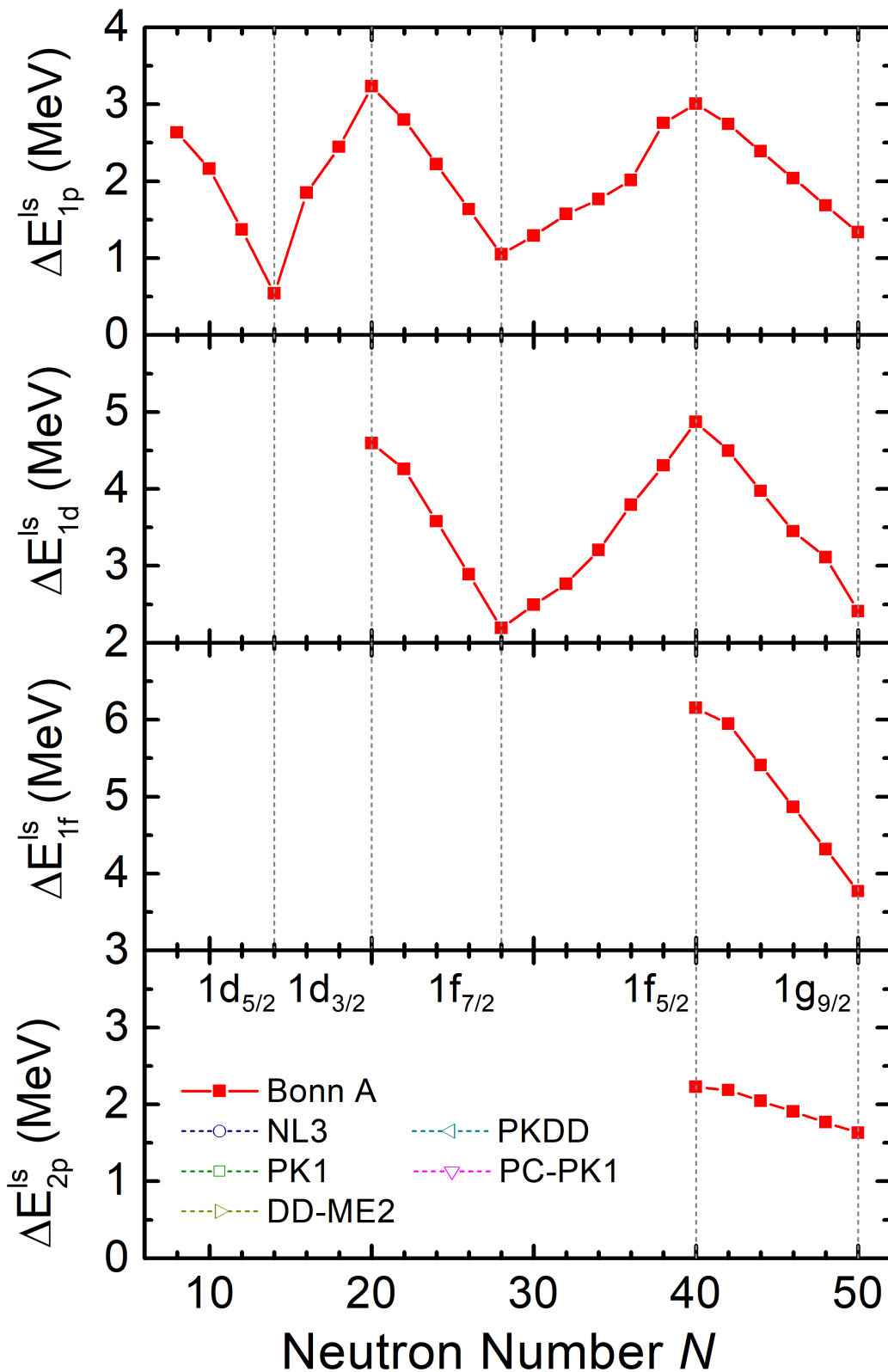
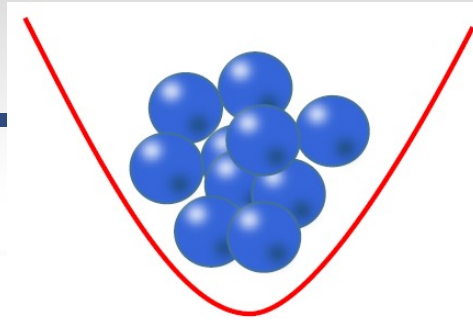


Binding energy per nucleon for symmetric nuclear matter by RBHF theory in full Dirac space

Wang, Zhao, Ring, Meng,
Nuclear matter in RBHF theory
with Bonn potential in the full Dirac
Phys. Rev. C 103(2021)054319



Spin-Orbit Splitting



Otsuka *et al.*, *Phys. Rev. Lett.* **95**, 232502 (2005)

□ The SO splitting **decreases** as the spin-up $j_> = l + 1/2$ orbitals are filled, while the SO splitting **increases** as the spin-down $j_< = l - 1/2$ orbitals are filled.

Shi-Hang Shen, Hao-Zhao Liang, Jie Meng, Peter Ring, Shuang-Quan Zhang,

Effects of tensor forces in nuclear spin-orbit splittings from ab initio calculations.

Phys. Lett. **B778** (2018) 344–348

Relativistic Brueckner-Hartree-Fock theory for neutron drops

Phys. Rev. C **97**, 054312 (2018)



北京大學

Fully self-consistent relativistic Brueckner theory

Progress in Particle and Nuclear Physics 109 (2019) 103713



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Review

Towards an *ab initio* covariant density functional theory for nuclear structure

Shihang Shen^{a,b,c}, Haozhao Liang^{d,e}, Wen Hui Long^{f,g}, Jie Meng^{a,h,i,*},
Peter Ring^{a,j}

^a State Key Laboratory of Nuclear Physics and Technology, School of Physics, Peking University, Beijing 100871, China

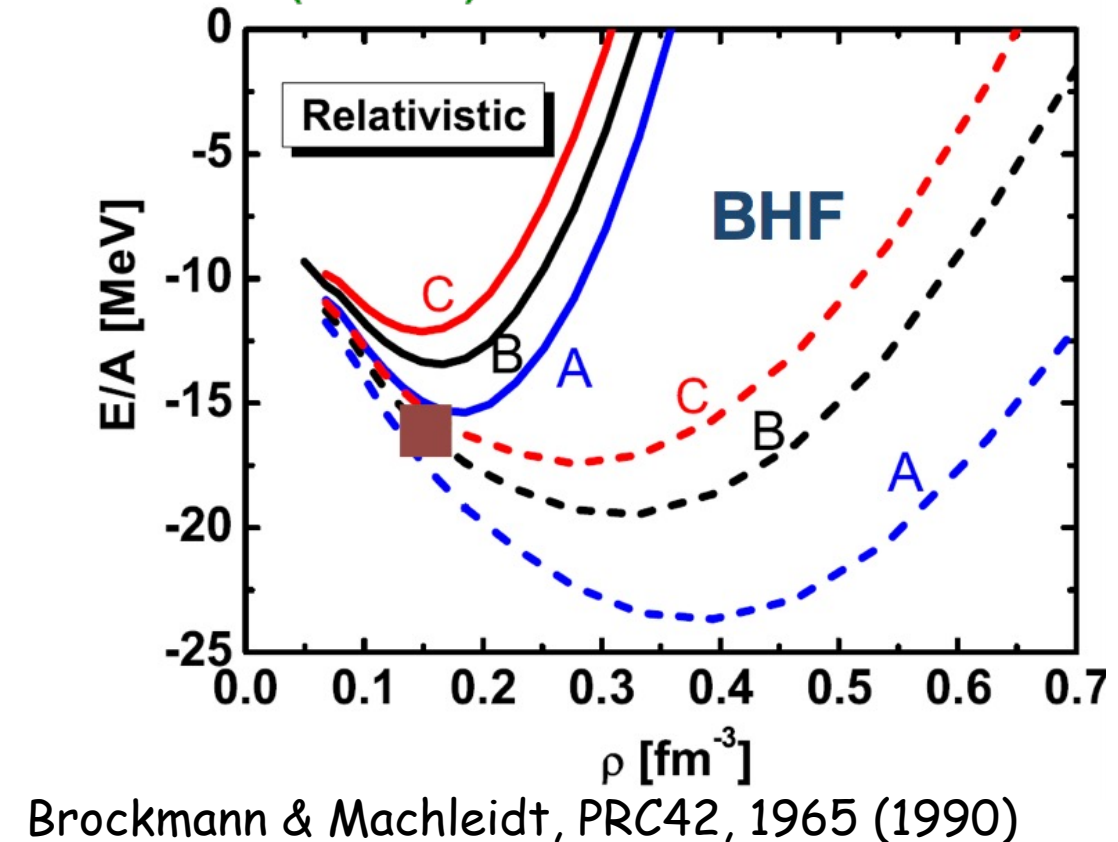
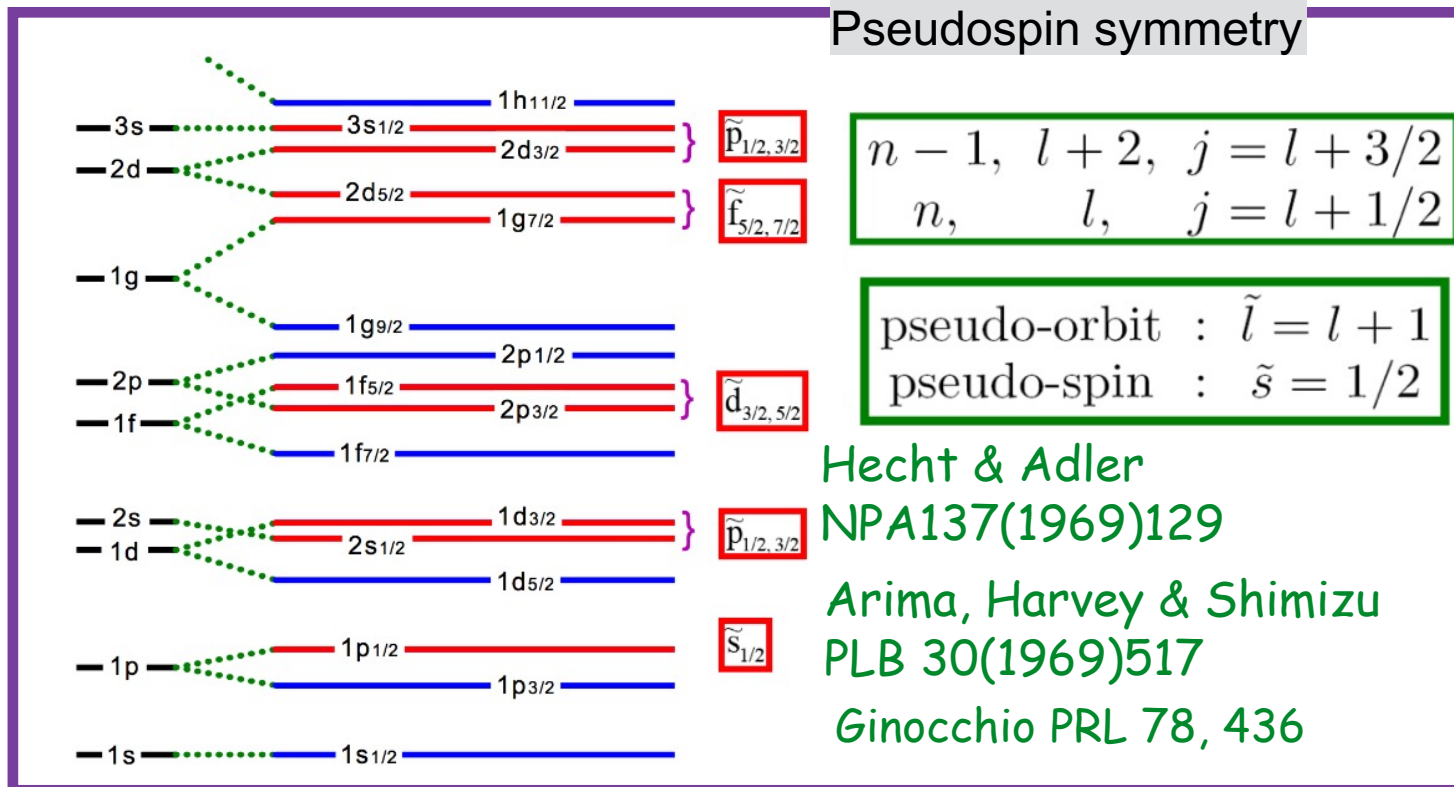
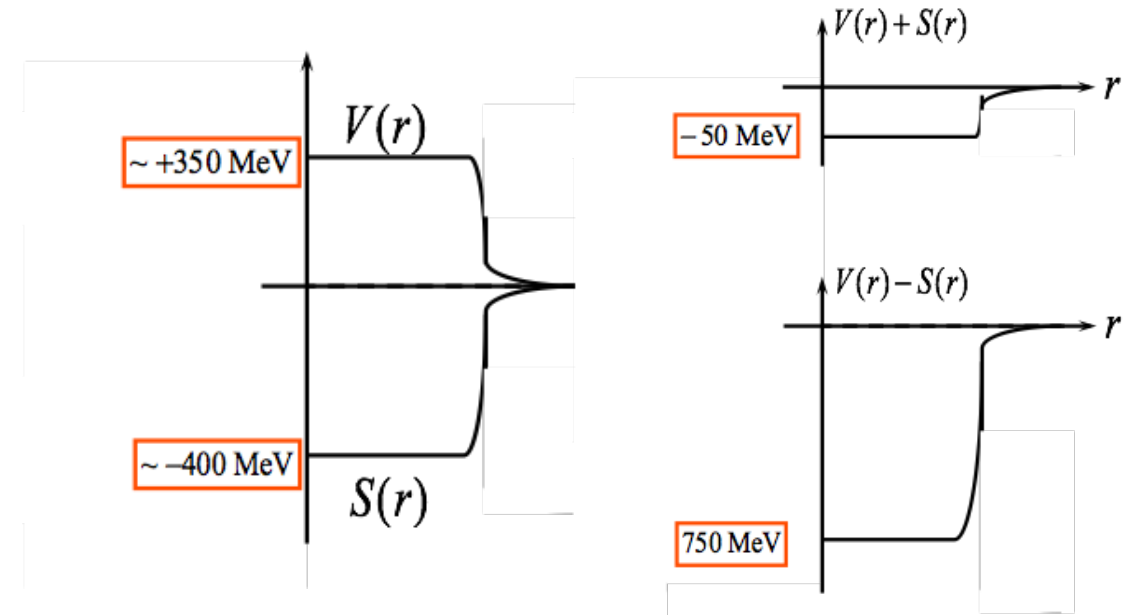
^b Dipartimento di Fisica, Università degli Studi di Milano, Italy

^c INFN, Sezione di Milano, via Celoria 16, I-20133 Milano, Italy

^d RIKEN Nishina Center, Wako 351-0198, Japan



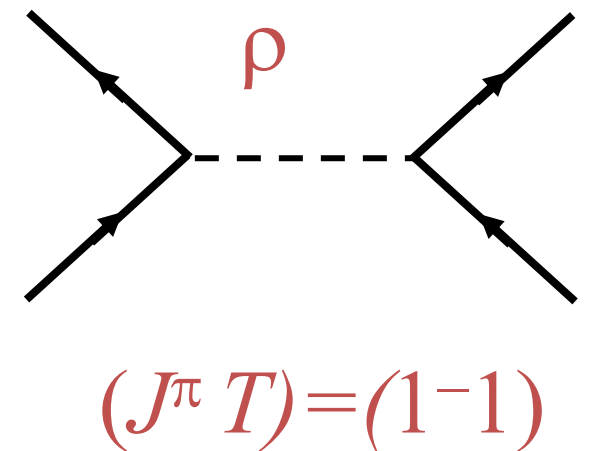
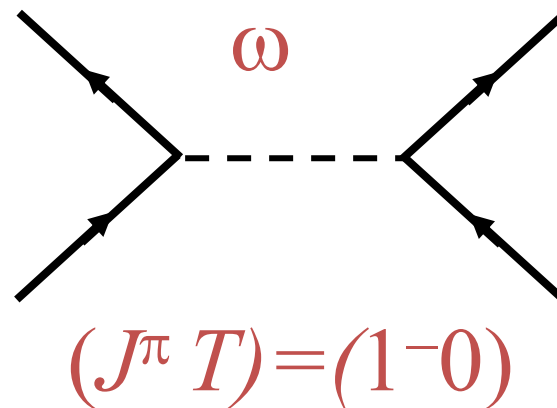
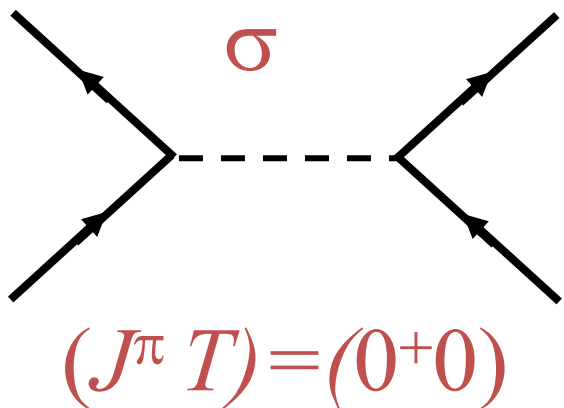
- ✓ **Spin-orbit** automatically included
- ✓ **Lorentz covariance** restricts parameters
- ✓ **Pseudo-spin** Symmetry
- ✓ Connection to QCD: big $V/S \sim \pm 400$ MeV
- ✓ Consistent treatment of **time-odd fields**
- ✓ Relativistic **saturation mechanism**
- ✓ ... **Liang, Meng, Zhou, Physics Reports 570 : 1-84 (2015).**





CDFT: Relativistic quantum many-body theory based on DFT and effective field theory for strong interaction

Strong force: Meson-exchange of the nuclear force



Sigma-meson:
attractive scalar field

Omega-meson:
Short-range repulsive

Rho-meson:
Isovector field

Electromagnetic force: The photon

Covariant Density Functional Theory

Elementary building blocks

$$(\bar{\psi} \mathcal{O}_\tau \Gamma \psi) \quad \mathcal{O}_\tau \in \{1, \tau_i\} \quad \Gamma \in \{1, \gamma_\mu, \gamma_5, \gamma_5 \gamma_\mu, \sigma_{\mu\nu}\}$$

Densities and currents

Isoscalar-scalar

$$\rho_S(\mathbf{r}) = \sum_k^{occ} \bar{\psi}_k(\mathbf{r}) \psi_k(\mathbf{r})$$

Isoscalar-vector

$$j_\mu(\mathbf{r}) = \sum_k^{occ} \bar{\psi}_k(\mathbf{r}) \gamma_\mu \psi_k(\mathbf{r})$$

Isovector-scalar

$$\vec{\rho}_S(\mathbf{r}) = \sum_k^{occ} \bar{\psi}_k(\mathbf{r}) \vec{\tau} \psi_k(\mathbf{r})$$

Isovector-vector

$$\vec{j}_\mu(\mathbf{r}) = \sum_k^{occ} \bar{\psi}_k(\mathbf{r}) \vec{\tau} \gamma_\mu \psi_k(\mathbf{r})$$

Energy Density Functional

$$E_{kin} = \sum_k v_k^2 \int \bar{\psi}_k (-\gamma \nabla + m) \psi_k d\mathbf{r}$$

$$E_{2nd} = \frac{1}{2} \int (\alpha_S \rho_S^2 + \alpha_V \rho_V^2 + \alpha_{tV} \rho_{tV}^2) d\mathbf{r}$$

$$E_{hot} = \frac{1}{12} \int (4\beta_S \rho_S^3 + 3\gamma_S \rho_S^4 + 3\gamma_V \rho_V^4) d\mathbf{r}$$

$$E_{der} = \frac{1}{2} \int (\delta_S \rho_S \Delta \rho_S + \delta_V \rho_V \Delta \rho_V + \delta_{tV} \rho_{tV} \Delta \rho_{tV}) d\mathbf{r}$$

$$E_{em} = \frac{e}{2} \int j_\mu^p A^\mu d\mathbf{r}$$



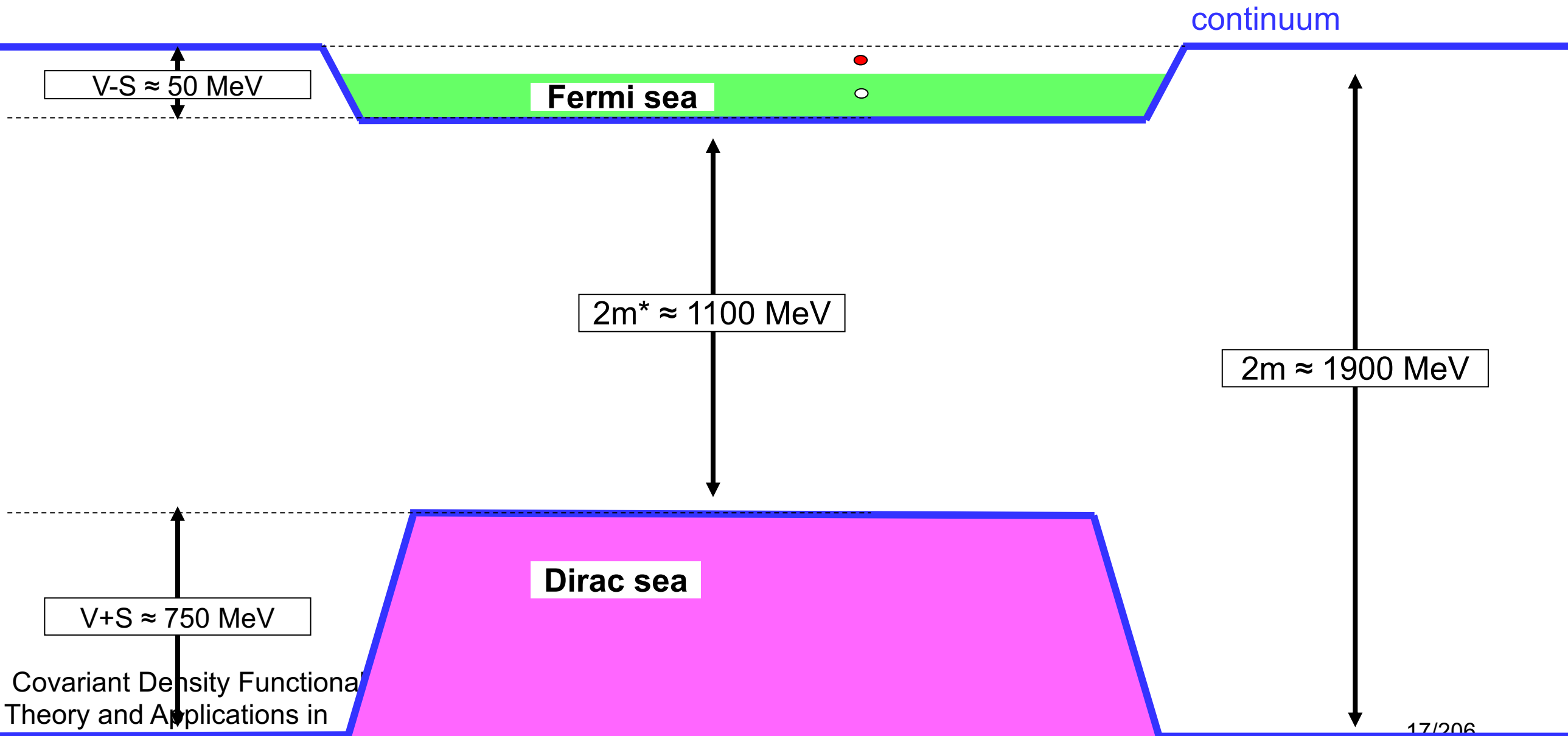
$$\begin{pmatrix} m + S + V & \sigma(p - V) \\ \sigma(p - V) & -m - S + V \end{pmatrix} \begin{pmatrix} f \\ g \end{pmatrix} = \epsilon \begin{pmatrix} f \\ g \end{pmatrix}$$

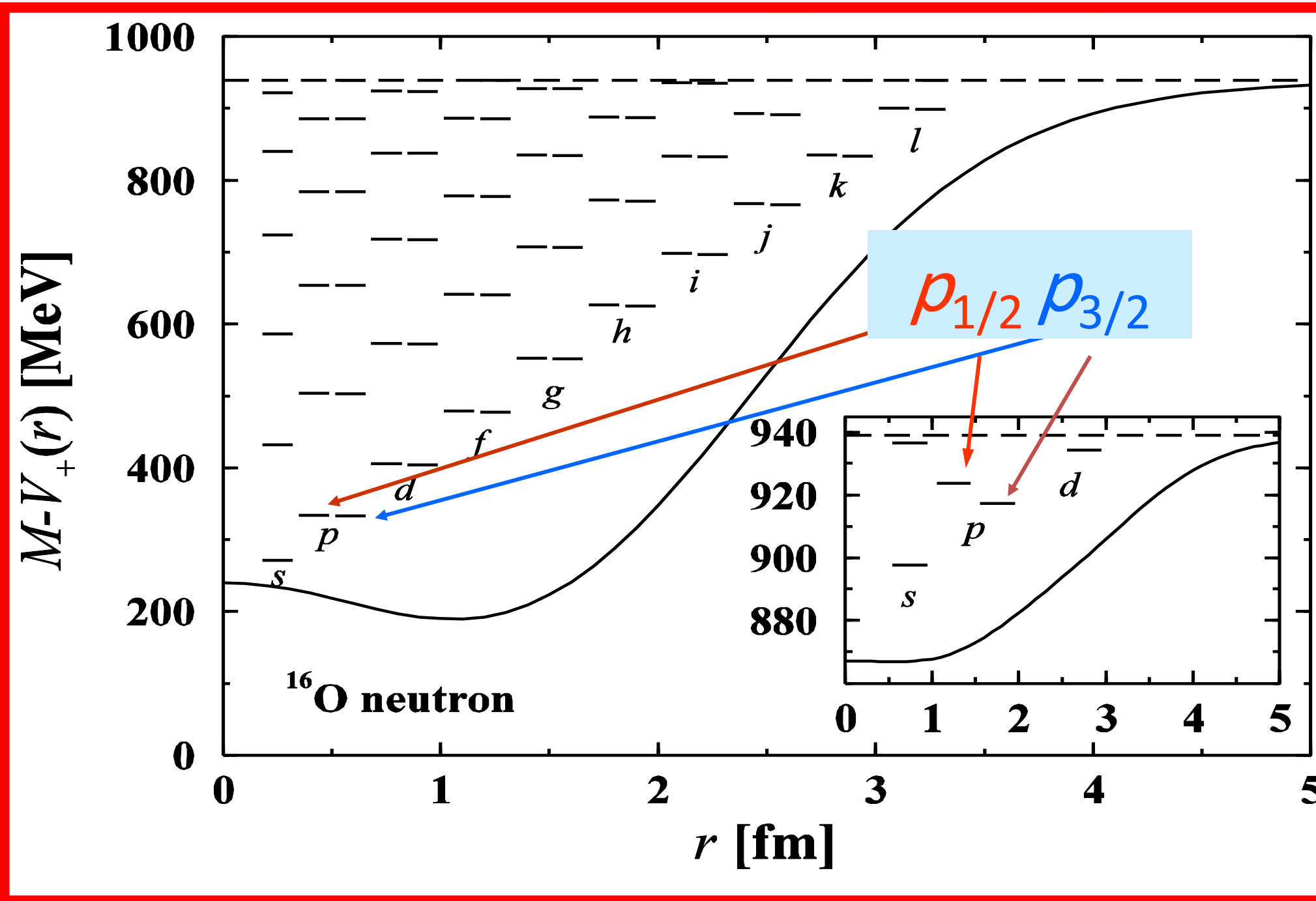
scalar potential:

$S(r) \approx -400 \text{ MeV}$

vector potential:

$V(r) \approx 350 \text{ MeV}$

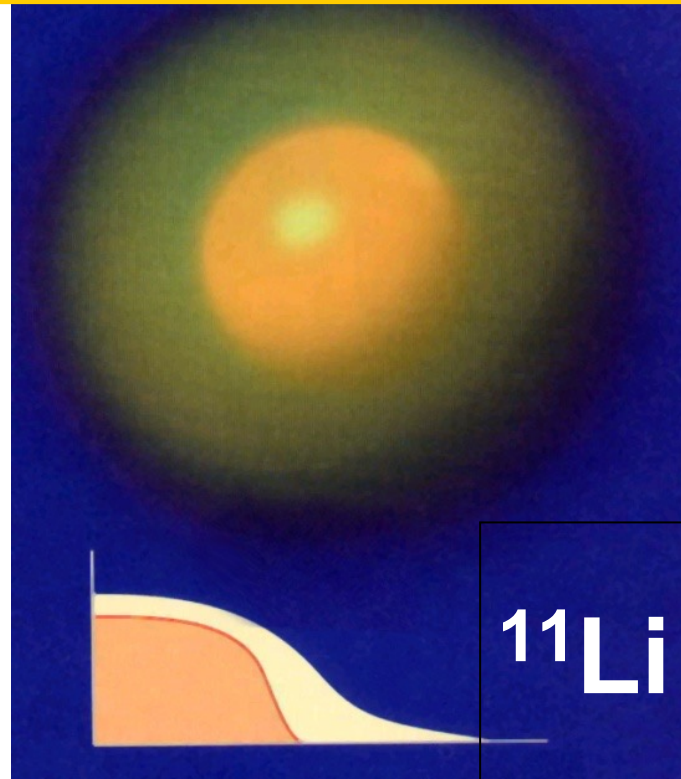
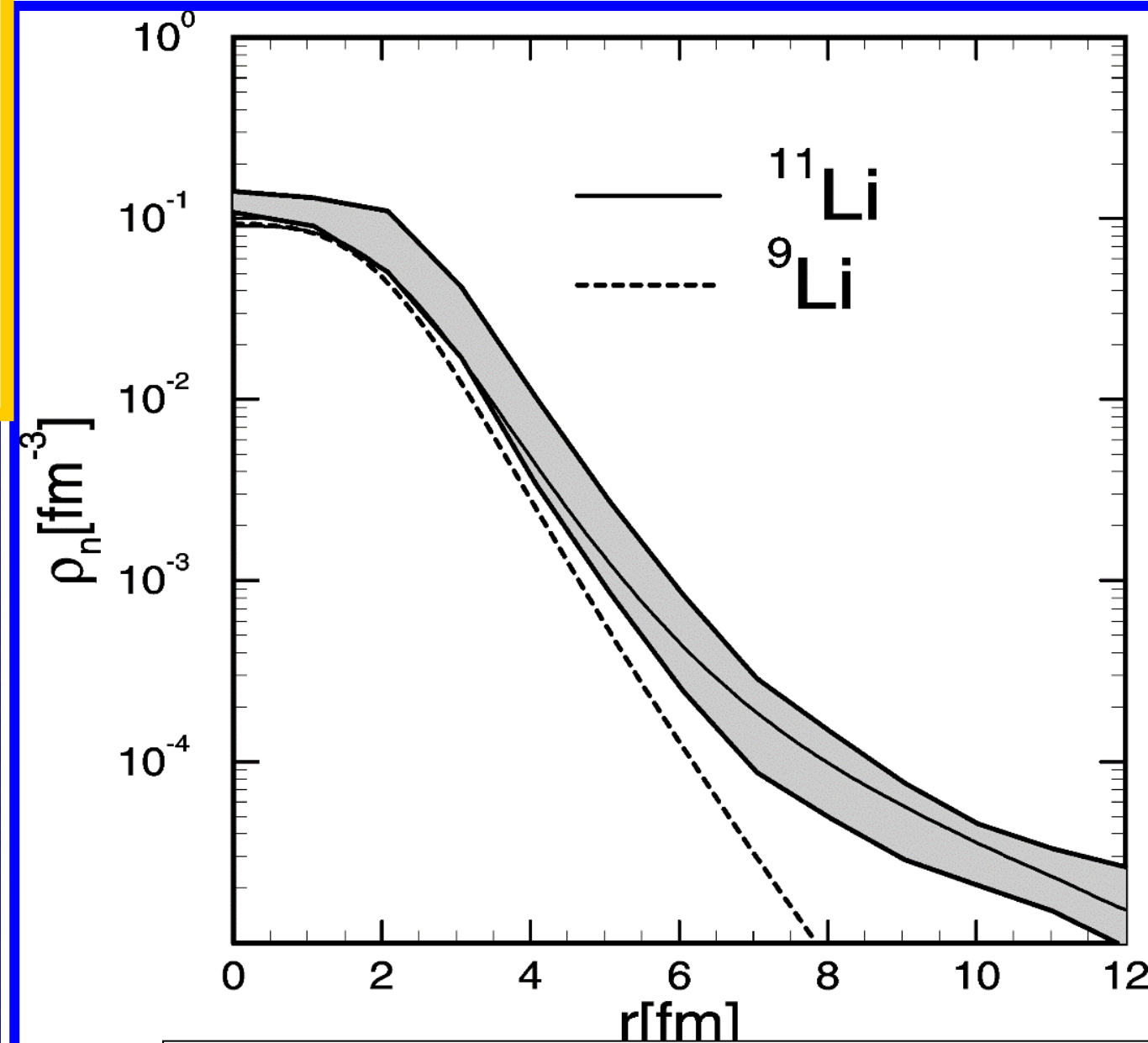
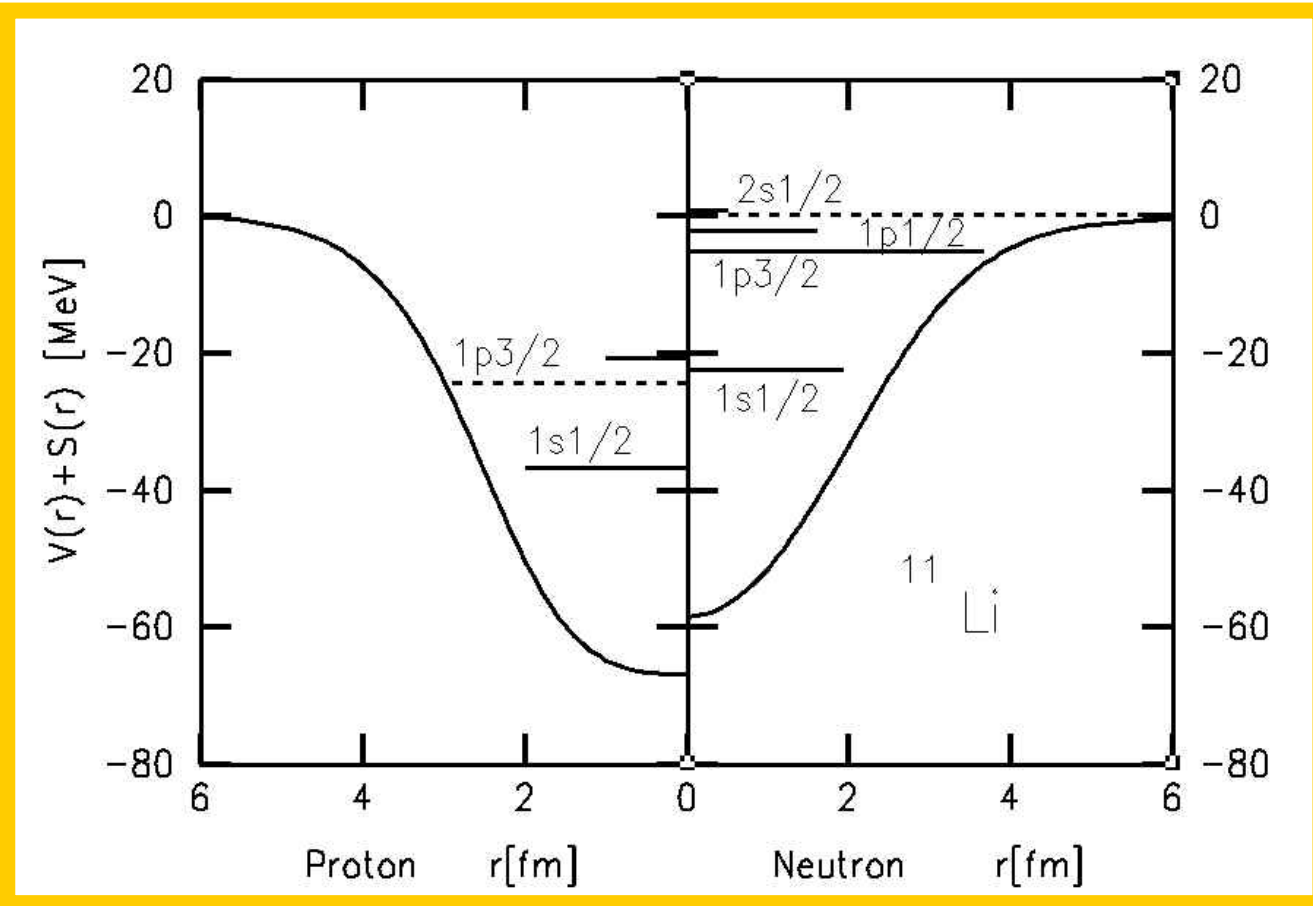




Zhou, Meng, Ring, PRL92(03)262501

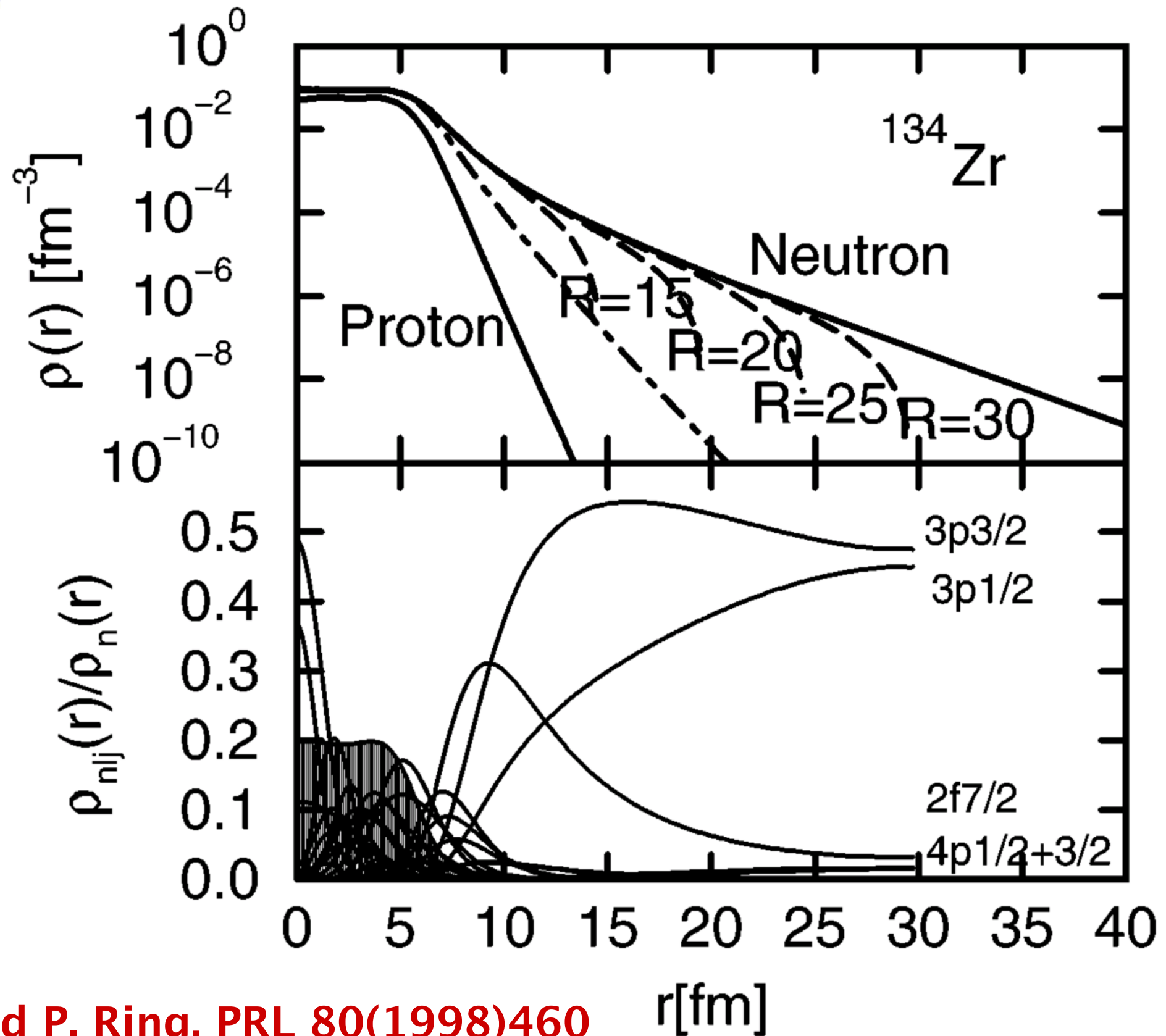


Relativistic Continuum Hartree-Bogoliubov theory with density dependent pairing force



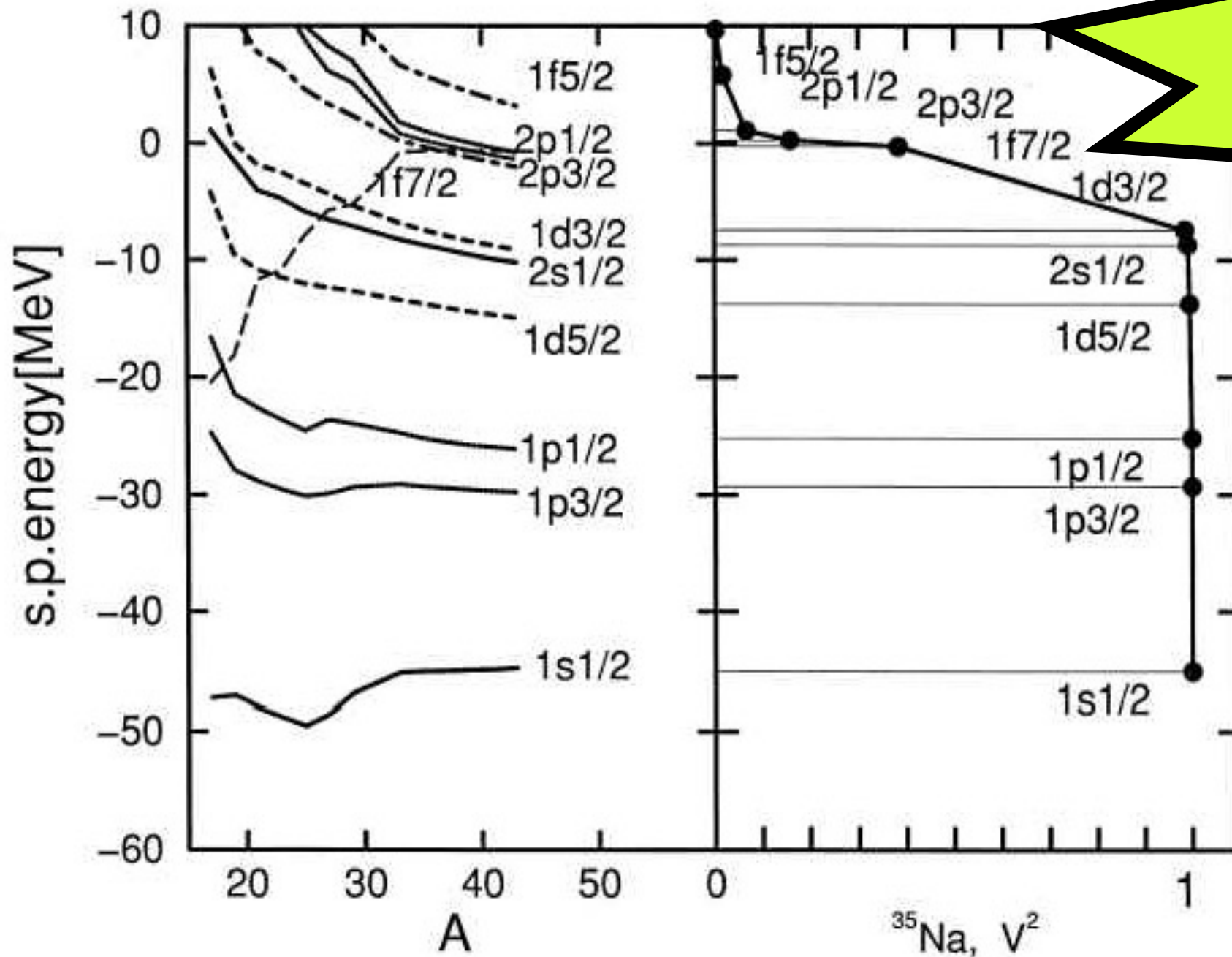


Giant halos

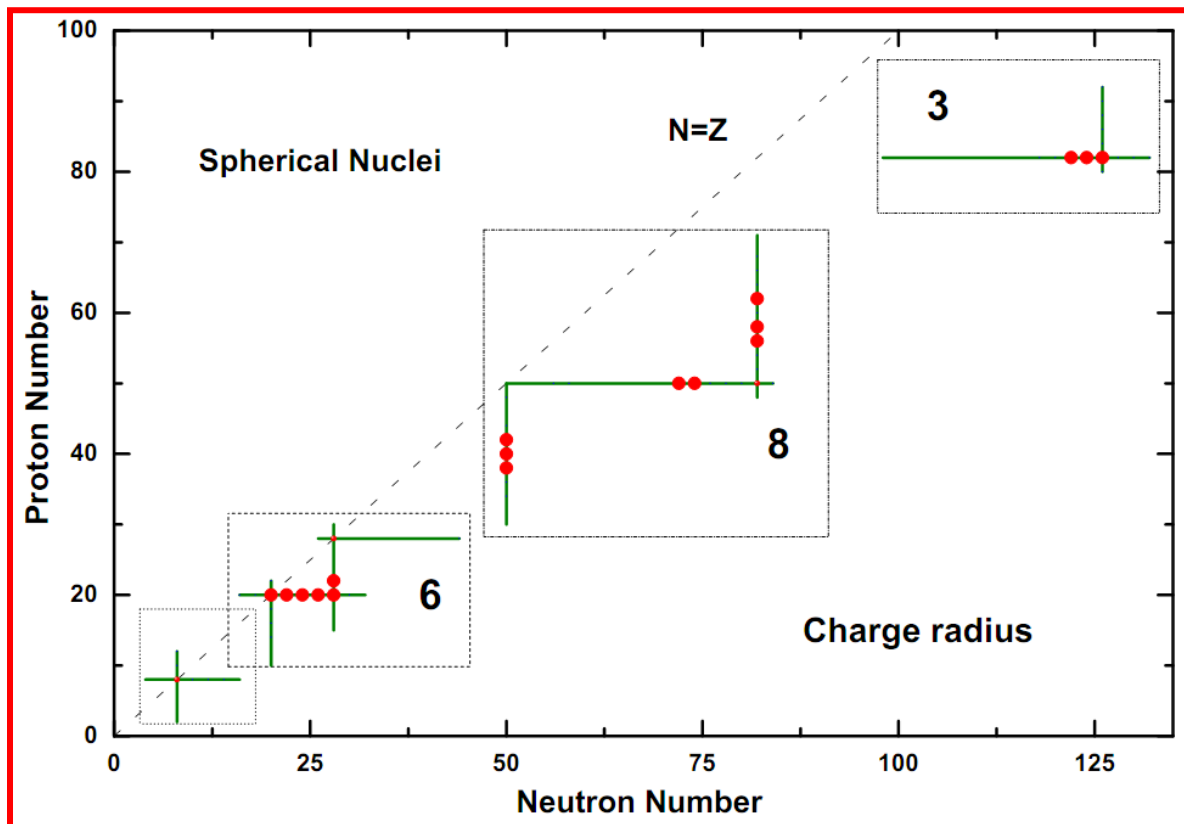
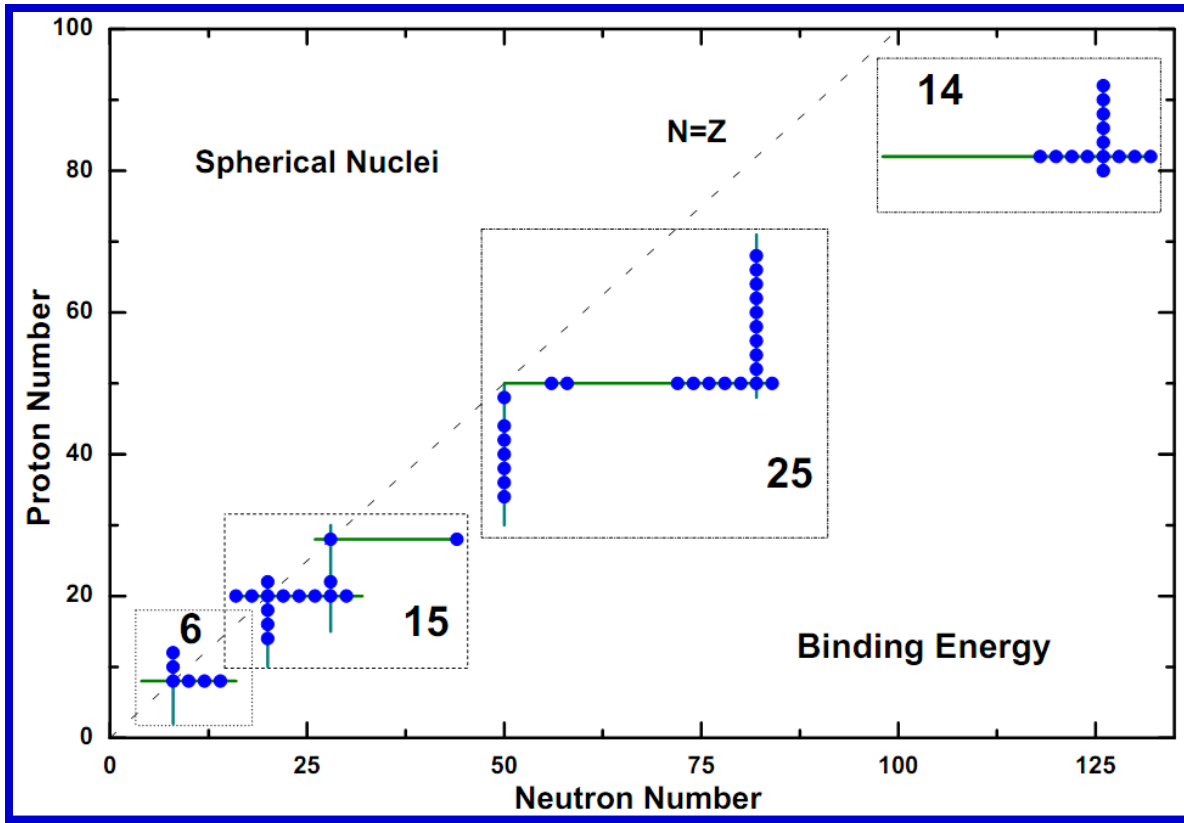




Meng, Tanihata & Yamaji, PLB419, 1(1998)

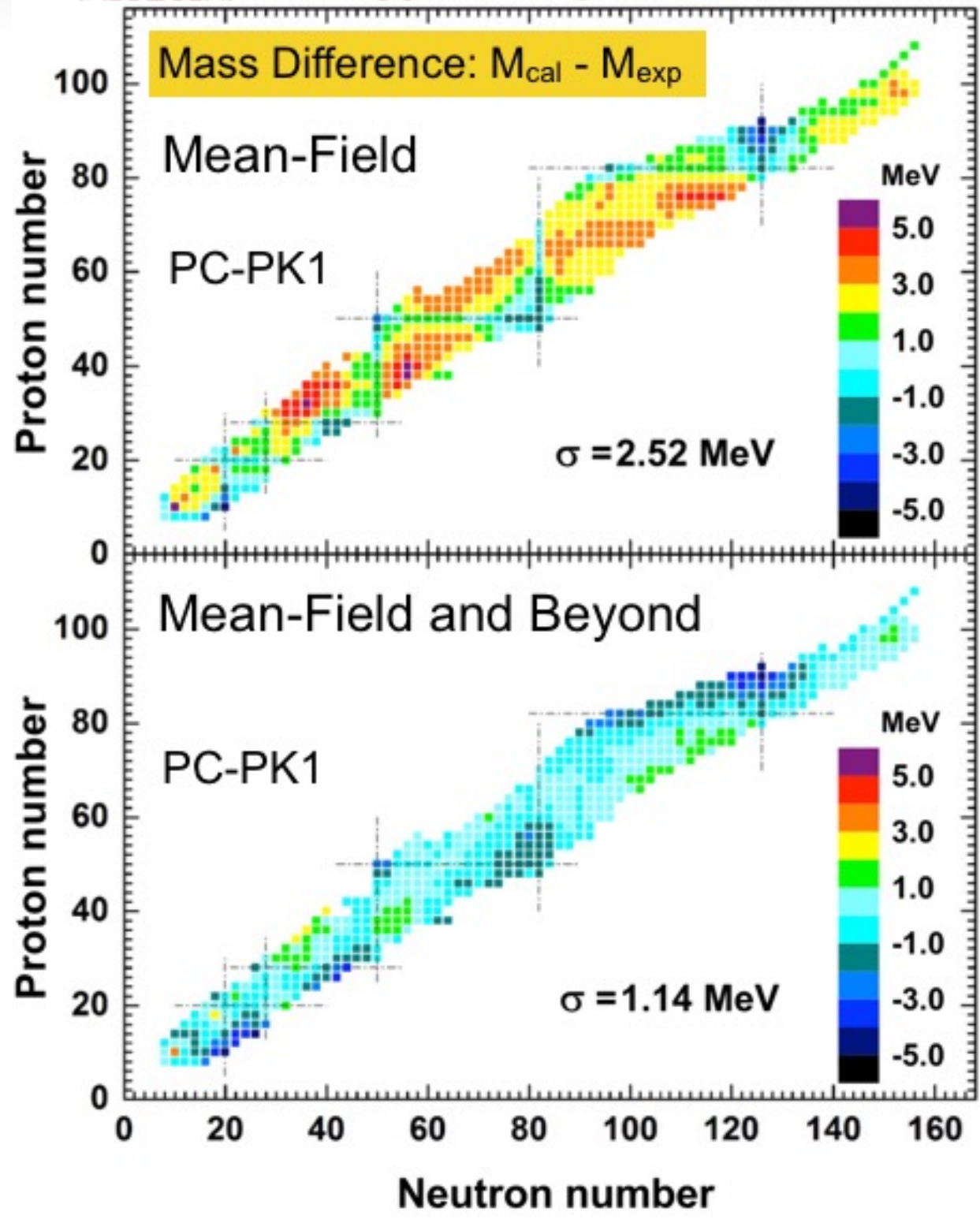


Earlier prediction
on giant halos
in Na isotopes

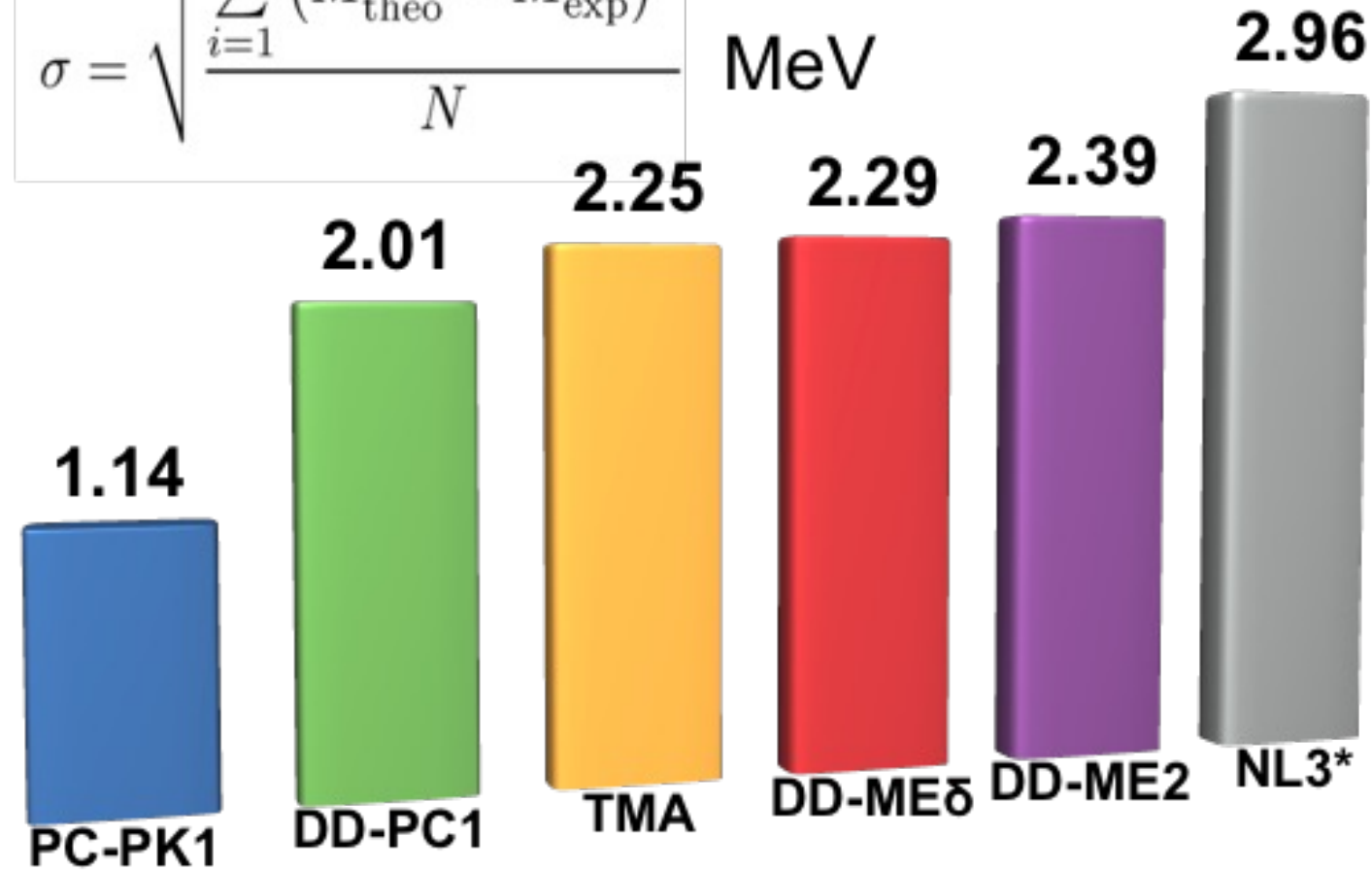


Coupl. Cons.	PC-PK1	Dimension
α_S [10 ⁻⁴]	-3.96291	MeV ⁻²
β_S [10 ⁻¹¹]	8.66530	MeV ⁻⁵
γ_S [10 ⁻¹⁷]	-3.80724	MeV ⁻⁸
δ_S [10 ⁻¹⁰]	-1.09108	MeV ⁻⁴
α_V [10 ⁻⁴]	2.69040	MeV ⁻²
γ_V [10 ⁻¹⁸]	-3.64219	MeV ⁻⁸
δ_V [10 ⁻¹⁰]	-4.32619	MeV ⁻⁴
α_{TV} [10 ⁻⁵]	2.95018	MeV ⁻²
δ_{TV} [10 ⁻¹⁰]	-4.11112	MeV ⁻⁴
V_n [10 ⁰]	-349.5	MeV fm ³
V_p [10 ⁰]	-330	MeV fm ³

Zhao, Li, Yao, Meng, PRC 82, 054319 (2010)



$$\sigma = \sqrt{\frac{\sum_{i=1}^N (M_{theo}^i - M_{exp}^i)^2}{N}}$$



Agbemava PRC 2014
Geng PTP 2005

Zhao, Li, Yao, Meng, PRC 82, 054319 (2010)

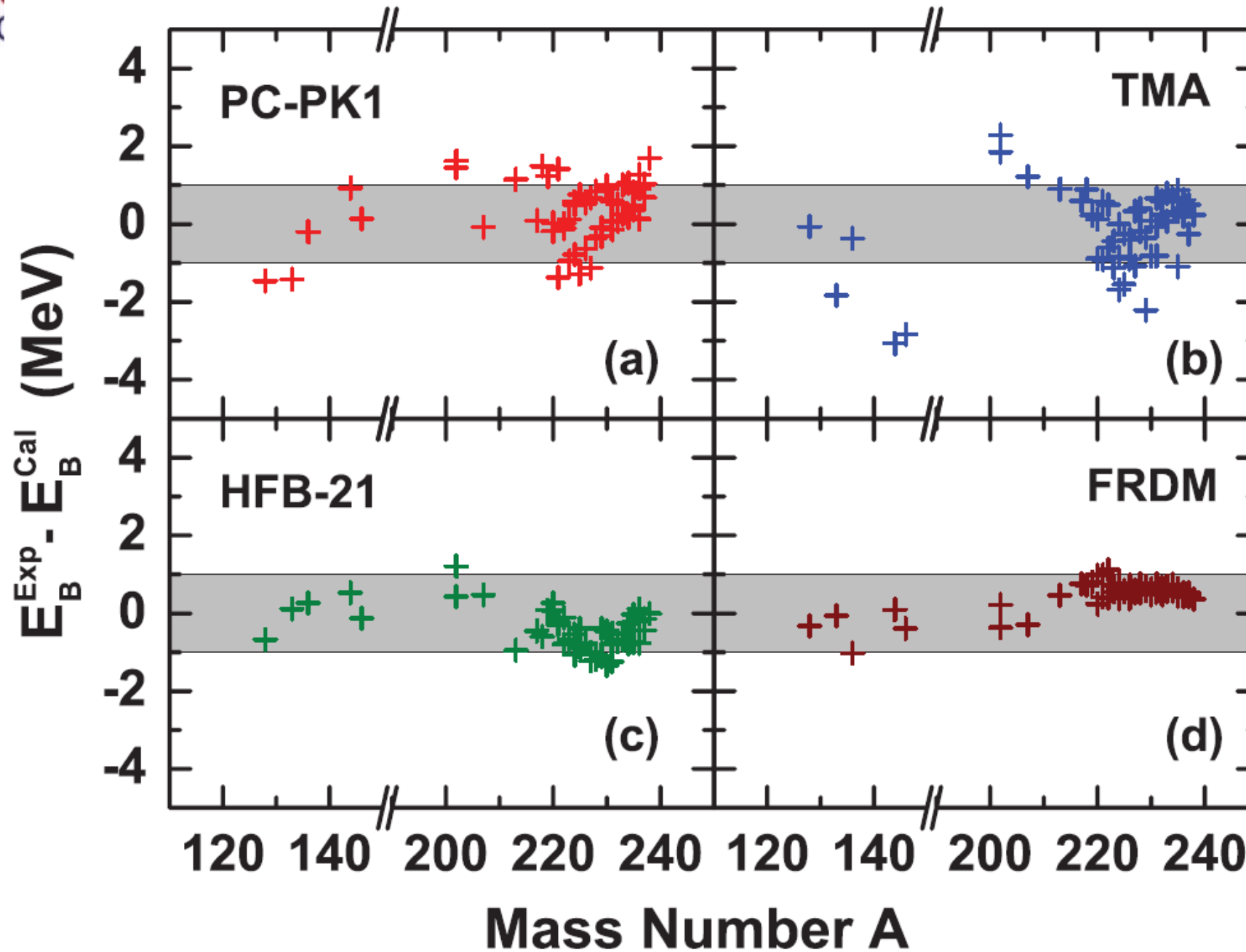
Zhang, Niu, Li, Yao, Meng, Front. Phys. 9 (2014) 529

Lu, Li, Li, Yao, Meng PRC 91 (2015) 027304

Best density functional for
nuclear masses so far!



Predictive power



P. W. Zhao, *et al.* Phys. Rev. C, 86 024324 (2012)

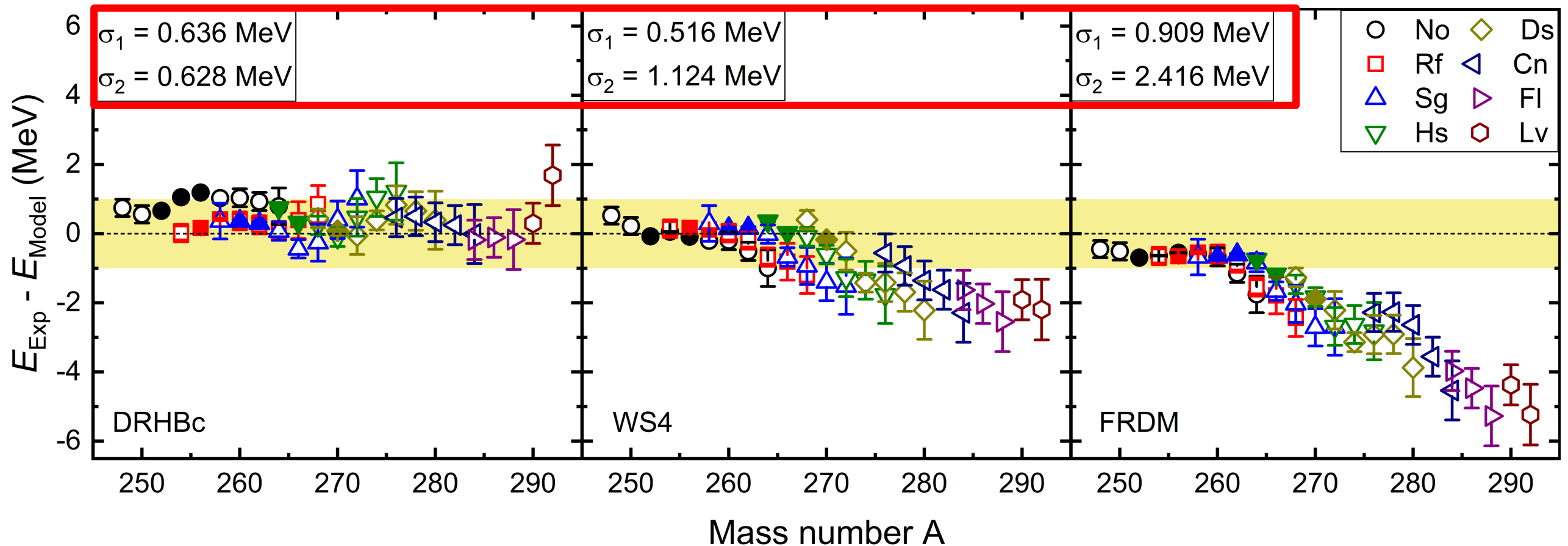
Data from L. Chen, *et al.* Nucl. Phys. A 882 71 (2012)

✓ 53 new mass measured at GSI are reproduced well by PC-PK1 (only 11 parameters) with a rms deviation of 0.859 MeV.



Predictive power

$Z = 102-116$



Kaiyuan Zhang, et al

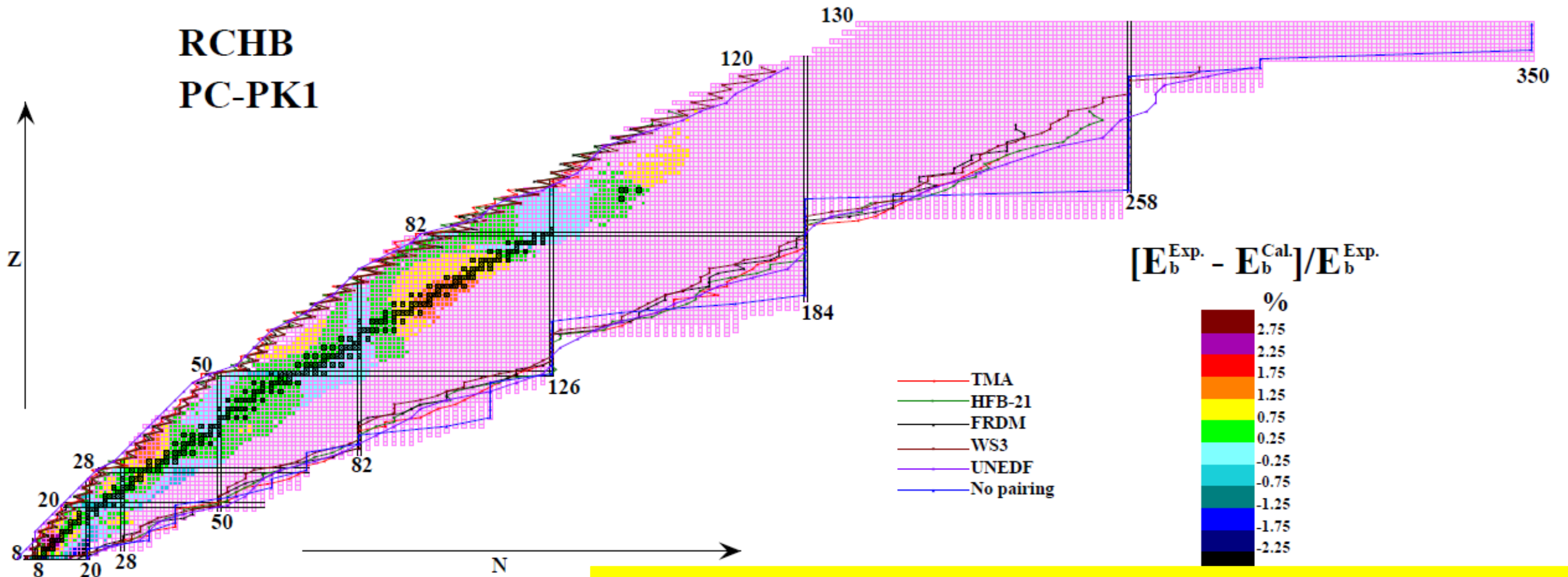
Phys. Rev. C104 (2021) L021301

Predictive power for superheavy nuclear mass and possible stability beyond the neutron drip line in deformed relativistic Hartree-Bogoliubov theory in continuum



Drip-lines in variant models

The number of bound nuclides with between 2 and 120 protons is around 7,000 28 JUNE 2012 | VOL 486 | NATURE | 509



$8 \leq Z \leq 120$: 9035 nuclei predicted to be bound
 Atomic Data and Nuclear Data Tables 121-122 (2018) 1-215

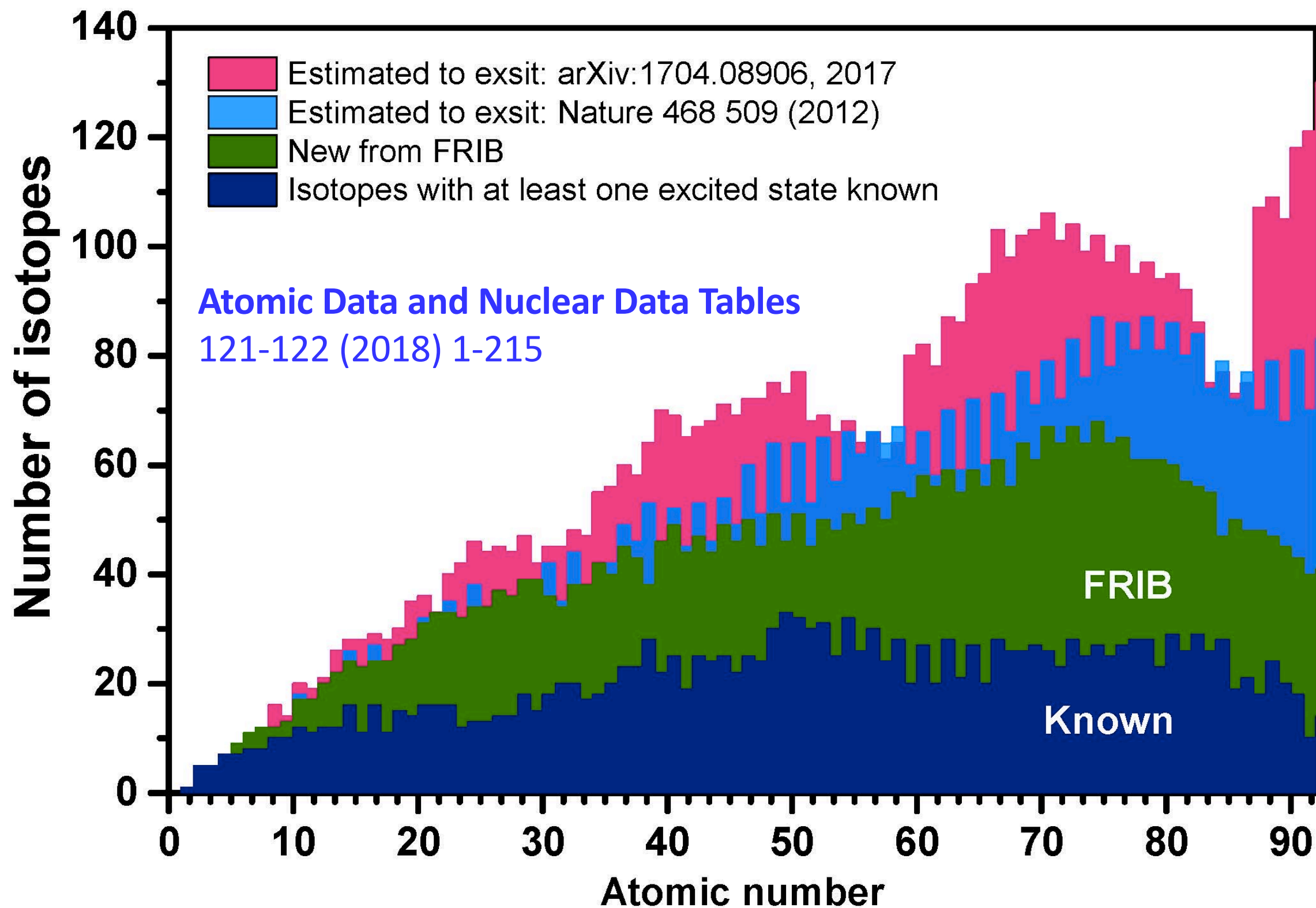
10532 bound nuclei from $Z=8$ to $Z=130$ predicted by RCHB theory with PC-PK1. For 2227 nuclei with data, binding energy differences between data and calculated results are shown in different color. The nucleon drip-lines predicted TMA, HFB-21, WS3, FRDM, UNEDF and without pairing correlation are plotted for comparison.

See also: Afanasjev, Agbemava, Ray, Ring, PLB726(2013)680



Possible existing isotopes

Atomic Data and Nuclear Data Tables 121-122(2018)1-215





First nuclear mass table including continuum effects

Atomic Data and Nuclear Data Tables 121–122 (2018) 1–215



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The limits of the nuclear landscape explored by the relativistic continuum Hartree–Bogoliubov theory

X.W. Xia^a, Y. Lim^{b,c}, P.W. Zhao^{d,e}, H.Z. Liang^f, X.Y. Qu^{a,g}, Y. Chen^{d,h}, H. Liu^d, L.F. Zhang^d, S.Q. Zhang^d, Y. Kim^c, J. Meng^{d,a,i,*}

^a School of Physics and Nuclear Energy Engineering, Beihang University, Beijing 100191, China

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^e Physics Division, Argonne National Laboratory, Argonne, IL 60439, USA

^f RIKEN Nishina Center, Wako 351-0198, Japan

^g School of Mechatronics Engineering, Guizhou Minzu University, China

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ⁱ Department of Physics, University of Stellenbosch, Stellenbosch, South Africa

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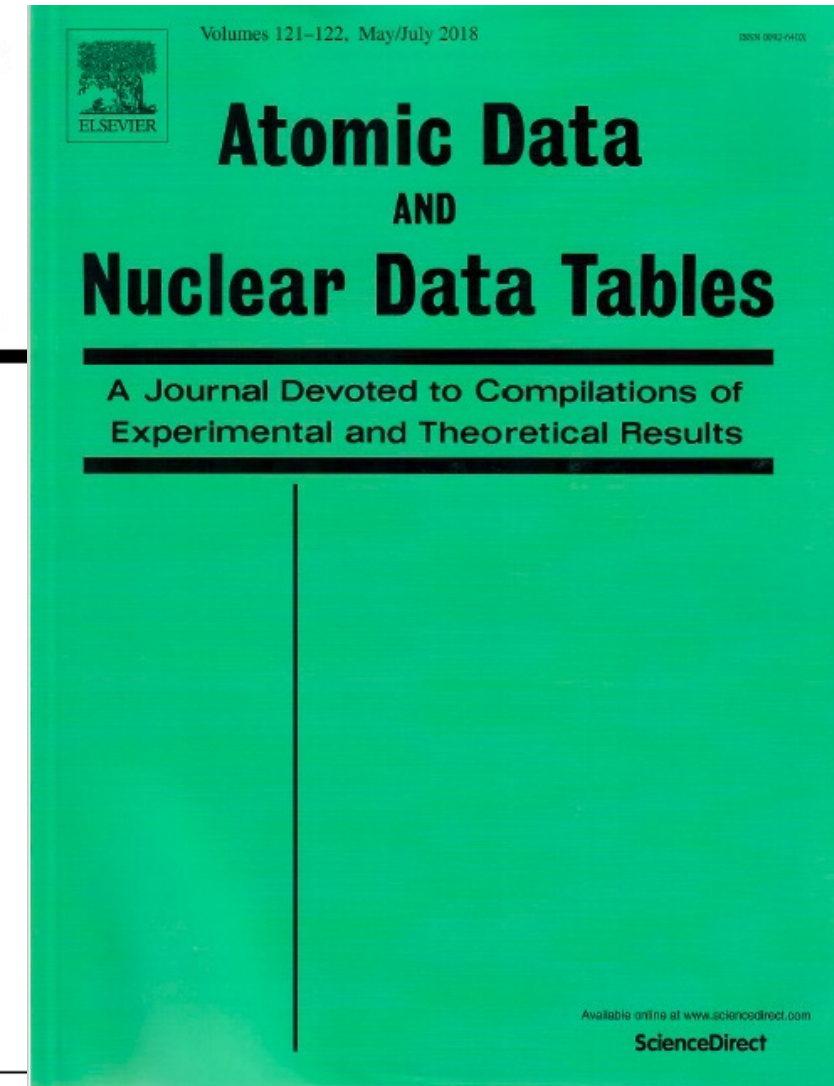
Received in revised form 12 August 2017

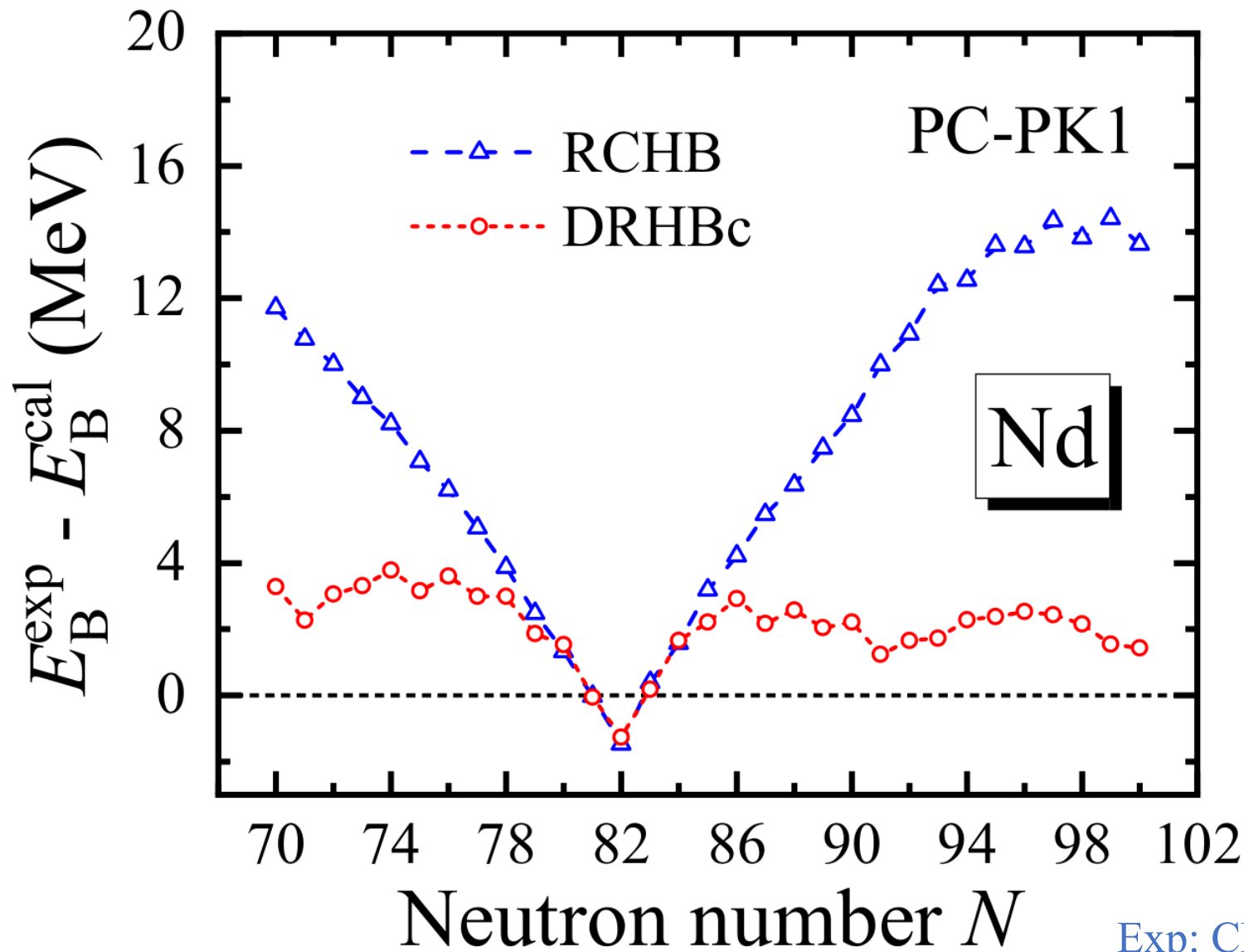
Accepted 5 September 2017

Available online 1 November 2017

ABSTRACT

The ground-state properties of nuclei with $8 \leq Z \leq 120$ from the proton drip line to the neutron drip line have been investigated using the spherical relativistic continuum Hartree–Bogoliubov (RCHB) theory with the relativistic density functional PC-PK1. With the effects of the continuum included, there are totally 9035 nuclei predicted to be bound, which largely extends the existing nuclear landscapes predicted with other methods. The calculated binding energies, separation energies, neutron and proton Fermi surfaces,





Exp: CPC 45, 030003 (2021)
 Even-even: PRC 102, 024314 (2020)

- ✓ Root-mean-square (rms) deviations:
 - **DRHBc 2.38 MeV** **RCHB 9.08 MeV**
- ✓ With deformation effect included, the data can be better reproduced.
- ✓ The rotational correction energy is expected to further improve the results for odd nuclei.



Deformed halos

✓ There has been controversy over the existence of deformed halo nuclei.

Otsuka, Muta, Yokoyama, Fukunishi, and Suzuki, NPA 588, 113c (1995)

Misu, Nazarewicz, and Aberg, NPA 614, 44 (1997)

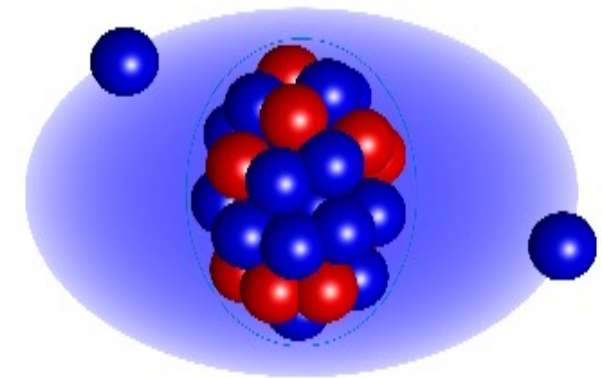
Tanihata, Hirata, and Toki, NPA 583, 769 (1995)

Nunes, NPA 757, 349 (2005)

✓ Considering deformation, pairing, and continuum effects, **the deformed relativistic Hartree-Bogoliubov theory in continuum (DRHBc)** predicts deformed halo nuclei.

Zhou, Meng, Ring, and Zhao, PRC 82, 011301(R) (2010)

Li, Meng, Ring, Zhao, and Zhou, PRC 85, 024312 (2012)



✓ Recently, candidates of deformed halo nuclei have been suggested in experiment, ^{31}Ne and ^{37}Mg .

Nakamura *et al.*, PRL 112, 142501 (2014)

Kobayashi *et al.*, PRL 112, 242501 (2014)

✓ DRHBc theory has been applied for halo and other exotic phenomena.

Sun, Zhao, and Zhou, PLB 785, 530 (2018)

Zhang, Wang, and Zhang PRC 100, 034312 (2019)

Sun, Zhao, and Zhou, NPA 1003, 122011 (2020)

Yang *et al.*, PRL 126, 082501 (2021)

Sun, PRC 103, 054315 (2021)

Zhang *et al.*, PRC 104, L021301 (2021)

Pan *et al.*, PRC 104, 024331 (2021)

He *et al.*, CPC 45, 101001 (2021)



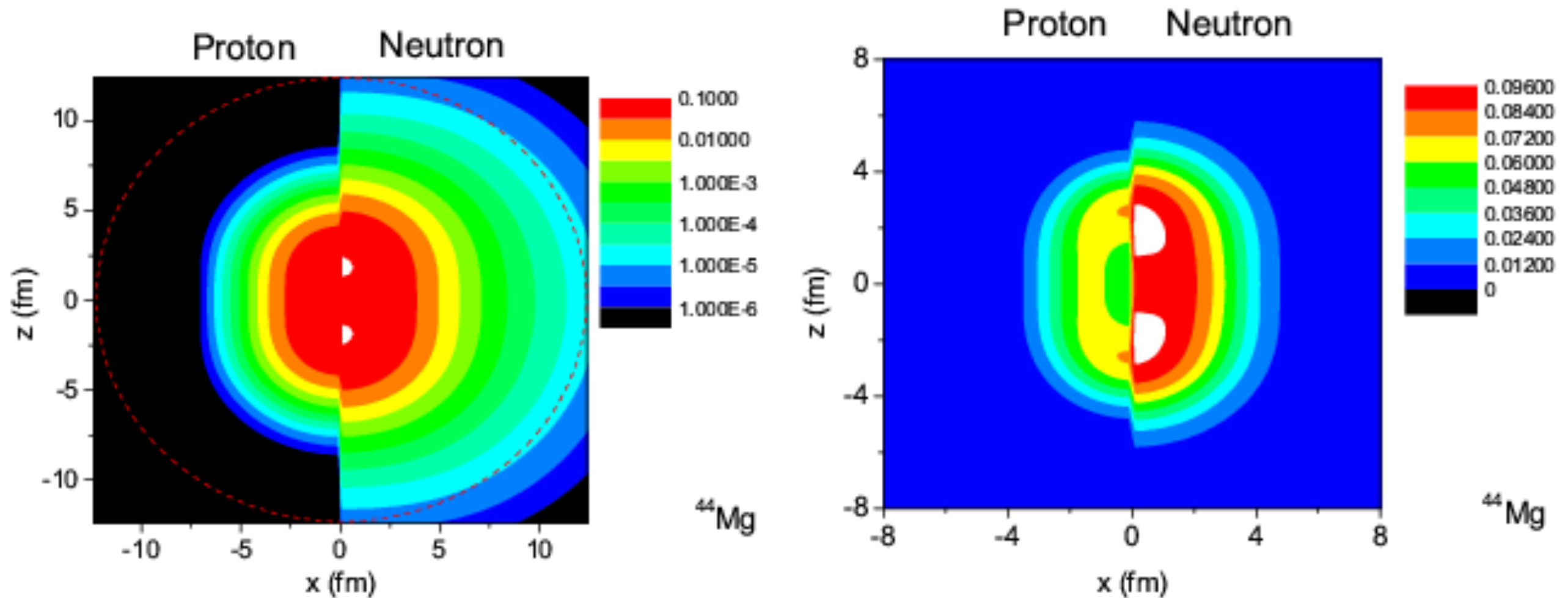
^{44}Mg : Density distributions

Zhou_Meng_Ring_Zhao2010_PRC82-011301R

Zhou_Meng_Ring_Zhao2011_JPConfProc312-092067

Li_Meng_Ring_Zhao_Zhou2012_PRC85-024312

- Prolate deformation
- Large spatial extension in neutron density distribution

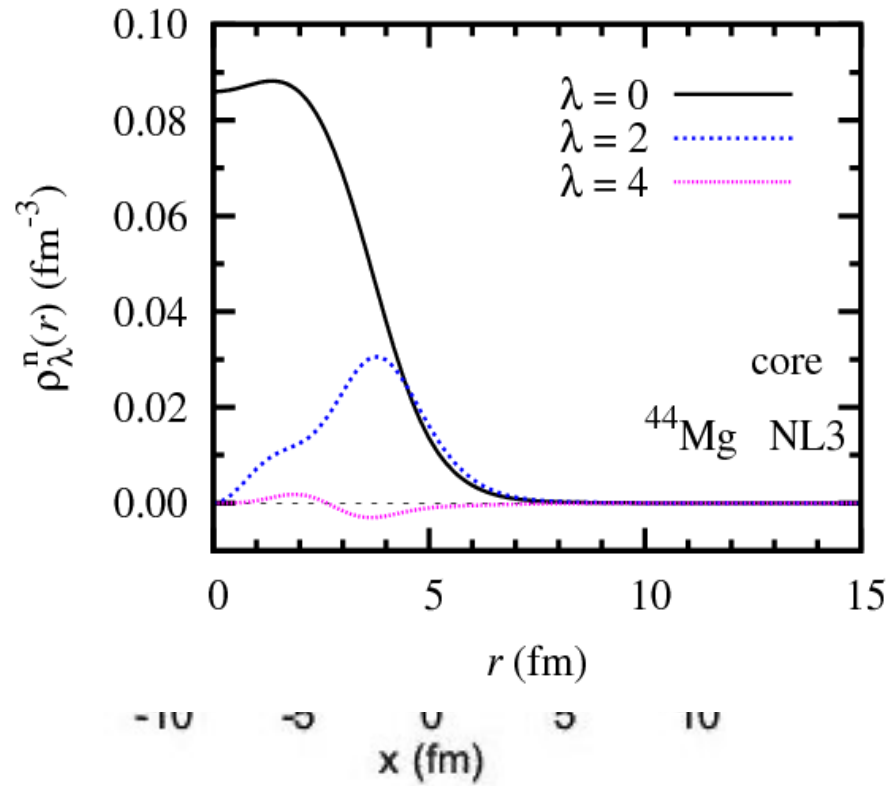


Viewpoint: A Walk Along the Dripline by Paul Cottle and Kirby Kemper
<http://link.aps.org/doi/10.1103/Physics.5.49>



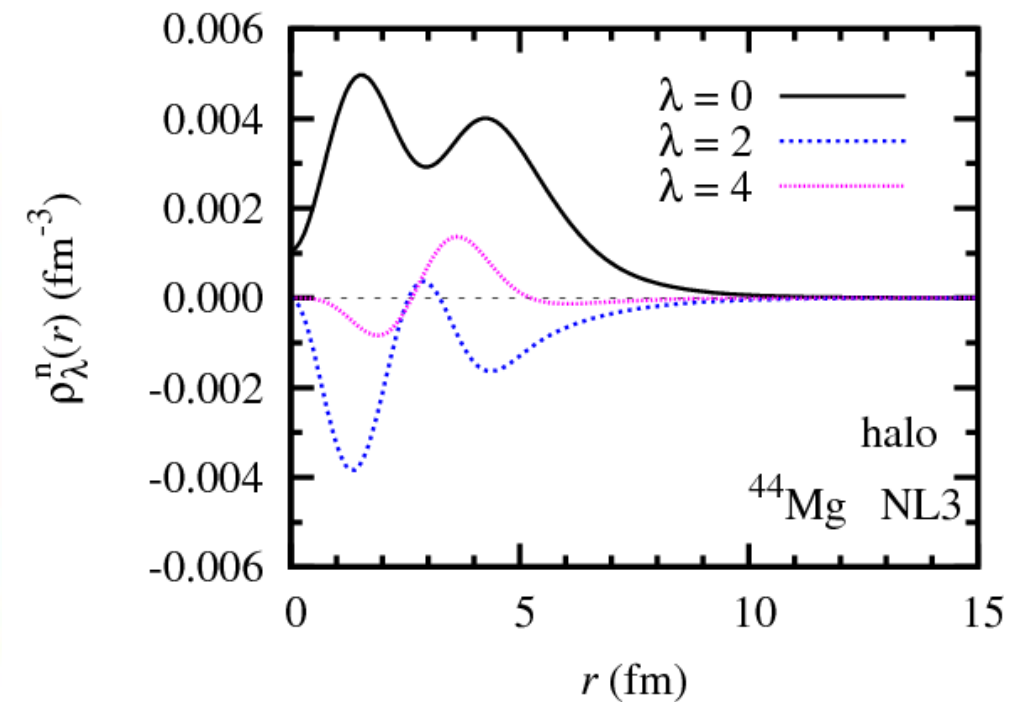
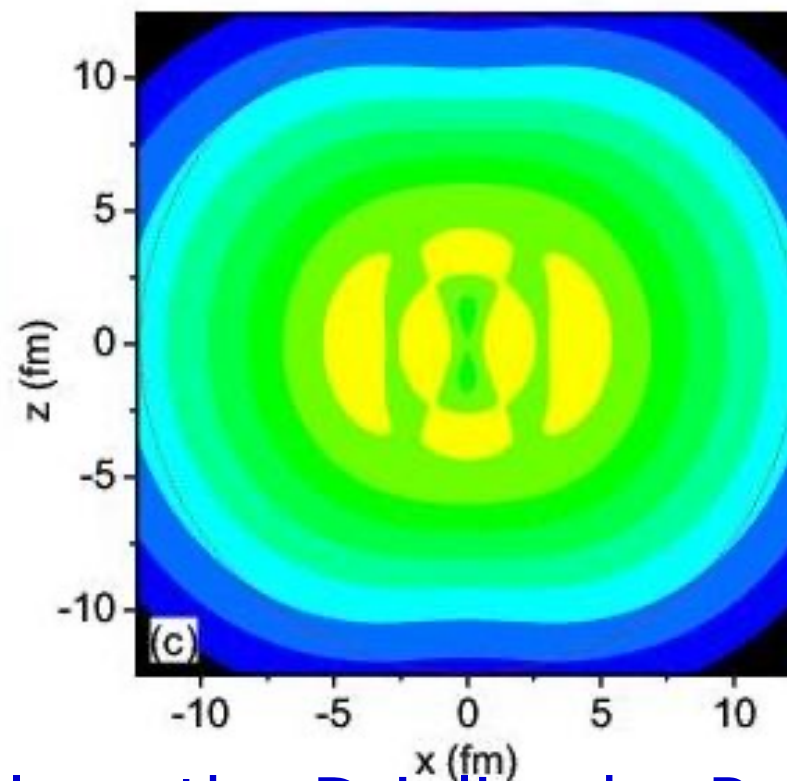
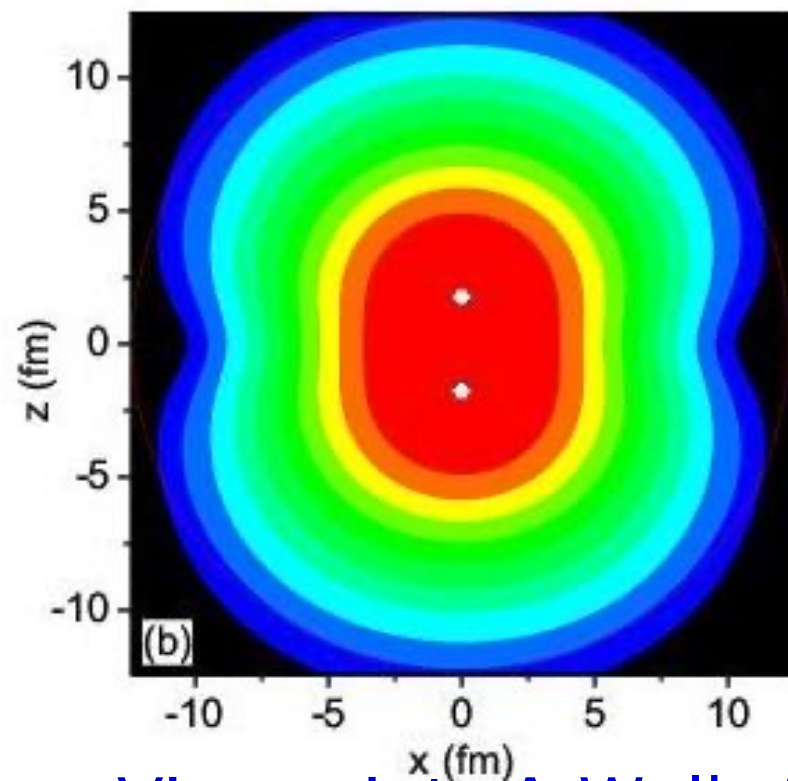
Prolate core & oblate halo

Zhou, Meng, Ring & Zhao, Phys. Rev. C 82, 011301 (2010)



❖ Prolate core, but slightly oblate halo with sizable hexadecapole component !

❖ Decoupling of deformation between core & halo



Viewpoint: A Walk Along the Dripline by Paul Cottle and Kirby Kemper

<http://link.aps.org/doi/10.1103/Physics.5.49>

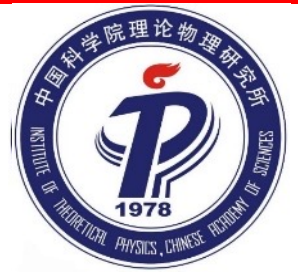
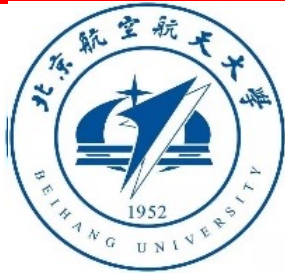


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DRHBc mass table collaboration

PC-PK1 + DRHBc

- I. Even-even nuclei
- II. Even Z-Odd N nuclei
- III. Odd-Z nuclei





Deformed relativistic Hartree-Bogoliubov theory in continuum with a point-coupling functional: Examples of even-even Nd isotopes

Kaiyuan Zhang (张开元) *et al.* (DRHBc Mass Table Collaboration)
Phys. Rev. C **102**, 024314 – Published 12 August 2020



PHYSICAL REVIEW C **102**, 024314 (2020)

Article

Deformed relativistic Hartree-Bogoliubov theory in continuum with a point-coupling functional: Examples of even-even Nd isotopes

Kaiyuan Zhang (张开元),¹ Myung-Ki Cheoun,² Yong-Beom Choi,³ Pooi Seong Chong,⁴ Jianmin Dong (董建敏),^{5,6} Lisheng Geng (耿立升),⁷ Eunja Ha,² Xiaotao He (贺晓涛),⁸ Chan Heo,⁴ Meng Chit Ho,⁴ Eun Jin In,⁹ Seonghyun Kim,² Youngman Kim,¹⁰ Chang-Hwan Lee,³ Jenny Lee,⁴ Zhipan Li (李志攀),¹¹ Tianpeng Luo (骆天鹏),¹ Jie Meng (孟杰) ^{1,*} Myeong-Hwan Mun,¹² Zhongming Niu (牛中明),^{13,14} Cong Pan (潘琮),¹ Panagiota Papakonstantinou,¹⁵ Xinle Shang (尚新乐),^{5,6} Caiwan Shen (沈彩万),¹⁶ Guofang Shen (申国防),⁷ Wei Sun (孙玮),¹¹ Xiang-Xiang Sun (孙向向),^{17,18} Chi Kin Tam,⁴ Thaivayongnou,⁷ Chen Wang (王晨),⁸ Sau Hei Wong,⁴ Xuewei Xia (夏学伟),¹⁹ Yijun Yan (晏一珺),^{5,6} Ryan Wai-Yen Yeung,⁴ To Chung Yiu,⁴ Shuangquan Zhang (张双全),¹ Wei Zhang (张炜),²⁰ and Shan-Gui Zhou (周善贵)^{17,18,21,22}
(DRHBc Mass Table Collaboration)

¹State Key Laboratory of Nuclear Physics and Technology, School of Physics, Peking University, Beijing 100871, China

²Department of Physics and Origin of Matter and Evolution of Galaxy (OMEG) Institute, Soongsil University, Seoul 156-743, Korea

³Department of Physics, Pusan National University, Busan 46241, Korea

⁴Department of Physics, The University of Hong Kong, Pokfulam 999077, Hong Kong

⁵Institute of Modern Physics, Chinese Academy of Sciences, Lanzhou 730000, China

⁶School of Physics, University of Chinese Academy of Sciences, Beijing 100049, China



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PHYSICAL REVIEW C 106, 014316 (2022)

Deformed relativistic
with a point-coupling

Cong Pan (潘琮) et al. (DRHBc M
Phys. Rev. C 106, 014316 – Publi

Article

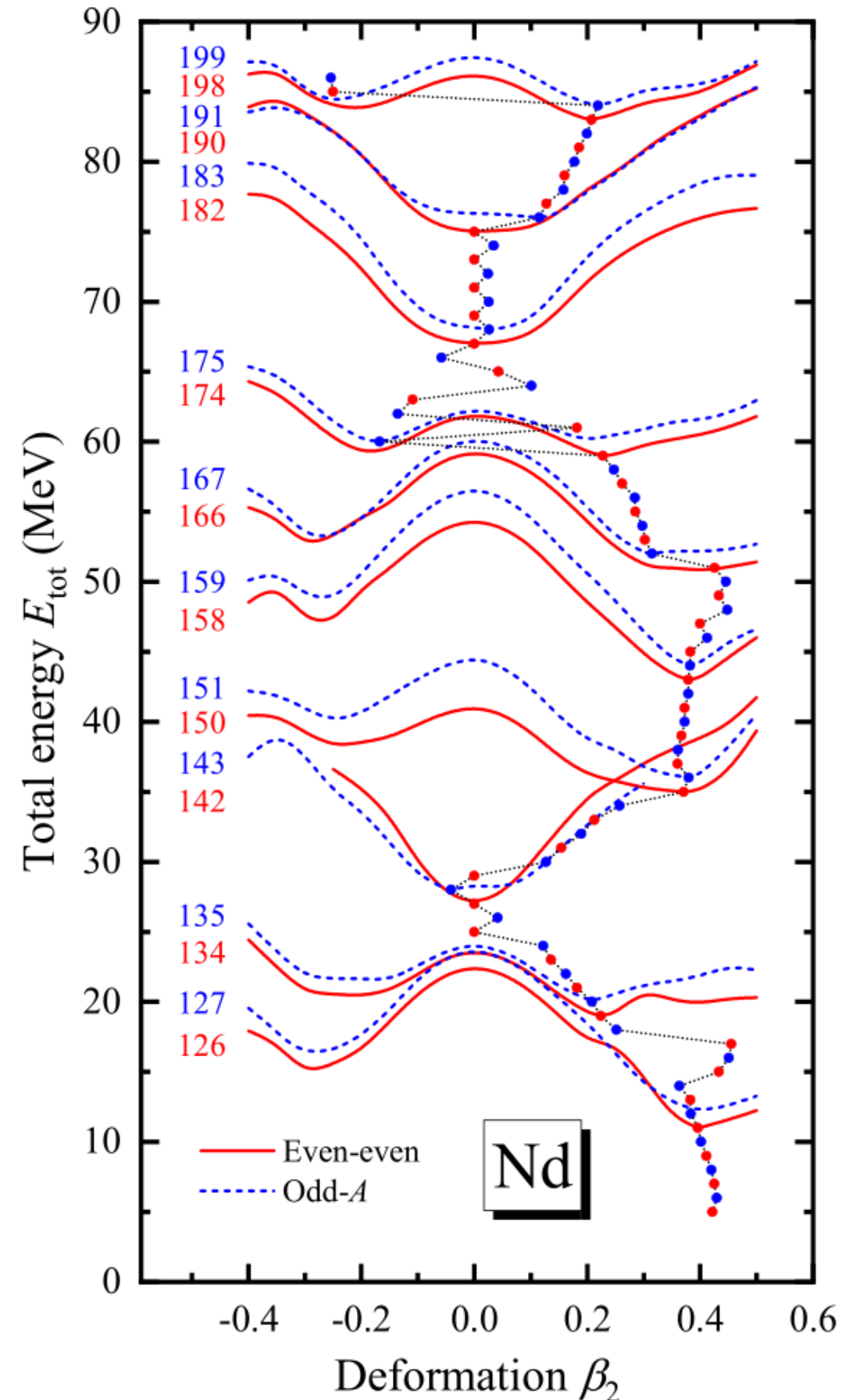
Deformed relativistic Hartree-Bogoliubov theory in continuum with a point-coupling functional. II. Examples of odd Nd isotopes

Cong Pan (潘琮),1 Myung-Ki Cheoun,2 Yong-Beom Choi,3 Jianmin Dong (董建敏),4,5 Xiaokai Du (杜晓凯),1
Xiao-Hua Fan (范小华),6 Wei Gao (高威),7 Lisheng Geng (耿立升),8,7 Eunja Ha,9 Xiao-Tao He (贺晓涛),10
Jinke Huang (黄靳苛),7 Kun Huang (黄坤),10 Seonghyun Kim,2 Youngman Kim,11 Chang-Hwan Lee,3 Jenny Lee,12
Zhipan Li (李志攀),6 Zhi-Rui Liu (刘治瑞),10 Yiming Ma (马艺铭),13 Jie Meng (孟杰),1,* Myeong-Hwan Mun,2,14
Zhongming Niu (牛中明),15 Panagiota Papakonstantinou,11 Xinle Shang (尚新乐),4,5 Caiwan Shen (沈彩万),16
Guofang Shen (申国防),8 Wei Sun (孙玮),6 Xiang-Xiang Sun (孙向向),17,18 Jiawei Wu (吴佳威),10 Xinhui Wu (吴鑫辉),1
Xuewei Xia (夏学伟),19 Yijun Yan (晏一珺),4,5 To Chung Yiu,12 Kaiyuan Zhang (张开元),1,20 Shuangquan Zhang (张双全),1
Wei Zhang (张炜),7 Xiaoyan Zhang (张晓燕),15 Qiang Zhao (赵强),21,1 Ruyou Zheng (郑茹尤),8
and Shan-Gui Zhou (周善贵)18,22,23,24
(DRHBc Mass Table Collaboration)

1State Key Laboratory of Nuclear Physics and Technology, School of Physics, Peking University, Beijing 100871, China
2Department of Physics and Origin of Matter and Evolution of Galaxy Institute, Soongsil University, Seoul 156-743, Korea
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4Institute of Modern Physics, Chinese Academy of Sciences, Lanzhou 730000, China
5School of Physics, University of Chinese Academy of Sciences, Beijing 100049, China
6School of Physical Science and Technology, Southwest University, Chongqing 400715, China
7School of Physics and Microelectronics, Zhengzhou University, Zhengzhou 450001, China



- ✓ Ground state for odd- A nuclei are double checked by different blocking.
- ✓ The PEC of odd- A nuclei are similar to their even-even neighbors.
- ✓ Sudden change of β_2 corresponds to possible shape coexistence.





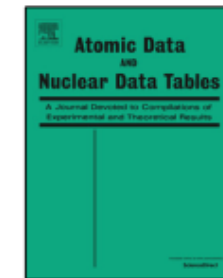
Atomic Data and Nuclear Data Tables 144 (2022) 101488



Contents lists available at ScienceDirect

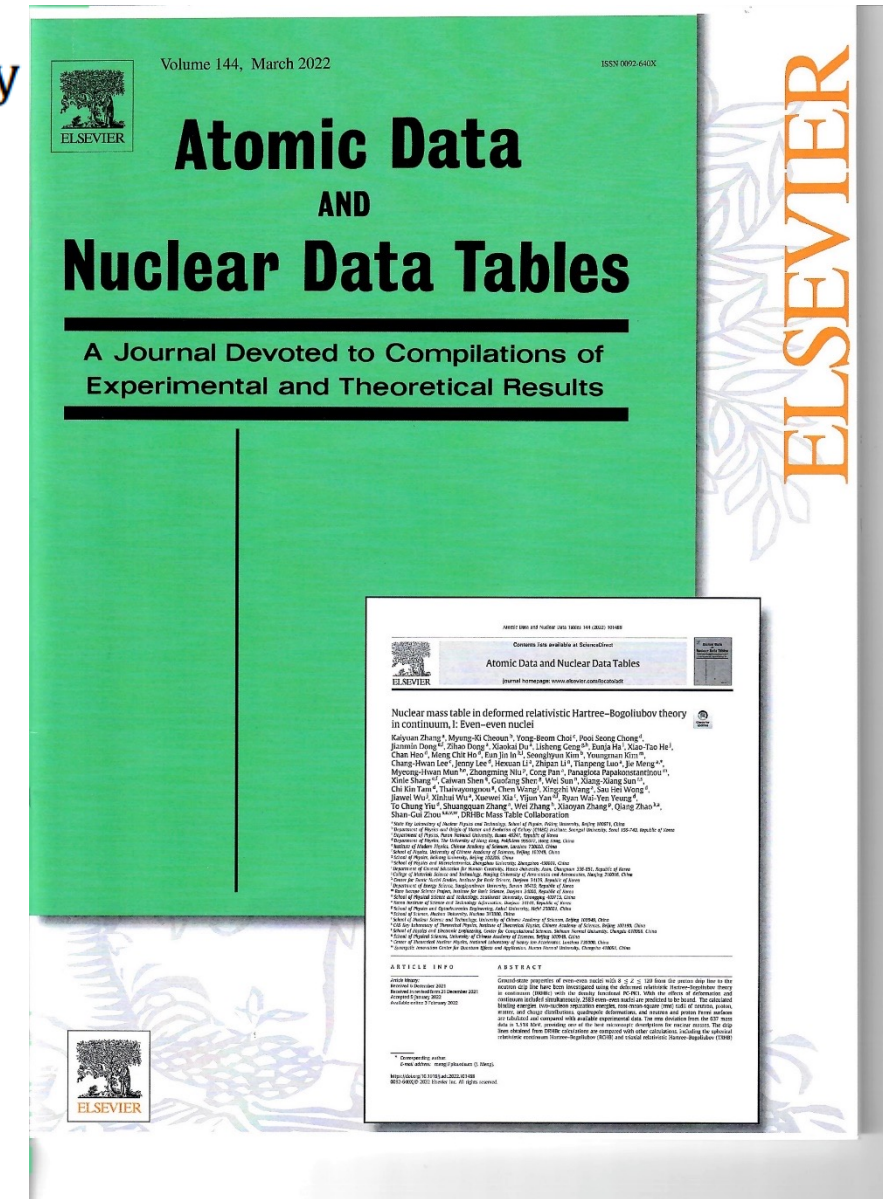
Atomic Data and Nuclear Data Tables

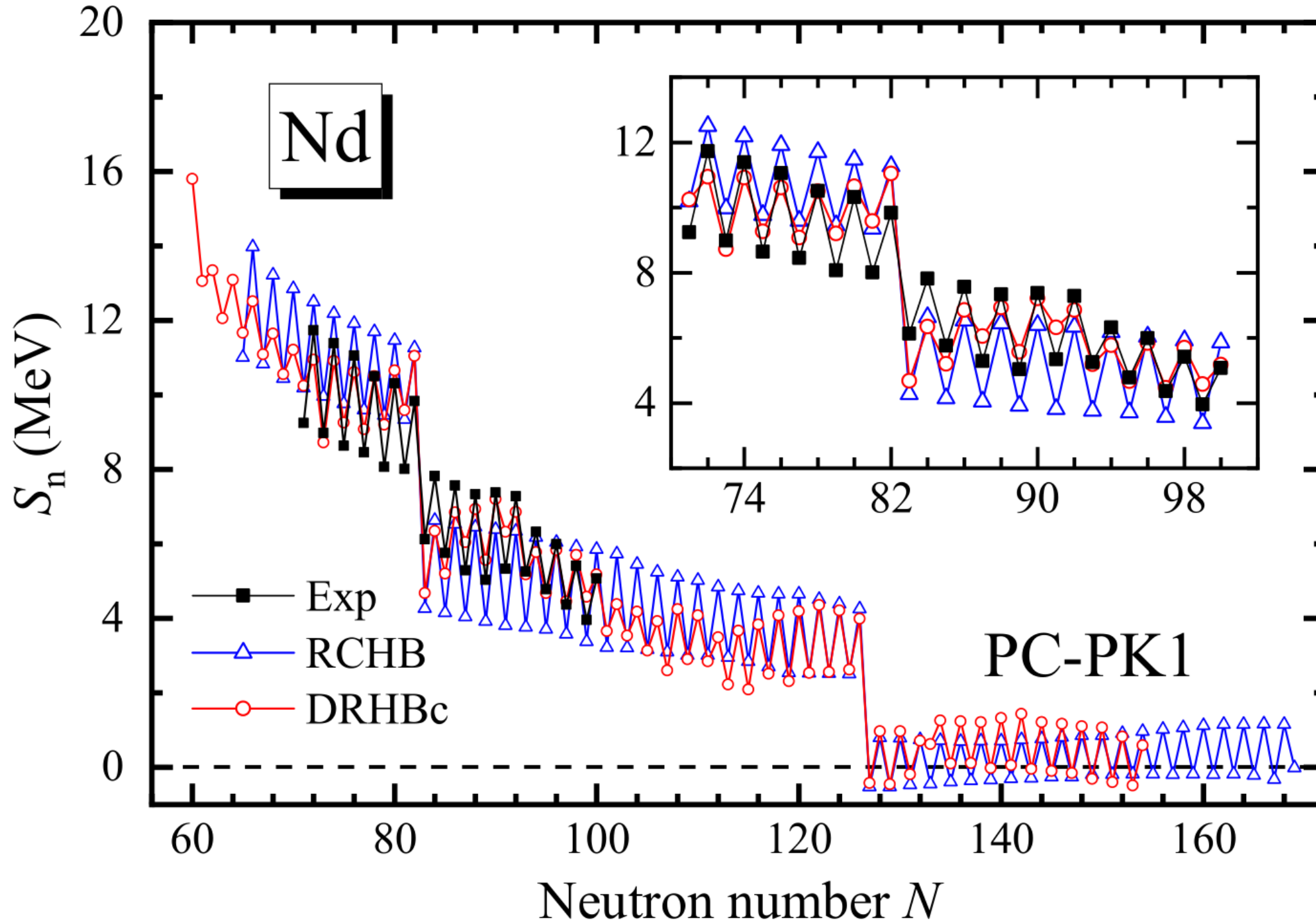
journal homepage: www.elsevier.com/locate/adt



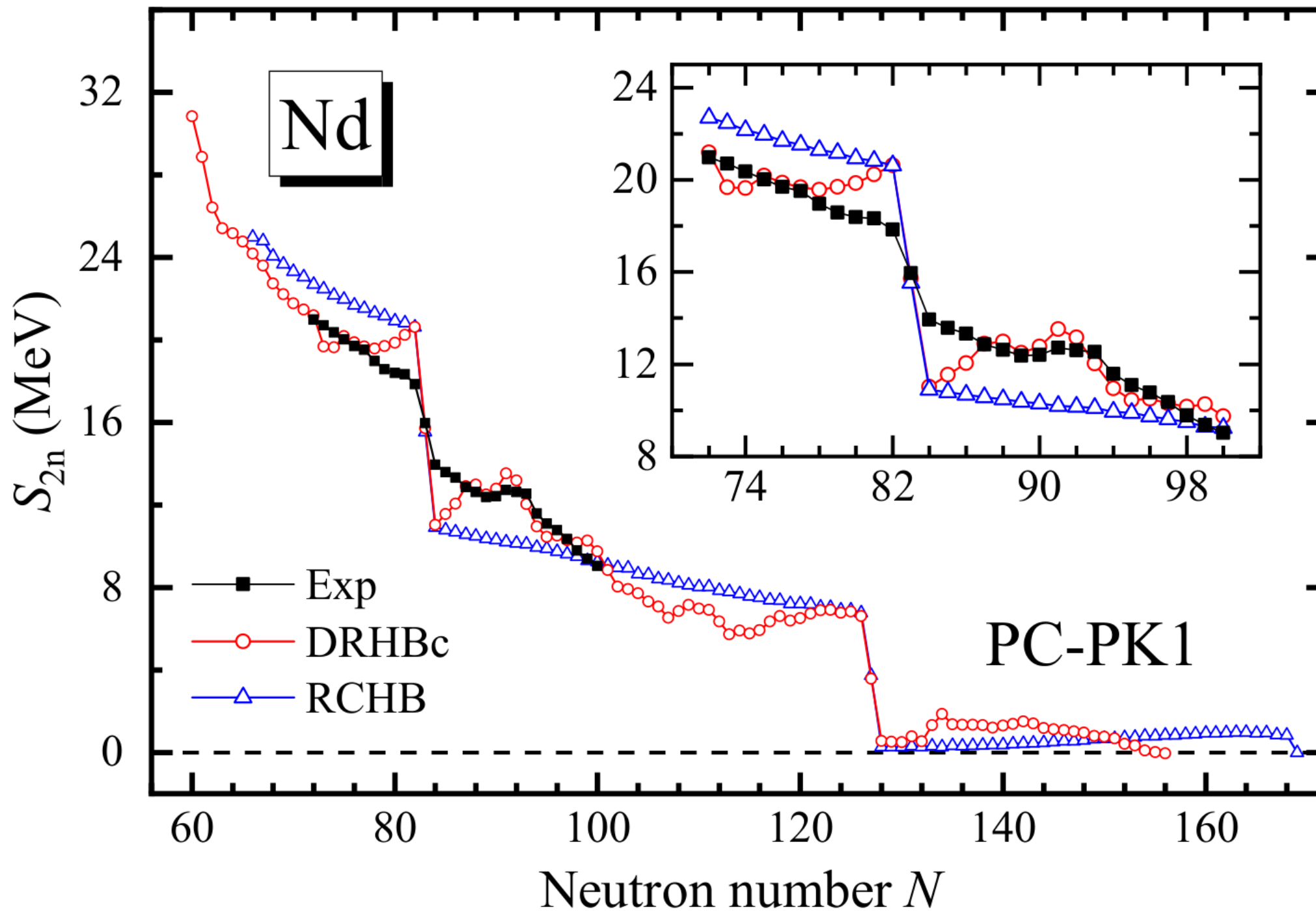
Nuclear mass table in deformed relativistic Hartree–Bogoliubov theory in continuum, I: Even–even nuclei

Kaiyuan Zhang^a, Myung-Ki Cheoun^b, Yong-Beom Choi^c, Pooi Seong Chong^d, Jianmin Dong^{e,f}, Zihao Dong^a, Xiaokai Du^a, Lisheng Geng^{g,h}, Eunja Haⁱ, Xiao-Tao He^j, Chan Heo^d, Meng Chit Ho^d, Eun Jin In^{k,l}, Seonghyun Kim^b, Youngman Kim^m, Chang-Hwan Lee^c, Jenny Lee^d, Hexuan Li^a, Zhipan Liⁿ, Tianpeng Luo^a, Jie Meng^{a,*}, Myeong-Hwan Mun^{b,o}, Zhongming Niu^p, Cong Pan^a, Panagiota Papakonstantinou^m, Xinle Shang^{e,f}, Caiwan Shen^q, Guofang Shen^g, Wei Sunⁿ, Xiang-Xiang Sun^{r,s}, Chi Kin Tam^d, Thaivayongnou^g, Chen Wang^j, Xingzhi Wang^a, Sau Hei Wong^d, Jiawei Wu^j, Xinhui Wu^a, Xuewei Xia^t, Yijun Yan^{e,f}, Ryan Wai-Yen Yeung^d, To Chung Yiu^d, Shuangquan Zhang^a, Wei Zhang^h, Xiaoyan Zhang^p, Qiang Zhao^{k,a}, Shan-Gui Zhou^{s,u,v,w}, DRHBc Mass Table Collaboration





- ✓ Rms deviations: **DRHBc: 0.74 MeV** **RCHB: 1.10 MeV**
- ✓ One-neutron drip line: **DRHBc: $N = 126$** **RCHB: $N = 126$**

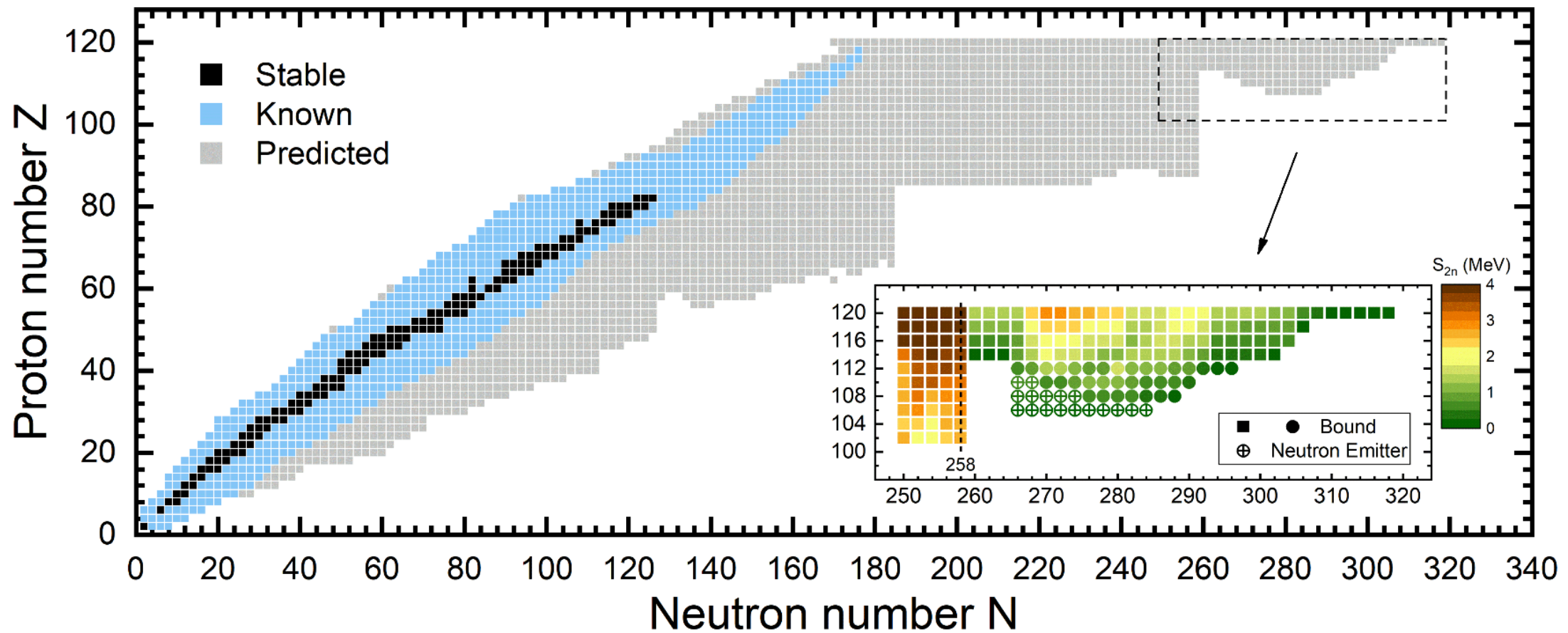


- ✓ Rms deviations: DRHBc: 1.10 MeV RCHB: 2.04 MeV
- ✓ Two-neutron drip line: DRHBc: $N = 154$ RCHB: $N = 168$

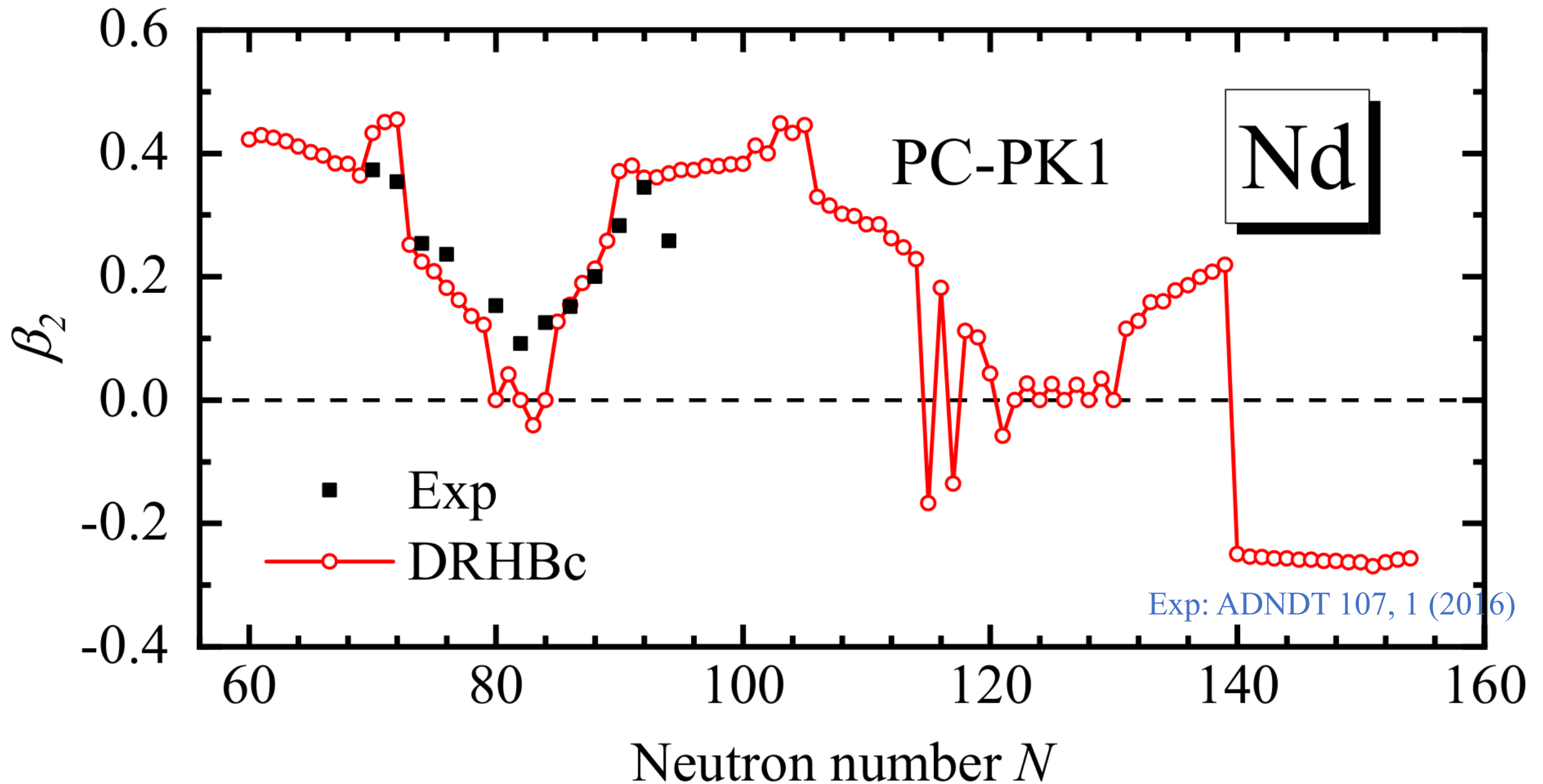


➤ PC-PK1 + DRHBc, 2583 even-even nuclei with $8 \leq Z \leq 120$, **first** mass table including both **deformation** and **continuum**, $\sigma = 1.5$ MeV

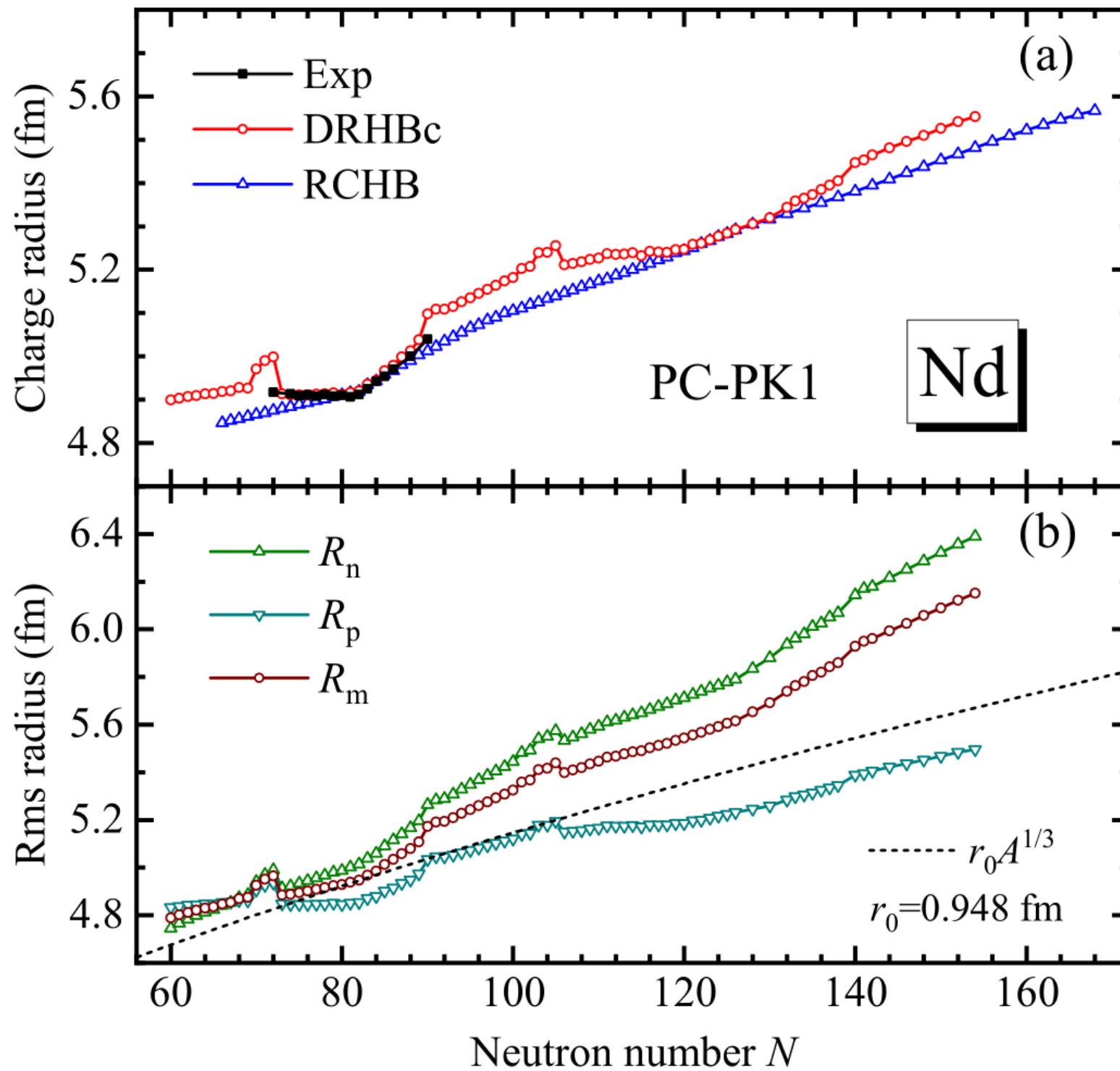
K. Y. Zhang *et al.* (DRHBc Collaboration), Nuclear mass table in deformed relativistic Hartree-Bogoliubov theory in continuum, I: Even-even nuclei, **At. Data Nucl. Data Tables** 144, 101488 (2022)



✓ DRHBc mass table for even-even nuclei has been constructed'



- ✓ Calculation for even-even nuclei reproduce with the data and the odd- A nuclei follow the trend.

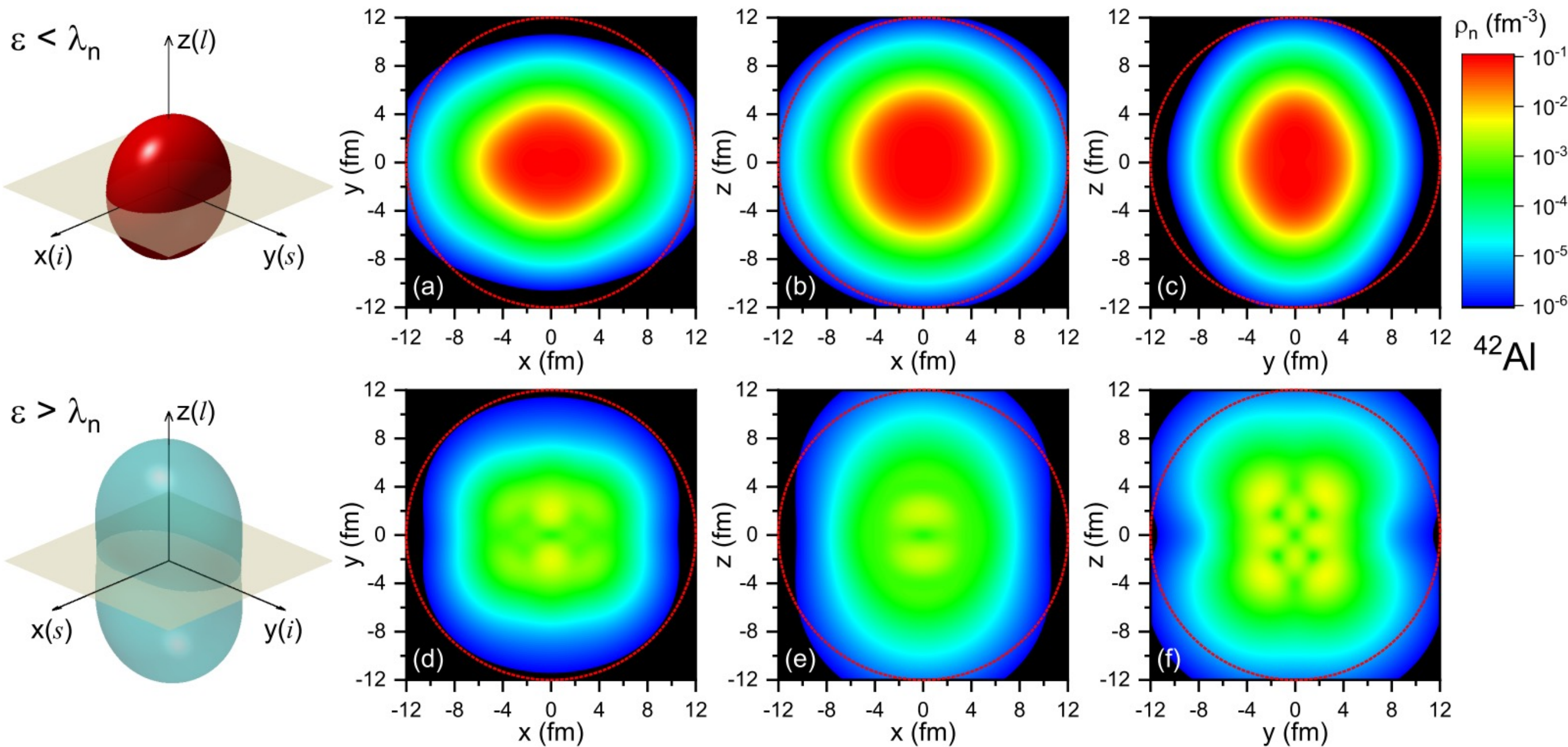


✓ DRHBc theory reproduced the observed rms radii well



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Halo in triaxial nucleus ^{42}Al



^{42}Al

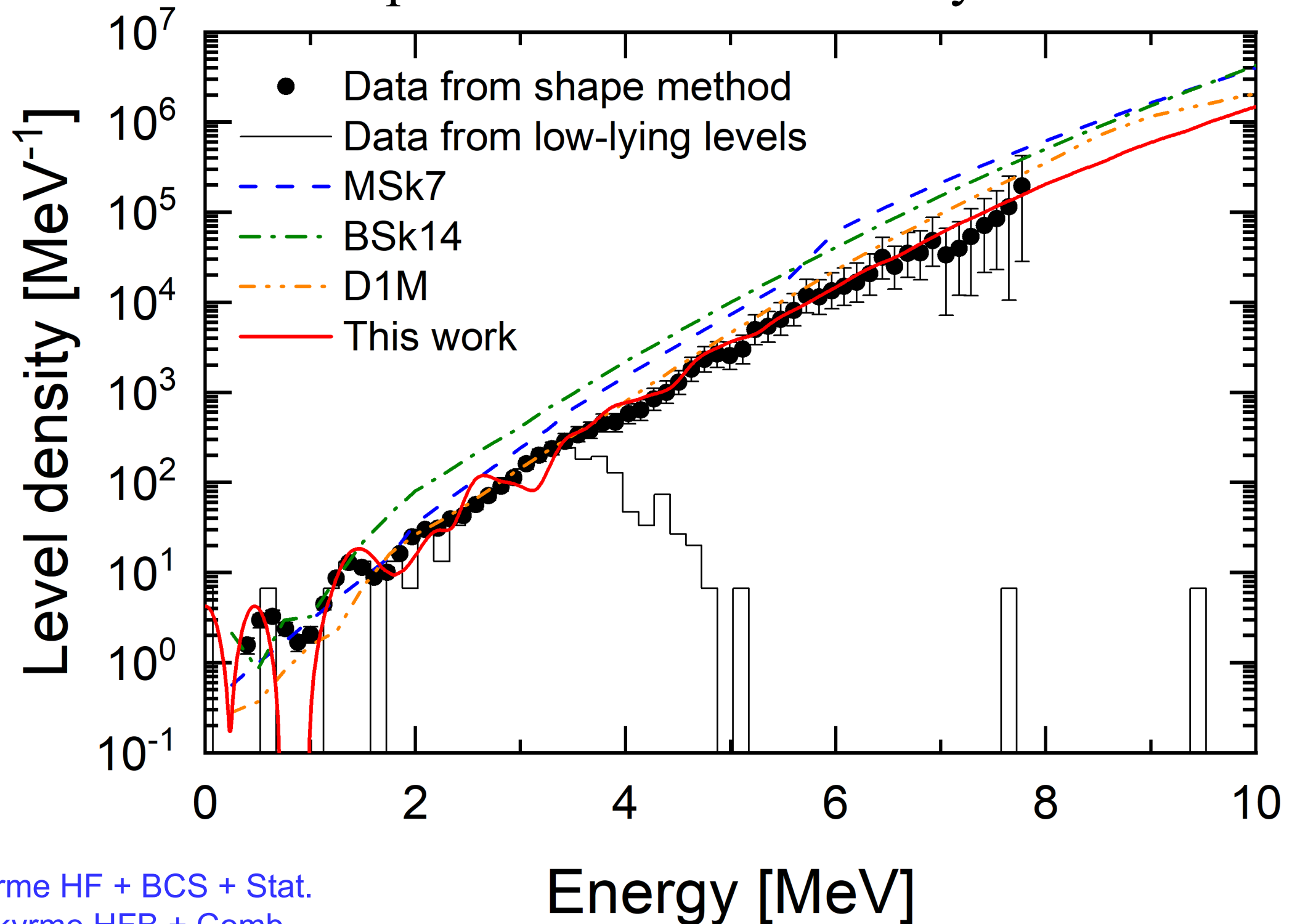
✓ Core: $r = 3.85$ fm, $\beta = 0.38$, $\gamma = 50^\circ$, $z > x > y$

✓ Halo: $r = 5.26$ fm, $\beta = 0.79$, $\gamma = -23^\circ$, $z > y > x$



Nuclear level density

CDFT + combination + Strutinski well
reproduce the level density in ^{112}Cd



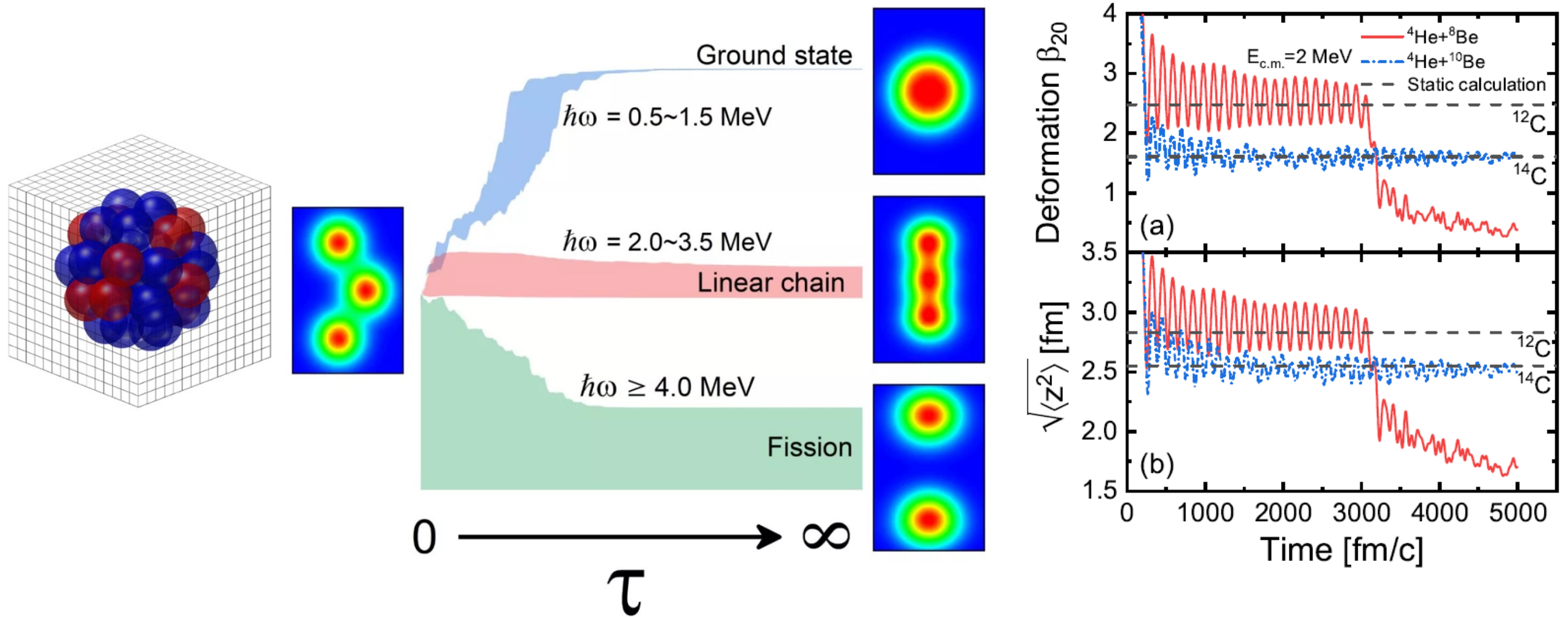
MSk7: Skyrme HF + BCS + Stat.
BSk14: Skyrme HFB + Comb.
D1M: Gogny THFB + Comb.



(Time-depend) CDFT in 3D lattice

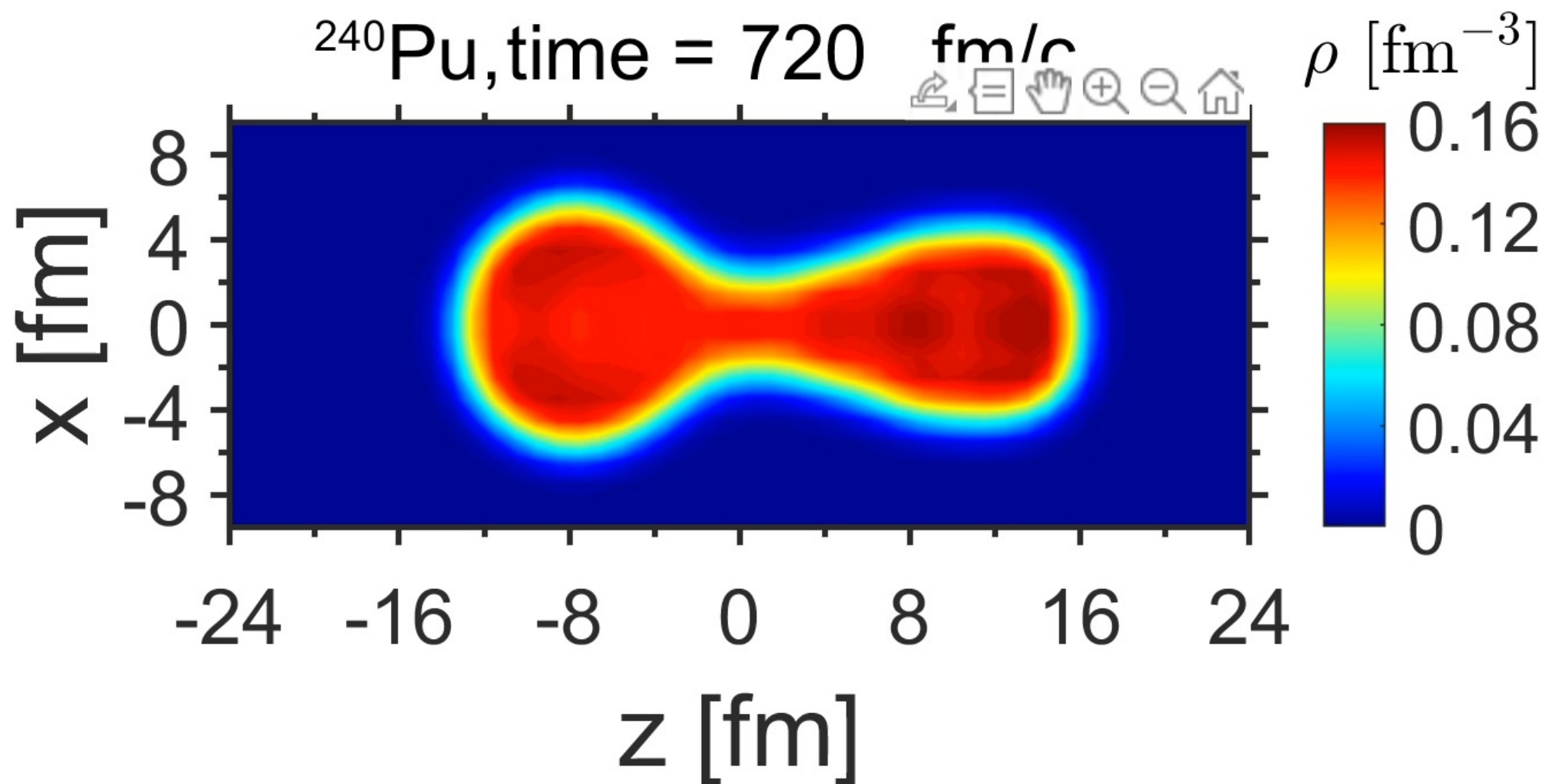
EoM on 3D lattice with the inverse Hamiltonian and Fourier spectral methods.

Linear 3α clusters chain structure for ^{12}C against the bending and fission in **cranking CDFT** and **TD CDFT** on a 3D lattice



Ren, Zhang, Zhao, Itagaki, Maruhn, Meng, SCPMA 62, 112062 (2019)
 Ren, Zhao, Meng, Physics Letters B 801 (2020) 135194

^{240}Pu : Nuclear density



Ren, Vretenar, Nikšić, PWZ, Zhao, Meng, PRL 128, 172501 (2022)



PHYSICAL REVIEW LETTERS **128**, 172501 (2022)

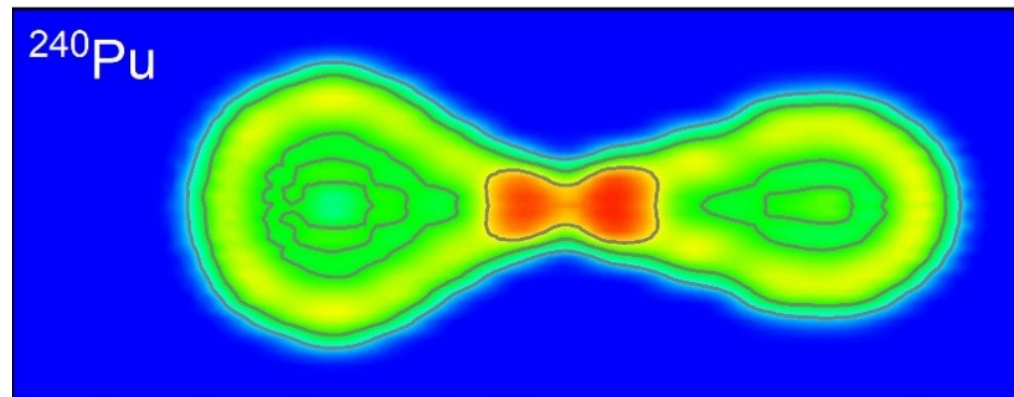
Dynamical Synthesis of ^4He in the Scission Phase of Nuclear Fission

Z. X. Ren¹, D. Vretenar^{2,1,*}, T. Nikšić^{2,1}, P. W. Zhao^{1,†}, J. Zhao³, and J. Meng^{1,‡}

¹State Key Laboratory of Nuclear Physics and Technology, School of Physics, Peking University, Beijing 100871, China

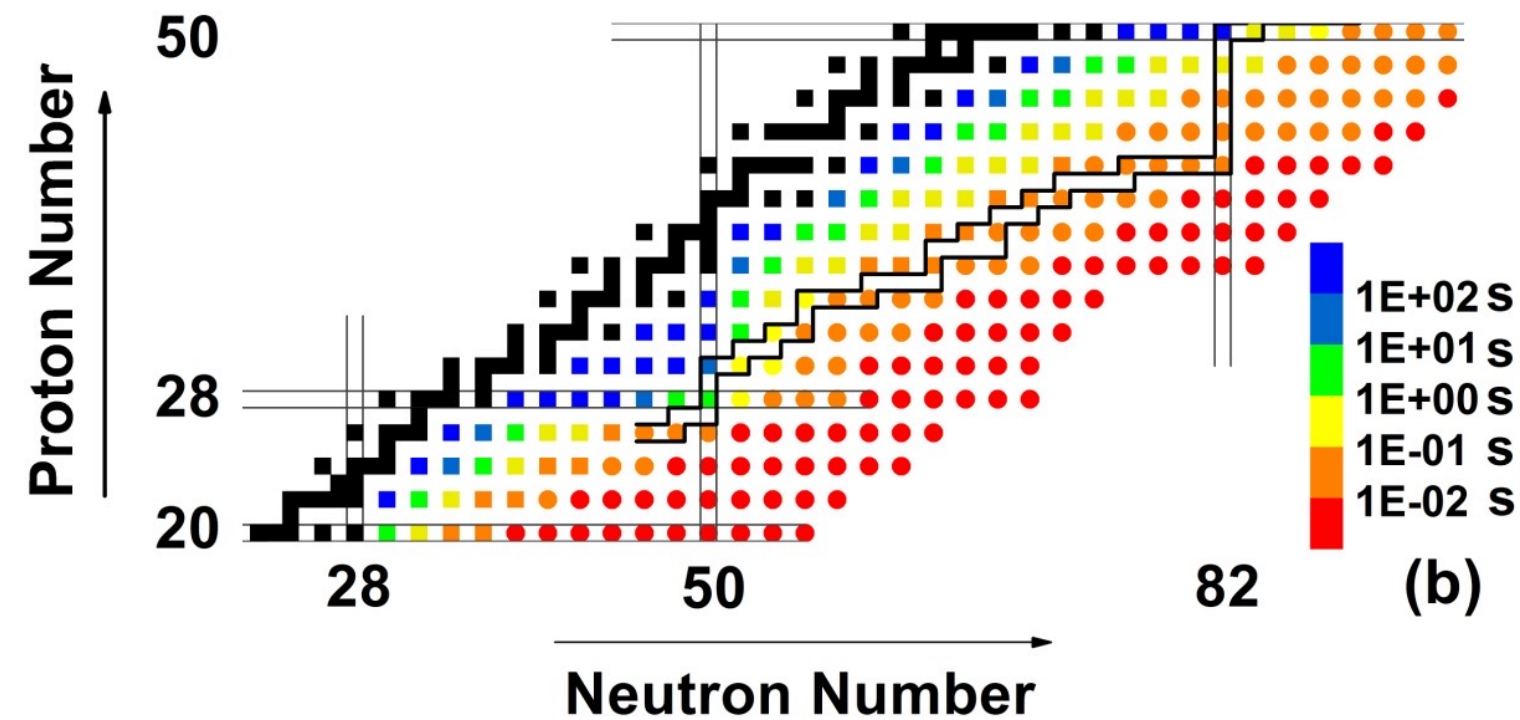
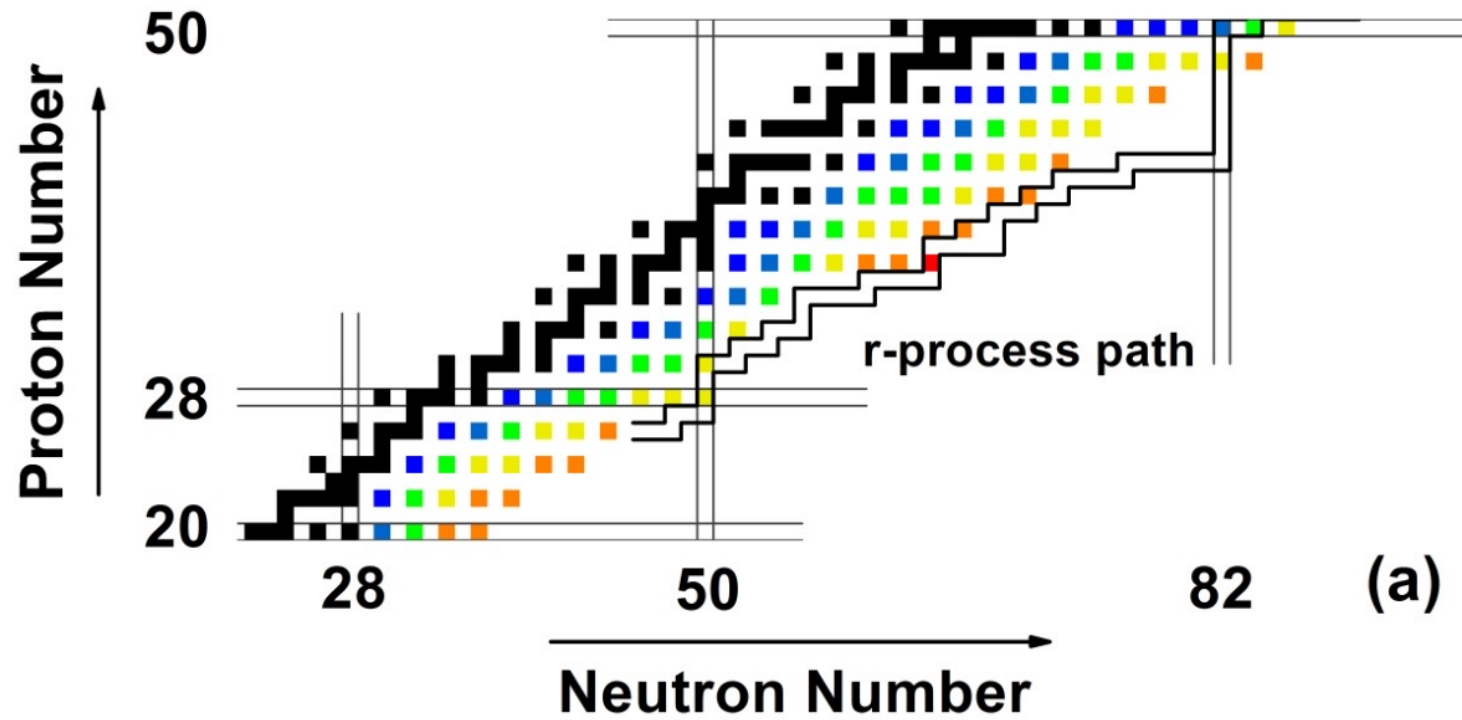
²Physics Department, Faculty of Science, University of Zagreb, 10000 Zagreb, Croatia

³Center for Circuits and Systems, Peng Cheng Laboratory, Shenzhen 518055, China



Localization functions in the x-z coordinate near the scission

- Z. X. Ren, J. Zhao, D. Vretenar, T. Nikšić, P. W. Zhao, and J. Meng, **Microscopic analysis of induced nuclear fission dynamics**, *Phys. Rev. C* **105**, 044313 (2022)
- Z. X. Ren, D. Vretenar, T. Nikšić, P. W. Zhao, J. Zhao, and J. Meng, **Dynamical synthesis of ^4He in the scission phase of nuclear fission**, *Phys. Rev. Lett.* **128**, 172501 (2022)



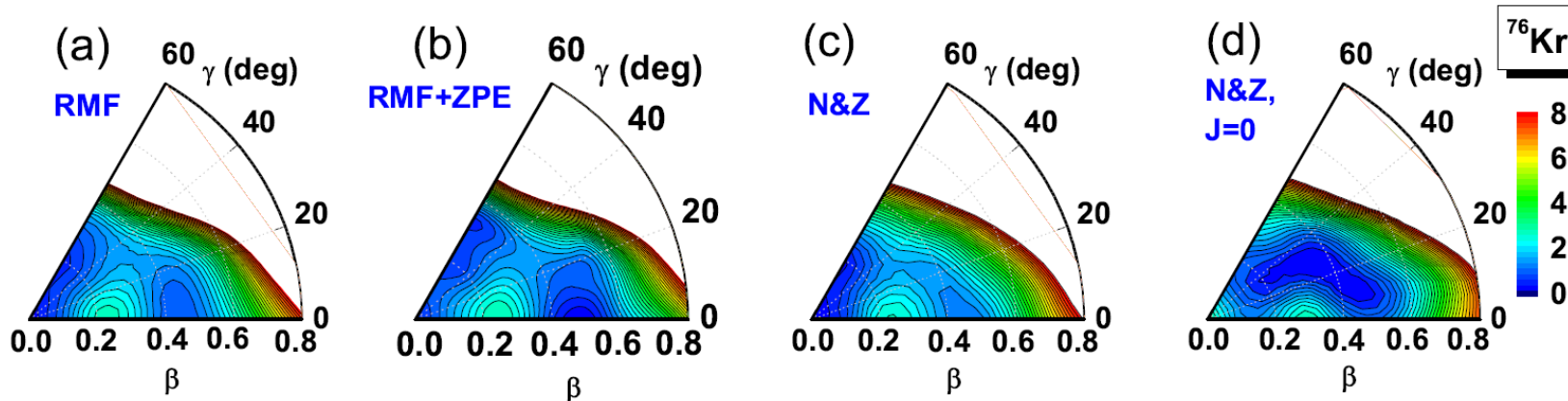
◆ Available data are well reproduced by including an isospin-dependent proton-neutron pairing interaction in the isoscalar channel of the RHFB+QRPA model.

$$V_{T=0}(1,2) = -V_0 \sum_{j=1}^2 g_j e^{-r_{12}^2/\mu_j^2} \hat{\Pi}_{S=1,T=0},$$

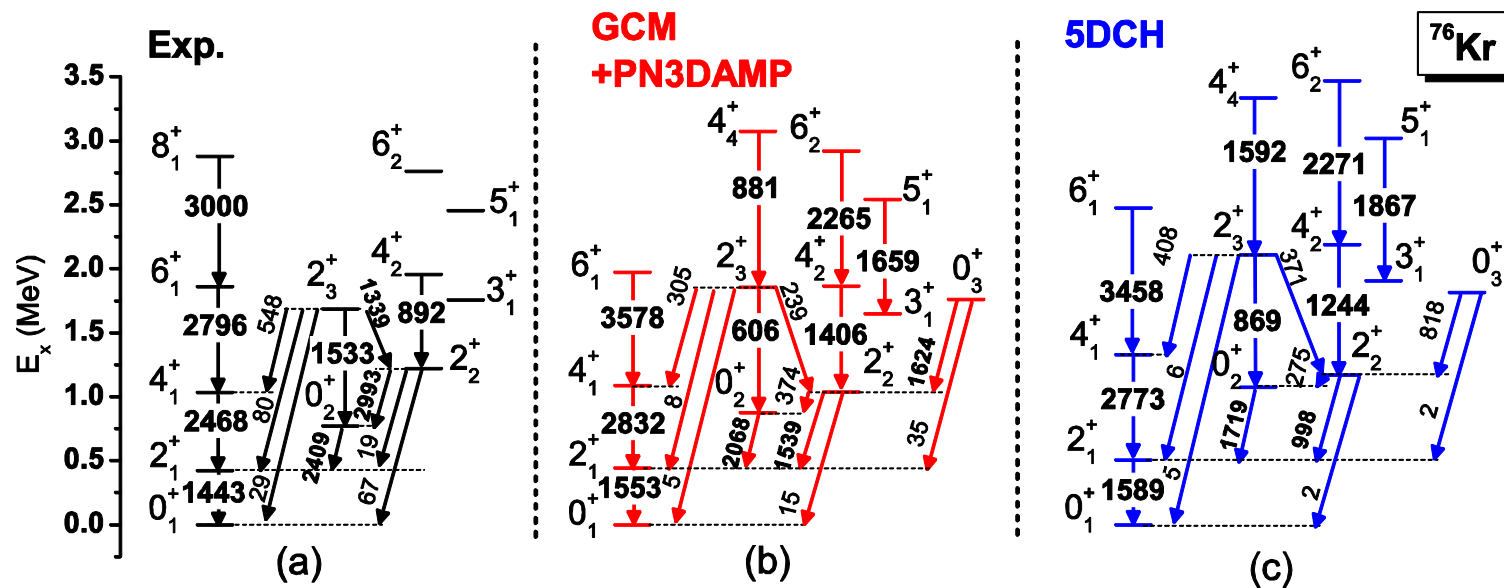
$$V_0 = V_1 + \frac{V_2}{1 + e^{a+b(N-Z)}},$$



7D GCM: two deformation parameters + projection 3DAM and 2PN



◆ The low-energy spectrum in ^{76}Kr are well reproduced after including triaxiality in the full microscopic GCM+ PN3DAMP calculation based on the CDFT using PC-PK1.



◆ This study answers the important question of dynamic correlations and triaxiality in shape-coexistence nucleus ^{76}Kr and provides the first benchmark for the EDF based collective Hamiltonian method.

Yao, Hagino, Li, Meng, Ring, Phys. Rev. C 89, 054306 (2014)

Benchmark for the collective Hamiltonian in five dimensions



- ✓ Origin of the heavy elements is one of the fundamental problems in modern science.
- ✓ Strategy to build Relativistic density functional based on QCD-spirited NN interaction and *ab initio* calculation is proposed.
- ✓ Predictive power of the functional PC-PK1 is shown for both nuclear ground and excited states.
- ✓ DRHBc mass table calculations are completed for even Z nuclei and will be started for odd Z nuclei .
- Experimental data are **reproduced well** with continuum and deformation effects. Interesting topics including the bound states beyond the neutron drip line, and the tensor force manifestations are discussed.



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**Thank you for your
attention!**



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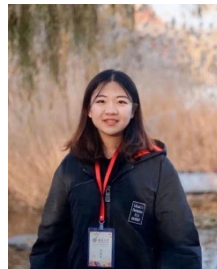
Students:



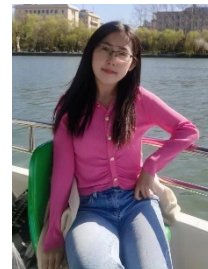
Yan Lyu



Cong Pan



Yanyu Chen



Yiping Wang



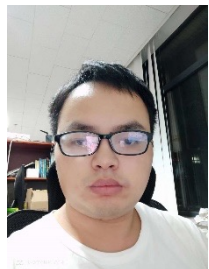
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Xiaokai Du



Fangfang Xu



Weijiang Zou



Xiaofei Jiang



Bo Li



Yilong Yang



Lingyi Dai



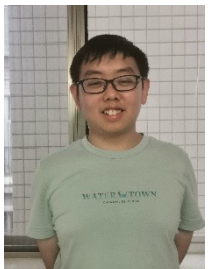
Teng Qu



Chang Zhou



Tianxing Huang



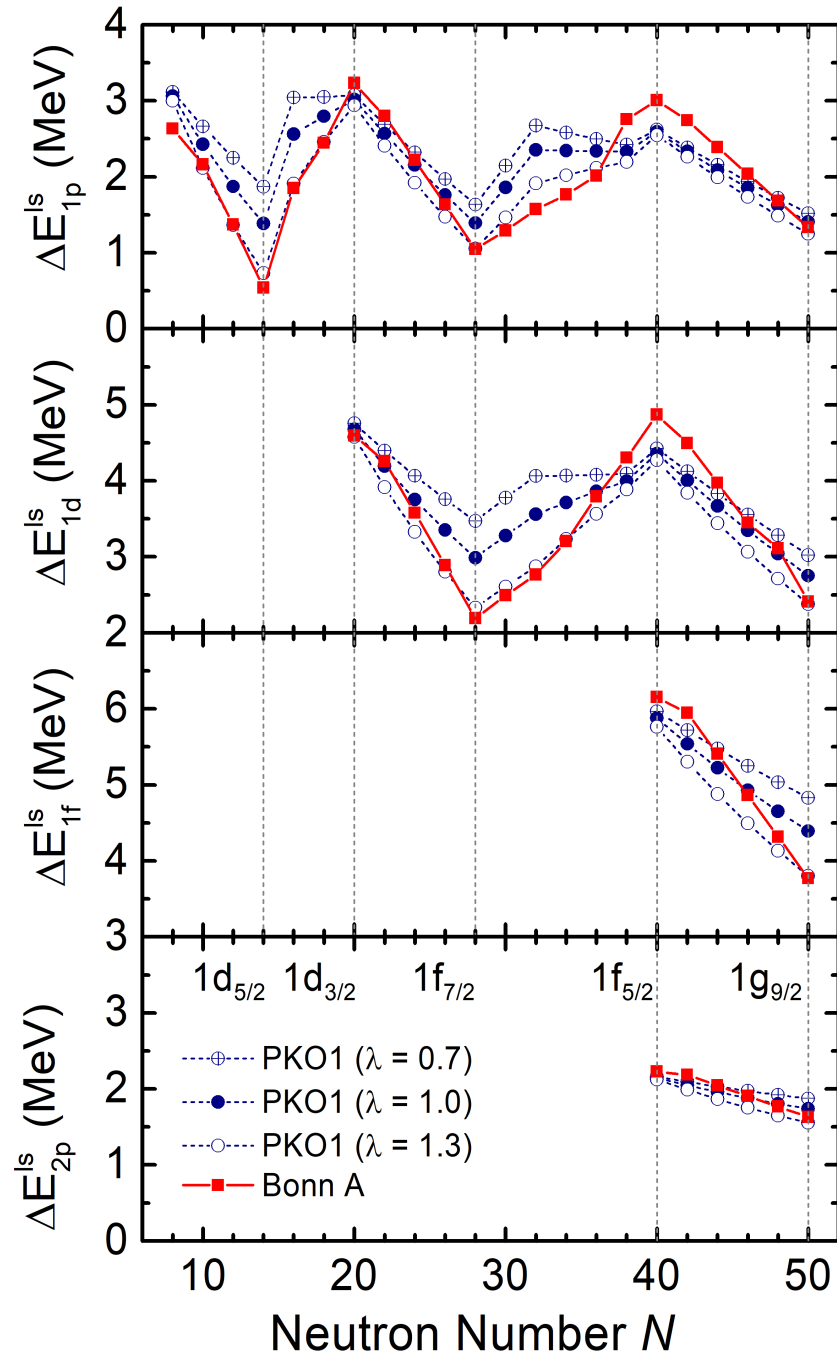
Peng Guo



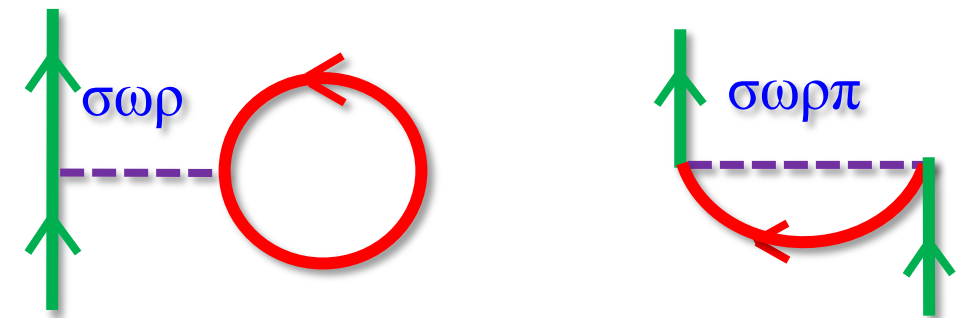
The origin of the heavy elements is one of the fundamental problems in modern science. To solve this problem, the knowledge of nuclear properties is essential. Before the new generation of nuclear facilities can provide the missing data, the reliable and accurate theoretical predictions are indispensable. In this presentation, approaches based on the relativistic density functional with continuum and deformation effects are introduced. Related physics applications are discussed, including masses and shapes of exotic nuclei, bound states beyond the neutron drip line, and the tensor force manifestations.



Tensor effects on spin-Orbit Splitting



- Neutron drop is a neutron system confined in an external field.
-
- A neutron drop provides also an ideal and simple system to investigate the effects of tensor forces.



Shi-Hang Shen, Hao-Zhao Liang, Jie Meng, Peter Ring, Shuang-Quan Zhang,

Effects of tensor forces in nuclear spin-orbit splittings from ab initio calculations.

Phys. Lett. B 778 (2018) 344–348

Relativistic Brueckner-Hartree-Fock theory for neutron drops

Phys. Rev. C 97, 054312 (2018)

❑ **RHF** shows similar pattern, mainly contributed by **π NN tensor interaction**.

❑ Neither RBHF nor CDFT includes **beyond-mean-field effects** ➔ **a fair comparison!**



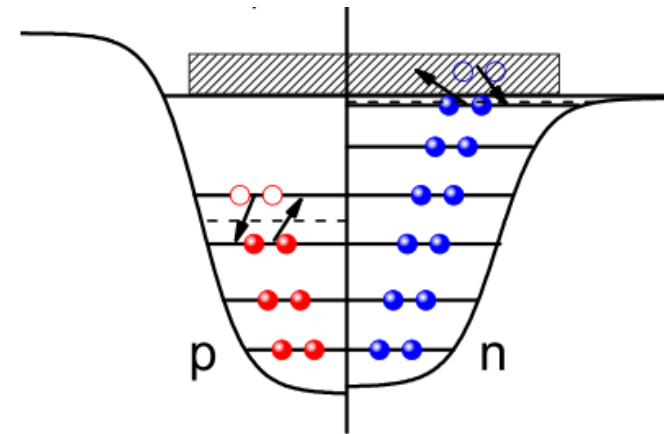
- ✓ Self-consistent description of the neutron halo in ^{11}Li is achieved by the relativistic continuum Hartree-Bogoliubov (RCHB) theory.

Meng and Ring, PRL 77, 3963 (1996)

- ✓ Pairing correlations and continuum effects are very important for the description of halos.

Meng and Ring, PRL 77, 3963 (1996)

Meng *et al.*, PPNP 57, 470 (2006)



- ✓ The RCHB theory also predicts giant halos in Zr isotopes.

Meng and Ring, PRL 80, 460 (1998)

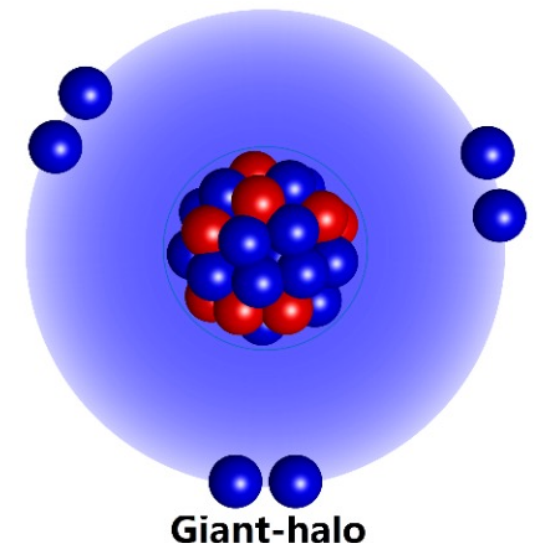
- ✓ Later studies support the prediction of giant halos in Zr and Ca isotopes.

Meng, Toki, Zeng, Zhang, and Zhou, PRC 65, 041302(R) (2002)

Sandulescu, Geng, and Hillhouse, PRC 68, 054323 (2003)

Terasaki, Zhang, Zhou, Meng, PRC 74, 054318 (2006)

Grasso, Yoshida, Sandulescu, and Van Giai, PRC 74, 064317 (2006)





- MDC-CDFT: all $\beta_{\lambda\mu}$ with even μ included
- Triaxial & octupole shapes both crucial around the outer barrier

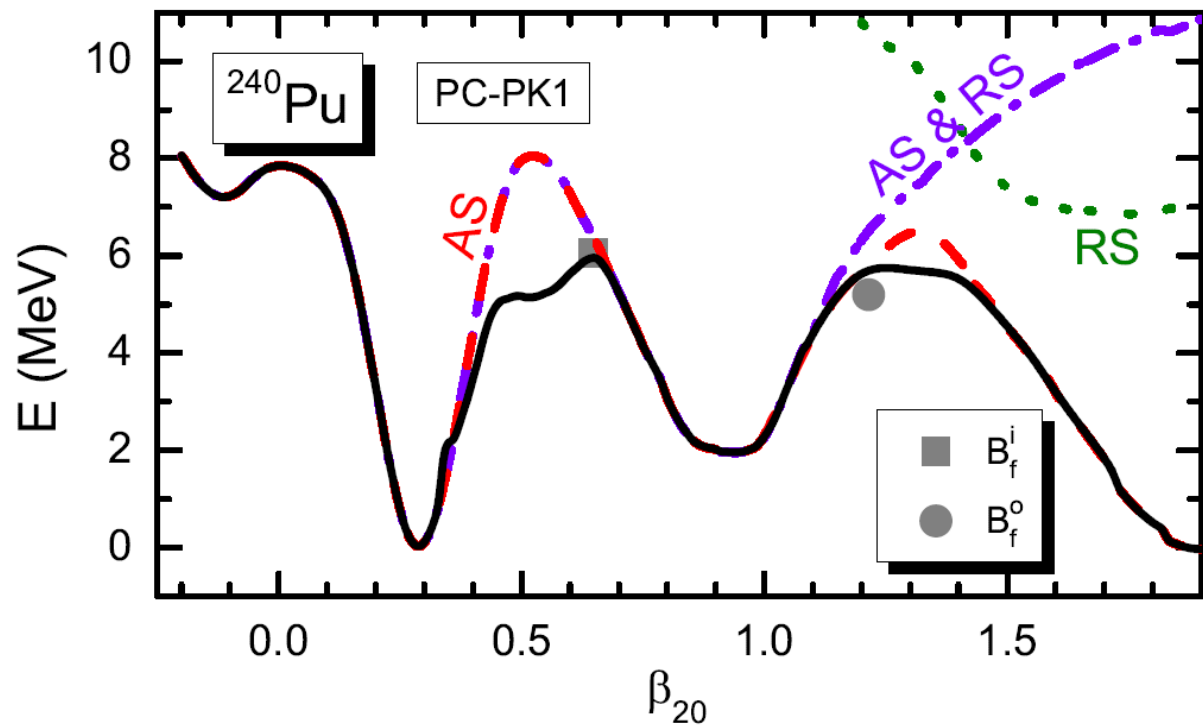


Figure: Potential energy curve of ^{240}Pu

Lu, Zhao, Zhou, PRC 85, 011301 (2012)

Zhao, Lu, Zhao, Zhou, PRC 86, 057304 (2012)

Lu, Zhao, Zhao, Zhou, PRC 89, 014323 (2014)

Zhao, Lu, Vretenar, Zhao, Zhou, arXiv:1404.5466 (2014)

Triaxial deformation only: Abusara, Afanasjev, Ring PRC 85, 024314 (2012)

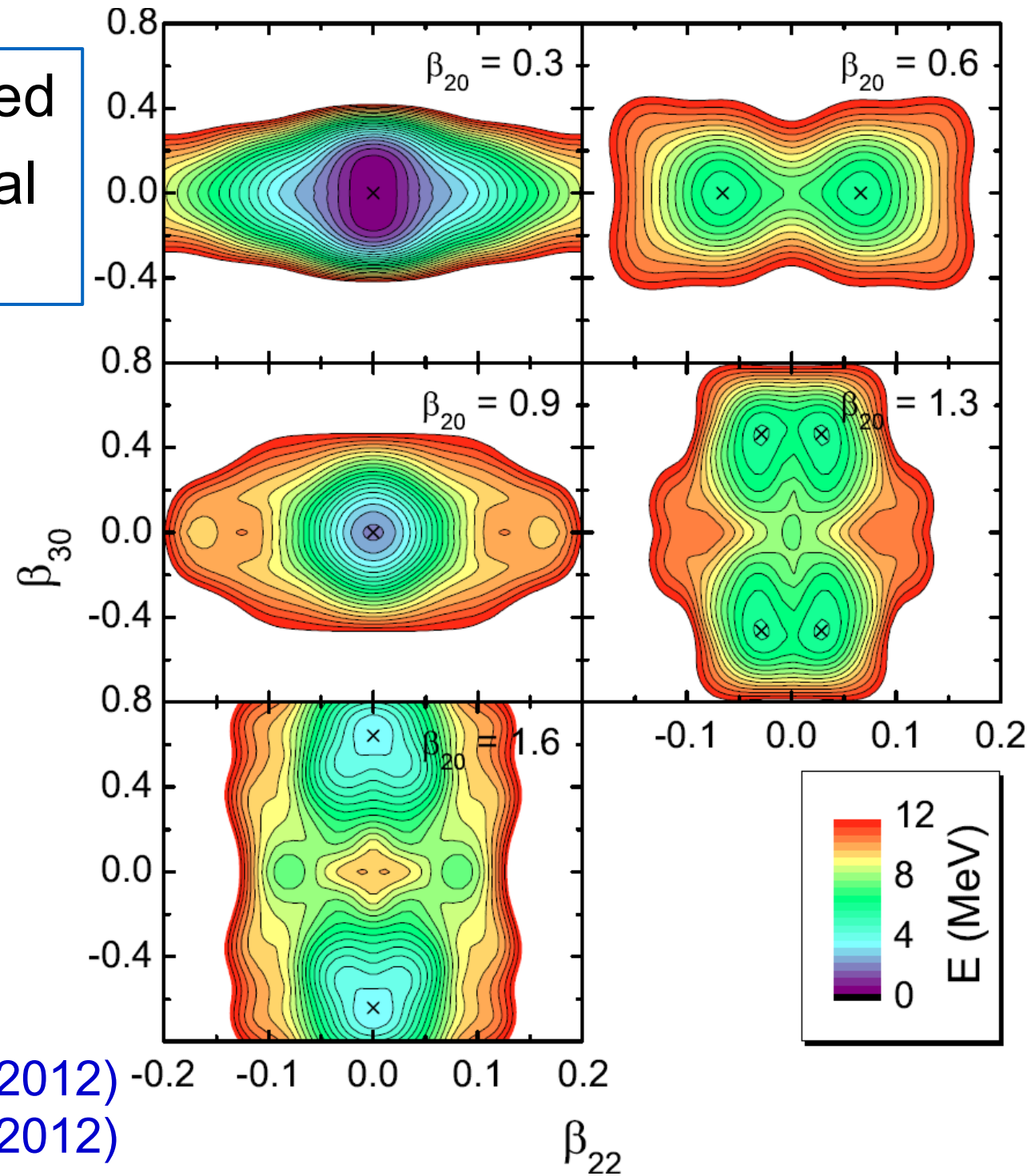
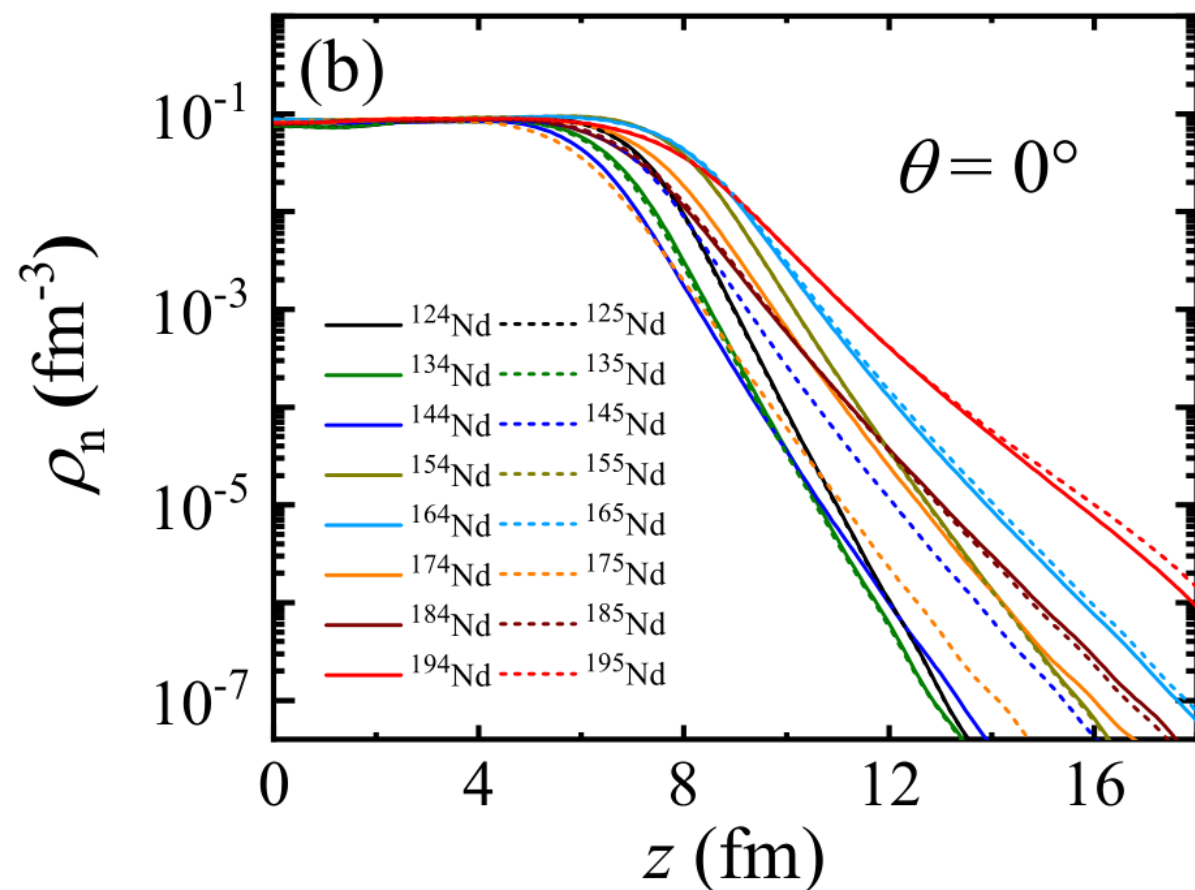
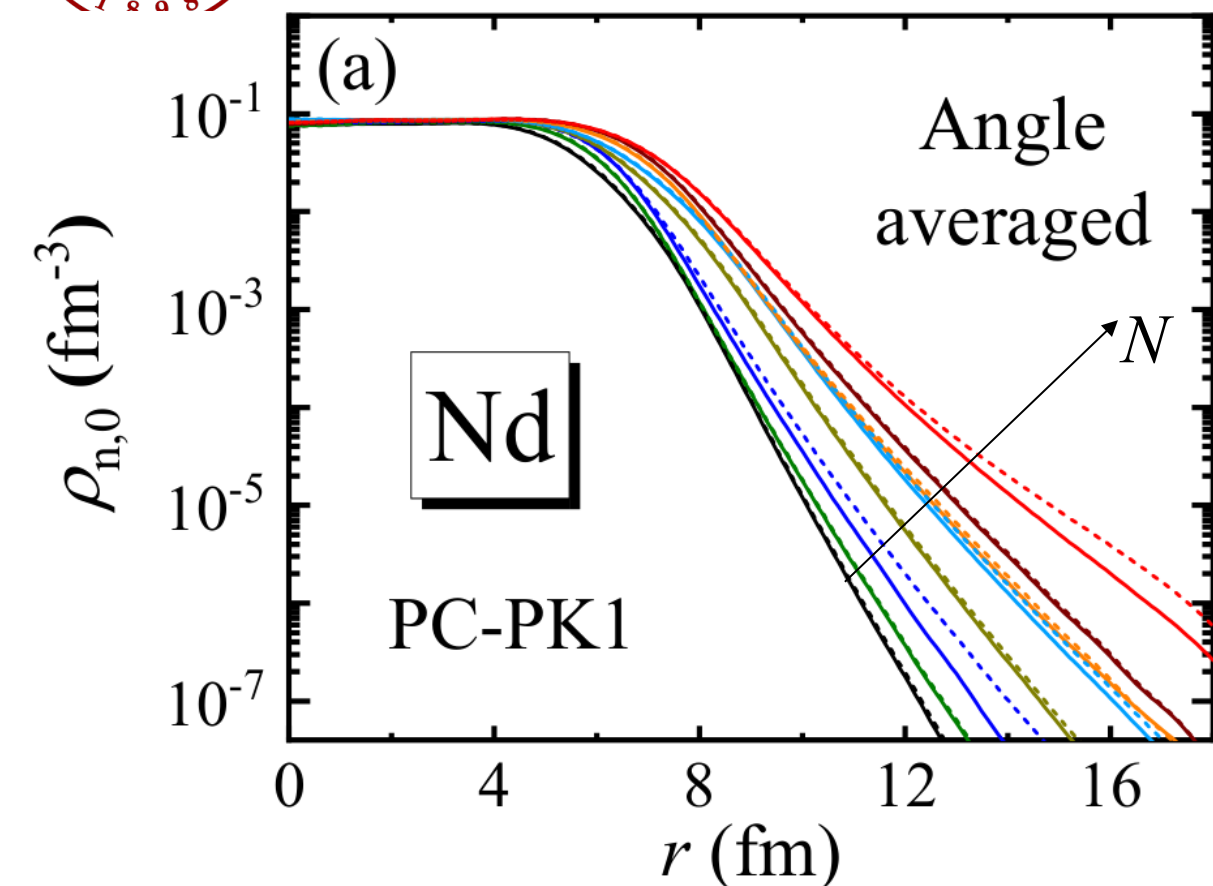
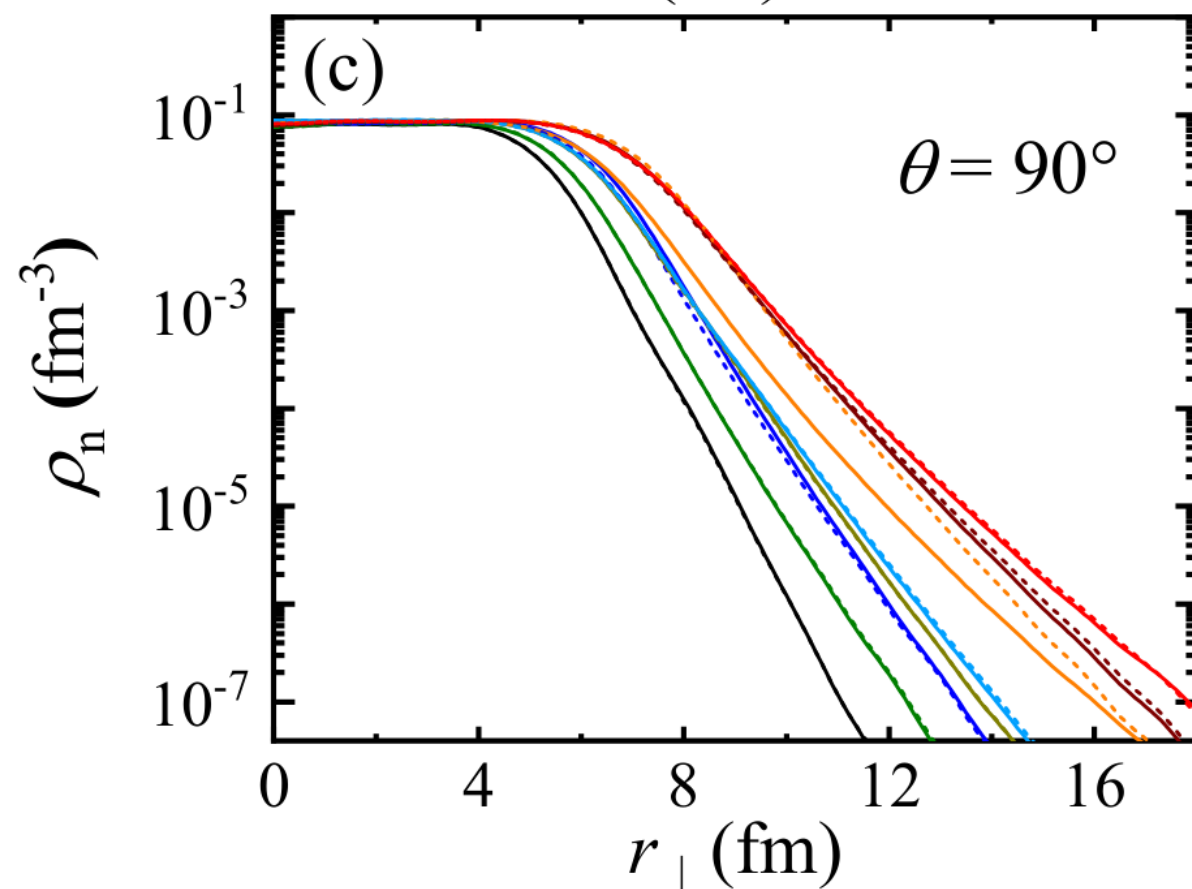


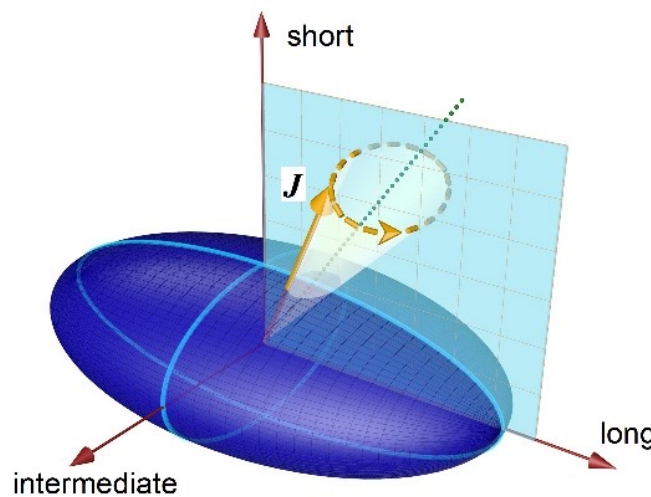
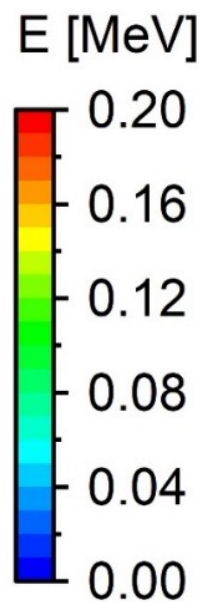
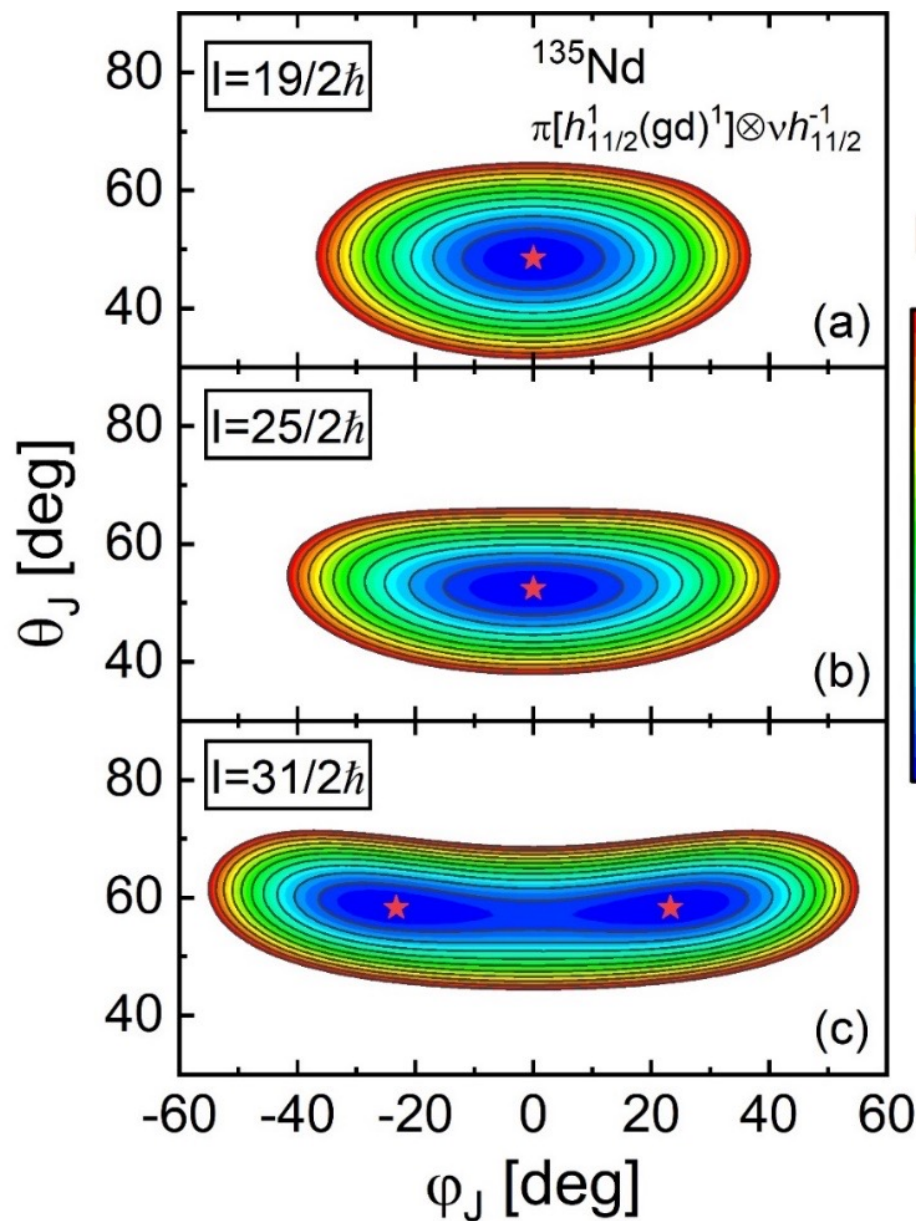
Figure: 3D PES of ^{240}Pu



- ✓ Angle-averaged density $\rho_{n,0}$ increases monotonically with N .
- ✓ An increase of $\rho_{n,0}$ is shown at ^{195}Nd .
- ✓ Density behavior at $\theta = 0^\circ$ with N is related to deformation effect.



(DRHBc Mass Table Collaboration), PRC 102, 024314 (2020)



Dynamics of rotation in chiral nuclei

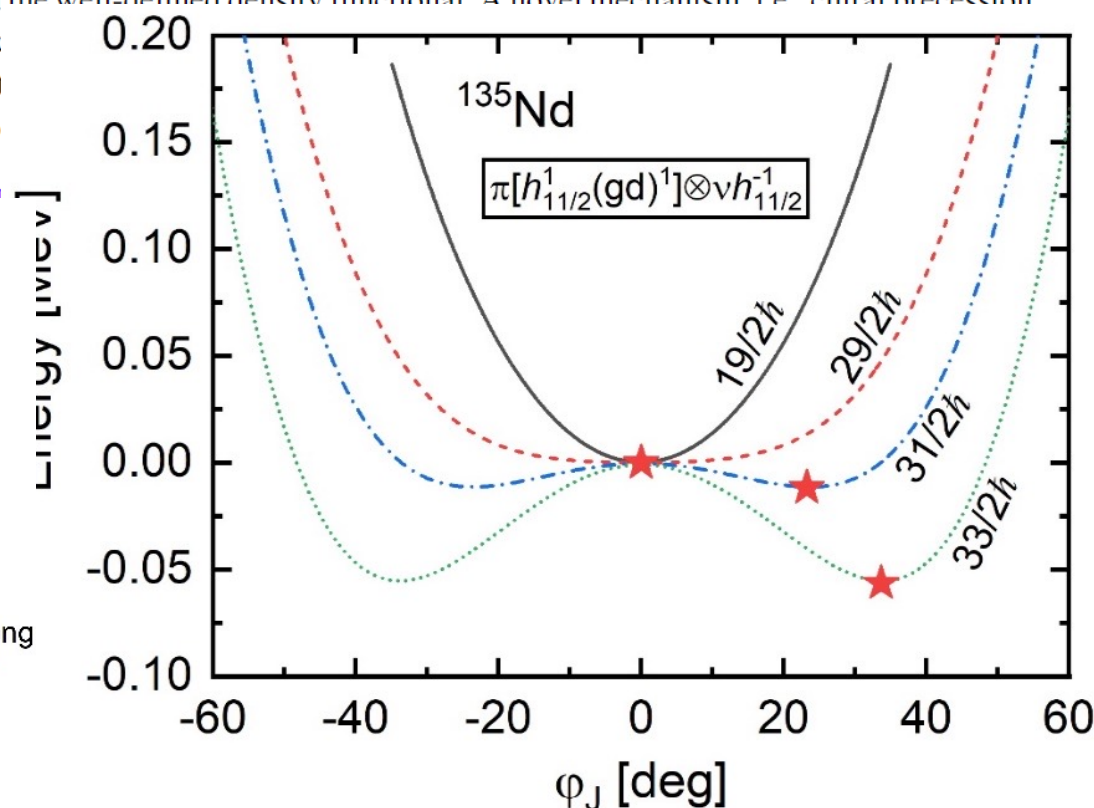
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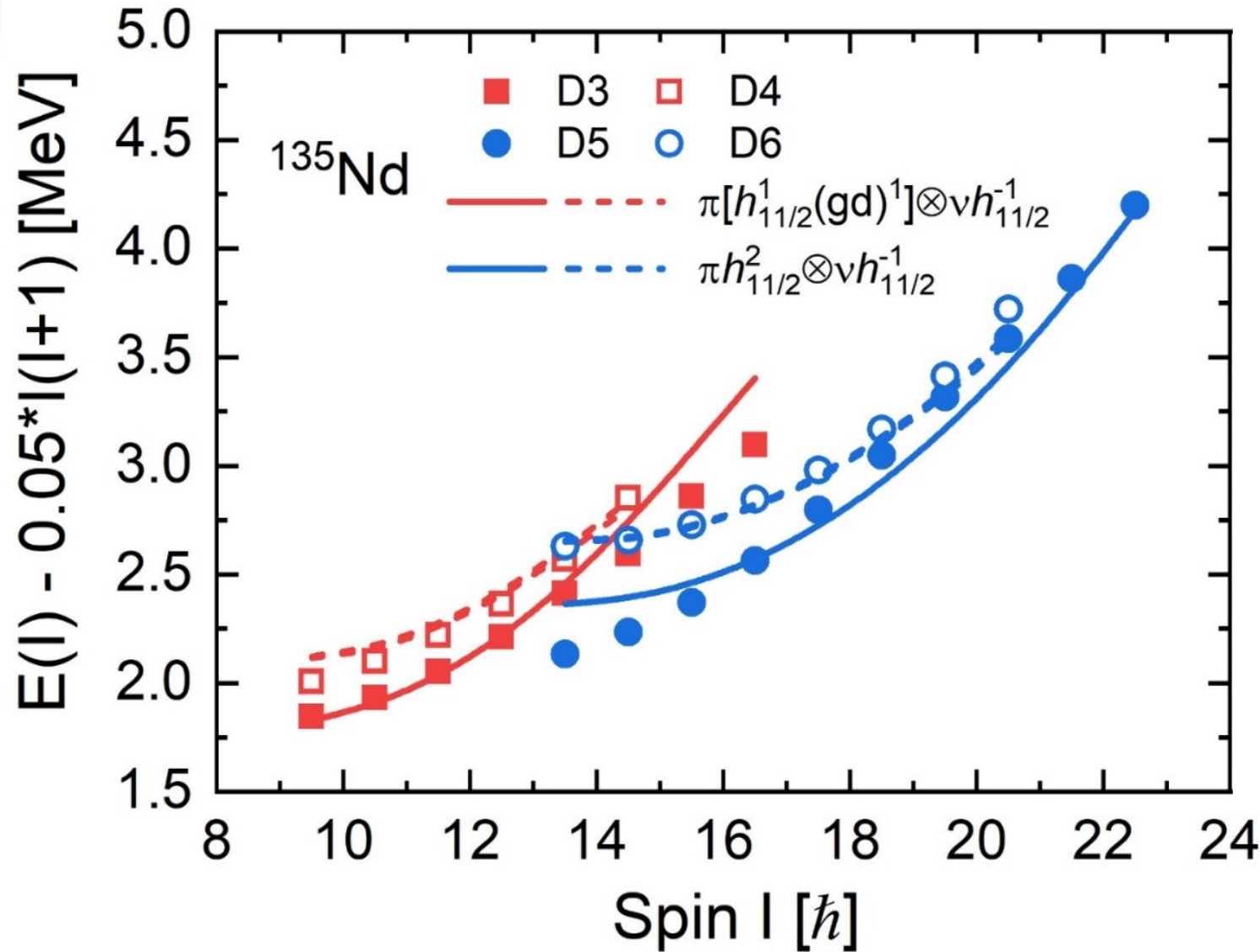
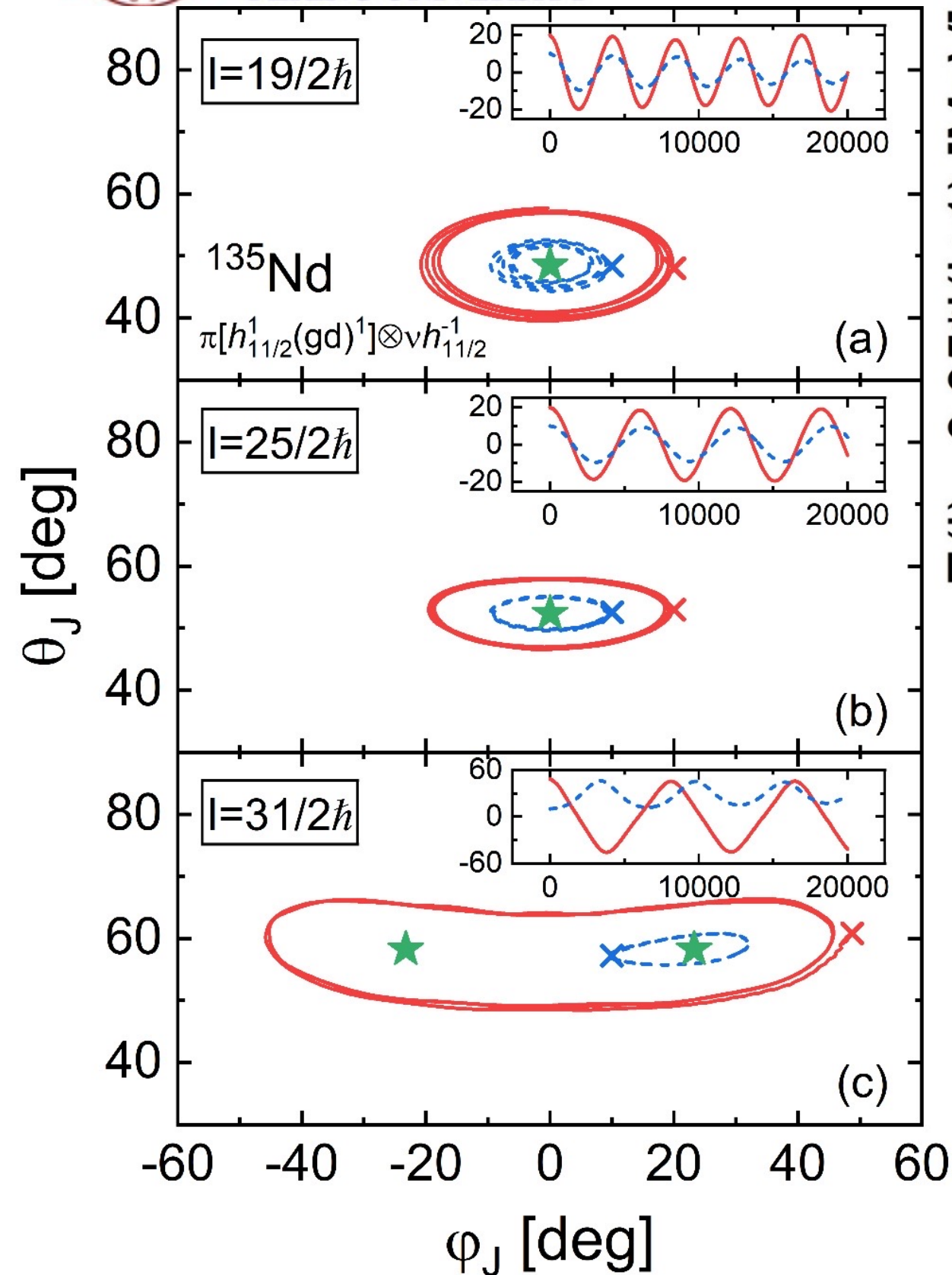
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The dynamics of chiral nuclei is investigated for the first time with the time-dependent and tilted axis cranking covariant density functional theories on a three-dimensional space lattice in a microscopic and self-consistent way. The experimental energies of the two pairs of the chiral doublet bands in ^{135}Nd are well reproduced without any adjustable parameters beyond the well-defined density functional. A novel mechanism, i.e. chiral precession, is revealed from the microscopic harmonicity is associated with a provides a fully microscopic and

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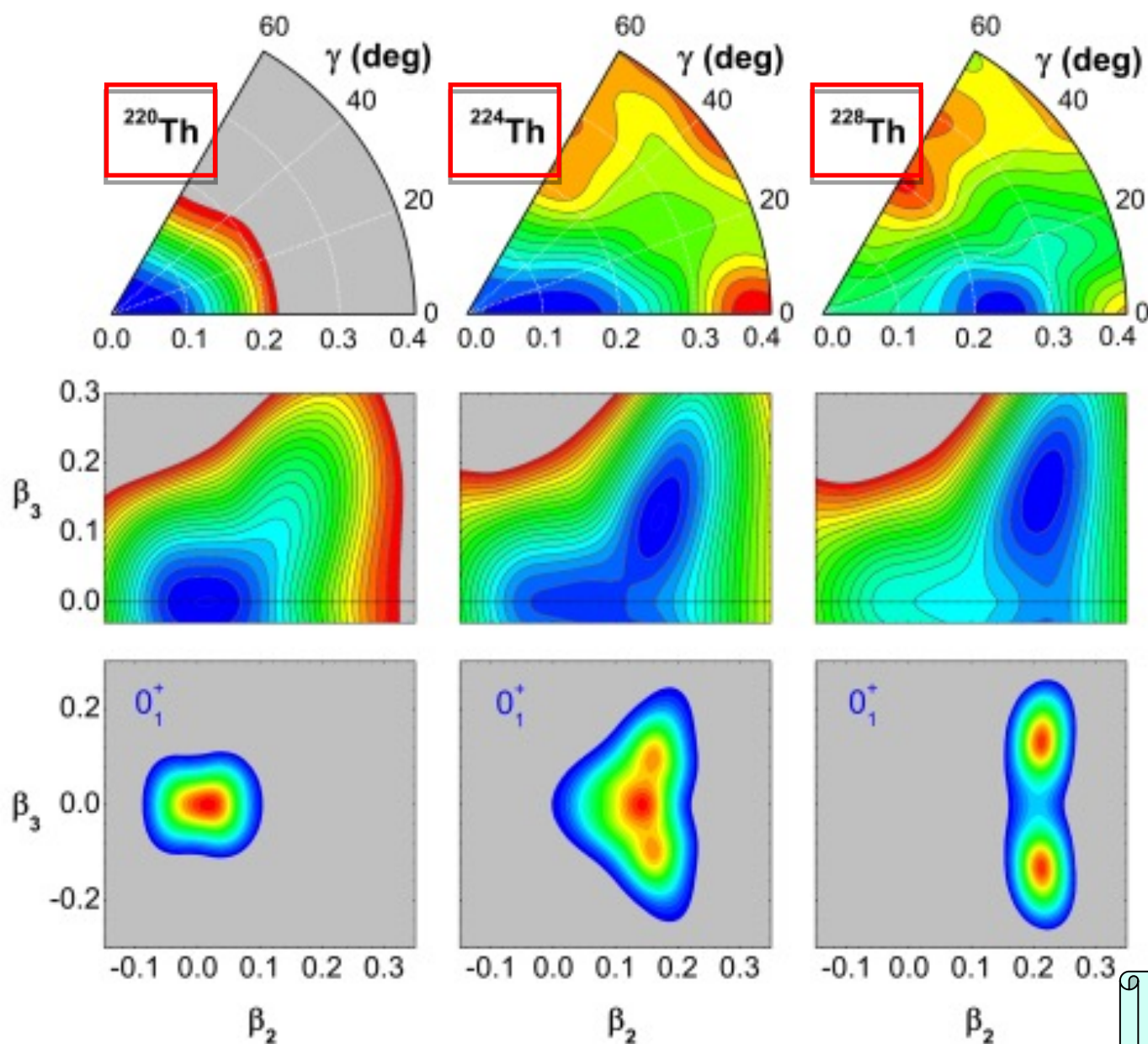
- 随着自旋 I 增加, 总能量相对于角动量倾斜角 φ_J 的位能曲线逐渐变软, 当自旋 $I \geq 31/2\hbar$, 系统出现三维转动.



- 结合推转和 TDCDFT 含时演化提取出振动能量, 可以描述手征晕带和伴带
- 理论计算再现了手征双带 D3&D4 和 D5&D6 的实验能谱



5DCH Calculations based on CDFT PC-PK1 indicate a simultaneous quantum shape phase transition from spherical to prolate shapes, and from reflection symmetric to octupole shapes.



triaxial quadrupole energy surfaces

axially-symmetric quadrupole-octupole energy surfaces

probability density distributions for the ground states