



# Total Reaction Cross-Section Measurements in the S444 Commissioning Experiment

Lukas Ponnath

R3B Week - Budapest  
May 2023

Overview: Setup & Total Reaction Cross-Section

Sensitivity of Carbon Identification

Influence of Position Dependent Efficiency



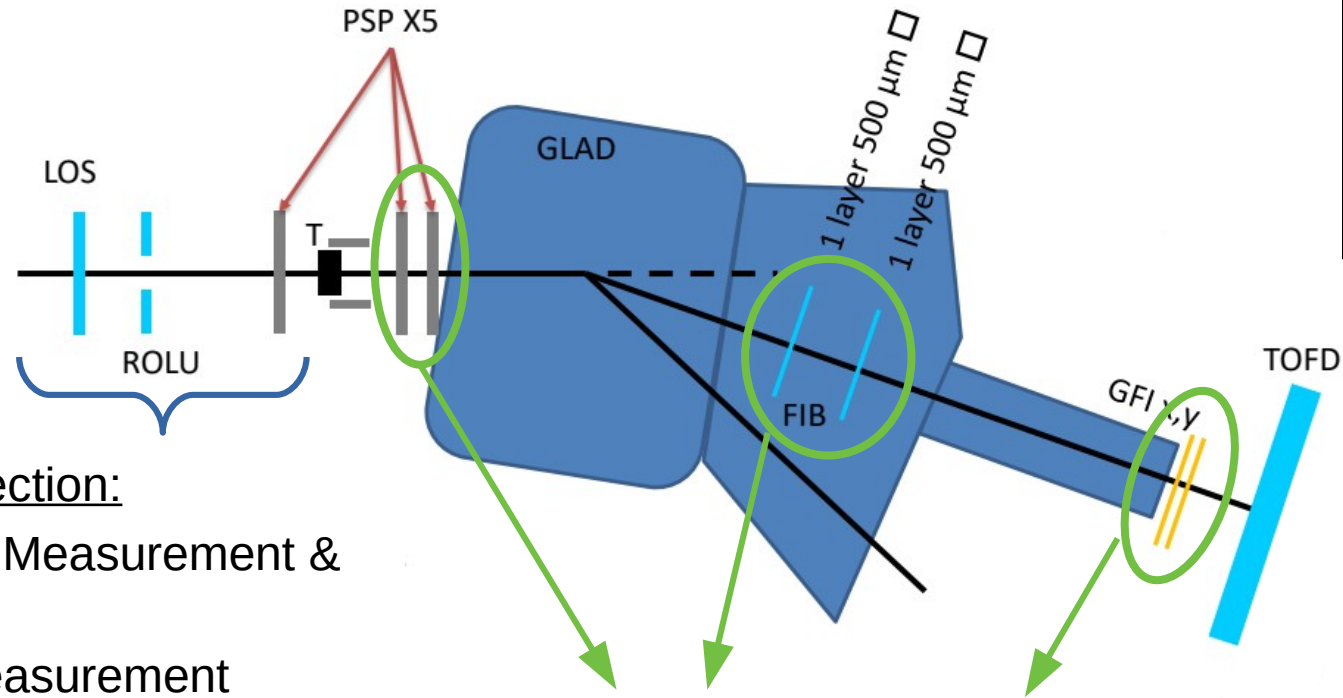
Supported by BMBF 05P21WOFN1 and 05P19WOFN1.

The results presented here are based on the experiment s444/s473, which was performed at the beam line/infrastructure Cave C at the GSI Helmholtzzentrum für Schwerionenforschung, Darmstadt (Germany) in the frame of FAIR Phase-0.

Funded by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) under Germany's Excellence Strategy – EXC 2094 – 390783311.



## First common operation of GLAD and R<sup>3</sup>B detectors



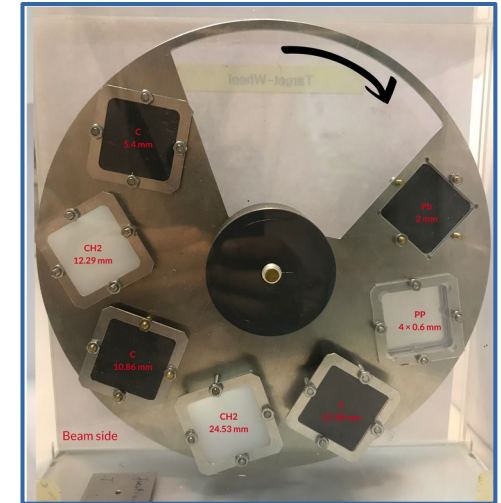
- Beam: 400 – 1000 AMeV <sup>12</sup>C
- Targets: C, CH<sub>2</sub> (different thickness)

### Event-Selection:

- Position Measurement & Veto
- Time Measurement
- Charge Identification

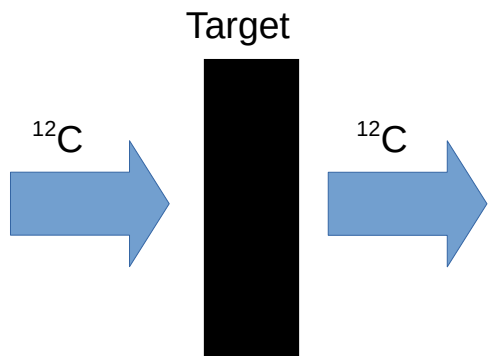
### Silicon- & Fiber-Tracking:

- Position Measurement
- Charge Identification after the target



## Precision Measurement:

Energy dependence of the total reaction cross-section of  $^{12}\text{C} \rightarrow ^{12}\text{C}$   
 (Tom Aumann)

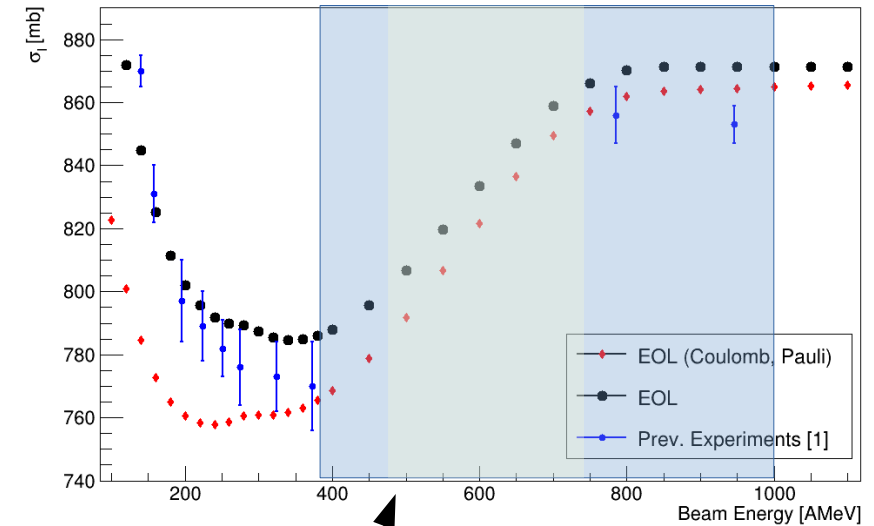


**Total reaction cross-section:**  $\sigma_R = \sigma_I + \sigma_{inel}$

**Total interaction cross-section  $\sigma_I$ :**  
 The projectile changes its identity.  
 At least one nucleon is removed.

**Total inelastic cross-section  $\sigma_{inel}$ :**  
 The projectile is excited to a bound state.  
 No nucleon is removed.

**Total Reaction Cross Section  $^{12}\text{C} \rightarrow ^{12}\text{C}$**



[1] I.Tanihata et al. (Radioactive Nuclear Beams 1990), M. Takechi et al. (PRC – 79 2009) , A. Ozawa et al. (Nuc. Phys. A – 691 2001)

EOL data: E.A. Teixeira, T. Aumann, C.A. Bertulani, B.V. Carlson (Eur. Phys. J.A – 58:205 2022)

$^{12}\text{C}$  Beam Energies in S444 Experiment:  
 400, 550, 650, 800 & 1000 AMeV





# Measurement Concept

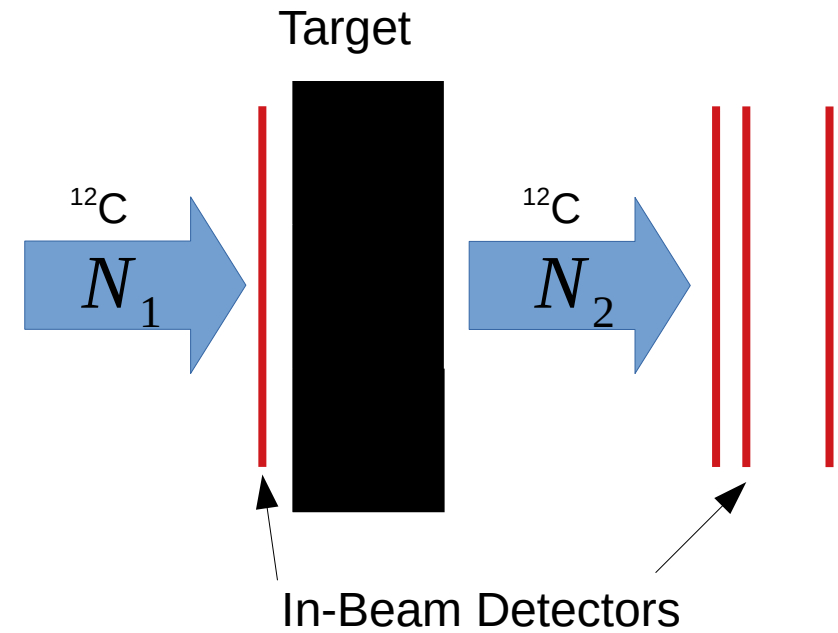
Surviving-Probability: 
$$P_{surv.} = \frac{N_2}{N_1} = e^{-N_t \cdot \sigma_R}$$

Exclude reactions in Setup:

$$\frac{\overbrace{N_2^i / N_1^i}^{\text{Target-In}}}{\underbrace{N_2^o / N_1^o}_{\text{Target-Out}}} = e^{-N_t \cdot \sigma_R}$$

Transmission method:

$$\sigma_R = -\frac{1}{N_t} \ln \left( \frac{N_2^i / N_1^i}{N_2^o / N_1^o} \right)$$





# Measurement Concept

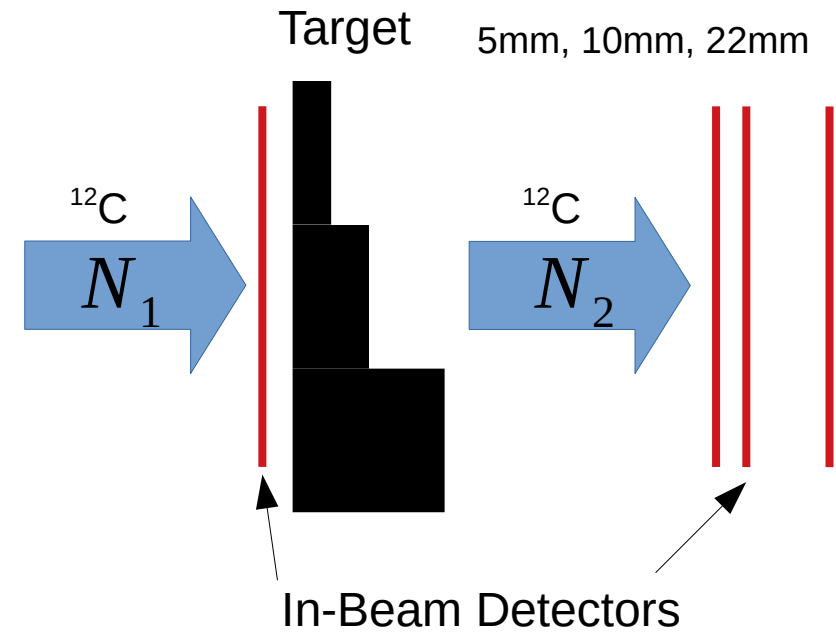
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- $N_t$  is a target specific constant (density, Thickness)
- $N_1$ , number of incident  $^{12}\text{C}$  nuclei (stable beam, Event-Selection)





# Measurement Concept

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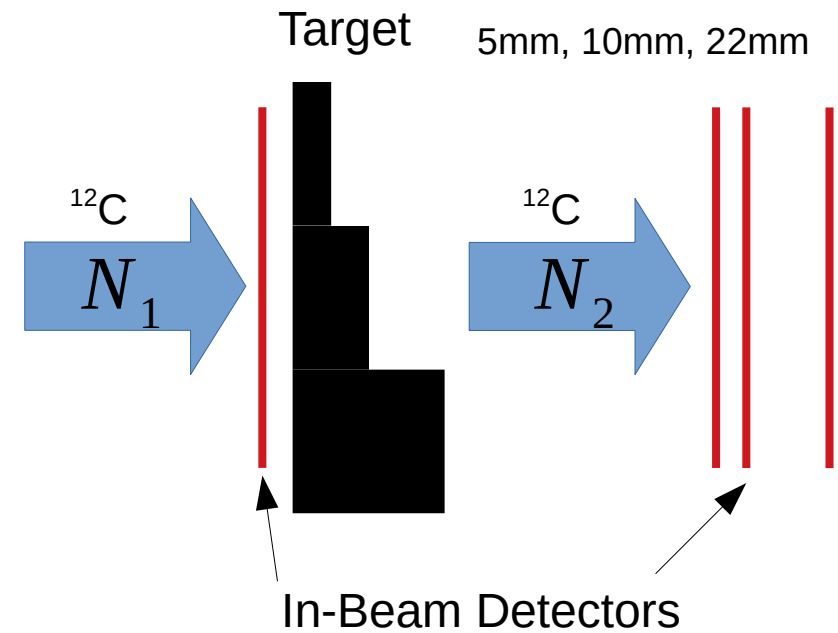
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Challenge: Time- & Rate-depended Efficiency & geometrical Acceptance of Detectors



- $N_t$  is a target specific constant (density, Thickness)
- $N_1$ , number of incident  $^{12}\text{C}$  nuclei (stable beam, Event-Selection)
- $N_2$ , number of non-reacting  $^{12}\text{C}$  nuclei, identified after the target (that's our big challenge)



# Number of non-reacting Nuclei



Strategy: minimize systematic uncertainties → minimize Number of detectors

1. Count the number of all Carbon (Q=6) isotopes with TOFD  $N_{Q=6}$

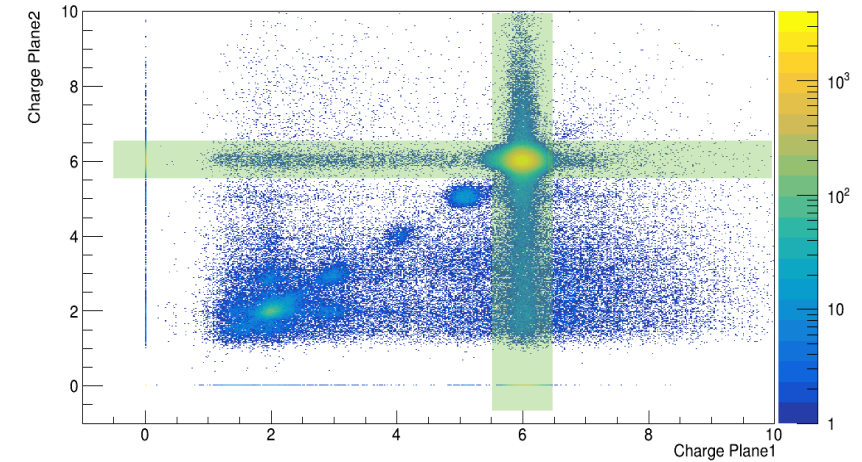
2. Define Correction factors:

2a. Ratio of  $^{12}\text{C}$  to all identified Carbon isotopes  $R(^{12}\text{C})$

2b. Correction of variable geometrical acceptance  $A$

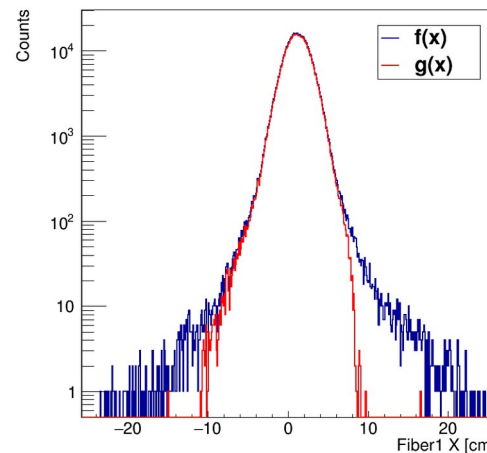
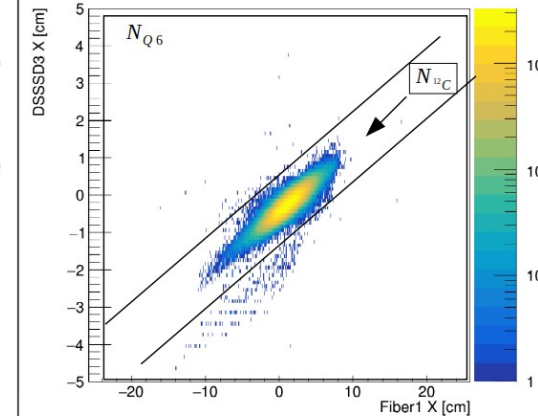
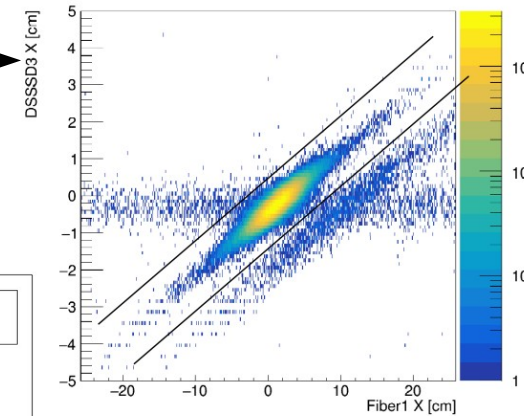
Non-reacting  $^{12}\text{C}$  nuclei:

$$N_2^{i/o} = \frac{N_{Q=6}^{i/o} \cdot R^{i/o}(^{12}\text{C})}{\varepsilon^{i/o} \cdot A^{i/o}}$$



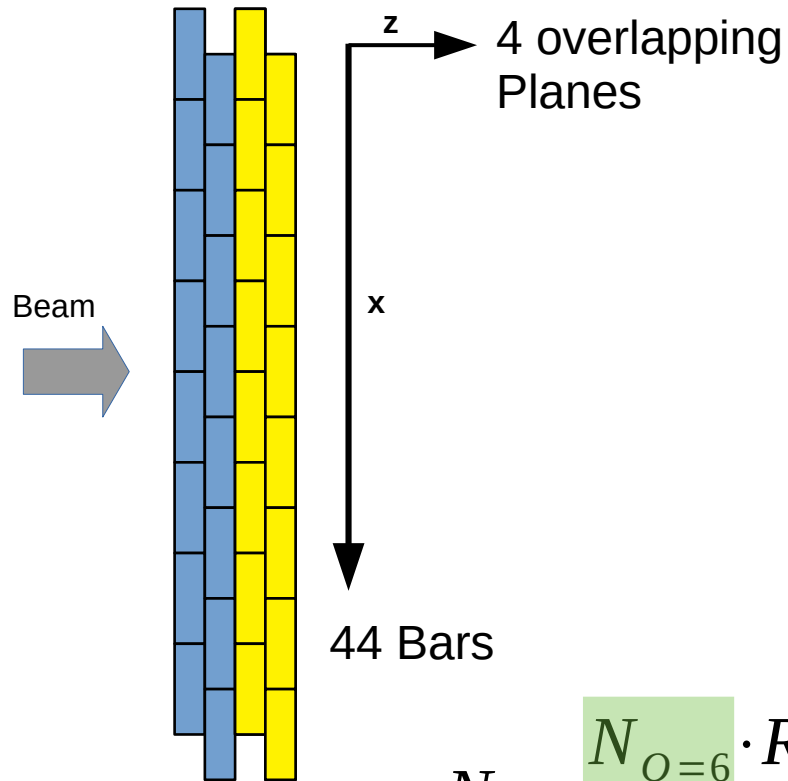
PSP - Q=6

PSP & TOFD - Q=6



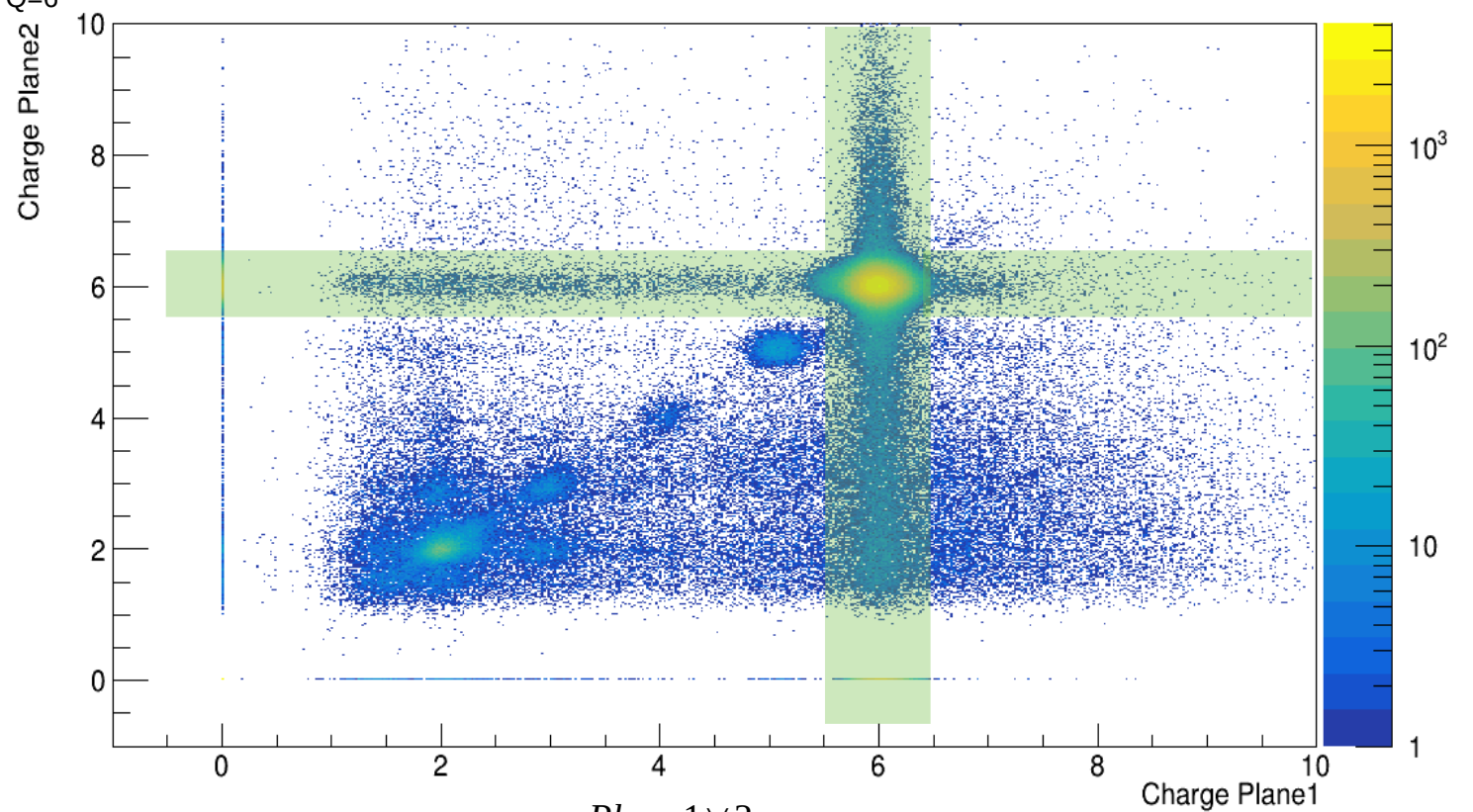


# Carbon Identification



$$N_2 = \frac{N_{Q=6} \cdot R(^{12}\text{C})}{\epsilon \cdot A}$$

$N_{Q=6}$  = Plane1 or Plane2 saw a particle with  $Q = 6. \pm 0.5$  (>99.9993 %)



Check efficiency of Carbon identification:

$$\epsilon = \frac{N_{Q=6}^{Plane\ 1 \vee 2}}{N_{Q=6}^{Plane\ 3 \wedge 4}} = 0.999916 (17) \%$$

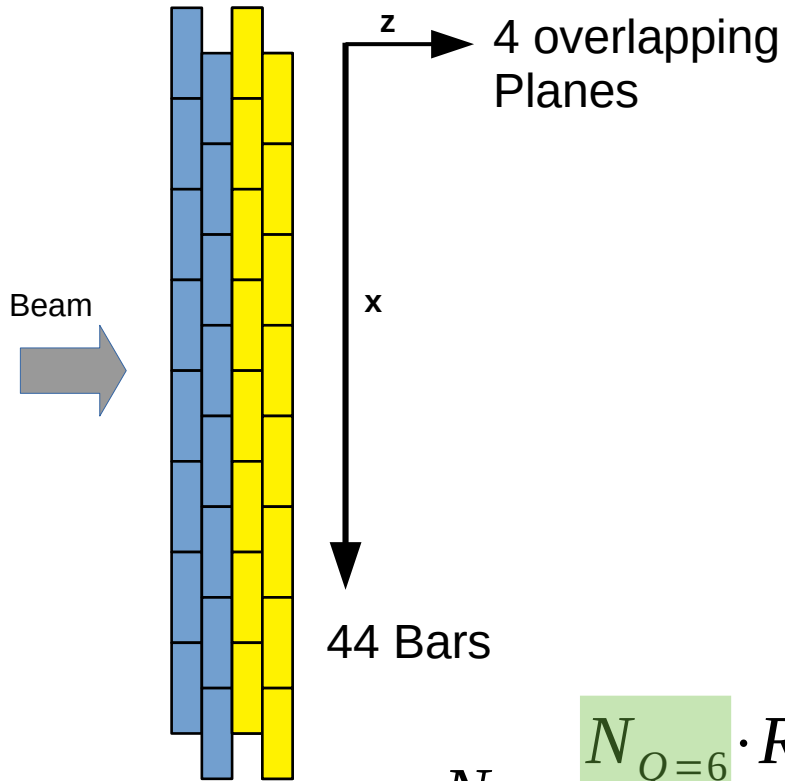




# Carbon Identification

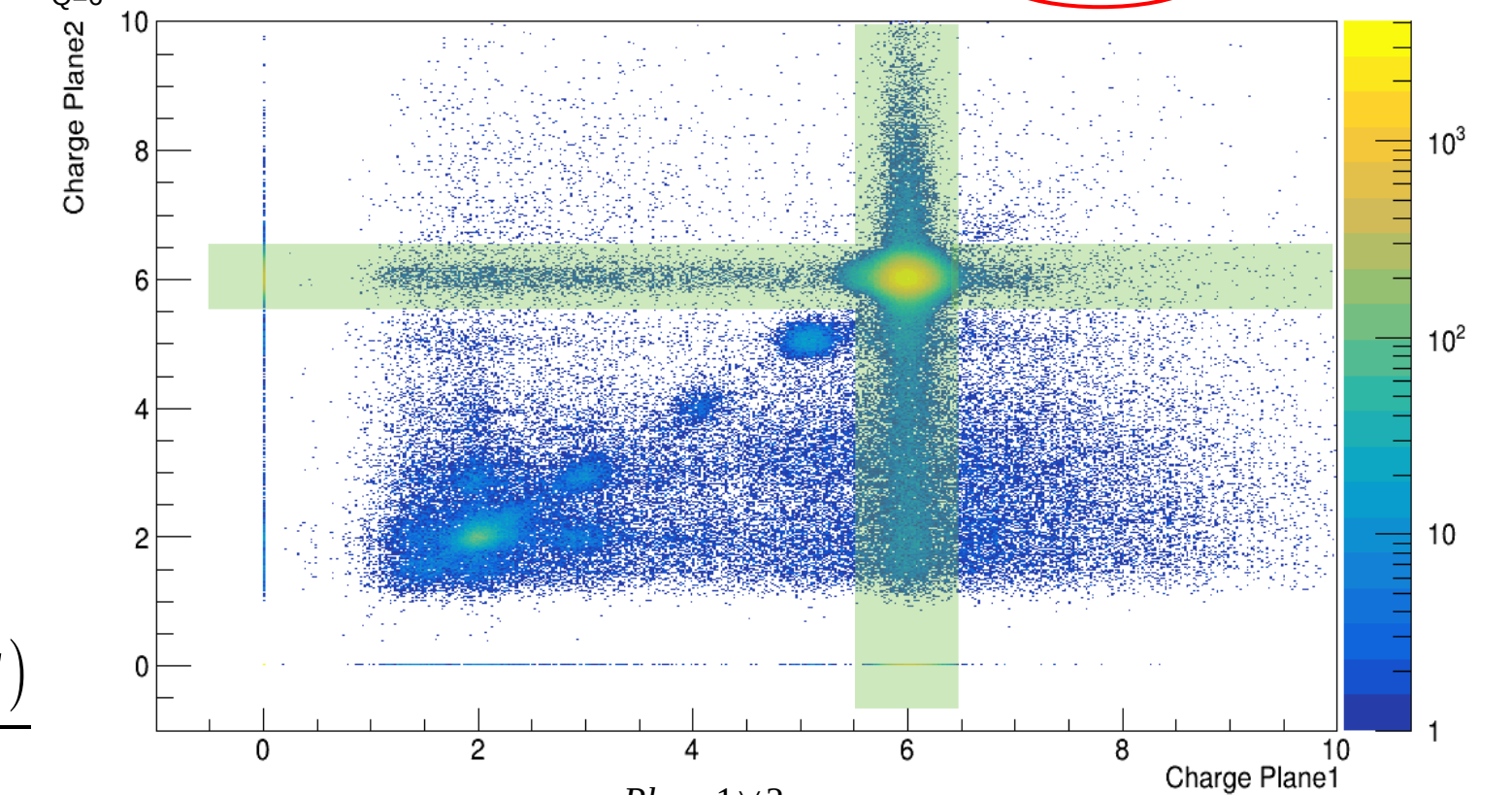


Is  $\sigma_1$  sensitive to the cut-width?



$$N_2 = \frac{N_{Q=6} \cdot R(^{12}C)}{\epsilon \cdot A}$$

$N_{Q=6}$  = Plane1 or Plane2 saw a particle with  $Q = 6. \pm 0.5$  (>99.9993 %)

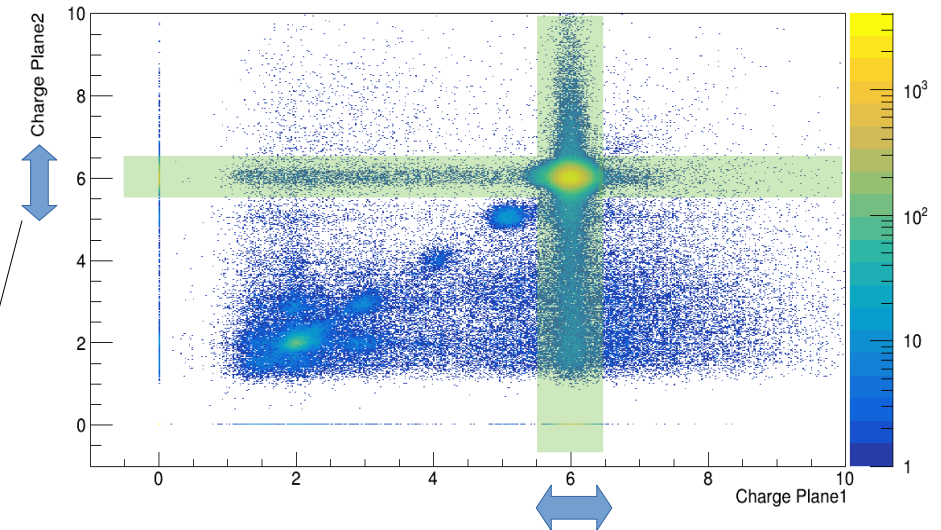
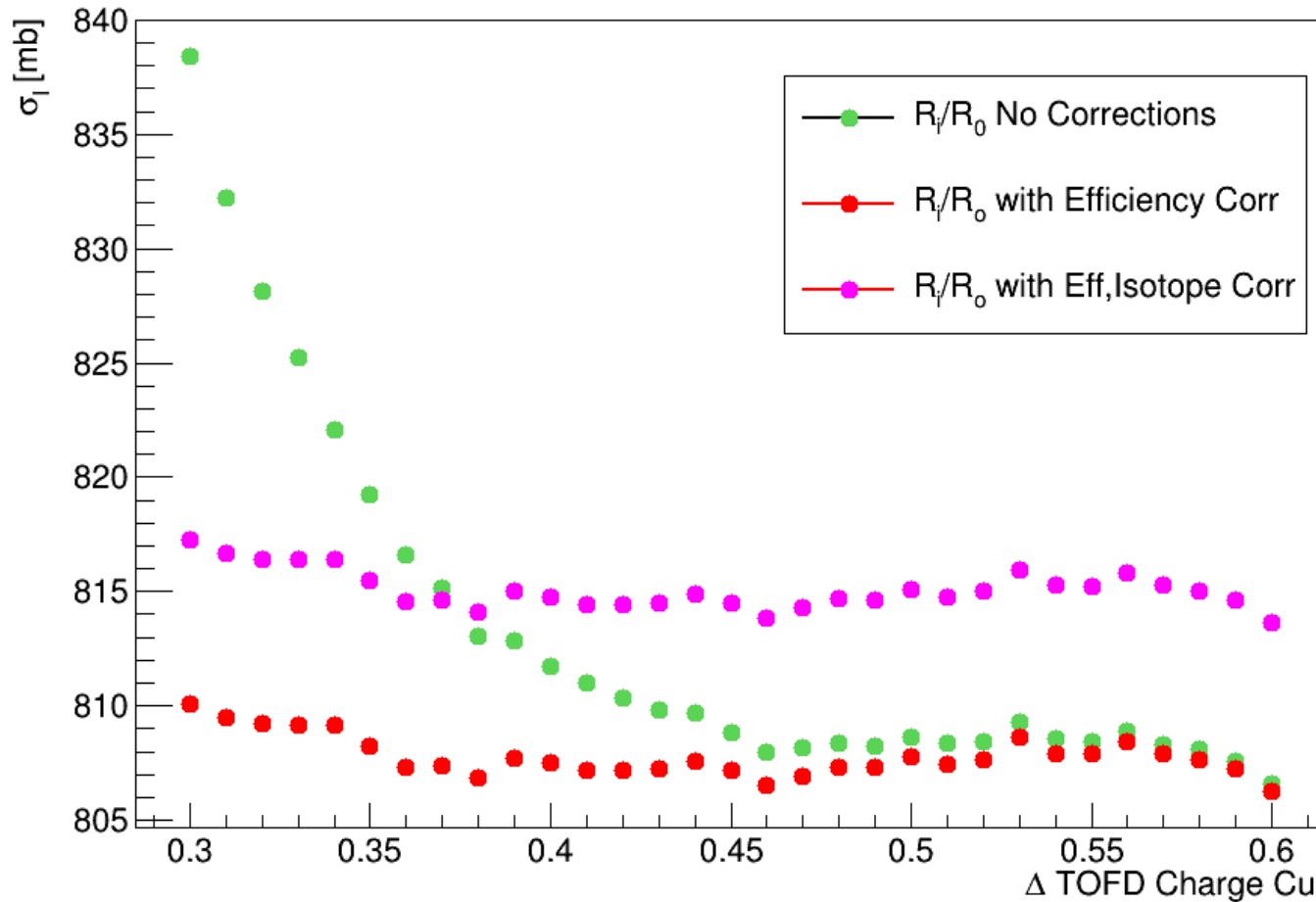


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# Dependance on Cut Width - Missing Particles

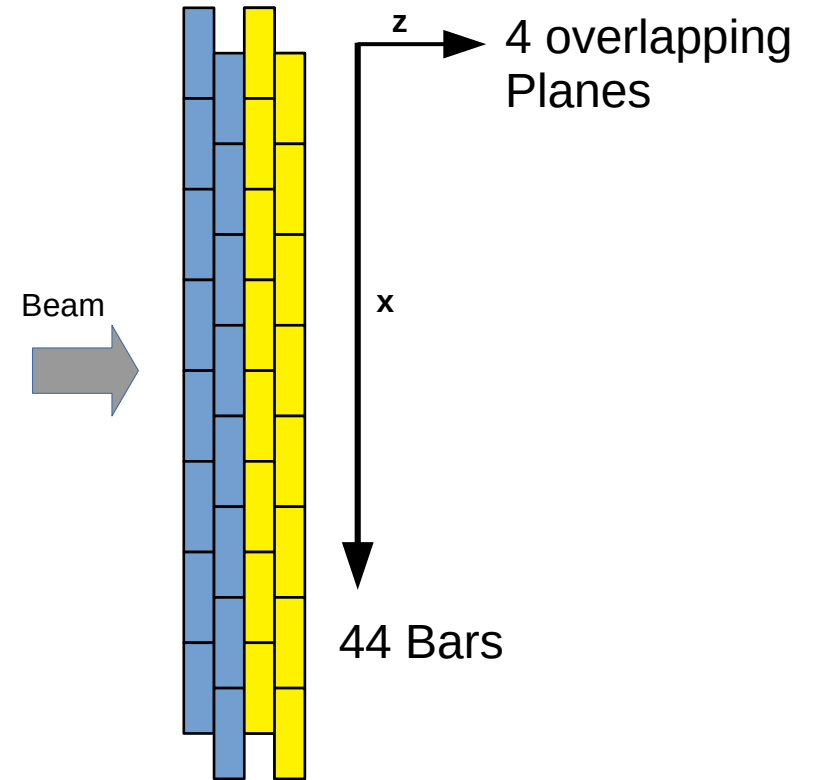
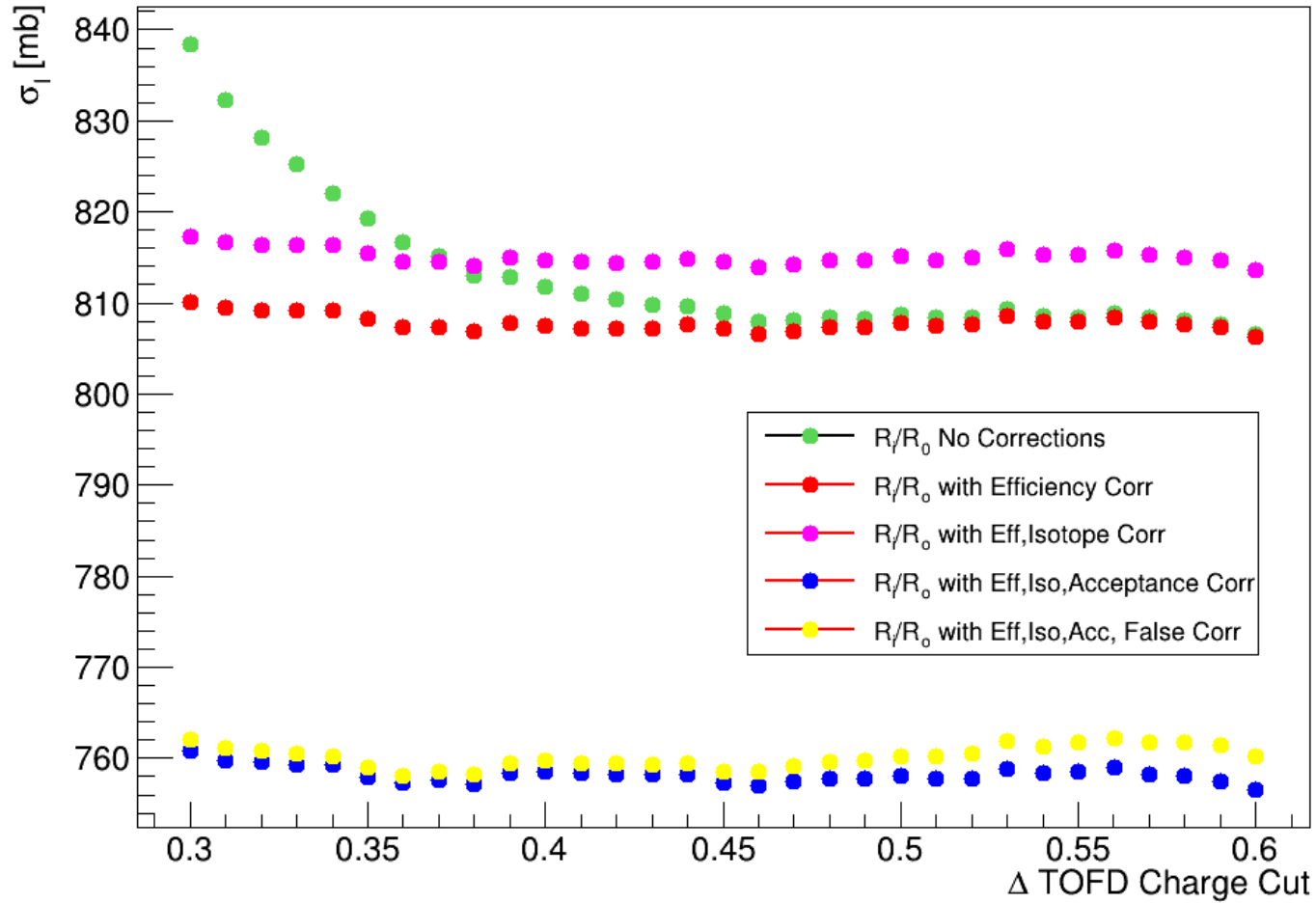


$$\sigma_R = -\frac{1}{N_t} \ln \left( \frac{N_2^i / N_1^i}{N_2^o / N_1^o} \right)$$

$$N_2^{i/o} = \frac{N_{Q=6}^{i/o} \cdot R^{i/o}(^{12}\text{C})}{\epsilon^{i/o} \cdot A^{i/o}}$$



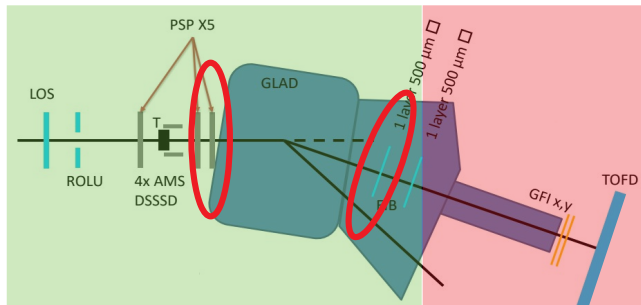
# Dependance on Cut Width - False Particles



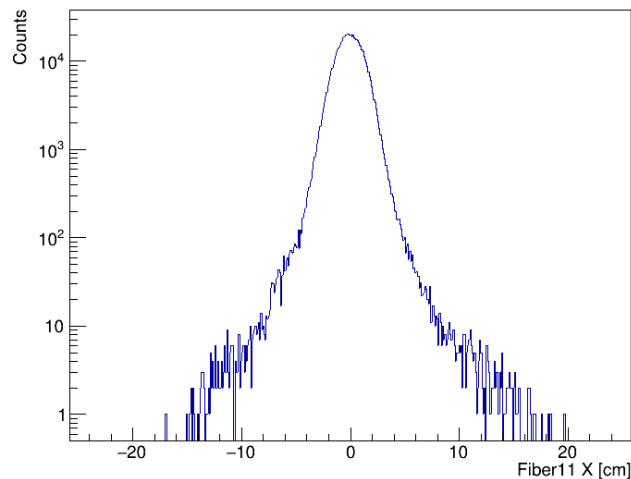
$$False = \frac{N_{Q \neq 6}^{Plane 1 \vee 2}}{N_{Q=6}^{Plane 3 \vee 4}}$$



# Acceptance-Correction

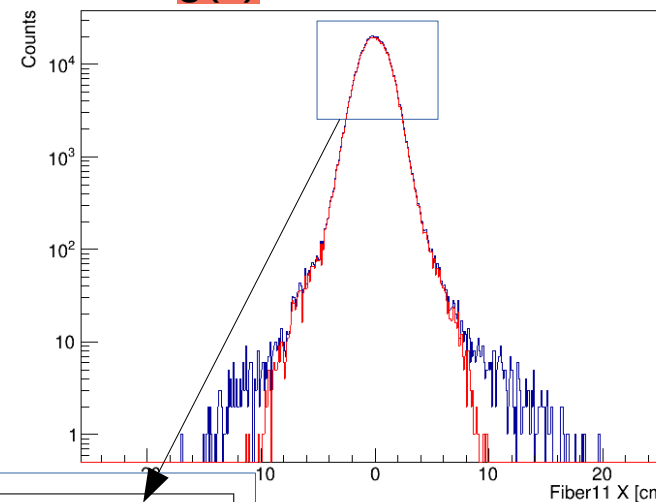


Position-Distribution of  $^{12}\text{C}$   $f(x)$



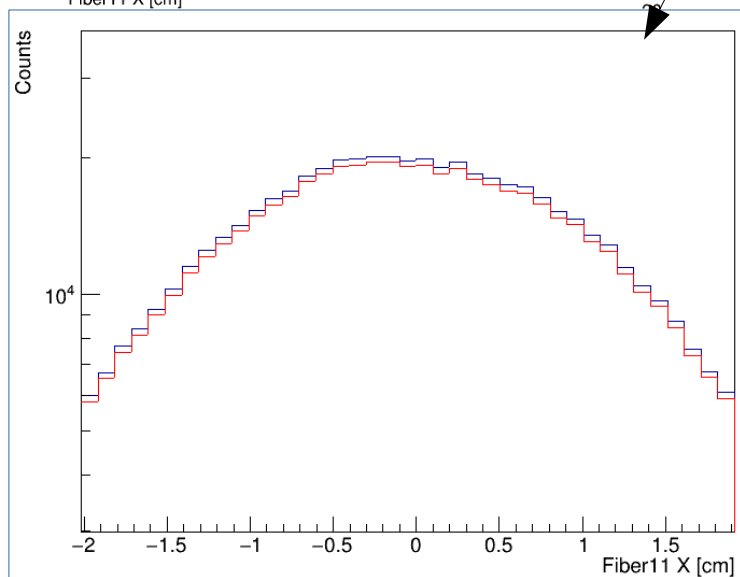
TOFD Q=6

Position-Distribution of  $^{12}\text{C}$  with TOFD  $g(x)$



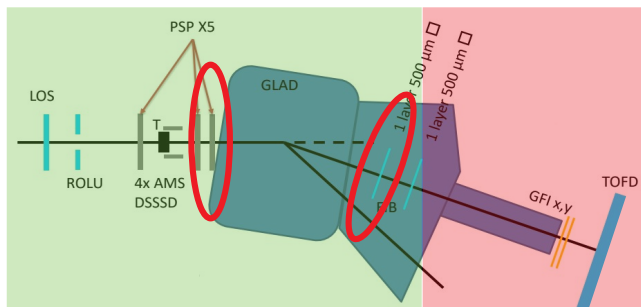
$$A = \frac{\int_{-25.8 \text{ cm}}^{25.8 \text{ cm}} g(x)}{\int_{-25.8 \text{ cm}}^{25.8 \text{ cm}} S \cdot f(x)}$$

Scaling-Factor

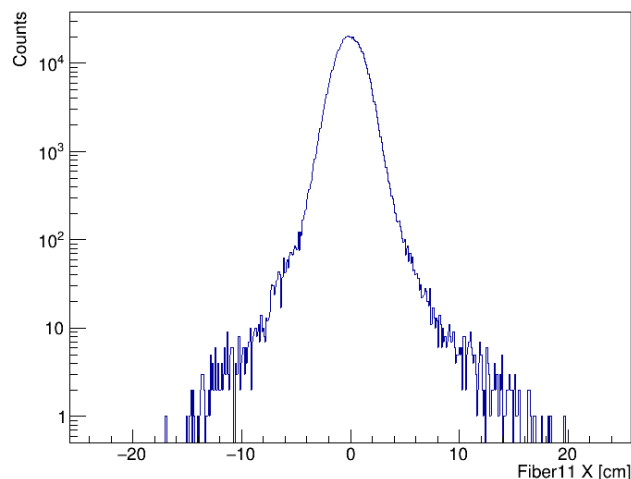




# Acceptance-Correction

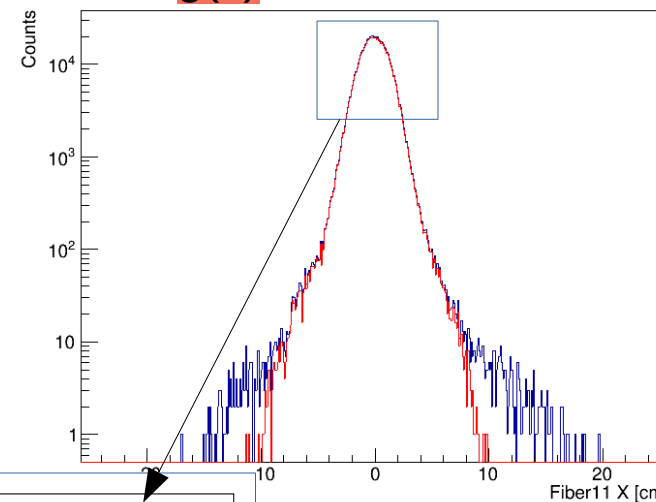


Position-Distribution of  $^{12}\text{C}$   $f(x)$



TOFD Q=6

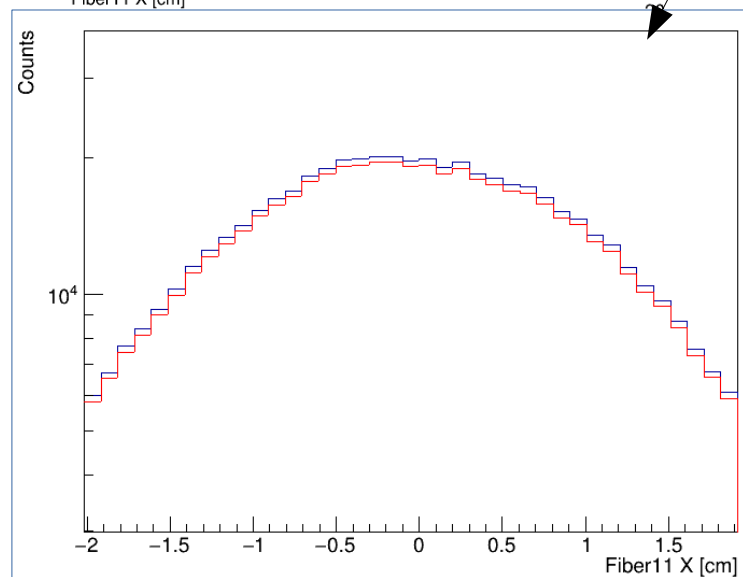
Position-Distribution of  $^{12}\text{C}$  with TOFD  $g(x)$



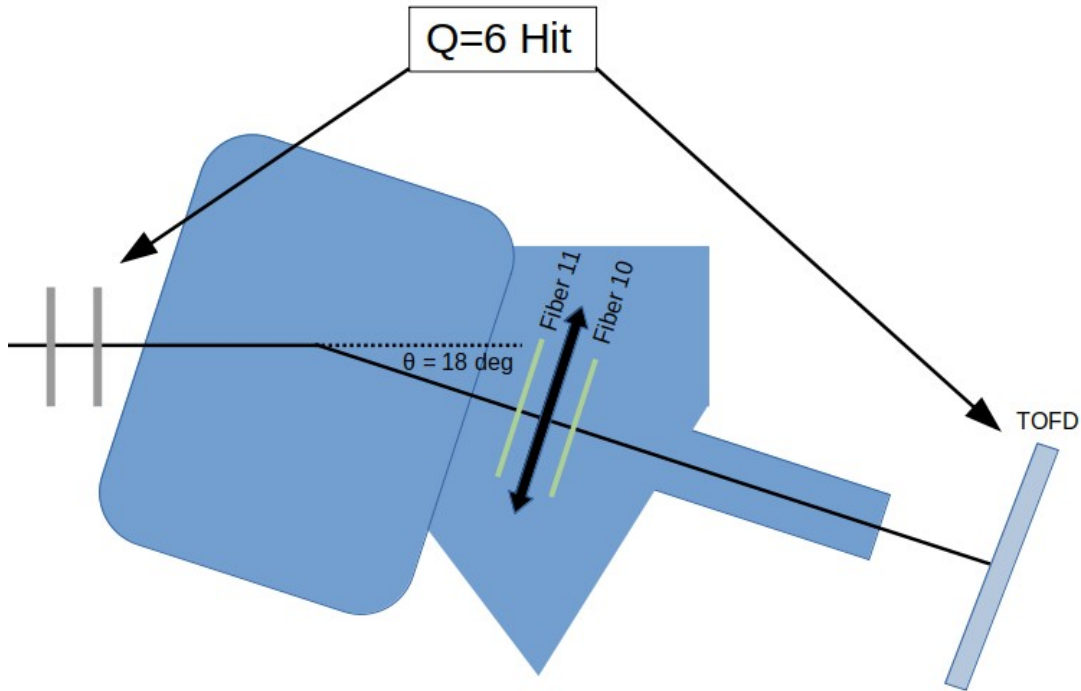
$$A = \frac{\int_{-25.8\text{ cm}}^{25.8\text{ cm}} g(x)}{\int_{-25.8\text{ cm}}^{25.8\text{ cm}} S \cdot f(x)}$$

Scaling-Factor

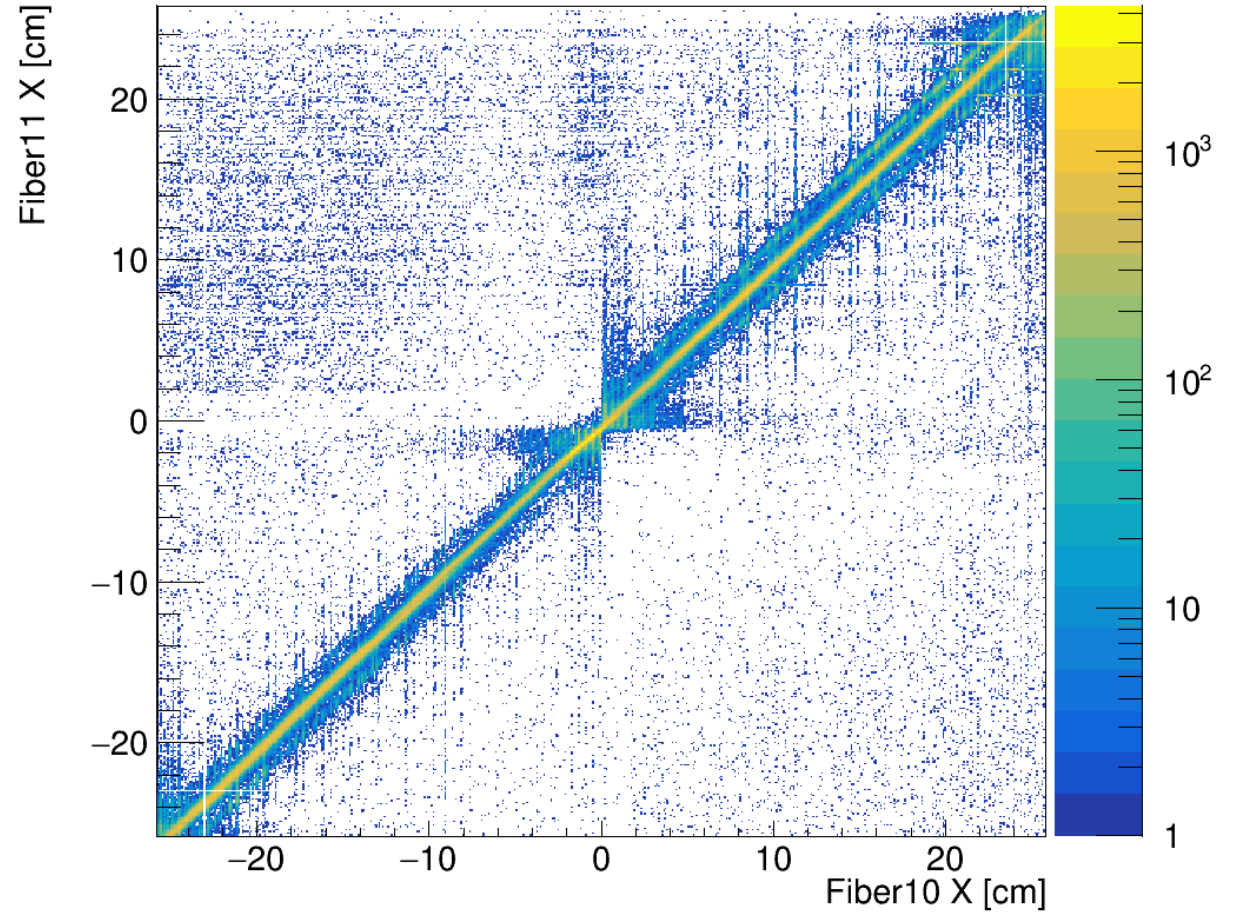
Is  $\sigma_1$  sensitive to a position dependent efficiency?





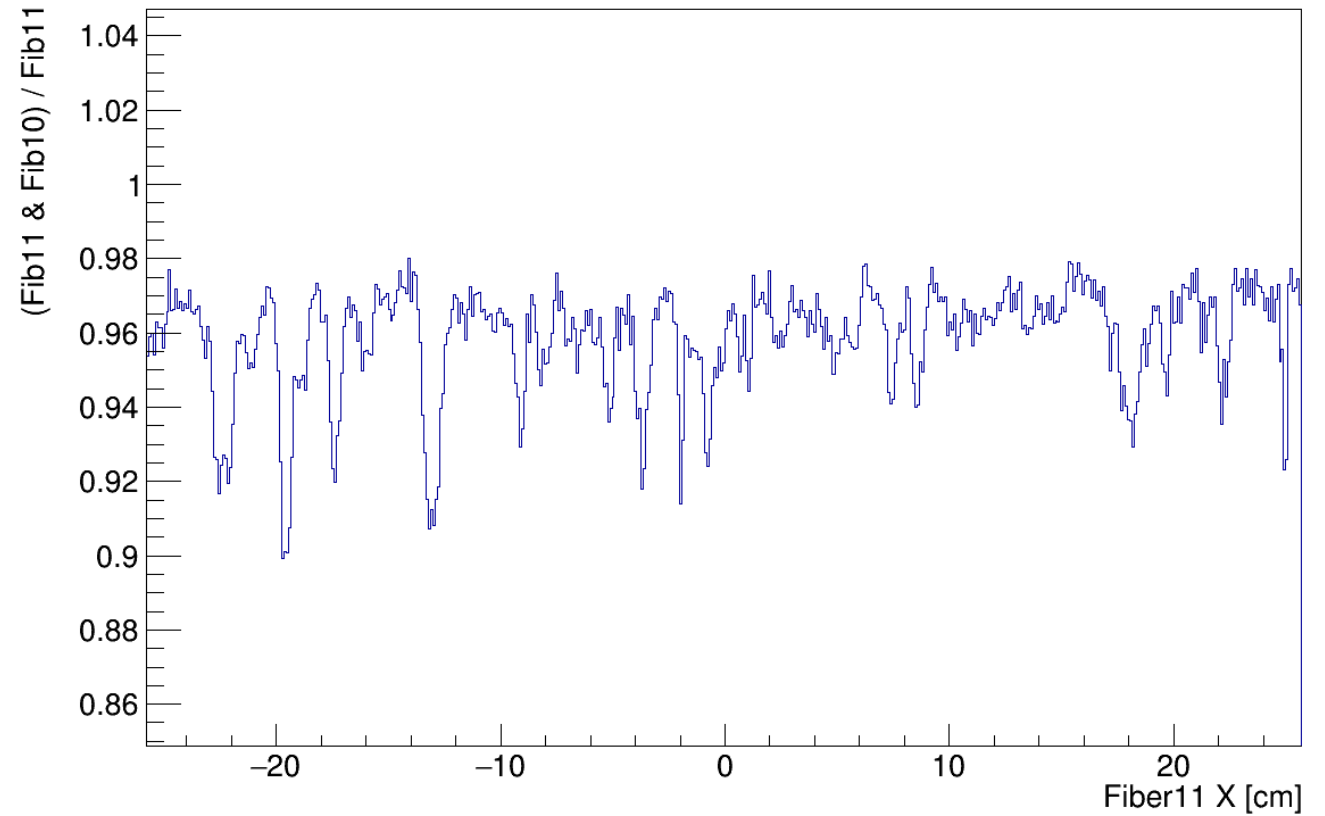
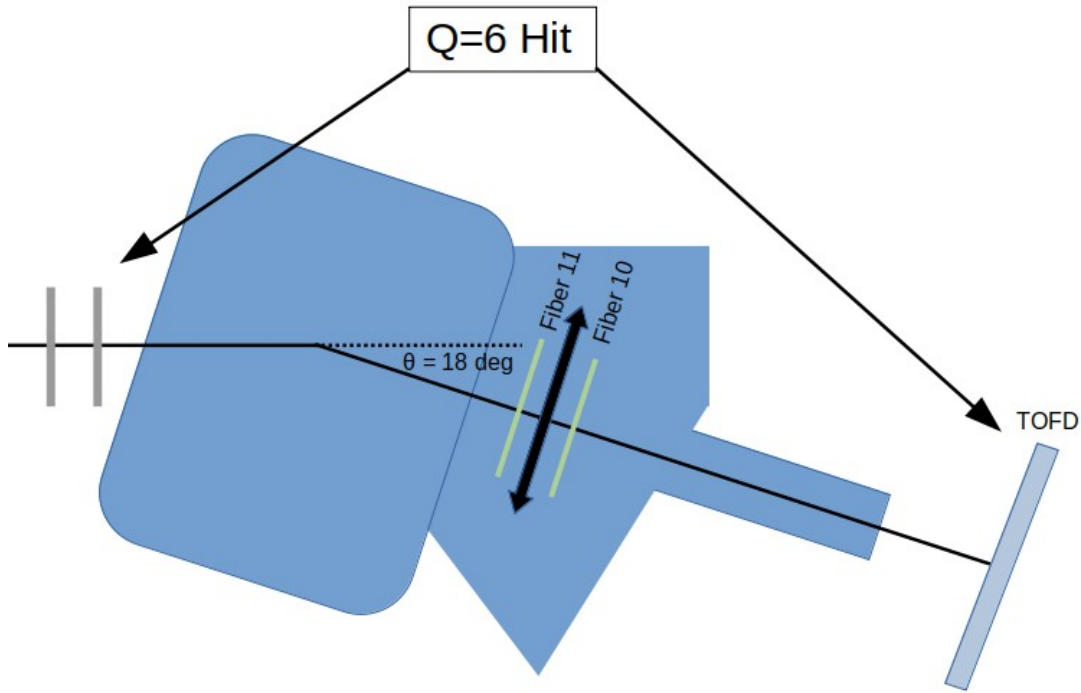


**Fiber Sweep-Run**



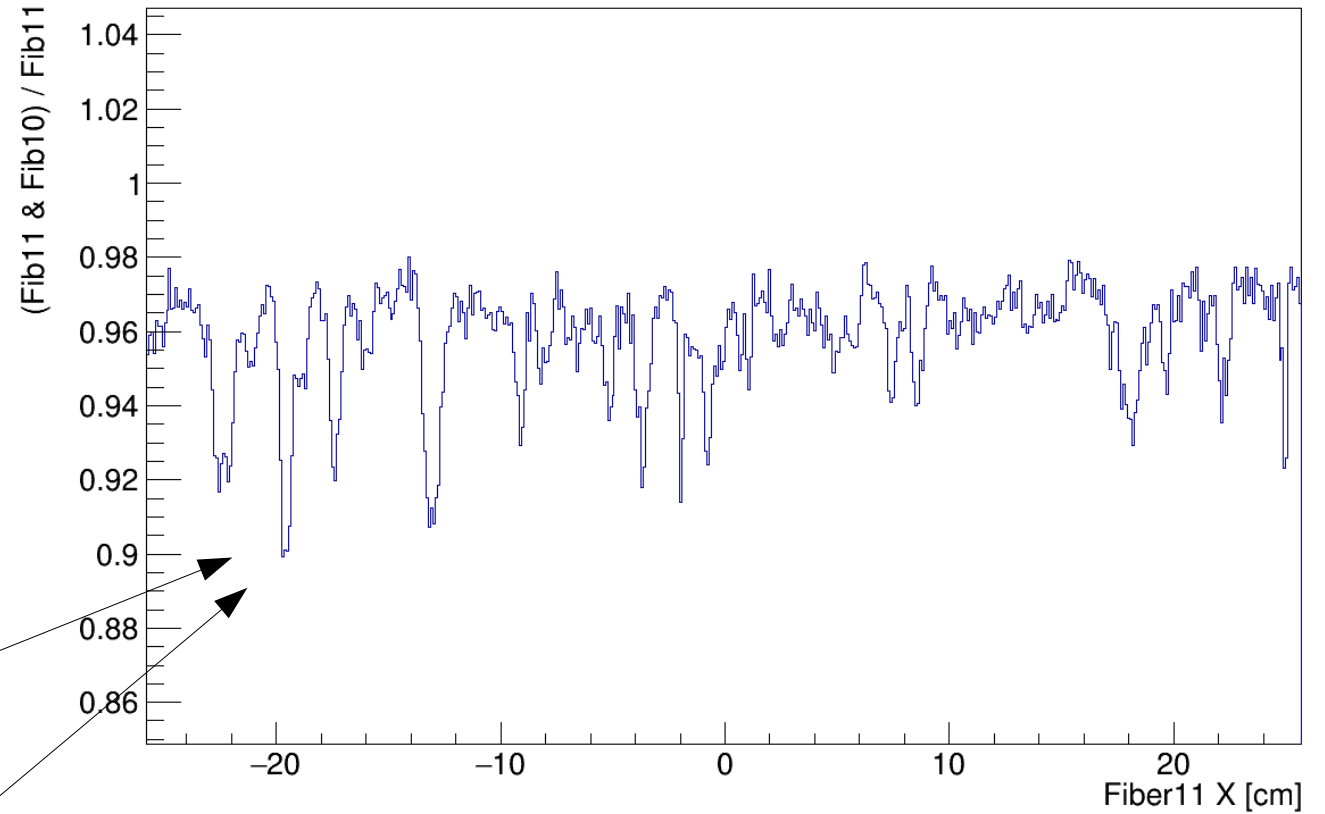
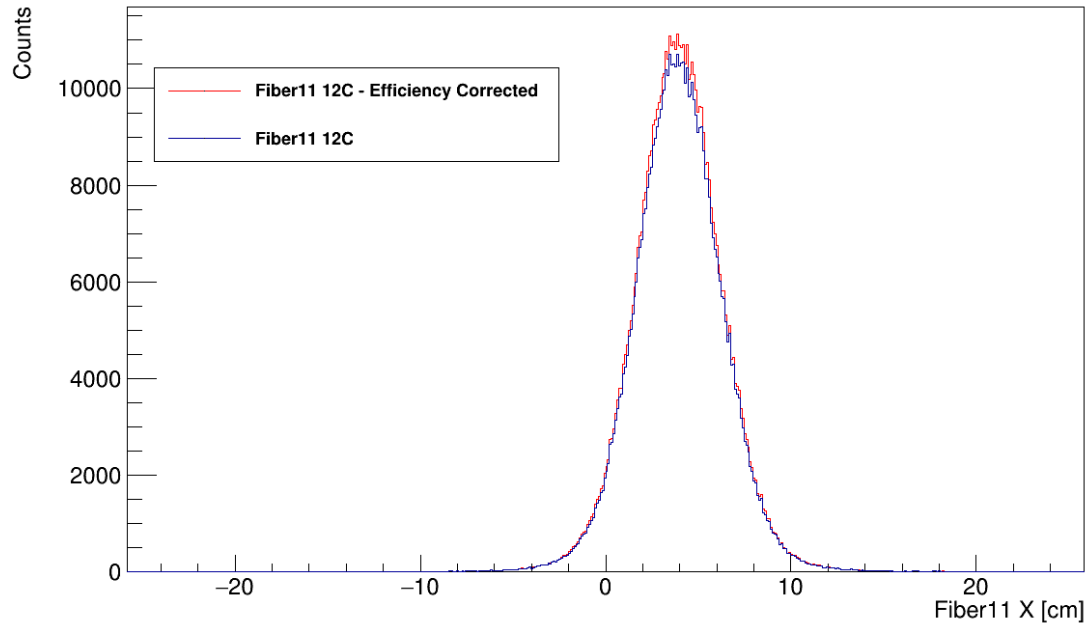


# Position Dependent Efficiency



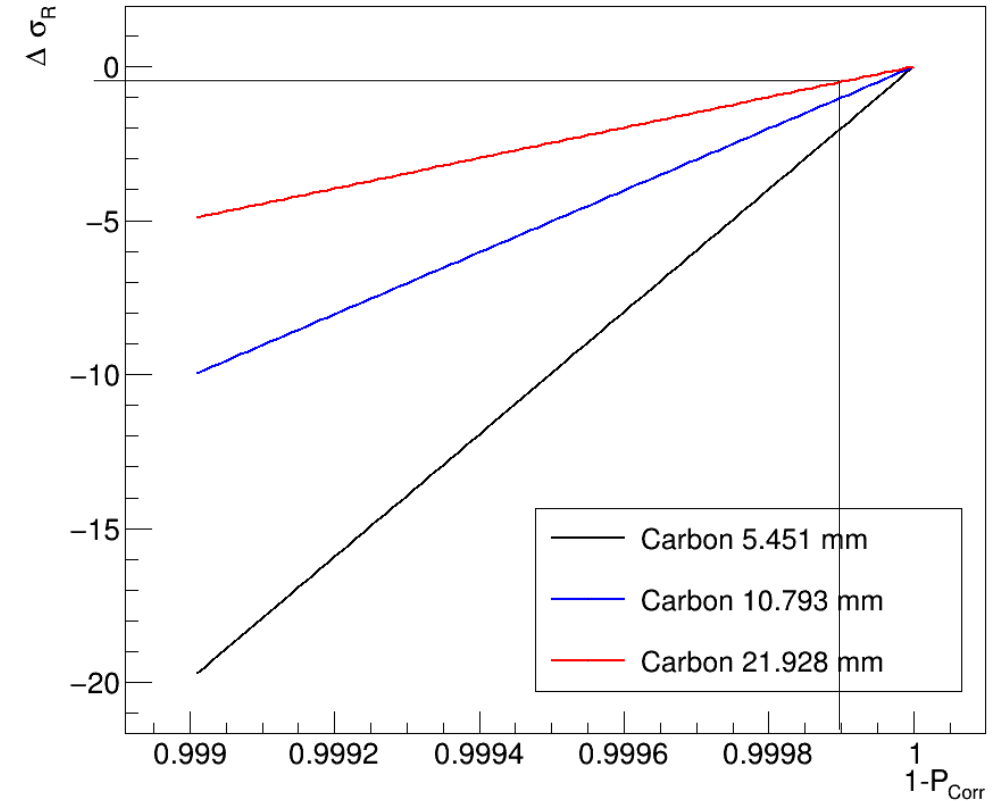
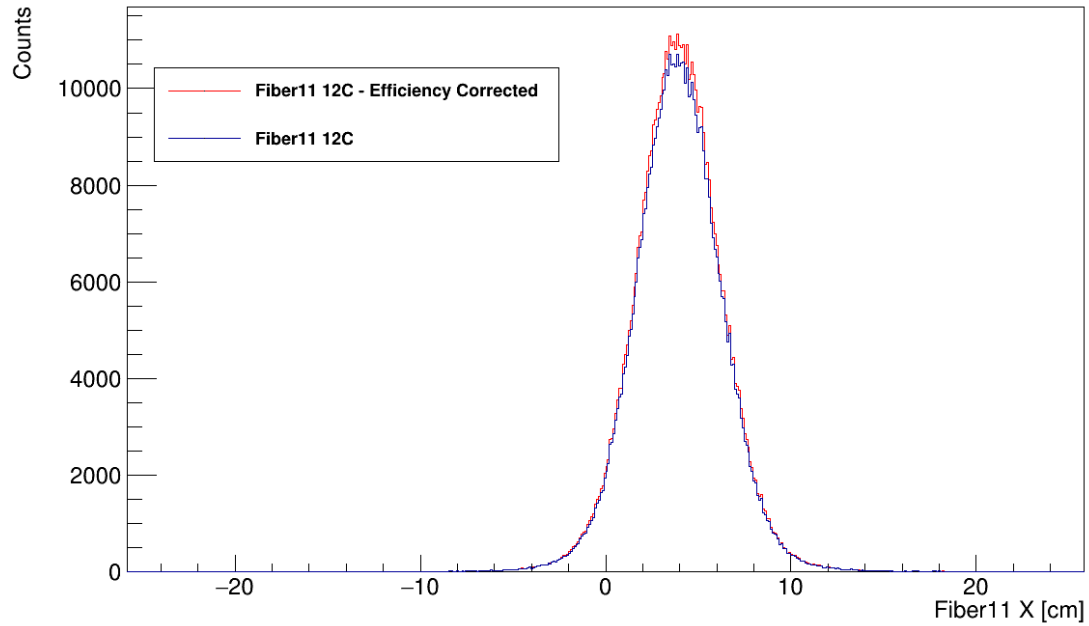
$$\varepsilon_{fib}(X) = \frac{Fib\ 11 \wedge Fiber\ 10}{Fib\ 11}$$





$$A_{Eff.Corr} = \frac{\int_{-25.8\text{ cm}}^{25.8\text{ cm}} g(x) \cdot \epsilon_{fib}(x) dx}{\int_{-25.8\text{ cm}}^{25.8\text{ cm}} S \cdot f(x) \cdot \epsilon_{fib}(x) dx}$$

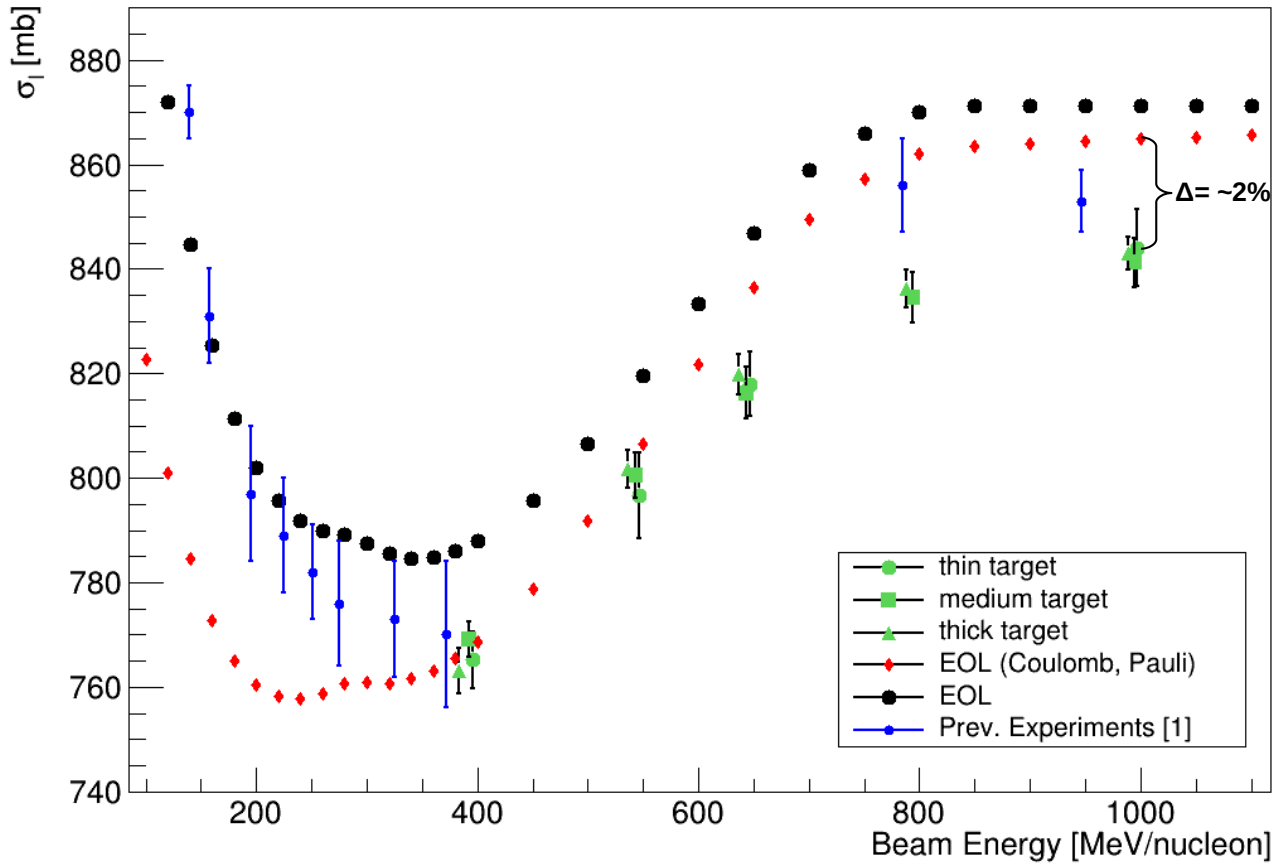




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$$A_{Eff.Corr} - A \approx 0.008\%$$

Deviation will be included in systematic uncertainty



## Status:

- Experimental results are in agreement with previous experiments at low energies
- Theory overestimates exp. results at high energies
- No evidence for underestimation in analysis
- Possible explanation in model?
  - Clustering in  $^{12}\text{C}$
  - Neutron Density
  - QCD effect?

[1] I. Tanihata et al. (Radioactive Nuclear Beams 1990), M. Takechi et al. (PRC – 79 2009), A. Ozawa et al. (Nuc. Phys. A – 691 2001)

EOL data: E.A. Teixeira, T. Aumann, C.A. Bertulani, B.V. Carlson (Eur. Phys. J. A – 58:205 2022)





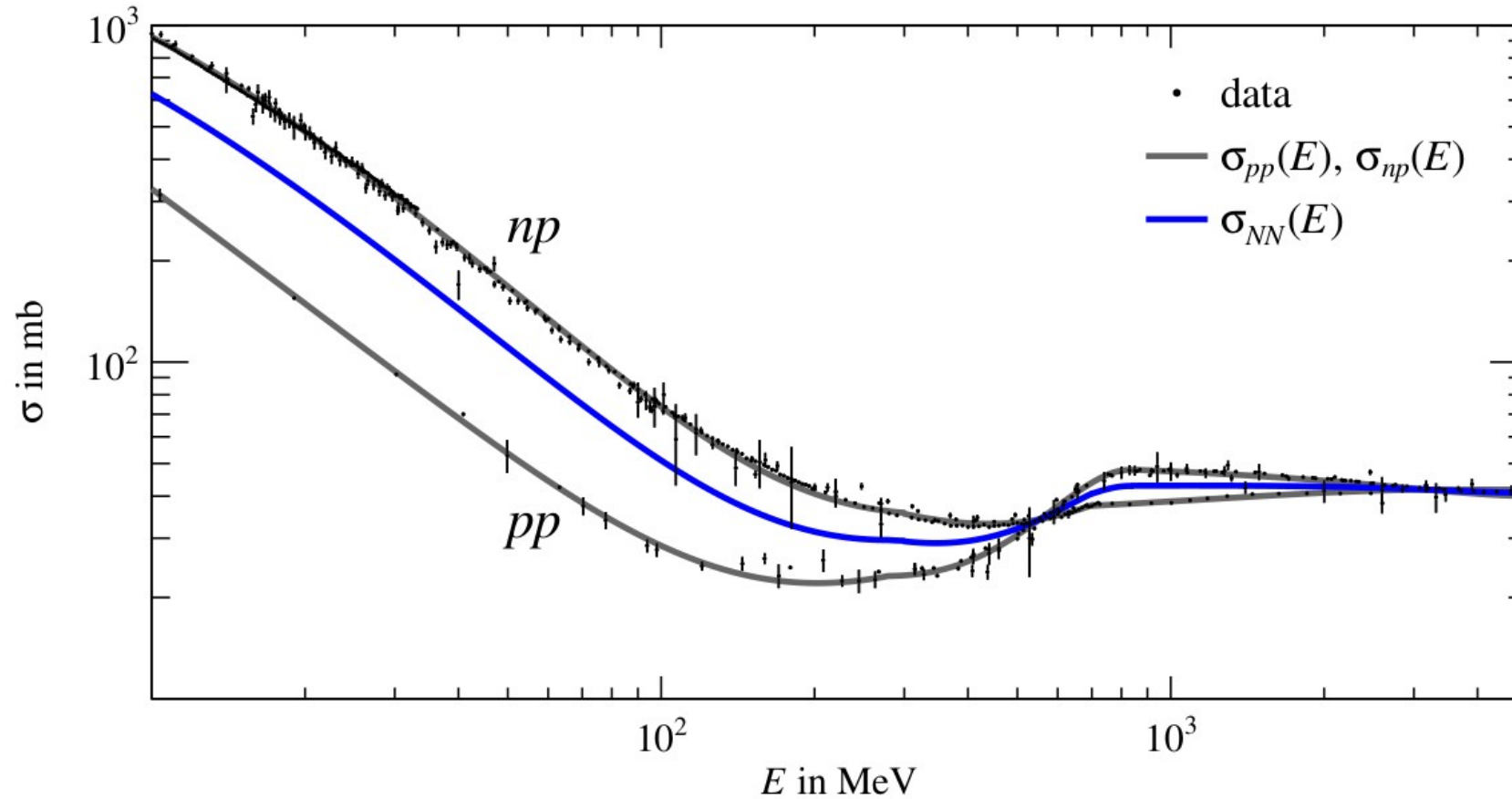
# Thank you!

## Paper Draft is (almost) ready

**CALIFA @ Technical University of Munich (TUM)**

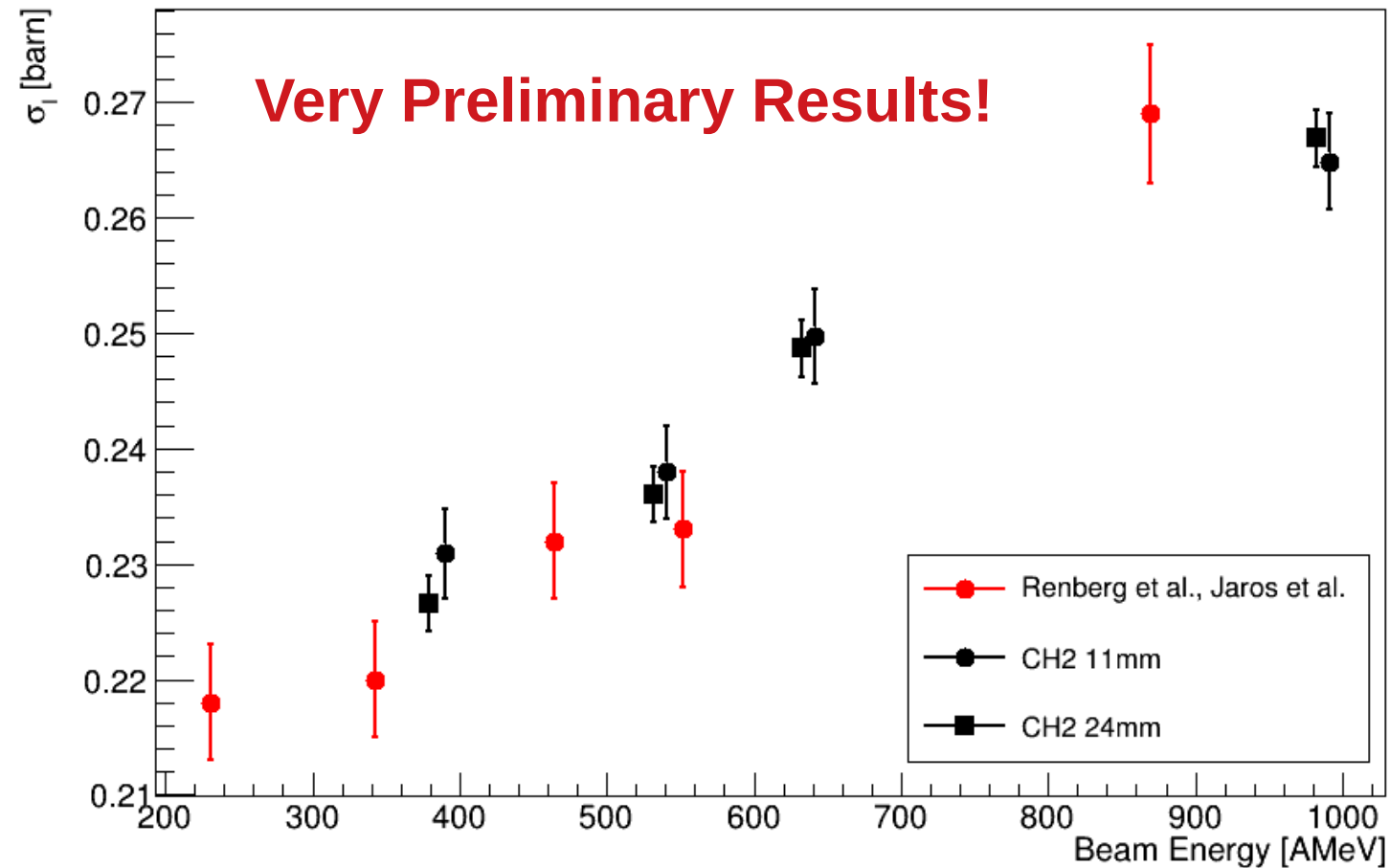
Roman Gernhäuser, Philipp Klenze, Lukas Ponnath, Tobias Jenegger





$$V_{OL}(\vec{b}) \propto \sigma_{NN} \cdot \int \rho_P(\vec{r}) \rho_T(\vec{r} - \vec{b})$$

## $^{12}\text{C} \rightarrow \text{p}$ Total Interaction Cross Section



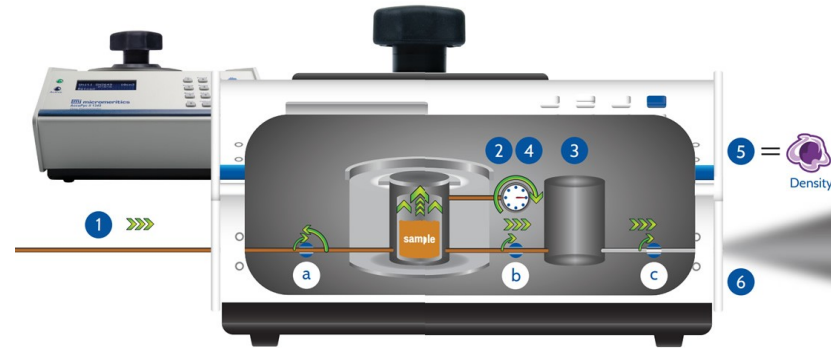
P. Renberg et al. Nuclear Physics A 183 (1972) 81-104



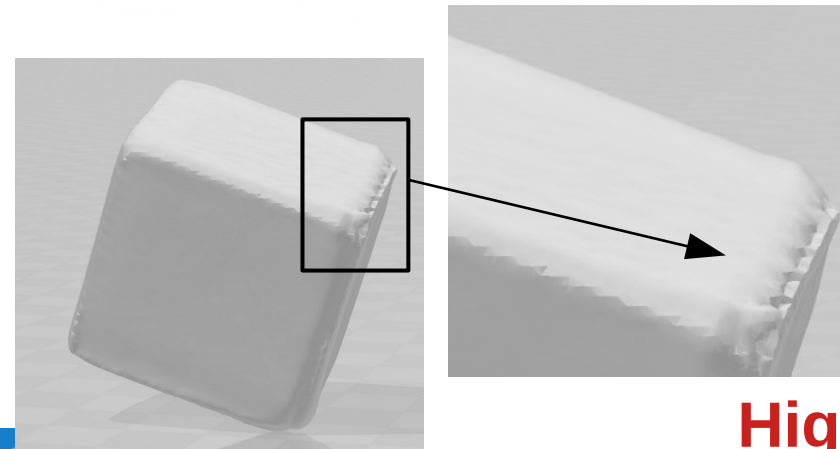
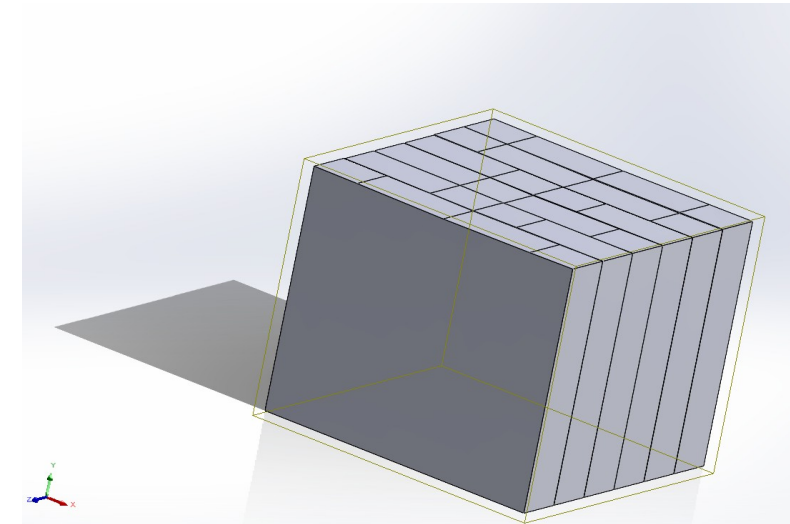
## 1. Photometry



## 2. Gas pycnometer



## 3. By Hand / CAD



**High uncertainties in all measurements!**

**But: A density  $< 1.84 \text{ g/cm}^3$  could be excluded**

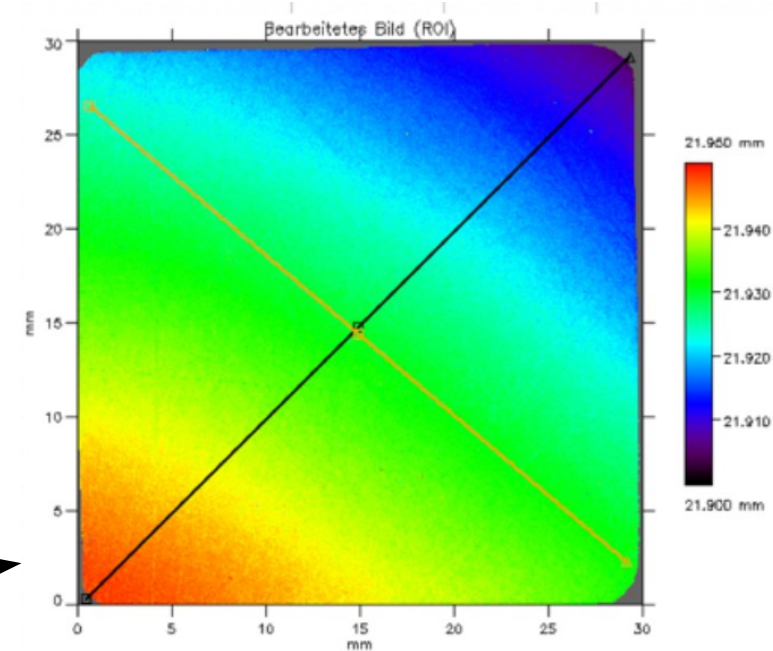
# Total Reaction Cross-Section

Number of target scattering centers:

$$N_t = \frac{\rho_t \cdot d_t \cdot N_A}{A_t}$$

where

- $\rho_t$  is the volume density of the target (1.84 g/cm<sup>3</sup>)
- $d_t$  is the target thickness
- $N_A$  is Avogadro's constant (6.02214\*10<sup>23</sup> mol<sup>-1</sup>)
- $A_t$  is the molar mass of the target (12.0107 u)



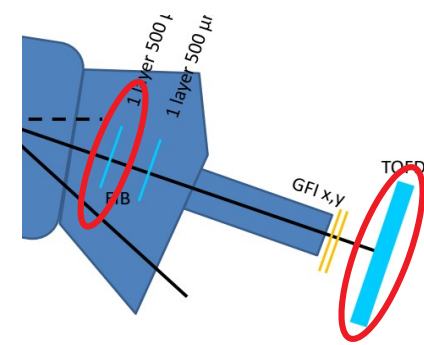
Dt [cm]	Nt
0.5451	5.50334*10 <sup>23</sup>
1.0793	1.09904*10 <sup>24</sup>
2.1928	2.120248*10 <sup>25</sup>

$$\sigma_R = -\frac{1}{N_t} \ln \left( \frac{N_2^i / N_1^i}{N_2^o / N_1^o} \right)$$

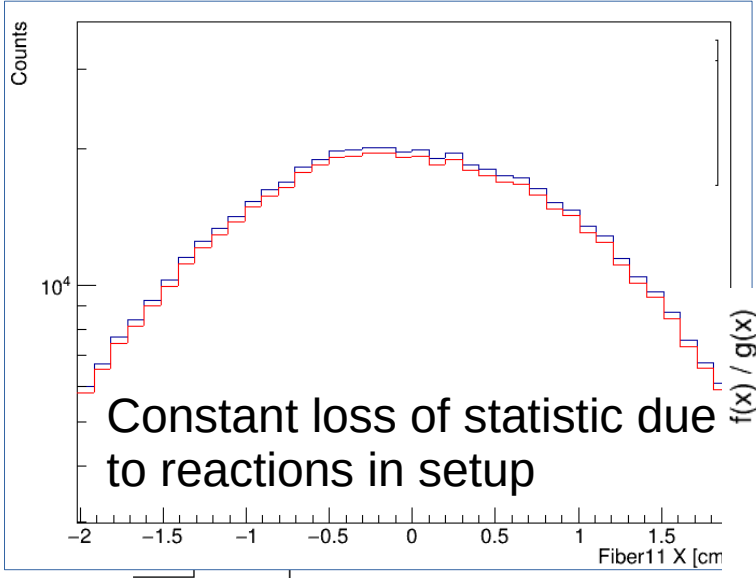
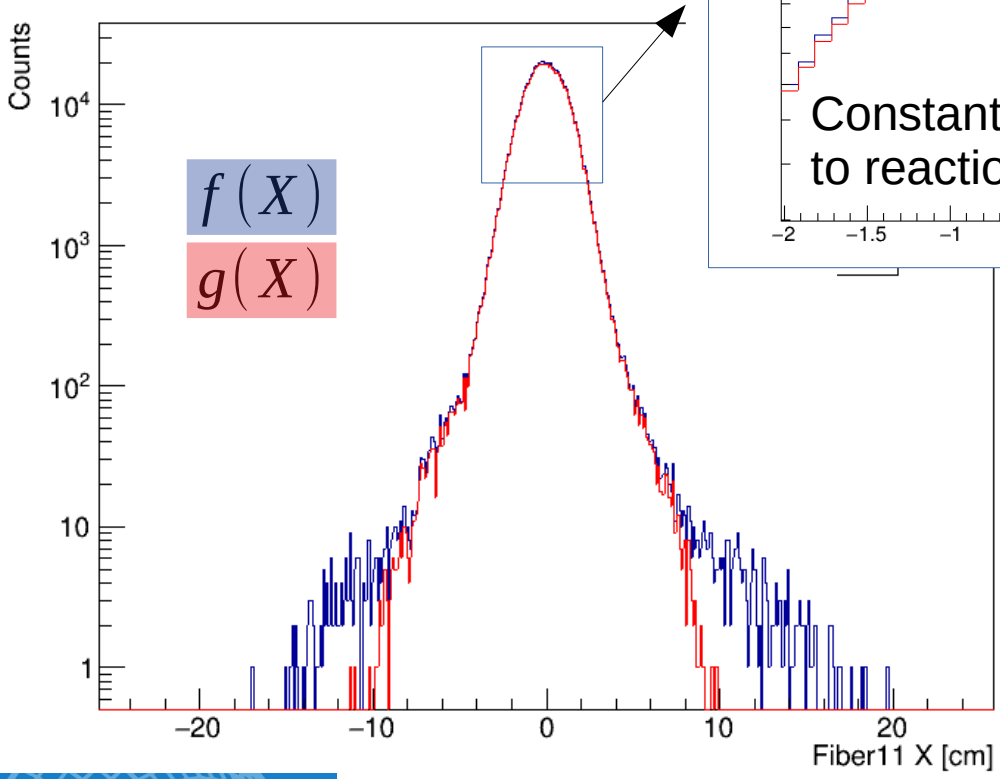


# Total Reaction Cross-Section

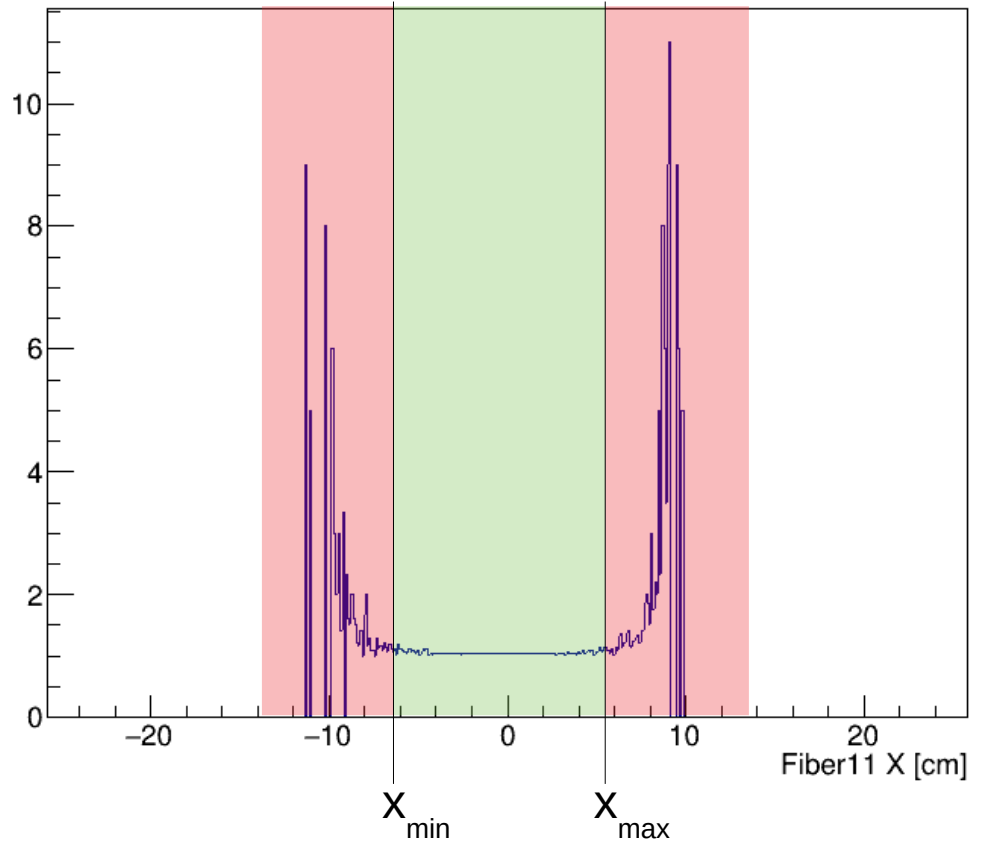
## Acceptance-Correction



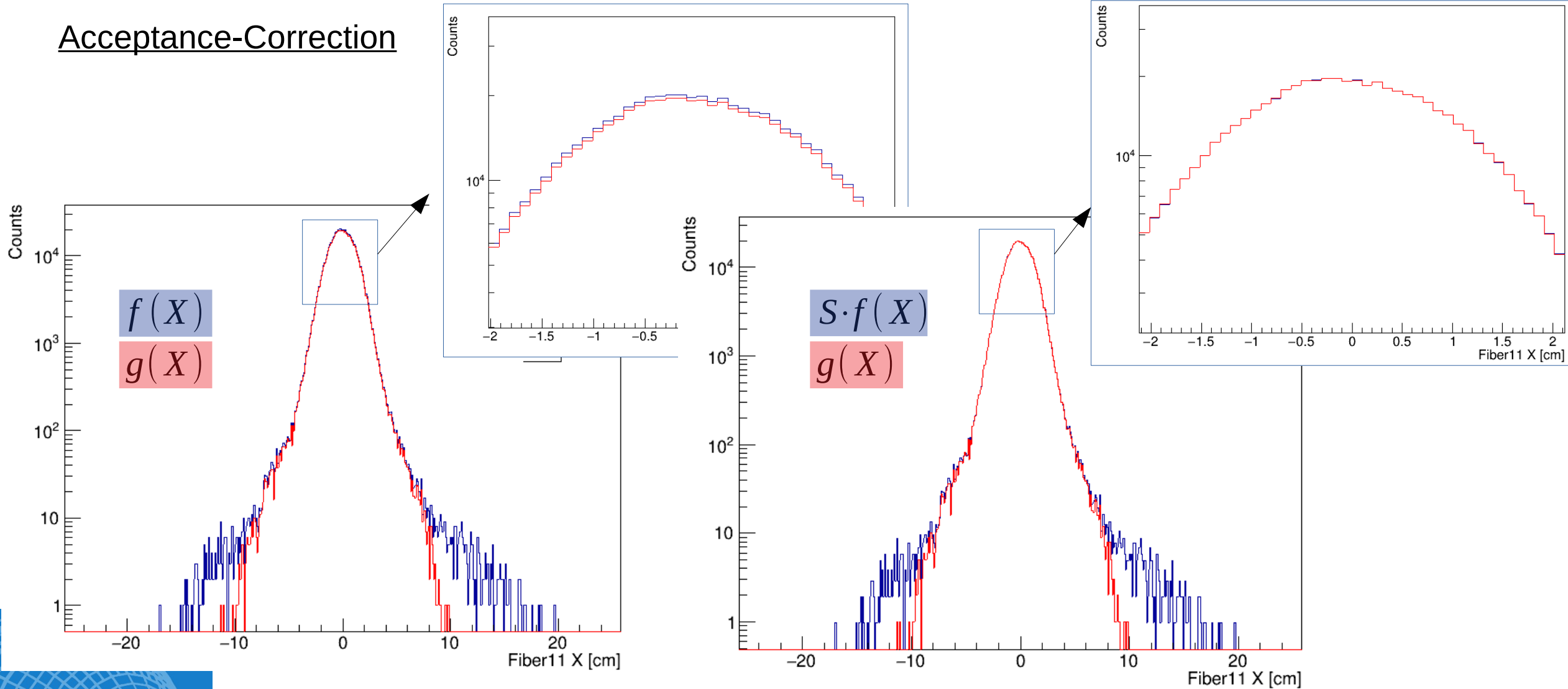
Dividing both distribution



$$S = \frac{\int_{x_{min}}^{x_{max}} g(x)}{\int_{x_{min}}^{x_{max}} f(x)}$$



Acceptance-Correction





# Measurement Concept

Surviving-Probability: 
$$P_{surv.} = \frac{N_2}{N_1} = e^{-N_t \cdot \sigma_R}$$

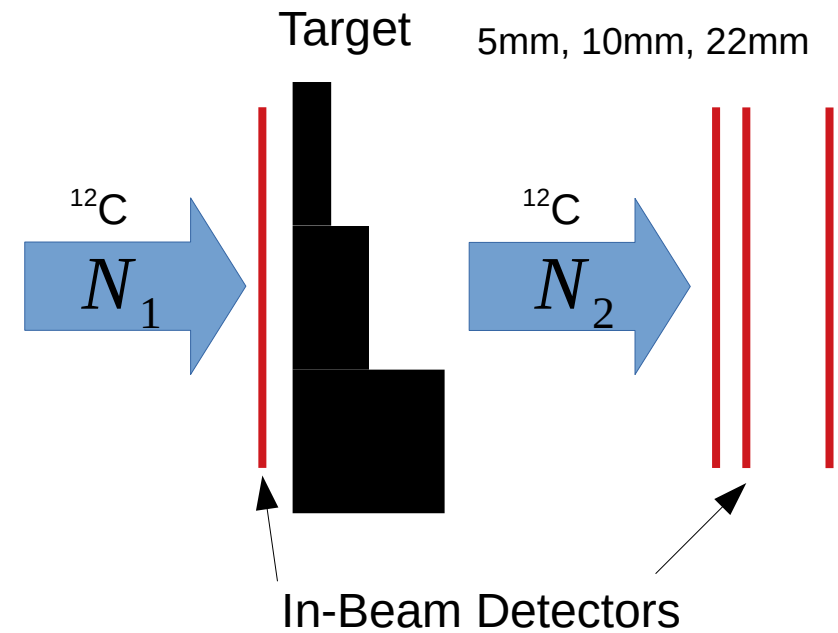
Exclude reactions in Setup:

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Transmission method:

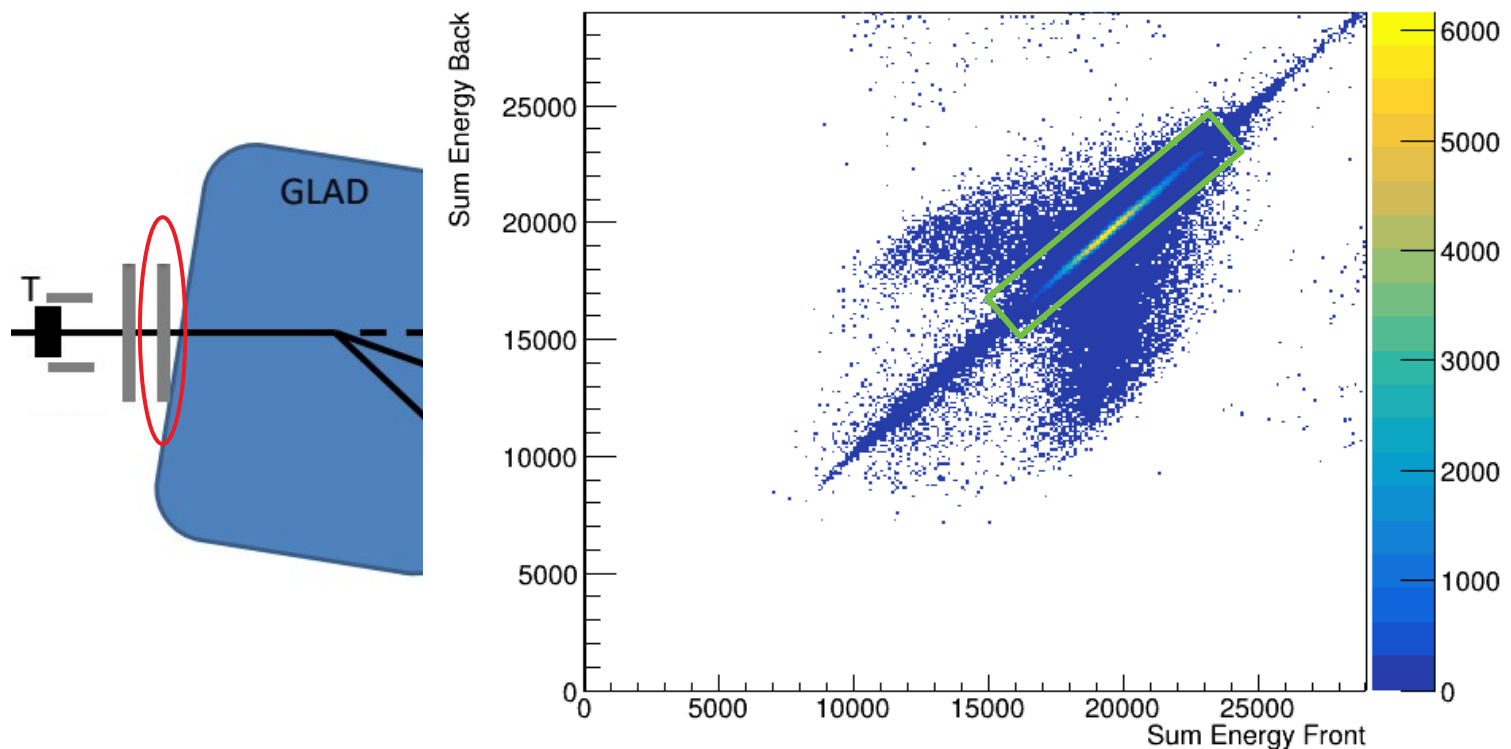
$$\sigma_R = -\frac{1}{N_t} \ln \left( \frac{N_2^i / N_1^i}{N_2^o / N_1^o} \right)$$

Challenge: Time- & Rate-depended Efficiency & geometrical Acceptance of Detectors



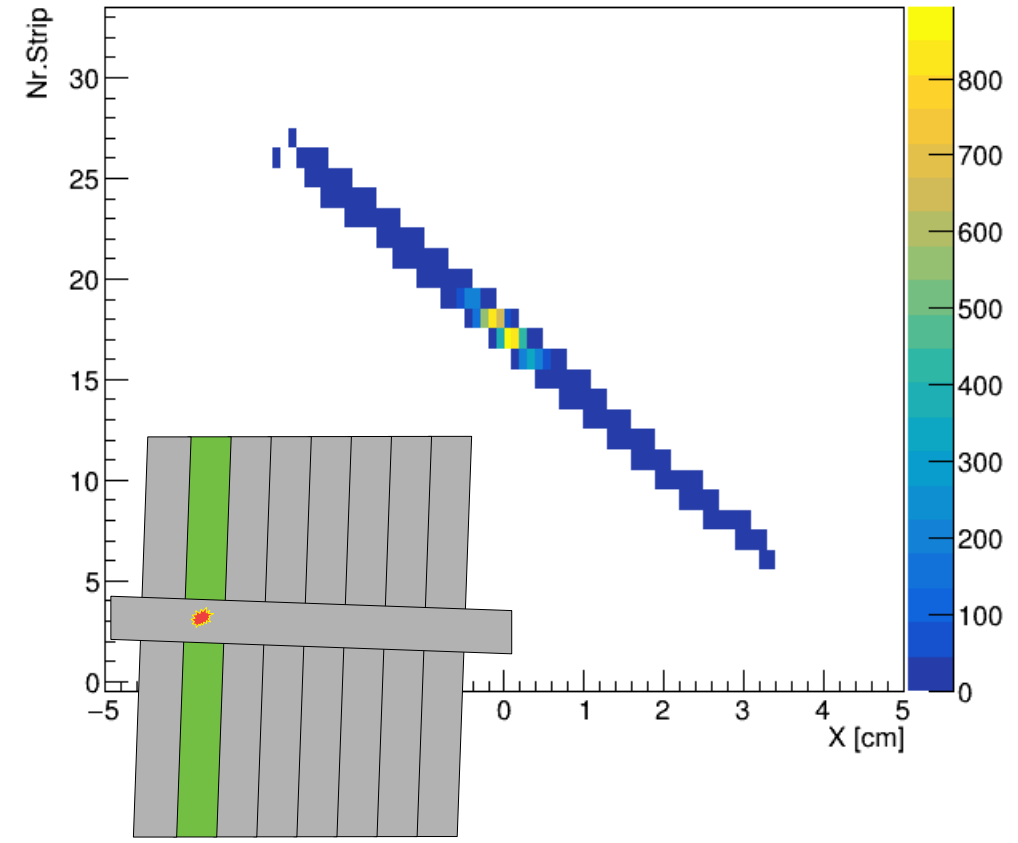
- $N_t$  is a target specific constant (density, Thickness)
- $N_1$ , number of incident  $^{12}\text{C}$  nuclei (stable beam, Event-Selection)
- $N_2$ , number of non-reacting  $^{12}\text{C}$  nuclei, identified after the target (that's our big challenge)

## PSP Detector - X-Position



- Multiplicity=1 on Front- & Back-Layer
- Same Energy (Q=6) Deposition in both Layers

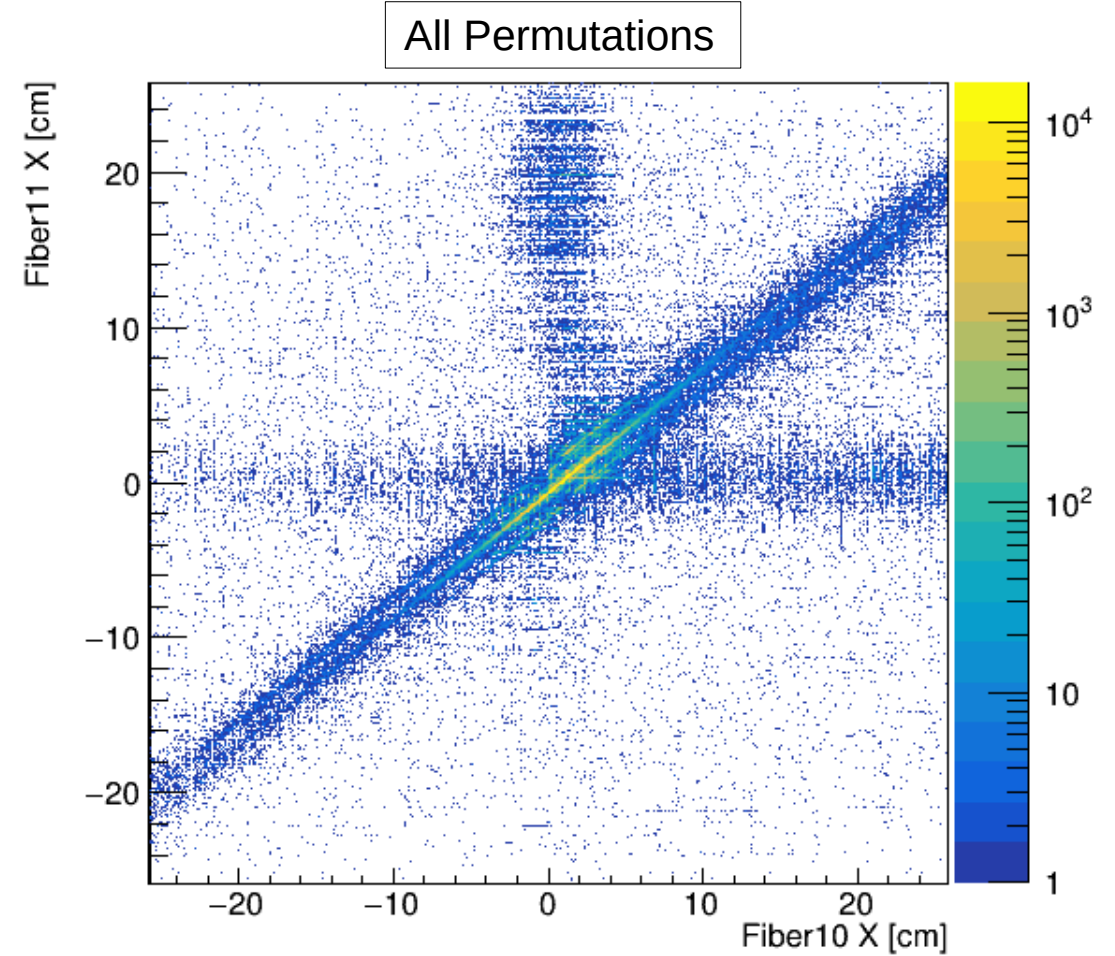
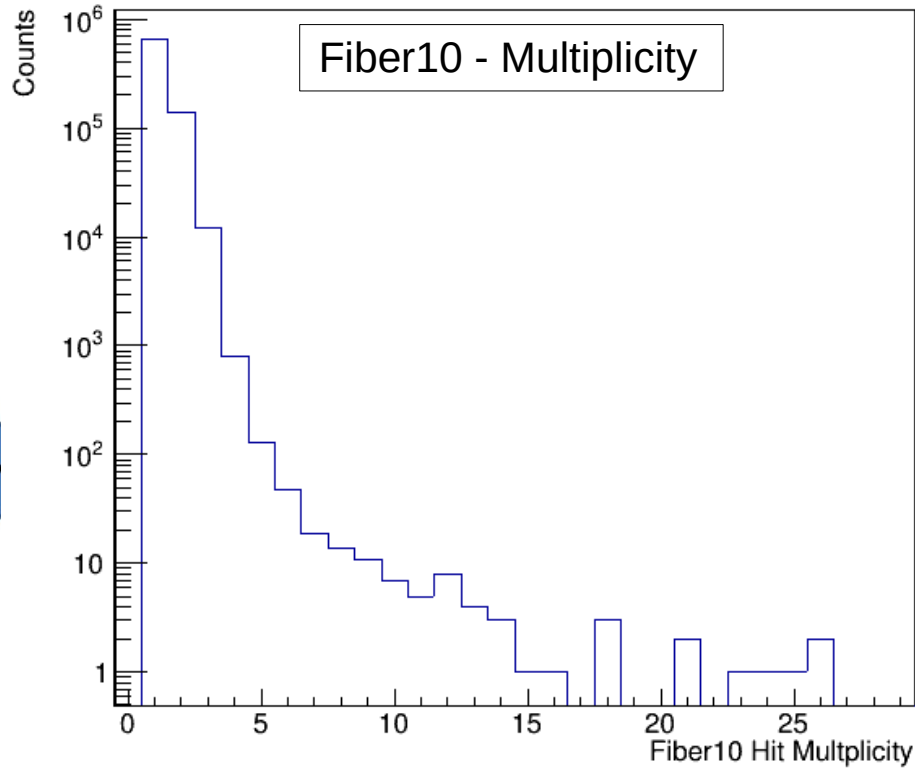
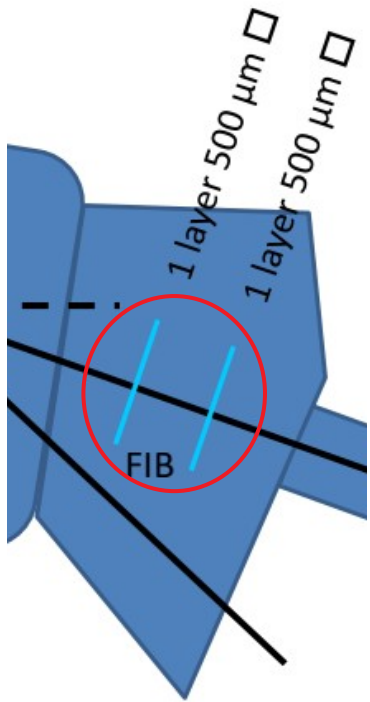
PSP3 XPosition Check



We can cross-check the x-position with the Strip-Nr. of the Front-Layer



## Fiber Detector - X-Position



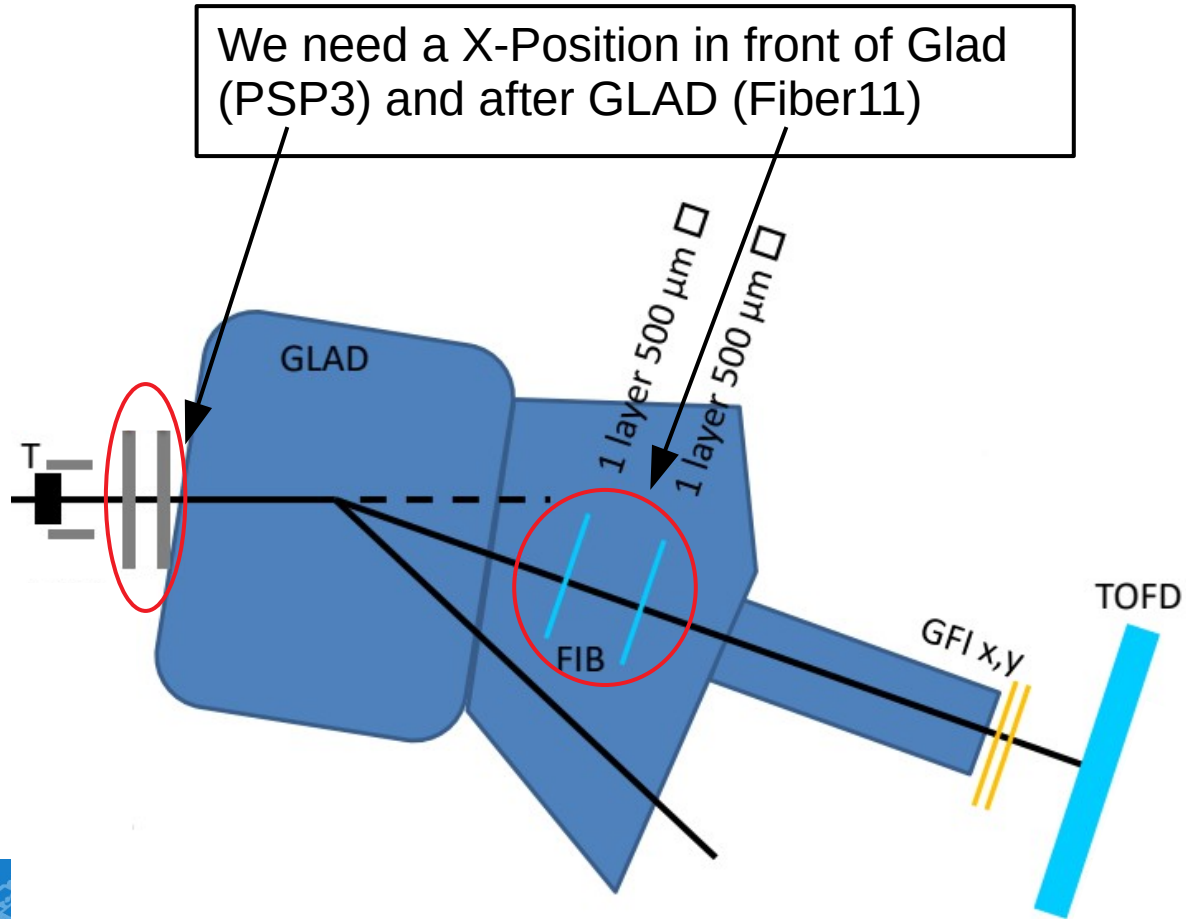
Problem: High Multiplicity due to light cross-talk  
How can we find the correct Hit / the correct X-Position?





## Isotope-Correction

We need a X-Position in front of Glad (PSP3) and after GLAD (Fiber11)



Isotopes with different mass ( $A$ ) have a different bending-radius ( $\rho$ ) in a const. Magnetic field ( $B$ ).

$$B\rho = \frac{A}{q} \cdot c \cdot \gamma \cdot \beta$$

