



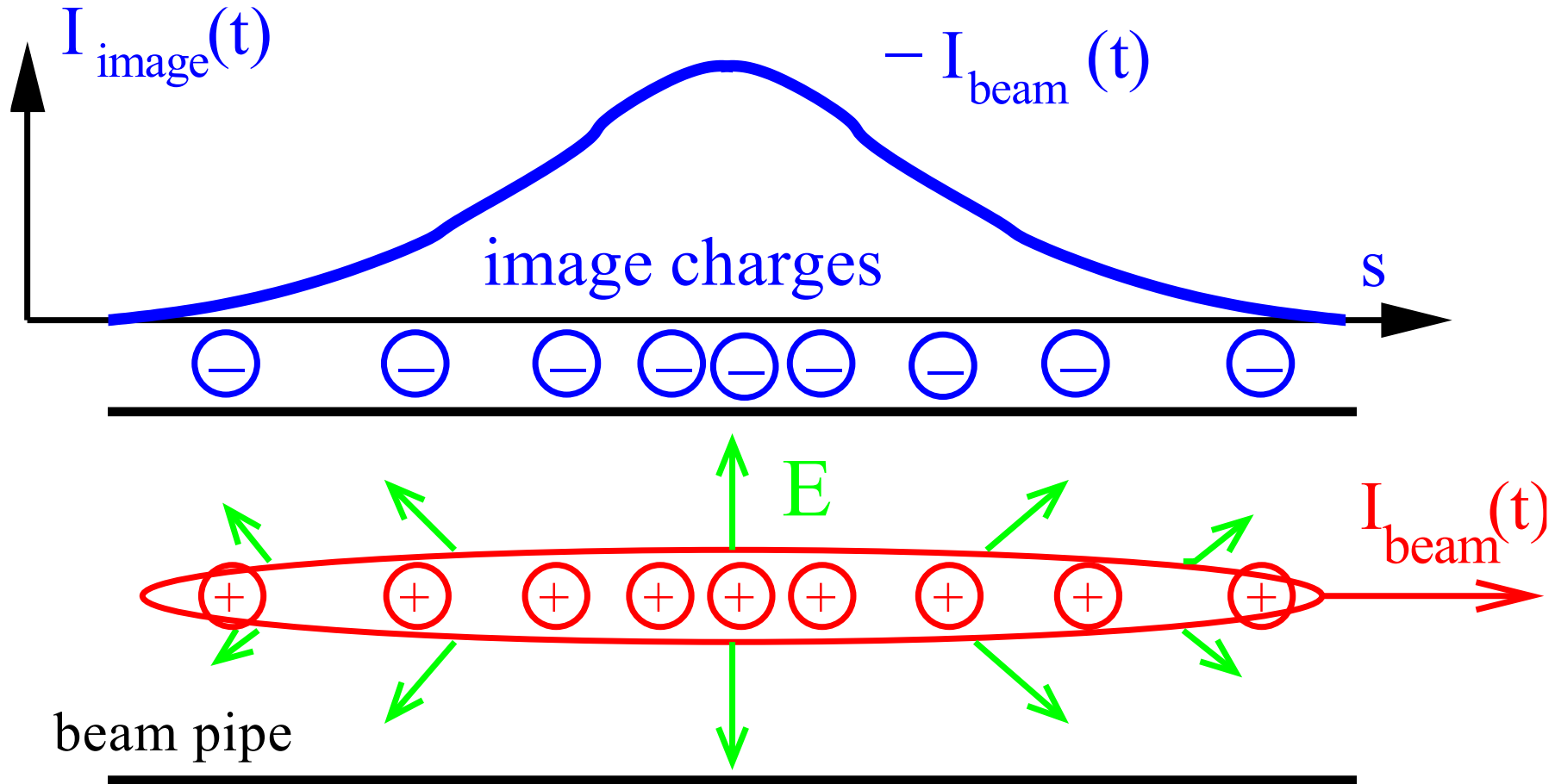
LIGHT Collaboration Meeting 2023
Longitudinal Beam Profile Measurement Methods

Outline

- Pick-Ups
 - Default Design
 - General Working Principle
 - Use Cases
- GHz Transition Radiation Monitor
 - General Properties of Transition Radiation
 - Basic Principle
 - Measurement Results at GSI X2
- Fast Faraday Cups
 - Axial vs. Radial Coupled FFC

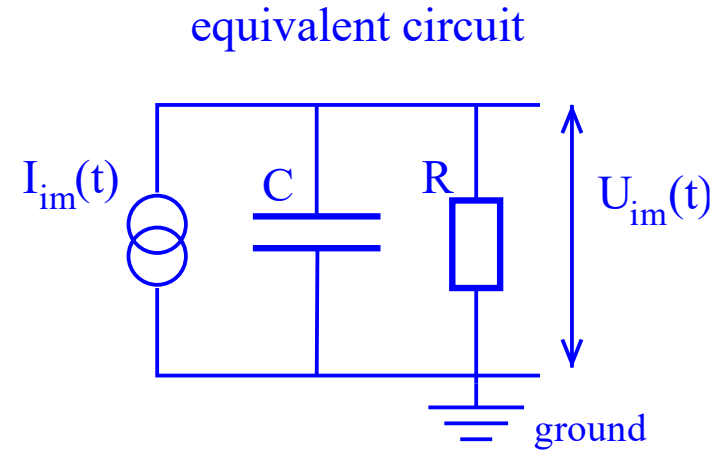
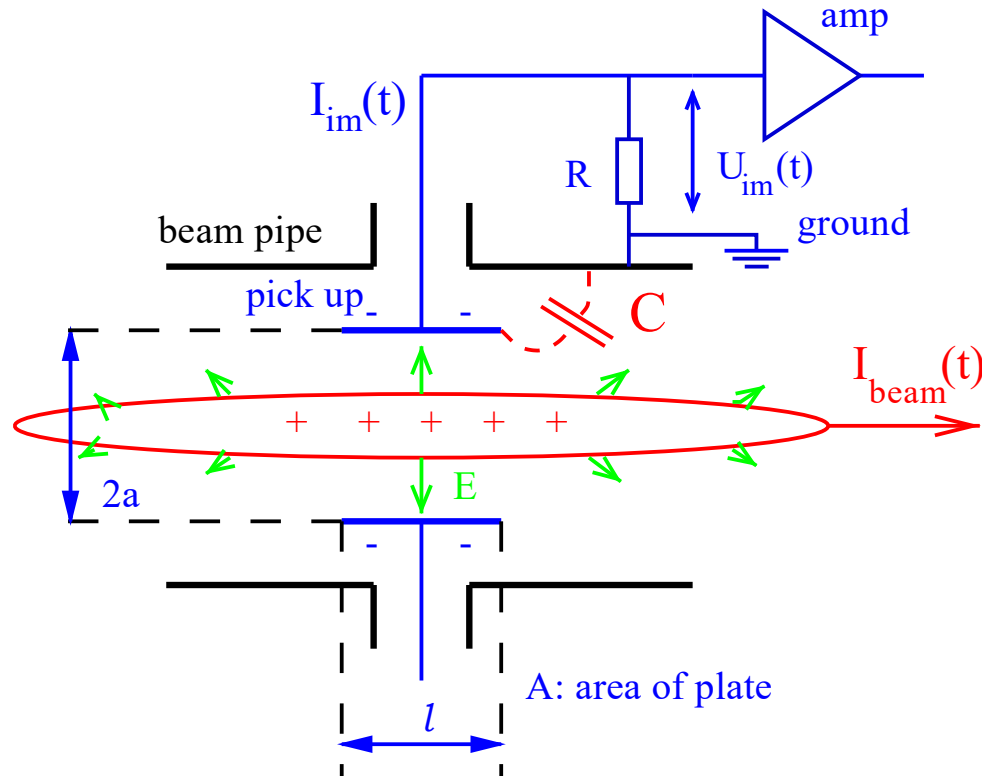
Pick-Ups

Pick-Ups - General Working Principle



[1]

Pick-Ups - General Working Principle



$$I_{im}(t) \equiv \frac{dQ_{im}}{dt} = -\frac{A}{2\pi a l} \cdot \frac{dQ_{beam}(t)}{dt}$$

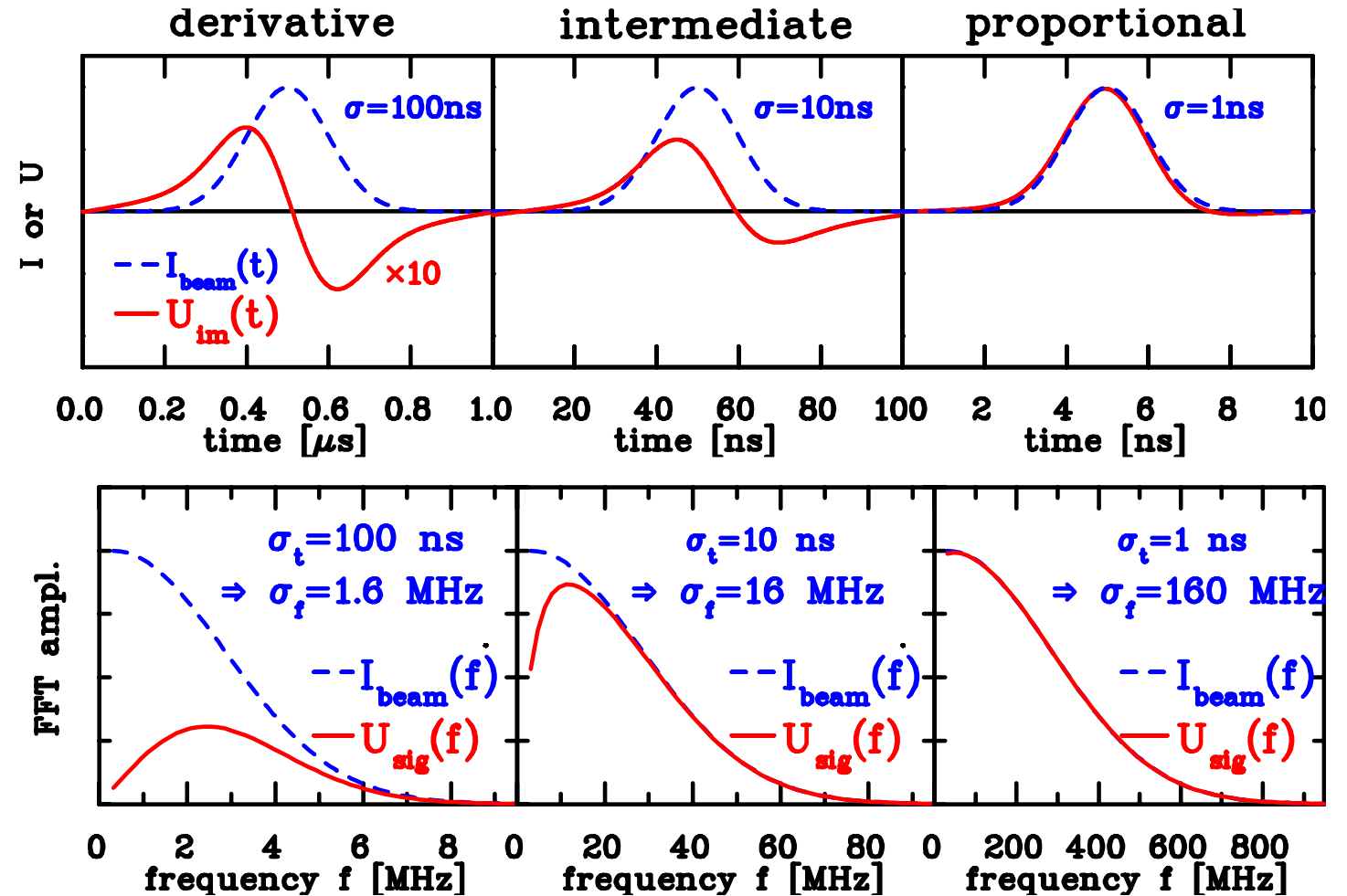
[1]

Pick-Ups - General Working Principle

$$\begin{aligned}
 I_{im}(t) &\equiv \frac{dQ_{im}}{dt} = -\frac{A}{2\pi a l} \cdot \frac{dQ_{beam}(t)}{dt} \\
 &= \frac{1}{\beta c} \cdot \frac{A}{2\pi a} \cdot i\omega I_{beam}
 \end{aligned}$$

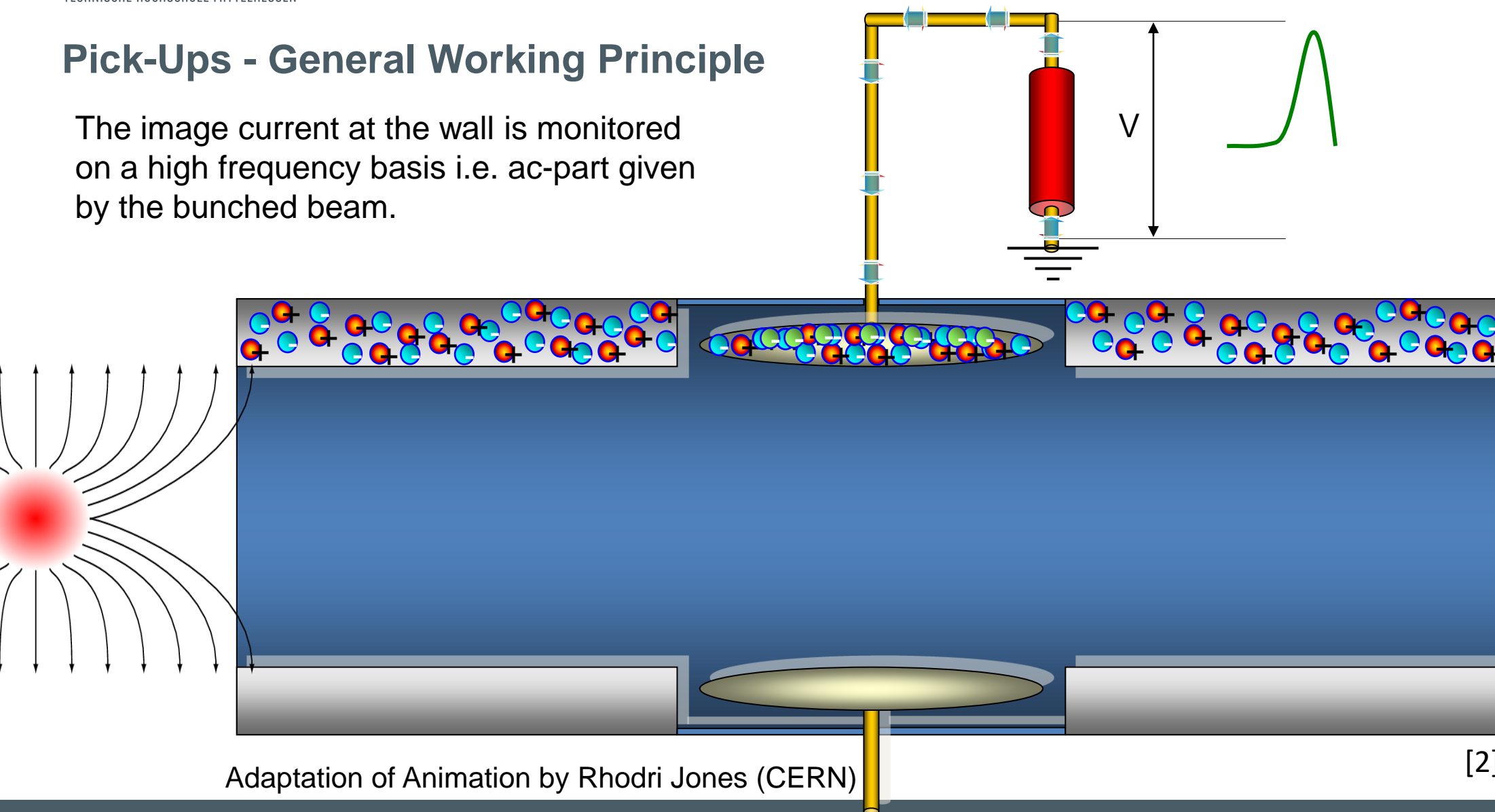
$$\begin{aligned}
 U_{im}(\omega) &= R \cdot I_{im}(\omega) = Z_t(\omega, \beta) \cdot I_{beam}(\omega) \\
 &= \underbrace{\frac{1}{\beta c} \frac{1}{C} \frac{A}{2\pi a} \frac{i\omega RC}{1 + i\omega RC}}_{\text{Transfer Impedance}} I_{beam}(\omega)
 \end{aligned}$$

[1]



Pick-Ups - General Working Principle

The image current at the wall is monitored on a high frequency basis i.e. ac-part given by the bunched beam.



Adaptation of Animation by Rhodri Jones (CERN)

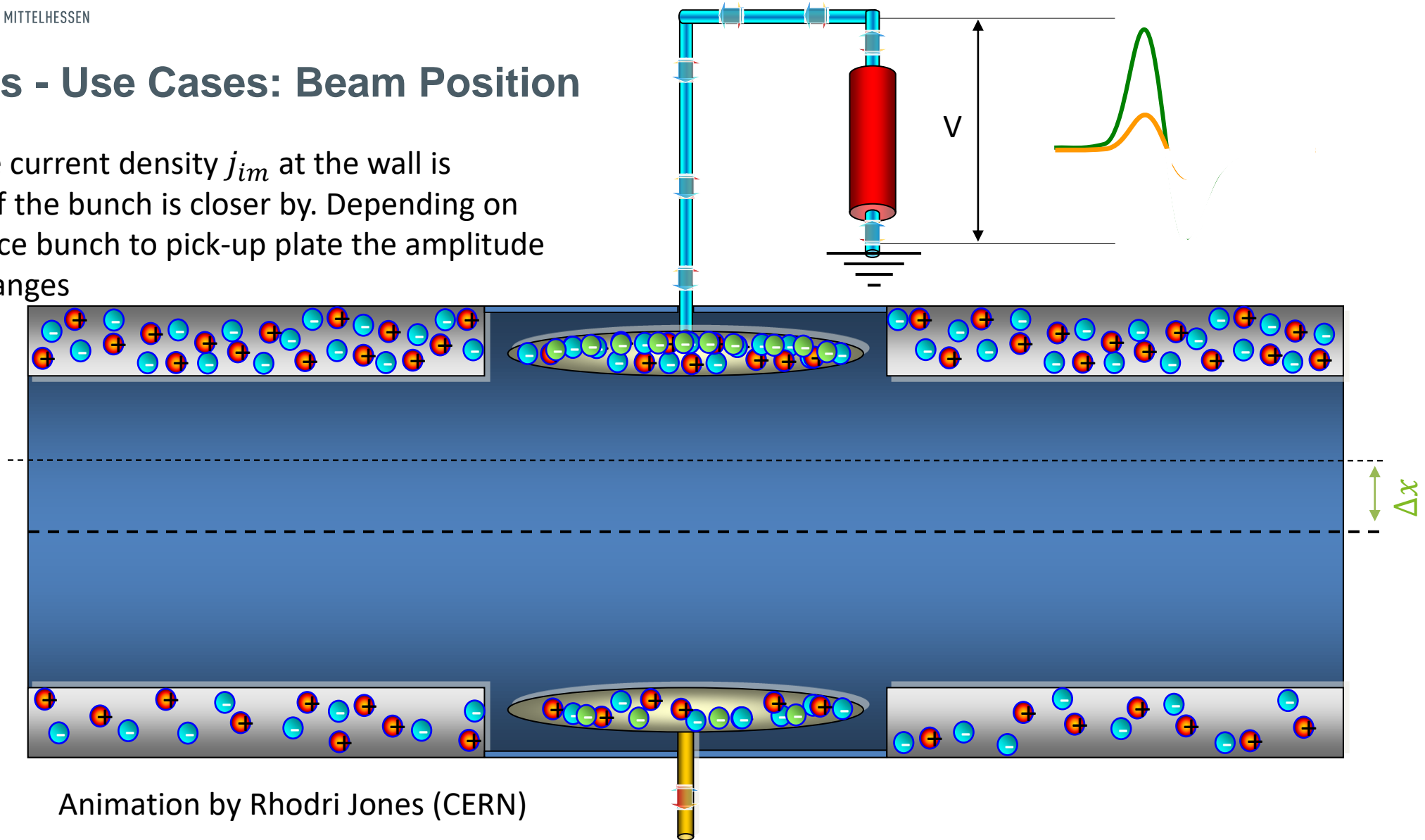
[2]

Pick-Ups - Use Cases

- Pick-Ups can be used for many purposes
- For each purpose there are specialized designs
- Some use cases are:
 - Beam Position
 - Beam Velocity (ToF)
 - Bunch Arrival (BAM)
 - Bunch Shape
 - Total Charge

Pick-Ups - Use Cases: Beam Position

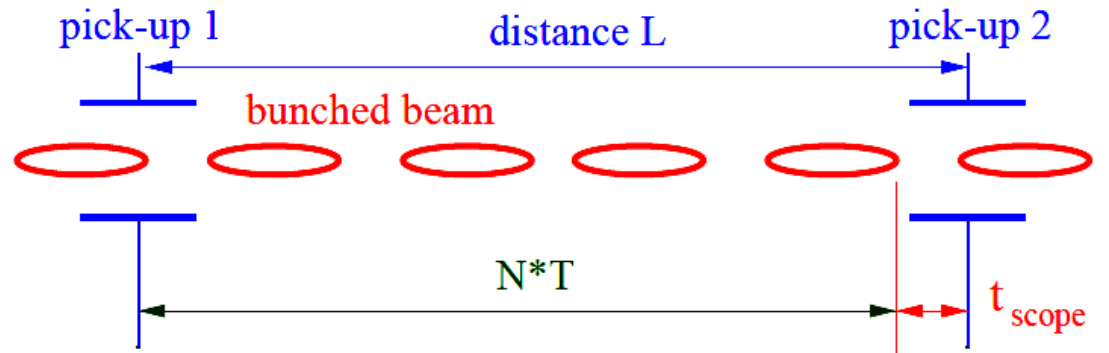
The image current density j_{im} at the wall is stronger, if the bunch is closer by. Depending on the distance bunch to pick-up plate the amplitude of U_{im} changes



Animation by Rhodri Jones (CERN)

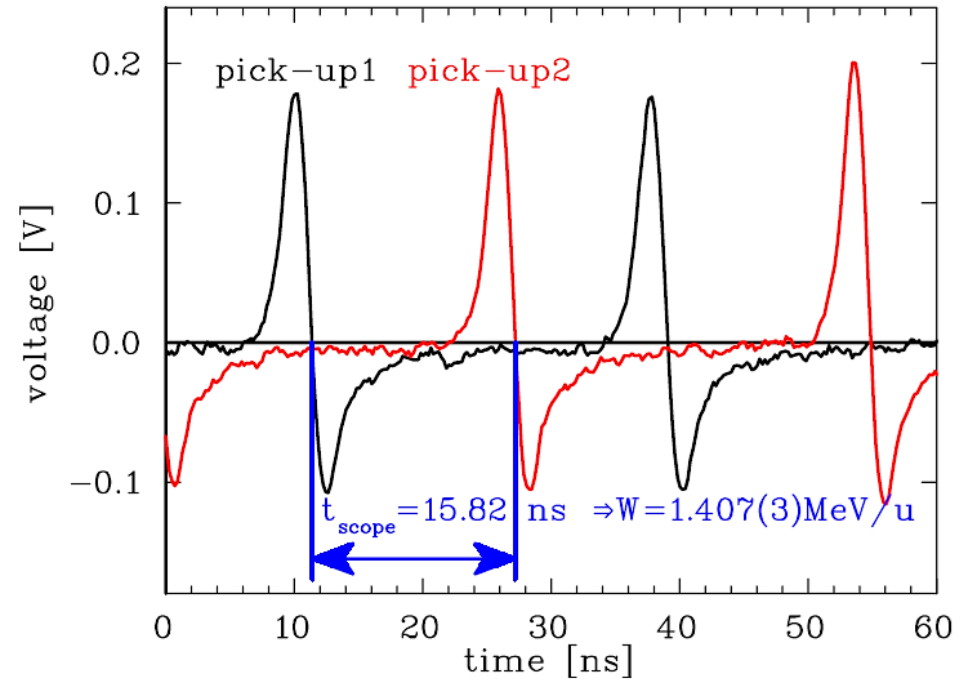
Pick-Ups - Use Cases: Beam Velocity (ToF)

- RF-Frequency $f_{rf} \Leftrightarrow$ Period T
- Known number of bunches in between N
- $$\beta c = \frac{L}{NT + t_{scope}}$$



Example: ToF at proton LINACS:

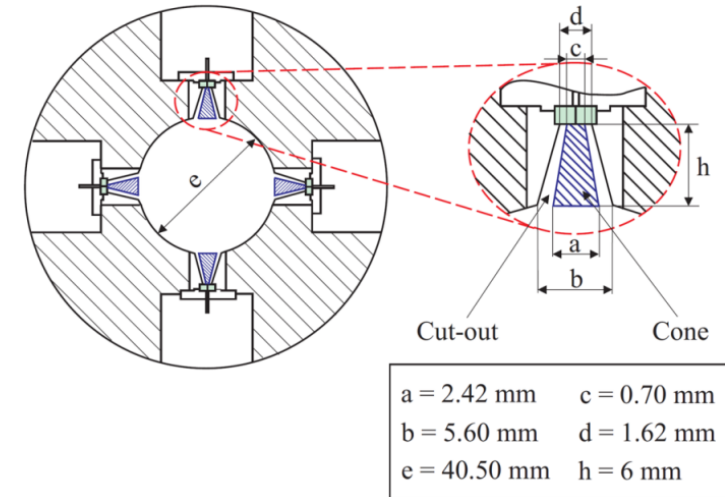
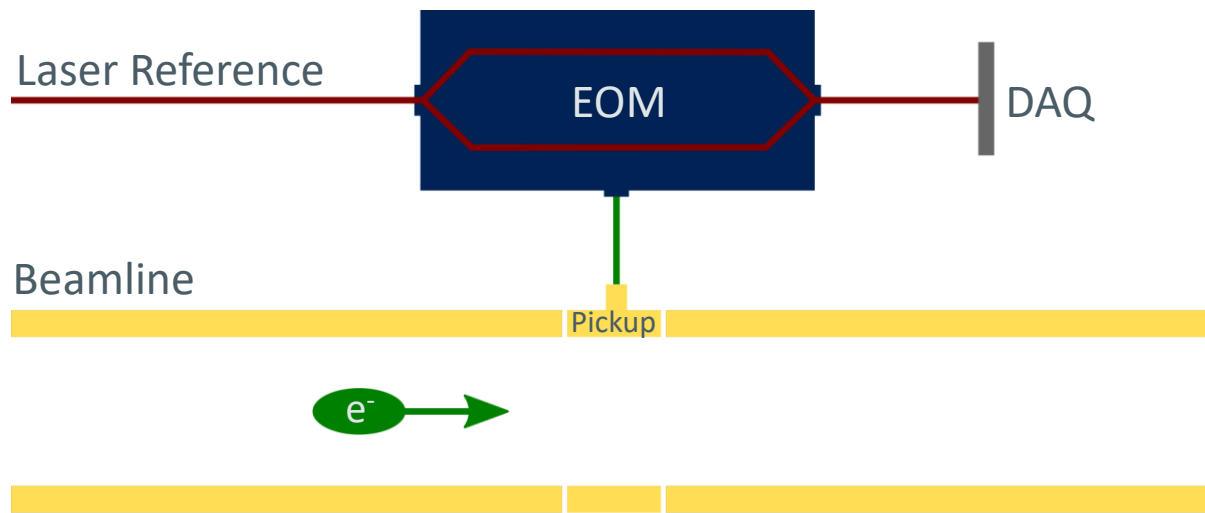
- Estimated kinetic energy 1.4MeV/u
 - $t_{scope} = 15.82(5)$ ns
 - $f_{rf} = 36.136$ MHz $\Leftrightarrow T = 27.673$ ns
 - $L = 1.629(1)$ m
 - $N = 3$
- $\Rightarrow \beta = 0.05497(7) \Leftrightarrow E_{kin} = 1.407(3)$ MeV/u



[1]

Pick-Ups - Use Cases: Bunch Arrival Monitor (BAM)

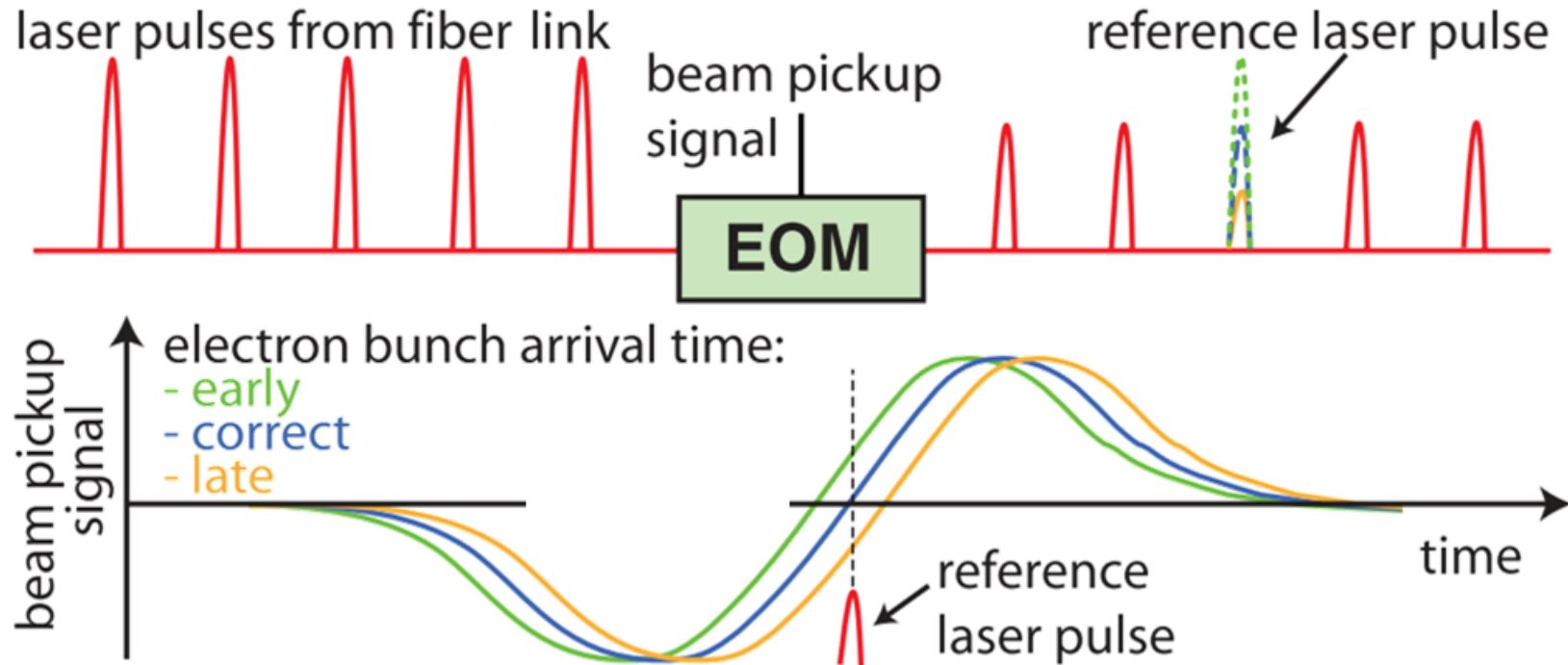
- Button pickups
 - Transient electric fields → voltage signal
- (Main) laser oscillator
 - Pulsed laser reference
- Electro-optical modulator
 - Laser amplitude modulated according to voltage signal
- Data acquisition
 - Decoding the timing information



Pickup-Geometry [10]

By B. Scheible

Pick-Ups - Use Cases: Bunch Arrival Monitor (BAM)



by Löhl et al. [9]

Pick-Ups - Use Cases: Bunch Shape

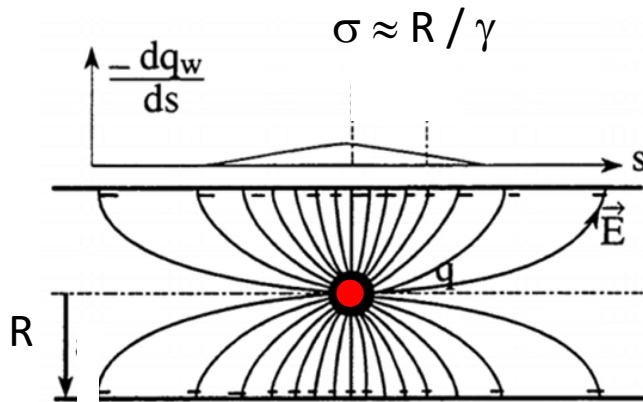
- $\beta = 1$ Pick-Ups may be used for bunch shape measurements
- $\beta < 1$ E-field is significantly modeled smearing out the actual longitudinal shape

- Transversal E_{\perp} lab.-frame of a point charge

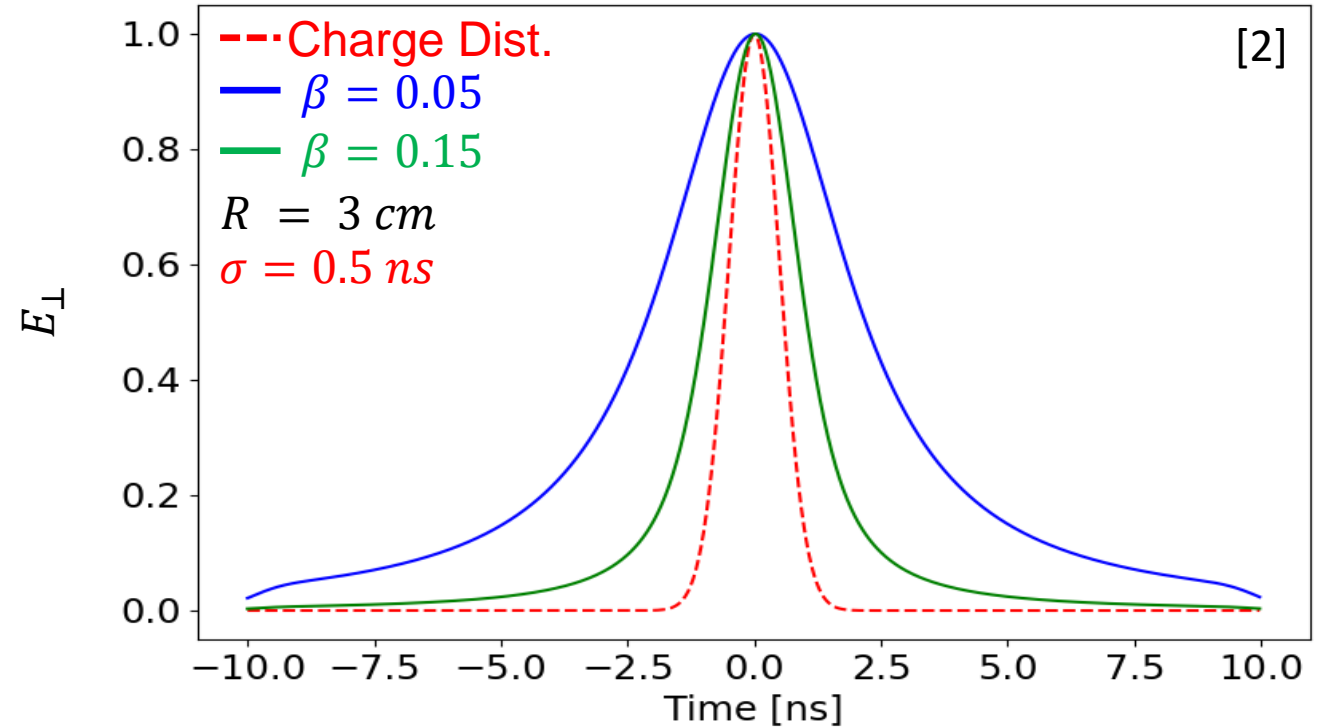
$$E_{\perp}(t) = \frac{e}{4\pi\epsilon_0} \frac{\gamma R}{[R^2 + (\gamma\beta ct)^2]^{3/2}}$$

- Longitudinal E_{\parallel} lab. frame of a point charge

$$E_{\parallel}(t) = -\frac{e}{4\pi\epsilon_0} \frac{\gamma\beta ct}{[R^2 + (\gamma\beta ct)^2]^{3/2}}$$



[1]



For $\beta < 1 \rightarrow$ Field distribution is not the same as charge distribution. Effect visible for shorter bunches $<$ few ns

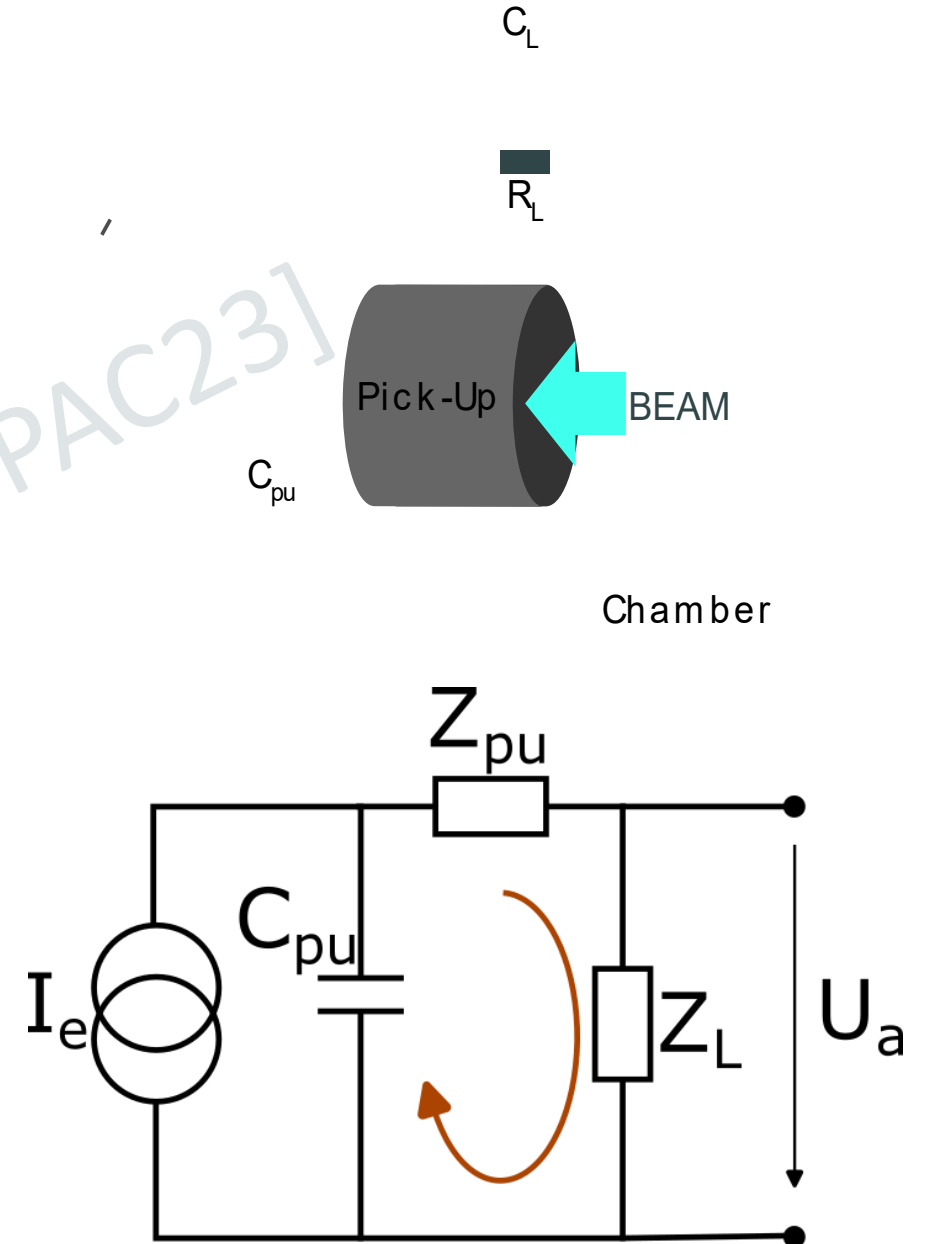
Pick-Ups - Use Cases: Total Charge

- Total charge $Q_b = \int_V \rho dV = \frac{l}{\beta c} I_b(t)$
- Mirror current $I_e(t) = \frac{l}{\beta c} \frac{d}{dt} I_b(t) \equiv \frac{l}{\beta c} i\omega I_b(\omega)$

$$I_e(\omega) = \underbrace{\frac{1+i\omega C_{pu}[Z_L+Z_{pu}]}{Z_L}}_{\text{transfer function}} U_a$$
- The total charge can be calculated by measuring U_a

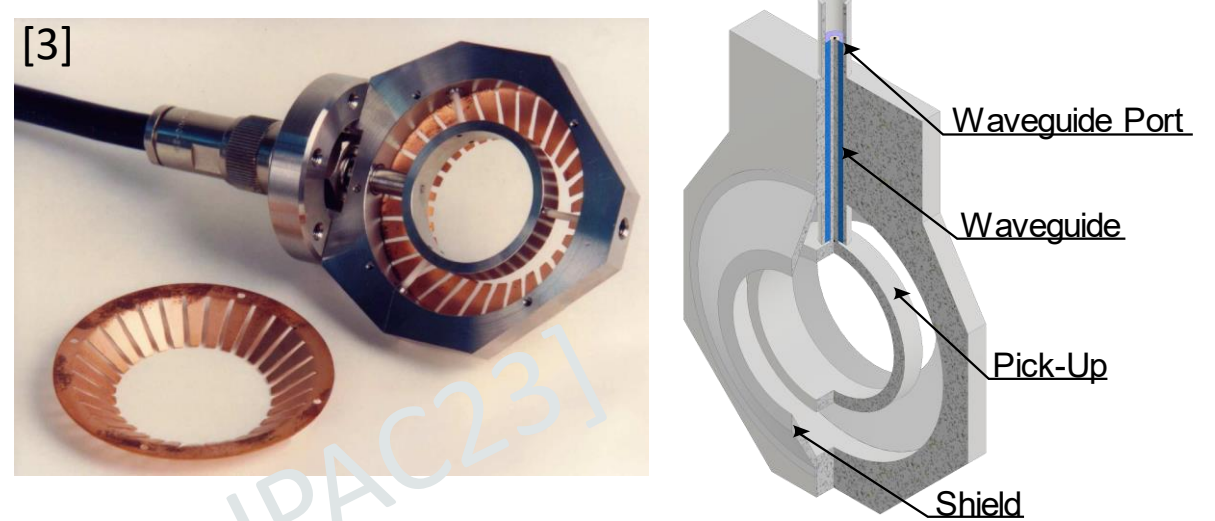
$$Q_b = \int_t I_b(t) dt$$

$$= \frac{\beta c}{l} \left(\frac{1}{Z_L} \int_t \int_\tau U_a(\tau) d\tau dt + C_{pu} \frac{Z_L+Z_{pu}}{Z_L} \int_t U_a(t) dt \right)$$
- Two cases arise for the calculation of Q_b
 - Low impedance Z_L
 - High impedance Z_L

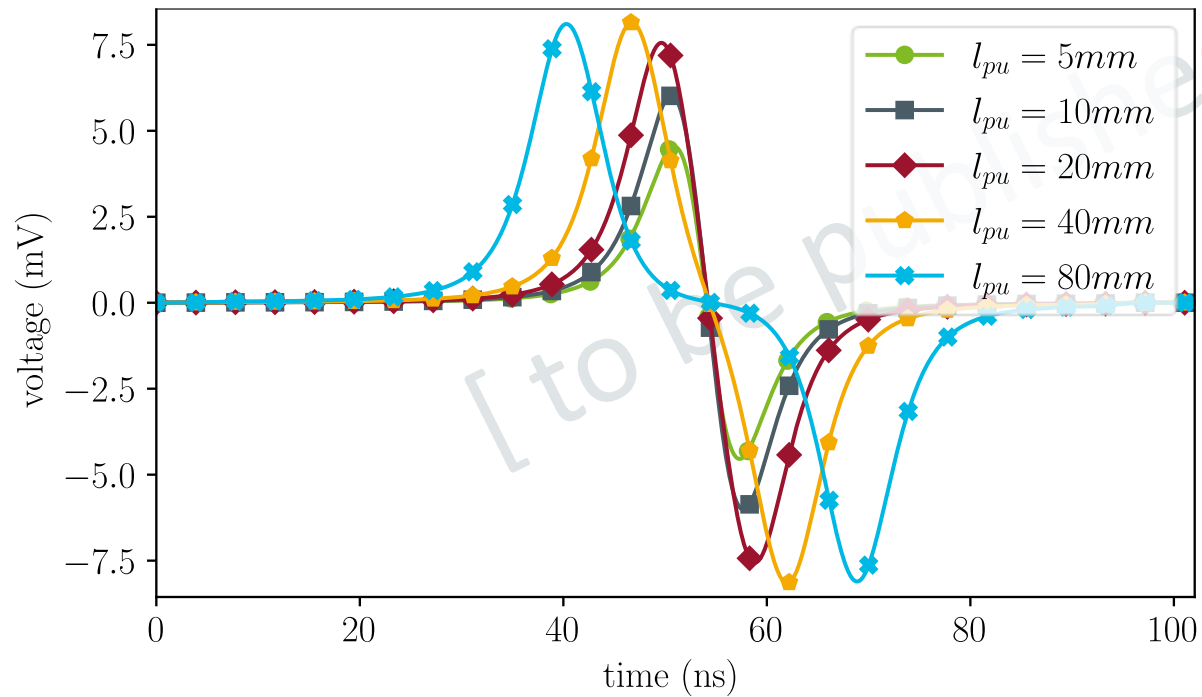


Pick-Ups - Use Cases: Total Charge

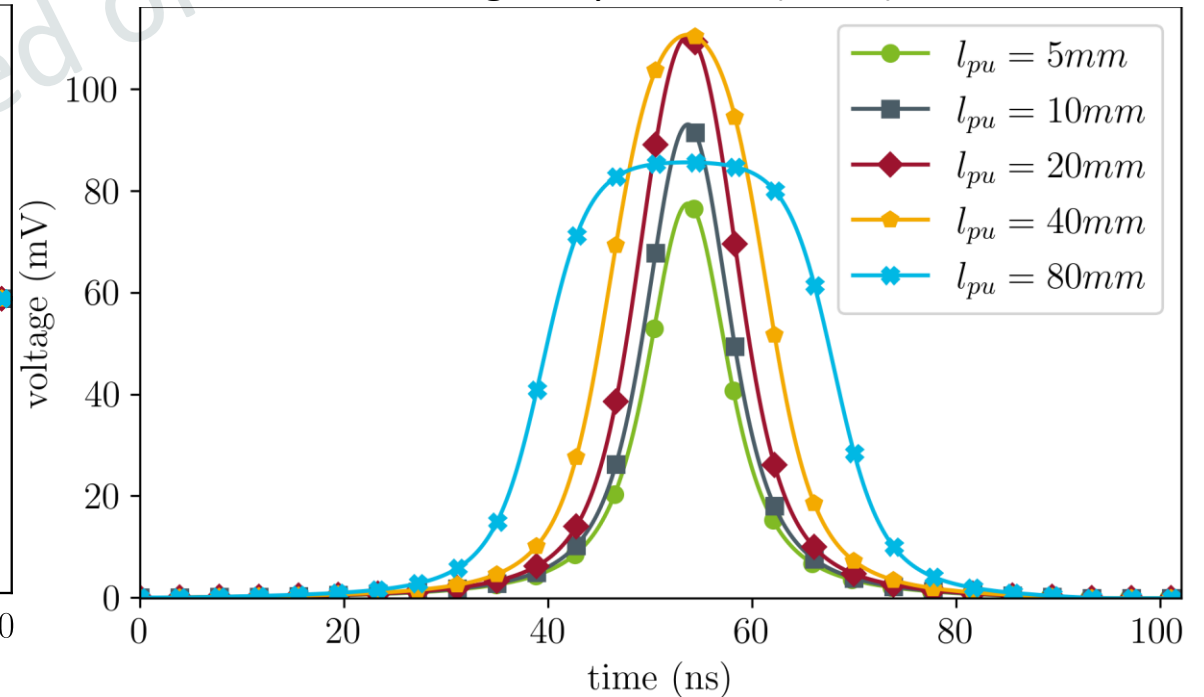
Simulations performed with CST with $1E6$ particles on simplified model



Low Impedance (50Ω)



High Impedance ($1M\Omega$)

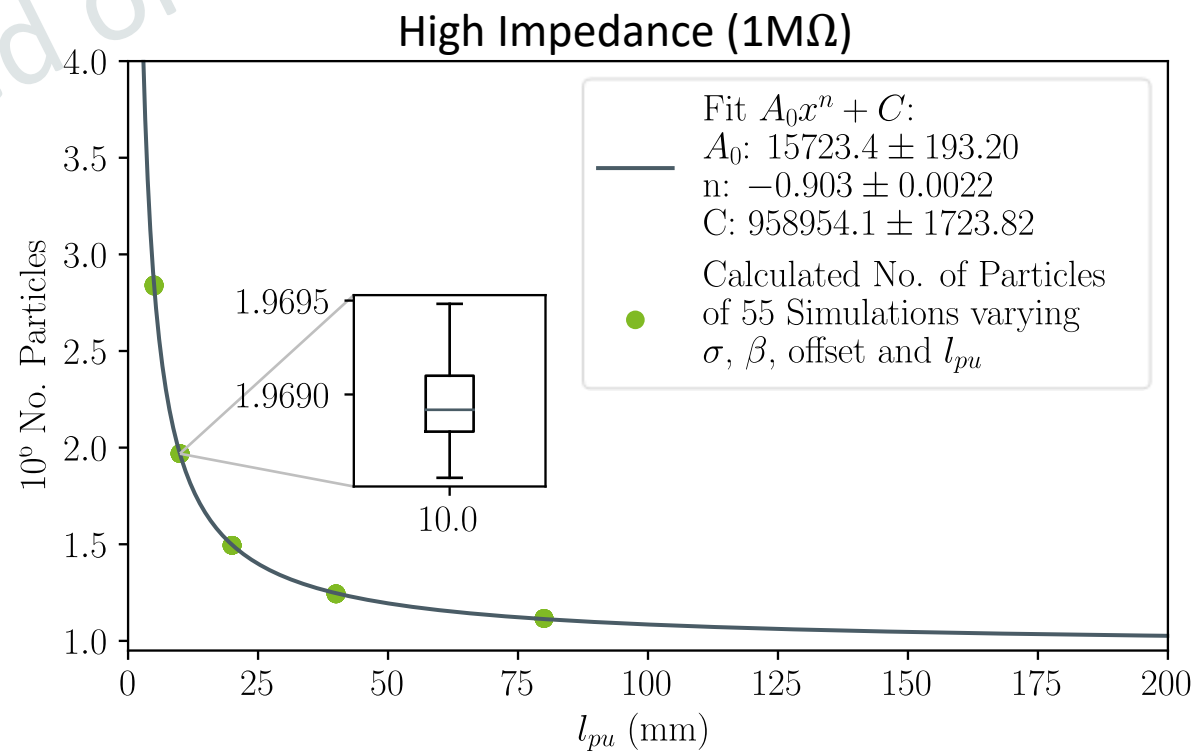
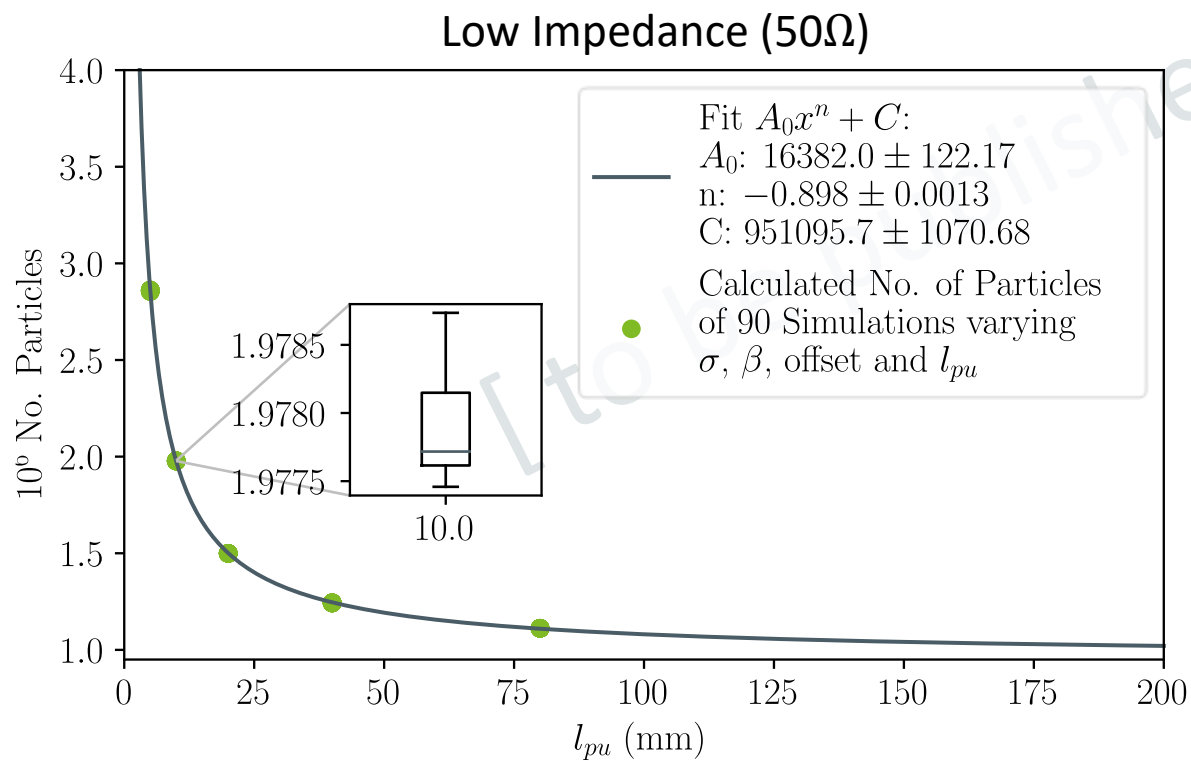


$$\sigma \ 1ns, \Delta y = 0mm, \beta \ 0.01$$

$N_{sim} = 1E6$
 $\sigma = [1ns, 10ns]$,
 $\Delta y = [0mm, 5mm, 10mm]$
 $\beta = [0.01, 0.05, 0.2]$

Pick-Ups - Use Cases: Total Charge

- Raw calculated $Q_b = \frac{\beta c}{l_{pu}} \left(\frac{1}{Z_L} \int_t \int_\tau U_a(\tau) d\tau dt + C_{pu} \frac{Z_L + Z_{pu}}{Z_L} \int_t U_a(t) dt \right)$
- Strong dependency on PU length l_{pu} , very low dependency on velocity βc , bunch width σ and beam axis offset Δy



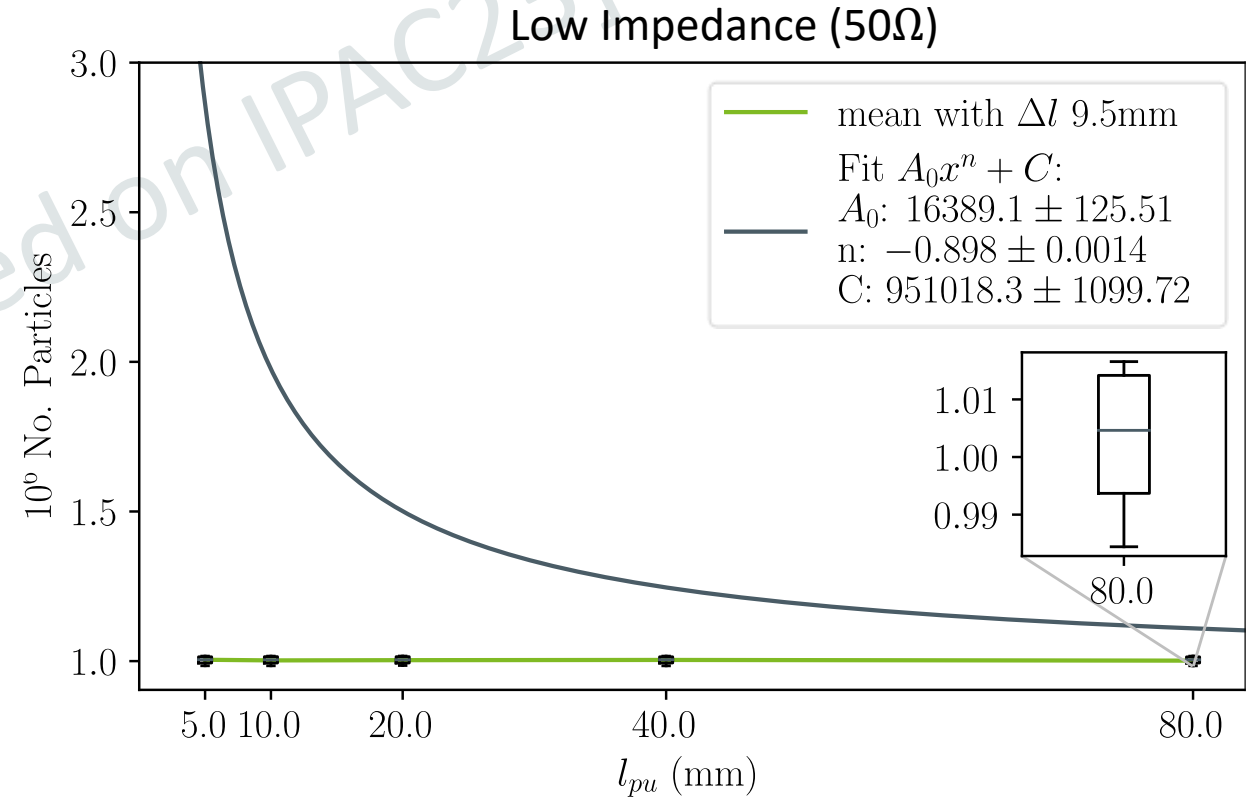
$N_{sim} = 1E6$
 $\sigma = [1ns, 10ns]$,
 $\Delta y = [0mm, 5mm, 10mm]$
 $\beta = [0.01, 0.05, 0.2]$

Pick-Ups - Use Cases: Total Charge

- Ignored fringe fields effects of the PU in the derivation.
 ⇒ An effective length should replace the PU length.

$$Q_b = \frac{\beta c}{l_{eff}} \left(\frac{1}{Z_L} \int_t \int_\tau U_a(\tau) d\tau dt + C_{pu} \frac{Z_L + Z_{pu}}{Z_L} \int_t U_a(t) dt \right)$$

- A simple model $l_{eff} = l_{pu} + \Delta l$ may be used to compensate the fringe field effects up to an error of $\pm 1.7\%$ for $\Delta l = 9.5mm$
- Calibration is needed for absolute values, otherwise only relative charge measurement possible
- Alternative calibration: Test bench with known signal
- Applicable also on shoe-boxes and other types of capacitive PUs



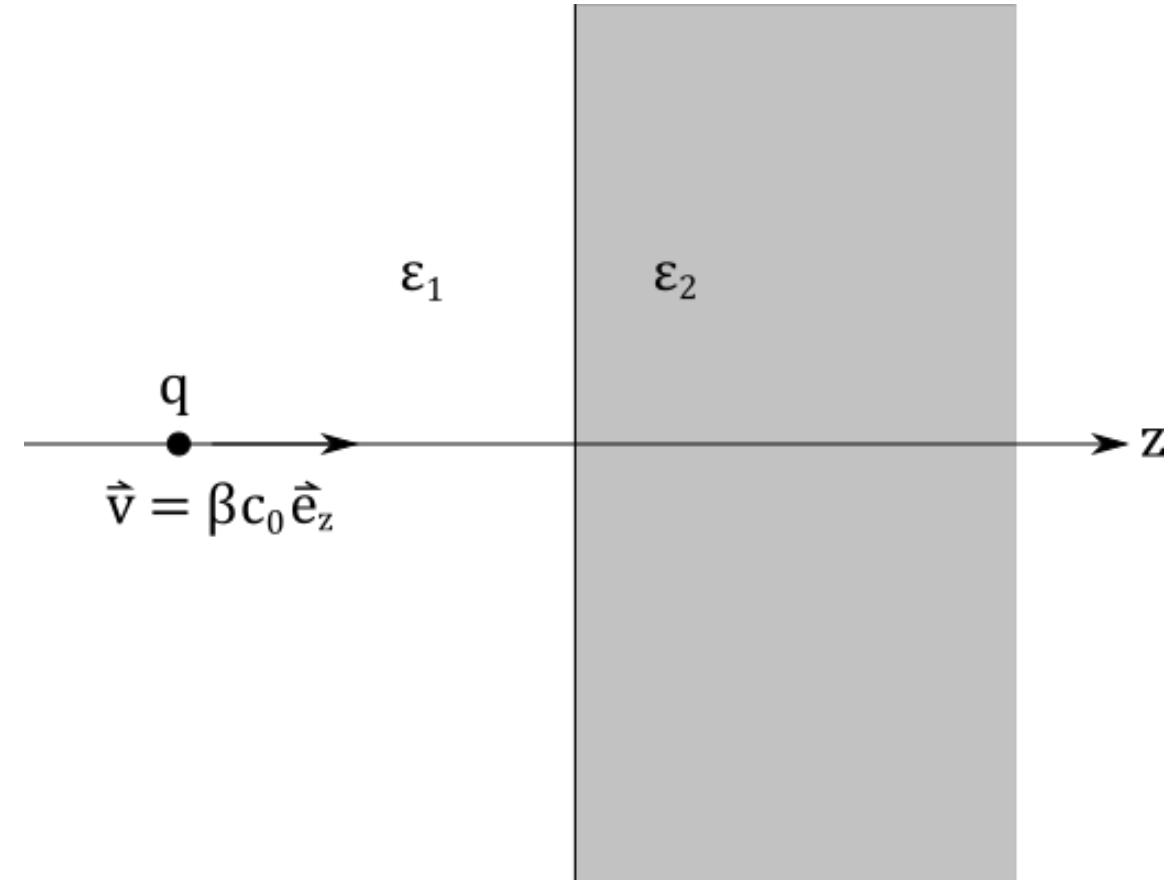
Transition Radiation Monitors

Transition Radiation (TR)

A charge with velocity $v = \text{const.}$ crossing an interface between two media radiates.

- an interface ($z = 0$) separating two half-spaces of different media
- solving MW-equations subject to interface conditions exhibit radiation field
- Surface electromagnetic phenomenon \rightarrow prompt radiation
- In GHz regime, **coherent** transition radiation for \sim ns bunches

A potential method un-affected by pre-field and secondary emission



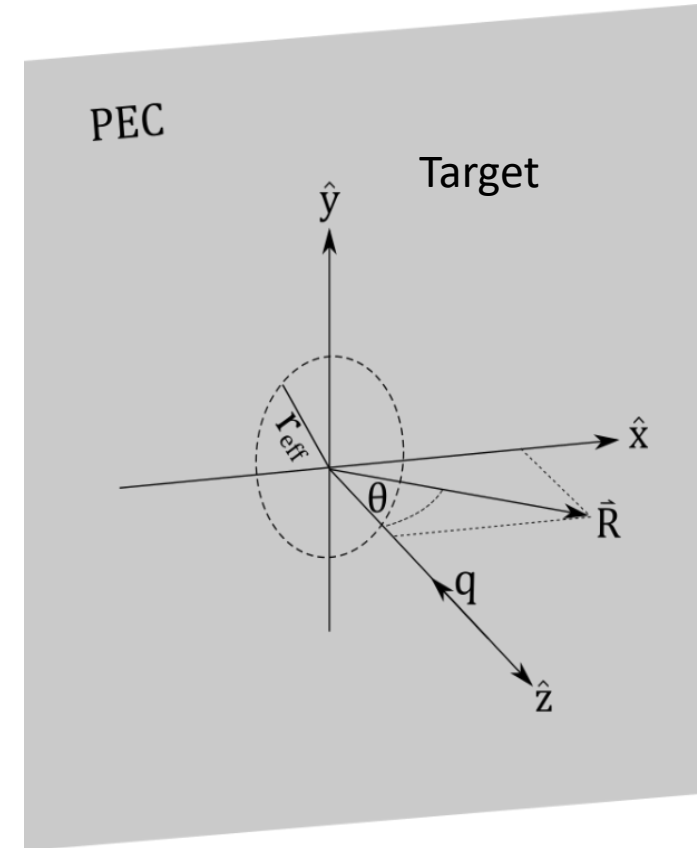
[2]

Transition Radiation (TR) – Properties in the GHz Regime

GTR electric field for single charge:

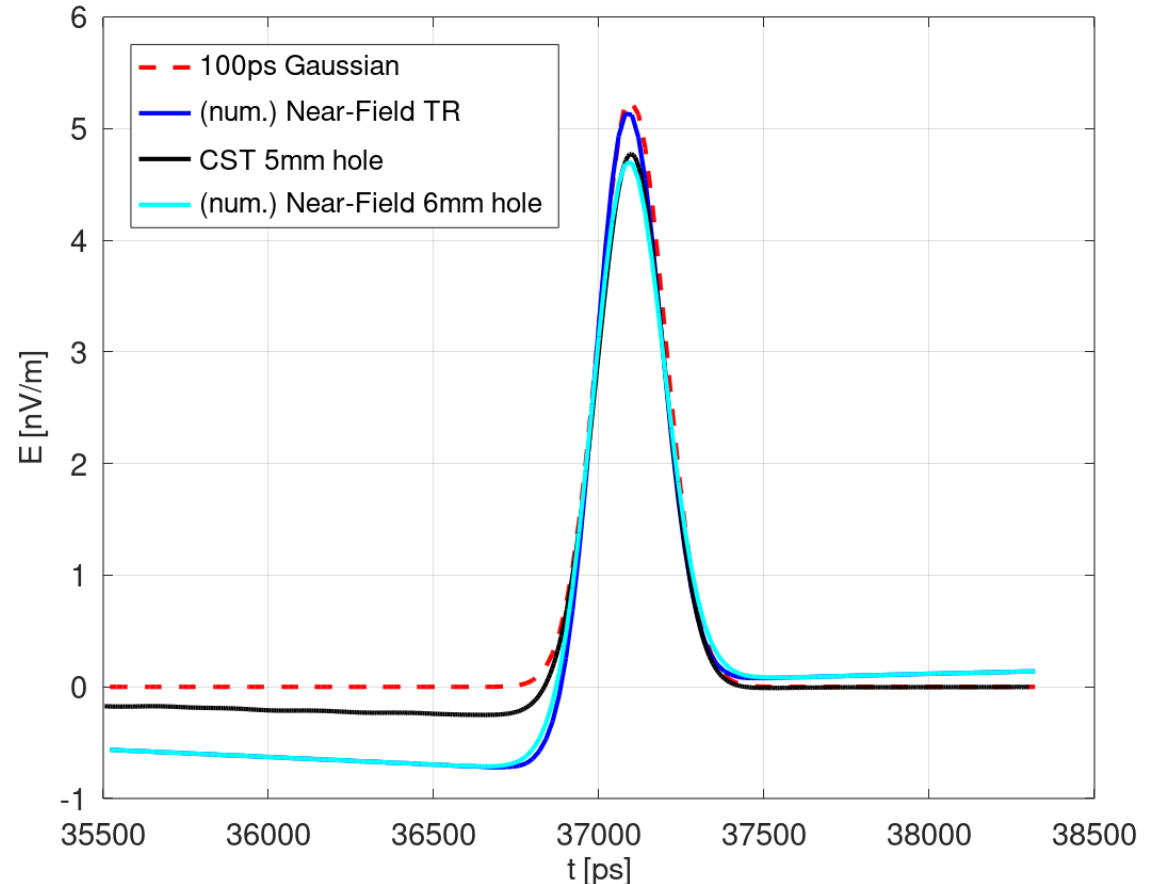
$$\vec{E} = \frac{q\beta}{2\pi\epsilon_0 cR} \frac{\sin\theta \delta\left(\frac{R}{c}-t\right)}{1-\beta^2 \cos^2\theta} (\hat{e}_x \cos\theta + \hat{e}_z \sin\theta)$$

- Linear q and β dependence
- Parallel polarization for normal incidence
- Good signal: 10pC charges in 100 ps (σ) with $\beta=0.15$
 → 10 mV peak



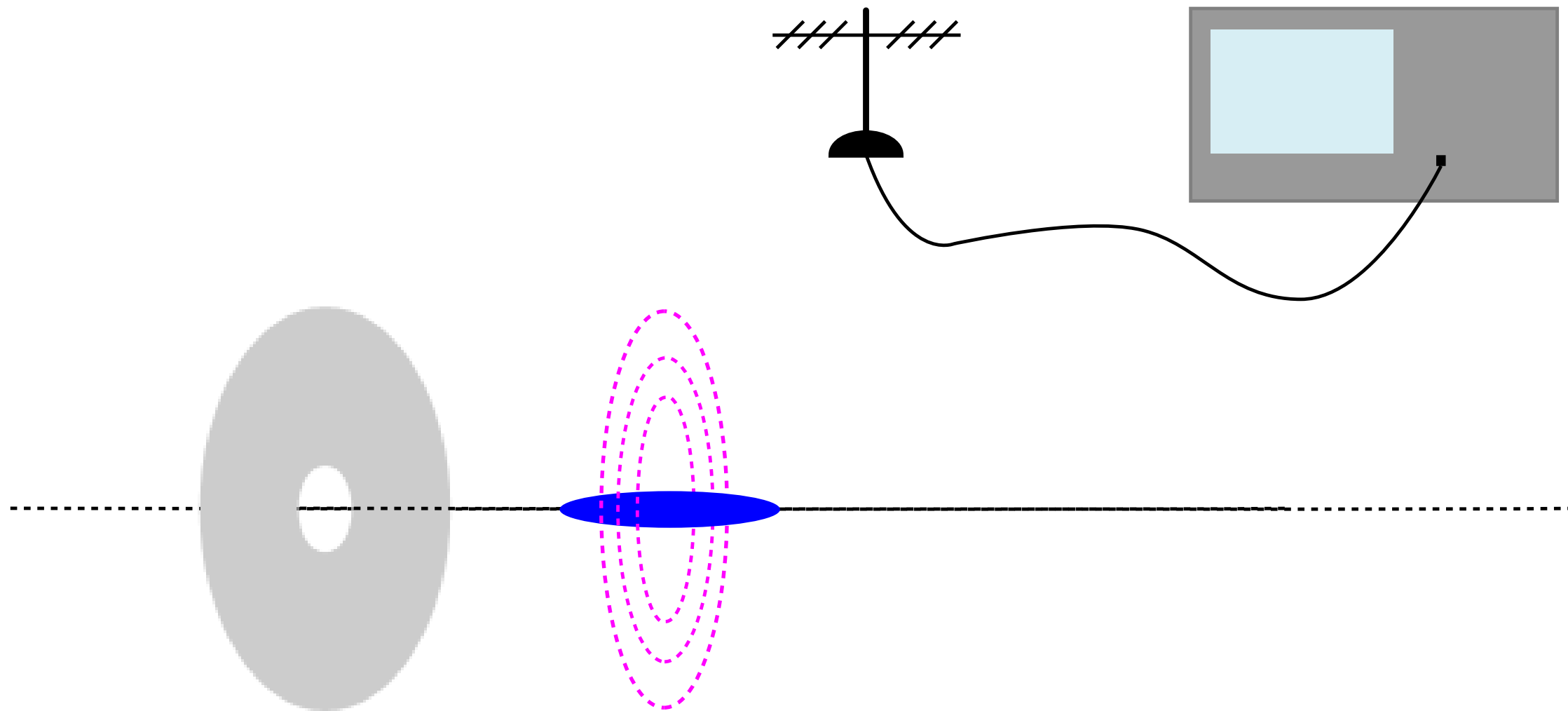
Transition Radiation (TR) – Properties in the GHz Regime

- Diffraction Radiation is very similar to TR but charge traverses close to the media interface
- Here: Instead of impacting on the target bunch can go through hole
- Allowable hole size: $\varnothing \downarrow$ for $\beta \downarrow$
- For $\beta \sim 0.15$, $\varnothing \leq 6\text{mm}$
- **Non-destructive measurements possible!**

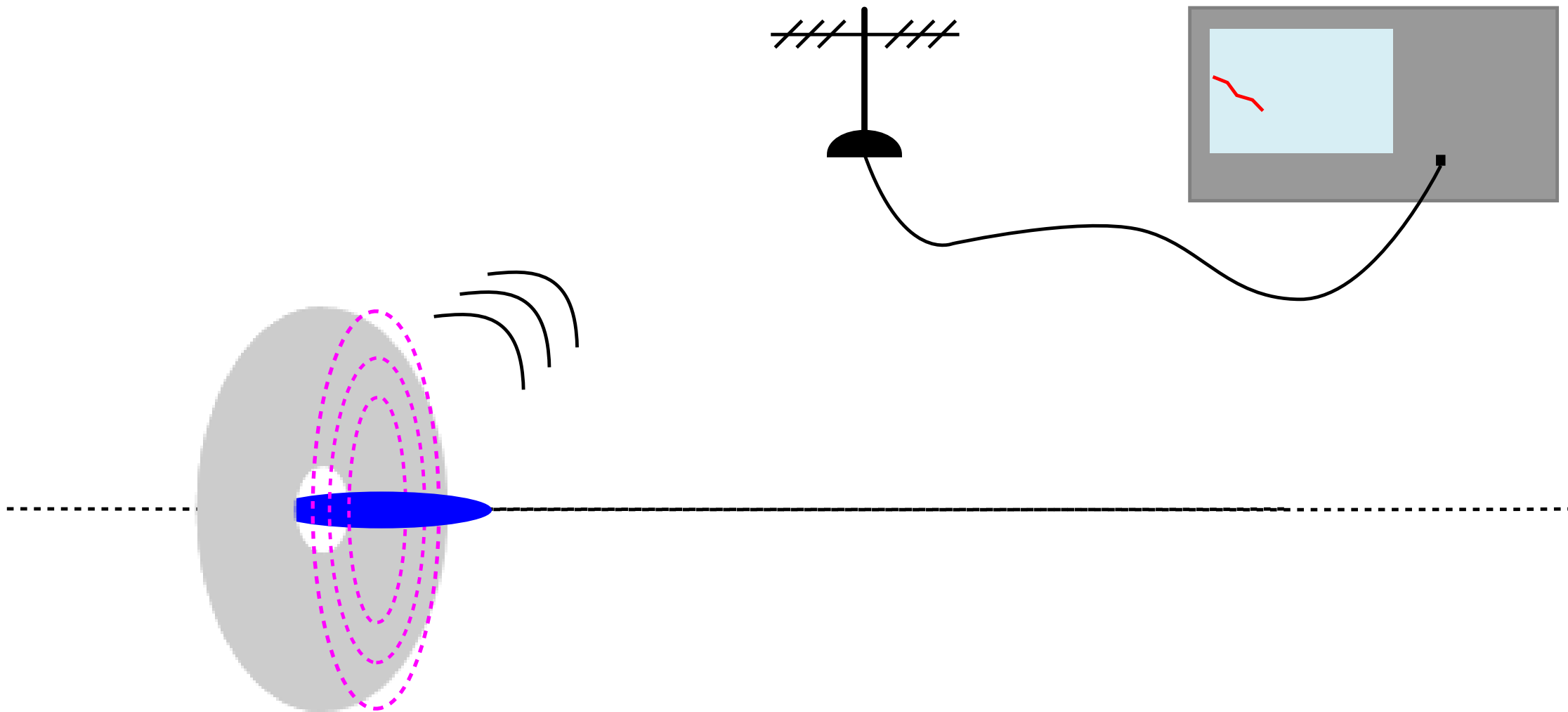


[2]

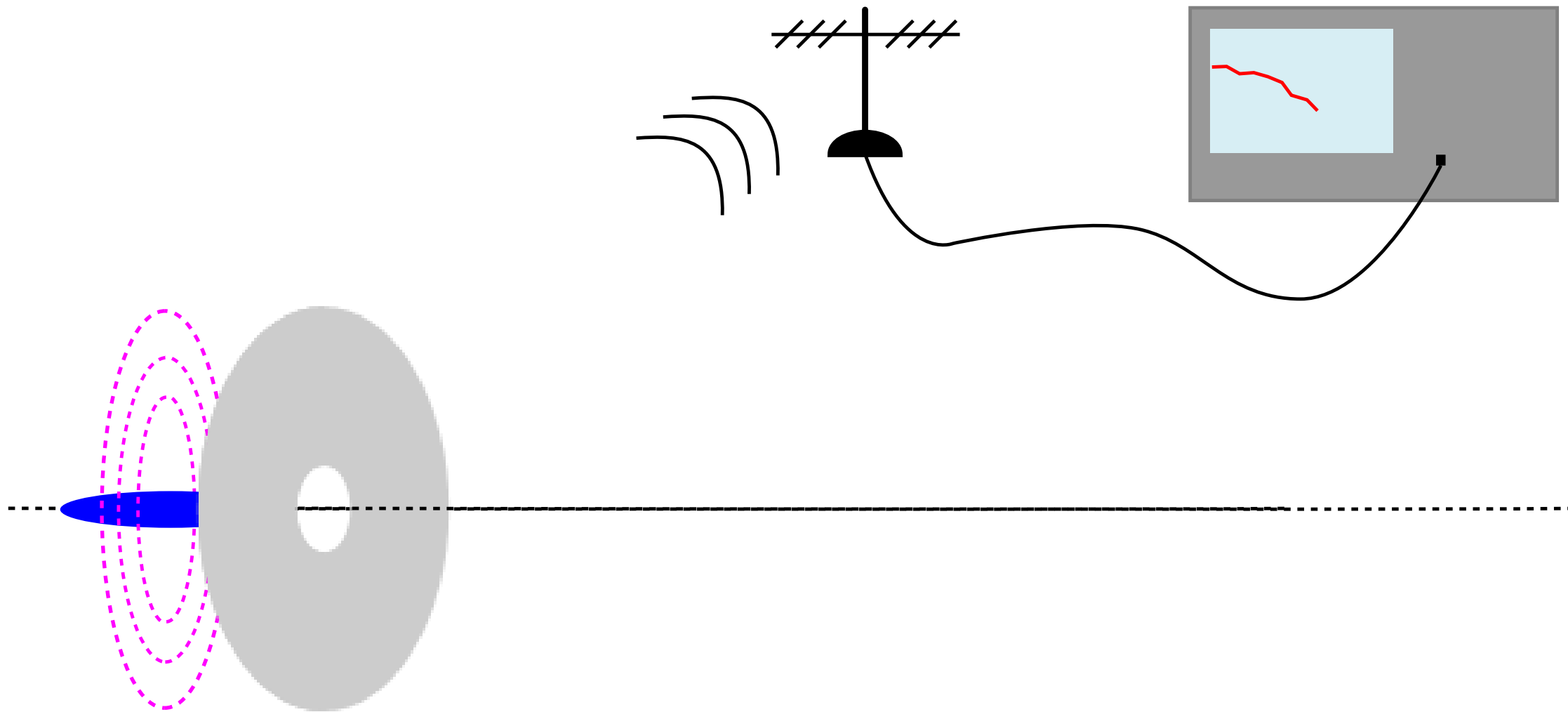
Transition Radiation Monitors Basic Concept



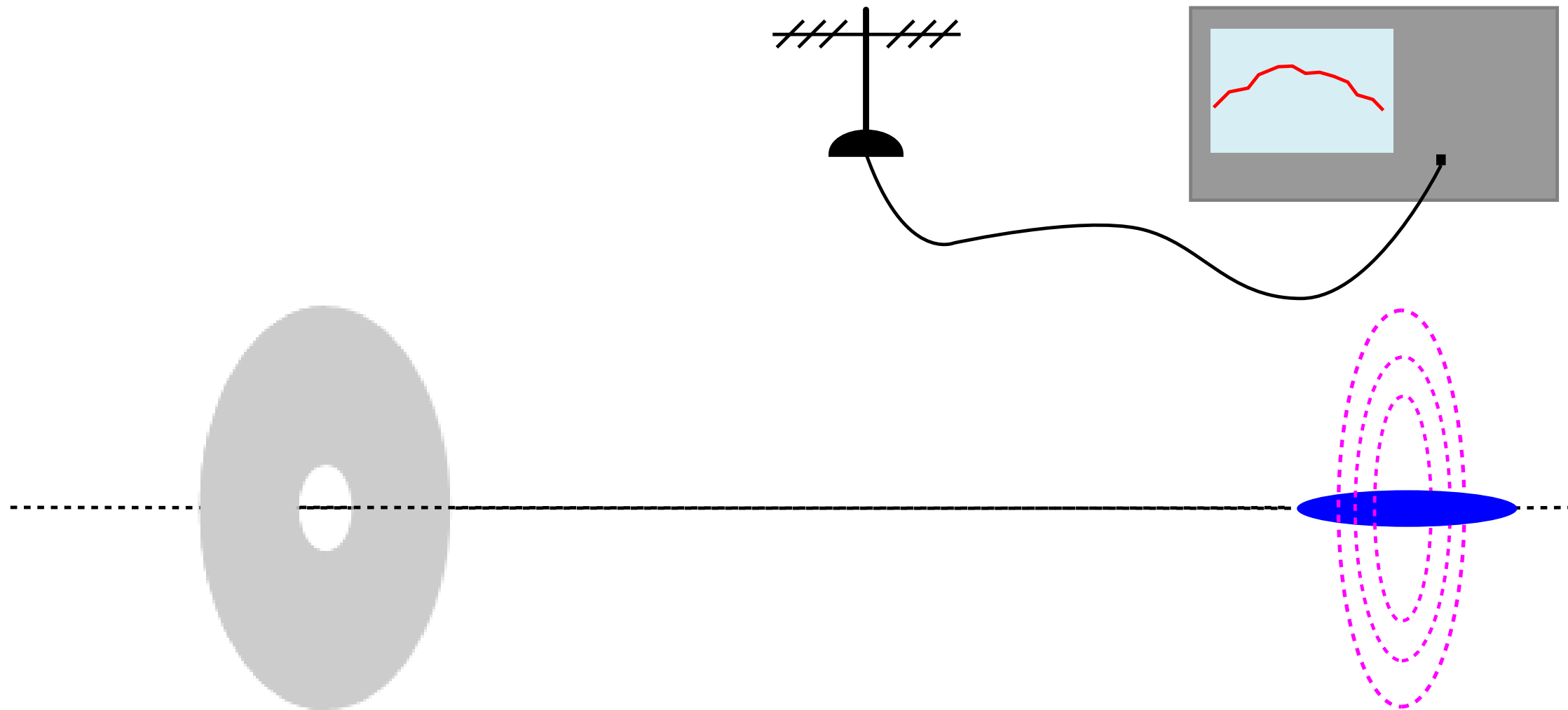
Transition Radiation Monitors Basic Concept



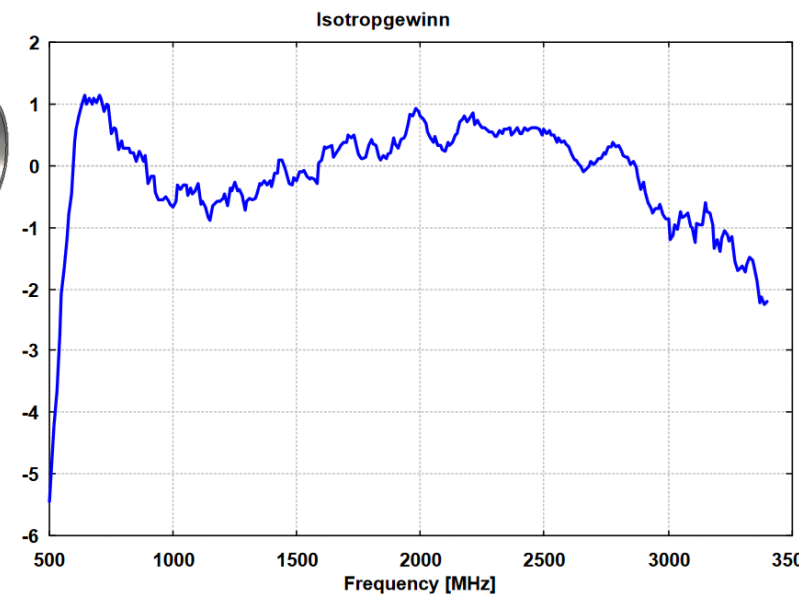
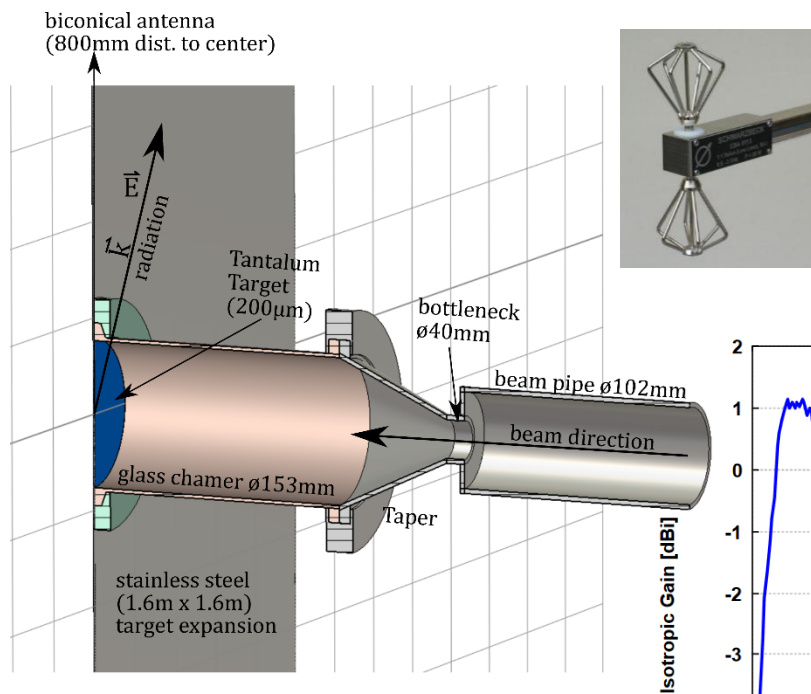
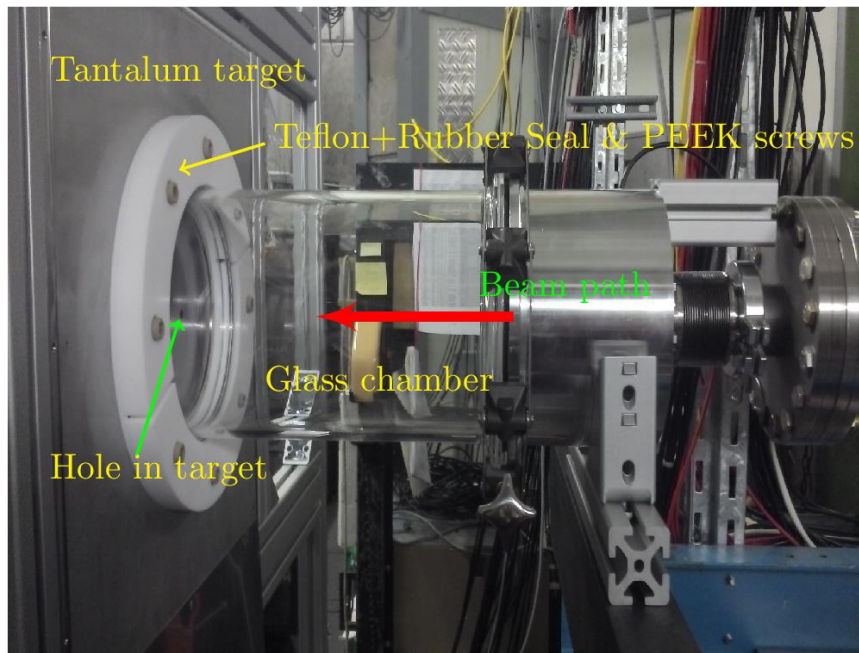
Transition Radiation Monitors Basic Concept



Transition Radiation Monitors Basic Concept



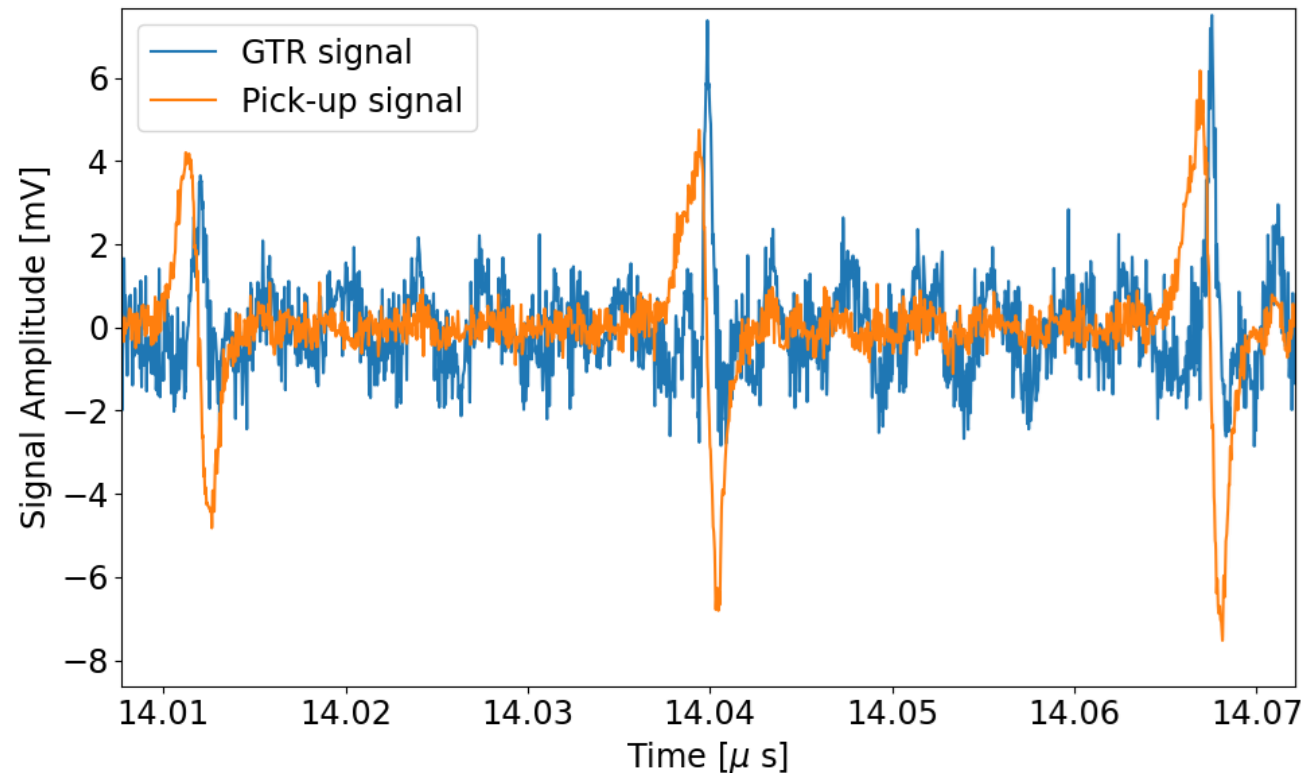
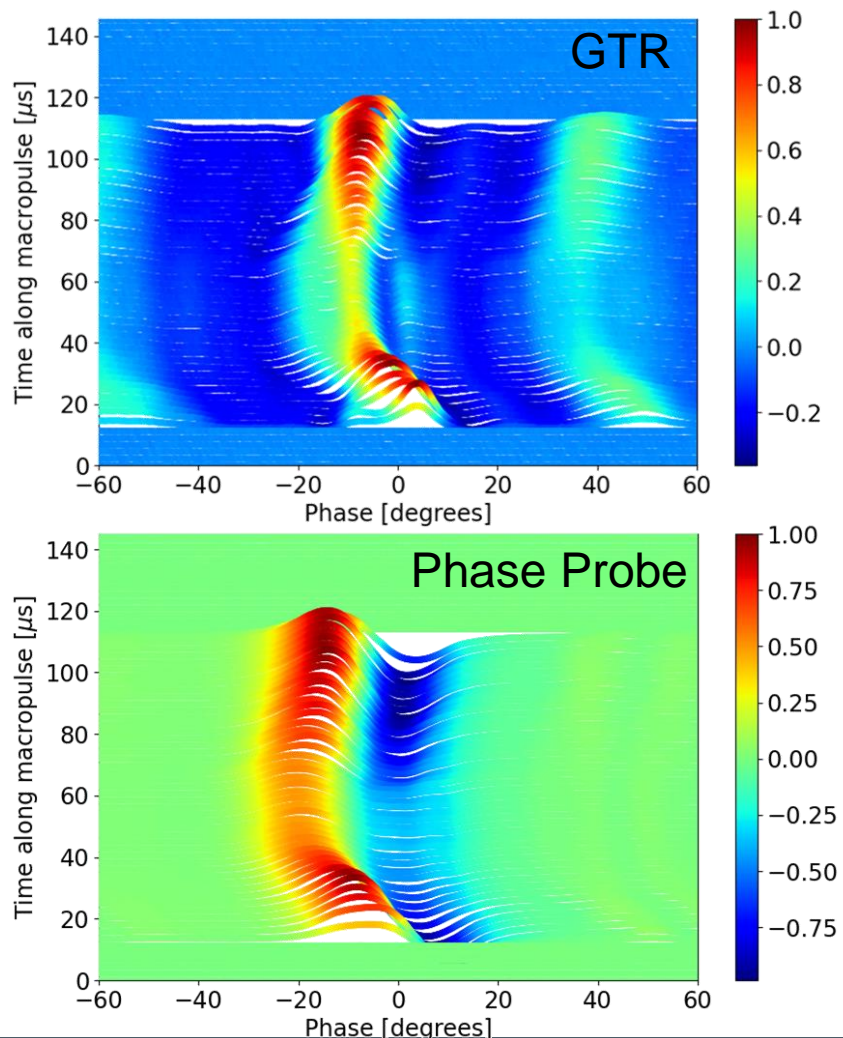
Transition Radiation (TR) – Measurements at X2 (GSI)



- An RF window to couple out the TR signal → Vacuum tolerance → critical
- Absorbers to avoid reflections
- Linear phase antenna designs

[2]

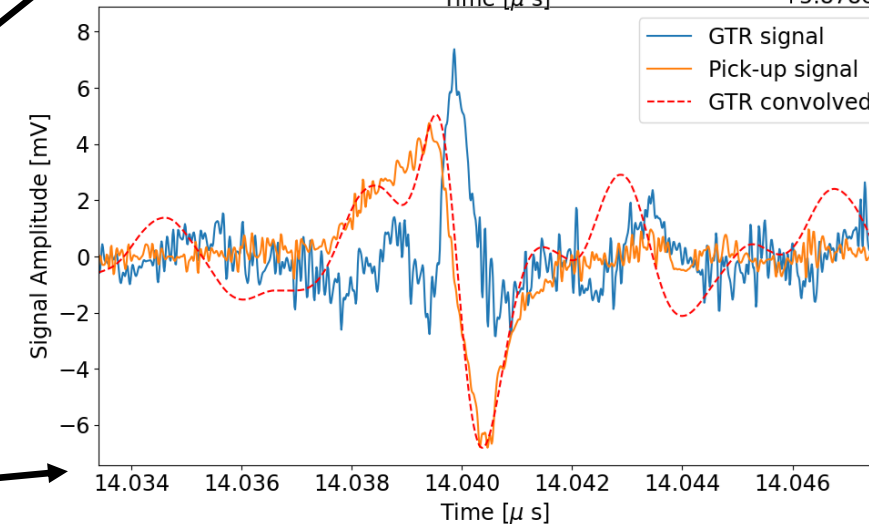
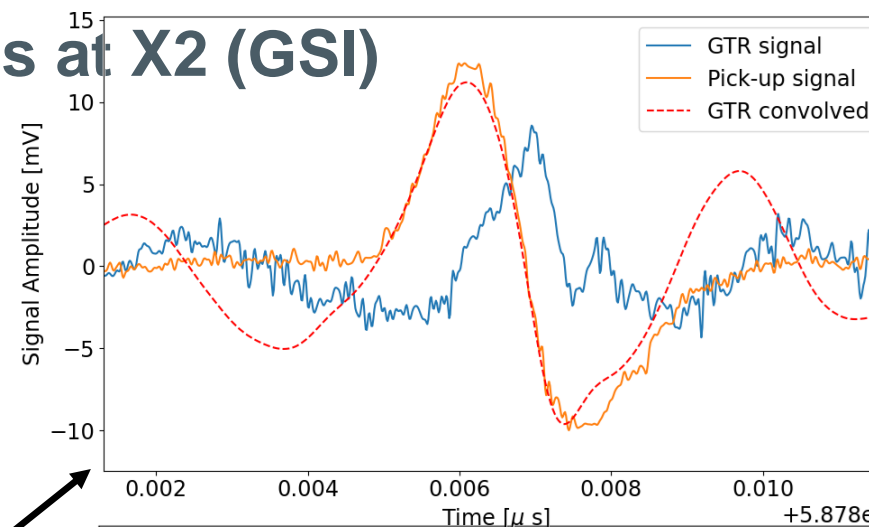
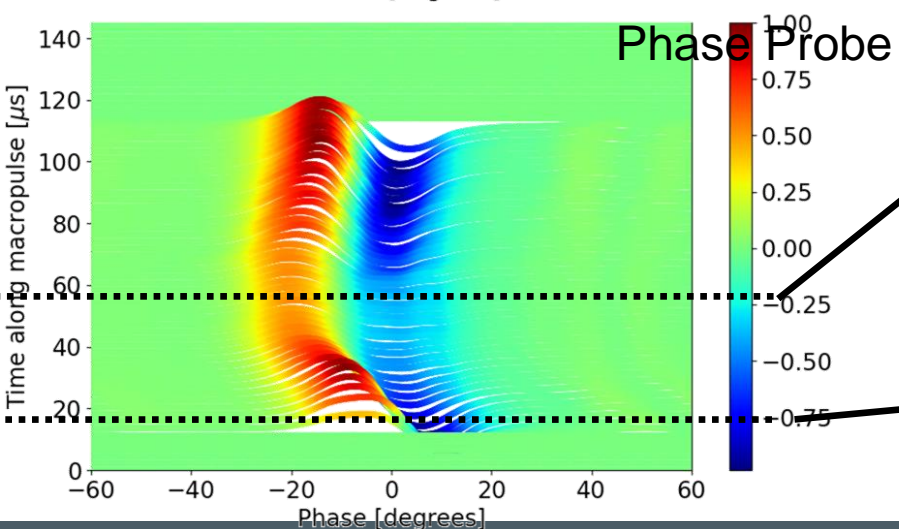
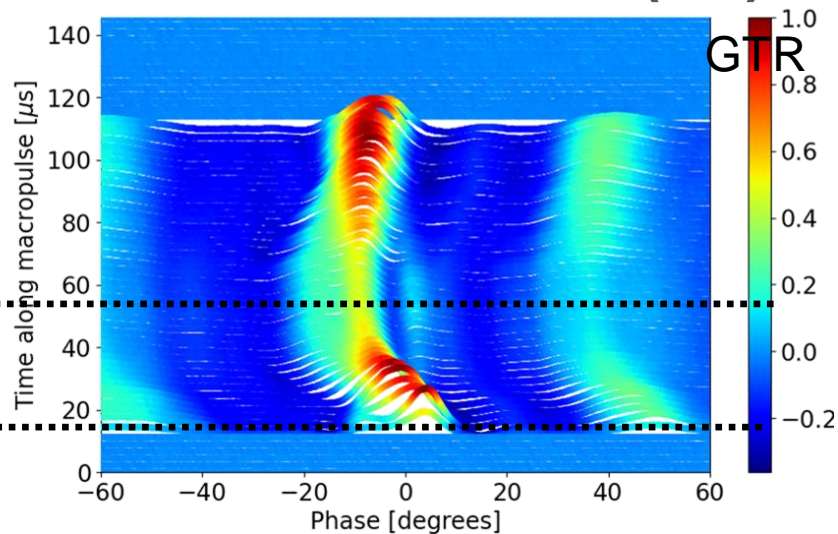
Transition Radiation (TR) – Measurements at X2 (GSI)



- Good correlation with the pick-up data
- Mean beam energy matches with ToF between pick-up and GTR

[2]

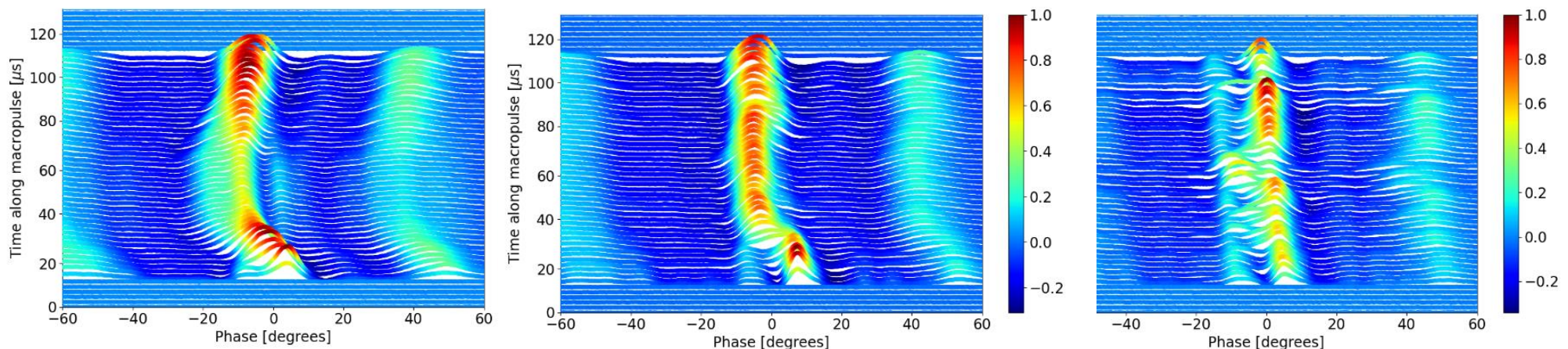
Transition Radiation (TR) – Measurements at X2 (GSI)



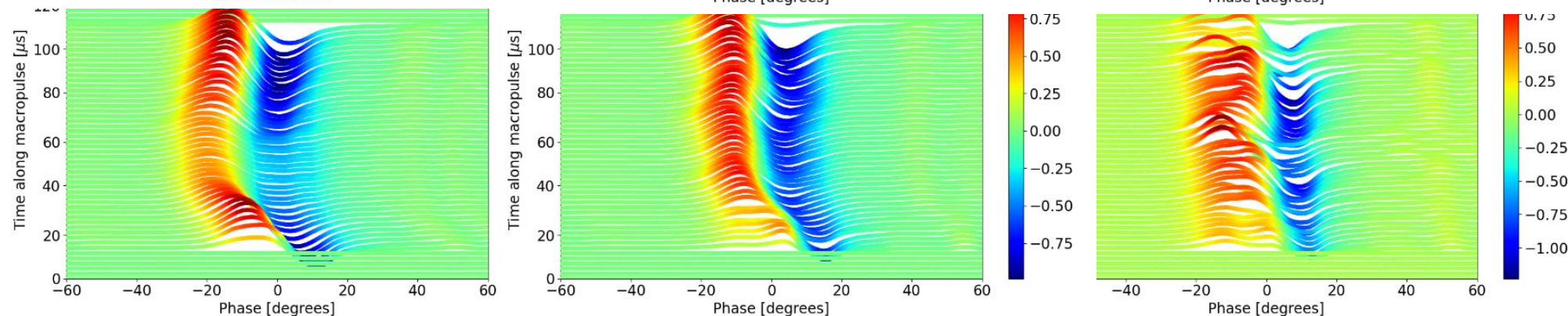
Convolved GTR has **precise** agreement with phase probe signal! [2]

Transition Radiation (TR) – Measurements at X2 (GSI)

GTR



Phase Probe



- Three consecutive macropulses show different charge distributions
- Longitudinal diagnostics need to be prepared for such fast changes

[6] R. Singh and T. Reichert,
Phys. Rev. Accel. Beams 25, 032801

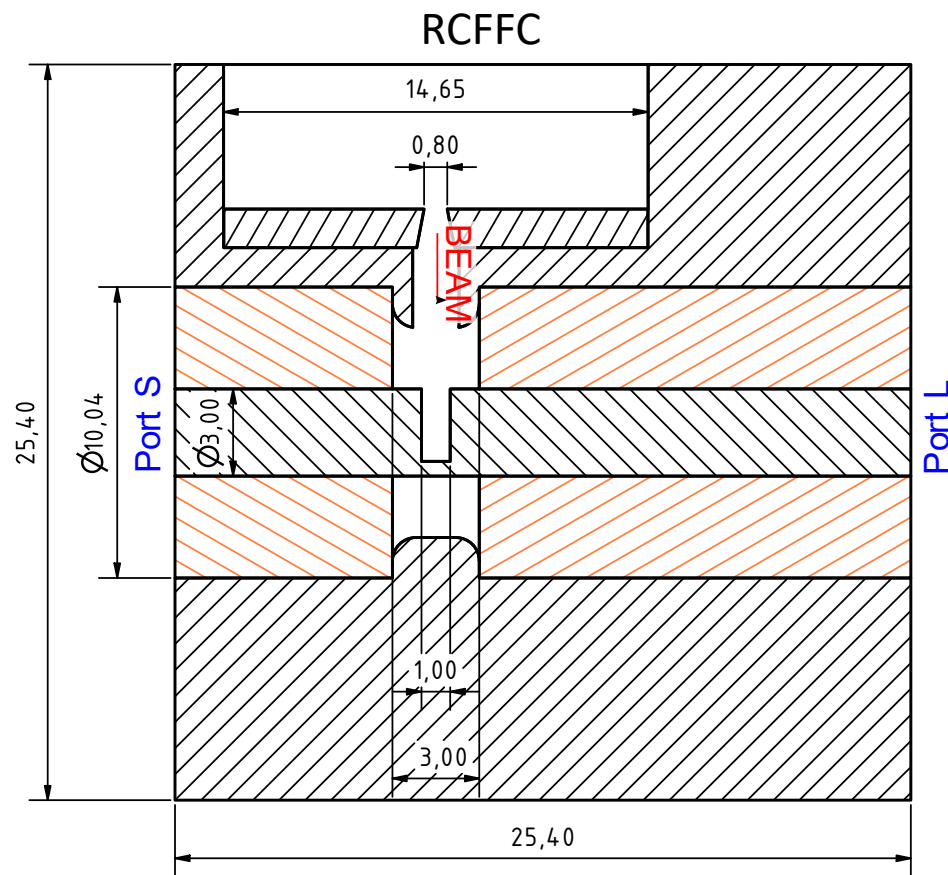
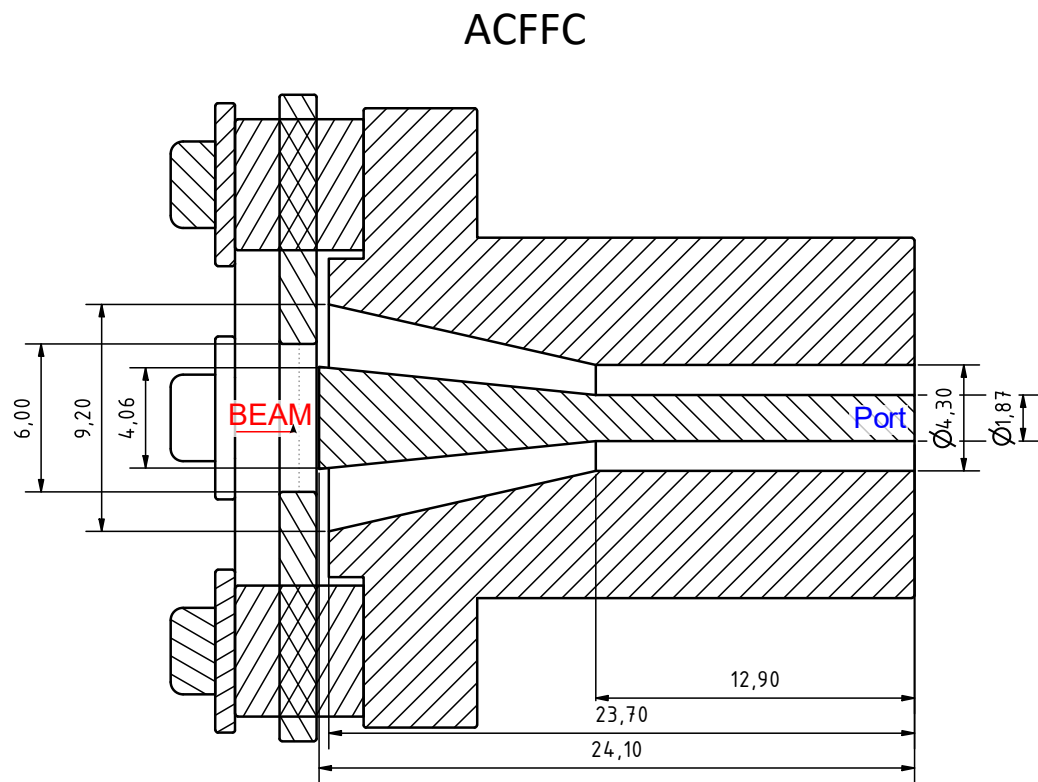
Fast Faraday Cups

Fast Faraday Cups (FFC)

- FFCs are design to measure fast longitudinal bunch structures
- Challenges:
 - Matching of the out-coupling should be done very well till high frequencies
i.e. $BW > 5\sigma_f = 5 \frac{1}{2\pi\sigma_t}$
 - Measuring the self-field should be avoided
 - Suppress distortion of the signal caused by secondaries
 - Cooling of the FFC / avoid melting of the FFC
- Despite being known for decades, FFCs are still under research in many shapes and use cases.
Axial, Radial, Strip-Line, ...

[7] J. M. Bogaty et al. (1990): A very wide bandwidth Faraday cup suitable for measuring GHz structure on ion beams with velocities to beta < 0.01

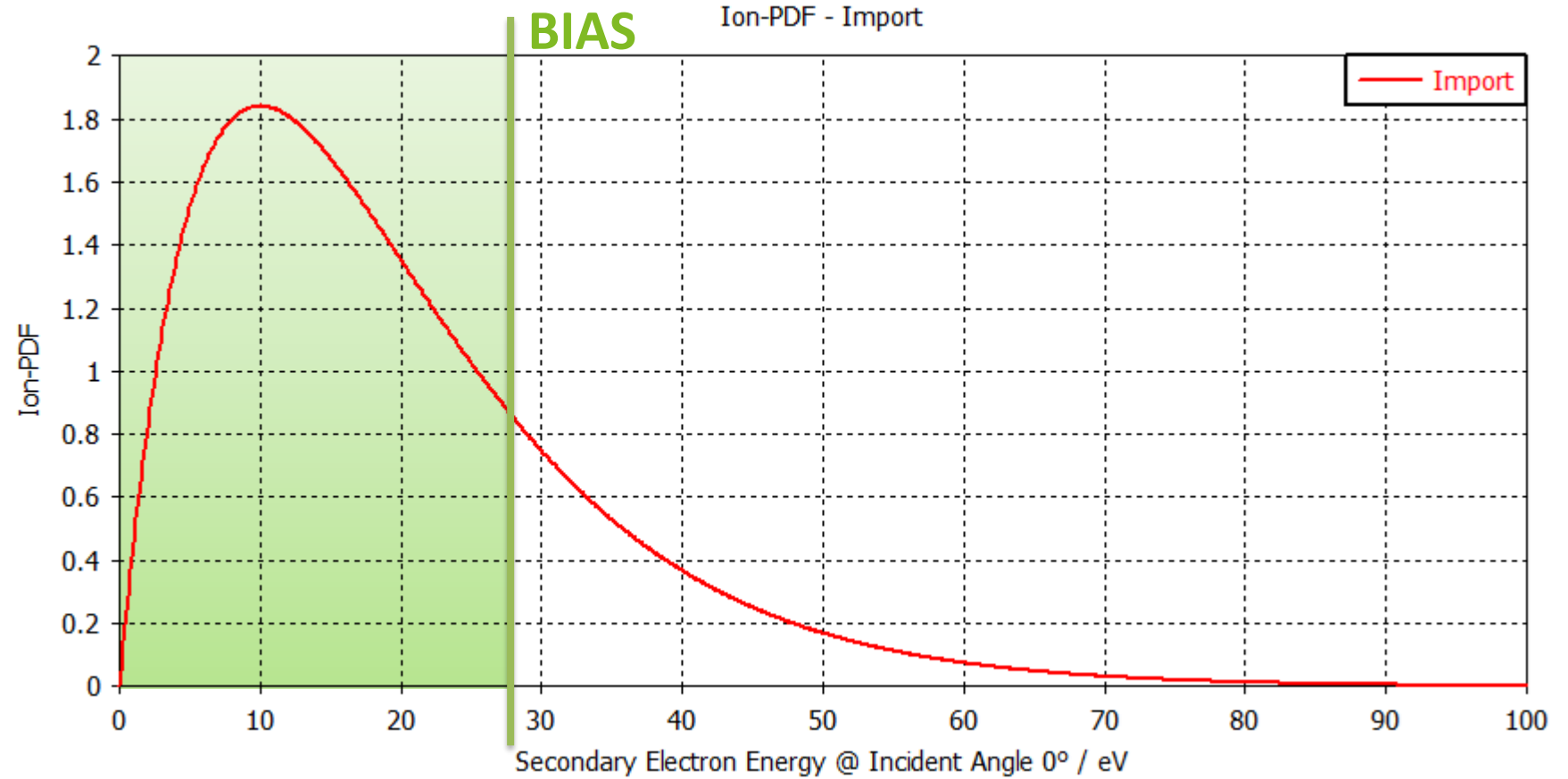
Fast Faraday Cups (FFC) – Comparing Axially Coupled and Radially Coupled FFC



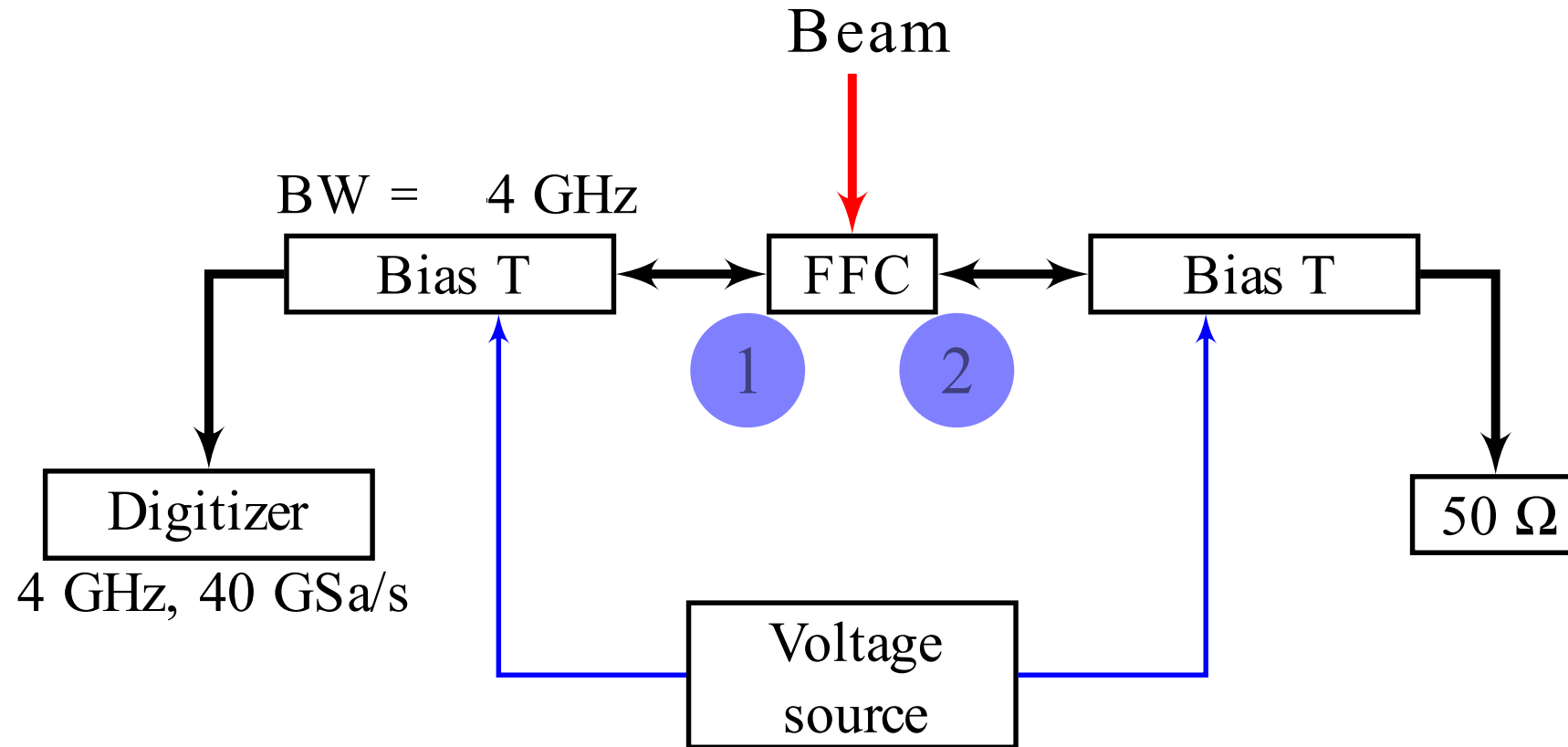
[8,11,12]

Fast Faraday Cups (FFC) – Comparing Axially Coupled and Radially Coupled FFC

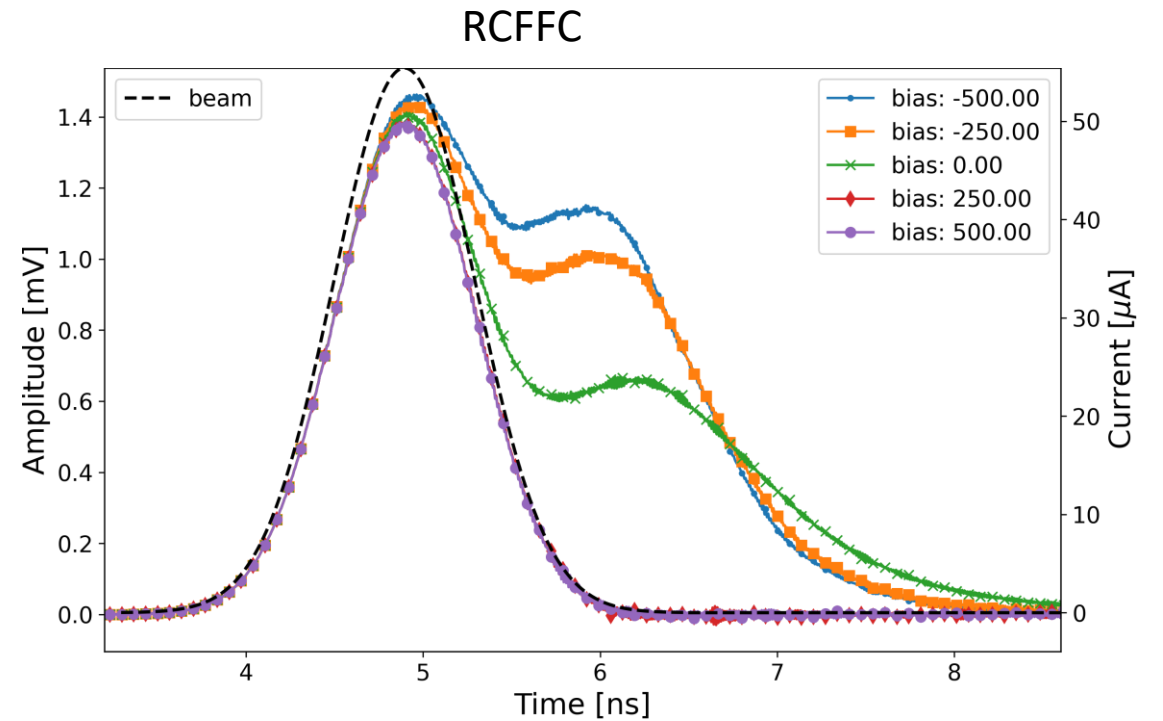
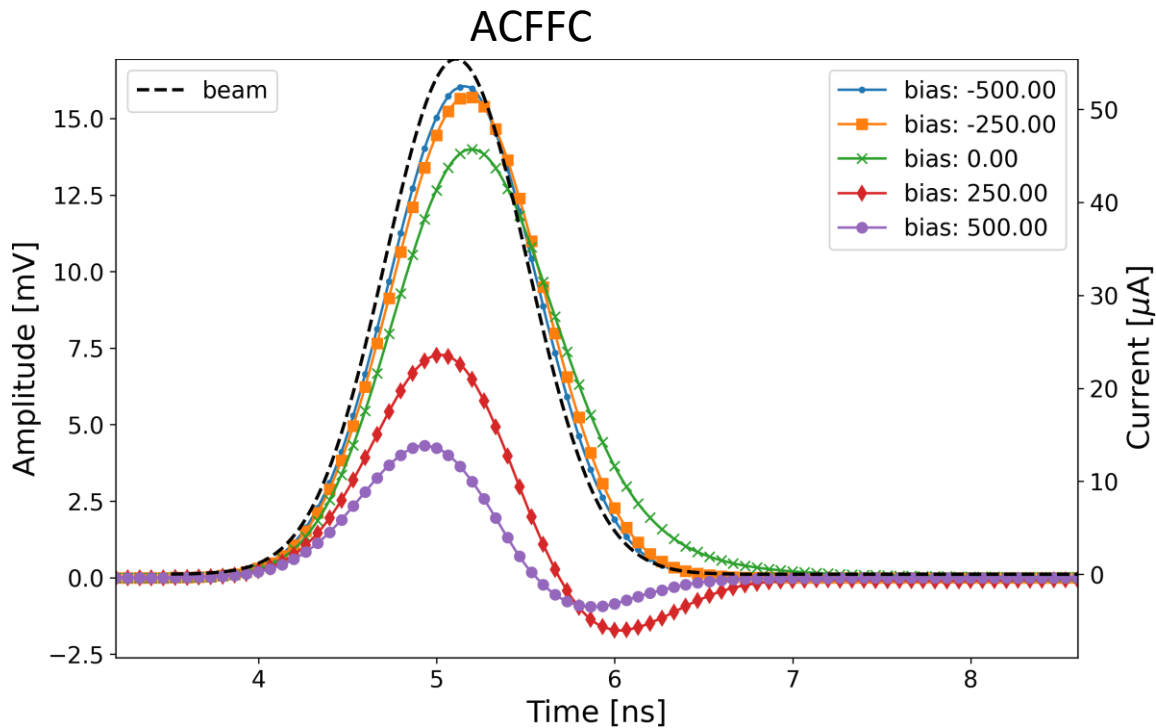
- Simulation Settings:
 - $T_e = 10\text{eV}$
 - 50 SE/Ion
 - No SE through electrons
 - SE emitted only from central conductor
- Suppression of SEE:
 - BIAS reattracts SE to central conductor
 - RCFFC recollects SE within drill hole. These SE will not contribute to signal.



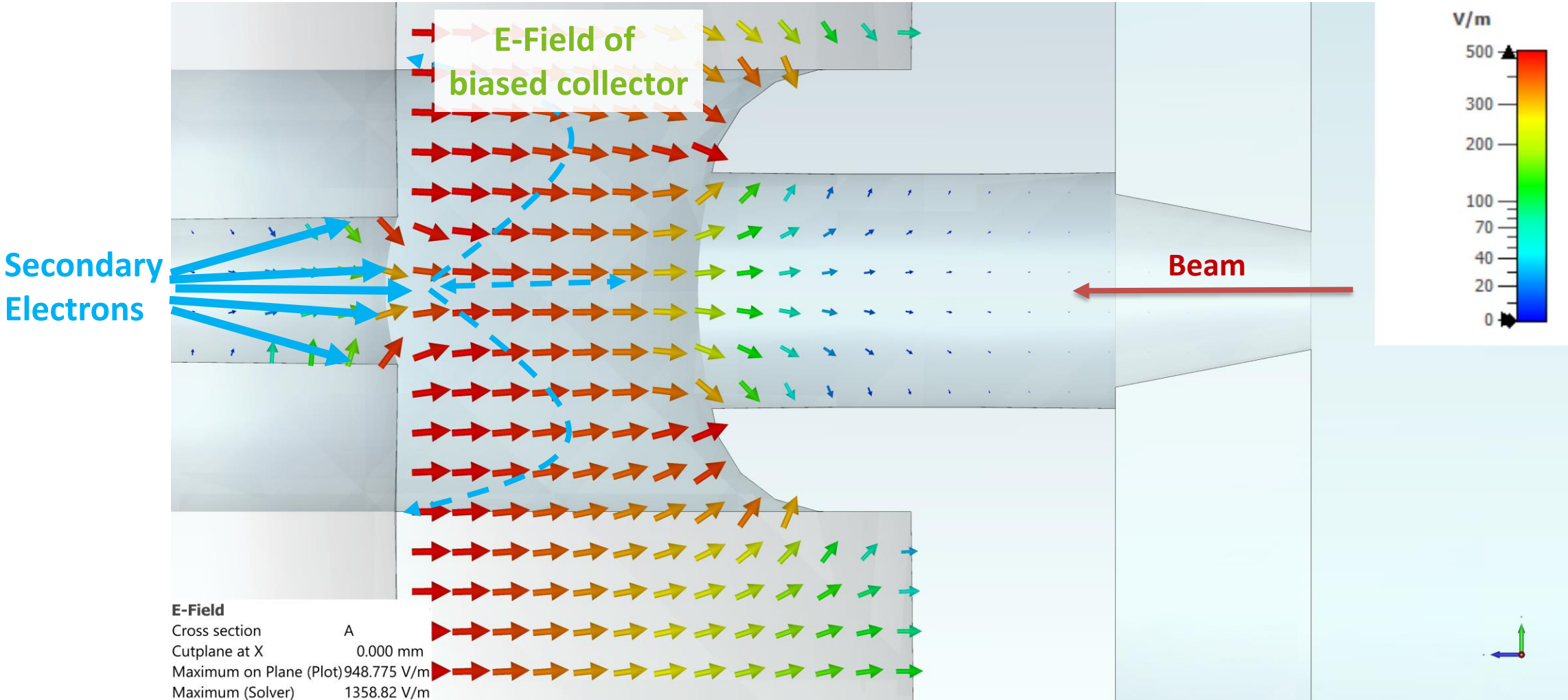
Fast Faraday Cups (FFC) – Comparing Axially Coupled and Radially Coupled FFC



Fast Faraday Cups (FFC) – Comparing Axially Coupled and Radially Coupled FFC

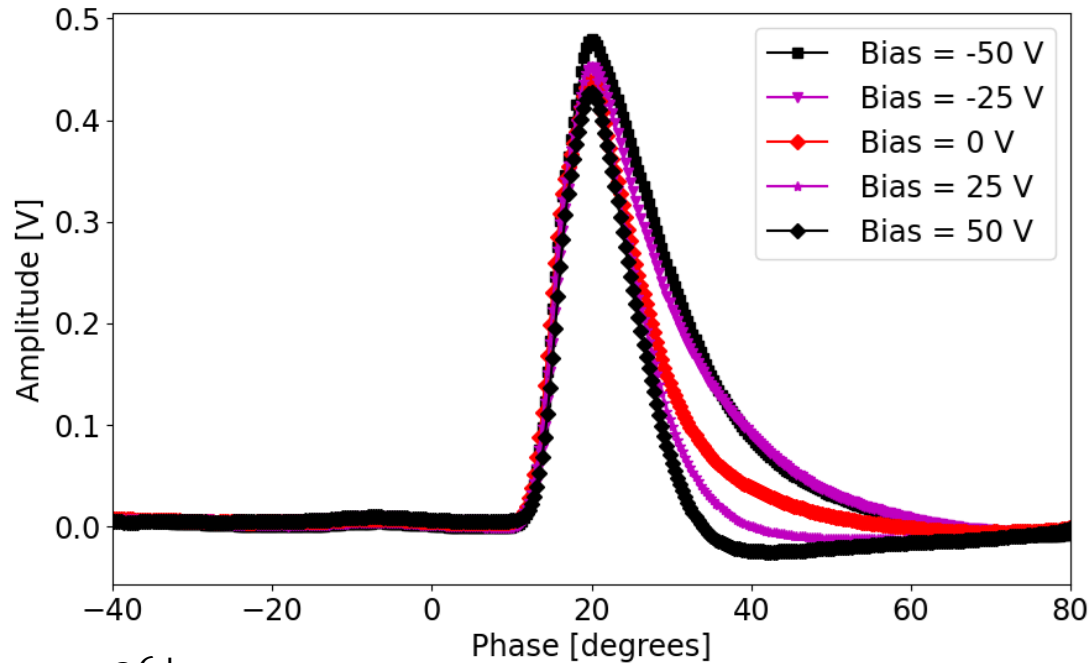


Fast Faraday Cups (FFC) – Comparing Axially Coupled and Radially Coupled FFC



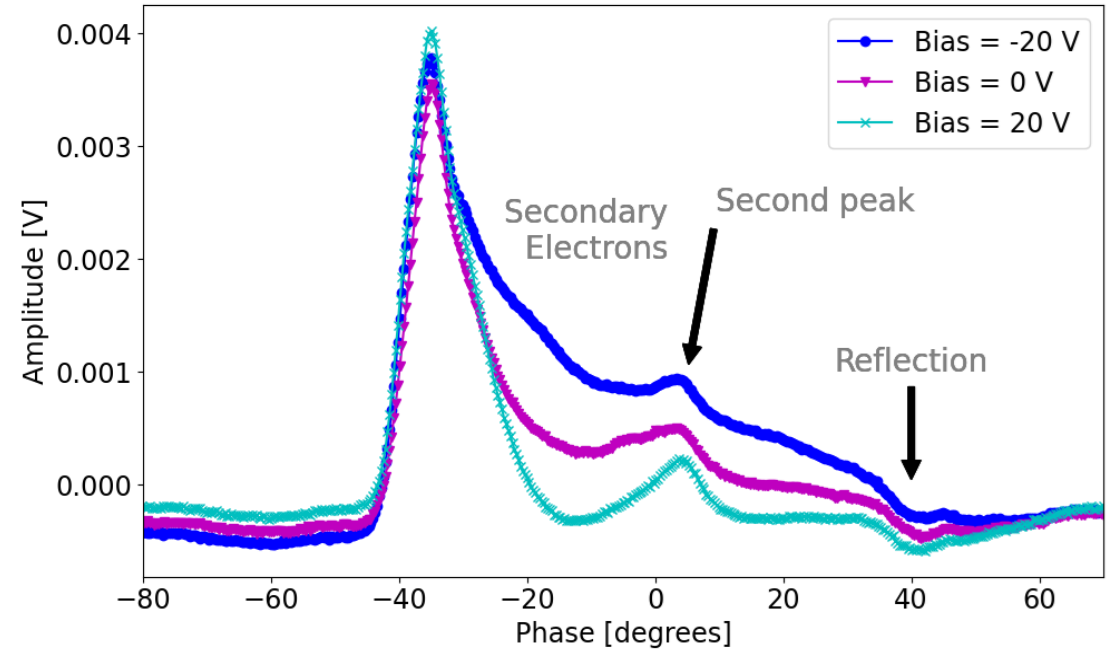
Comparing Axially Coupled and Radially Coupled FFC

ACFFC



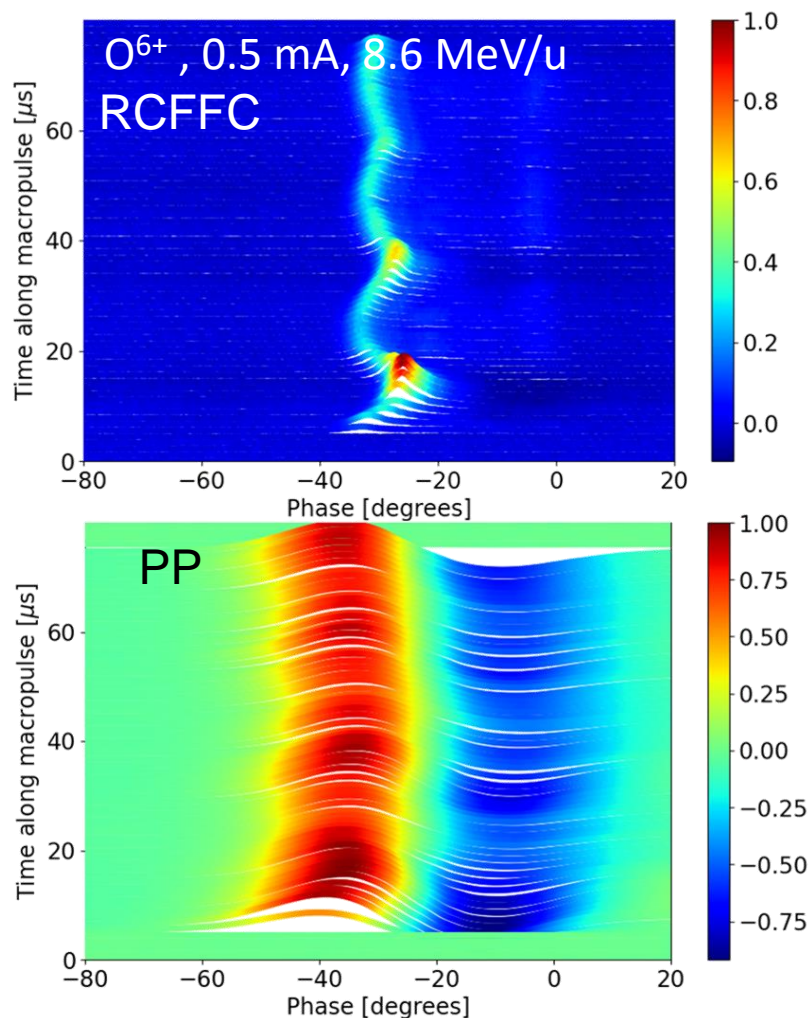
O^{6+}
 8.6 MeV/u
 0.4 mA

RCFFC

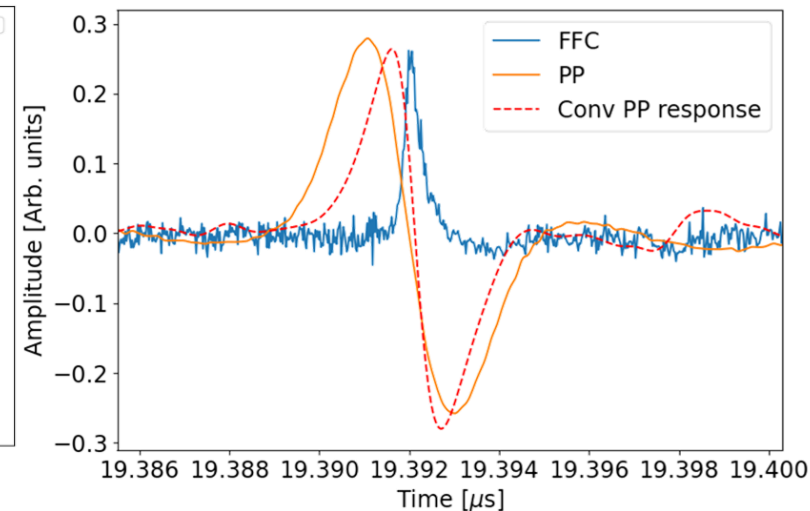
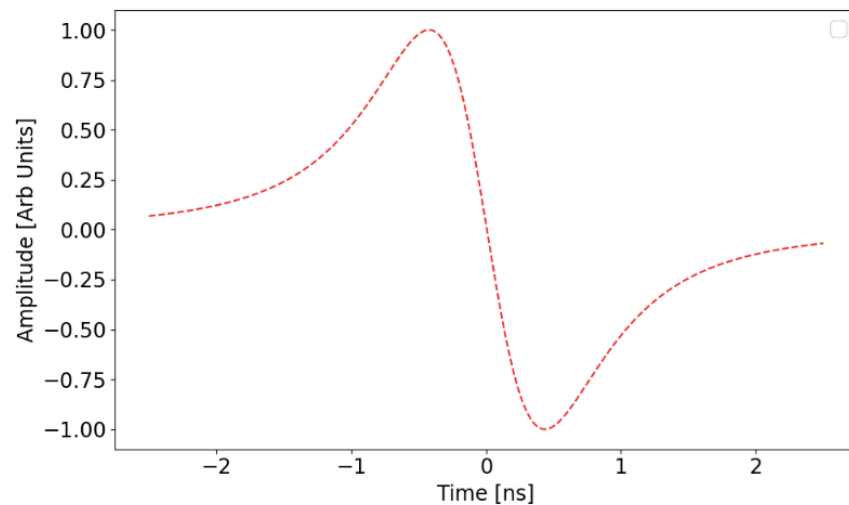


Ar^{10+}
 8.6 MeV/u
 0.4 mA

Comparing Phase Probe and Radially Coupled FFC



Phase probe low velocity beam response ($\beta = 0.134$) at R = 3 cm



Phase probe remains a validation device!

Conclusions

- Fast and robust longitudinal diagnostics is important for various alignments.
- Pick-Up field distribution is not equal to the charge distribution for $\beta < 1$
- Total charge measurements are possible and insensitive to other beam parameters
- Combined purpose possible: e.g., TOF, BAM, Total Charge with just two Pick-Ups
- GTR a promising **non-invasive option for high currents** *but* not a compact installation. Further investigation under BMBF project ongoing
- FFC is a promising **compact option** *but* requires careful placement and biasing is essential depending on the energy regimes. New designs being tested, comparison with calculated phase space needed

Room for Questions!

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Machine operating team!

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IUAC: K. Mal, G. Rodrigues, S. Kumar , **FNAL:** V. Scarpine, A. Shemyakin, D. Sun

B. Scheible, A. Penirschke, H. De Gersem

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References

- [1] P. Forck, JUAS Lecture notes on beam instrumentation, 2022
- [2] R. Singh, “Longitudinal Beam Diagnostics R&D at GSI-UNILAC”, in *Proc. HIAT’22*, Darmstadt, Germany, Jun.-Jul. 2022, pp. 144-149. doi:10.18429/JACoW-HIAT2022-TH2I2
- [3] P. Forck, JUAS Lecture notes on beam instrumentation, 2021
- [4] A. G. Shkvarunets and R. B. Fiorito, *Phys. Rev. ST Accel. Beams* 11, 012801
- [5] R. Singh and T. Reichert, *Phys. Rev. Accel. Beams* 25, 032801
- [6] R. Singh and T. Reichert, “Longitudinal charge distribution measurement of nonrelativistic ion beams using coherent transition radiation”, *Phys. Rev. Accel. Beams*, vol. 25, no. 3, p. 032801, 2022, doi:10.1103/PhysRevAccelBeams.25.032801
- [7] J. M. Bogaty et al.: A very wide bandwidth Faraday cup suitable for measuring GHz structure on ion beams with velocities to $\beta < 0.01$, *Proc. of Linear Accelerator Conference 1990*, Albuquerque, New Mexico, USA
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