

How meson crossing terms reconcile the recent observational data

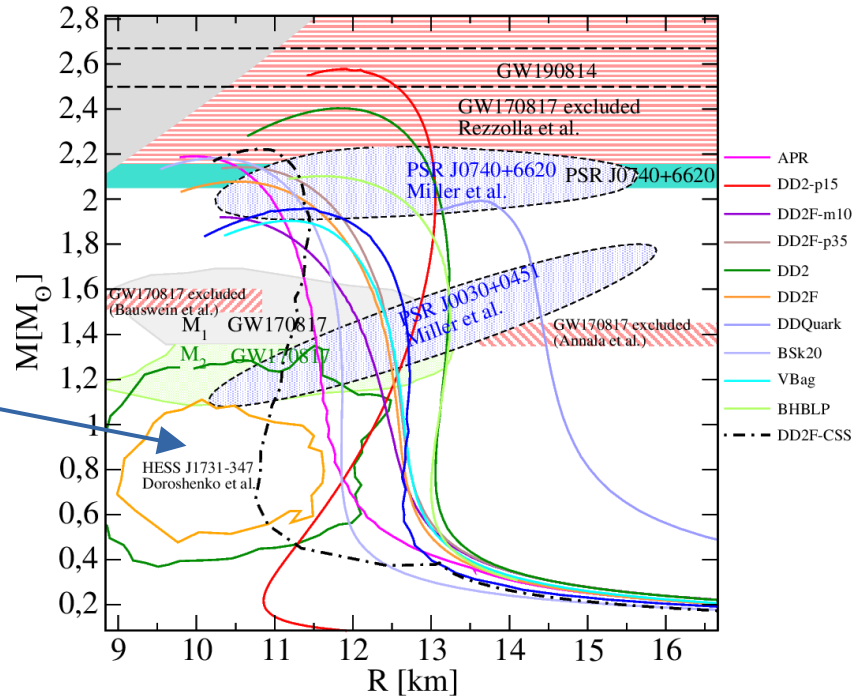
Sebastian Kubis

Cracow University of Technology

/with W.Wójcik, N.Zabari, D.Alvarez-Castillo/

HESS J1731-347
CCO in SN remnant
the lightest NS !

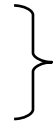
exotica required ?



Historical perspective

RMF (*J.D. Walecka '74*) :

- scalar mesons → attraction
- vector mesons → repulsion



saturation of nuclear forces

relativistic Lagrangian with $\sigma, \omega, \vec{\rho}$ coupled to n, p

lightest true mesons:

σ now $f_0(600)$ – very broad resonance

$\omega(782)$

$\rho(780)$

~~experimental coupling constants~~

effective couplings fitted to sat. properties:
(infinite nuclear matter)
binding energy, compressibility
symmetry energy...
all at $n_0 = 0.16 \text{ fm}^{-3}$

However!

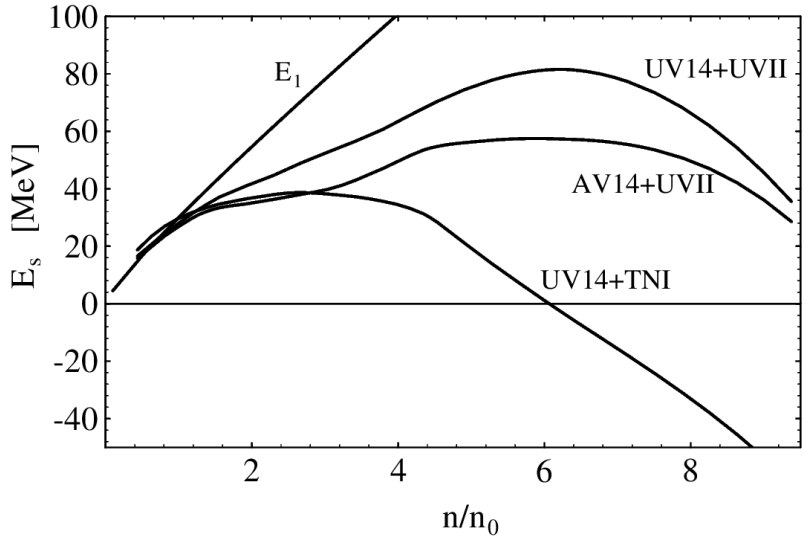
isospin symmetry \longrightarrow four nuclear currents:

$$\bar{\psi}\psi, \quad \bar{\psi}\gamma^\mu\psi, \quad \bar{\psi}\gamma^\mu\vec{\tau}\psi, \quad \bar{\psi}\vec{\tau}\psi$$

so, the fourth „meson” $\longrightarrow \vec{\delta}$ /true $a_0(980)$ /
 scalar-isovector

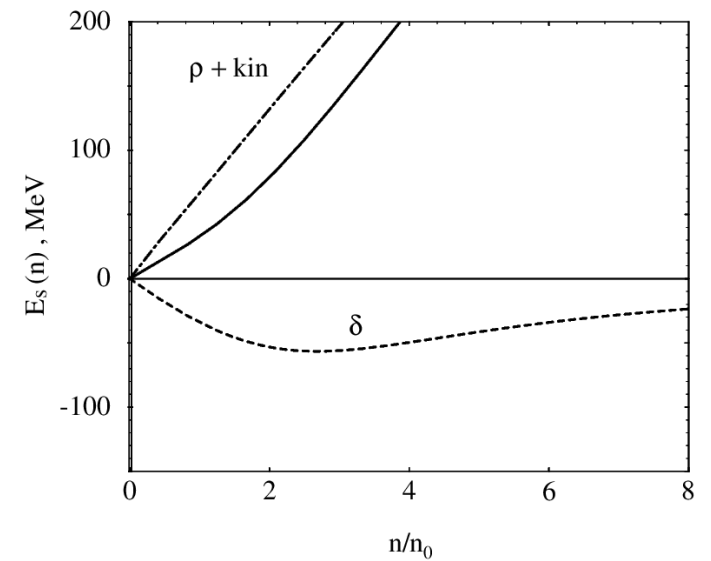
nucleon mass splitting $m_i = m_B - g_\sigma\sigma \pm g_\delta\delta_3$

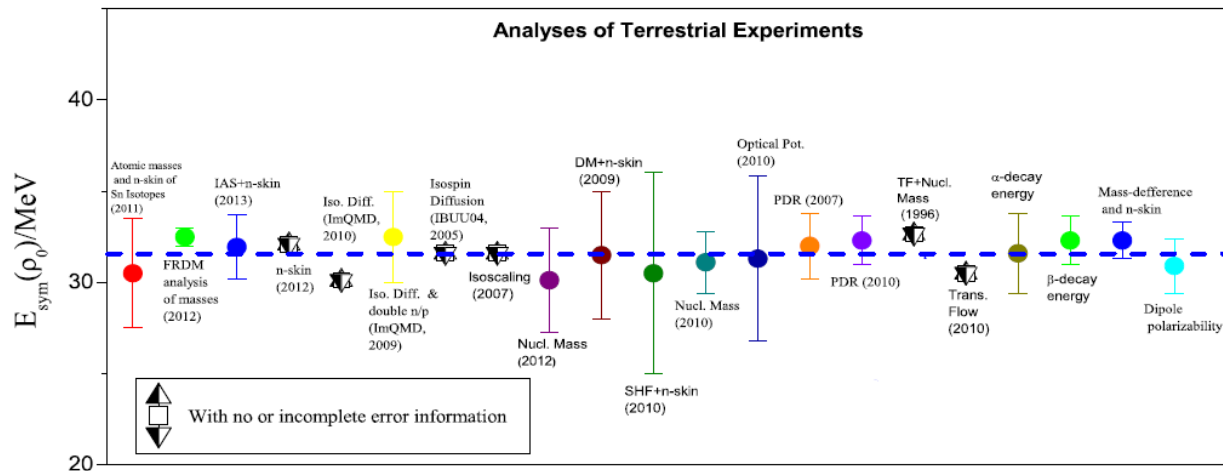
$$E_{\text{sym}}(n) = \frac{1}{8}C_\rho^2 n + \frac{k_0^2}{3E_{F,0}} - C_\delta^2 \frac{m_0^2 n}{2E_{F,0}^2 \left(1 - 3C_\delta^2 \left(\frac{n}{E_{F,0}} - \frac{n_s}{m_0}\right)\right)}$$



δ - contribution
 decreases with n

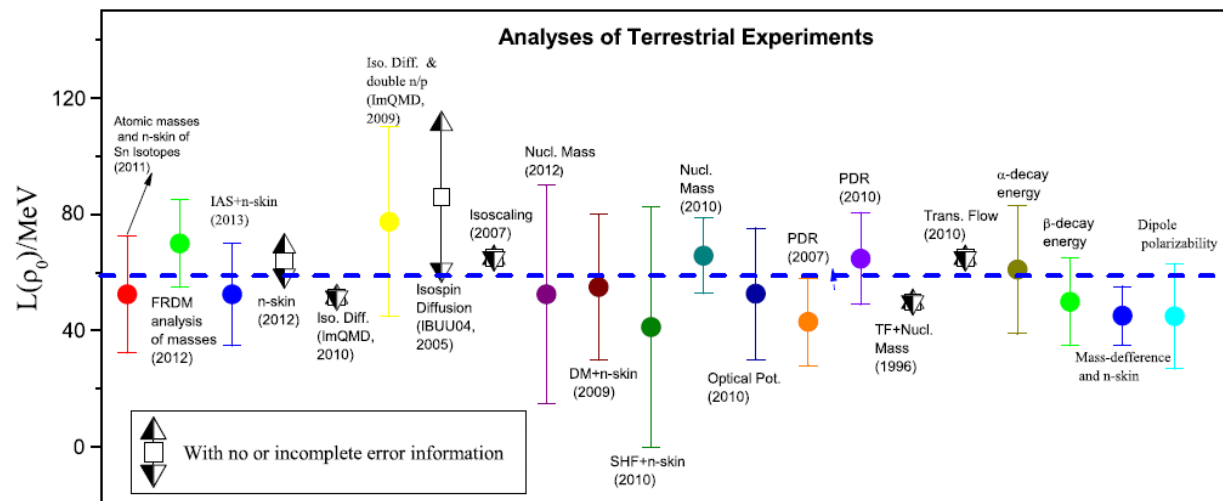
Kubis, Kutschera PLB399 (1997)



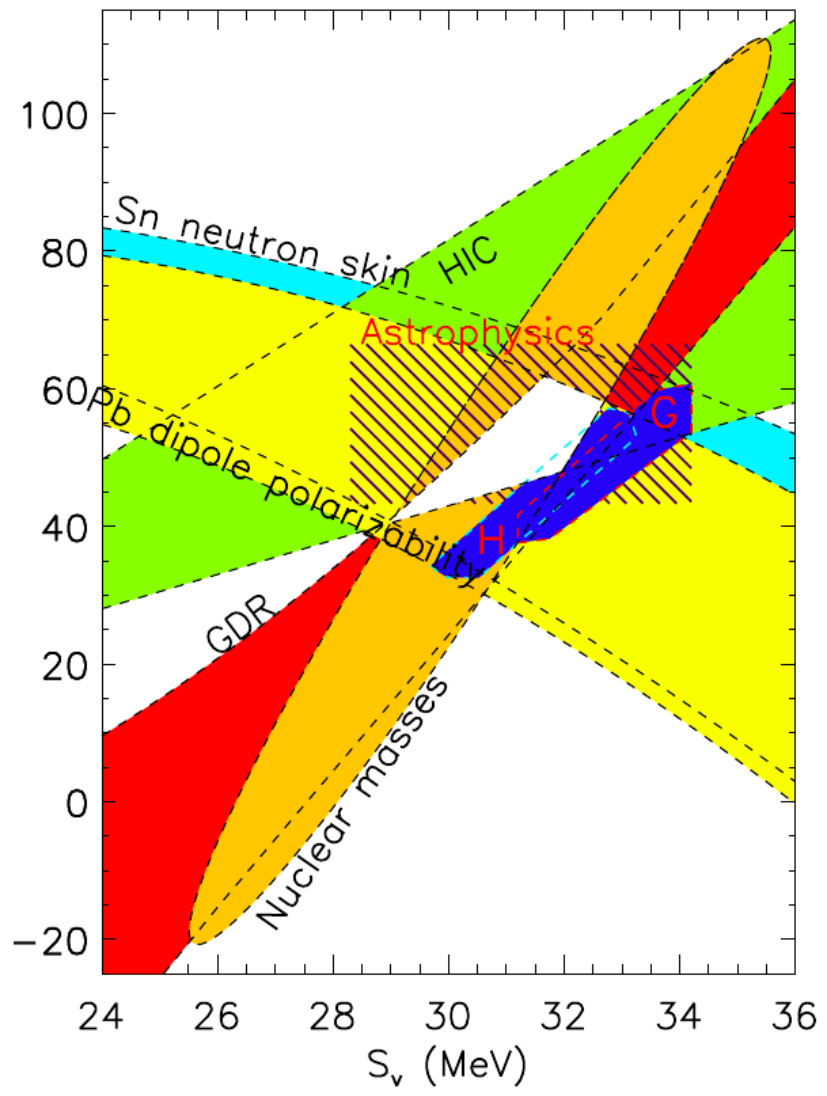
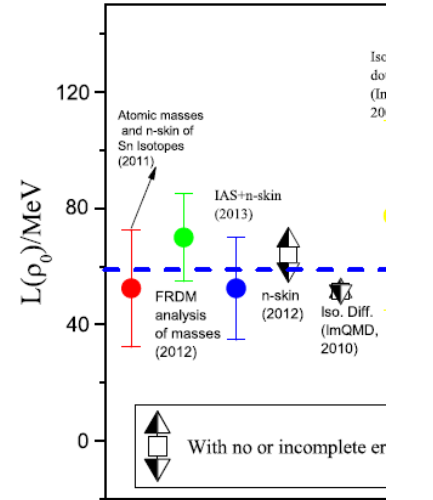
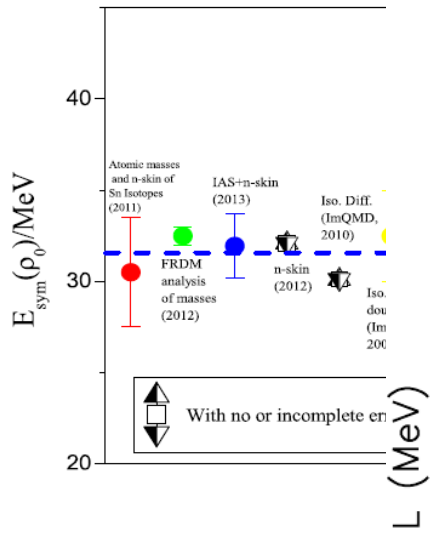


Li, Han, PLB727 (2013)

$$E_s = 30 - 32 \text{ MeV}$$



$$L = 20 - 100 \text{ MeV}$$



Li, Han, PLB727 (2013)

$$E_s = 30 - 32 \text{ MeV}$$

$$L \approx 50 \text{ MeV}$$

standard RMF : $L > 90 \text{ MeV}$?

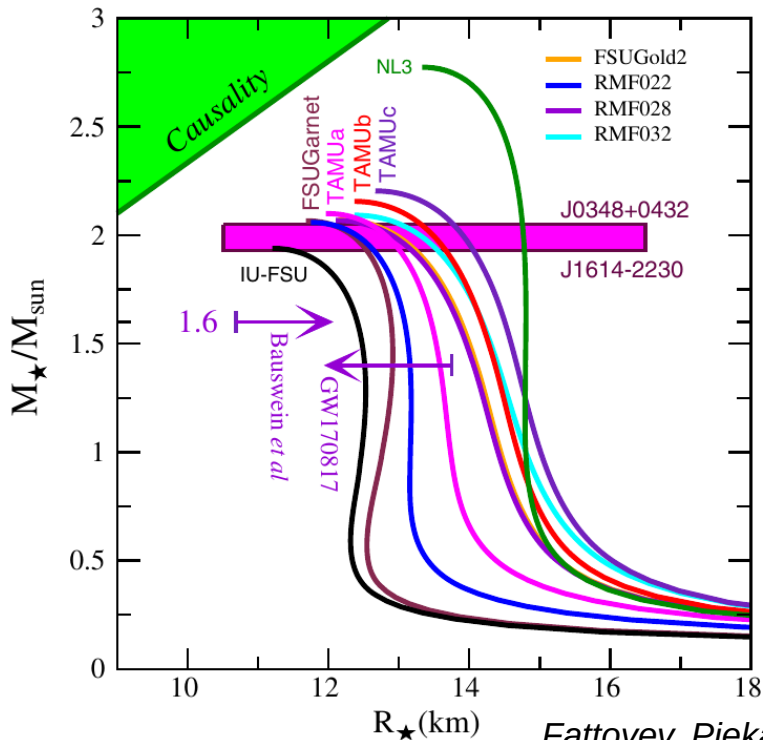
Lattimer, Lim ApJ771 (2013)

Crossing terms come into play

FSUGold model: $(\omega_\mu \omega^\mu)^2 \longrightarrow$ EoS stiffness , max mass of NS

Todd-Rutel, Piekarewicz PRL95

$\omega_\mu \omega^\mu \vec{\rho}_\mu \cdot \vec{\rho}^\mu \longrightarrow$ symmetry energy behaviour



Fattoyev, Piekarewicz PRL120 (2018)

fitted to ground state properties of nuclei

FSUGold „families” - different parametrization

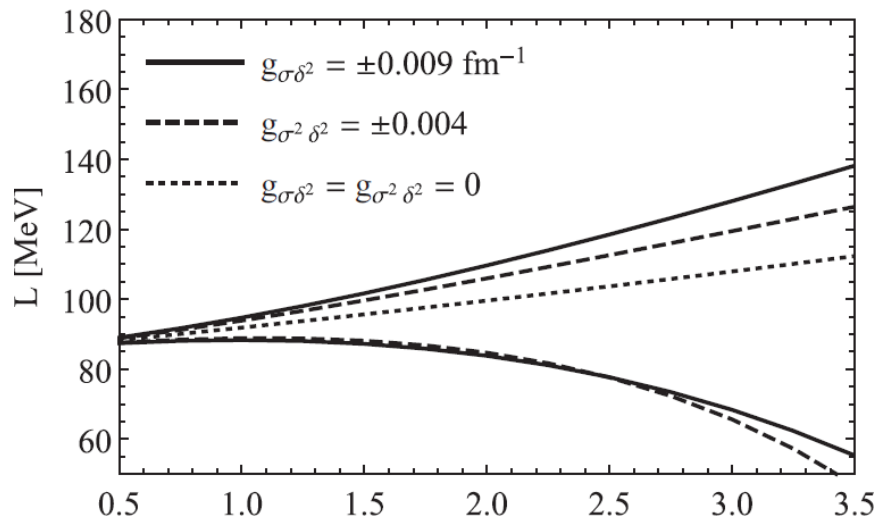
$L = 45 - 108$ MeV

two scalars crossing term

why not scalars? work well at low energy - ChiralPT

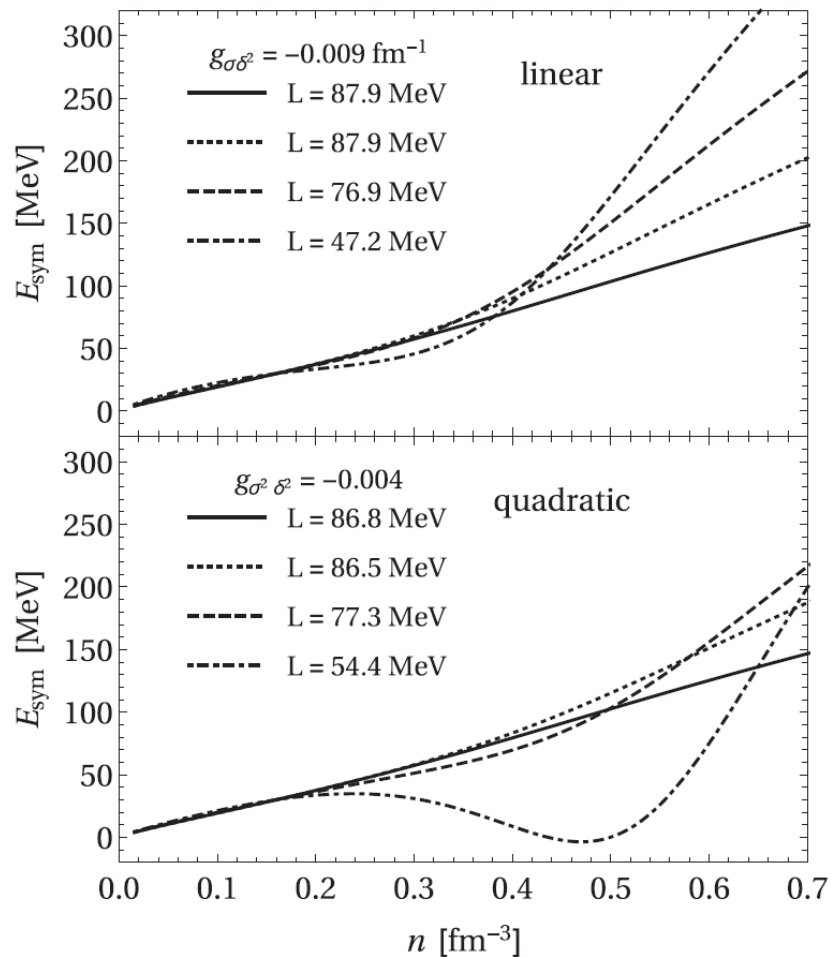
$\sigma^n (\vec{\delta} \cdot \vec{\delta})^m$ justified by isospin symmetry

$\sigma \vec{\delta} \cdot \vec{\delta}$ „linear” strategy:
 $\sigma^2 \vec{\delta} \cdot \vec{\delta}$ „quadratic” keep fixed coupling for crossing term
 and vary delta-nucleon coupling

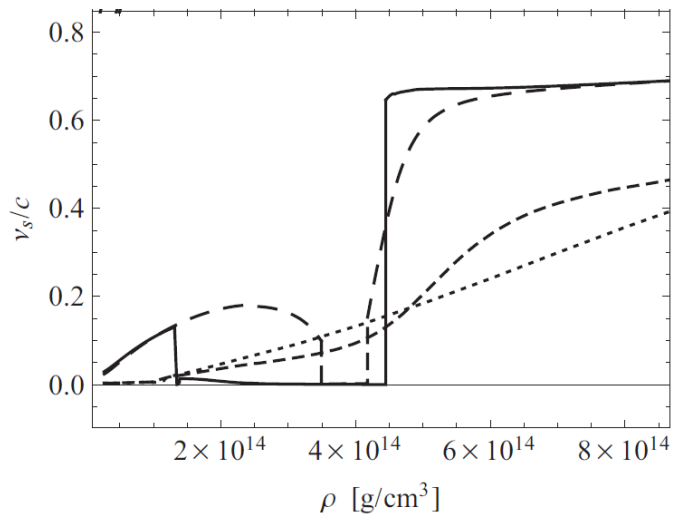
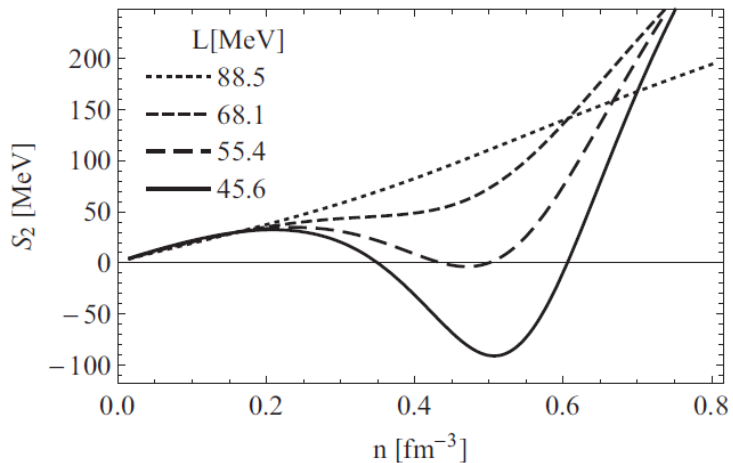


$$g_\delta \bar{\psi} \vec{\delta} \cdot \vec{\tau} \psi \longrightarrow C_\delta^2 = \frac{g_\delta}{m_\delta} \quad C_\delta^2 \text{ [fm}^2\text{]}$$

Zabari, Kubis, PRC99 (2018)

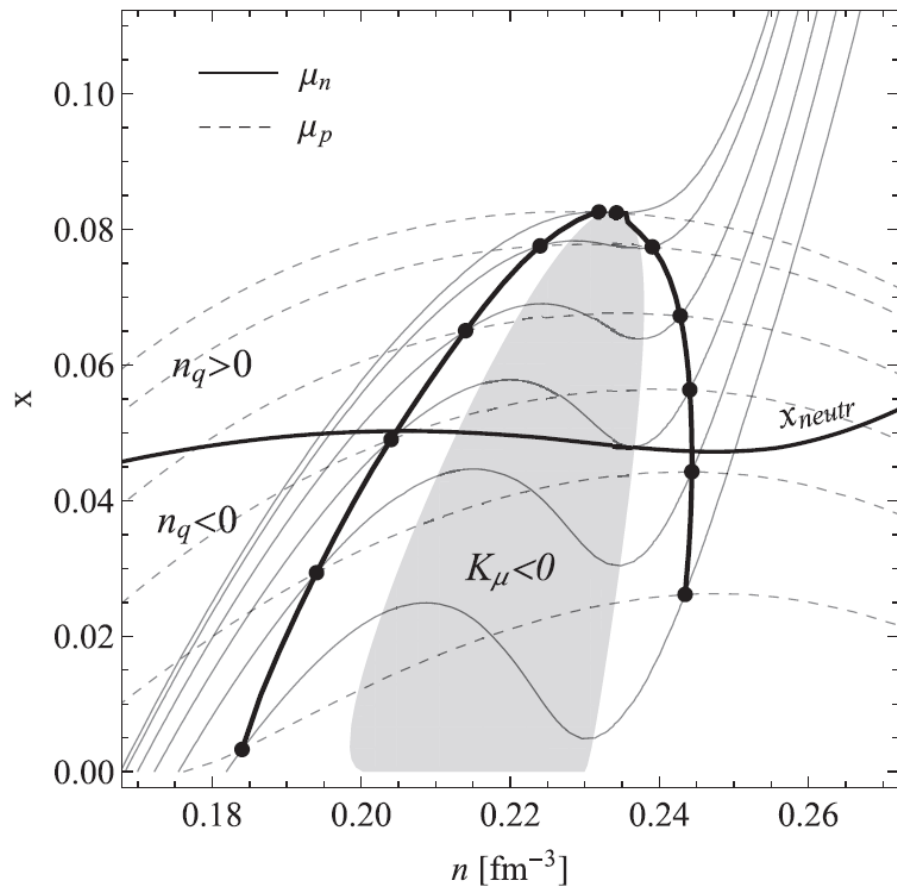


low $L \rightarrow$ symm. energy bending
phase transition



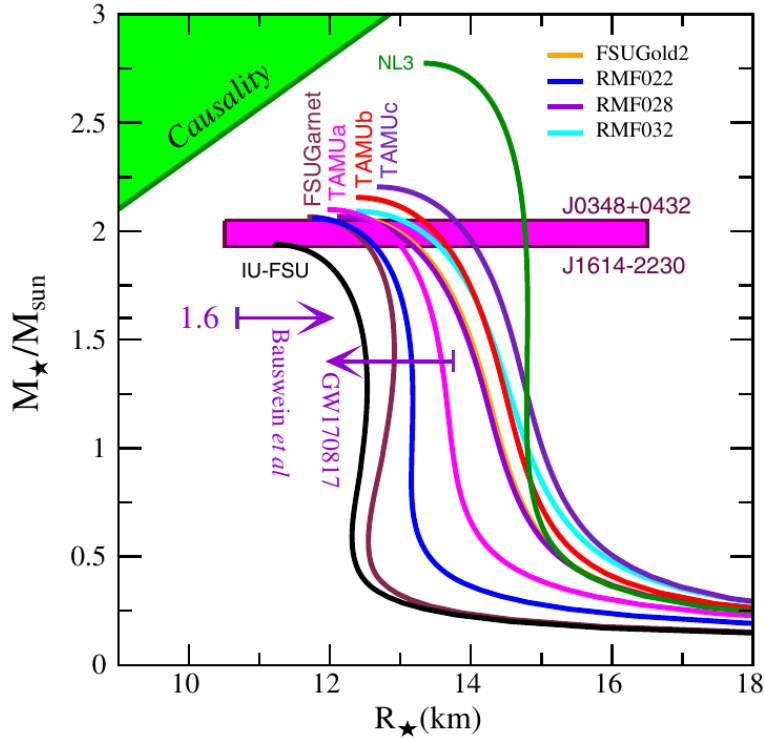
$$\sigma^2 \vec{\delta} \cdot \vec{\delta}$$

spinodal region, Gibbs conditions

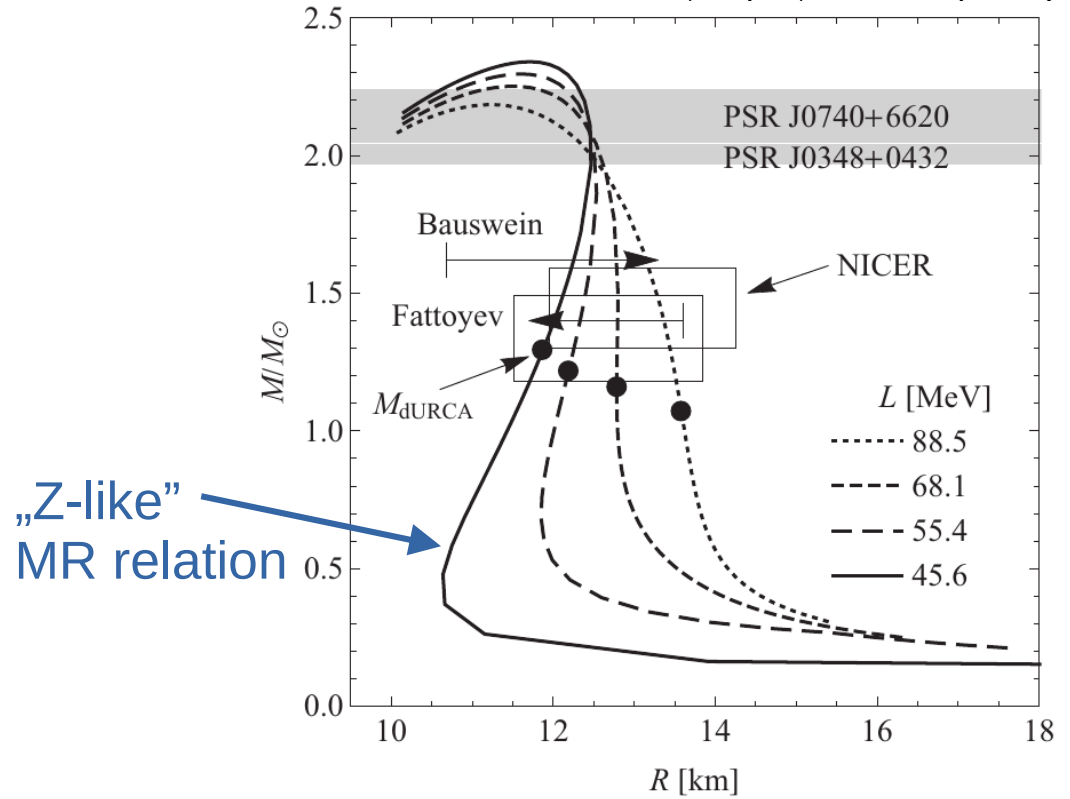


symmetry energy and NS radius

larger $L \rightarrow$ larger R



Kubis, Wóicik, PRC102 (2018)



scalar „works” at lower densities!

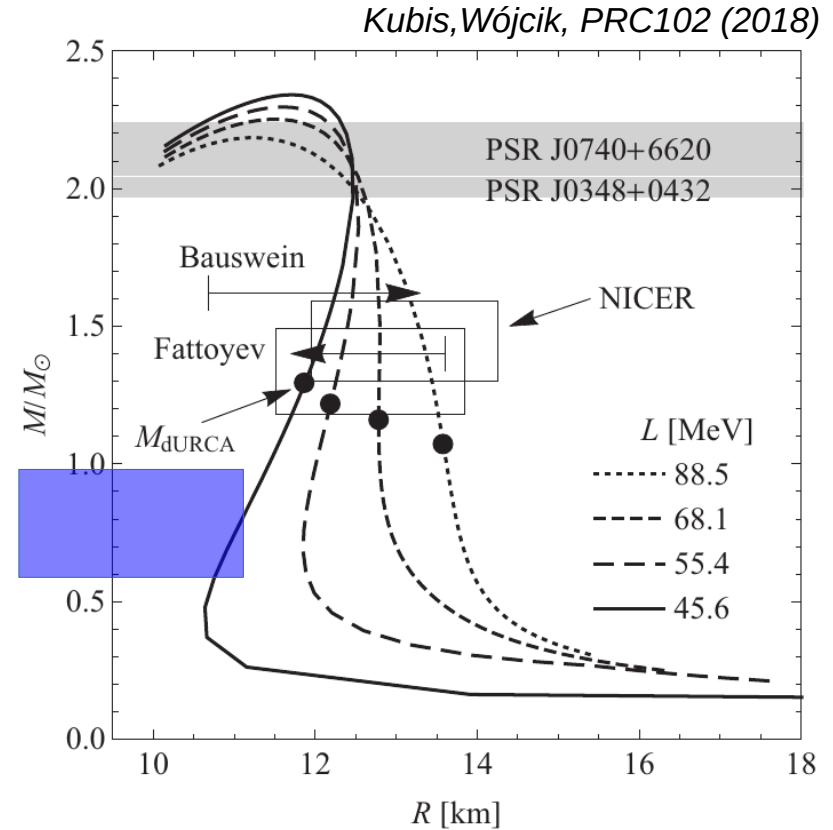
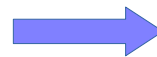
symmetry energy and NS radius

HESS 1731-347
CCO in supernova remnant

$$R = 10.4^{+0.86}_{-0.78} \text{ km}$$

$$M = 0.77^{+0.20}_{-0.17} M_{\odot}$$

Doroshenko et.al. Nature Astr. 6 (2022)

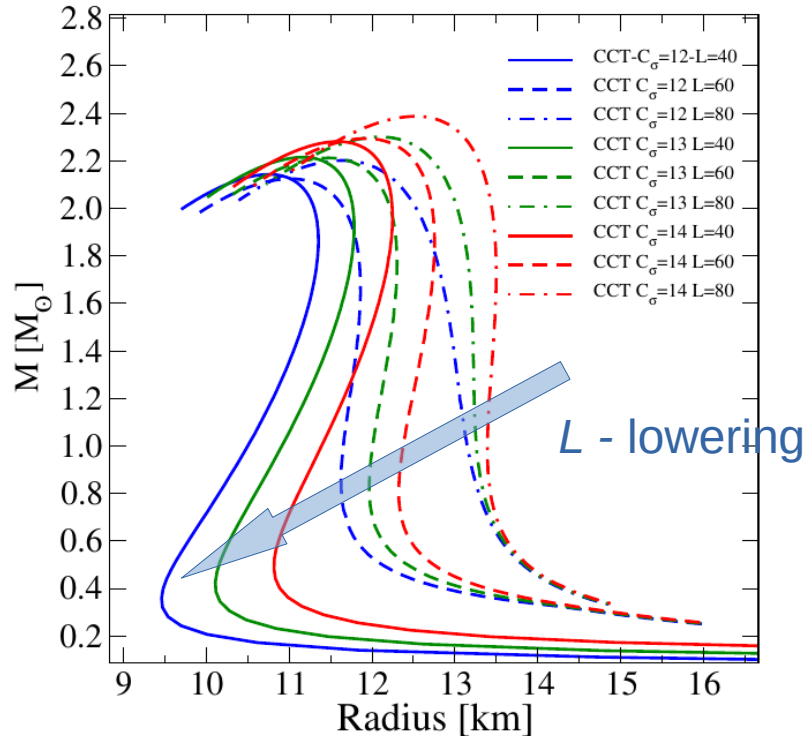


can't be $L < 40$??

scalar-scalar OK , why not vector-scalar ?

$$\mathcal{L}_{\text{CCT}} = \frac{1}{2}g_{\sigma\delta} \sigma^2 \vec{\delta}^2 + \frac{1}{2}g_{\omega\delta} \omega_\mu \omega^\mu \vec{\delta}^2$$

Cracow Crossing Terms model 



submitted to PRC

6 model parameters fitted to sat.point properties

two free parameters:

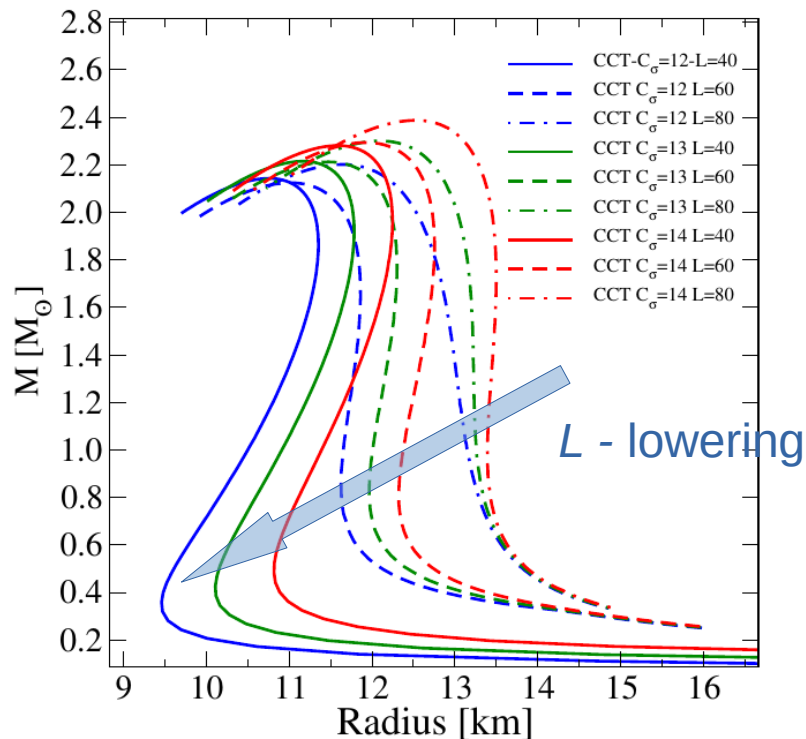
$$C_\sigma^2 = 12 - 14 \text{ fm}^2 \quad \text{EoS stiffness}$$

$$C_\delta \text{ controls } L = 40 - 80 \text{ MeV}$$

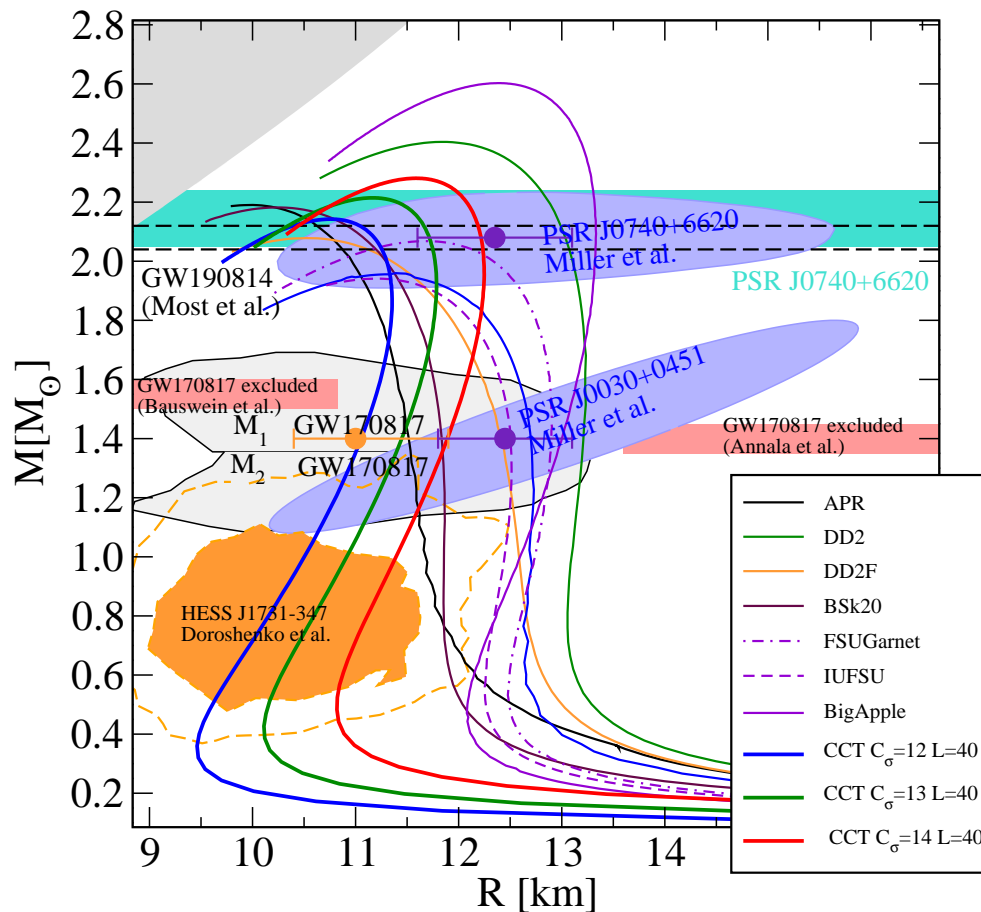
phase transition occurs for $L < 50 \text{ MeV}$

scalar-scalar OK , why not **vector-scalar** ?

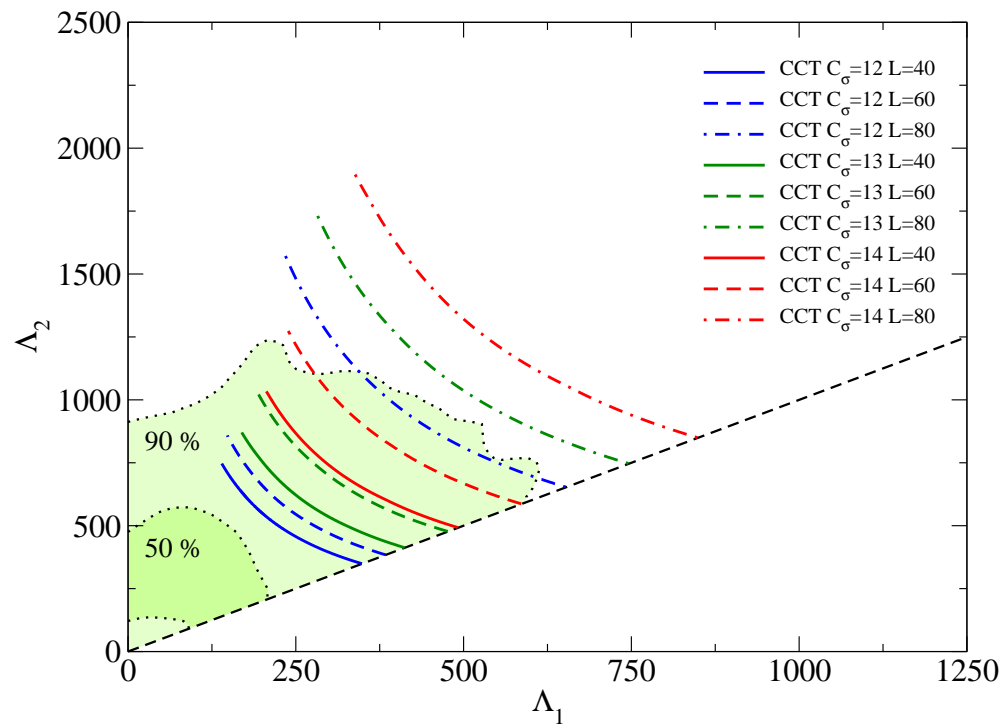
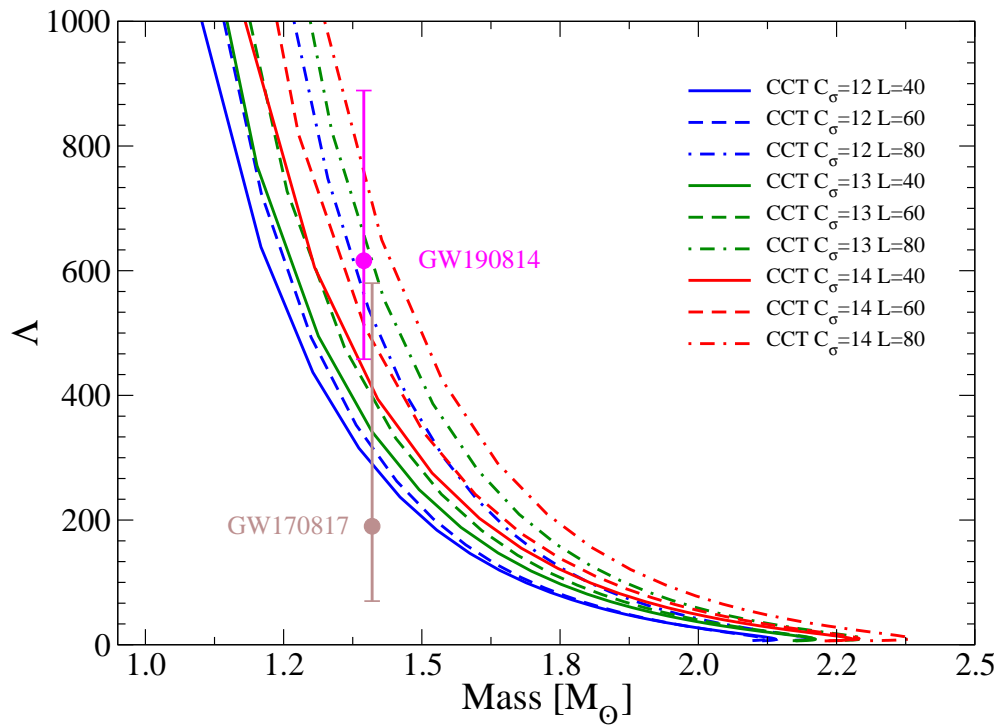
$$\mathcal{L}_{\text{CCT}} = \frac{1}{2} g_{\sigma\delta} \sigma^2 \delta^2 + \frac{1}{2} g_{\omega\delta} \omega_\mu \omega^\mu \delta^2$$



submitted to PRC



tidal deformabilities from GW events



open question:

- at $n \approx 3n_0$ a gap between proton and neutron eff. mass
→ isospin symmetry breaking

for future:

- cooling with dUrca - amplitude dependent on eff. masses
- fit the model to ground-state properties of nuclei
- include vector-vector crossing terms