

Spectroscopic factors for halo states from knockout reactions and Coulomb breakup



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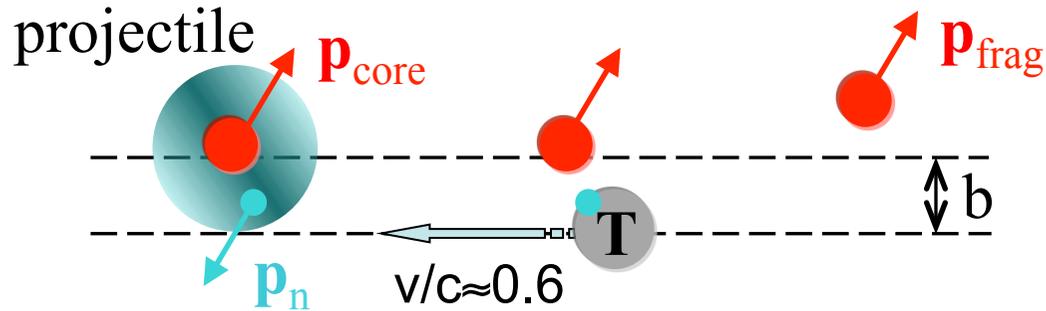


24th April 2012

***The Extreme Matter Physics of Nuclei:
From Universal Properties to Neutron-Rich Extremes
EMMI workshop April 2012 (GSI)***

- Knockout reactions with radioactive beams
- Comparison with Coulomb breakup and sensitivity

One-Nucleon Knockout: a Spectroscopic Tool



Sudden process

Reaction: $\Delta t \approx 10^{-22}$ s

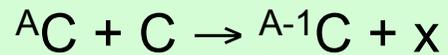
Internal motion: $\approx 10^{-21}$ s

$$\Rightarrow \mathbf{P}_{\text{frag}} = -\mathbf{P}_{\text{n}}$$

\Rightarrow probing the valence nucleon wave function (at the surface: $b_c > r_c$)

Example:

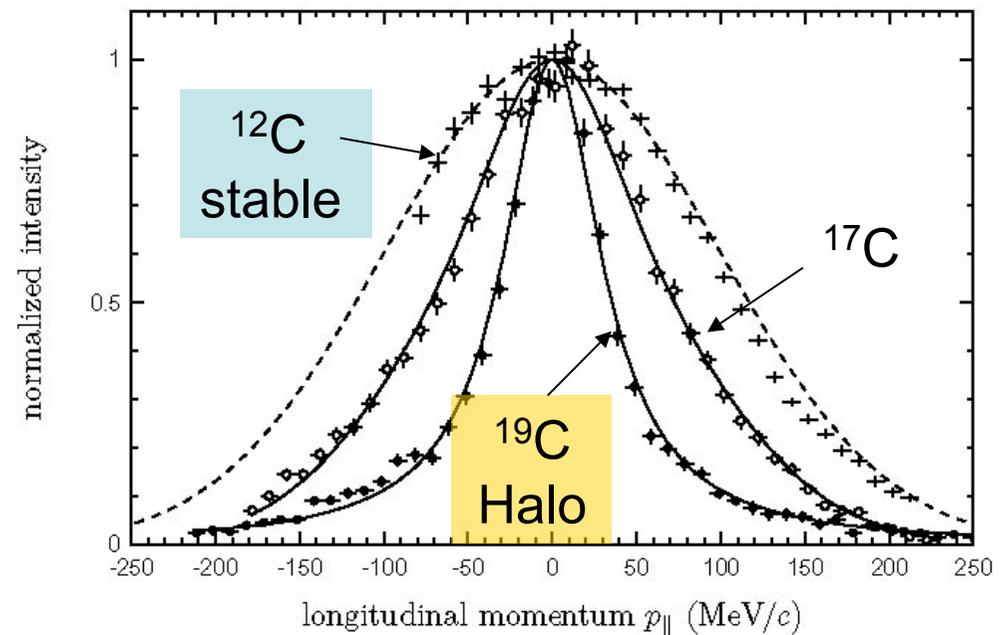
Carbon isotopes



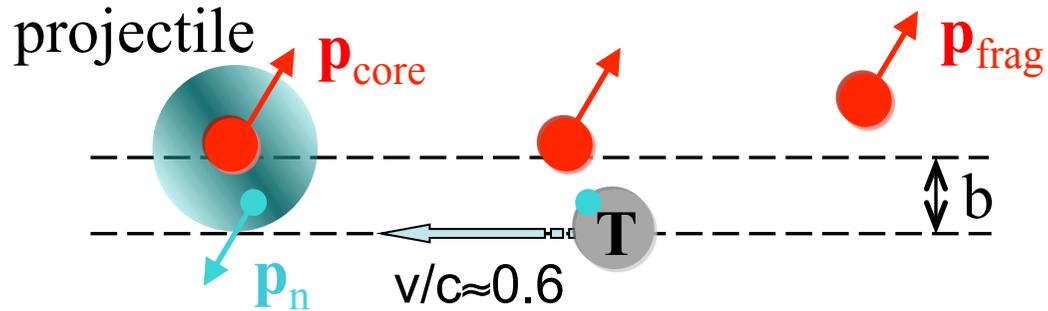
$E \approx 900$ MeV/u

FRS@GSI

T. Baumann et al.



One-Nucleon Knockout: a Spectroscopic Tool



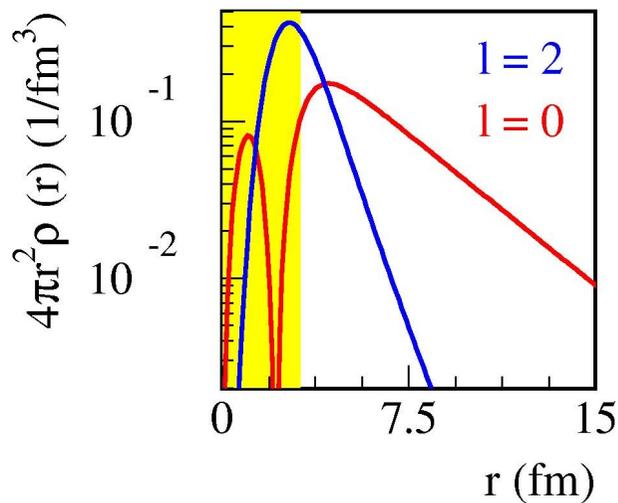
Sudden process

Reaction: $\Delta t \approx 10^{-22}$ s

Internal motion: $\approx 10^{-21}$ s

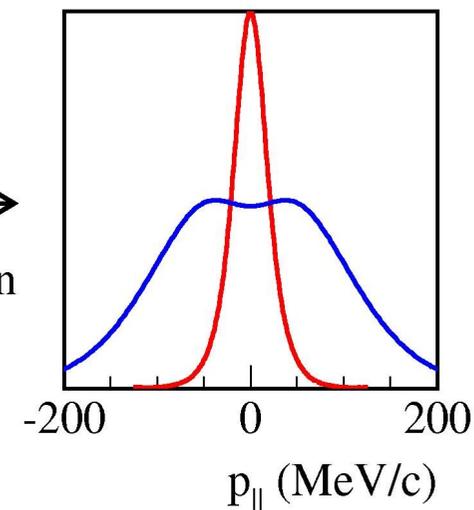
$$\Rightarrow \mathbf{P}_{\text{frag}} = -\mathbf{P}_n$$

\Rightarrow probing the valence nucleon wave function (at the surface: $b_c > r_c$)



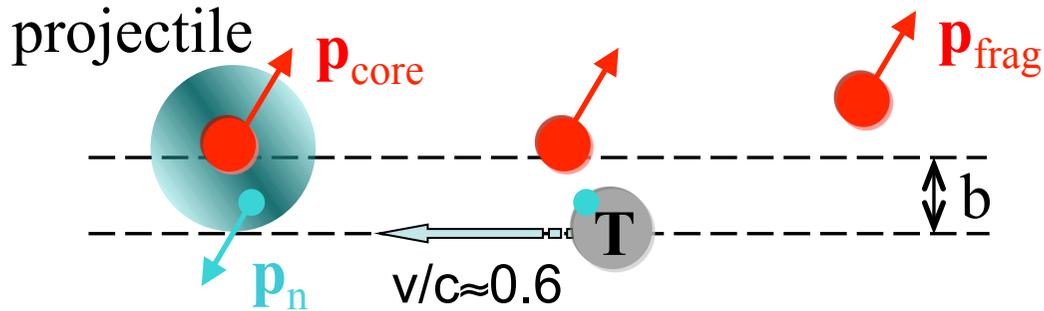
Extended
Wavefunction

Fourier
transformation



Narrow
Momentum Distribution

One-Nucleon Knockout: a Spectroscopic Tool



Sudden process

Reaction: $\Delta t \approx 10^{-22}$ s

Internal motion: $\approx 10^{-21}$ s

$$\Rightarrow \mathbf{P}_{\text{frag}} = -\mathbf{P}_n$$

\Rightarrow probing the valence nucleon wave function (at the surface: $b_c > r_c$)

Measurement	Extracted Information
Momentum distribution	\Rightarrow l -value of removed nucleon
γ -ray coincidence	\Rightarrow identification of core-state
invariant mass (unbound states)	
Cross section	\Rightarrow spectroscopic factor

$$\sigma_{ln}(J^\pi) = S(J^\pi) \times \sigma_{sp}(l, S_n)$$

Eikonal
calculation

Single-particle cross sections

$$\sigma_{sp}(J^\pi) = \sigma_{sp}^{knockout} + \sigma_{sp}^{diffraction}$$

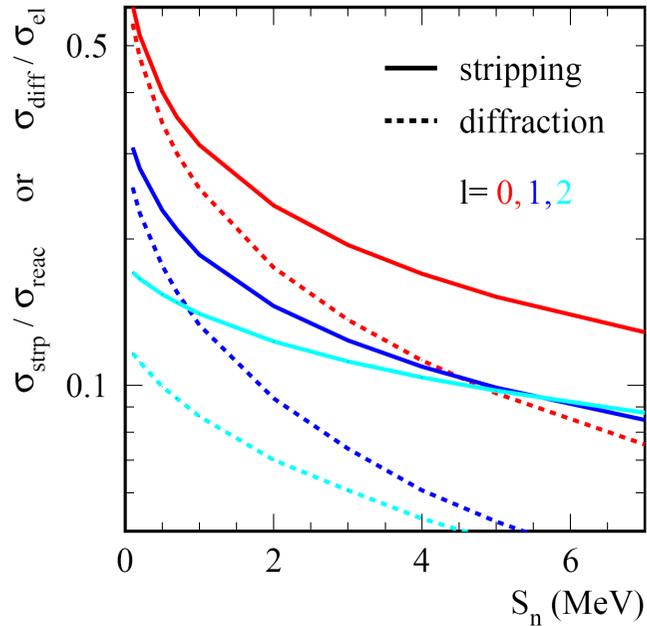
Eikonal approximation:

$$\sigma_{sp}^{knockout}(J^\pi) = \int d^2b \int d^3r |\Phi_{l,S_n}(\mathbf{r})|^2 S_c^2(\mathbf{b}_c) (1 - S_n^2(\mathbf{b}_n))$$


core survival reaction
'shadowing' n + target

- $\Phi_{l,S_n}(\mathbf{r})$ is calculated for a Woods-Saxon Potential
- S_c, S_n are calculated using target and core density distributions
+ free NN cross sections + energy dep. ratio of imaginary to real part
- no free parameters

One-neutron removal reaction (nuclear breakup)



Reaction mechanisms:

- knockout (stripping)
- inelastic scattering (diffraction)

cross section dominated by knockout for

- high beam energies
- non-halo states

$$p_{stripping} = \langle S_c^2(\mathbf{b}_c)[1 - S_n^2(\mathbf{b}_n)] \rangle$$

$$p_{inelastic} = \langle [1 - S_c(\mathbf{b}_c)S_n(\mathbf{b}_n)]^2 \rangle - \langle 1 - S_c(\mathbf{b}_c)S_n(\mathbf{b}_n) \rangle^2$$

no-recoil limit: $A_c \gg 1$, $\mathbf{b}_c = \mathbf{b}$

$$p_{diffraction} = S_c^2 \langle [1 - S_n(\mathbf{b}_n)]^2 \rangle - S_c^2 \langle 1 - S_n(\mathbf{b}_n) \rangle^2$$

elastic scattering
of neutron

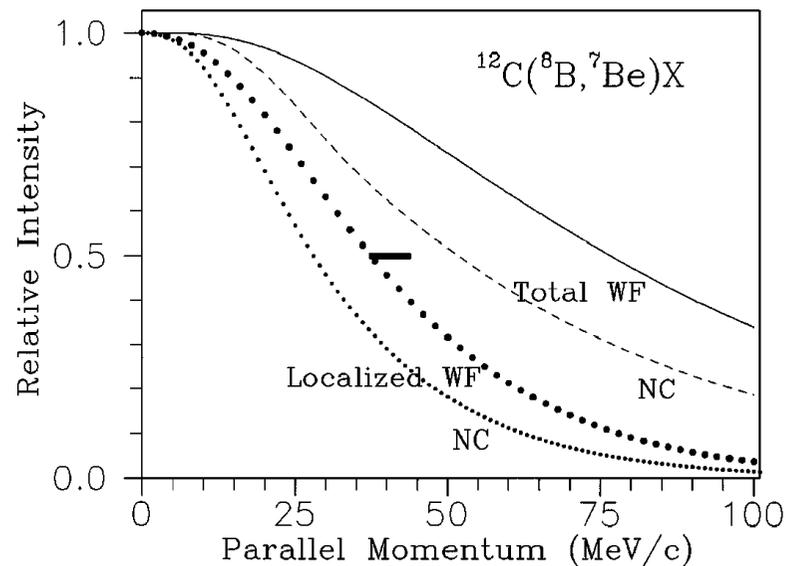
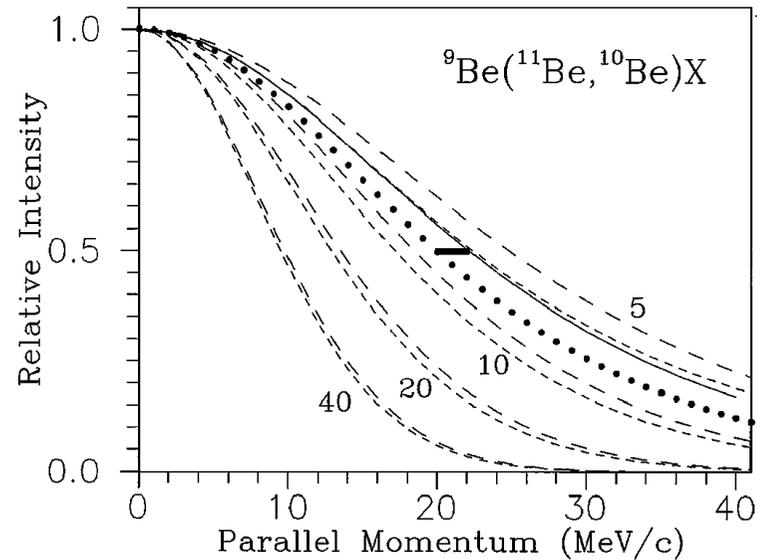
elastic scattering
of projectile

Momentum distributions and reaction mechanism

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PHYSICAL REVIEW LETTERS

5 AUGUST 1996

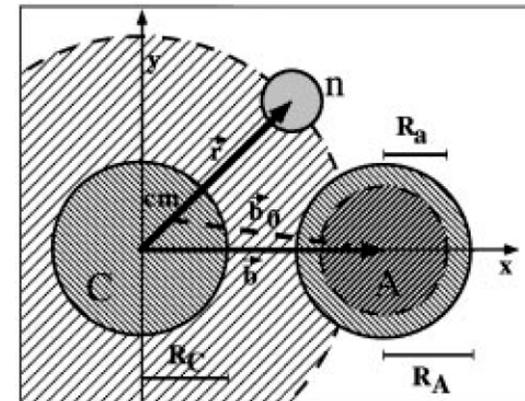


Momentum Content of Single-Nucleon Halos

P. G. Hansen

*National Superconducting Cyclotron Laboratory and Department of Physics and Astronomy,
Michigan State University, East Lansing, Michigan 48824-1321*

(Received 12 January 1996)



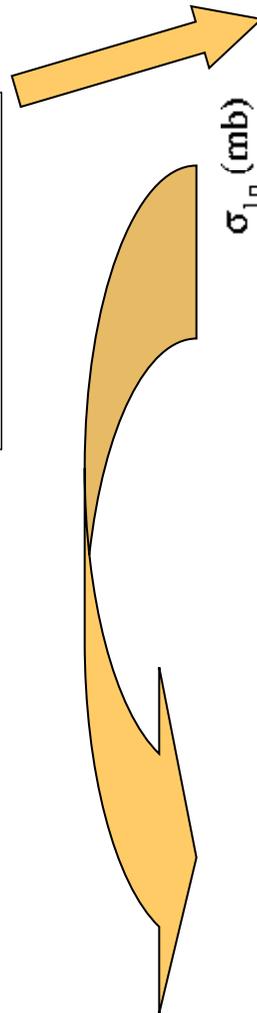
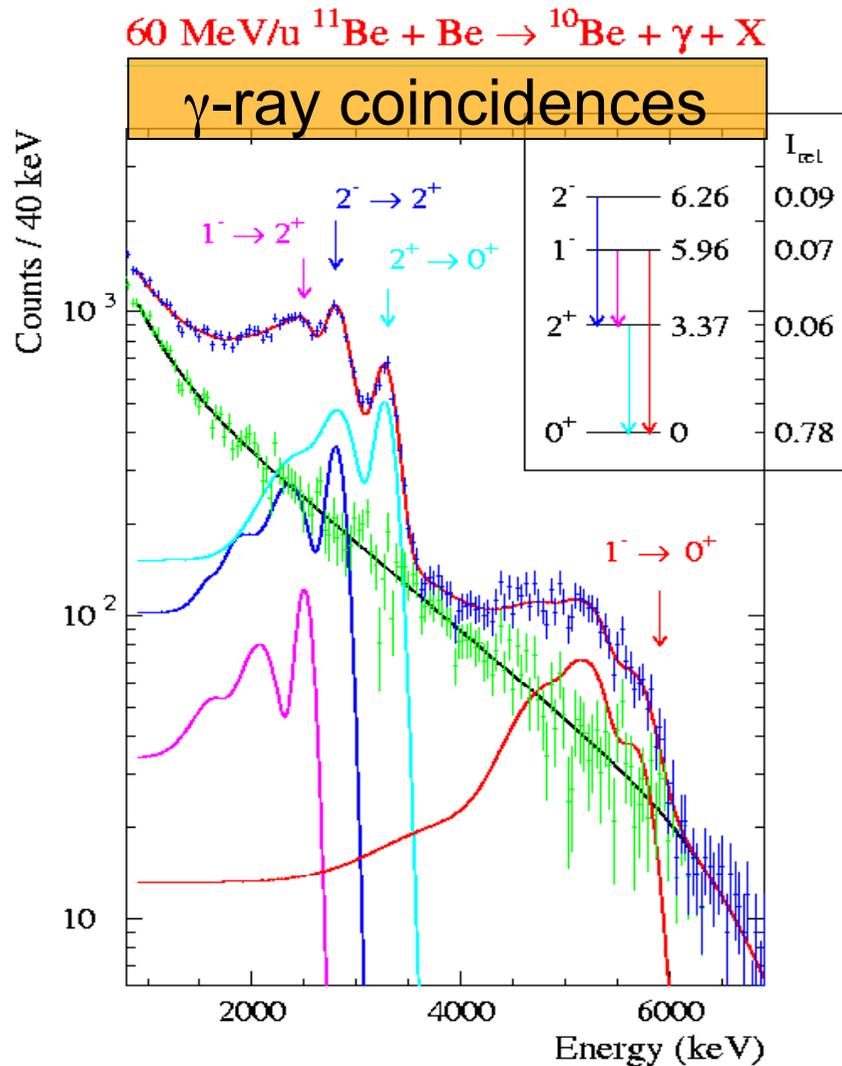
reaction samples only the surface of the nucleus

→ momentum distributions are more narrow than the full Fourier transform

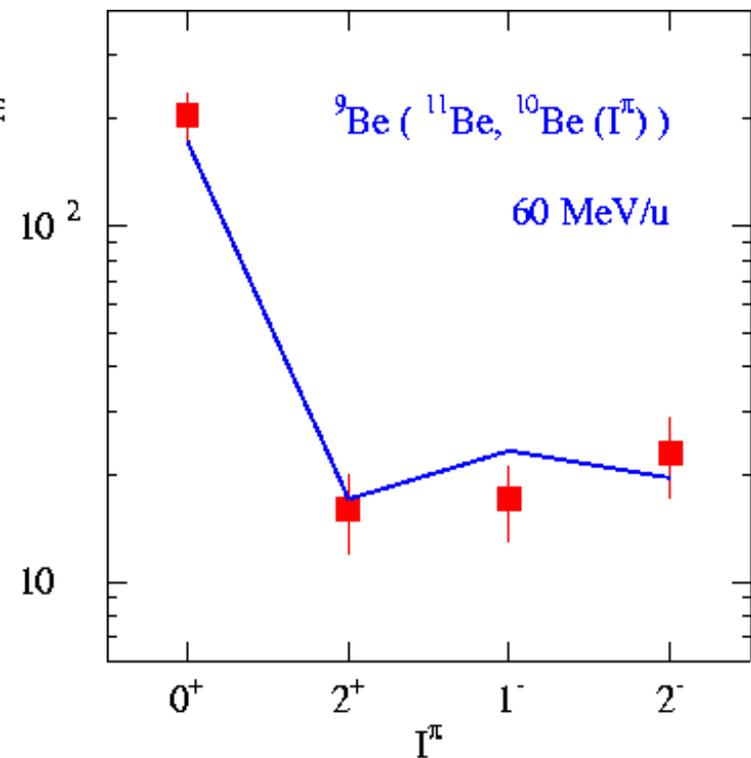
effect less pronounced for well developed halos

Neutron removal from individual single-particle states: $^{11}\text{Be} \rightarrow ^{10}\text{Be} (I^\pi) + \gamma + X$

Wave function: e.g. $|^{11}\text{Be}\rangle = \alpha |^{10}\text{Be}(0^+) \otimes 2s_{1/2}\rangle + \beta |^{10}\text{Be}(2^+) \otimes 1d_{5/2}\rangle + \dots$



Partial cross sections

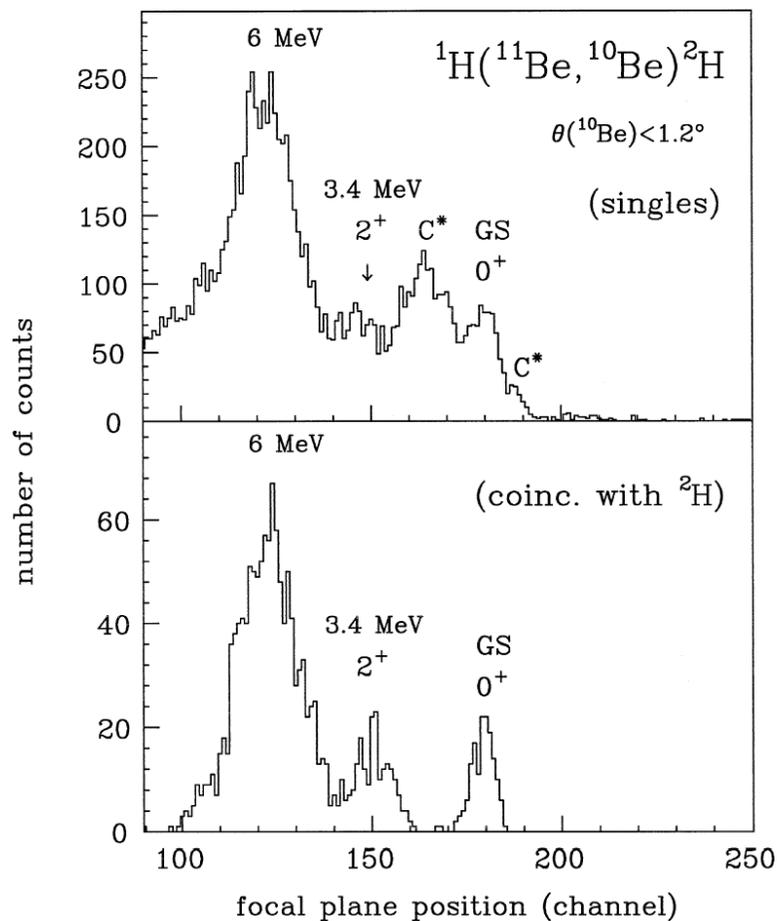


Spectroscopic factors

$S(0^+) \approx 0.8$
 $S(2^+) \approx 0.2$

Data: S800@MSU, T.Aumann *et al.*, PRL 84 (2000) 35

Comparison to transfer reactions

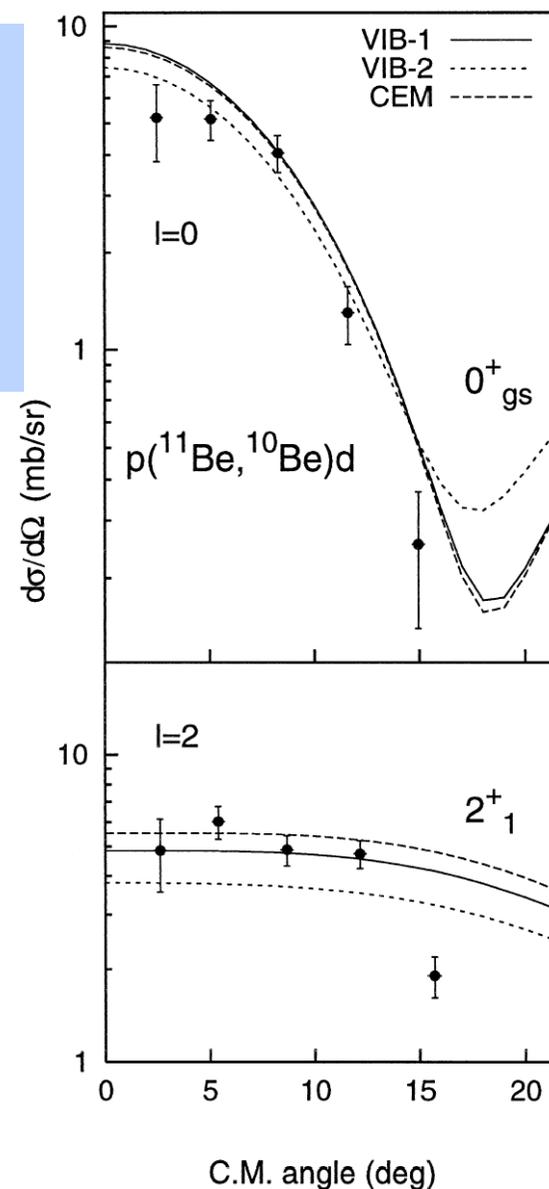


Transfer reaction in
 inverse kinematics:

GANIL, 35 MeV/u ${}^{11}\text{Be}$

S. Fortier et al.,
 PLB 461 (1999) 22

deduced
 spectroscopic
 factors in
 agreement with
 knockout reaction



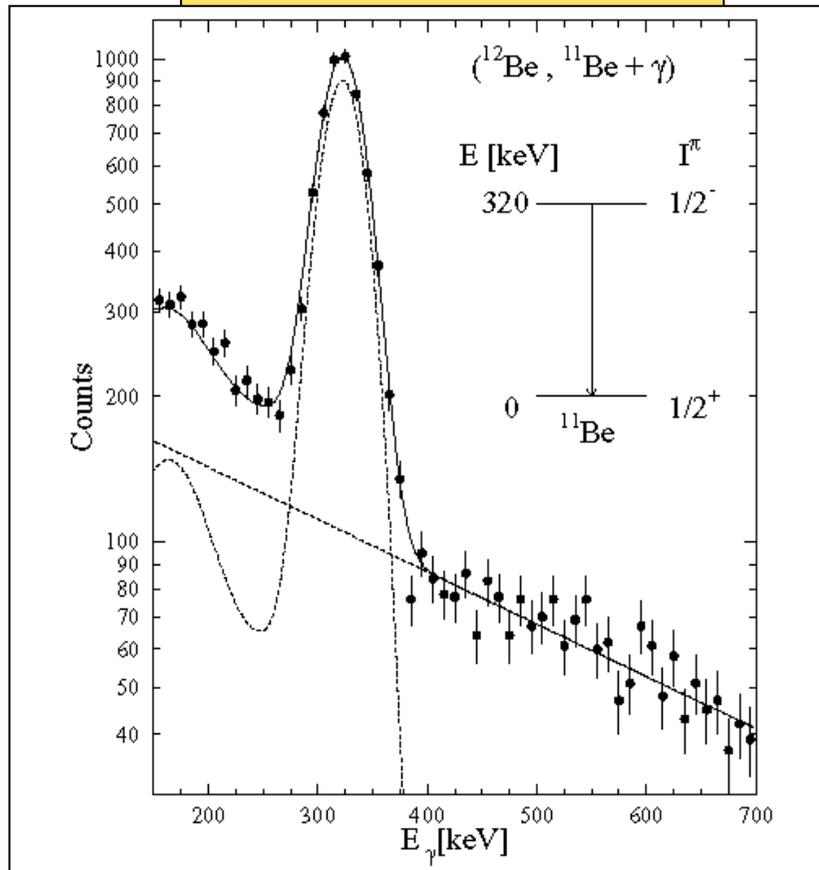
E_x (MeV)	J^π	SE-1 S_{exp}	VIB-1 S_{exp}	VIB-1 S_{th}	SE-2 S_{exp}	VIB-2 S_{exp}	VIB-2 S_{th}
0	0^+	0.66	0.67	0.84	0.79	0.79	0.84
3.368	2^+	0.28	0.17	0.16	0.38	0.22	0.16

^{12}Be : Breakdown of the N=8 Shell Closure

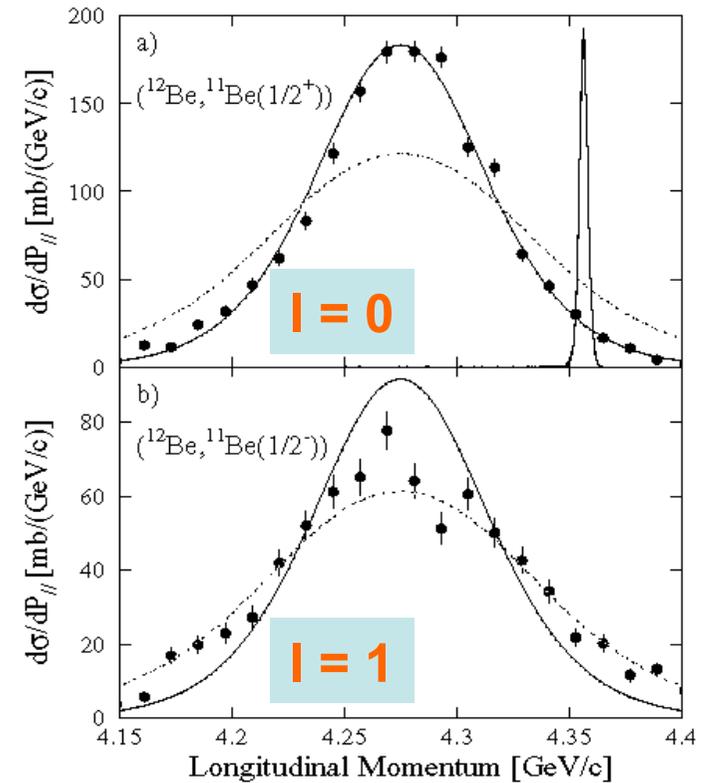
One-neutron removal reaction:



γ -ray coincidences



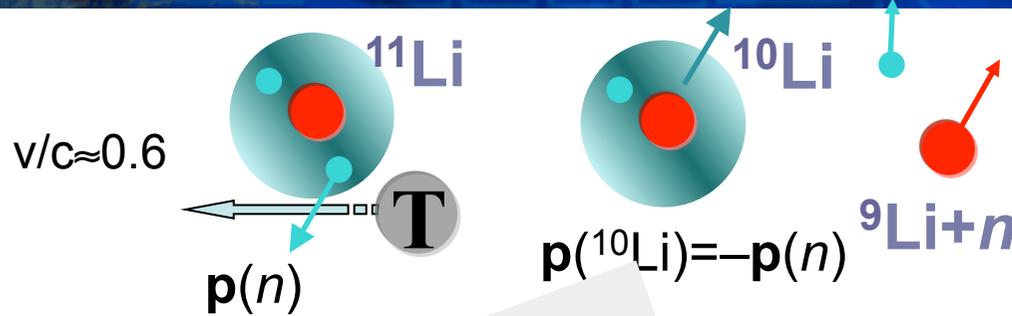
Momentum distributions



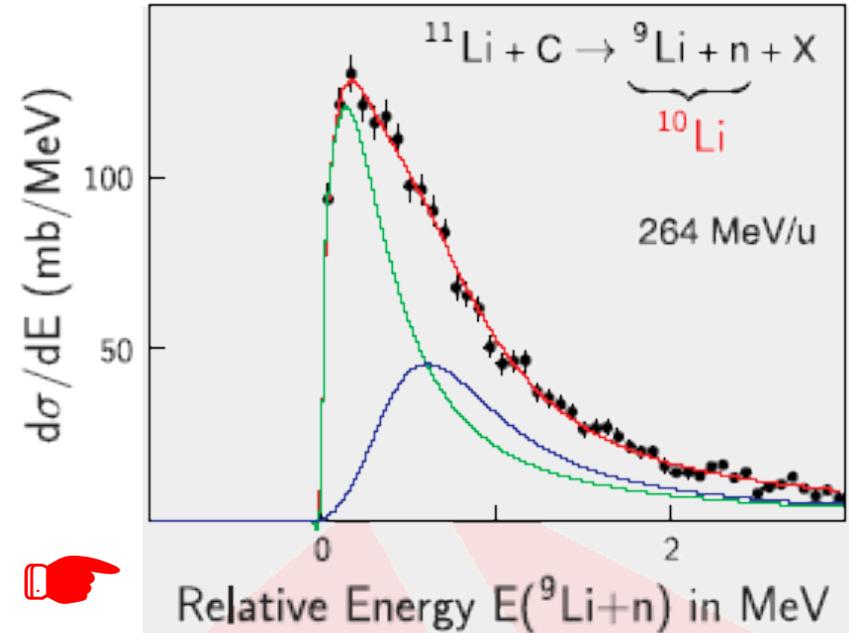
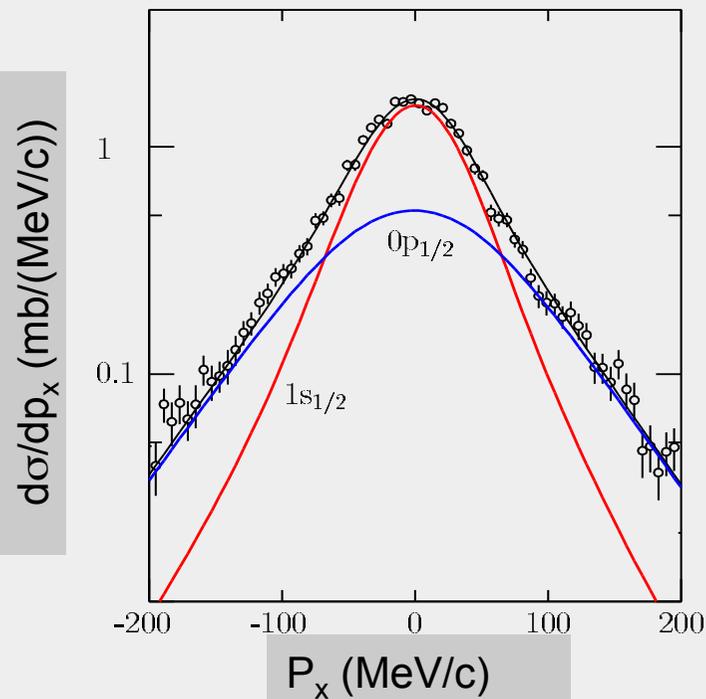
\Rightarrow Mixed configurations

$$(\nu s_{1/2})^2 / (\nu p_{1/2})^2 \approx 1$$

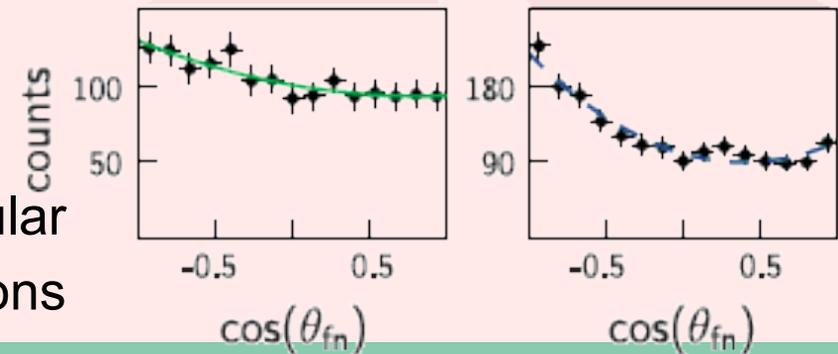
The halo of ^{11}Li : s and p waves



Momentum distribution ^{10}Li



Angular correlations



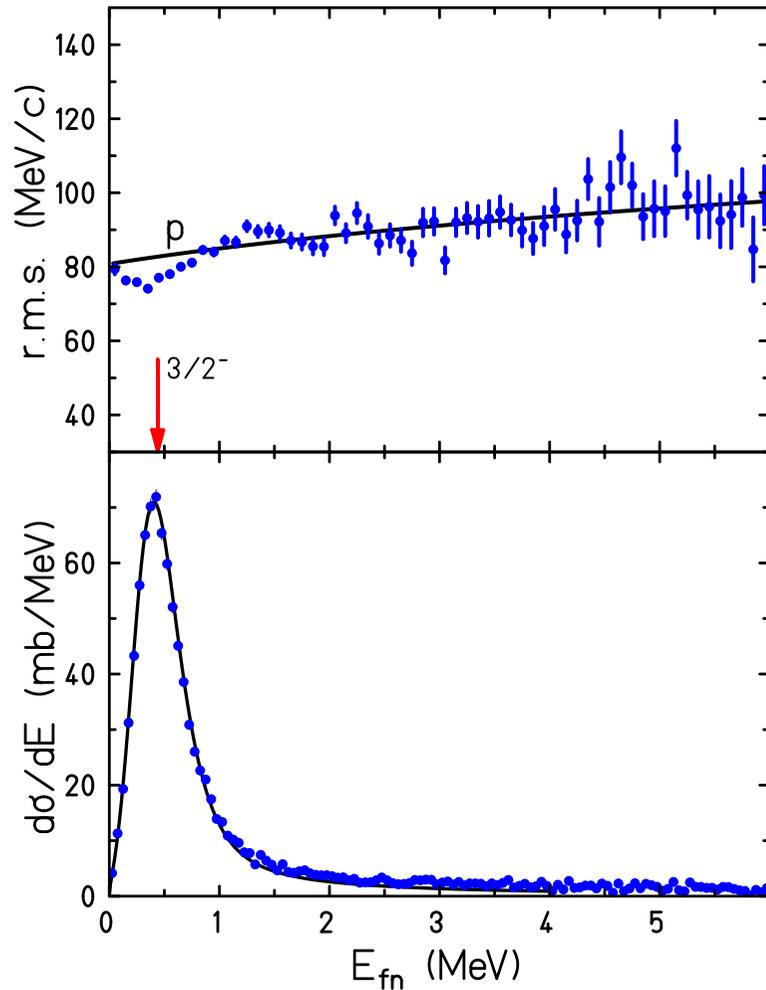
\Rightarrow Strong **s-wave** admixture

$$(s_{1/2})^2 / (p_{1/2})^2 \approx 1$$

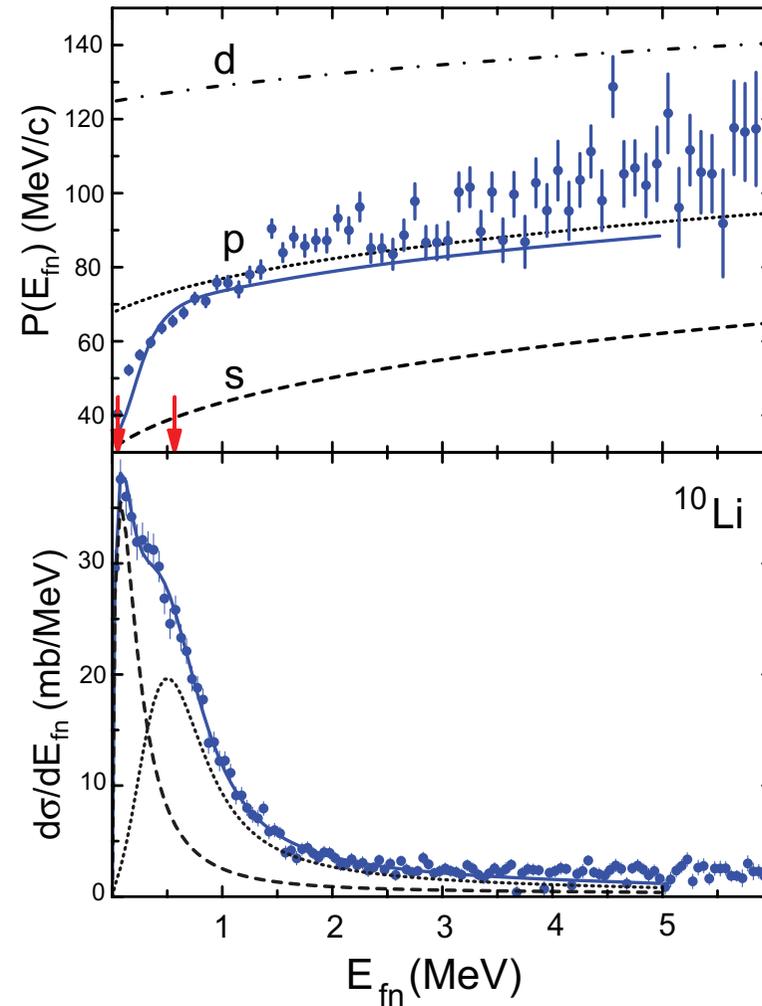
Data: LAND-FRS@GSI, H. Simon et al.,
Phys. Rev. Lett. 83 (99) 496

Momentum profile (rms width) as a function of relative energy in the unbound subsystem populated in 1n knockout

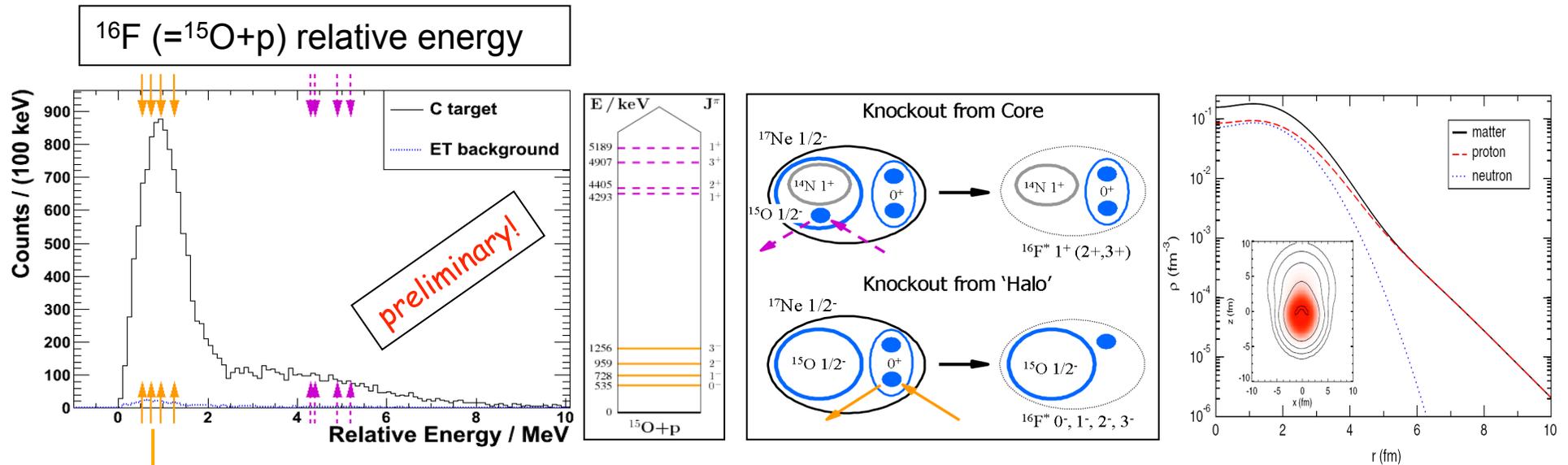
8He (p,pn) 7He -> 6He + n



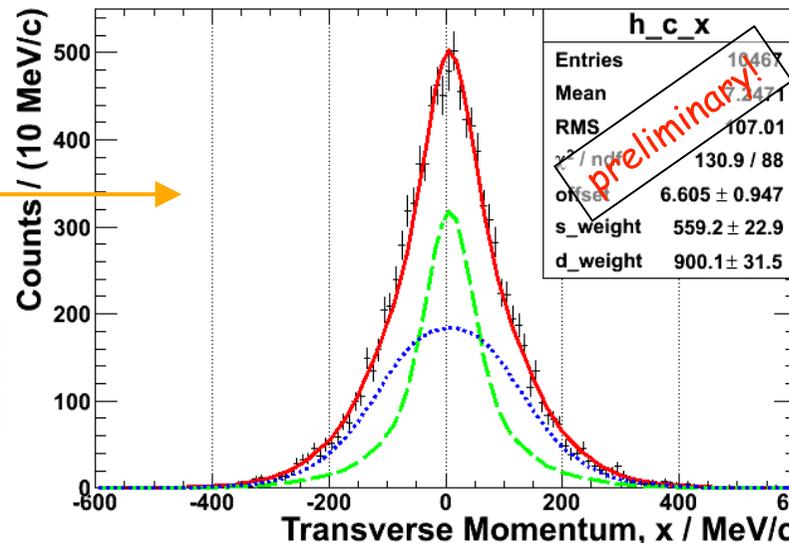
11Li (p,pn) 10Li -> 9Li + n



Selective one-proton knockout from core- and 'Halo'- states in ^{17}Ne

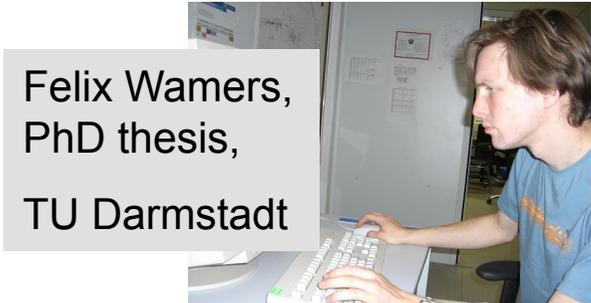


Exclusive selection of knockout from 'halo'-states for the first time possible!



s-wave content of ~40% moderate halo character

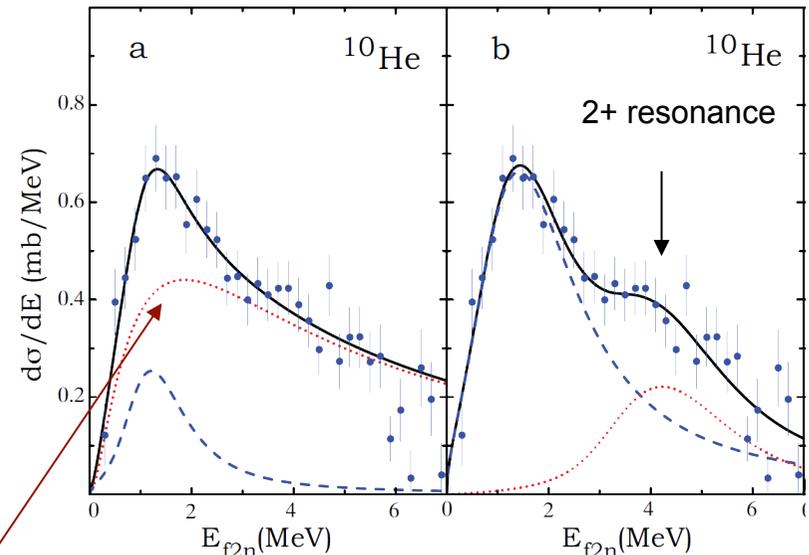
Good agreement with charge-radius measurement and FMD prediction of Geithner and Neff et al. *PRL* 101 (2008) 252502. and from 3b-model of Grigorenko, *PRC* 71 (2005) 051604(R).



Beyond the dripline: Ground and first excited state of ^{10}He - three-body correlations in the decay of unbound nuclei -

Li 4	Li 5	Li 6	Li 7	Li 8	Li 9	Li 10	Li 11	Li 12	Li 13
He 3	He 4	He 5	He 6	He 7	He 8	He 9	He 10		
H 1	H 2	H 3	H 4	H 5	H 6	H 7			
	n 1								

unbound nuclei observed at R3B



Unbound nuclear systems

problem of overlapping resonances

ambiguity: resonances or correlated background?

solution demonstrated for ^{10}He :

observation of characteristic 3-body correlations in the decay



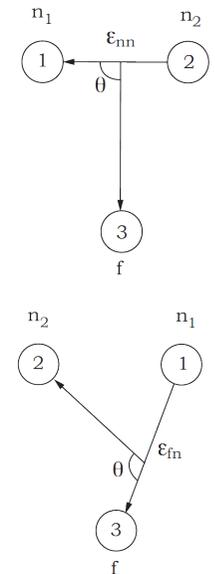
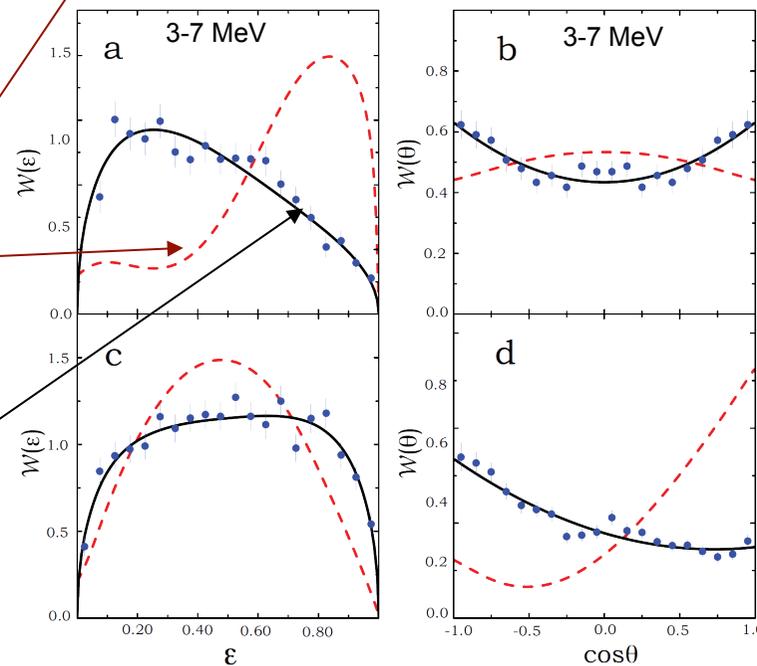
identification of ^{10}He resonances produced in $^{11}\text{Li}(p,2p)$ reactions:

0^+ ground state

2^+ excited state

correlated background (initial-state correlations, ^{11}Li wave function)

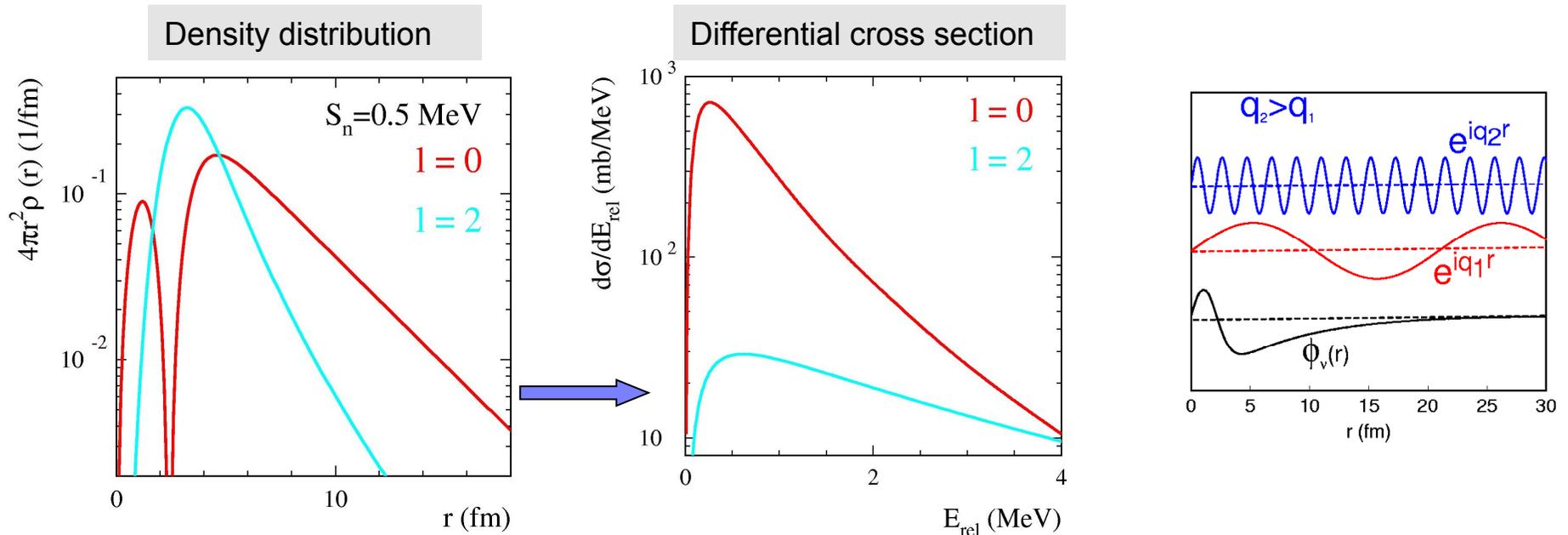
2^+ resonance



Low-Lying E1 Strength as Spectroscopic Tool

Wave function: e.g. $|^{11}\text{Be}\rangle = \alpha|^{10}\text{Be}(0^+)\otimes 2s_{1/2}\rangle + \beta|^{10}\text{Be}(2^+)\otimes 1d_{5/2}\rangle + \dots$

$$d\sigma(I_c^\pi)/dE_{\text{rel}} = \frac{16\pi^3}{9\hbar c} N_{E1}(E^*) S(I_c^\pi, nlj) \sum_m \left| \langle q | \frac{Ze}{A} r Y_m^1 | \Phi_{nlj} \rangle \right|^2$$



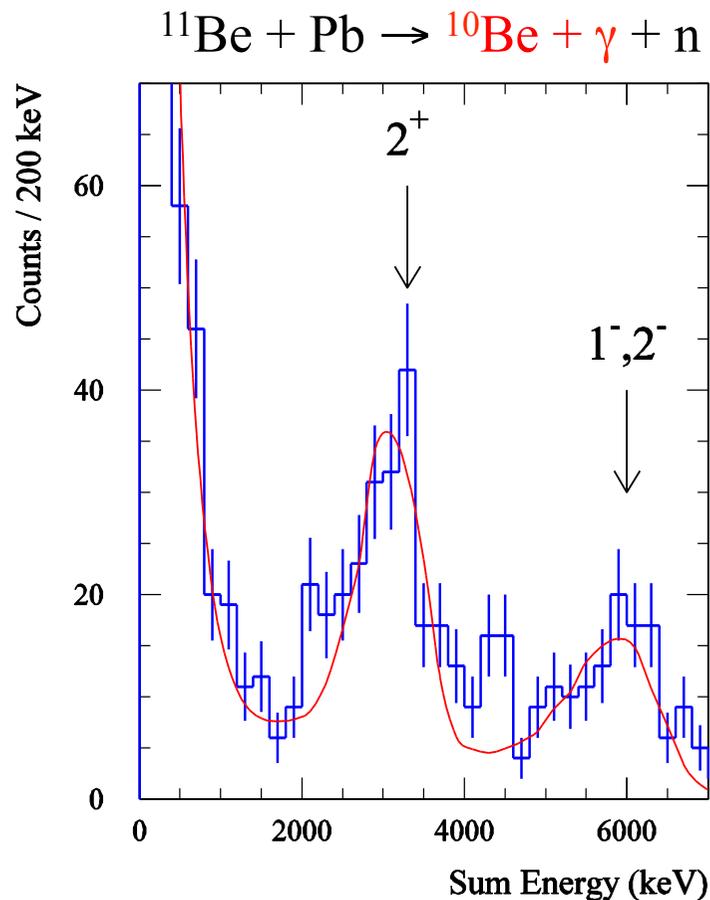
Shape of differential cross section \Rightarrow angular momentum l

γ -ray coincidence \Rightarrow identification of core state

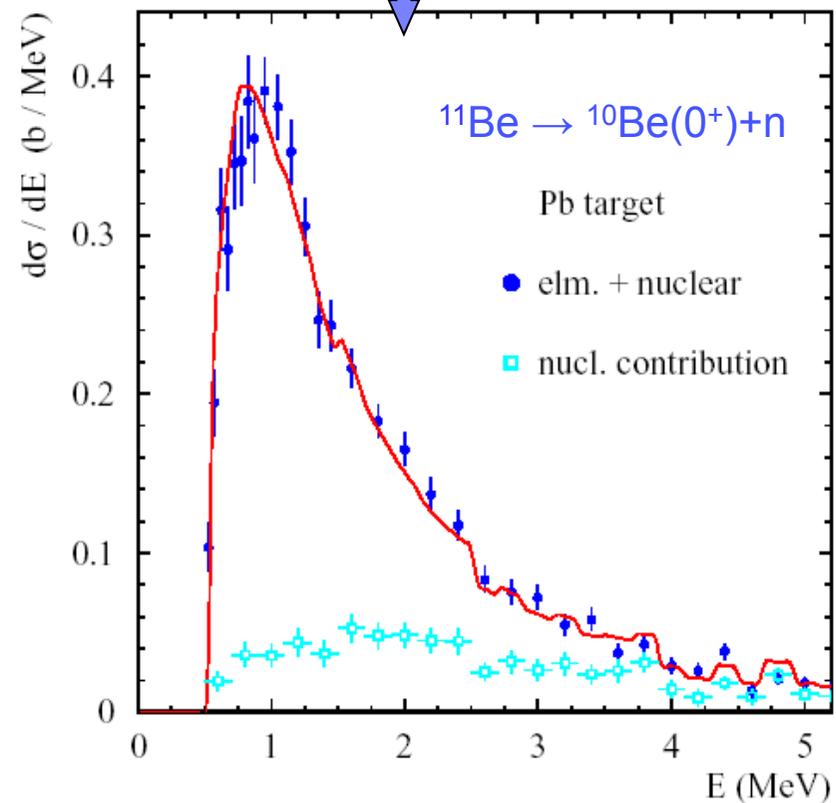
Cross section \Rightarrow spectroscopic factor

Coulomb Breakup of ^{11}Be at 500 MeV/nucleon: The Classical One-Neutron Halo

$$|^{11}\text{Be}\rangle = \sqrt{S(2^+)} |^{10}\text{Be}(2^+) \otimes 1d_{5/2}\rangle + \underbrace{\sqrt{S(0^+)} |^{10}\text{Be}(0^+) \otimes 2s_{1/2}\rangle}_{\text{Classical One-Neutron Halo}} + \dots$$



ph states at 6 MeV (inner shell
p neutrons lifted into continuum)



R. Palit et al., PRC 68 (2003) 034218

Coulomb Breakup of ^{11}Be : The Classical One-Neutron Halo

$$|^{11}\text{Be}\rangle = \sqrt{S(2^+)} |^{10}\text{Be}(2^+) \otimes 1d_{5/2}\rangle + \underbrace{\sqrt{S(0^+)} |^{10}\text{Be}(0^+) \otimes 2s_{1/2}\rangle}_{\text{E1 strength distribution}} + \dots$$

Spectroscopic factor

Analysis in the effective range approach:

$$S(0^+) = 0.70(5)$$

S. Typel, G. Baur, PRL **93** (2004) 142502

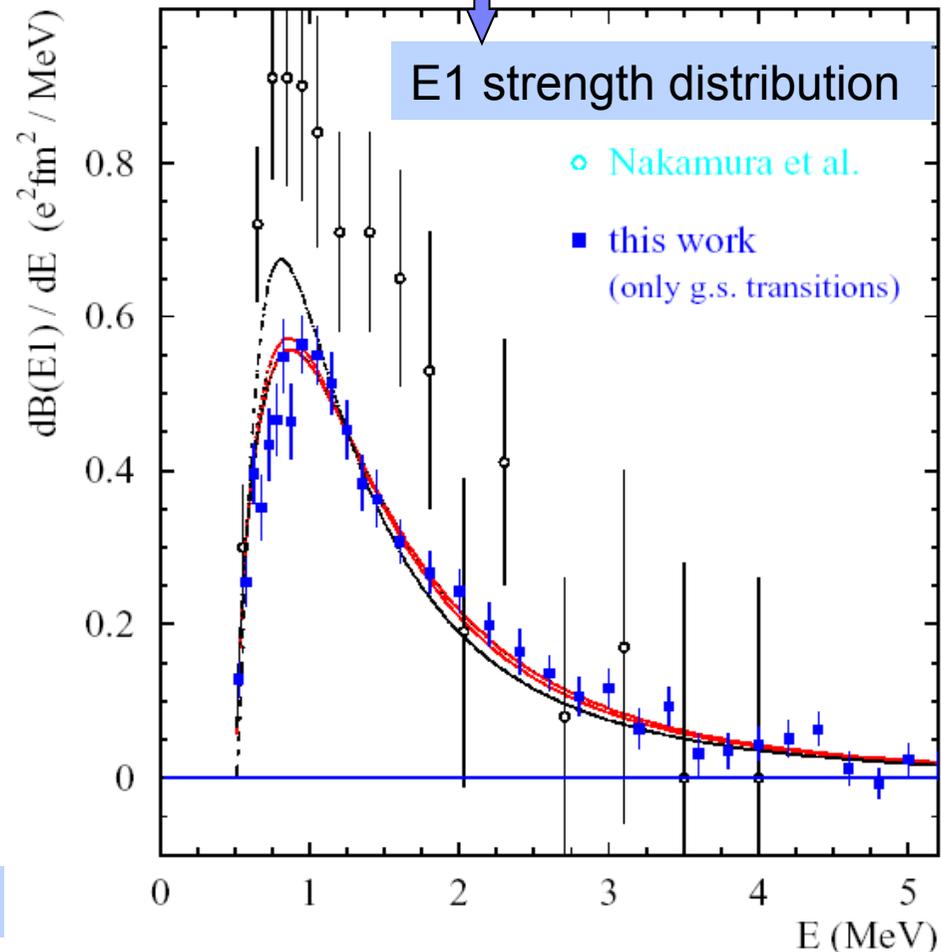
Distorted wave analysis:

$S = 0.61(5)$ with diff. opt. pot.
($S = 0.54$ for plane waves)

$S = 0.74(6)$ for WS changed from
 $r_0/a = 1.25/0.7$ to $1.15/0.5$

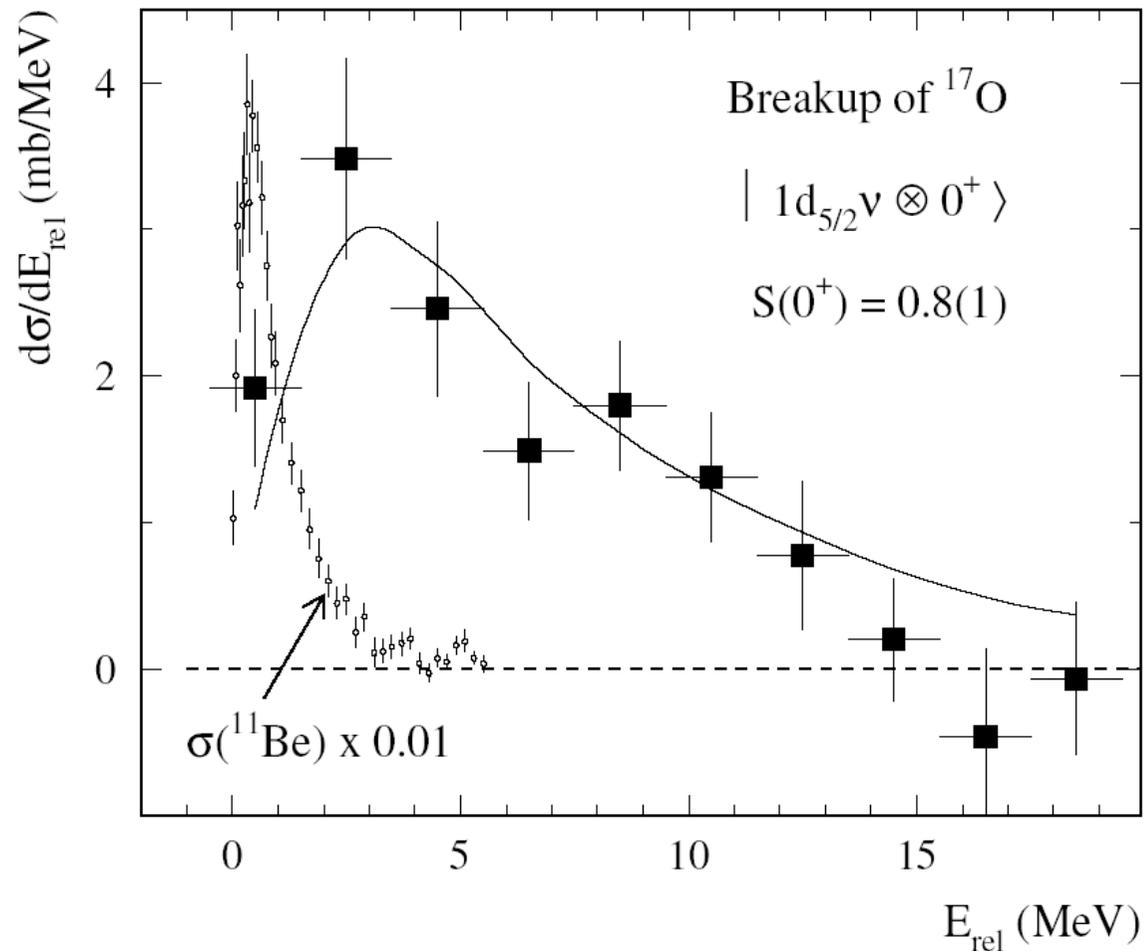
Alex Brown: 0.74

R. Palit et al., PRC **68** (2003) 034218



Sensitivity of Coulomb breakup

Comparison of the one-neutron halo ^{11}Be with the well bound ^{17}O d neutron



Coulomb breakup is very sensitive to extended neutron-density distributions (halo)

→ applicability as a spectroscopic tool mainly for weakly bound nuclei (large cross sections)

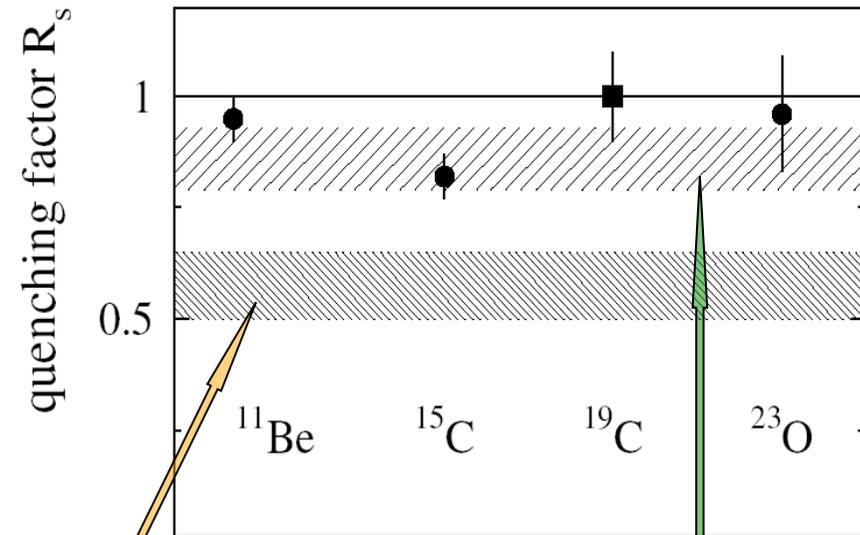
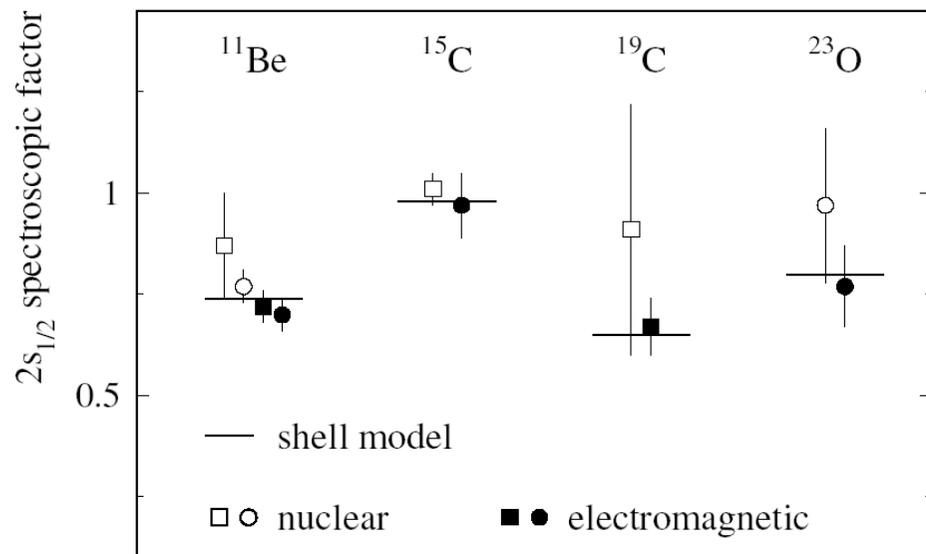
R. Palit et al.,

NPA 731 (2004) 235

Single-particle spectroscopic factors for halo nuclei derived from nuclear and electromagnetic knockout reactions

Spectroscopic factors for $2s_{1/2}$ halo states derived from nuclear and Coulomb breakup in comparison to the shell model

Ratio of experimental occupancies to shell-model values

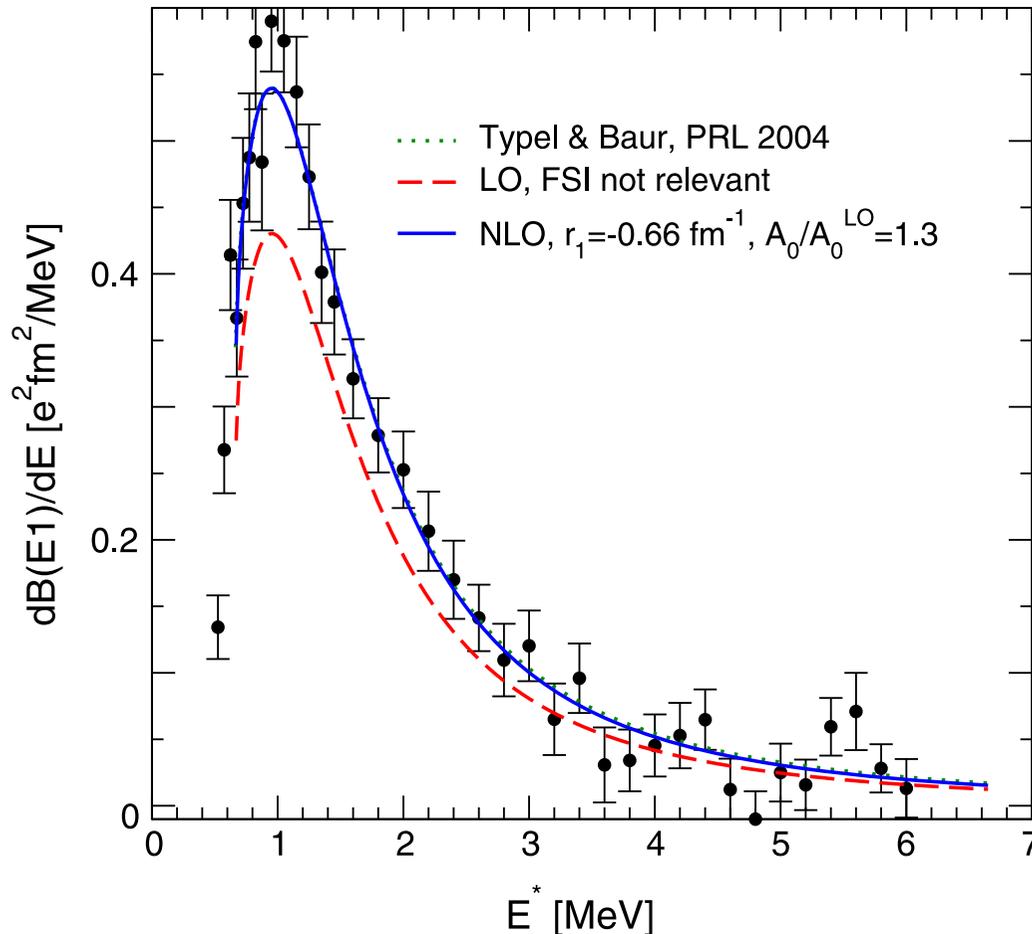


Typical reduction observed for stable nuclei (deduced from electron-induced knockout reactions)

effect of short- and long-range correlations ?

Halo states (pure single-particle states)

Electric properties of the Beryllium-11 system in Halo EFT



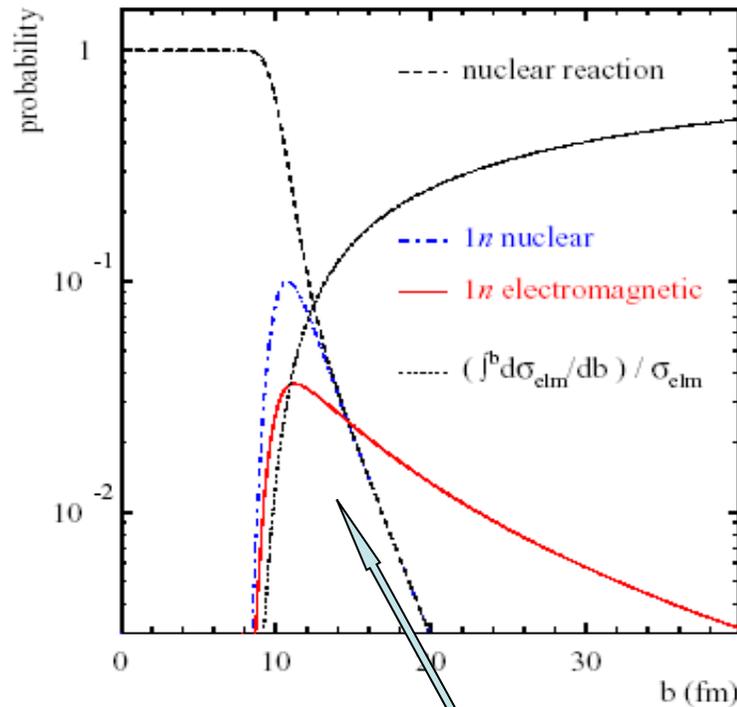
Differential B(E1) strength for Coulomb dissociation of Beryllium-11 into a neutron and a ^{10}Be nucleus, plotted versus the excess energy of the detected neutron E^* , in MeV. The data are from Ref. [5]. The theory curves have been folded with detector resolution. The red dashed line is the leading-order Halo EFT prediction, which does not include any final-state interactions. Final-state interactions, with the effective range taking on a value fixed from the bound-to-bound E1 transition strength, are included in the NLO result, which is shown by the solid blue line. The result of Ref. [30] is the green dotted line, which essentially matches the solid blue line

H.-W. Hammer and D.R. Phillips, Nucl. Phys. A 865 (2011) 17

GSI/LAND data: R. Palit et al., PRC 68 (2003) 034218

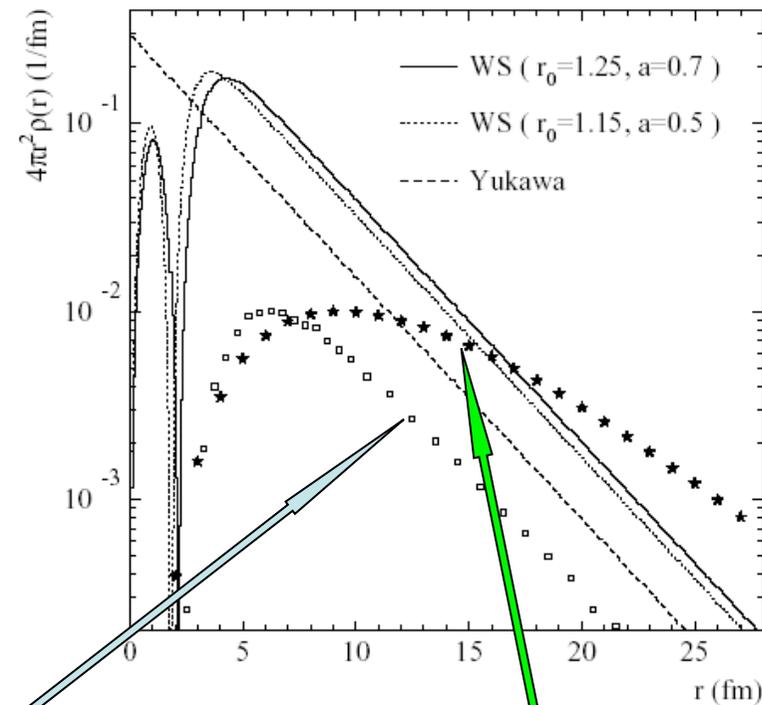
Sensitivity of Coulomb and nuclear breakup

Reaction probabilities



Nuclear breakup

Halo-Neutron Densities



Coulomb breakup

Overlap with continuum wave function

Sensitivity to the tail of the wave function only

Alternative approach: quasi-free scattering: (p,2p), (p,pn) etc. at LAND and R3B

(or (e,e'p) at the e-A collider at FAIR)

See talk of Roy Lemmon

Single-particle cross sections Quenching for neutron-proton asymmetric nuclei

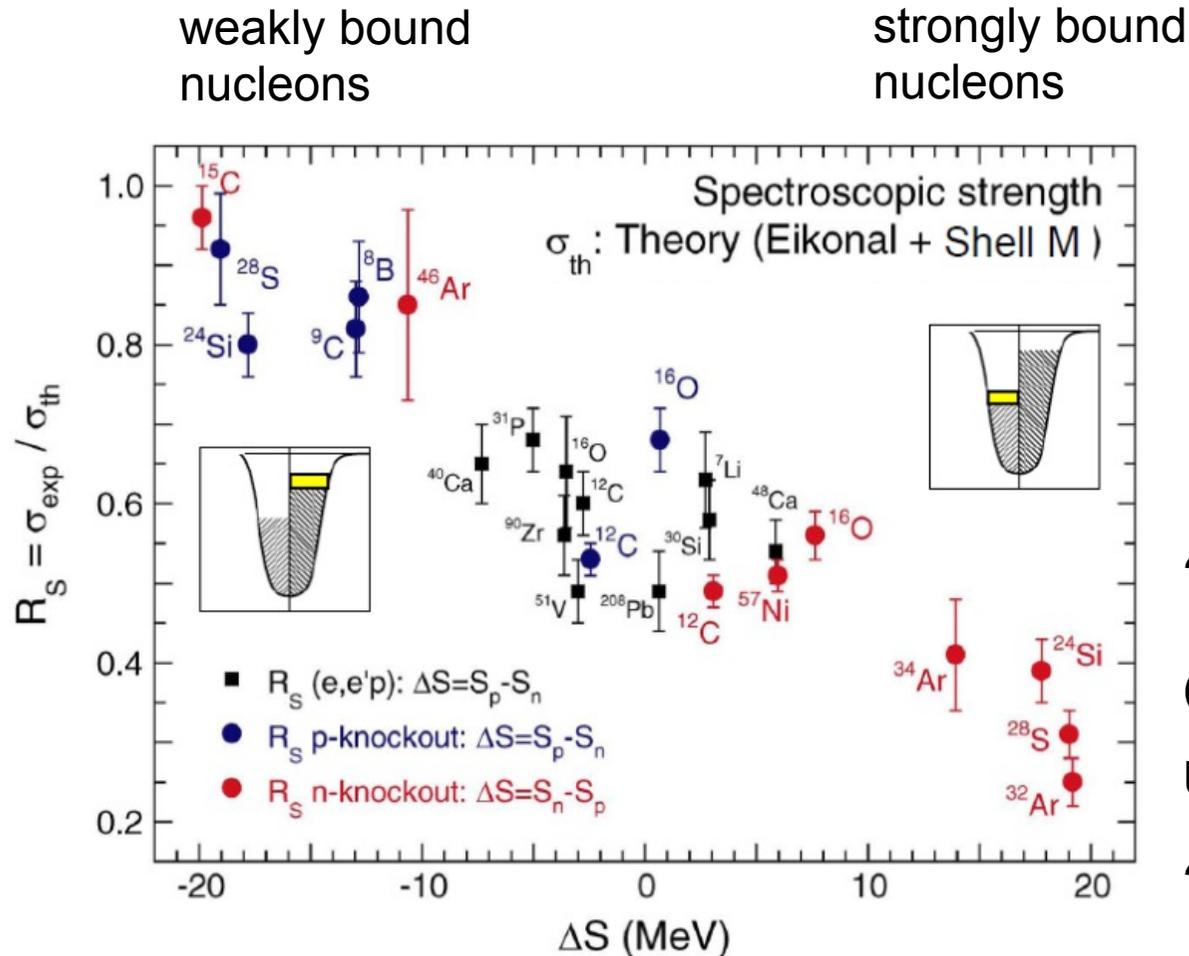
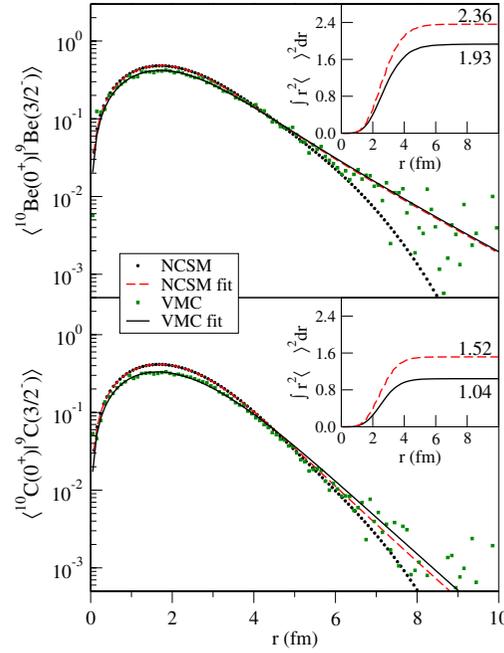
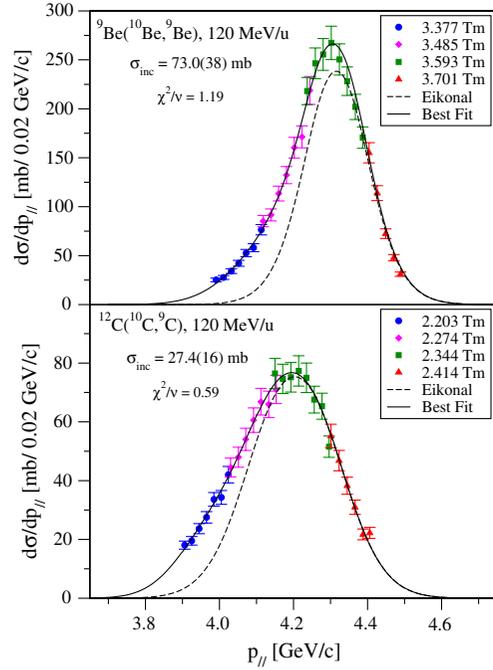


Figure from Alexandra Gade, Phys. Rev. C 77, 044306 (2008)



G. F. Grinyer et al.
PRL 106, 162502 (2011)
MSU data

FIG. 2 (color online). Bound-state VMC and NCSM wave function overlaps and resulting fits that use a Woods-Saxon-plus-spin-orbit potential. (Inset) Integrals of the square overlaps that saturate at the theoretical spectroscopic factor.

TABLE II. Woods-Saxon parameters r , a , and potential depth V_0 for the $\langle^{10}\text{Be}|^9\text{Be} + n\rangle$ and $\langle^{10}\text{C}|^9\text{C} + n\rangle$ overlap fits. Single-particle cross sections σ_{sp} were derived for projectile beam energies of 120 MeV/u on a ^9Be target. Spectroscopic factors S_F from each model are used to derive theoretical cross sections σ_{th} and can be compared to the experimental results σ_{exp} .

$\langle^{10}\text{Be} ^9\text{Be} + n\rangle$	r (fm)	a (fm)	V_0 (MeV)	σ_{sp} (mb)	S_F	σ_{th} (mb)	σ_{exp} (mb)
SM	1.25	0.70	60.4	36.8	2.62	96.6	
NCSM	1.34(2)	0.57(2)	42.9	36.8(7)	2.36	86.9(16)	73(4)
VMC	1.25(3)	0.78(4)	48.0	37.7(7)	1.93	72.8(13)	
$\langle^{10}\text{C} ^9\text{C} + n\rangle$							
SM	1.06	0.70	91.1	24.8	1.93	48.0	
NCSM	1.51(2)	0.79(2)	61.6	28.6(6)	1.52	43.4(9)	23.2(10)
VMC	1.38(4)	1.14(6)	70.9	29.5(6)	1.04	30.8(6)	