

Feasibility studies to measure the neutron skin of nuclei using hyperon-antihyperon pairs

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Exploring the neutron skin by hyperon–antihyperon production in antiproton–nucleus interactions

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Abstract. In this work we propose a new method to measure the evolution of the neutron skin thickness between different isotopes. We consider antiproton–nucleus interactions close to the production threshold of $\Lambda\bar{\Lambda}$ and $\Sigma^-\bar{\Lambda}$ pairs. At low energies, $\Lambda\bar{\Lambda}$ pairs are produced in $\bar{p} + p$ collisions, while $\Sigma^-\bar{\Lambda}$ pairs can only be produced in $\bar{p} + n$ interactions. Measuring these cross sections provides information on the neutron skin thickness.

<https://arxiv.org/pdf/2209.03875.pdf>

Introduction

- Neutron-rich nuclei expected to have neutron skin

$$\Delta r_{np} = r_{\text{rms},n} - r_{\text{rms},p}$$

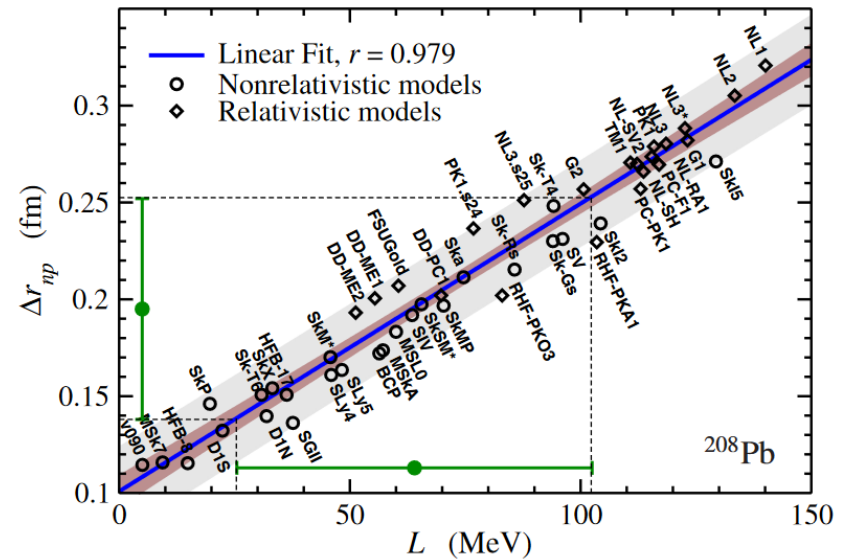
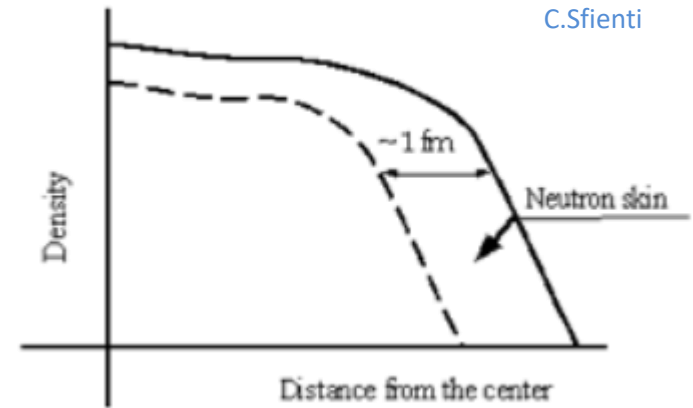
- Correlated with nuclear symmetry energy
 - Energy cost associated with additional neutron-proton asymmetry

- Slope of the symmetry energy L quantifies difference between:

- Saturation density in nuclear core
- Low density on the surface

$$L = 3\rho_0 \left. \frac{\partial E_{\text{sym}}(\rho)}{\partial \rho} \right|_{\rho_0}$$

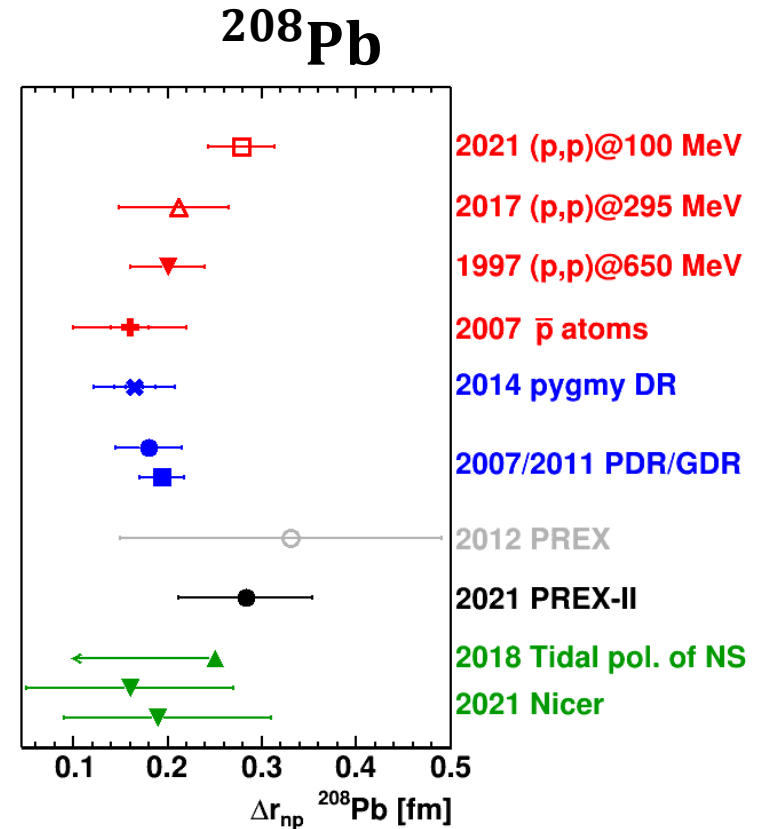
- Important parameter in equation of state in neutron rich systems



X. Roca-Maza, et al. Phys. Rev. Lett. 106, 252501 (2011)

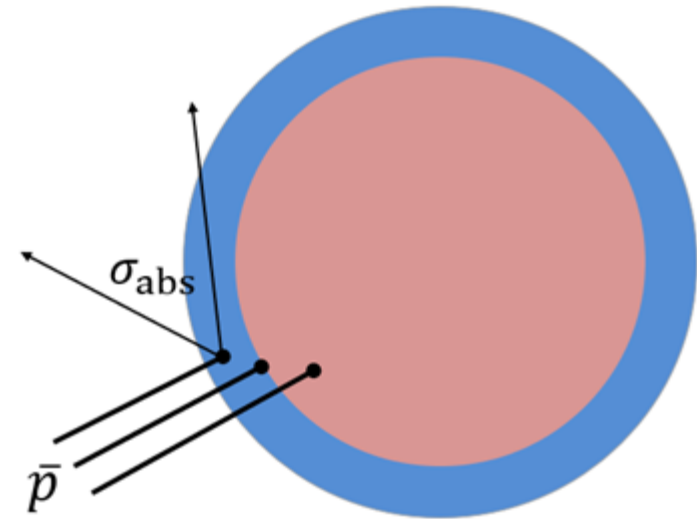
Approaches to the neutron skin

- Many different approaches to determine neutron skin
- Using hadronic probes:
 - Proton-Nucleus elastic scattering
 - Pion, Alpha, d scattering
 - Heavy ion collisions
 - Antiprotonic atoms
- Using electromagnetic probes:
 - Pion photoproduction
 - Electric dipole polarizabilities (GDR, PDR)
- Using weak interaction:
 - Parity violating asymmetry (PREX/CREX)
- Using astrophysical observations of neutron stars



Exclusive antiproton annihilation in nuclei

- New approach
 - Exclusive antiproton annihilation in nuclei
 - Using hyperons as tool for measurement
- Advantages
 - Strong absorption due to annihilation
 - ⇒ High sensitivity to the nuclear periphery
 - ⇒ Neutron skin
- Antiprotons absorption in the neutron skin



- Absorption length:

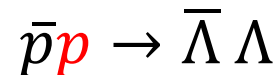
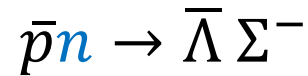
$$r_{\text{abs}} = \frac{1}{\sigma_{\bar{p}n} \cdot \rho} \approx 1 \text{ fm} \cdot \frac{\rho}{\rho_0} \sim \text{neutron skin thickness } \Delta r_{\text{np}}$$

- Survival probability:

$$p_{\text{abs}} = \exp\left(-\frac{r_n}{r_{\text{abs}}}\right)$$

Antiproton annihilation in nuclei

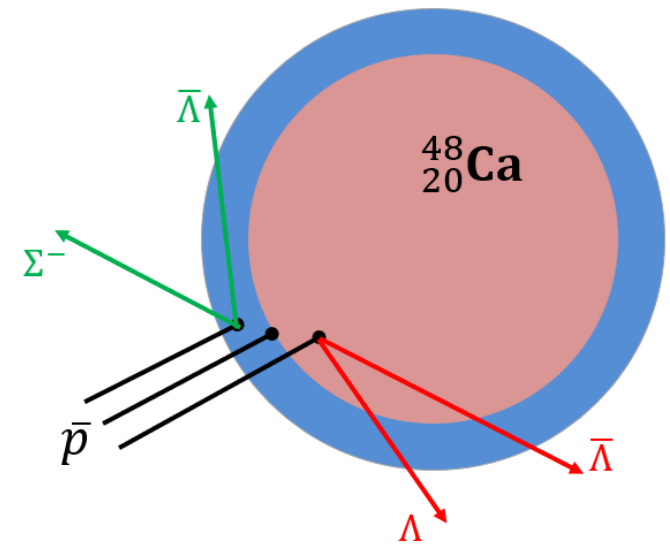
- Simultaneously measure exclusive pair production close to threshold :



- $\Sigma \bar{\Lambda}$ production only with neutrons
- $\Lambda \bar{\Lambda}$ production only with protons
- Thicker neutron skin:
 - $\Sigma \bar{\Lambda}$ production increased
 - $\Lambda \bar{\Lambda}$ production decreased
- Using ratio of exclusive pair production probabilities as observable for one isotope

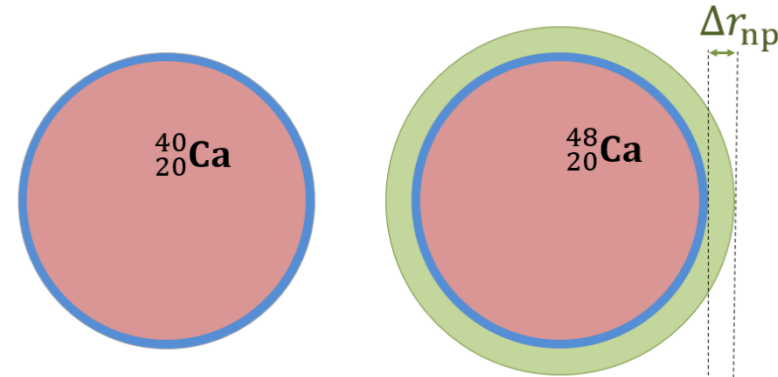
$$R = \frac{P(\bar{p}n \rightarrow \bar{\Lambda} \Sigma^-)}{P(\bar{p}p \rightarrow \bar{\Lambda} \Lambda)}$$

- But for single isotope model dependencies may exist:
 - Rescattering
 - Absorption antihyperon
 - Both cross section required



Isotope pairs : simple analytic consideration

- Compare two different isotopes under assumptions
 - Same proton distribution, e.g. $^{40}\text{Ca}/^{48}\text{Ca}$
 - Neutron density inside nucleus unchanged
 - **Additional** neutron skin Δr_{np}
- Define double ratio of these two isotopes:



$$DR = \frac{R_{^{48}\text{Ca}}}{R_{^{40}\text{Ca}}} = \frac{P(\bar{\Lambda}\Sigma^-)_{48}}{P(\bar{\Lambda}\Sigma^-)_{40}} \cdot \frac{P(\bar{\Lambda}\Lambda)_{40}}{P(\bar{\Lambda}\Lambda)_{48}} \approx \frac{(1 + \Delta p_{\text{abs}}) \cdot P(\bar{\Lambda}\Sigma^-)_{40}}{P(\bar{\Lambda}\Sigma^-)_{40}} \cdot \frac{P(\bar{\Lambda}\Lambda)_{40}}{(1 - \Delta p_{\text{abs}}) \cdot P(\bar{\Lambda}\Lambda)_{40}}$$

$$DR \approx \frac{1 + \Delta p_{\text{abs}}}{1 - \Delta p_{\text{abs}}} \approx 1 + \frac{2}{r_{\text{abs}}} \cdot \Delta r_{np} + O(\Delta r_{np}^2) \sim \sigma_{\bar{p}n} \cdot \rho_n \cdot \Delta r_{np}$$

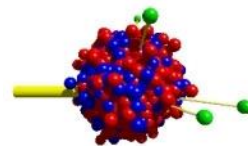
- Many systematic effects are suppressed, e.g.
 - Acceptance
 - Efficiency
 - Rescattering
- Influence of $\sigma_{\bar{p}p \rightarrow \bar{\Lambda}\Lambda}$ (nearly) eliminated

Why a transport calculation is needed?

- Simplified geometrical picture still has deficiencies :
 - Not all antiprotons traverse the neutron skin radially
 - ⇒ Absorption probability depends on impact parameter
 - Absorption of produced antihyperons $\bar{\Lambda}$ inside nucleus
 - ⇒ Favors peripherally produced pairs
 - ⇒ Will depend on neutron skin thickness
 - Often slight modification of proton distribution for different isotopes
- ⇒ Use more realistic simulations to verify the sensitivity of the double ratio to the variation of neutron skin thickness

Simulation with GiBUU

- Using GiBUU software framework
 - Relativistic meanfield transport model
- On the Mogon2 supercomputer at the university of Mainz



GiBUU

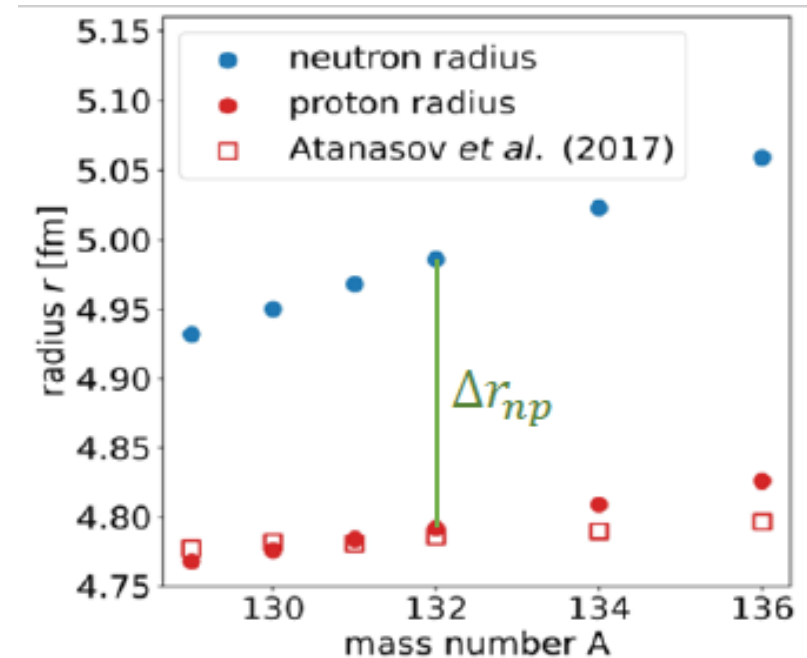
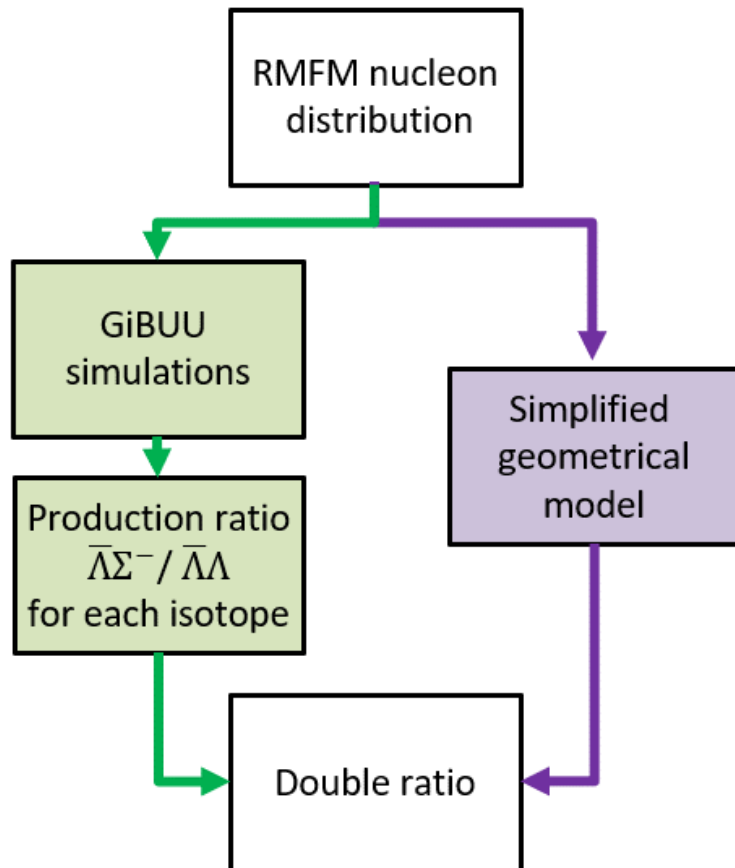
The Giessen Boltzmann-Uehling-Uhlenbeck Project



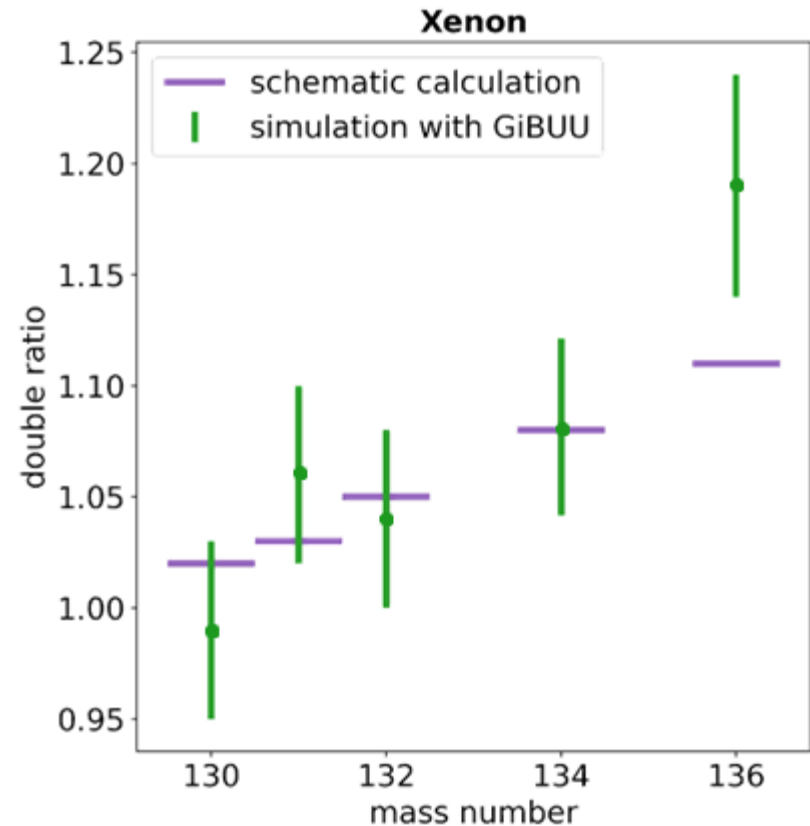
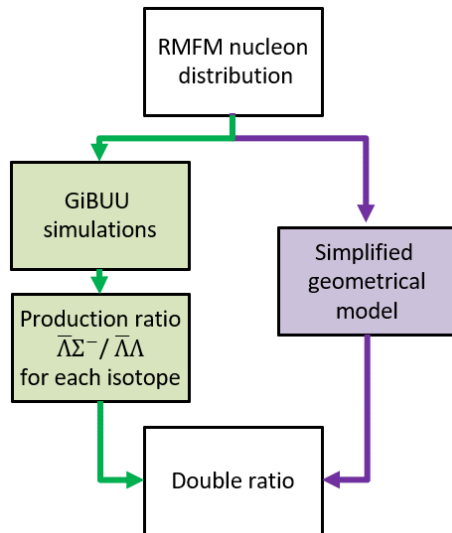
- Simulated $\sim 28\text{M}$ events ($\bar{p}A$) at 2.40 GeV/c for each isotope
 - Computationally expensive: $\sim 2\text{d}$
 - $\sim 5\text{s}$ of PANDA run time
- For same statistics, taking detector efficiencies into account: $\mathcal{O}(\text{hours})$

Xenon isotope chain – proof of principle

- Xenon was calculated first
 - Many stable isotopes with sufficient abundance
 - Gas jet target



Xenon isotope chain



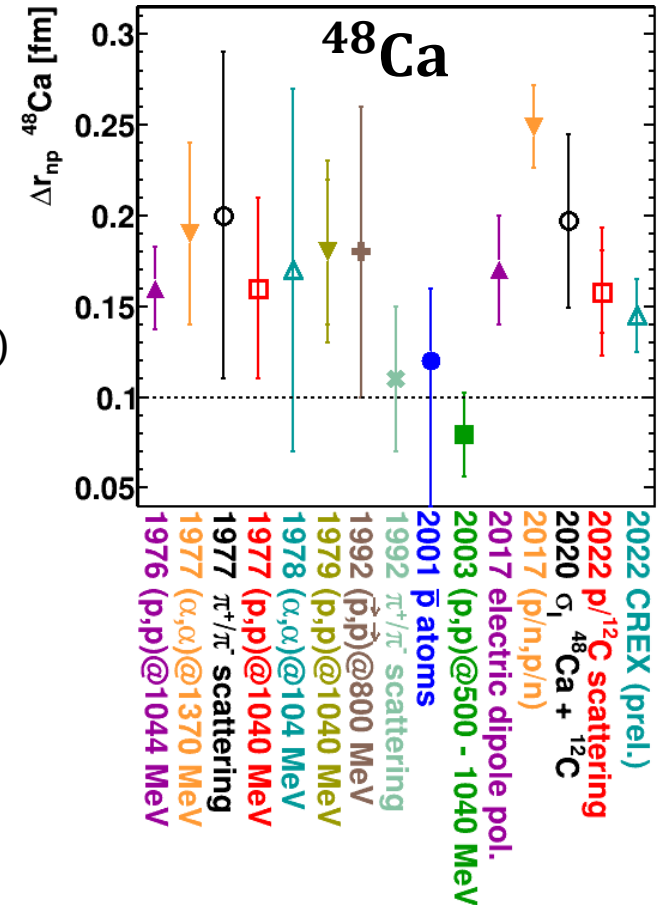
- **Double ratio from GiBUU simulation is related to neutron skin thickness which is assumed as input**
- However: Isotopically pure gas targets extremely expensive $\mathcal{O}(100\text{g})$
- Solid state target affordable $\mathcal{O}(\text{mg})$

Calcium isotope

- Target ^{40}Ca and ^{48}Ca
 - Double magic nuclei
 - Nearly identical proton distribution
 - Ab initio calculation possible
- Expected: $\Delta r_{\text{np}}(^{48}\text{Ca})$ strongly related to $\Delta r_{\text{np}}(^{208}\text{Pb})$
- Tension between PREX2 and CREX(prel.)
- Any new measurement of calcium welcome
- 80M Events at 2.40 GeV/c for each isotopes

Simplified model	GiBUU
1.37	1.41 ± 0.03

- $\Delta\text{DR} = 0.03 \Rightarrow \frac{\Delta(\Delta r_{\text{np}})}{\Delta r_{\text{np}}} \approx 10\%$
 - @PANDA** $\rightarrow \mathcal{O}(5 \text{ hours})$ measurement time



$$\Delta r_{\text{np}}(^{208}\text{Pb}) = 0.283 \pm 0.071 \text{ fm}$$

D. Adhikari et al. (PREX),
Phys. Rev. Lett. 126, 172502 (2021).

Current work and outlook

- Improving statistical error:
 - Simulating additional events for Xenon isotopes
 - Goal: factor 4 more events
 - Simulations almost completed
- Systematic effects and their uncertainty still need to be studied
 - Reaction cross sections
 - $\sigma_{\bar{p}n \rightarrow \Sigma^- \bar{\Lambda}}$, $\sigma_{\bar{p}p \rightarrow \Lambda \bar{\Lambda}}$
 - Sensitivity of double ratio on the neutron skin thickness by varying the cross sections in GiBUU
 - Experimentally: Measurement on proton and deuterium with PANDA
 - Neutron and proton distribution
 - Implement different nucleon distributions in GiBUU and explore sensitivity
- Feasibility to use this method with PANDA needs to be studied in the future

To summarize:

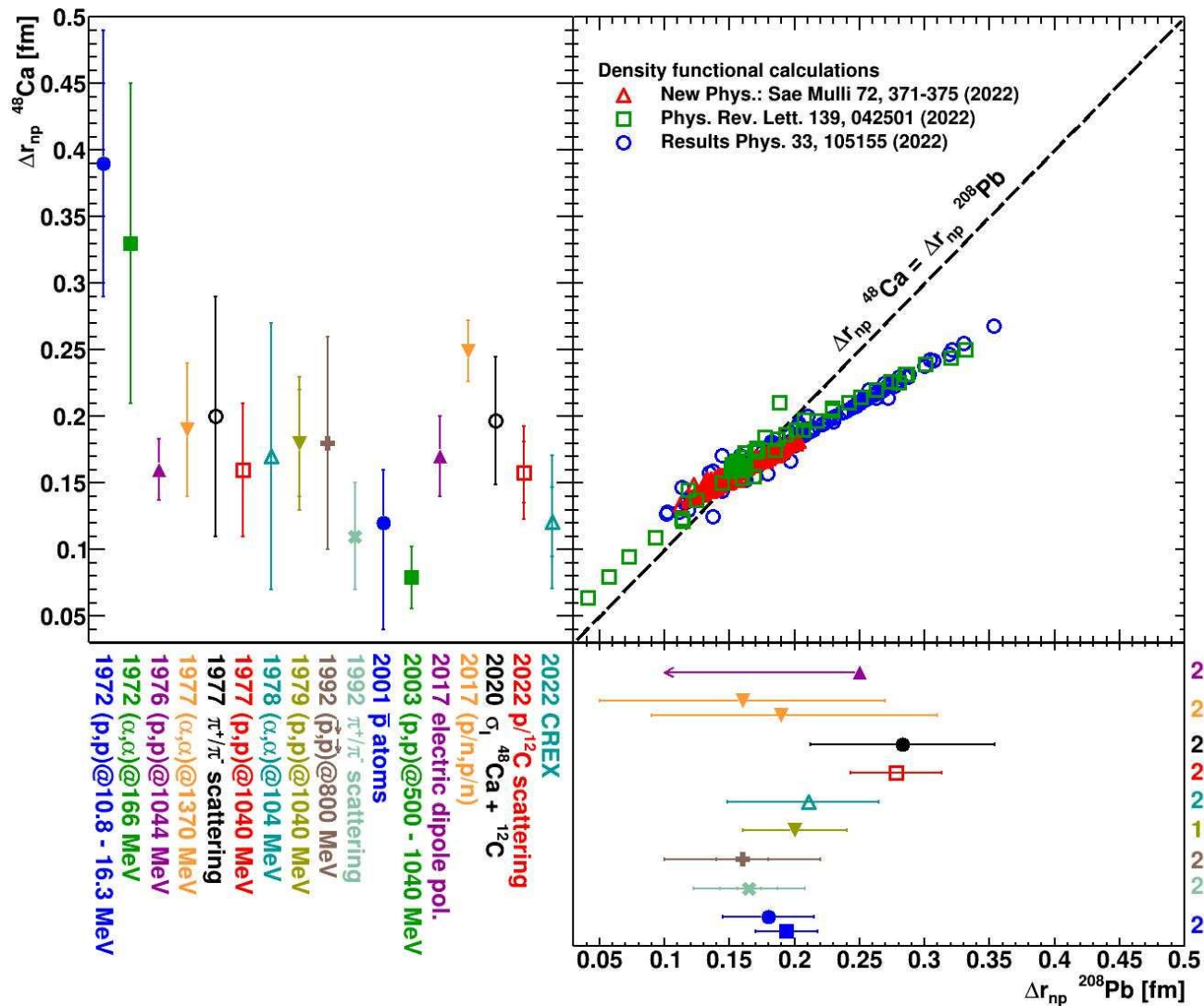
- New method to measure the neutron skin variation for isotope pairs using antiprotons
 - Short measuring time sufficient for high statistics
⇒ small statistical error
 - Large sensitivity on neutron skin thickness

Thank you for your attention

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Backup slides

Calcium isotope



D. Atanasov et al. In: J Phys G Nucl Part Phys 44.4 (2017), p. 044004

