

# TAMU Transport Approach to Quarkonia in Heavy-Ion Collisions

B. Wu, X. Du, R. Rapp



TEXAS A&M UNIVERSITY  
Cyclotron Institute



College Station, TX

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# Transport Approach

[Grandchamp *et al.*'04, Zhao *et al.*'11, Du *et al.*'17]

- Rate equation used in calculating quarkonia ( $\mathcal{Q}$ ) in URHICs

Reaction rate

$$\frac{dN_{\mathcal{Q}}}{d\tau} = -\Gamma_{\mathcal{Q}}(T) [N_{\mathcal{Q}} - N_{\mathcal{Q}}^{\text{eq}}(T, \gamma_c)]$$

Primordial      Regeneration

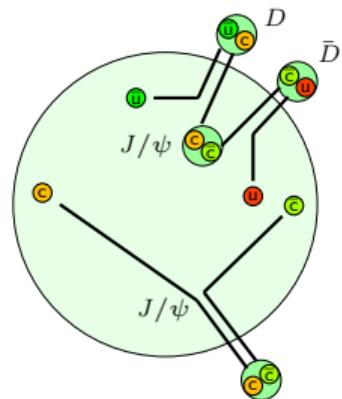
- Equilibrium limit from statistical model

$$N_{\mathcal{Q}}^{\text{eq}}(E_B, T) = dV_{\text{FB}} \gamma_{Q_1} \gamma_{Q_2} \int \frac{d^3 p}{(2\pi)^3} e^{-\sqrt{m_{\mathcal{Q}}^2 + p^2}/T}$$

$E_B$ : from in-medium Cornell potential  $\Rightarrow$  vacuum spectroscopy as  $T \Rightarrow 0$

- Fugacity  $\gamma_Q(T)$ : Heavy Quark (HQ) number conservation

$$N_{Q\bar{Q}} = \frac{1}{2} \gamma_Q(T) n_{\text{op}} V_{\text{FB}} \frac{I_1(\gamma_Q(T) n_{\text{op}} V_{\text{FB}})}{I_0(\gamma_Q(T) n_{\text{op}} V_{\text{FB}})} + \gamma_Q^2(T) n_{\text{hid}} V_{\text{FB}}, \quad N_{Q\bar{Q}} = \frac{N_{\text{coll}} \sigma_{Q\bar{Q}}^{\text{pp}}}{\sigma_{\text{inel}}^{\text{pp}}}$$

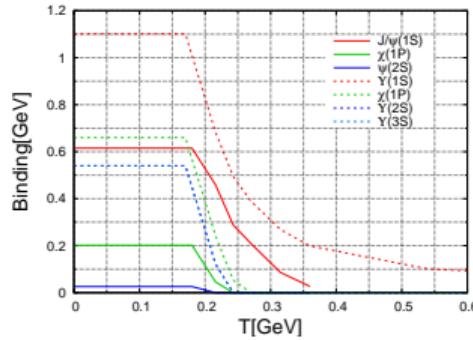
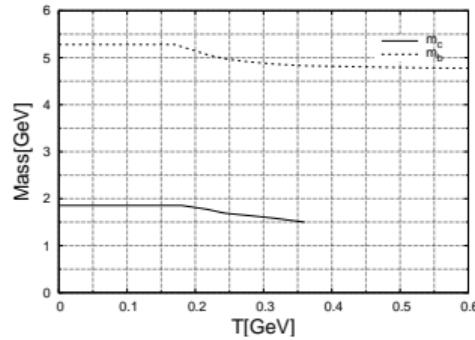


# In-Medium Charm- and Bottom-quark Masses and Binding Energies

- In-medium potential  $U$

[Riek *et al.*'10, Zhao *et al.*'10, Du *et al.*'17]

- Constraint from lattice: Euclidean correlators  $G_\alpha(\tau, T) = \int \frac{dE}{2\pi} \rho_\alpha(E, T) \frac{\cosh[E(\tau - 1/2T)]}{\sinh[E/2T]}$

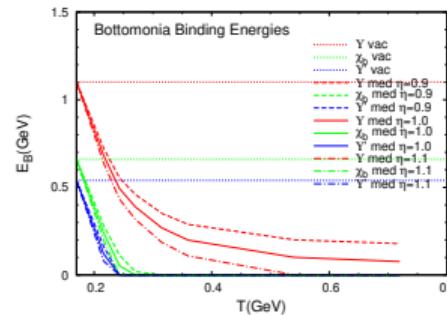
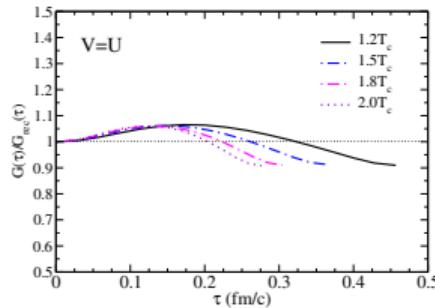


- Increase (decrease) the binding:

$$E_B^\eta(T) \equiv E_B^{\text{vac}} - \eta \Delta E_B(T)$$

$$\eta = 0.9 \quad (1.1)$$

$$\Delta E_B(T) = E_B^{\text{vac}} - E_B^\eta(T)$$

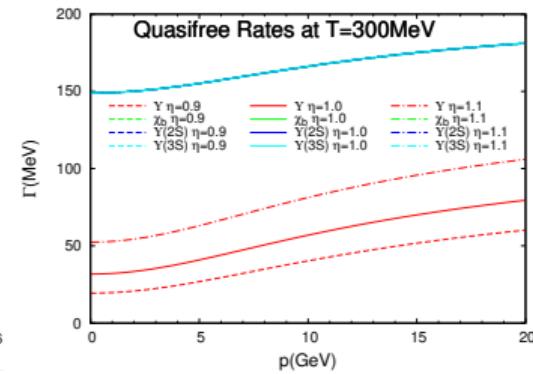
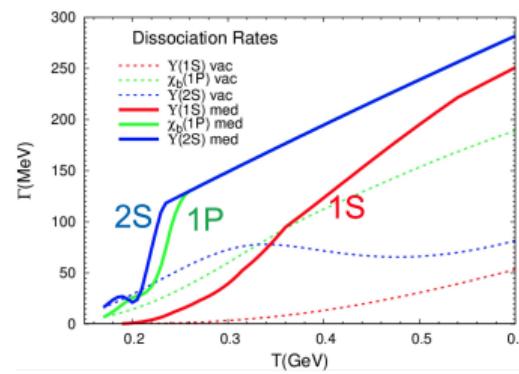
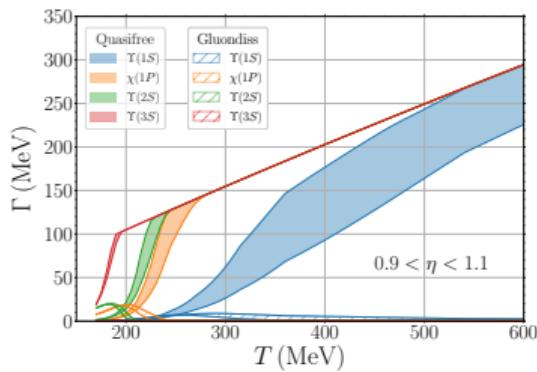
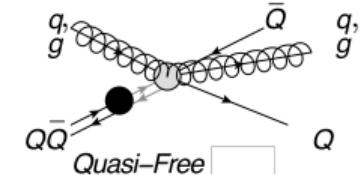


# Reaction Rates $\Gamma_Q(T)$

[Grandchamp *et al.*'01+'04, Zhao *et al.*'11, Du *et al.*'15+'17,  
Lin *et al.*'00]

- Quasi-free (massive quasi-particles):  $Q+q, g \rightleftharpoons Q + \bar{Q} + q, g$
- Sensitive to the in-medium binding energies
- Hadronic rates: effective SU(4) interaction  $\Rightarrow$  hadron resonance gas
- Interference effects in the quasi-free rate: decrease for deeply bonded mesons:

$$\Gamma_Y^{\text{qf}}(p, T) = \sum_p \int \frac{d^3 p_p}{(2\pi)^3} d_p f_p(\omega_p, T) v_{\text{rel}} \sigma_{Yp \rightarrow b\bar{b}p}(s) \Rightarrow (1 - e^{i\vec{q} \cdot \vec{r}})$$

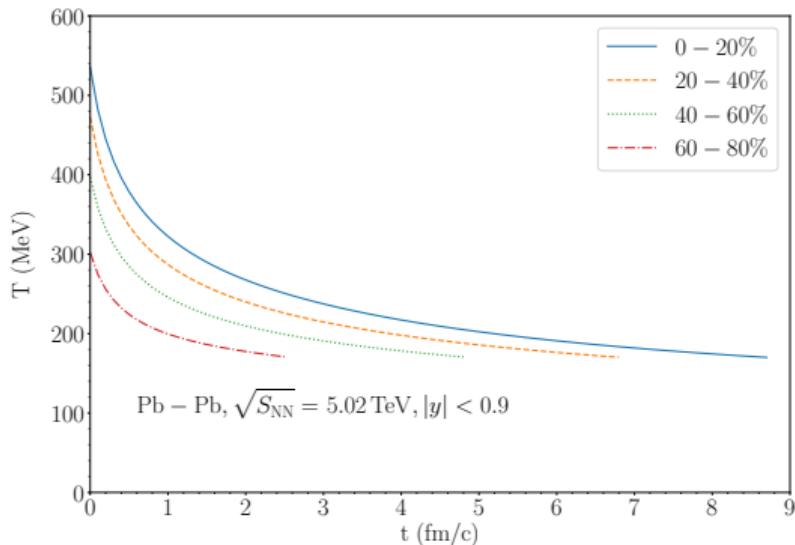


# Medium evolution

[Grandchamp *et al.*'01+'04, Zhao *et al.*'10]

- Isentropically and cylindrically expanding isotropic fireball:

$$V_{FB}(\tau) = \left( z_0 + v_z \tau + \frac{1}{2} a_z \tau^2 \right) \pi \left( R_0 + \frac{\sqrt{1+(a_\perp \tau)^2}-1}{a_\perp} \right)^2$$

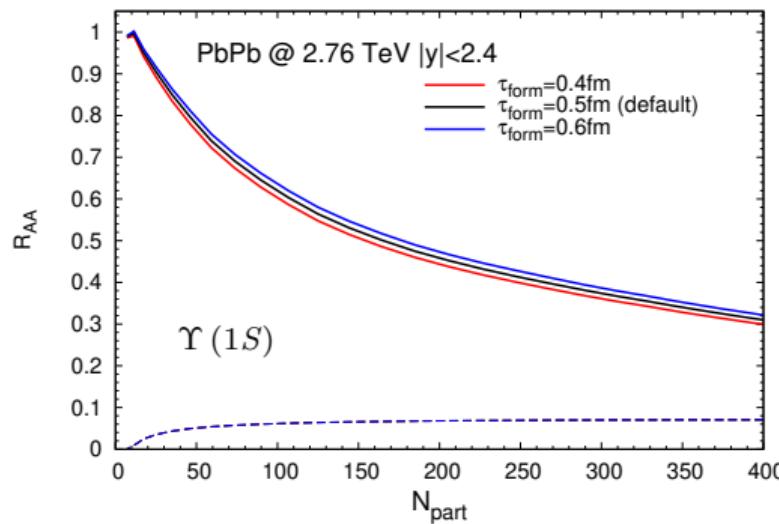


- Blast-wave type, taken from fits to experimental data for  $\pi$ ,  $p$  and  $K$  hadrons
- Total entropy fit to experimentally measured charged-hadron multiplicities
- Conservation of entropy and EoS with massive quasi-particles  $\Rightarrow T(t)$

# Quarkonium Formation times

[Du *et al.*'17]

- Pair production time  $\tau_{Q\bar{Q}} \leq 0.1 \text{ fm}/c$
- Bound-states formation time  $\tau_{\text{form}} \sim 1/E_B \sim 0.2\text{-}2 \text{ fm}/c$
- Build-up of wave function reduces dissociation rate  $\alpha_Y(\vec{p}, T(\tau)) \equiv \Gamma_Y(\vec{p}, T(\tau)) \frac{\tau}{\tau_{\text{form}}} \frac{m_Y}{\sqrt{p^2 + m_Y^2}}$

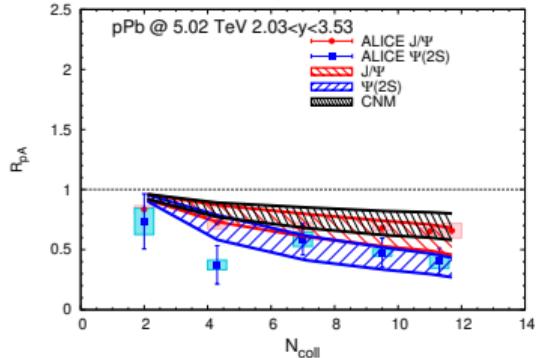
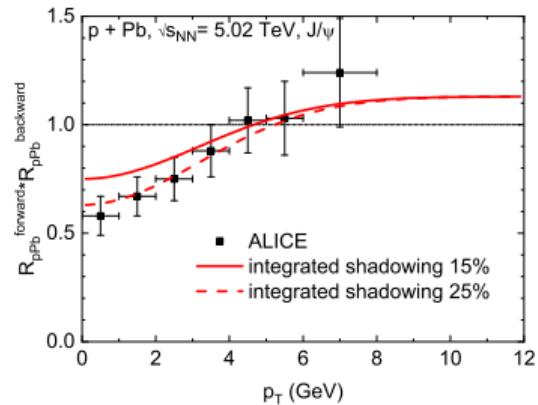
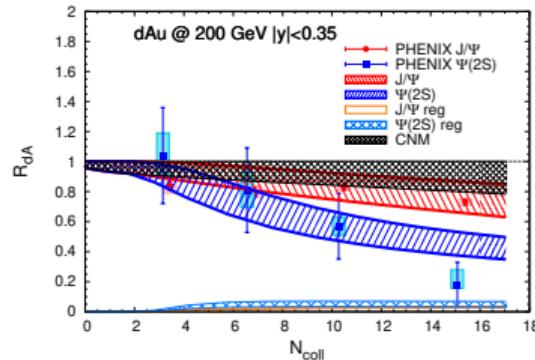
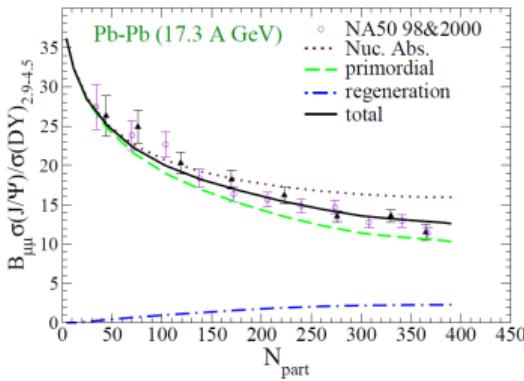


- Higher excited  $\Upsilon$  and  $\psi$  states have larger formation time
- Relatively small effect in heavy-ion collisions
- Microscopically: quantum evolution of wave package

# Cold-Nuclear Matter Effects

[Grandchamp *et al.*'01+'03, Zhao *et al.*'07, He *et al.*'22]

- Nuclear shadowing: modification of the initial production
- Cronin effect + Nuclear absorption (low  $\sqrt{s}$ : SPS+RHIC)
- Non-perturbative (K factor): constraint on  $\psi(2S)$  rates

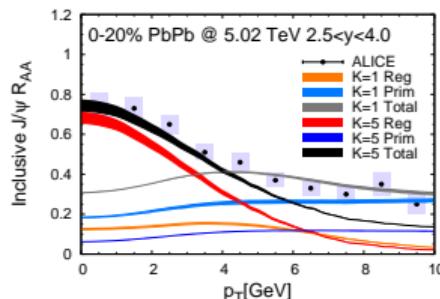
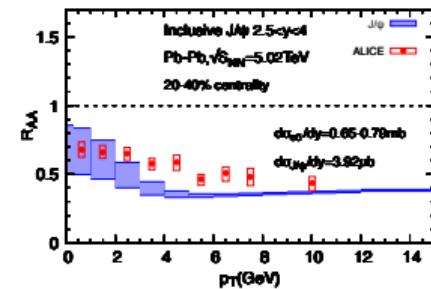
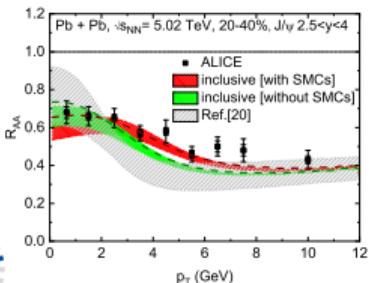
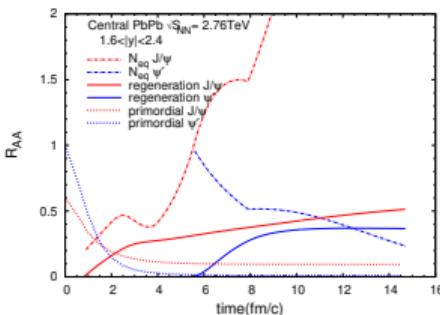


# Transverse momentum spectra

[Zhao *et al.*'07+'11, Du *et al.*'17, He *et al.*'20 ]

- $p_T$  dependence from blast-wave at average freezeout time  $\tau$

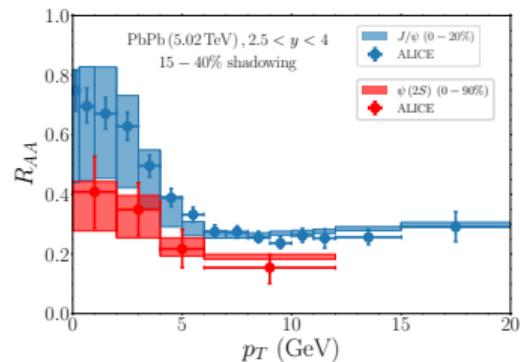
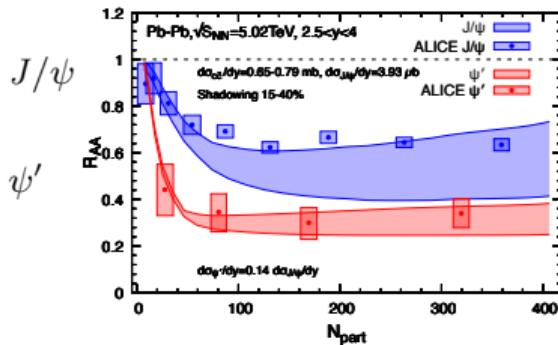
$$\frac{dN_\Psi^{\text{reg}}}{p_t \, dp_t} = N_0 (b) m_t \int_0^R r dr K_1 \left( \frac{m_t \cosh y_t}{T(\tau)} \right) I_0 \left( \frac{p_t \sinh y_t}{T(\tau)} \right), \quad m_t = \sqrt{m_\Psi^2 + p_t^2}$$



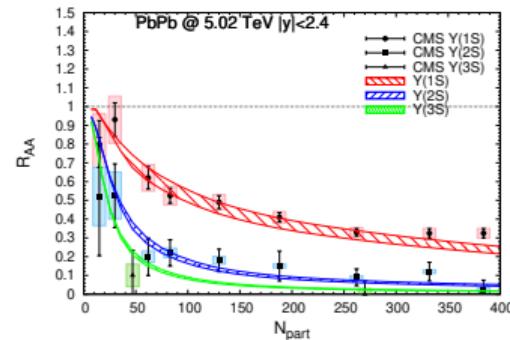
- $p_T$  suppression  $\Rightarrow$  Boltzmann equation
- Average regeneration temperatures  $T(\tau)$  (taken from the **average production time**): different for ground and excited states
- Resonance recombination model (**RRM**)  $\Rightarrow$  space-momentum correlations (**SMCs**) of heavy quarks with partons in expanding fireball.
- Transported charm-quarks essential for large regeneration (**softening**)

# Results for Quarkonia in 5 TeV Pb-Pb Collisions

[ALICE, '20]



[CMS, '19] [Du *et al.*, '17]



$\Upsilon$

- Charmonia with most recent open-charm cross section + shadowing
  - $\psi'$  results predictions
- Bottomonia,  $B_c$  and  $X(3872)$  are treated in the same approach

Thank you!

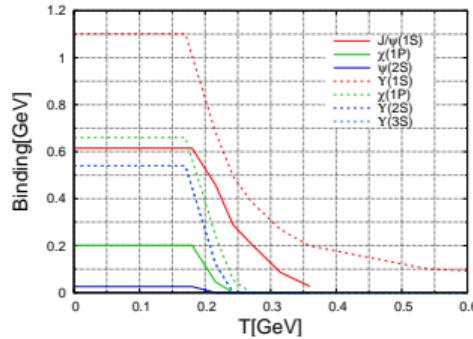
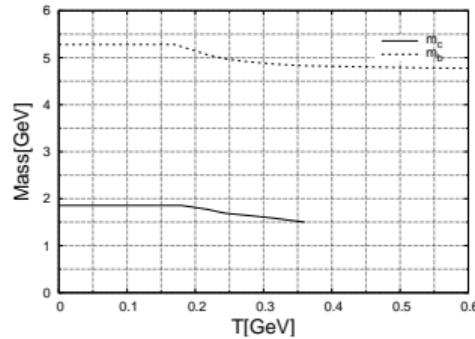
# Backup

# In-Medium Charm- and Bottom-quark Masses and Binding Energies

- Free Energy F

[Riek *et al.*'13, Zhao *et al.*'10, Du *et al.*'17]

- Constraint from lattic: Euclidean correlators  $G_\alpha(\tau, T) = \int \frac{dE}{2\pi} \rho_\alpha(E, T) \frac{\cosh[E(\tau-1/2T)]}{\sinh[E/2T]}$

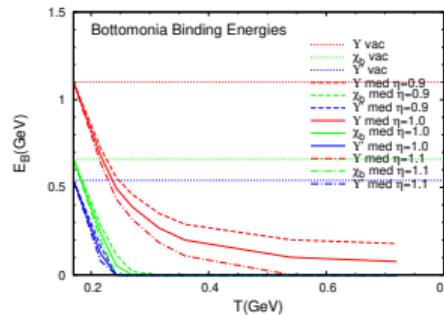
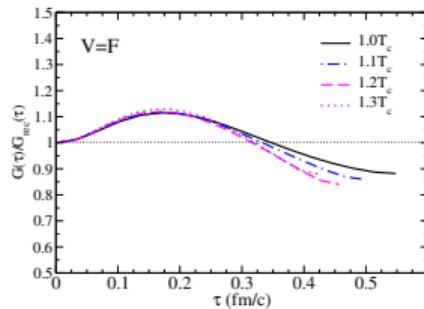


- Increase (decrease) the binding:

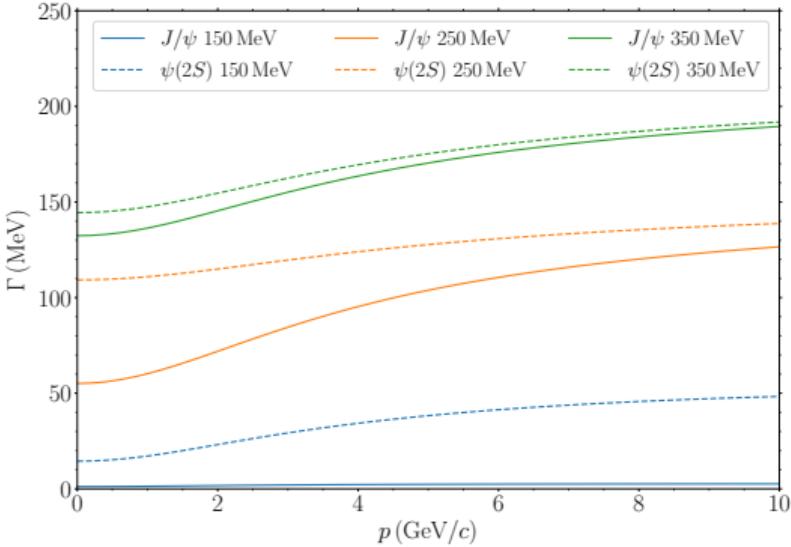
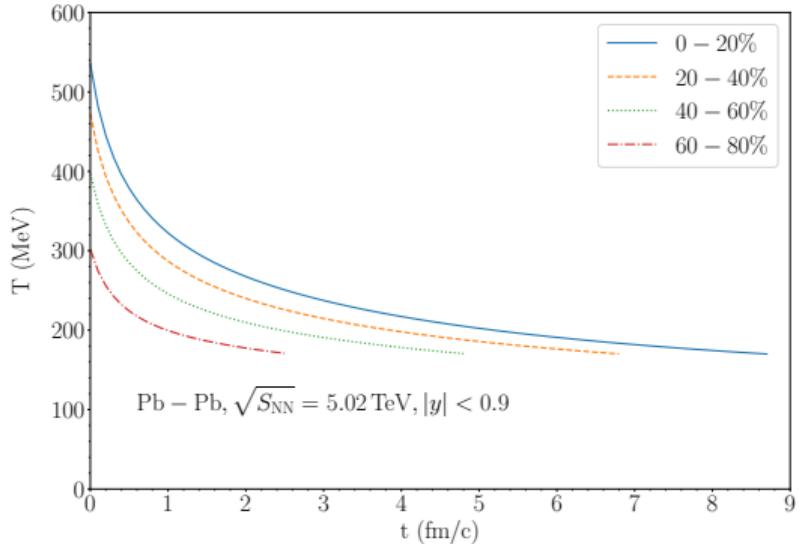
$$E_B^\eta(T) \equiv E_B^{\text{vac}} - \eta \Delta E_B(T)$$

$$\eta = 0.9 \quad (1.1)$$

$$\Delta E_B(T) = E_B^{\text{vac}} - E_B^\eta(T)$$



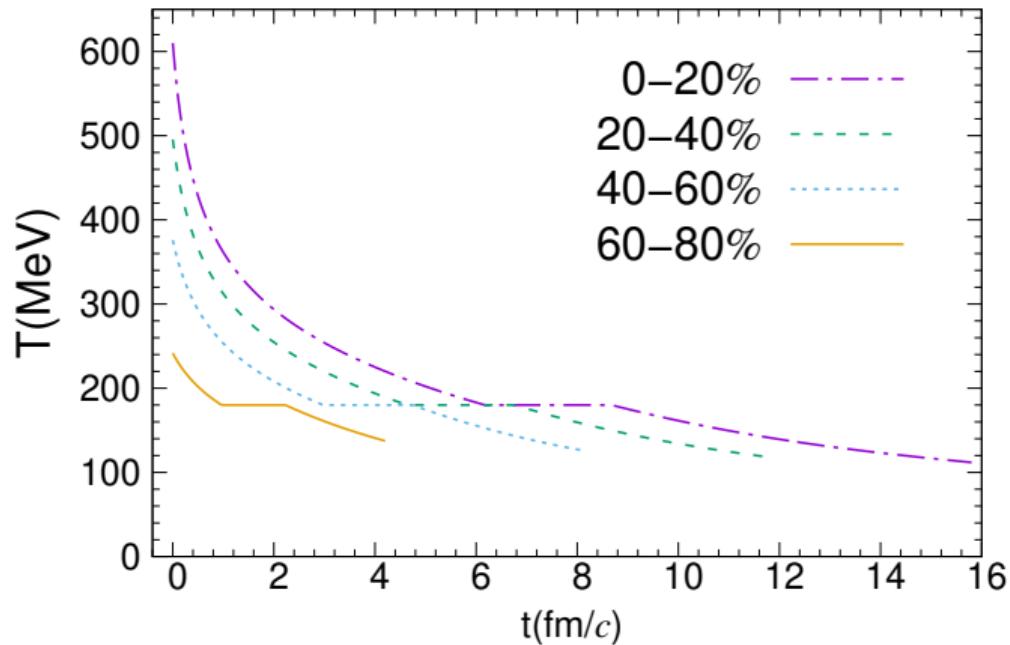
# The space time evolution



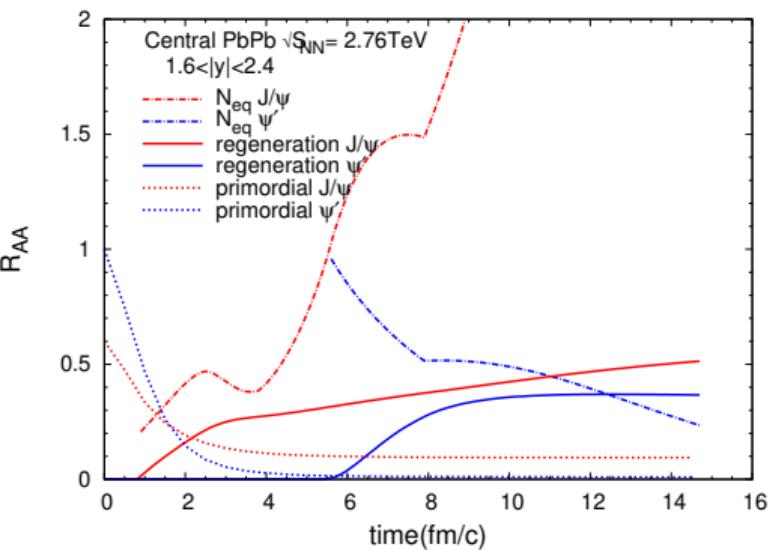
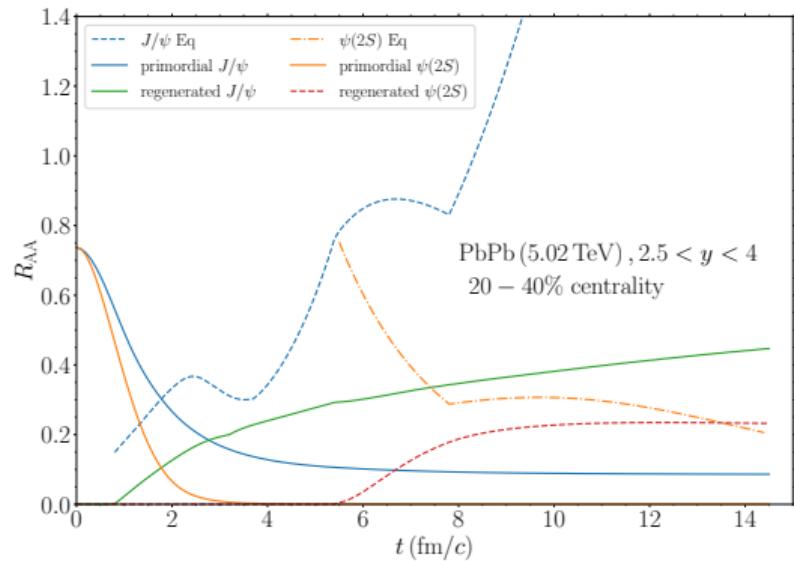
- Expanding fireball
- Conservation of entropy and EoS  $\Rightarrow T(t)$

- Quasi-free reaction rate

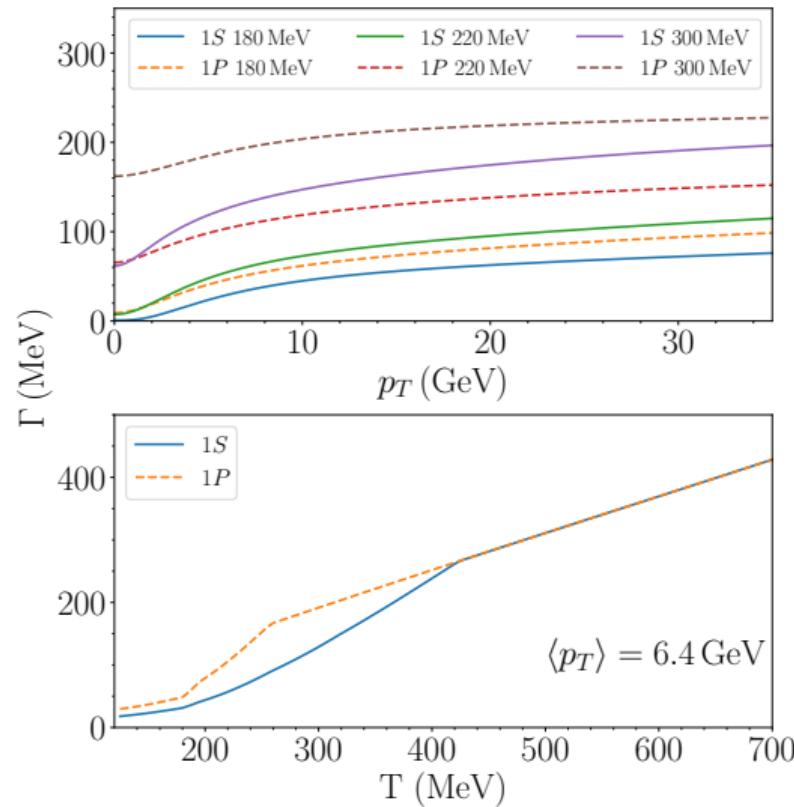
# Temperature of the Fireball



# Time evolution of Charmonia

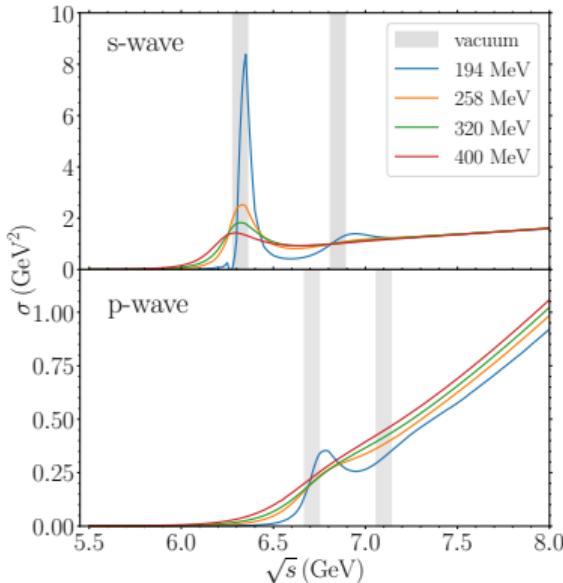


## $B_c$ Quasi-free rates

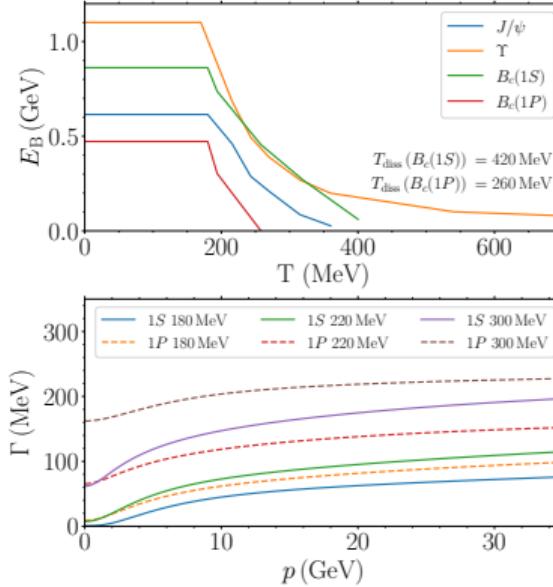


# $B_c$ In-medium Binding Energy and Reaction Rates

[Z. Tang *et al.* '21]

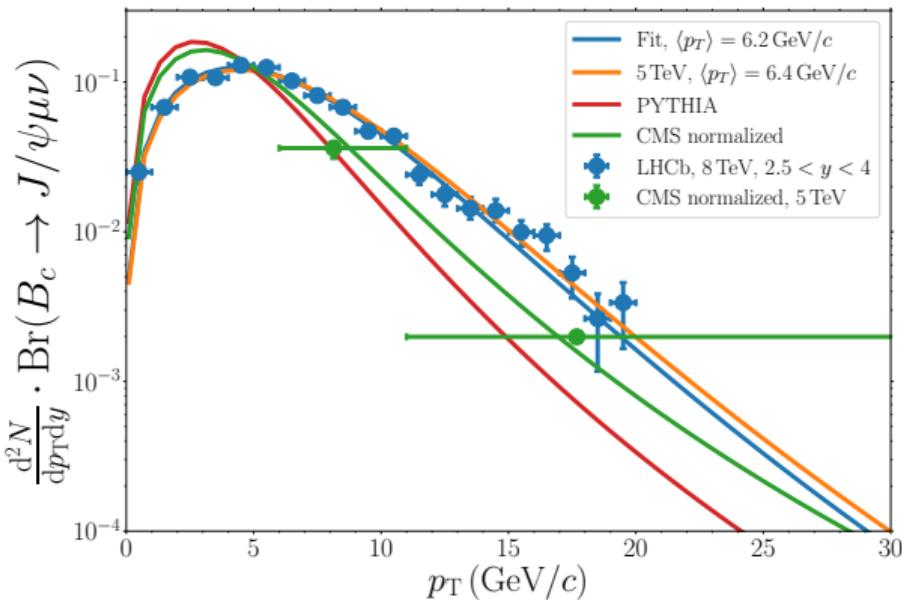


- **Vacuum mass:**  $B_c(1S) = 6324 \text{ MeV}$   
 $B_c(2S) = 6850 \text{ MeV}$
- **$B_c$  spectral functions:**  
 In-medium T-matrix calculation



- **PDG:**  $B_c(1S) = 6274.47 \pm 0.27 \pm 0.17 \text{ MeV}$   
 $B_c(2S) = 6871.2 \pm 1.0 \text{ MeV}$
- $T_{\text{diss}}(1S) = 420 \text{ MeV}$   
 $T_{\text{diss}}(1P) = 260 \text{ MeV}$

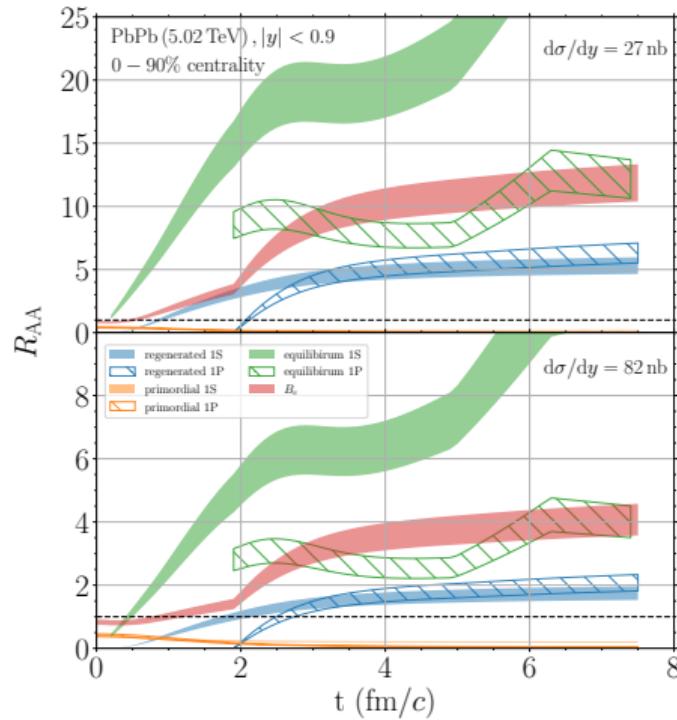
# $B_c$ $p_T$ spectra and cross section in 5 TeV $pp$ Collisions



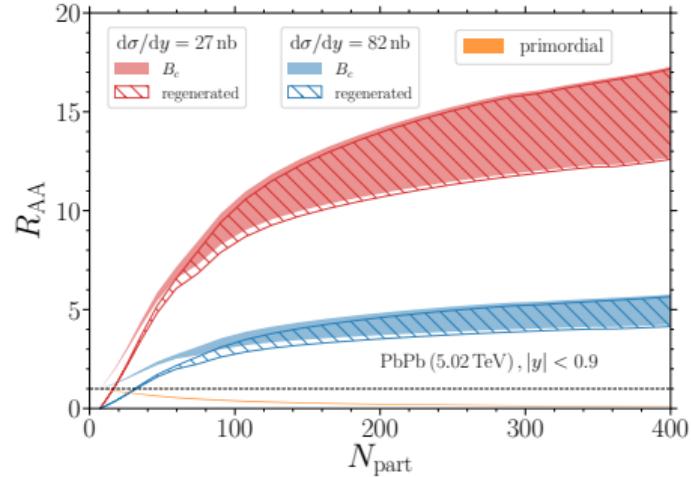
- $\frac{dN_{pp}^{B_c}}{2\pi p_T dp_T} = \frac{N}{(1 + \frac{p_T}{A(p_T)})^n}$   
fitted to 8 TeV, forward-rapidity
- $\langle p_T \rangle \Rightarrow 5.02 \text{ TeV}$  and mid-rapidity
- Theoretical calculations:  
 $\text{BR}(B_c \rightarrow J/\psi \mu \bar{\nu}) \sim 1.4\% - 7.5\%$
- $\text{BR} \sim 4 \pm 2\%$ ,  $\frac{d\sigma_{B_c}^{pp}}{dy} = 27 - 82 \text{ nb}$

[LHCb, '15] [S. Acharya *et al.*, '19, '17]

# $B_c$ Time Evolution in 5.02 TeV Pb-Pb Collisions

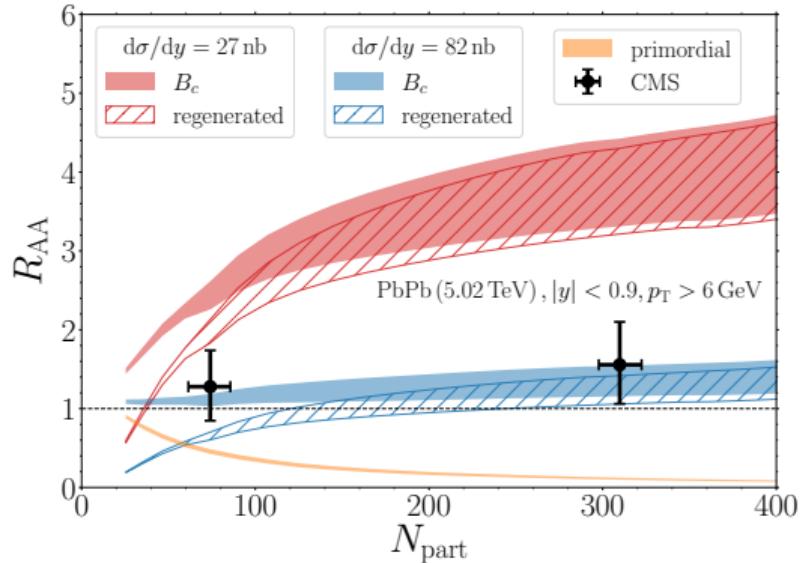
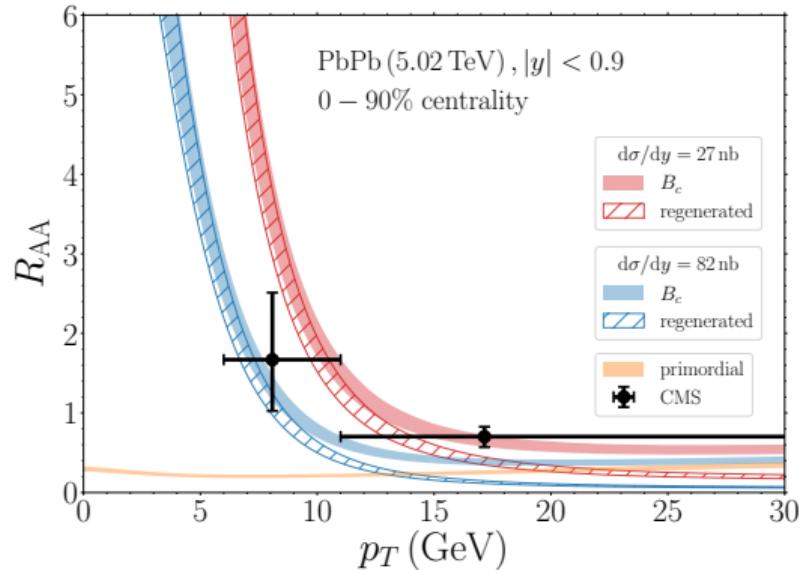


- Onset of regeneration at  $T_{\text{diss}}$



- $$R_{AA} = \frac{N_{\text{Coll}} N_{B_c}^{\text{pp}} S_{B_c} + N_{B_c}^{\text{reg}}}{N_{\text{Coll}} N_{B_c}^{\text{pp}}}$$
- $$N^{\text{tot}}(1S) = N^{\text{dir}}(1S) + \text{BR}(1P \rightarrow 1S) N^{\text{dir}}(1P)$$
- $\text{BR}(1P \rightarrow 1S) = 100\%$
- regeneration predicted without new parameters

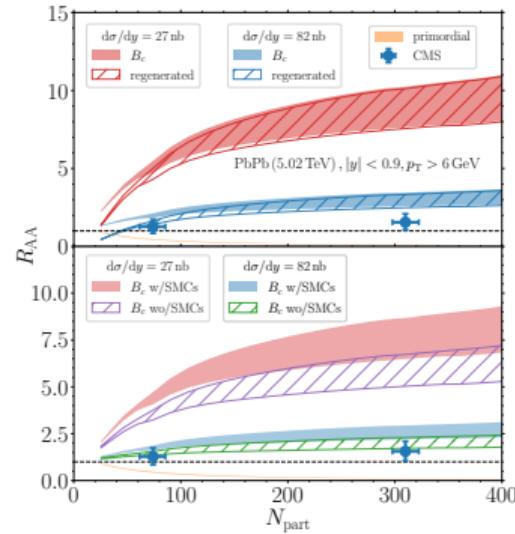
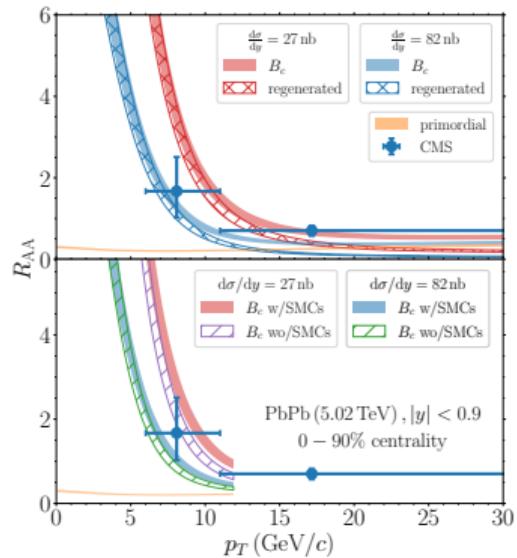
# $B_c$ in 5 TeV Pb-Pb Collisions



- $B_c (p_T)$ : coalescence:  $\bar{b} + c \rightarrow B_c^+$
- Dominated by regeneration, better agreement for smaller  $\sigma_{B_c}^{pp}$

# Results with/without Momentum Space Correlations (SMCs)

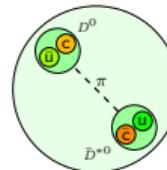
[He *et al.*, PRL 128, 162301]



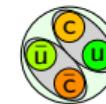
- $B_c$   $p_T$  is harder than the spectra without SMCs.
- $B_c$   $R_{AA}$  is enhanced by the implement of SMCs.

# X(3872): Molecular vs. Tetraquark Scenario

- Vacuum mass of  $X(3872) \approx \bar{D}^{*0}(2007) + D^0(1865) \sim$



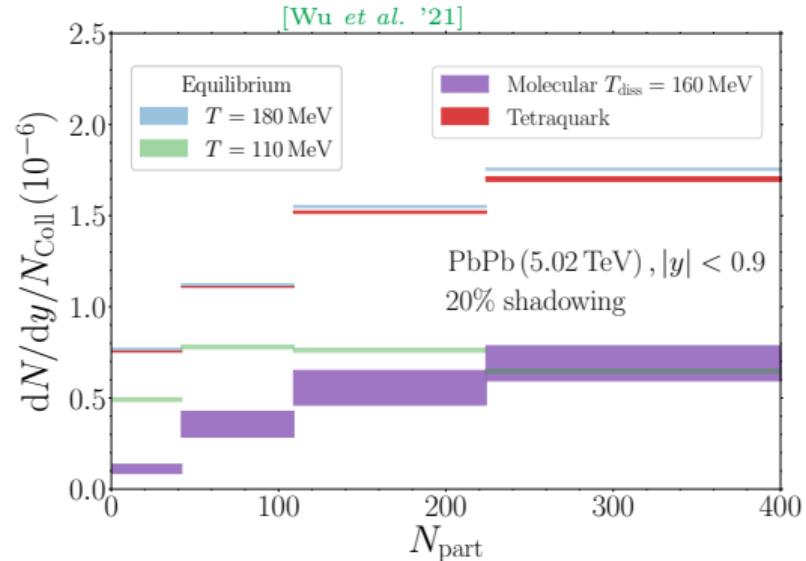
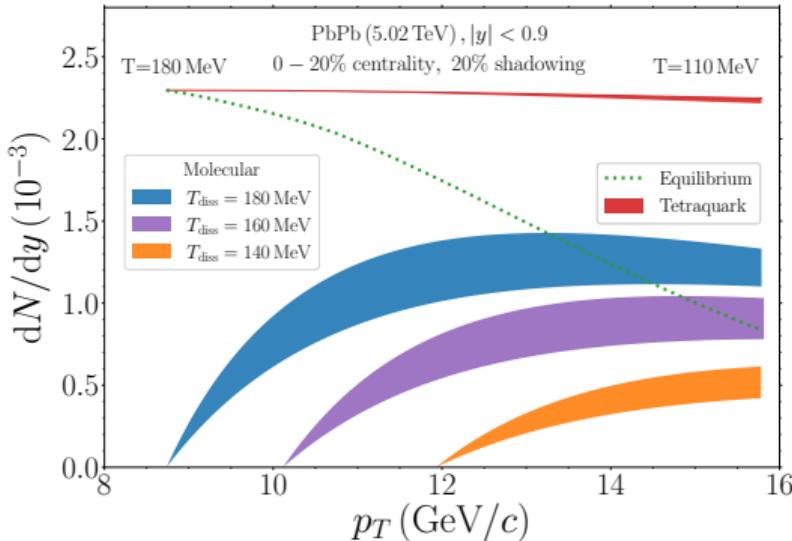
- Vacuum width:  $\Gamma(X(3872)) < 1.2 \text{ MeV} \sim$



- Reaction rate in fireball:  $\Gamma \sim \Gamma_0 \left( \frac{T}{T_0} \right)^n$ 
  - Molecular: Loosely-bound molecular state  
 $\Gamma_0 \sim 300\text{-}500 \text{ MeV}$  [Cleven *et al.*'19]
  - Tetraquark: Compact diquark anti-diquark bound state  
 $\Gamma_0 \sim 30\text{-}50 \text{ MeV}$
  - Depends weakly on  $n$

- Initial condition at hadronization
  - Molecular:  $N(T = T_C) = 0$   
Small binding energy, destroyed in QGP
  - Tetraquark:  $N(T = T_C) = N^{eq}(T_C)$   
Likely to form in the QGP phase

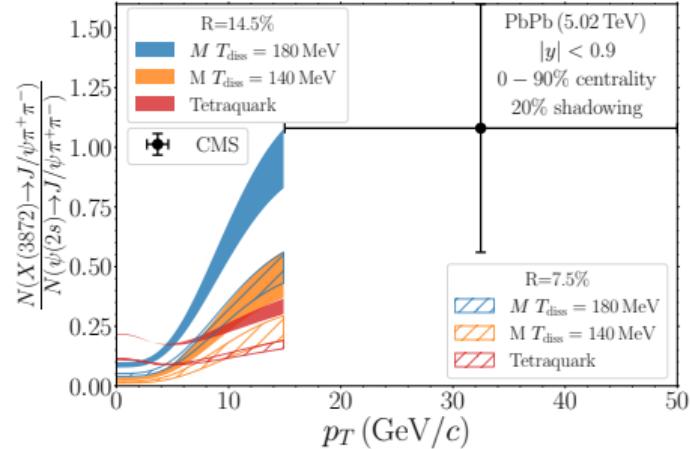
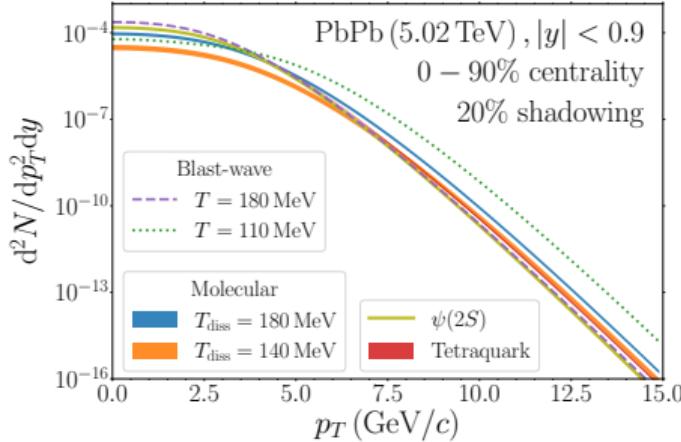
# X(3872) Time and Centrality Dependence in 5 TeV Pb-Pb Collisions



- Tetraquark: small reaction rate  $\Rightarrow$  mainly from the initial yield at hadronization
- Molecular: large reaction rate  $\Rightarrow$  approaches the equilibrium at  $T = 110 \text{ MeV}$
- Molecular: close to the thermal freeze-out equilibrium limit
- Tetraquark: close to the equilibrium limit at hadronization
- Final ratio  $N_{\text{Tet}}/N_{\text{Mol}} \sim 3$  for most centralities

# X(3872) $p_T$ Spectra in 5 TeV Pb-Pb Central Collisions

[CMS, '22]



- Both scenarios in between of the blast wave  $p_T$  spectra at hadronization and thermal freeze-out
- Tetraquark: close to the blast wave  $p_T$  at hadronization
- Molecular: produced later  $\Rightarrow$  has harder  $p_T$  spectra

[PDG, '22]

- $\text{BR}(\psi(2S) \rightarrow J/\psi \pi^+ \pi^-) = 34.68 \pm 0.30\%$
  - $\text{BR}(X(3872) \rightarrow J/\psi \pi^+ \pi^-) = 3.8 \pm 1.2\%$
- $$R = \frac{\text{BR}(X(3872) \rightarrow J/\psi \pi^+ \pi^-)}{\text{BR}(\psi(2S) \rightarrow J/\psi \pi^+ \pi^-)} = 11.0 \pm 3.5\%$$