



Uniwersytet  
Wrocławski

# Early quark deconfinement in neutron stars

**Oleksii Ivanytskyi**

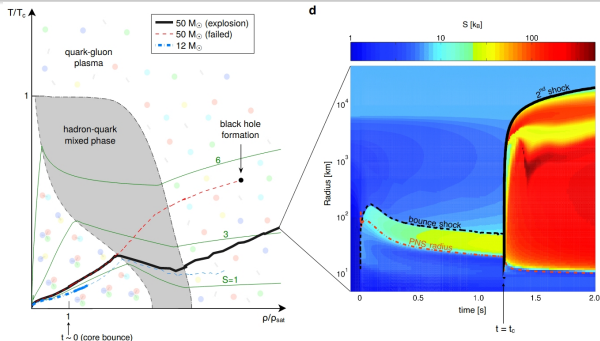
with **David Blaschke**

EMMI workshop on anti-matter, hyper-matter & exotica

Bologna, 17 February 2023

# Quark matter in supernova explosions

- $2M_{\odot}$  stars formation? (accretion is too slow)
- Supernovae with progenitor mass  $\sim 50 M_{\odot}$
- Quark-hadron transition stabilizes collapse



T. Fischer et al., Nature Astronomy 2, 980–986 (2018)

**Table 1 | Summary of the supernova simulation results with hadron–quark phase transition**

$M_{\text{ZAMS}}$ ( $M_{\odot}$ )	$t_{\text{onset}}$ (s)	$t_{\text{collapse}}$ (s)	$\rho_{\text{collapse}}$ ( $\rho_{\text{sat}}$ )	$T_{\text{collapse}}$ (MeV)	$M_{\text{PNS,collapse}}^a$ ( $M_{\odot}$ )	$t_{\text{final}}$ (s)	$\rho_{\text{final}}$ ( $\rho_{\text{sat}}$ )	$T_{\text{final}}$ (MeV)	$M_{\text{PNS,final}}^a$ ( $M_{\odot}$ )	$E_{\text{expl}}^*$ ( $10^{51}$ erg)
$12^{12}$	3.251	3.489	2.49	28	1.727	3.598	5.5	17	1.732	0.1
$18^{12}$	1.465	1.518	2.53	27	1.958	1.575	5.9	18	1.964	1.6
$25^{11}$	0.905	0.976	2.40	31	2.163	0.983	9.6	19	2.171 <sup>b</sup>	–
$50^{\dagger}$	1.110	1.215	2.37	32	2.105	1.224	5.8	31	2.092	2.3

Deconfinement is a supernova engine for massive blue giants

# Hyperon puzzle

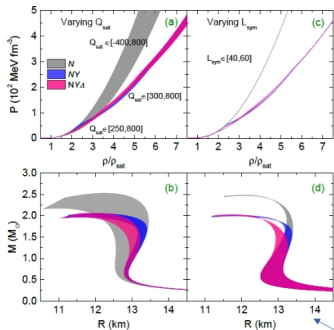


FIG. 4. EoS models and MR relations for  $N$ ,  $NY$ , and  $NY\Delta$  compositions of stellar matter. The bands are generated by varying the parameters  $Q_{\text{sat}}$  [MeV] (a, b) and  $L_{\text{sym}}$  [MeV] (c, d). The ranges of  $Q_{\text{sat}}$  and  $L_{\text{sym}}$  allowed by  $\chi$ EFT and maximum mass constraints are indicated in the figures.

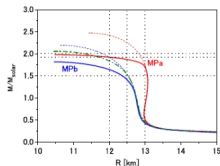


FIG. 7. Neutron-star masses as a function of the radius  $R$ . Solid (dashed) curves are with (without) hyperon ( $\Lambda$  and  $\Sigma^-$ ) mixing for ESC+MPa and ESC+MPb. The dot-dashed curve for MPb is with  $\Lambda$  mixing only. Also see the caption of Fig. 3.

Yamamoto et al., Phys.Rev.C 96 (2017) 06580;  
arXiv:1708.06163 [nucl-th]  
Yamamoto et al., Eur. Phys. J. A 52 (2016) 19;  
arXiv:1510.06099 [nucl-th]  
Ji & Sedrakian, Phys. Rev. C 100 (2019) 015809;  
arXiv:1903.06057 [astro-ph.HE]

Examples for realistic hadronic EoS which suggest a Berlin Wall is inferior to the line  $M = 2.0 M_{\text{sun}}$

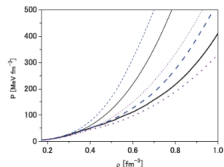


Fig. 8. Pressure  $P$  as a function of baryon density  $\rho$ . Thick (thin) curves are with (without) hyperon mixing. Solid, dashed and dotted curves are for MPa, MPa\* and MPb.

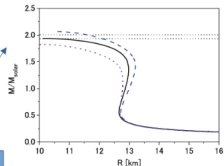


Fig. 9. Neutron-star masses as a function of the radius  $R$ . Solid, dashed and dotted curves are for MPa, MPa\* and MPb. Two dotted lines show the observed mass  $(1.97 \pm 0.04)M_{\odot}$  of J1614-2230.

Hyperons soften EoS, prevent neutron stars from reaching  $2M_{\odot}$

# False quark dominance in hybrid quark-hadron EoS

- Hadronic EoS consistent with astro (DDf4) + NJL model



False quark onset already @  $T \simeq 60$  MeV

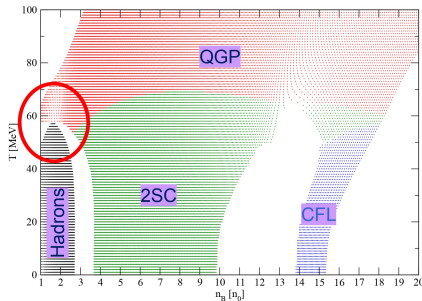
- Hadron decays are energetically favorable

$$M_q \simeq 330 \text{ MeV}$$

$$M_\omega = 783 \text{ MeV} \Rightarrow$$

$$M_\rho = 775 \text{ MeV}$$

*quarks are too light  
to be confined*



Effective quark “confinement” is needed

# Relativistic density functional

$$\mathcal{L} = \bar{q}(i\partial\!\!\!/ - \hat{m})q + \mathcal{L}_V + \mathcal{L}_D - \mathcal{U}$$

- **Vector repulsion**

$$\mathcal{L}_V = -G_V(\bar{q}\gamma_\mu q)^2$$

- needed to reach  $2M_\odot$
- motivated by non-perturbative gluon exchange

S. Yong et al., Phys. Rev. D 100, 034018 (2019)

- **Diquark pairing**

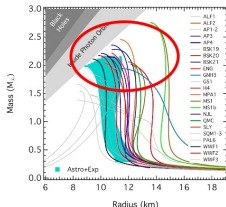
$$\mathcal{L}_D = G_D \sum_{A=2,5,7} (\bar{q}i\gamma_5\tau_2\lambda_A q^c)(\bar{q}^c i\gamma_5\tau_2\lambda_A q)$$

- motivated by Cooper theorem
- color superconductivity

- **Density functional** ( $G_0$  – coupling,  $\alpha \geq 0$ ,  $\langle \bar{q}q \rangle_0$  –  $\chi$ -condensate in vacuum)

$$\mathcal{U} = G_0 \left[ (1 + \alpha) \langle \bar{q}q \rangle_0^2 - (\bar{q}q)^2 - (\bar{q}i\vec{\tau}\gamma_5 q)^2 \right]^{\frac{1}{3}}$$

- motivated by String Flip Model
- $\chi$ -symmetric interaction



# Expansion around $\langle \bar{q}q \rangle$ and $\langle \bar{q}i\vec{\tau}\gamma_5 q \rangle = 0$

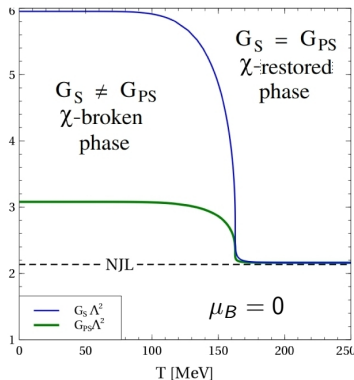
$$\mathcal{U} = \underbrace{\mathcal{U}_{MF}}_{0^{\text{th}} \text{ order}} + \underbrace{(\bar{q}q - \langle \bar{q}q \rangle) \Sigma_{MF}}_{1^{\text{st}} \text{ order}} - \underbrace{G_S (\bar{q}q - \langle \bar{q}q \rangle)^2 - G_{PS} (\bar{q}i\vec{\tau}\gamma_5 q)^2}_{2^{\text{nd}} \text{ order}} + \dots$$

- Mean-field self-energy

$$\Sigma_{MF} = \frac{\partial \mathcal{U}_{MF}}{\partial \langle \bar{q}q \rangle}$$

- Effective medium dependent couplings

$$G_S = -\frac{1}{2} \frac{\partial^2 \mathcal{U}_{MF}}{\partial \langle \bar{q}q \rangle^2}, \quad G_{PS} = -\frac{1}{6} \frac{\partial^2 \mathcal{U}_{MF}}{\partial \langle \bar{q}i\vec{\tau}\gamma_5 q \rangle^2}$$



# Expansion around $\langle \bar{q}q \rangle$ and $\langle \bar{q}i\vec{\tau}\gamma_5 q \rangle = 0$

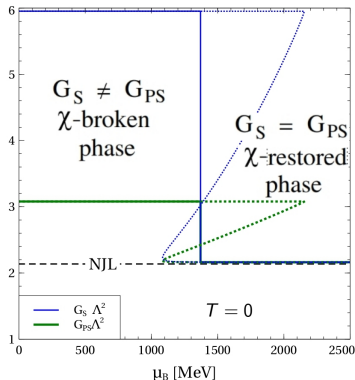
$$\mathcal{U} = \underbrace{\mathcal{U}_{MF}}_{0^{\text{th}} \text{ order}} + \underbrace{(\bar{q}q - \langle \bar{q}q \rangle) \Sigma_{MF}}_{1^{\text{st}} \text{ order}} - \underbrace{G_S (\bar{q}q - \langle \bar{q}q \rangle)^2 - G_{PS} (\bar{q}i\vec{\tau}\gamma_5 q)^2}_{2^{\text{nd}} \text{ order}} + \dots$$

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# Comparison to NJL model

$$\mathcal{L} = \bar{q}(i\not{\partial} - \underbrace{(m + \Sigma_{MF})}_{\text{effective mass } m^*})q + G_S(\bar{q}q)^2 + G_{PS}(\bar{q}i\vec{\tau}\gamma_5q)^2 + \dots + \mathcal{L}_V + \mathcal{L}_D$$

## • Similarities:

- current-current interaction
- (pseudo)scalar, vector, diquark, ... channels

## • Differences:

- high  $m^*$  at low  $T$ ,  $\mu \Rightarrow$  “**confinement**”

$$\langle \bar{q}q \rangle = \langle \bar{q}q \rangle_0 \Rightarrow m^* = m - \frac{2G_0}{3\alpha^{2/3}\langle \bar{q}q \rangle_0^{1/3}}$$

$\Downarrow$

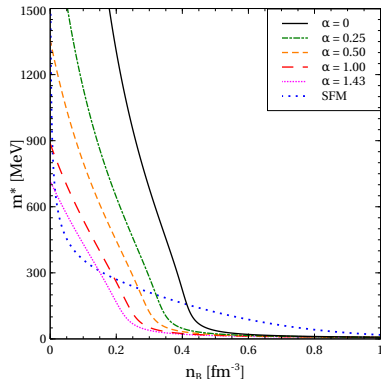
$$m^* \rightarrow \infty \text{ at } \alpha \rightarrow 0$$

- medium dependent couplings:

$$\text{low } T, \mu, \Rightarrow G_S \neq G_{PS} \Rightarrow \chi\text{-broken}$$

$$\text{high } T, \mu, \Rightarrow G_S = G_{PS} \Rightarrow \chi\text{-symmetric}$$

**T = 0**





# Parameterization of the model

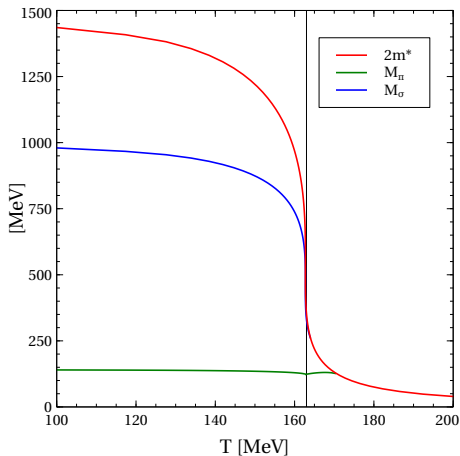
## Meson propagators

$$D_\pi = \frac{1}{2G_{PS}} - \text{diagram}$$

$$D_\sigma = \frac{1}{2G_S} - \text{diagram}$$

$m$ [MeV]	$\Lambda$ [MeV]	$\alpha$	$D_0\Lambda^{-2}$
4.2	573	1.43	1.39
$M_\pi$ [MeV]	$F_\pi$ [MeV]	$M_\sigma$ [MeV]	$\langle \bar{l}l \rangle_0^{1/3}$ [MeV]
140	92	980	-267

$$T_c(\mu_B = 0) = 163 \text{ MeV}$$



$$2m^* > M_{\text{meson}} \Rightarrow \text{stable meson}$$

$$2m^* < M_{\text{meson}} \Rightarrow \text{meson dissolves}$$

# Hybrid quark-hadron EoS

- **Charge neutrality:** electrons

- **$\beta$ -equilibrium:**

$$\mu_d = \mu_u + \mu_e$$

- **Hadron EoS:** DD2

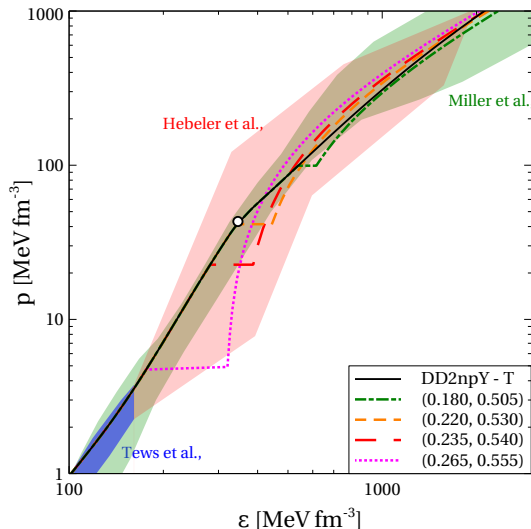
S. Typel et al., PRC 81, 015803 (2010)

- **Maxwell construction:**

$$p_q(\mu_B^c) = p_h(\mu_B^c)$$

- **Model labeling:**

$$(\eta_V, \eta_D), \quad \eta_{V,D} \equiv \frac{G_{V,D}}{G_S}|_{T=\mu=0}$$



O. Ivanytskyi and D. Blaschke, Phys. Rev. D 105, 114042 (2022)

# Mass radius diagram

- Hydrostatic equilibrium

$$\frac{dp}{dr} = -\frac{Gm\epsilon}{r^2} \left(1 + \frac{p}{\epsilon}\right) \left(1 + \frac{4\pi r^3 \rho}{m}\right) \left(1 - \frac{2Gm}{r}\right)^{-1}$$

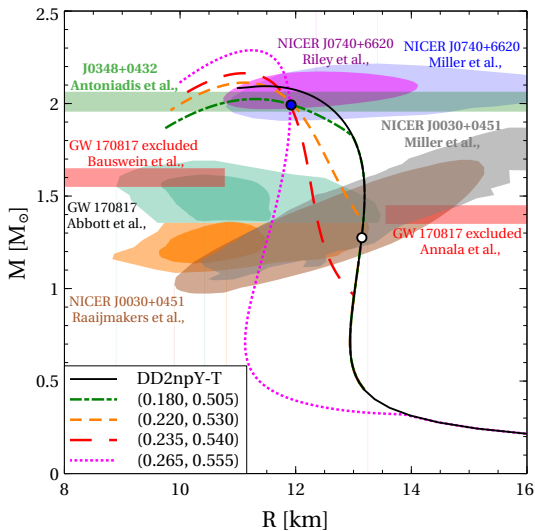
$$\frac{dm}{dr} = 4\pi r^2 \epsilon$$

- Cold matter EoS

$$\begin{cases} p = p(\mu_B) \\ \epsilon = \mu_B \frac{\partial p}{\partial \mu_B} - p \end{cases} \Rightarrow p = p(\epsilon)$$

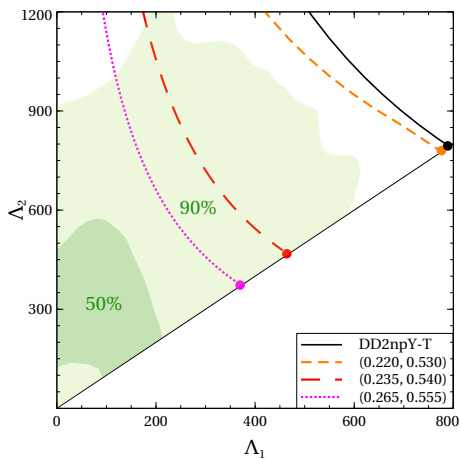
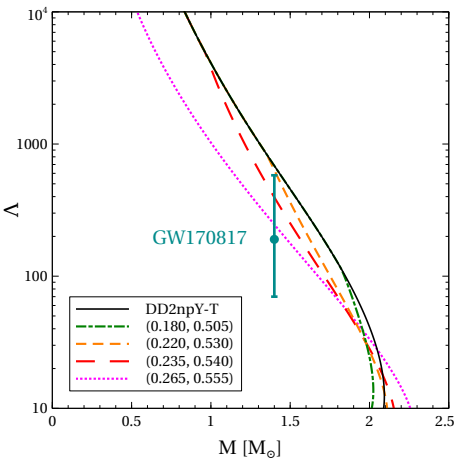
- Total radius  $R$  and mass  $M$

$$r = R \Rightarrow \begin{cases} p = 0 \\ m = M \end{cases}$$



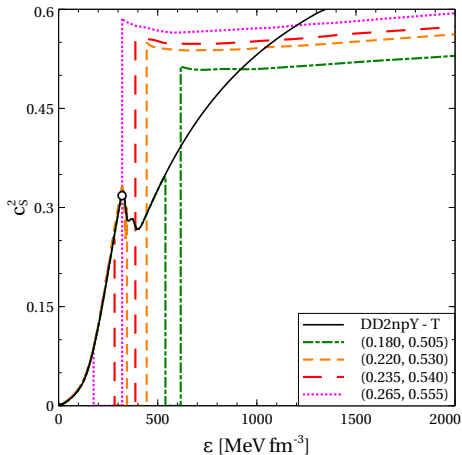
O. Ivanytskyi and D. Blaschke, Phys. Rev. D 105, 114042 (2022)

# Tidal deformability



O. Ivanytskyi and D. Blaschke, Phys. Rev. D 105, 114042 (2022)

# Speed of sound



O. Ivanytskyi and D. Blaschke, Phys. Rev. D 105, 114042 (2022)

- $c_s^2 \simeq \text{const}$  at  $\epsilon \leq 2 \text{ GeV}/\text{fm}^3$

**Constant speed of sound  
parameterization of quark EoS  
with  $c_s^2 = 0.5 - 0.6$   
at the neutron star densities**

- $c_s^2 \rightarrow 1$  at  $\epsilon \rightarrow \infty$

**Can conformality be restored?**

**Yes. Requires suppressing  
vector repulsion and  
diquark pairing**

# Restoring conformal limit

- Fock energy via non-perturbative gluon exchange with  $D_{gluon} \propto \frac{1}{k^2 - M_{gluon}^2}$

$$\varepsilon_{\text{repulsion}} = G_V \langle q^+ q \rangle^2 \quad \text{with} \quad G_V = \frac{4\pi\alpha_s/3}{9M_{gluon}^2 + 8k_F^2}, \quad \alpha_s - \text{frozen}$$

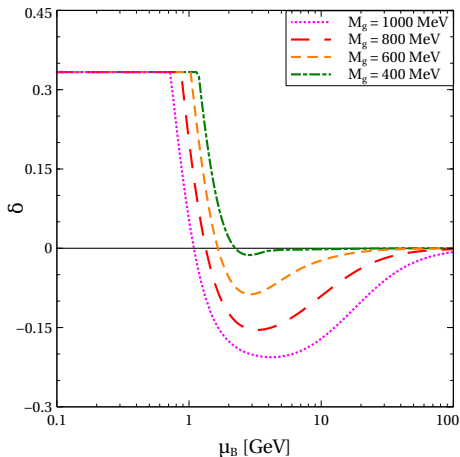
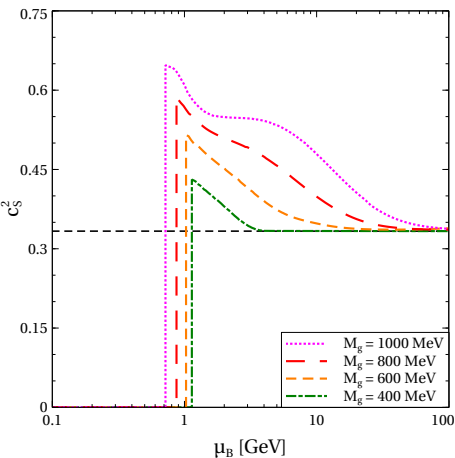
Y. Song, G. Baym, T. Hatsuda, and T. Kojo Phys. Rev. D 100, 034018 (2019)

- Medium dependent vector and diquark couplings

$$G_V = \frac{G_V^{\text{vacuum}}}{1 + \frac{8}{9M_{gluon}^2} \left( \frac{\pi^2 \langle q^+ q \rangle}{2} \right)^{2/3}} \quad \text{and} \quad G_D = \frac{G_D^{\text{vacuum}}}{1 + \frac{8}{9M_{gluon}^2} \left( \frac{\pi^2 \langle \bar{q}^c i\tau_2 \gamma^5 \lambda_2 q \rangle}{2} \right)^{2/3}}$$

**Don't forget rearrangement terms in pressure needed to provide thermodynamic consistency**

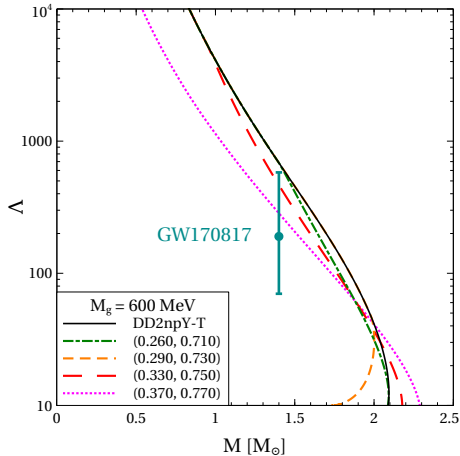
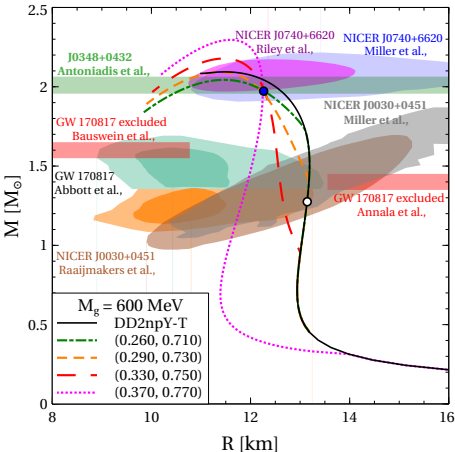
# Asymptotically conformal EoS (symmetric matter @ $T=0$ )



O. Ivanytskyi and D. Blaschke, arXiv:2209.02050

Conformality is reached at  $\mu_B/3 \gg M_{gluon}$

# Compact stars with asymptotically conformal EoS



O. Ivanytskyi and D. Blaschke, arXiv:2209.02050

The same quality at  $M_{gluon} = 700$  and  $800 \text{ MeV}$



# Phase diagram (Q-neutral, $\beta$ -equilibrium, $M_{gluon} \rightarrow \infty$ )

- **Normal quark matter**

$$2 \text{ spin} \times 2 \text{ flavor} \times 3 \text{ color} = 12$$

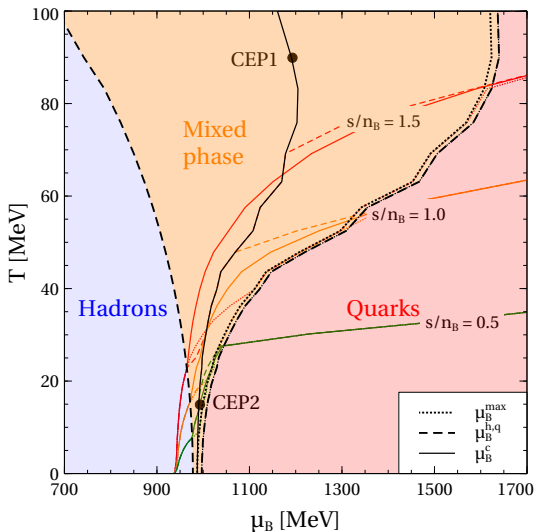
- **2SC quark matter**

$$2 \text{ spin} \times 2 \text{ flavor} \times 1 \text{ color} + 1 = 5$$

Quark pairing reduces  
number of quark states



requires higher T  
along adiabat



O. Ivanytskyi, D. Blaschke, 2205.03455 [nucl-th], accepted to EPJ A

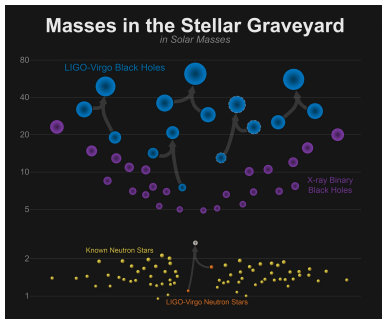
# Conclusions

- Deconfined of quark matter is essential for the supernovae explosions of Blue Supergiants producing compact stars of mass  $> 2M_{\odot}$
- Gravitational wave signal from postmerger could unambiguously identify compact stars with quark cores
- Effective "confining" NJL model with color superconductivity is derived based on the  $\chi$ -symmetric density functional
- Medium dependent quark-meson couplings provide conformal limit
- Agreement with the observational data on compact stars implies early onset of quark matter
- Deconfinement to color superconducting quark matter leads to the temperature growth along the adiabats

**Thank you for your attention**

# Ultra heavy compact stars?

GW190814 – merger of  $23 M_{\odot}$  black hole and  $2.6 M_{\odot}$  enigma

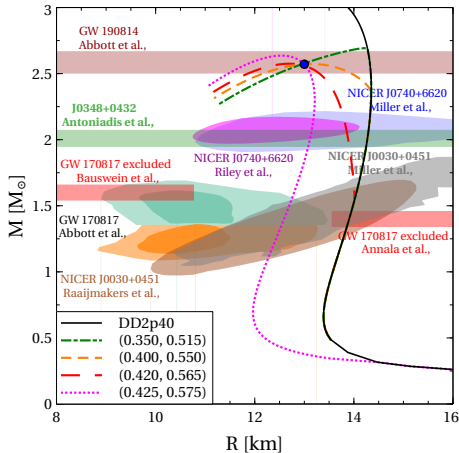


Adopted from <https://www.ligo.caltech.edu/image/ligo20200902a>

No known objects at  $\sim 2 - 5 M_{\odot}$



$2.6 M_{\odot}$  enigma can be  
a neutron star



$$\Lambda_{1.4} = 543$$

O. Ivanytskyi and D. Blaschke, Phys. Rev. D 105, 114042 (2022)



- Low chemical potential

$$m^* \gg m \Rightarrow \Delta = 0$$

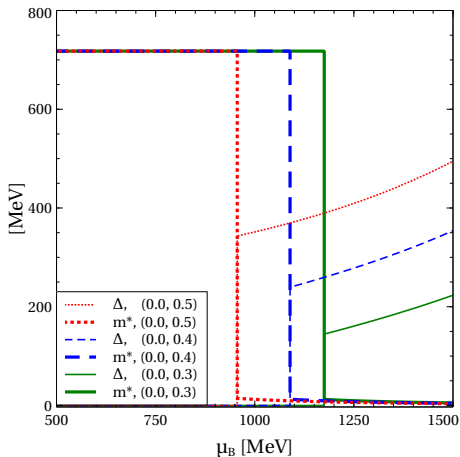
$\chi$  – broken  
normal phase

- High chemical potential

$$m^* \rightarrow 0 \Rightarrow \chi \text{ – restored SC phase}$$

Holds for  $T \neq 0$

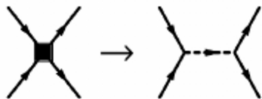
$T = 0$



# Bosonization of (pseudo)scalar interaction

- Hubbard-Stratonovich transformation

$$\exp \left[ \int dx G_i (\bar{q} \Gamma_i q)^2 \right] = \int [D\phi_i] \exp \left[ - \int dx \left( \frac{\phi_i^2}{4G_i} + \bar{q} \phi_i \Gamma_i q \right) \right], \quad i = \sigma, \vec{\pi}$$



$$\begin{aligned} \Gamma_\sigma &= 1 & - & \sigma \text{ vertex} \\ \vec{\Gamma}_\pi &= i\gamma_5 \vec{\tau} & - & \vec{\pi} \text{ vertex} \end{aligned}$$

- Bosonized Lagrangian ( $m^* = m + \Sigma_{MF}$  - effective quark mass)

$$\begin{aligned} \mathcal{L} &= \bar{q}(i\not{D} - m^*)q + \mathcal{L}_V + \mathcal{L}_D - U + \langle \bar{q}q \rangle \Sigma_{MF} \\ &\quad - \underbrace{\frac{\sigma^2}{4G_S} - \frac{\vec{\pi}^2}{4G_{PS}} - \bar{q}(\sigma + i\vec{\pi}\vec{\tau}\gamma_5)q + \sigma \langle \bar{q}q \rangle}_{\text{fully beyond mean field terms}} \end{aligned}$$

- Field equations for  $\sigma$  and  $\vec{\pi}$

$$\begin{cases} \sigma = 2G_S(\langle \bar{q}q \rangle - \bar{q}q) \\ \vec{\pi} = -2G_{PS}\bar{q}i\vec{\tau}\gamma_5 q \end{cases} \Rightarrow \langle \sigma \rangle = \langle \vec{\pi} \rangle = 0 \Rightarrow \sigma, \vec{\pi} - \text{beyond MF}$$

comment:  $\langle \sigma \rangle = 0$  does not assume  $\chi$ -symmetry since  $\langle \bar{q}q \rangle \neq 0$

# Mean field ( $\omega_\mu = g_{\mu 0} \omega$ , $\Delta = \text{const}$ , $\sigma = \vec{\pi} = \mathbf{0}$ )

- Nambu-Gorkov Lagrangian with bosonized vector and diquark channels

$$\mathcal{L} + q^+ \hat{\mu} q = \bar{Q} \hat{S}_{NG}^{-1} Q + \frac{\omega_\mu \omega^\mu}{4G_V} - \frac{\Delta_A \Delta_A^*}{4G_D} - U + \langle \bar{q} q \rangle \Sigma_{MF}$$

$$Q = \frac{1}{\sqrt{2}} \begin{pmatrix} q \\ q^c \end{pmatrix} \quad \hat{S}_{NG}^{-1} = \begin{pmatrix} i\not{\partial} + \not{\psi} - m^* + \gamma_0 \hat{\mu} & i\Delta_A \gamma_5 \tau_2 \lambda_A \\ i\Delta_A \gamma_5 \tau_2 \lambda_A & i\not{\partial} + \not{\psi} - m^* + \gamma_0 \hat{\mu} \end{pmatrix}$$

- Statistical partition and thermodynamic potential

$$\mathcal{Z} = \int [D\bar{q}][Dq] \exp \left[ \int dx (\mathcal{L} + q^+ \hat{\mu} q) \right]$$

$$\Omega = -\frac{1}{\beta V} \ln \mathcal{Z} = -\frac{1}{2\beta V} \text{Tr} \ln(\beta S_{NG}^{-1}) - \frac{\omega^2}{4G_V} + \frac{\Delta^2}{4G_D} + U - \langle \bar{q} q \rangle \Sigma_{MF}$$

- Vector field, diquark gap,  $\chi$ -condensate

$$\frac{\partial \Omega}{\partial \omega} = 0, \quad \frac{\partial \Omega}{\partial \Delta} = 0, \quad \langle \bar{q} q \rangle = \sum_f \frac{\partial \Omega}{\partial m_f}$$

# Superconductivity onset

- **Single quark energy and distribution**

$$E_f^\pm = \sqrt{(E_f \mp \mu_f)^2 + \Delta^2}$$

$$f_f^\pm = [\exp(E_f^\pm / T) + 1]^{-1}$$

- **Gap equation**

$$\frac{\partial \Omega}{\partial \Delta} = \frac{\Delta}{2G_D} - 2\Delta \sum_{f,a=\pm} \int \frac{d\mathbf{k}}{(2\pi)^3} \frac{1 - 2f_f^a}{E_f^a} = 0$$

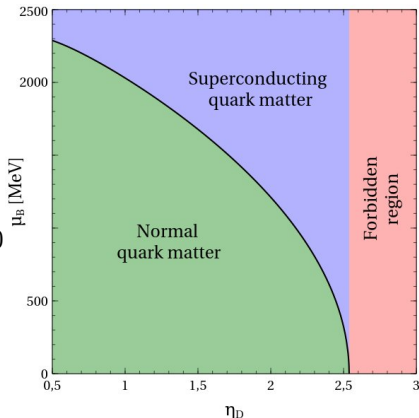
⇓

**two solutions :  $\Delta = 0$  or  $\Delta \neq 0$**

- **Two solutions coincide  $\Rightarrow$  SC onset**

$$\left. \frac{\partial^2 \Omega}{\partial \Delta^2} \right|_{\Delta=0} = 0 \quad \Rightarrow \quad \mu_B = \mu_B(G_D)$$

$T = 0$



No vacuum superconductivity

⇓

$$\eta_D \lesssim 2.5$$



# Beyond mean field ( $\hat{\mu} = \mathbf{0} \Rightarrow \omega = \Delta = \mathbf{0}$ )

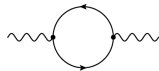
$$\mathcal{L} = \bar{q} \hat{S}^{-1} q - \frac{\sigma^2}{4G_S} - \frac{\vec{\pi}^2}{2G_{PS}} + \sigma \langle \bar{q} q \rangle - U + \Sigma_{MF} \langle \bar{q} q \rangle$$

$$\hat{S}^{-1} = \hat{S}_{MF}^{-1} + \Sigma_m, \quad \begin{cases} \hat{S}_{MF}^{-1} = i\not{\partial} - m^* - \text{MF propagator} \\ \Sigma_m = -\sigma \cdot \Gamma_\sigma - \vec{\pi} \cdot \vec{\Gamma}_\pi - \text{beyond MF self-energy} \end{cases}$$

- Integrating  $\bar{q}$ ,  $q$  and expanding up to  $\mathcal{O}(\Sigma_m^3)$

$$\begin{aligned} \mathcal{L}^{\text{eff}} &= \frac{\text{tr} \ln(\beta \hat{S}^{-1})}{\beta V} - \frac{\sigma^2}{4G_S} - \frac{\vec{\pi}^2}{4G_{PS}} + \sigma \langle \bar{q} q \rangle - U + \Sigma_{MF} \langle \bar{q} q \rangle \\ &\simeq -\Omega_{MF} - \frac{\sigma^2}{4G_S} - \frac{\vec{\pi}^2}{4G_{PS}} + \underbrace{\sigma \langle \bar{q} q \rangle - \text{tr}(\hat{S}_{MF} \Sigma_m)}_{\text{vanishes under } \int dx} + \frac{1}{2} \text{tr}(\hat{S}_{MF} \Sigma_m)^2 \end{aligned}$$

- Polarization operators of mesons



$$\Pi_{\sigma,\pi} = -\text{tr}(\hat{S}_{MF} \Gamma_{\sigma,\pi})^2 \Rightarrow -\text{tr}(\hat{S}_{MF} \Sigma_m)^2 = \sigma \Pi_\sigma \sigma + \vec{\pi} \Pi_\pi \vec{\pi}$$

# Beyond mean field thermodynamic potential

$$\Omega = \underbrace{\Omega_{MF} + \frac{1}{2\beta V} \text{tr} \ln \left[ \beta^{-2} \left( \frac{1}{2G_S} - \Pi_\sigma \right) \right]}_{\Omega_\sigma} + \underbrace{\frac{3}{2\beta V} \text{tr} \ln \left[ \beta^{-2} \left( \frac{1}{2G_{PS}} - \Pi_\pi \right) \right]}_{\Omega_\pi}$$

- **Meson propagators**

$$D_\sigma^{-1} = \frac{1}{2G_S} - \Pi_\sigma, \quad D_\pi^{-1} = \frac{1}{2G_{PS}} - \Pi_\pi$$

- **Meson masses**

$$D_j^{-1} = 0 \quad \Rightarrow \quad E_j(k), \quad M_j = E_j(0)$$

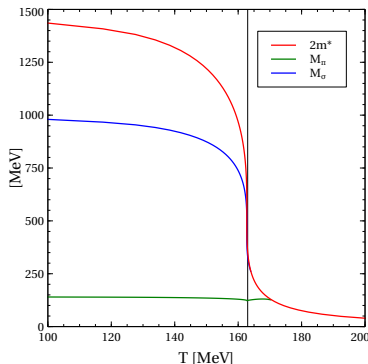
- **Meson phase shifts**

$$D_j = |D_j| e^{i\delta_j} \quad \Rightarrow \quad \delta_j = \text{Im} \ln(\beta^{-2} D_j)$$

- **Beth-Uhlenbeck EoS**

$$\Omega = \Omega_{MF} + \sum_{j=\sigma,\pi} \Omega_j, \quad \Omega_j = d_j T \int \frac{d^4 k}{(2\pi)^4} \ln(1 - e^{-\beta k_0}) \frac{\partial \delta_j}{\partial k_0}$$

$f_\pi = 90 \text{ MeV}$



# Beyond mean field pressure

- Approximation for  $\sigma_\pi$  (agrees with the Levinson theorem)

$$\delta_\pi = \pi [\theta(k_0 - E_b) - \theta(k_0 - E_{cont})] \theta(E_{cont} - E_b)$$

$$E_b^2 = k^2 + M_\pi^2 - \text{bound state}$$

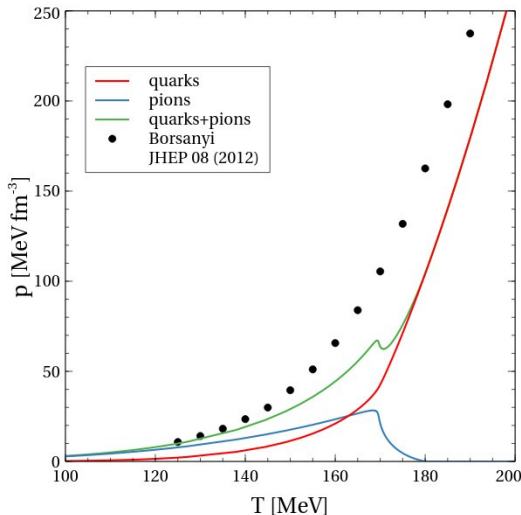
$$E_{cont}^2 = k^2 + (2m^*)^2 - \text{continuum}$$

D. Blaschke et al., *Symmetry* 13 (3), 514 (2021)

- Total pressure

$$p = p_{quarks} + p_{hadrons} + \underbrace{\mathcal{U}(\Phi) + p_{pert}}_{\text{missing}}$$

$$\mathcal{U}(\Phi), p_{pert} - \text{provide } \frac{\partial p}{\partial T} > 0$$



# Beyond mean field $\chi$ -condensate

- $\pi$  contribution to  $\chi$ -condensate

$$\langle \bar{q}q \rangle_\pi = -\frac{\partial p_\pi}{\partial m_q}$$

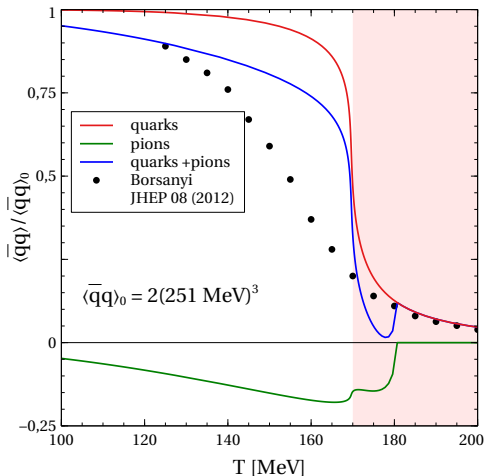
- Reliability

$$T \lesssim 170 \text{ MeV}$$

- $\chi$ -condensate melts too slowly



More hadrons are needed



# Confining density functional for quark matter

$$\mathcal{L} = \bar{q}(i\cancel{\partial} - m)q - \mathcal{U}(\bar{q}q, \bar{q}\gamma_0 q)$$

- Scalar and vector densities

$$\langle \bar{q}q \rangle = n_s, \quad \langle \bar{q}\gamma_0 q \rangle = n_v$$

- Scalar and vector self-energies

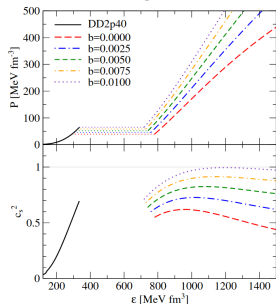
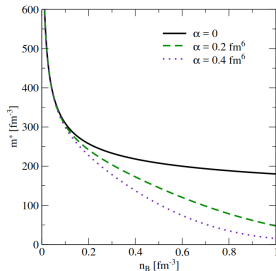
$$\Sigma_s = \frac{\partial \mathcal{U}(n_s, n_v)}{\partial n_s}, \quad \Sigma_v = \frac{\partial \mathcal{U}(n_s, n_v)}{\partial n_v}$$

- String-flip model

$$\mathcal{U} = \underbrace{D(n_v)n_s^{2/3}}_{\text{confinement}} + \underbrace{an_v^2 + \frac{bn_v^4}{1 + cn_v^2}}_{\text{modified vector repulsion}}$$

- Effective mass

$$m^* = m + \Sigma_s = m + \frac{2}{3}D(n_v)n_s^{-1/3}$$



M. Kaltenborn, N.-U. Bastian, and D. Blaschke. *PRD* **96**, 056024 (2017)

# Comparison to NJL model

$$\mathcal{L} = \bar{q}(i\not{D} - \underbrace{(m + \Sigma_{MF})}_{\text{effective mass } m^*})q + G_S(\bar{q}q)^2 + G_{PS}(\bar{q}i\vec{\tau}\gamma_5q)^2 + \dots + \mathcal{L}_V + \mathcal{L}_D$$

- **Similarities:**

- current-current interaction
- (pseudo)scalar, vector, diquark, ... channels

- **Differences:**

- high  $m^*$  at low  $T$ ,  $\mu \Rightarrow$  **“confinement”**

$$\langle \bar{q}q \rangle = \langle \bar{q}q \rangle_0 \Rightarrow m^* = m - \frac{2G_0}{3\alpha^{2/3}\langle \bar{q}q \rangle_0^{1/3}}$$

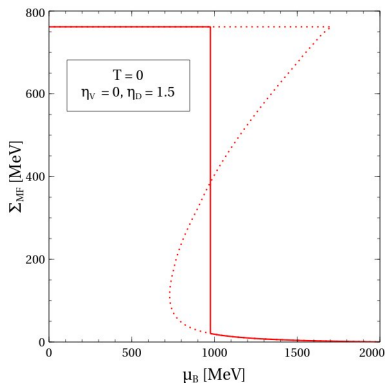
↓

$$m^* \rightarrow \infty \text{ at } \alpha \rightarrow 0$$

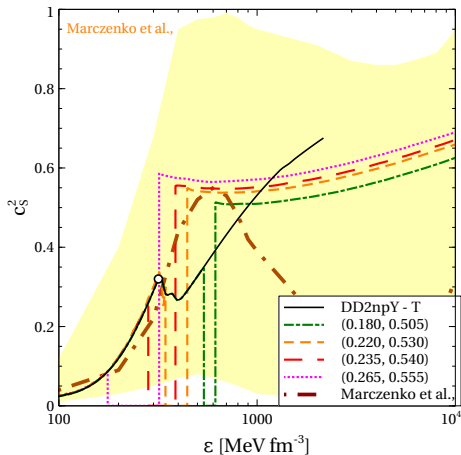
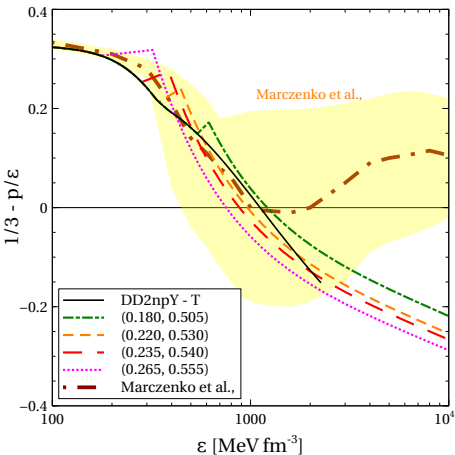
- medium dependent couplings:

low  $T$ ,  $\mu$ ,  $\Rightarrow G_S \neq G_{PS} \Rightarrow \chi$ -broken

high  $T$ ,  $\mu$ ,  $\Rightarrow G_S = G_{PS} \Rightarrow \chi$ -symmetric



# Hybrid quark-hadron EoS



# GW170817 – a merger of two compact stars

## Neutron Star Merger Dynamics

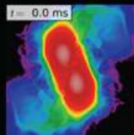
(General) Relativistic (Very) Heavy-Ion Collisions at  $\sim 100$  MeV/nucleon

Simulations: Rezzola et al (2013)

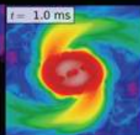
$t = -8.1$  ms



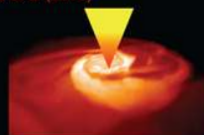
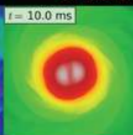
$t = 0.0$  ms



$t = 1.0$  ms



$t = 10.0$  ms



Inspiral:

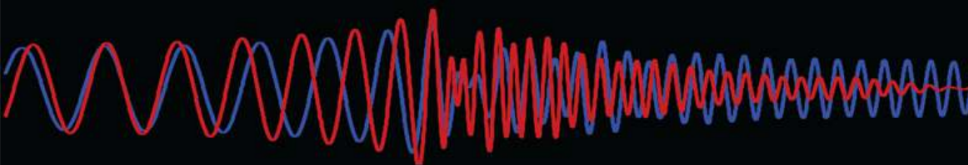
Gravitational waves,  
Tidal Effects

Merger:

Disruption, NS oscillations,  
ejecta and r-process nucleosynthesis

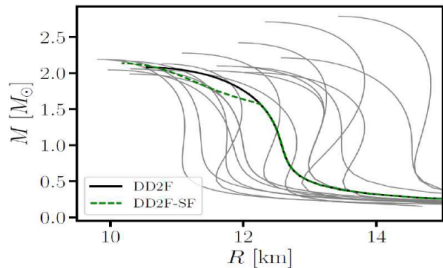
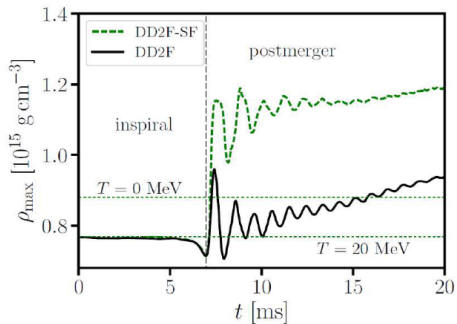
Post Merger:

GRBs, Afterglows, and  
Kilonova

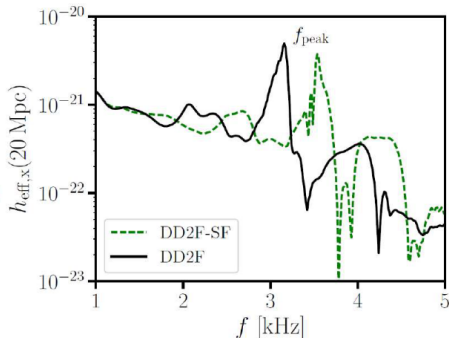




# Hybrid star formation in postmerger phase



Strong phase transition in postmerger GW,  
A. Bauswein et al. arxiv:1809.01116

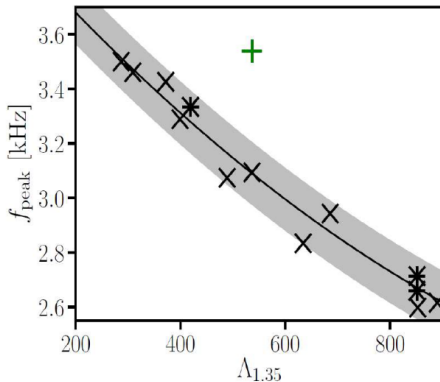
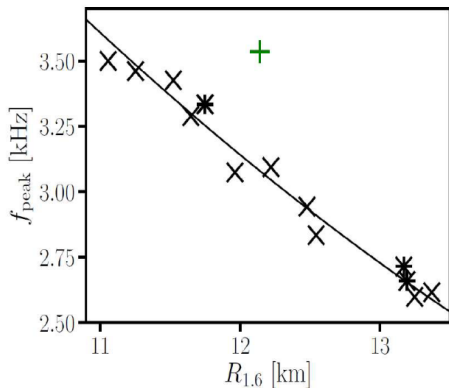


Hybrid star formation during NS merger  
→ higher densities and compacter star  
→ higher peak frequency of the GW

A. Bauswein et al., PRL 122 (2019) 061102

# Hybrid star formation in postmerger phase

Strong phase transition in postmerger GW signal,  
A. Bauswein et al., PRL 122 (2019) 061102; [arxiv:1809.01116]



**Strong deviation** from  $f_{\text{peak}} - R_{1.6}$  relation signals **strong phase transition** in NS merger!

**Complementarity** of  $f_{\text{peak}}$  from **postmerger** with tidal deformability  $\Lambda_{1.35}$  from **inspiral phase**.