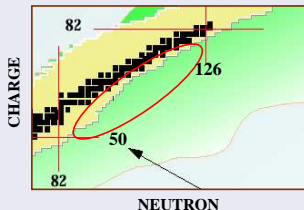


# Neutron Rich Nuclei via MNT Reactions

Giovanni POLLAROLO

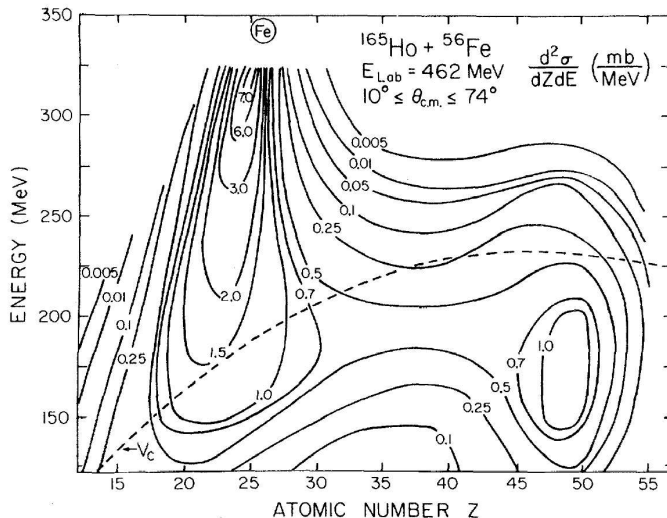
*Dipartimento di Fisica Teorica, Università di TORINO  
e INFN Sezione di Torino*



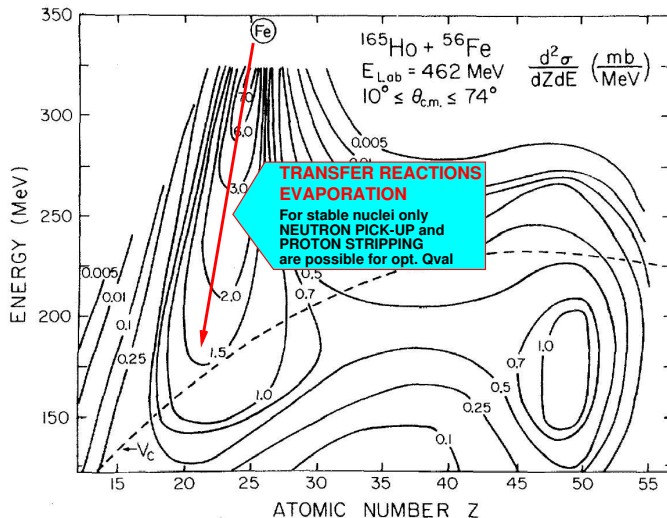
**IRIS 10** 1st Workshop on  
Inelastic Reaction Isotope Separator for Heavy Elements  
March 01, 2010, GSI, Darmstadt, Germany



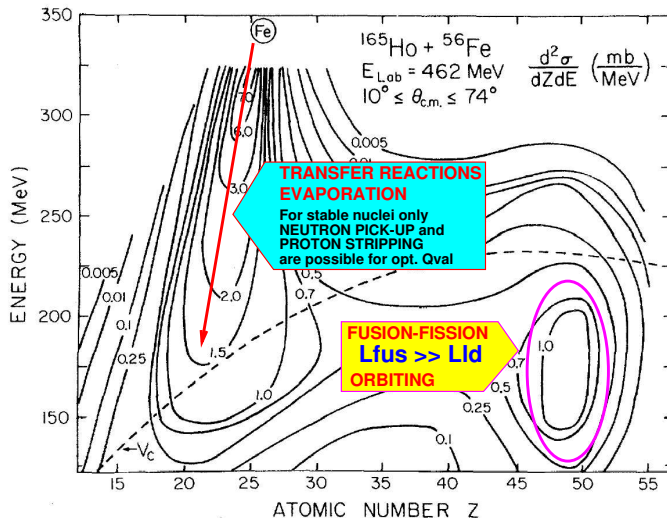
# HI reactions, a short overview



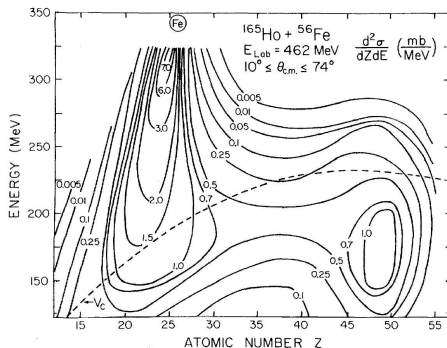
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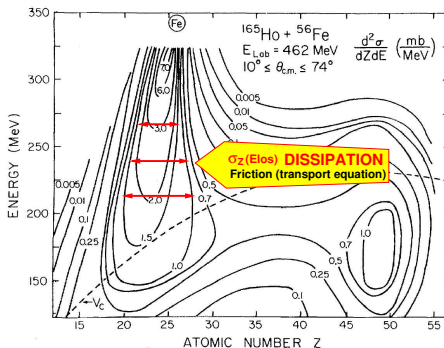
# HI reactions, a short overview



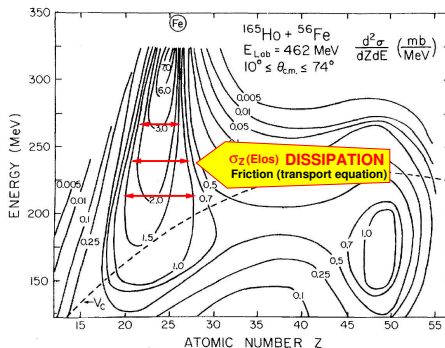
# Macroscopic approach



## Macroscopic approach



# Macroscopic approach



- **Transport equations**  
for the exchange of mass and charge.
- **friction forces**  
for energy and angular momentum dissipation



# Microscopic approach (elementary modes)

## Nuclear degrees of freedom

(collision time  $\tau = \sqrt{a/\ddot{r}_o}$ )

- **INELASTIC**  $f_{in}(r) \sim e^{-r/a_{in}}$   $a_{in} = 0.65 \text{ fm}$

(few channels but strong)

- low lying: mass (D) large  
force (C) small
- high lying: mass (D) small  
force (C) large

**NON** adiabatic  
coupled-channels  
adiabatic

- **TRANSFER**  $f_{tr}(r) \sim e^{-\kappa_{a'} r}$   $\frac{1}{\kappa_{a'}} = a_{tr} = 1.2 \text{ fm}$

(many channels but weak)

play an important role in: energy dissipation (friction),  
Imaginary ( $iW$ ) and polarization ( $\Delta V$ ) potentials

$$\langle n \rangle = Np$$

$$E_{loss} = \Delta E \langle n \rangle$$





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# About transfer reactions

Transfer reactions are driven by **Optimum Q-value** condition. In the time-dependent picture the amplitude for a transfer is:

$$c_{\beta\alpha} = \frac{1}{i\hbar} \int_{-\infty}^{+\infty} dt \langle \psi_{\beta} | H_{int} | \psi_{\alpha} \rangle_t$$

and the probability becomes:

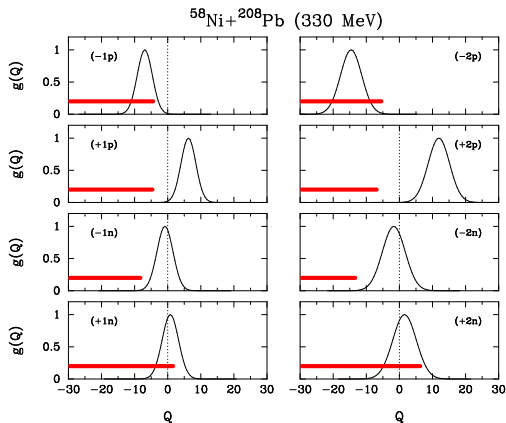
$$P_{\beta\alpha} = (\dots) |f_{\beta\alpha}(0, r_0)|^2 \exp\left(-\frac{(Q - Q_{opt})^2}{\hbar^2 \ddot{r}_0 \kappa_{a'_1}}\right)$$

- $\psi_{\alpha} = \psi_a(\xi_a)\psi_A(\xi_A)e^{i\delta_{aA}}$  is the channels wave function
- $\delta_{aA}$  the semi-classical phase
- $f_{\beta\alpha}(\vec{R}(t))$  the transfer form-factors
- $Q_{opt}$  the Q-optimun of the reactions



# About transfer reactions

The **optimum-Q value** amount to require that the entrance and exit trajectories must match smoothly.



# GRAZING (A. Winther)

GRAZING solves in the semiclassical approximation the system of coupled equations derived from the Hamiltonian:

$$\hat{H}_0 = \sum_i^{(a)} \epsilon_i a_i^\dagger a_i + \sum_{\lambda\mu}^{(a)} \hbar\omega_\lambda a_{\lambda\mu}^\dagger a_{\lambda\mu} + (A)$$

$$\hat{V}_{int}(t) = \hat{V}_{tr}(t) + \hat{V}_{in}(t) + \Delta U_{aA}(t)$$

$V_{int}$  contains the well known **form-factors** for **inelastic excitation** and for **one-particle transfer** (both protons and neutrons).



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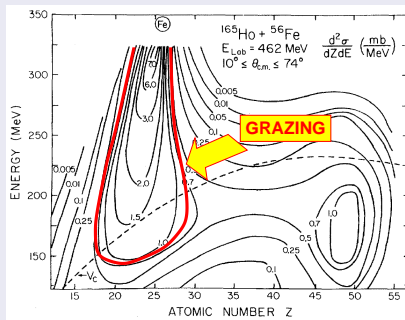
$V_{int}$  contains the well known **form-factors** for **inelastic excitation** and for **one-particle transfer** (both protons and neutrons).

The **time dependence** of the matrix elements is obtained by solving the Newtonian equations for the relative motion in the nuclear plus Coulomb field. For the nuclear potential we use the **Akyüz-Winther parametrization** that describes quite well elastic scattering data for several projectile and target combinations.



# What can be calculated (by GRAZING)

GRAZING calculates how the reaction cross section is shared among the different final mass partitions up to the ORBITING:

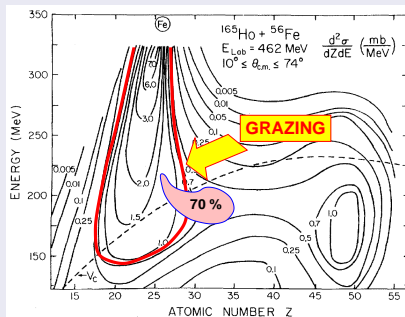


Beyond the ORBITING only the **capture probability** can be estimated.



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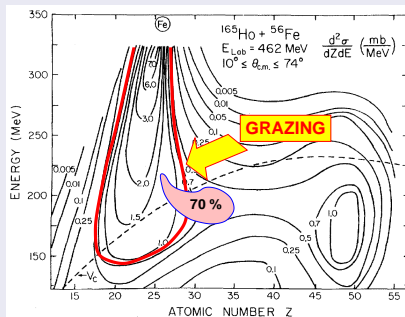


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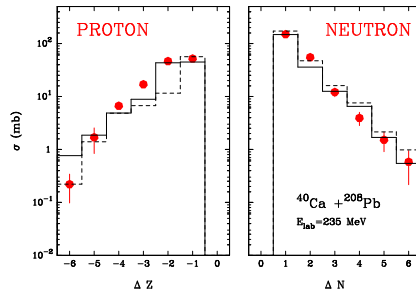
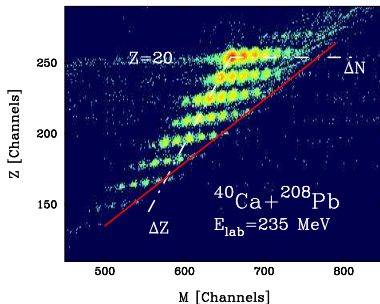


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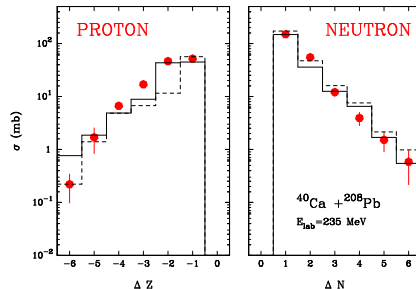
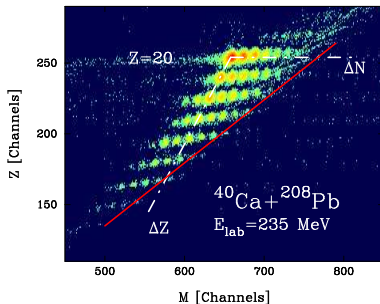




# Some Phenomenology of MNT



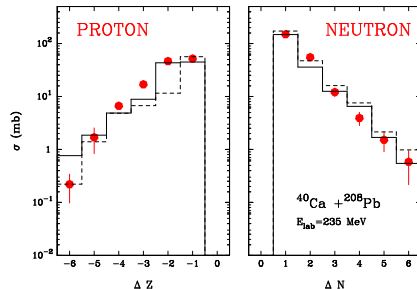
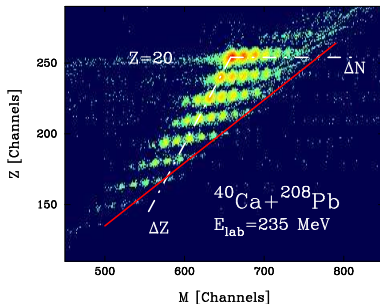
# Some Phenomenology of MNT



- The system does not reach charge equilibration. The population in the  $(N,Z)$  plane is dictated by the  $Q_{\text{opt}}$
- For each transferred neutron the cross section drops by a constant factor ( $\sim 3.5$ ) (**sequential transfer**)



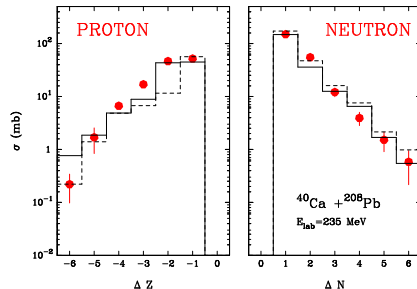
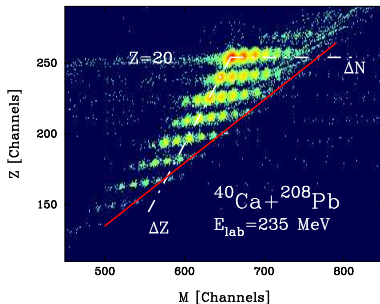
# Some Phenomenology of MNT



- The **ONE-neutron** transfer channel is much larger than the **ONE-proton** transfer channel
- The pure **TWO-proton** transfer is as large as the **ONE-proton** transfer (**pair-transfer mode ?**)



# Some Phenomenology of MNT



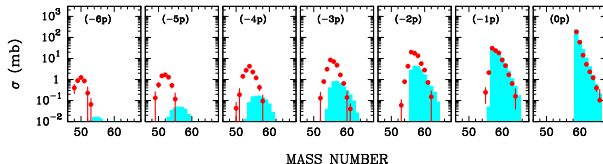
- EVAPORATION may strongly influence the isotopic distribution of the final fragments, these are indeed produced quite **HOT** (at high excitation energies)



# The $^{58}\text{Ni}+^{208}\text{Pb}$ reactions



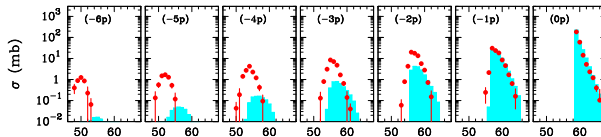
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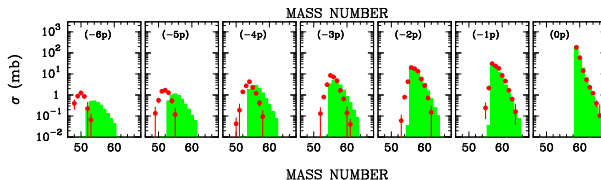
1pt



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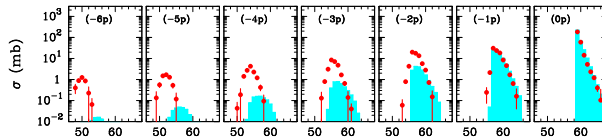
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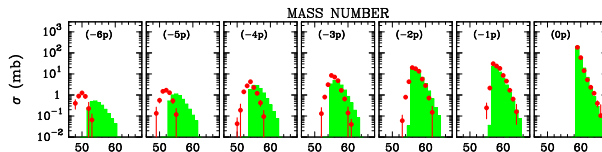
1pt+2pt



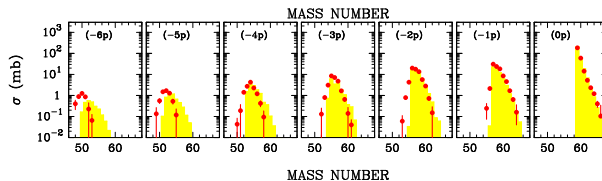
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1pt



1pt+2pt



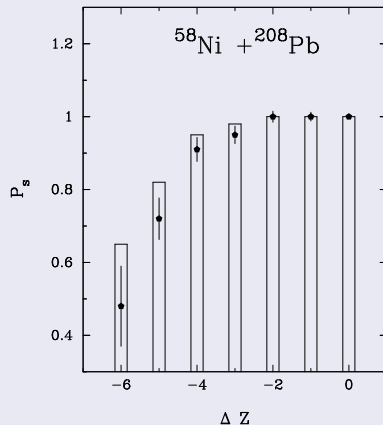
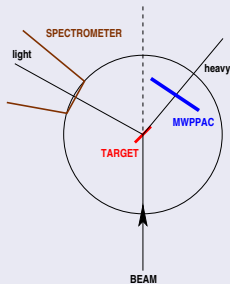
+Evap.





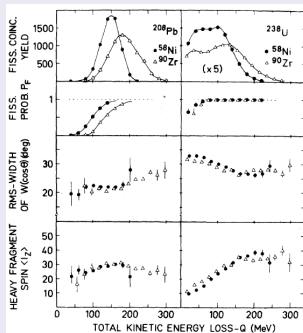
# The $^{58}\text{Ni} + ^{208}\text{Pb}$ reactions

For the population of the heavy fragments is important to consider FISSION.



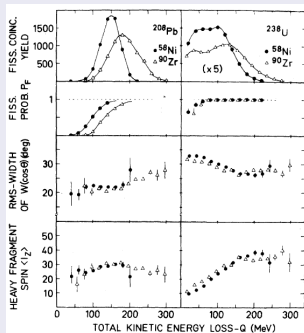
# Fission and Angular momentum loss in DIC

FISSION has been used to study angular momentum loss in DIC.

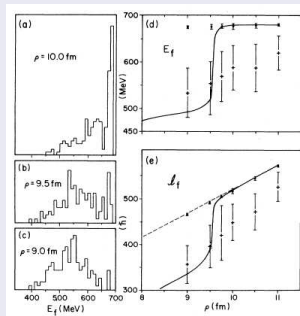


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The precursor (1978) of **GRAZING**. Importance of surface modes. (ZPM and large fluctuations)



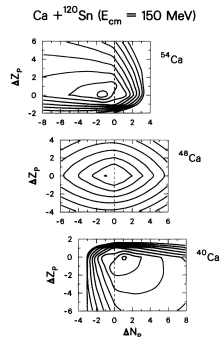
# Neutron Rich

What we have seen up to now concern stable nuclei. To populate **N-rich nuclei** besides:

- proton stripping (-1p)
- neutron pick-up (+1n)

we have to **OPEN** also the channels:

- proton pick-up (+1p)
- neutron stripping (-1n)



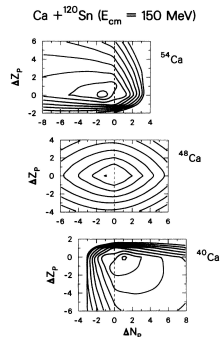
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## N-rich projectiles

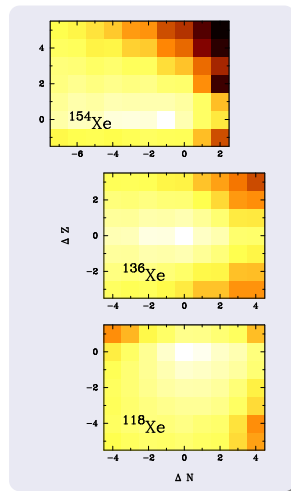


# The Xe + $^{208}\text{Pb}$ reaction at $E_{c.m.}=700$ MeV

The population of projectile-like fragments (corrected by evaporation of the light)

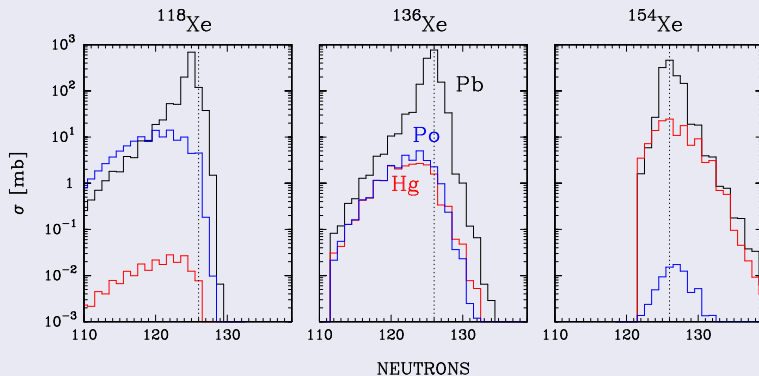
For **stable nuclei** the  $Q_{opt}(N, Z)$  is such that only:

- proton stripping (-1p)
  - neutron pick-up (+1n)
- are possible.

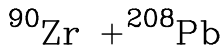


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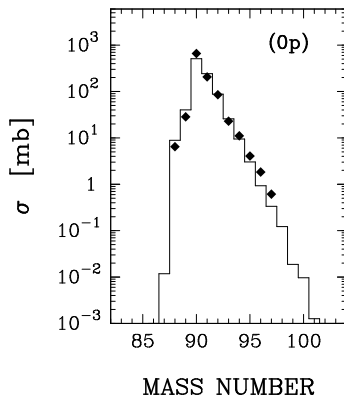
The population of the target-like fragments:



# The $^{90}\text{Zr} + ^{208}\text{Pb}$ system

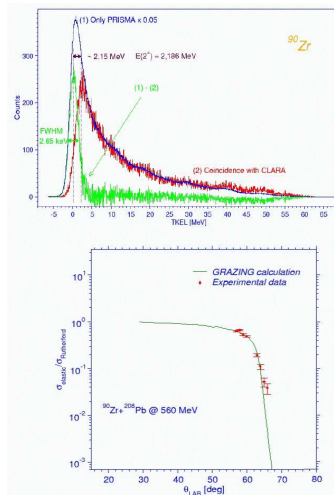
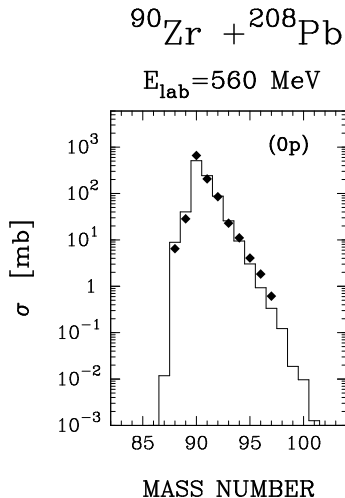


$$E_{\text{lab}} = 560 \text{ MeV}$$





# The $^{90}\text{Zr} + ^{208}\text{Pb}$ system



# References

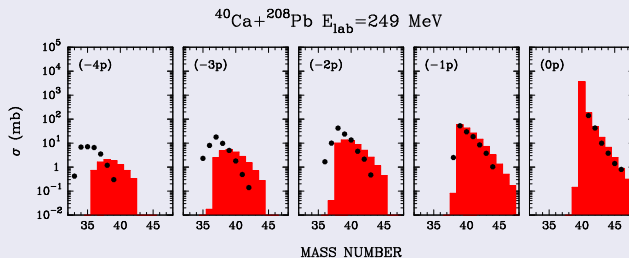
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# The $^{40}\text{Ca} + ^{208}\text{Pb}$ : Isotopic distribution



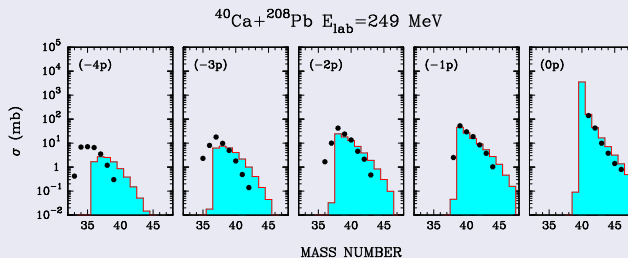
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1pt



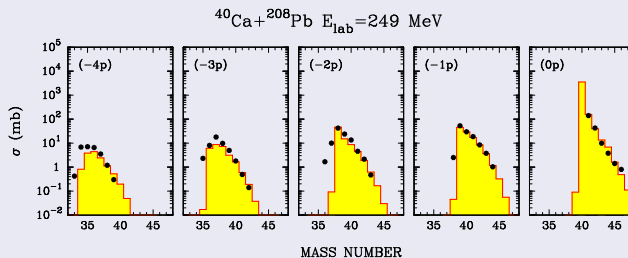
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1pt+2pt



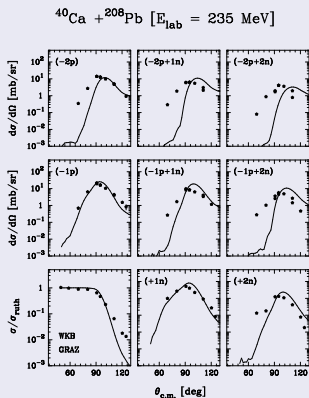
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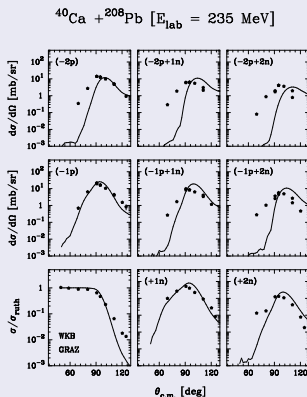
+Evap.



# The $^{40}\text{Ca} + ^{208}\text{Pb}$ : Angular distribution



# The $^{40}\text{Ca} + ^{208}\text{Pb}$ : Angular distribution



## Nuclear Potential

From Grazing we extract the **imaginary potential**  $iW_{tr}(r)$  to calculate with a quantal coupled-channels calculation elastic and inelastic scattering.

