# **% TRIUMF**

### Ab initio nuclear structure & reaction theory: Applications to nuclear astrophysics and tests of fundamental symmetries

Hirschegg 2023 -

Effective field theories for nuclei and nuclear matter

Darmstadter Haus, Hirschegg, Austria, 15-21 January 2023

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## NCSMC applications to capture reactions and β-delayed proton emission

- NCSMC extended to describe exotic <sup>11</sup>Be  $\beta$ p emission
- Radiative capture of deuterons on <sup>4</sup>He reaction responsible for the <sup>6</sup>Li in BBN
- Radiative capture of protons on <sup>7</sup>Be solar pp chain reaction, solar <sup>8</sup>B neutrinos
  - Evaluation with reduced theoretical uncertainties
- NCSMC calculations of <sup>8</sup>Be structure and <sup>7</sup>Li+p scattering and capture (in progress)
  - X17 anomaly

Ab initio calculation of the	$\beta$ decay from <sup>11</sup> Be to a <sup>10</sup> Be + <i>p</i> resonance
M. C. Atkinson <sup>©</sup> , <sup>1</sup> P. Navrátil	I, <sup>1</sup> G. Hupin, <sup>0</sup> , <sup>2</sup> K. Kravvaris, <sup>3</sup> and S. Quaglioni <sup>3</sup>
PHYSICAL R	REVIEW LETTERS 129, 042503 (2022)

Ab initio prediction for the radiative capture of protons on <sup>7</sup>Be

K. Kravvaris,<sup>1</sup> P. Navrátil,<sup>2</sup> S. Quaglioni,<sup>1</sup> C. Hebborn,<sup>3,1</sup> and G. Hupin<sup>4</sup>

arXiv: 2202.11759

## **NCSM(C)** applications to tests of fundamental symmetries

- Ab initio calculations of nuclear electric dipole moments (EDMs) and anapole moments in light nuclei
- Ab initio calculations of <sup>6</sup>He β-decay electron spectrum including nuclear structure and recoil corrections
- Ongoing calculations of nuclear structure corrections  $\delta_c$  and  $\delta_{NS}$  for the extraction of the  $V_{ud}$  matrix element from the superallowed Fermi transitions (current focus on  ${}^{10}C \rightarrow {}^{10}B$ )

PHYSICAL REVIEW C 104, 025502 (2021)	PHYSICAL REVIEW A 102, 052828 (2020)
Ab initio calculations of electric dipole moments of light nuclei Paul Froese" TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia V6T 2A3, Canada and Department of Physics and Astronomy, University of British Columbia, Vancouver, British Columbia V6T 1Z1, Canada Petr Navrátil © <sup>†</sup> TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia V6T 2A3, Canada Physics Letters B 822 (2022) 137259	Editors' Suggestion Nuclear spin-dependent parity-violating effects in light polyatomic molecules Yongliang Hao <sup>(a)</sup> , <sup>1</sup> Petr Navrátil <sup>(a)</sup> , <sup>2</sup> Eric B. Norrgard <sup>(a)</sup> , <sup>3</sup> Miroslav Iliaš <sup>(a)</sup> , <sup>4</sup> Ephraim Eliav, <sup>5</sup> Rob G. E. Timmermans <sup>(a)</sup> , <sup>1</sup> Victor V. Flambaum <sup>(a)</sup> , <sup>6</sup> and Anastasia Borschevsky <sup>(a)</sup> , <sup>*</sup>
Contents lists available at ScienceDirect Physics Letters B www.elsevier.com/locate/physletb	Calculations performed within the no-core shell model (NCSM); $\delta_C$ within NCSM with continuum (NCSMC)
Nuclear <i>ab initio</i> calculations of <sup>6</sup> He $\beta$ -decay for beyond the Standard Model studies Ayala Glick-Magid <sup>a</sup> , Christian Forssén <sup>b,*</sup> , Daniel Gazda <sup>c</sup> , Doron Gazit <sup>a,*</sup> , Peter Gysbers <sup>d,e</sup> , Petr Navrátil <sup>d</sup>	

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## **NCSMC** applications to uncertainty quantifications in n-<sup>4</sup>He scattering

- Study how the 3N LECs contribute to the overall uncertainty budget of many-body calculations of neutron - <sup>4</sup>He elastic scattering
  - Constructed a Gaussian process model that acts as a statistical emulator for the theory



Quantifying uncertainties in neutron-α scattering with chiral nucleon-nucleon and three-nucleon forces

Konstantinos Kravvaris<sup>0</sup>,<sup>1,\*</sup> Kevin R. Quinlan,<sup>1,†</sup> Sofia Quaglioni,<sup>1</sup> Kyle A. Wendt,<sup>1</sup> and Petr Navrátil<sup>02</sup>

#### First principles or ab initio nuclear theory



#### Ab Initio Calculations of Structure, Scattering, Reactions Unified approach to bound & continuum states

No-Core Shell Model with Continuum (NCSMC)

$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} \left| {}^{(A)} \mathfrak{B}, \lambda \right\rangle + \sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} \left| \mathfrak{B}_{(A-a)}^{\vec{r}} \mathfrak{B}_{(a)}, \nu \right\rangle$$

S. Baroni, P. Navratil, and S. Quaglioni, PRL **110**, 022505 (2013); PRC **87**, 034326 (2013).

# Ab Initio Calculations of Structure, Scattering, Reactions

Unified approach to bound & continuum states

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$$N = N_{\max} + 1 \stackrel{\vec{h}\Omega}{\longrightarrow}_{N=1} (A) \stackrel{\vec{h}\Omega}{\longrightarrow}_{N=0} (A) \stackrel{\vec{h}\Omega}{\longrightarrow}_{N=0} (A) \stackrel{\vec{h}\Omega}{\longrightarrow}_{N=1} (A) \stackrel{\vec{h}\Omega}{\longrightarrow}_{N=0} (A) \stackrel{\vec{h}\Omega}$$

Static solutions for aggregate system, describe all nucleons close together

# Ab Initio Calculations of Structure, Scattering, Reactions

Unified approach to bound & continuum states

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Unified approach to bound & continuum states

No-Core Shell Model with Continuum (NCSMC)



Static solutions for aggregate system, describe all nucleons close together

## **Coupled NCSMC equations**

$$H \Psi^{(A)} = E \Psi^{(A)} \qquad \Psi^{(A)} = \sum_{\lambda} c_{\lambda} | {}^{(A)} \mathfrak{D}_{\lambda} , \lambda \rangle + \sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} | \mathfrak{D}_{\lambda} | \mathfrak{D}_{\lambda} , \nu \rangle$$

$$E_{\lambda}^{NCSM} \delta_{\lambda\lambda'} \qquad \begin{pmatrix} \langle A \mathfrak{D}_{\lambda} \mid H \hat{A}_{\nu} \mid \mathfrak{D}_{\lambda} \\ \mathfrak{D}_{\lambda} \rangle = E \begin{pmatrix} \delta_{\lambda\lambda'} \mid \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \\ \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \rangle \\ \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \rangle \\ \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \rangle \\ \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \rangle \\ \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_{\lambda'} \rangle \\ \mathfrak{D}_{\lambda'} \mid \mathfrak{D}_$$

Physica Scripta doi:10.1088/0031-8949/91/5/053002

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d ab initio approaches to nuclear structure and reactions

Petr Navrátil<sup>1</sup>, Sofia Quaglioni<sup>2</sup>, Guillaume Hupin<sup>3,4</sup>, Carolina Romero-Redondo<sup>2</sup> and Angelo Calci<sup>1</sup>

Novel chiral Hamiltonian and observables in light and medium-mass nuclei

V. Somà,<sup>1,\*</sup> P. Navrátil<sup>®</sup>,<sup>2,†</sup> F. Raimondi,<sup>3,4,‡</sup> C. Barbieri<sup>®</sup>,<sup>4,§</sup> and T. Duguet<sup>1,5,∥</sup>

#### Input for NCSMC calculations: Nuclear forces from chiral Effective Field Theory

- Quite reasonable description of binding energies across the nuclear charts becomes feasible
  - The Hamiltonian fully determined in A=2 and A=3,4 systems
    - Nucleon–nucleon scattering, deuteron properties, <sup>3</sup>H and <sup>4</sup>He binding energy, <sup>3</sup>H half life
  - Light nuclei NCSM
  - Medium mass nuclei Self-Consistent Green's Function method

NN N<sup>3</sup>LO (Entem-Machleidt 2003) 3N N<sup>2</sup>LO w local/non-local regulator



PHYSICAL	REVIEW	C 101,	, 014318	(2020)
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  - Light nuclei NCSM
  - Heavy nuclei HF-MBPT(3)





NN N<sup>3</sup>LO (Entem-Machleidt 2003) 3N N<sup>2</sup>LO w local/non-local regulator

## $\beta$ -delayed proton emission in <sup>11</sup>Be

14





<sup>11</sup>Be( $\beta$ p), a quasi-free neutron decay?

K. Riisager<sup>a,\*</sup>, O. Forstner<sup>b,c</sup>, M.J.G. Borge<sup>d,e</sup>, J.A. Briz<sup>e</sup>, M. Carmona-Gallardo<sup>e</sup>, L.M. Fraile<sup>f</sup>, H.O.U. Fynbo<sup>a</sup>, T. Giles<sup>g</sup>, A. Gottberg<sup>e,g</sup>, A. Heinz<sup>h</sup>, J.G. Johansen<sup>a,1</sup>, B. Jonson<sup>h</sup>, J. Kurcewicz<sup>d</sup>, M.V. Lund<sup>a</sup>, T. Nilsson<sup>h</sup>, G. Nyman<sup>h</sup>, E. Rapisarda<sup>d</sup>, P. Steier<sup>b</sup>, O. Tengblad<sup>e</sup>, R. Thies<sup>h</sup>, S.R. Winkler<sup>b</sup>

- Indirectly observed  ${}^{11}\text{Be}(\beta p){}^{10}\text{Be}$
- Measured an extremely high branching ratio  $b_p = 8.3 \pm 0.9 \times 10^{-6}$ 
  - Orders of magnitude larger than theoretical predictions (e.g.  $3.0 \times 10^{-8}$ )
- Two proposed explanations:

D. Baye and E.M. Tursunov, PLB 696, 4, 464-467 (2011)

- The neutron decays to an unobserved  $p+^{10}Be$  resonance in <sup>11</sup>B
- 2 There are unobserved dark decay modes

#### β-delayed proton emission in <sup>11</sup>Be

PHYSICAL REVIEW LETTERS 123, 082501 (2019)

**Editors' Suggestion** 

#### Direct Observation of Proton Emission in <sup>11</sup>Be

Y. Ayyad,<sup>1,2,\*</sup> B. Olaizola,<sup>3</sup> W. Mittig,<sup>2,4</sup> G. Potel,<sup>1</sup> V. Zelevinsky,<sup>1,2,4</sup> M. Horoi,<sup>5</sup> S. Beceiro-Novo,<sup>4</sup> M. Alcorta,<sup>3</sup>
C. Andreoiu,<sup>6</sup> T. Ahn,<sup>7</sup> M. Anholm,<sup>3,8</sup> L. Atar,<sup>9</sup> A. Babu,<sup>3</sup> D. Bazin,<sup>2,4</sup> N. Bernier,<sup>3,10</sup> S. S. Bhattacharjee,<sup>3</sup> M. Bowry,<sup>3</sup>
R. Caballero-Folch,<sup>3</sup> M. Cortesi,<sup>2</sup> C. Dalitz,<sup>11</sup> E. Dunling,<sup>3,12</sup> A. B. Garnsworthy,<sup>3</sup> M. Holl,<sup>3,13</sup> B. Kootte,<sup>3,8</sup>
K. G. Leach,<sup>14</sup> J. S. Randhawa,<sup>2</sup> Y. Saito,<sup>3,10</sup> C. Santamaria,<sup>15</sup> P. Šiurytė,<sup>3,16</sup> C. E. Svensson,<sup>9</sup>
R. Umashankar,<sup>3</sup> N. Watwood,<sup>2</sup> and D. Yates<sup>3,10</sup>

- Directly observed the protons from  ${}^{11}\text{Be}(\beta p){}^{10}\text{Be}$
- Measured consistent branching ratio  $b_p = 1.3(3) \times 10^{-5}$ 
  - Still orders of magnitude larger than theoretical predictions
- Predict the proton resonance at 11.425(20) MeV from the proton energy distribution
  - Predicted to be either  $\frac{1}{2}^+$  or  $\frac{3}{2}^+$
  - Corresponds to excitation energy of 197 keV

#### NCSMC extended to describe exotic <sup>11</sup>Be $\beta$ p emission, supports large branching ratio due to narrow $\frac{1}{2}$ resonance

<sup>11</sup>Be  $\rightarrow$  (<sup>10</sup>Be+p) +  $\beta^-$  +  $\bar{\nu}_e$  GT transition



#### NCSMC extended to describe exotic <sup>11</sup>Be $\beta$ p emission, supports large branching ratio due to narrow $\frac{1}{2}$ resonance



# NCSMC extended to describe exotic <sup>11</sup>Be $\beta$ p emission, supports large branching ratio due to narrow <sup>1</sup>/<sub>2</sub>+ resonance



#### **Radiative capture of deuterons on** <sup>4</sup>**He**

- Reaction  ${}^{4}\text{He}(d,\gamma){}^{6}\text{Li}$  responsible for  ${}^{6}\text{Li}$  production in BBN
- Three orders of magnitude discrepancy between BBN predictions and observations
  - Problem with astronomical observations?
  - Problem with our understanding of the reaction rate?
  - New physics?



Radiative capture of deuterons on <sup>4</sup>He

NCSMC calculations with chiral NN+3N interaction



#### Structure of <sup>6</sup>Li

#### Ab Initio Prediction of the ${}^{4}\text{He}(d,\gamma){}^{6}\text{Li}$ Big Bang Radiative Capture

C. Hebborn<sup>(0)</sup>,<sup>1,2,\*</sup> G. Hupin<sup>(0)</sup>,<sup>3</sup> K. Kravvaris<sup>(0)</sup>,<sup>2</sup> S. Quaglioni<sup>(0)</sup>,<sup>2</sup> P. Navrátil<sup>(0)</sup>,<sup>4</sup> and P. Gysbers<sup>(0)</sup>,<sup>5</sup>

#### Ground state properties: Energy Asymptotic normalization constants Magnetic moment

	NN-only	$3 \mathrm{N}_\mathrm{loc}$	$3N_{loc}$ -pheno	Exp. or Eval.
$E_{g.s.}$	-1.848	-1.778	-1.474	-1.4743
$\mathcal{C}_0$	2.95	2.89	2.62(4)	2.28(7) 2.29(12)
$\mathcal{C}_2$	-0.0369	-0.0642	-0.0554(305)	-0.077(18)
$\mathcal{C}_2/\mathcal{C}_0$	-0.013	-0.022	-0.021(11)	-0.025(6)(10)
$\mu$	0.85	0.84	0.84(1)	0.8220473(6)

## <sup>4</sup>He+*d* threshold

#### **Radiative capture of deuterons on <sup>4</sup>He**

NCSMC calculations with chiral NN+3N interaction



#### Structure of <sup>6</sup>Li

Elastic scattering  ${}^{4}\text{He}(d,d){}^{4}\text{He}$  cross section at the deuteron back scattered angle 164°



Ab Initio Prediction of the  ${}^{4}\text{He}(d,\gamma){}^{6}\text{Li}$  Big Bang Radiative Capture

C. Hebborn<sup>0</sup>,<sup>1,2,\*</sup> G. Hupin<sup>0</sup>,<sup>3</sup> K. Kravvaris<sup>0</sup>,<sup>2</sup> S. Quaglioni<sup>0</sup>,<sup>2</sup> P. Navrátil<sup>0</sup>,<sup>4</sup> and P. Gysbers<sup>0<sup>4,5</sup></sup>

#### **Radiative capture of deuterons on** <sup>4</sup>**He**

NCSMC calculations with chiral NN+3N interaction

Capture S-factor

Dominated by E2 M1 significant at low energy E1 negligible – isospin supressed (T=0  $\rightarrow$  T=0)





Low energy S-factor consistent with LUNA data, below the <sup>6</sup>Li Coulomb breakup data

Ab Initio Prediction of the  ${}^{4}\text{He}(d,\gamma){}^{6}\text{Li}$  Big Bang Radiative Capture

C. Hebborn<sup>1,2,\*</sup> G. Hupin<sup>0,3</sup> K. Kravvaris<sup>0,2</sup> S. Quaglioni<sup>0,2</sup> P. Navrátil<sup>0,4</sup> and P. Gysbers<sup>04,5</sup>

#### **Radiative capture of deuterons on <sup>4</sup>He**

- NCSMC calculations with chiral NN+3N interaction
  - Thermonuclear reaction rate



Thermonuclear reaction rate smaller than NACRE II evaluation, agreement with LUNA result with less uncertainty

Ab initio prediction for the radiative capture of protons on <sup>7</sup>Be

K. Kravvaris,<sup>1</sup> P. Navrátil,<sup>2</sup> S. Quaglioni,<sup>1</sup> C. Hebborn,<sup>3,1</sup> and G. Hupin<sup>4</sup>

arXiv: 2202.11759

#### **Radiative capture of protons on 7Be**

- Solar pp chain reaction, solar <sup>8</sup>B neutrinos
- NCSMC calculations with a set of chiral NN+3N interactions as input
- Example of <sup>8</sup>B structure results



#### **Radiative capture of protons on 7Be**

NCSMC S-factor results



E1 non-resonant, M1/E2 at 1<sup>+</sup> and 3<sup>+</sup> resonances

	$C_{p_{1/2}}$	$C_{p_{3/2}}$	$a_1$	$a_2$	$S_{17}(0)$
$N^2LO+3N_{lnl}$	0.384	0.691	4.4(1)	-0.5(1)	23.9
$N^{3}LO + 3N_{lnl}$	0.390	0.678	1.3(1)	-4.7(1)	23.5
${ m N}^4{ m LO}{+}3{ m N}_{ m lnl}$	0.354	0.669	1.6(1)	-4.4(1)	22.0
$N^4LO+3N^*_{lnl}$	0.343	0.621	1.3(1)	-5.0(1)	19.3
$\rm N^3LO^*{+}3N_{\rm lnl}$	0.334	0.663	0.1(1)	-7.7(1)	21.1
$N^3LO^*{+}3N_{\rm loc}$	0.308	0.584	2.5(1)	-3.6(2)	16.8
Ref. [41]	0.315(9)	0.66(2)	$17.34^{+1.11}_{-1.33}$	$-3.18^{+0.55}_{-0.50}$	



Ab initio prediction for the radiative capture of protons on <sup>7</sup>Be K. Kravvaris,<sup>1</sup> P. Navrátil,<sup>2</sup> S. Quaglioni,<sup>1</sup> C. Hebborn,<sup>3,1</sup> and G. Hupin<sup>4</sup> arXiv: 2202.11759

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NCSMC S-factor results



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#### **Radiative capture of protons on 7Be**

NCSMC S-factor results



Recommended value  $S_{17}(0) \sim 19.8(3) \text{ eV b}$ 

Latest evaluation in *Rev. Mod. Phys.* **83**,195–245 (2011):  $S_{17}(0) = 20.8 \pm 0.7(expt) \pm 1.4(theory) eV b$ 

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#### X17 Anomaly



Feng PRD 95, 035017 (2017)

"An anomaly in the internal pair creation on the M1 transition depopulating the 18.15 MeV isoscalar  $1^+$  state on  ${}^8\text{Be}$  was observed. This could be explained by the creation and subsequent decay of a new boson .. mass 17.01(16) MeV"



Fig. from PLB 813, 136061 (2021)

#### **NCSMC** calculations of <sup>8</sup>Be structure and <sup>7</sup>Li+p scattering and capture

Wave function ansatz

$$\Psi_{\mathsf{NCSMC}}^{(8)} = \sum_{\lambda} c_{\lambda} \left| {}^{8}\mathrm{Be}, \lambda \right\rangle + \sum_{\nu} \int \mathrm{d}r \gamma_{\nu}(r) \hat{A}_{\nu} \left| {}^{7}\mathrm{Li} + p, \nu \right\rangle + \sum_{\mu} \int \mathrm{d}r \gamma_{\mu}(r) \hat{A}_{\mu} \left| {}^{7}\mathrm{Be} + n, \mu \right\rangle$$

- 3/2<sup>-</sup>, 1/2<sup>-</sup>, 7/2<sup>-</sup>, 5/2<sup>-</sup>, 5/2<sup>-</sup> <sup>7</sup>Li and <sup>7</sup>Be states in cluster basis
- 15 positive and 15 negative parity states in <sup>8</sup>Be composite state basis



In collaboration with UBC/TRIUMF PhD student Peter Gysbers

TUNL Nuclear Data Evaluation Project

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- 3/2<sup>-</sup>, 1/2<sup>-</sup>, 7/2<sup>-</sup>, 5/2<sup>-</sup>, 5/2<sup>-</sup> <sup>7</sup>Li and <sup>7</sup>Be states in cluster basis
- 15 positive and 15 negative parity states in <sup>8</sup>Be composite state basis

In collaboration with UBC/TRIUMF PhD student Peter Gysbers



#### <sup>8</sup>Be structure

Calculated <sup>8</sup>Be bound states w.r.t. <sup>7</sup>Li + p threshold ( $N_{max} = 8/9$ )

State	Energy [MeV]		Excitation Energy [MeV	
	NCSMC	Expt.	NCSMC	Expt.
$0^+$	-16.13	-17.25	0.00	0.00
$2^+$	-12.72	-14.23	3.41	3.03
$4^+$	-4.31	-5.91	11.82	11.35
$2^+$	-0.10	-0.63	16.03	16.63
$2^+$	+0.31	-0.33	16.44	16.92

Matches experiment well, except the 3rd  $2^+$  is slightly above the  $^{7}\text{Li} + p$  threshold.





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#### <sup>8</sup>Be structure – calculated positive-parity eigenphase shifts



- Motivated by ATOMKI experiments (Firak, Krasznahorkay et al., EPJ Web of Conferences 232, 04005 (2020))
- No-core shell model with continuum (NCSMC) with wave function ansatz

$$\Psi_{\mathsf{NCSMC}}^{(8)} = \sum_{\lambda} c_{\lambda} \left| {}^{8}\mathrm{Be}, \lambda \right\rangle + \sum_{\nu} \int \mathrm{d}r \gamma_{\nu}(r) \hat{A}_{\nu} \left| {}^{7}\mathrm{Li} + p, \nu \right\rangle + \sum_{\mu} \int \mathrm{d}r \gamma_{\mu}(r) \hat{A}_{\mu} \left| {}^{7}\mathrm{Be} + n, \mu \right\rangle$$



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Data: Zahnow *et al.* Z.Phys.A **351** 229-236 (1995) Latest developments (arXiv: 2205.07744): Anomaly in E1 direct capture – X17 a vector boson



... more calculations to do

## Why investigate the EDM and the anapole moment?

- The EDM is a promising probe for CP violation beyond the standard model as well as CP violating QCD  $\bar{\theta}$  parameter
- Nuclear structure can enhance the EDM
- Nuclear EDMs can be measured in storage rings (CERN feasibility study: arXiv:1912.07881)
- Parity violation in atomic and molecular systems sensitive to a variety of "new physics"
  - Probes electron-quark electroweak interaction
  - Best limits on the Z' boson parity violating interaction with electrons and nucleons

#### Nuclear spin dependent parity violating effects in light polyatomic molecules

- Experiments proposed for <sup>9</sup>BeNC, <sup>25</sup>MgNC
- To extract the underlying physics, atomic, molecular and nuclear structure effects must be understood
  - Ab initio calculations

- Spin dependent PV
  - Z-boson exchange between nucleon axialvector and electron-vector currents (b)
  - Electromagnetic interaction of atomic electrons with the nuclear anapole moment (c)



#### Parity violating nucleon-nucleon interaction

- Meson exchange approach
- Chiral EFT
- Unknown parameters (LECs)
  - DDH (1980) estimates based on the quark model

43 JOHN F. DONOGHUE<sup>†</sup> Center for Theoretical Physics, Laboratory for Nuclear Science and Physics Department, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139 AND BARRY R. HOLSTEIN Physics Division, National Science Foundation, Washington, D. C. 20550  $V_{12}^{\mathbf{p.v.}} = rac{f_{\pi}g_{\pi NN}}{21/2} i\left(rac{ec{ au}_1 imes ec{ au}_2}{2}
ight)^z (ec{\sigma}_1 + ec{\sigma}_2) \cdot \left[rac{ec{p}_1 - ec{p}_2}{2M}, f_{\pi}(r)
ight]$  $-g_{\rho}\left(h_{\rho}^{0}\vec{\tau}_{1}\cdot\vec{\tau}_{2}+h_{\rho}^{1}\left(\frac{\vec{\tau}_{1}+\vec{\tau}_{2}}{2}\right)^{z}+h_{\rho}^{2}\frac{\left(3\tau_{1}^{z}\tau_{2}^{z}-\vec{\tau}_{1}\cdot\vec{\tau}_{2}\right)}{2(6)^{1/2}}\right)$  $\times \left( (\vec{\sigma}_1 - \vec{\sigma}_2) \cdot \left\{ \frac{\vec{p}_1 - \vec{p}_2}{2M}, f_{\rho}(r) \right\} + i(1 + \chi_v) \, \vec{\sigma}_1 \times \vec{\sigma}_2 \cdot \left[ \frac{\vec{p}_1 - \vec{p}_2}{2M}, f_{\rho}(r) \right]$  $-g_{\omega}\left(h_{\omega}^{0}+h_{\omega}^{1}\left(\frac{\dot{\tau}_{1}+\dot{\tau}_{2}}{2}\right)^{z}\right)$  $\times \left(\left(ec{\sigma}_1-ec{\sigma}_2
ight)\cdot\left\{rac{ec{p}_1-ec{p}_2}{2M},f_\omega(r)
ight\}+i(1+\chi_S)\,ec{\sigma}_1 imesec{\sigma}_2\cdot\left[rac{ec{p}_1-ec{p}_2}{2M},f_\omega(r)
ight]
ight\}$  $-(g_{\omega}h_{\omega}^{1}-g_{\rho}h_{\rho}^{1})\left(\frac{\dot{\tau}_{1}-\dot{\tau}_{2}}{2}\right)^{z}(\dot{\sigma}_{1}+\dot{\sigma}_{2})\cdot\left\{\frac{\ddot{p}_{1}-\ddot{p}_{2}}{2M},f_{\rho}(r)\right\}$  $-g_{\rho}h_{\rho}^{\prime 1}i\left(\frac{\dot{\tau}_{1}\times\dot{\tau}_{2}}{2}\right)^{z}(\dot{\sigma}_{1}+\dot{\sigma}_{2})\cdot\left[\frac{\ddot{p}_{1}-\dot{p}_{2}}{2M},f_{\rho}(r)\right],$ 

$$f_{\pi}(\mathbf{r}) = \frac{e^{-m_{\pi}r}}{4\pi r},$$
$$f_{\rho}(\mathbf{r}) = f_{\omega}(\mathbf{r}) = \frac{e^{-m_{\rho}r}}{4\pi r}.$$

ANNALS OF PHYSICS 124, 449-495 (1980)

Unified Treatment of the Parity Violating Nuclear Force

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I. Novikov,<sup>11</sup> S. Penttila,<sup>3</sup> E. M. Scott,<sup>5</sup> J. Watts,<sup>9</sup> and C. Wickersham<sup>9</sup>

 $V_{12}^{p.v.}$ 

#### Parity violating nucleon-nucleon interaction

A. Salas-Bacci,<sup>3</sup> S. Santra,<sup>24</sup> S. Schröder,<sup>3,25</sup> E. Scott,<sup>5</sup> P.-N. Seo,<sup>3,26</sup> E. I. Sharapov,<sup>27</sup> F. Simmons,<sup>13</sup> W. M. Snow,<sup>4</sup> A. Sprow,<sup>13</sup> J. Stewart,<sup>15</sup> E. Tang,<sup>136</sup> Z. Tang,<sup>46</sup> X. Tong,<sup>7</sup> D. J. Turkoglu,<sup>28</sup> R. Whitehead,<sup>5</sup> and W. S. Wilburn<sup>6</sup> (NPDGamma Collaboration)

- Meson exchange approach
- Chiral EFT
- Unknown parameters (LECs)
  - DDH (1980) estimates based on the quark model
  - Two recent precision experiments constraining the parameters



$$= \frac{f_{\pi}g_{\pi NN}}{2^{1/2}} i\left(\frac{\dot{\tau}_{1} \times \dot{\tau}_{2}}{2}\right)^{z} (\dot{\sigma}_{1} + \dot{\sigma}_{2}) \cdot \left[\frac{\ddot{p}_{1} - \ddot{p}_{2}}{2M}, f_{\pi}(r)\right] \\ - g_{\rho}\left(h_{\rho}^{0}\dot{\tau}_{1} \cdot \dot{\tau}_{2} + h_{\rho}^{1}\left(\frac{\dot{\tau}_{1} + \dot{\tau}_{2}}{2}\right)^{z} + h_{\rho}^{2}\frac{(3\tau_{1}^{z}\tau_{2}^{z} - \dot{\tau}_{1} \cdot \dot{\tau}_{2})}{2(6)^{1/2}}\right) \\ \times \left((\dot{\sigma}_{1} - \dot{\sigma}_{2}) \cdot \left\{\frac{\ddot{p}_{1} - \ddot{p}_{2}}{2M}, f_{\rho}(r)\right\} + i(1 + \chi_{v}) \dot{\sigma}_{1} \times \dot{\sigma}_{2} \cdot \left[\frac{\ddot{p}_{1} - \ddot{p}_{2}}{2M}, f_{\rho}(r)\right] \\ - g_{\omega}\left(h_{\omega}^{0} + h_{\omega}^{1}\left(\frac{\dot{\tau}_{1} + \dot{\tau}_{2}}{2}\right)^{z}\right) \\ \times \left((\dot{\sigma}_{1} - \dot{\sigma}_{2}) \cdot \left\{\frac{\ddot{p}_{1} - \ddot{p}_{2}}{2M}, f_{\omega}(r)\right\} + i(1 + \chi_{S}) \dot{\sigma}_{1} \times \dot{\sigma}_{2} \cdot \left[\frac{\ddot{p}_{1} - \ddot{p}_{2}}{2M}, f_{\omega}(r)\right] \\ - \left(g_{\omega}h_{\omega}^{1} - g_{\rho}h_{\rho}^{1}\right)\left(\frac{\dot{\tau}_{1} - \dot{\tau}_{2}}{2}\right)^{z} (\dot{\sigma}_{1} + \dot{\sigma}_{2}) \cdot \left\{\frac{\ddot{p}_{1} - \ddot{p}_{2}}{2M}, f_{\rho}(r)\right\} \\ - g_{\rho}h_{\rho}^{\prime 1}i\left(\frac{\dot{\tau}_{1} \times \dot{\tau}_{2}}{2}\right)^{z} (\dot{\sigma}_{1} + \dot{\sigma}_{2}) \cdot \left[\frac{\ddot{p}_{1} - \ddot{p}_{2}}{2M}, f_{\rho}(r)\right],$$

$$f_{\pi}(\mathbf{r}) = \frac{e^{-m_{\pi}r}}{4\pi r},$$
  
$$f_{\rho}(\mathbf{r}) = f_{\omega}(\mathbf{r}) = \frac{e^{-m_{\rho}r}}{4\pi r}.$$

 $f_{\pi} \equiv h_{\pi}^1$ 

 $h_{\rho-\omega} \equiv h_{\omega}^1 + 0.46h_{\rho}^1 - 0.46h_{\omega}^0 - 0.76h_{\rho}^0 - 0.02h_{\rho}^2$ 

#### Parity and time-reversal violating nucleon-nucleon interaction

Introduced through Hamiltonian H<sub>PVTV</sub> :

$$H_{PVTV}(\mathbf{r}) = \frac{1}{2m_n} \boldsymbol{\sigma}_- \cdot \boldsymbol{\nabla} \left( -\bar{G}^0_{\omega} y_{\omega}(r) \right) + \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2 \boldsymbol{\sigma}_- \cdot \boldsymbol{\nabla} \left( \bar{G}^0_{\pi} y_{\pi}(r) - \bar{G}^0_{\rho} y_{\rho}(r) \right) + \frac{\tau_+^2}{2} \boldsymbol{\sigma}_- \cdot \boldsymbol{\nabla} \left( \bar{G}^1_{\pi} y_{\pi}(r) - \bar{G}^1_{\rho} y_{\rho}(r) - \bar{G}^1_{\omega} y_{\omega}(r) \right) + \frac{\tau_-^2}{2} \boldsymbol{\sigma}_+ \cdot \boldsymbol{\nabla} \left( \bar{G}^1_{\pi} y_{\pi}(r) + \bar{G}^1_{\rho} y_{\rho}(r) - \bar{G}^1_{\omega} y_{\omega}(r) \right) + (3\tau_1^z \tau_2^z - \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2) \boldsymbol{\sigma}_- \cdot \boldsymbol{\nabla} \left( \bar{G}^2_{\pi} y_{\pi}(r) - \bar{G}^2_{\rho} y_{\rho}(r) \right)$$

Based on one meson exchange model  $\sigma_{\pm} = \sigma_1 \pm \sigma_2$  $y_x(r) = e^{-m_x r} / (4\pi r)$ •  $\tau_{\pm}^z = \tau_1^z \pm \tau_2^z$ 

#### Parity and time-reversal violating nucleon-nucleon interaction

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 $\sigma_{\pm} = \sigma_1 \pm \sigma_2$ 

 $\tau_{\pm}^z = \tau_1^z \pm \tau_2^z$ 

- Based on one meson exchange model
- $y_x(r) = e^{-m_x r} / (4\pi r)$
- Coupling constants

Parity and time-reversal violating nucleon-nucleon interaction and nuclear EDM

H<sub>PVTV</sub> introduces parity admixture in the ground state (perturbation theory):

 $|0\rangle \longrightarrow |0\rangle + |\tilde{0}\rangle$  $|\tilde{0}\rangle = \sum_{n \neq 0} \frac{1}{E_0 - E_n} |n\rangle \langle n|H_{PVTV}|0\rangle$ 

Nuclear EDM is dominated by polarization contribution:

$$D^{(pol)} = \langle 0 | \widehat{D}_z | \widetilde{0} \rangle + c.c.$$

$$\widehat{D}_{z} = \frac{e}{2} \sum_{i=1}^{A} (1 + \tau_{i}^{z}) z_{i}$$

#### Parity and time-reversal violating nucleon-nucleon interaction and nuclear EDM

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#### Parity violating nucleon-nucleon interaction and the nuclear anapole moment

- Parity violating (non-conserving) V<sub>NN</sub><sup>PNC</sup> interaction
  - Conserves total angular momentum I
  - Mixes opposite parities
  - Has isoscalar, isovector and isotensor components
  - Admixes unnatural parity states in the ground state

$$\psi_{\rm gs} I\rangle = |\psi_{\rm gs} I^{\pi}\rangle + \sum_{j} |\psi_{j} I^{-\pi}\rangle$$
$$\times \frac{1}{E_{\rm gs} - E_{j}} \langle \psi_{j} I^{-\pi} | V_{\rm NN}^{\rm PNC} | \psi_{\rm gs} I^{\pi} \rangle$$

Anapole moment operator dominated by spin contribution

$$oldsymbol{a} = -\pi \int d^3 r \, r^2 \, oldsymbol{j}(oldsymbol{r})$$

Λ



$$\hat{\boldsymbol{a}}_{s} = \frac{\pi e}{m} \sum_{i=1}^{A} \mu_{i} (\boldsymbol{r}_{i} \times \boldsymbol{\sigma}_{i})$$
$$\mu_{i} = \mu_{p} (1/2 + t_{z,i}) + \mu_{n} (1/2 - t_{z,i})$$

$$a_s = \langle \psi_{\rm gs} \ I \ I_z = I | \hat{a}_{s,0}^{(1)} | \psi_{\rm gs} \ I \ I_z = I \rangle$$

Here is what we want to calculate:

$$\kappa_{A} = \frac{\sqrt{2}e}{G_{F}}a_{s} \qquad \qquad \kappa_{A} = -i4\pi \frac{e^{2}}{G_{F}}\frac{\hbar}{mc}\frac{(II10|II)}{\sqrt{2I+1}} \sum_{j} \langle\psi_{\rm gs} \ I^{\pi}||\sqrt{4\pi/3}\sum_{i=1}^{A}\mu_{i}r_{i}[Y_{1}(\hat{r}_{i})\sigma_{i}]^{(1)}||\psi_{j} \ I^{-\pi}\rangle \frac{1}{E_{\rm gs}-E_{j}}\langle\psi_{j} \ I^{-\pi}|V_{\rm NN}^{\rm PNC}|\psi_{\rm gs} \ I^{\pi}\rangle$$

How to calculate the sum of intermediate unnatural parity states?

$$|\psi_{\rm gs} I\rangle = |\psi_{\rm gs} I^{\pi}\rangle + \sum_{j} |\psi_{j} I^{-\pi}\rangle \frac{1}{E_{\rm gs} - E_{j}} \langle \psi_{j} I^{-\pi} | V_{\rm NN}^{\rm PNC} | \psi_{\rm gs} I^{\pi}\rangle$$

Solving Schroedinger equation with inhomogeneous term

 $(E_{\rm gs} - H)|\psi_{\rm gs} I\rangle = V_{\rm NN}^{\rm PNC}|\psi_{\rm gs} I^{\pi}\rangle$ 

• To invert this equation, we apply the Lanczos algorithm

How to calculate the sum of intermediate unnatural parity states?

$$|\psi_{\rm gs} I\rangle = |\psi_{\rm gs} I^{\pi}\rangle + \sum_{j} |\psi_{j} I^{-\pi}\rangle \frac{1}{E_{\rm gs} - E_{j}} \langle \psi_{j} I^{-\pi} | V_{\rm NN}^{\rm PNC} | \psi_{\rm gs} I^{\pi}\rangle$$

Solving Schroedinger equation with inhomogeneous term

 $(E_{\rm gs} - H)|\psi_{\rm gs} I\rangle = V_{\rm NN}^{\rm PNC}|\psi_{\rm gs} I^{\pi}\rangle$ 

To invert this equation, we apply the Lanczos algorithm

$$|\mathbf{v}_1\rangle = V_{\rm NN}^{\rm PNC} |\psi_{\rm gs} \ I^{\pi}\rangle$$

$$\psi_{\rm gs} I \rangle \approx \sum_k g_k(E_0) |\mathbf{v}_k\rangle$$

$$\hat{g}_1(\omega) = \frac{1}{\omega - \alpha_1 - \frac{\beta_1^2}{\omega - \alpha_2 - \frac{\beta_2^2}{\omega - \alpha_3 - \beta_3^2}}}$$

Lanczos continued fraction method

#### E egral **Transforms of Reaction Cross Sections**

Few-Body Systems 33, 259-276 (2003) DOI 10.1007/s00601-003-0017-z

M. A. Marchisio<sup>1</sup>, N. Barnea<sup>2</sup>, W. Leidemann<sup>1</sup>, and G. Orlandini<sup>1</sup>

#### Ab initio calculations of electric dipole moments of light nuclei

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> Petr Navrátil ⊙† TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia V6T 2A3, Canada

### N<sub>max</sub> convergence for <sup>3</sup>He N<sup>3</sup>LO NN



#### <sup>3</sup>He EDM Benchmark Calculation

### Discrepancy between calculations?

	PLB 665:165-172 (2008) (NN EFT)	PRC 87:015501 (2013)	PRC 91:054005 (2015)	Our calculation (NN EFT)
$\overline{G}_{\pi}^{0}$	0.015	(x 1/2)	(x 1/2)	0.0073 (x 1/2)
$\overline{G}_{\pi}^{1}$	0.023	(x 1/2)	(x 1/2)	0.011 (x 1/2)
$\overline{G}_{\pi}^{2}$	0.037	(x 1/5)	(x 1/2)	0.019 (x 1/2)
$\overline{G}^0_ ho$	-0.0012	(x 1/2)	(x 1/2)	-0.00062 (x 1/2)
$\overline{G}^1_ ho$	0.0013	(x 1/2)	(x 1/2)	0.00063 (x 1/2)
$\overline{G}_{ ho}^2$	-0.0028	(x 1/5)	(x 1/2)	-0.0014 (x 1/2)
$\overline{G}^0_\omega$	0.0009	(x 1/2)	(x 1/2)	0.00042 (x 1/2)
$\overline{G}^1_\omega$	-0.0017	(x 1/2)	(x 1/2)	-0.00086 (x 1/2)

Our results confirm those of Yamanaka and Hiyama, PRC 91:054005 (2015)

#### **Calculated EDMs of selected stable nuclei**

Ab initio calculations of electric dipole moments of light nuclei







#### PHYSICAL REVIEW A 102, 052828 (2020)

Editors' Suggestion

Nuclear spin-dependent parity-violating effects in light polyatomic molecules

Yongliang Hao<sup>®</sup>,<sup>1</sup> Petr Navrátil<sup>®</sup>,<sup>2</sup> Eric B. Norrgard<sup>®</sup>,<sup>3</sup> Miroslav Iliaš<sup>®</sup>,<sup>4</sup> Ephraim Eliav,<sup>5</sup> Rob G. E. Timmermans<sup>®</sup>,<sup>1</sup> Victor V. Flambaum<sup>®</sup>,<sup>6</sup> and Anastasia Borschevsky<sup>®</sup>,<sup>\*</sup>
54

#### Nuclear spin-dependent parity-violating effects from NCSM

	<sup>9</sup> Be	<sup>13</sup> C	$^{14}$ N	<sup>15</sup> N	<sup>25</sup> Mg
$I^{\pi}$	3/2-	1/2-	1+	1/2-	$5/2^{+}$
$\mu^{ ext{exp.}}$	$-1.177^{a}$	0.702 <sup>b</sup>	0.404 <sup>c</sup>	$-0.283^{d}$	$-0.855^{e}$
		NCSM	calculations		
$\mu$	-1.05	0.44	0.37	-0.25	-0.50
$\kappa_{\mathrm{A}}$	0.016	-0.028	0.036	0.088	0.035
$\langle s_{p,z} \rangle$	0.009	-0.049	-0.183	-0.148	0.06
$\langle s_{n,z} \rangle$	0.360	-0.141	-0.1815	0.004	0.30
$\kappa_{\rm ax}$	0.035	-0.009	0.0002	0.015	0.024
κ	0.050	-0.037	0.037	0.103	0.057

Contributions from nucleon axial-vector and the anapole moment



 $\kappa_{ax} \simeq -2C_{2p} \langle s_{p,z} \rangle - 2C_{2n} \langle s_{n,z} \rangle \simeq -0.1 \langle s_{p,z} \rangle + 0.1 \langle s_{n,z} \rangle$ 

$$\langle s_{\nu,z} \rangle \equiv \langle \psi_{\rm gs} \ I^{\pi} I_z = I | \hat{s}_{\nu,z} | \psi_{\rm gs} \ I^{\pi} I_z = I \rangle$$
  
 $C_{\rm 2p} = -C_{\rm 2n} = g_A (1 - 4 \sin^2 \theta_W) / 2 \simeq 0.05$ 

# Applications of *ab initio* nuclear theory to tests of fundamental symmetries

- Precision measurements of β-decay observables offer the possibility to search for deviations from the Standard Model
- Discovering such small deviations demands high-precision theoretical calculations
- Theoretical analysis of β-decay observables of the pure Gamow-Teller (GT) transition <sup>6</sup>He(0<sup>+</sup>) → <sup>6</sup>Li(1<sup>+</sup>) using *ab initio* NCSM nuclear structure calculations in combination with the chiral effective field theory (*χ*EFT)
- Four experiments investigating <sup>6</sup>He β decay at present
- We find up to 1% correction for the β spectrum and up to 2% correction for the angular correlation
- Propagating nuclear structure and *x*EFT uncertainties results in an overall uncertainty of 10<sup>-4</sup>
  - Comparable to the precision of current experiments

#### Non-zero Fierz interference term due to nuclear structure corrections

 $b_{\rm F}^{1^+\beta^-} = \delta_b^{1^+\beta^-} = -1.52\,(18)\cdot 10^{-3}$ 

Note that new physics at TeV scale implies  $b_{\rm Fierz}^{\rm BSM} = \frac{C_T + C_T^{'}}{C_A} \sim 10^{-3}$ 

55

Nuclear *ab initio* calculations of  ${}^{6}$ He  $\beta$ -decay for beyond the Standard Model studies

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#### Structure corrections for the extraction of the $V_{ud}$ matrix element from the ${}^{10}C \rightarrow {}^{10}B$ Fermi transition

- CKM unitarity sensitive probe of BSM physics
  - V<sub>ud</sub> element from super-allowed Fermi transitions

$$|V_{ud}|^2 = \frac{\hbar^7}{G_F^2 m_e^5 c^4} \frac{\pi^3 \ln(2)}{\mathcal{F}t} \qquad \qquad \mathcal{F}t = \frac{K}{G_V^2 |M_{F0}|^2 (1 + \Delta_R^V)}$$

$$\mathcal{F}t(1+\Delta_R^V) = ft(1+\delta_R')(1-\delta_C+\delta_{NS})$$

- $\delta_{NS}$  parametrizes correction to free  $\gamma W$  box  $\delta_{NS} = 2[\Box_{\gamma W}^{VA, \text{nuc.}} \Box_{\gamma W}^{VA, \text{free n}}]$
- Apply NCSM and calculate

$$T_{3}(q_{0},Q^{2}) = -4\pi i \frac{q_{0}}{q} \sqrt{M_{i}M_{f}} \sum_{J=1}^{\infty} (2J+1)$$

$$\times \left\langle A\lambda_{f}J_{f}M_{f} \right| \left[ T_{J0}^{mag}(q) G(M_{f}+q_{0}+i\epsilon) T_{J0}^{5,el}(q) + T_{J0}^{el}(q) G(M_{f}+q_{0}+i\epsilon) T_{J0}^{5,mag}(q) + T_{J0}^{5,mag}(q) G(M_{i}-q_{0}+i\epsilon) T_{J0}^{el}(q) + T_{J0}^{5,el}(q) G(M_{i}-q_{0}+i\epsilon) T_{J0}^{mag}(q) \right] \left| A\lambda_{i}J_{i}M_{i} \right\rangle$$

- $\delta_C$  isospin symmetry breaking correction
- Apply NCSMC:  ${}^{10}C \rightarrow {}^{9}B+p$ ;  ${}^{10}B \rightarrow {}^{9}Be+p$ ,  ${}^{9}B+n$

$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} \left| \stackrel{(A)}{\Longrightarrow}, \lambda \right\rangle + \sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} \left| \stackrel{\overrightarrow{r}}{\underset{(A-a)}{\textcircled{\ onlymbox{\ onlymbox\\ onlymbox{\ onlymbox{\ onlymbx\\ onlymbx{\ onlymbox{\ onlymbx\\ onlymbx{\ onlymbx\ \$$

Work in progress...

In collaboration with C.-Y. Seng & M. Gorchtein See talk by Chien-Yeah Seng

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## Conclusions

- Ab initio nuclear theory
  - Makes connections between the low-energy QCD and many-nucleon systems
  - Applicable to nuclear structure, reactions including those relevant for astrophysics, electroweak processes, tests of fundamental symmetries
  - Very recently reach extended to heavy nuclei
- Applications of *ab initio* NCSMC to
  - <sup>11</sup>Be  $\beta$  decay with the proton emission
  - Radiative capture of protons on <sup>7</sup>Be and deuteron capture on <sup>4</sup>He
  - Proton capture on <sup>7</sup>Li internal pair conversion and the X17 boson claim
- Ab initio NCSM capable to calculate accurately nuclear structure effects needed for analysis of parity-violation and time-reversal violation experiments in atoms and molecules
  - First results available; 10% precision within the reach
  - Different nuclei can be used to probe different terms of the parity & time-reversal violating interaction
- NCSM applied to analyze the nuclear-structure corrections to <sup>6</sup>He β-decay observables
- NCSM and NCSMC calculations of structure corrections for the extraction of the V<sub>ud</sub> matrix element from Fermi transitions

In synergy with experiments, ab initio nuclear theory is the right approach to understand low-energy properties of atomic nuclei