

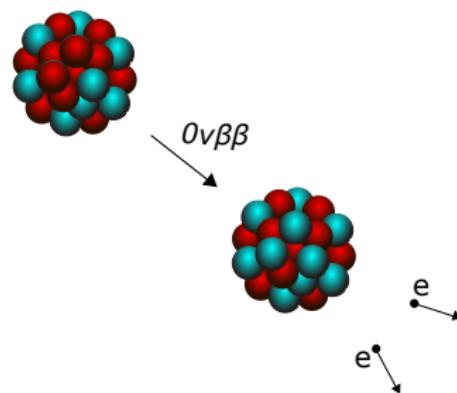
Neutrinoless double-beta decay from an effective field theory for heavy nuclei

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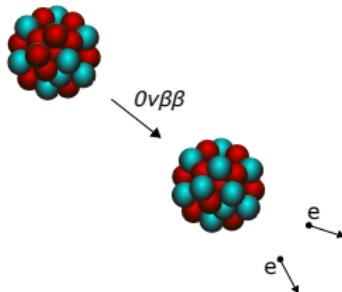


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$0\nu\beta\beta$ decay

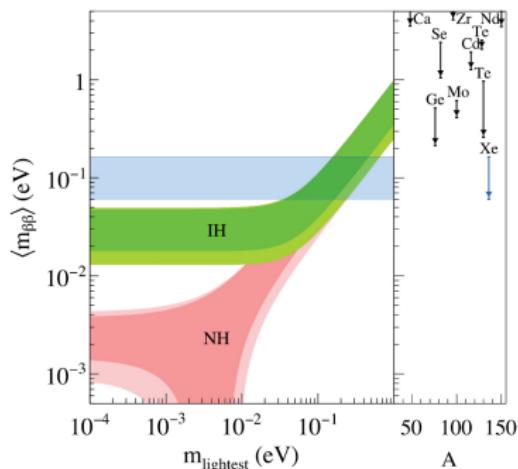


- ✚ lepton-number violation: no ν -emission
→ insights to matter and anti-matter asymmetry
- ✚ ν : neutral and massive
→ Majorana ($\nu = \bar{\nu}$) or Dirac ($\nu \neq \bar{\nu}$) particles?
- ✚ Standard Model: lepton-number conservation
→ BSM physics

open questions

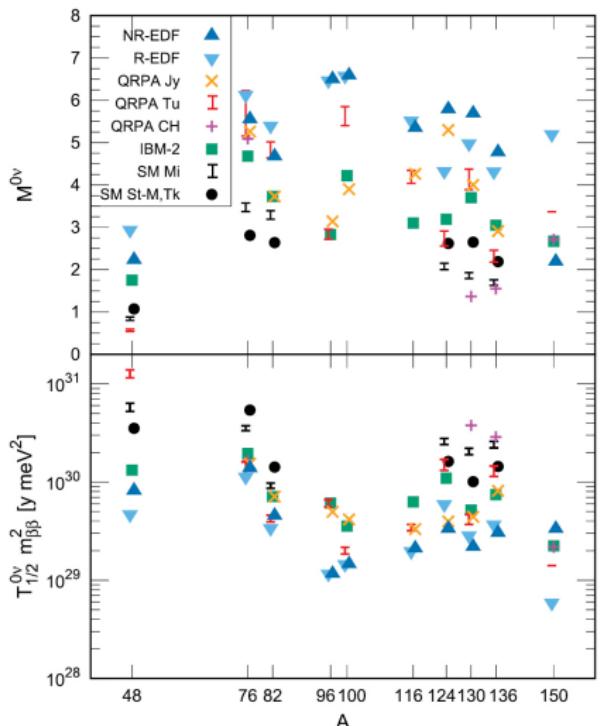
- ✚ mechanism(s) governing $0\nu\beta\beta$ decay
- ✚ mass hierarchy of neutrinos

answering these questions can be hindered
by uncertainty of NMEs



Engel and Menéndez,
Rep. Prog. Phys. 80, 046301 (2017)

Motivation: experimental side



- ✖ phenomenological calculations for medium-mass or heavy nuclei
- ✖ top:
deviation up to factor of three
- ✖ bottom - translation:
up to an order of magnitude in half-life
- ✖ experiment:
half-life \sim required material

large NME uncertainty:

- ✖ severe consequences for planning experiments
- ✖ current uncertainty estimation:
variation of model parameters

Engel and Menéndez, Rep. Prog. Phys. 80, 046301 (2017)

reliable uncertainty quantification \rightarrow EFT for medium-mass and heavy nuclei

Effective Field Theory for heavy nuclei

Coello Pérez and Papenbrock Phys. Rev. C 92, 014323 (2015),

Coello Pérez and Papenbrock Phys. Rev. C 92, 064309 (2015),

Coello Pérez, Menéndez and Schwenk, Phys. Rev. C 98, 045501 (2018)

-
- ⊕ phonon (quadrupole excitation) and fermion (neutron or proton) degrees of freedom

$$[d_\mu, d_\nu^\dagger] = \delta_{\mu\nu}, \quad \{n_\mu, n_\nu^\dagger\} = \delta_{\mu\nu}, \quad \{p_\mu, p_\nu^\dagger\} = \delta_{\mu\nu}$$

- ⊕ reference state: ground state (gs) of spherical even-even core $|0\rangle$
- ⊕ nucleus: reference state coupled to fermions and/or phonons

$$|J_f M_f; j_p, j_n\rangle = \left(n^\dagger \otimes p^\dagger \right)^{(J_f)} |0\rangle, \quad \text{gs of odd-odd nucleus}$$

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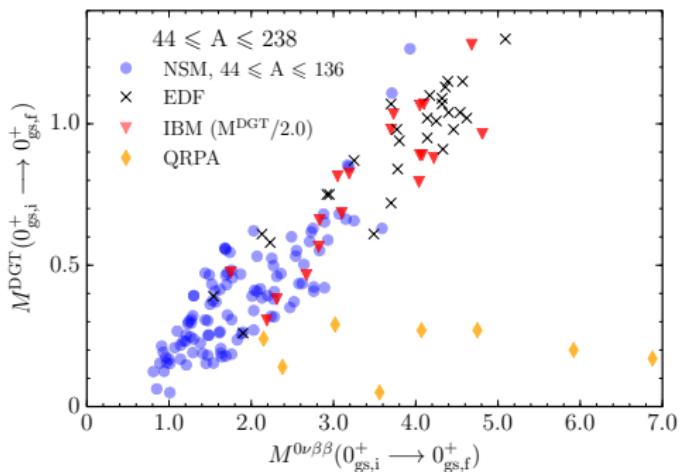
- ⊕ power counting: $Q^n = \left(\frac{\omega}{\Lambda}\right)^n$, n = number of phonons
breakdown scale Λ at three-phonon level: $\Lambda = 3\omega \approx 2 - 3$ MeV
 \rightarrow quantification of theoretical uncertainties
- ⊕ low-energy constants (LECs):
quenching, high-energy physics & microscopic information
 \rightarrow fit to experimental data required

$0\nu\beta\beta$ not observed - how to fit low-energy constants?

- ✖ LECs: experimental data of GT transitions available
- ✖ correlation between DGT and $0\nu\beta\beta$ NMEs
[Shimizu et al., Phys. Rev. Lett. 120 14, 142502 \(2018\)](#),

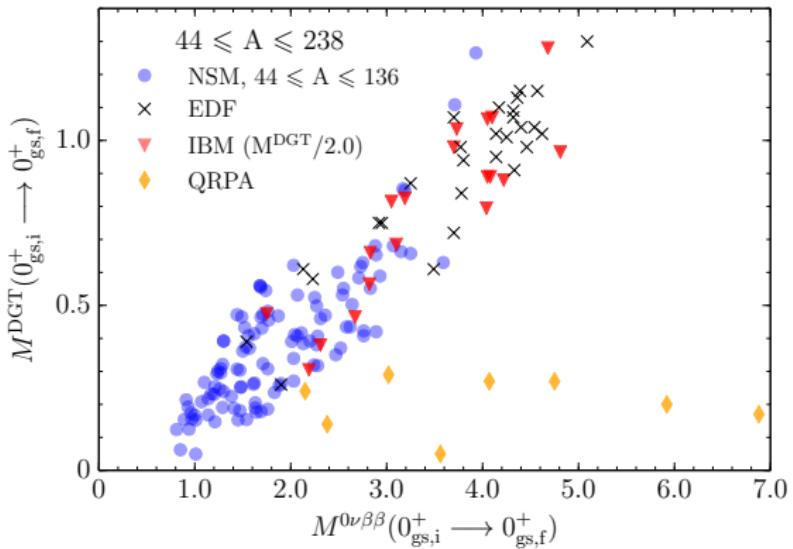
strategy:

1. DGT NMEs within EFT
 2. correlation + DGT NMEs
- EFT $0\nu\beta\beta$ NME prediction with systematic quantified uncertainties



but first: correlation

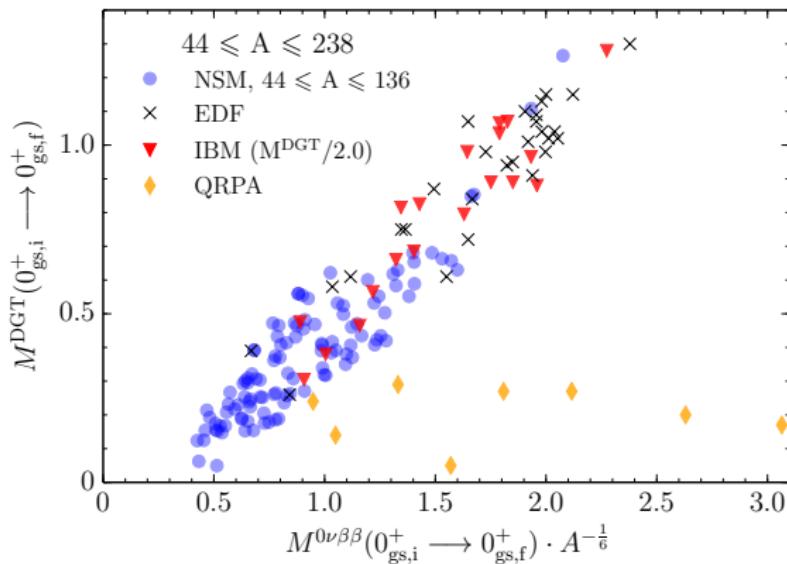
Correlation



- NSM, IBM and EDF results correlate very well
- QRPA results do not (see Javier's talk)

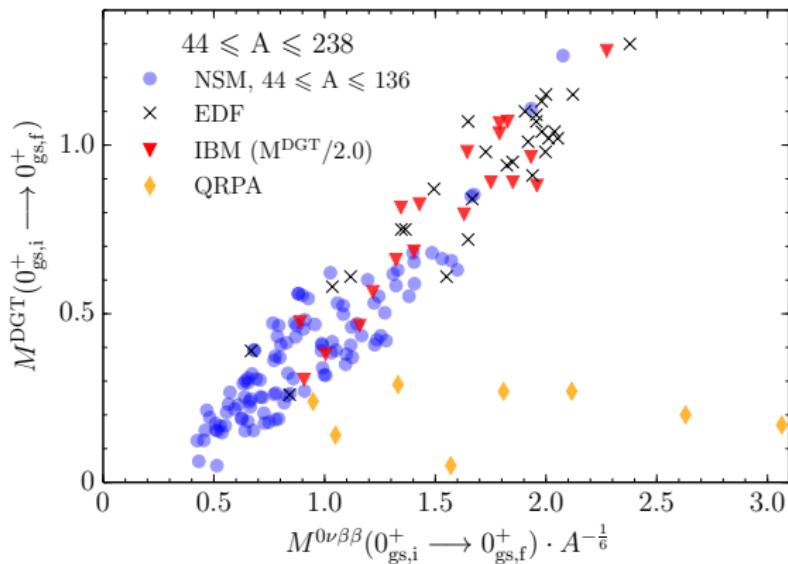
Variations of correlation

	correlation	correlation coefficient r				
DGT	$0\nu\beta\beta$	NSM	EDF	IBM	QRPA	NSM, EDF, IBM
$\cdot R[\text{fm}]$		0.83	0.91	0.88	-0.03	0.93
$\cdot A^{-\frac{1}{6}}$		0.64	0.85	0.66	-0.04	0.86
		0.90	0.93	0.93	-0.03	0.95

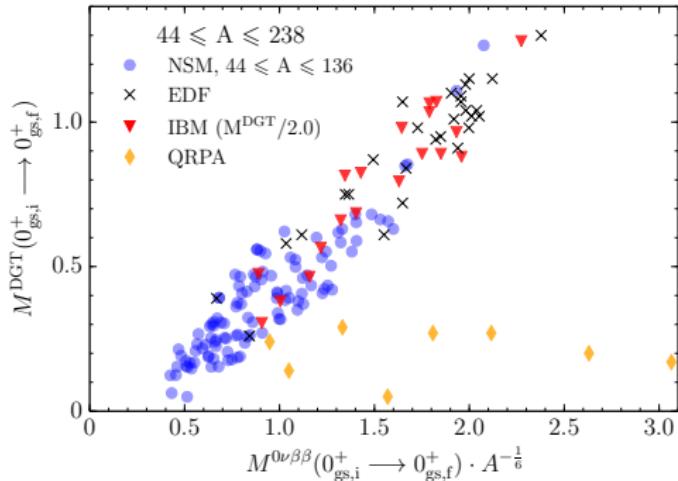


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Correlation - motivation of factor



CB, Menéndez, Coello Pérez and Schwenk PRC 106 (2022) 3, 034309

$M_{\text{NSM/IBM}}^{0\nu\beta\beta}$ implicit dependence on

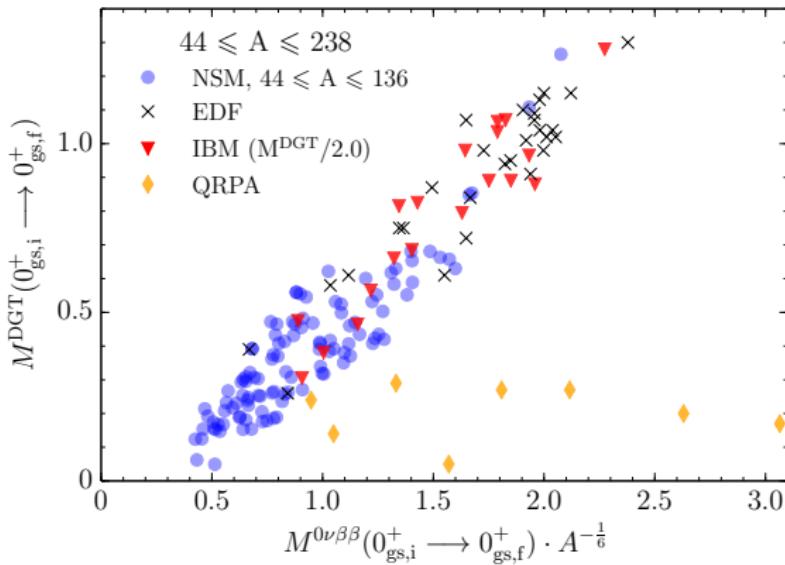
- harmonic oscillator length $b \sim A^{1/6}$
- inverse radius $1/R$ with $R \sim A^{1/3}$

best fit accounts for implicit dependence $\rightarrow b/R \sim A^{-1/6}$

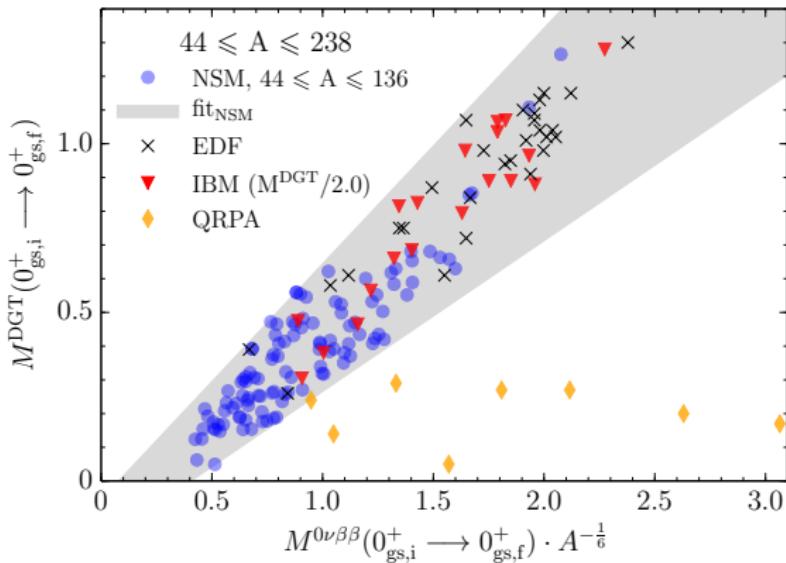
Correlation - linear fit of band

- * application of correlation → band
- * fit of three linear functions to NSM data:

$$m \cdot \left(M^{0\nu\beta\beta} \cdot A^{-1/6} \right) + n = M^{\text{DGT}}$$



Correlation



CB, Menéndez, Coello Pérez and Schwenk PRC 106 (2022) 3, 034309

- EDF and IBM enclosed by fit_{NSM}
- impressive mass range across nuclear chart (close to valley of stability)

Double Gamow-Teller transitions within EFT

- effective double GT operator between even-even states

$$\hat{O}_{\text{DGT}} = \left(\hat{O}_{\text{GT}} \otimes \hat{O}_{\text{GT}} \right)^{(0)} = \underbrace{\overline{C}_\beta^2 \left((\tilde{p} \otimes \tilde{n})^{(1)} \otimes (\tilde{p} \otimes \tilde{n})^{(1)} \right)^{(0)}}_{\text{LO}} + \dots$$

- define spherical-tensor annihilation operator: $\tilde{a}_\mu = (-1)^{j_a + \mu} a_{-\mu}$
- higher-order terms not considered \rightarrow uncertainty

$$\delta \sim \sum_{n=1}^{\infty} \left(\frac{\omega}{\Lambda} \right)^n = 0.5$$

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- multifermion excitation of reference state

$$|0_{\text{gs}}^+\rangle = \frac{1}{2} \left(\left(n^\dagger \otimes n^\dagger \right)^{(0)} \otimes \left(p^\dagger \otimes p^\dagger \right)^{(0)} \right)^{(0)} |0\rangle$$

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- final even-even nucleus \rightarrow reference state $|0\rangle$

LO nuclear matrix element

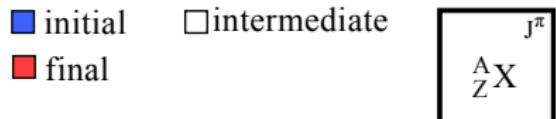
$$M_{\text{EFT}}^{\text{DGT}} = \sqrt{\frac{4}{3(2j_n + 1)(2j_p + 1)}} \bar{C}_{\beta}^2$$

LO nuclear matrix element - Low-energy constant

$$M_{\text{EFT}}^{\text{DGT}} = \sqrt{\frac{4}{3(2j_n + 1)(2j_p + 1)}} \bar{C}_{\beta}^2$$

\bar{C}_{β}^2 fit to GT data: $\bar{C}_{\beta}^2 = C_{\beta 1} C_{\beta 2}$

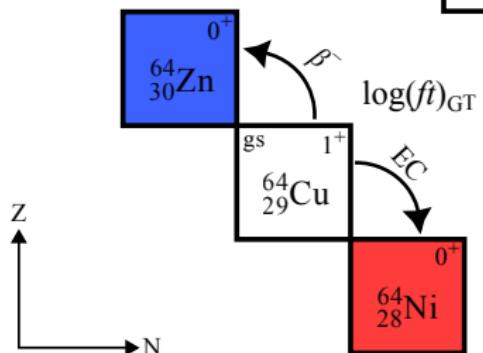
Coello Pérez, Menéndez, and Schwenk,
Phys. Lett. B 797, 134885 (2019)



- * GT transition selection rule:

$$\Delta J_{\text{GT}} = 1 \quad \Delta \pi_{\text{GT}} = +$$

- * $\log(ft)$ -values of GT decays
- * GT strengths from charge-exchange reactions



<https://www.nndc.bnl.gov/ensdf/>,

Grawe et al., Phys. Rev. C 76, 054307 (2007), Thies et al., Phys. Rev. C 86, 014304 (2012)

Frekers et al., Phys. Rev. C 94, 014614 (2016), Thies et al., Phys. Rev. C 86, 054323 (2012)

Puppe et al., Phys. Rev. C 86, 044603 (2012), Puppe et al., Phys. Rev. C 84, 051305 (2011)

Guess et al., Phys. Rev. C 83, 064318 (2011)

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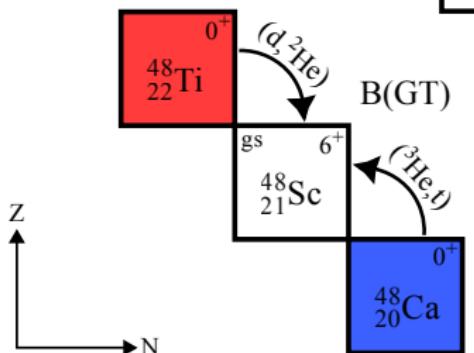
■ initial □ intermediate
■ final

${}^A_Z X^{J^\pi}$

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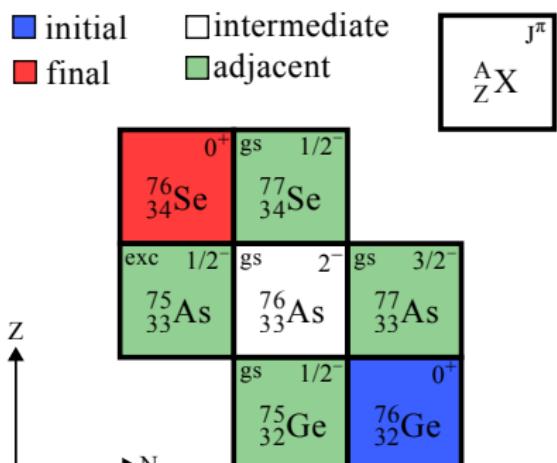
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Nucleon orbitals

$$M_{\text{EFT}}^{\text{DGT}} = \sqrt{\frac{4}{3(2j_n + 1)(2j_p + 1)}} \bar{C}_\beta^2$$

- * idea: nucleon orbitals from adjacent odd-mass nuclei
- * dominant orbitals:
ground or low-lying single-particle excited states
- * $j_n = \frac{1}{2}$
- * $j_p = \frac{3}{2}$ or $j_p = \frac{1}{2}$

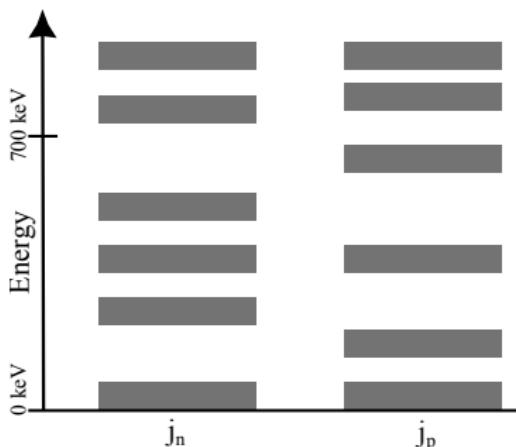


CB, Menéndez, Coello Pérez and Schwenk
PRC 106 (2022) 3, 034309

conditions:

- * physically motivated thresholds
 - * $E \leq 700$ keV (dominance)
 - * $T_{1/2} \geq 0.1$ ns (single particle)
- * GT transition selection rules
 - * $|j_n - j_p| \leq 1 \leq |j_n + j_p|$
 - * $\pi_n \cdot \pi_p = +$
- * additional restrictions from
 - * NSM: collective/not dominant

spectra of adjacent odd-mass nuclei

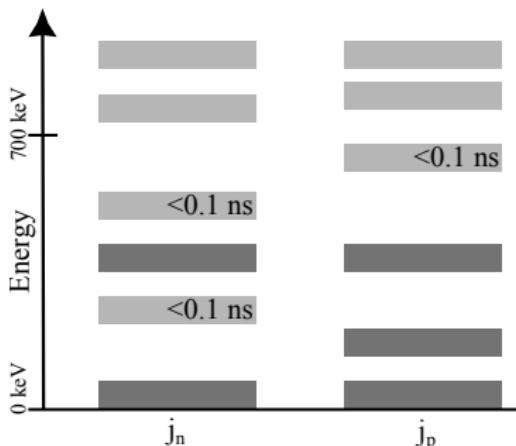


experimental data of odd-mass adjacent nuclei,
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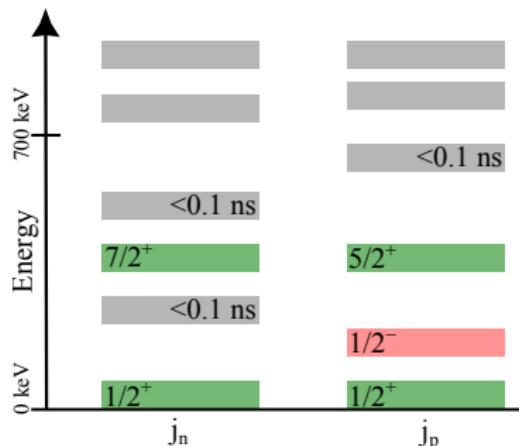
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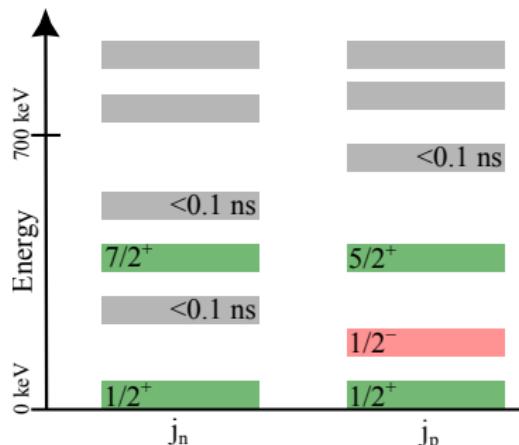
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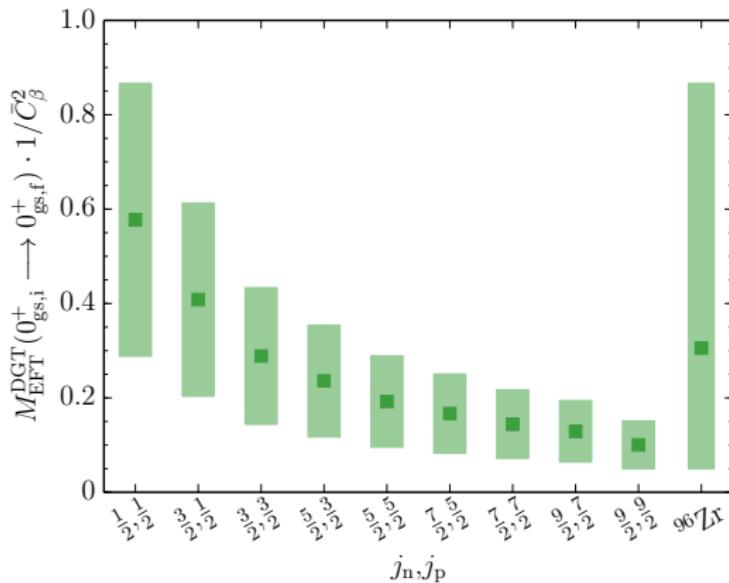
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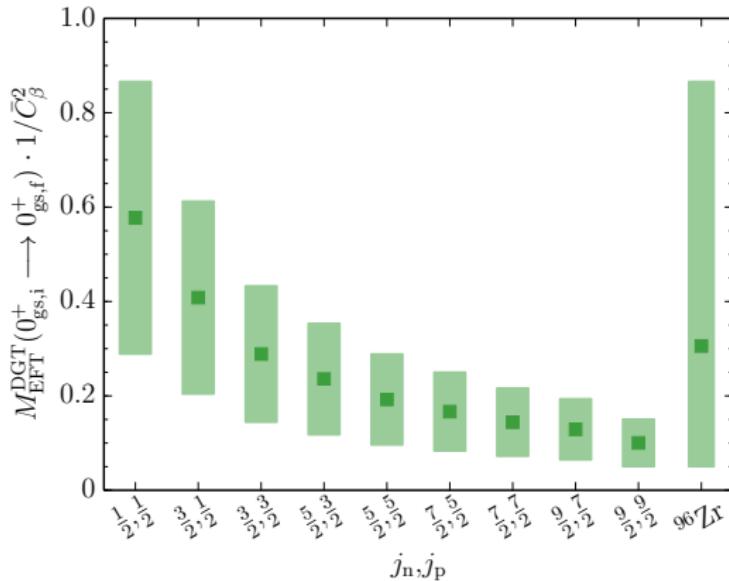
Nucleon orbitals contributions



CB, Menéndez, Coello Pérez and Schwenk PRC 106 (2022) 3, 034309

- ✚ truncation uncertainty: 50%
- ✚ ^{96}Zr central value: average of EFT DGT NME central values
- ✚ ^{96}Zr uncertainty: complete uncertainty range

Nucleon orbitals contributions

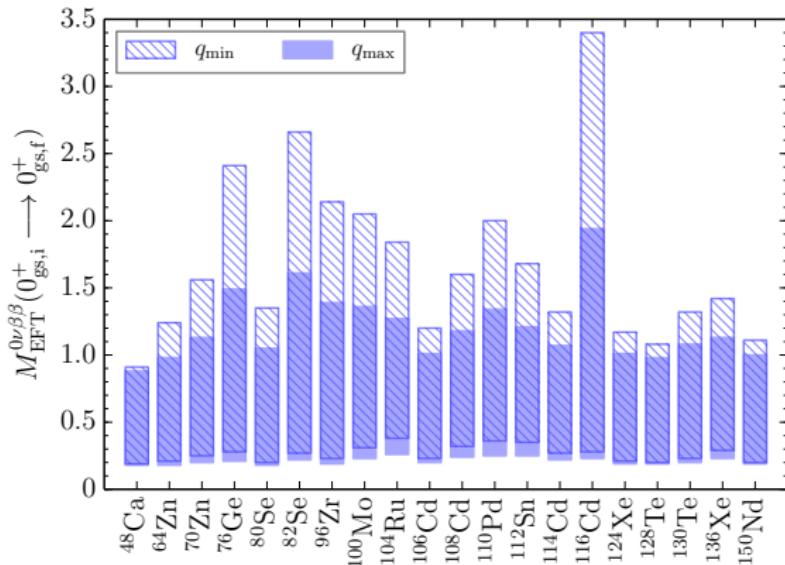


CB, Menéndez, Coello Pérez and Schwenk PRC 106 (2022) 3, 034309

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DGT NME + correlation band $\rightarrow 0\nu\beta\beta$ NME

$0\nu\beta\beta$ nuclear matrix elements

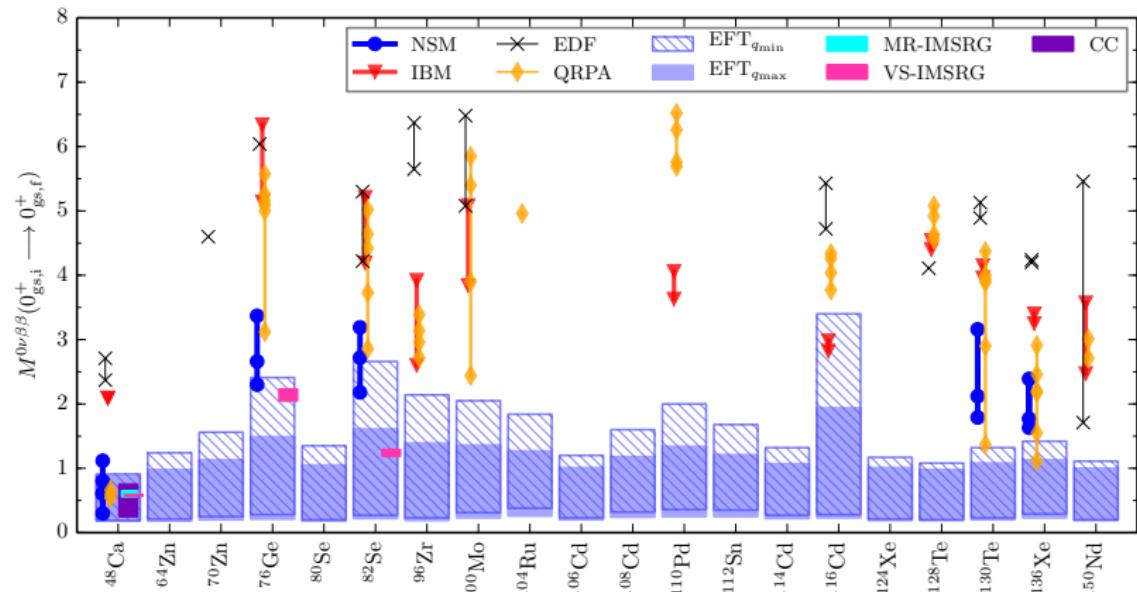


CB, Menéndez, Coello Pérez and Schwenk PRC 106 (2022) 3, 034309

- ✖ include quenching uncertainty from NSM GT transition
- ✖ $A > 48$: $q_{\min} = 0.42$ and $q_{\max} = 0.65$
- ✖ $A = 48$: $q_{\min} = 0.70$ and $q_{\max} = 0.80$
- ✖ range: $0.18 \leqslant M_{\text{EFT}}^{0\nu\beta\beta} \leqslant 3.40$

Predictions in comparison

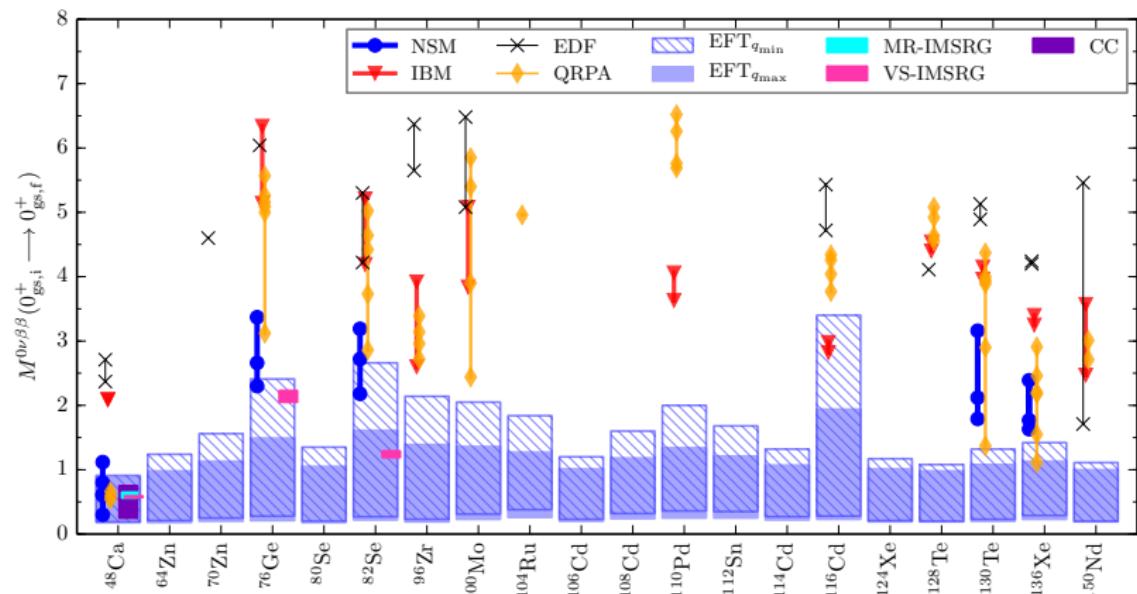
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- Menéndez *et al.*, Nucl. Phys. A 818, 139 (2009), Horoi *et al.*, Phys. Rev. C 101, 044315 (2020), Iwata *et al.*, Phys. Rev. Lett. 116, 112502 (2016), Rodríguez *et al.*, Phys. Rev. Lett. 105, 252503 (2010), Song *et al.*, Phys. Rev. C 95, 024305 (2017), Šimkovic *et al.*, Phys. Rev. C 87, 045501 (2013), Fang *et al.*, Phys. Rev. C 97, 045503 (2018), Hyvärinen and Suhonen, Phys. Rev. C 91, 024613 (2015), Mustonen and Engel, Phys. Rev. C 87, 064302 (2013), Šimkovic *et al.*, Phys. Rev. C 98, 064325 (2018), Barea *et al.*, Phys. Rev. C 91, 034304 (2015), Yao *et al.*, Phys. Rev. Lett. 124, 232501 (2020), Belley *et al.*, Phys. Rev. Lett. 126, 042502 (2021), Novario *et al.*, Phys. Rev. Lett. 126, 182502 (2021)

Predictions in comparison

CB, Menéndez, Coello Pérez and Schwenk PRC 106 (2022) 3, 034309



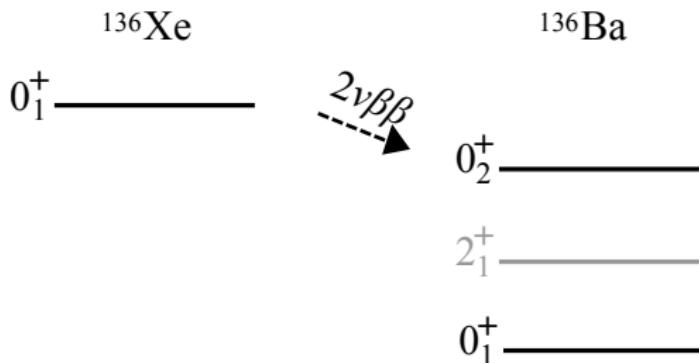
- ✚ range: $M_{\text{EFT}}^{0\nu\beta\beta} \leqslant 3.40$ vs. $M_{\text{other}}^{0\nu\beta\beta} \leqslant 6.5$ \rightarrow EFT smaller predictions
- ✚ (almost) overlap: ${}^{48}\text{Ca}$, ${}^{76}\text{Ge}$, ${}^{82}\text{Se}$, ${}^{100}\text{Mo}$, ${}^{116}\text{Cd}$ and ${}^{136}\text{Xe}$
- ✚ combined unc. from other models larger than EFT unc.
- ✚ consistent with *ab initio* predictions (MR-/VS-IMSRG & CC)



Jokiniemi, Romeo, CB, Kotila, Soriano, Schwenk and Menéndez

arXiv:2211.03764 in press at PLB

Motivation - ${}^{136}\text{Xe}(\text{gs}, 0_1^+) \xrightarrow{2\nu\beta\beta} {}^{136}\text{Ba}(\text{exc}, 0_2^+)$



- ✚ test of predictions from different nuclear many body calculations
- ✚ useful, because applying these same methods for $0\nu\beta\beta$
- ✚ ongoing search for this decay at KamLAND-Zen and nEXO
 - K. Asakura, et al., Nucl. Phys. A 946 (2016) 171,
 - G. Adhikari, et al, J. Phys. G: Nucl. Part. Phys. 49 015104 (2022)

- ⊕ fit LECs to data from β decay or from charge-exchange reaction (GT-strength)
 → predict $2\nu\beta\beta$ decay from gs to gs $M_{\text{EFT}}^{2\nu}(0_{\text{gs}}^+ \rightarrow 0_{\text{gs}}^+)$ with single state dominance (SSD) approximation

$$M_{\text{GT}}^{2\nu} \sim \langle f | \hat{O}_{\text{GT}} | 1_1^+ \rangle \langle 1_1^+ | \hat{O}_{\text{GT}} | i \rangle$$

- ⊕ uncertainty associated to SSD approximation can be explicitly included
[Coello Pérez, Menéndez and Schwenk, PRC 98, 045501 \(2018\)](#)
- ⊕ subsequently decay to first excited 0_2^+ can be predicted
[Coello Pérez, Menéndez and Schwenk, PRC 98, 045501 \(2018\)](#)

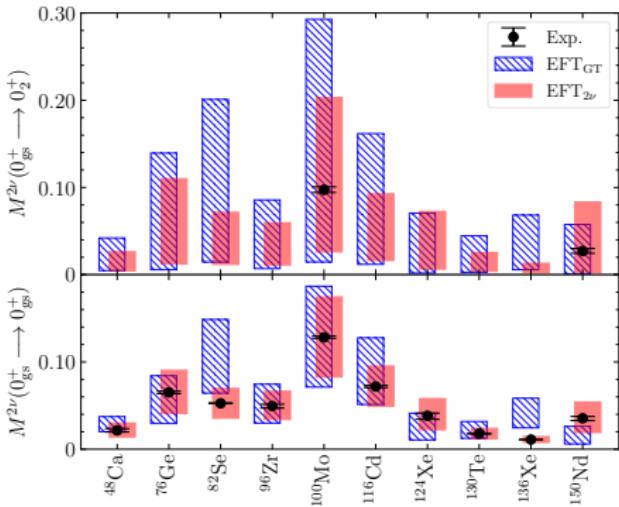
$$M_{\text{EFT}}^{2\nu}(0_{\text{gs}}^+ \rightarrow 0_2^+) \approx \left(1 + \frac{D_{10_2^+}}{D_{20_2^+}} + \frac{D_{10_2^+}}{D_{30_2^+}} \right) \frac{D_{10_{\text{gs}}^+}}{D_{10_2^+}} \frac{\sqrt{2}}{3} M_{\text{EFT}}^{2\nu}(0_{\text{gs}}^+ \rightarrow 0_{\text{gs}}^+)$$

$$\delta(\text{gs} \rightarrow 0_2^+) = \frac{\omega}{\Lambda} \left(\frac{D_{10_2^+}}{D_{20_2^+}} + \frac{D_{10_2^+}}{D_{30_2^+}} \right) + \frac{D_{10_2^+}}{\Lambda} \phi \left(\frac{\omega}{\Lambda}, 1, \frac{D_{30_2^+} + \omega}{\omega} \right)$$

Results

fit to GT data

- * EFT works very well for gs to gs and for gs to exc(0_2^+)
- * but for ^{136}Xe gs to gs not consistent with experiment

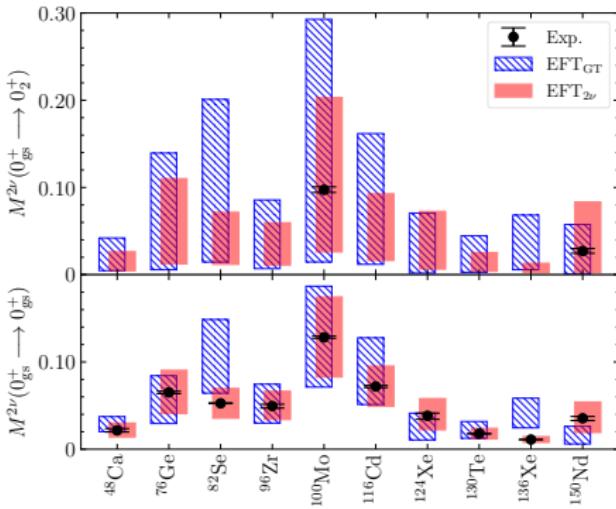


Jokiniemi, Romeo, CB, Kotila, Soriano, Schwenk and
Menéndez arXiv:2211.03764 in press at PLB

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Jokiniemi, Romeo, CB, Kotila, Soriano, Schwenk and
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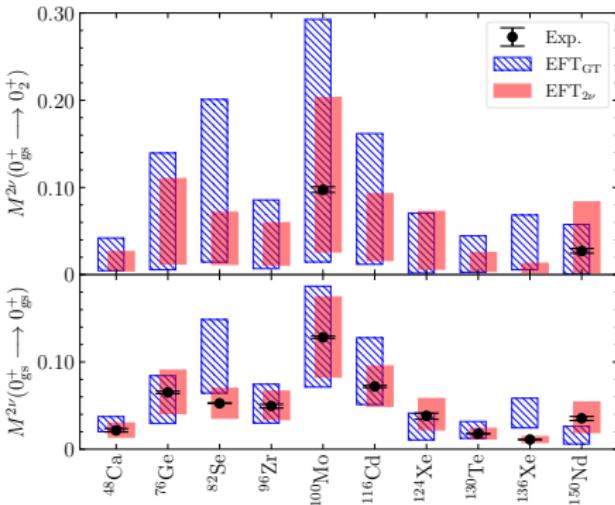
fit to $\beta\beta$ -decay data

- * fit directly to $2\nu\beta\beta$ data \rightarrow gs to gs agreement perfect by construction

Results

fit to GT data

- * EFT works very well for gs to gs and for gs to exc(0_2^+)
- * but for ^{136}Xe gs to gs not consistent with experiment



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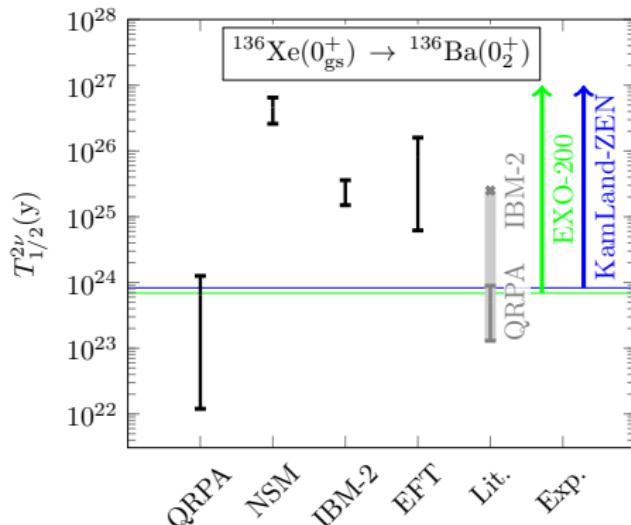
comparison

- * fit to $2\nu\beta\beta$: NMEs generally smaller
- * overlap of fitting strategies: smallest for ^{136}Xe

Results: comparison with predictions from other methods

half-lives!

- * EFT advantage:
systematic theoretical
uncertainties
- * QRPA only small overlap with
lower limits
- * NSM, IBM-2 and EFT in
complete agreement with exp.
lower limit
- * IBM-2 and EFT consistent



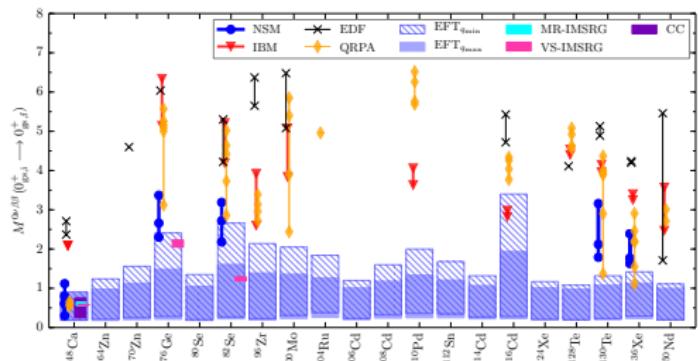
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So I am excited about future experimental measurements

Summary

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- ✚ rare decays within EFT for heavy nuclei at LO
- ✚ in general: $0\nu\beta\beta$ EFT NMEs smaller in comparison
- ✚ consistent with *ab initio* calculations

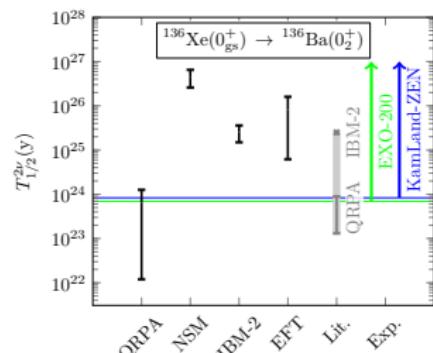
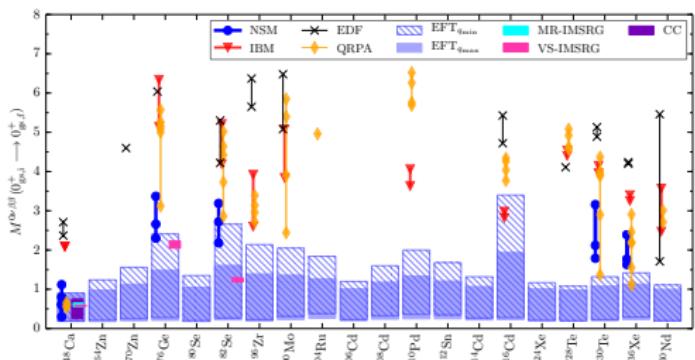


CB, Menéndez, Coello Pérez and Schwenk

PRC 106 (2022) 3, 034309

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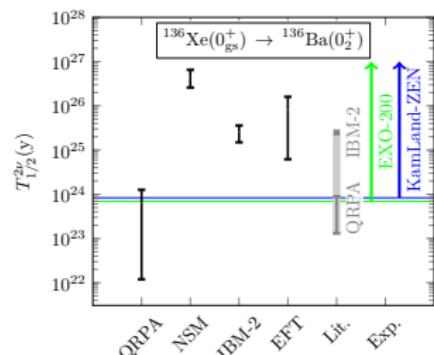
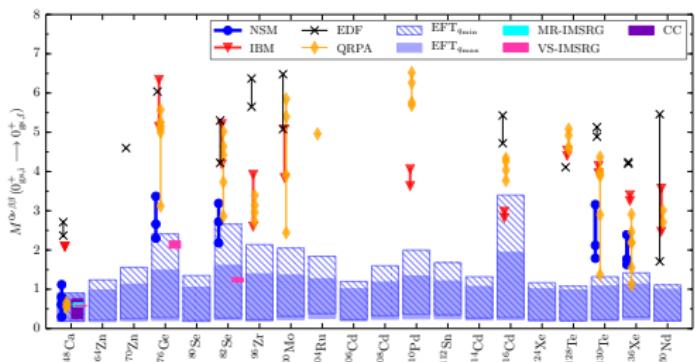
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Thank you!!

