

Simulation of muon pairs production at PANDA experiment in

*" $p\bar{p} \rightarrow \mu^+\mu^- + X$ " events at
 $E_{beam} = 5\text{ GeV}$*



A.N.Skachkova

(JINR, Dubna)


FAIRNESS
3-8 SEPTEMBER 2012,
HERSONISSOS,
GREECE

Publications

for the higher energy $E_{beam} = 14 \text{ GeV}$

- ***“Monte-Carlo simulation of lepton pair production in “ $p \bar{p} \rightarrow \ell^+ \ell^- + X$ ” events at $E_{beam} = 14 \text{ GeV}$ ”***
Authors: A.N.Skachkova, N.B.Skachkov, G.D.Alexeev
arXiv: hep-ph/0506139 PANDA-NOTE PHY-003
- ***“On Lepton Pair Production in Proton-Antiproton Collisions at Intermediate Energies ”***
Authors: A.N.Skachkova, N.B.Skachkov
PepanLetters: JINR,
ISSN:1814-5957, eISSN:1814-5973,
V.6 №:4 (153) – 2009. - Pp.504-518

V.A. Matveev, R.M. Muradian, A.N. Tavkhelidze (MMT)

(V.A. Matveev, R.M. Muradian, A.N. Tavkhelidze, JINR P2-4543, JINR, Dubna, 1969; SLAC-TRANS-0098, JINR R2-4543, Jun 1969; 27p.)

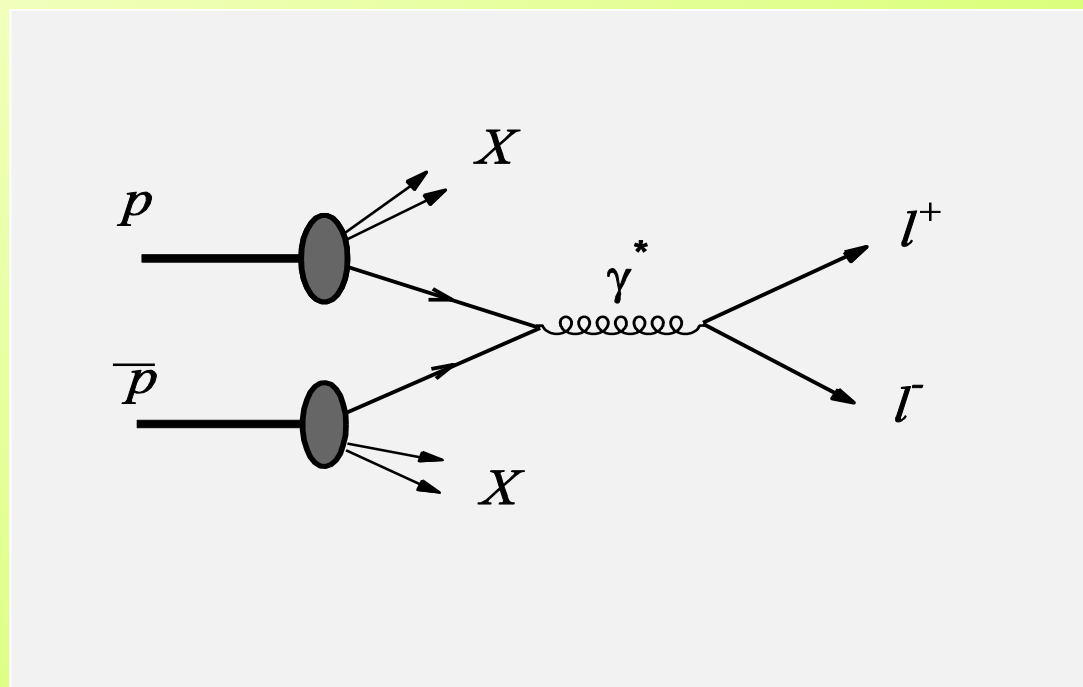
process, called also as Drell-Yan

(S.D. Drell, T.M. Yan, SLAC-PUB-0755, Jun 1970, 12p.; Phys.Rev.Lett. 25(1970)316-320, 1970)

The dominant mechanism
of the $\ell^+ \ell^-$ production is
the perturbative QED/QCD
partonic $2 \rightarrow 2$ process

$$\bar{q} q \rightarrow \gamma^* / Z^0 \rightarrow \ell^+ \ell^-$$

$$\sigma = 1.6 * 10^2 \text{ pb}$$



PYTHIA 6 simulation for the $E_{\text{beam}} = 5 \text{ GeV}$ (3.3 GeV center-of-mass energy)
without detector effects (“ideal detector” --> all particles are detected)
allows a proper account of the relativistic kinematics during the simulation

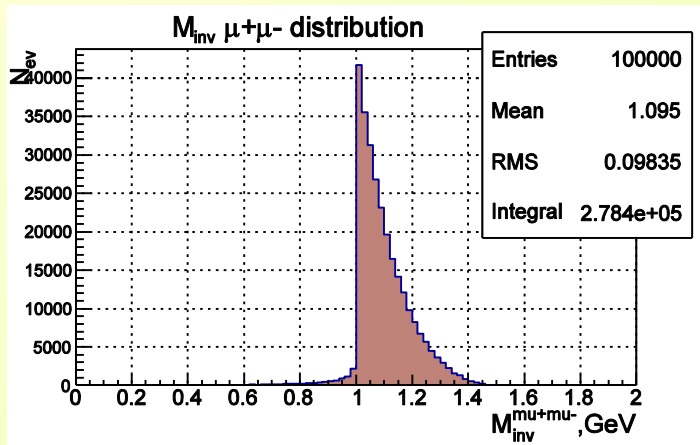
- I. Antiproton beam with $E_{\text{beam}} < 15 \text{ GeV}$ may provide an interesting information about *quark dynamics inside the hadron* and *proton structure* in the **energy region** where the **Perturbative QCD** comes into interplay with a reach **resonance** (i.e., Nonperturbative) **physics**.
- II. Different to electron beams, used for measurements of **proton structure functions** in the region of **!negative!** values of the square of transferred momentum ($q^2 < 0$, “**space-like**” region),

antiproton-proton collisions allow to make measurements of **proton structure functions** in the region of **!positive!** values of the square of the transferred momentum ($q^2 > 0$, “**time-like**”, region, which is less studied !).

The process of lepton pair production $q \bar{q} \rightarrow \gamma^* / Z^0 \rightarrow \ell^+ \ell^-$ is of big physical interest because:

- A. The **spectrum** of final state **leptons** (e and muons) obviously **depends** on the form of **parton distributions** inside colliding protons and may provide an interesting information about the ***quark dynamics inside the hadron***.
- B. The measurement of the total transverse momentum of a lepton pair PT ($\ell^+ \ell^-$) as a whole may provide an important information about the ***intrinsic transverse momentum*** $\langle k_T \rangle$ that appears due to the Fermi motion of quarks inside the nucleon

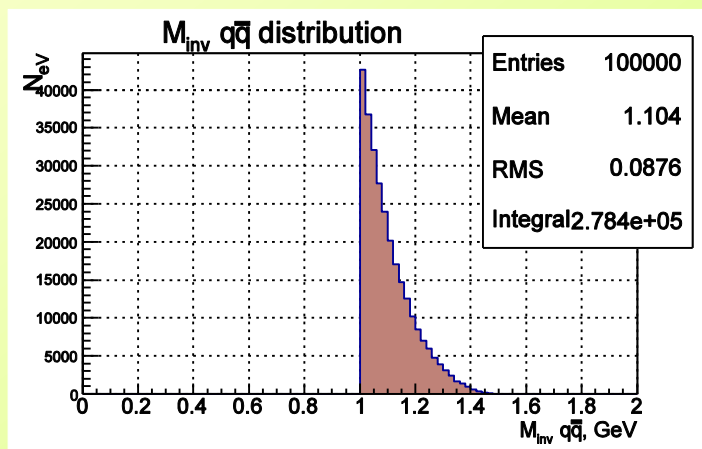
$\bar{q}q \rightarrow \gamma^* \rightarrow \ell^+\ell^-$ process - $M_{\text{inv}} \ell^+\ell^-$



- $M_{\text{inv}} \ell^+\ell^- = \sqrt{(P_{\ell^+} + P_{\ell^-})^2}$

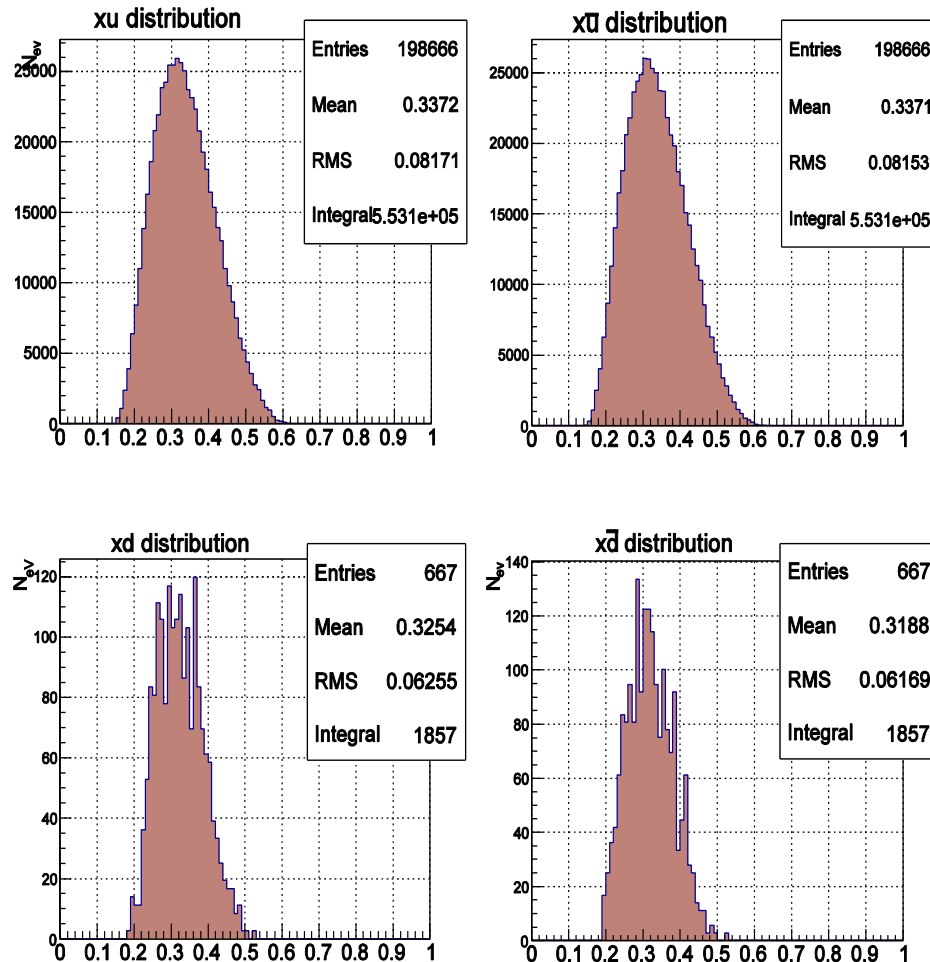
$M_{\text{inv}} \ell^+\ell^- \text{ min} = M_{\text{inv}} \bar{q}q = 1 \text{ GeV}$
 – originates from the internal
 PYTHIA restriction

- $M_{\text{inv}} \bar{q}q = \sqrt{(P_q + P_{\bar{q}})^2}$
 $= m_{\text{hat}} \approx 1.45 \text{ GeV}$
 $\rightarrow Q^2 < 2.1 \text{ GeV}^2$



Estimation of the x - Q^2 region, available for the structure functions measurement

$xU/XUbar$ & $xD/xDbar$ histograms

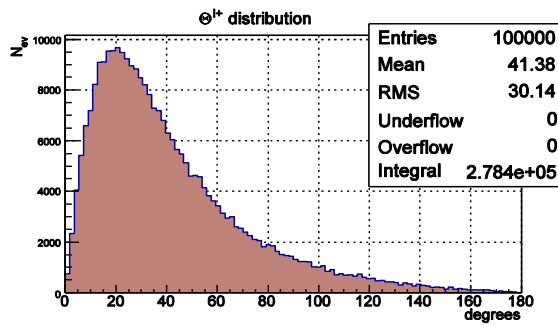
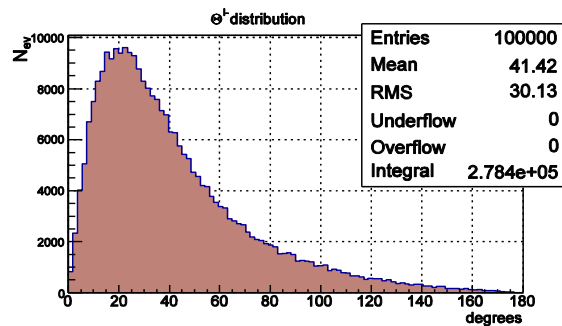
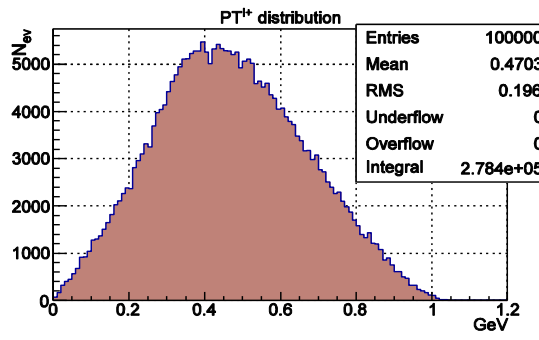
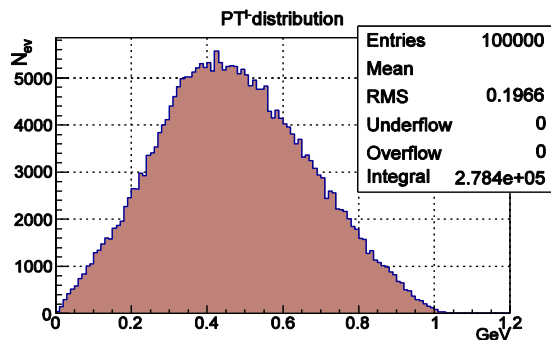
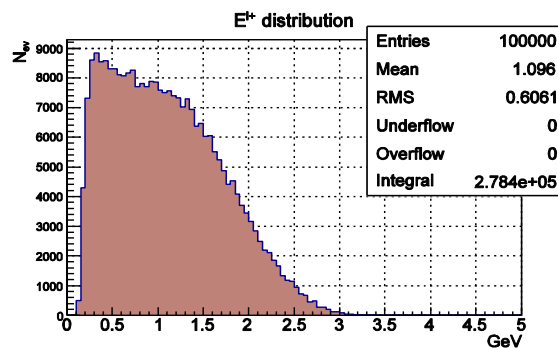
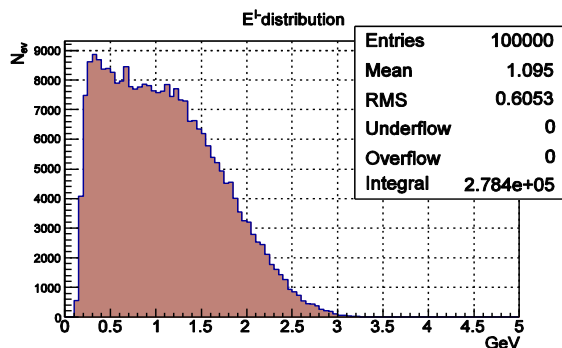


For the PANDA
experiment with
the $E_{\text{beam}} = 5 \text{ GeV}$

$$0.15 < x < 0.6$$

$$Q^2 < 2.1 \text{ GeV}^2$$

Signal Lepton histograms



$$0 \leq E_\ell \leq 3 \text{ GeV},$$

$$\langle E_\ell \rangle = 1.09 \text{ GeV},$$

$$E_{\text{peak}} = 0.3 \text{ GeV}$$

$$0 \leq PT_\ell \leq 1 \text{ GeV},$$

$$\langle PT_\ell \rangle = 0.47 \text{ GeV}$$

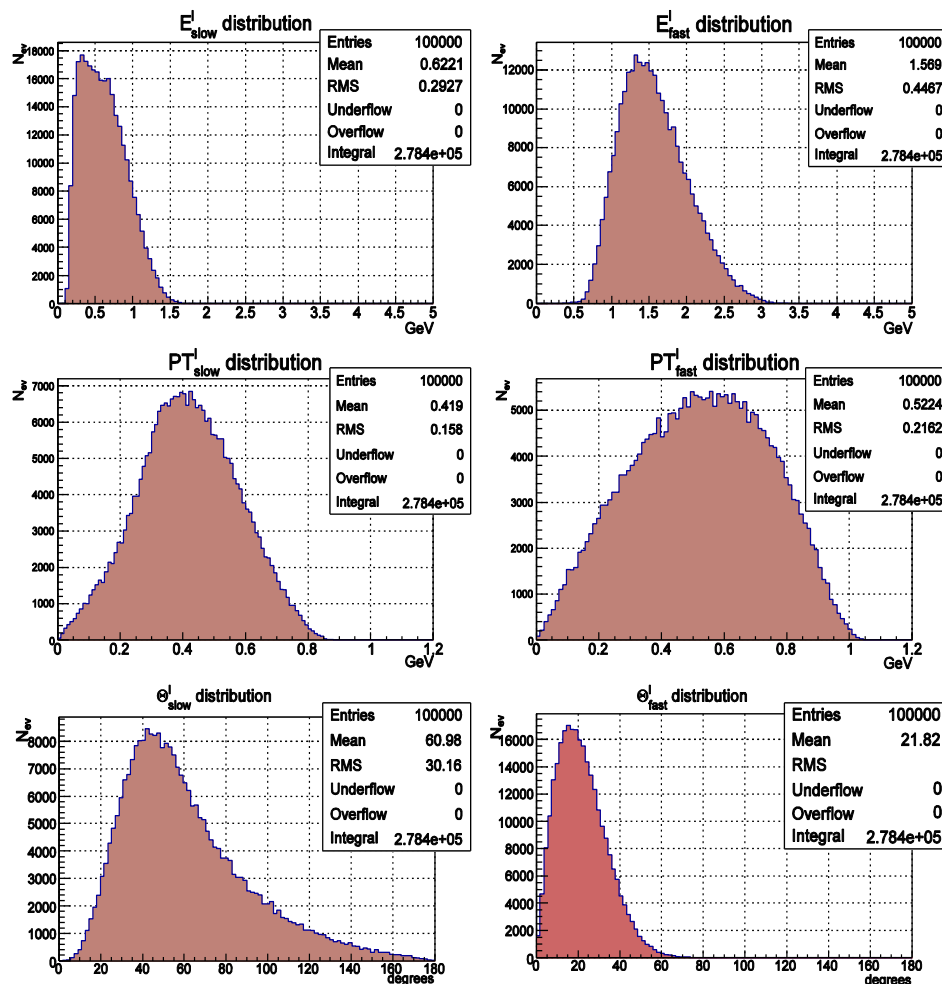
$$\langle \Theta_\ell \rangle = 41.4^\circ$$

some $\Theta_\ell > 90^\circ!!!$

In each signal ℓ^\pm event:

$$E_{\ell \text{ "fast" }} > E_{\ell \text{ "slow" }}$$

E_{Lepton} histograms



Left column

$$0.2 < E_{\text{slow}}^\mu < 1.6 \text{ GeV}$$

$$E_{\text{slow}}^{\mu \text{ peak}} \approx 0.3 \text{ GeV},$$

$$\langle E_{\text{slow}}^\mu \rangle = 0.62 \text{ GeV}$$

$$0 < \Theta_{\text{slow}}^\mu < 180^\circ$$

Less energetic slow leptons some have $\Theta_{\text{slow}}^\mu > 90^\circ$

Right column

$$0.6 < E_{\text{fast}}^\mu < 3.1 \text{ GeV}$$

$$E_{\text{fast}}^{\mu \text{ peak}} \approx 1.3 \text{ GeV},$$

$$\langle E_{\text{fast}}^\mu \rangle = 1.57 \text{ GeV}$$

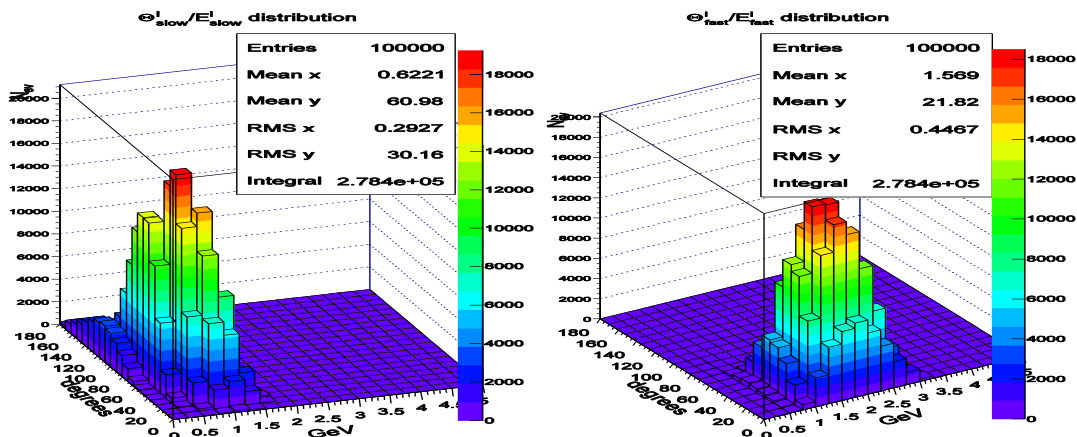
$$0 < \Theta_{\text{fast}}^\mu < 70^\circ$$

High energetic fast leptons fly in a forward direction

$\Theta_{\ell''\text{slow}}/E_{\ell''\text{slow}}$

$\Theta_{\ell''\text{fast}}/E_{\ell''\text{fast}}$

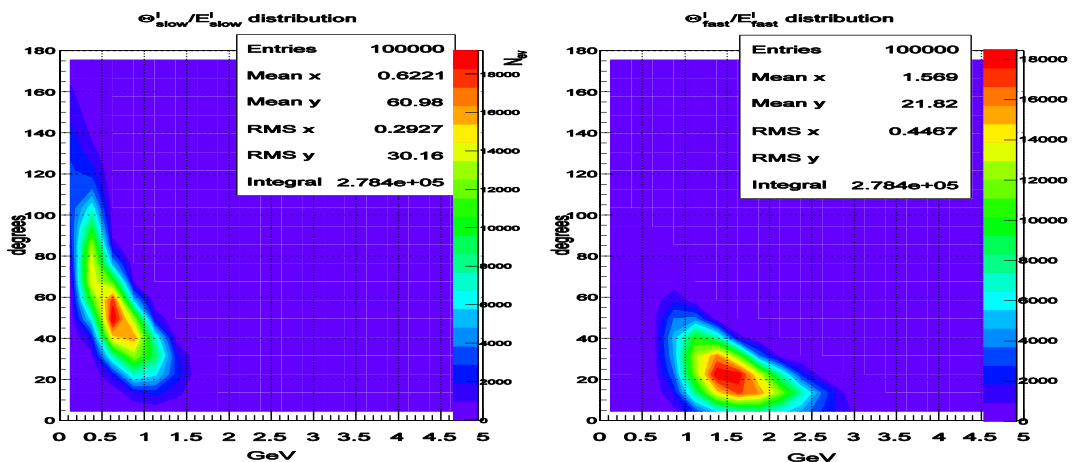
Angle/Energy Lepton Correlations LEGO



Left column – “slow” μ ,

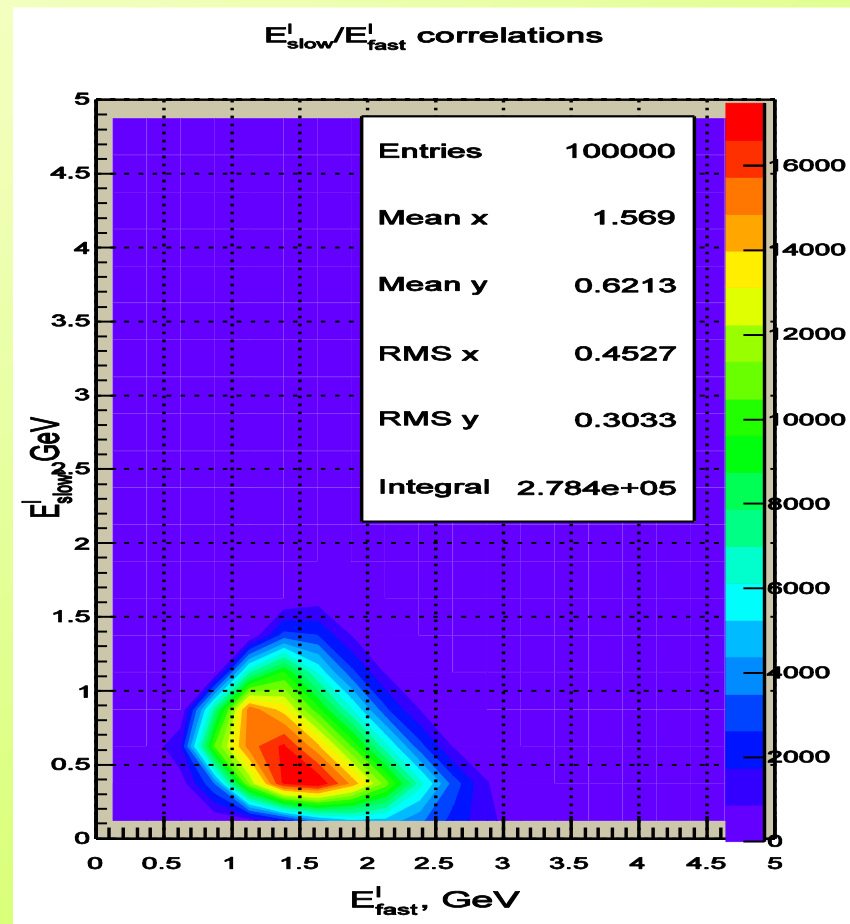
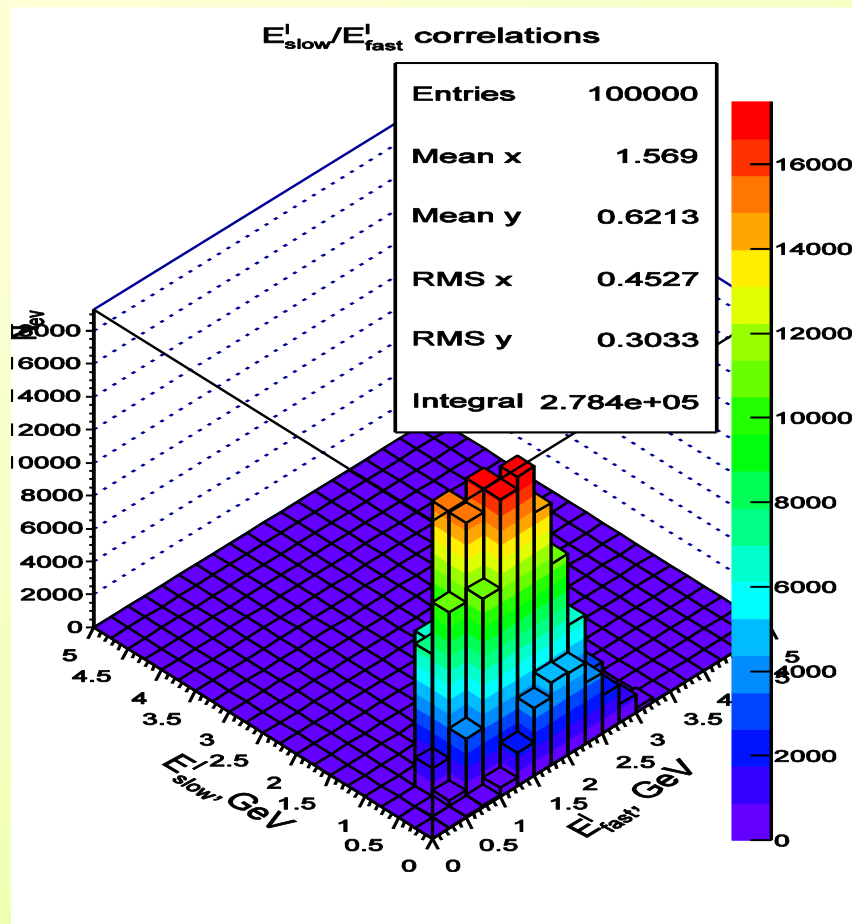
Right column – “fast” μ

Angle/Energy Lepton Correlations

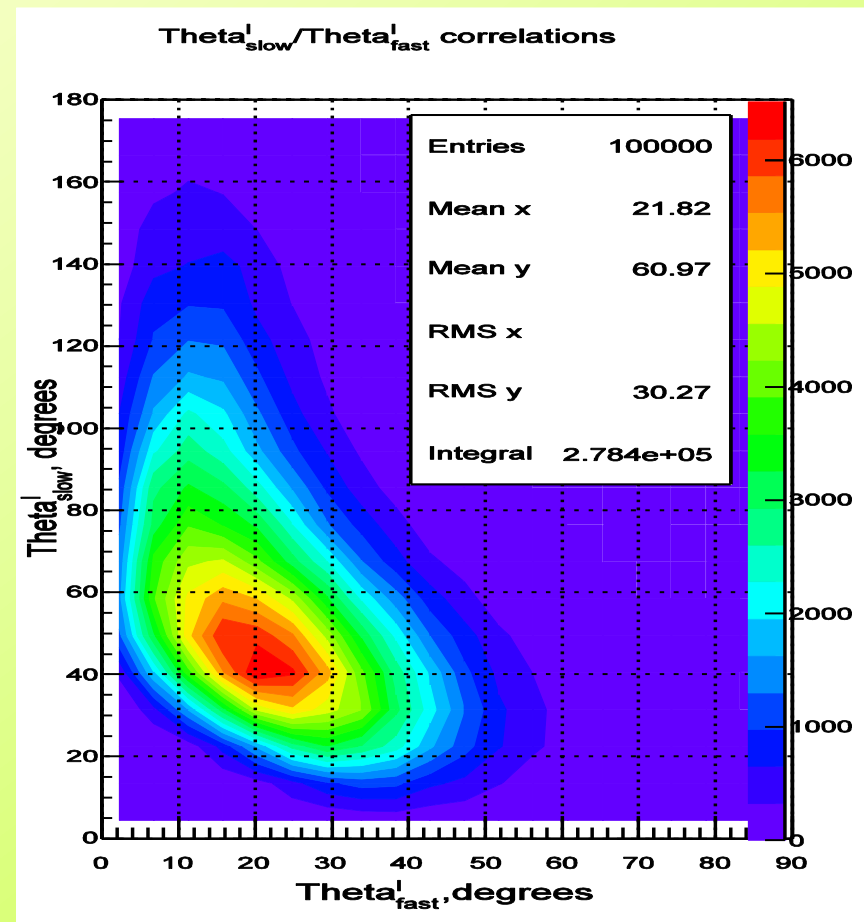
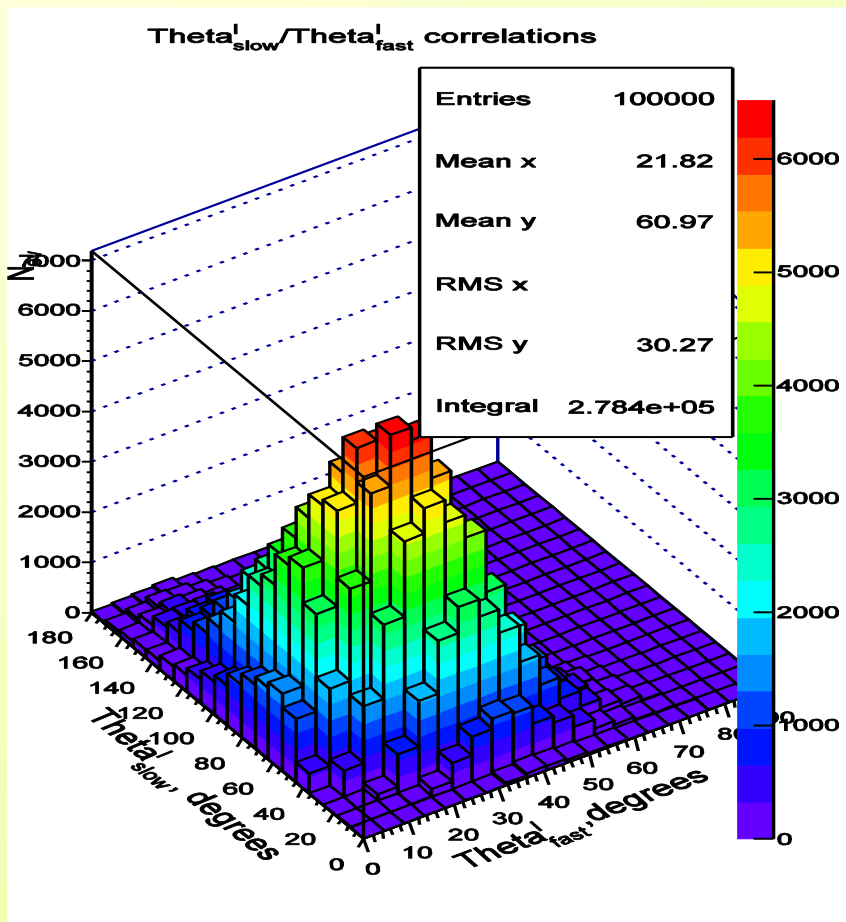


Tendency:

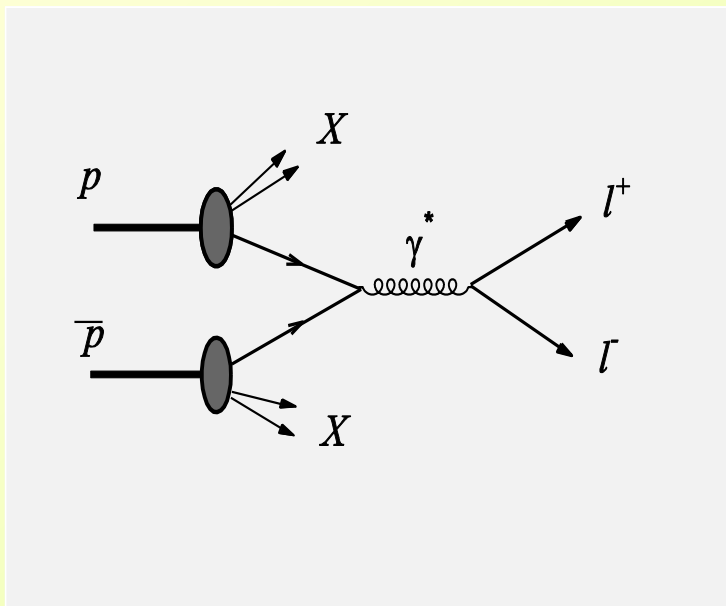
the higher is energy –
the less is angle



$\Theta_{slow}^\mu / \Theta_{fast}^\mu$ correlation



MMT-DY process



Simulation of muon's kinematical characteristics was done with use of PandaRoot & Geant 3 (presented by pink histograms) at the level of stand alone muon system with the set of 10000 events simulated by PYTHIA6.4.

The corresponding histograms done with use of the PYTHIA6.4 alone are superimposed for comparison (violet line).

From the statistical numbers (entries) of distributions one can see that the total loss of muons in detector is about 34.61% for μ^- and 34.2% for μ^+ .

PYTHIA6.4

Momenta distributions, obtained in the full simulation,

differ from those, simulated in PYTHIA6.4,

by the loss of quantity and some loss in momenta $\sim 0,25$ GeV for each component.

PandaRoot & Geant 3

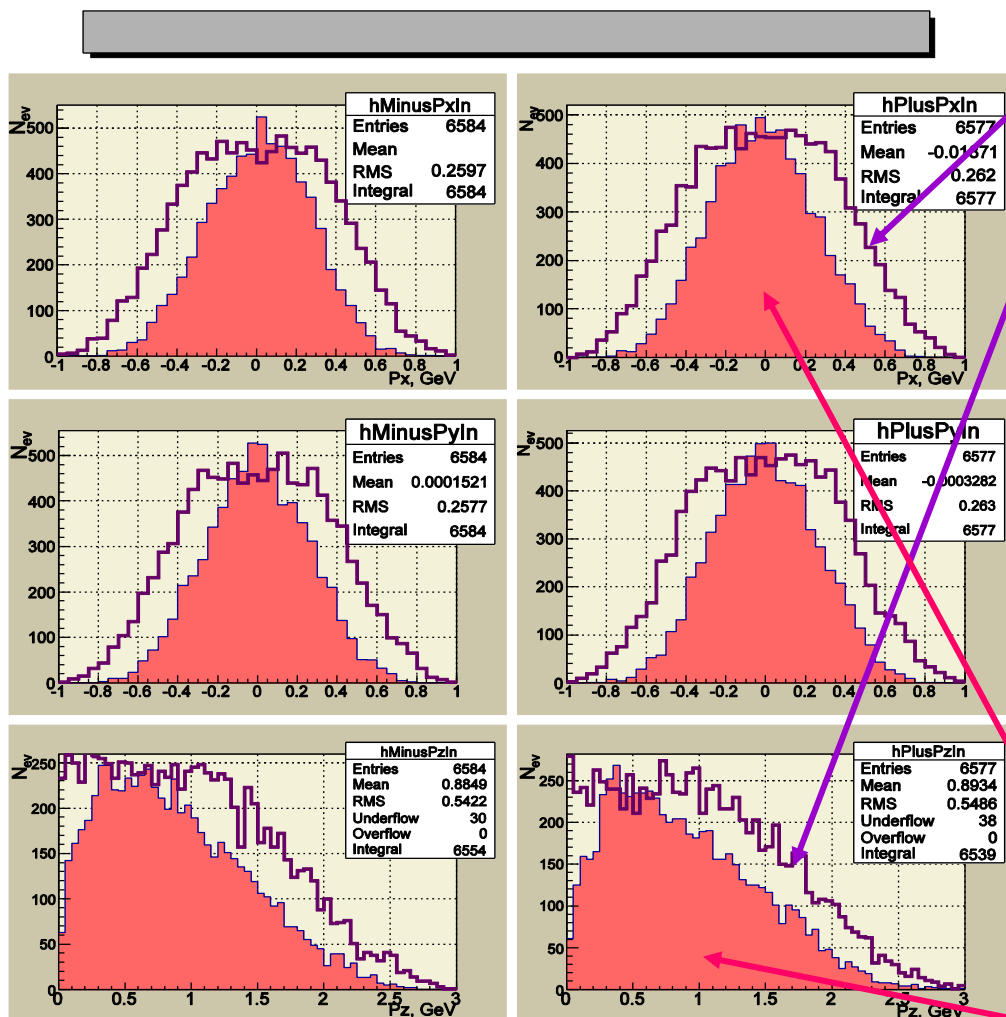
P_x^μ

P_y^μ

P_z^μ

μ^-

μ^+

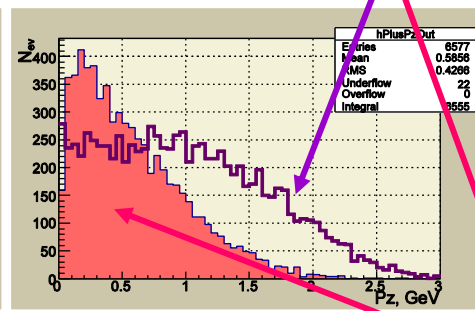
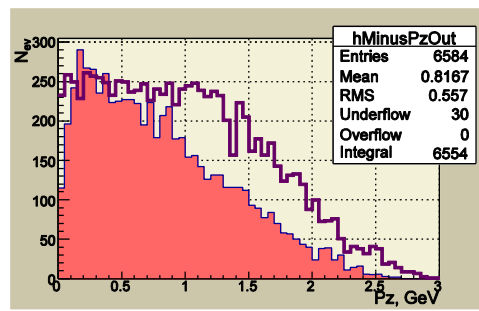
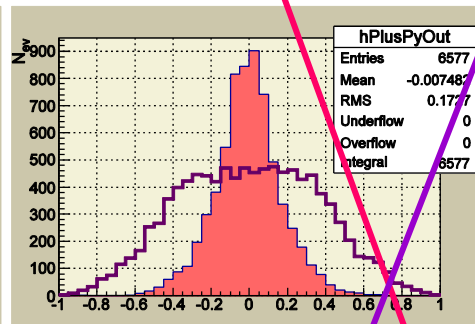
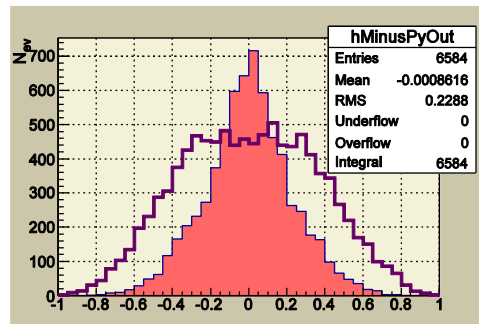
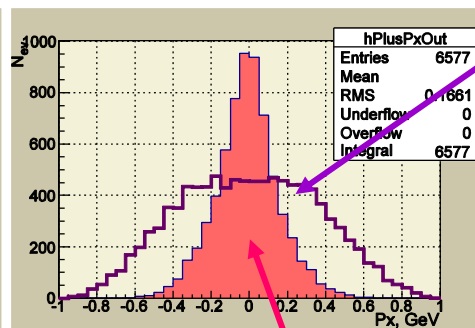
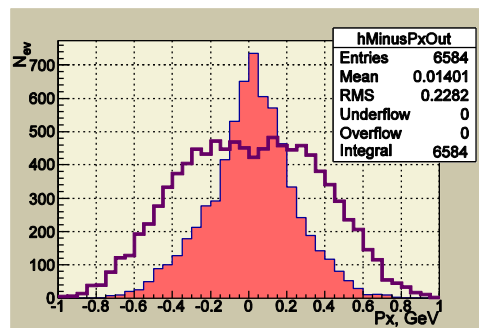


PYTHIA6.4

Momenta distributions, obtained in result of full simulation, in this case is **significantly differ** from the ones simulated in PYTHIA6.4, and **show noticeable loss of momentum** (about 0.3-0.6 GeV for each component).

Let us mention that for the positive charged muons the momentum losses are higher.

PandaRoot & Geant 3



μ^-

μ^+

PT μ , P μ , E μ from the 1-st hit in the muon system

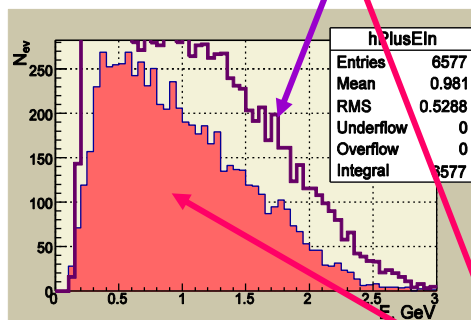
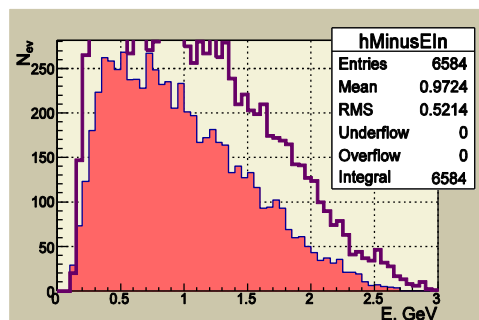
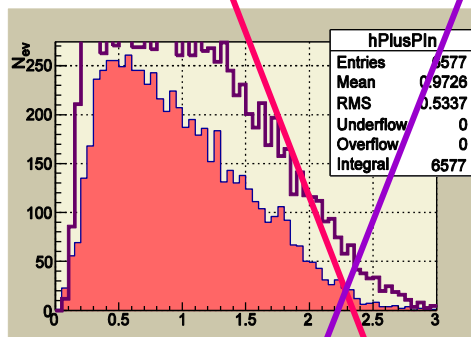
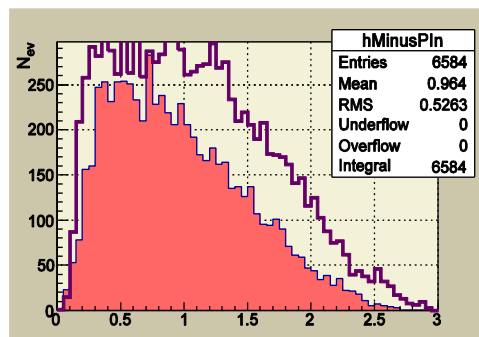
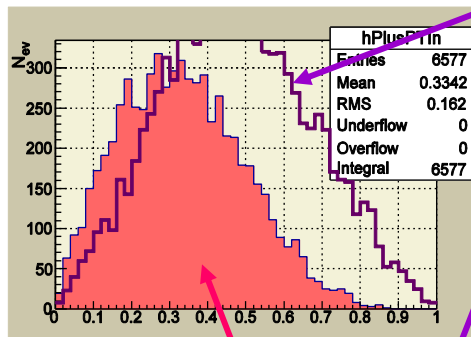
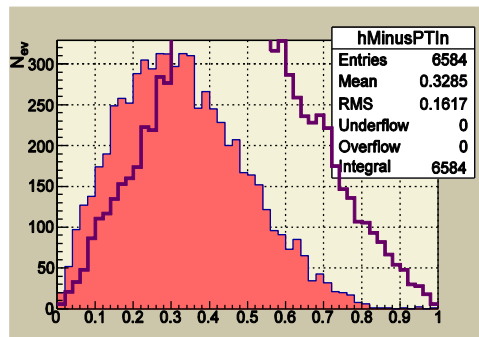
PYTHIA6.4

Momenta & Energy
distributions,
obtained in result of
full simulation,

differ from the ones,
simulated in
PYTHIA6.4 by

some loss of
quantity and
by the loss of
E (PT) ~ 0.2 GeV

PandaRoot & Geant 3



μ^-

μ^+

PT μ , P μ , E μ from the last hit in the muon system

PYTHIA6.4

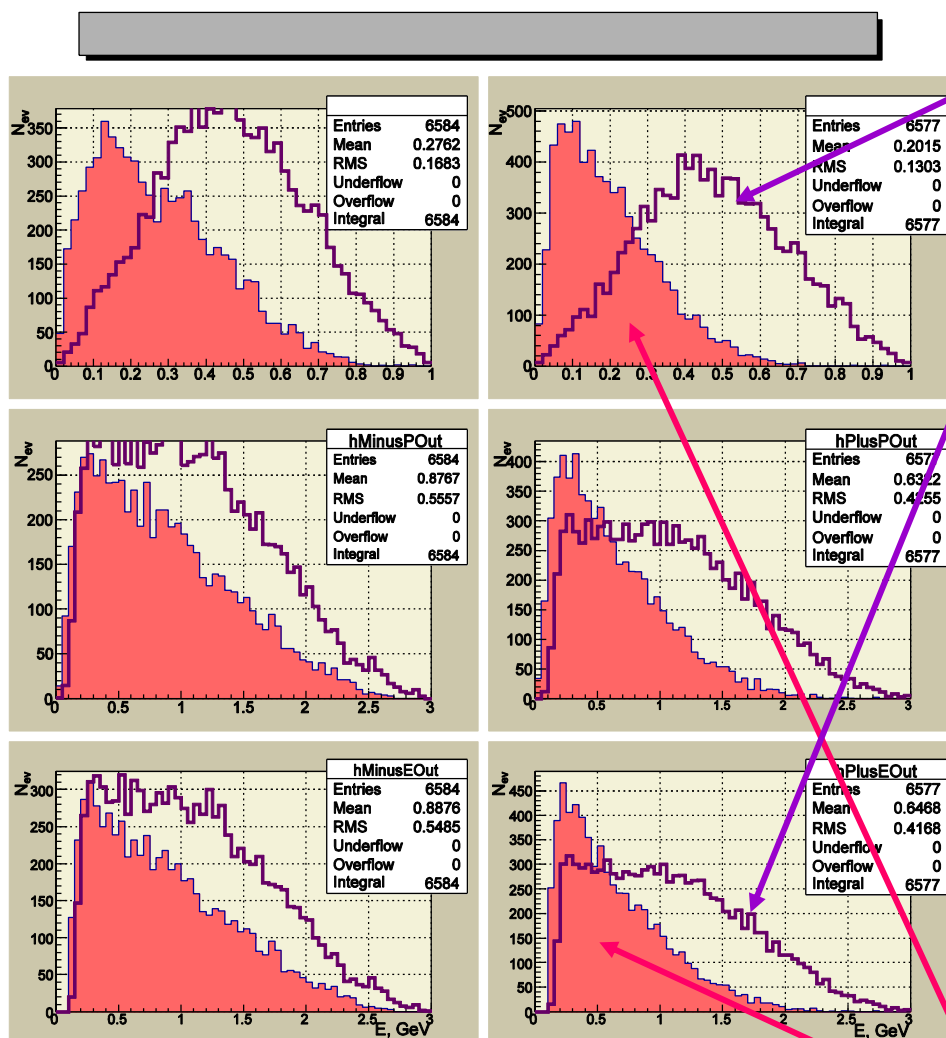
Momenta & Energy distributions, obtained in result of full simulation, in this case is

differ significantly from the ones, simulated in PYTHIA6.4, and

show noticeable loss of momentum & energy (up to 0.7 GeV) in result of penetrating through the material of the muon system.

Positive charged muons show higher loss of momentum.

PandaRoot & Geant 3



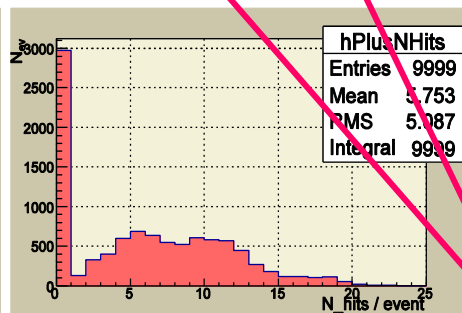
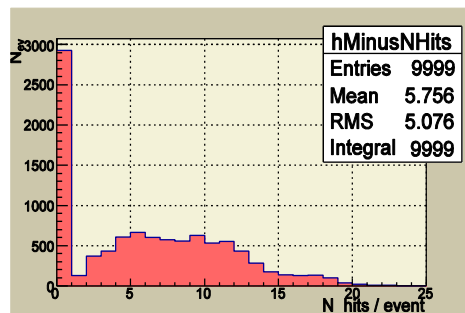
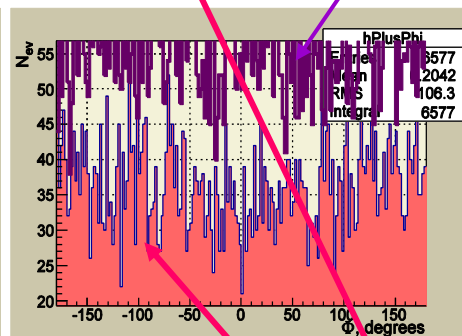
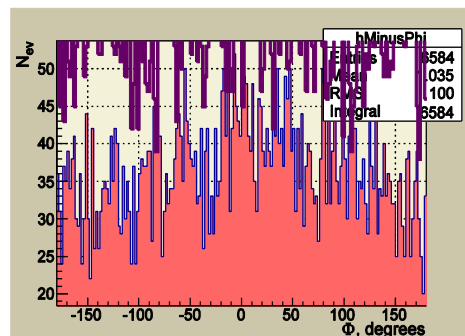
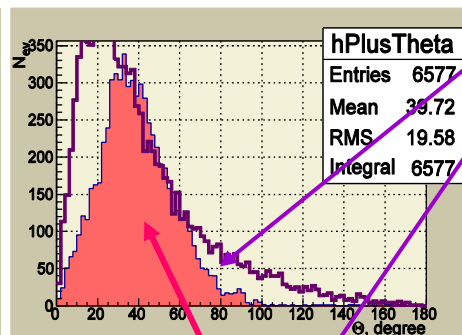
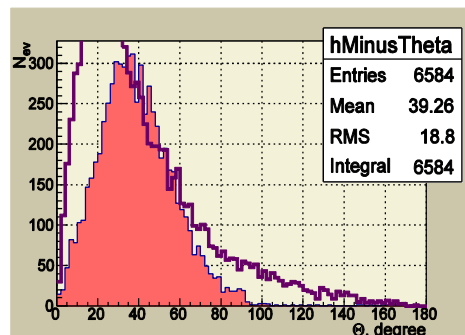
μ^-

μ^+

Angle θ^μ , φ^μ distributions and N_{hits} in the muon system

Signal Lepton Theta, Phi, Nhits

PYTHIA6.4



- θ^μ - polar angle
- φ^μ - azimuth angle
- N_{hits} - number of hits, made by muon in muon system per event
- The **significant difference in distributions of polar angle θ^μ** can be explained by deviation in magnetic field.
- Practically no difference in distributions of the azimuth angle φ^μ .
- The first column in muon hits distributions shows the number of events, in which the corresponding muons gave no hits in the muon system (lost muons).

μ^-

μ^+

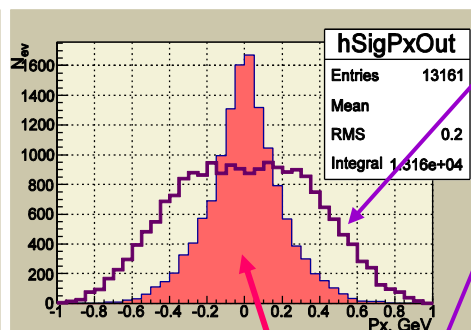
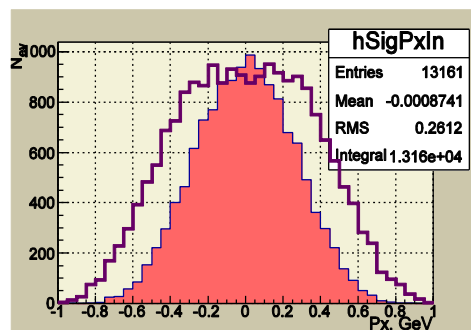
PandaRoot & Geant 3



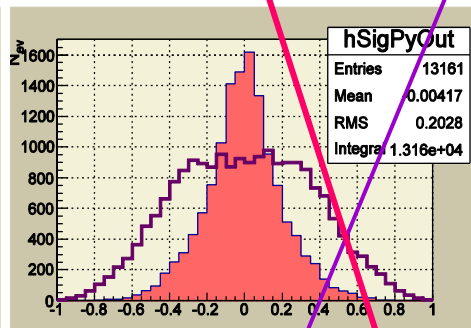
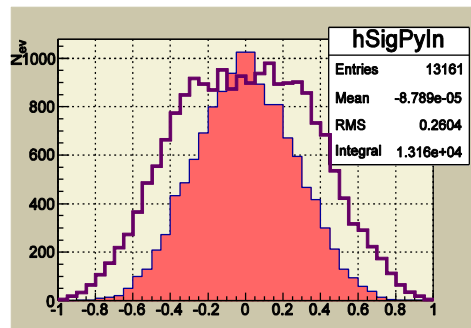
$P_x^\mu, P_y^\mu, P_z^\mu$ of $(\mu^+\mu^-)$ from the 1-st & last hit in the muon system

PYTHIA6.4

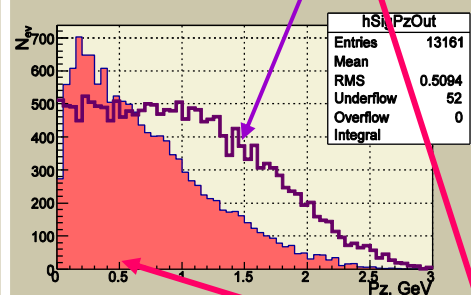
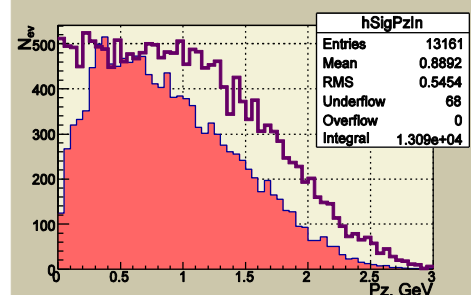
P_x^μ



P_y^μ



P_z^μ



1-st hit

last hit

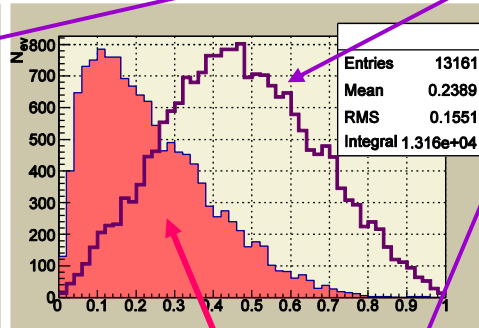
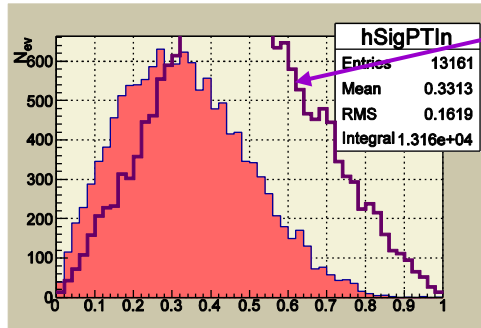
- Like in the case of separate taken muons, the *momenta distributions, obtained in result of full simulation, do not much differ* to the ones simulated in PYTHIA6.4 for the *values from the first hit*, except some loss of quantity &
- noticeably differ* to the ones simulated in PYTHIA6.4 in the *case of the last hit*, and show here the noticeable loss of momentum (about 0.4-0.5 GeV for each components).

PandaRoot & Geant 3

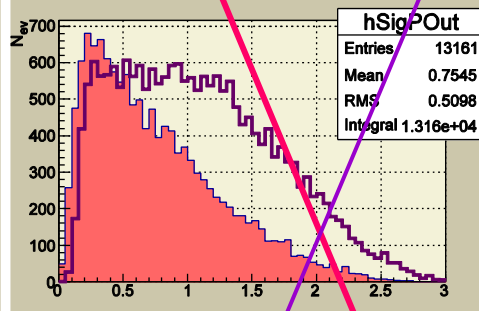
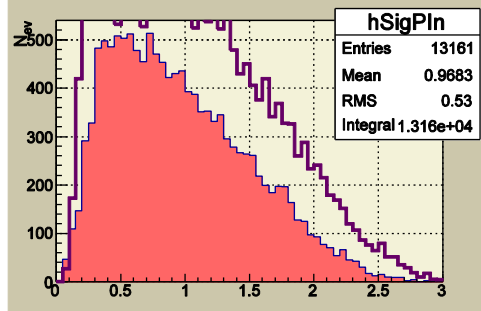
PT $^\mu$, P $^\mu$, E $^\mu$ of ($\mu^+\mu^-$) from the 1-st & last hit in the muon system

PYTHIA6.4

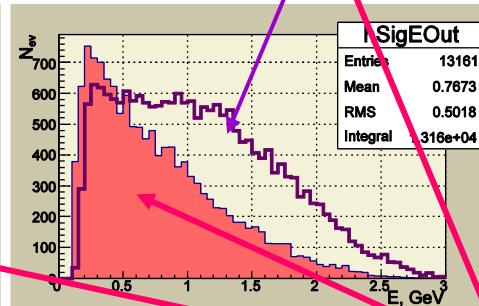
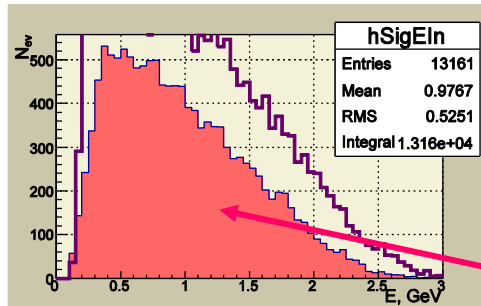
PT $^\mu$



P $^\mu$



E $^\mu$



1-st hit

last hit

- Like in the case of the muons, taken separately, the **momenta and energetical distributions** of the **first hit**, obtained during a full simulation, **do not differ significantly** from the ones simulated in PYTHIA6.4. The differences is, in general, in a loss of quantity and E&PT ~0.2 GeV.
- In the **case of a last hit**, they are **noticeably differ** from the ones, simulated in PYTHIA6.4, and **show significant loss of momentum and energy** (about 0.2-0.5 GeV) as a result of penetrating through the material of the muon system

PandaRoot & Geant 3

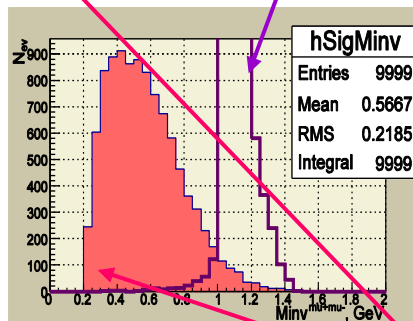
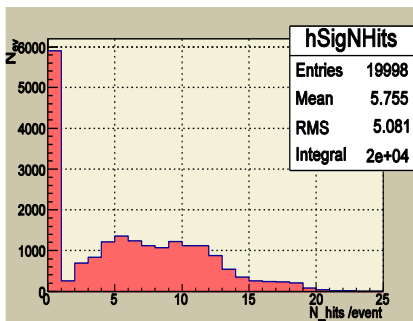
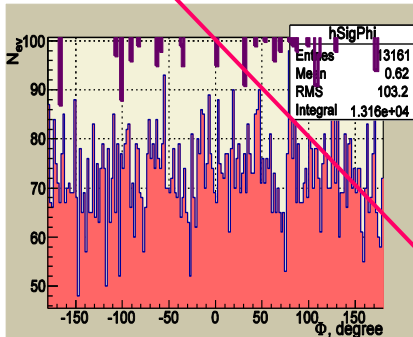
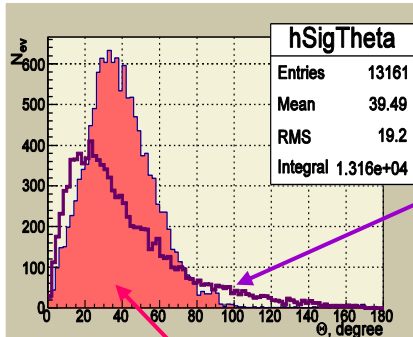
Total θ^μ , φ^μ distributions & N_{hits} in muon system, $M_{\text{inv}}(\mu^+, \mu^-)$

PYTHIA6.4

- θ^μ - polar angle
- φ^μ - azimuth angle
- N_{hits} - number of hits, made by muon in muon system per event
- The **significant difference in distributions of polar angle θ^μ** can be explained by deviation in magnetic field.
- Practically **no difference** in distributions of the azimuth angle φ^μ .
- The first column in muon hits distributions shows the number of events, in which the corresponding muons gave no hits in the muon system (lost muons).
- Distribution of invariant mass $M_{\text{inv}}(\mu^+, \mu^-)$ also **differ** from the initial one, simulated by PYTHIA.

PandaRoot & Geant 3

Signal Lepton Theta, Phi, Nhits



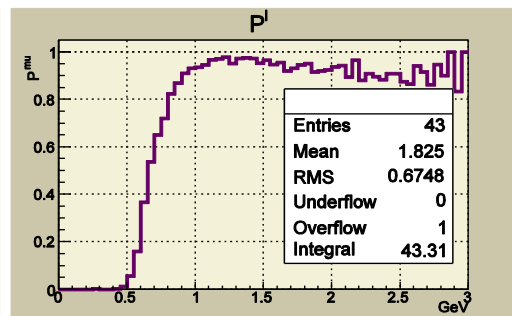
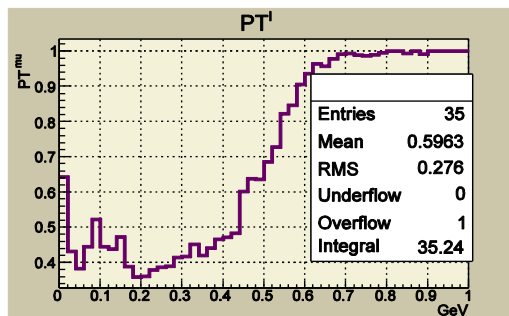
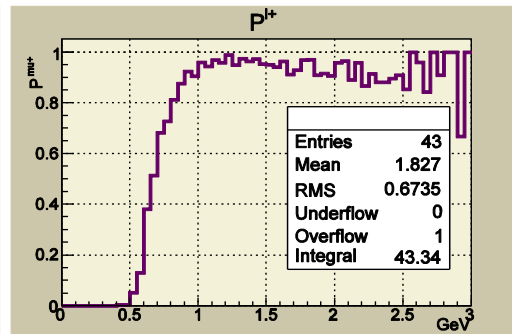
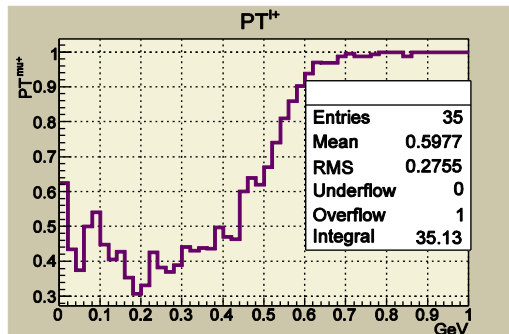
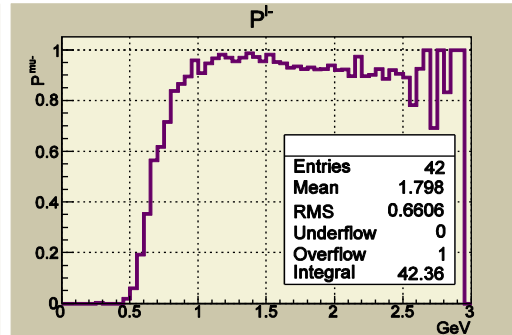
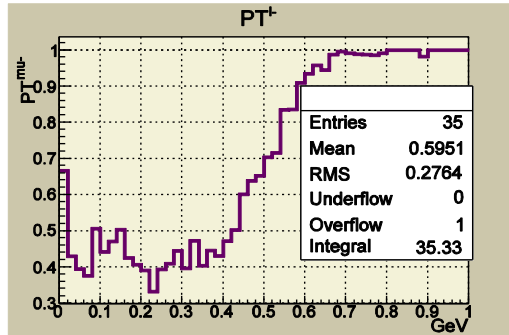
$M_{\text{inv}}(\mu^+, \mu^-)$

Signal muon P & PT registration efficiency

μ^-

μ^+

$\mu^+ + \mu^-$



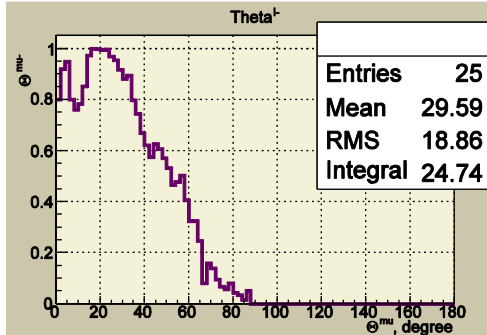
PT

P

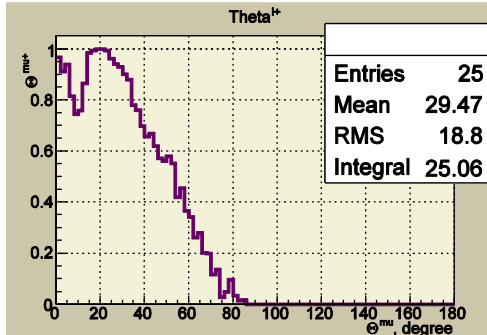
At very low (< 0.5 GeV) full momentum and transverse momentum, the efficiency of muon registration is noticeably decreasing. At the momenta > 0.8 GeV the efficiency goes to 1.

Signal muon registration efficiency by polar angle θ

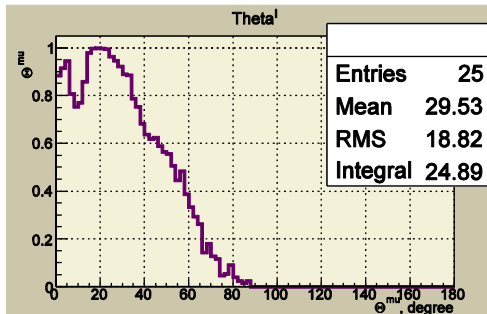
μ^-



μ^+



$\mu^+ + \mu^-$



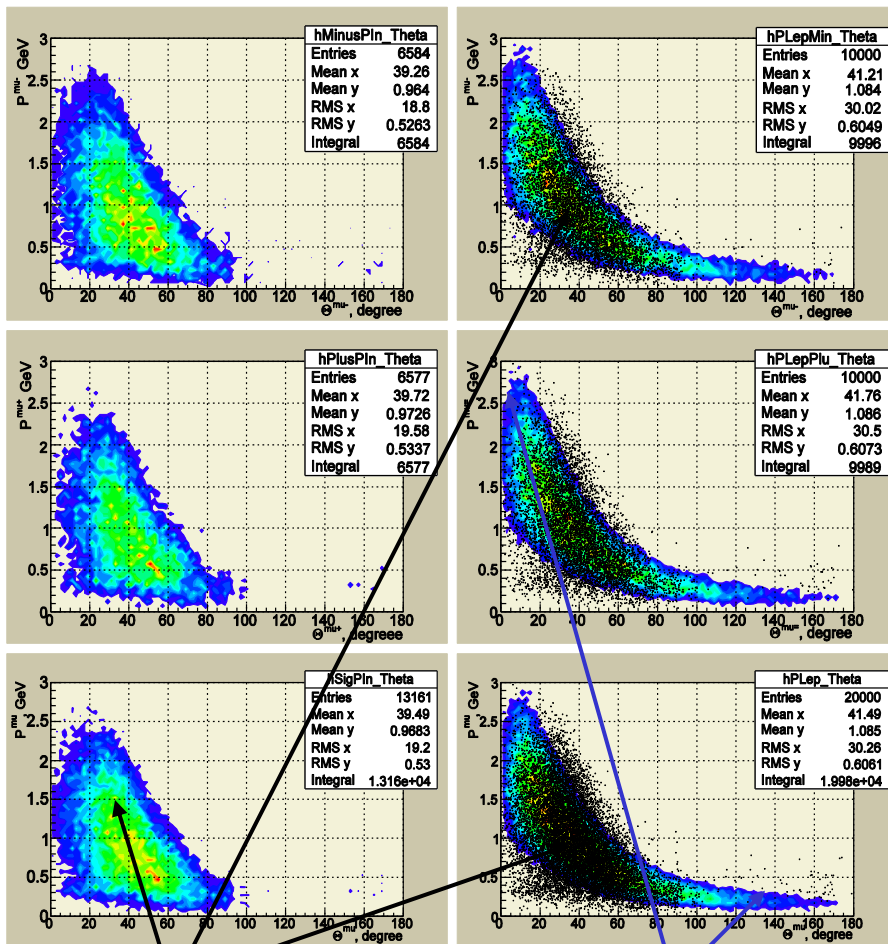
θ

The efficiency of muon registration is noticeably decreasing at the angles $> 40^\circ$

μ^-

μ^+

$\mu^+\mu^-$



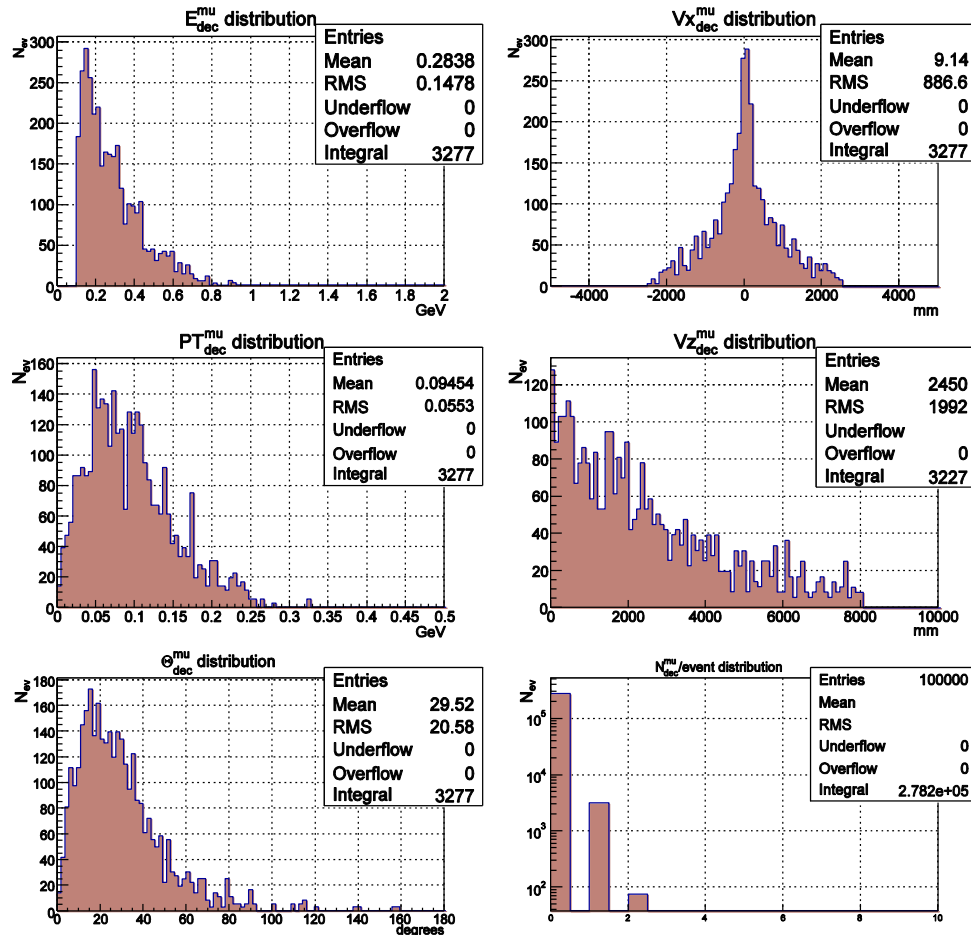
PandaRoot & Geant 3

PYTHIA6.4

- The figures are **projections of 3-D signal muons correlation distributions** of polar angle θ and modulus of momentum P (that correspond to the first hit in the muon system):
- Left column** presents the results, obtained by the full simulation (PANDARoot and GEANT3).
- Right column** - the color area presents the results of PYTHIA simulation. The black dots, which correspond to the results, shown in the left column, are superimposed for comparison.
- As it was already shown before in 2-D figures, due to the magnetic field influence, muons are moving aside to an angle of about 40° .

Fake muons distributions in signal events

Background μ^+/μ^- histograms in signal events



- The part of signal events which include fake muons is about 1.2%.
- Up to 2 fake muons in the final state.
- Fake muons production vertices are distributed within detector volume → *Vertex position* information will be useful for Signal / Background separation

Fake muons are less energetic than the signal ones

Applied cuts for signal events

1. We select the events with only **2** leptons with $E_\ell > 0.2 \text{ GeV}$, $PT_\ell > 0.2 \text{ GeV}$
2. These 2 leptons must be of the **opposite sign**
3. The vertex of origin lies within the **$R < 15 \text{ mm}$** from the interaction point

These criteria allow to discriminate completely events with the fake decay muons with the loss of 15.8% signal events

The main source of background for $q \bar{q} \rightarrow \gamma^* \rightarrow l^+ l^-$ are the Minimum-Bias processes:

Some examples:

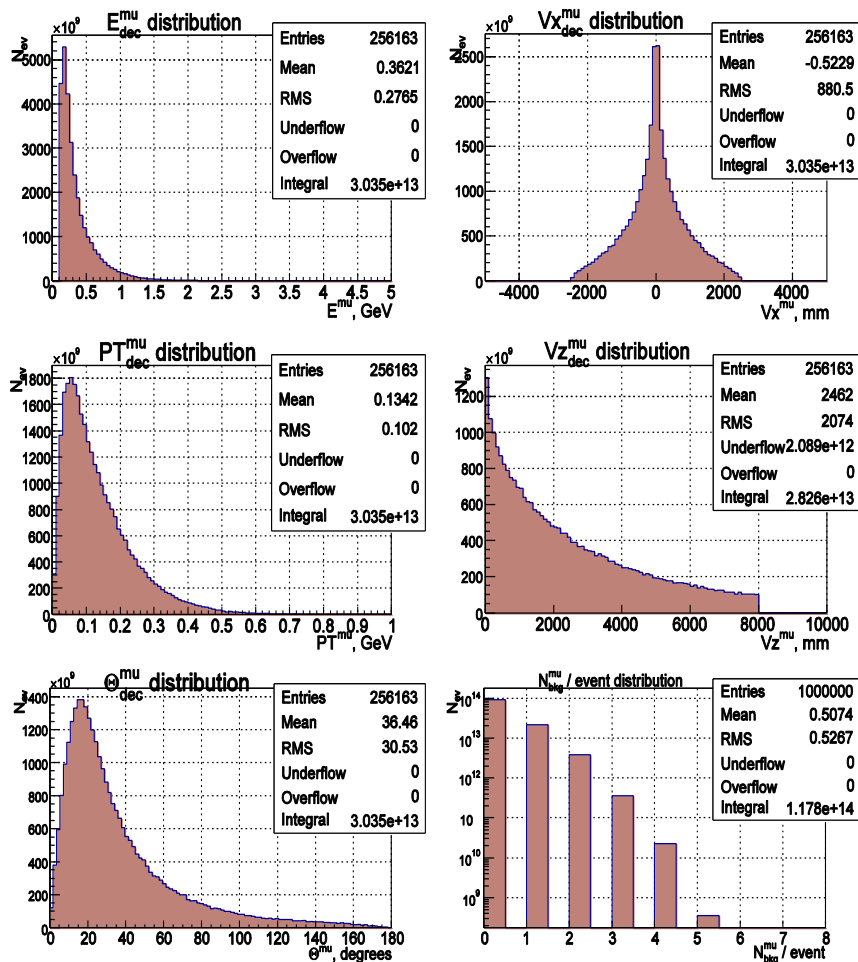
- *Low - PT scattering* (gives 68% of events with the $\sigma = 39.48$ mb);
- *Single diffractive* (gives 6% of events with the $\sigma = 1.58$ mb);
- $\bar{q} + q \rightarrow l^+ + l^-$ (gives 0.0000015% of events, $\sigma = 5.09 \cdot 10^{-7}$ mb);

So, we have 3 signal event against 200.000.000 of Mini-bias bkgd \rightarrow $S/B \approx 10^{-8}$

Mini-bias background is 5 order harder than QCD background

Muon's distributions from background events

mu+/mu- distributions in background events



Up to 6 μ per event \rightarrow
 \rightarrow a rather high probability of appearing the **muon pair** with the different signs of their charges in “*Minimum_bias*” events (which are other than the signal one)
 \rightarrow fake pretty well the signal events

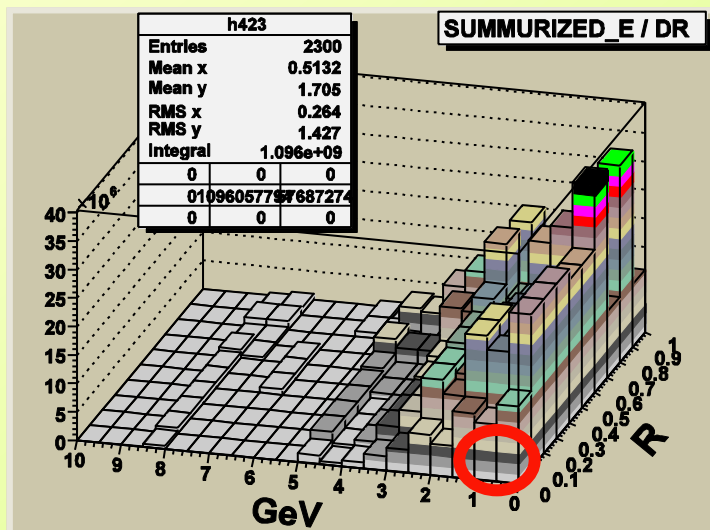
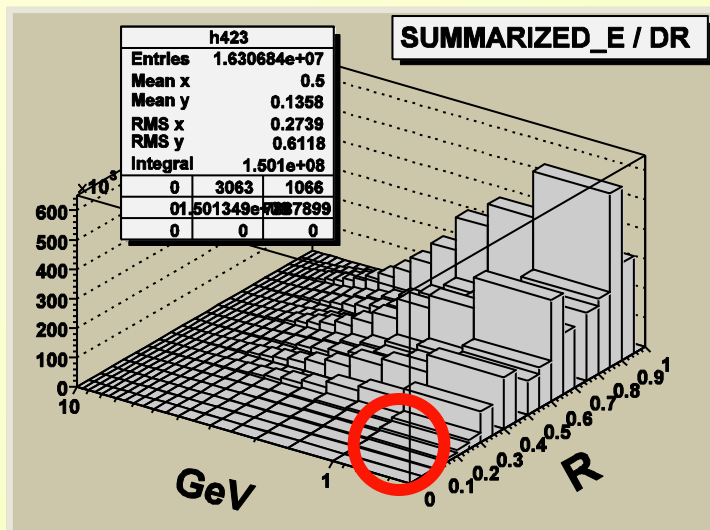


Cuts for mini-bias and QCD processes (including the signal one)



The following cuts were applied to the minimum bias and QCD sample:

1. selection of events with the only **2 leptons**, having $E_1 > 0.2 \text{ GeV}$, $PT_1 > 0.2 \text{ GeV}$;
2. these 2 leptons have charges of the opposite charge;
3. the vertex of lepton origin lies within the $R < 15 \text{ mm}$ from the interaction point;
4. $M_{\text{inv}}(\ell^+\ell^-) \geq 0.9 \text{ GeV}$;
5. **leptons** have to satisfy the **isolation criteria**:
the summed energy of particles $E_{\text{sum}} < 0.5 \text{ GeV}$ within the **cone** of
 $R_{\text{isolation}} = \sqrt{\Delta_\eta^2 + \Delta_\phi^2} = 0.2$.



The plots show the distributions over **summarized energy** of the final state particles in the cones of radius

$$R_{\text{isolation}} = \sqrt{\eta^2 + \phi^2} \text{ respect to the } (\eta - \text{pseudorapidity})$$

upper plot → **signal events**

bottom plot → **Mini-bias background**

Isolation criteria ($R_{\text{isolation}} = 0.2$)

E (of particles) = 0.5 GeV

Applied cuts & efficiency for Minimum-Bias background events

$PT_1 > 0.2 \text{ GeV}$

$PT_1 > 0.5 \text{ GeV}$

N of cuts	S/B ratio	Efficiency	S/B ratio	Efficiency
1 (exactly 2 leptons with $E_l > 0.2 \text{ GeV}$, $PT_1 > 0.2 \text{ GeV}$)	$1.02 * 10^{-6}$	$1.47 * 10^{-3}$	$2.37 * 10^{-6}$	$4.22 * 10^{-4}$
2 (2 leptons are of the opposite sign	$1.13 * 10^{-6}$	0.906	$2.57 * 10^{-6}$	0.921
3 (The vertex is within the $R < 15 \text{ mm}$)	$3.70 * 10^{-4}$	$3.04 * 10^{-3}$	$6.09 * 10^{-4}$	$4.21 * 10^{-3}$
4 ($M_{inv}(l_1 l_2) > 0.9$)	$6.58 * 10^{-2}$	0.056	$7.04 * 10^{-3}$	0.086
5 Isolation	1.5	0.004	2	0.003

- ✓ *“Theoretical” Monte-Carlo distributions of individual muons from the leptons pair production process were presented on the basis of PYTHIA6.4 for the case of $E_{beam} = 5 \text{ GeV}$*
- ✓ *Final distributions of these muons after propagation through the detector volume were obtained by use of PANDARoot program*
- ✓ *Preliminary set of criteria for Signal and Background separation was shown on the basis of PYTHIA simulation*
- ✓ *Futher study of the backgrounds with a full simulation in PANDARoot is needed*

This work was generously supported by the Helmholtz Association under grant agreement IK-RU-002